

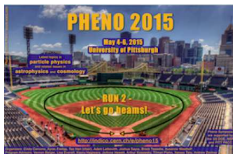
Electroweak Corrections at the LHC

John M. Campbell¹, Doreen Wackeroth², Jia Zhou²

¹Fermilab, Batavia, IL 60510

²Department of Physics, SUNY at Buffalo, Buffalo, NY 14260

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Outline

- Introduction
- Electroweak corrections in MCFM for
 - Neutral current Drell-Yan process
 - Top pair production
 - Di-jets production
- Conclusion and outlook

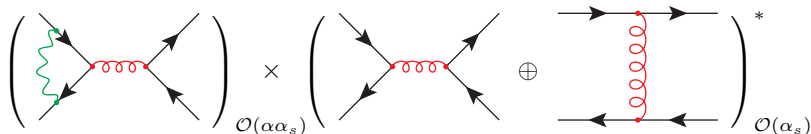
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 - Motivation
- 2 Implementation of NLO electroweak corrections in MCFM
 - Processes under consideration
 - Related work
 - Drell-Yan
 - $t\bar{t}$ production
 - Dijets
- 3 Conclusion and outlook

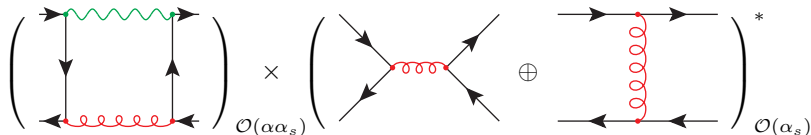
Example of electroweak corrections

- Electroweak corrections to di-jet production ($\mathcal{O}(\alpha\alpha_s^2)$)

- EW vertex correction



- EW box correction



Electroweak corrections enhanced via Sudakov logarithms

- Electroweak corrections at the LHC can be enhanced at high energies due to soft/collinear radiation of W and Z bosons.
- When all kinematic invariants $r_{ij} = (p_j + p_k)^2$ are much larger than the heavy particles in the loop, i.e., $|r_{ij}| \sim Q^2 \gg M_W^2 \sim M_Z^2 \sim M_H^2 \sim m_t^2$, electroweak corrections are dominated by Sudakov-like corrections:

$$\alpha_W^l \log^n(Q^2/M_W^2) \quad (n \leq 2l, \alpha_W = \frac{\alpha}{4\pi s_W^2})$$

▶ $Q = 1\text{TeV}$,

$$\alpha_W \log^2(Q^2/M_W^2) \sim \boxed{6.6\%}, \quad \alpha_W \log(Q^2/M_W^2) \sim \boxed{1.3\%}$$

▶ $Q = 14\text{TeV}$,

$$\text{DL} \sim \boxed{27\%}, \quad \text{SL} \sim \boxed{2.6\%}$$

Why electroweak corrections?

- The inclusion of EW corrections in LHC predictions is important for the search of new physics in tails of distributions, e.g., search for W' , Z' , non-standard couplings.
- It is also important for constraints on PDFs measurement.
- EW NLO $\mathcal{O}(\alpha)$ is expected comparable with QCD NNLO $\mathcal{O}(\alpha_s^2)$.

Why electroweak corrections?

- Calculations of electroweak corrections are often not readily available in public codes and can quickly become complicated (and CPU intensive) for high multiplicities.
- As a first step to improve predictions for the LHC at high energies, one could implement the Sudakov approximation of electroweak corrections.

Example: Weak Sudakov corrections to $Z + \leq 3$ jets in Alpgen
M. Chiesa *et al*, PRL111 (2013).

See also a recent proposal to add EW corrections to HERWIG:

[\[http://arxiv.org/pdf/1401.3964.pdf\]](http://arxiv.org/pdf/1401.3964.pdf) [▶ Link Here](#)

- Our goal is to implement EW corrections in MCFM so that they become readily available to the experimental community and can be studied together with the already implemented QCD corrections.

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Processes implemented in MCFM

- We will provide both the Sudakov approximation for EW corrections valid at high energies and the complete 1-loop weak corrections to be able to quantify the goodness of the approximation.
 - ▶ **NC Drell Yan process**
 - I Weak Sudakov correction ✓
 - II Exact NLO weak correction ✓
 - ▶ **Top-pair production**
 - I Weak Sudakov correction ✓
 - II Exact NLO weak correction ✓
 - ▶ **Dijet production**
 - I Weak Sudakov correction ✓
 - II Exact NLO weak correction ✓ *preliminary*
- For a recent review of status of EW corrections see: [▶ Link Here](#)
[\[https://phystev.in2p3.fr/wiki/_media/2013:groups:lh13_ew.pdf\]](https://phystev.in2p3.fr/wiki/_media/2013:groups:lh13_ew.pdf)

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Sudakov logarithms calculations

- Vertex Part at Very High Energies in QED
V. V. Sudakov, *Soviet Phys. JETP*3 (1956) 65
- Some Refs. for the general Sudakov logarithmic corrections
P. Ciafaloni, D. Comelli, *PLB*446 (1999), [arXiv:hep-ph/9809321](#); M. Beccaria *et al*, *PRD*61 (2000), [arXiv:hep-ph/9906319](#); J. H. Kühn, A. A. Penin, [arXiv:hep-ph/9906545](#); M. Melles, *Phys. Rept.*375(2003), [arXiv:hep-ph/0104232](#); A. Denner, S. Pozzorini, *EPJC*18 (2001), [arXiv:hep-ph/0010201](#); A. Denner, S. Pozzorini, *EPJC*21(2001), [arXiv:hep-ph/0104127](#); S. Pozzorini, [arXiv:hep-ph/0201077](#); W. Beenakker, A. Werthenbach, *NPB*630 (2002), [arXiv:hep-ph/0112030](#); A. Denner *et al*, *JHEP*0811 (2008), [arXiv:0809.0800](#).
- ▶ The general algorithm of Denner and Pozzorini is adopted in the implementation in MCFM

Relevant studies in existing references

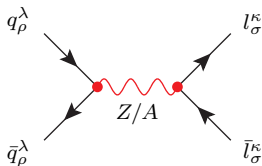
- Electroweak Radiative Corrections to Neutral-Current Drell-Yan Processes at Hadron Colliders,
U. Baur, O. Brein, W. Hollik, C Schappacher, and D. Wackeroth, *PRD65* 033007 (2002), [arXiv:hep-ph/010827](#)
- Electroweak corrections to top-quark pair production in quark-antiquark annihilation,
J. H. Kühn, A. Scharf and P. Uwer, *Eur.Phys.J. C45* (2006) 139-150, [arXiv:hep-ph/0508092](#)
- Electroweak effects in top-quark pair production at hadron colliders,
J. H. Kühn, A. Scharf and P. Uwer, *Eur.Phys.J. C51* (2007) 37-53, [arXiv:hep-ph/0610335](#)
- Weak radiative corrections to dijet production at hadron colliders,
S. Dittmaier, A. Huss and C. Speckner, *JHEP1211* (2012) 095, [arXiv:1210.0438](#)

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Sudakov approximation to Drell-Yan process

Process under consideration: $\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa \rightarrow 0$



Born amplitude

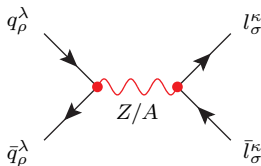
$$\mathcal{M}^{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa} = e^2 R_{q_\rho^\lambda l_\sigma^\kappa} \frac{\mathcal{A}}{\hat{s}} + \mathcal{O}\left(\frac{M_Z^2}{\hat{s}}\right),$$

$$R_{\phi_i \phi_k} := \sum_{N=Z,A} I_{\phi_i}^N I_{\phi_k}^N = \frac{1}{4c_W^2} Y_{\phi_i} Y_{\phi_k} + \frac{1}{s_W^2} T_{\phi_i}^3 T_{\phi_k}^3,$$

$Y_{\phi_{i,k}}$ — weak hypercharge; $T_{\phi_{i,k}}^3$ — 3rd component of weak isospin.

Sudakov approximation to Drell-Yan process

Process under consideration: $\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa \rightarrow 0$



Born amplitude

$$\mathcal{M}_{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa} = e^2 R_{q_\rho^\lambda l_\sigma^\kappa} \frac{\mathcal{A}}{\hat{s}} + \mathcal{O}\left(\frac{M_Z^2}{\hat{s}}\right),$$

$$R_{\phi_i \phi_k} := \sum_{N=Z,A} I_{\phi_i}^N I_{\phi_k}^N = \frac{1}{4c_W^2} Y_{\phi_i} Y_{\phi_k} + \frac{1}{s_W^2} T_{\phi_i}^3 T_{\phi_k}^3,$$

$Y_{\phi_{i,k}}$ — weak hypercharge; $T_{\phi_{i,k}}^3$ — 3rd component of weak isospin.

Sudakov approximation to Drell-Yan process

Leading and subleading soft-collinear corrections

$$\delta_{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa}^{LSC} = -\sum_{f_\tau^\mu = q_\rho^\lambda, l_\sigma^\kappa} \left[C_{f_\tau^\mu}^{\text{ew}} L(\hat{s}) - 2(I_{f_\tau^\mu}^Z)^2 \log \frac{M_Z^2}{M_W^2} l_Z + Q_{f_\tau^\mu}^2 L^{\text{em}}(\hat{s}, \lambda^2, m_{f_\tau^\mu}^2) \right],$$

$$\delta_{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa}^{SSC} = -l(s) \left[4R_{q_\rho^\lambda l_\sigma^\kappa} \log \frac{\hat{t}}{\hat{u}} + \frac{\delta_{\lambda L} \delta_{\kappa L}}{s_w^4 R_{q_\rho^\lambda l_\sigma^\kappa}} \left(\delta_{\rho\sigma} \log \frac{|\hat{t}|}{s} - \delta_{-\rho\sigma} \log \frac{|\hat{u}|}{s} \right) \right]$$

$$-4Q_{q_\rho} Q_{l_\sigma} l(M_W^2, \lambda^2) \log \frac{\hat{t}}{\hat{u}}$$

$$L(\hat{s}) := \frac{\alpha}{4\pi} \log^2 \frac{\hat{s}}{M_W^2}, \quad l_Z = l(\hat{s}) := \frac{\alpha}{4\pi} \log \frac{\hat{s}}{M_W^2}.$$

$$C^{\text{ew}} := \sum_{V^a=A,Z,W^\pm} I^{V^a} I^{\bar{V}^a}, \text{ Casimir operator.}$$

Sudakov approximation to Drell-Yan process

Collinear or soft SL corrections

$$\delta_{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa}^C = \sum_{f_\tau^\mu = q_\rho^\lambda, l_\sigma^\kappa} \left[3C_{f_\mu}^{\text{ew}} l_C - \frac{1}{4s_W^2} \left((1 + \delta_{\mu R}) \frac{m_{f_\tau}^2}{M_W^2} + \delta_{\mu L} \frac{m_{f_{-\tau}}^2}{M_W^2} \right) l_{Yuk} \right. \\ \left. + 2Q_{f_\tau}^2 \cancel{l_{f_\tau}^{\text{em}}} (m_{f_\tau}^2) \right]$$

Parameter renormalization corrections

$$\delta_{\bar{q}_\rho^\lambda q_\rho^\lambda l_\sigma^\kappa \bar{l}_\sigma^\kappa}^{PR} = \left[\frac{s_W}{c_W} b_{AZ}^{\text{ew}} \Delta_{q_\rho^\lambda l_\sigma^\kappa} - b_{AA}^{\text{ew}} \right] l_{PR} + \cancel{2\delta Z_e^{\text{em}}} \\ \Delta_{\phi_i \phi_k} := \frac{-\frac{1}{4c_W^2} Y_{\phi_i} Y_{\phi_k} + \frac{c_W^2}{s_W^4} T_{\phi_i}^3 T_{\phi_k}^3}{R_{\phi_i \phi_k}}$$

$$l_C = l_{Yuk} = l_{PR} = l(\hat{s}) := \frac{\alpha}{4\pi} \log \frac{\hat{s}}{M_W^2}, \quad b_{AZ}^{\text{ew}} = -\frac{19 + 22s_W^2}{6s_W^2 c_W^2}, \quad b_{AA}^{\text{ew}} = -\frac{11}{3}.$$

The input parameter setup

- Both calculations are included in MCFM
 - ▶ Exact
 - ▶ Sudakov

The input parameter setup in MCFM:

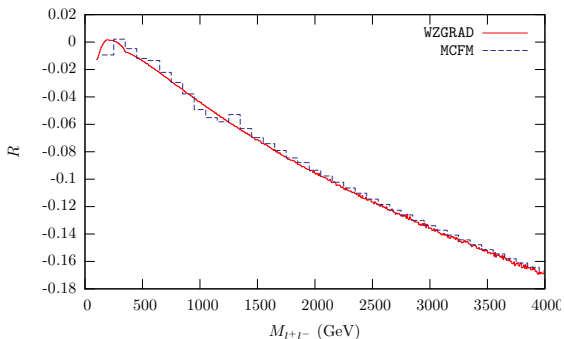
$$\begin{aligned}
 G_\mu &= 1.16639 \times 10^{-5} \text{ GeV}^{-2}, \quad \sin^2 \theta_W = 1 - M_W^2/M_Z^2, \\
 \alpha_\mu &= 1/132.5605045, \quad \Gamma_Z = 2.4952 \text{ GeV}, \quad \cos^2 \theta_W = M_W^2/M_Z^2, \\
 M_Z &= 91.1876 \text{ GeV}, \quad M_W = 80.425 \text{ GeV}, \quad M_H = 120 \text{ GeV}, \\
 m_e &= 0.51099892 \text{ MeV}, \quad m_\mu = 105.658369 \text{ MeV}, \quad m_\tau = 1.777 \text{ GeV}, \\
 m_u &= 66 \text{ MeV}, \quad m_c = 1.2 \text{ GeV}, \quad m_t = 173.2 \text{ GeV}, \\
 m_d &= 66 \text{ MeV}, \quad m_s = 150 \text{ MeV}, \quad m_b = 4.6 \text{ GeV}, \\
 \mu_F &= \mu_R = M_Z.
 \end{aligned}$$

One-loop weak correction: Numerical result

- Comparison with WZGRAD at 14 TeV

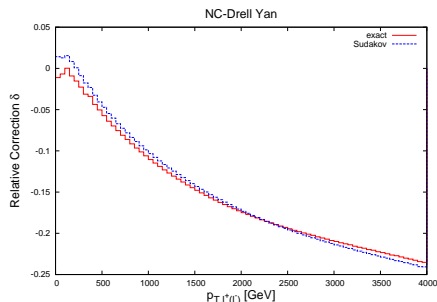
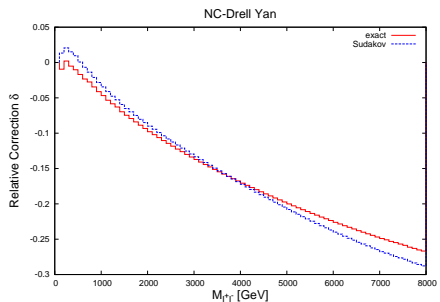
$$M_{l+l^-} > 100 \text{ GeV}, |p_{T,l^\pm}| > 20 \text{ GeV}, |\eta_{l^\pm}| < 2.5$$

$$R = \frac{\sigma_{NLO} - \sigma_{LO}}{\sigma_{LO}}$$



Comparison: Sudakov approximation and exact calculation

- Invariant mass and transverse momentum distributions at LHC (14 TeV) with MCFM

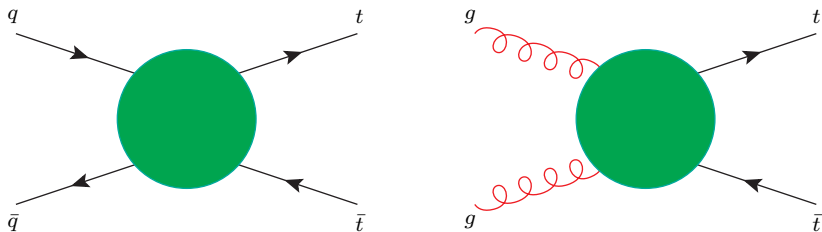


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Sudakov approximation to $t\bar{t}$ production

Processes under consideration: $\bar{q}_\rho^\lambda q_\rho^\lambda t^\kappa \bar{t}^\kappa \rightarrow 0$ and $gg t^\kappa \bar{t}^\kappa \rightarrow 0$



- Chiralities to initial and final states
 - massless initial quarks(gluons) \rightarrow chirality = helicity, conserved during transportation,
 - massive final top quarks \rightarrow chirality \neq helicity, oscillating along the moving direction.
- Use projector to restore the weak corrections in the chiral coupling

Sudakov approximation to $t\bar{t}$ production

- Two ways to proceed the calculation
 - ① break down the amplitude with chiralities ✓
 - ② calculate the matrix element square directly ✓

Chiral Born

$$|\mathcal{M}|_{\text{Born}}^2 = |\mathcal{M}_{\text{LL}}|^2 + |\mathcal{M}_{\text{RR}}|^2 + |\mathcal{M}_{\text{LR}}|^2 + |\mathcal{M}_{\text{RL}}|^2,$$

$$|\mathcal{M}_{\text{LL}}|^2 = |\mathcal{M}_{\text{RR}}|^2, \quad |\mathcal{M}_{\text{LR}}|^2 = |\mathcal{M}_{\text{RL}}|^2$$

- Universal correction independent of chirality

$$\sum_{f_\tau^\sigma} \left[-C_{f_\tau^\sigma}^{\text{ew}}(\text{L}(\hat{s}) - 3 \cdot l_c) \right] |\mathcal{M}|_{\text{Born}}^2$$

- Angular dependence ($q\bar{q}$ channel) and Yukawa enhanced terms
- No parameter renormalization

One-loop correction to $t\bar{t}$ production: Numerical result

- Input parameters

$$\begin{aligned}
 M_Z &= 91.1876 \text{ GeV}, \quad M_W = 84.425 \text{ GeV}, \quad M_H = 120 \text{ GeV}, \\
 m_b &= 4.6 \text{ GeV}, \quad m_t = 173.2 \text{ GeV}, \quad s_W^2 = 0.2221236, \\
 \alpha &= \alpha_\mu = 1/132.5605045, \quad \alpha_s(2m_t) = 0.09897922, \\
 \mu_F &= \mu_R = 2m_t.
 \end{aligned}$$

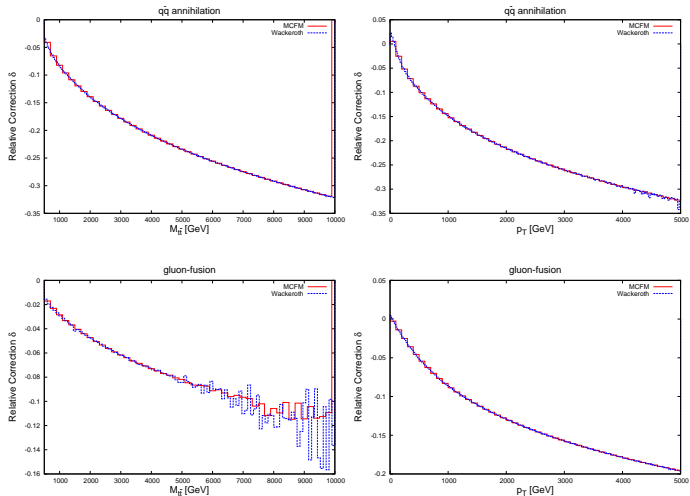
- The total cross sections

σ (fb)	$q\bar{q}$	gg	
$\mathcal{O}(\alpha_s^2)$	55408(9)	354251(66)	(MCFM)
LO	55386(18)	354254(47)	ref. ^[1]
$\mathcal{O}(\alpha\alpha_s^2)$	-1012.2(5)	-3887(1)	(MCFM)
NLO weak	-1011(1)	-3886(2)	ref. ^[1]

[1] W. Beenakker *et al*, *Nuclear Physics B*411(1994) 343

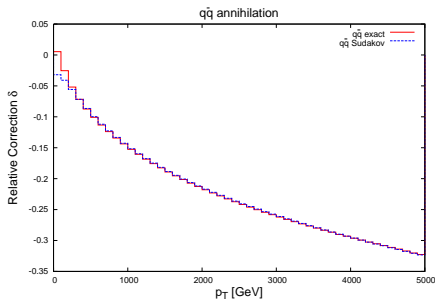
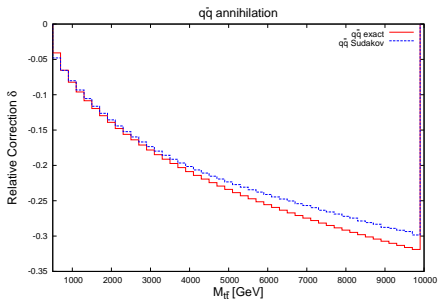
One-loop correction to $t\bar{t}$ production: Numerical result

- Cross-check of the exact result at LHC = 14 TeV



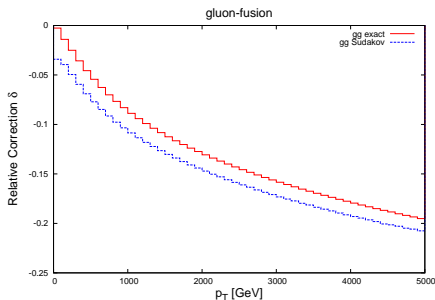
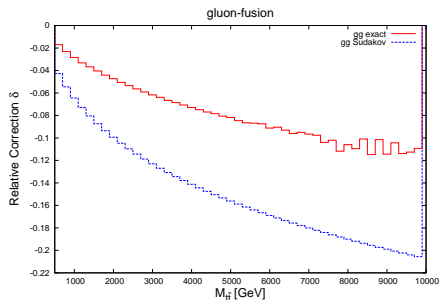
Comparison with Sudakov approximation

- Comparison between Sudakov approx and 1-loop exact calculation at LHC = 14 TeV with MCFM



Comparison with Sudakov approximation

- Comparison between Sudakov approx and 1-loop exact calculation at LHC = 14 TeV with MCFM



$$p_t = (m_T \cosh y_t, p_T \sin \phi, p_T \cos \phi, m_T \sinh y_t),$$

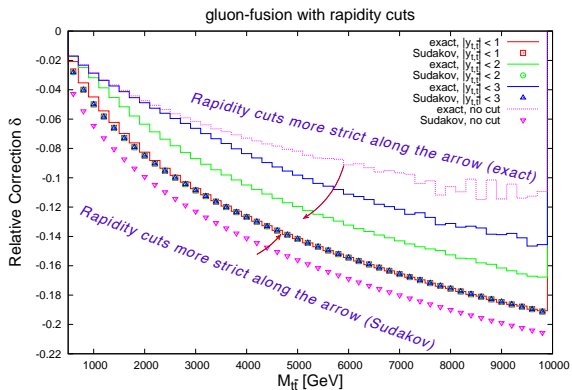
$$p_{\bar{t}} = (m_T \cosh y_{\bar{t}}, -p_T \sin \phi, -p_T \cos \phi, m_T \sinh y_{\bar{t}}),$$

$$M_{t\bar{t}}^2 = 2m_t^2 + 2m_T^2 \cosh(y_t - y_{\bar{t}}) + 2p_T^2,$$

$$m_T = \sqrt{p_T^2 + m_t^2}.$$

Comparison with Sudakov approximation

- ▶ The invariant mass distributions with rapidity cuts; Sudakov approximation agrees well with the exact when $|y_{t,\bar{t}}| \lesssim 1$.



"... it is clear that for the logarithmic approximation described be valid all Mandelstam variables \hat{s} , \hat{t} , \hat{u} must be very large, condition which is obviously not fulfilled at small/large scattering angles." [Weak corrections to gluon-induced top-antitop hadro-production]

[S. Moretti et al, PLB639 (2006) 513]

"The gluon induced part, in contrast, is markedly angular dependent. For large \hat{s} and small scattering angle the corrections are small, since the Sudakov-like behaviour cannot be expected in this case. At ninety degrees, in contrast, the Sudakov limit is applicable and the corrections become large." [Weak Interactions in Top-Quark Pair Production at Hadron Colliders: An Update]

J. H. Kühn et al, [arXiv:1305.5773]

Summary to $t\bar{t}$ production

- We implement EW corrections to the top-pair production in MCFM, making the calculation accessible to the public.
- Both EW Sudakov approximation and exact weak NLO are implemented in MCFM.
- Sudakov approximation works much better in quark-antiquark annihilation channel, in contrary to gluon-fusion channel which has a obvious discrepancy between Sudakov approximation and exact NLO in invariant mass distribution due to the information of angular dependence is missing in Sudakov approximation.
- With a scattering angle cut to gluon-fusion channel, we are able to get an agreement between both calculations.

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Di-jet production

- Processes under consideration:

- ▶ **quark-induced:** $q_i \bar{q}_i \rightarrow q_j \bar{q}_j$, and its crossing symmetries such as $q_i q_j \rightarrow q_i q_j$, etc.

- ▶ **gluon-induced:** $gg \rightarrow q \bar{q}$, and its crossing symmetries such as $gq \rightarrow qg$, etc.

- Processes calculated directly:

- ▶ $q_i \bar{q}_i \rightarrow q_j \bar{q}_j$, for both $i \neq j$ and $i = j$, respectively.

- ▶ $gg \rightarrow q \bar{q}$

- The rest of the production processes is obtained via crossing symmetries of the directly calculated production

Note: $q_{i,j}, q \in \{u, d, s, c\}$

Crossing symmetries

► All quark-induced production via crossing symmetries $i \neq j$

1 $q_i \bar{q}_i \rightarrow q_j \bar{q}_j$, **direct calculation**

2 $q_i q_j \rightarrow q_i q_j$, ($2 \rightarrow 3$, $3 \rightarrow 4$, $4 \rightarrow 2$; $s \rightarrow t$, $t \rightarrow u$, $u \rightarrow s$)

3 $\bar{q}_i q_i \rightarrow \bar{q}_j q_j$, ($1 \leftrightarrow 2$, $3 \leftrightarrow 4$; --)

4 $\bar{q}_i \bar{q}_j \rightarrow \bar{q}_i \bar{q}_j$, ($1 \rightarrow 3$, $3 \rightarrow 2$, $2 \rightarrow 1$; $s \rightarrow t$, $t \rightarrow u$, $u \rightarrow s$)

5 $q_i \bar{q}_j \rightarrow q_i \bar{q}_j$, ($2 \leftrightarrow 3$; $s \leftrightarrow t$)

6 $\bar{q}_i q_j \rightarrow \bar{q}_i q_j$, ($1 \rightarrow 3$, $3 \rightarrow 4$, $4 \rightarrow 2$, $2 \rightarrow 1$; $s \leftrightarrow t$)

7 $q_i \bar{q}_i \rightarrow q_i \bar{q}_i$, **direct calculation**

8 $\bar{q}_i q_i \rightarrow q_i \bar{q}_i$, ($1 \leftrightarrow 2$; $t \leftrightarrow u$)

9 $q_i q_i \rightarrow q_i q_i$, ($2 \rightarrow 3$, $3 \rightarrow 4$, $4 \rightarrow 2$; $s \rightarrow t$, $t \rightarrow u$, $u \rightarrow s$)

10 $\bar{q}_i \bar{q}_i \rightarrow \bar{q}_i \bar{q}_i$, ($1 \rightarrow 3$, $3 \rightarrow 2$, $2 \rightarrow 1$; $s \rightarrow t$, $t \rightarrow u$, $u \rightarrow s$)

where $12 \rightarrow 34$ denotes $q_i \bar{q}_i \rightarrow q_j \bar{q}_j$

Crossing symmetries

► All gluon-induced production via crossing symmetries

1 $gg \rightarrow q\bar{q}$, **direct calculation**

2 $gq \rightarrow gq$, ($2 \leftrightarrow 3, 3 \leftrightarrow 4, 4 \leftrightarrow$; $s \leftrightarrow t, t \leftrightarrow u, u \leftrightarrow s$)

3 $g\bar{q} \rightarrow g\bar{q}$, ($2 \rightarrow 3$; $s \leftrightarrow t$)

4 $qq \rightarrow qq$, ($1 \leftrightarrow 4$; $s \leftrightarrow t$)

5 $\bar{q}g \rightarrow \bar{q}g$, ($1 \rightarrow 2, 2 \rightarrow 4, 4 \rightarrow 3, 3 \rightarrow 1$; $s \leftrightarrow t$)

6 $q\bar{q} \rightarrow gg$, ($1 \leftrightarrow 3, 2 \leftrightarrow 4$; $t \leftrightarrow u$)

7 $\bar{q}q \rightarrow gg$ ($1 \leftrightarrow 4, 2 \leftrightarrow 3$; --)

8 $gg \rightarrow gg$, **no weak correction**

where $12 \rightarrow 34$ denotes $gg \rightarrow q\bar{q}$

Sudakov approximation to di-jet production

- EW corrections to QCD leading order
- Processes calculated directly:
 - I $\bar{q}_\rho^\lambda q_\rho^\lambda q_\sigma^\kappa \bar{q}_\sigma^\kappa \rightarrow 0$ (subprocesses 1 & 7 in four-quark category)
 - II $gg q_\sigma^\kappa \bar{q}_\sigma^\kappa \rightarrow 0$ (subprocess 1 in two-gluon-two-quark category)
- Calculations are analogous to that in $t\bar{t}$ production (i.e., taking massless limit of the top-quark $m_t \rightarrow 0$)

terms contribute to logarithmic corrections

- Universal correction independent of chirality

$$\sum_{f_\tau^\sigma} \left[-C_{f_\tau^\sigma}^{\text{ew}}(\mathbf{L}(\hat{s}) - 3 \cdot l_c) \right] |\mathcal{M}|_{\text{Born}}^2$$

- Angular dependence ($q\bar{q}$ channel)
- No Yukawa enhanced terms
- No parameter renormalization

One-loop weak corrections to di-jet production

- Structure of the full NLO calculation

- ▶ QCD & EW LO cross sections of $\mathcal{O}(\alpha_s^2, \alpha_s \alpha, \alpha^2)$
- ▶ fixed $\mathcal{O}(\alpha_s^2 \alpha)$:

$$d\hat{\sigma}(\alpha_s^2 \alpha) \propto \begin{cases} 2\text{Re} [\mathcal{M}(\alpha_s \alpha) \cdot \mathcal{M}^*(\alpha_s)] \\ 2\text{Re} [\mathcal{M}(\alpha_s^2) \cdot \mathcal{M}^*(\alpha)] \end{cases}$$

- Input settings

$$G_\mu = 1.16637 \times 10^{-5} \text{ GeV}^{-2},$$

$$M_W = 80.398 \text{ GeV}, \quad M_Z = 91.1876 \text{ GeV},$$

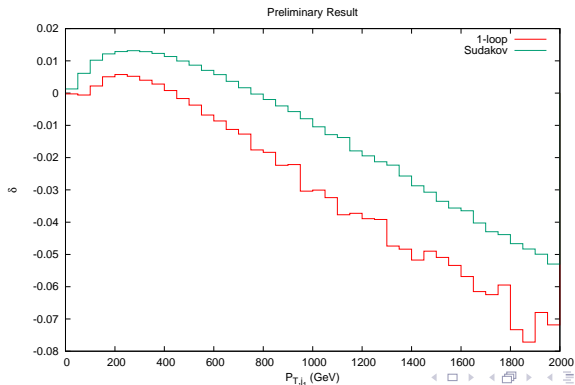
$$\Gamma_W = 2.141 \text{ GeV}, \quad \Gamma_Z = 2.4952 \text{ GeV},$$

$$\mu_R = \mu_F = p_{T,1}.$$

Comparison with Sudakov approximation (preliminary)

- Comparison between Sudakov approximation and 1-loop exact calculations at LHC = 14 TeV

$$|p_{T,j}| > 25 \text{ GeV}, |y_j| < 2.5; \text{ anti} - k_t, R = 0.6$$



Conclusion and outlook

- The EW radiative corrections are very important at the LHC due to the Sudakov logarithmic terms.
- We have completed the implementation of both the Sudakov and exact weak NLO corrections to NC-DY and top-pair production into MCFM.
- In top pair production, sudakov approximation works better in quark-antiquark annihilation channel; while it deviates off the exact NLO corrections in gluon-fusion channel due to the missing information on angular dependence.
- The implementation of EW corrections to dijet production in MCFM is ongoing.
- We would like to continue, for instance, with implementation for ZZ/WW production etc.