

Heavy hadron production asymmetry at the LHC from heavy quark recombination mechanism

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D^\pm PRODUCTION ASYMMETRY

Asymmetry in D^\pm partial width:

$$a_{CP}^f = \frac{\Gamma(D^+ \rightarrow f) - \Gamma(D^- \rightarrow \bar{f})}{\Gamma(D^+ \rightarrow f) + \Gamma(D^- \rightarrow \bar{f})} \quad (1)$$

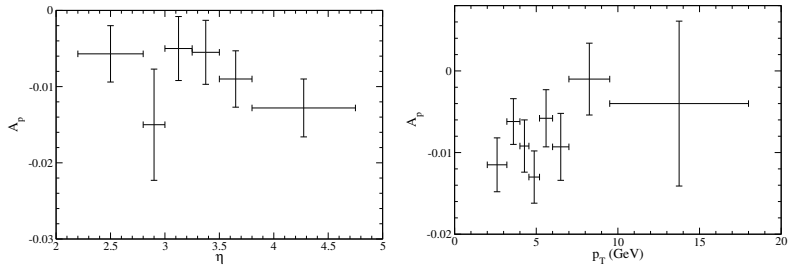
- ▶ Signal for CP violation
- ▶ Expected to be $\lesssim \mathcal{O}(0.1\%)$
- ▶ Measurement affected by D^\pm production asymmetry
 \implies Need good theoretical prediction for production asymmetry

D^\pm production asymmetry:

$$A_p = \frac{\sigma(D^+) - \sigma(D^-)}{\sigma(D^+) + \sigma(D^-)} \quad (2)$$

LHCb¹:

$A_p = -0.96 \pm 0.26 \pm 0.18\%$ at 7 TeV ($2.0 \text{ GeV} < p_T < 18 \text{ GeV}, 2.2 < \eta < 4.75$)



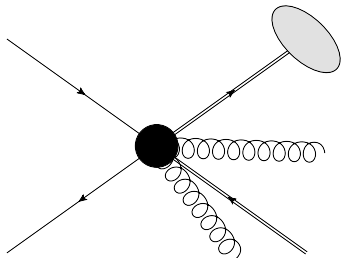
Surplus of D^- ($d\bar{c}$) over D^+ ($\bar{d}c$)

¹R. Aaij et al. (LHCb Collaboration) (2013) [1210.4112]

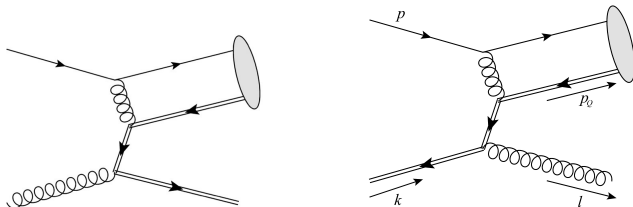
Standard perturbative QCD:

$$d\sigma[pp \rightarrow D + X] = \sum_{i,j} f_{i/p} \otimes f_{j/p} \otimes d\hat{\sigma}[ij \rightarrow c + X] \otimes D_{c \rightarrow D} \quad (3)$$

- ▶ Gives $A_p = 0$
- ▶ Neglect $1/p_T$ corrections



Heavy quark recombination mechanism²:



²E. Braaten, Y. Jia and T. Mehen (2002) [hep-ph/0108201]

$$(a) \quad d\hat{\sigma}[\bar{D}] = d\hat{\sigma}[qg \rightarrow (\bar{c}q)^n + c]\rho[(\bar{c}q)^n \rightarrow \bar{D}] \quad (4a)$$

$$(b) \quad d\hat{\sigma}[\bar{D}] = d\hat{\sigma}[q\bar{c} \rightarrow (\bar{c}q)^n + g]\rho[(\bar{c}q)^n \rightarrow \bar{D}] \quad (4b)$$

$$(c) \quad d\hat{\sigma}[\bar{D}] = d\hat{\sigma}[\bar{q}g \rightarrow (c\bar{q})^n + \bar{c}]\rho[(c\bar{q})^n \rightarrow H] \otimes D_{\bar{c} \rightarrow \bar{D}} \quad (4c)$$

$(\bar{c}q)^n$: $\bar{c}q$ pair with relative momentum $\sim \Lambda_{QCD}$ at state $n = 2S+1 L_J^{(1,8)}$

$\rho[(\bar{c}q)^n \rightarrow \bar{D}]$: probability for $(\bar{c}q)^n$ to hadronize into \bar{D}

- ▶ $d\hat{\sigma}$ suppressed by $\alpha_s \left(\frac{m_Q}{p_T}\right)^2$ relative to Eq. (3) at large p_T
- ▶ $\rho \sim \Lambda_{QCD}/m_Q$ at leading power
- ▶ Successfully applied to explain asymmetries in fixed target experiments

ρ at leading power:

$$\begin{aligned} \rho_1^{sm} &= \rho[c\bar{d}(^1S_0^{(1)}) \rightarrow D^+] & \rho_1^{sf} &= \rho[c\bar{d}(^3S_1^{(1)}) \rightarrow D^+] \\ \rho_8^{sm} &= \rho[c\bar{d}(^1S_0^{(8)}) \rightarrow D^+] & \rho_8^{sf} &= \rho[c\bar{d}(^3S_1^{(8)}) \rightarrow D^+] \end{aligned} \quad (5)$$

Heavy quark spin symmetry:

$$\begin{aligned} \rho[c\bar{d}(^1S_0^{(c)}) \rightarrow D^+] &= \rho[c\bar{d}(^3S_1^{(c)}) \rightarrow D^{*+}] \\ \rho[c\bar{d}(^3S_1^{(c)}) \rightarrow D^+] &= \rho[c\bar{d}(^1S_0^{(c)}) \rightarrow D^{*+}] \end{aligned} \quad (6)$$

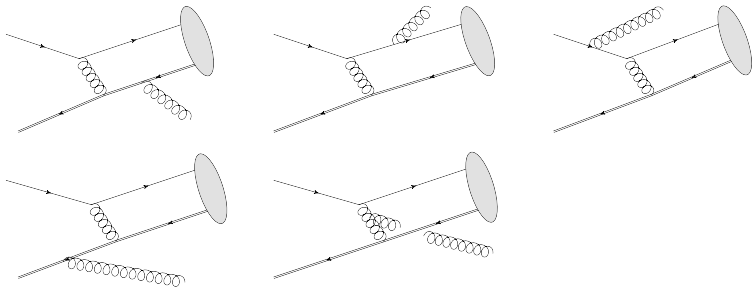
$d\hat{\sigma}[qg \rightarrow (\bar{c}q)^n + c]$ calculated by Braaten et al.
 We calculate $d\hat{\sigma}[q\bar{c} \rightarrow (\bar{c}q)^n + g]$:

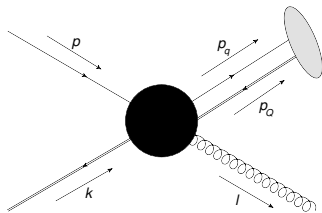
$$\begin{aligned}
 \frac{d\hat{\sigma}}{d\hat{t}}[\bar{Q}q(^1S_0^{(1)})] &= \frac{2\pi^2\alpha_s^3}{243} \frac{m_Q^2}{S^3} \left[\frac{64S^2}{T^2} - \frac{m_Q^2 S}{UT} \left(79 - \frac{112S}{U} - \frac{64S^2}{U^2} \right) + \frac{16m_Q^4}{U^2} \left(1 - \frac{8S}{U} \right) \right] \\
 \frac{d\hat{\sigma}}{d\hat{t}}[\bar{Q}q(^3S_1^{(1)})] &= \frac{2\pi^2\alpha_s^3}{243} \frac{m_Q^2}{S^3} \left[\frac{64S^2}{T^2} \left(1 + \frac{2S^2}{U^2} \right) - \frac{m_Q^2}{T} \left(28 - \frac{4U}{S} - \frac{19S}{U} - \frac{368S^2}{U^2} + \frac{64S^3}{U^3} \right) \right. \\
 &\quad \left. + \frac{48m_Q^4}{U^2} \left(1 - \frac{8S}{U} \right) \right] \\
 \frac{d\hat{\sigma}}{d\hat{t}}[\bar{Q}q(^1S_0^{(8)})] &= \frac{4\pi^2\alpha_s^3}{243} \frac{m_Q^2}{S^3} \left[\left(9 + \frac{9S}{T} + \frac{4S^2}{T^2} \right) - \frac{m_Q^2}{T} \left(\frac{9U}{S} - \frac{79S}{2U} - \frac{7S^2}{U^2} - \frac{4S^3}{U^3} \right) \right. \\
 &\quad \left. - \frac{m_Q^4}{U^2} \left(8 + \frac{8S}{U} + \frac{9U}{S} \right) \right] \\
 \frac{d\hat{\sigma}}{d\hat{t}}[\bar{Q}q(^3S_1^{(8)})] &= \frac{4\pi^2\alpha_s^3}{243} \frac{m_Q^2}{S^3} \left[\left(16 + \frac{13U}{T} + \frac{14T}{U} + \frac{12U^2}{T^2} + \frac{8T^2}{U^2} \right) \right. \\
 &\quad \left. + \frac{m_Q^2}{T} \left(158 + \frac{133U}{S} + \frac{233S}{2U} + \frac{5S^2}{U^2} - \frac{4S^3}{U^3} \right) \right. \\
 &\quad \left. - \frac{3m_Q^4}{U^2} \left(8 + \frac{8S}{U} + \frac{9U}{S} \right) \right]
 \end{aligned} \tag{7}$$

$$S = \hat{s} - m_Q^2 = (k+p)^2 - m_Q^2, T = \hat{t} = (k-p_Q)^2, U = \hat{u} - m_Q^2 = (k-l)^2 - m_Q^2$$

Illustrating the method:

Do a tree level matching for $d\hat{\sigma}[\bar{D}] = d\hat{\sigma}[q\bar{c} \rightarrow (\bar{c}q)^n + g]\rho[(\bar{c}q)^n \rightarrow \bar{D}]$





In rest frame of p_Q , $p_q \sim \mathcal{O}(\Lambda_{QCD})$. So take the leading singular piece for $p_q \rightarrow 0$.

$$\mathcal{M} = g^3 \text{Tr} \left[v(p_Q) \bar{u}(p_q) \left(\frac{A_1}{2p \cdot p_q} + \frac{A_2}{2l \cdot p_q} \right) \right] \quad (8)$$

where

$$A_1 = \epsilon_\nu T^b \gamma_\mu u(p) \bar{v}(k) \left\{ T^b \gamma^\mu \frac{1}{-(\not{p}_Q + \not{l}) - m_Q} T^a \gamma^\nu + T^a \gamma^\nu \frac{1}{\not{l} - \not{k} - m_Q} T^b \gamma^\mu \right. \\ \left. + i f^{abc} T^c \frac{[(-\not{l} - \not{p})g^{\mu\nu} + 2p^\nu \gamma^\mu + 2l^\mu \gamma^\nu]}{(k - p_Q)^2} \right\} \\ A_2 = -\epsilon_\nu \frac{T^a \gamma^\nu \not{l} T^b \gamma^\mu u(p) \bar{v}(k) T^b \gamma_\mu}{(k - p_Q)^2} \quad (9)$$

For $\bar{Q}q(^1S_0^{(1)})$, $v_i(p_Q)\bar{u}_j(p_q) \rightarrow \frac{\delta_{ij}}{\sqrt{N_c}}m_Q(\not{p}_Q - m_Q)\gamma_5$

Define ρ in HQET:

$$\rho[\bar{Q}q(^1S_0^{(1)}) \rightarrow \bar{H}] = \frac{1}{2m_Q} \int \frac{d\eta_1}{\eta_1} \int \frac{d\eta_2}{\eta_2} W(\eta_1, \eta_2) \quad (10)$$

$$W(\eta_1, \eta_2) = -\frac{1}{4} \int \frac{d\omega_1}{2\pi} \int \frac{d\omega_2}{2\pi} e^{-i\eta_1\omega_1 + i\eta_2\omega_2} \langle 0 | \bar{h}_v(0) \gamma_5 q(\omega_2 v) a_{\bar{H}}^\dagger a_{\bar{H}}(\omega_1 v) \gamma_5 h_v(0) | 0 \rangle \quad (11)$$

- ▶ Easily see $\rho \sim \Lambda_{QCD}/m_Q$ by power counting
- ▶ $1/\eta$ absorbs IR divergence $1/\Lambda_{QCD}$ of partonic diagrams

$$\rho[\bar{Q}q(^1S_0^{(1)}) \rightarrow \bar{Q}q(^1S_0^{(1)})] = \frac{N_c m_Q^2}{(v \cdot p_q)^2} + \mathcal{O}(\alpha_s) \quad (12)$$

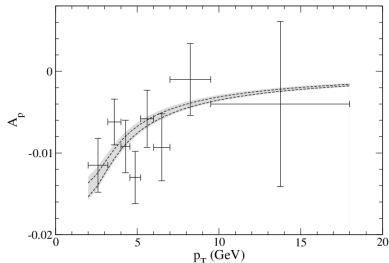
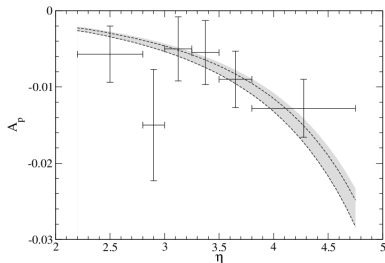
So tree-level matching is equivalent to

$$\begin{aligned} v_i(p_Q)\bar{u}_j(p_q) &\rightarrow \frac{\delta_{ij}}{N_c} m_Q(\not{p}_Q - m_Q)\gamma_5 \rho[\bar{Q}q(^1S_0^{(1)}) \rightarrow \bar{H}] \\ \frac{1}{p \cdot p_q} &\rightarrow \frac{1}{p \cdot p_Q} \\ \frac{1}{l \cdot p_q} &\rightarrow \frac{1}{l \cdot p_Q} \end{aligned} \quad (13)$$

Similarly for $^1S_0^{(8)}$, $^3S_1^{(1)}$, $^3S_1^{(8)}$

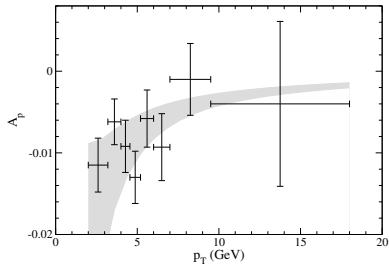
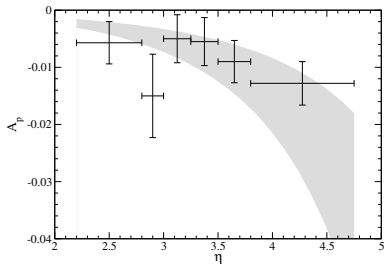
Result

- ▶ Use ρ_1^{sm} and ρ_8^{sm} determined from fixed target experiments with single-parameter fit. Set $\rho_1^{sf} = \rho_8^{sf}$ and fit to data.
- ▶ Include feeddown from $D^{*\pm}$
- ▶ Restrict H in (c) to be D or D^* only; sum over $\bar{q} = \bar{u}, \bar{d}$ and \bar{s} with $SU(3)$ flavor symmetry assumed
- ▶ Use Peterson fragmentation function $D_{c \rightarrow H}(z) = \frac{N_H}{z(1-\frac{1}{z} - \frac{\epsilon_c}{1-z})^2}$ (N_H and ϵ_c from ZEUS Collaboration)
- ▶ Take $\mu_f = \sqrt{p_T^2 + m_Q^2}$. Use MSTW 2008 LO PDFs. Use LO cross section for the standard pQCD part.



Grey band from varying the ρ s in the intervals $0.055 < \rho_1^{sm} < 0.065$, $0.65 < \rho_8^{sm} < 0.8$, $0.24 < \rho_1^{sf} < 0.30$ and $0.24 < \rho_8^{sf} < 0.30$ respectively. Dashed lines from varying $0.055 < \epsilon_c < 0.69$.

Integrated A_p : $-0.88\% < A_p < -1.07\%$ (data: $A_p = -0.96 \pm 0.26 \pm 0.18\%$)



A_p distributions with $\frac{1}{2}\sqrt{p_T^2 + m_Q^2} < \mu_f < 2\sqrt{p_T^2 + m_Q^2}$

BARYON PRODUCTION ASYMMETRY

No data from LHCb yet. Here we simply make an order-of-magnitude prediction.

Production asymmetry of Λ_Q (udQ):

$$A_p = \frac{\sigma(\Lambda_Q) - \sigma(\bar{\Lambda}_Q)}{\sigma(\Lambda_Q) + \sigma(\bar{\Lambda}_Q)} \quad (14)$$

$$(a) \quad d\hat{\sigma}[\Lambda_Q] = d\hat{\sigma}[qg \rightarrow (Qq)^n + \bar{Q}] \eta_{inc}[(Qq)^n \rightarrow \Lambda_Q] \quad (15)$$

$$(b) \quad d\hat{\sigma}[\Lambda_Q] = d\hat{\sigma}[Qq \rightarrow (Qq)^n + g] \eta_{inc}[(Qq)^n \rightarrow \Lambda_Q] \quad (16)$$

$$(c) \quad d\hat{\sigma}[\Lambda_Q] = \sum_n d\hat{\sigma}[qg \rightarrow (\bar{Q}q)^n + Q] \sum_{\bar{H}_{meson}} \rho[(\bar{Q}q)^n \rightarrow \bar{H}_{meson}] \otimes D_{Q \rightarrow \Lambda_Q} \quad (17)$$

$$(d) \quad d\hat{\sigma}[\Lambda_Q] = \sum_n d\hat{\sigma}[\bar{q}g \rightarrow (\bar{Q}\bar{q})^n + Q] \sum_{\bar{H}_{baryon}} \eta[(\bar{Q}\bar{q})^n \rightarrow \bar{H}_{baryon}] \otimes D_{Q \rightarrow \Lambda_Q} \quad (18)$$

H taken to be a low-lying heavy hadron

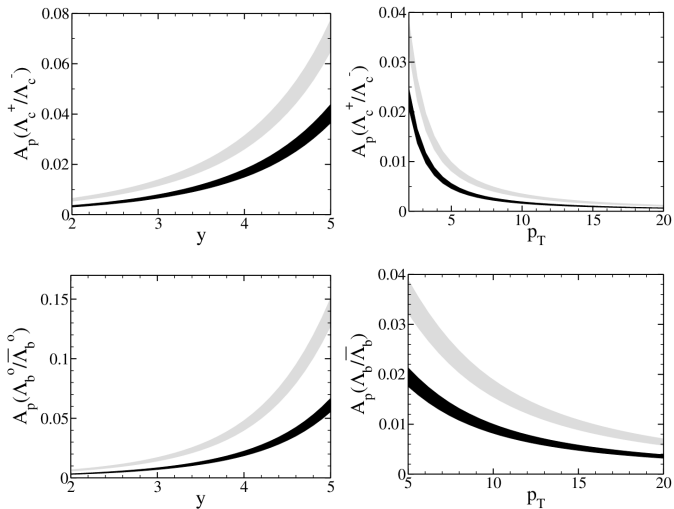
$$\eta_{inc}[(Qq)^n \rightarrow \Lambda_Q] = \eta[(Qq)^n \rightarrow \Lambda_Q] + \sum_{H_{baryon} \neq \Lambda_Q} \eta[(Qq)^n \rightarrow H_{baryon}] B[H_{baryon} \rightarrow \Lambda_Q + X] \quad (19)$$

$$\sum_{\bar{H}_{baryon}} \eta[(\bar{Q}\bar{q})^n \rightarrow \bar{H}_{baryon}] \approx \frac{3}{2} \eta_{inc}[(Qq)^n \rightarrow \Lambda_Q] \quad (20)$$

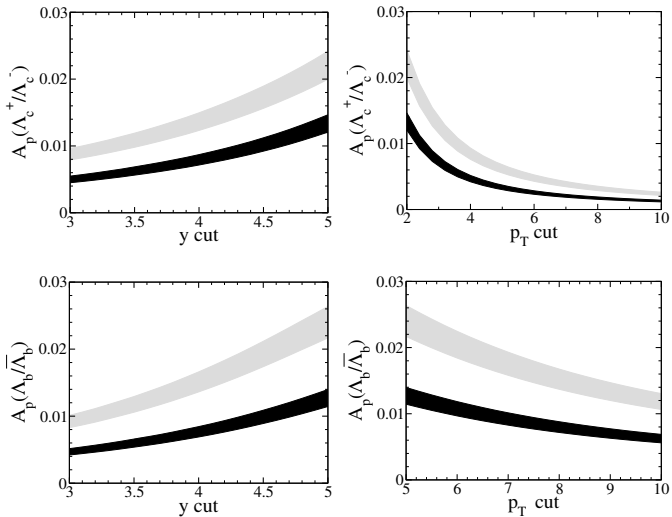
η at leading power:

$$\begin{aligned}\eta_3 &= \eta[Qq(^1S_0^{(\bar{3})}) \rightarrow \Lambda_Q] & \tilde{\eta}_3 &= \eta[Qq(^3S_1^{(\bar{3})}) \rightarrow \Lambda_Q] \\ \eta_6 &= \eta[Qq(^1S_0^{(6)}) \rightarrow \Lambda_Q] & \tilde{\eta}_6 &= \eta[Qq(^3S_1^{(6)}) \rightarrow \Lambda_Q]\end{aligned}\tag{21}$$

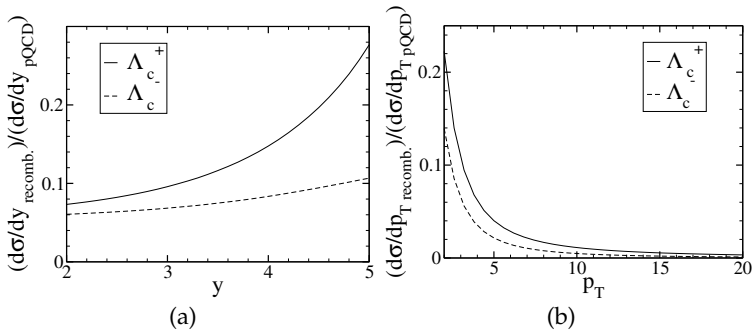
- ▶ Use same values of ρ_s as for D^\pm case
- ▶ For Λ_c^\pm production, use $\tilde{\eta}_{3,inc}$ determined from fixed-target experiment with single-parameter fit. Set $\eta_{3,inc} = \eta_{6,inc} = \tilde{\eta}_{6,inc} = 0$.
- ▶ For η_s for Λ_b and ρ_s for B , simply multiply Λ_c and D counterparts by the theoretical scaling factor m_c/m_b
- ▶ Take $D_{Q \rightarrow \Lambda_Q}(z) = f_{\Lambda_Q} \delta(1-z)$



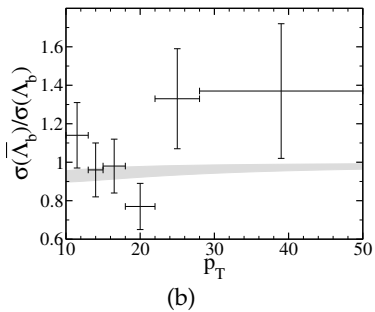
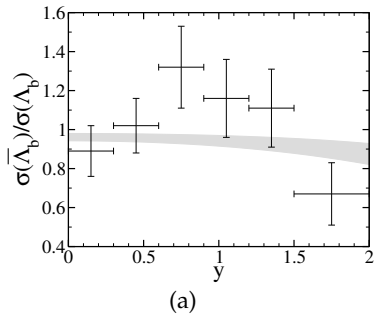
A_p distributions, $2 < y < 5$ and $2 \text{ GeV} < p_T < 20 \text{ GeV}$ in 7 TeV (grey band) and 14 TeV (black band) pp collisions



Integrated A_p versus cuts, $2 < y < 5$ and $2 \text{ GeV} < p_T < 20 \text{ GeV}$ in 7 TeV (grey band) and 14 TeV (black band) pp collisions



$d\sigma_{recomb.}/d\sigma_{pQCD}$ distributions in 7 TeV pp collisions.



Data at 7 TeV from CMS (S. Chatrchyan et al. (CMS Collaboration) (2012) [1205.0594]). Grey band from heavy quark recombination mechanism with all η_{inc} s set equal to each other, with $0.2 < \eta_{inc} < 1$.

OUTLOOK

- ▶ Global fit for ρ in D^\pm production asymmetry (mostly done)
- ▶ NLO calculation of heavy quark recombination mechanism. Add soft Wilson lines to definition of ρ :

$$\rho[\bar{Q}q(^1S_0^{(1)}) \rightarrow \bar{H}] = \frac{1}{2m_Q} \int \frac{d\eta_1}{\eta_1} \int \frac{d\eta_2}{\eta_2} W(\eta_1, \eta_2) \quad (22)$$

$$W(\eta_1, \eta_2) = -\frac{1}{4} \int \frac{d\omega_1}{2\pi} \int \frac{d\omega_2}{2\pi} e^{-i\eta_1\omega_1 + i\eta_2\omega_2} \langle 0 | \bar{h}_v(0) \gamma_5 S(0, \omega_2 v) q(\omega_2 v) a_{\bar{H}}^\dagger a_{\bar{H}} \bar{q}(\omega_1 v) \gamma_5 S(\omega_1 v, 0) h_v(0) | 0 \rangle \quad (23)$$

(in progress)

- ▶ Compare with predictions from other models of soft QCD processes

Thank you.