

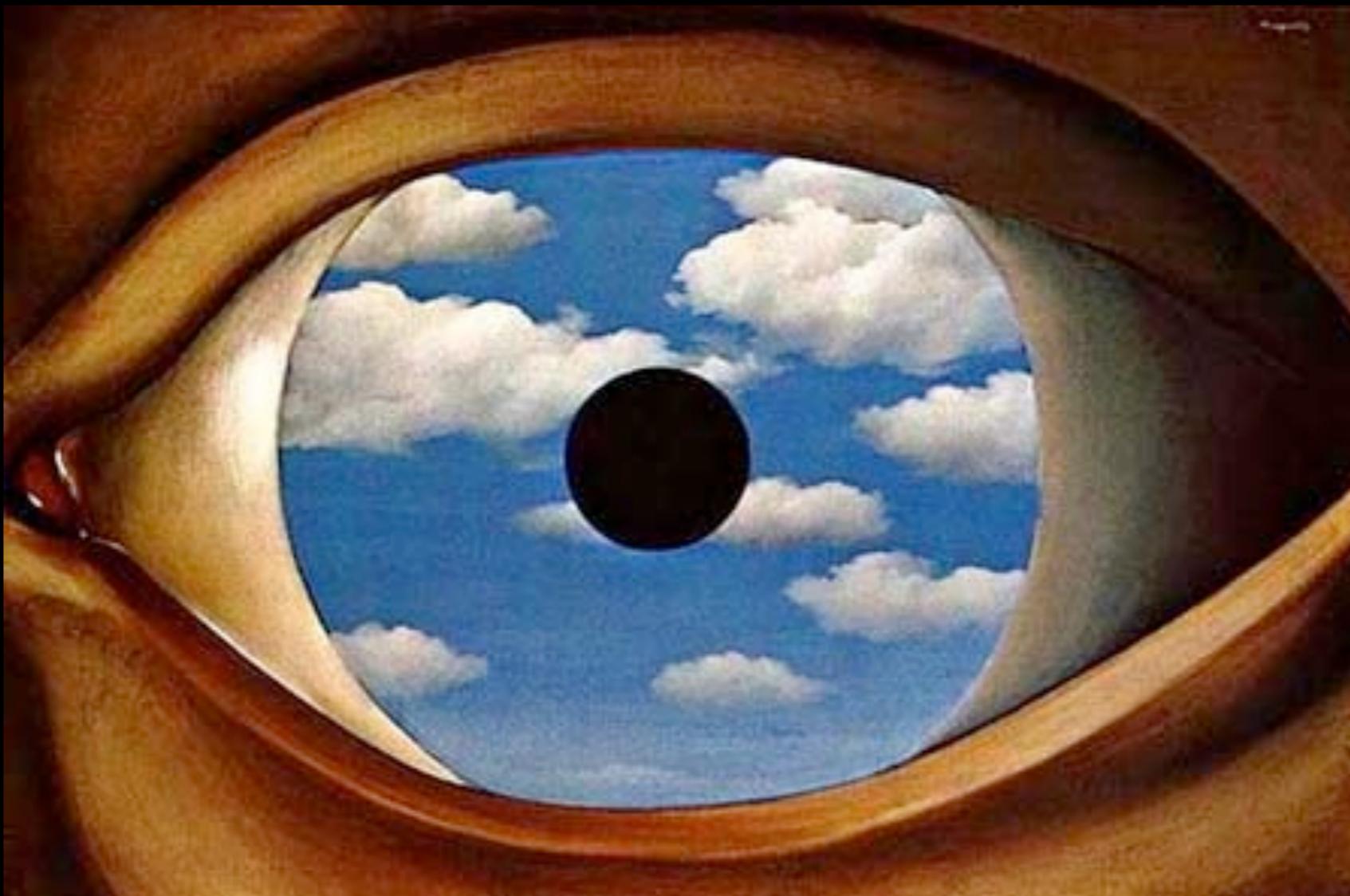
Direct Detection of Dark Matter

From Microphysics to Observational Signatures

James Dent

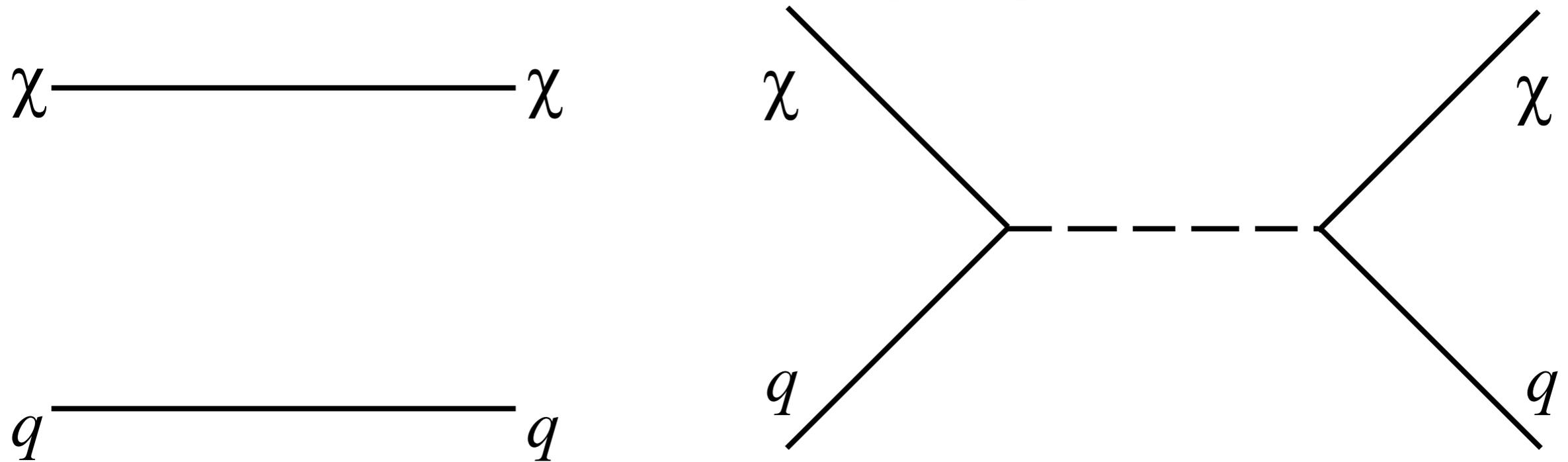
JBD, L.M. Krauss, J.L. Newstead, and S. Sabharwal, arXiv: 1505.03117

Texas A&M May 18, 2015



Direct Detection: Standard Approach

Model WIMP-nuclear interactions as WIMP-quark/gluon interactions



Hadronic matrix elements encode nucleon interactions

$$\langle N_o | m_q \bar{q} q | N_i \rangle \longrightarrow f_T^N \bar{N} N$$

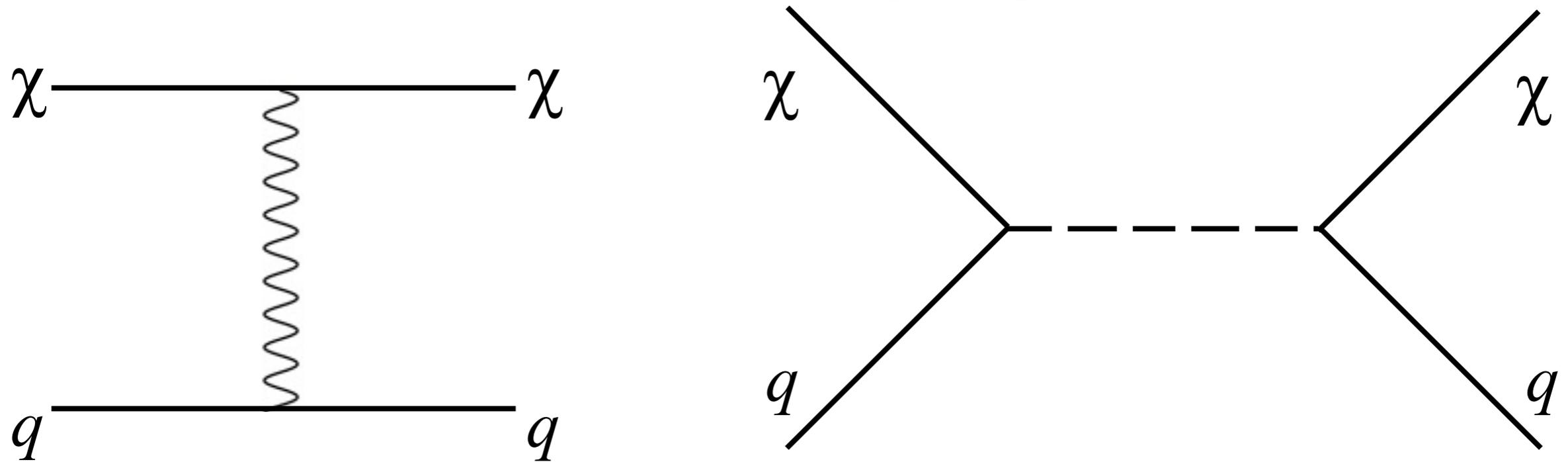
$$\langle N_o | \bar{q} \gamma^5 q | N_i \rangle \longrightarrow \Delta_{\tilde{q}}^N \bar{N} \gamma^5 N$$

$$\langle N_o | \bar{q} \gamma^\mu q | N_i \rangle \longrightarrow \mathcal{N}_q^N \bar{N} \gamma^\mu N$$

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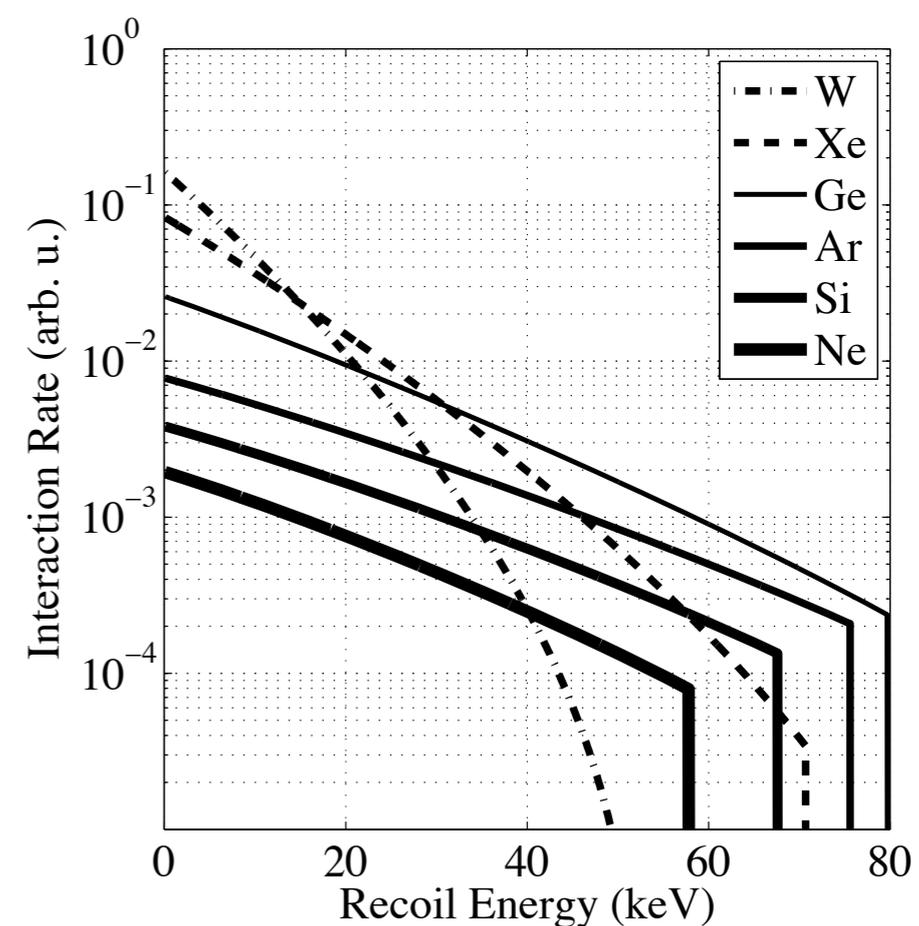
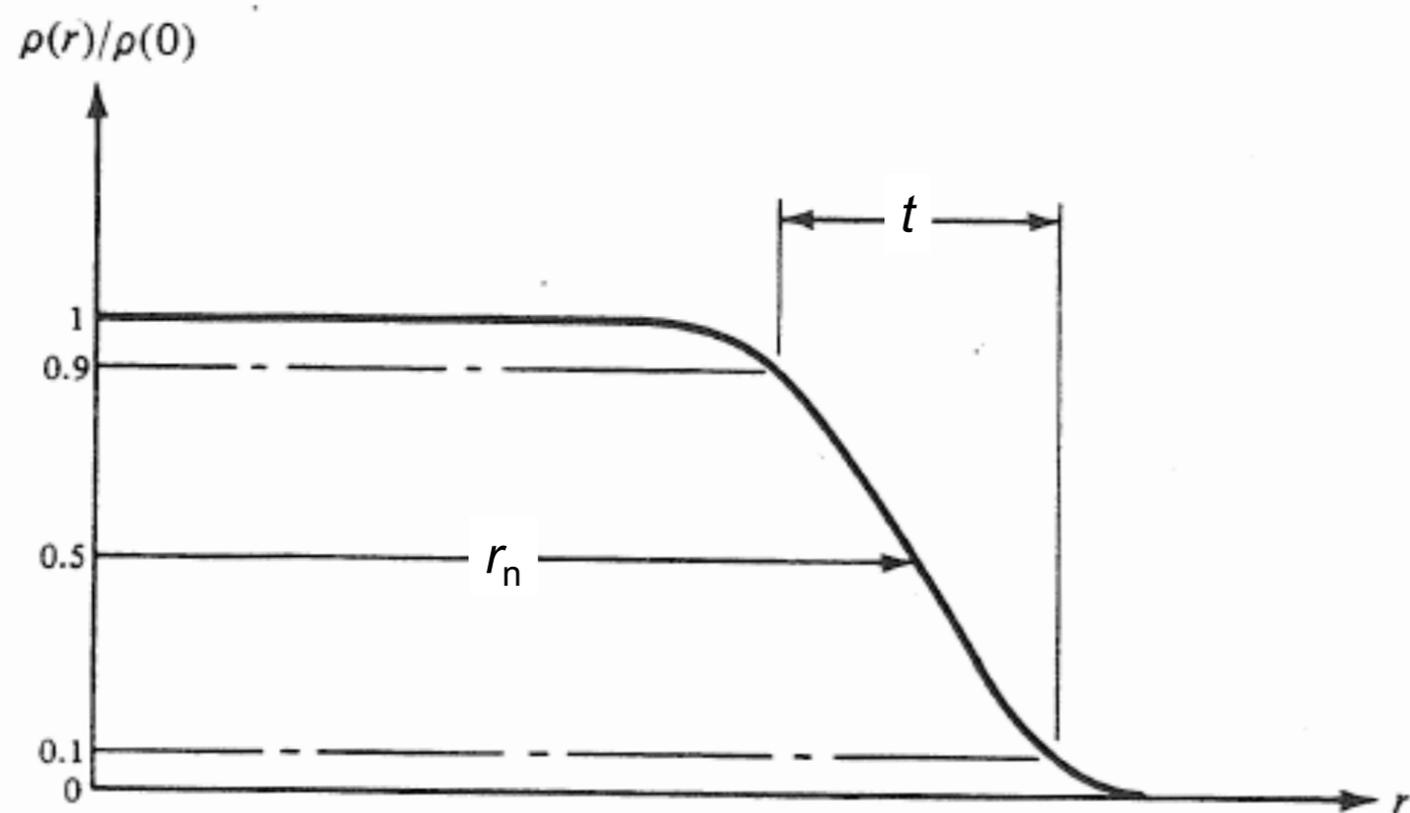
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Interaction types include coupling to nuclear charge (spin-independent) or spin (spin-dependent), giving two nuclear response types

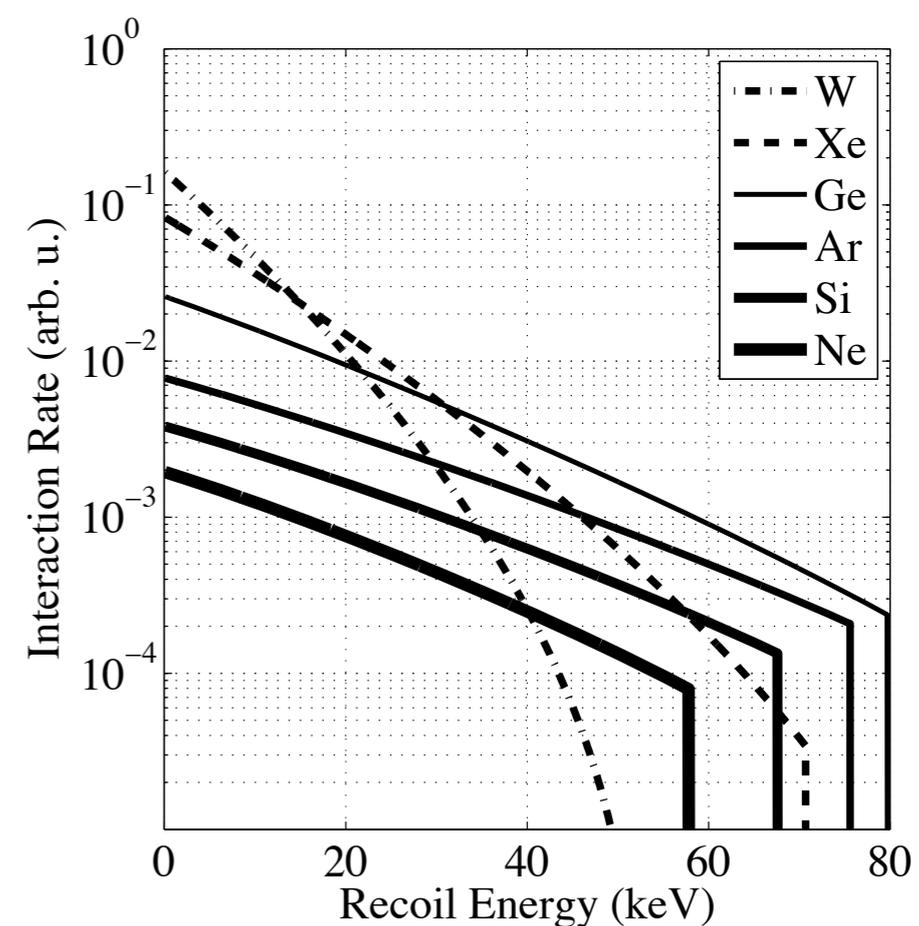
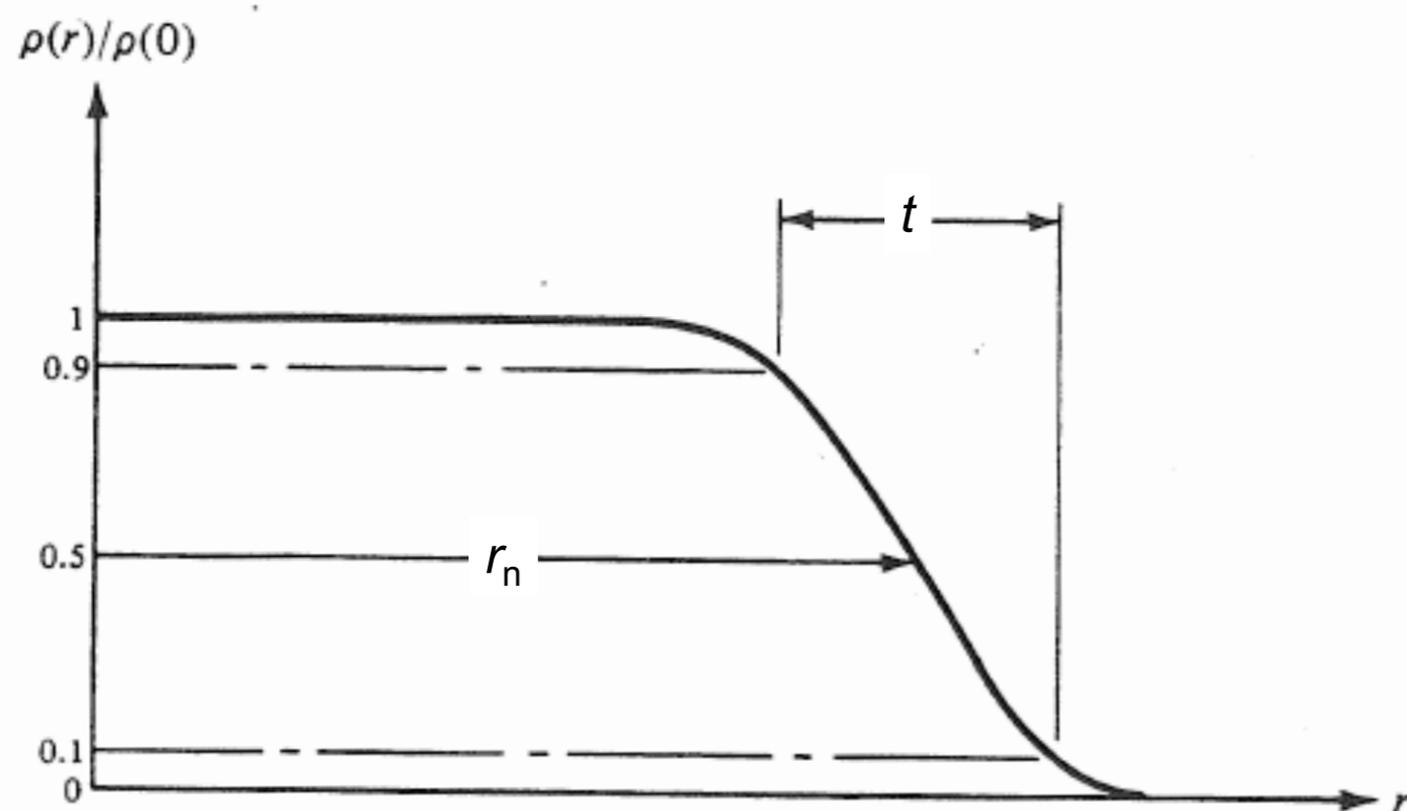
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Target specific nuclear physics is also taken into account

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R. Schnee, arXiv:1101.5205

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counts/ton/day/keV

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$$\mu_A \equiv M_\chi M_A / (M_\chi + M_A)$$

WIMP-nucleon scattering is factorized

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Nucleon spin expectation values

$$\sigma_{\text{SI}} \equiv \frac{4\mu_n^2 f_n^2}{\pi}$$

Coherent scattering

It has been shown that the standard approach neglects a large set of possible non-relativistic operators beyond the SI/SD ones

$$1_{\chi}1_N \qquad \vec{S}_{\chi} \cdot \vec{S}_N$$

There also exist four more nuclear responses that arise in the most general nucleus-WIMP elastic scattering

$$M, \Phi'', \Sigma', \Delta, \Sigma'', \tilde{\Phi}'$$

A.L. Fitzpatrick, W.C. Haxton, E. Katz, N. Lubbers, and Y. Xu, JCAP 1302 (2013) 004, arXiv:1203.3542
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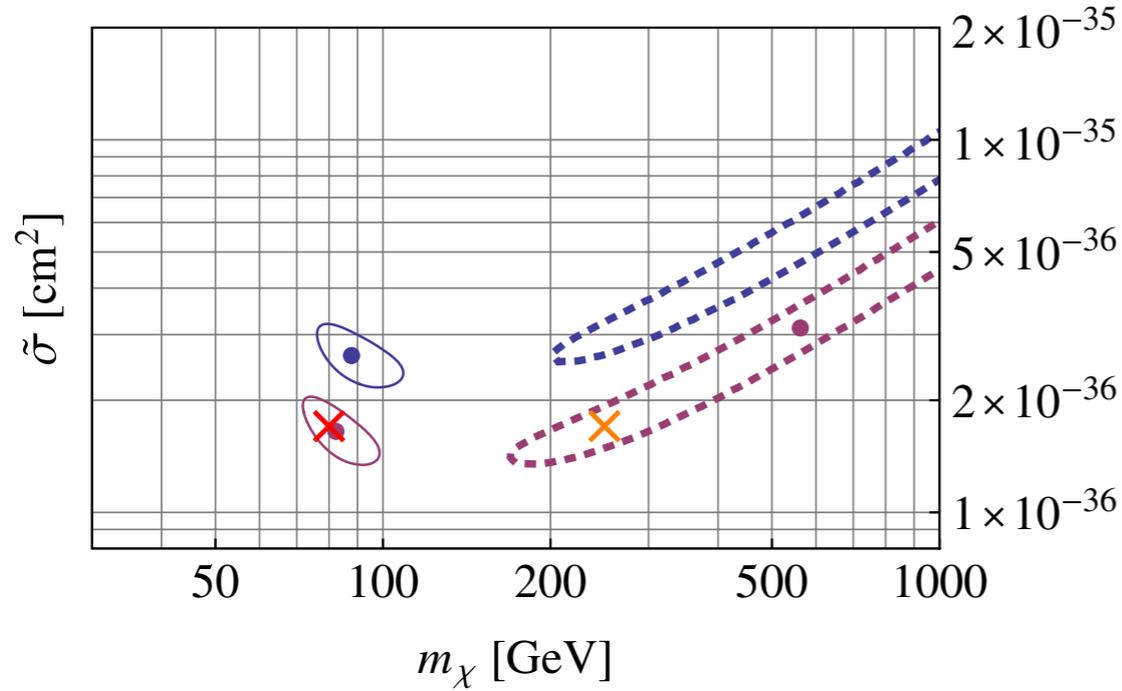
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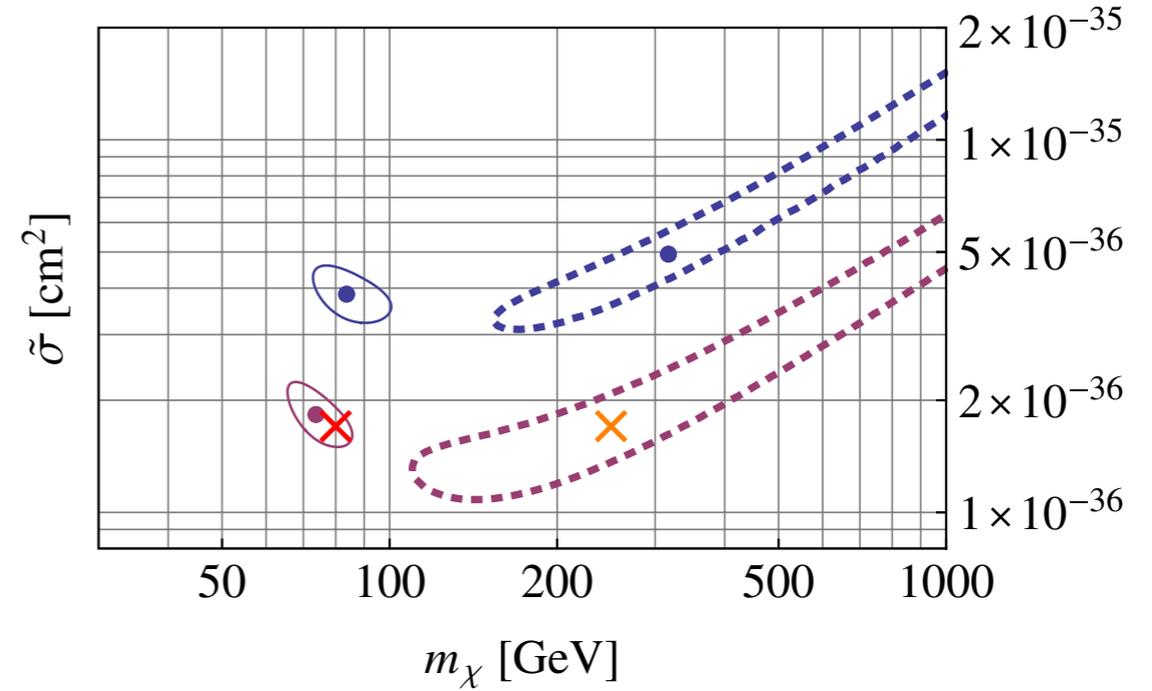
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Gresham & Zurek (2014) showed that wildly incorrect interpretations are possible if only the standard SI/SD responses are used

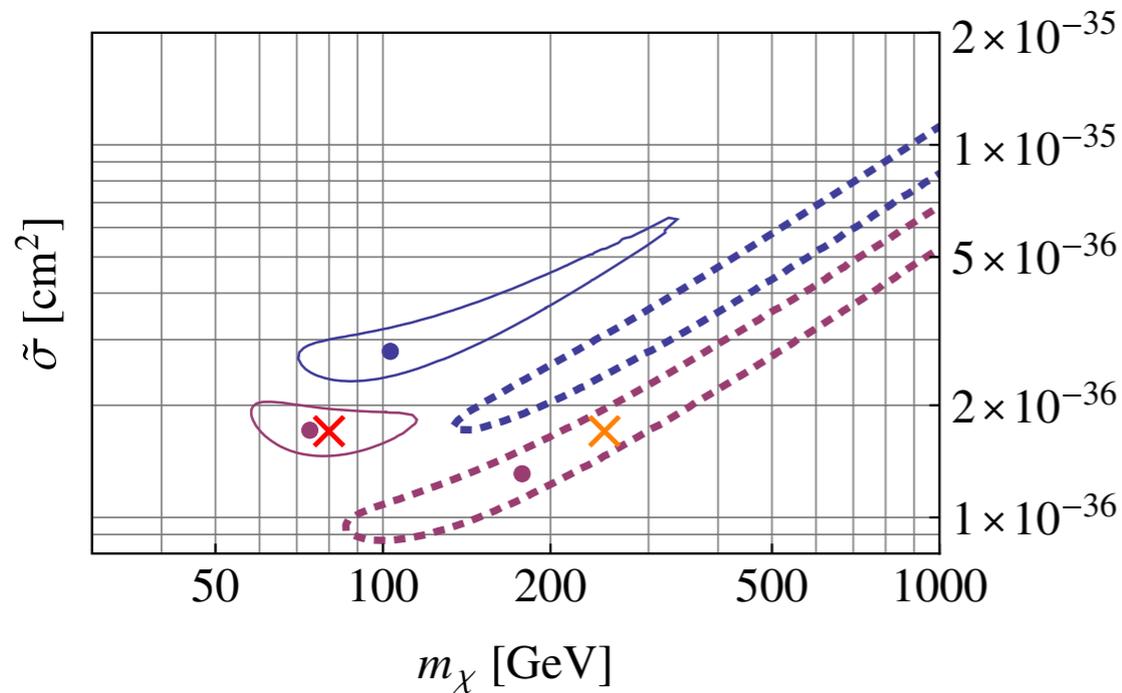
I target, 100 events with $E_R < 100$ keV



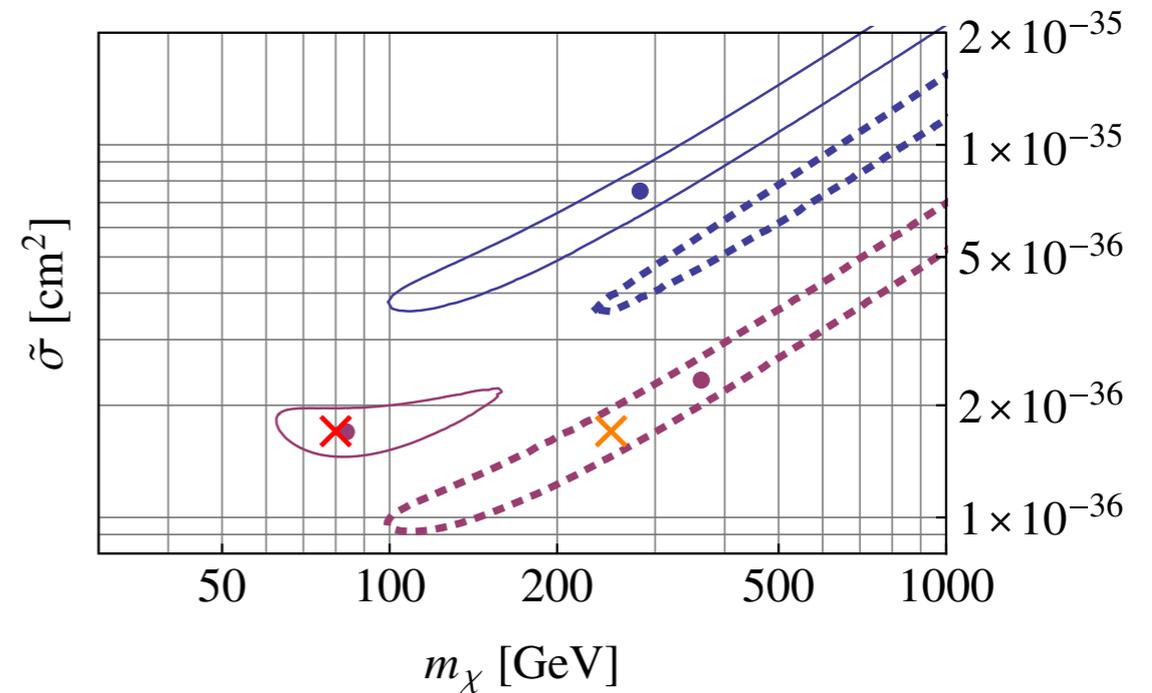
Xe target, 100 events with $E_R < 100$ keV



I target, 100 events with $E_R < 50$ keV



Xe target, 100 events with $E_R < 50$ keV



$$\langle \phi(x_1) \cdots \phi(x_k) \rangle_J \equiv e^{-iW[J]} \int \mathcal{D}\phi [\phi(x_1) \cdots \phi(x_k)] e^{iW[\phi]}$$

$$iW[J] = \int \mathcal{D}\phi \exp \left\{ i \int d^4x [\mathcal{L}[\phi] + J\phi] \right\}$$

Effective Field Theory

$$\Gamma[\varphi] \equiv W[J(\varphi)] - \int d^4x$$

Incorporating Galilean invariance, energy conservation, and Hermiticity, all non-relativistic operators will be built out of four quantities

$$\boxed{\text{Exchanged momentum}} \quad i \frac{\vec{q}}{m_N}, \quad \vec{v}^\perp, \quad \vec{S}_\chi, \quad \vec{S}_N \quad \boxed{\text{Nucleon spin}}$$

$$\boxed{\text{DM spin}}$$

Relative velocities

$$\vec{v}^\perp = \frac{1}{2} (\vec{v}_{\chi,in} - \vec{v}_{N,in} + \vec{v}_{\chi,out} - \vec{v}_{N,out}) \quad \vec{v}^\perp \cdot \vec{q} = 0$$

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There are fifteen combinations of these operators

\mathcal{O}_1	$1_\chi 1_N$	\mathcal{O}_8	$\vec{S}_\chi \cdot \vec{v}^\perp$
\mathcal{O}_2	$(\vec{v}^\perp)^2$	\mathcal{O}_9	$i\vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_N})$
\mathcal{O}_3	$i\vec{S}_N \cdot (\frac{\vec{q}}{m_N} \times \vec{v}^\perp)$	\mathcal{O}_{10}	$i\frac{\vec{q}}{m_N} \cdot \vec{S}_N$
\mathcal{O}_4	$\vec{S}_\chi \cdot \vec{S}_N$	\mathcal{O}_{11}	$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$
\mathcal{O}_5	$i\vec{S}_\chi \cdot (\frac{\vec{q}}{m_N} \times \vec{v}^\perp)$	\mathcal{O}_{12}	$\vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp)$
\mathcal{O}_6	$(\frac{\vec{q}}{m_N} \cdot \vec{S}_N)(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi)$	\mathcal{O}_{13}	$i(\vec{S}_\chi \cdot \vec{v}^\perp)(\frac{\vec{q}}{m_N} \cdot \vec{S}_N)$
\mathcal{O}_7	$\vec{S}_N \cdot \vec{v}^\perp$	\mathcal{O}_{14}	$i(\vec{S}_N \cdot \vec{v}^\perp)(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi)$
		\mathcal{O}_{15}	$-(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}) \left((\vec{S}_N \times \vec{v}^\perp) \cdot \frac{\vec{q}}{m_N} \right)$

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Spin-independent

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 \mathcal{O}_2

$(\vec{v}^\perp)^2$

 \mathcal{O}_3

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 \mathcal{O}_8

$\vec{S}_\chi \cdot \vec{v}^\perp$

 \mathcal{O}_9

$i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N}\right)$

 \mathcal{O}_{10}

$i\frac{\vec{q}}{m_N} \cdot \vec{S}_N$

 \mathcal{O}_{11}

$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$

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$\vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp)$

 \mathcal{O}_5

$i\vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right)$

 \mathcal{O}_{13}

$i(\vec{S}_\chi \cdot \vec{v}^\perp) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right)$

 \mathcal{O}_6

$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right)$

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 \mathcal{O}_7

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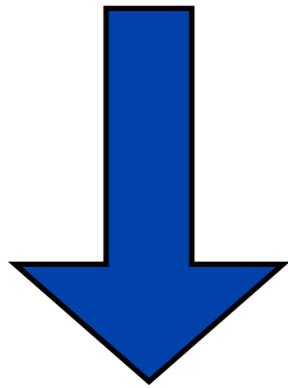
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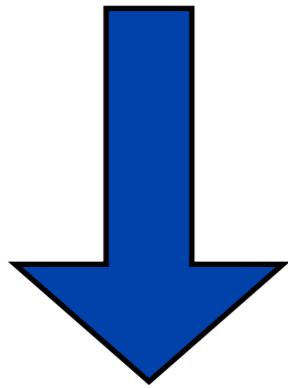
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$$c_1 1_\chi 1_N$$

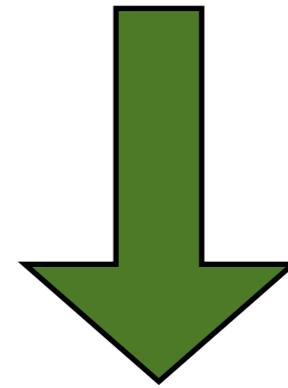
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$$-4c_4 \vec{S}_\chi \cdot \vec{S}_N$$

From the relativistic EFT there are 20 combinations of fermionic bilinears

From two scalar $\bar{\chi}\chi$ $\bar{\chi}\gamma^5\chi$ 2×2

$\bar{\chi}\gamma^\mu\chi$ $\bar{\chi}\gamma^\mu\gamma^5\chi$

and four vector terms 4×4

$P^\mu\bar{\chi}\chi$ $P^\mu\bar{\chi}\gamma^5\chi$

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In general one can write down the non-relativistic Lagrangian

$$\mathcal{L}_{NR} = \sum_{\alpha=n,p} \sum_{i=1}^{15} c_i^\alpha \mathcal{O}_i^\alpha$$

General isospin couplings can be incorporated

$$\mathcal{L}_{NR} = \sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \mathcal{O}_i t^\tau$$

The total interaction can be considered as a sum over single nucleon interactions

$$\sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \mathcal{O}_i t^\tau \rightarrow \sum_{\tau=0,1} \sum_{i=1}^{15} c_i^\tau \sum_{j=1}^A \mathcal{O}_i(j) t^\tau(j)$$

The DM-nucleon interactions can then be written

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot \vec{Q} + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

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Nuclear

DM

$$S = \sum_{i=1}^A e^{-i\vec{q}\cdot\vec{x}_i}$$

$$T = \sum_{i=1}^A \frac{1}{2M} \left[-\frac{1}{i} \overleftarrow{\nabla}_i \cdot \vec{\sigma}(i) e^{-i\vec{q}\cdot\vec{x}_i} + e^{-i\vec{q}\cdot\vec{x}_i} \vec{\sigma}(i) \cdot \frac{1}{i} \overrightarrow{\nabla}_i \right]$$

$$\vec{P} = \sum_{i=1}^A \vec{\sigma}(i) e^{-i\vec{q}\cdot\vec{x}_i}$$

$$\vec{Q} = \sum_{i=1}^A \frac{1}{2M} \left[-\frac{1}{i} \overleftarrow{\nabla}_i e^{-i\vec{q}\cdot\vec{x}_i} + e^{-i\vec{q}\cdot\vec{x}_i} \frac{1}{i} \overrightarrow{\nabla}_i \right]$$

$$\vec{R} = \sum_{i=1}^A \frac{1}{2M} \left[\overleftarrow{\nabla}_i \times \vec{\sigma}(i) e^{-i\vec{q}\cdot\vec{x}_i} + e^{-i\vec{q}\cdot\vec{x}_i} \vec{\sigma}(i) \times \overrightarrow{\nabla}_i \right]$$

Given a non-relativistic reduction, one can identify the dark matter operator coefficients

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot Q + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

Nuclear

DM

$$l_0^\tau = c_1^\tau + ic_5^\tau \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}_T^\perp \right) + c_8^\tau (\vec{S}_\chi \cdot \vec{v}_T^\perp) + ic_{11}^\tau \frac{\vec{q} \cdot \vec{S}_\chi}{m_N}$$

$$l_0^{A\tau} = -\frac{1}{2} \left[c_7^\tau + ic_{14}^\tau \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \right]$$

$$\vec{l}_5^\tau = \frac{1}{2} \left[c_3^\tau i \frac{(\vec{q} \times \vec{v}_T^\perp)}{m_N} + c_4^\tau \vec{S}_\chi + c_6^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) \vec{q}}{m_N^2} + c_7^\tau \vec{v}_T^\perp + ic_9^\tau \frac{(\vec{q} \times \vec{S}_\chi)}{m_N} + ic_{10}^\tau \frac{\vec{q}}{m_N} \right. \\ \left. c_{12}^\tau (\vec{v}_T^\perp \times \vec{S}_\chi) + ic_{13}^\tau \frac{(\vec{S}_\chi \cdot \vec{v}_T^\perp) \vec{q}}{m_N} + ic_{14}^\tau \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \vec{v}_T^\perp + c_{15}^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) (\vec{q} \times \vec{v}_T^\perp)}{m_N^2} \right]$$

$$\vec{l}_M^\tau = c_5^\tau \left(i \frac{\vec{q}}{m_N} \times \vec{S}_\chi \right) - \vec{S}_\chi c_8^\tau$$

$$\vec{l}_E^\tau = \frac{1}{2} \left[c_3^\tau \frac{\vec{q}}{m_N} + ic_{12}^\tau \vec{S}_\chi - c_{13}^\tau \frac{(\vec{q} \times \vec{S}_\chi)}{m_N} - ic_{15}^\tau \frac{(\vec{q} \cdot \vec{S}_\chi) \vec{q}}{m_N^2} \right]$$

These coefficients apply to the dark matter in and out states

The dark matter-nucleus amplitude can be written as

$$\mathcal{M} = \sum_{\tau=0,1} \langle j_\chi, M_\chi; j_N, M_N | \{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot \vec{Q} + \vec{l}_E^\tau \cdot \vec{R} \} t^\tau(i) | j_\chi, M_\chi; j_N, M_N \rangle$$

which can further be reduced to the standard nuclear electroweak responses

$$\begin{aligned} \mathcal{M} = & \sum_{\tau=0,1} \langle j_\chi, M_{\chi f}; j_N, M_{Nf} | \left(\sum_{J=0} \sqrt{4\pi(2J+1)} (-i)^J \left[l_0^\tau M_{J0;\tau} - i l_0^{A\tau} \frac{q}{m_N} \tilde{\Omega}_{J0;\tau}(q) \right] \right. \\ & + \sum_{J=1} \sqrt{2\pi(2J+1)} (-i)^J \sum_{\lambda \pm 1} (-1)^\lambda \left\{ l_{5\lambda}^\tau [\lambda \Sigma_{J-\lambda;\tau}(q) + i \Sigma'_{J-\lambda;\tau}(q)] \right. \\ & \left. - i \frac{q}{m_N} l_{M\lambda}^\tau [\lambda \Delta_{J-\lambda;\tau}(q)] - i \frac{q}{m_N} l_{E\lambda}^\tau [\lambda \tilde{\Phi}_{J-\lambda;\tau}(q) + i \tilde{\Phi}'_{J-\lambda;\tau}(q)] \right\} \\ & \left. + \sum_{J=0}^{\infty} \sqrt{4\pi(2J+1)} (-i)^J \left[i l_{50}^\tau \Sigma''_{J0;\tau}(q) + \frac{q}{m_N} l_{M0}^\tau \tilde{\Delta}''_{J0;\tau}(q) + \frac{q}{m_N} l_{E0}^\tau \tilde{\Phi}''_{J0;\tau}(q) \right] \right) | j_\chi, M_{\chi i}; j_N, M_{Ni} \rangle \end{aligned}$$

Assuming P and CP are good symmetries of the nuclear ground state leaves one with 6 responses

$$M_{JM}(q\vec{x}) \equiv j_J(qx)Y_{JM}(\Omega_x)$$

$$M, \Phi'', \Sigma', \Delta, \Sigma'', \tilde{\Phi}'$$

~~$$\vec{M}_{JL}^M \equiv j_J(qx)\vec{Y}_{JLM}(\Omega_x)$$~~

$$\Delta_{JM} \equiv \vec{M}_{JJ}^M(qx_i) \cdot \frac{1}{q}\vec{\nabla}_i$$

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To calculate cross-sections, one needs to square the amplitude, average over initial spins and sum over final states.

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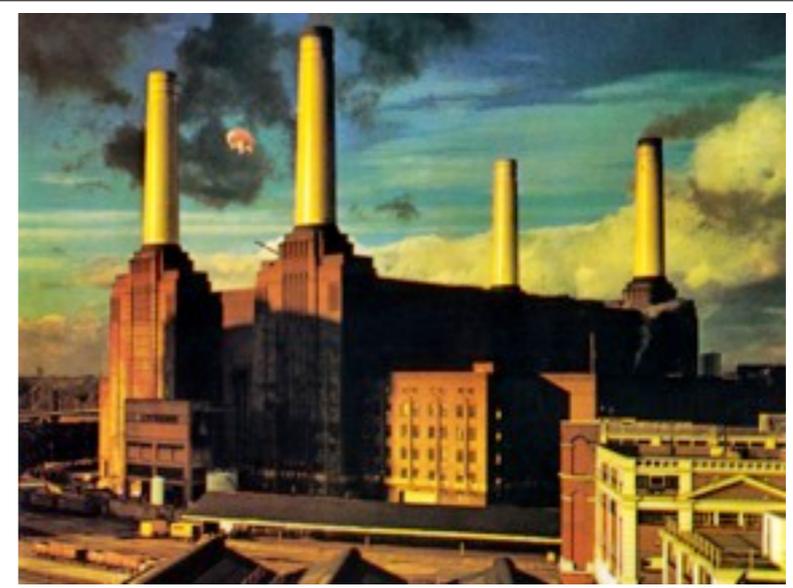
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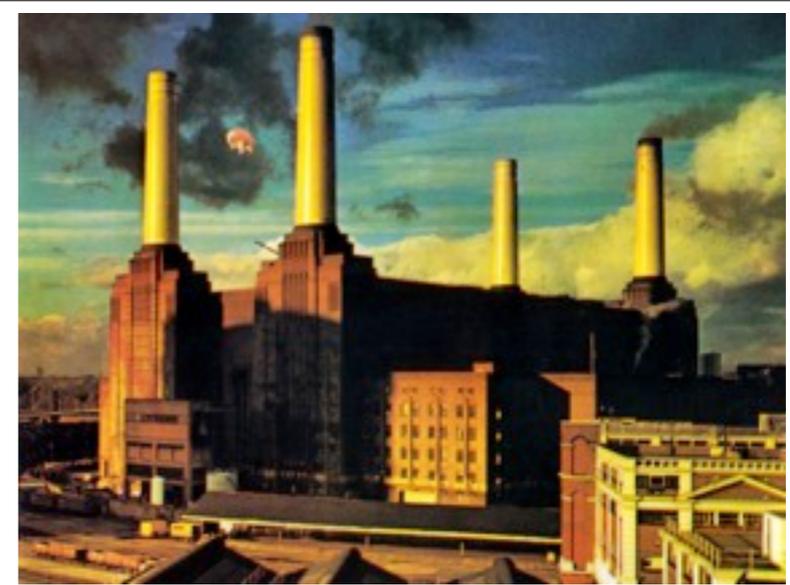
P. Agrawal, Z. Chacko, C. Kilic, and R.K. Mishra, arXiv:1003.1912

N. Anand, A.L. Fitzpatrick, and W.C. Haxton, Phys.Rev. C89, 065501 (2014)



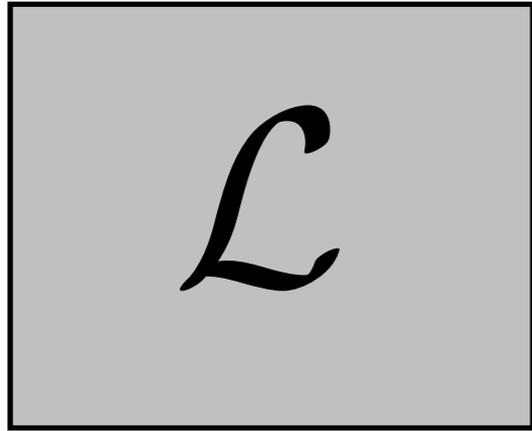
JBD, L.M. Krauss, J.L. Newstead, and S. Sabharwal, arXiv: 1505.03117

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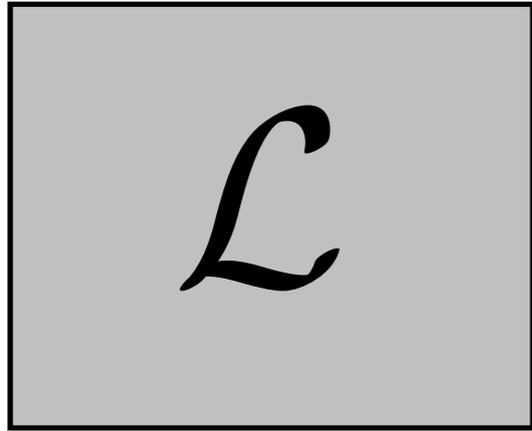
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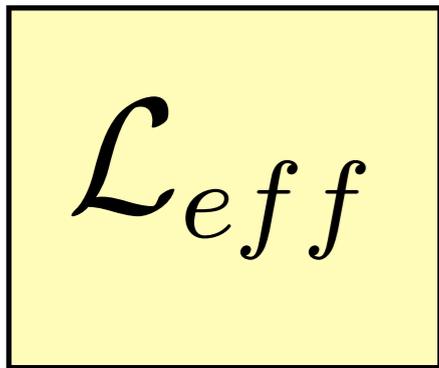
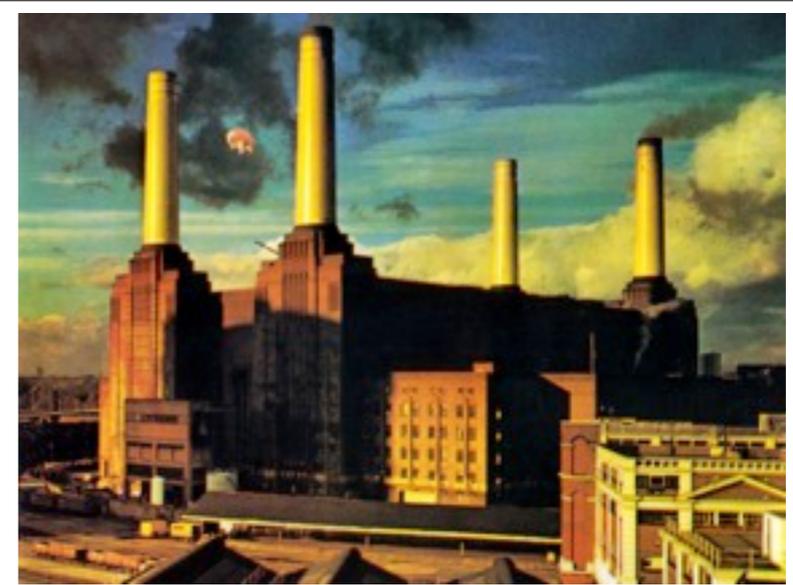
$$q\phi \quad \phi\chi$$



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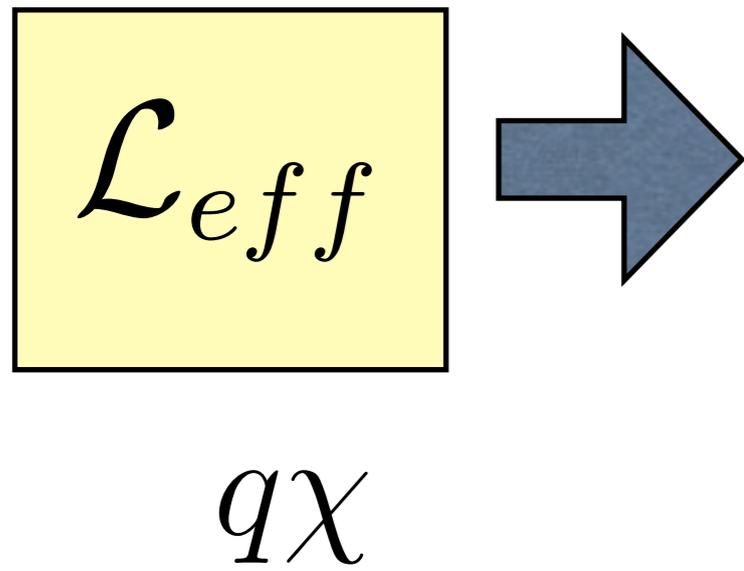
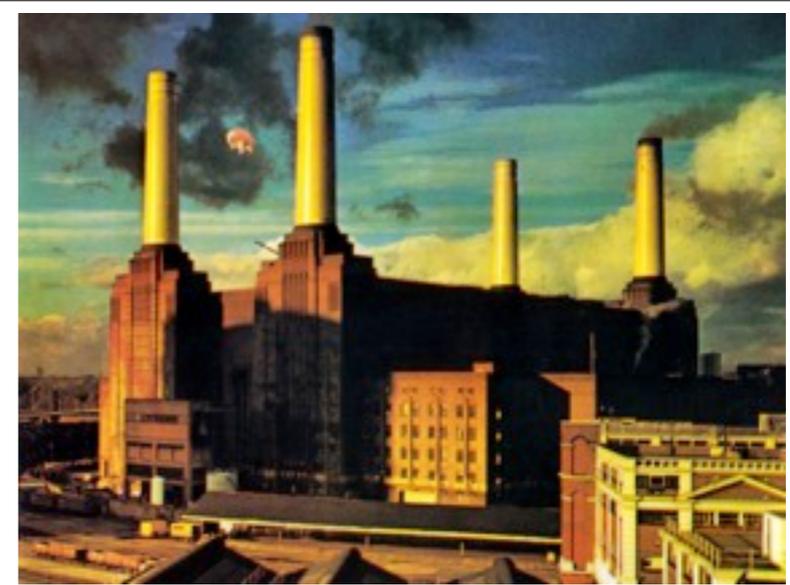
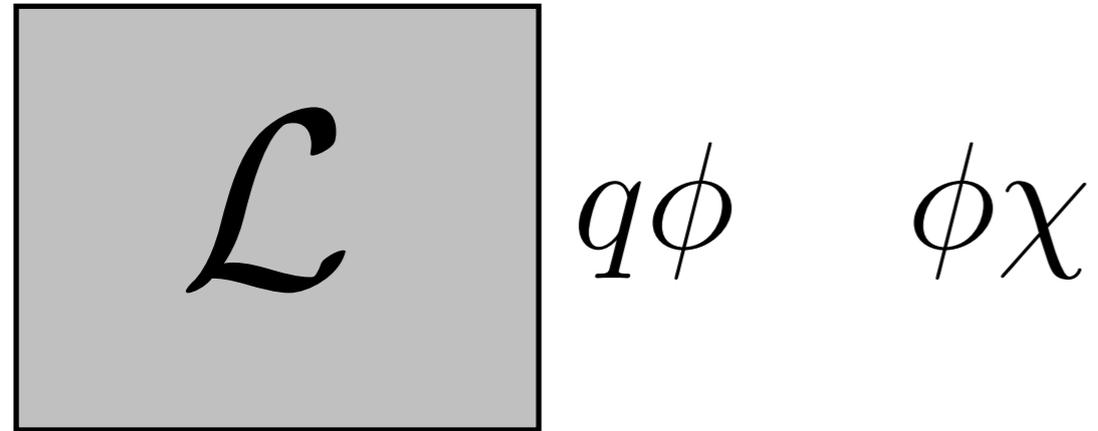


$q\phi$ $\phi\chi$



$q\chi$

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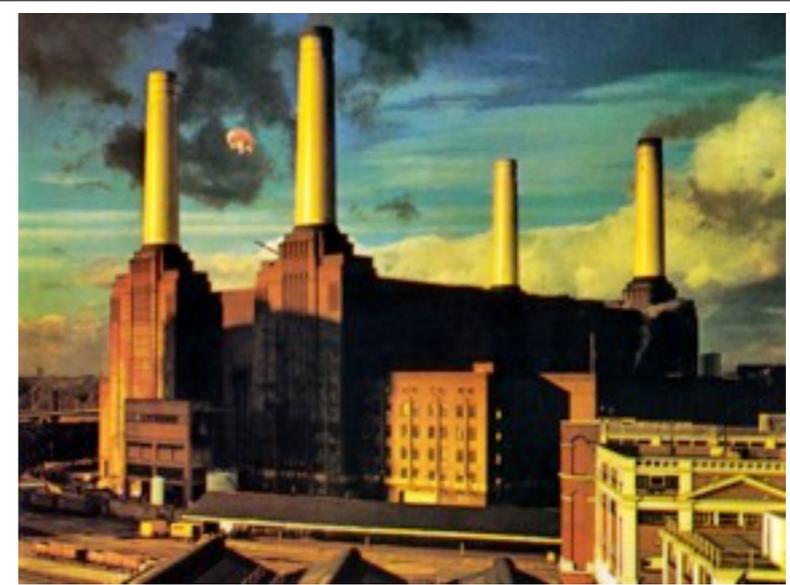


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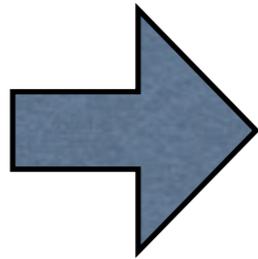
$$\mathcal{L}$$

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$$\mathcal{L}_{eff}$$



$$\langle N_o | m_q \bar{q}q | N_i \rangle$$
$$\longrightarrow f_{Tq}^N \bar{N}N$$

$$q\chi$$

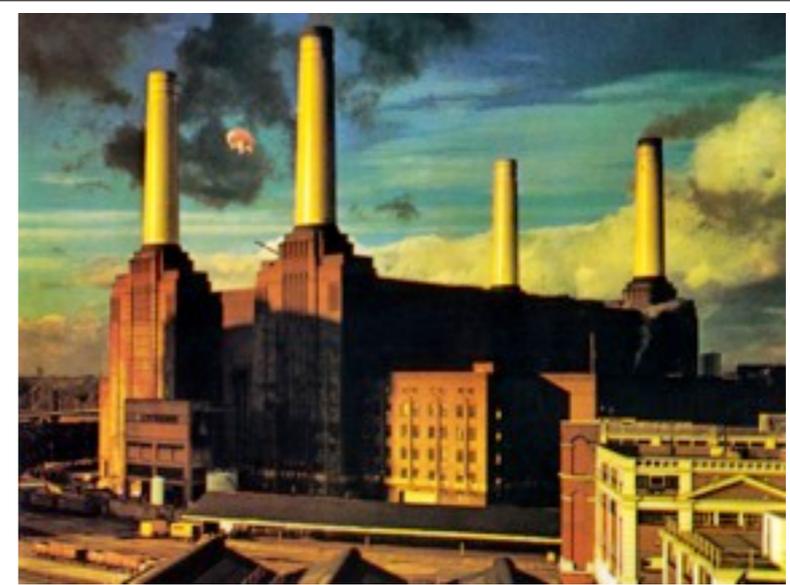
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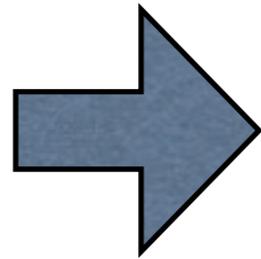
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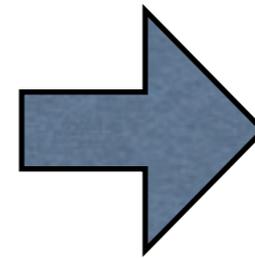


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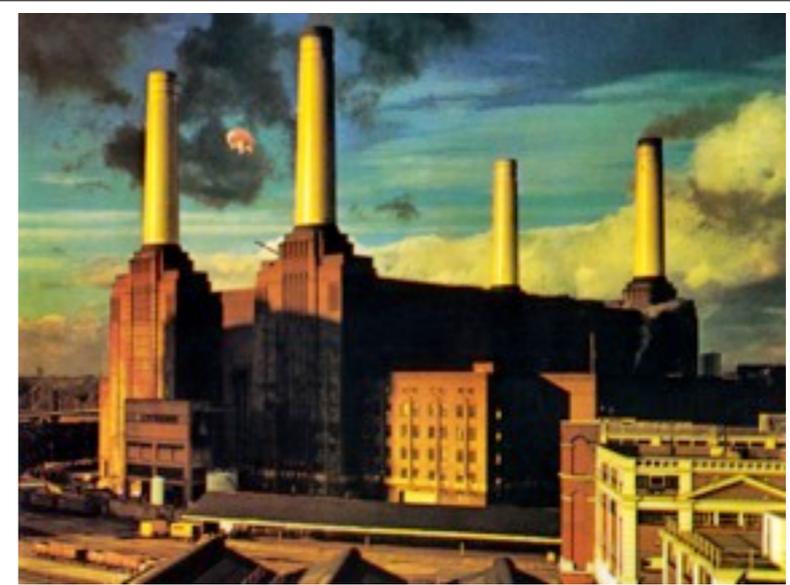
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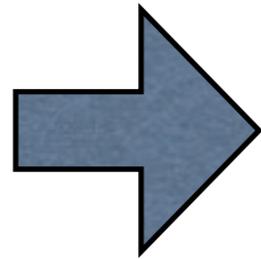
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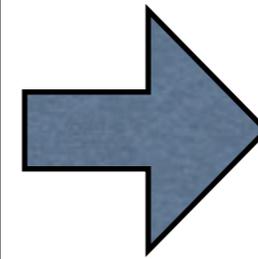


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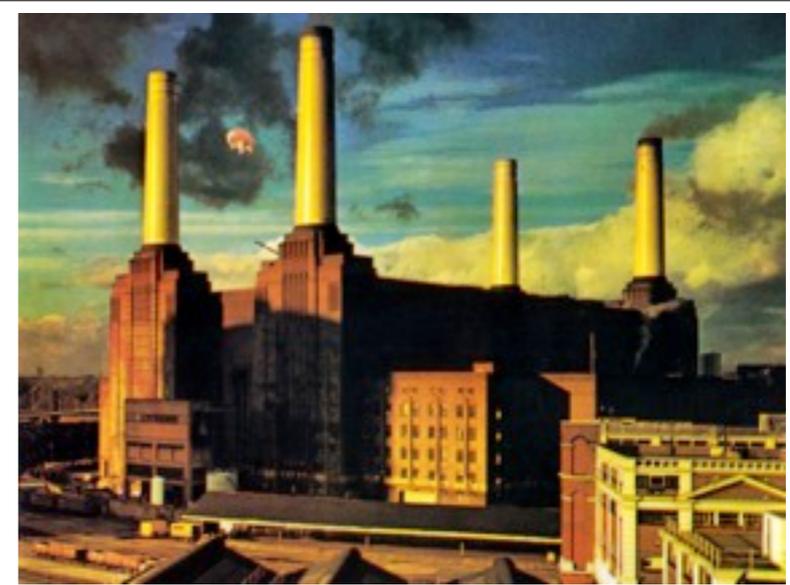
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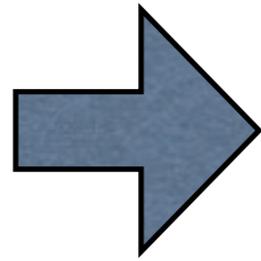
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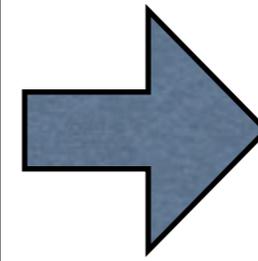
$$\phi\chi$$



$$\mathcal{L}_{eff}$$



$$\langle N_o | m_q \bar{q}q | N_i \rangle \longrightarrow f_{Tq}^N \bar{N}N$$



$$\mathcal{L}_{NR} = \sum_{\alpha=n,p} \sum_{i=1}^{15} c_i^\alpha \mathcal{O}_i^\alpha$$

$$q\chi$$

$$n\chi$$

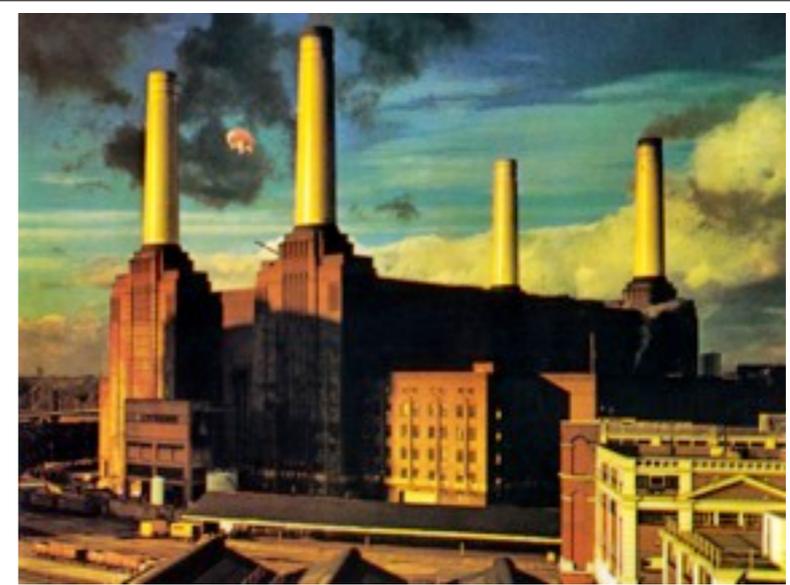
$$\frac{1}{2j_\chi + 1} \frac{1}{2j_N + 1} \sum_{\text{spins}} |\mathcal{M}|_{\text{nucleus/EFT}}^2$$

$$\chi - \text{nucleus}$$

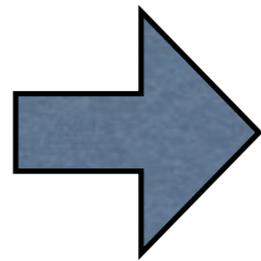
The full process takes the schematic form

$$\mathcal{L}$$

$$q\phi \quad \phi\chi$$

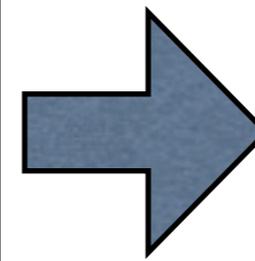


$$\mathcal{L}_{eff}$$



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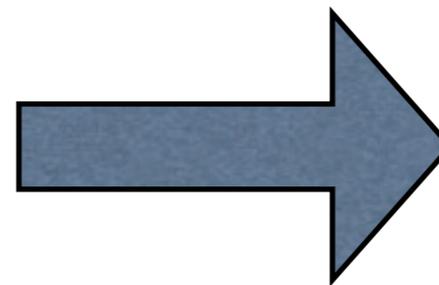


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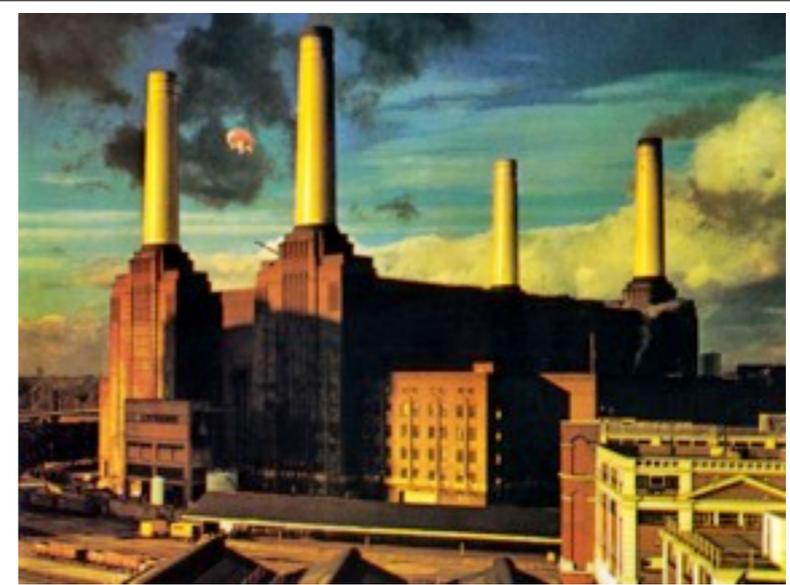
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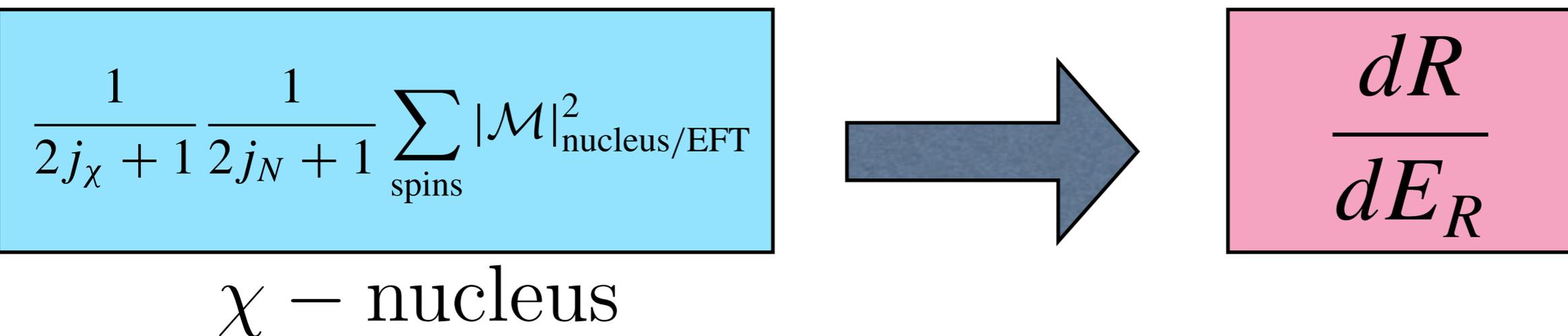
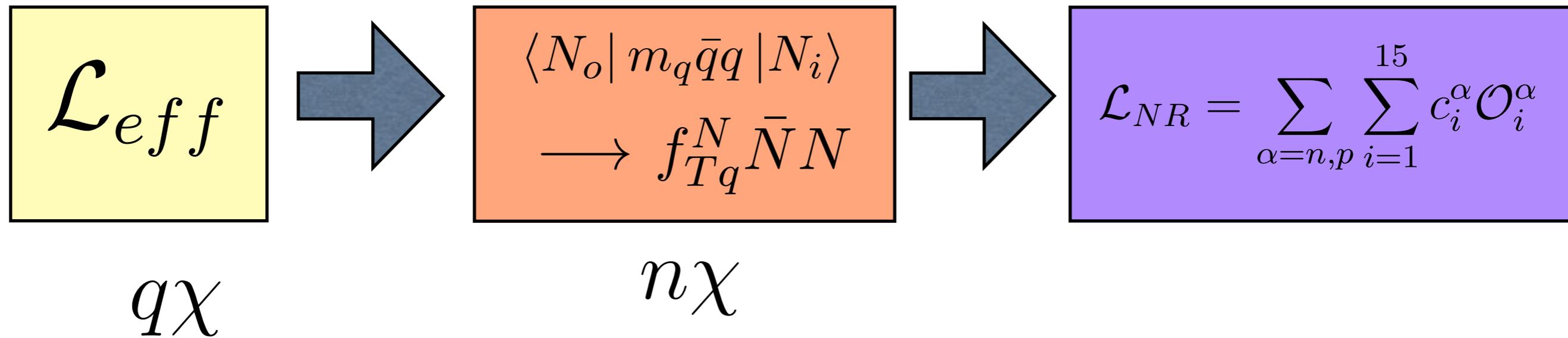


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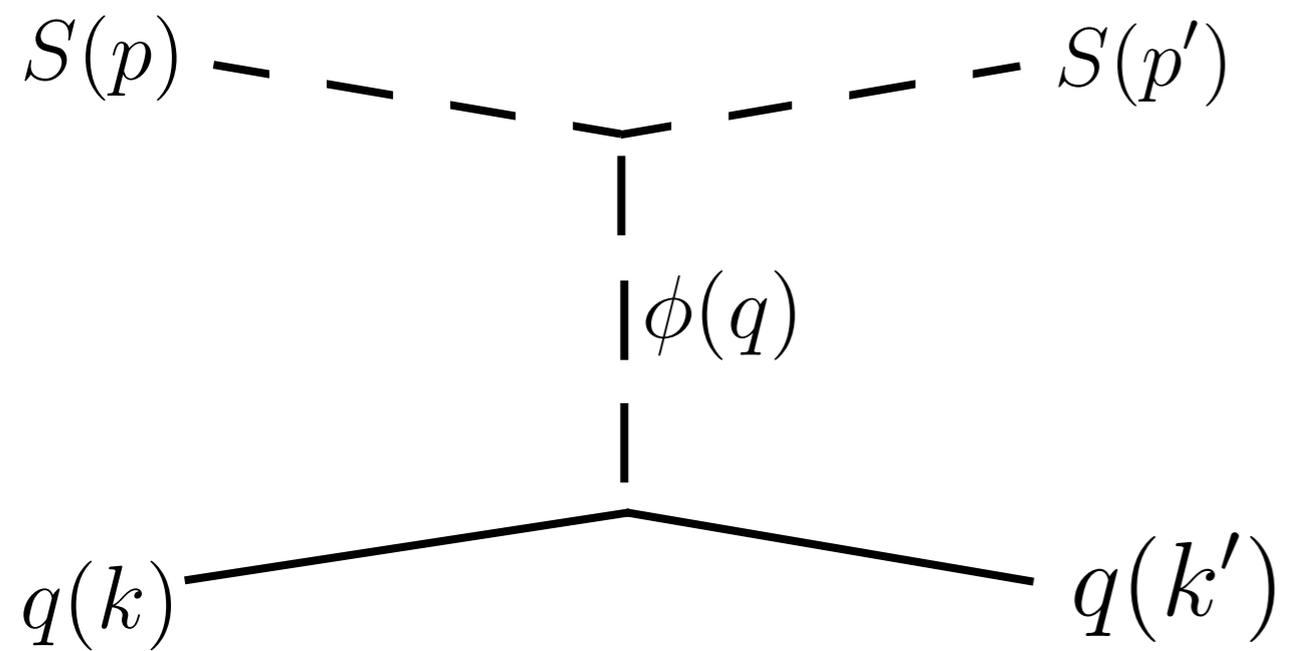


$$\mathcal{L} \quad q\phi \quad \phi\chi$$



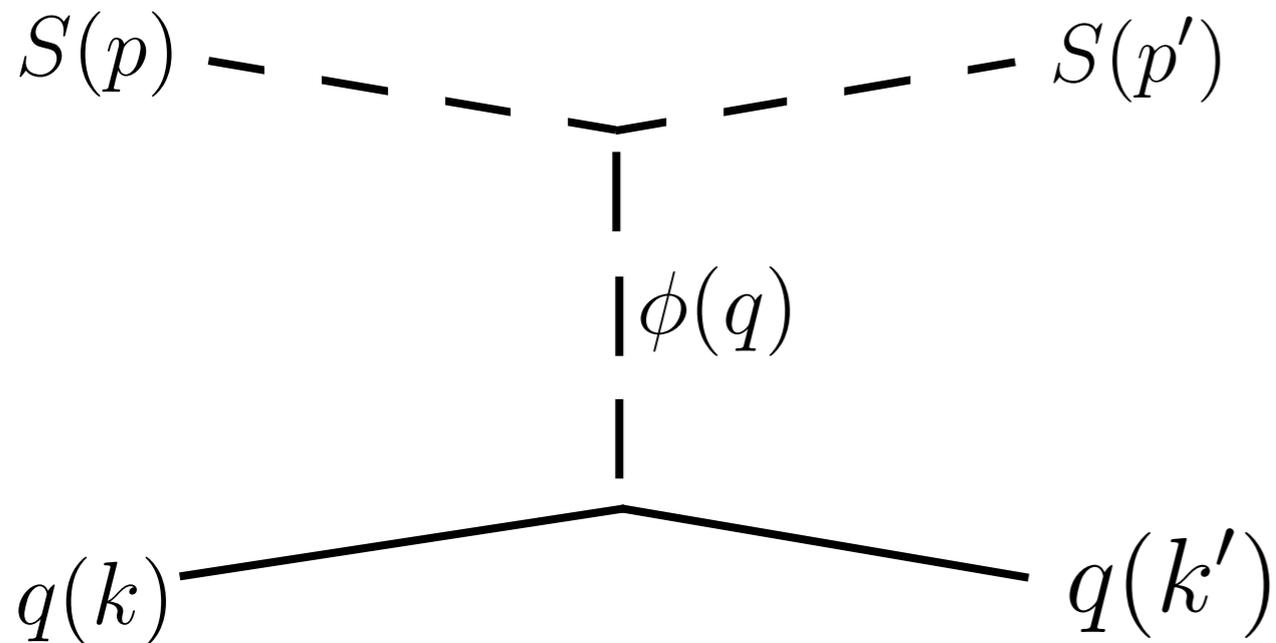
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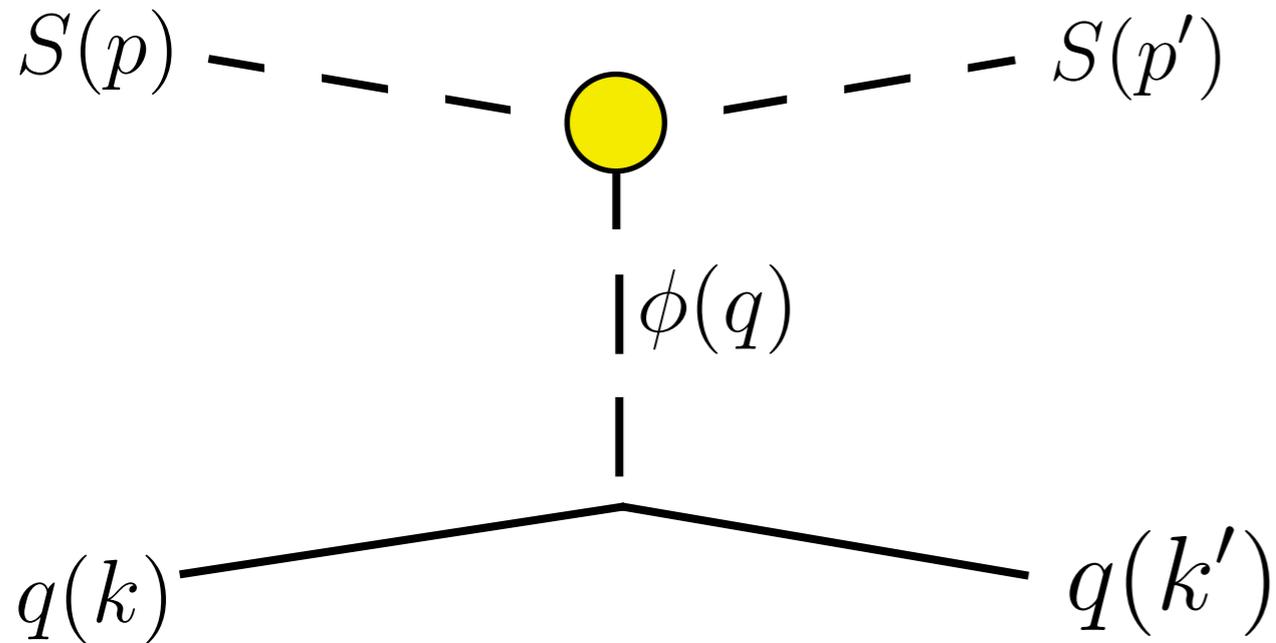
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$$\begin{aligned} \mathcal{L}_{S\phi q} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \frac{\lambda_S}{2} (S^\dagger S)^2 \\ & + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m_\phi^2 \phi^2 - \frac{m_\phi \mu_1}{3} \phi^3 - \frac{\mu_2}{4} \phi^4 \\ & + i \bar{q} \not{D} q - m_q \bar{q} q \\ & - g_1 S^\dagger S \phi - \frac{g_2}{2} S^\dagger S \phi^2 - h_1 \bar{q} q \phi - i h_2 \bar{q} \gamma^5 q \phi \end{aligned}$$

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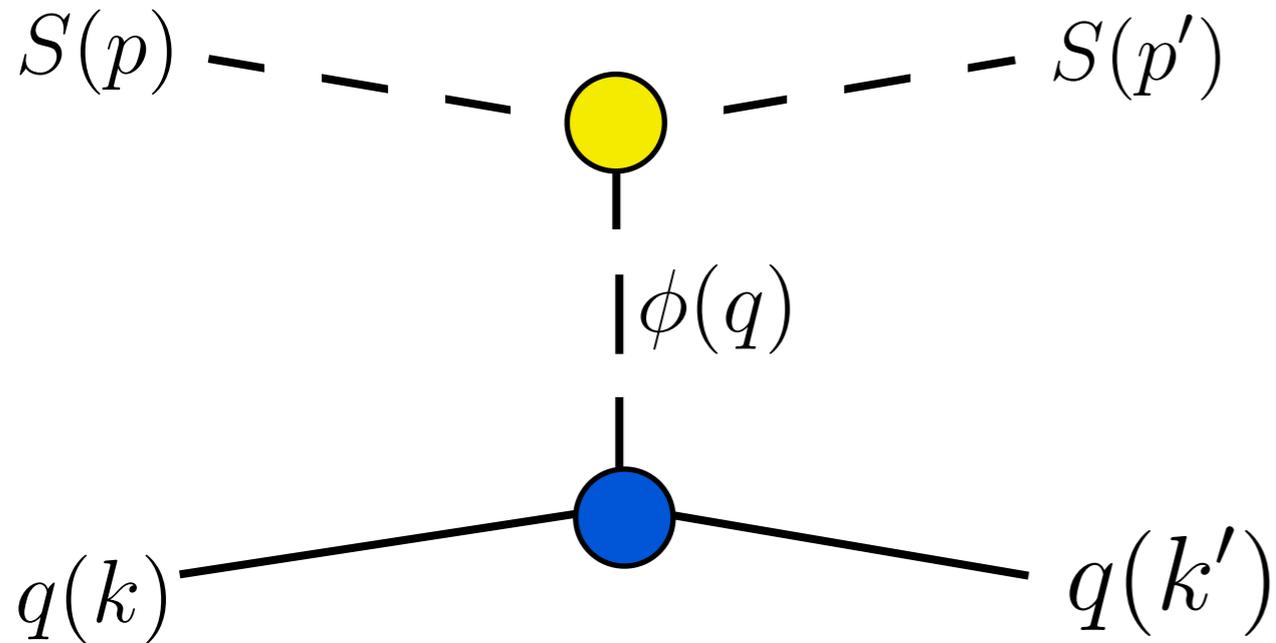
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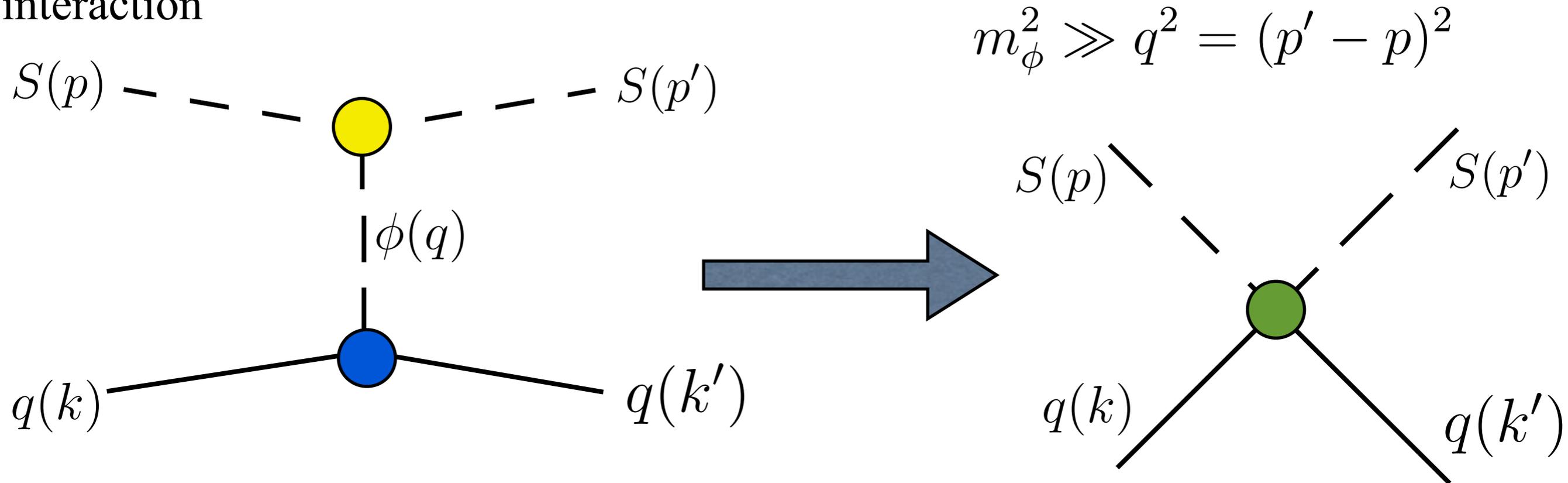
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$$\mathcal{L}_{eff} \supset \frac{h_1 g_1}{m_\phi^2} S^\dagger S \bar{q} q$$

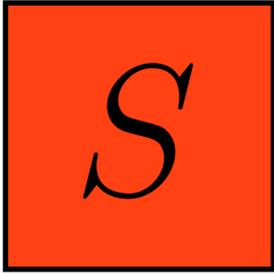
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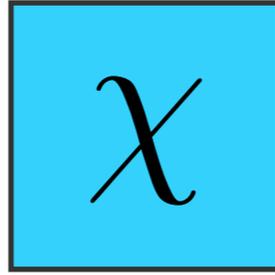
Dark Matter

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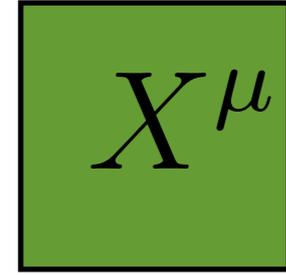
Dark Matter



spin-0



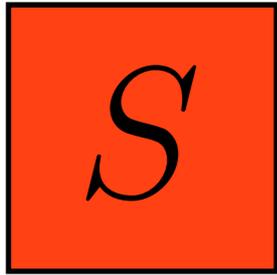
spin-1/2



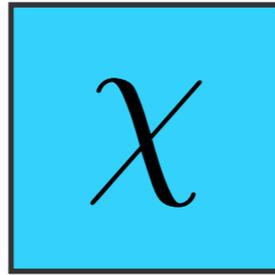
spin-1

We have analyzed the cases:

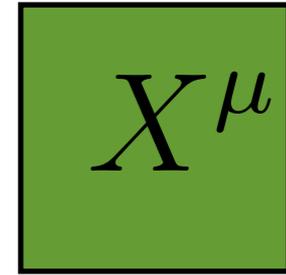
Dark Matter



spin-0



spin-1/2

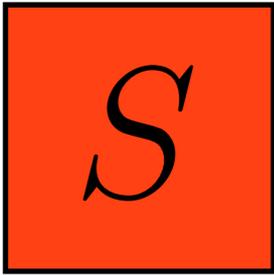


spin-1

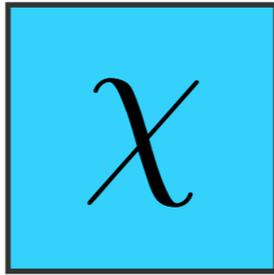
Uncharged mediators

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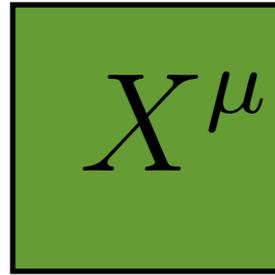
Dark Matter



spin-0

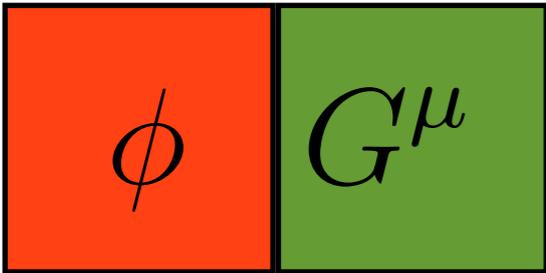


spin-1/2

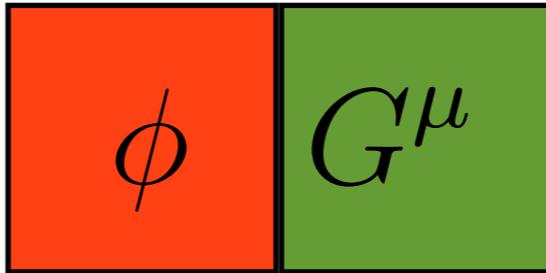


spin-1

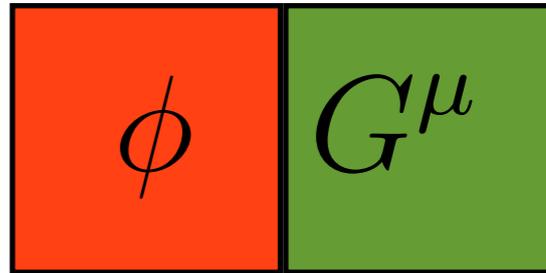
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spin-0 spin-1



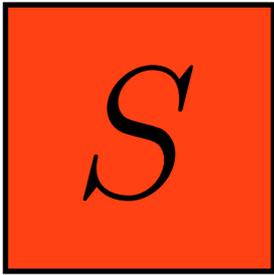
spin-0 spin-1



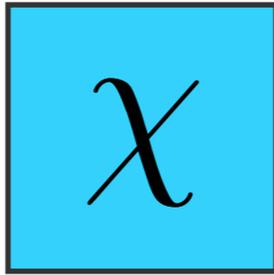
spin-0 spin-1

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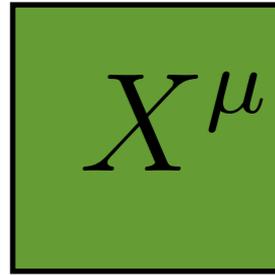
Dark Matter



spin-0

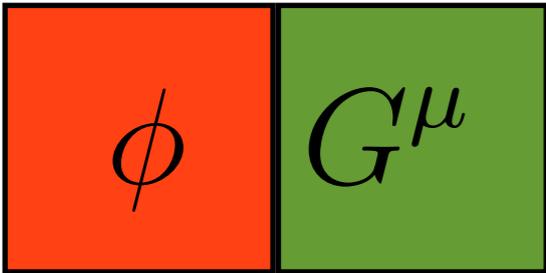


spin-1/2

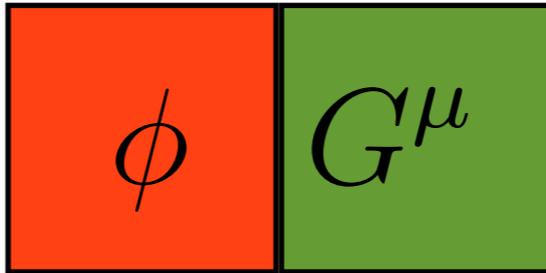


spin-1

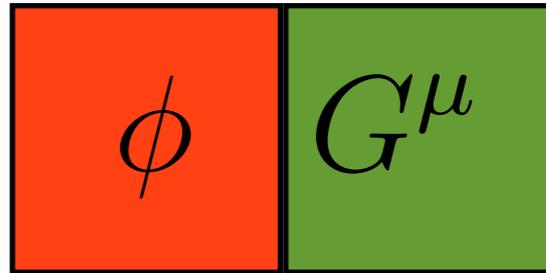
Uncharged mediators



spin-0 spin-1



spin-0 spin-1

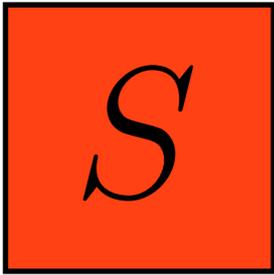


spin-0 spin-1

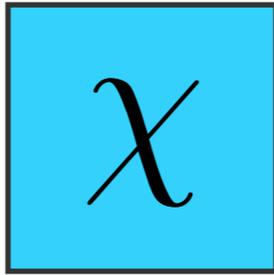
Charged mediators

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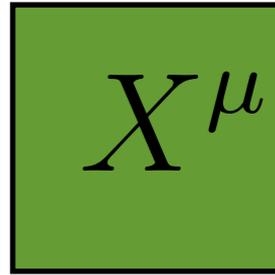
Dark Matter



spin-0

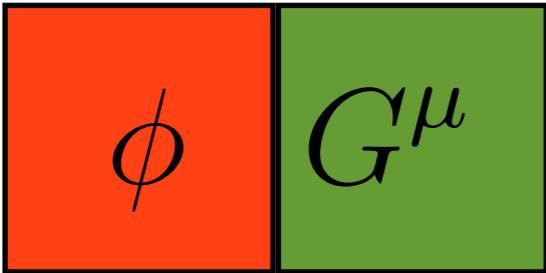


spin-1/2

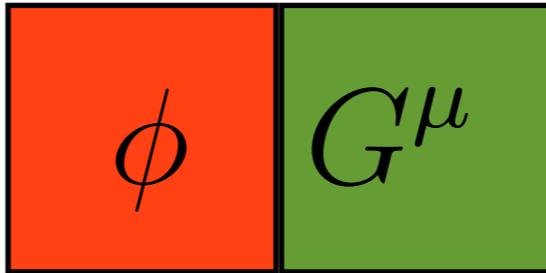


spin-1

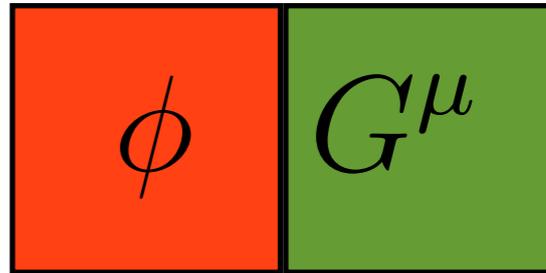
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spin-0 spin-1

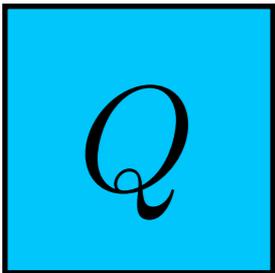


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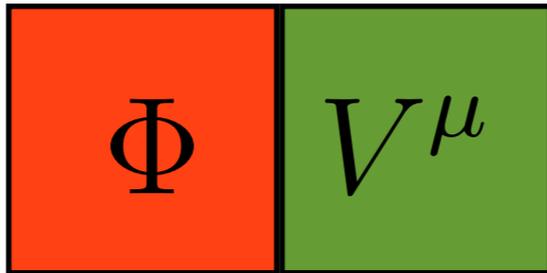


spin-0 spin-1

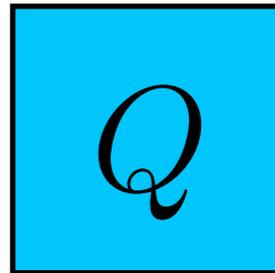
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spin-1/2



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- Two additional non-relativistic operators must be included in the vector dark matter case

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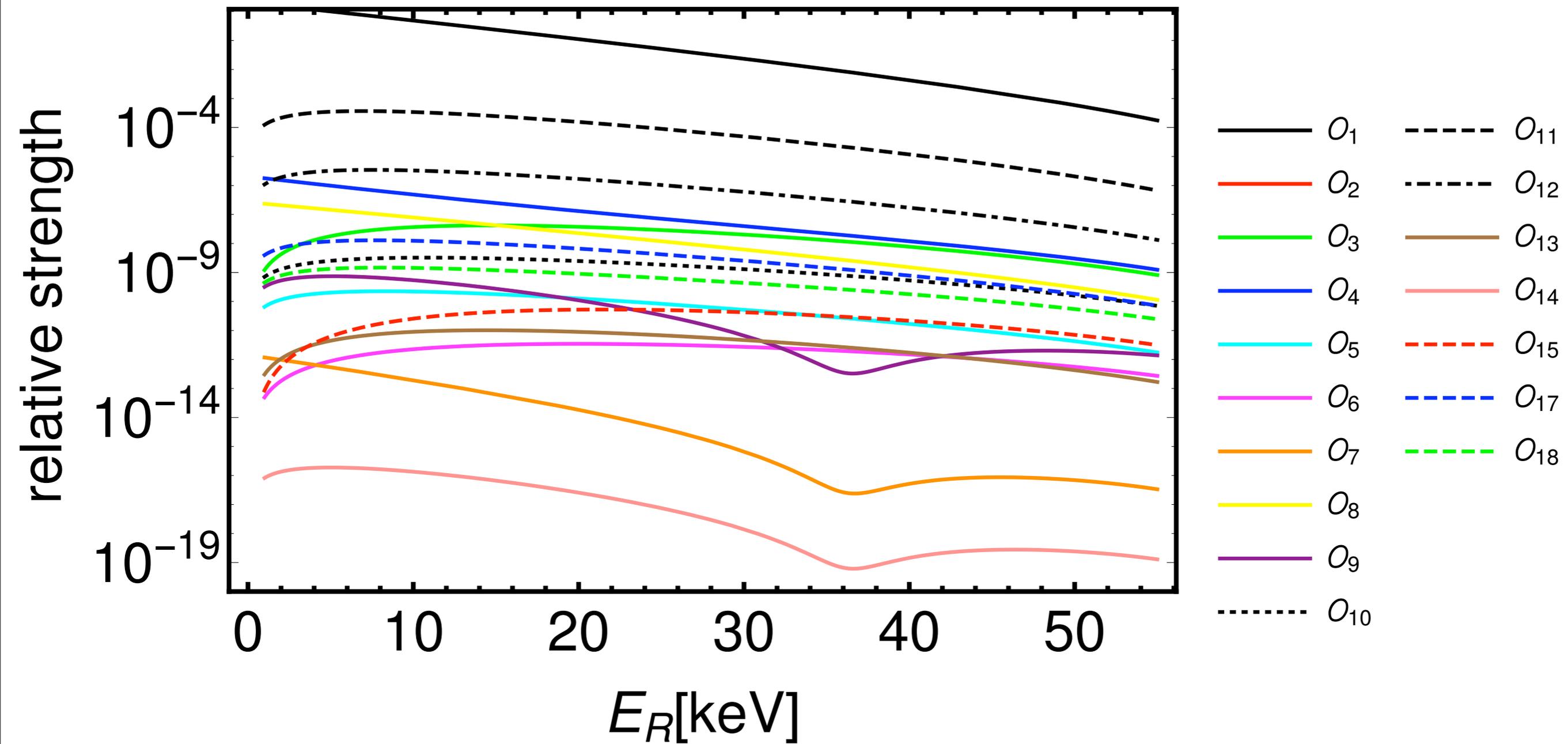
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- We calculated the leading order operator for each distinct interaction in a minimal fashion: only a single set of two couplings is non-zero
- Non-standard interactions were found to dominate for certain interaction types



Relative strength of operators, in order to compare which operators dominate when more than one are present

- Aside from scalar WIMPs each particular spin produces some non-relativistic operators that are unique to that spin

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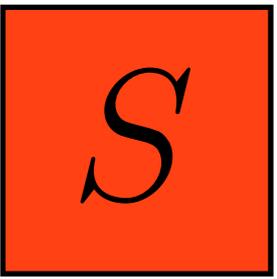
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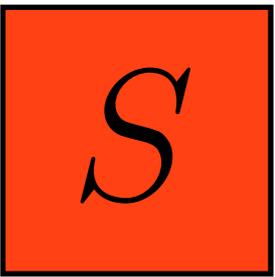
- In five scenarios relativistic operators generate unique non-relativistic operators at leading order.
- The operators can produce radically different energy dependence for scattering off different nuclear targets. Thus, a complementary use of different target materials will be helpful in order to reliably distinguish between different particle physics model possibilities for WIMP dark matter.



spin-0

Spin-0 WIMP		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}		
	(h_1, g_1)	✓																			
	(h_2, g_1)												✓								
	(h_4, g_4)												✓								
	(y_1)	✓											✓								
	(y_2)	✓											✓								
(y_1, y_2)												✓									

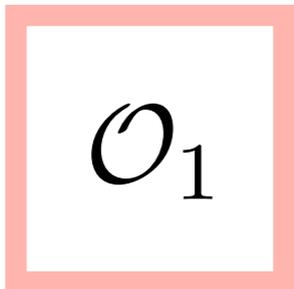
WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
0	0	h_1, g_1	\mathcal{O}_1	13 TeV
0	0	h_2, g_1	\mathcal{O}_{10}	14 GeV
0	1	h_4, g_4	\mathcal{O}_{10}	8 GeV
0	$\frac{1}{2}^*$	y_1	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_2	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_1, y_2	\mathcal{O}_{10}	41 GeV



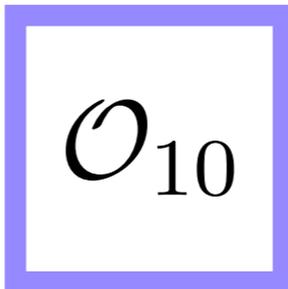
spin-0

	\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}
(h_1, g_1)	✓																	
(h_2, g_1)											✓							
(h_4, g_4)											✓							
(y_1)	✓										✓							
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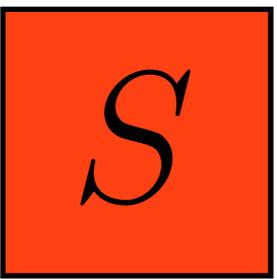
WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
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0	1	h_4, g_4	\mathcal{O}_{10}	8 GeV
0	$\frac{1}{2}^*$	y_1	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_2	\mathcal{O}_1	3.2 PeV
0	$\frac{1}{2}^*$	y_1, y_2	\mathcal{O}_{10}	41 GeV



$$1_\chi 1_N$$



$$i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$$

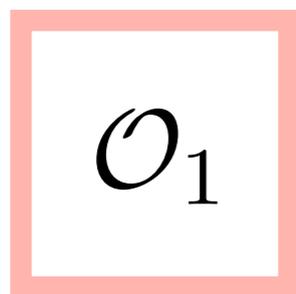


spin-0

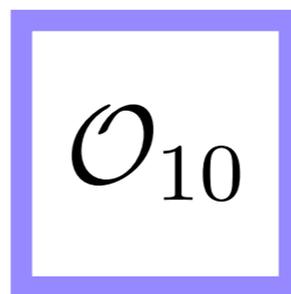
$$(S^\dagger S)(\bar{q}q)$$

$$(S^\dagger S)(\bar{q}\gamma^5 q)$$

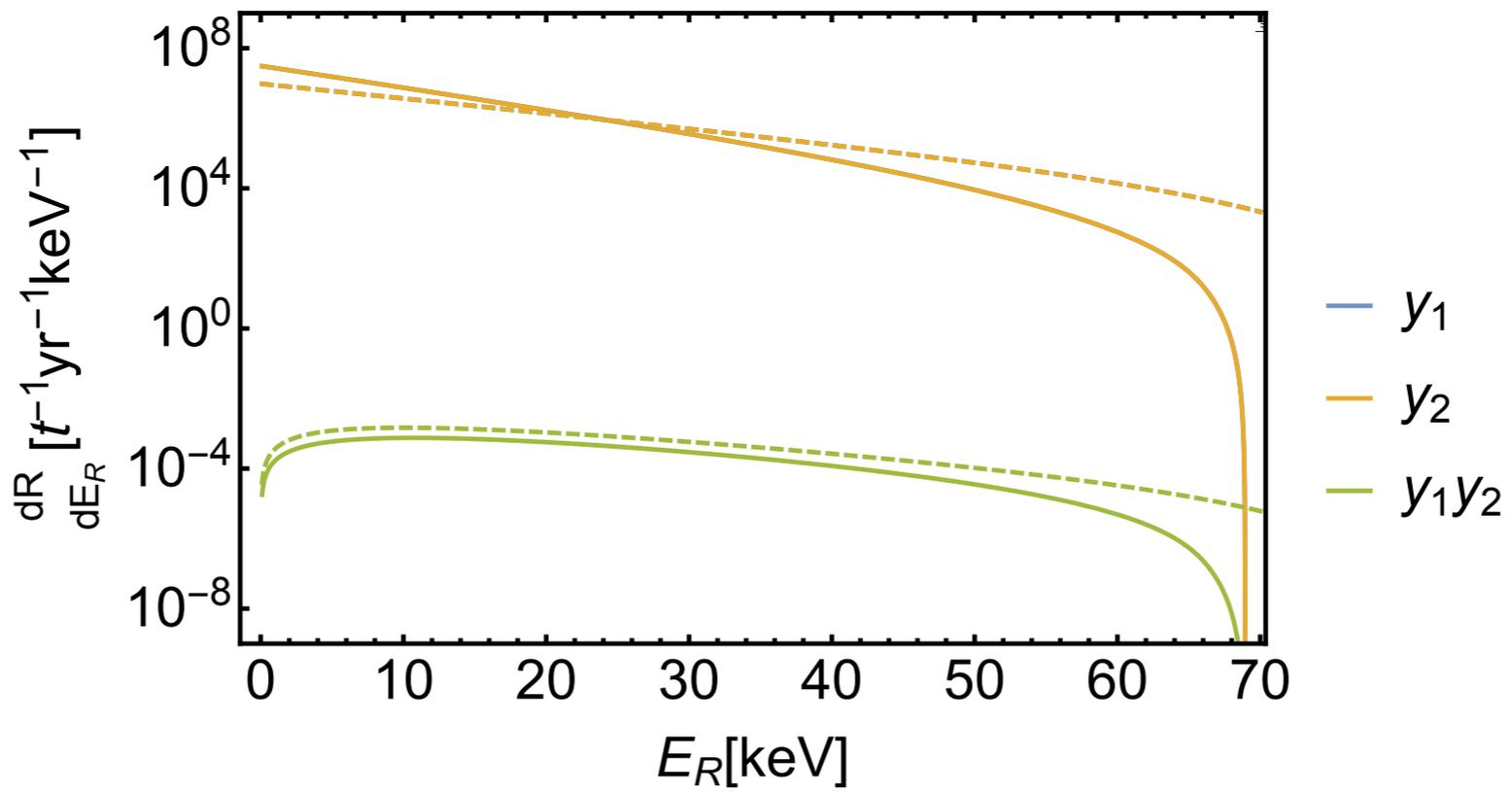
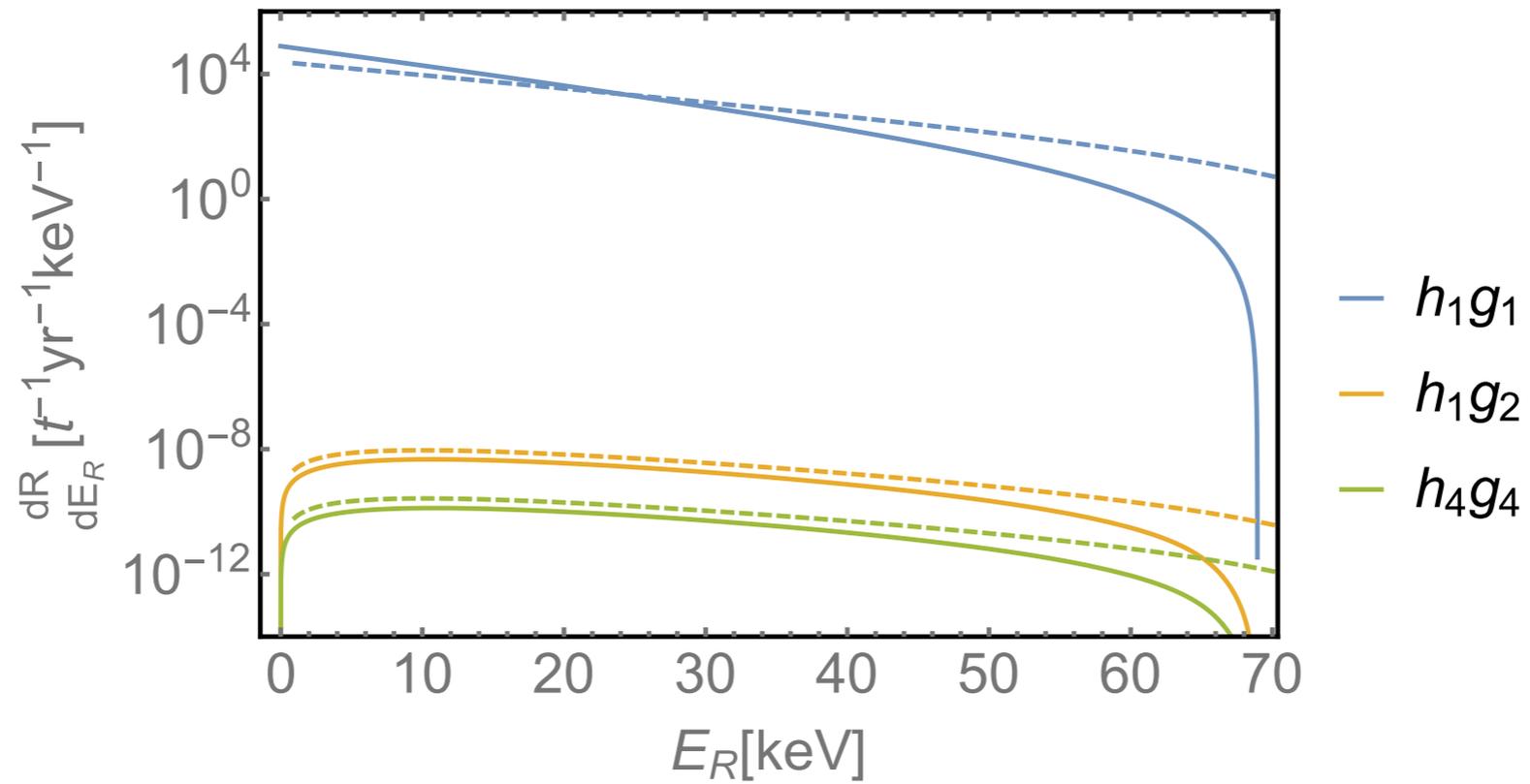
$$i(S^\dagger \partial_\mu S - \partial_\mu S^\dagger S)(\bar{q}\gamma^\mu \gamma^5 q)$$



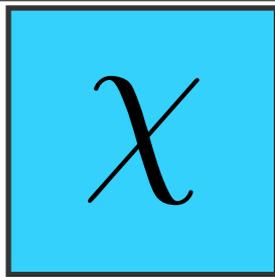
$$1_\chi 1_N$$



$$i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$$



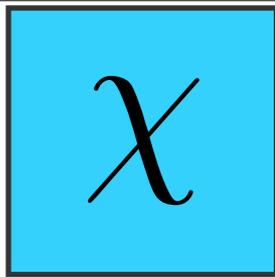
50 GeV spin-0 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid) with 1 TeV mediator



spin-1/2

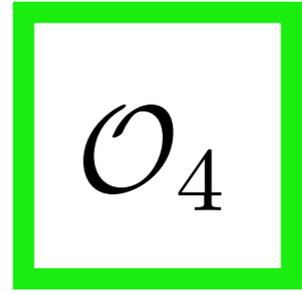
		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}
Spin- $\frac{1}{2}$ WIMP	(h_1, λ_1)	✓																	
	(h_2, λ_1)											✓							
	(h_1, λ_2)												✓						
	(h_2, λ_2)							✓											
	(h_3, λ_3)	✓																	
	(h_4, λ_3)							✓			✓								
	(h_3, λ_4)									✓	✓								
	(h_4, λ_4)				✓														
	(l_1)	✓			✓				✓										
	(l_2)	✓			✓				✓										
	(d_1)	✓			✓				✓										
	(d_2)	✓			✓				✓										

WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
$\frac{1}{2}$	0	h_1, λ_1	\mathcal{O}_1	12.7 TeV
$\frac{1}{2}$	0	h_2, λ_1	\mathcal{O}_{10}	293 GeV
$\frac{1}{2}$	0	h_1, λ_2	\mathcal{O}_{11}	14 GeV
$\frac{1}{2}$	0	h_2, λ_2	\mathcal{O}_6	1.9 GeV
$\frac{1}{2}$	1	h_3, λ_3	\mathcal{O}_1	6.3 TeV
$\frac{1}{2}$	1	h_4, λ_3	\mathcal{O}_9	6.4 GeV
$\frac{1}{2}$	1	h_3, λ_4	\mathcal{O}_8	180 GeV
$\frac{1}{2}$	1	h_4, λ_4	\mathcal{O}_4	135 GeV
$\frac{1}{2}$	0*	l_1	\mathcal{O}_1	7.1 TeV
$\frac{1}{2}$	0*	l_2	\mathcal{O}_1	5.5 TeV
$\frac{1}{2}$	1*	d_1	\mathcal{O}_1	5.9 TeV
$\frac{1}{2}$	1*	d_2	\mathcal{O}_1	6.7 TeV

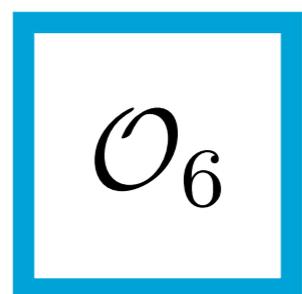


spin-1/2

		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}
Spin- $\frac{1}{2}$ WIMP	(h_1, λ_1)	✓																	
	(h_2, λ_1)											✓							
	(h_1, λ_2)												✓						
	(h_2, λ_2)							✓											
	(h_3, λ_3)	✓																	
	(h_4, λ_3)							✓				✓							
	(h_3, λ_4)										✓	✓							
	(h_4, λ_4)				✓														
	(l_1)	✓			✓				✓										
	(l_2)	✓			✓				✓										
	(d_1)	✓			✓				✓										
	(d_2)	✓			✓				✓										



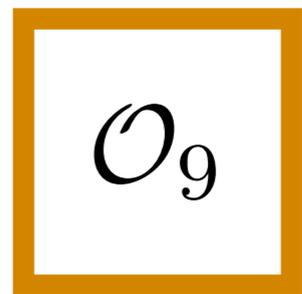
$$\vec{S}_\chi \cdot \vec{S}_N$$



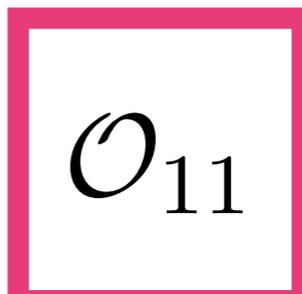
$$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right)$$



$$\vec{S}_\chi \cdot \vec{v}^\perp$$

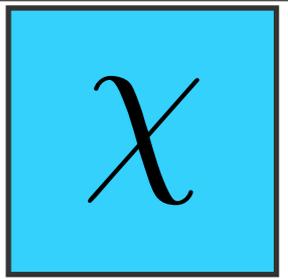


$$i\vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N}\right)$$



$$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$

WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
$\frac{1}{2}$	0	h_1, λ_1	\mathcal{O}_1	12.7 TeV
$\frac{1}{2}$	0	h_2, λ_1	\mathcal{O}_{10}	293 GeV
$\frac{1}{2}$	0	h_1, λ_2	\mathcal{O}_{11}	14 GeV
$\frac{1}{2}$	0	h_2, λ_2	\mathcal{O}_6	1.9 GeV
$\frac{1}{2}$	1	h_3, λ_3	\mathcal{O}_1	6.3 TeV
$\frac{1}{2}$	1	h_4, λ_3	\mathcal{O}_9	6.4 GeV
$\frac{1}{2}$	1	h_3, λ_4	\mathcal{O}_8	180 GeV
$\frac{1}{2}$	1	h_4, λ_4	\mathcal{O}_4	135 GeV
$\frac{1}{2}$	0*	l_1	\mathcal{O}_1	7.1 TeV
$\frac{1}{2}$	0*	l_2	\mathcal{O}_1	5.5 TeV
$\frac{1}{2}$	1*	d_1	\mathcal{O}_1	5.9 TeV
$\frac{1}{2}$	1*	d_2	\mathcal{O}_1	6.7 TeV



spin-1/2

$$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q$$

$$\mathcal{O}_4$$

$$\vec{S}_\chi \cdot \vec{S}_N$$

$$\bar{\chi} \gamma^5 \chi \bar{q} \gamma^5 q$$

$$\mathcal{O}_6$$

$$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N\right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi\right)$$

$$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu q$$

$$\mathcal{O}_8$$

$$\vec{S}_\chi \cdot \vec{v}^\perp$$

$$\bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu \gamma^5 q$$

$$\mathcal{O}_9$$

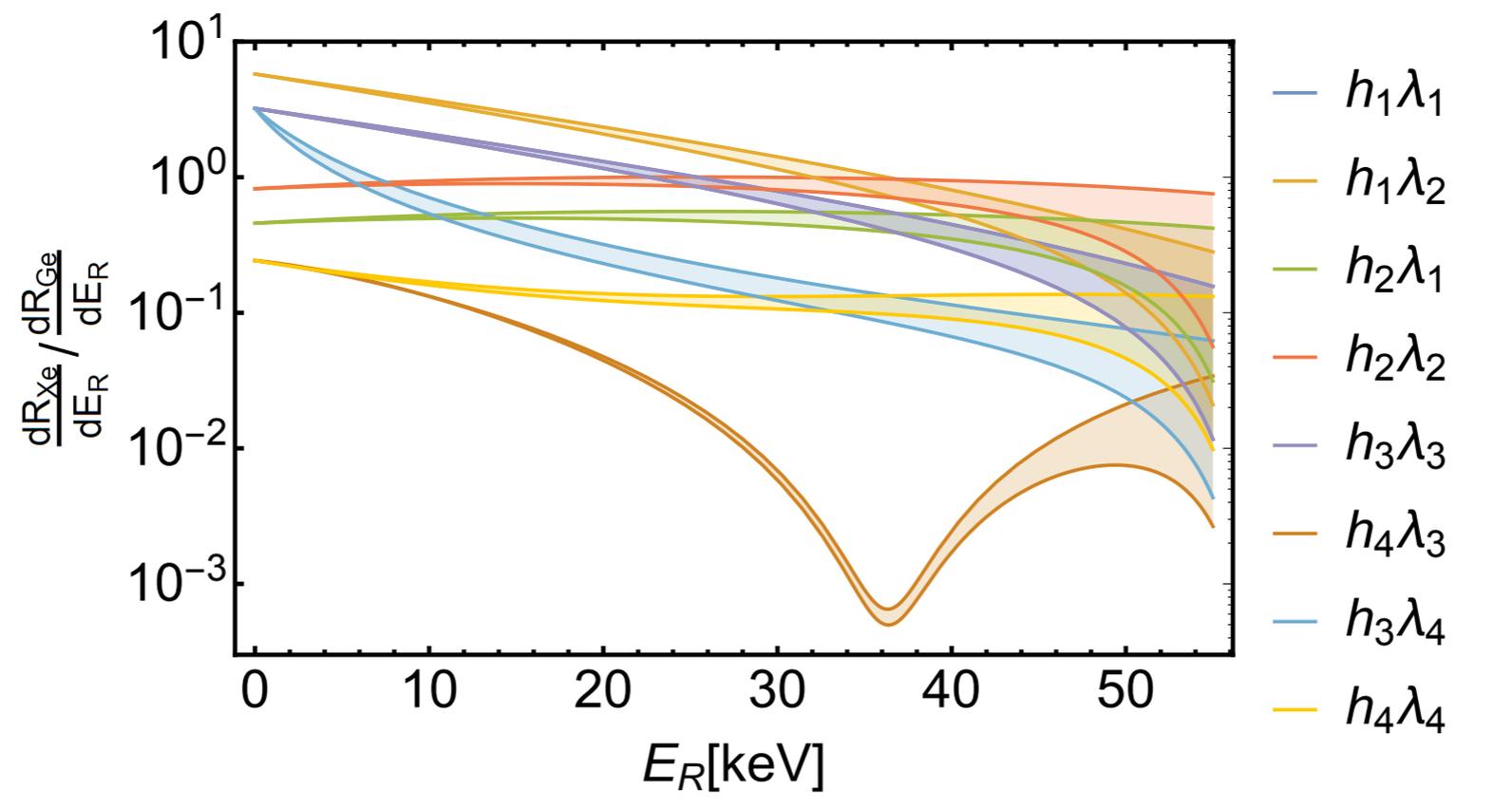
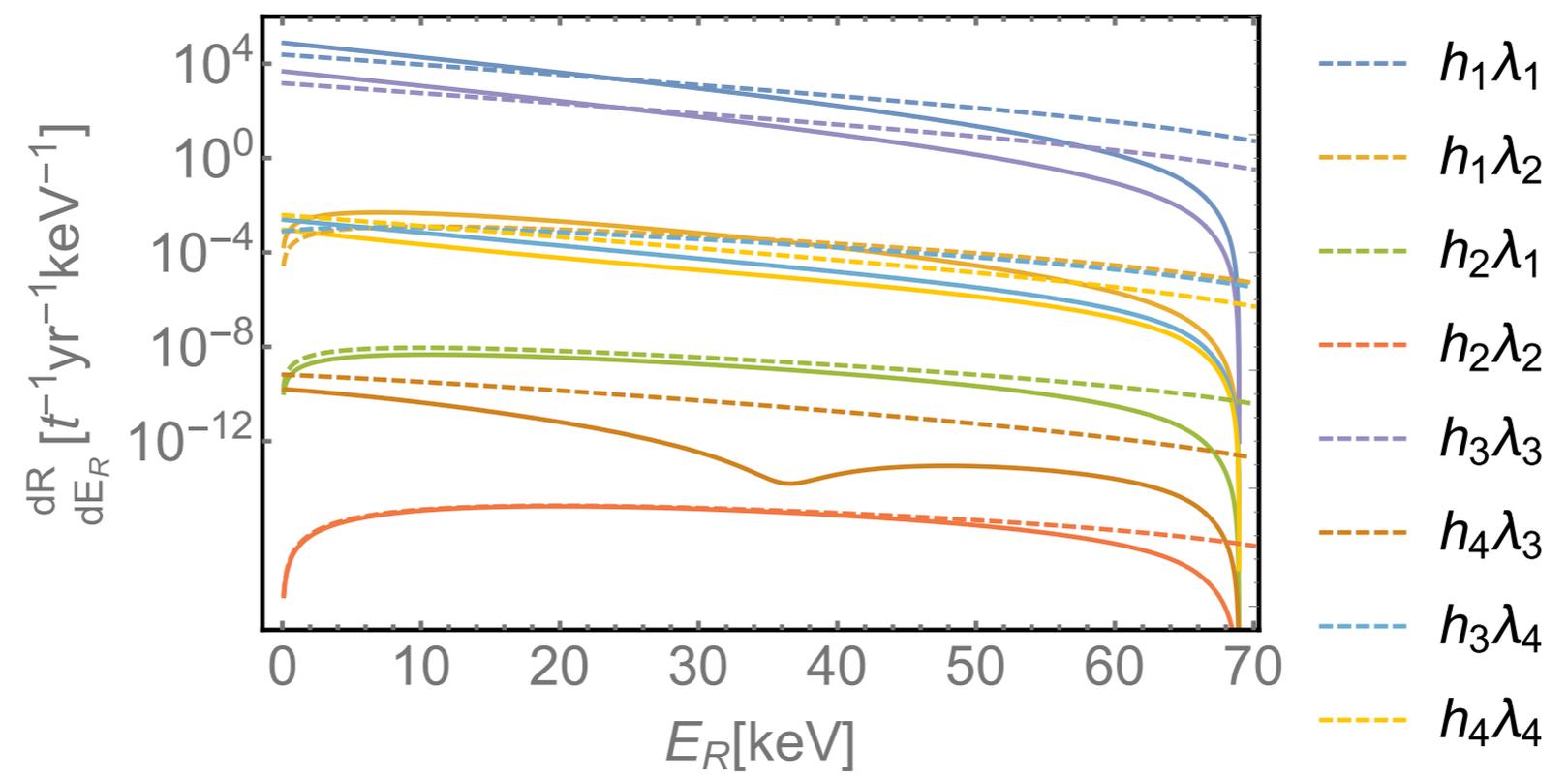
$$i \vec{S}_\chi \cdot \left(\vec{S}_N \times \frac{\vec{q}}{m_N}\right)$$

$$\bar{\chi} \gamma^5 \chi \bar{q} q$$

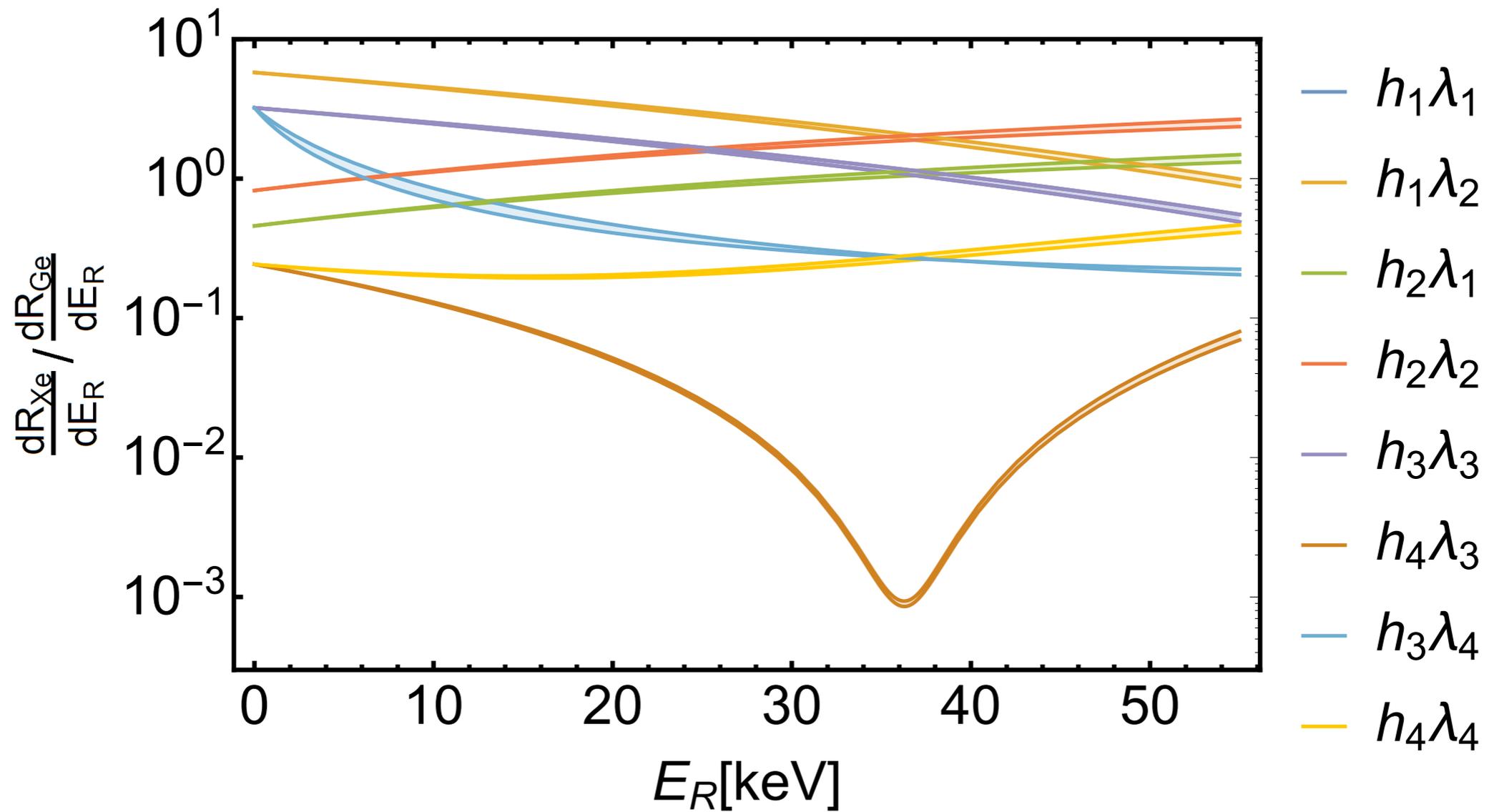
$$\mathcal{O}_{11}$$

$$i \frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$

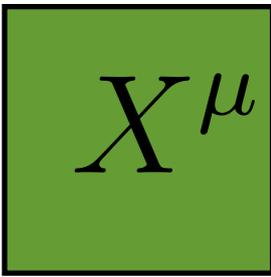
50 GeV spin-1/2 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid) for a 1TeV mediator



Ratio of rates for 50GeV spin-1/2 WIMP off Xe and Ge including astrophysical uncertainties



Ratio of rates for 500GeV spin-1/2 WIMP off Xe and Ge including astrophysical uncertainties

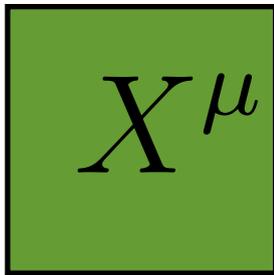


spin-1

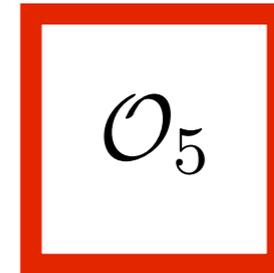
		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}	
Spin-1 WIMP	(h_1, b_1)	✓																		
	(h_2, b_1)											✓								
	(h_4, b_5)											✓								
	(h_3, b_6)					✓	✓	✓											✓*	
	(h_4, b_6)										✓								✓*	
	(h_3, b_7)									✓*	✓*		✓							
	(h_4, b_7)				✓*	✓		✓								✓				
	(y_3)	✓			✓								✓	✓	✓					✓
	(y_4)	✓			✓								✓	✓	✓					✓
	(y_3, y_4)												✓	✓	✓					✓

WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
1	0	h_1, b_1	\mathcal{O}_1	13 TeV
1	0	h_2, b_1	\mathcal{O}_{10}	10 GeV
1	1	h_4, b_5	\mathcal{O}_{10}	5.1 GeV
1	1	$h_3, b_6^{\text{Re}}(b_6^{\text{Im}})$	$\mathcal{O}_5(\mathcal{O}_{17})$	5.5 GeV(23 GeV)
1	1	$h_4, b_6^{\text{Re}}(b_6^{\text{Im}})$	$\mathcal{O}_9(\mathcal{O}_{18})$	3 GeV(4.6 GeV)
1	1	$h_3, b_7^{\text{Re}}(b_7^{\text{Im}})$	$\mathcal{O}_{11}(\mathcal{O}_8)$	186 GeV(228 GeV)
1	1	$h_4, b_7^{\text{Re}}(b_7^{\text{Im}})$	$\mathcal{O}_{14}(\mathcal{O}_4)$	65 MeV (172 GeV)
1	$\frac{1}{2}^*$	y_3	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_4	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_3, y_4	\mathcal{O}_{11}	120 TeV

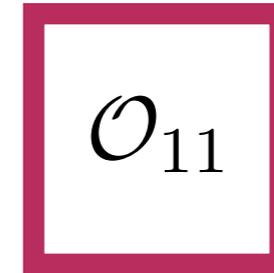
		\mathcal{O}_1	\mathcal{O}_2	\mathcal{O}_3	\mathcal{O}_4	$q^2\mathcal{O}_4$	\mathcal{O}_5	\mathcal{O}_6	\mathcal{O}_7	\mathcal{O}_8	\mathcal{O}_9	\mathcal{O}_{10}	\mathcal{O}_{11}	\mathcal{O}_{12}	\mathcal{O}_{13}	\mathcal{O}_{14}	\mathcal{O}_{15}	\mathcal{O}_{17}	\mathcal{O}_{18}	
Spin-1 WIMP	(h_1, b_1)	✓																		
	(h_2, b_1)											✓								
	(h_4, b_5)											✓								
	(h_3, b_6)					✓	✓	✓										✓*		
	(h_4, b_6)										✓								✓*	
	(h_3, b_7)									✓*	✓*		✓							
	(h_4, b_7)				✓*	✓		✓								✓				
	(y_3)	✓			✓								✓	✓	✓					✓
	(y_4)	✓			✓								✓	✓	✓					✓
	(y_3, y_4)												✓	✓	✓					✓



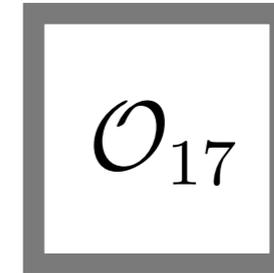
spin-1



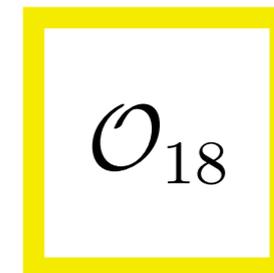
$$i\vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right)$$



$$i\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$



$$i\frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp$$



$$i\frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N$$

WIMP spin	Mediator spin	\mathcal{L} terms	leading NR operator	Eqv. M_m
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1	$\frac{1}{2}^*$	y_3	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_4	\mathcal{O}_1	3.2 PeV
1	$\frac{1}{2}^*$	y_3, y_4	\mathcal{O}_{11}	120 TeV

$$X^\mu$$

spin-1

$$\partial_\nu (X^{\nu\dagger} X_\mu + X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu q)$$

$$\mathcal{O}_5$$

$$i \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right)$$

$$\epsilon_{\mu\nu\rho\sigma} \left(X^{\nu\dagger} \partial^\rho X^\sigma + X^\nu \partial^\rho X^{\sigma\dagger} \right) (\bar{q} \gamma^\mu q)$$

$$\mathcal{O}_{11}$$

$$i \frac{\vec{q}}{m_N} \cdot \vec{S}_\chi$$

$$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu q)$$

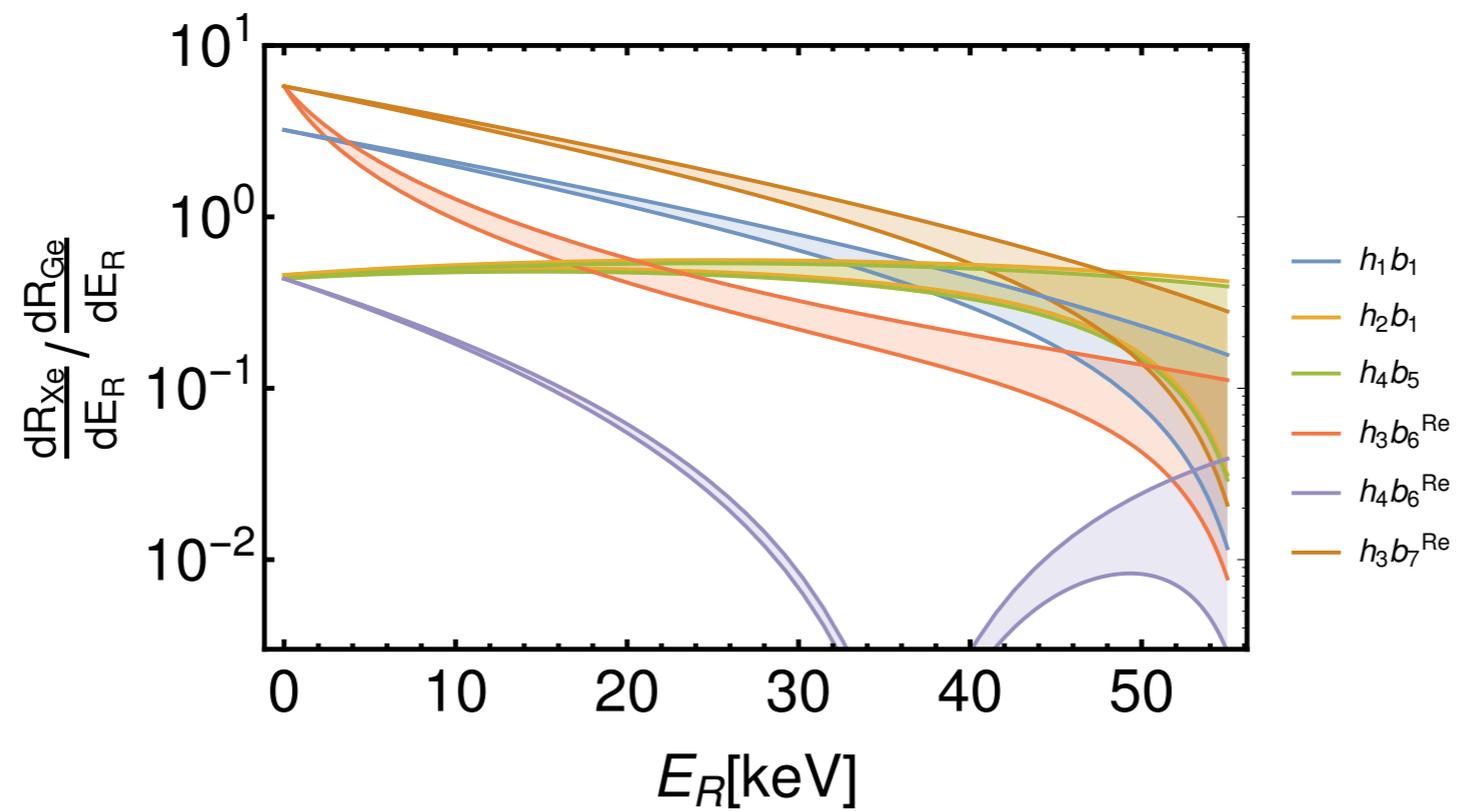
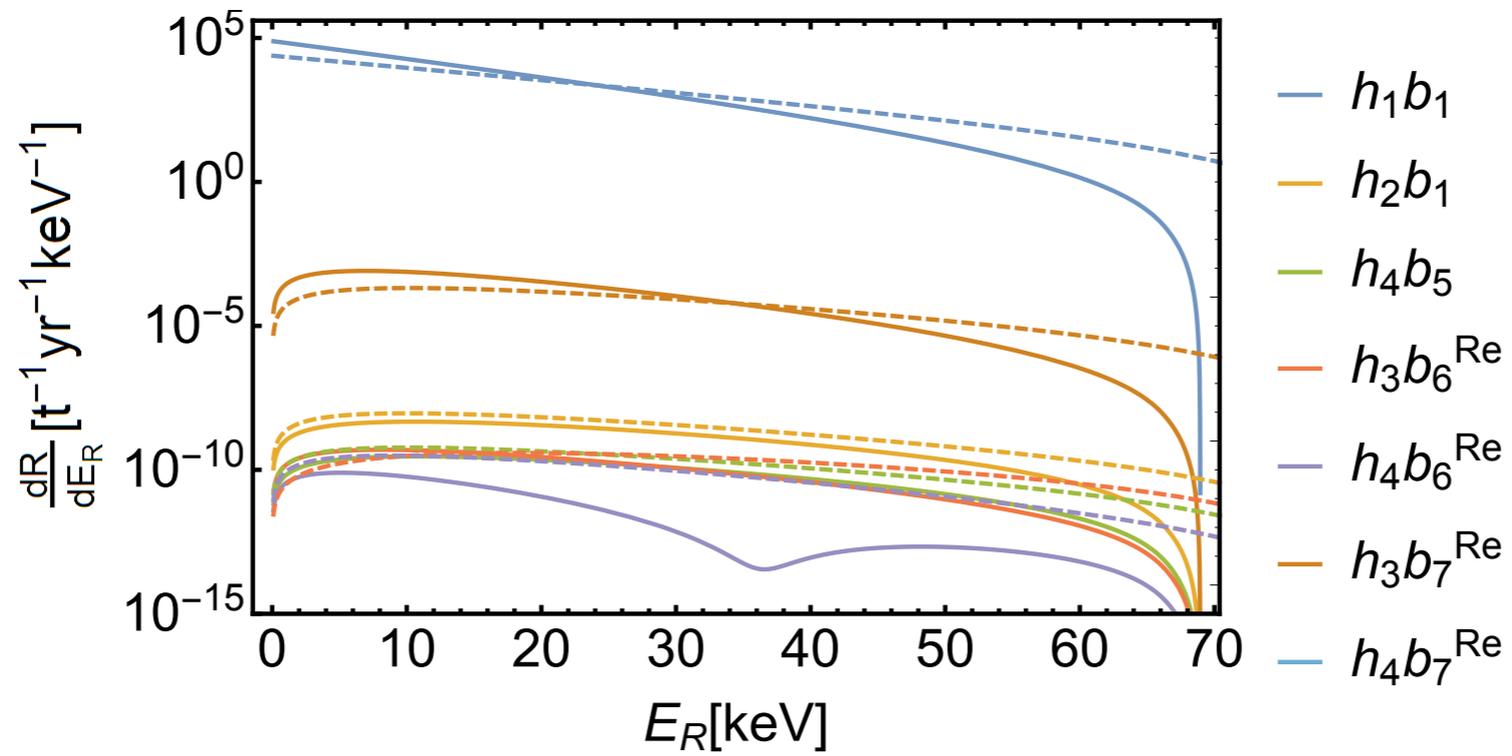
$$\mathcal{O}_{17}$$

$$i \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{v}_\perp$$

$$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu) (\bar{q} \gamma^\mu \gamma^5 q)$$

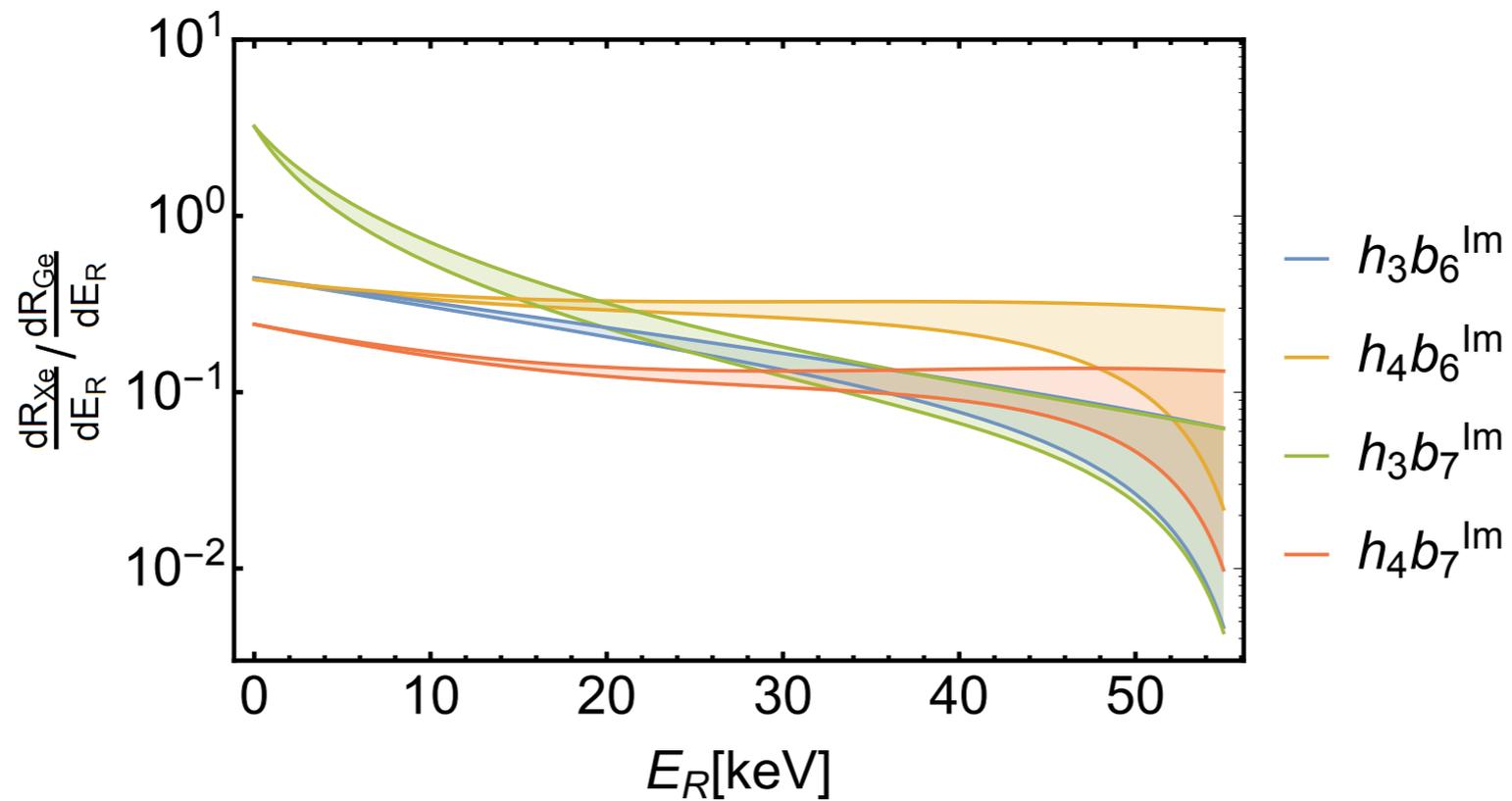
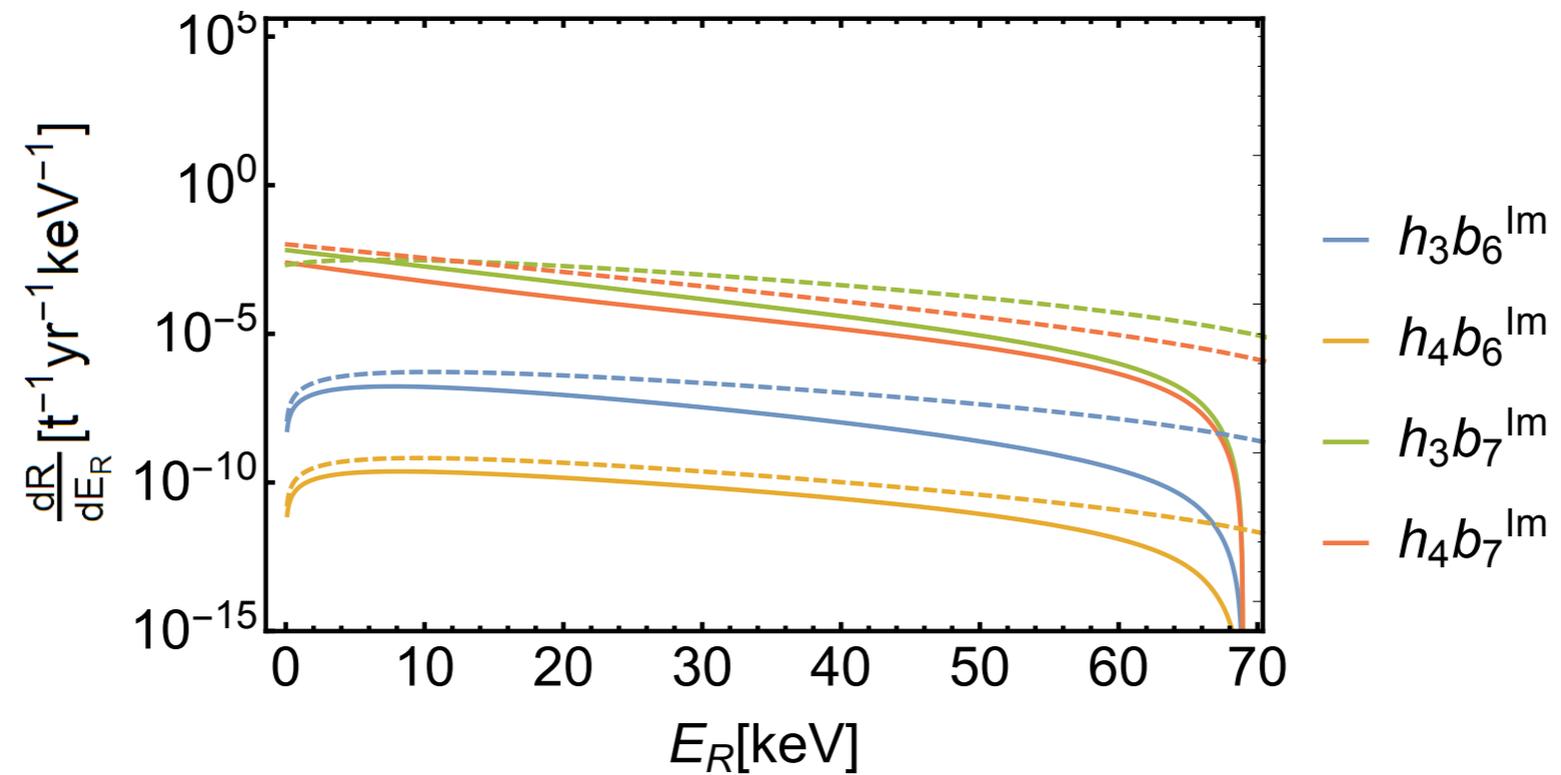
$$\mathcal{O}_{18}$$

$$i \frac{\vec{q}}{m_N} \cdot \mathcal{S} \cdot \vec{S}_N$$



50 GeV spin-1 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid)

50 GeV spin-1 WIMP off of ^{73}Ge (dashed) and ^{131}Xe (solid)



Ratio of rates for 50 GeV spin-1 WIMP off Xe and Ge including astrophysical uncertainties

Conclusions

As direct detection experiments becoming increasingly more sensitive, a discovery requires accurate modeling to discern particle properties

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Complementarity from colliders and astrophysical probes is also vital

An ongoing program with much to do!

Direct Detection of Dark Matter

From Microphysics to Observational Signatures

James Dent

JBD, L.M. Krauss, J.L. Newstead, and S. Sabharwal, arXiv: 1505.03117



Texas A&M May 18, 2015

One can also decompose the velocity difference into a center-of-mass piece and intrinsic parts

$$\begin{aligned}\vec{v}^\perp &\rightarrow \{\vec{v}_\chi - \vec{v}_N(i), i = 1, \dots, A\} \\ &\equiv \vec{v}_T^\perp - \{\dot{\vec{v}}_N(i), i = 1, \dots, A - 1\}\end{aligned}$$

where the nuclear center-of-mass (Target) is described by

$$\vec{v}_T^\perp = \vec{v}_\chi - \frac{1}{2A} \sum_{i=1}^A [\vec{v}_{N,in}(i) + \vec{v}_{N,out}(i)]$$

The nucleon velocities are decomposed into internal and ‘in’ and ‘out’ segments

Operators are decomposed as in

$$\begin{aligned}\vec{v}^\perp \cdot \vec{S}_N &\rightarrow \sum_{i=1}^A \frac{1}{2} [\vec{v}_{\chi,in} + \vec{v}_{\chi,out} - \vec{v}_{N,in}(i) - \vec{v}_{N,out}(i)] \cdot \vec{S}_N(i) \\ &= \vec{v}_T^\perp \cdot \sum_{i=1}^A \vec{S}_N(i) - \left\{ \sum_{i=1}^A \frac{1}{2} [\vec{v}_{N,in}(i) + \vec{v}_{N,out}(i)] \cdot \vec{S}_N(i) \right\}_{int}\end{aligned}$$

The nucleon positions and momenta are replaced by operators which account for the non-zero nuclear size

$$\vec{v}_{N,in} \longrightarrow \vec{p}_{N,in}/M \longrightarrow i \overleftarrow{\nabla} / M$$

$$\vec{v}_{N,out} \longrightarrow \vec{p}_{N,out}/M \longrightarrow -i \overrightarrow{\nabla} / M$$

$$e^{-i\vec{q}\cdot\vec{x}}$$

The DM-nucleon interactions can then be written

$$\sum_{\tau=0,1} \left\{ l_0^\tau S + l_0^{A\tau} T + \vec{l}_5^\tau \cdot \vec{P} + \vec{l}_M^\tau \cdot Q + \vec{l}_E^\tau \cdot \vec{R} \right\} t^\tau(i)$$

Effective Action

Non-rel limit

Operator Matching

j	$\mathcal{L}_{\text{int}}^j$	Nonrelativistic reduction	$\sum_i c_i \mathcal{O}_i$	P/T
1	$\bar{\chi} \chi \bar{N} N$	$1_\chi 1_N$	\mathcal{O}_1	E/E
2	$i \bar{\chi} \chi \bar{N} \gamma^5 N$	$i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$	\mathcal{O}_{10}	O/O
3	$i \bar{\chi} \gamma^5 \chi \bar{N} N$	$-i \frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi$	$-\frac{m_N}{m_\chi} \mathcal{O}_{11}$	O/O
4	$\bar{\chi} \gamma^5 \chi \bar{N} \gamma^5 N$	$-\frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi \frac{\vec{q}}{m_N} \cdot \vec{S}_N$	$-\frac{m_N}{m_\chi} \mathcal{O}_6$	E/E
5	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N$	$1_\chi 1_N$	\mathcal{O}_1	E/E
6	$\bar{\chi} \gamma^\mu \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$\frac{\vec{q}^2}{2m_N m_M} 1_\chi 1_N + 2 \left(\frac{\vec{q}}{m_\chi} \times \vec{S}_\chi + i \vec{v}^\perp \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$\frac{\vec{q}^2}{2m_N m_M} \mathcal{O}_1 - 2 \frac{m_N}{m_M} \mathcal{O}_3 + 2 \frac{m_N^2}{m_M m_\chi} \left(\frac{q^2}{m_N^2} \mathcal{O}_4 - \mathcal{O}_6 \right)$	E/E
7	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu \gamma^5 N$	$-2 \vec{S}_N \cdot \vec{v}^\perp + \frac{2}{m_\chi} i \vec{S}_\chi \cdot (\vec{S}_N \times \vec{q})$	$-2 \mathcal{O}_7 + 2 \frac{m_N}{m_\chi} \mathcal{O}_9$	O/E
8	$i \bar{\chi} \gamma^\mu \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$2i \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$2 \frac{m_N}{m_M} \mathcal{O}_{10}$	O/O
9	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} \gamma_\mu N$	$-\frac{\vec{q}^2}{2m_\chi m_M} 1_\chi 1_N - 2 \left(\frac{\vec{q}}{m_N} \times \vec{S}_N + i \vec{v}^\perp \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right)$	$-\frac{\vec{q}^2}{2m_\chi m_M} \mathcal{O}_1 + \frac{2m_N}{m_M} \mathcal{O}_5 - 2 \frac{m_N}{m_M} \left(\frac{\vec{q}^2}{m_N^2} \mathcal{O}_4 - \mathcal{O}_6 \right)$	E/E
10	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$4 \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$4 \left(\frac{\vec{q}^2}{m_M^2} \mathcal{O}_4 - \frac{m_N^2}{m_M^2} \mathcal{O}_6 \right)$	E/E
11	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} \gamma^\mu \gamma^5 N$	$4i \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \cdot \vec{S}_N$	$4 \frac{m_N}{m_M} \mathcal{O}_9$	O/E
12	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$- \left[i \frac{\vec{q}^2}{m_\chi m_M} - 4 \vec{v}^\perp \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_\chi \right) \right] \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$-\frac{m_N}{m_\chi} \frac{\vec{q}^2}{m_M^2} \mathcal{O}_{10} - 4 \frac{\vec{q}^2}{m_M^2} \mathcal{O}_{12} - 4 \frac{m_N^2}{m_M^2} \mathcal{O}_{15}$	O/O
13	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} \gamma_\mu N$	$2 \vec{v}^\perp \cdot \vec{S}_\chi + 2i \vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_N})$	$2 \mathcal{O}_8 + 2 \mathcal{O}_9$	O/E
14	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$4i \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right)$	$-4 \frac{m_N}{m_M} \mathcal{O}_9$	O/E
15	$\bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} \gamma^\mu \gamma^5 N$	$-4 \vec{S}_\chi \cdot \vec{S}_N$	$-4 \mathcal{O}_4$	E/E
16	$i \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$4i \vec{v}^\perp \cdot \vec{S}_\chi \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$4 \frac{m_N}{m_M} \mathcal{O}_{13}$	E/O
17	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} \gamma_\mu N$	$2i \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi$	$2 \frac{m_N}{m_M} \mathcal{O}_{11}$	O/O
18	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \left[i \frac{\vec{q}^2}{m_N m_M} - 4 \vec{v}^\perp \cdot \left(\frac{\vec{q}}{m_M} \times \vec{S}_N \right) \right]$	$\frac{\vec{q}^2}{m_M^2} \mathcal{O}_{11} + 4 \frac{m_N^2}{m_M^2} \mathcal{O}_{15}$	O/O
19	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} \gamma_\mu \gamma^5 N$	$-4i \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \vec{v}^\perp \cdot \vec{S}_N$	$-4 \frac{m_N}{m_M} \mathcal{O}_{14}$	E/O
20	$i \bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \gamma^5 \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$4 \frac{\vec{q}}{m_M} \cdot \vec{S}_\chi \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	$4 \frac{m_N^2}{m_M^2} \mathcal{O}_6$	E/E

Various profiles and their uncertainties



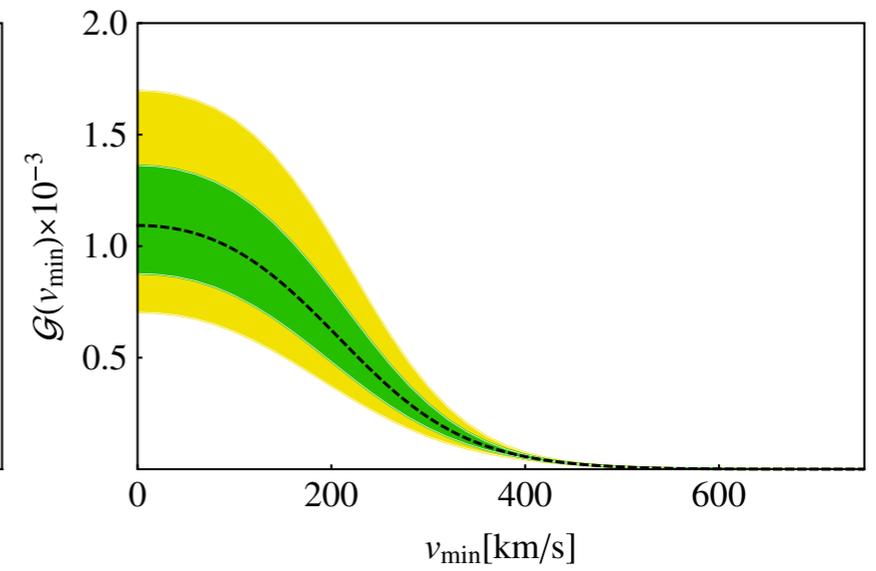
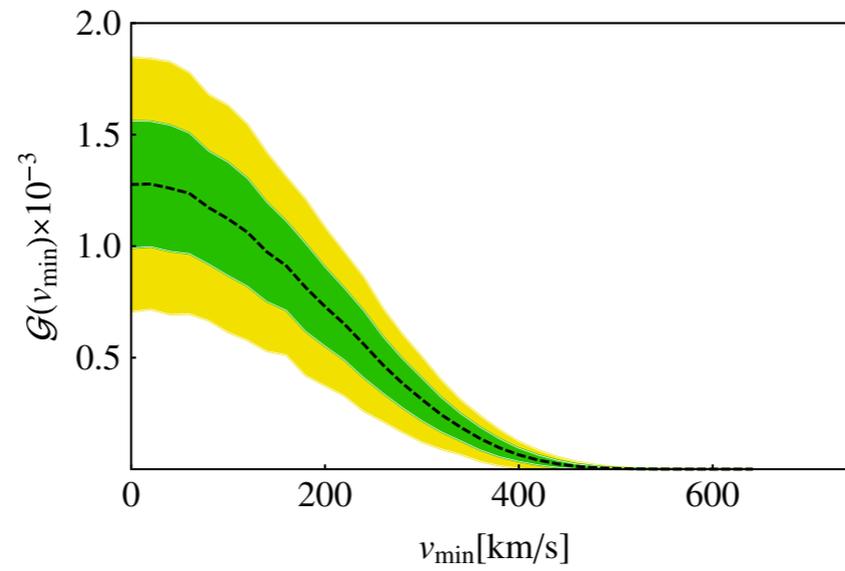
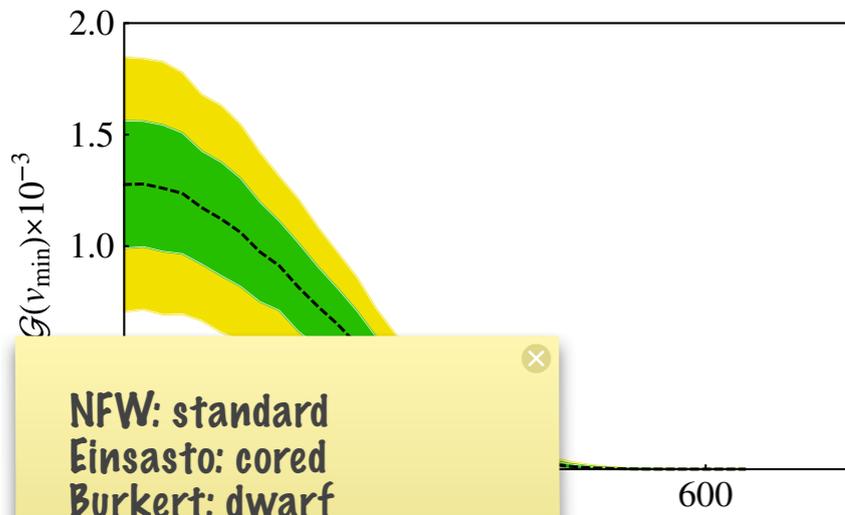
NFW: standard
Einsasto: cored
Burkert: dwarf
Hernquist: analytic
Via Lactea: simulation
MB: isothermal sphere

Various profiles and their uncertainties

MB

Hernquist

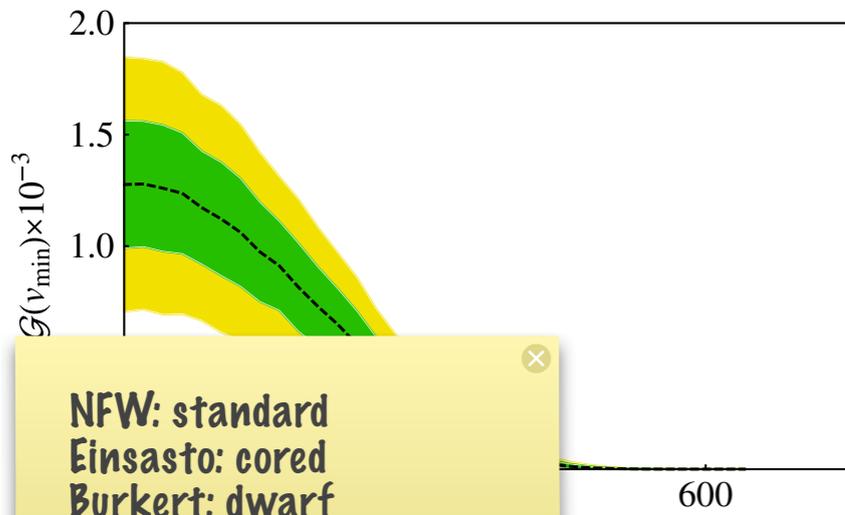
Via Lactea



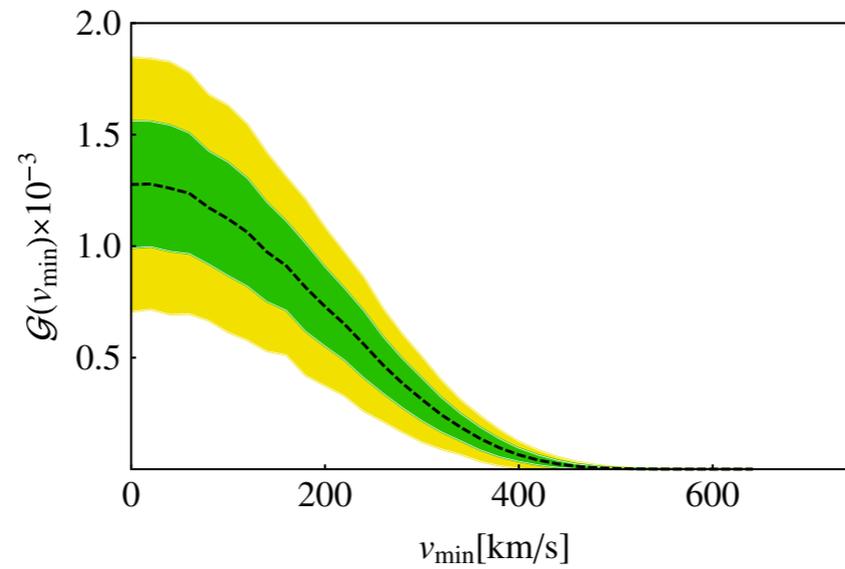
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Various profiles and their uncertainties

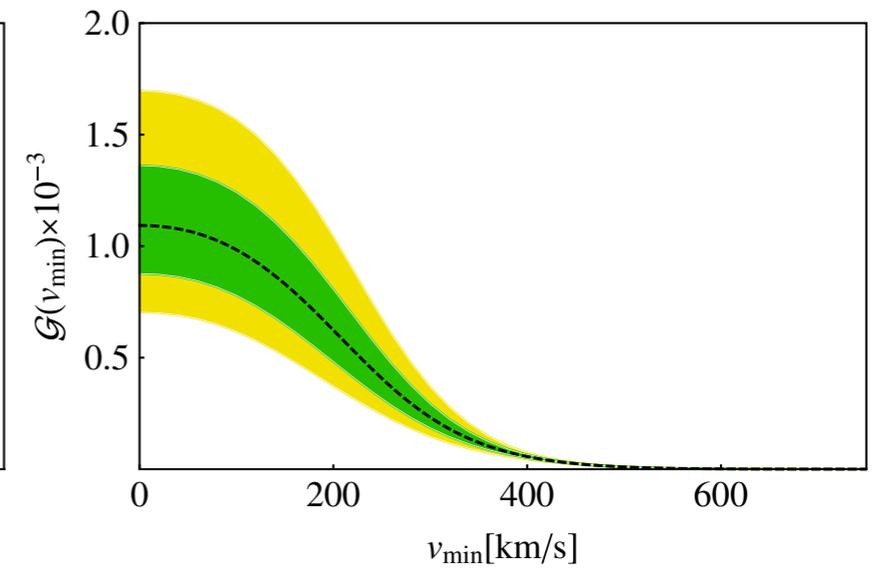
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Hernquist

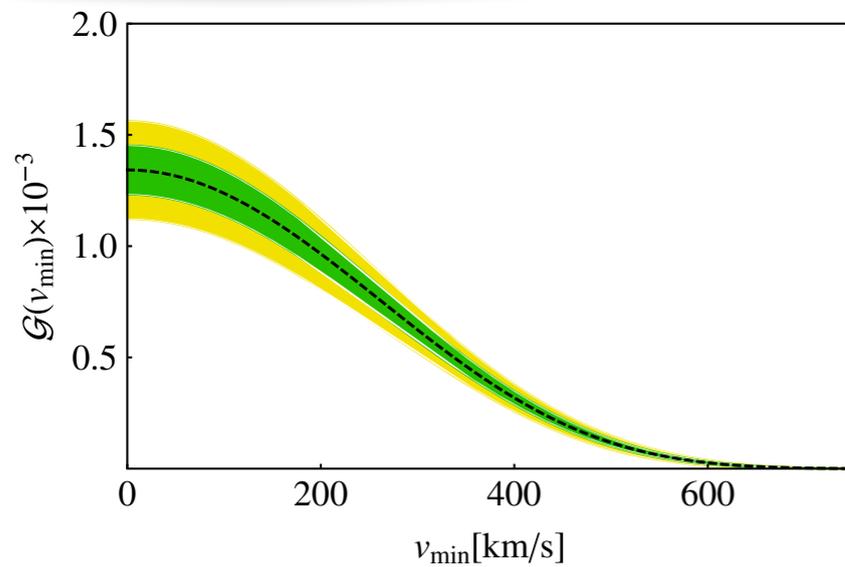


Via Lactea

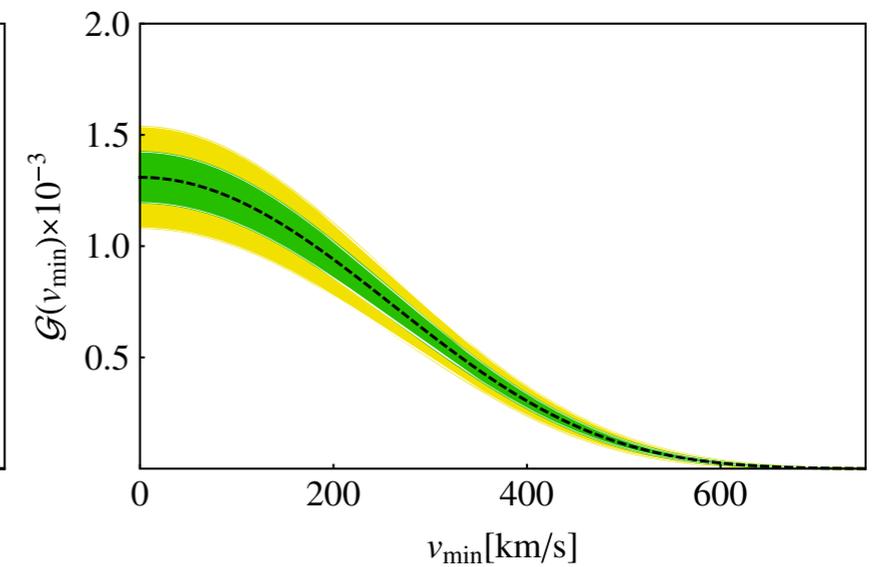
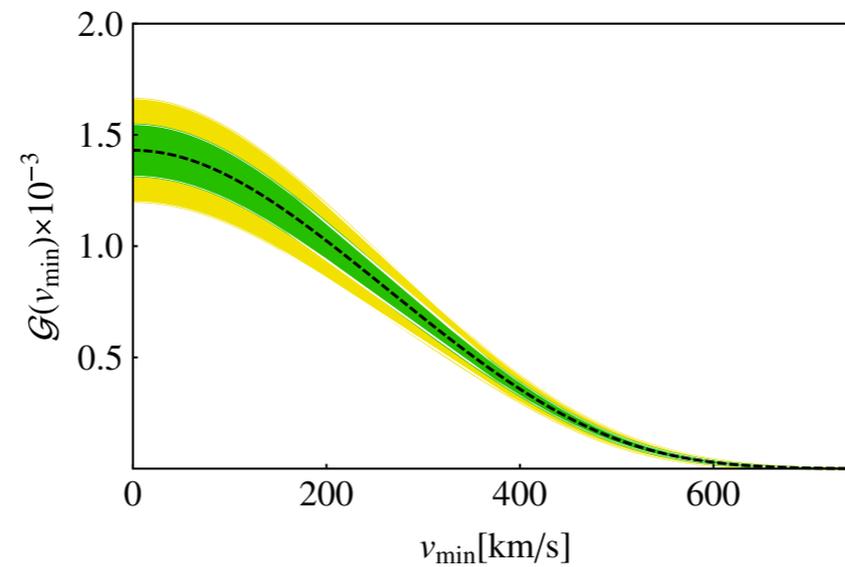


NFW: standard
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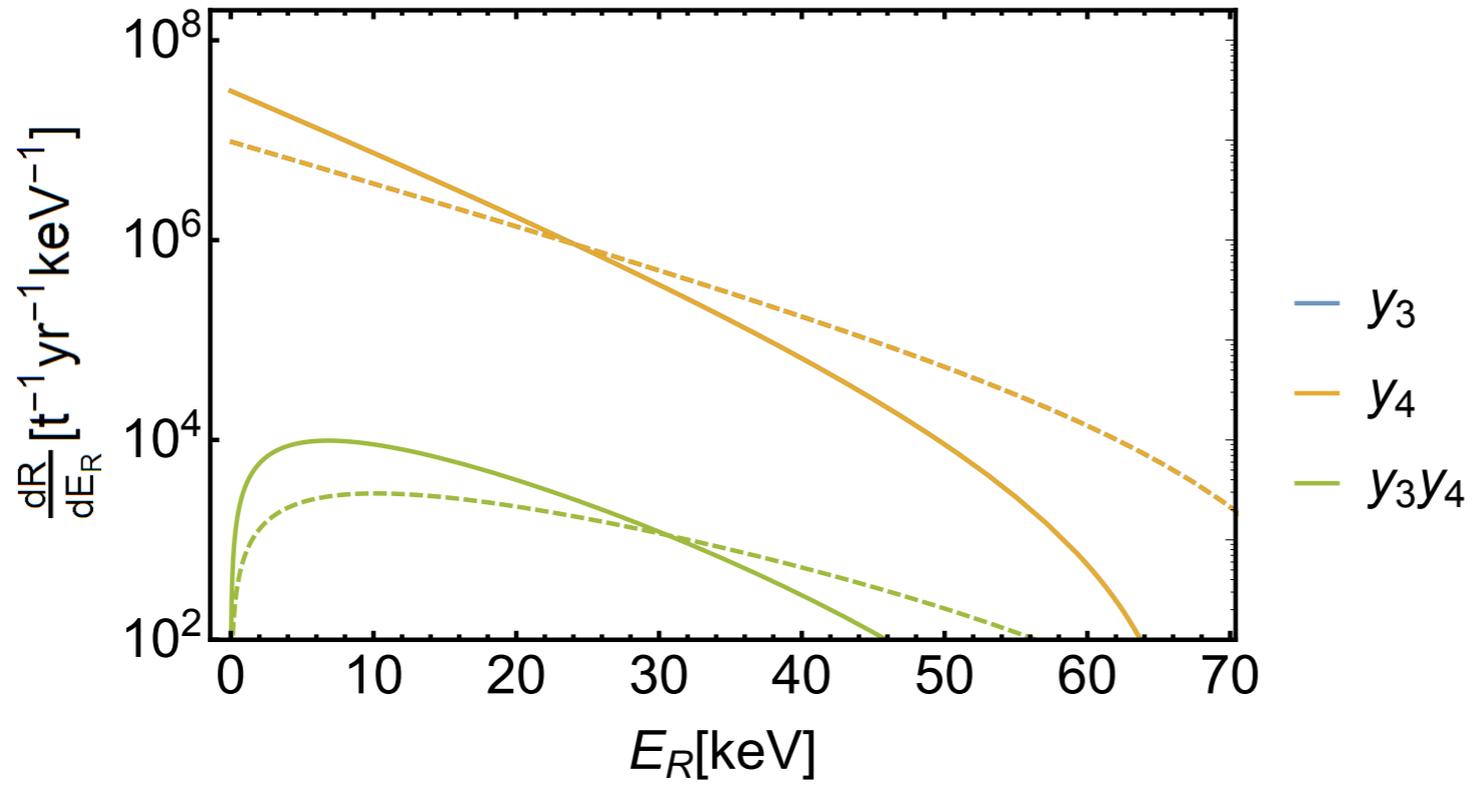
Burkert



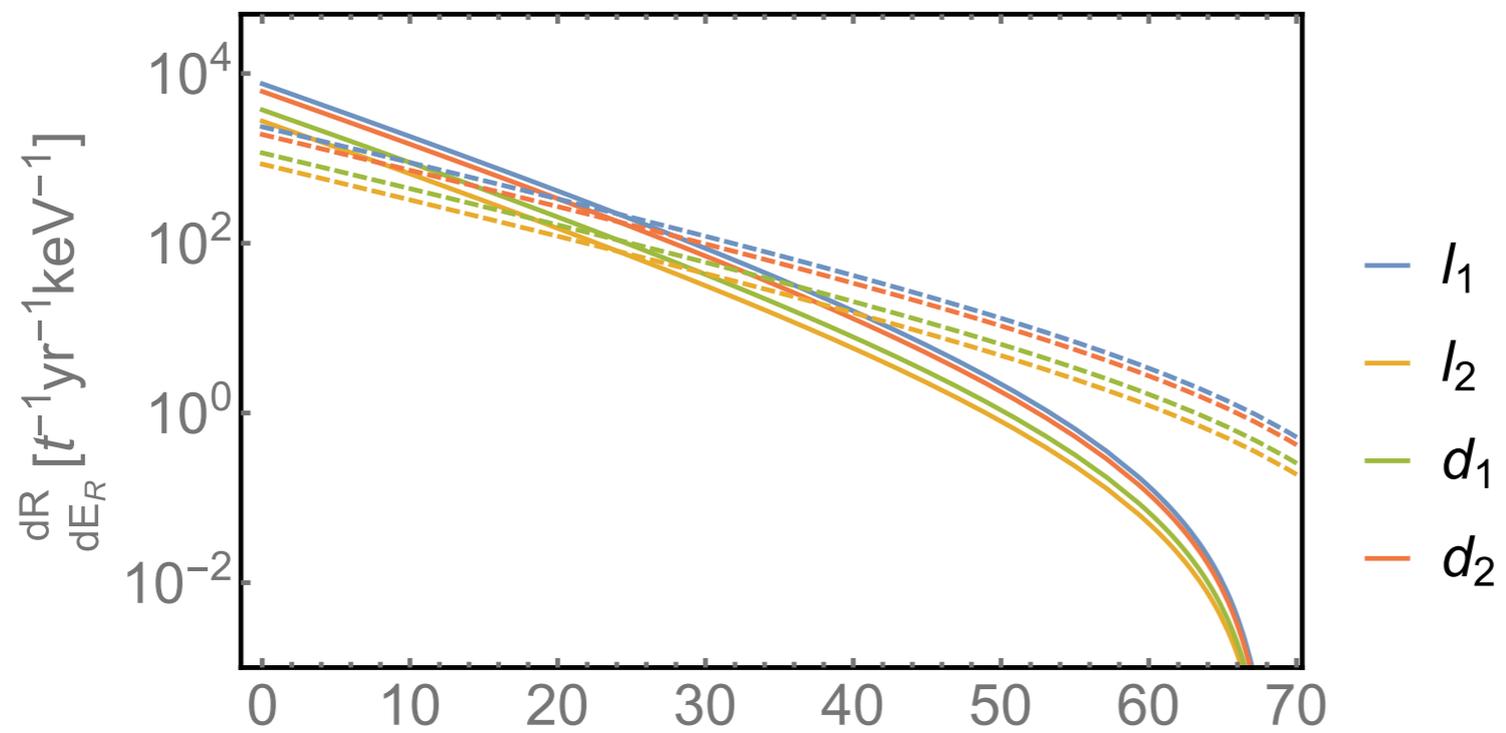
Einasto



Vector dark matter



Spin-1/2 dark matter



Quark bilinears: hadronic matrix elements

$$\langle N_o | m_q \bar{q} q | N_i \rangle \longrightarrow f_{Tq}^N \bar{N} N$$

$$\langle N_o | \bar{q} \gamma^5 q | N_i \rangle \longrightarrow \Delta \tilde{q}^N \bar{N} \gamma^5 N$$

$$\langle N_o | \bar{q} \gamma^\mu q | N_i \rangle \longrightarrow \mathcal{N}_q^N \bar{N} \gamma^\mu N$$

$$\langle N_o | \bar{q} \gamma^\mu \gamma^5 q | N_i \rangle \longrightarrow \Delta_q^N \bar{N} \gamma^\mu \gamma^5 N$$

$$\langle N_o | \bar{q} \sigma^{\mu\nu} q | N_i \rangle \longrightarrow \delta_q^N \bar{N} \sigma^{\mu\nu} N$$

for the heavy quarks

$$\langle N | m_q \bar{q} q | N \rangle = \frac{2}{27} m_N F_{TG}^N = \frac{2}{27} m_N \left(1 - \sum_{q=u,d,s} f_{Tq}^N \right)$$

Summing over all the quarks one finds

$$h_1^N = \sum_{q=u,d,s} h_1^q \frac{m_N}{m_q} f_{Tq}^N + \frac{2}{27} f_{TG}^N \sum_{q=c,b,t} h_1^q \frac{m_N}{m_q}$$

The psuedo-scalar bilinear

$$h_2^N = \sum_{q=u,d,s} h_2^q \Delta \tilde{q}^N - \Delta \tilde{G}^N \sum_{q=c,b,t} \frac{h_2^q}{m_q}$$

The vector bilinear essentially gives the number operator:

$$h_3^N = \begin{cases} 2h_3^u + h_3^d & N = p \\ h_3^u + 2h_3^d & N = n \end{cases}$$

The psuedo-vector bilinear counts the contributions of spin to the nucleon (note that sometimes this coupling has a G_F factored out to make it dimensionless)

$$h_4^N = \sum_{q=u,d,s} h_4^q \Delta_q^N$$

We use the values

$$f_{Tu}^n = 0.014 \quad f_{Tu}^p = 0.02$$

$$f_{Td}^n = 0.036 \quad f_{Td}^p = 0.026$$

$$f_{Ts}^n = 0.118 \quad f_{Ts}^p = 0.118$$

$$\Delta_u^n = -0.427 \quad \Delta_u^p = 0.842$$

$$\Delta_d^n = 0.842 \quad \Delta_d^p = -0.427$$

$$\Delta_s^n = -0.085 \quad \Delta_s^p = -0.085$$

$$\Delta\tilde{u}^n = -108.03 \quad \Delta\tilde{u}^p = 110.55$$

$$\Delta\tilde{d}^n = 108.60 \quad \Delta\tilde{d}^p = -107.17$$

$$\Delta\tilde{s}^n = -0.57 \quad \Delta\tilde{s}^p = -3.37$$

$$\Delta\tilde{G}^n = 35.7\text{MeV} \quad \Delta\tilde{G}^p = 395.2\text{MeV}$$

P. Agrawal, Z. Chacko, C. Kilic, and R. K. Mishra, arXiv:1003.1912 [hep-ph].

K. R. Dienes, J. Kumar, B. Thomas and D. Yaylali, Phys. Rev. D **90**, no. 1, 015012 (2014)

[arXiv:1312.7772 [hep-ph]].

Assuming a universal coupling of the mediators to all quarks, the nucleon level couplings can be written as

$$h_1^N = f_T^N h_1$$

$$h_2^N = \tilde{\Delta}^N h_2$$

$$h_3^N = \mathcal{N}^N h_3$$

$$h_4^N = \Delta^N h_4$$

where we have defined,

$$f_T^n = 11.93 \quad f_T^p = 12.31$$

$$\tilde{\Delta}^n = -0.07 \quad \tilde{\Delta}^p = -0.28$$

$$\mathcal{N}^n = 3 \quad \mathcal{N}^p = 3$$

$$\Delta^n = 0.33 \quad \Delta^p = 0.33$$

$$\delta^n = 0.564 \quad \delta^p = 0.564$$

Scalar DM

$$\begin{aligned}
 \mathcal{L}_{S\phi q} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \frac{\lambda_S}{2} (S^\dagger S)^2 \\
 & + \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m_\phi^2 \phi^2 - \frac{m_\phi \mu_1}{3} \phi^3 - \frac{\mu_2}{4} \phi^4 \\
 & + i\bar{q} \not{D} q - m_q \bar{q} q \\
 & - g_1 m_S S^\dagger S \phi - \frac{g_2}{2} S^\dagger S \phi^2 - h_1 \bar{q} q \phi - i h_2 \bar{q} \gamma^5 q \phi,
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{L}_{SGq} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \frac{\lambda_S}{2} (S^\dagger S)^2 \\
 & - \frac{1}{4} \mathcal{G}_{\mu\nu} \mathcal{G}^{\mu\nu} + \frac{1}{2} m_G^2 G_\mu G^\mu - \frac{\lambda_G}{4} (G_\mu G^\mu)^2 \\
 & + i\bar{q} \not{D} q - m_q \bar{q} q \\
 & - \frac{g_3}{2} S^\dagger S G_\mu G^\mu - i g_4 (S^\dagger \partial_\mu S - \partial_\mu S^\dagger S) G^\mu \\
 & - h_3 (\bar{q} \gamma_\mu q) G^\mu - h_4 (\bar{q} \gamma_\mu \gamma^5 q) G^\mu.
 \end{aligned}$$

Spinor DM

$$\begin{aligned}\mathcal{L}_{\chi\phi q} = & i\bar{\chi}\not{D}\chi - m_\chi\bar{\chi}\chi \\ & + \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{1}{2}m_\phi^2\phi^2 - \frac{m_\phi\mu_1}{3}\phi^3 - \frac{\mu_2}{4}\phi^4 \\ & + i\bar{q}\not{D}q - m_q\bar{q}q \\ & - \lambda_1\phi\bar{\chi}\chi - i\lambda_2\phi\bar{\chi}\gamma^5\chi - h_1\phi\bar{q}q - ih_2\phi\bar{q}\gamma^5q,\end{aligned}$$

$$\begin{aligned}\mathcal{L}_{\chi G q} = & i\bar{\chi}\not{D}\chi - m_\chi\bar{\chi}\chi \\ & - \frac{1}{4}\mathcal{G}_{\mu\nu}\mathcal{G}^{\mu\nu} + \frac{1}{2}m_G^2G_\mu G^\mu \\ & + i\bar{q}\not{D}q - m_q\bar{q}q \\ & - \lambda_3\bar{\chi}\gamma^\mu\chi G_\mu - \lambda_4\bar{\chi}\gamma^\mu\gamma^5\chi G_\mu \\ & - h_3\bar{q}\gamma_\mu q G^\mu - h_4\bar{q}\gamma_\mu\gamma^5 q G^\mu.\end{aligned}$$

Vector DM

$$\begin{aligned}
 \mathcal{L}_{X\phi q} = & -\frac{1}{2}\mathcal{X}_{\mu\nu}^\dagger\mathcal{X}^{\mu\nu} + m_X^2 X_\mu^\dagger X^\mu - \frac{\lambda_X}{2}(X_\mu^\dagger X^\mu)^2 \\
 & + \frac{1}{2}(\partial_\mu\phi)^2 - \frac{1}{2}m_\phi^2\phi^2 - \frac{m_\phi\mu_1}{3}\phi^3 - \frac{\mu_2}{4}\phi^4 \\
 & + i\bar{q}\not{D}q - m_q\bar{q}q \\
 & - b_1 m_X \phi X_\mu^\dagger X^\mu - \frac{b_2}{2}\phi^2 X_\mu^\dagger X^\mu - h_1\phi\bar{q}q - ih_2\phi\bar{q}\gamma^5 q.
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{L}_{XGq} = & -\frac{1}{2}\mathcal{X}_{\mu\nu}^\dagger\mathcal{X}^{\mu\nu} + m_X^2 X_\mu^\dagger X^\mu - \frac{\lambda_X}{2}(X_\mu^\dagger X^\mu)^2 \\
 & - \frac{1}{4}\mathcal{G}_{\mu\nu}\mathcal{G}^{\mu\nu} + \frac{1}{2}m_G^2 G_\mu^2 - \frac{\lambda_G}{4}(G_\mu G^\mu)^2 \\
 & + i\bar{q}\not{D}q - m_q\bar{q}q \\
 & - \frac{b_3}{2}G_\mu^2(X_\nu^\dagger X^\nu) - \frac{b_4}{2}(G^\mu G^\nu)(X_\mu^\dagger X_\nu) - [ib_5 X_\nu^\dagger \partial_\mu X^\nu G^\mu \\
 & + b_6 X_\mu^\dagger \partial^\mu X_\nu G^\nu + b_7 \epsilon_{\mu\nu\rho\sigma}(X^{\dagger\mu}\partial^\nu X^\rho)G^\sigma + h.c.] \\
 & - h_3 G_\mu \bar{q}\gamma^\mu q - h_4 G_\mu \bar{q}\gamma^\mu \gamma^5 q
 \end{aligned}$$

Scalar DM, charged mediator

$$\begin{aligned}\mathcal{L}_{SQq} = & \partial_\mu S^\dagger \partial^\mu S - m_S^2 S^\dagger S - \lambda_S (S^\dagger S)^2 \\ & + i\bar{Q}\not{D}Q - m_Q \bar{Q}Q \\ & + i\bar{q}\not{D}q - m_q \bar{q}q \\ & - (y_1 S \bar{Q}q + y_2 S \bar{Q}\gamma^5 q + h.c.),\end{aligned}$$

Spinor DM, charged mediator

$$\begin{aligned}\mathcal{L}_{\chi\Phi q} = & i\bar{\chi}\not{D}\chi - m_\chi\bar{\chi}\chi \\ & + (\partial_\mu\Phi^\dagger)(\partial^\mu\Phi) - m_\Phi^2\Phi^\dagger\Phi - \frac{\lambda_\Phi}{2}(\Phi^\dagger\Phi)^2 \\ & + i\bar{q}\not{D}q - m_q\bar{q}q \\ & - (l_1\Phi^\dagger\bar{\chi}q + l_2\Phi^\dagger\bar{\chi}\gamma^5q + h.c.),\end{aligned}$$

$$\begin{aligned}\mathcal{L}_{\chi V q} = & i\bar{\chi}\not{D}\chi - m_\chi\bar{\chi}\chi \\ & - \frac{1}{2}\mathcal{V}_{\mu\nu}^\dagger\mathcal{V}^{\mu\nu} + m_V^2V_\mu^\dagger V^\mu \\ & + i\bar{q}\not{D}q - m_q\bar{q}q \\ & - (d_1\bar{\chi}\gamma^\mu qV_\mu^\dagger + d_2\bar{\chi}\gamma^\mu\gamma^5qV_\mu^\dagger + h.c.),\end{aligned}$$

Vector DM, charged mediator

$$\begin{aligned}\mathcal{L}_{XQq} = & -\frac{1}{2}\mathcal{X}_{\mu\nu}^\dagger\mathcal{X}^{\mu\nu} + m_X^2 X_\mu^\dagger X^\mu - \frac{\lambda_X}{2}(X_\mu^\dagger X^\mu)^2 \\ & + i\bar{Q}\not{D}Q - m_Q\bar{Q}Q \\ & + i\bar{q}\not{D}q - m_q\bar{q}q \\ & - (y_3 X_\mu\bar{Q}\gamma^\mu q + y_4 X_\mu\bar{Q}\gamma^\mu\gamma^5 q + h.c.),\end{aligned}$$

TABLE II. Non-zero c_i coefficients for a spin-0 WIMP

	Uncharged Mediator	Charged Mediator
c_1	$\frac{h_1^N g_1}{m_\phi^2}$	$\frac{y_1^\dagger y_1 - y_2^\dagger y_2}{m_Q m_S} f_T^N$
c_{10}	$\frac{-ih_2^N g_1}{m_\phi^2} + \frac{2ig_4 h_4^N}{m_G^2} \frac{m_N}{m_S}$	$i \frac{y_2^\dagger y_1 - y_1^\dagger y_2}{m_Q m_S} \tilde{\Delta}^N$

 TABLE III. c_i coefficients for a spin- $\frac{1}{2}$ WIMP

	Uncharged Mediator	Charged Mediator
c_1	$\frac{h_1^N \lambda_1}{m_\phi^2} - \frac{h_3^N \lambda_3}{m_G^2}$	$\left(\frac{l_2^\dagger l_2 - l_1^\dagger l_1}{4m_\Phi^2} + \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} \right) f_T^N + \left(-\frac{l_2^\dagger l_2 + l_1^\dagger l_1}{4m_\Phi^2} + \frac{d_2^\dagger d_2 + d_1^\dagger d_1}{8m_V^2} \right) \mathcal{N}^N$
c_4	$\frac{4h_4^N \lambda_4}{m_G^2}$	$\frac{l_2^\dagger l_2 - l_1^\dagger l_1}{m_\Phi^2} \delta^N - \left(\frac{l_1^\dagger l_1 + l_2^\dagger l_2}{m_\Phi^2} + \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{2m_V^2} \right) \Delta^N$
c_6	$\frac{h_2^N \lambda_2 m_N}{m_\phi^2 m_\chi}$	$\left(\frac{l_1^\dagger l_1 - l_2^\dagger l_2}{4m_\Phi^2} + \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} \right) \frac{m_N}{m_\chi} \tilde{\Delta}^N$
c_7	$\frac{2h_4^N \lambda_3}{m_G^2}$	$\left(\frac{l_1^\dagger l_2 - l_2^\dagger l_1}{2m_\Phi^2} + \frac{d_1^\dagger d_2 + d_2^\dagger d_1}{4m_V^2} \right) \Delta^N$
c_8	$-\frac{2h_3^N \lambda_4}{m_G^2}$	$\left(\frac{l_1^\dagger l_2 - l_2^\dagger l_1}{2m_\Phi^2} - \frac{d_1^\dagger d_2 + d_2^\dagger d_1}{4m_V^2} \right) \mathcal{N}^N$
c_9	$-\frac{2h_4^N \lambda_3 m_N}{m_\chi m_G^2} - \frac{2h_3^N \lambda_4}{m_G^2}$	$\left(\frac{l_1^\dagger l_2 - l_2^\dagger l_1}{2m_\Phi^2} - \frac{d_1^\dagger d_2 + d_2^\dagger d_1}{4m_V^2} \right) \mathcal{N}^N - \left(\frac{l_1^\dagger l_2 - l_2^\dagger l_1}{2m_\Phi^2} - \frac{d_1^\dagger d_2 + d_2^\dagger d_1}{4m_V^2} \right) \frac{m_N}{m_\chi} \Delta^N$
c_{10}	$\frac{h_2^N \lambda_1}{m_\phi^2}$	$i \left(\frac{l_1^\dagger l_2 - l_2^\dagger l_1}{4m_\Phi^2} + \frac{d_2^\dagger d_1 - d_1^\dagger d_2}{4m_V^2} \right) \tilde{\Delta}^N - i \frac{l_1^\dagger l_2 - l_2^\dagger l_1}{m_\Phi^2} \delta^N$
c_{11}	$-\frac{h_1^N \lambda_2 m_N}{m_\phi^2 m_\chi}$	$i \left(\frac{l_2^\dagger l_1 - l_1^\dagger l_2}{4m_\Phi^2} + \frac{d_2^\dagger d_1 - d_1^\dagger d_2}{4m_V^2} \right) \frac{m_N}{m_\chi} f_T^N + i \frac{l_1^\dagger l_2 - l_2^\dagger l_1}{m_\Phi^2} \frac{m_N}{m_\chi} \delta^N$
c_{12}	0	$\frac{l_2^\dagger l_1 - l_1^\dagger l_2}{m_\Phi^2} \delta^N$

TABLE IV. c_i coefficients for a spin-1 WIMP

	Uncharged Mediator	Charged Mediator
c_1	$\frac{b_1 h_1^N}{m_\phi^2}$	$\frac{y_3^\dagger y_3 - y_4^\dagger y_4}{m_Q m_X} f_T^N$
c_4	$\frac{4\text{Im}(b_7) h_4^N}{m_G^2}$	$2 \frac{y_3^\dagger y_3 - y_4^\dagger y_4}{m_Q m_X} \delta^N$
c_5	$\frac{\text{Re}(b_6) h_3^N}{m_G^2} \frac{m_N}{m_X}$	0
c_8	$\frac{2\text{Im}(b_7) h_3^N}{m_G^2}$	0
c_9	$-\frac{2\text{Re}(b_6) h_4^N}{m_G^2} \frac{m_N}{m_X} + \frac{2\text{Im}(b_7) h_3^N}{m_G^2}$	0
c_{10}	$\frac{b_1 h_2^N}{m_\phi^2} - \frac{3b_5 h_4^N}{m_G^2} \frac{m_N}{m_X}$	$i \frac{y_4^\dagger y_3 - y_3^\dagger y_4}{m_Q m_X} \tilde{\Delta}^N$
c_{11}	$\frac{\text{Re}(b_7) h_3^N}{m_G^2} \frac{m_N}{m_X}$	$i \frac{y_4^\dagger y_3 - y_3^\dagger y_4}{m_Q m_X} \delta^N$
c_{12}	0	$2i \frac{y_3^\dagger y_4 - y_4^\dagger y_3}{m_Q m_X} \delta^N$
c_{14}	$-\frac{2\text{Re}(b_7) h_4^N}{m_G^2} \frac{m_N}{m_X}$	0
c_{17}	$-\frac{4\text{Im}(b_6) h_3^N}{m_G^2} \frac{m_N}{m_X}$	0
c_{18}	$\frac{4\text{Im}(b_6) h_4^N}{m_G^2} \frac{m_N}{m_X}$	$-2i \frac{y_4^\dagger y_3 - y_3^\dagger y_4}{m_Q m_X} \delta^N$