

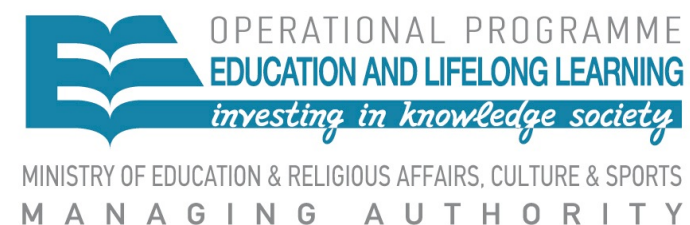


# *Determination of spin and parity of the Higgs boson in the $WW^* \rightarrow e\nu\mu\nu$ decay channel with the ATLAS detector*

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HEP2015  
Athens, Greece



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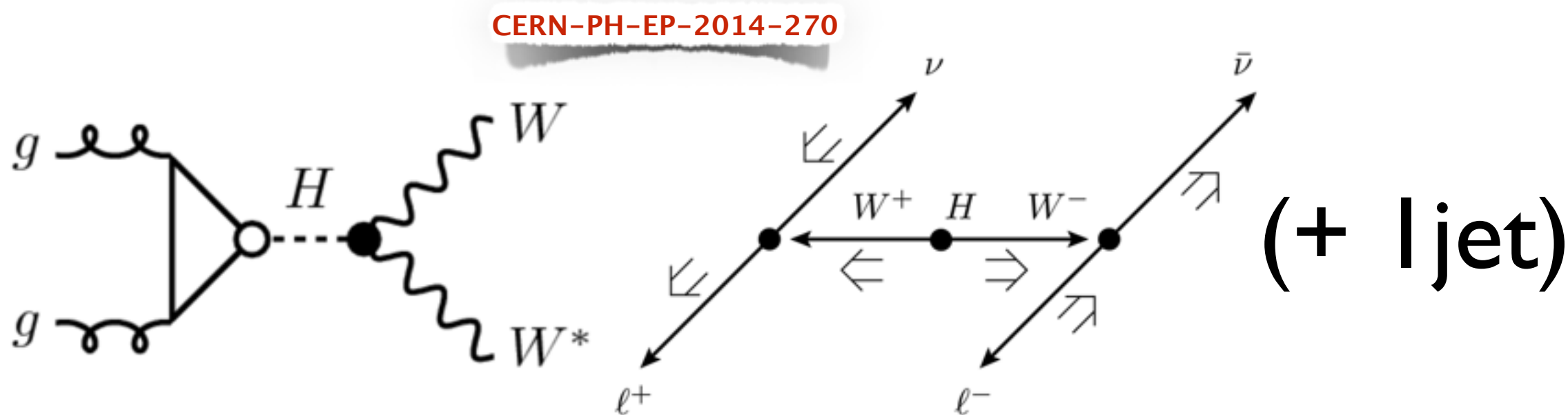
# Introduction

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- Newly discovered resonance at  $125.09 \pm 0.21$  (stat.)  $\pm 0.11$  (syst.) GeV :  
Determining the *spin* & *CP*  $\rightarrow$  establish the nature of the boson : *Is it the (a) Standard Model Higgs or not?*
- Using ATLAS Run-I  $\sqrt{s}=8\text{TeV}$  data to test the SM ( $J^{CP} = 0^{++}$ ) hypothesis vs alternative spin/CP models :
  - *Spin Analysis*
    - Spin  $2^+$  graviton-like model
  - *CP Analysis:*
    - Spin  $0^{+-}$  BSM
    - Spin  $0_h^{++}$  BSM
    - *CP-Mixing :*  
Implying CP violation in the Higgs sector  $\rightarrow$  *Observed resonance is a mass, but not a CP eigenstate.*

# Event Selection

- Share object definition, background estimates and some systematic uncertainties with the  $H \rightarrow WW^*$  couplings analysis
- Analysis restricted to the  $e\nu\mu\nu$  final state
  - 0 and 1 jet-bin for spin analysis
  - 0 jet-bin only for CP analysis



Variable	Requirements
Preselection	
$N_{\text{leptons}}$	Exactly 2 with $p_T > 10$ GeV, $e\mu$ , opposite sign
$p_T^{\ell_1}$	$> 22$ GeV
$p_T^{\ell_2}$	$> 15$ GeV
$m_{\ell\ell}$	$> 10$ GeV
$p_T^{\text{miss}}$	$> 20$ GeV

0-jet selection	
DY $p_T^{\ell\ell}$	$> 20$ GeV
WW $m_{\ell\ell}$	$< 80$ GeV
DY $\Delta\phi_{\ell\ell}$	$< 2.8$
non-U.C. $p_T^H$	$< 125$ or $300$ GeV (*)

1-jet selection	
top $b$ -veto	No $b$ -jets with $p_T > 20$ GeV
Z/ $\gamma^* \rightarrow \tau\tau$ $m_{\tau\tau}$	$< m_Z - 25$ GeV
W+jets $m_T^\ell$	$> 50$ GeV
$m_{\ell\ell}$	$< 80$ GeV
$\Delta\phi_{\ell\ell}$	$< 2.8$
top WW $m_T$	$< 150$ GeV
$p_T^H$	$< 125$ or $300$ GeV (*)

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	$N_{\text{ggF}}$	$N_{\text{WW}}$	$N_{t\bar{t}}$	$N_t$	$N_{\text{DY},\tau\tau}$	$N_{\text{W+jets}}$	$N_{\text{VV}}$	$N_{\text{DY,SF}}$	$N_{\text{bkg}}$	Data	Data/ $N_{\text{bkg}}$
0j SR	218	2796	235	135	515	366	311	32	4390	4730	$1.08 \pm 0.02$
1j SR:	77	555	267	103	228	123	131	5.8	1413	1569	$1.11 \pm 0.03$
1j SR: $p_T^H < 300$ GeV	77	553	267	103	228	123	131	5.8	1411	1567	$1.11 \pm 0.03$
1j SR: $p_T^H < 125$ GeV	76	530	259	101	224	121	128	5.8	1367	1511	$1.11 \pm 0.03$





# *Spin Analysis*



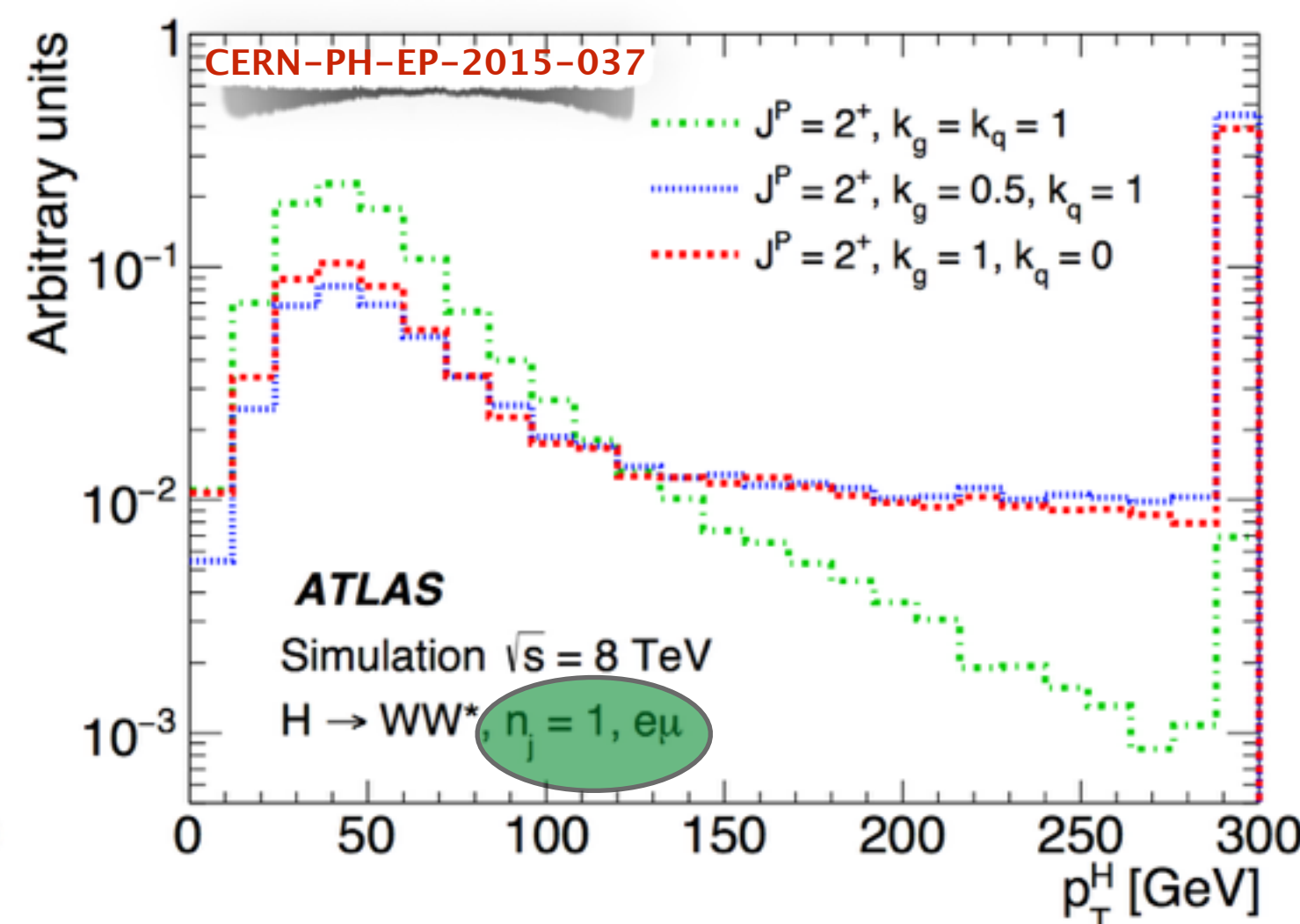
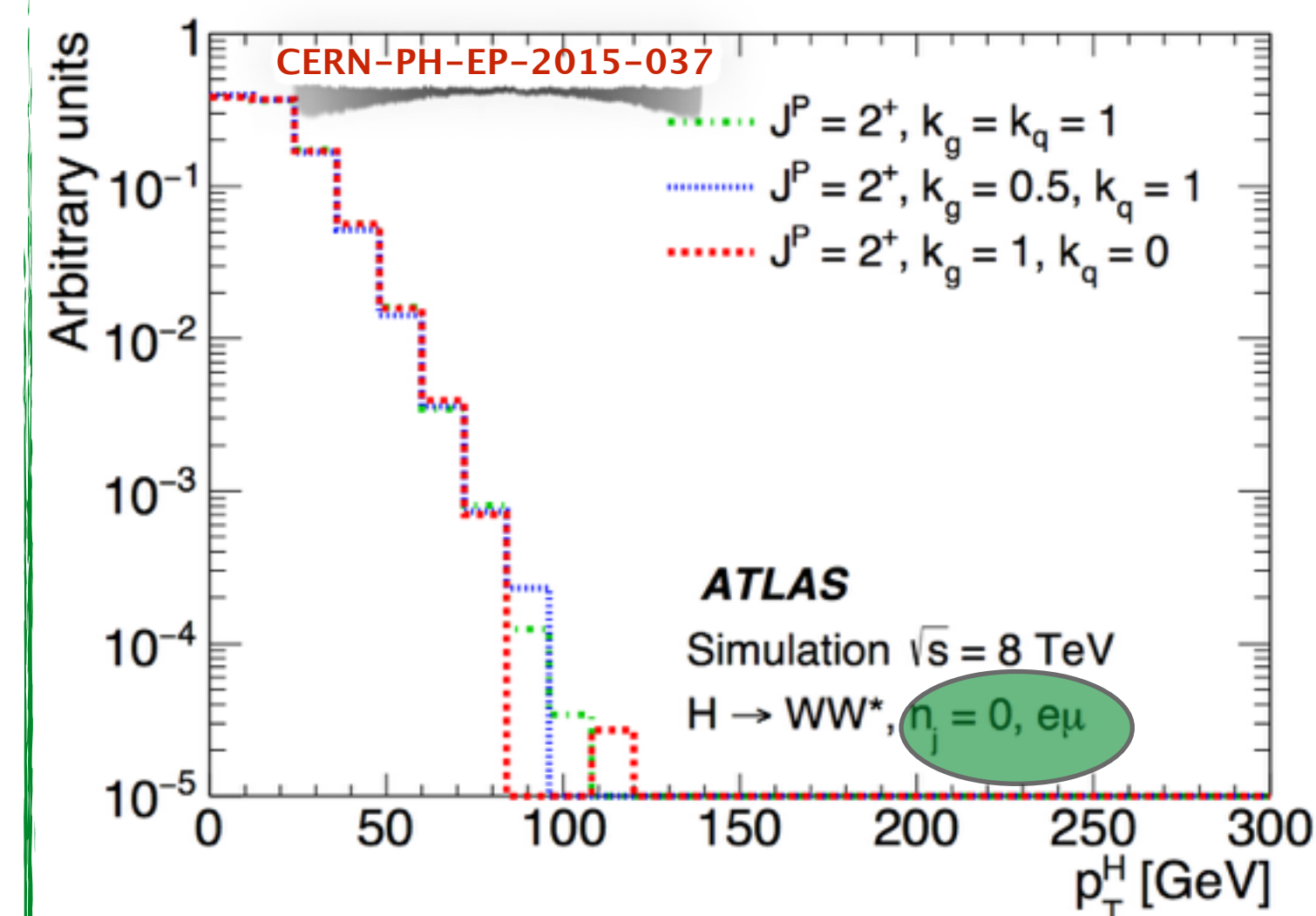
# Theoretical Framework

- Effective Field Theory with a cut-off scale at  $\Lambda = 1 \text{ TeV}$   
(Higgs Characterization Model within MadGraph5\_aMC@NLO)

$$\mathcal{L}_2^p = \sum_{p=V,f} -\frac{1}{\Lambda} \kappa_p T_{\mu\nu}^p X_2^{\mu\nu}$$

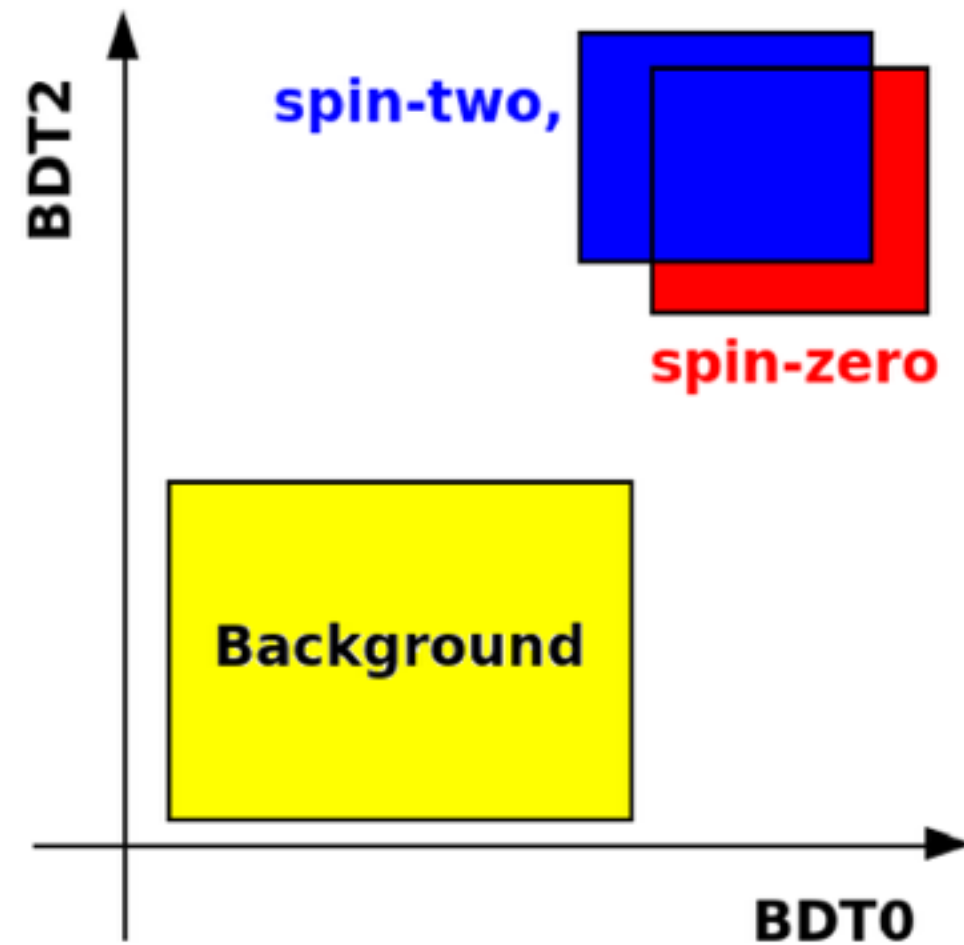
- Gravity is insensitive to the nature of other particle fields:
  - all  $\kappa$ -couplings should be equal (universal)
    - but observed BRs to  $gg, WW, ZZ$  not reproduced
    - still worth investigating
- need to consider benchmarks with non-universal couplings
  - cannot constrain  $\kappa_g, \kappa_q$  separately with data  $\rightarrow$  try various cases

- Spin-2 Benchmarks (fixed-hypothesis test)
  - universal couplings (U.C.)  $\kappa_g = \kappa_q$  (ggF 96% at LO)
  - non-universal couplings:
 
$$\left. \begin{array}{ll} \kappa_g = 0.5 & \kappa_q = 1 \\ \kappa_g = 0 & \kappa_q = 1 \end{array} \right\} p_T^H < 125 \text{ (300) GeV}$$



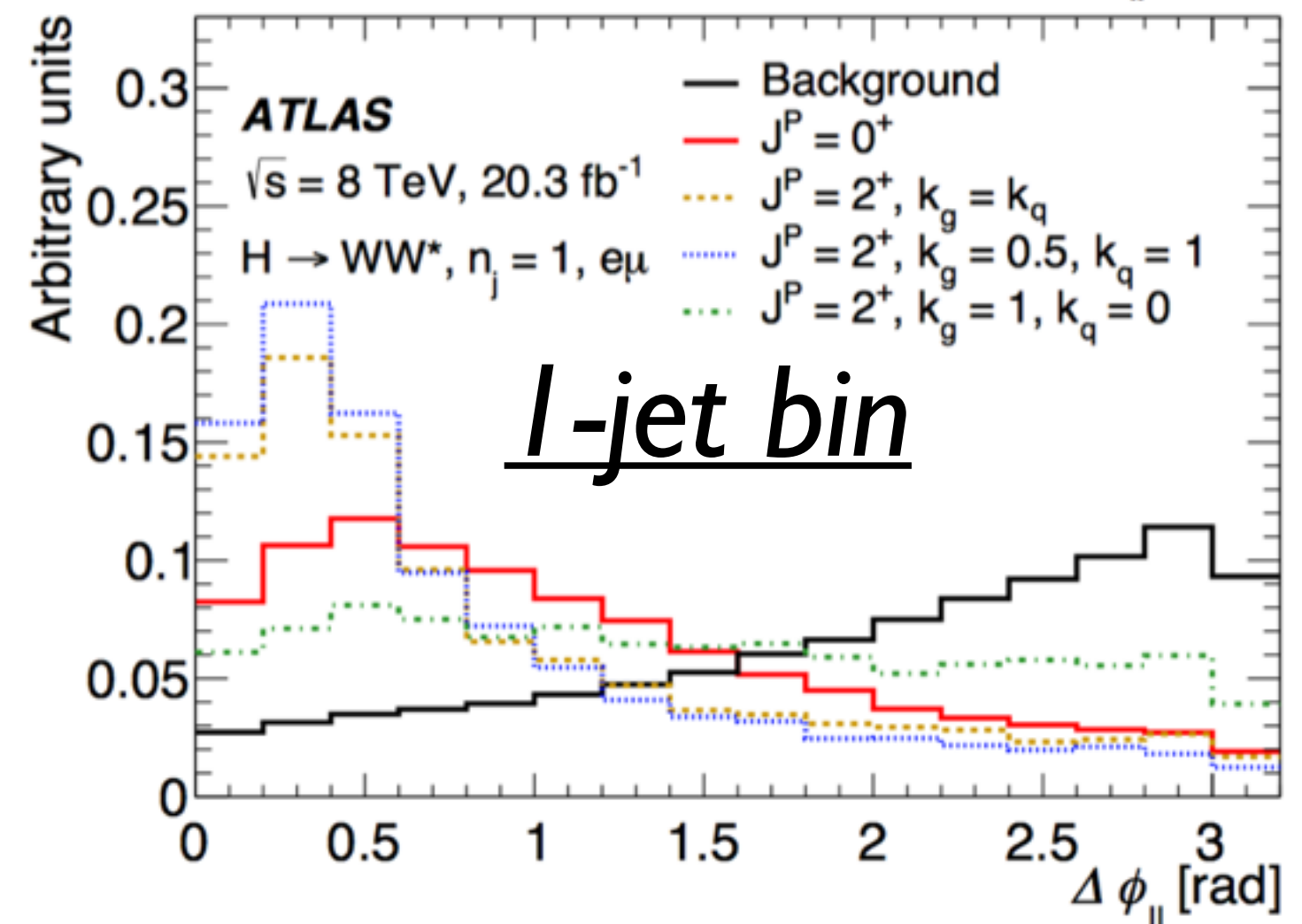
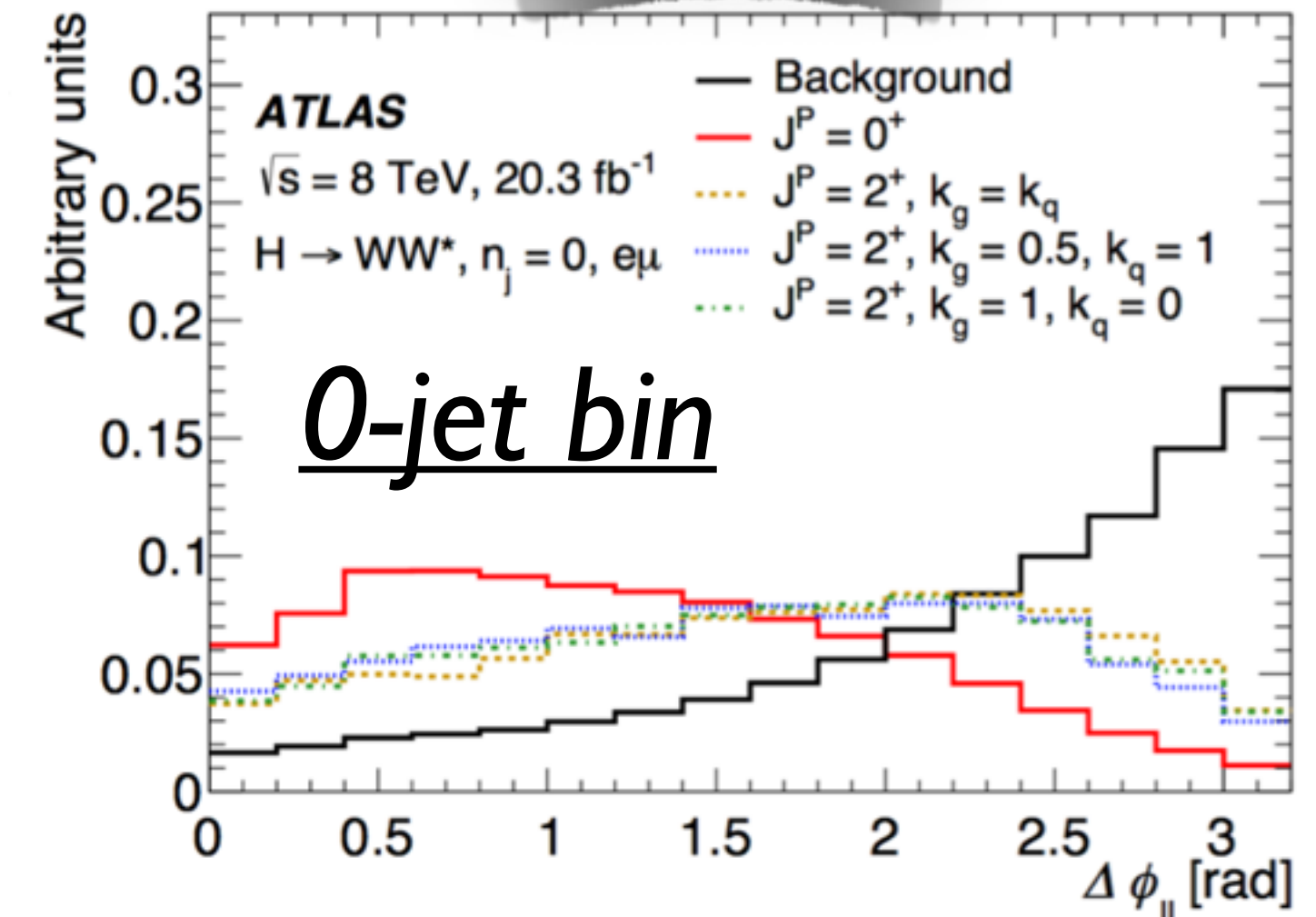
- NLO effects lead to a tail in  $p_T^H$  when jets are in the final state
- Apply a selection on  $p_T^H$  to preserve unitarity

# Analysis Strategy



- Exploiting *shape* and correlation variations with BDT analysis.
- Build two BDTs :  $m(\ell\ell), \Delta\phi^{\ell\ell}, p_T^{\ell\ell}, m_T$ 
  - **BDT0**: Trained with the SM signal vs SM backgrounds
  - **BDT2**: Trained with the spin-2 signal vs SM backgrounds
- Combine the BDT responses in a 2D space

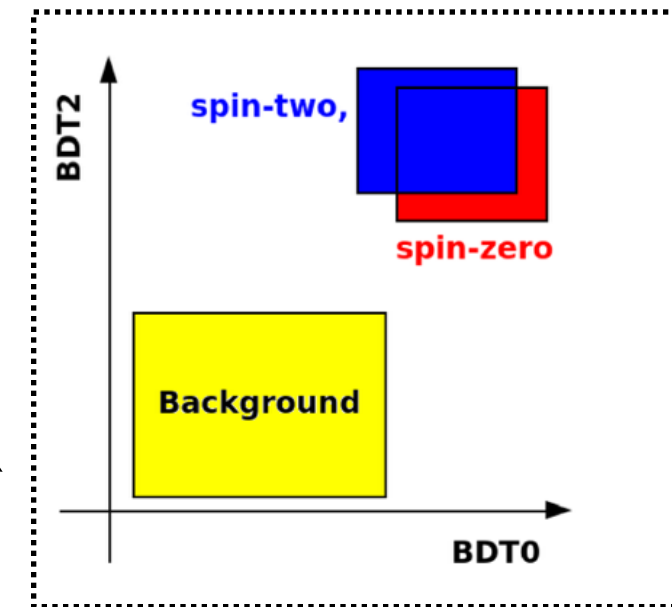
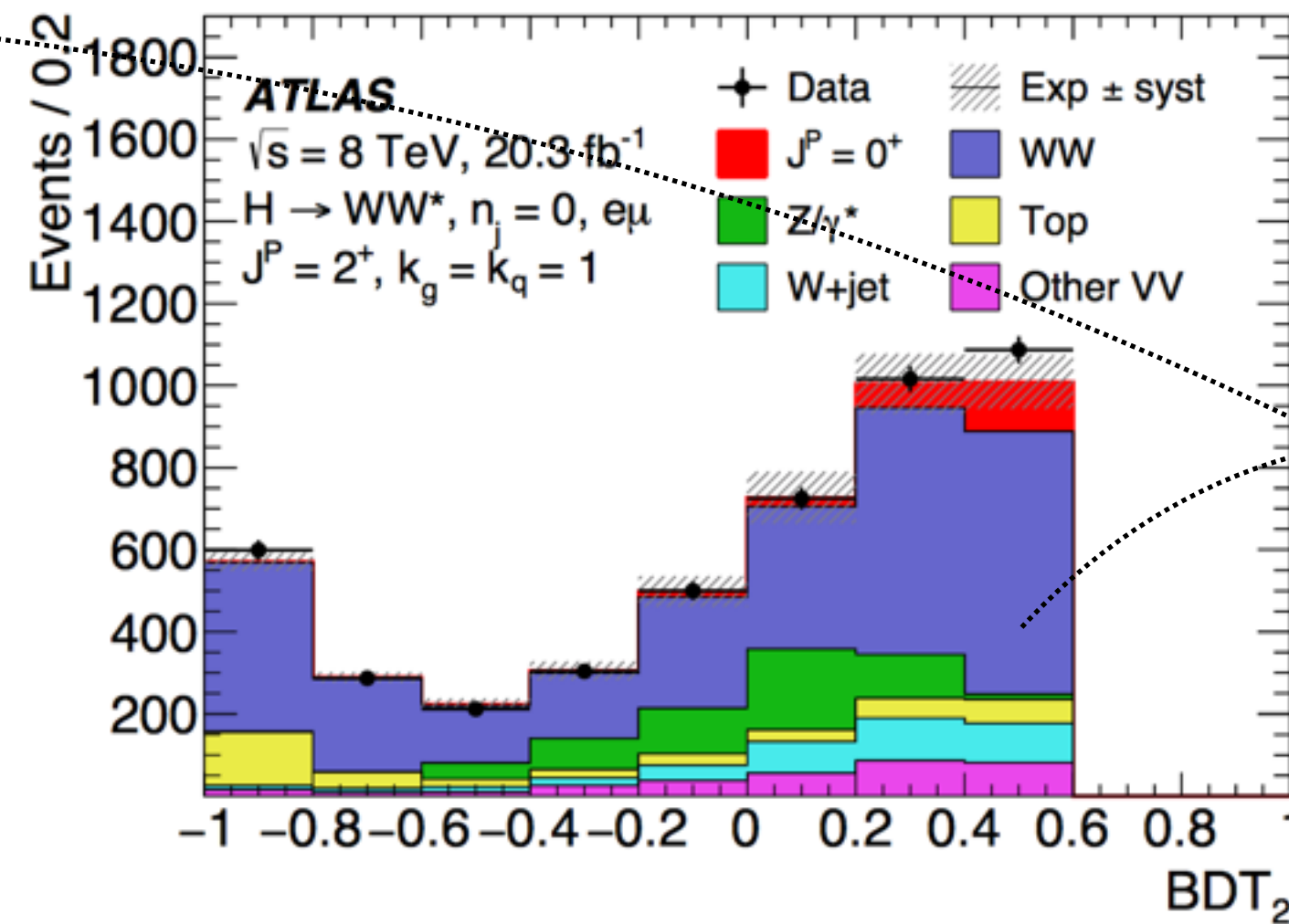
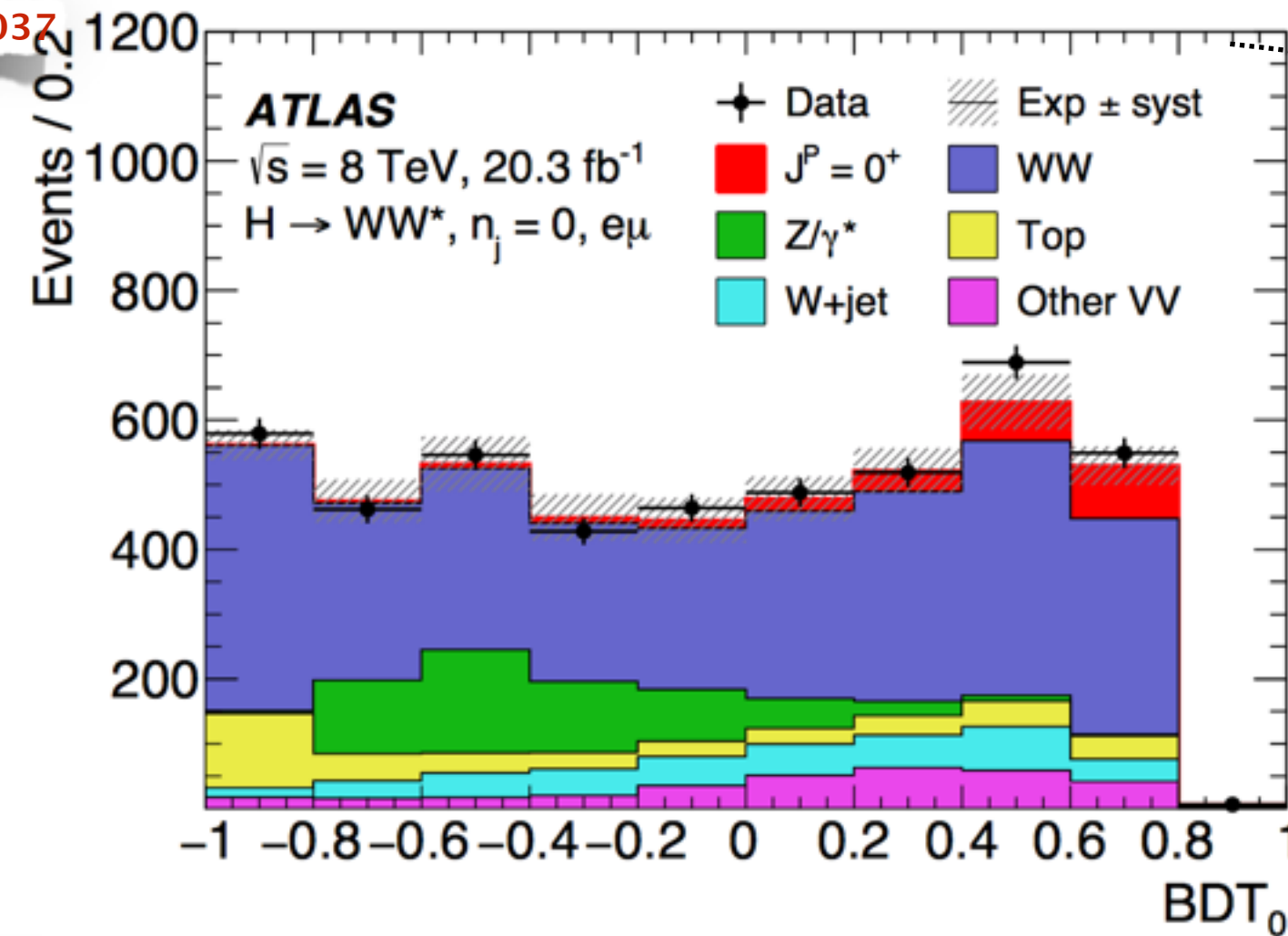
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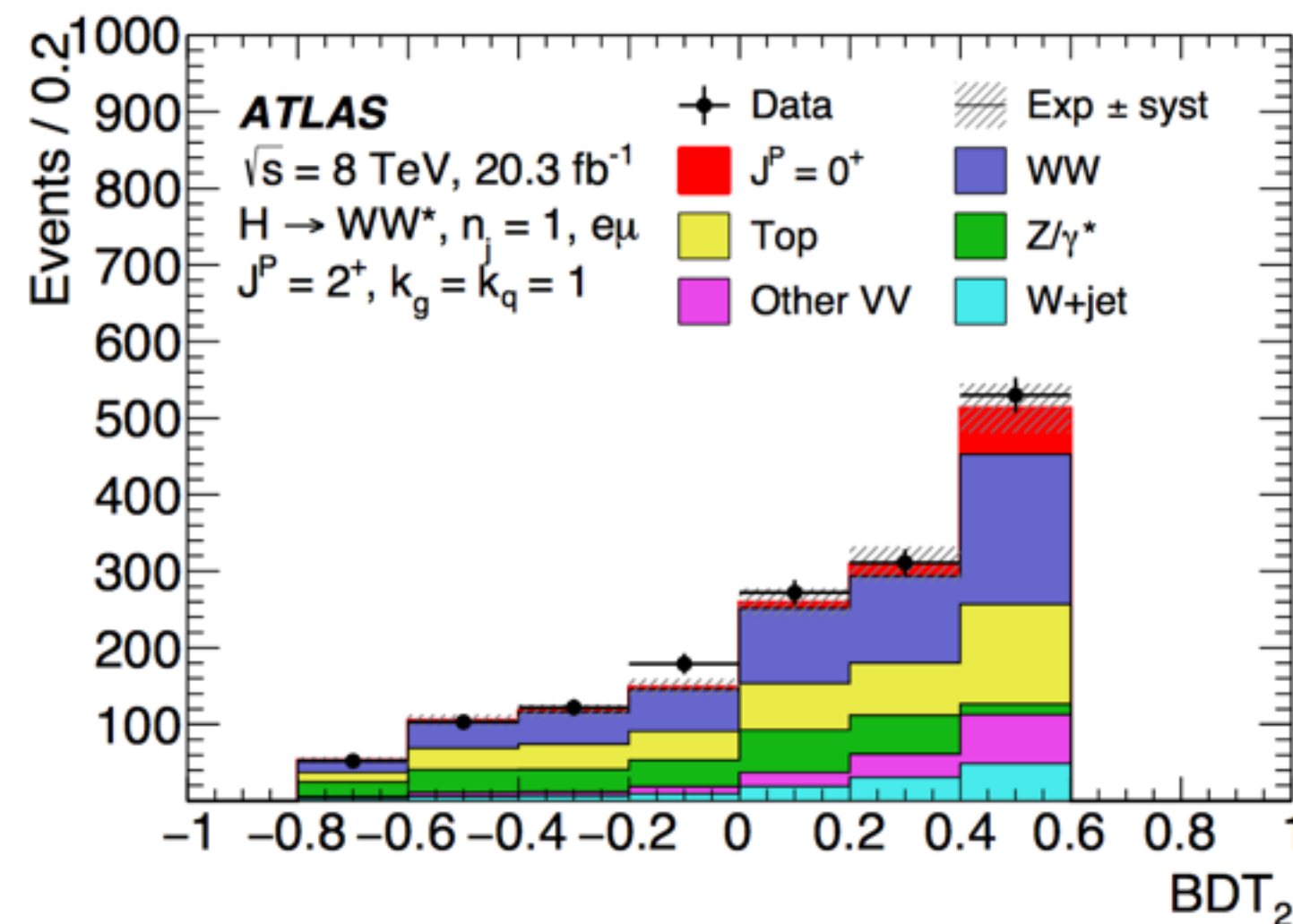
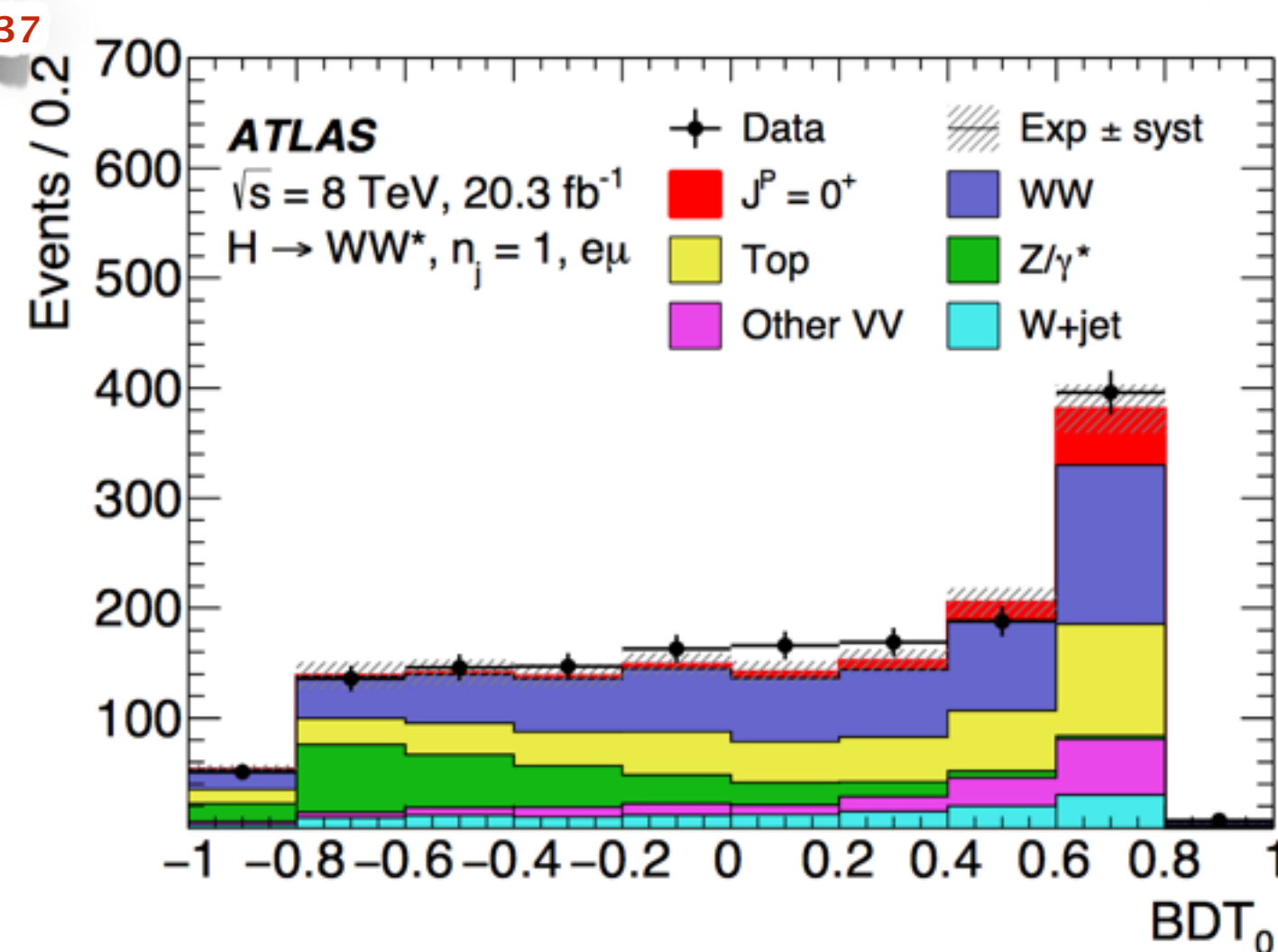


# BDT Response: Univ. Couplings

0-jet

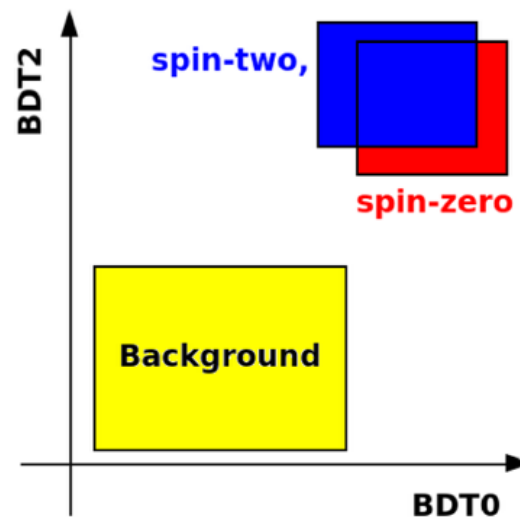


1-jet





# Statistical Interpretation



- The 2D space created out of the two BDTs is then unrolled row-by-row in a 1D distribution
- This unrolled 1D distribution is used for the fit.

- For the fit of the fixed hypothesis tests:

- Binned likelihood with P.O.I.  $\varepsilon$ , the fraction of SM events with respect to the expected.
- Template histograms for nominal signal and background rates construct the likelihood, while systematic uncertainties are treated as nuisance parameters

$$\mathcal{L}(\varepsilon, \mu, \theta) = \prod_i^{N_{\text{bins}}} P(N_i | \mu(\varepsilon S_{\text{SM},i}(\theta) + (1 - \varepsilon) S_{\text{ALT},i}(\theta)) + B_i(\theta)) \times \prod_i^{N_{\text{sys}}} \mathcal{A}(\tilde{\theta}_i | \theta_i)$$

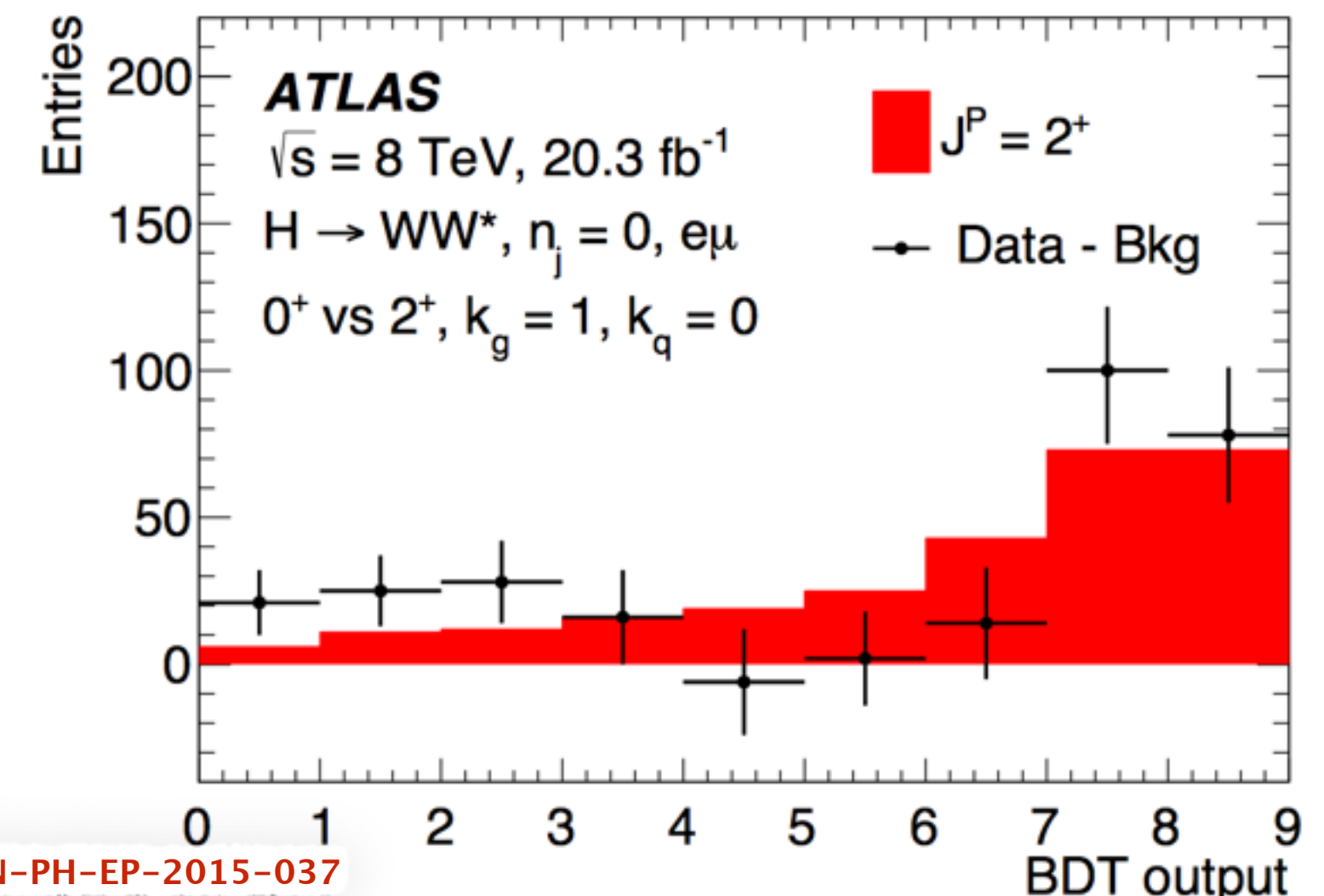
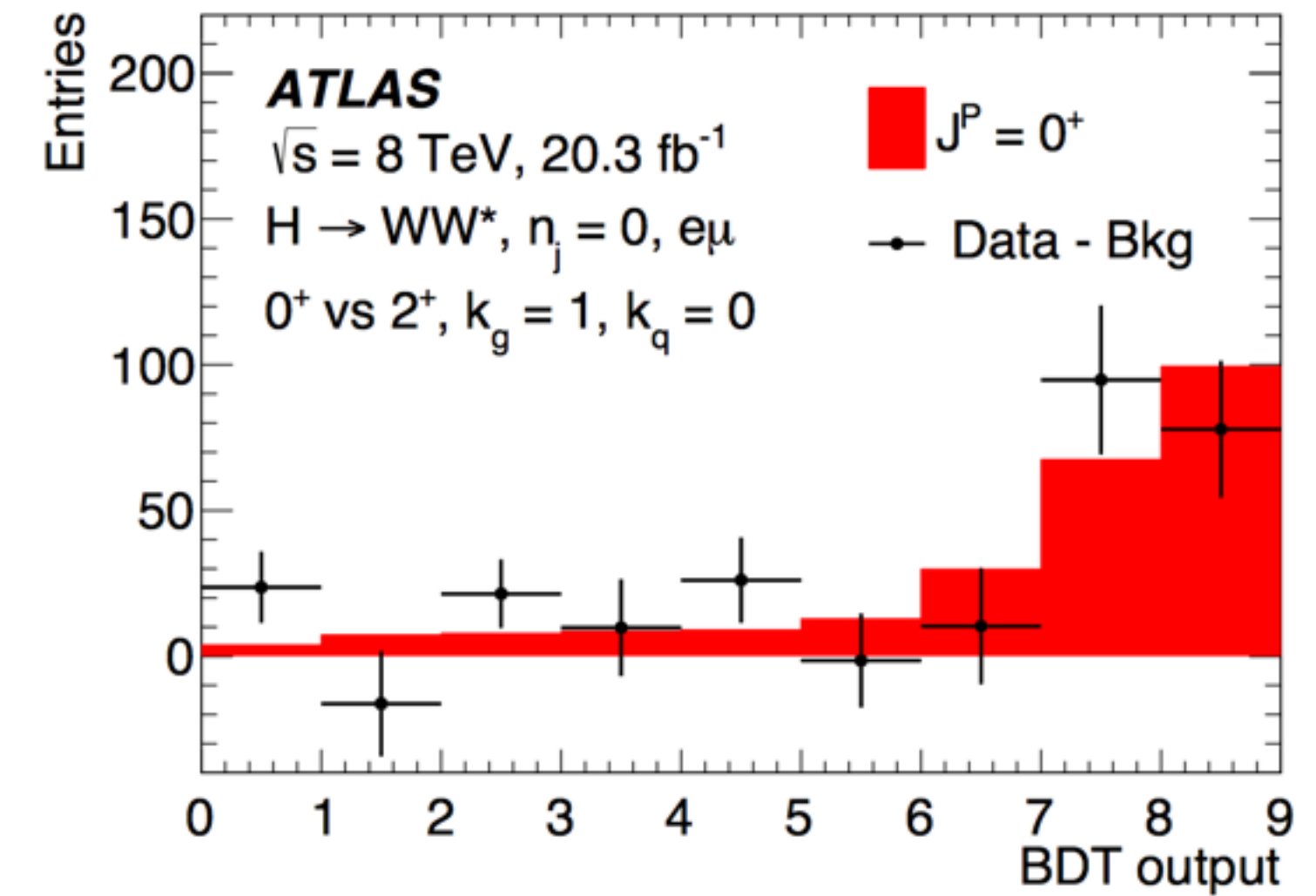
- The compatibility with the data is estimated with the statistic test

$$q = \ln \frac{\mathcal{L}(\varepsilon = 1, \hat{\mu}_{\varepsilon=1}, \hat{\theta}_{\varepsilon=1})}{\mathcal{L}(\varepsilon = 0, \hat{\mu}_{\varepsilon=0}, \hat{\theta}_{\varepsilon=0})} \quad \text{CL}_s = \frac{p_{\text{obs}}^{\text{ALT}}}{1 - p_{\text{obs}}^{\text{SM}}}$$

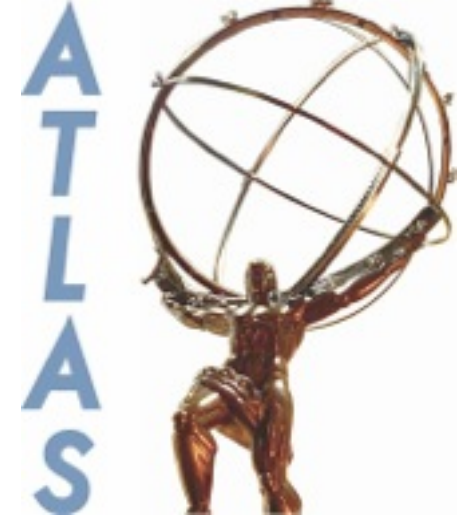
and pseudo-experiments are used to calculate the  $p0$ -values and the CLs

# Spin Results

Channel	$p_{\text{exp}, \mu=1}^{\text{SM}}$	$p_{\text{exp}, \mu=\hat{\mu}}^{\text{SM}}$	$p_{\text{exp}, \mu=\hat{\mu}}^{\text{ALT}}$	$p_{\text{obs}}^{\text{SM}}$	$p_{\text{obs}}^{\text{ALT}}$	$1 - \text{CL}_s$
Spin-2, $\kappa_g = \kappa_q$						
0+1-jet	0.131	0.039	0.033	0.246	0.117	84.5%
Spin-2, $\kappa_g = 0.5, \kappa_q = 1, p_T^H < 125 \text{ GeV}$						
0+1-jet	0.105	0.047	0.022	0.685	0.007	97.8%
Spin-2, $\kappa_g = 0.5, \kappa_q = 1, p_T^H < 300 \text{ GeV}$						
0+1-jet	0.023	0.014	0.004	0.524	0.003	99.3%
Spin-2, $\kappa_g = 1, \kappa_q = 0, p_T^H < 125 \text{ GeV}$						
0+1-jet	0.109	0.041	0.029	0.421	0.044	92.5%
Spin-2, $\kappa_g = 1, \kappa_q = 0, p_T^H < 300 \text{ GeV}$						
0+1-jet	0.015	0.016	0.004	0.552	0.003	99.4%



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# *CP Analysis*



$$\mathcal{L}_0^W = \left\{ c_\alpha \kappa_{SM} \left[ \frac{1}{2} g_{HWW} W_\mu^+ W^{-\mu} \right] - \frac{1}{2} \frac{1}{\Lambda} \left[ c_\alpha \kappa_{HWW} W_{\mu\nu}^+ W^{-\mu\nu} + s_\alpha \kappa_{AWW} W_{\mu\nu}^+ \tilde{W}^{-\mu\nu} \right] \right\} X_0$$

**SM:**  $\kappa_{SM} = 1, \kappa_{HWW} = \kappa_{AWW} = 0, c_\alpha = 1$

**BSM CP-Even:**  $\kappa_{SM} = 0, \kappa_{HWW} = 1, \kappa_{AWW} = 0, c_\alpha = 1$

**BSM CP-Odd:**  $\kappa_{SM} = 0, \kappa_{HWW} = 0, \kappa_{AWW} = 1, c_\alpha = 0$

## 1. Fixed Hypothesis Tests:

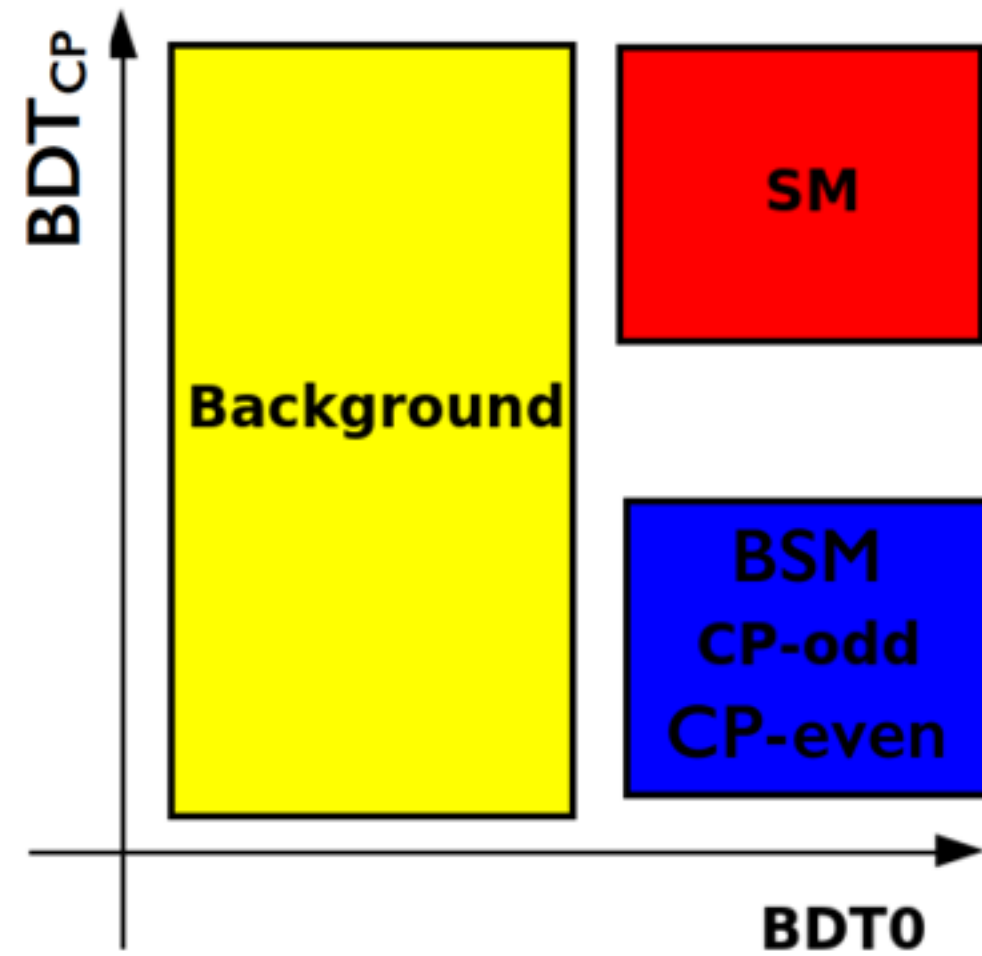
- SM vs pure CP-Odd & SM vs pure CP-Even

2. *BSM CP-Even Scan* : Scan on  $\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}}$  where  $\tilde{\kappa}_{HWW} = \frac{1}{4} \frac{v}{\Lambda} \kappa_{HWW}$

3. *BSM CP-Odd Scan* : Scan on  $\frac{\tilde{\kappa}_{AWW}}{\kappa_{SM}} \tan \alpha$  where  $\tilde{\kappa}_{AWW} = \frac{1}{4} \frac{v}{\Lambda} \kappa_{AWW}$

} *CP Mixed States*

# Analysis Strategy



- We build 2 BDT's:
  - *BDT0*: Same as for spin
  - *BDTCP*: Trained with the SM signal vs the ALternative signal  
No backgrounds in the training
- *Inputs for the BDTCP :*
  - *CP-Even* (  $m_{\ell\ell}$ ,  $\Delta\phi_{\ell\ell}$ ,  $p_T^{\ell\ell}$ ,  $p_T^{\text{miss}}$  )
  - *CP-Odd* (  $m_{\ell\ell}$ ,  $\Delta\phi_{\ell\ell}$ ,  $E_{\ell\ell\nu\nu}$ ,  $\Delta p_T$  )

$$\Delta p_T = |p_T^{\ell_1} - p_T^{\ell_2}|$$

$$E_{\ell\ell\nu\nu} = p_T^{\ell_1} - 0.5p_T^{\ell_2} + 0.5p_T^{\text{miss}}$$

- *Training is performed only on the pure CP cases - no retraining on the mixed signal hypotheses*

.....

- The statistical treatment for the fixed hypothesis test is the same as for spin where now the POI  $\varepsilon$  corresponds to CP
- For the CP Mixing scans:
  - the likelihood definition is the same
  - the asymptotic approximation is used and the results are given as  $-2\Delta\text{LL}$  vs the scan parameter





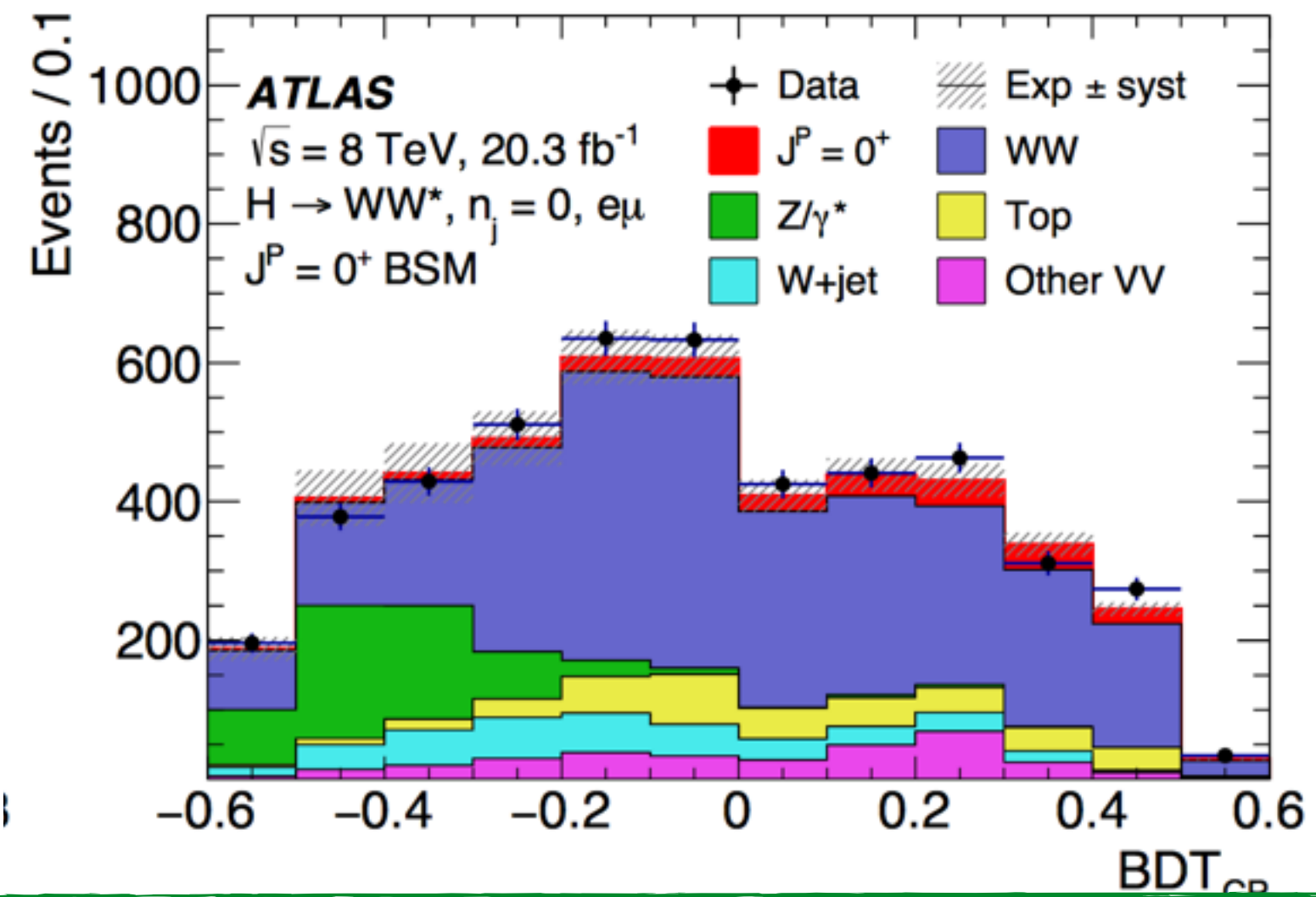
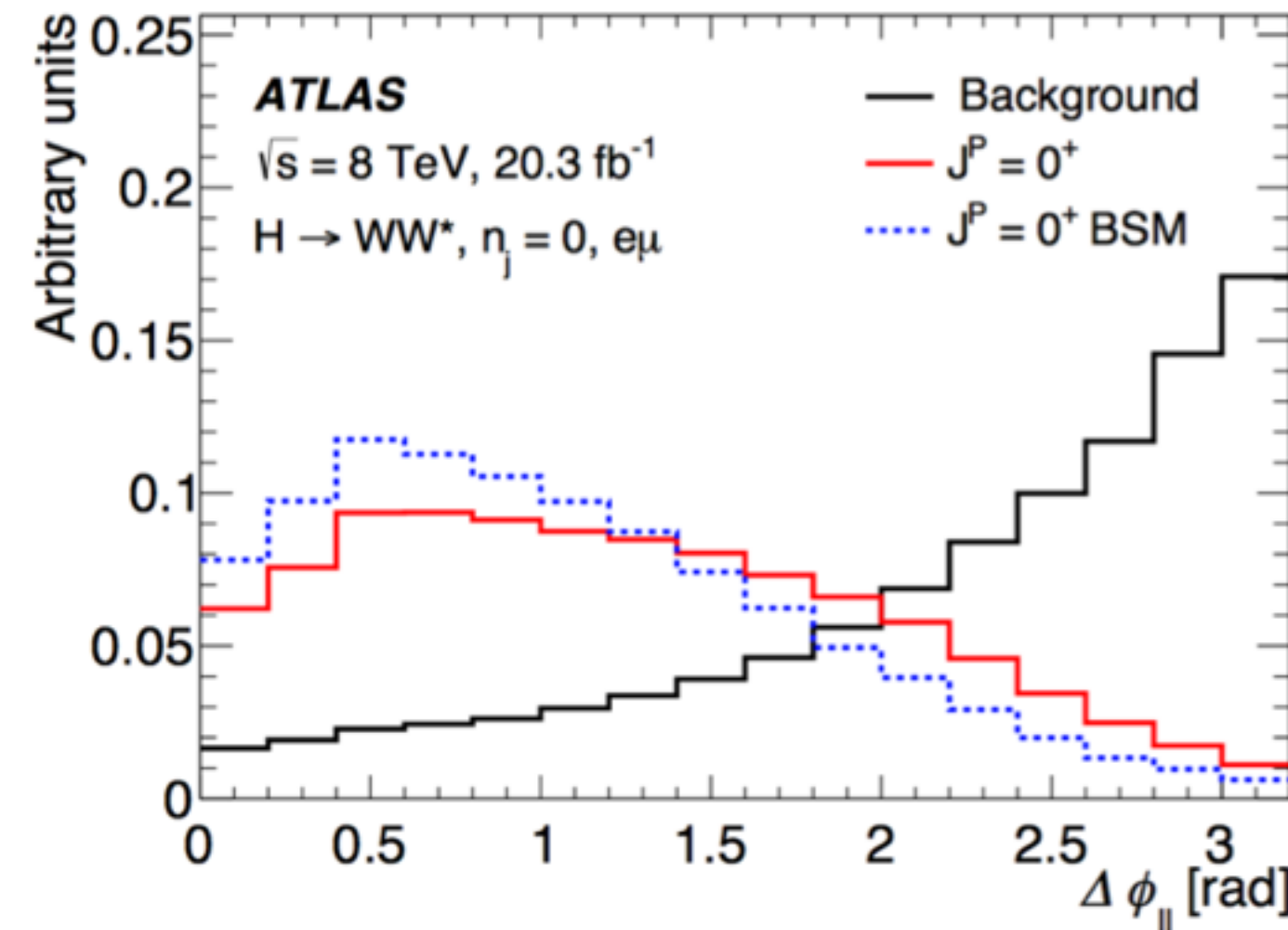
# Input Shapes & BDT Responses

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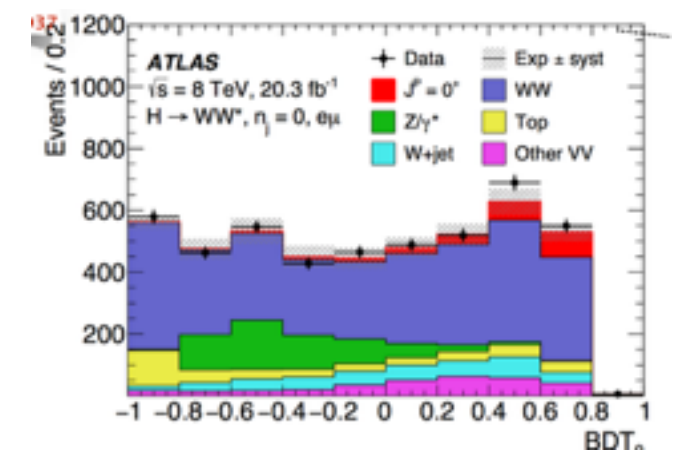


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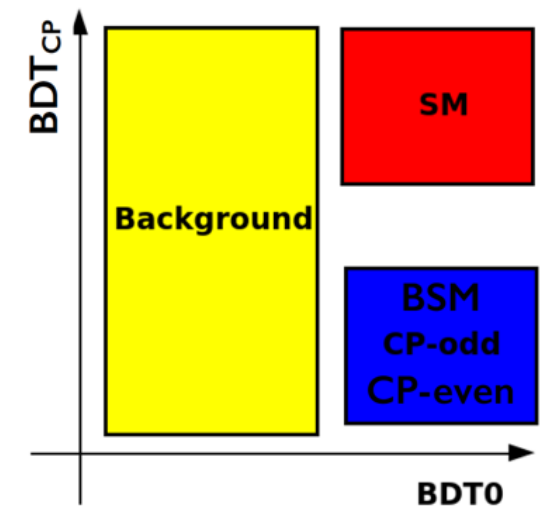
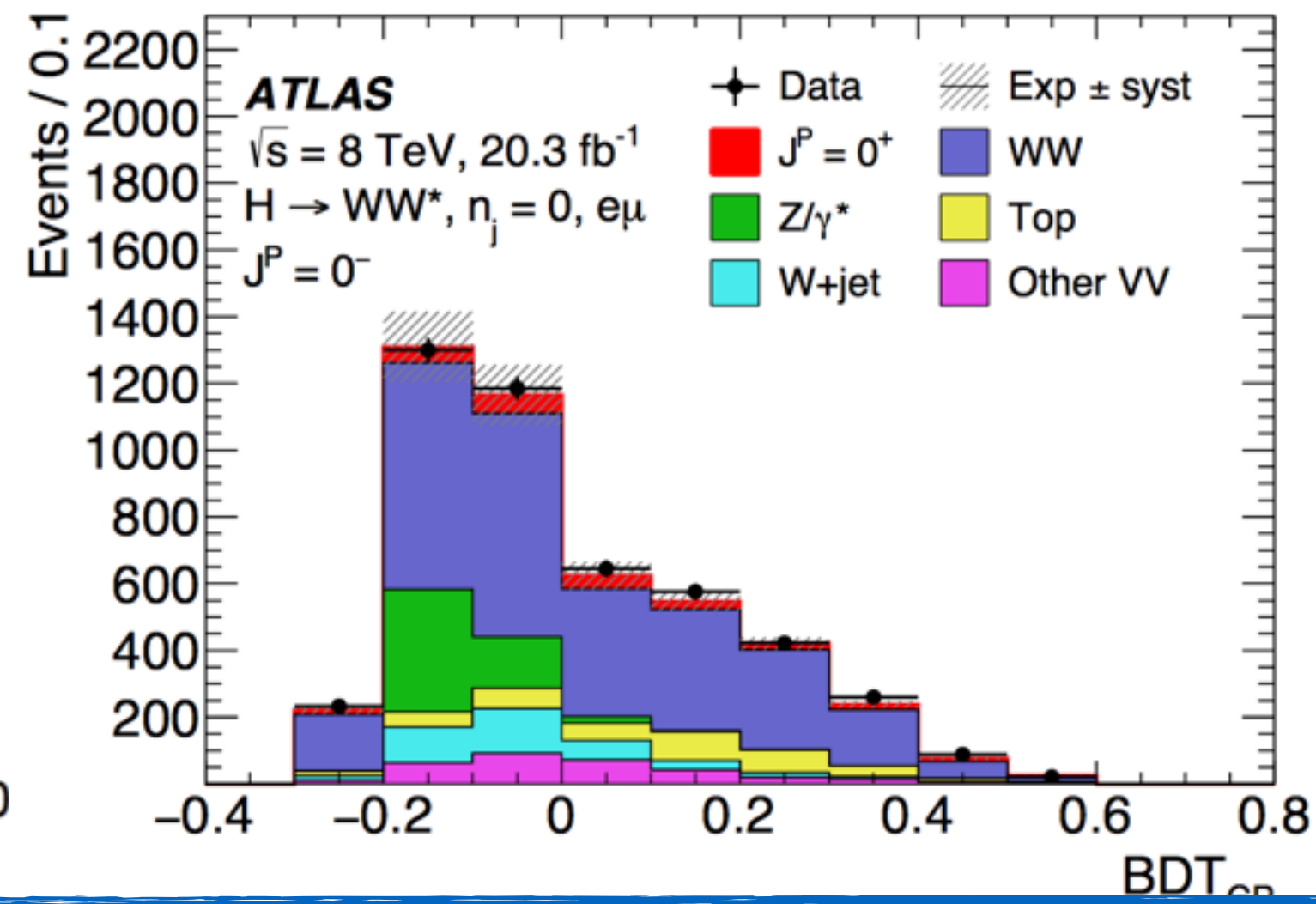
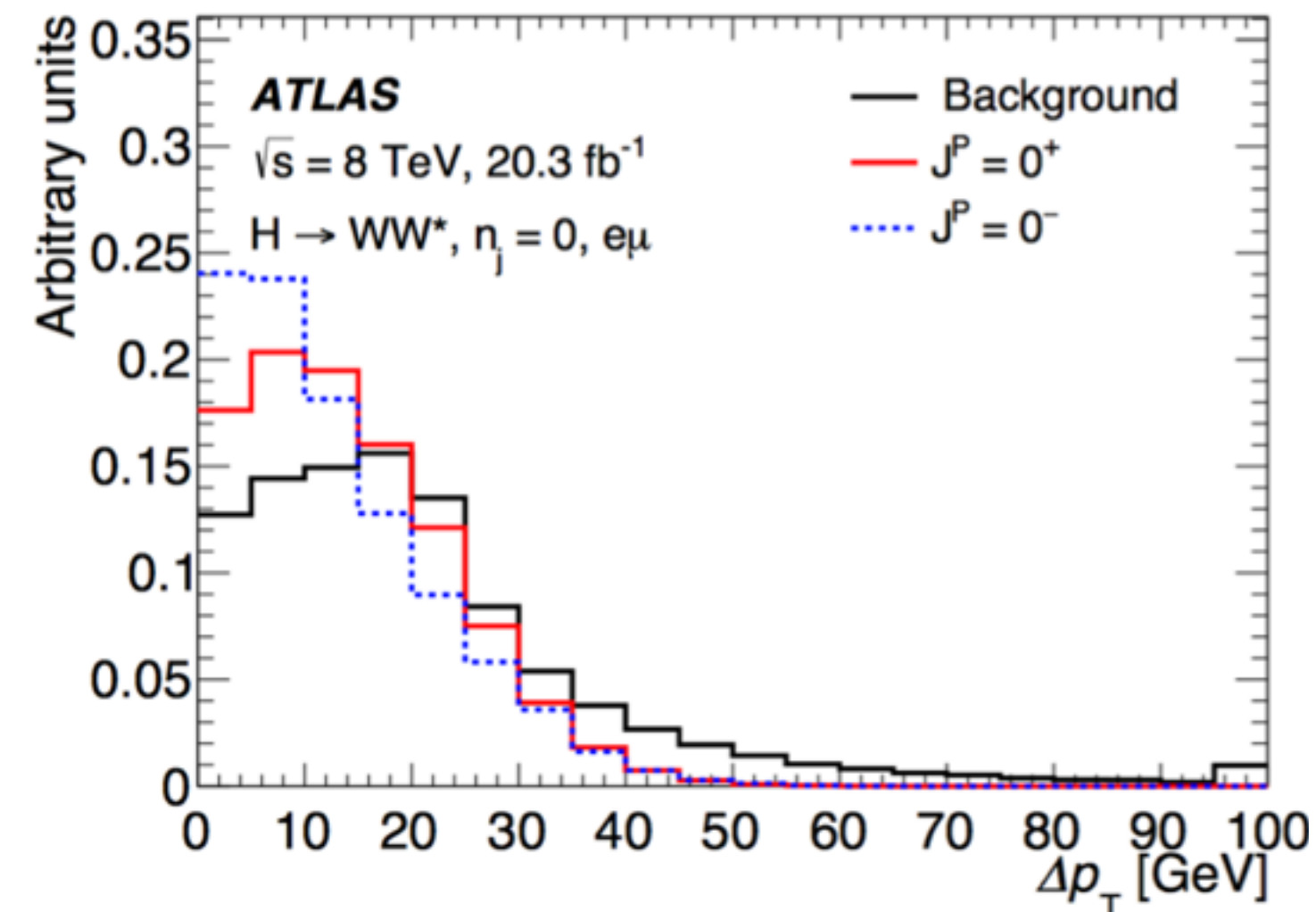
CP Even



for each  
 +



CP Odd

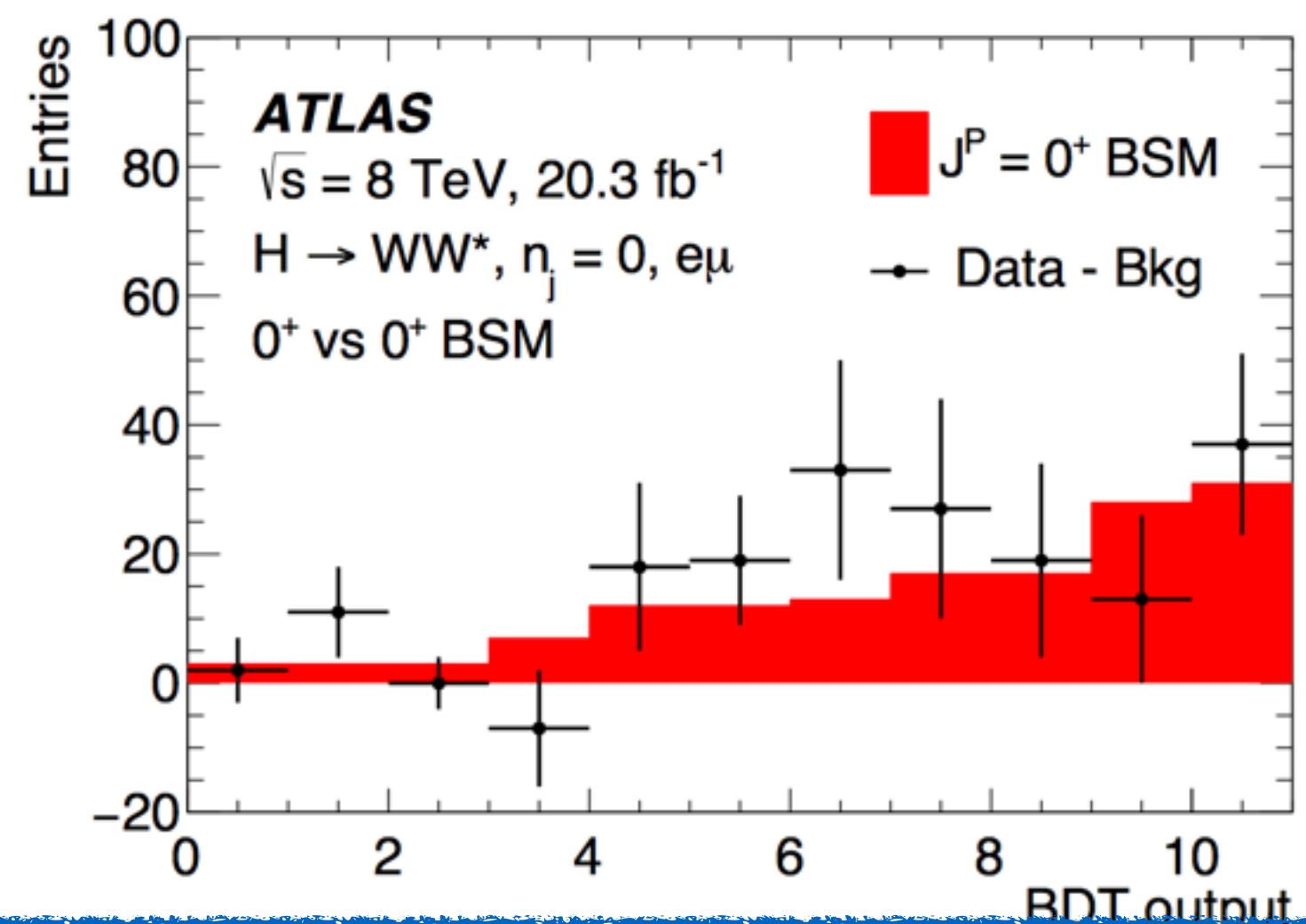
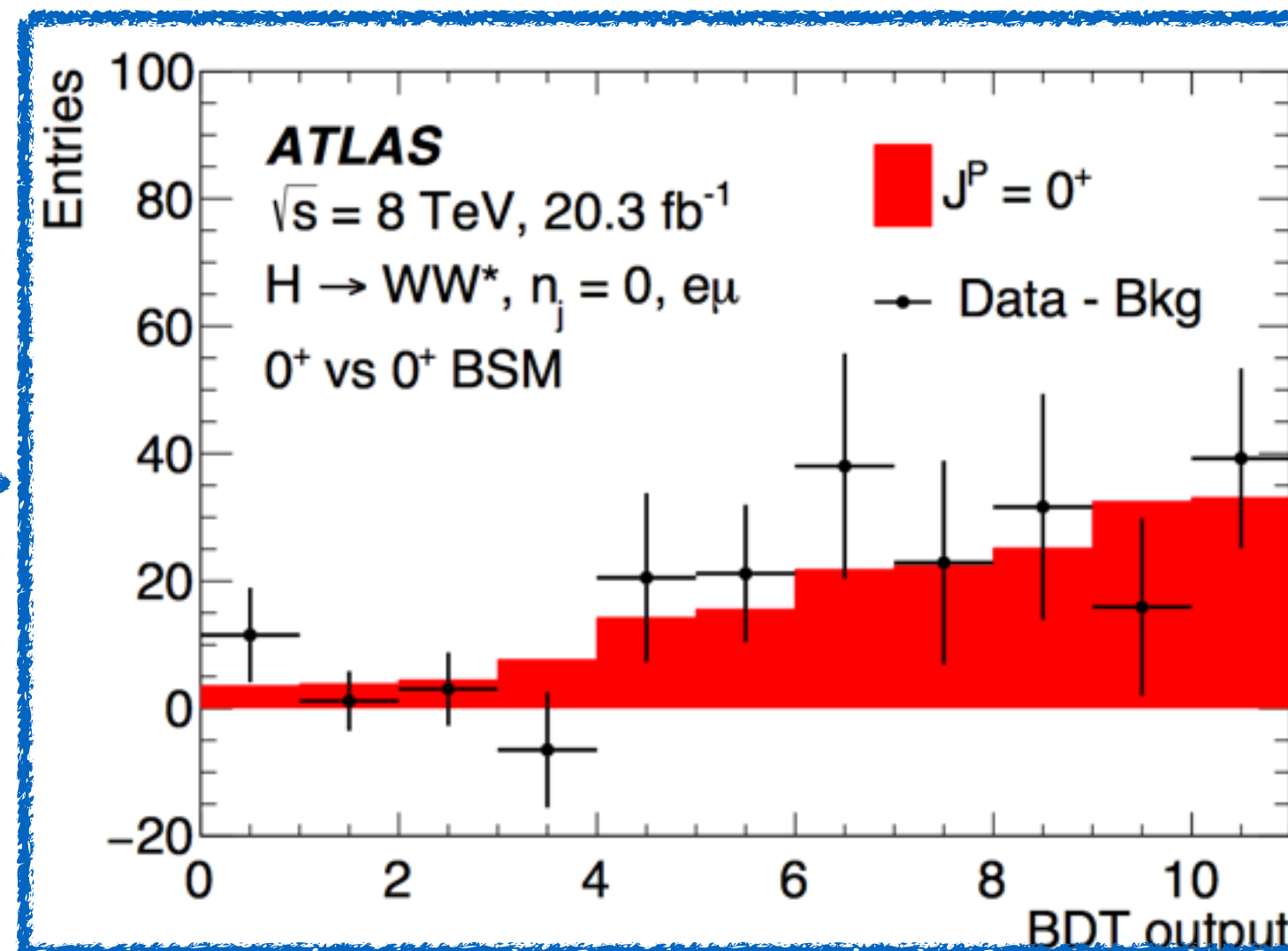
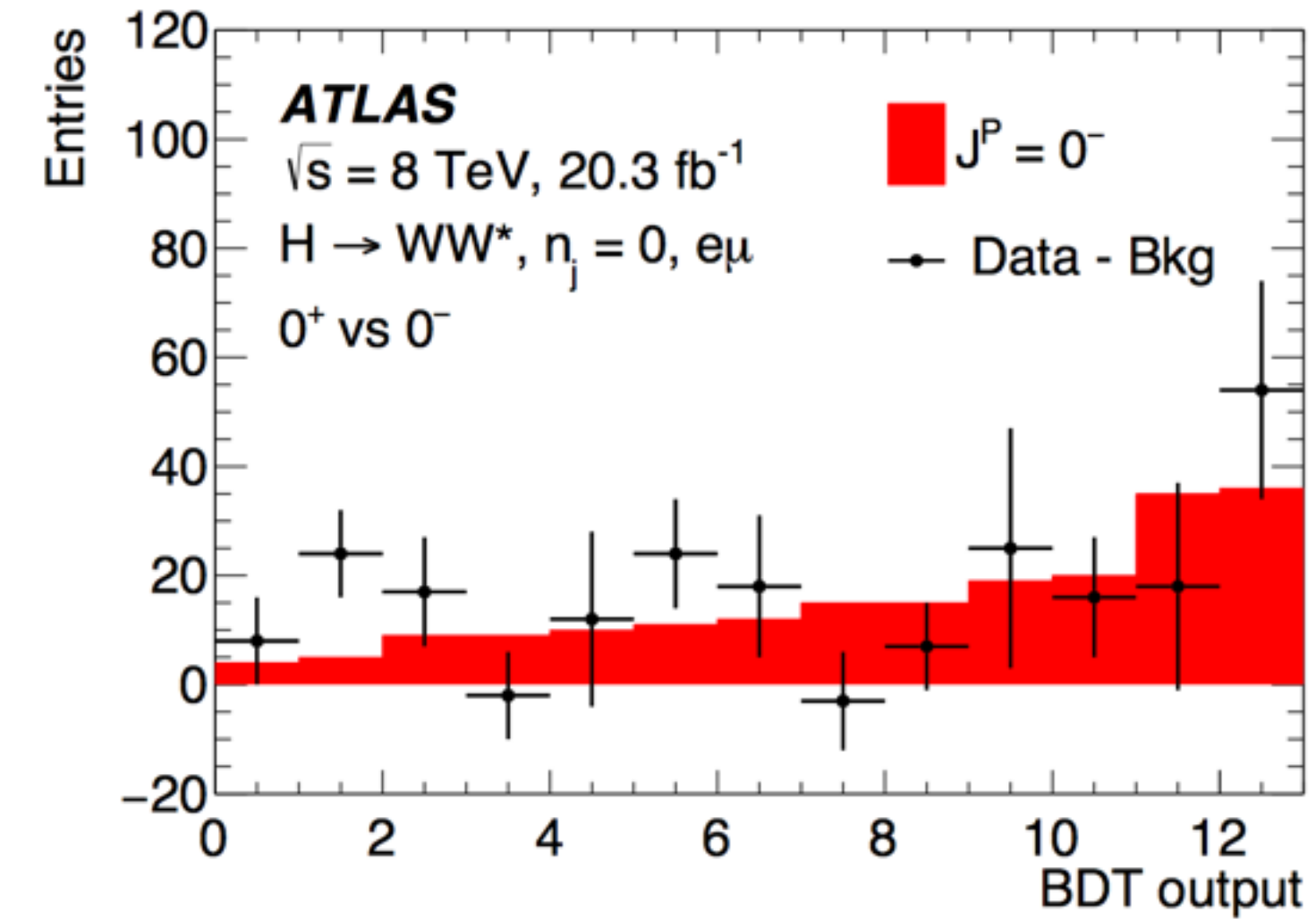
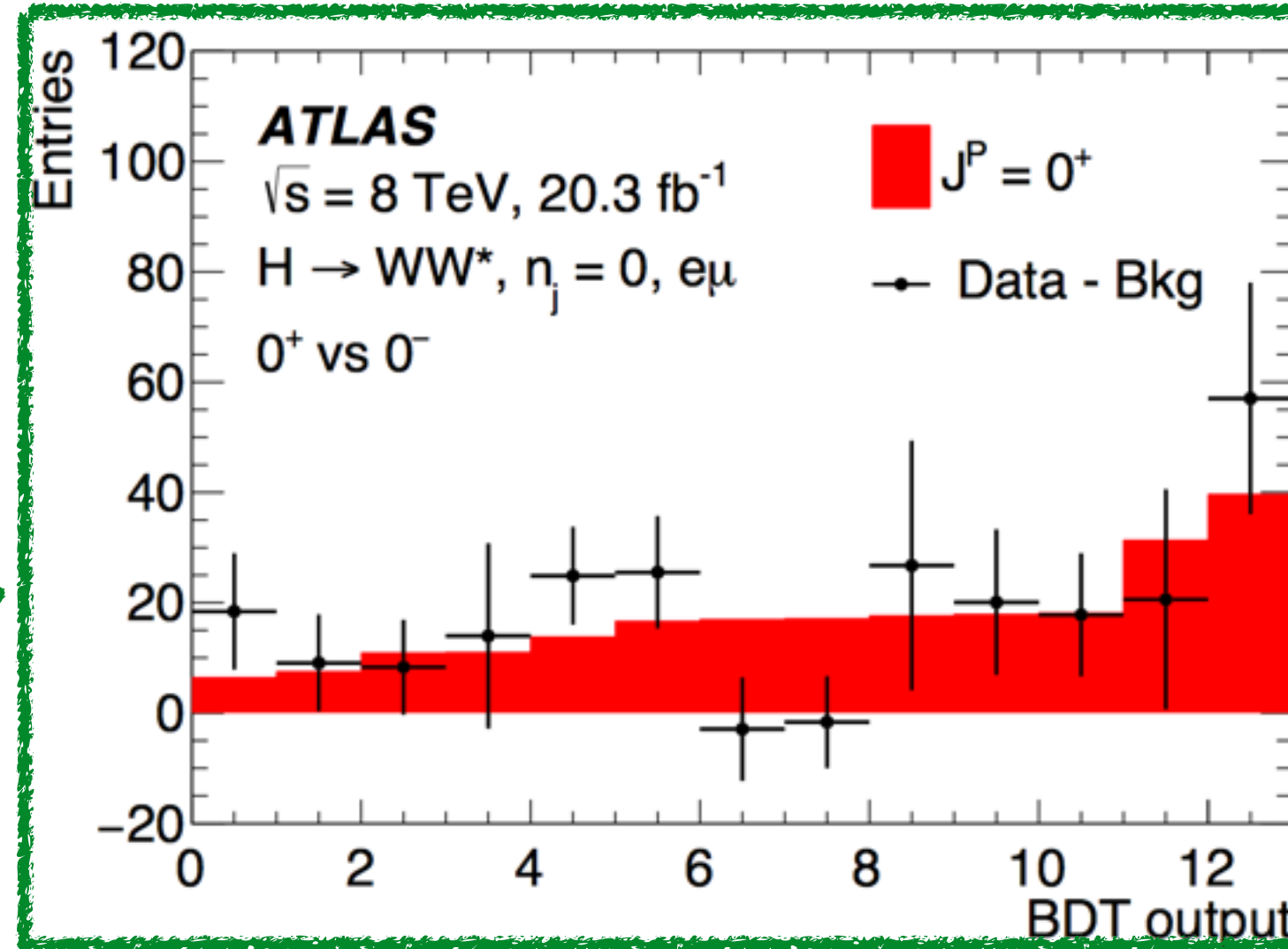




# CP: Fixed Results

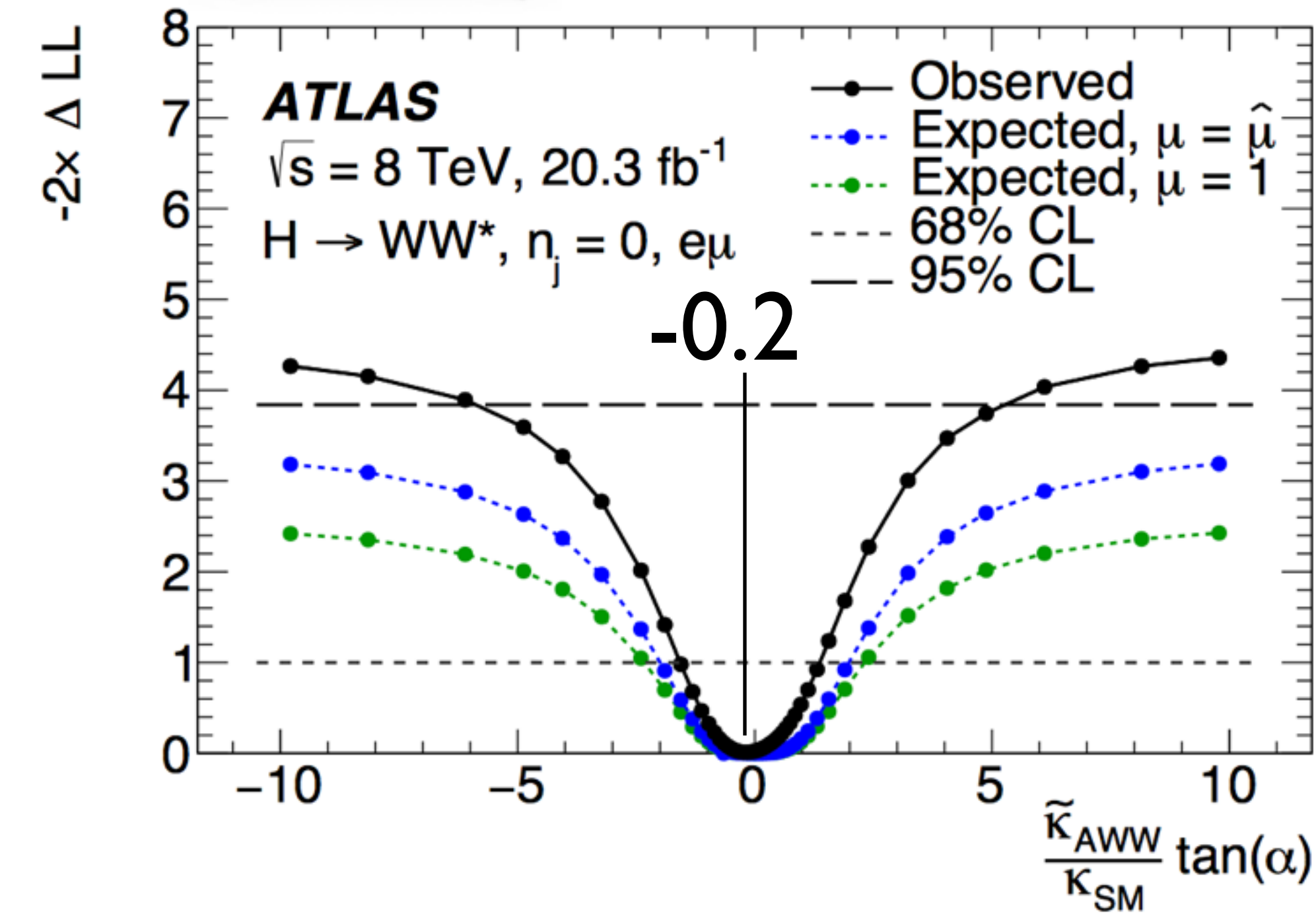
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Channel	$P_{\text{exp}, \mu=1}^{\text{SM}}$	$P_{\text{exp}, \mu=\hat{\mu}}^{\text{SM}}$	$P_{\text{exp}, \mu=\hat{\mu}}^{\text{ALT}}$	$P_{\text{obs}}^{\text{SM}}$	$P_{\text{obs}}^{\text{ALT}}$	$-CL_s$
BSM CP-odd						
0-jet	0.078	0.062	0.032	0.652	0.012	96.5%
BSM CP-even						
0-jet	0.271	0.310	0.287	0.907	0.027	70.8%



# CP-Mixing Scan Results

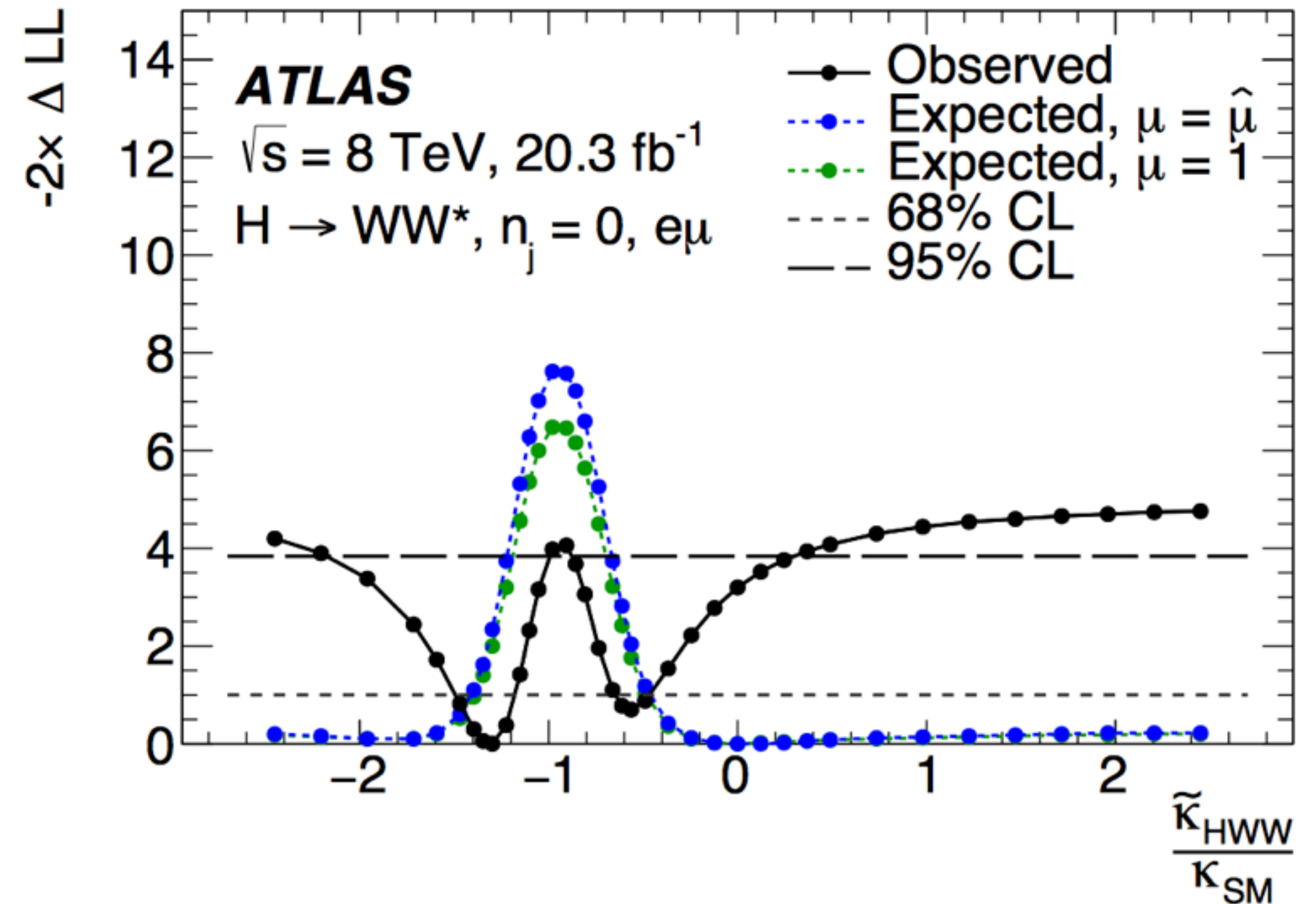
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**95% CL**  $\frac{\tilde{\kappa}_{AWW}}{\kappa_{SM}} \tan \alpha < -6.0$  and  $\frac{\tilde{\kappa}_{AWW}}{\kappa_{SM}} \tan \alpha > 5.0$

**68% CL**  $\frac{\tilde{\kappa}_{AWW}}{\kappa_{SM}} \tan \alpha < -1.6$  and  $\frac{\tilde{\kappa}_{AWW}}{\kappa_{SM}} \tan \alpha > 1.3$

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$\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} < -2.2$  ,  $\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} > 0.4$  and  $\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} \in [-0.85, -1]$

$\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} < -1.5$  ,  $\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} > -0.5$  and  $\frac{\tilde{\kappa}_{HWW}}{\kappa_{SM}} \in [-1.20, -0.65]$



# Summary

- The SM Hypothesis for the Higgs boson have been tested against the alternative spin-2 hypothesis, and different CP states.
- For the spin-2 benchmarks the alternative model is :
  - disfavoured at **84.5%** CLs for the universal couplings
  - excluded up to **99.4%** CL for the non-universal couplings case.
- For the CP study
  - For fixed hypotheses:  
CP-Even alternative hypothesis is disfavoured at **70.8%** && the CP-Odd is excluded at **96.5%** CLs.
  - For the CP-mixing case:  
CP-Even : compatible with SM within **1.9 $\sigma$**   
  
CP-Odd : compatible with SM within **0.5 $\sigma$**

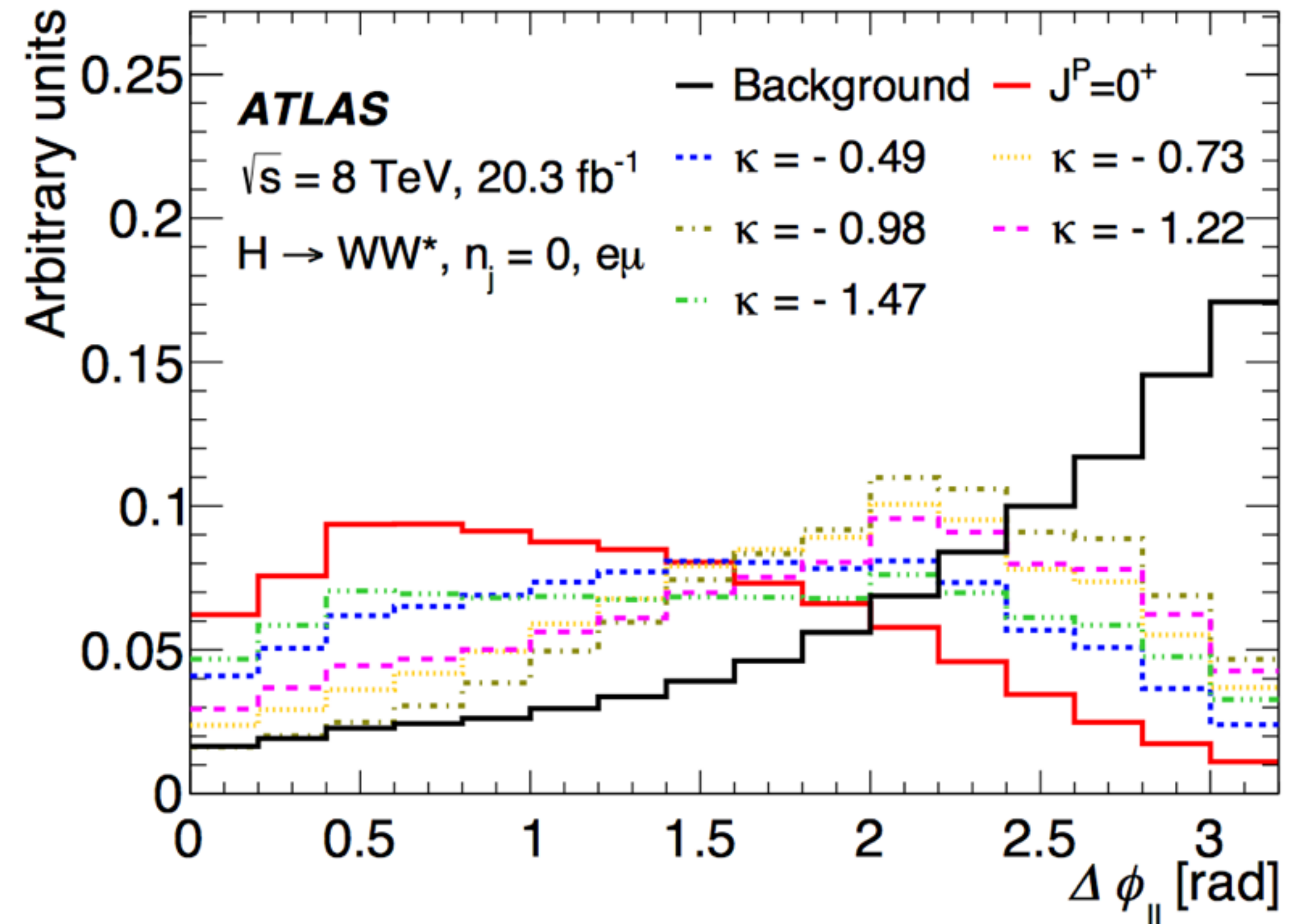
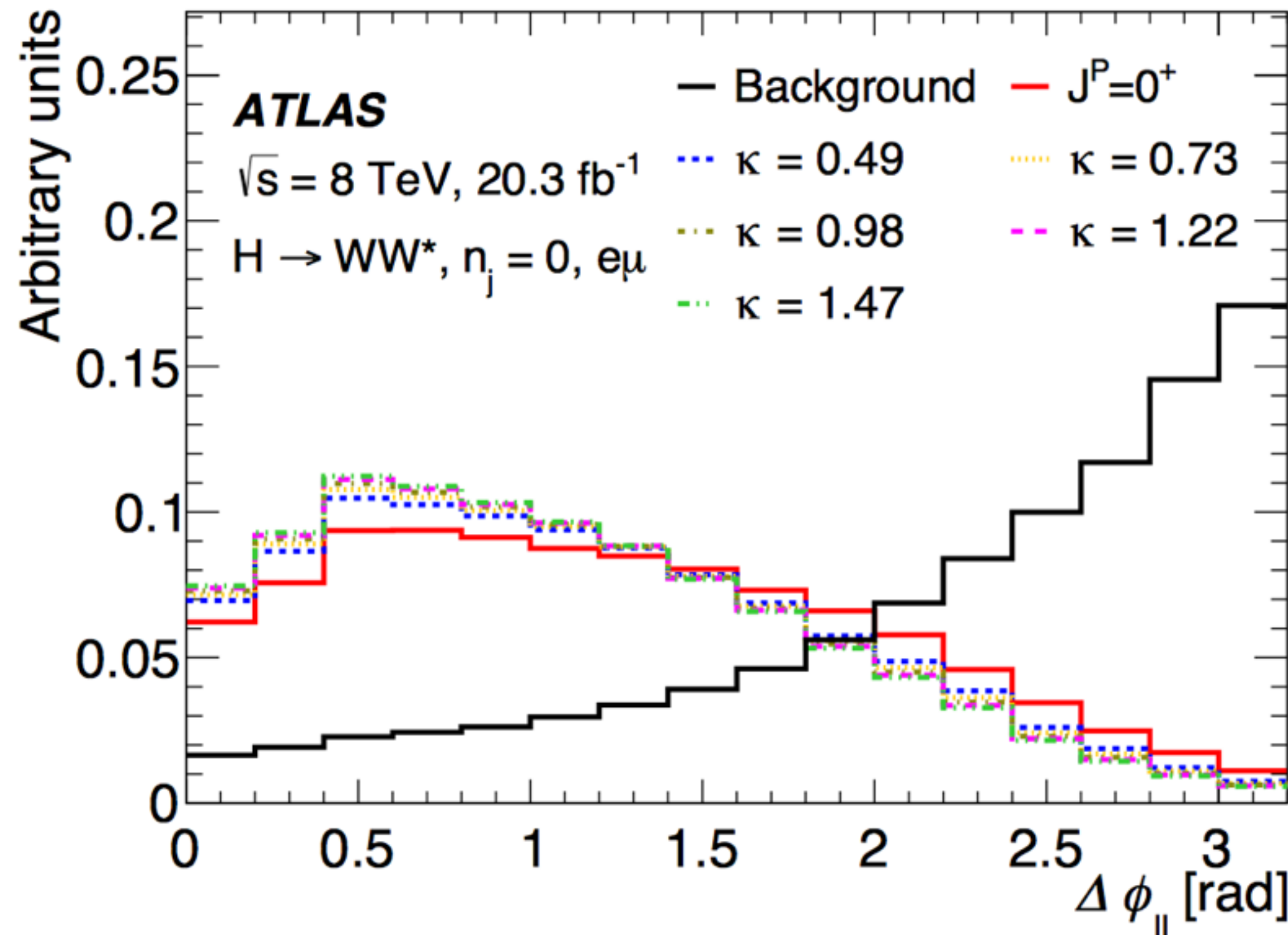




# Backup

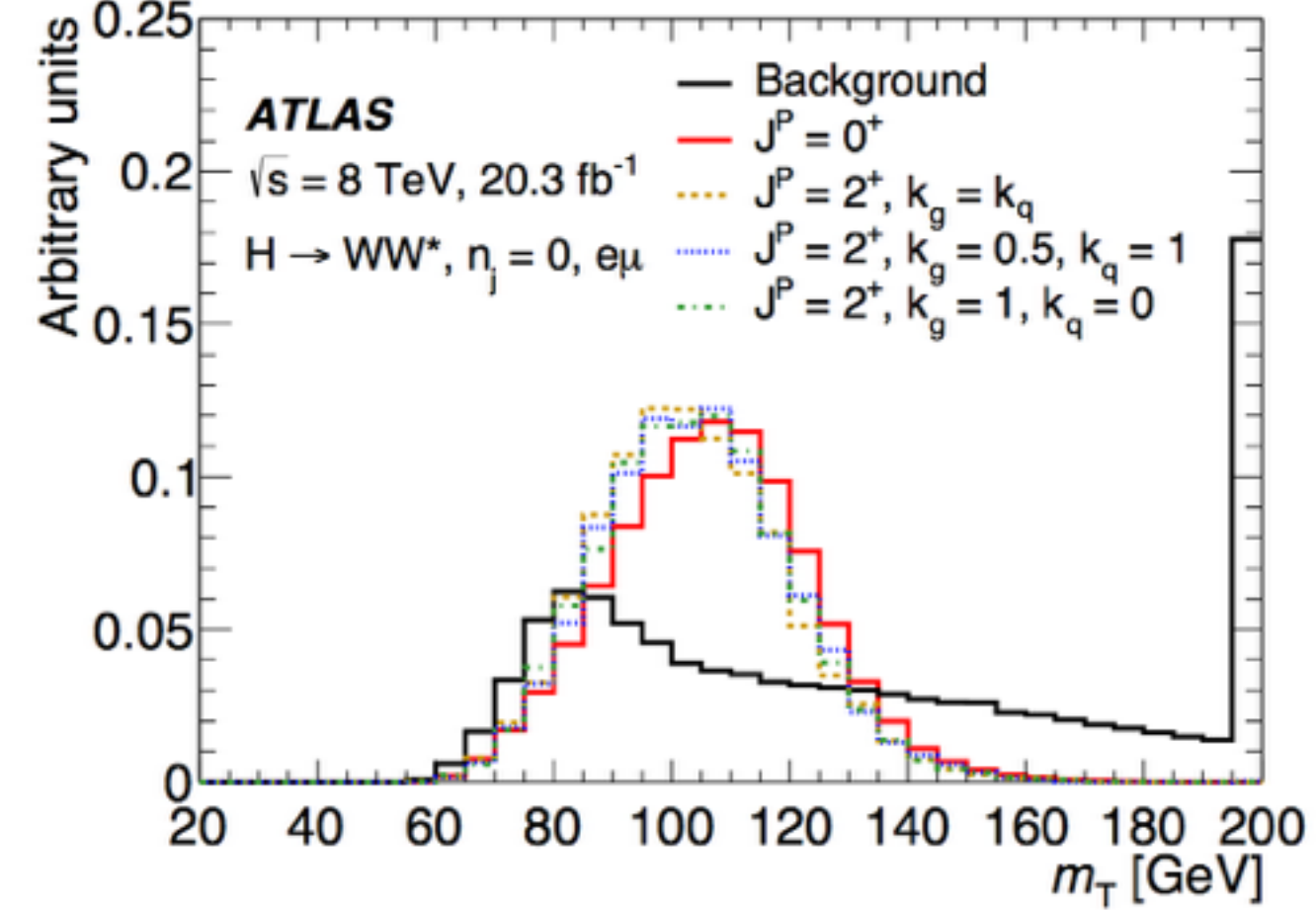
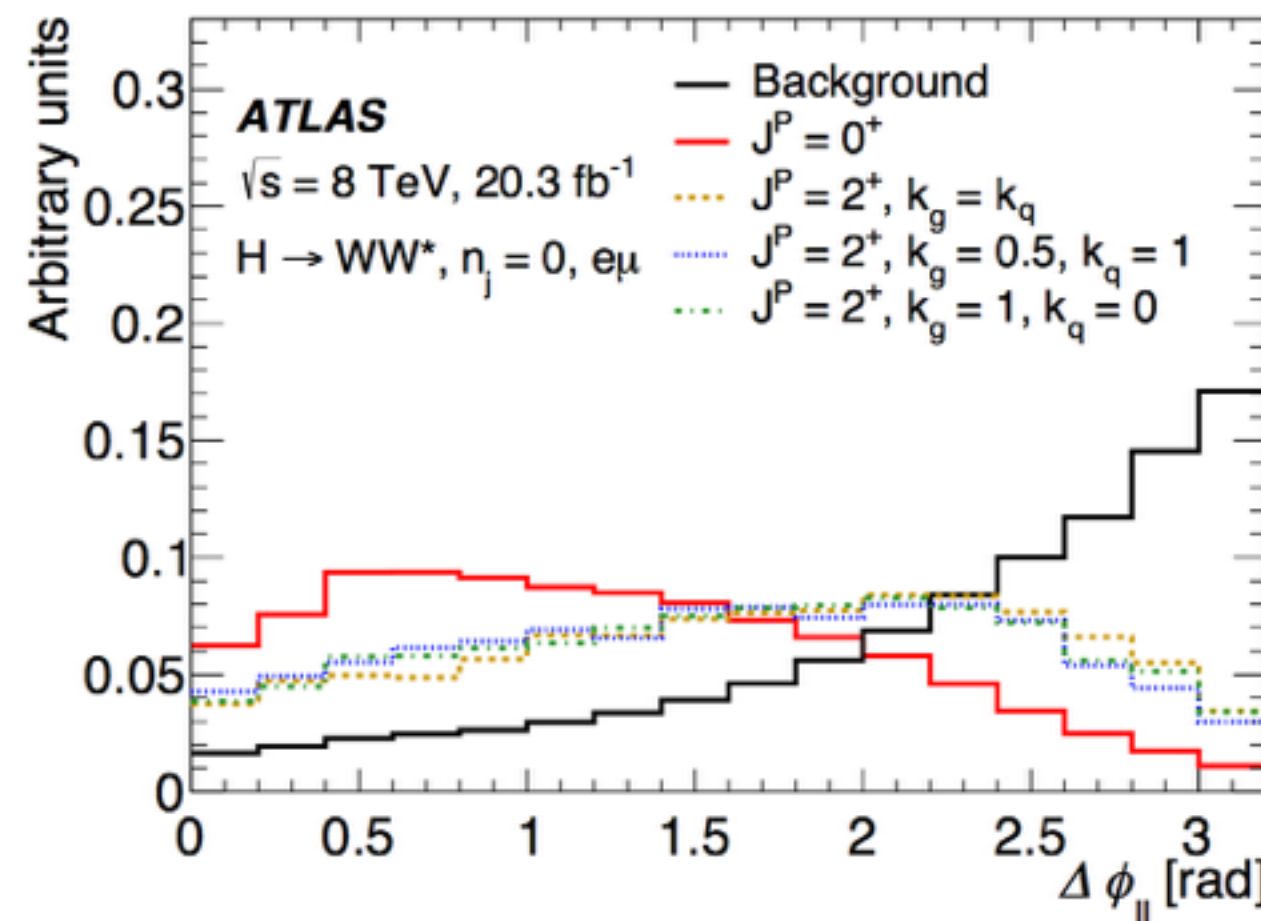
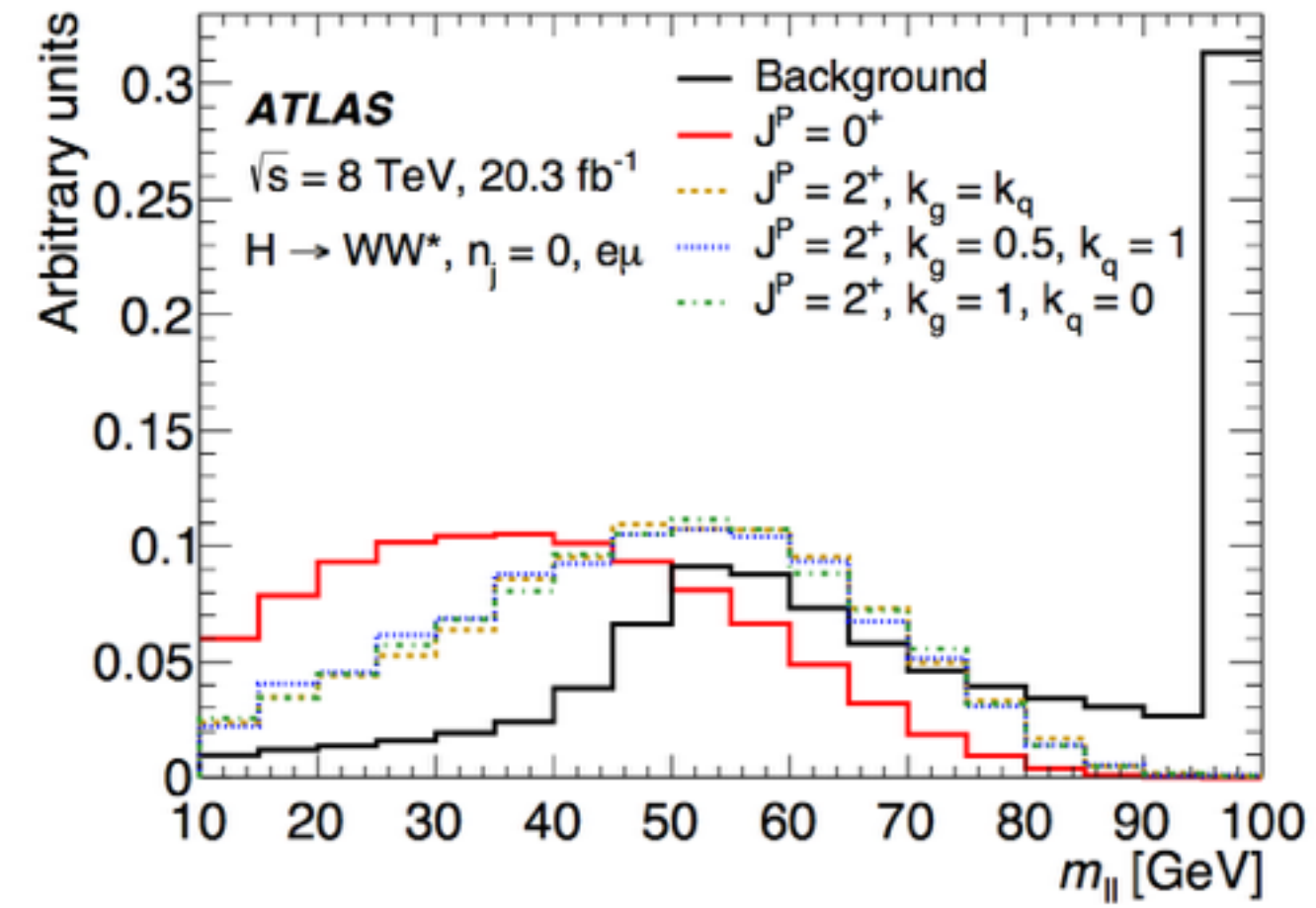
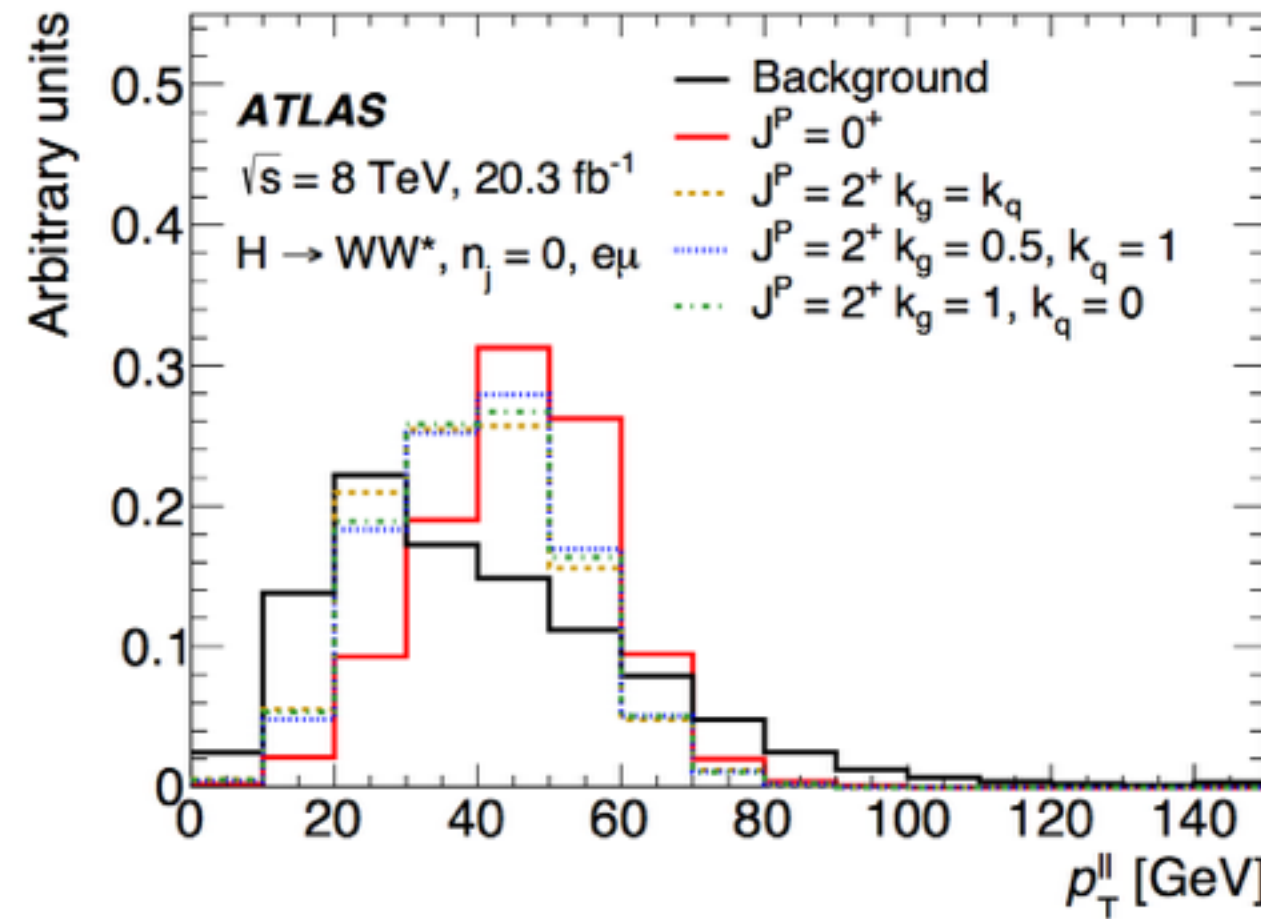
# kHWW Interference

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- In negative  $\kappa$  values a negative interference appears which cancels out the amplitudes of SM/BSM -> Huge discrimination as shape but normalization (x-sect) falls dramatically.

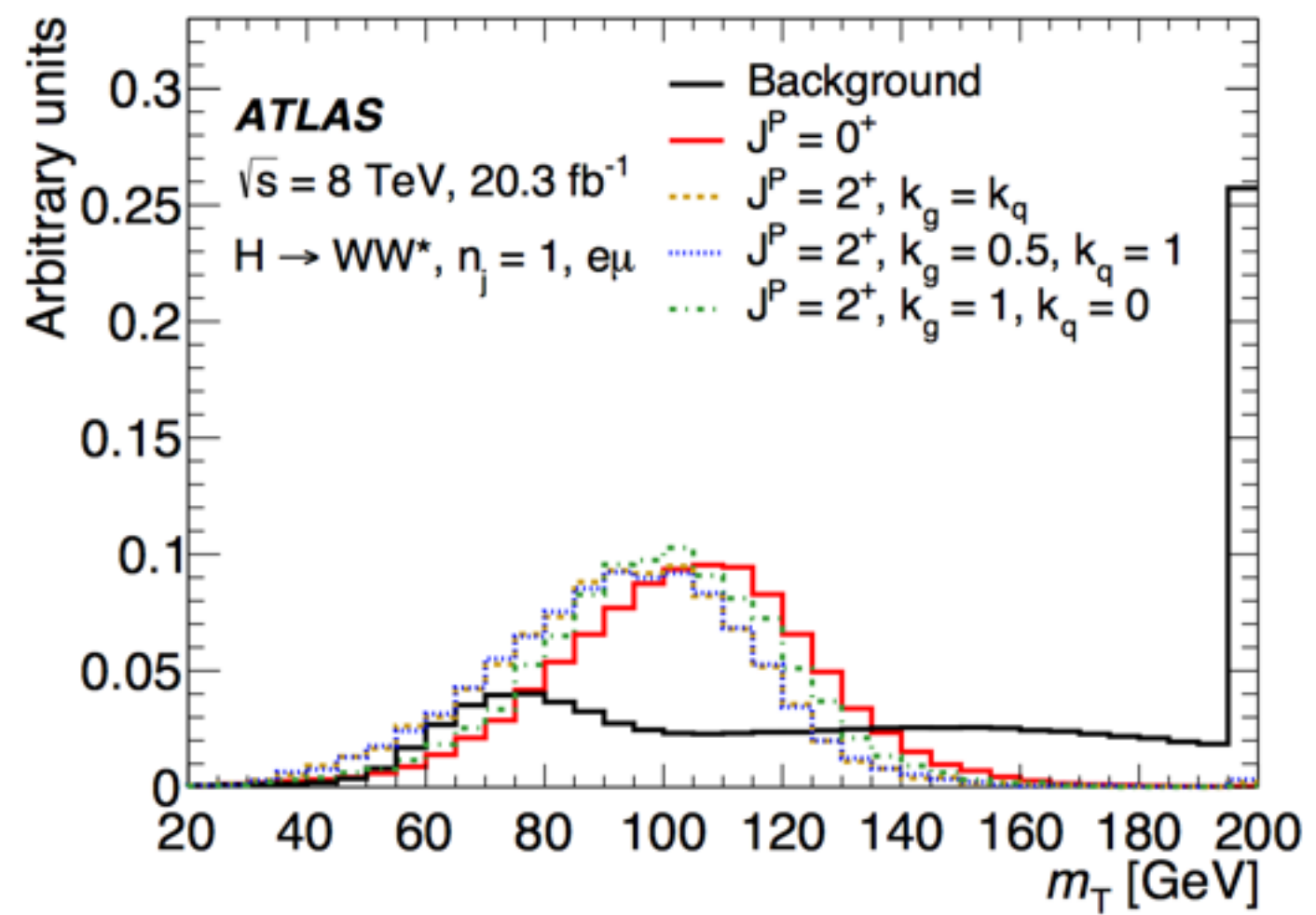
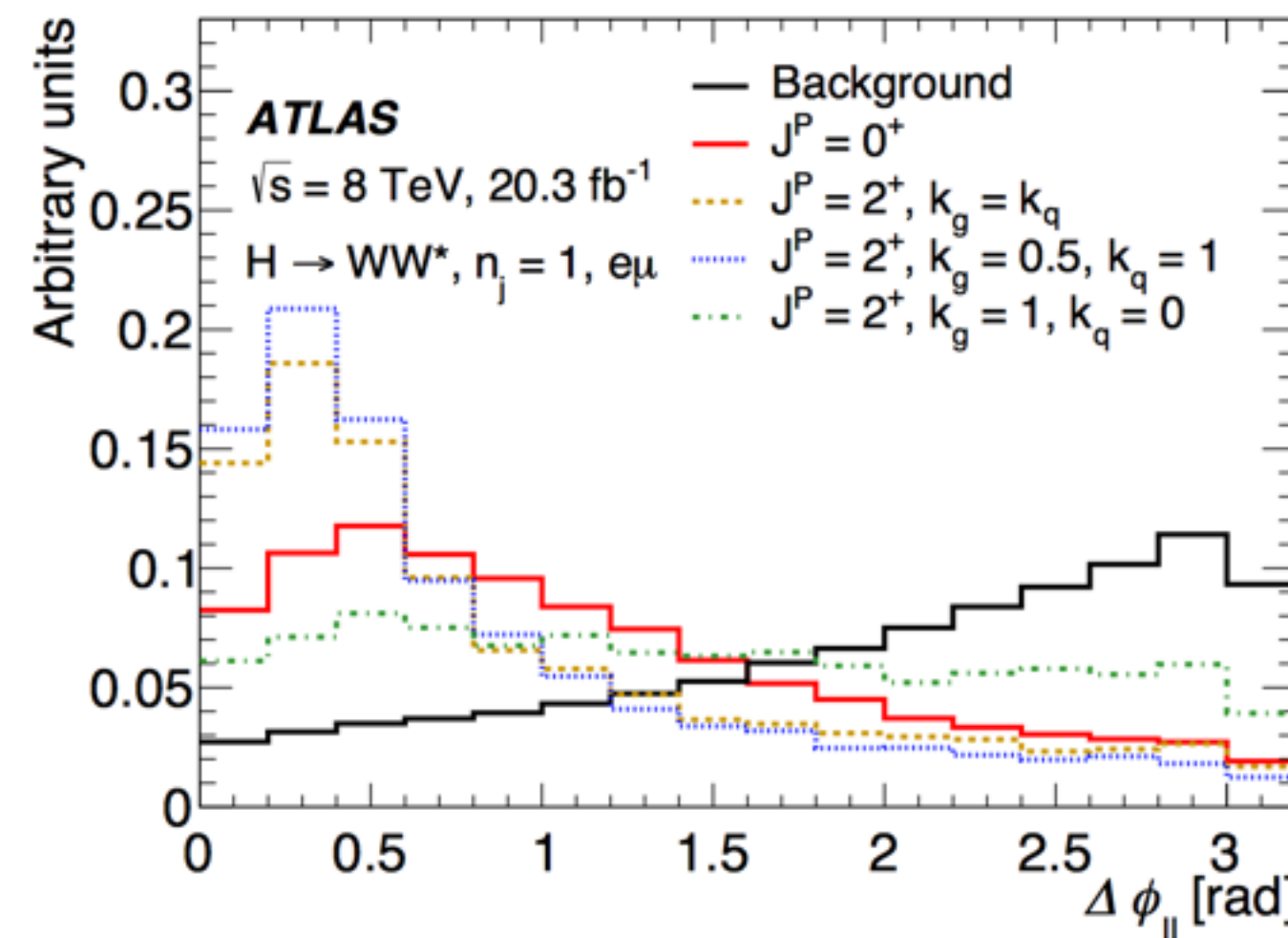
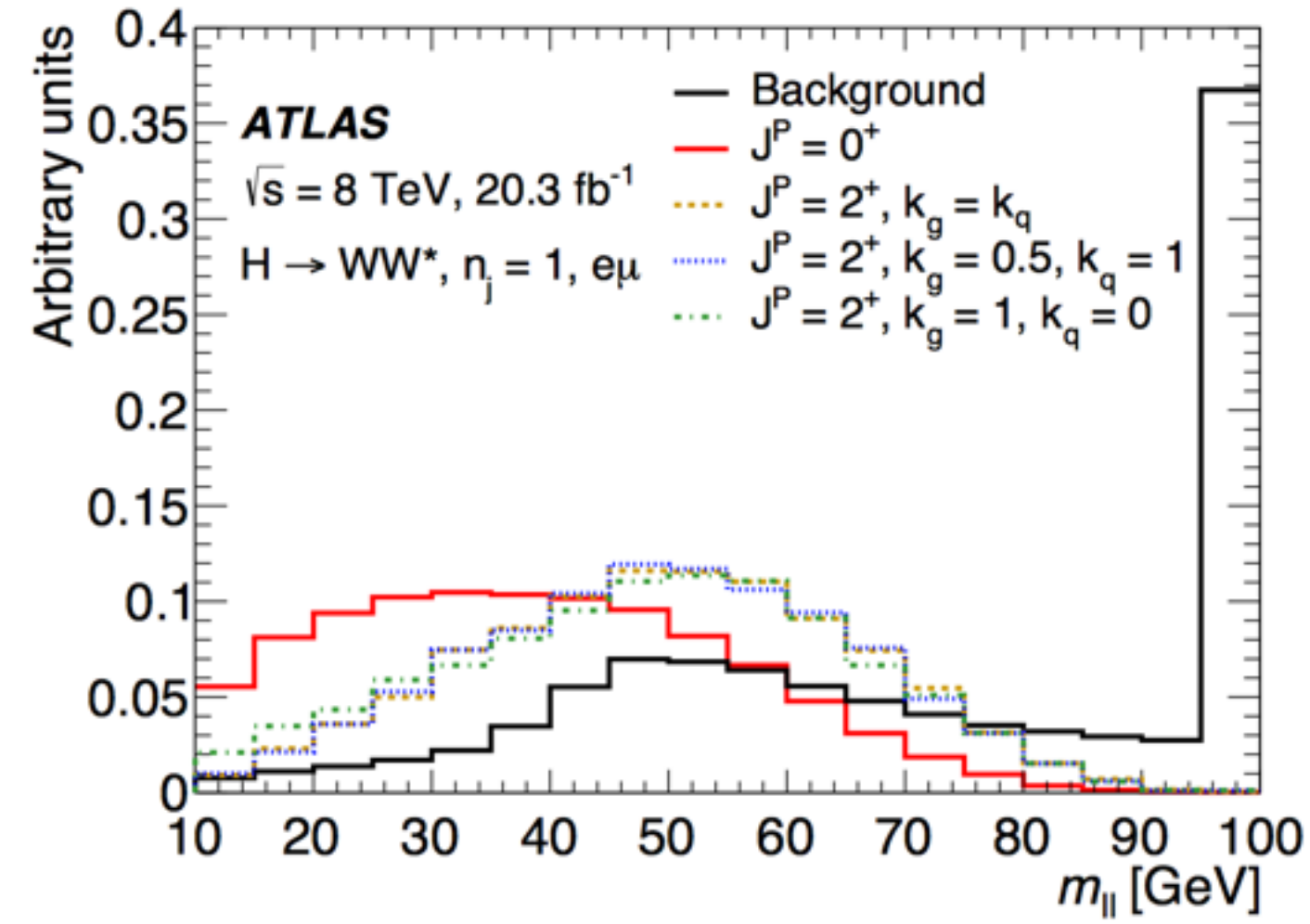
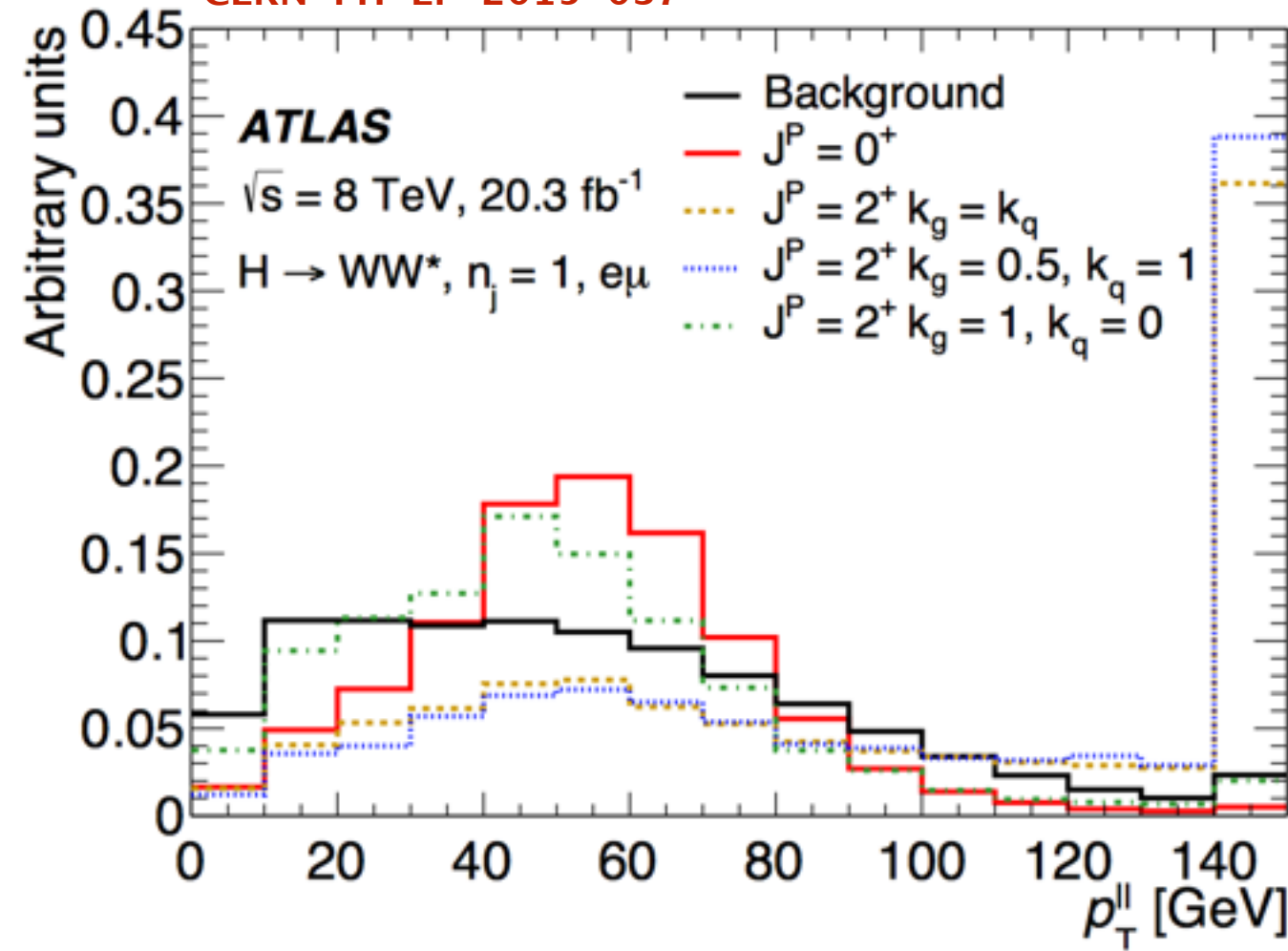
# Spin.Input Shapes.0j





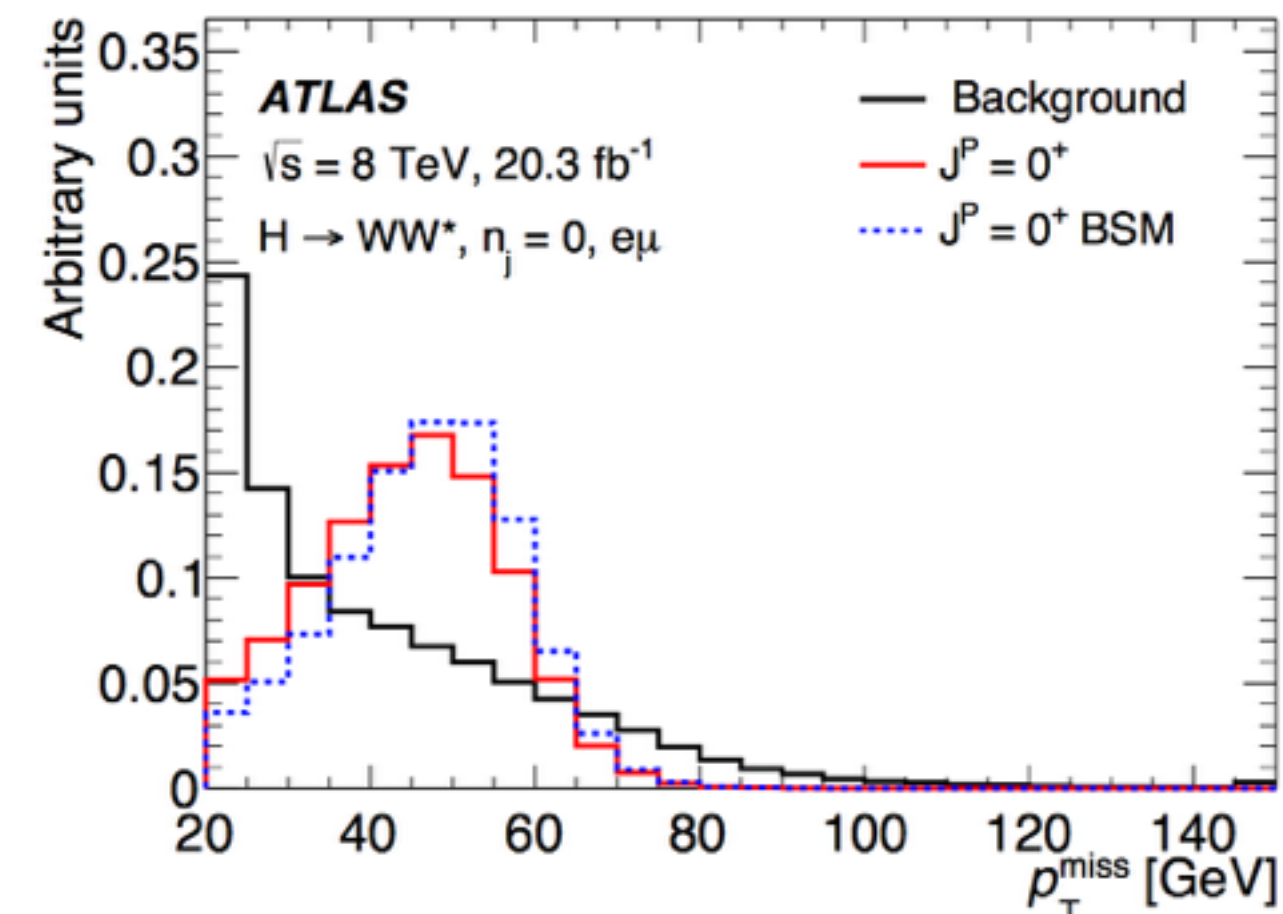
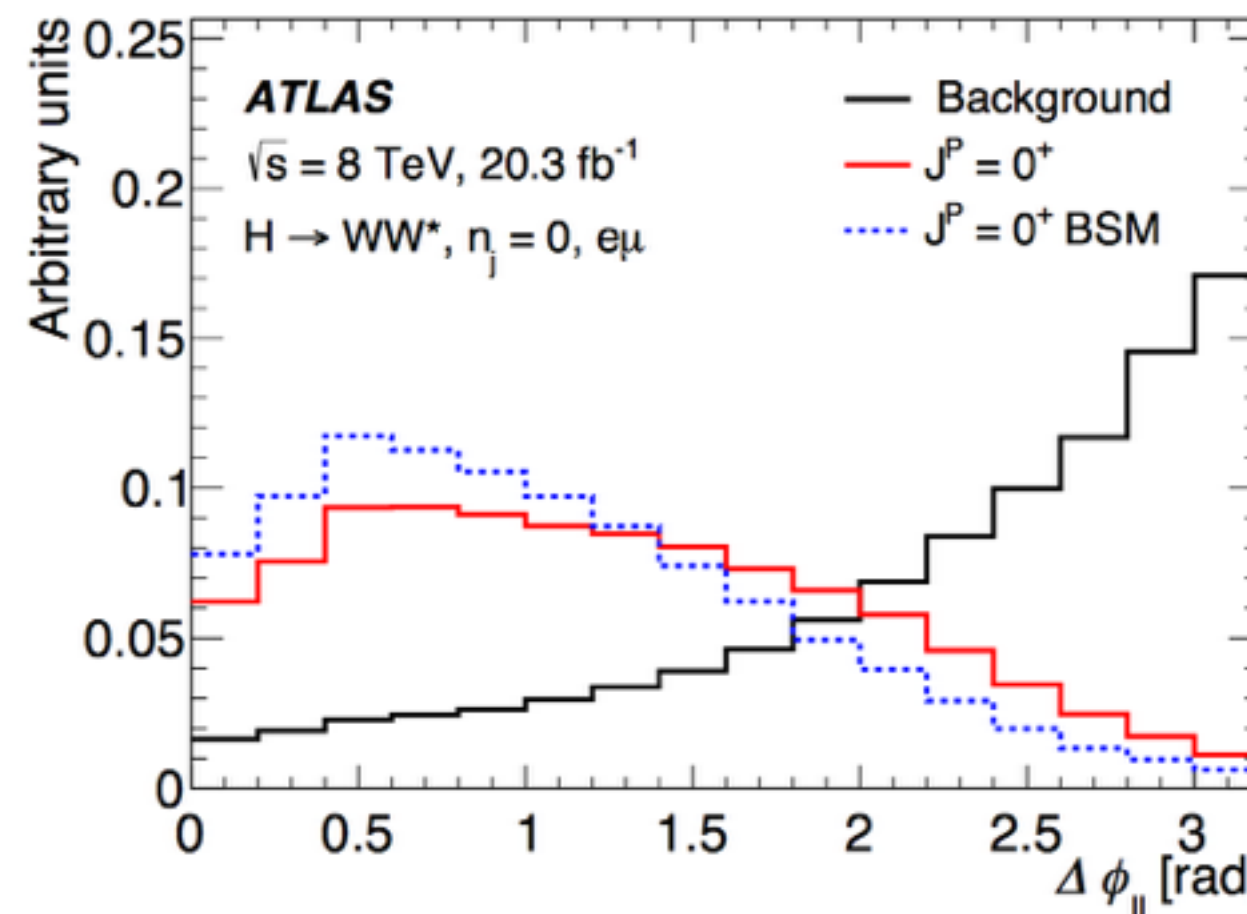
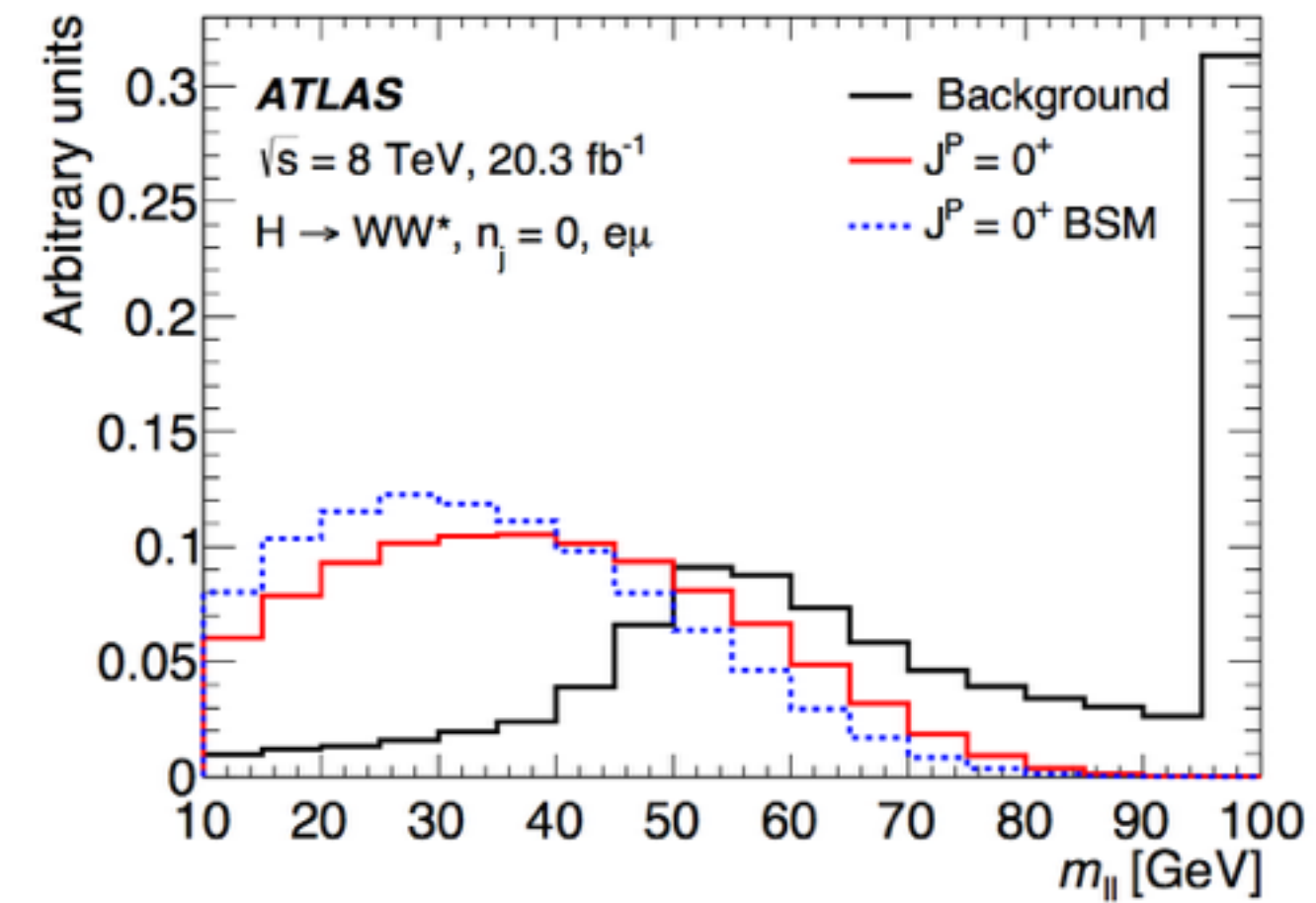
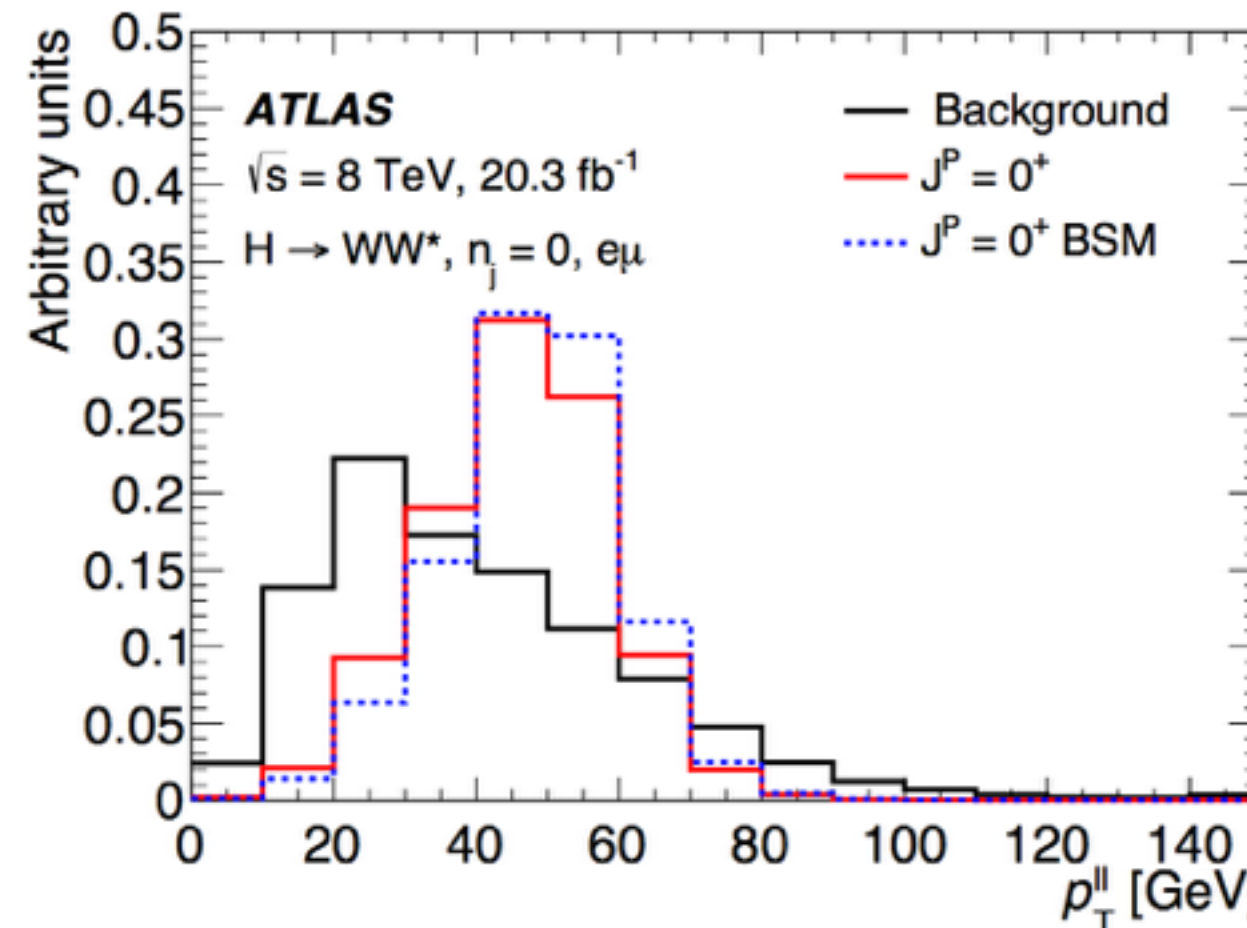
# I-jet Input Shapes

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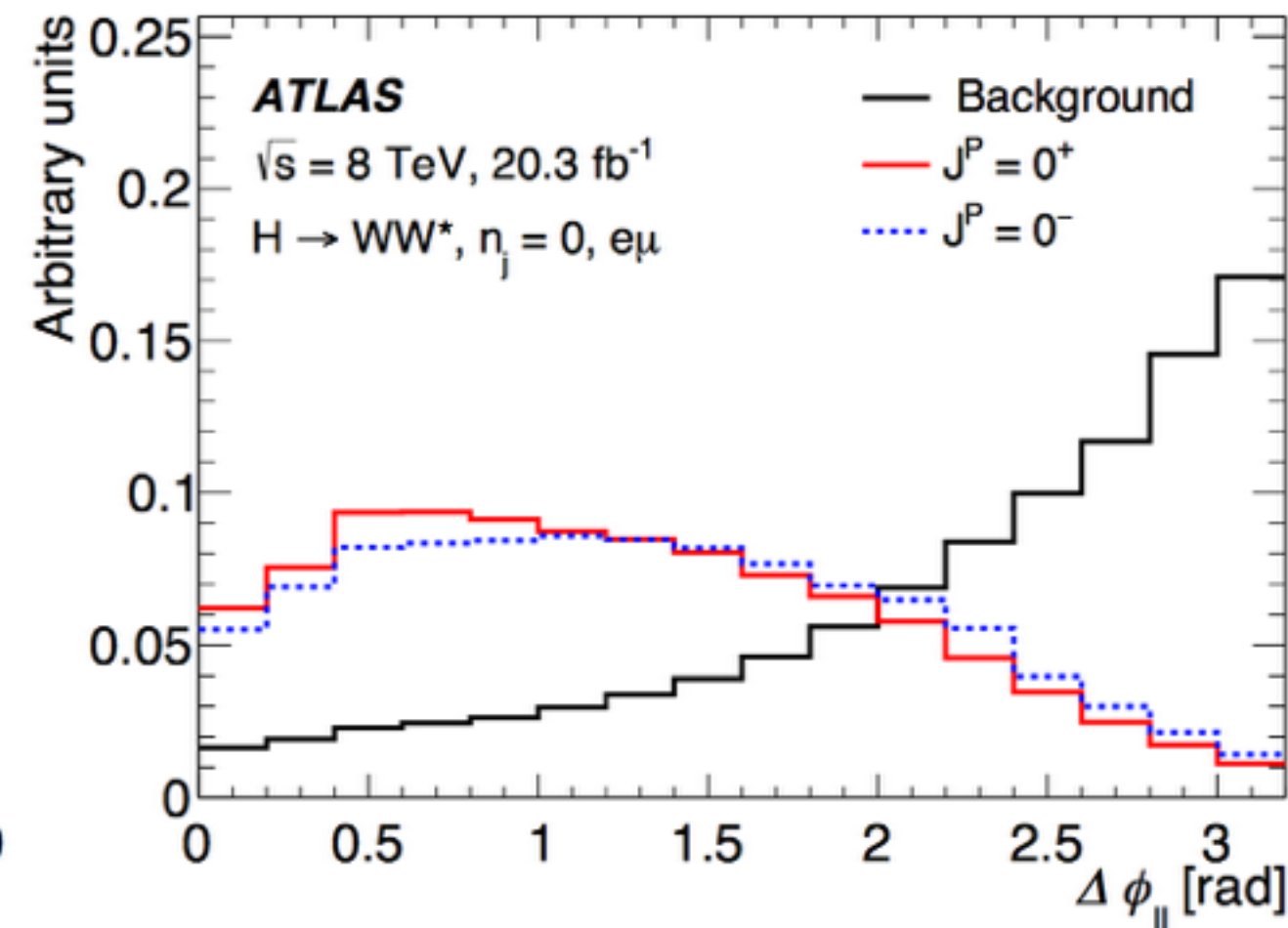
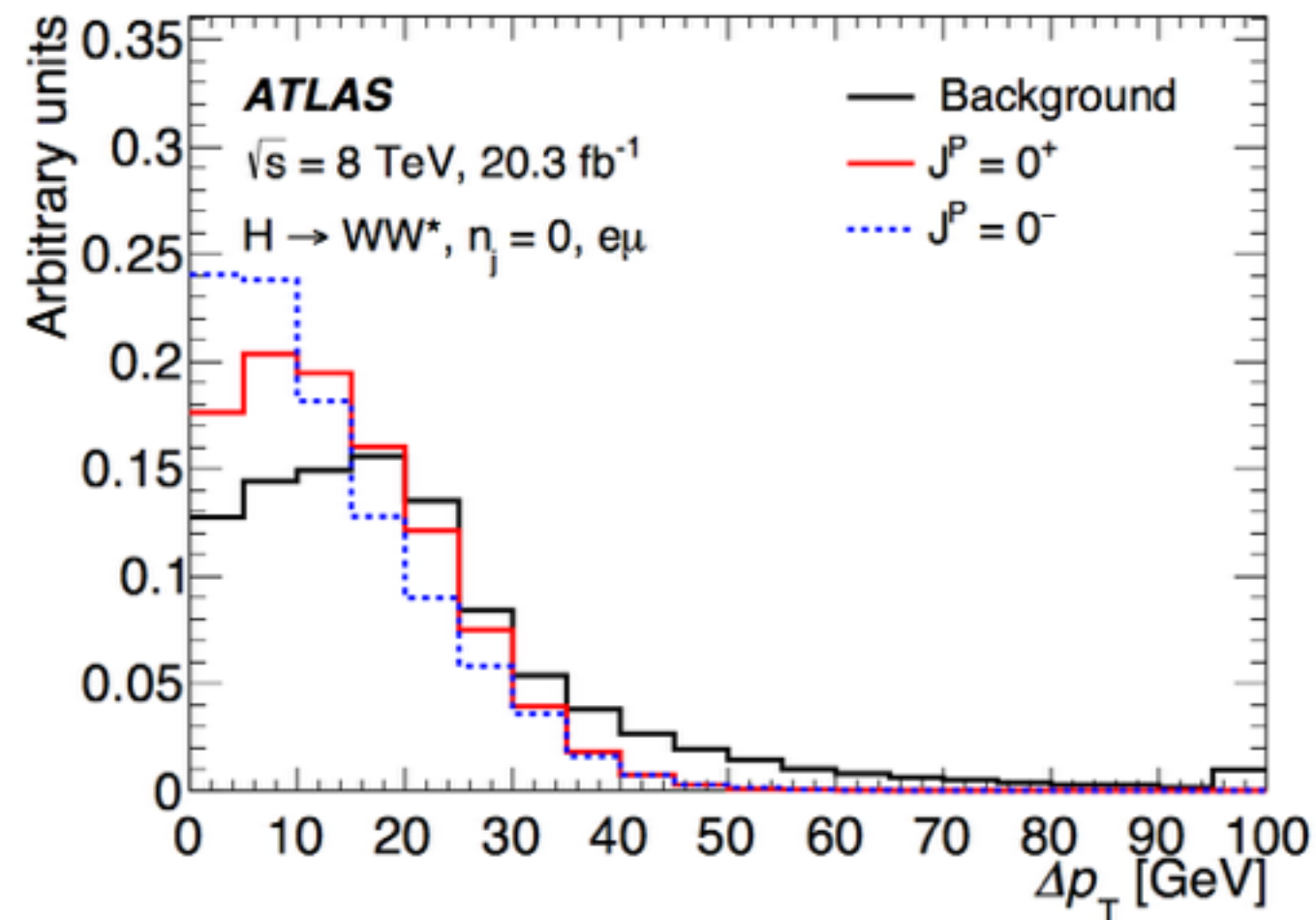
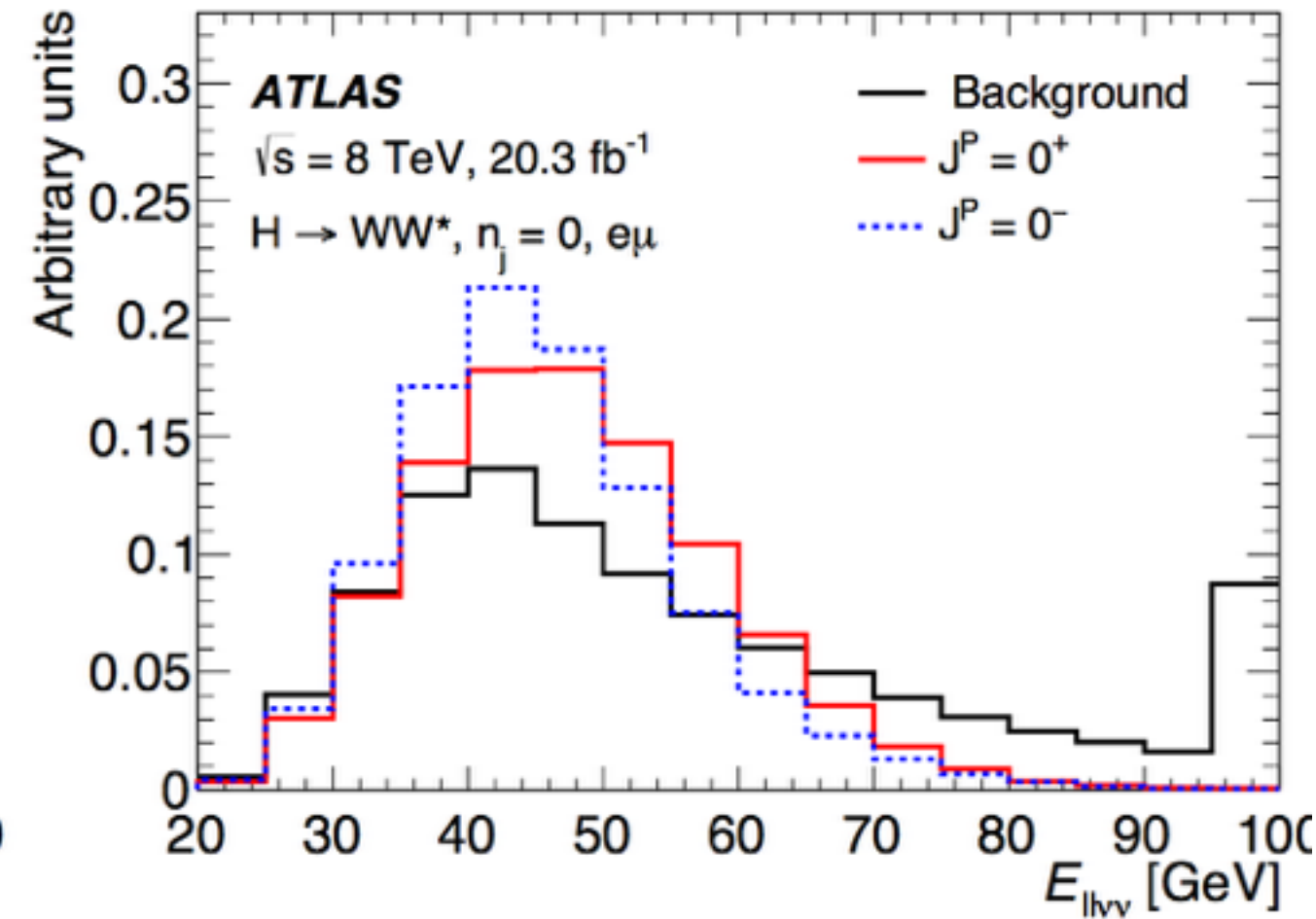
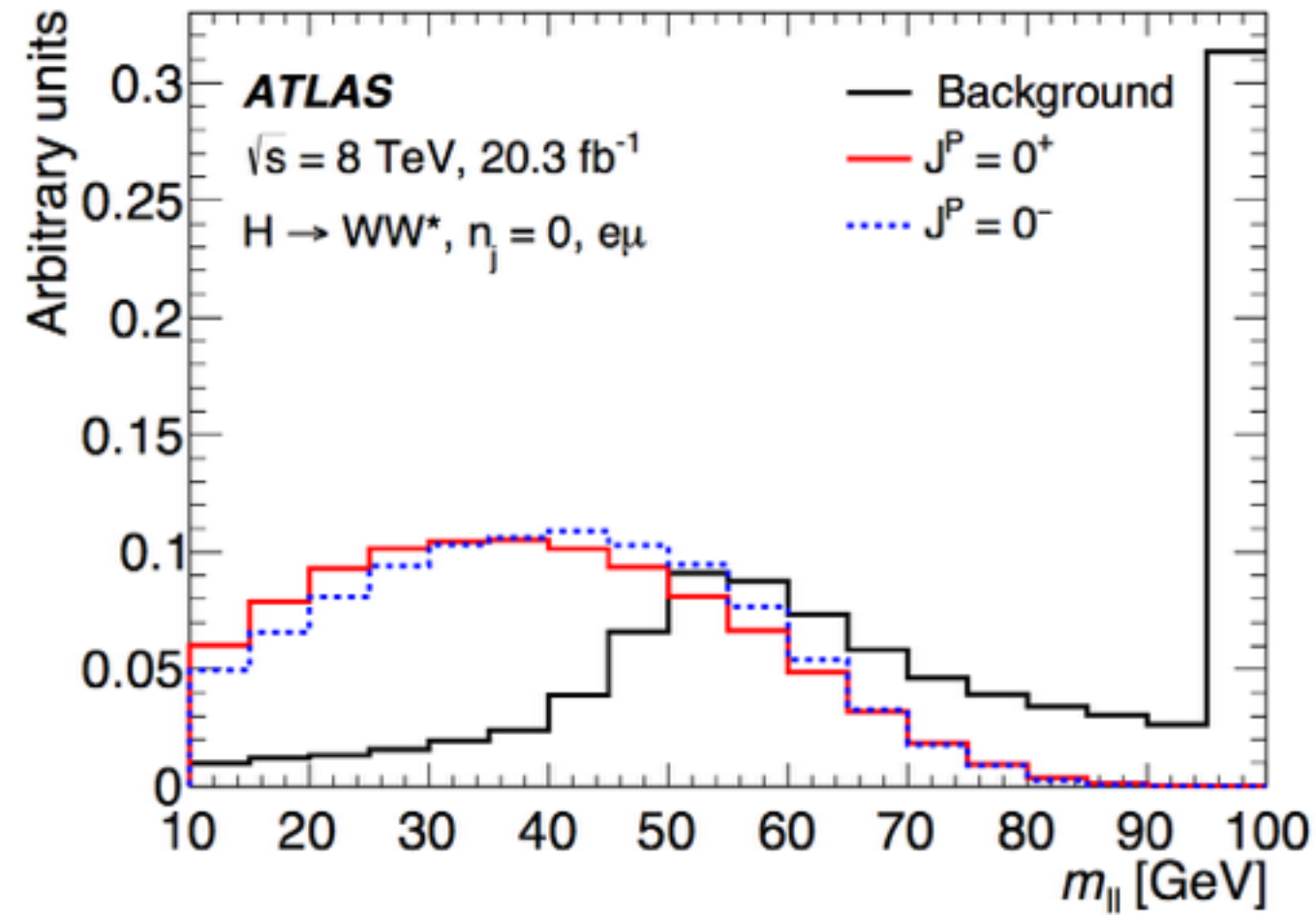
*Variations on the shapes  
for the alternative case  
more apparent!*

# CP even input shapes





# CP odd input shapes

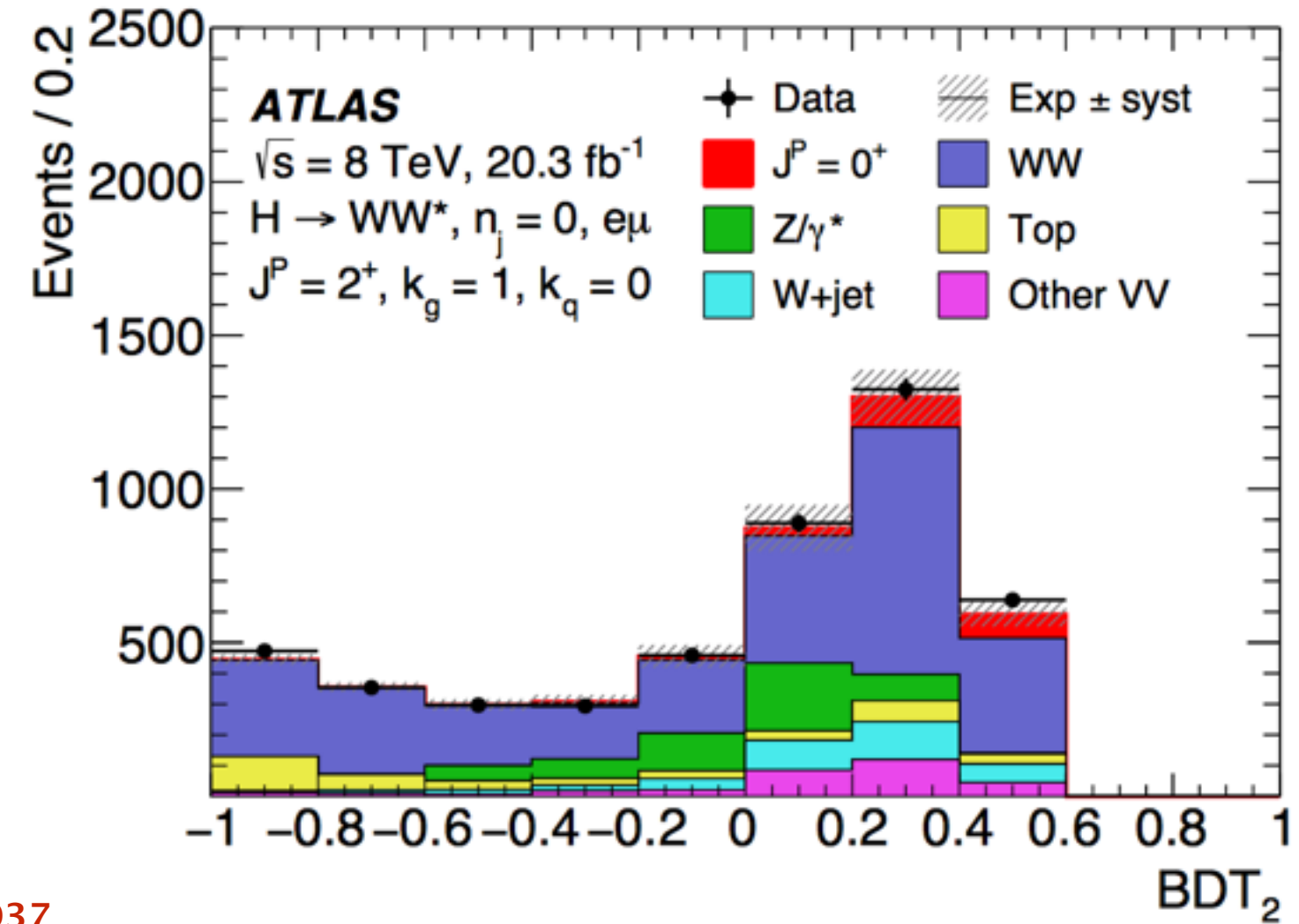
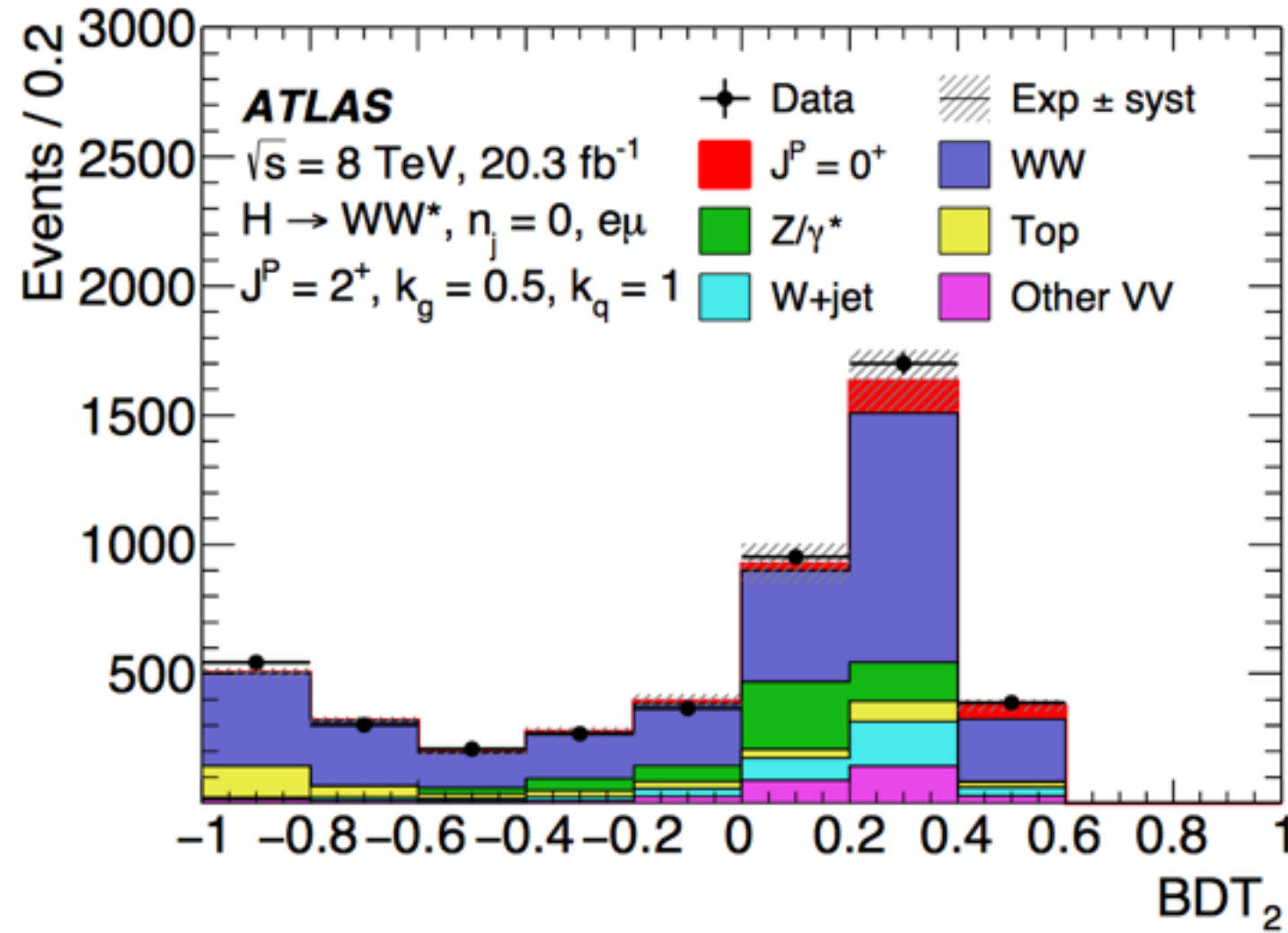


# Non U.C - BDT Output

$$\kappa_g = 0.5, \kappa_q = 1, p_T^H > 125 \text{ GeV}$$

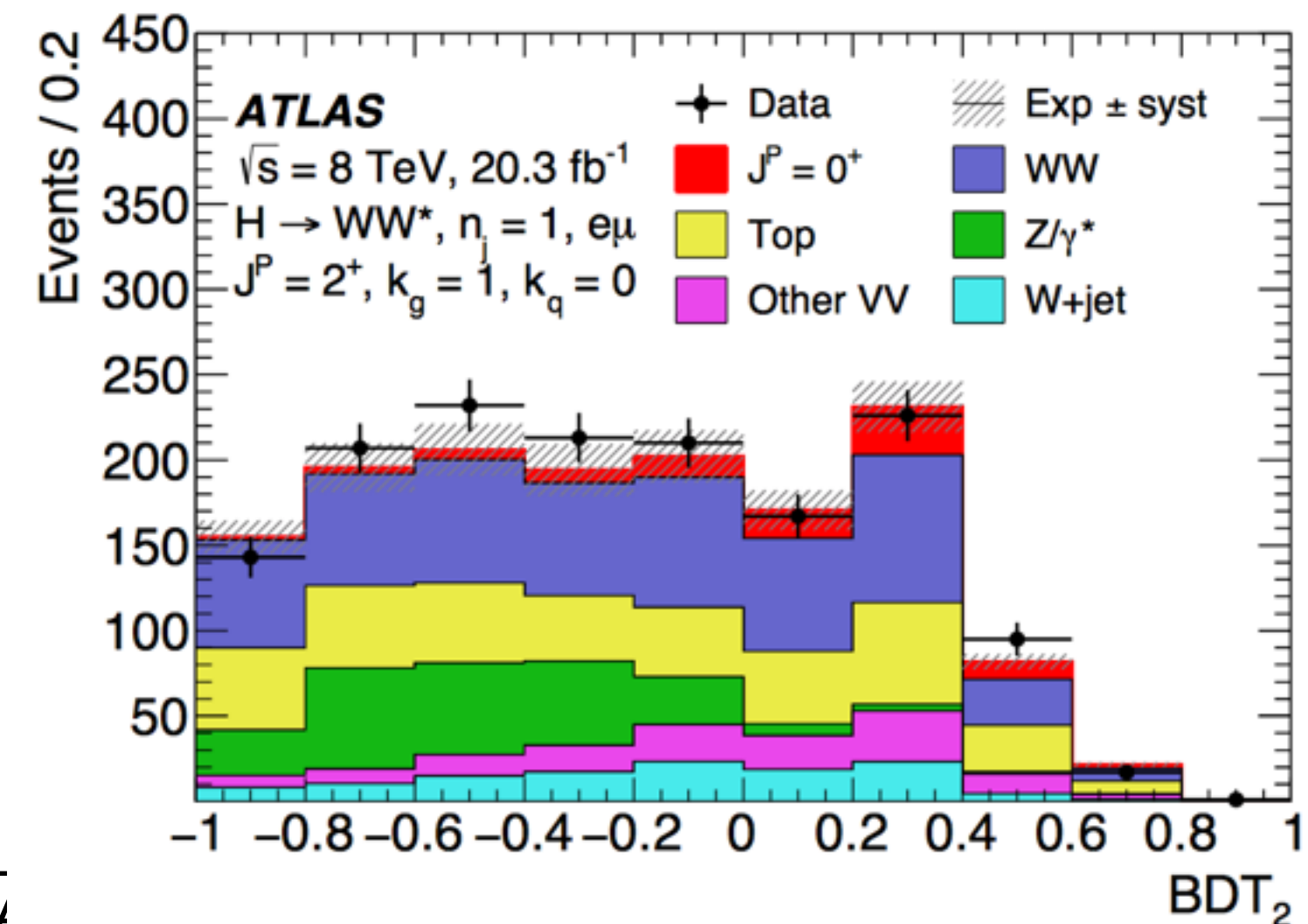
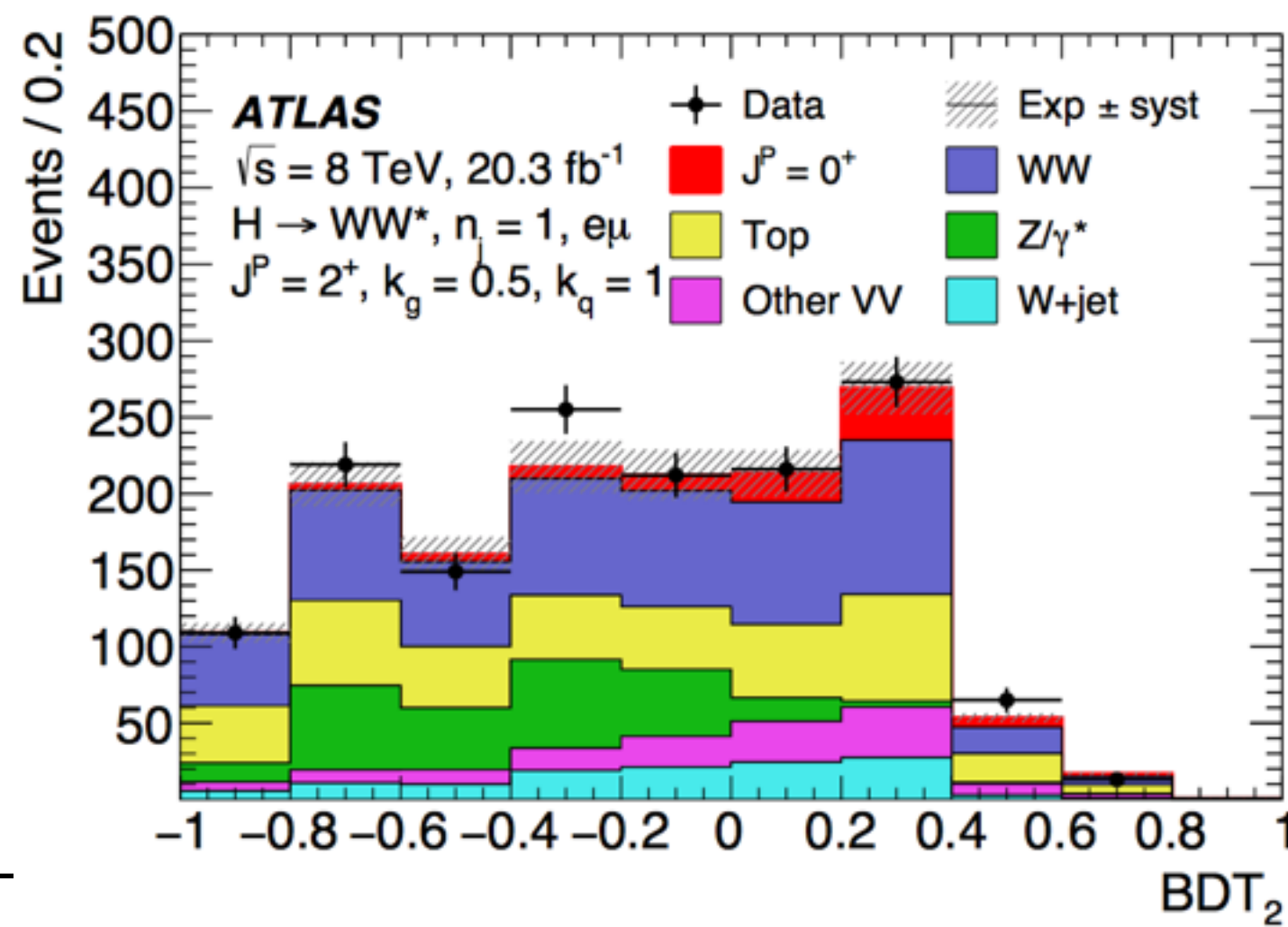
$$\kappa_g = 0, \kappa_q = 1, p_T^H > 125 \text{ GeV}$$

0-jet



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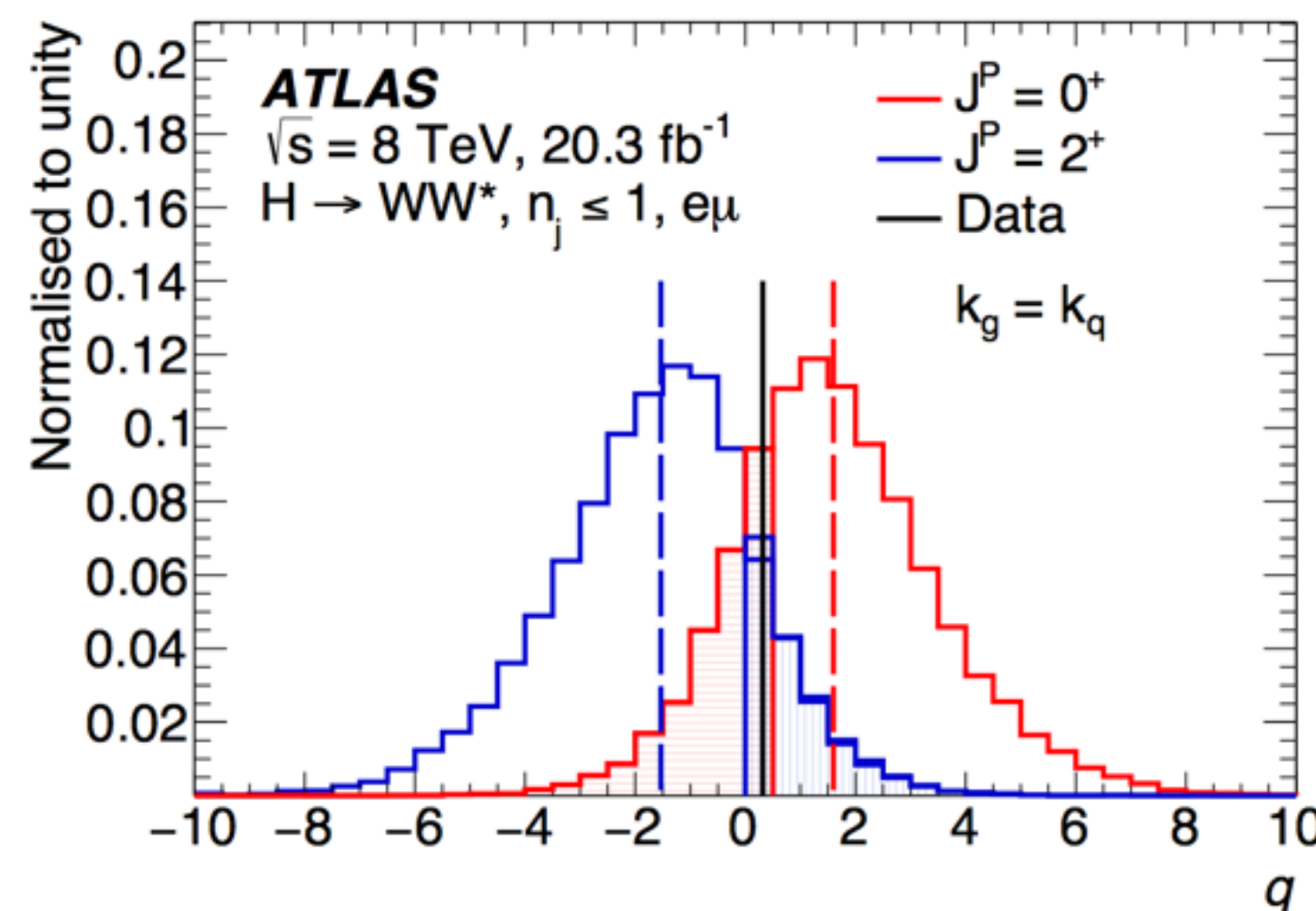
1-jet



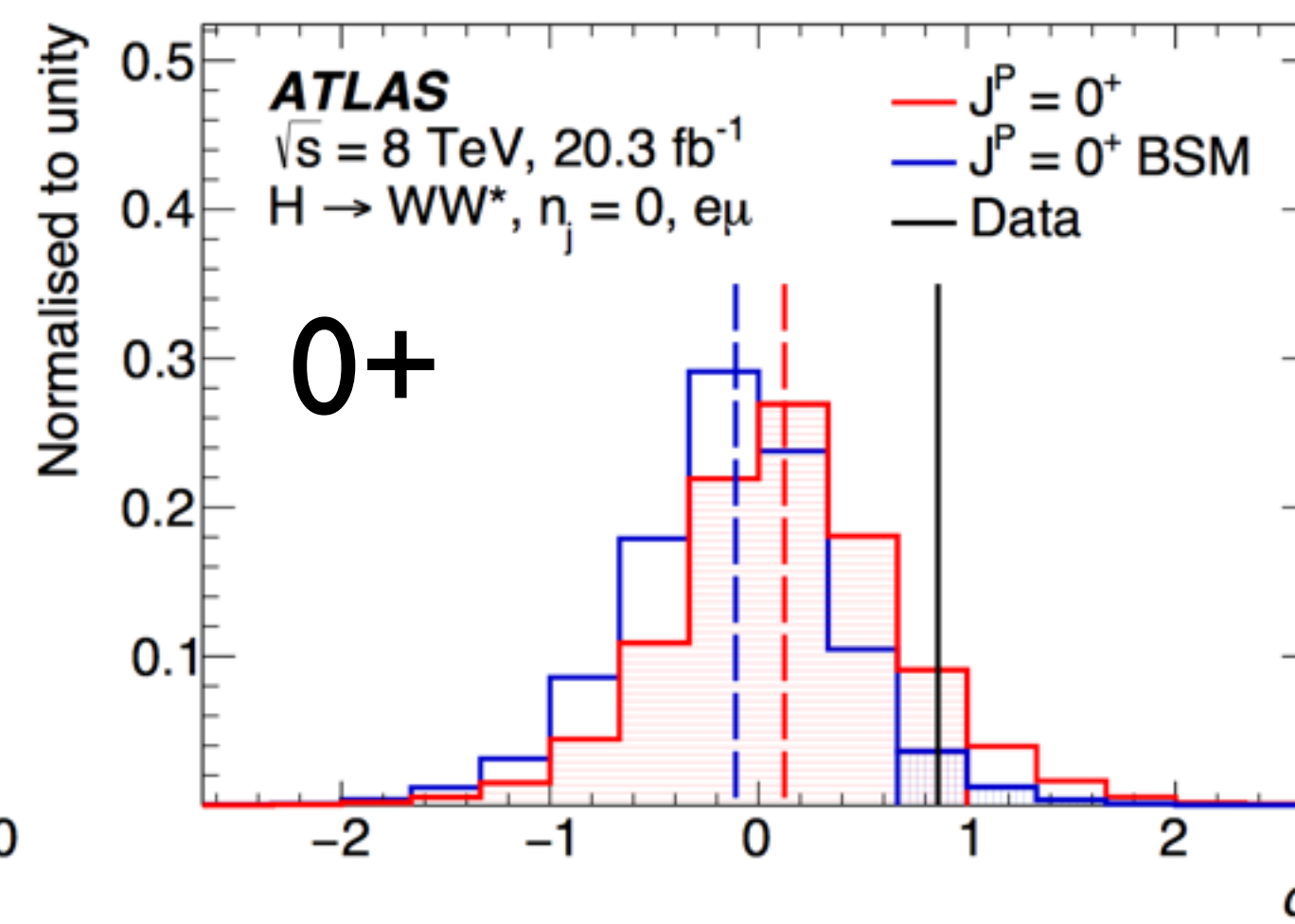
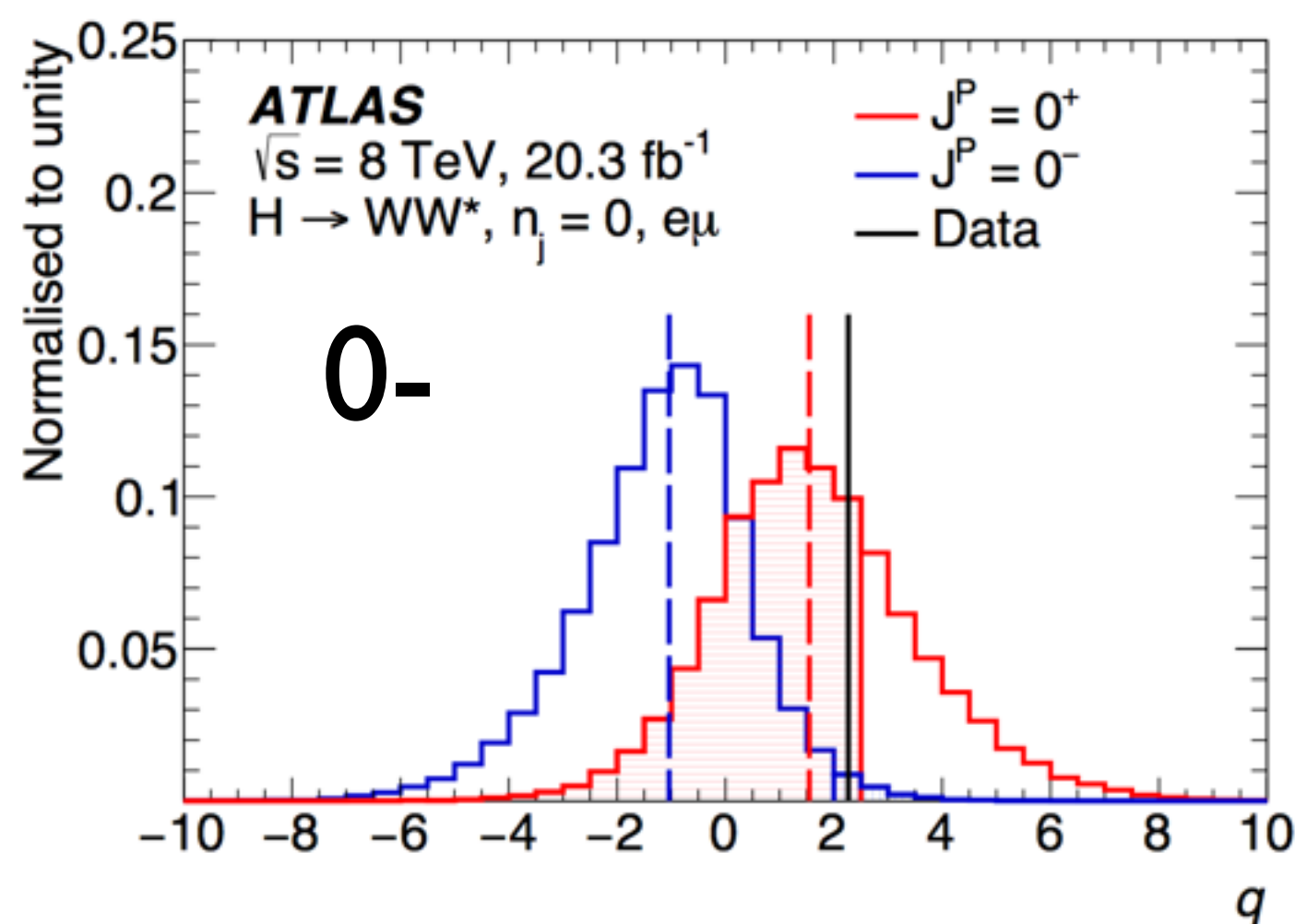
of  $H \rightarrow WW$  with  $l$



# Test Statistics



spin-2  $0^+ 1j$



# Post-fit event yields - U.C.

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Benchmark	Signal		Total background	
	0-jet	1-jet	0-jet	1-jet
$\kappa_g = \kappa_q$	$360 \pm 100$	$126 \pm 34$	$4370 \pm 240$	$1430 \pm 60$
$\kappa_g = 0.5, \kappa_q = 1, p_T^H < 125 \text{ GeV}$	$300 \pm 100$	$103 \pm 33$	$4430 \pm 240$	$1390 \pm 60$
$\kappa_g = 0.5, \kappa_q = 1, p_T^H < 300 \text{ GeV}$	$230 \pm 80$	$82 \pm 29$	$4490 \pm 230$	$1460 \pm 70$
$\kappa_g = 1, \kappa_q = 0, p_T^H < 125 \text{ GeV}$	$320 \pm 90$	$111 \pm 32$	$4410 \pm 240$	$1390 \pm 60$
$\kappa_g = 1, \kappa_q = 0, p_T^H < 300 \text{ GeV}$	$200 \pm 80$	$71 \pm 28$	$4520 \pm 240$	$1480 \pm 70$
BSM CP-odd	$240 \pm 80$	–	$4490 \pm 260$	–
BSM CP-even	$180 \pm 60$	–	$4530 \pm 240$	–

	Data	Signal	Tot. bkg.	WW	Top	DY	W+jets	Other
SM 0-jet	4730	$270 \pm 70$	$4460 \pm 240$	2904	376	464	370	345
SM 1-jet	1569	$95 \pm 26$	$1450 \pm 70$	607	355	233	124	133



# Systematic Uncertainties

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Table 6: Sources of experimental systematic uncertainty considered in the analysis. The source and magnitude of the uncertainties and their impact on the reconstructed objects is indicated.

Source of uncertainty	Treatment in the analysis and its magnitude
Jet energy scale	1 –7% in total as a function of jet $\eta$ and $p_T$
Jet energy resolution	5 –20% as a function of jet $\eta$ and $p_T$ Relative uncertainty on the resolution is 2 –40%
$b$ -tagging	$b$ -jet identification: 1 –8% decomposed in $p_T$ bins Light-quark jet misidentification: 9 –19% as a function of $\eta$ and $p_T$ $c$ -quark jet misidentification: 6 –14% as a function of $p_T$
Leptons	Reconstruction, identification, isolation, trigger efficiency: below 1% except for electron identification: 0.2 –2.7% depending on $\eta$ and $p_T$ Momentum scale and resolution: < 1%
Missing transverse momentum	Propagated jet-energy and lepton-momentum scale uncertainties Resolution (1.5 –3.3 GeV) and scale variation (0.3 –1.4 GeV)
Pile-up	The number of pile-up events is varied by 10%
Luminosity	2.8% [47]

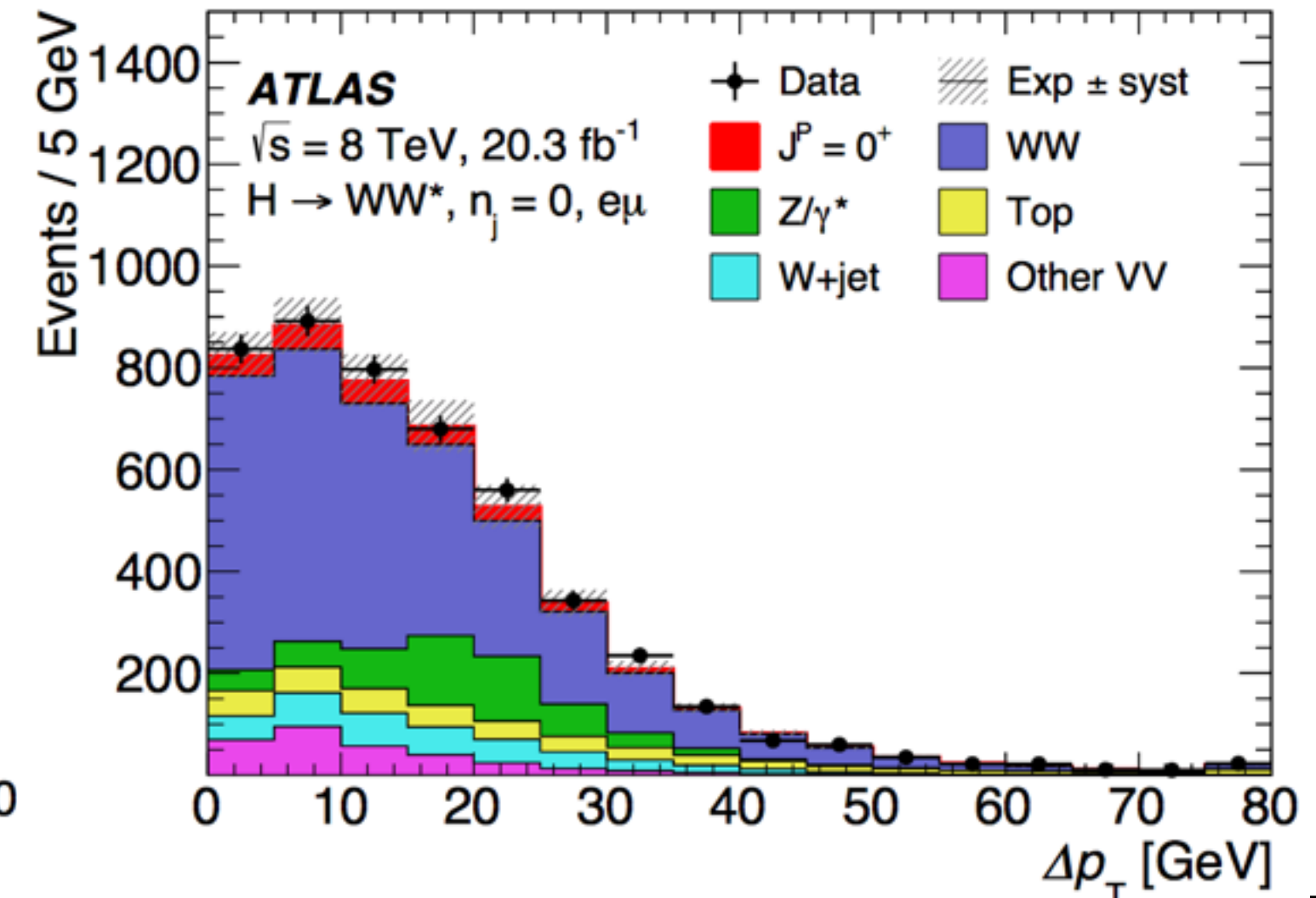
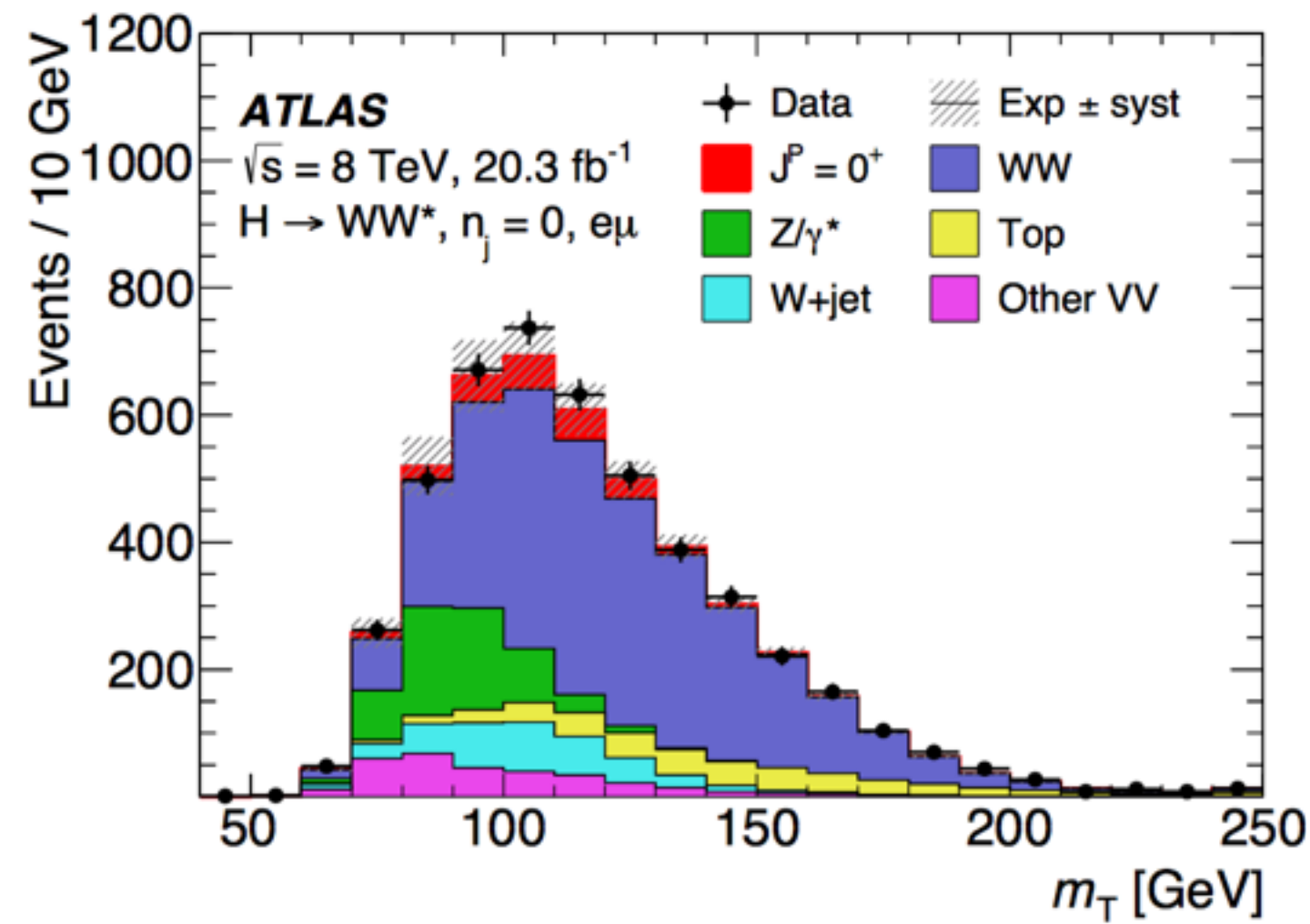
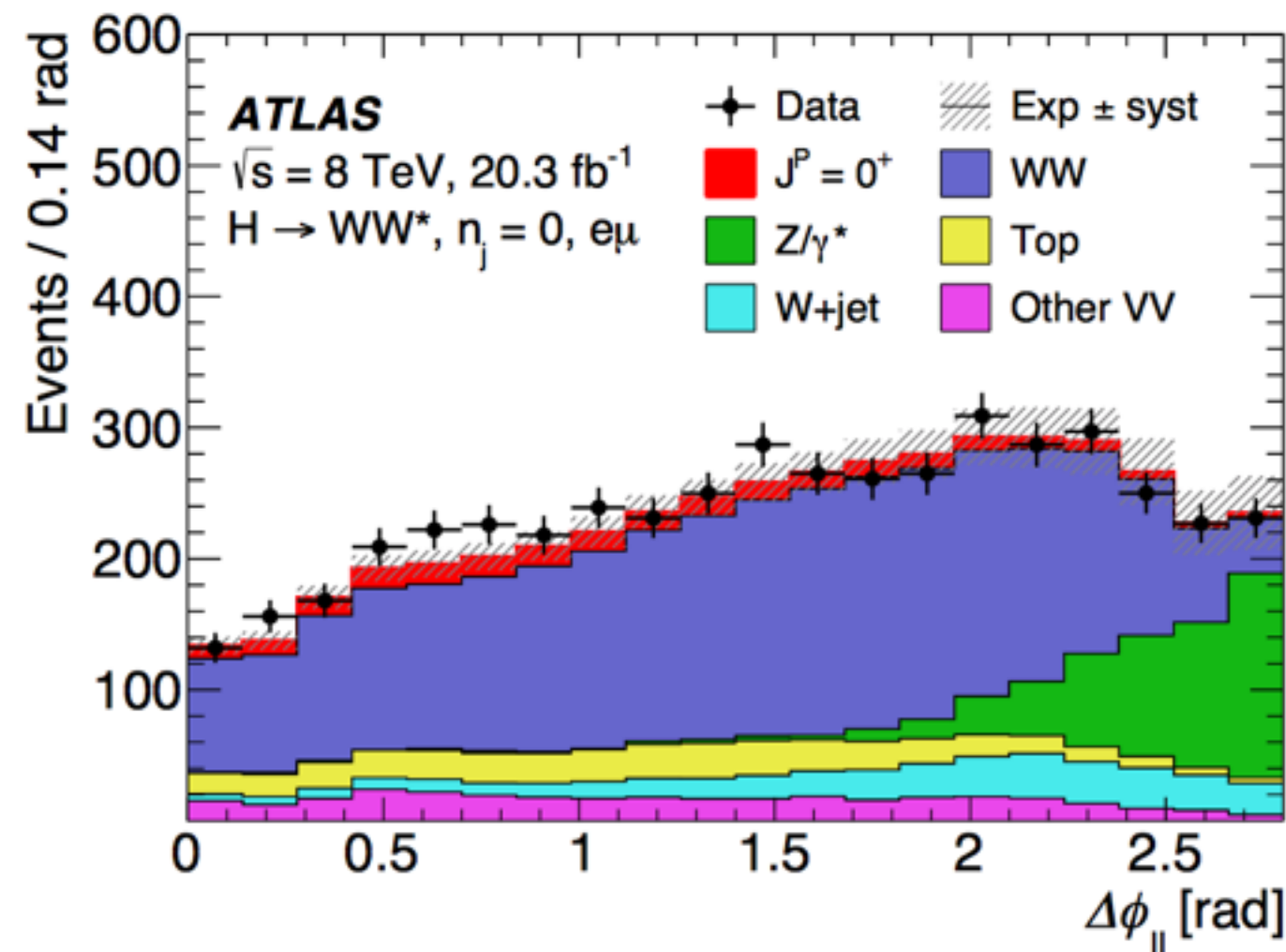
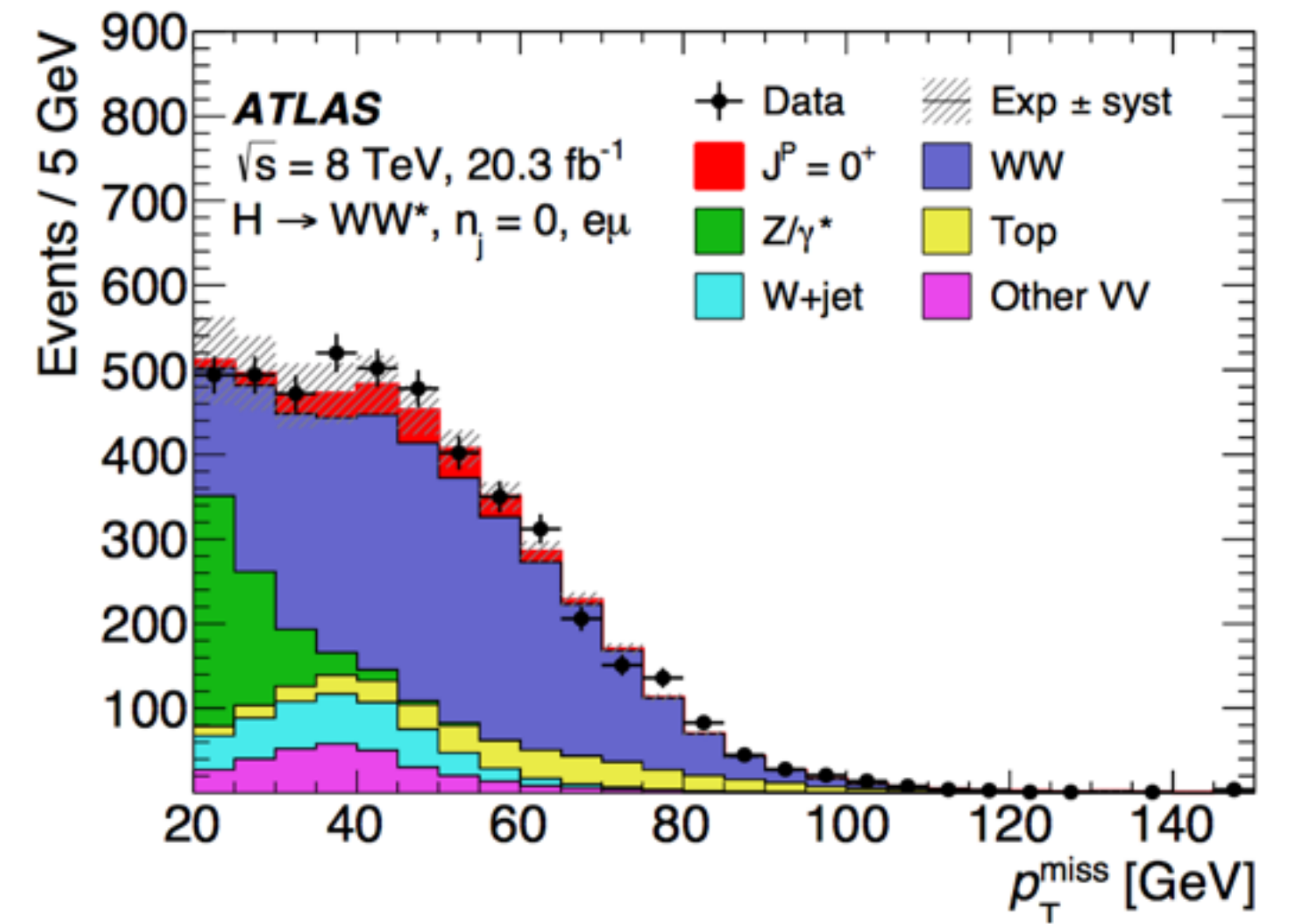
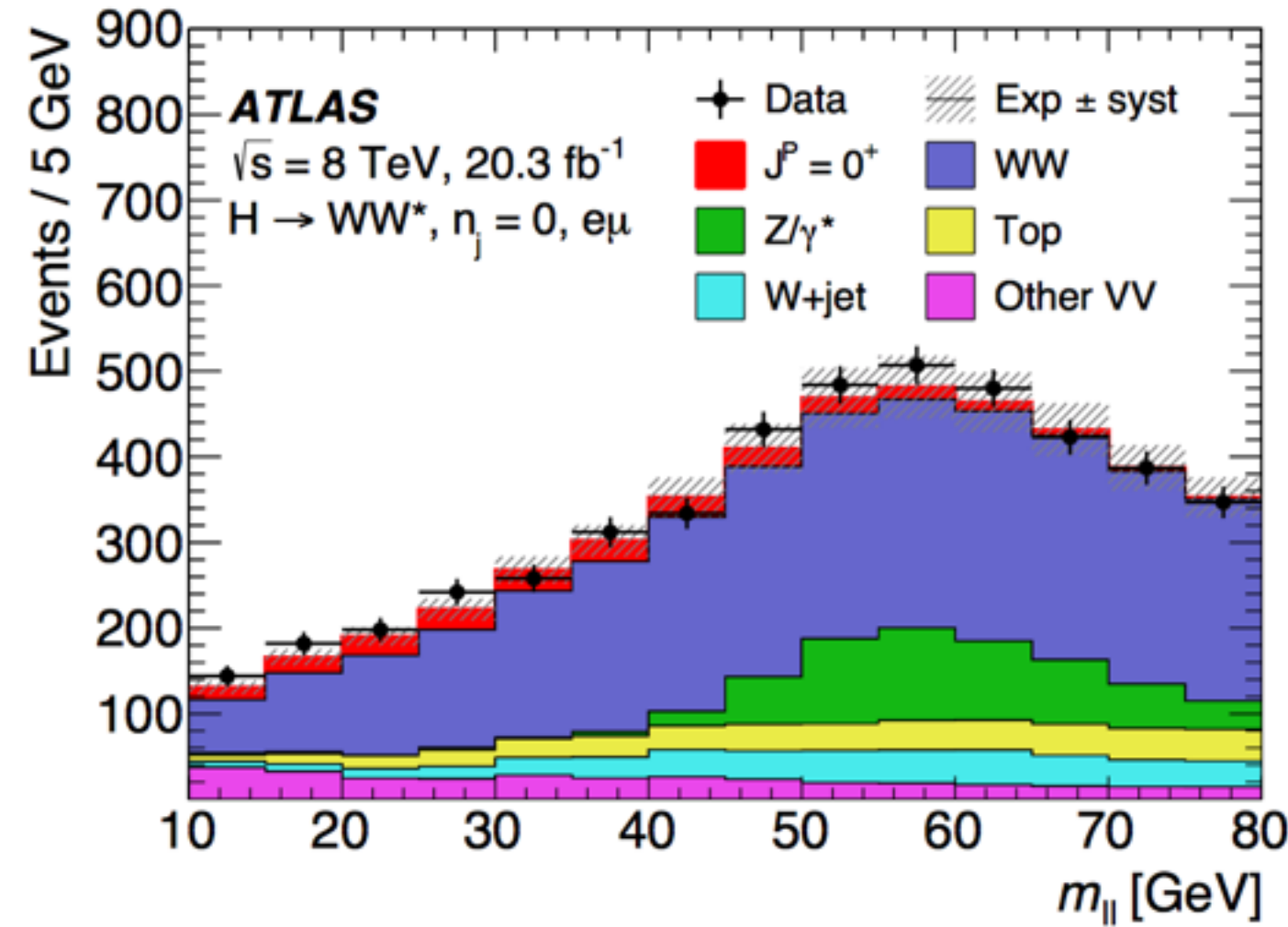
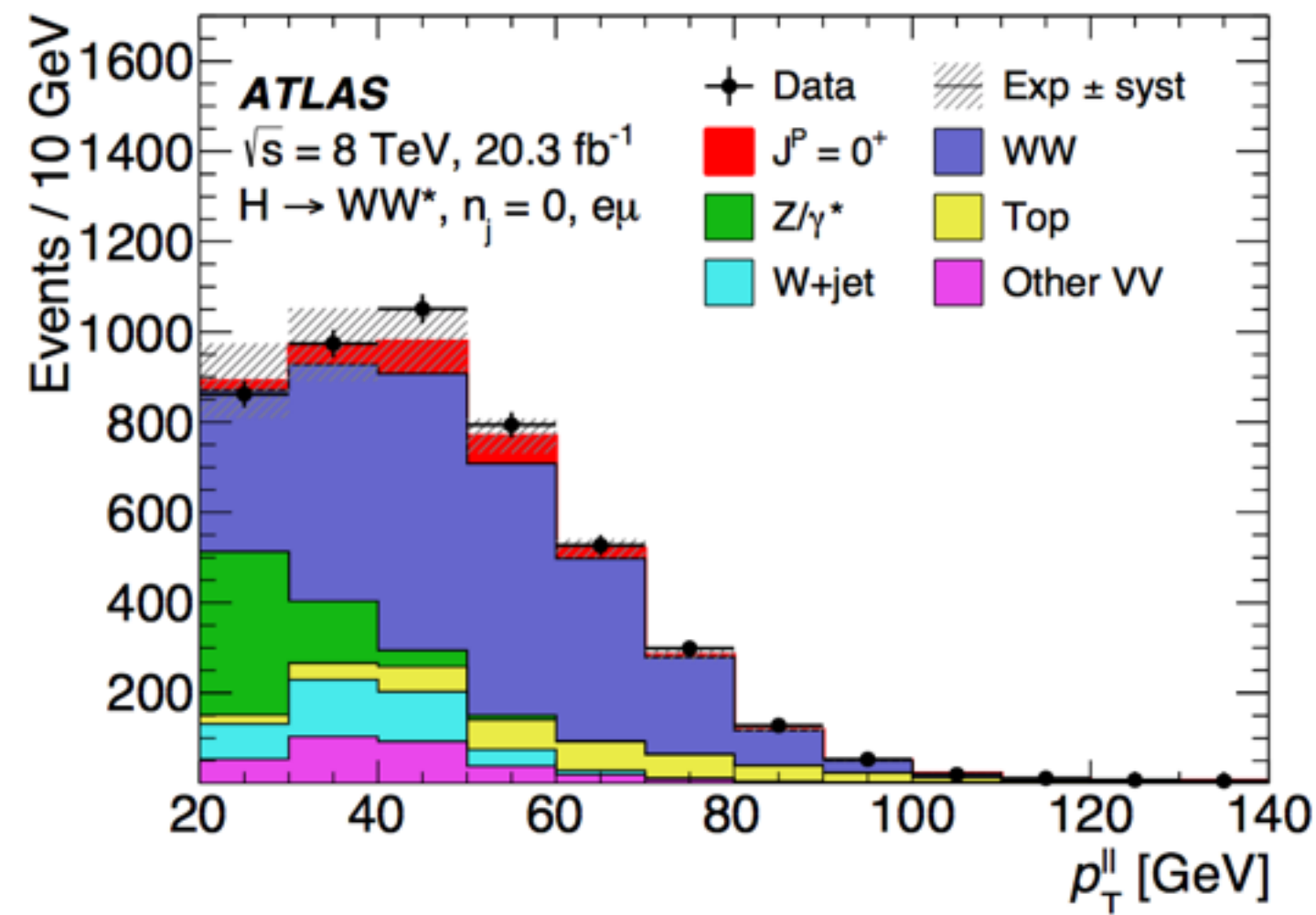
Category	Scale	PDF	Gen	EW	UE/PS	$p_T^Z$	Total
WW background							
SR 0-jet	0.9	3.8	6.9	–0.8	–4.1	–	8.2
SR 1-jet	1.2	1.9	3.3	–2.1	–3.2	–	5.3
Top-quark background							
SR 1-jet	–0.8	–1.4	1.9	–	2.4	–	3.5
WW CR 1-jet	0.6	0.3	–2.4	–	2.0	–	3.2
$Z/\gamma^* \rightarrow \tau\tau$ background							
SR 0-jet	–7.1	1.3	–	–	–6.5	19	21.3
SR 1-jet	6.6	0.66	–	–	–4.2	–	7.9
WW CR 0-jet	–11.4	1.7	–	–	–8.3	16	21.4
WW CR 1-jet	–5.6	2.2	–	–	–4.8	–	7.7

Table 7: From top to bottom, systematic uncertainties (in %) with the largest impact on the spin-2 universal couplings, BSM CP-odd and CP-even Higgs-boson fixed-hypothesis tests. This ranking is based on the impact of each systematic uncertainty on the  $CL_s$  estimator (see Sect. 7). For the exact meaning of the different uncertainties related to the misidentified lepton rates (the  $W$ +jets background estimate uncertainty), see Sect. 5.4 and Ref. [9].

Spin-2		BSM CP-odd		BSM CP-even	
WW generator:	2.6	WW generator:	0.73	WW UE/PS:	21
$p_T^Z$ reweighting:	1.2	WW UE/PS:	0.66	Misid. rate (elec. stats):	9.2
Misid. rate (elec. stats):	1.1	QCD scale $Wg^*$ :	0.45	Misid. rate (elec. flavour):	8.4
Misid. rate (elec. flavour):	1.0	$p_T^Z$ reweighting:	0.43	Misid. rate (muon flavour):	7.4
WW UE/PS:	0.86	QCD scale $VV$ :	0.39	Misid. rate (muon stats):	7.3
Misid. rate (muon stats):	0.81	QCD scale $Wg$ :	0.38	Misid. rate (elec. other):	7.3
$Z/\gamma^* \rightarrow \tau\tau$ generator:	0.76	Misid. rate (elec. stats):	0.37	WW PDF $qq$ -production:	6.9
Misid. rate (muon flavour):	0.75	Misid. rate (elec. other):	0.34	WW PDF $gg$ -production:	6.9
Misid. rate (elec. other):	0.67	Misid. rate (elec. flavour):	0.33	WW generator:	3.6



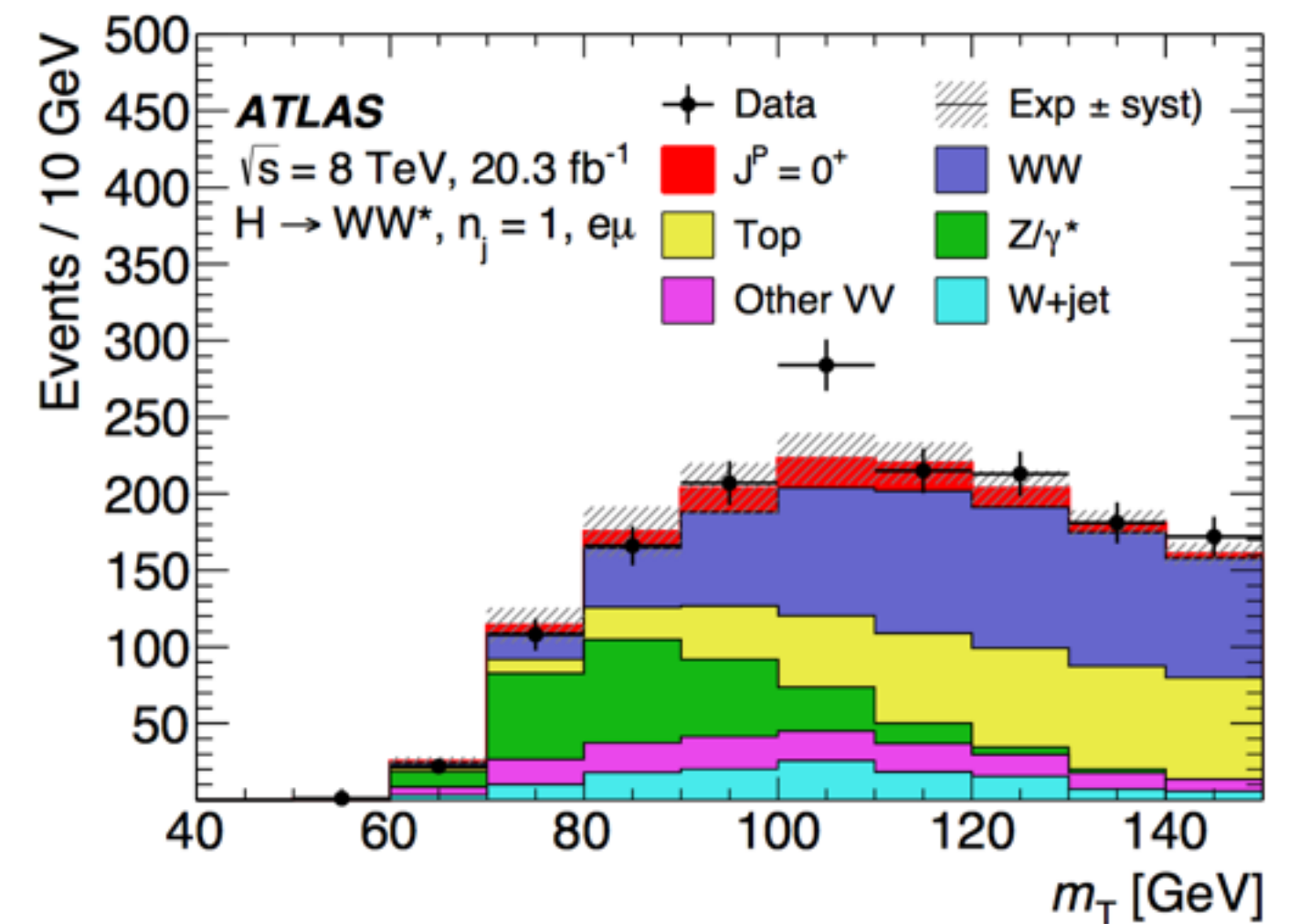
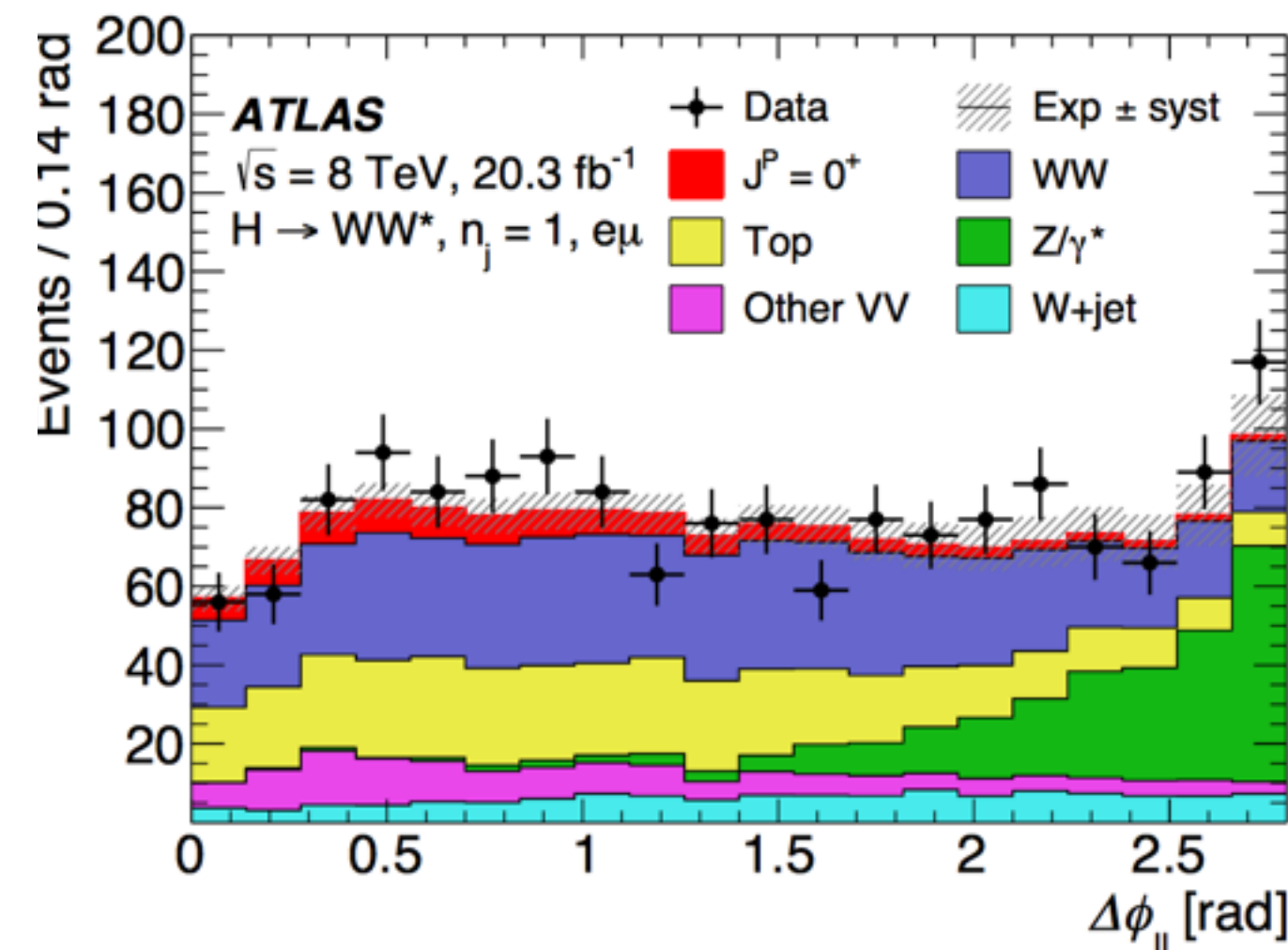
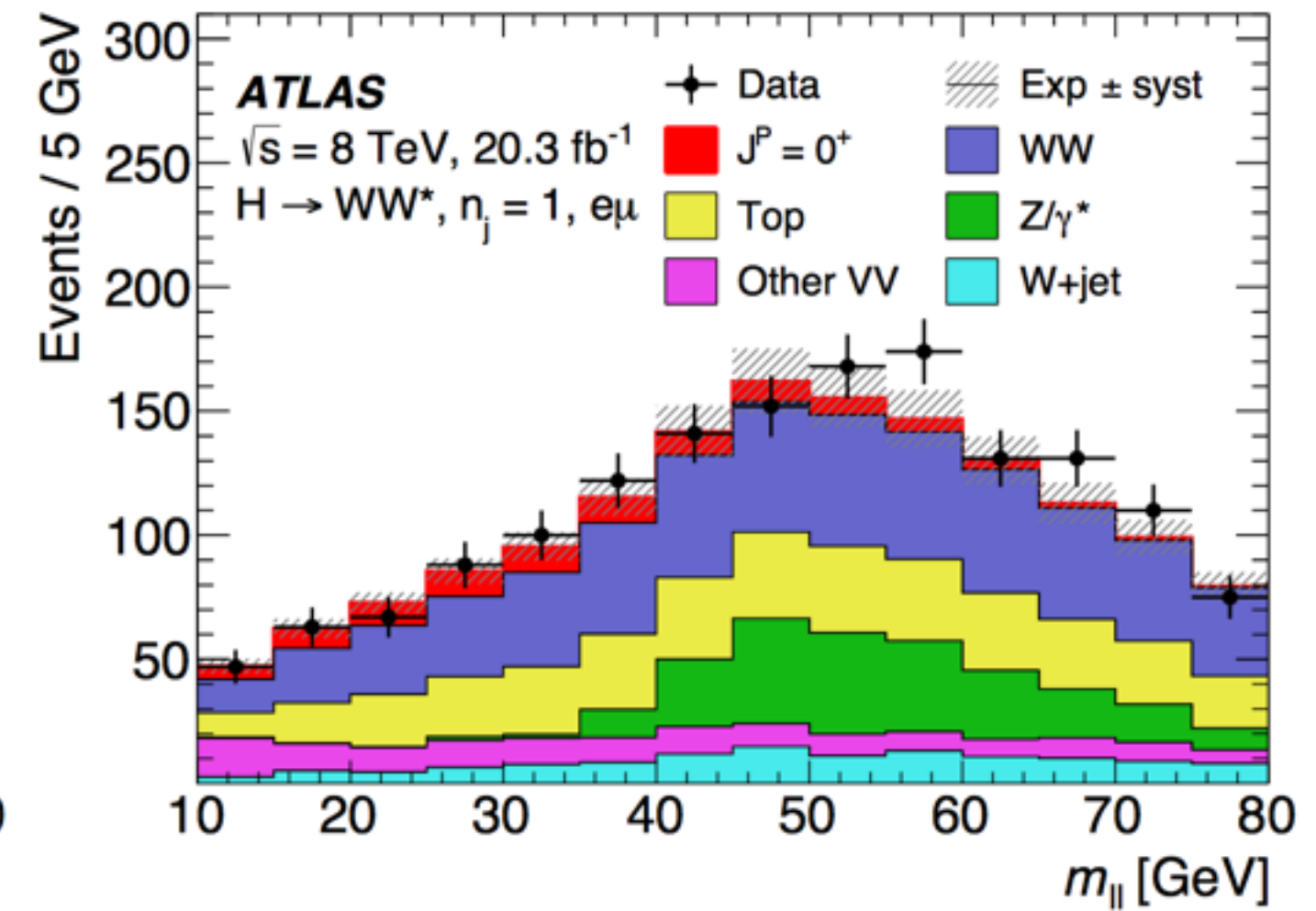
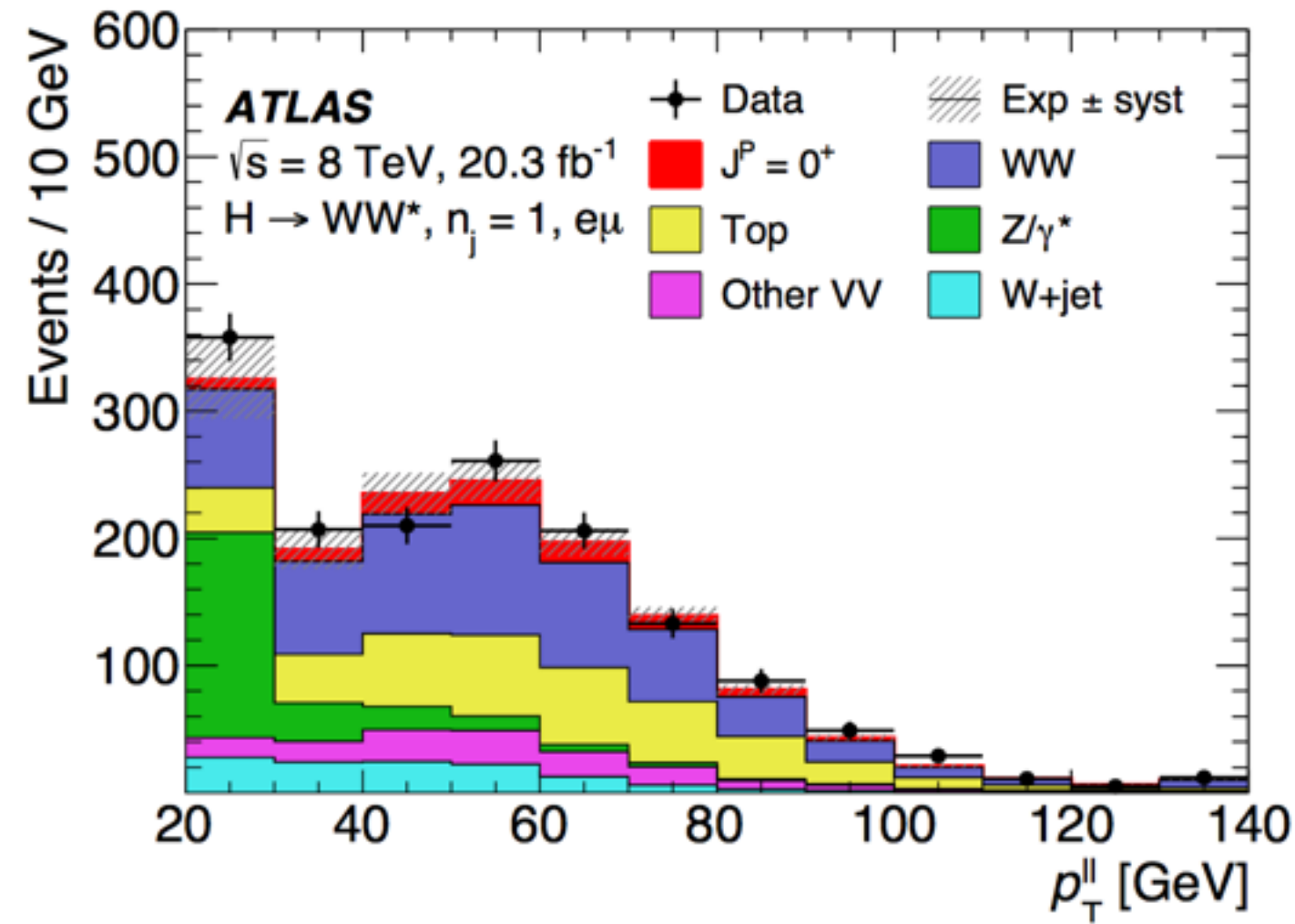
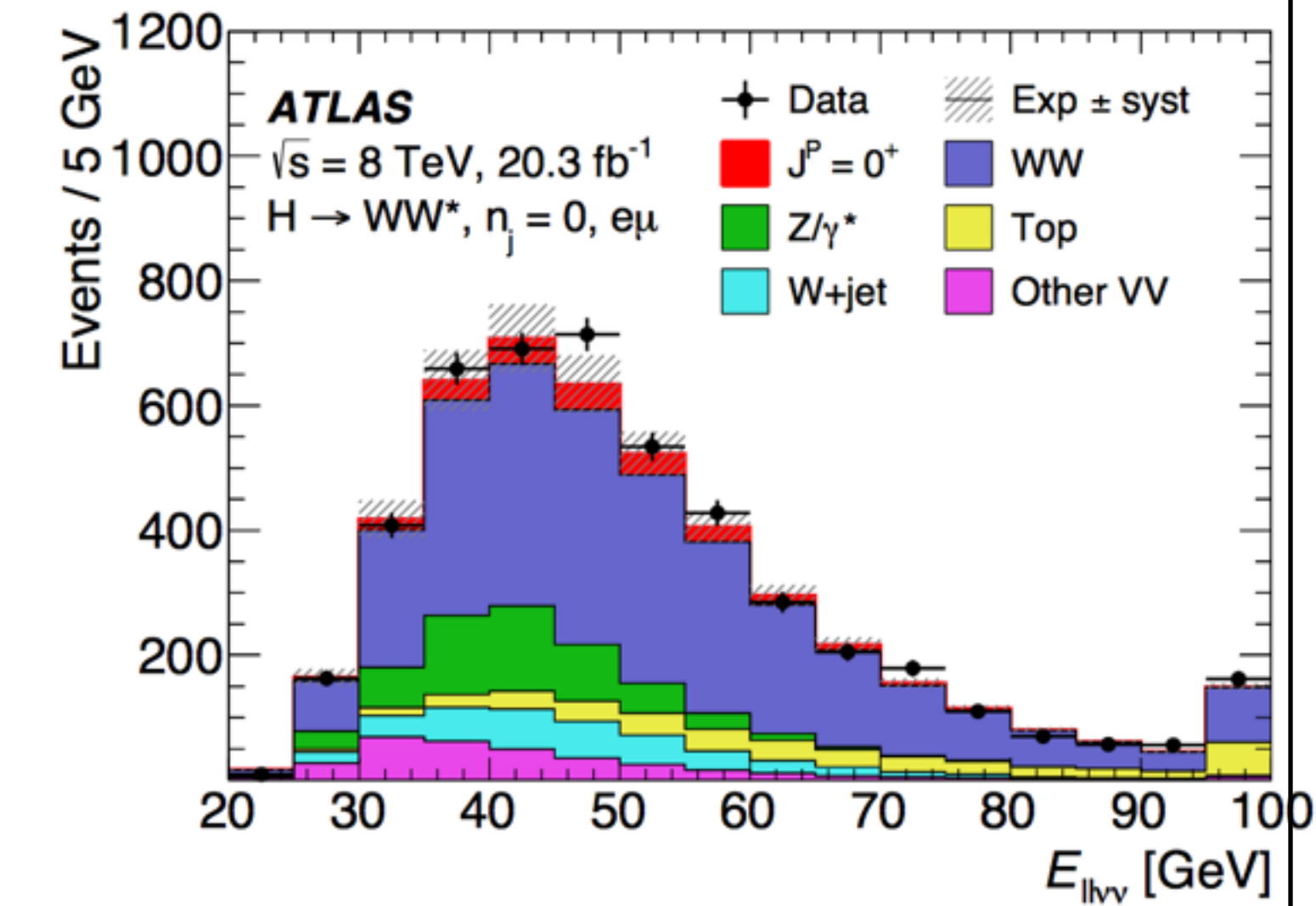
# 0jet Inputs





# 0jet Ellvv & 1jet Inputs

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# CR Definition

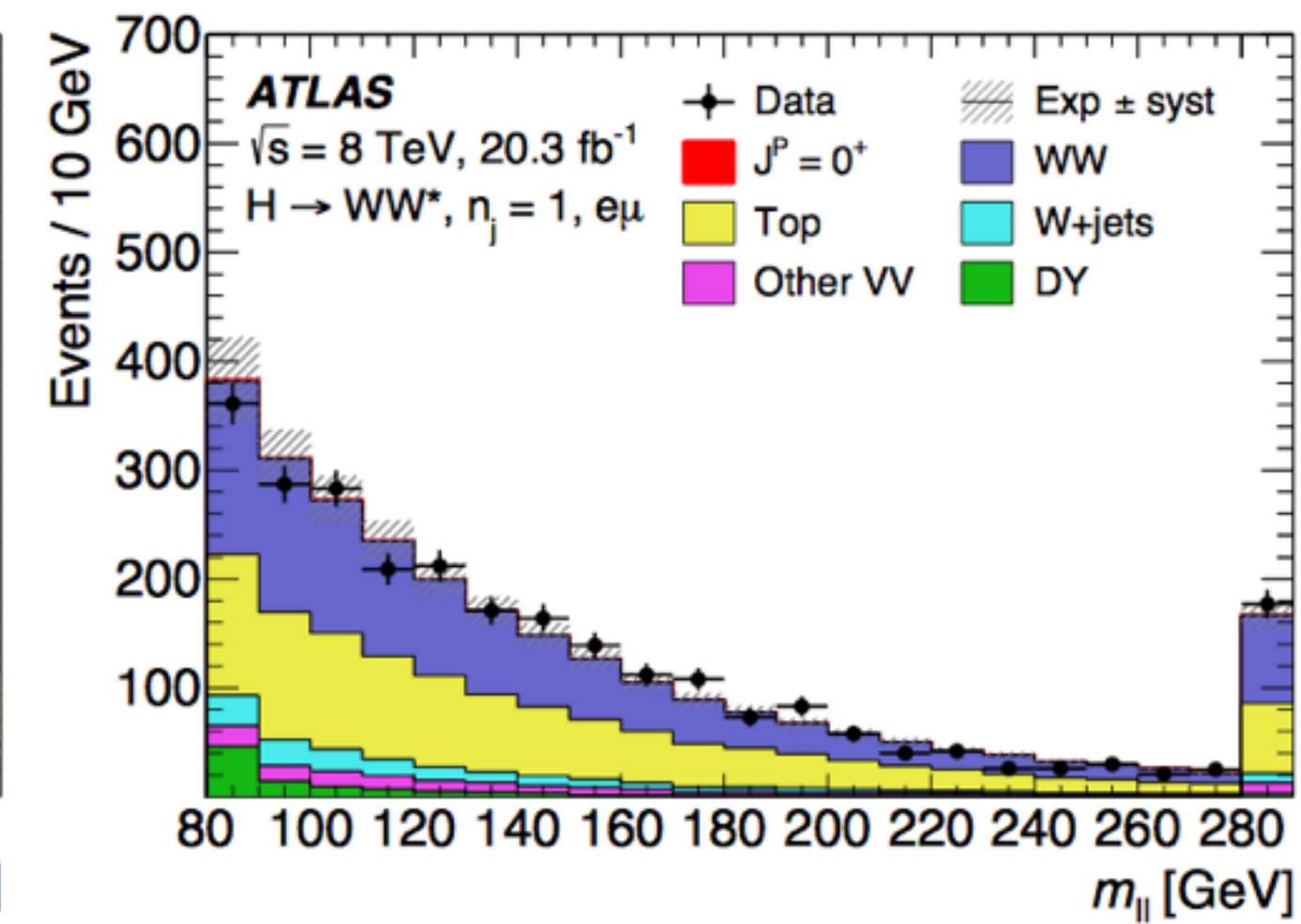
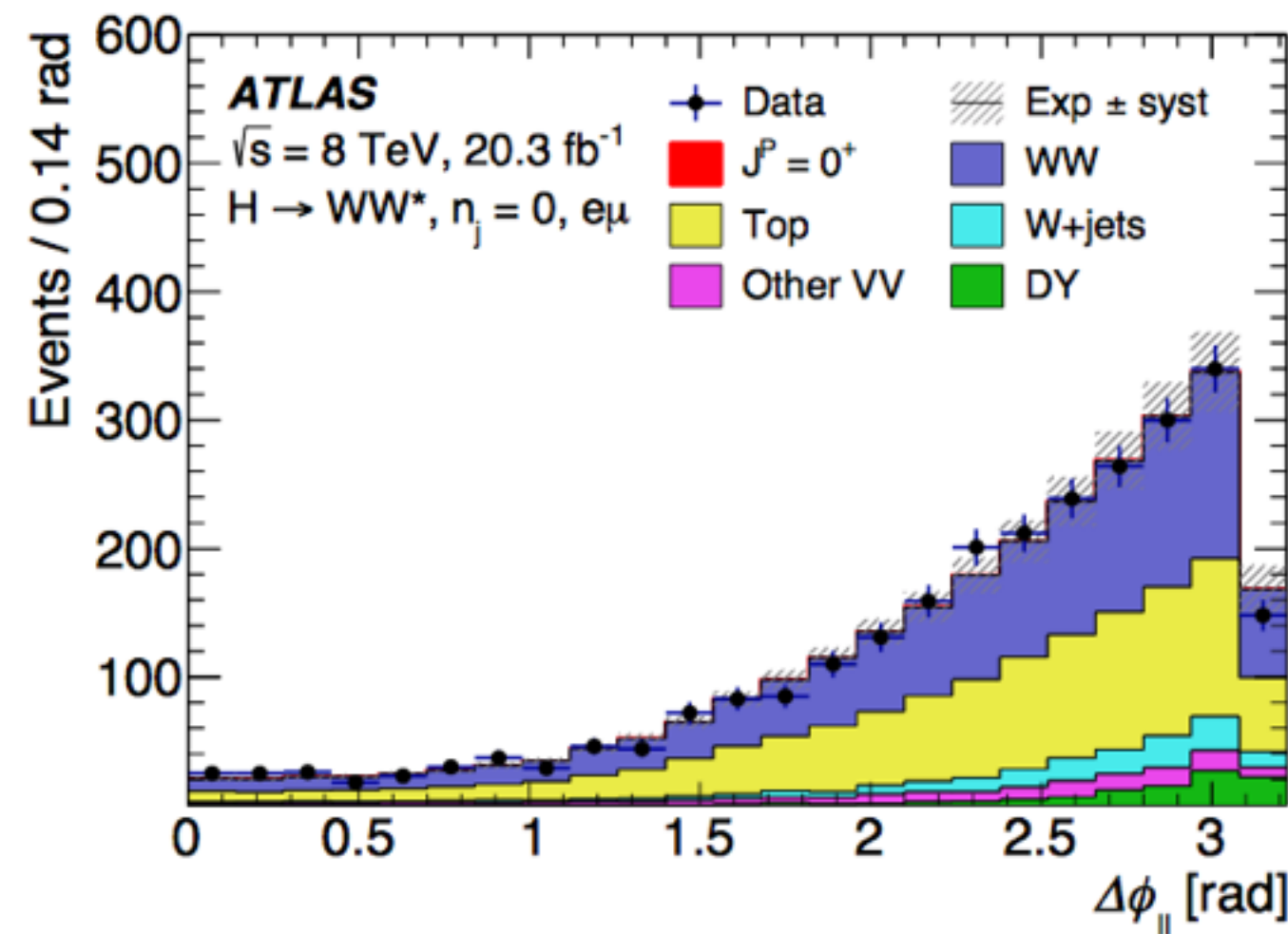
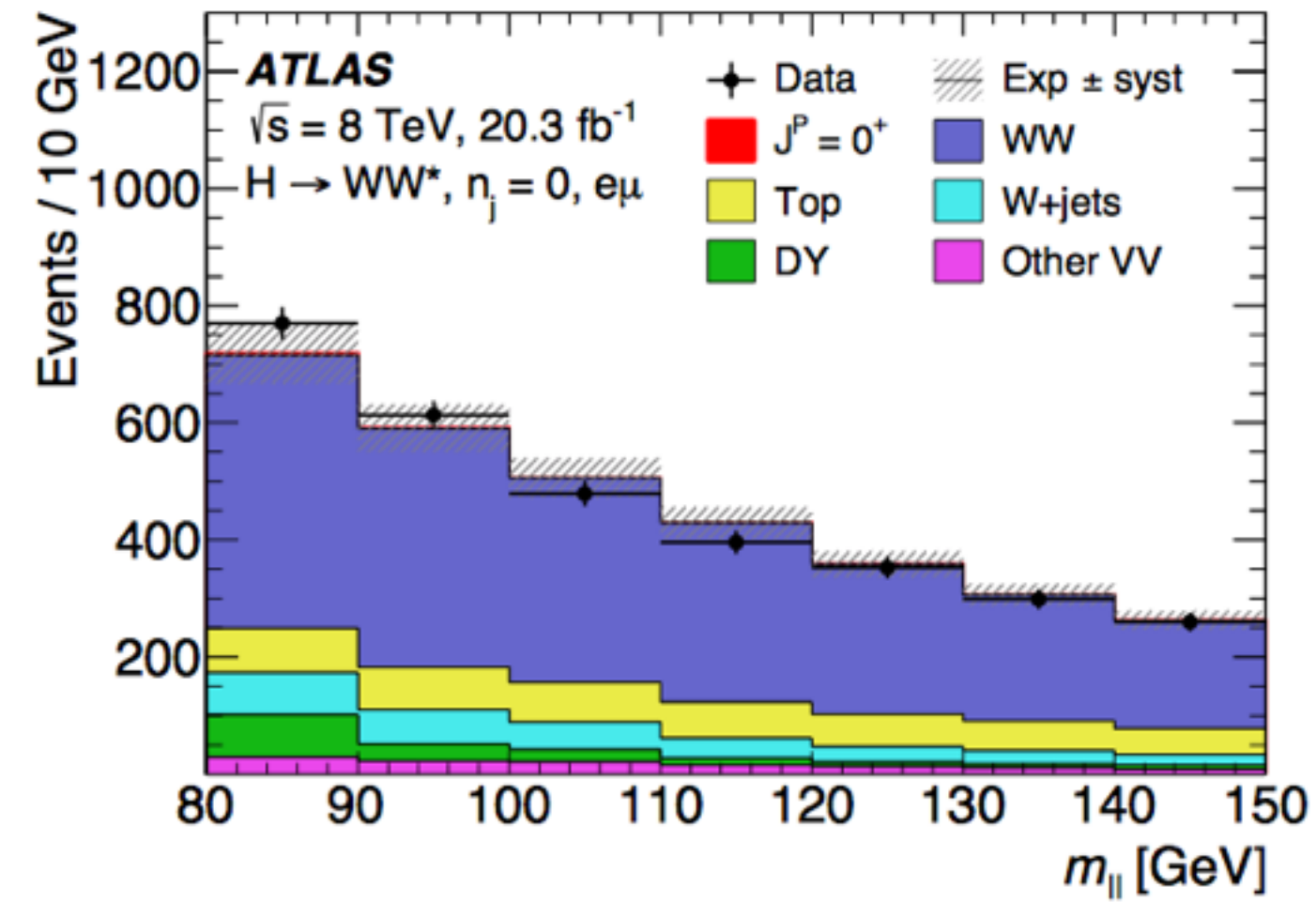
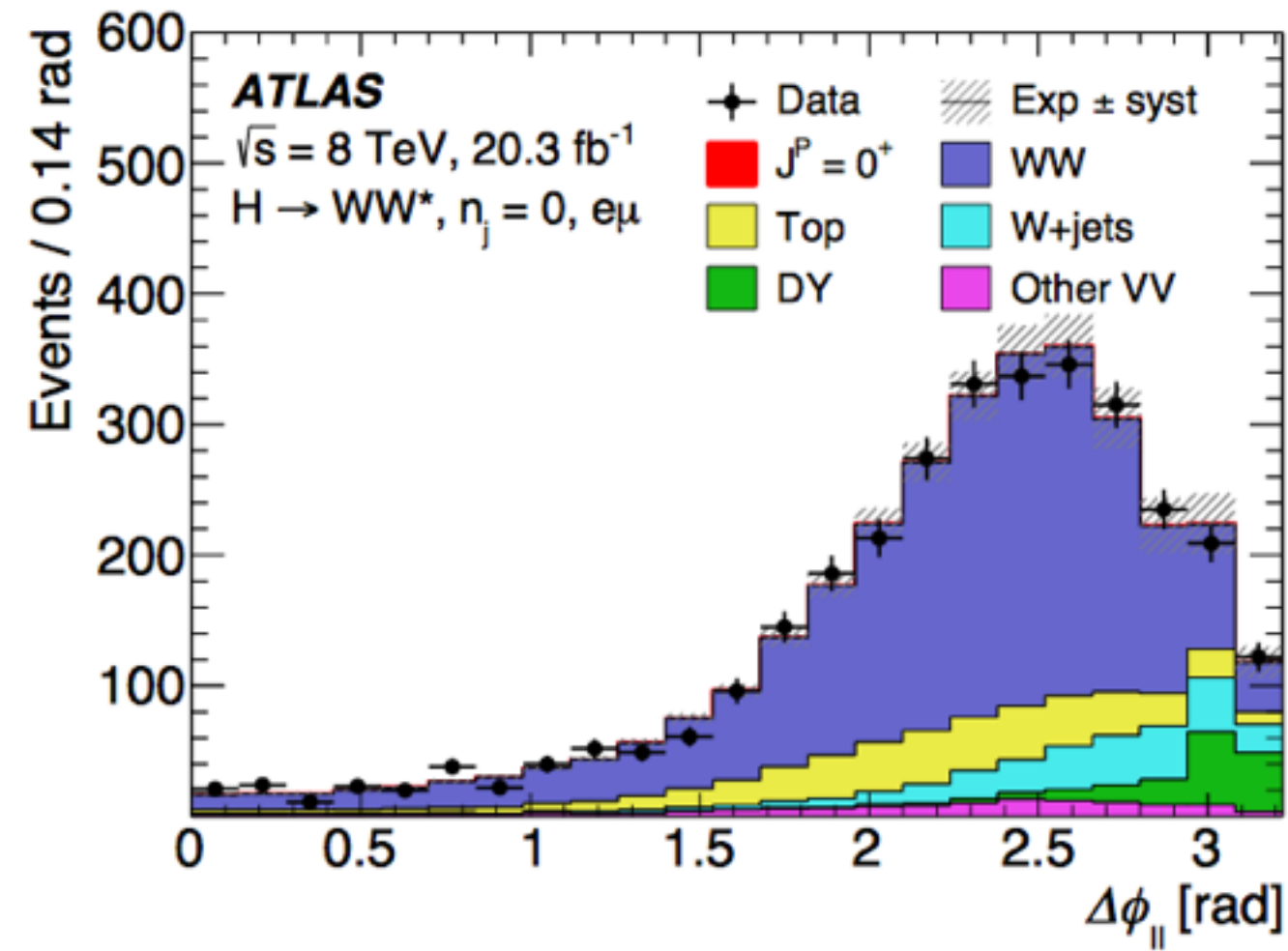
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Control region	Selection
WW CR 0-jet	Preselection, $p_T^{\ell\ell} > 20$ GeV, $80 < m_{\ell\ell} < 150$ GeV
WW CR-1 jet	Preselection, $b$ -veto, $m_{\tau\tau} < m_Z - 25$ GeV $m_T^\ell > 50$ GeV, $m_{\ell\ell} > 80$ GeV
Top CR 0-jet	Preselection, $\Delta\phi_{\ell\ell} < 2.8$ , all jets inclusive
Top CR 1-jet	At least one $b$ -jet, $m_{\tau\tau} < m_Z - 25$ GeV
$Z/\gamma^* \rightarrow \tau\tau$ CR 0-jet	Preselection, $m_{\ell\ell} < 80$ GeV, $\Delta\phi_{\ell\ell} > 2.8$
$Z/\gamma^* \rightarrow \tau\tau$ CR 1-jet	Preselection, $b$ -veto, $m_T^\ell > 50$ GeV, $m_{\ell\ell} < 80$ GeV, $ m_{\tau\tau} - m_Z  < 25$ GeV



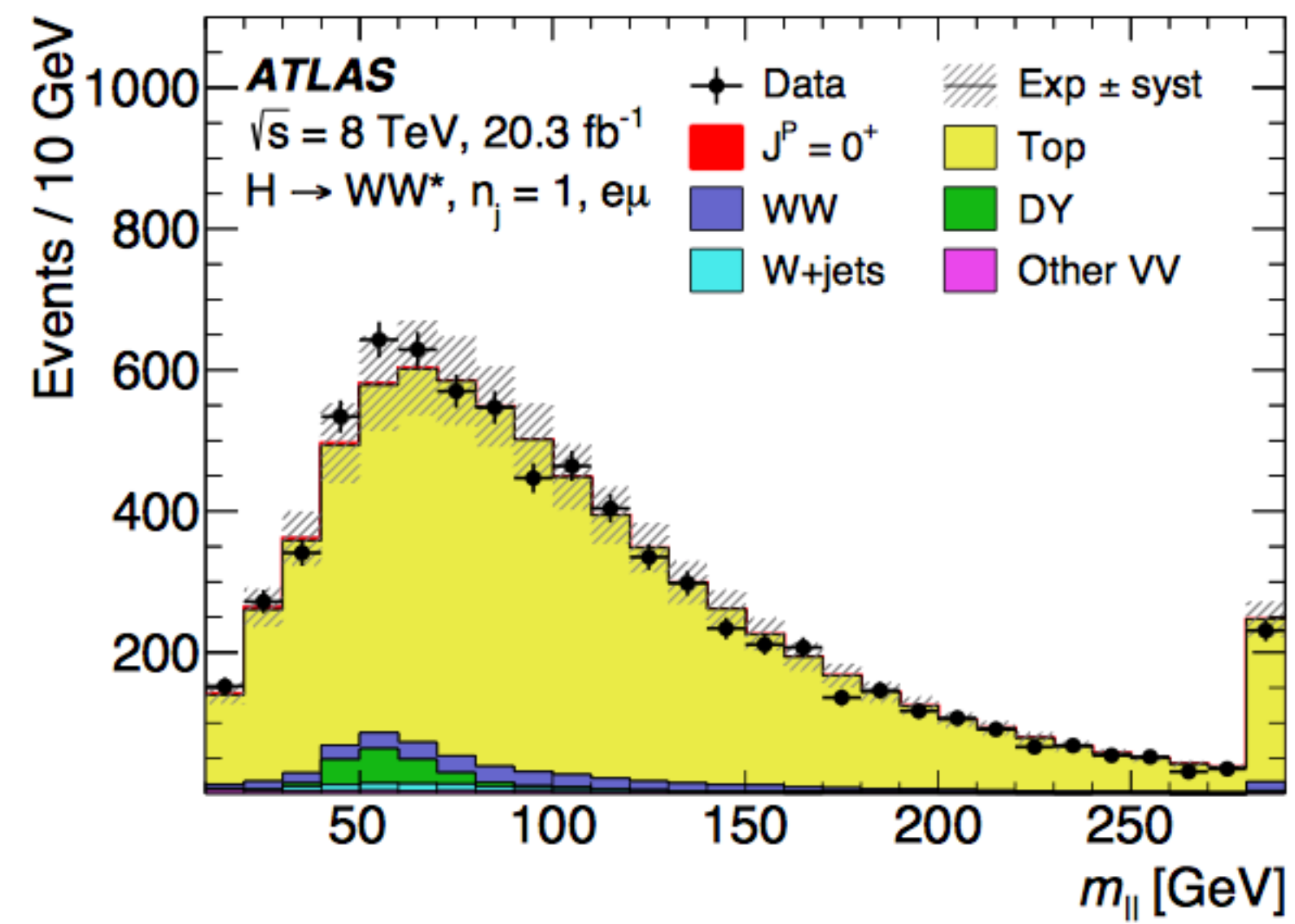
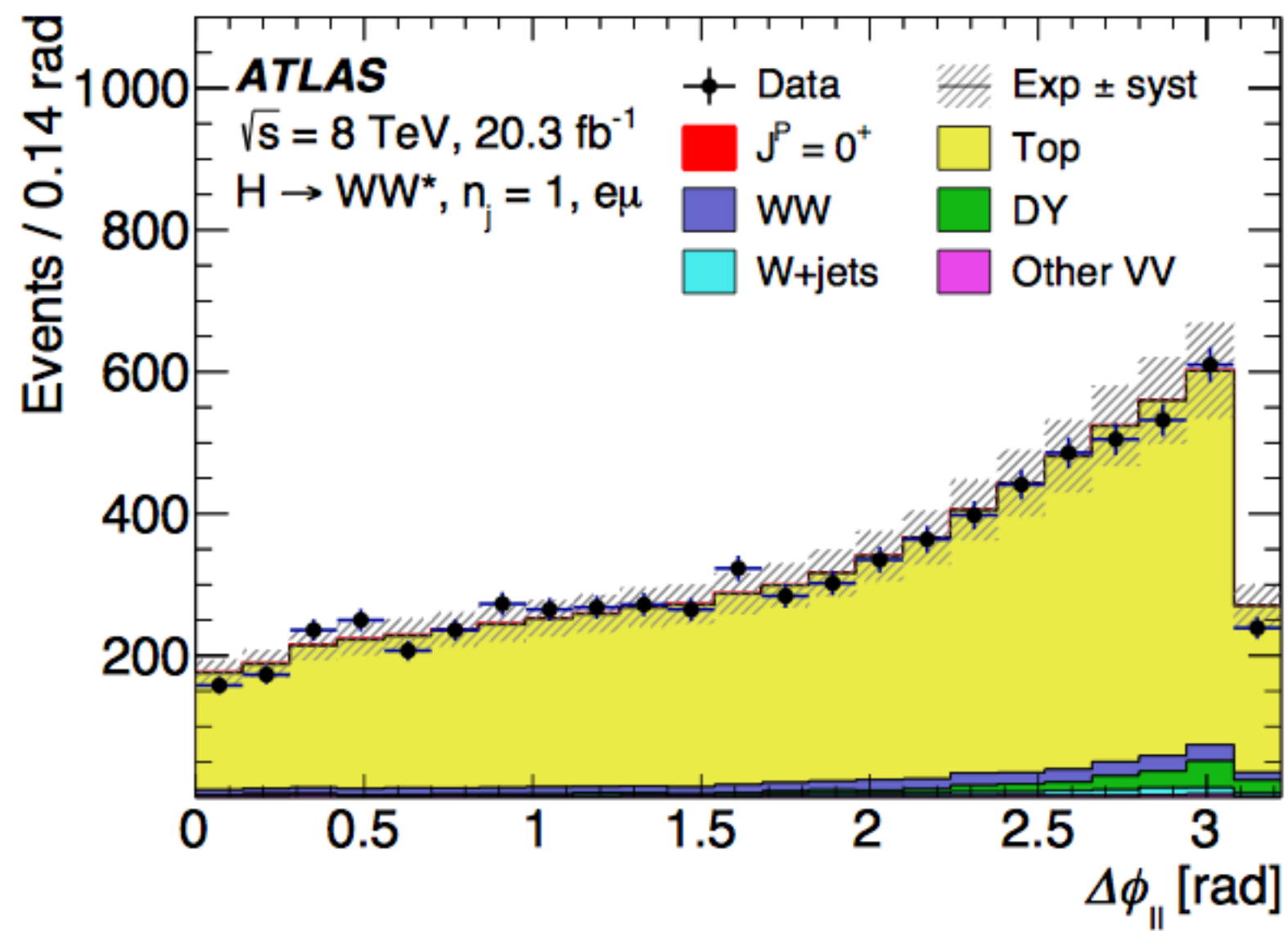


# Top CR

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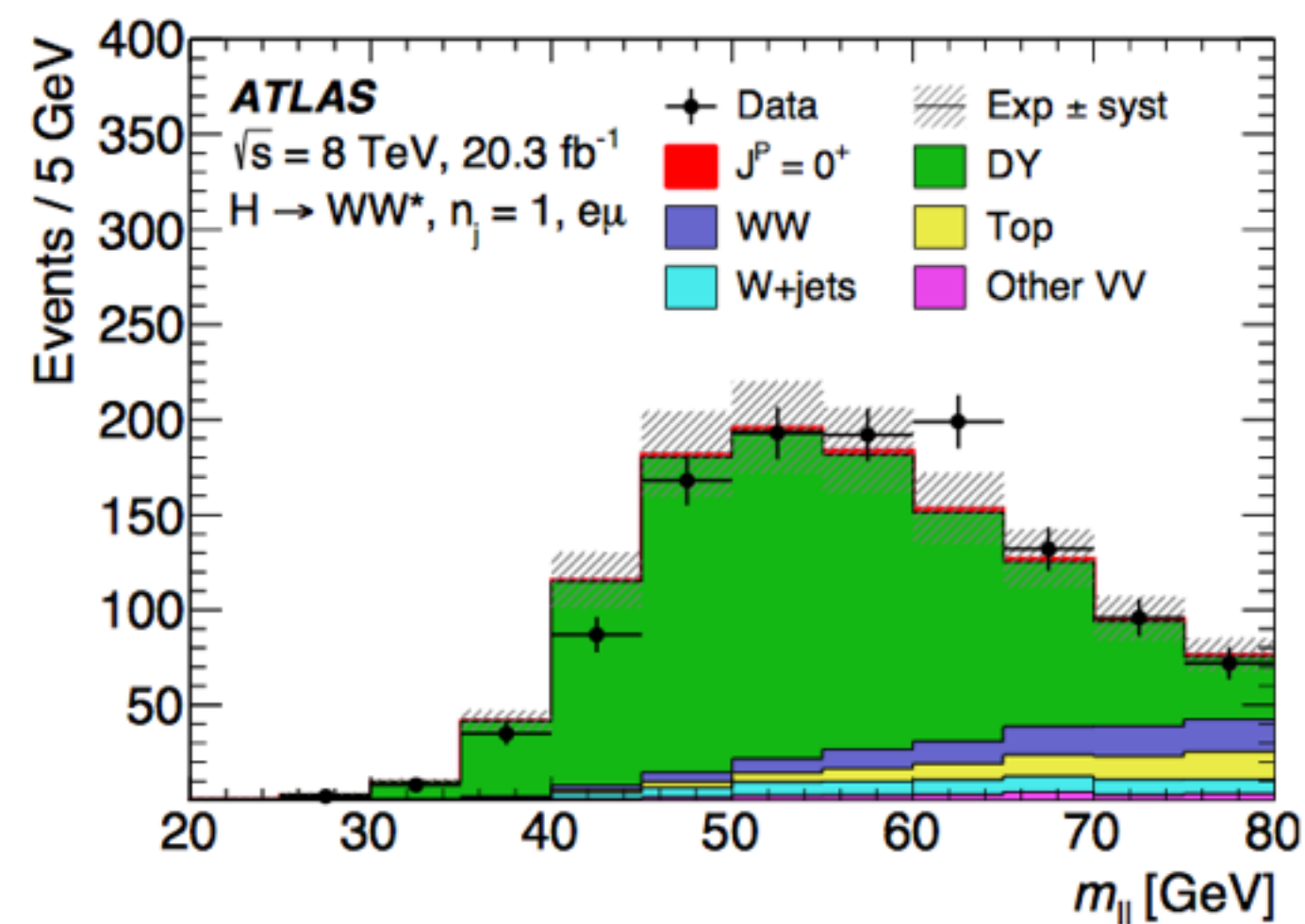
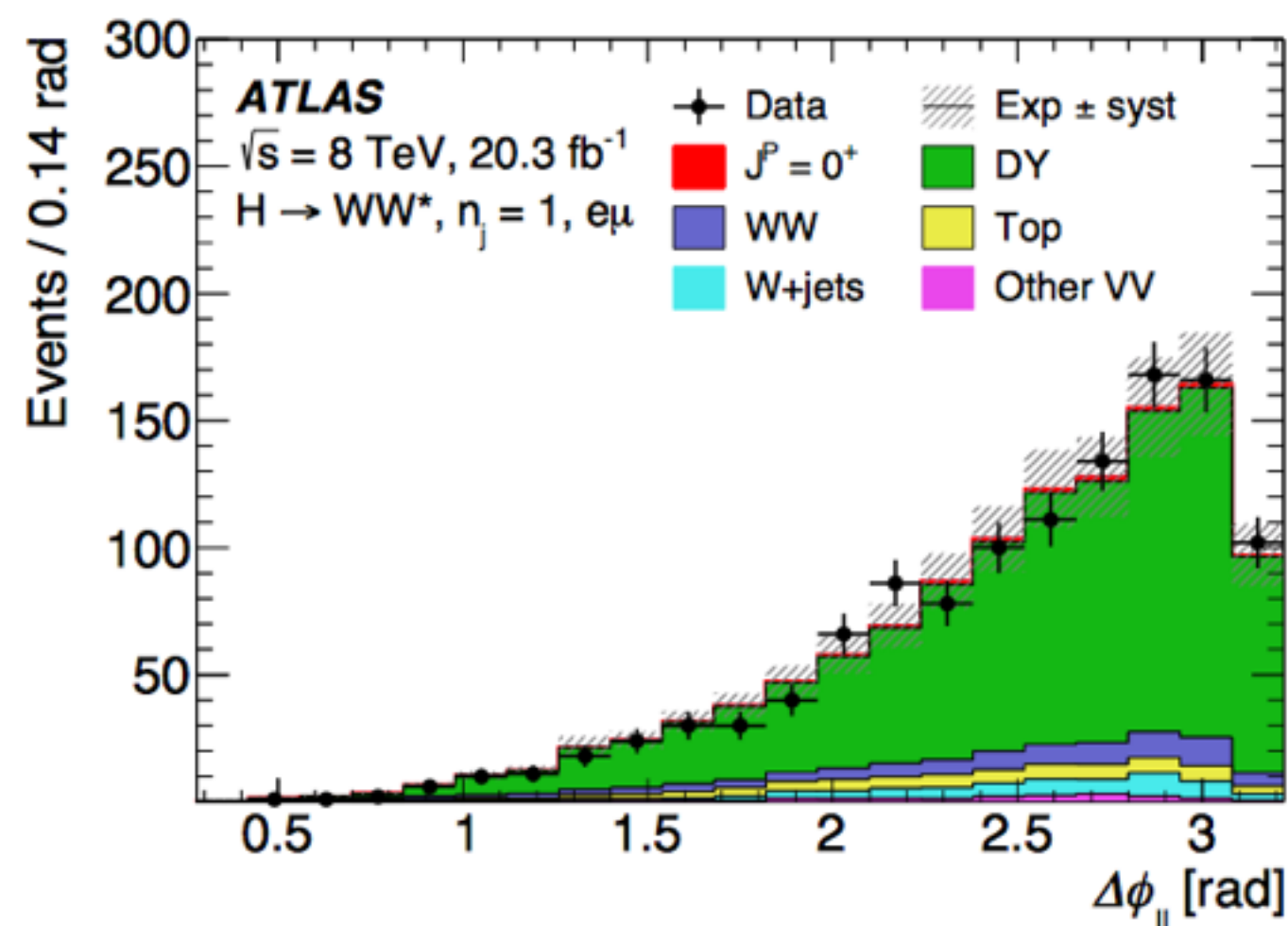
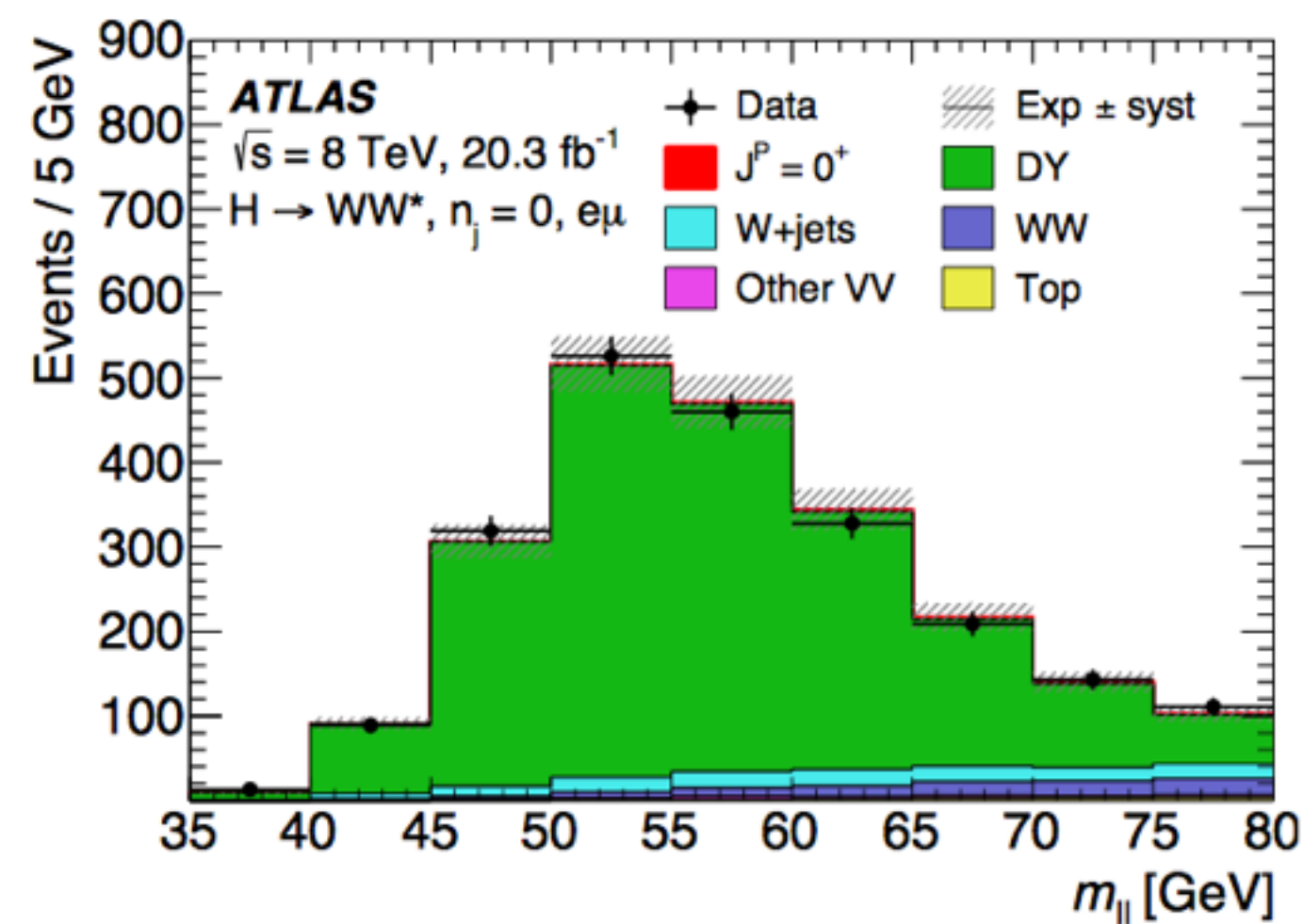
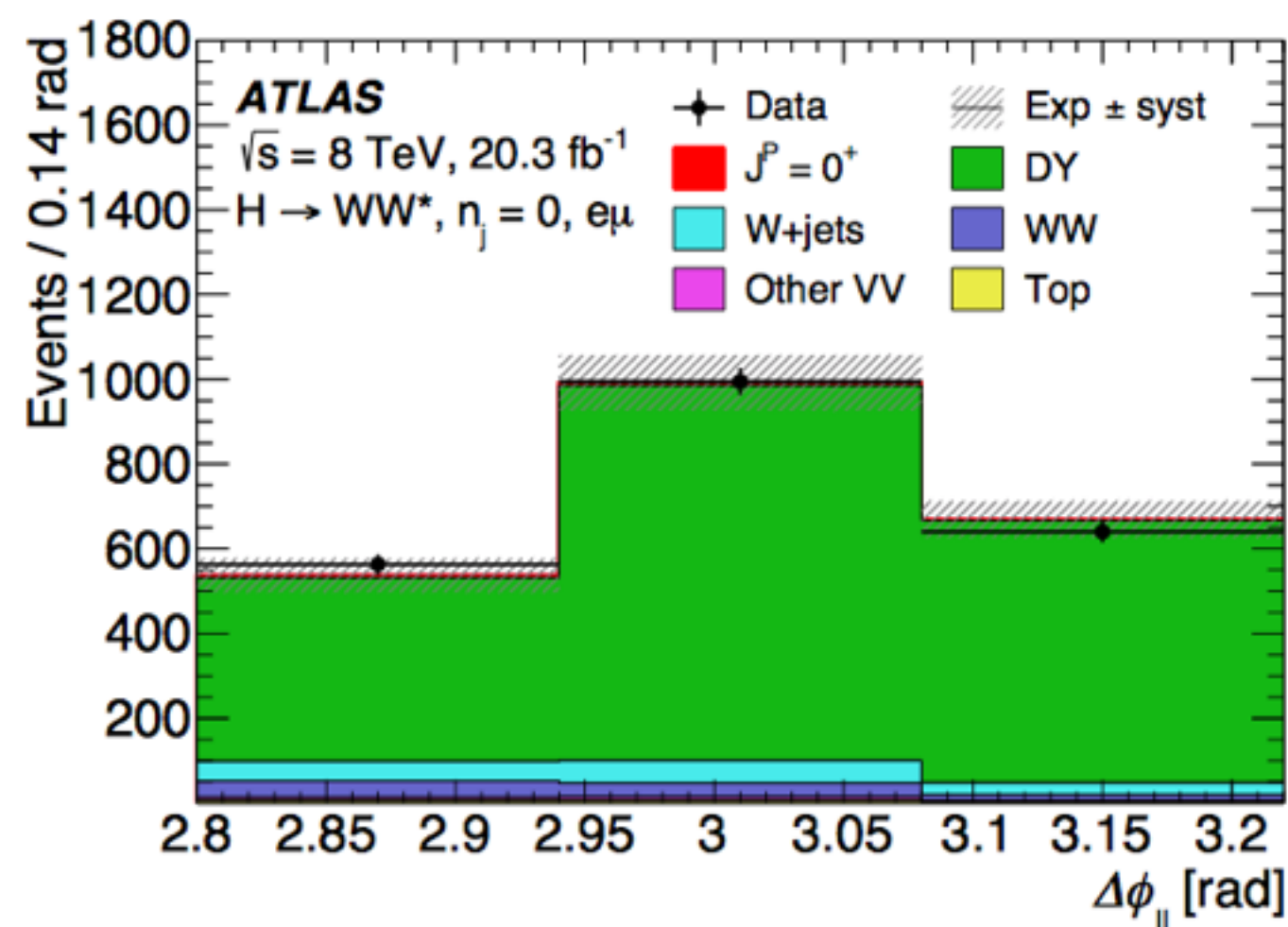


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# Z $\tau\tau$ CR



# Samples

Table 1: Monte Carlo samples used to model the signal and background processes. The corresponding cross-sections times branching fractions,  $\sigma \cdot \mathcal{B}$ , are quoted at  $\sqrt{s} = 8$  TeV. The branching fractions include the decays  $t \rightarrow Wb$ ,  $W \rightarrow \ell\nu$ , and  $Z \rightarrow \ell\ell$  (except for the process  $ZZ \rightarrow \ell\ell\nu\nu$ ). Here  $\ell$  refers to  $e$ ,  $\mu$ , or  $\tau$ . The neutral current  $Z/\gamma^* \rightarrow \ell\ell$  process is denoted  $Z$  or  $\gamma^*$ , depending on the mass of the produced lepton pair. The parameters  $\kappa_g$ ,  $\kappa_q$  are defined in Sect. 2.1.1, while  $\kappa_{SM}$ ,  $\kappa_{HWW}$ ,  $\kappa_{AWW}$ ,  $c_\alpha$  are defined in Sect. 2.2.1.

Process	MC generator	Filter	$\sigma \cdot \mathcal{B}$ (pb)
Signal samples used in $J^P = 2^+$ analysis			
SM $H \rightarrow WW^*$	POWHEG+PYTHIA8		0.435
$\kappa_g = \kappa_q$	MADGRAPH5_aMC@NLO+PYTHIA6		-
$\kappa_g = 1, \kappa_q = 0$	MADGRAPH5_aMC@NLO+PYTHIA6		-
$\kappa_g = 0.5, \kappa_q = 1$	MADGRAPH5_aMC@NLO+PYTHIA6		-
Signal samples used in CP-mixing analysis			
$c_\alpha = 0.3, \kappa_{SM} = 1$ $\kappa_{HWW} = 2, \kappa_{AWW} = 2$	MADGRAPH5_aMC@NLO+PYTHIA6		-
Background samples			
$WW$			
$q\bar{q} \rightarrow WW$ and $qg \rightarrow WW$	POWHEG+PYTHIA6		5.68
$gg \rightarrow WW$	GG2VV+HERWIG		0.196
Top quarks			
$t\bar{t}$	POWHEG+PYTHIA6		26.6
$Wt$	POWHEG+PYTHIA6		2.35
$tq\bar{b}$	ACERMC+PYTHIA6		28.4
$t\bar{b}$	POWHEG+PYTHIA6		1.82
Other dibosons (VV)			
$W\gamma$	ALPGEN+HERWIG	$p_T^\gamma > 8$ GeV	369
$W\gamma^*$	SHERPA	$m_{\ell\ell} \leq 7$ GeV	12.2
$WZ$	POWHEG+PYTHIA8	$m_{\ell\ell} > 7$ GeV	12.7
$Z\gamma$	SHERPA	$p_T^\gamma > 8$ GeV	163
$Z\gamma^*$	SHERPA	min. $m_{\ell\ell} \leq 4$ GeV	7.31
$ZZ$	POWHEG+PYTHIA8	$m_{\ell\ell} > 4$ GeV	0.733
$ZZ \rightarrow \ell\ell\nu\nu$	POWHEG+PYTHIA8	$m_{\ell\ell} > 4$ GeV	0.504
Drell –Yan			
$Z/\gamma^*$	ALPGEN+HERWIG	$m_{\ell\ell} > 10$ GeV	16500