

Imperial College
London

Inflationary GW: prospects [for] measurement in the near future

Andrew Jaffe

eLISA Cosmology 2015

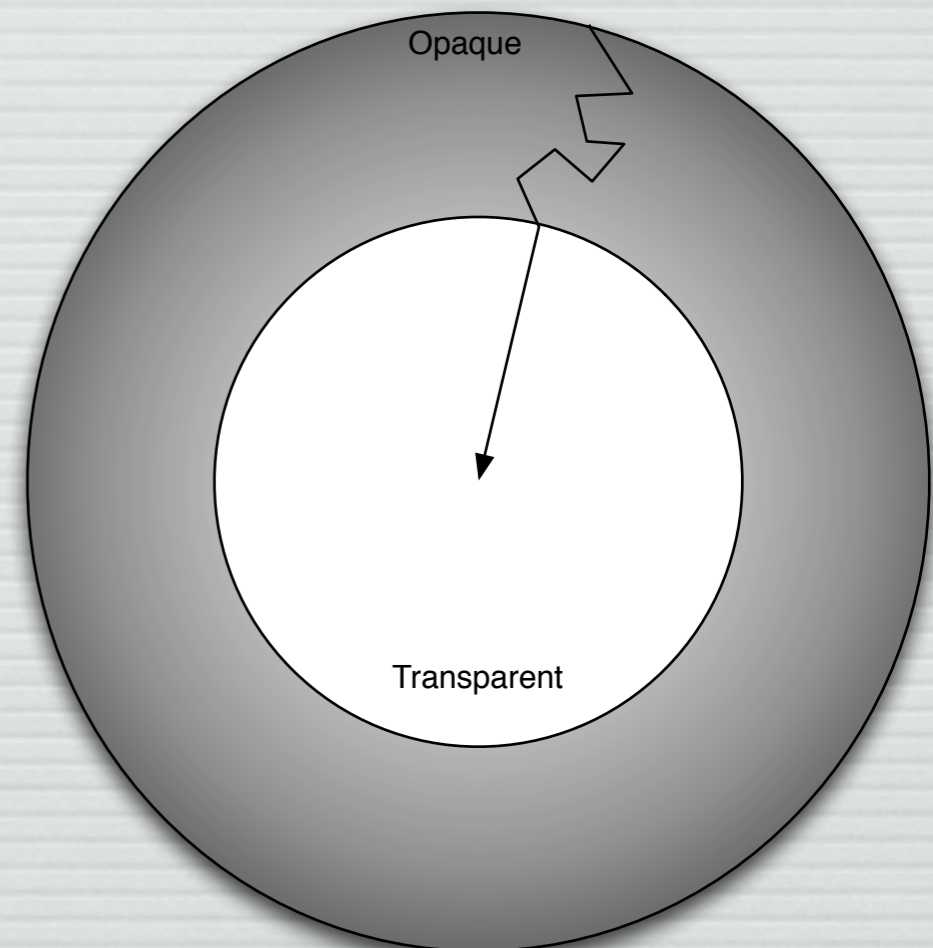
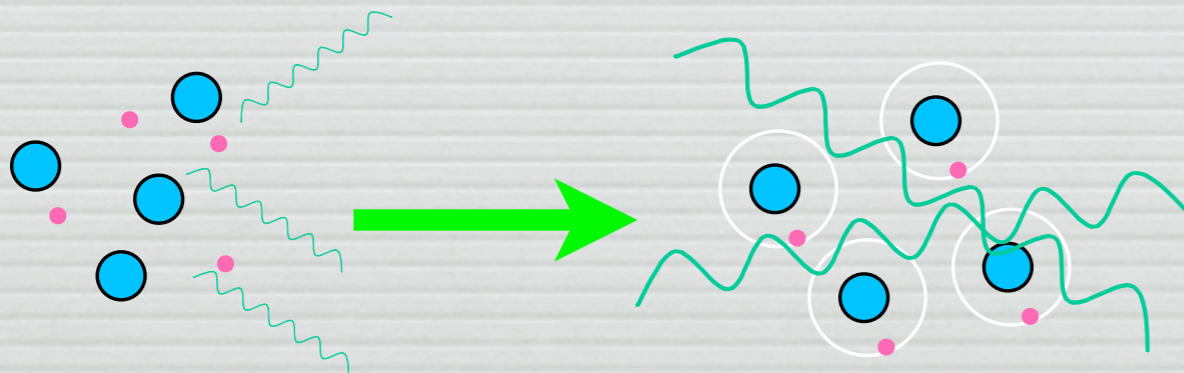
CERN

Inflationary GW: prospects for measurement in the near future

- Background: polarization and gravitational radiation
- State of the art: Planck, BICEP, Polarbear, etc.
- The next generation
- The next decade
- Beyond detection: characterising inflation

Evidence & Observations: Cosmic Microwave Background

- 400,000 years after the Big Bang, the temperature of the Universe was $T \sim 3,000$ K
- Hot enough to keep hydrogen atoms *ionized* until this time
 - *proton + electron* \rightarrow *Hydrogen* + *photon* [$p^+ + e^- \rightarrow H + \gamma$]
 - *charged plasma* \rightarrow *neutral gas*
- depends on *entropy* of the Universe
- Photons (light) can't travel far in the presence of charged particles
 - *Opaque* \rightarrow *transparent*

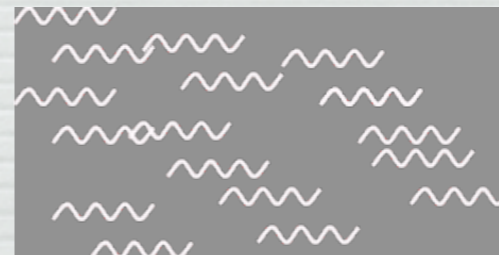


What affects the CMB temperature?

$$\frac{\Delta T}{T}(\hat{\mathbf{x}}) \simeq \frac{1}{4} \frac{\delta \rho_\gamma}{\rho_\gamma} + \mathbf{v} \cdot \hat{\mathbf{x}} + \int_{\eta_{rec}}^{\eta_0} d\eta \dot{h}_{ij} \hat{x}_i \hat{x}_j$$

- Initial temperature (density) of the photons

Cooler



Hotter

- Doppler shift due to movement of baryon-photon plasma
- Gravitational red/blue-shift as photons climb out of potential wells or fall off of overdensities



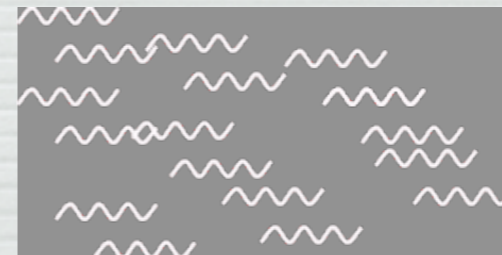
- Photon path from LSS to today
- All linked by initial conditions $\Rightarrow 10^{-5}$ fluctuations

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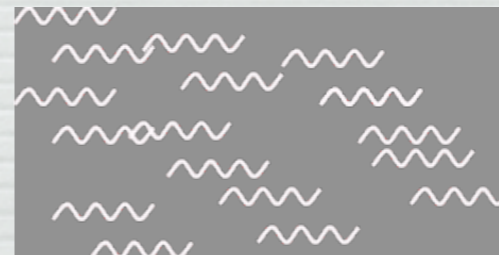
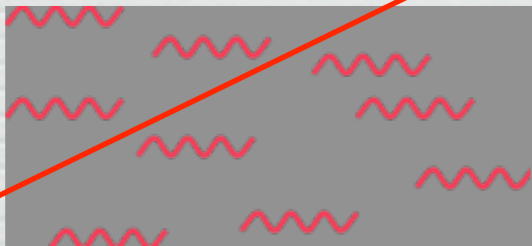
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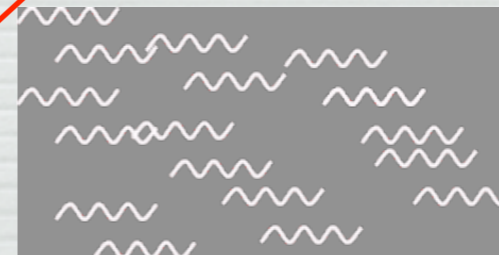
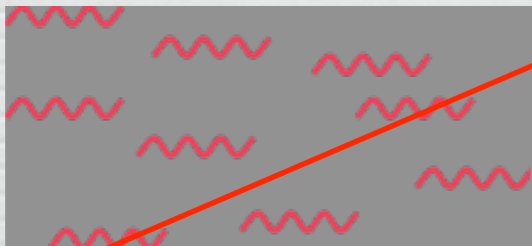
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CMB Statistics

$z \sim 1300$: $p+e \rightarrow H$ & Universe becomes transparent.

$$\frac{T(\hat{x}) - \bar{T}}{\bar{T}} \equiv \frac{\Delta T}{T}(\hat{x}) = \sum_{\ell m} a_{\ell m} Y_{\ell m}(\hat{x})$$

i.e., Fourier Transform, but on a sphere

Determined by **temperature**, **velocity** and **metric** on the **last scattering surface**.

Power Spectrum:

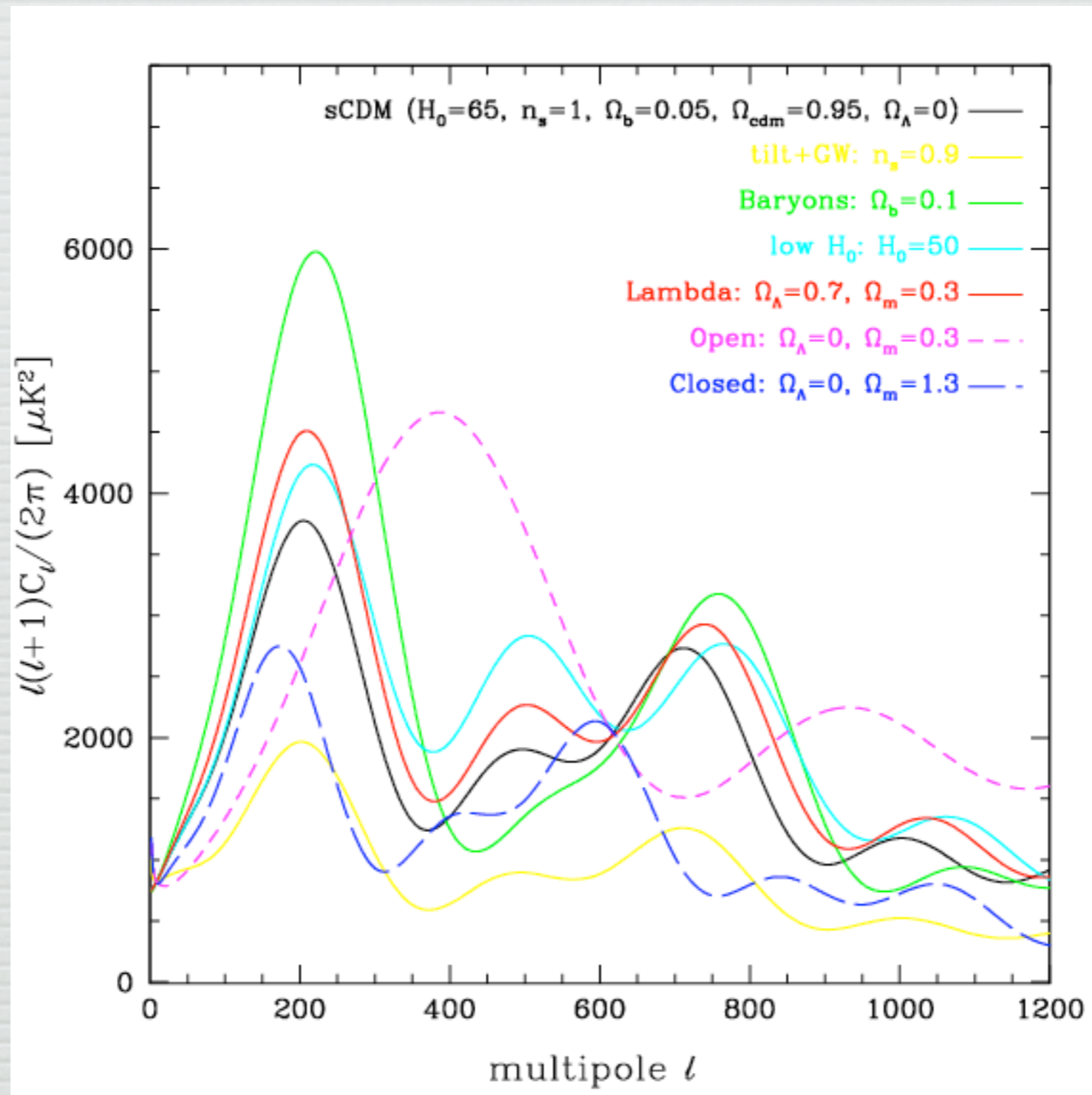
$$\langle a_{\ell m}^* a_{\ell' m'} \rangle = \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

Multipole $\ell \sim$ angular scale $180^\circ/\ell$

For a **Gaussian** theory, C_{ℓ} completely determines the statistics of the temperature.

Theoretical Predictions

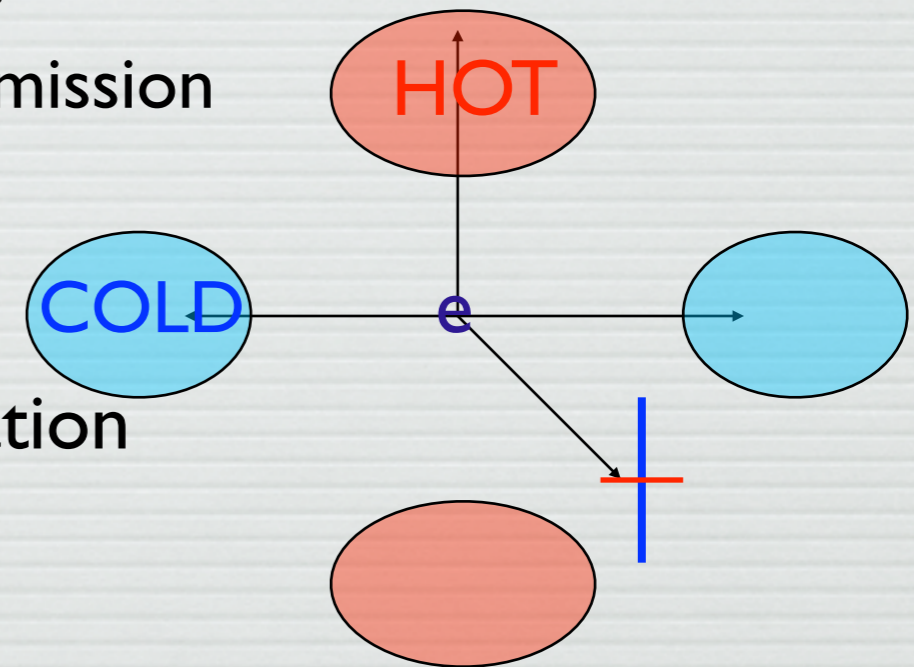
Mean square fluctuation amplitude



$\sim 180^\circ/\text{Angular scale}$

CMB Polarization: Generation

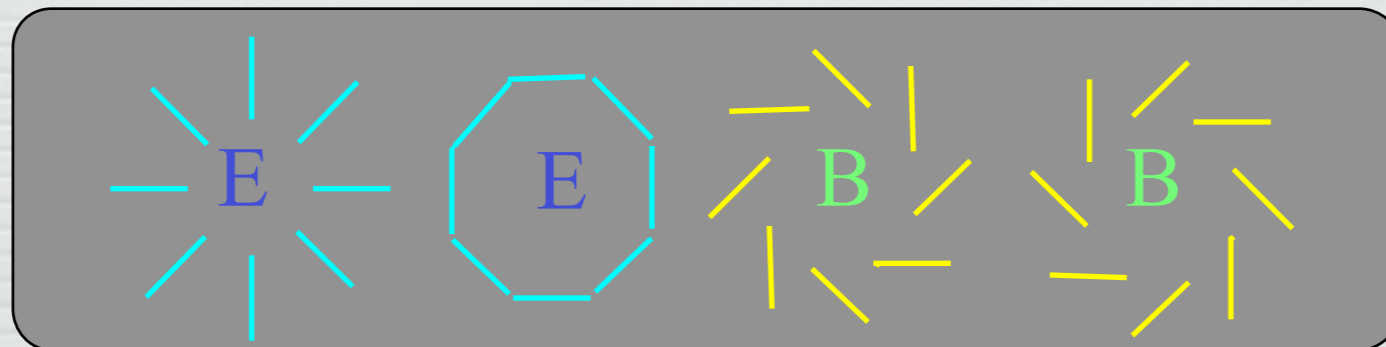
- **Ionized** plasma + **quadrupole** radiation field:
 - Thomson scattering \Rightarrow [linearly] **polarized** emission



- Unlike intensity, only generated when ionization fraction, $0 < x < 1$ (i.e., during transition)
- **Scalar** perturbations: traces \sim gradient of velocity
 - same initial conditions as temperature and density fluctuations
- **Tensor** perturbations: independent of density fluctuations
 - +, × patterns of quadrupoles (**impossible to form via linear scalar perturbations**)
 - at last-scattering, from primordial background of gravitational radiation, *predicted by inflation*

CMB Polarization: E/B Decomposition

- 2-d (headless) vector field on a sphere
- Spin-2/tensor spherical harmonics
- grad/scalar/E + curl/pseudoscalar/B patterns



- NB. From polarization pattern \Rightarrow E/B decomposition requires integration (*non-local*) or differentiation (*noisy*)
 - *Lewis et al; Bunn et al; Smith & Zaldarriaga; Grain et al; Bowyer & Aj; ...*
 - (data analysis problems)

E/B decomposition: the math

- Scalar and tensor modes are isotropic, parity-symmetric fields on the sky.
- T is a scalar, E is the “gradient” of a scalar, B is the “curl” of a pseudoscalar

$$Q(\hat{n}) = -\frac{1}{2} \sum_{lm} (a_{lm}^E [{}_2Y_{lm}(\hat{n}) + {}_{-2}Y_{lm}(\hat{n})] + ia_{lm}^B [{}_2Y_{lm}(\hat{n}) - {}_{-2}Y_{lm}(\hat{n})])$$

*Spin-weighted
spherical harmonics*

$$U(\hat{n}) = -\frac{1}{2} \sum_{lm} (a_{lm}^B [{}_2Y_{lm}(\hat{n}) + {}_{-2}Y_{lm}(\hat{n})] + ia_{lm}^E [{}_2Y_{lm}(\hat{n}) - {}_{-2}Y_{lm}(\hat{n})])$$

$$e(\hat{n}) = \sum_{lm} \sqrt{\frac{(l-2)!}{(l+2)!}} a_{lm}^E Y_{lm}(\hat{n}) \quad b(\hat{n}) = \sum_{lm} \sqrt{\frac{(l-2)!}{(l+2)!}} a_{lm}^B Y_{lm}(\hat{n})$$

*Newman-Penrose
derivative*

$$\nabla^4 e = -\frac{1}{2} [\bar{\delta}^2(Q + iU) + \delta^2(Q - iU)] \quad \nabla^4 b = \frac{i}{2} [\bar{\delta}^2(Q + iU) - \delta^2(Q - iU)]$$

- everything **except scalar perturbations** sources B
- parity: expect $\langle EB \rangle = \langle TB \rangle = 0$
- try to measure $\langle TT \rangle, \langle BB \rangle, \langle EE \rangle, \langle TE \rangle$

Gravitational Radiation from Inflation

- Gravitational radiation produced during **inflation**
- Characterized by ratio of amplitudes of tensor perturbation power (GWs) to scalar power (density), $r = T/S$
 - \Rightarrow Energy scale of inflation: $V^{1/4} / M_{Pl} \approx 3 \times 10^{-3} r^{1/4}$
- Contributes to *all* CMB power spectra (T, E, B)
- In single-field, “slow-roll” models, r is further related to the scalar and tensor spectral indices:
 - $P_t(k) \propto k^{n_t}$ $P_s(k) \propto k^{1-n_s}$

Models of inflation

□ Scalar & tensor spectra:

$$\mathcal{P}_{\mathcal{R}}(k) = A_s \left(\frac{k}{k_*} \right)^{n_s - 1 + \frac{1}{2} \frac{dn_s}{d \ln k} \ln(k/k_*) + \frac{1}{6} \frac{d^2 n_s}{d \ln k^2} (\ln(k/k_*))^2 + \dots}$$

$$\mathcal{P}_t(k) = A_t \left(\frac{k}{k_*} \right)^{n_t + \frac{1}{2} \frac{dn_t}{d \ln k} \ln(k/k_*) + \dots}$$

■ Energy scale of inflation $V^{1/4} / M_{pl} \approx 3 \times 10^{-3} r^{1/4}$

□ Single-field Slow-roll

$$\epsilon_V = \frac{M_{pl}^2 V_{,\phi}^2}{2V^2} \ll 1 \quad \eta_V = \frac{M_{pl}^2 V_{,\phi\phi}}{V} \quad |\eta_V| \ll 1$$

$$n_s - 1 \approx 2\eta_V - 6\epsilon_V,$$

$$n_t \approx -2\epsilon_V,$$

$$\frac{dn_s}{d \ln k} \approx +16\epsilon_V \eta_V - 24\epsilon_V^2 - 2\xi_V^2,$$

$$\frac{dn_t}{d \ln k} \approx +4\epsilon_V \eta_V - 8\epsilon_V^2,$$

$$A_s \approx \frac{V}{24\pi^2 M_{pl}^4 \epsilon_V}, \quad (\text{measured by } C_\ell)$$

$$A_t \approx \frac{2V}{3\pi^2 M_{pl}^4},$$

■ Consistency: $r = \frac{A_t}{A_s} \approx 16\epsilon_V \approx -8n_t$

□ Beyond slow-roll: model-dependent

- large derivatives of V
- multiple fields
- non Bunch-Davies vacuum
- non-standard kinetic term
- not inflation: pre-BB, string gas, ...

(Also, GWs from preheating, etc—see Arttu's, Enrico's, ... talks)

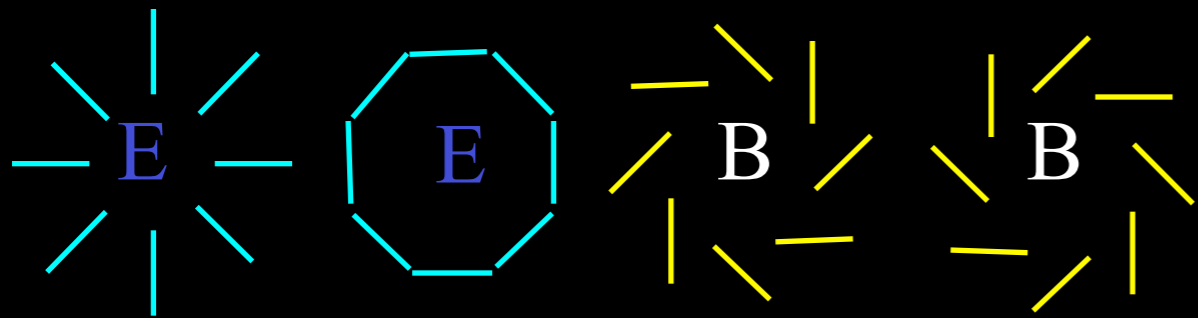
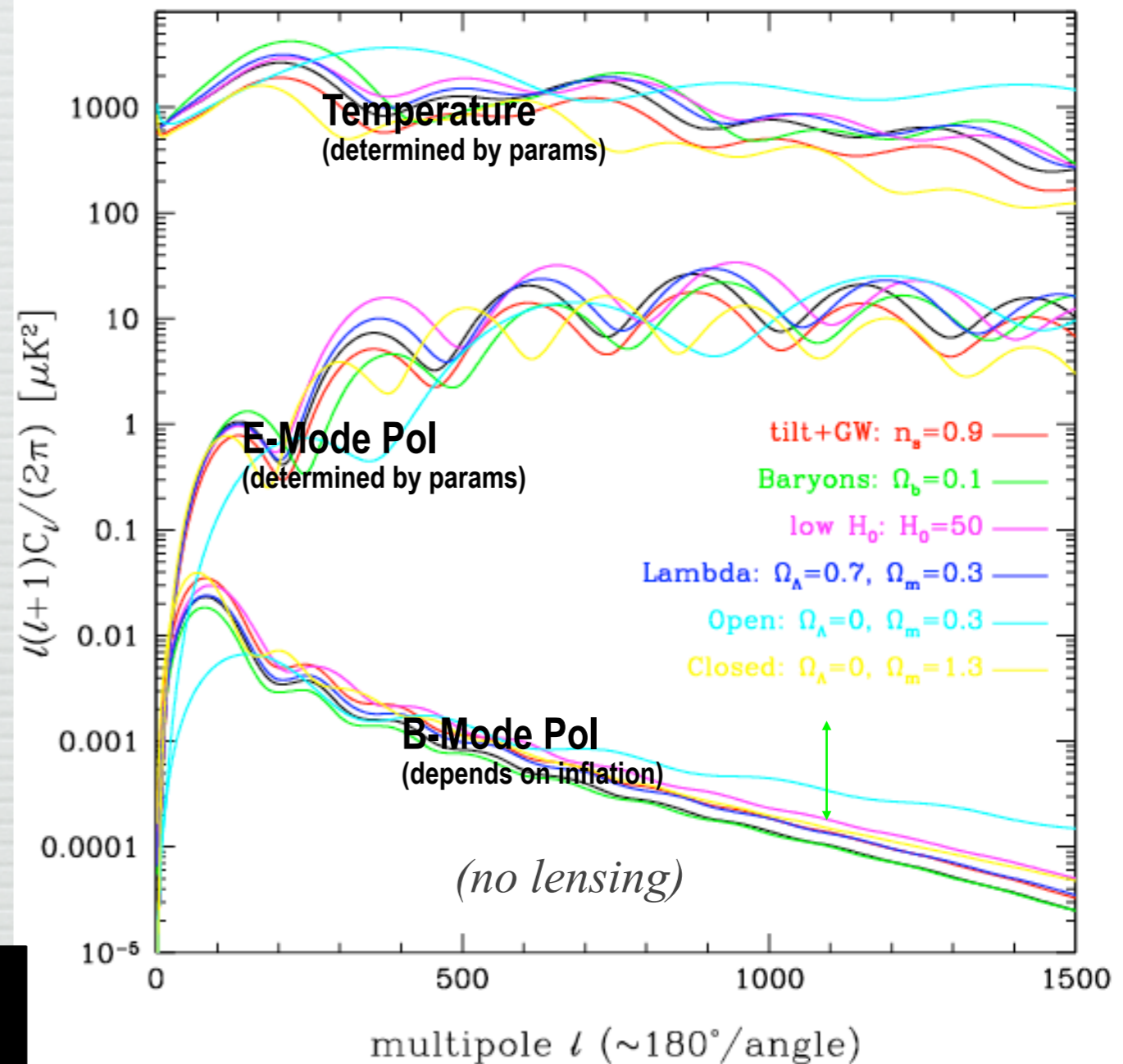
¹List of available inflation models – non exhaustive : eternal inflation, hybrid inflation, chaotic, Ghost inflation, Tilted Ghost inflation, DBI inflation, brane inflation, N-flation, bubble inflation, extended inflation, false vacuum inflation, power law inflation, k-inflation, hyperextended inflation, supersymmetric inflation, Quintessential inflation, Natural inflation, Super inflation, Supernatural inflation, D-term inflation, B -inflation, Thermal inflation, discrete inflation, Assisted inflation, Polar cap inflation, Open inflation, Topological inflation, Double inflation, Multiple inflation, Induced-gravity inflation, Warm inflation, stochastic inflation, Generalized assisted inflation, self-sustained inflation, Graduated inflation, Local inflation, Singular inflation, Slinky inflation, locked inflation, Elastic inflation, Mixed inflation, Phantom inflation, Boundary inflation, Non-commutative inflation, Tachyonic inflation, Tsunami inflation, Lambda inflation, Steep inflation, Oscillating inflation, Mutated Hybrid inflation, intermediate inflation, Inhomogeneous inflation.

CMB Signals from inflation

- Want to probe **inflaton potential** $V(\varphi)$
- Induce scalar and tensor power spectra
 - Observables:
 - temperature and polarization CMB spectra
 - functionally linear relationships
$$C_\ell^{BB} = \int dk T_\ell^{hB}(k) P_h(k)$$
$$C_\ell^{TT} = \int dk [T_\ell^{hT}(k) P_h(k) + T_\ell^{RT}(k) P_R(k)]$$
 - Transfer functions T depend on cosmological parameters
 - Amplitude ($r=T/S$) and shape (n_s, n_T) of the spectra probe the inflaton potential
- Non-gaussianity:
 - specific inflationary models \Rightarrow departures from Gaussianity
 - e.g., $f_{NL} \sim 1$ (in reach of Planck, but not [yet] detected)

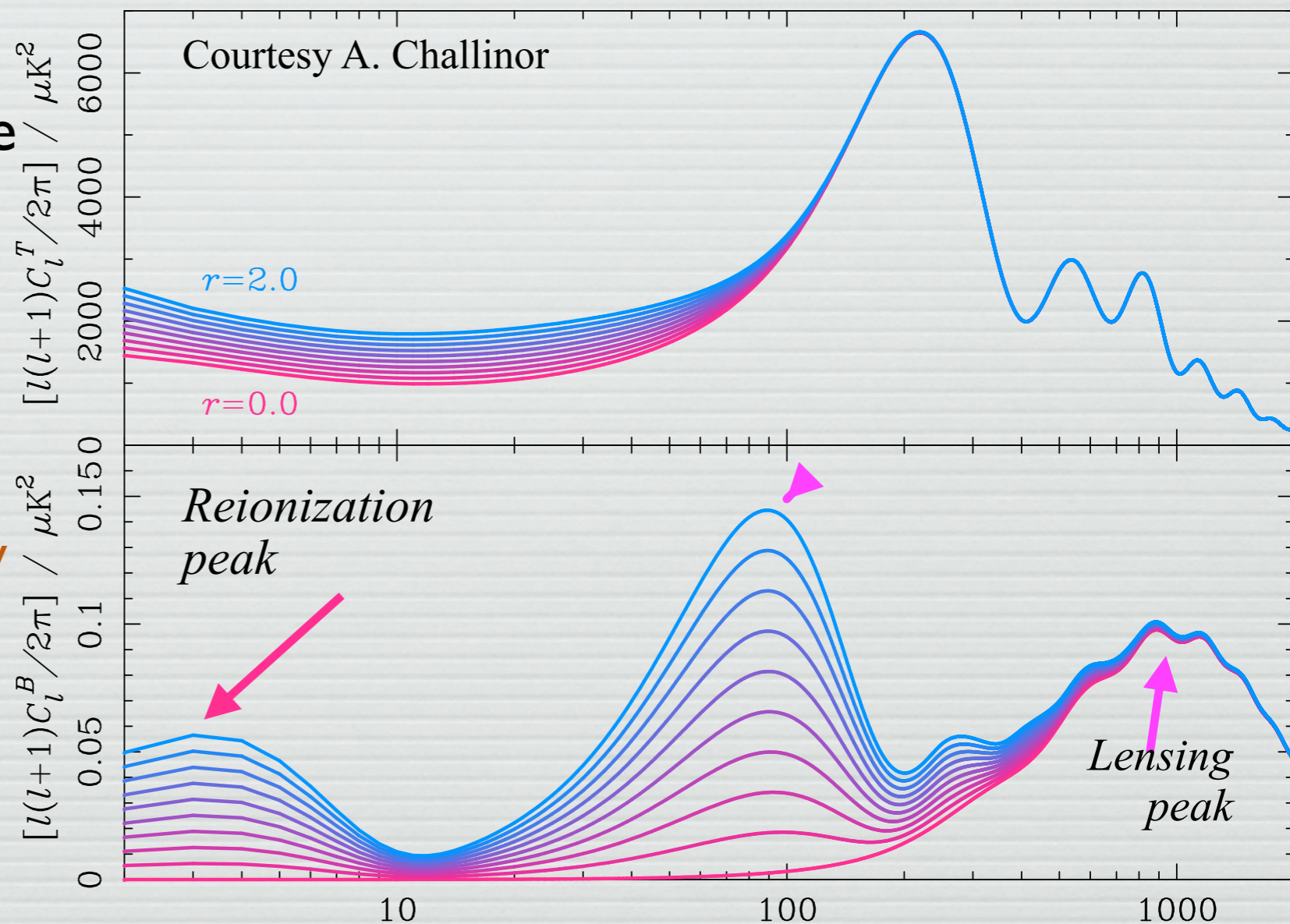
The Polarization of the CMB

- Anisotropic radiation field at **last scattering** → polarization
- “Grad” or *E* mode
 - Breaks degeneracies
 - New parameters:
 - reionization
- “Curl” or *B* sensitive to **gravity waves**
 - “Smoking gun” of inflation?
 - Very low amplitude
- Need [better] handle on
 - systematics,
 - lensing
 - polarized foregrounds



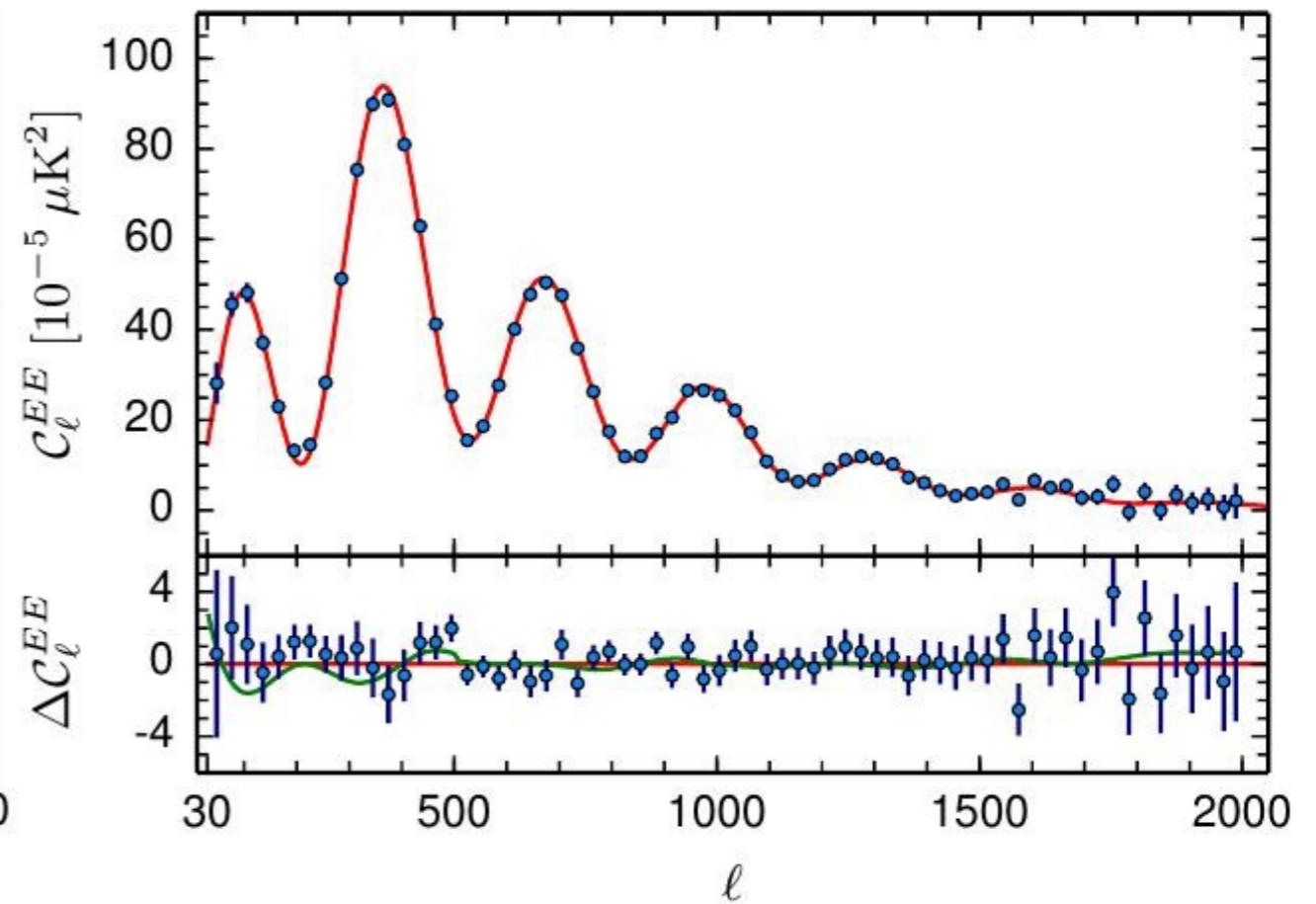
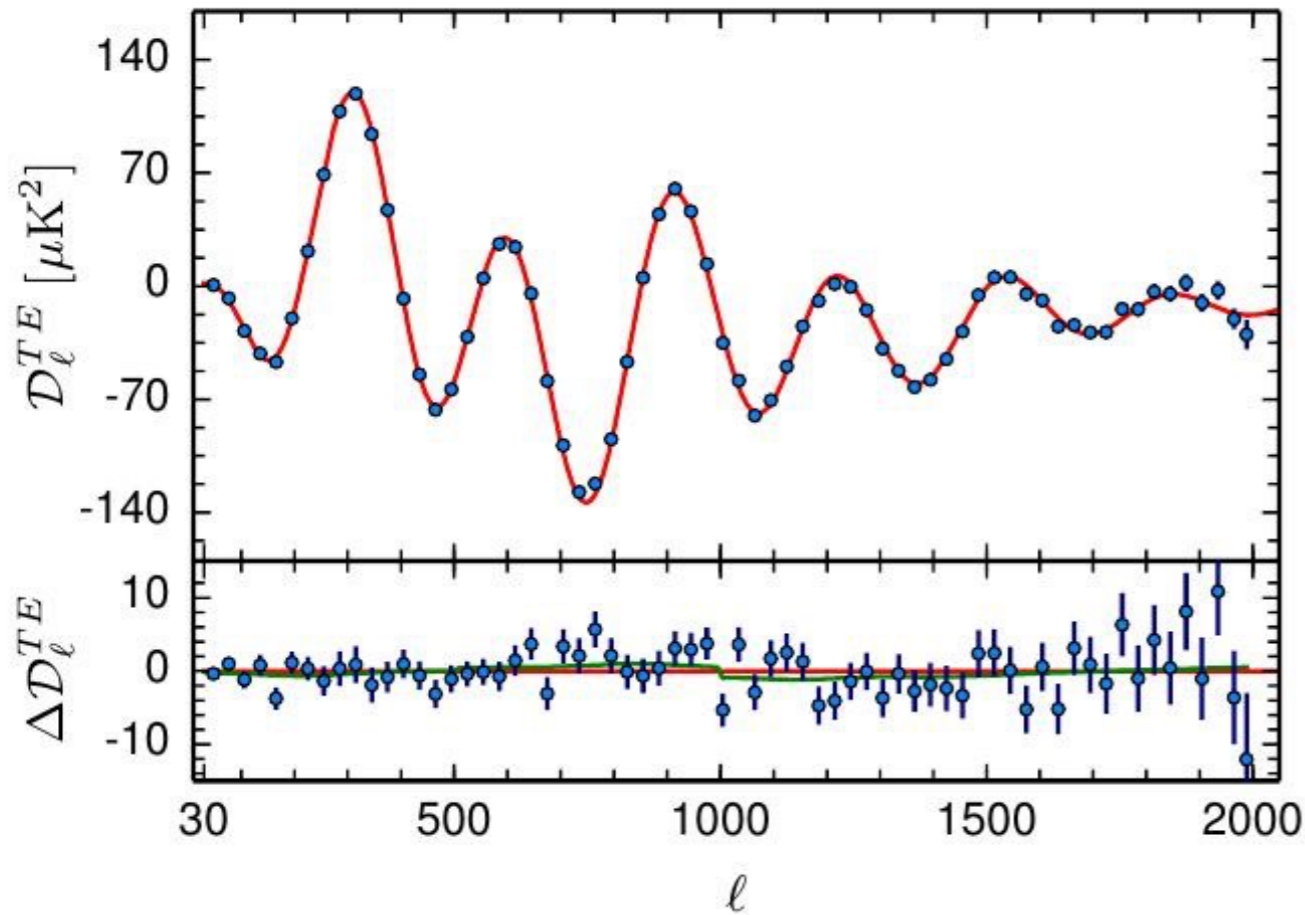
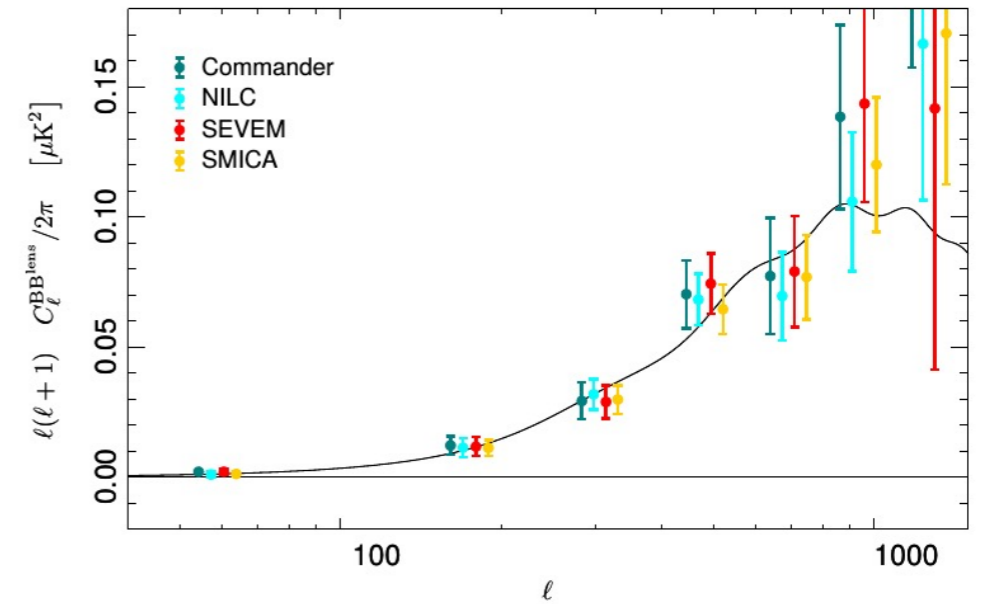
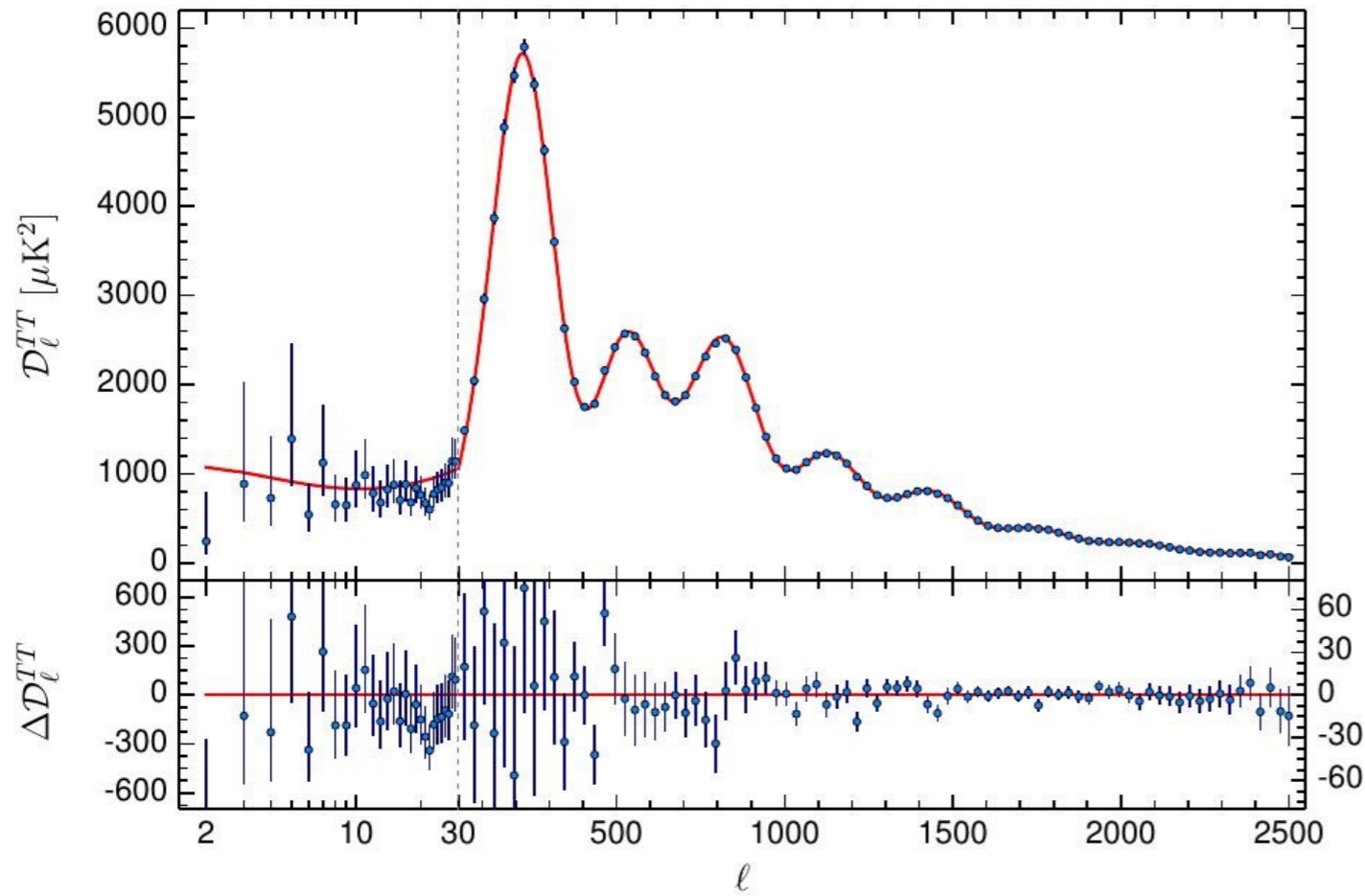
Gravitational Radiation & CMB

- Last scattering: “direct” effect of **tensor modes** (primordial GWs) on the primordial plasma
- inflationary potential
- dominated by *lensing of $E \Rightarrow B$* for $\ell \gtrsim 200$
- [sensitive to $m_\nu \lesssim 0.06\text{eV}$ (i.e., hot dark matter)]
- Reionization peak $\ell \lesssim 20$
- need \sim full-sky. Difficult for single suborbital experiments
- Planck 2015: $\tau \approx 0.07$ — low
- *Limits depend on full set of parameters*



Suborbital experiments target $\ell \sim 100$ peak: kilopixel telescopes give order-of-magnitude increase in sensitivity over Planck

Planck 2015

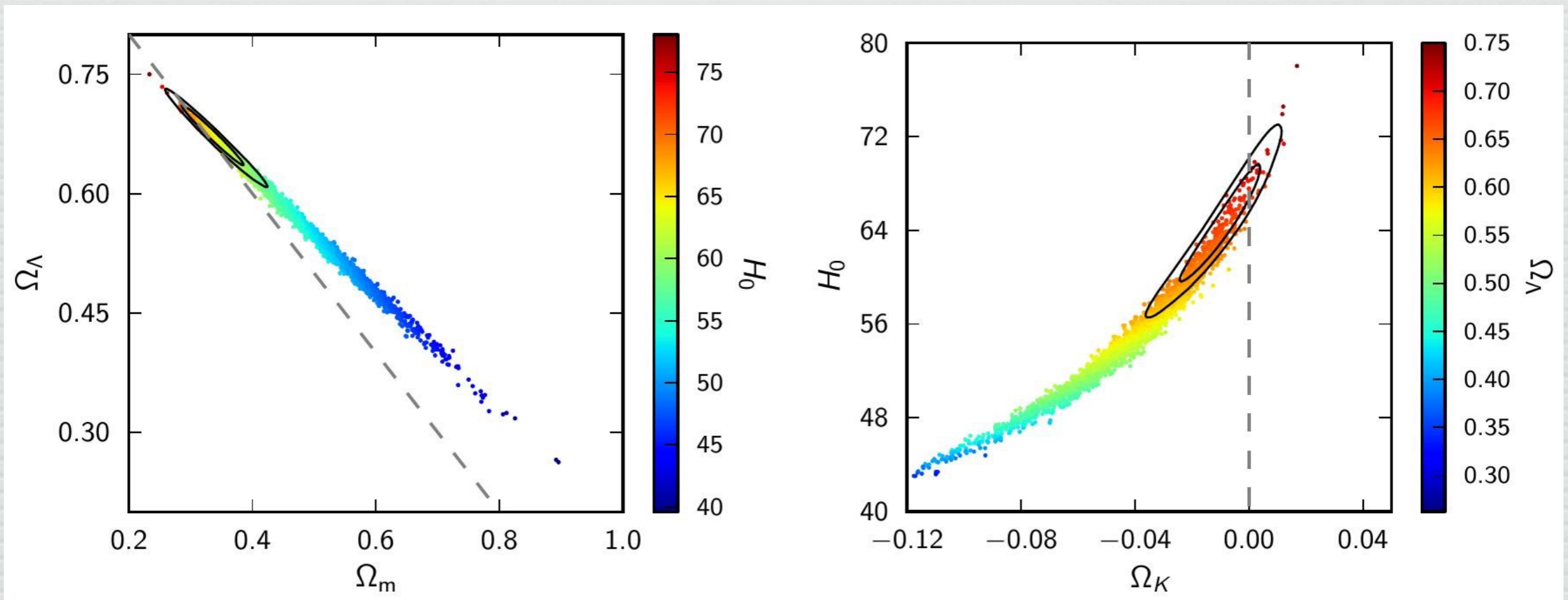


Planck 2015-2016

- **2015** data release
 - To be completed ~June 2015 (with likelihood code)
 - Temperature: all
 - Polarization: full high- ℓ data, only 70 GHz low- ℓ
 - polarization is hard: differencing sensitive to detector drifts (low-frequency noise/systematics)
 - temperature remains baseline
- **2016** data release
 - full-mission temperature and polarization
 - better measurements of τ , reionization history

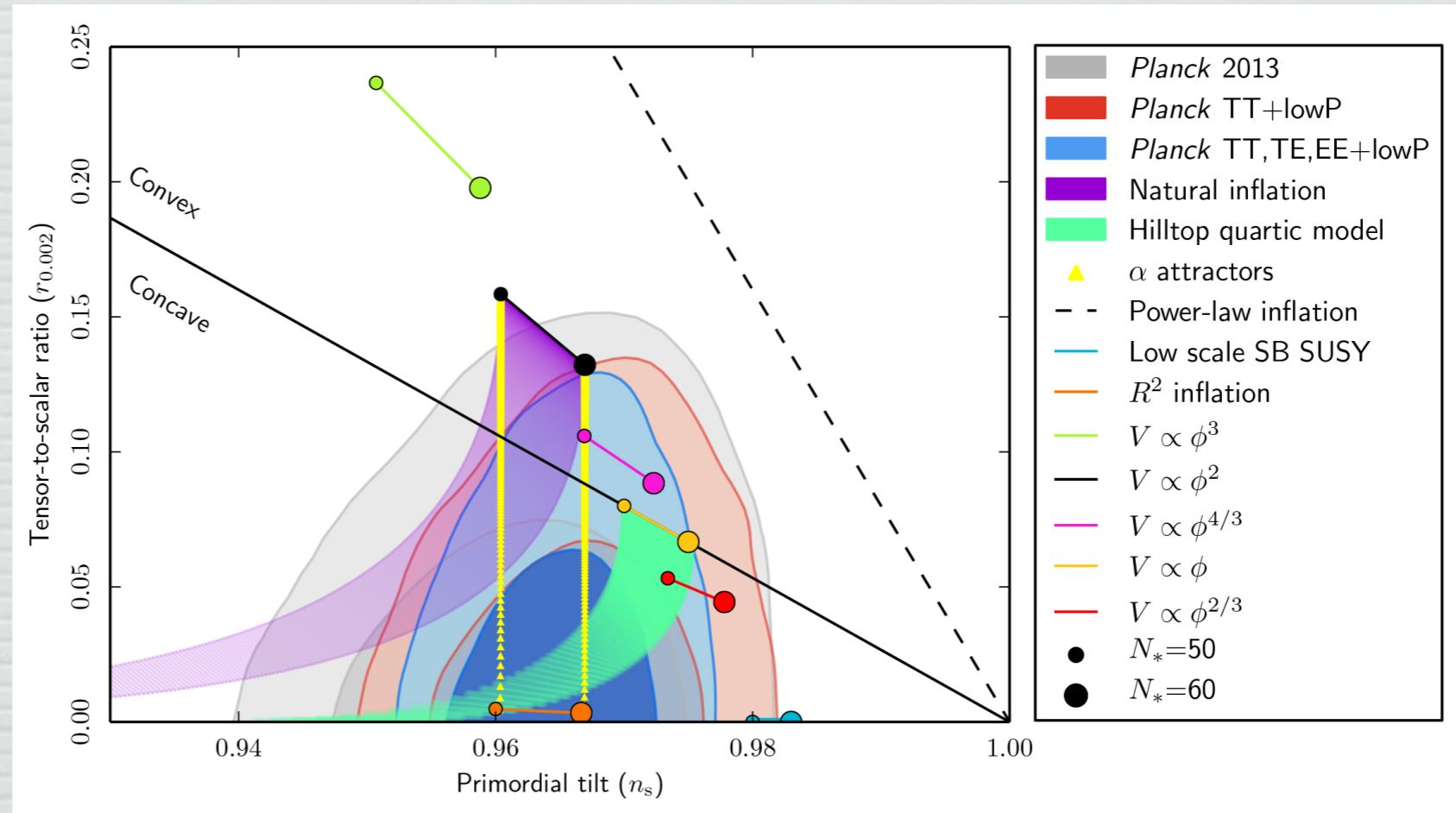
Evidence for inflation?

- A flat universe



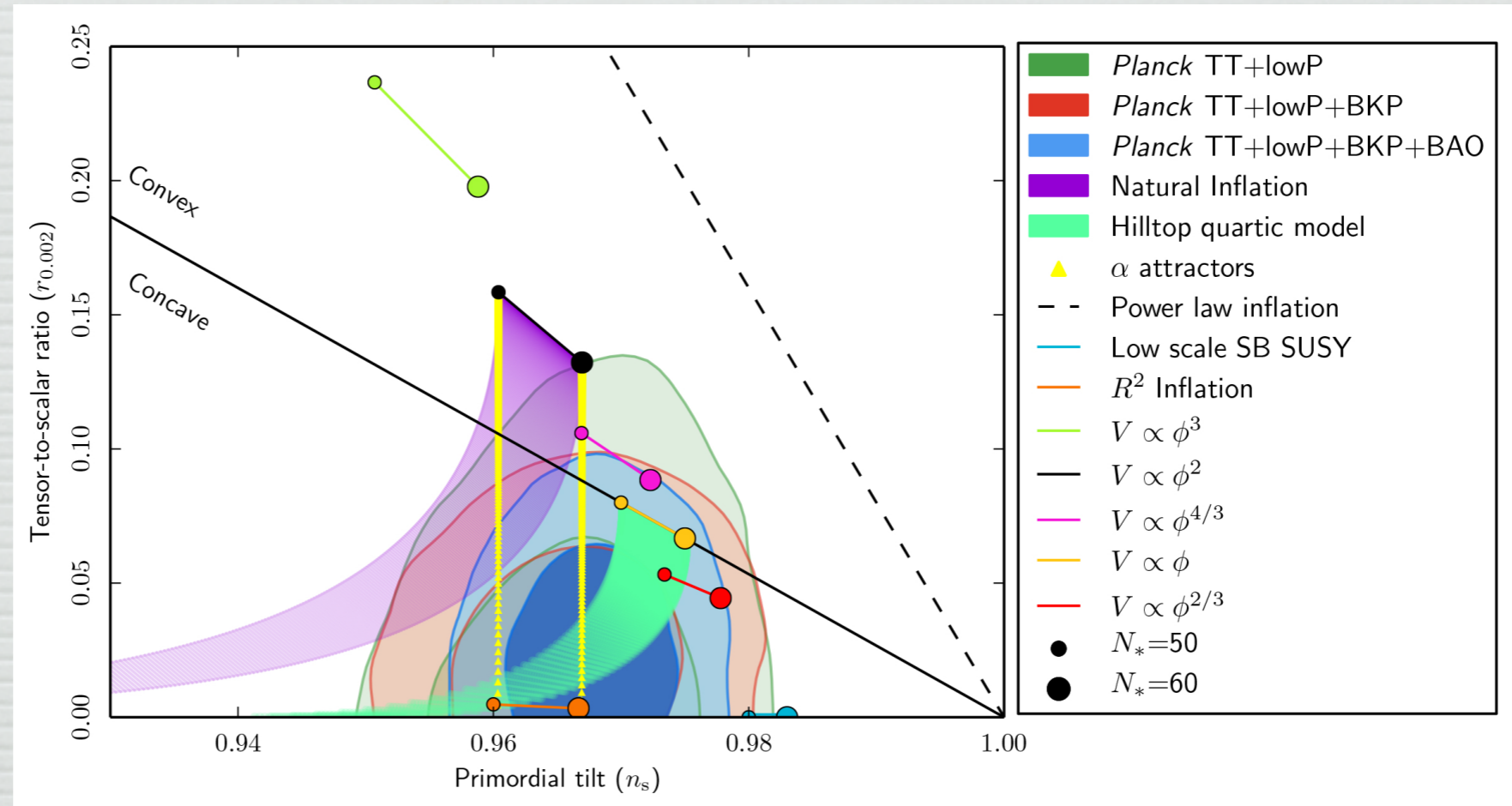
Inflation: Models

- Slightly redder than scale-invariant ($n_s \approx 1$)
- Simplest models: scalar field ϕ w/very flat potential $V(\phi)$
- *Planck* constrains specific models of inflation
- **No evidence** of gravitational radiation in the early universe



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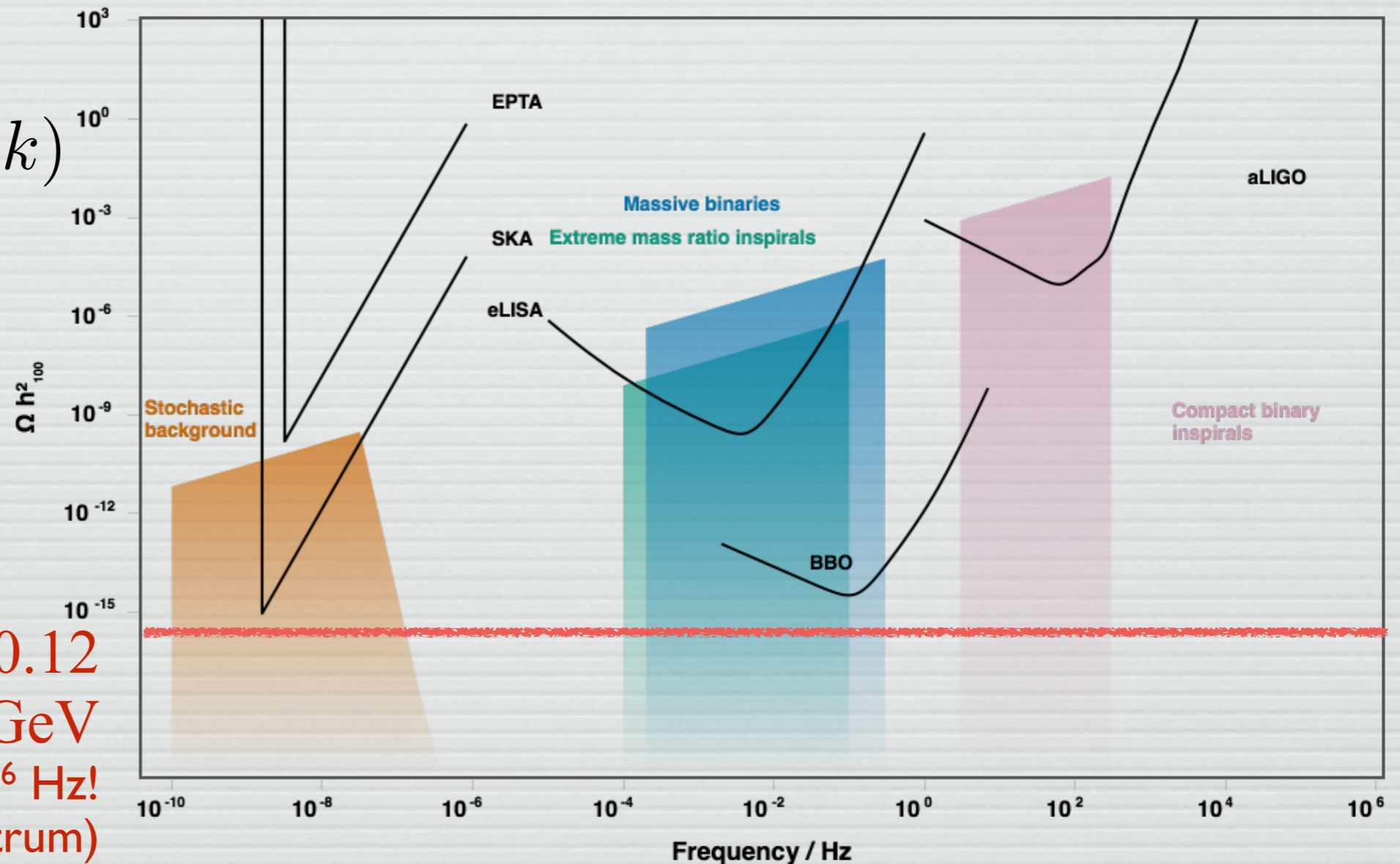
From low frequency to high: Future and Current limits

$$\Omega_{\text{GW}}(k) \propto P_t(k)$$

$$\propto V$$

$$\propto r$$

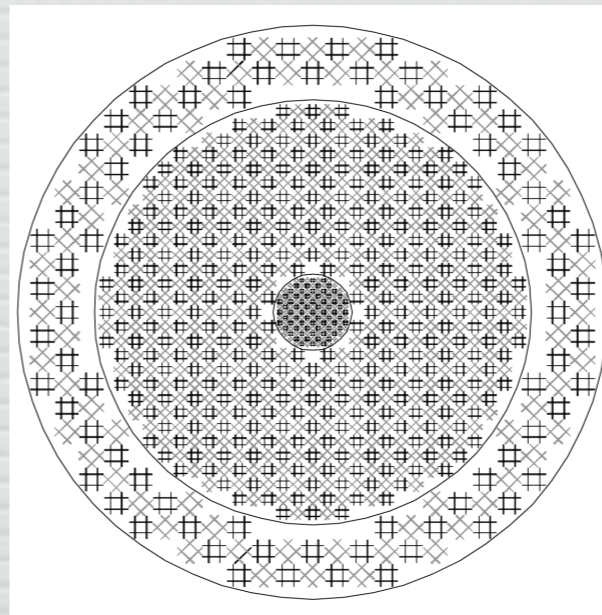
current CMB: $r < 0.12$
 $\rightarrow V^{1/4} < 2 \times 10^{16} \text{ GeV}$
 extrapolated from 10^{-16} Hz !
 (assuming non-blue spectrum)



- courtesy <http://rhcole.com/apps/GWplotter/>
- (see Moore, Cole & Berry 2014, arXiv:1408.0740)
- nb. Joe Romano's caveats on these figures...

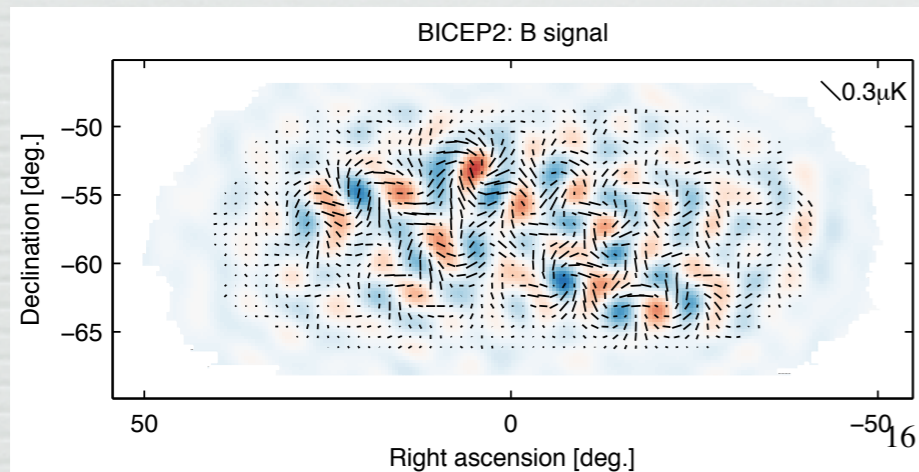
Post-Planck CMB

- Since late 1990s, (bolometric) detectors at \sim quantum limits
 - need many detectors (low noise)
 - Can only improve by \sqrt{N}
 - ... at many frequencies (discriminate foregrounds)
 - narrow bands (or even Fourier-transform spectroscopy)
 - (fewer photons per band, so see above — many detectors)
- e.g., lithography + antenna coupling



Original Polarbear design, c. 2000

BICEP2



□ 256 × 2 = 512
TES bolos
@ 150GHz

□ 0.5 deg FWHM

□ Strategy: large sky area 380 deg² (AJ et al '00)

BICEP2 Collaboration

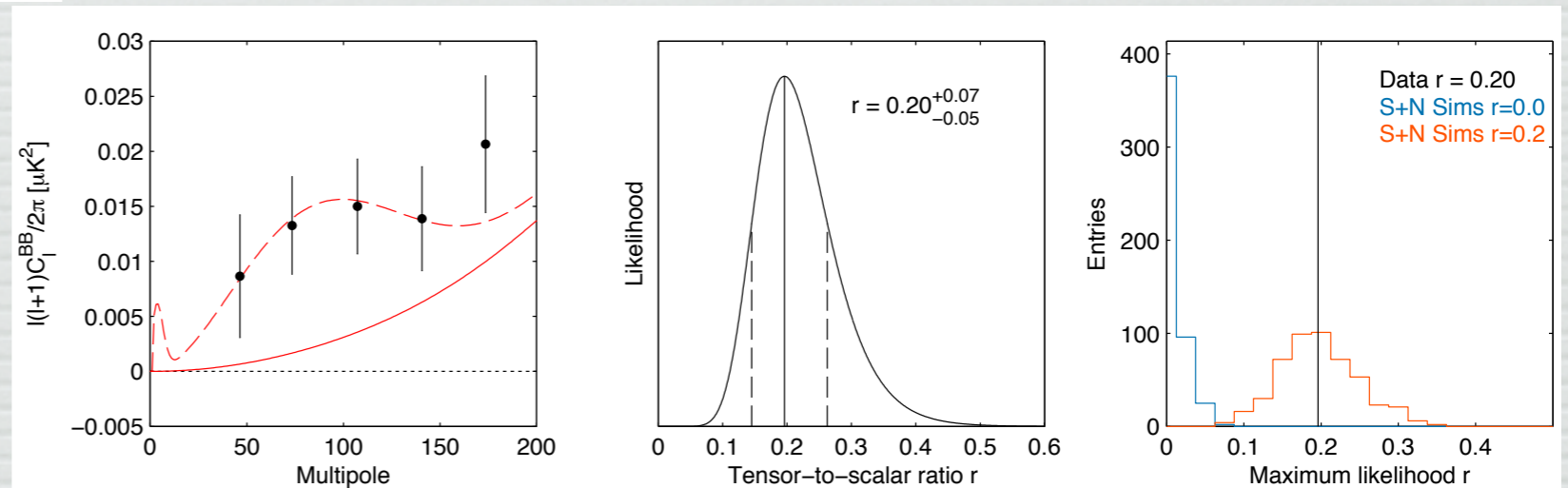
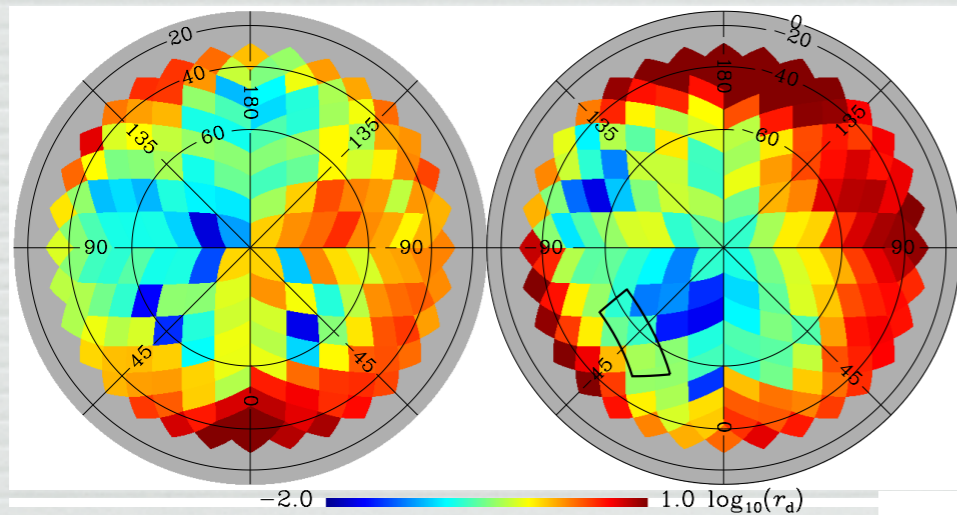


FIG. 10.— *Left:* The BICEP2 bandpowers plotted with the maximum likelihood lensed- Λ CDM+ $r = 0.20$ model. The uncertainties are taken from that model and hence include sample variance on the r contribution. *Middle:* The constraint on the tensor-to-scalar ratio r . The maximum likelihood and $\pm 1\sigma$ interval is $r = 0.20^{+0.07}_{-0.05}$, as indicated by the vertical lines. *Right:* Histograms of the maximum likelihood values of r derived from lensed- Λ CDM+noise simulations with $r = 0$ (blue) and adding $r = 0.2$ (red). The maximum likelihood value of r for the real data is shown by the vertical line.

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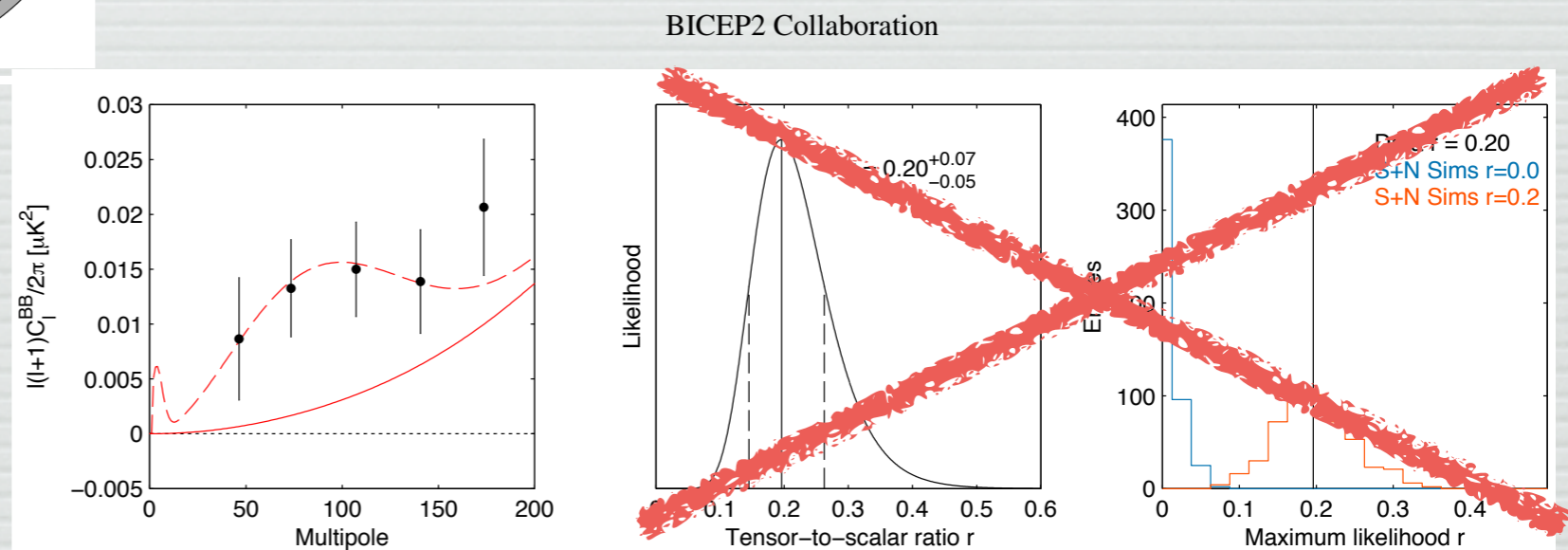
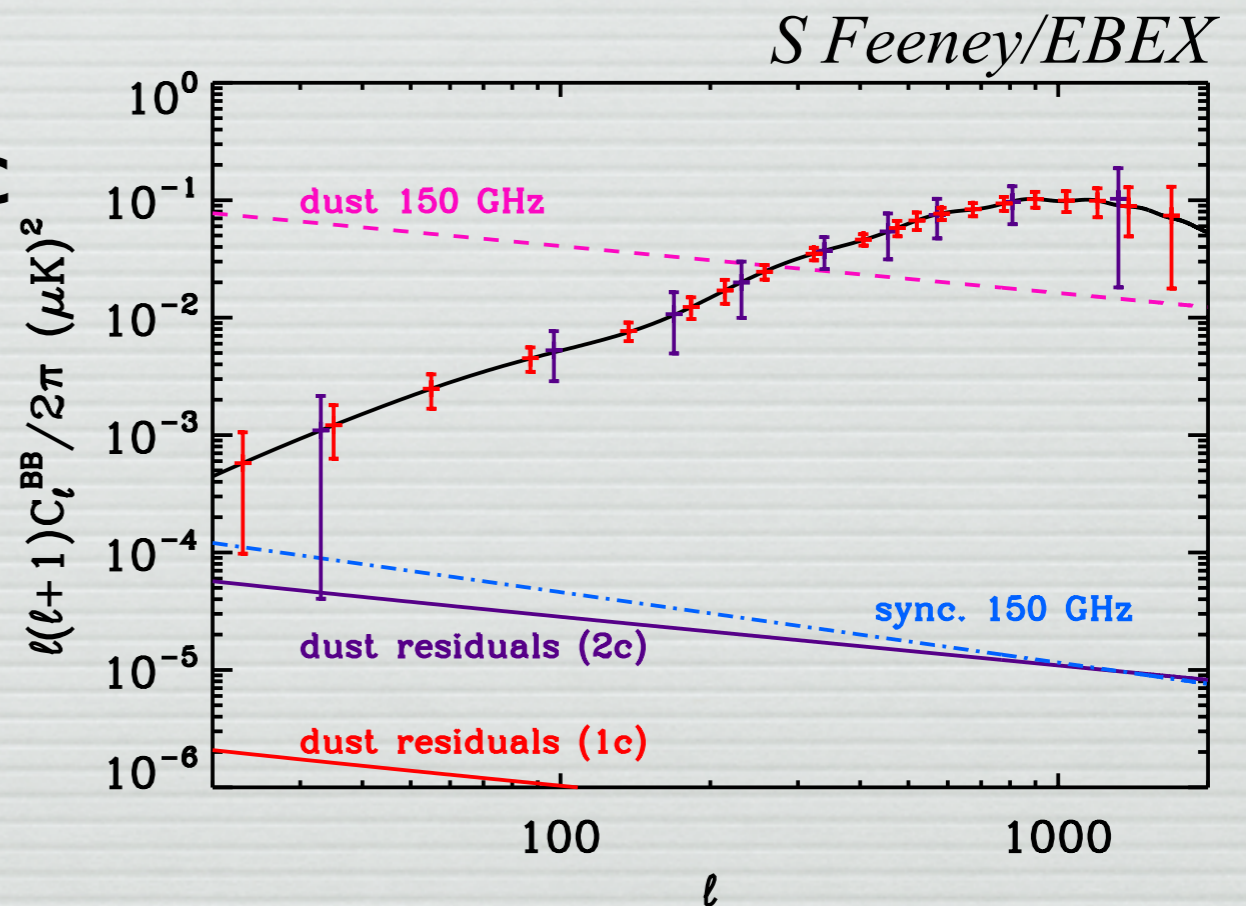


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Foreground modelling

- The Planck/BICEP2 experience has shown that foregrounds dominate even “clean” areas of sky
 - low dust **intensity** \neq low dust **polarisation**
- need enough frequency coverage to measure dust (&c) properties on small patches.
 - e.g. two-temperature grey-body models, galactic magnetic field
 - traced better at higher (dust) and lower (synch, free-free) frequencies than 100-200 GHz where CMB dominates.

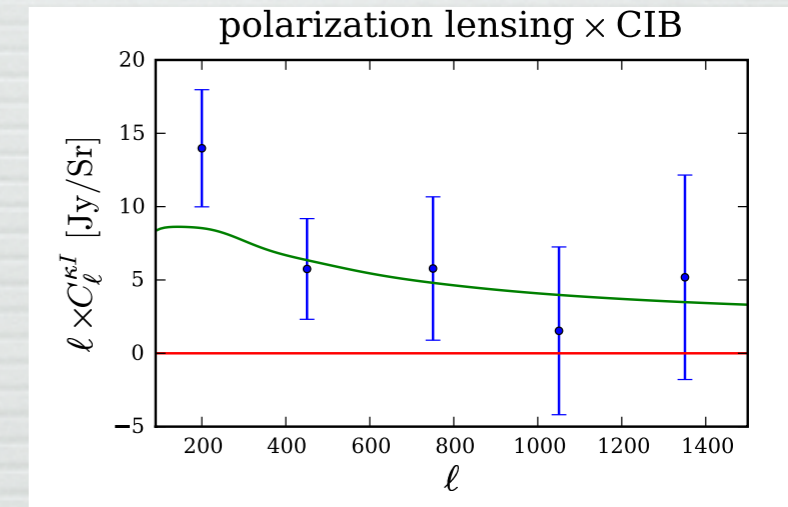


The Post-Planck generation: Lensing

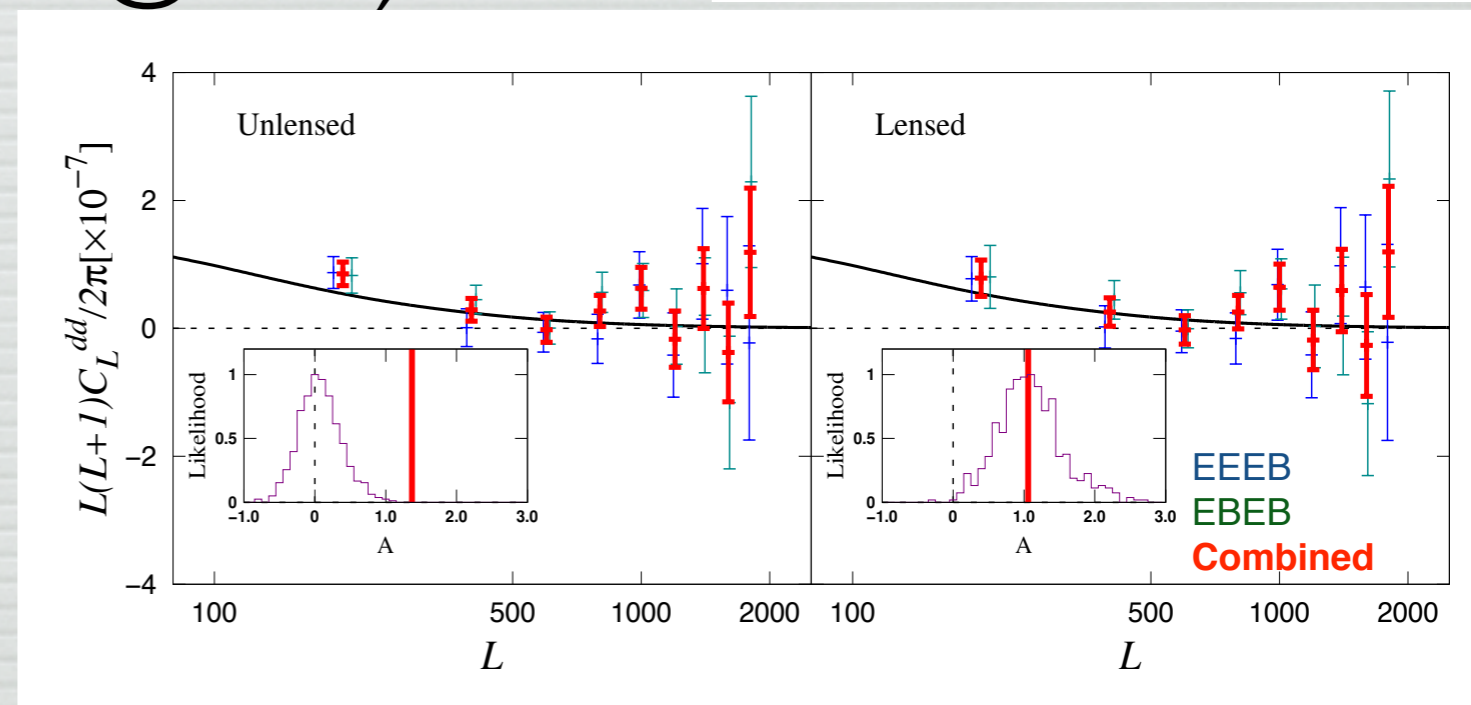
- Polarization: Starting to get the first results from **kilo-pixel CMB detector arrays** — sufficient to detect lensing conversion of $E \rightarrow B$

- Sensitive to growth of structure (e.g., neutrinos)
- Cross-correlation with **large-scale structure** (SPTPol: Hanson et al; ACT: Hand et al; Polarbear @ $\sim 4\sigma$)

PB x Herschel H-Atlas CIB measurement

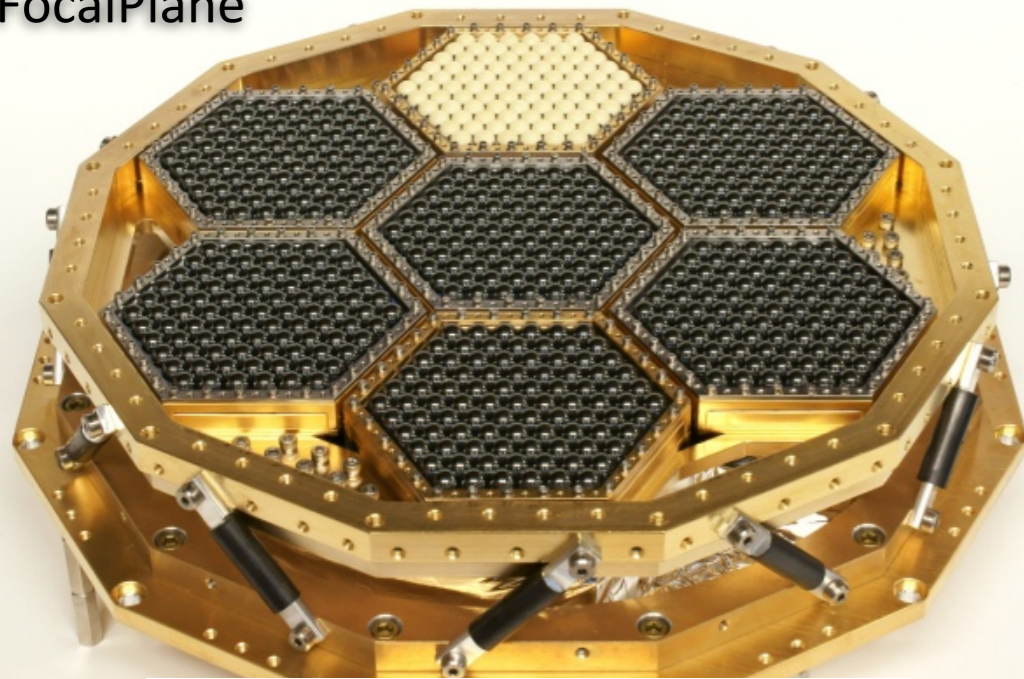


- $\langle EEEB \rangle$ & $\langle EBEB \rangle$ (Polarbear @ $\sim 4\sigma$)
- These are *not* **primordial** B modes (gravitational radiation)



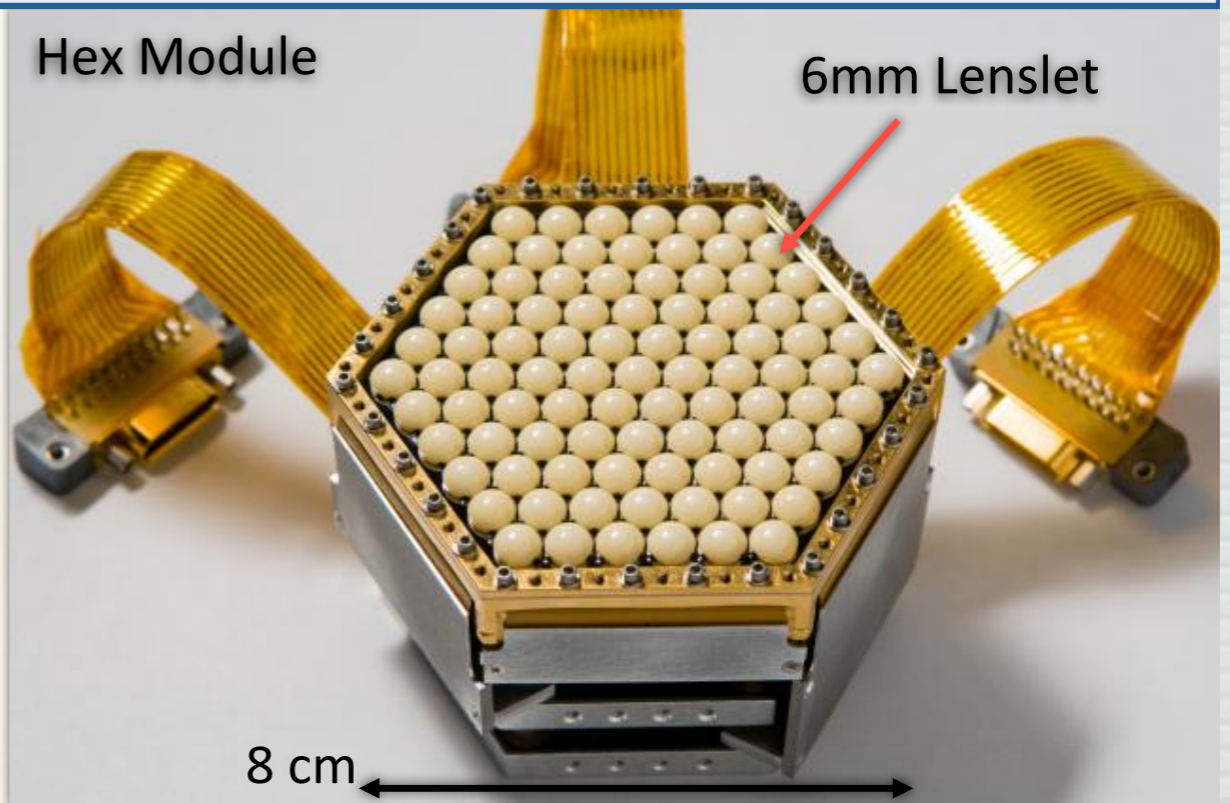
The Polarbear focal plane

FocalPlane



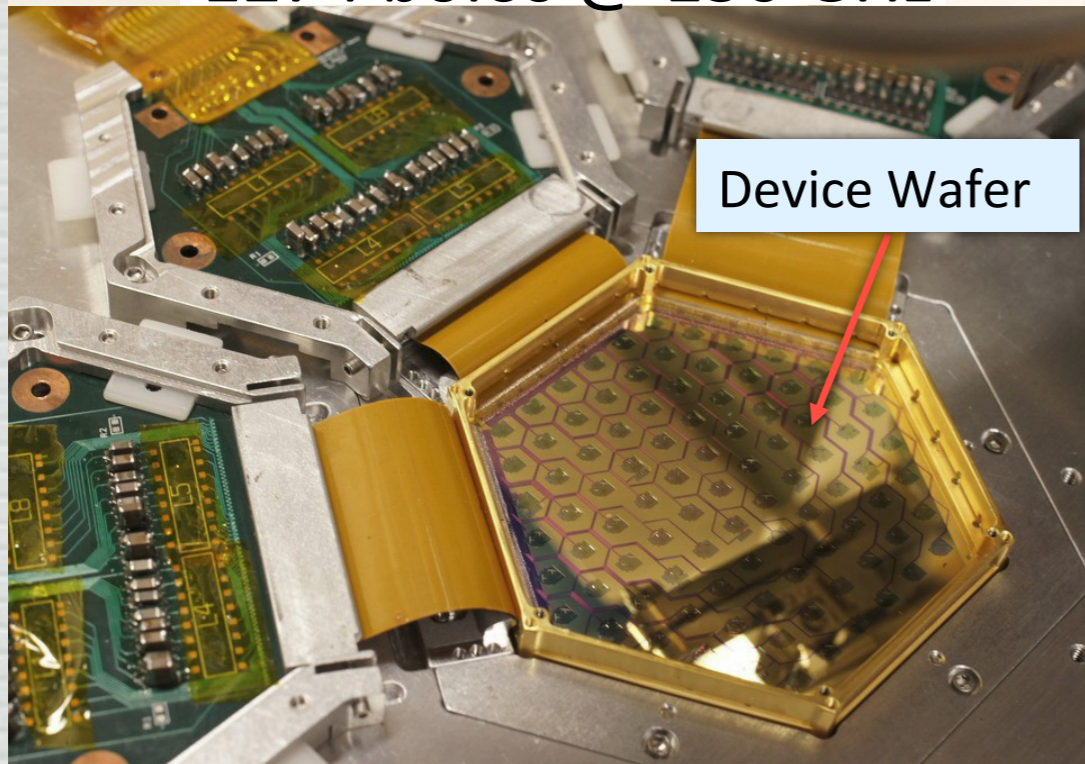
1274 bolos @ 150 GHz

Hex Module

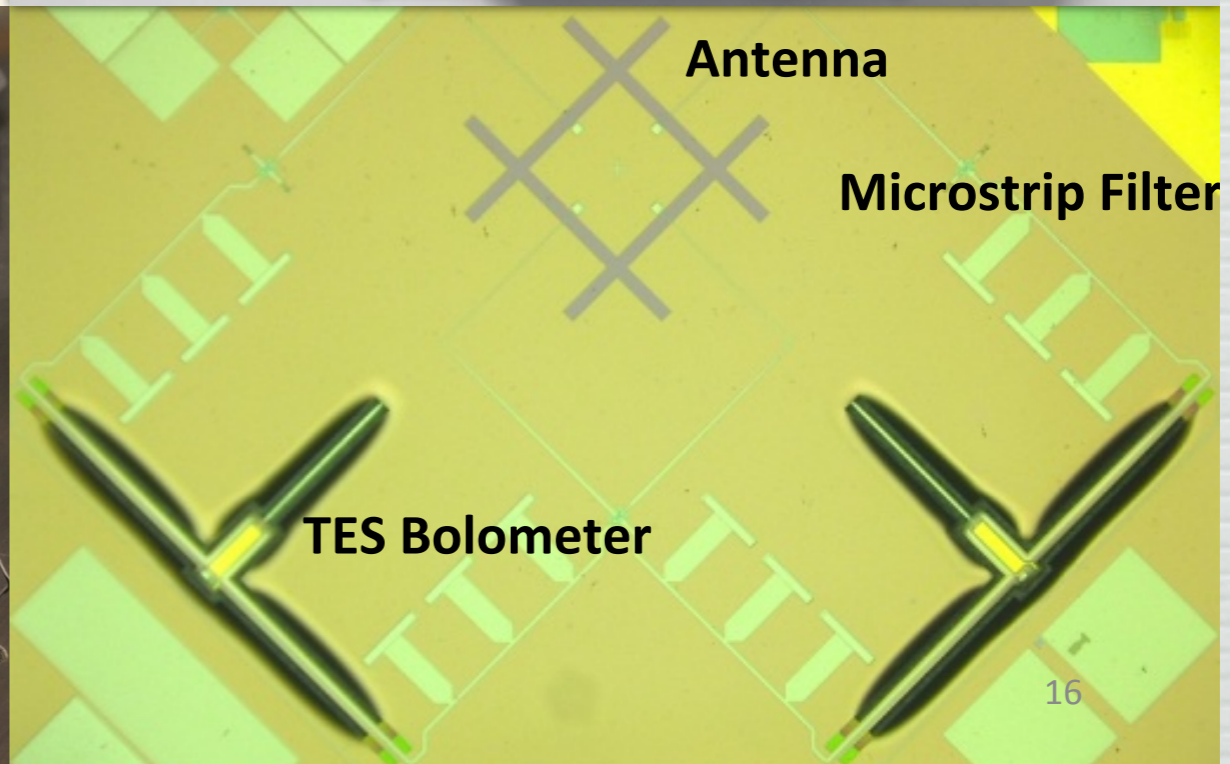


6mm Lenslet

8 cm



Device Wafer

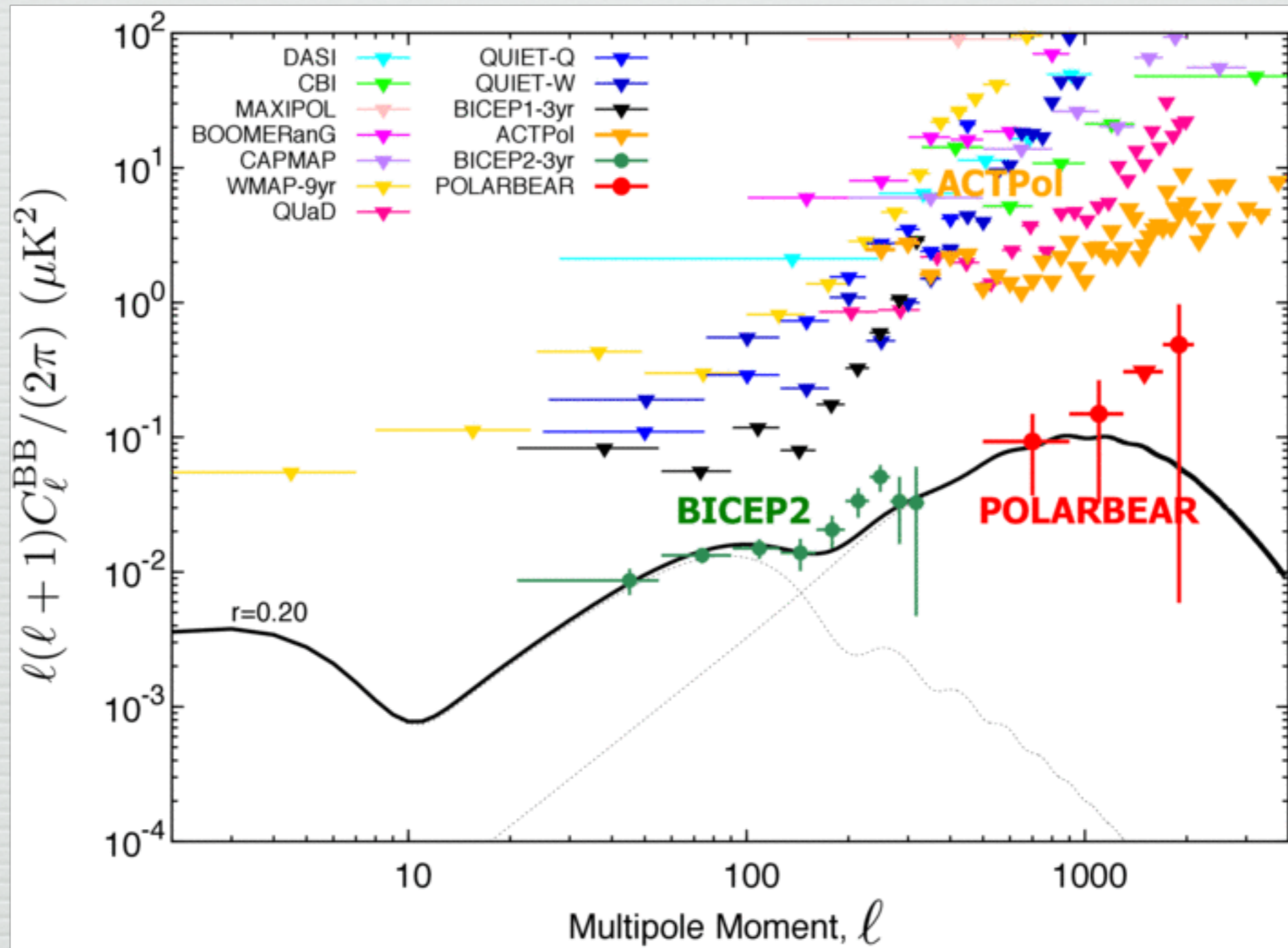


Antenna

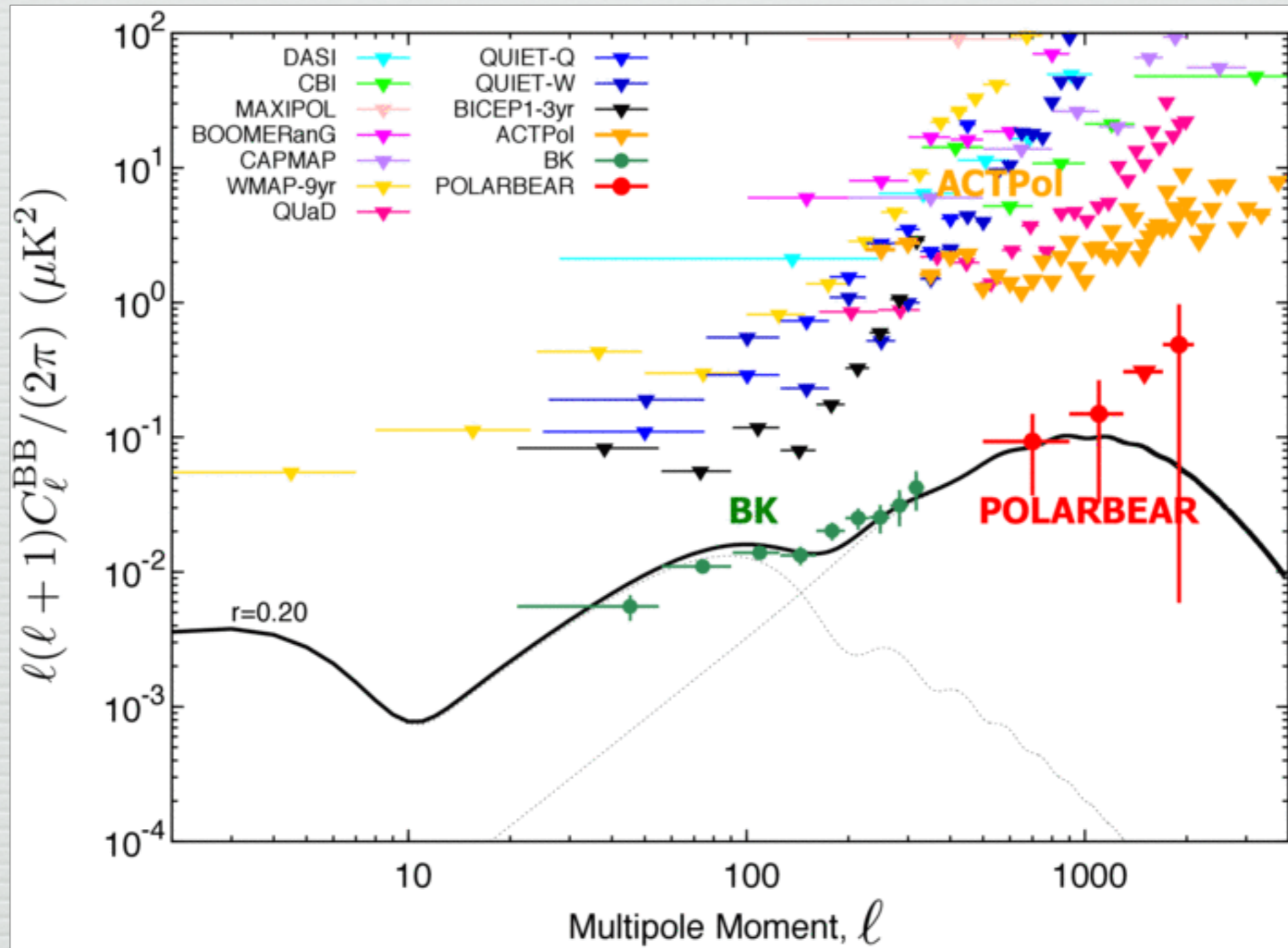
Microstrip Filter

TES Bolometer

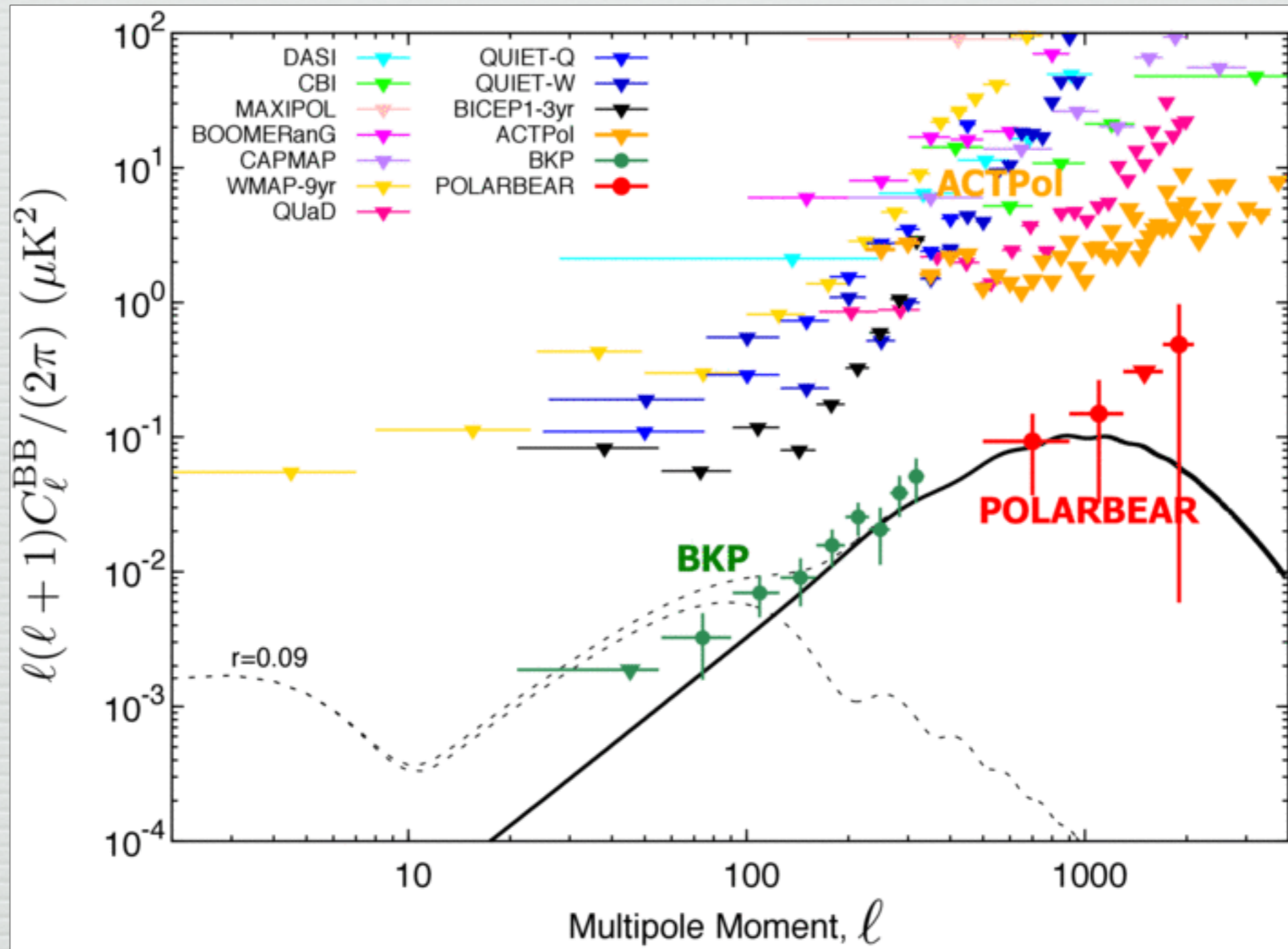
State of the art



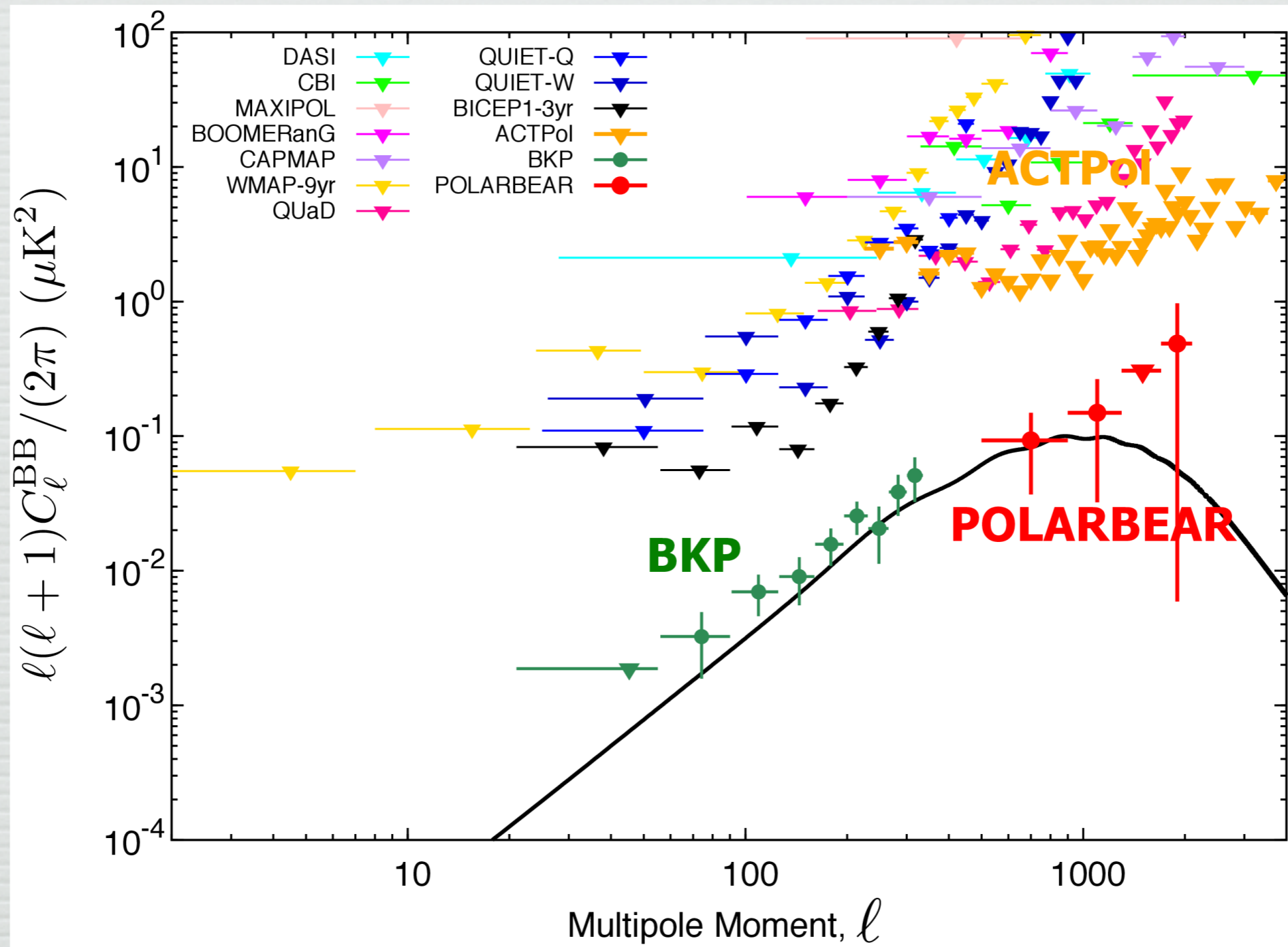
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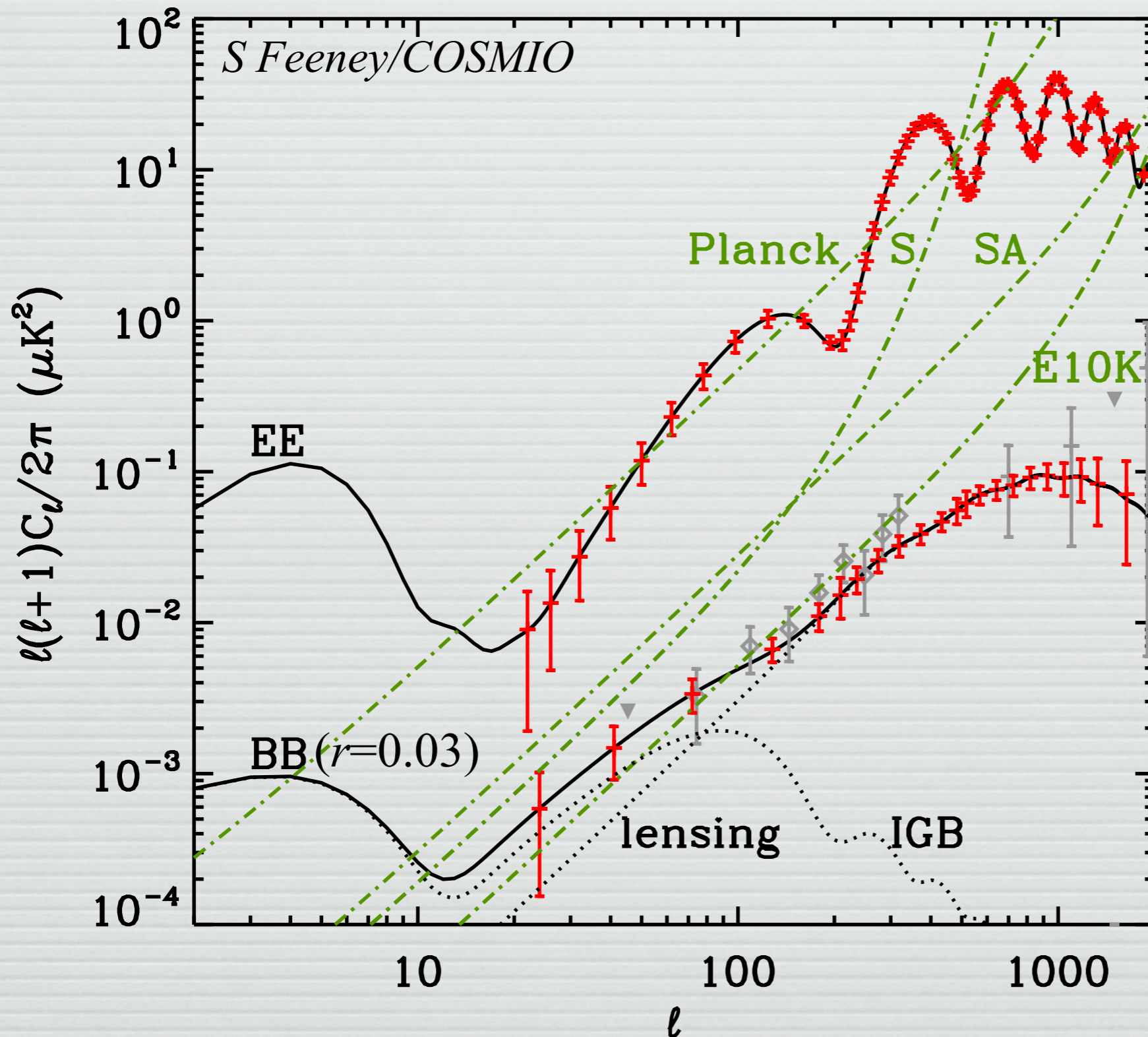
State of the art



State of the art



The near future



Noise levels

Planck

S: Spider

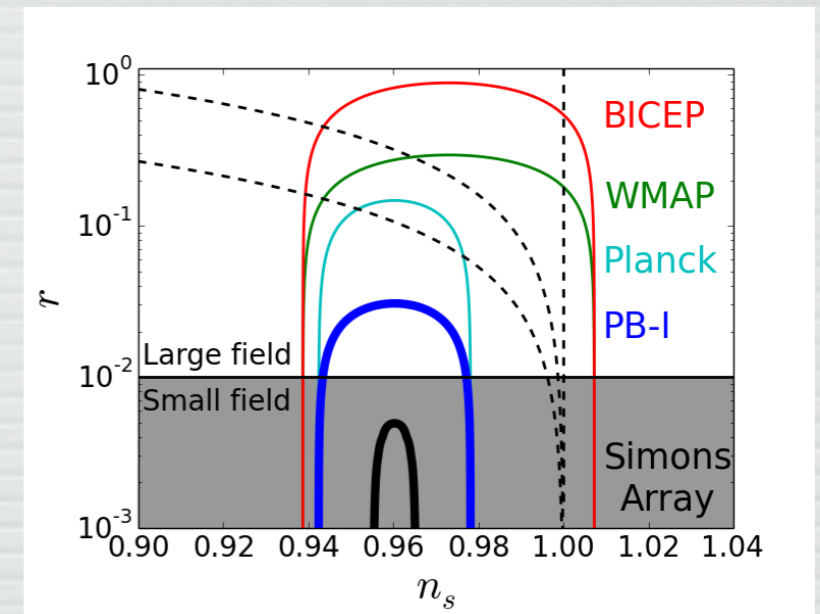
SA: Simons Array
(Polarbear)

E10K: EBEX

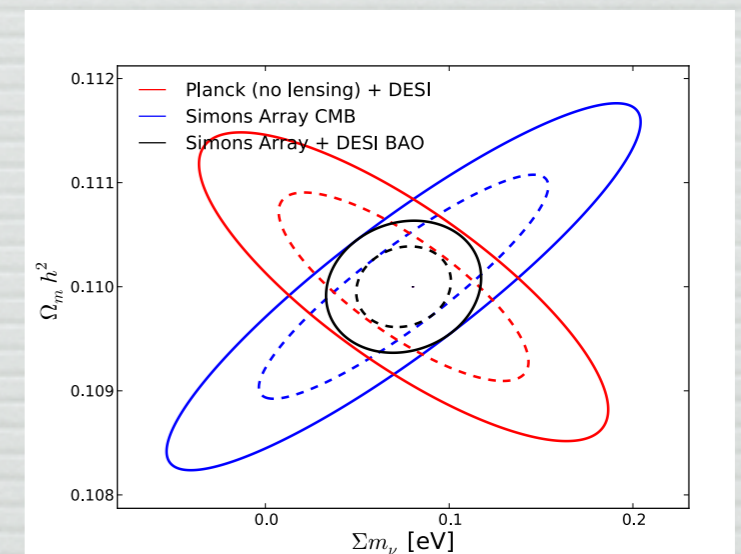
Similar performance
expected from
other 3d-gen
experiments:
Keck Array, LSPE,
SPT3G ...

Beyond detections

- already done: $\Omega_k=1$, $n_s \neq 1$
- detection: $r \neq 0$
- characterisation:
 - measure r to a “few sigma”
 - measure running
 - measure shape of tensor power spectrum, n_T
 - for single-field inflation these essentially give derivatives of the potential $V(\varphi)$
 - (also, detect non-Gaussianity, isocurvature modes)
 - other physics, e.g., neutrino mass



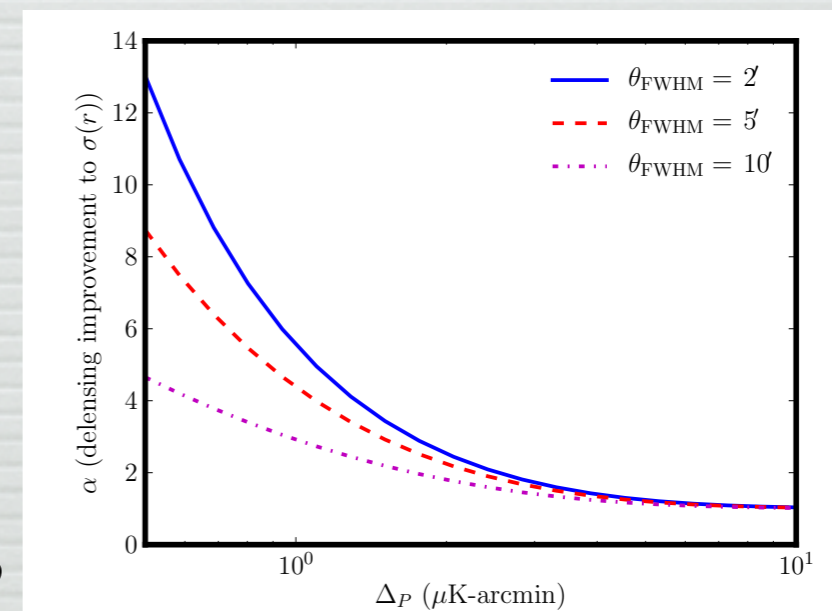
Polarbear/Simons Array



Polarbear/Simons Array

delensing

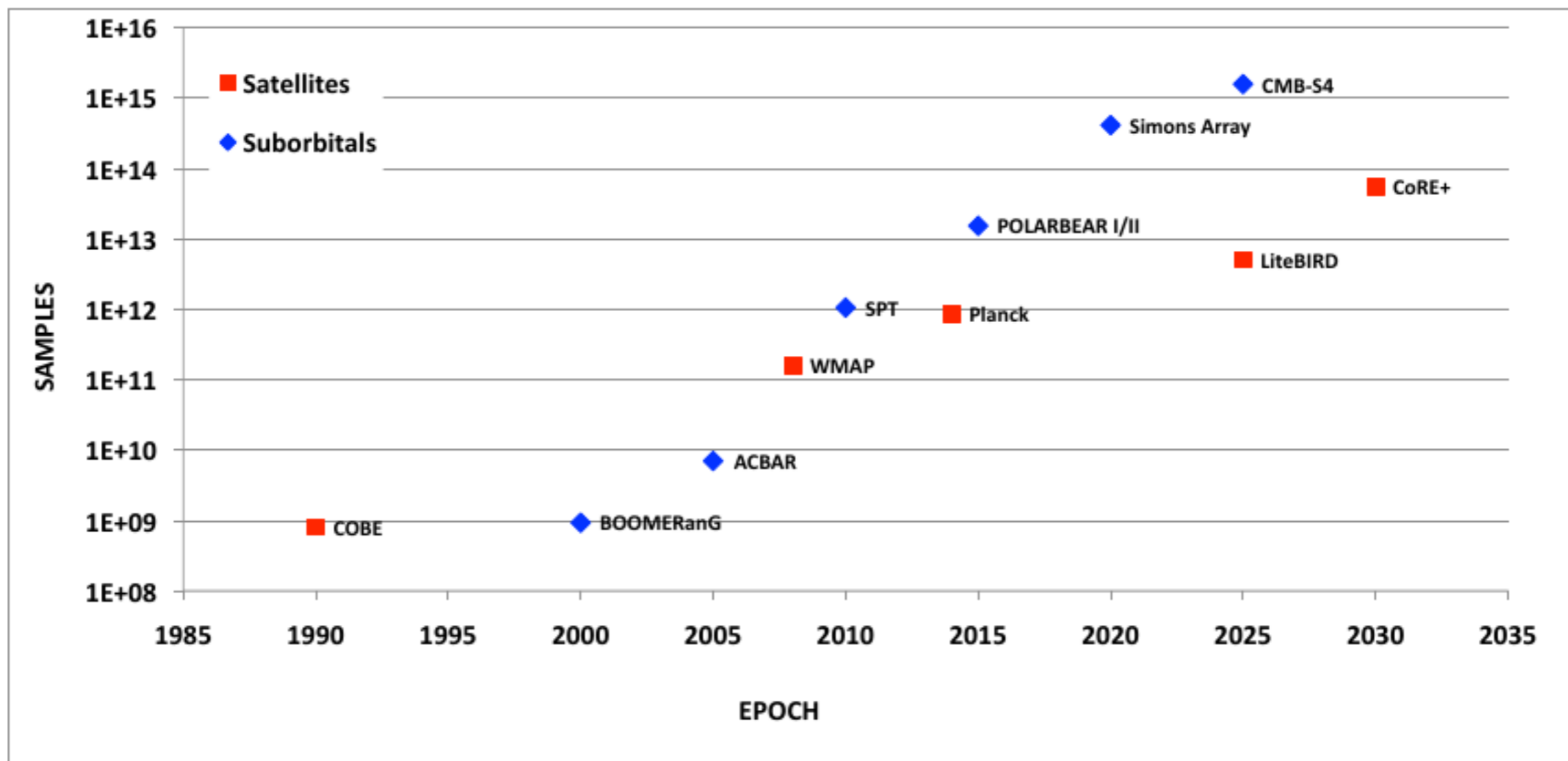
- Matter along the line of sight shifts photon trajectories
E→B (and B→E)
- Already observed in CMB alone and in cross-correlation with LSS observations
 - modifies the distribution function of temperature and polarisation
 - induces non-Gaussianity (Hu and Okamoto)
 - use high-resolution observations to de-lens low- l spectra
 - correlates signal with ρ along line of sight (Smith et al)
 - with LSS obs'ns, not as powerful as CMB-only; 2l cm a possibility
 - What about “mass maps” from GW sirens?
 - In principal, can use these to separate the lensing effect from the primordial contribution.



Smith et al 2012

The next (last?) generation: S4

- Currently planning/funding 10^4 -detector experiments — need another order of magnitude to take full advantage of the sky



The Polarbear Collaboration

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POLARBEAR Collaboration Meeting @ KEK Japan Mar. 24-28, 2013



planck



DTU Space
National Space Institute



Science & Technology
Facilities Council



National Research Council of Italy



Deutsches Zentrum
für Luft- und Raumfahrt e.V.



UNIVERSITY OF
CAMBRIDGE



Infrared Processing
and Analysis Center



Imperial College
London



MilliLab



US
University of Sussex



UNIVERSITÉ
DE GENÈVE



UNIVERSITY OF
TORONTO



UNIVERSITÉ DE
PARIS-SUD XI



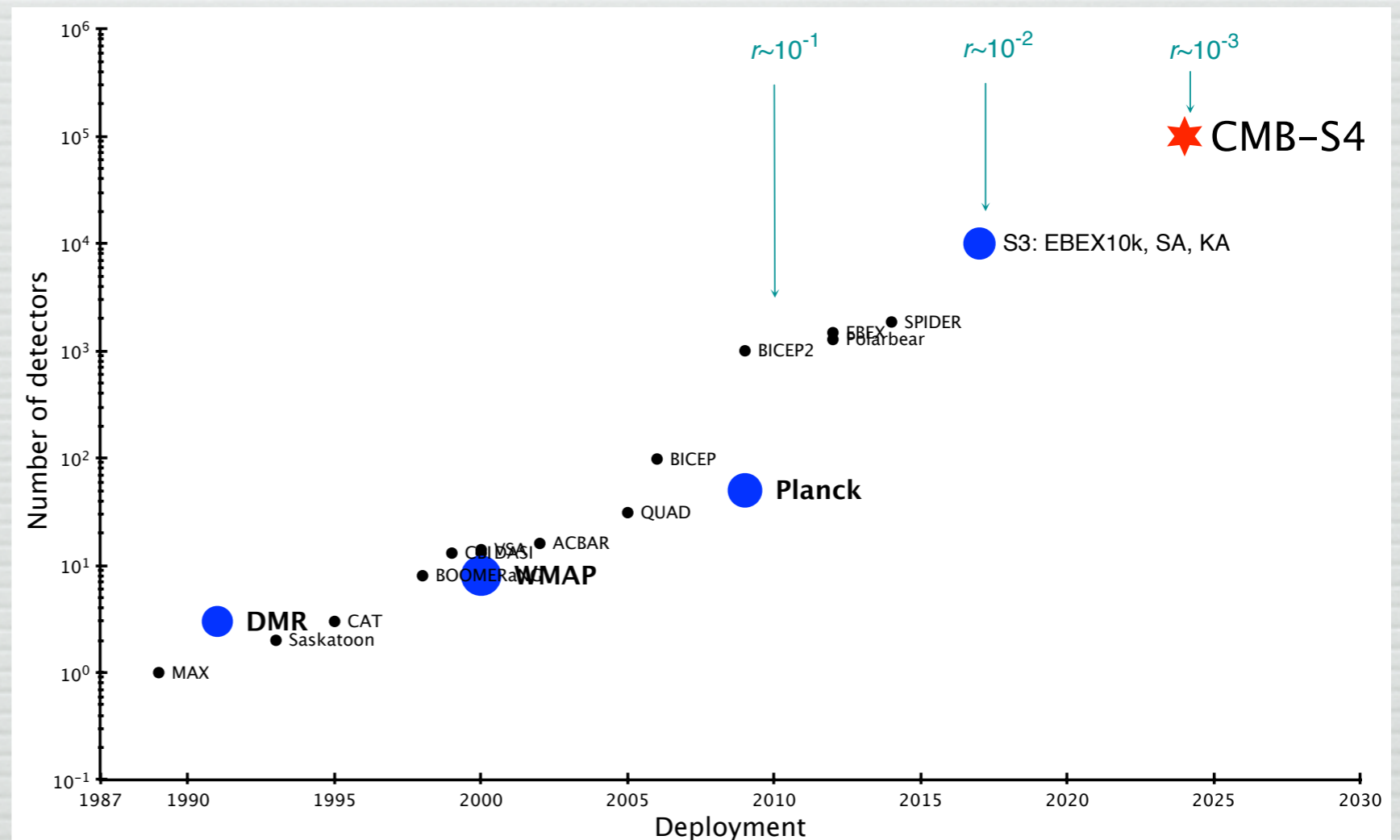
Parts of this talk based on data & papers released 2013-15 by the 400-person Planck Collaboration

Moore's law for CMB experiments?

- Goal $r \sim 10^{-3}$
 - Starobinsky, Higgs
 - trans-Planckian excursions
 - (Creminelli et al 2015)
 - also $n_t \sim 0.1$
- Multiple ground-based telescopes
- $> 10^5$ detectors
- 50% sky
- 40-240 GHz for foreground removal

- 1 μK arcmin sensitivity
- TES bolos
- 1 TB/day

- (supplemented by balloons for > 300 GHz?)
- similar to a future satellite (!)

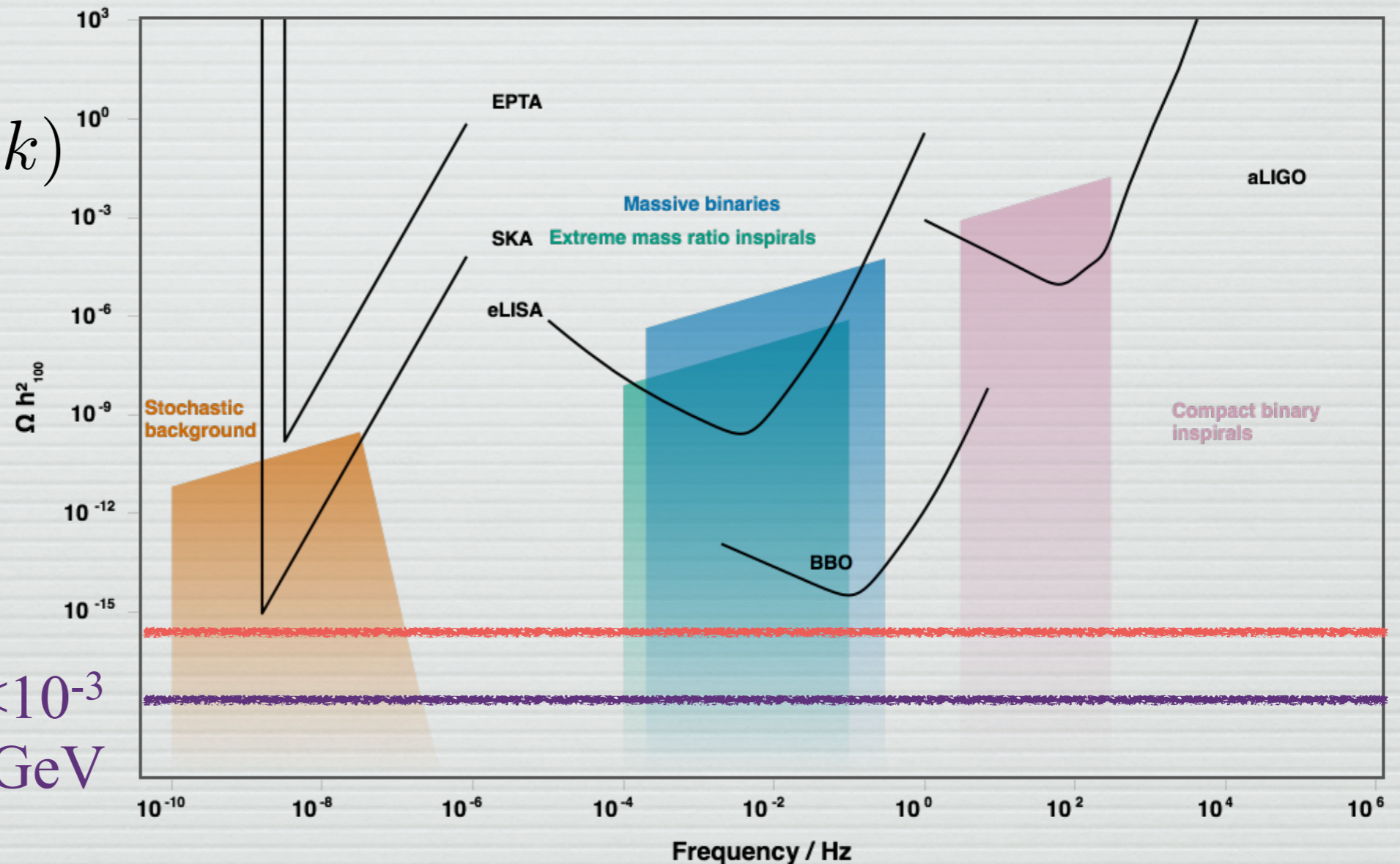


Prospects for the coming decade+

$$\Omega_{\text{GW}}(k) \propto P_t(k)$$

$$\propto V$$

$$\propto r$$



CMB goal: $r < 10^{-3}$
 $\rightarrow V^{1/4} < 6 \times 10^{15} \text{ GeV}$

- Still have 1-2 more orders of magnitude in r to observe
- Interesting models to see or rule out.
- Technical challenges — 100k detector arrays, foregrounds, lensing