

# Single Top Quark and Higgs-Boson Production in ep collisions

MUKESH KUMAR

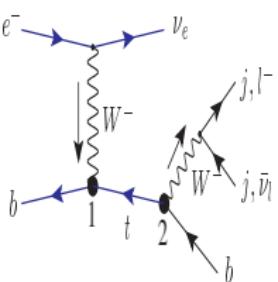
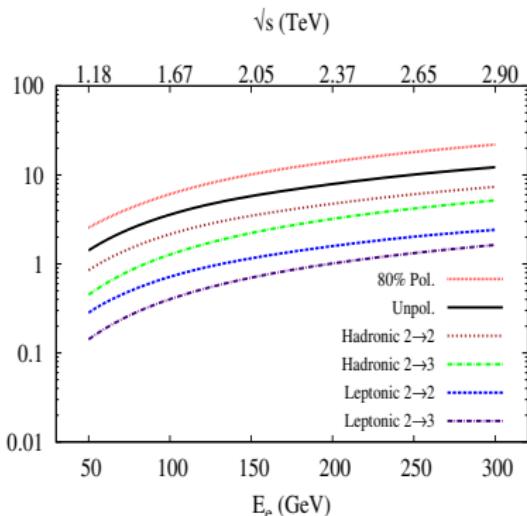
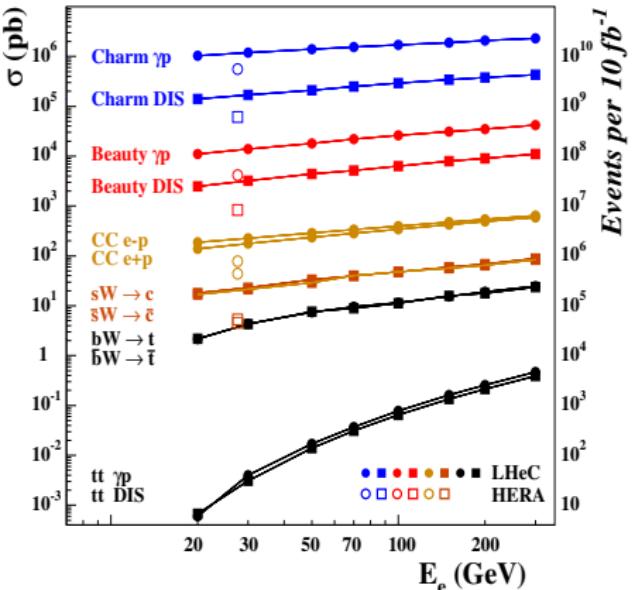
University of the Witwatersrand  
Johannesburg, South Africa

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HEPPW 2015

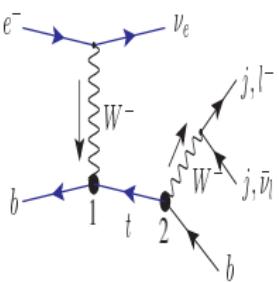
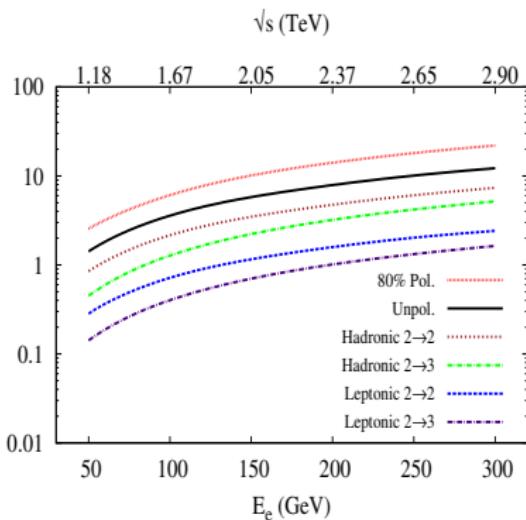
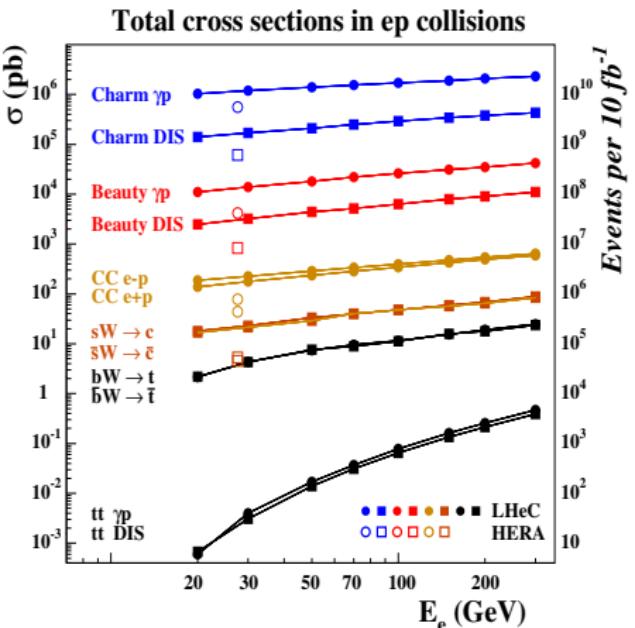
arXiv: 1307.1688, 1203.6285, 1502.xxxxx

# Single Top at LHeC: $Wtb$ vertex

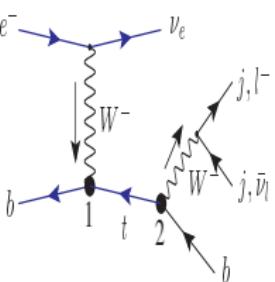
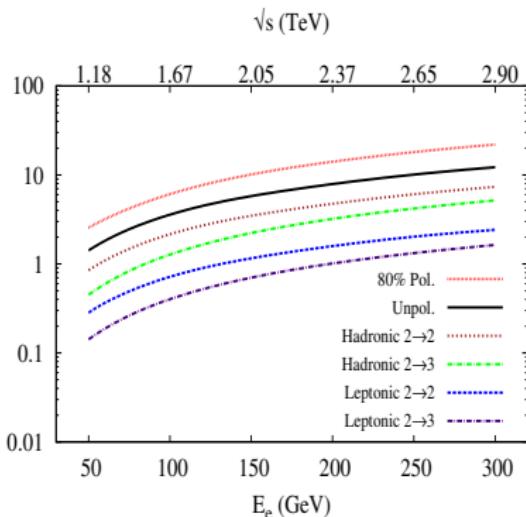
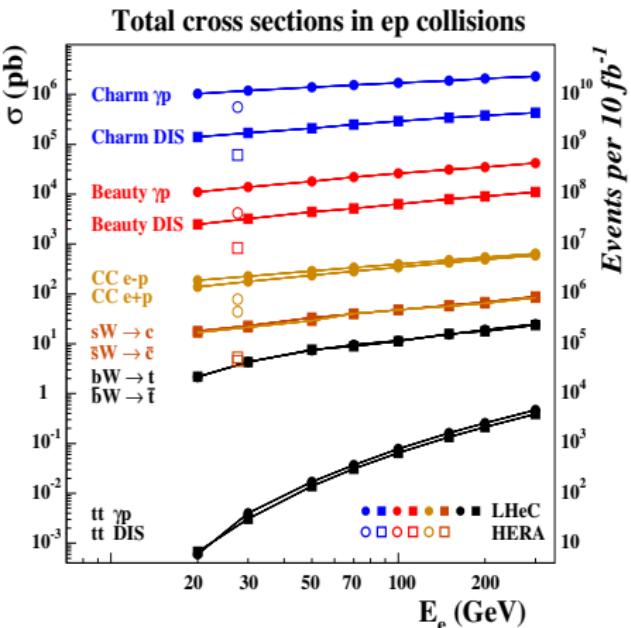
Total cross sections in ep collisions



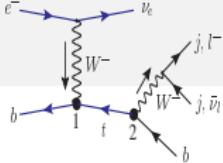
## Single Top at LHeC: $Wtb$ vertex



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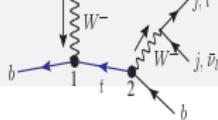


# Lagrangian & Processes:



- ▶  $\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}} \left[ W_\mu \bar{t} \gamma^\mu (V_{tb} f_1^L P_L + f_1^R P_R) b - \frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_2^L P_L + f_2^R P_R) b \right] + \text{h.c.}$  ;  
where  $f_1^L \equiv 1 + \Delta f_1^L$ ,  $W_{\mu\nu} = D_\mu W_\nu - D_\nu W_\mu$ ,  $D_\mu = \partial_\mu - ieA_\mu$ ,  
 $\sigma^{\mu\nu} = i/2 (\gamma^\mu \gamma^\nu - \gamma^\nu \gamma^\mu)$ .
- ▶ In SM  $|V_{tb}| f_1^L \approx 1$  and at tree level  $\Delta f_1^L, f_1^R, f_2^L$  &  $f_2^R$  vanishes.
- ▶ CP-conseving → (can take) real couplings
- ▶ CP-violation → complex couplings [arXiv:06050190]
  - ▶  $f_1^R = 0.1e^{i\phi_f^R}, f_2^L = 0.1e^{i\phi_f^L}, f_2^R = 0.1e^{i\phi_f^R}$
  - ▶  $f_1^R, f_2^L$  not affected but in case of  $f_2^R$  phase is dominant → Angular asymmetries are not sufficient
  - ▶ Other observable: Spin Asymmetry, triple product asymmetries in dileptonic channel in  $t\bar{t}$  production
- ▶ Processes:  $e^- p \rightarrow \bar{t}\nu_e, \bar{t} \rightarrow W^- \bar{b}$ 
  - ▶ Helicity fractions:  $\mathcal{F}_0 = N_0/N, \mathcal{F}_+ = N_+/N, \mathcal{F}_- = N_-/N, N = N_0 + N_+ + N_-$
  - ▶ Hadronic decay:  $W^- \rightarrow jj$
  - ▶ Leptonic decay:  $W^- \rightarrow l\nu_l, l = e, \mu$

## Constrain on $f_i$ 's

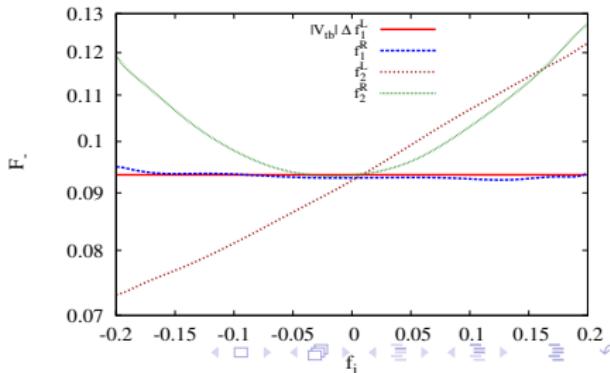
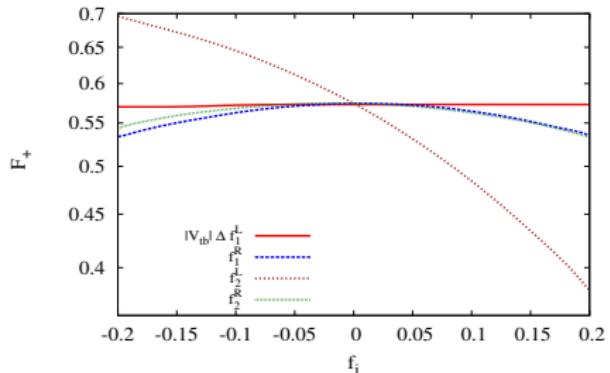
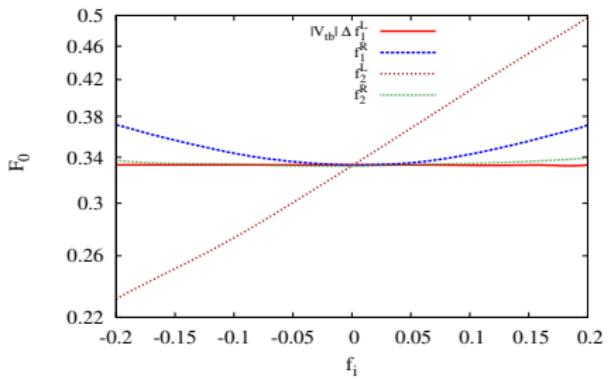
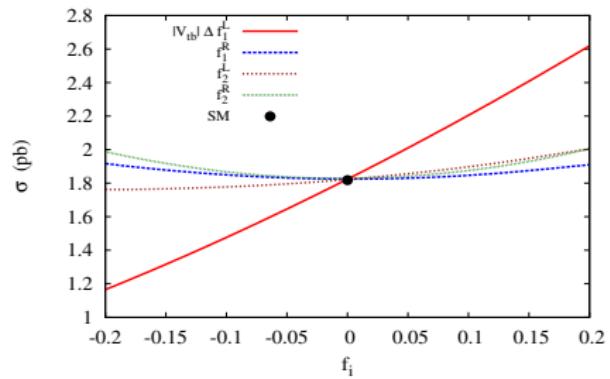
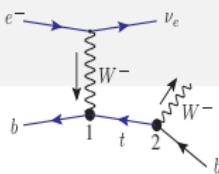


- ▶ Assuming only one anomalous coupling to be non-zero at a time  
 $-0.13 \leq |V_{tb}|f_1^L \leq 0.03$ ,  $-0.0007 \leq f_1^R \leq 0.0025$ ,  $-0.0015 \leq f_2^L \leq 0.0004$ ,  
 $-0.15 \leq f_2^R \leq 0.57$  from  $B$  decays [[Phys. Rev. D 78, 077501 \(2008\)](#)]
- ▶ Single top production at DØ assuming  $|V_{tb}|f_1^L = 1$ ,  $|f_1^R| \leq 0.548$ ,  $|f_2^L| \leq 0.224$ ,  
 $|f_2^R| \leq 0.347$  [[Phys. Lett. B 713, 165 \(2012\)](#)]
- ▶ Associated  $tW$  production at LHC through  $\gamma p$  collision  $|f_1^R| \leq 0.55$ ,  $|f_2^L| \leq 0.22$ ,  
 $|f_2^R| \leq 0.35$  [[Phys. Rev. D 86, 074026 \(2012\)](#)]
- ▶ ATLAS: asymmetries associated through angular distribution  $\text{Re}(f_1^R) \in [-0.44, 0.48]$ ,  $\text{Re}(f_2^L) \in [-0.24, 0.21]$ ,  $\text{Re}(f_2^R) \in [-0.49, 0.15]$ . [[ATLAS-CONF-2011-037](#)]

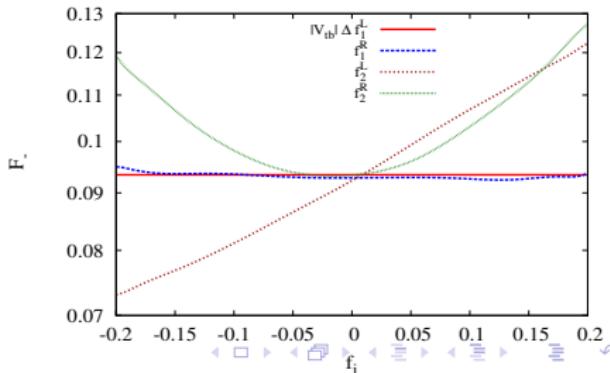
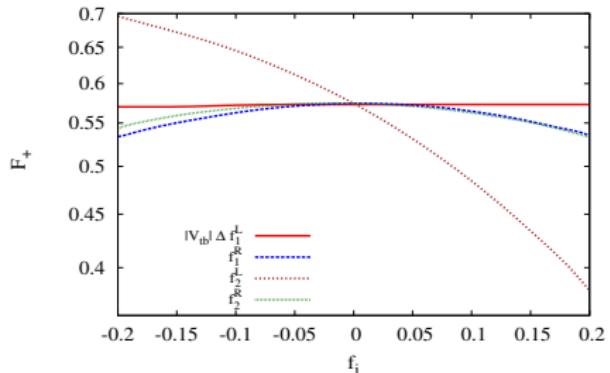
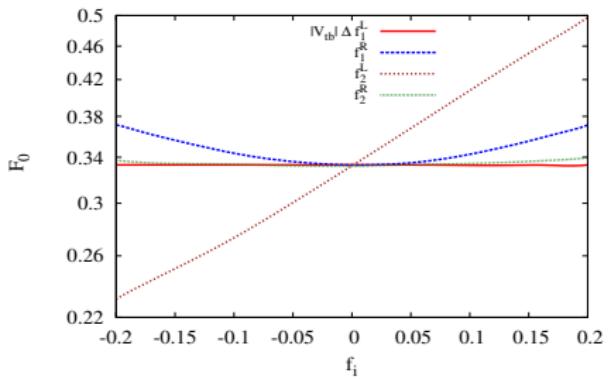
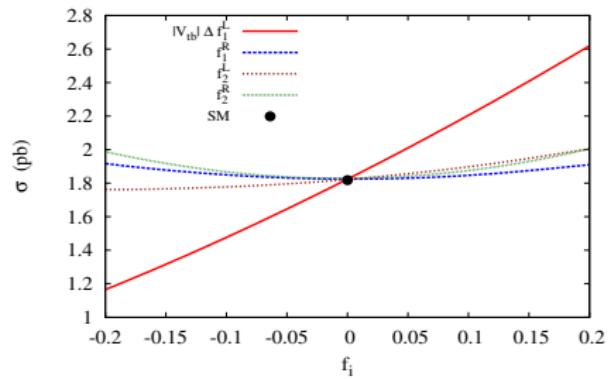
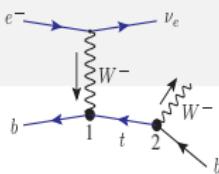
Loop Corrections:[[arXiv:1308.3652](#)]

- ▶ QCD:  $f_2^R = -6.61 \times 10^{-3}$ ,  $f_2^L = -1.118 \times 10^{-3}$  ( $m_t = 171$  GeV)
- ▶ EW:  $f_2^R = -(1.24 \pm 1.23i) \times 10^{-3}$ ,  $f_2^L = -(0.102 \pm 0.014i) \times 10^{-3}$  ( $m_H = 126$  GeV)
- ▶ SM:  $f_2^R = -(7.85 \pm 1.23i) \times 10^{-3}$ ,  $f_2^L = -(1.220 \pm 0.014i) \times 10^{-3}$

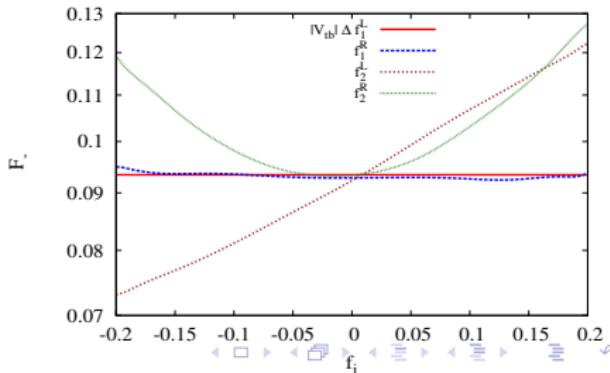
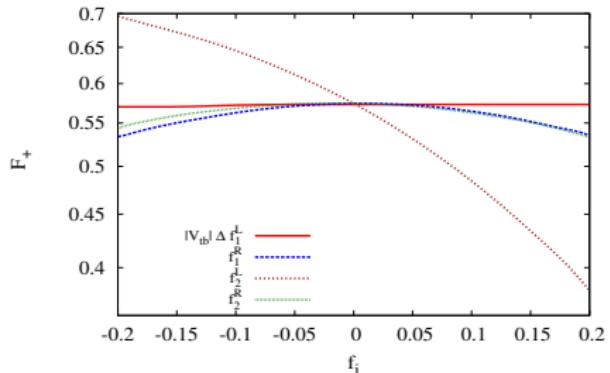
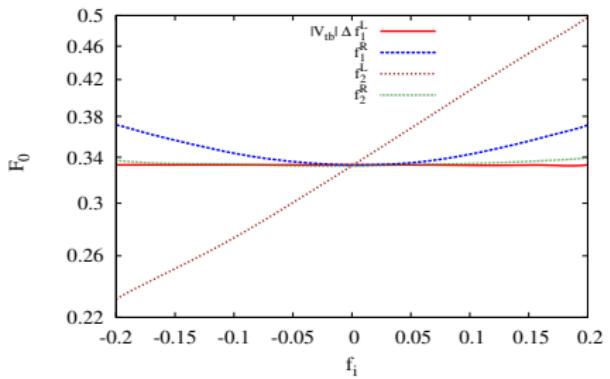
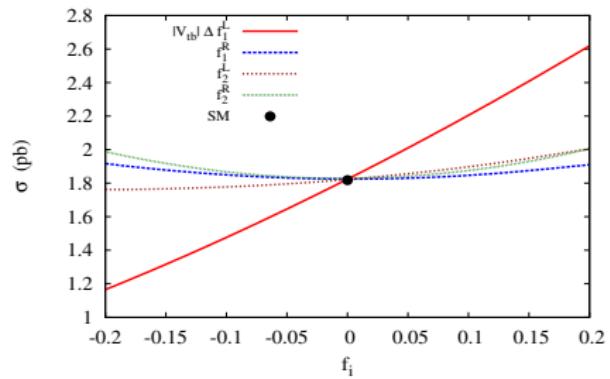
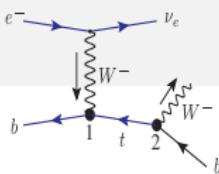
$e^- p \rightarrow \bar{t} \nu_e \rightarrow \bar{b} W^- \nu_e$  &  $W^-$  helicity fractions:



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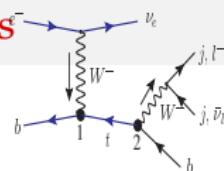
# Hadronic: $E_e = 60 \text{ GeV}$ , $E_p = 7 \text{ TeV}$ , $L = 100 \text{ fb}^{-1}$

No.	Background Process	$p_{T,j,b} \geq 20 \text{ GeV}$ $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$	$ m_{j_1 j_2} - m_W  \leq 22 \text{ GeV}$	$\sigma_{\text{eff.}}$	
1	$e^- p \rightarrow \nu_e W^- b$ without anti-top line	$7.5 \times 10^{-3}$	$6.8 \times 10^{-3}$	$4.5 \times 10^{-3}$	$2.7 \times 10^{-3}$	
2	$e^- p \rightarrow \nu_e jjjj$	$4.2 \times 10^0$	$3.6 \times 10^0$	$2.4 \times 10^0$	$7.2 \times 10^{-2}$	
3	$e^- p \rightarrow \nu_e cjj$ & $e^- p \rightarrow \nu_e \bar{c}jj$	$1.5 \times 10^0$	$1.2 \times 10^0$	$8.6 \times 10^{-1}$	$8.6 \times 10^{-2}$	
4	$e^- p \rightarrow \nu_e c\bar{c}j$	$5.8 \times 10^{-2}$	$5.0 \times 10^{-2}$	$3.2 \times 10^{-2}$	$6.7 \times 10^{-3}$	
5	$e^- p \rightarrow \nu_e b\bar{b}j$	$2.5 \times 10^{-2}$	$2.2 \times 10^{-2}$	$5.6 \times 10^{-3}$	$1.3 \times 10^{-3}$	
6	$e^- p \rightarrow \bar{c}\nu_e$ ( $\bar{c} \rightarrow W^- \bar{s}$ )	$2.5 \times 10^{-2}$	$2.2 \times 10^{-2}$	$1.5 \times 10^{-2}$	$1.5 \times 10^{-4}$	
<hr/>						
Event Selection		$p_{T,j,b} \geq 20 \text{ GeV}$ $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$	$ m_{j_1 j_2} - m_W  \leq 22 \text{ GeV}$	Fiducial Efficiency	$S/\sqrt{S+B}$
<hr/>						
$SM$		$3.2 \times 10^4$	$2.3 \times 10^4$	$2.2 \times 10^4$	66.7 %	
$SM + \sum_i \text{Bkg}_i$		$6.5 \times 10^4$	$5.0 \times 10^4$	$4.0 \times 10^4$	61.5 %	
$ V_{tb}  \Delta f_1^L = .5$		$7.3 \times 10^4$	$5.0 \times 10^4$	$5.0 \times 10^4$	68.0 %	
$f_1^R = .5$		$4.6 \times 10^4$	$3.2 \times 10^4$	$3.2 \times 10^4$	69.7 %	
$f_2^L = .5$		$4.9 \times 10^4$	$3.6 \times 10^4$	$3.6 \times 10^4$	73.2 %	
$f_2^L = -.5$		$3.4 \times 10^4$	$2.3 \times 10^4$	$2.3 \times 10^4$	69.6 %	
$f_2^R = .5$		$5.7 \times 10^4$	$4.1 \times 10^4$	$4.1 \times 10^4$	72.3 %	

# Leptonic: $E_e = 60 \text{ GeV}$ , $E_p = 7 \text{ TeV}$ , $L = 100 \text{ fb}^{-1}$

No.	Background Process	$p_{T,j,b,l} \geq 20 \text{ GeV}$ , $\Delta R_{j,b/j} \geq 0.4$ , $\cancel{E}_T \geq 25$ $ \eta_j  \geq 5$ , $ \eta_{b,l}  \geq 2.5$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$ $\Delta\Phi_{\cancel{E},l} \geq 0.4$	$\sigma_{\text{eff.}}$
1	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e j$	$1.5 \times 10^{-1}$	$1.4 \times 10^{-1}$	$1.4 \times 10^{-3}$
2	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e c$ & $e^- p \rightarrow l^- \bar{\nu}_l \nu_e \bar{c}$	$6.6 \times 10^{-3}$	$6.1 \times 10^{-3}$	$6.1 \times 10^{-4}$
3	$e^- p \rightarrow l^- \bar{\nu}_l \nu_e b$ & $e^- p \rightarrow l^- \bar{\nu}_l \nu_e \bar{b}$ Without top line	$3.6 \times 10^{-3}$	$3.2 \times 10^{-3}$	$1.9 \times 10^{-3}$
4	$e^- p \rightarrow e^- l^- \bar{\nu}_l c$	$1.5 \times 10^{-2}$	$6.9 \times 10^{-3}$	$6.9 \times 10^{-4}$
5	$e^- p \rightarrow e^- l^- \bar{\nu}_l j$	$1.2 \times 10^{-1}$	$5.5 \times 10^{-2}$	$5.5 \times 10^{-4}$
Event Selection		$p_{T,j,b} \geq 20 \text{ GeV}$ $ \eta_j  \leq 5,  \eta_b  \leq 2.5$ $\Delta R_{j,b/j} \geq 0.4$ $\cancel{E}_T \geq 25$	$\Delta\Phi_{\cancel{E},j} \geq 0.4$ $\Delta\Phi_{\cancel{E},b} \geq 0.4$ $\Delta\Phi_{\cancel{E},l} \geq 0.4$	Fiducial Efficiency $S/\sqrt{S+B}$
SM		$1.2 \times 10^4$	$1.1 \times 10^4$	92.0 %
$\text{SM} + \sum_i \text{Bkg}_i$		$1.3 \times 10^4$	$1.2 \times 10^4$	92.0 %
$ V_{tb}  \Delta f_1^L = .5$		$4.5 \times 10^4$	$2.5 \times 10^4$	92.6 %
$f_1^R = .5$		$2.8 \times 10^4$	$1.6 \times 10^4$	94.1 %
$f_2^L = .5$		$3.1 \times 10^4$	$1.7 \times 10^4$	89.5 %
$f_2^L = -.5$		$1.8 \times 10^4$	$1.0 \times 10^4$	90.9 %
$f_2^R = .5$		$3.6 \times 10^4$	$2.0 \times 10^4$	90.9 %

# Estimators and $\chi^2$ Analysis: Angular Asymmetries

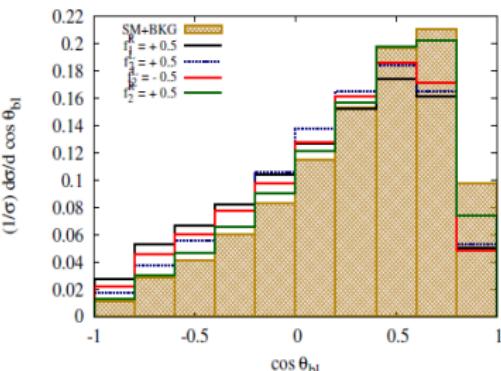
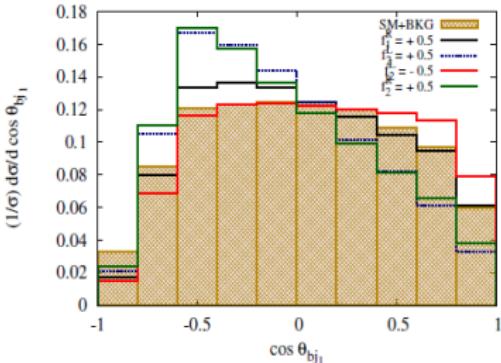


## Angular Asymmetries from Histogram:

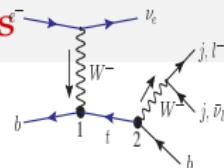
- ▶  $A_{\theta_{ij}} = \frac{N_+^A (\cos \theta_{ij} > 0) - N_-^A (\cos \theta_{ij} < 0)}{N_+^A (\cos \theta_{ij} > 0) + N_-^A (\cos \theta_{ij} < 0)}$
- ▶  $A_{\Delta \eta_{ij}} = \frac{N_+^A (\Delta \eta_{ij} > 0) - N_-^A (\Delta \eta_{ij} < 0)}{N_+^A (\Delta \eta_{ij} > 0) + N_-^A (\Delta \eta_{ij} < 0)}$
- ▶  $A_{\Delta \Phi_{ij}} = \frac{N_+^A (\Delta \phi_{ij} > \frac{\pi}{2}) - N_-^A (\Delta \phi_{ij} < \frac{\pi}{2})}{N_+^A (\Delta \phi_{ij} > \frac{\pi}{2}) + N_-^A (\Delta \phi_{ij} < \frac{\pi}{2})}, 0 \leq \Delta \phi_{ij} \leq \pi.$

where  $i, j$  may be any partons (including  $b$ ), charged lepton or missing energy.

- ▶ Statistical error in Asymmetry:  $\sigma_a = \sqrt{\frac{1-a^2}{L \cdot \sigma}}$ , where  $a = \frac{N_+^A - N_-^A}{N_+^A + N_-^A}$  and  $N = (N_+^A + N_-^A) = L \cdot \sigma$ ,  
 $\sigma \equiv \sigma(e^- p \rightarrow \bar{t} t \rightarrow W^- \bar{b}) \times BR(W^- \rightarrow jj/l^- \nu_l)$



# Estimators and $\chi^2$ Analysis: Angular Asymmetries

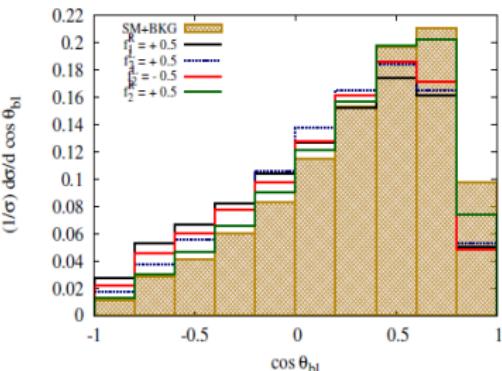
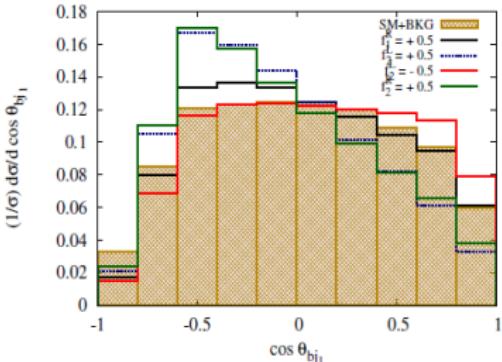


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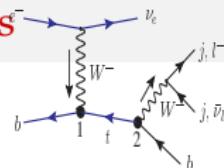
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# Estimators and $\chi^2$ Analysis: Angular Asymmetries

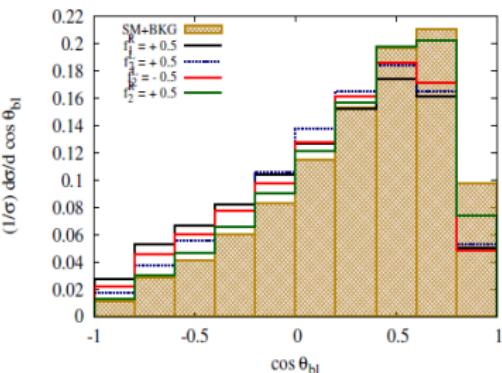
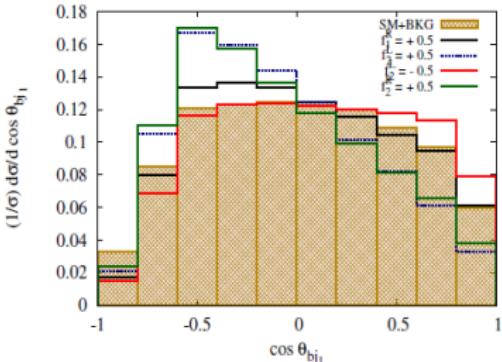


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## Estimators and $\chi^2$ Analysis: Angular Asymmetries

Hadronic:

	$A_{\Delta\Phi_{\ell_T j_1}}$	$A_{\Delta\Phi_{\ell_T \bar{b}}}$	$A_{\Delta\Phi_{\ell_T W^-}}$	$A_{\Delta\Phi_{W^- \bar{b}}}$	$A_{\theta_{\bar{b}j_1}}$	$A_{\Delta\eta_{bj_1}}$
SM + $\sum_i$ Bkg <sub>i</sub>	.532 ± .003	.282 ± .005	.503 ± .004	.799 ± .003	.023 ± .001	-.712 ± .003
$f_1^R = +.5$	.327 ± .004	.231 ± .004	.564 ± .004	.778 ± .003	.0005 ± .004	-.806 ± .003
$f_2^L = -.5$	.528 ± .004	.082 ± .004	.716 ± .003	.748 ± .003	-.196 ± .004	-.868 ± .002
$f_2^L = +.5$	.390 ± .005	.269 ± .004	.585 ± .004	.683 ± .004	.106 ± .005	-.795 ± .003
$f_2^R = +.5$	.330 ± .004	.363 ± .004	.566 ± .003	.656 ± .003	-.197 ± .004	-.823 ± .002

Leptonic:

	$A_{\Delta\Phi_{\ell_T l_1}}$	$A_{\Delta\Phi_{\ell_T \bar{b}}}$	$A_{\theta_{\bar{b}l_1}}$	$A_{\Delta\eta_{\bar{b}l_1}}$
SM + $\sum_i$ Bkg <sub>i</sub>	.384 ± .004	.710 ± .003	.551 ± .006	-.765 ± .007
$f_1^R = +.5$	.484 ± .004	.702 ± .003	.332 ± .006	-.821 ± .003
$f_2^L = -.5$	.526 ± .004	.620 ± .003	.410 ± .006	-.831 ± .002
$f_2^L = +.5$	.353 ± .005	.812 ± .003	.392 ± .007	-.850 ± .003
$f_2^R = +.5$	.424 ± .004	.684 ± .003	.507 ± .005	-.809 ± .003

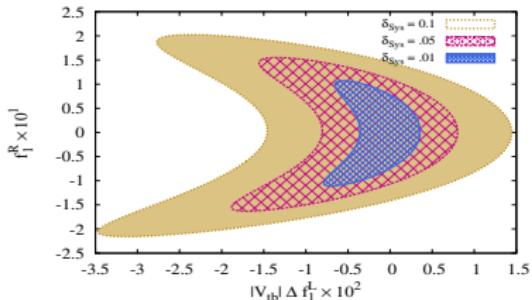
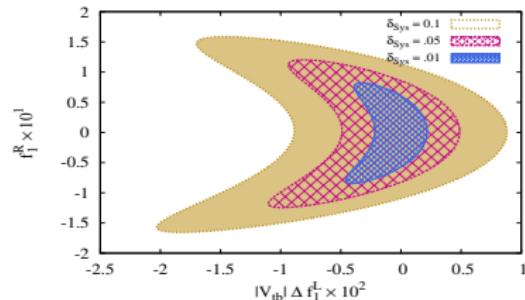


# Estimators and $\chi^2$ Analysis: Bin Analysis

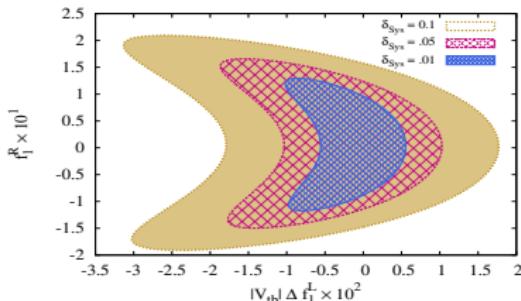
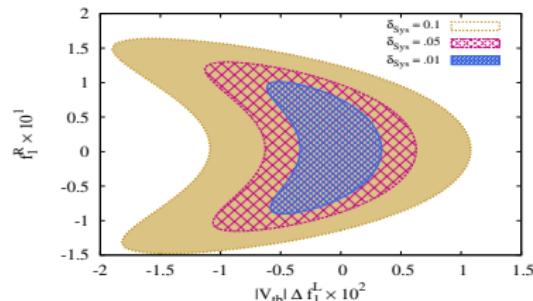
$$\chi^2(f_i, f_j) = \sum_{k=1}^N \left( \frac{\mathcal{N}_k^{\text{SM}+\sum_i \text{Bkg}_i} - \mathcal{N}_k^{\text{th}}(f_i, f_j)}{\delta \mathcal{N}_k^{\text{SM}+\sum_i \text{Bkg}_i}} \right)^2,$$

where  $\delta \mathcal{N}_k^{\text{SM}+\sum_i \text{Bkg}_i} = \sqrt{\mathcal{N}_k^{\text{SM}+\sum_i \text{Bkg}_i} \left( 1 + \delta_{\text{sys}}^2 \mathcal{N}_k^{\text{SM}+\sum_i \text{Bkg}_i} \right)}$ .

Hadronic



Leptonic



# Estimators and $\chi^2$ Analysis: Error & Correlation

Errors and Correlation matrix:

- $\chi^2(f_i, f_j) = \chi_{\min}^2 + \sum_{i,j} (f_i - \bar{f}_i) [V^{-1}]_{ij} (f_j - \bar{f}_j)$ , where  
 $f_i - \bar{f}_i = \pm \Delta f_i = \pm \sqrt{V_{ii}}$ ,  $\rho_{ij} = V_{ij} / \sqrt{V_{ii} V_{jj}}$ .
- $\chi_{\text{comb.}}^2(f_i, f_j) = \sum_{k=1}^n \chi_{\text{mink}}^2 + \sum_{k=1}^n \sum_{i,j} (f_i - \bar{f}_i) [V^{-1}]_{ij} (f_j - \bar{f}_j)$   
 $|V_{tb}| \Delta f_1^L = \pm 3.2 \times 10^{-4}$        $f_1^R = \pm 4.6 \times 10^{-4}$        $f_2^L = \pm 4.2 \times 10^{-4}$        $f_2^R = \pm 2.6 \times 10^{-4}$   
$$\begin{pmatrix} 1 & & & \\ -.05 & 1 & & \\ -.04 & -.06 & 1 & \\ -.02 & .03 & -.04 & 1 \end{pmatrix}$$

Luminosity Error:  $L \equiv \beta \bar{L}$ ,  $\beta = 1 \pm \Delta\beta$ ;  $\chi_{\text{comb.}}^2(f_i, f_j) \rightarrow \chi_{\text{comb.}}^2(f_i, f_j, \beta)$

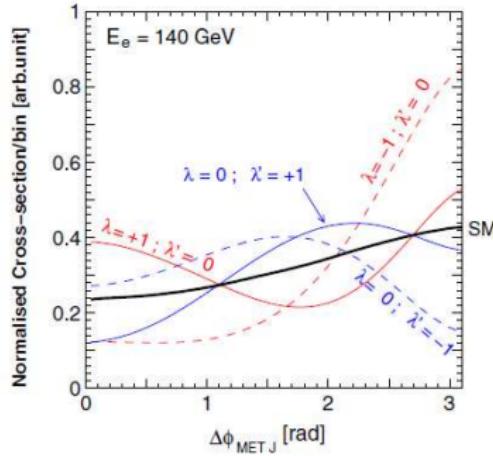
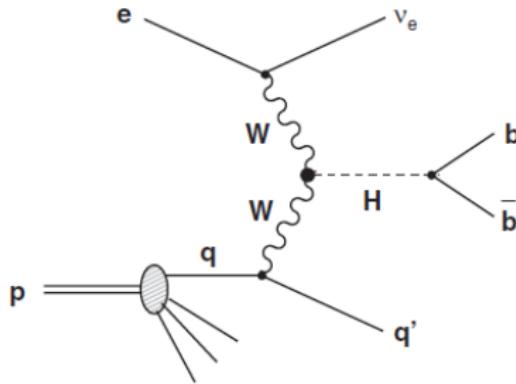
- $\chi_{\text{comb.}}^2(f_i, f_j, \beta) = \sum_{k=1}^n \chi_{\text{mink}}^2 + \sum_{k=1}^n \sum_{i,j} (f_i - \bar{f}_i) [V^{-1}]_{ij} (f_j - \bar{f}_j) + \left( \frac{\beta_k - 1}{\Delta\beta_k} \right)^2$   
 $|V_{tb}| \Delta f_1^L = \pm 5.0 \times 10^{-2}$        $f_1^R = \pm 4.6 \times 10^{-4}$        $f_2^L = \pm 4.2 \times 10^{-4}$        $f_2^R = \pm 2.6 \times 10^{-4}$   
$$\begin{pmatrix} 1 & & & \\ 0 & 1 & & \\ 0 & -.068 & 1 & \\ 0 & .032 & -.041 & 1 \end{pmatrix}$$
 with  $\Delta\beta = 10\%$ .

## Conclusion

- ▶ We observe high yields of single anti-top quark production with fiducial efficiency of  $\sim 70\%$  and  $\sim 90\%$  in the hadronic and leptonic decay of  $W^-$ , respectively after imposing selection cuts.
- ▶ Sensitivity of polarization of  $W^-$  helicities are studied with respect to variation of anomalous couplings.
- ▶ Asymmetries of different kinematic variable provide the sensitivity of anomalous couplings of the order of  $10^{-1}$ .
- ▶ Exclusion contours through bin analysis further improves the sensitivity of anomalous couplings to the order of  $10^{-3} - 10^{-2}$  for  $|V_{tb}| \Delta f_1^L$  with the variation of 1%-10% systematic error and others are of order  $10^{-2}-10^{-1}$  at 95%.
- ▶ Combined analysis through error and correlation matrix improves the sensitivity of the left-handed vector and tensor couplings to the order of  $10^{-4}$ , while right-handed anomalous couplings remain same as in bin analysis.
- ▶ Luminosity error affect  $|V_{tb}| \Delta f_1^L$ .
- ▶ Overall comparison with different data shows that  $Wtb$  anomalous couplings can be probed at LHeC with very high accuracy.

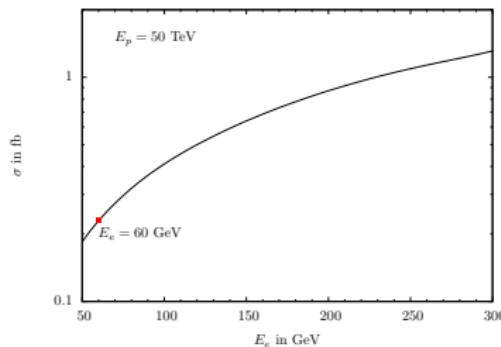
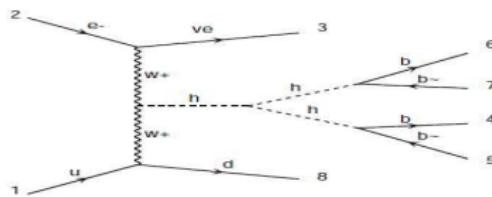
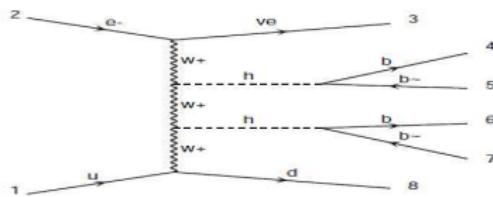
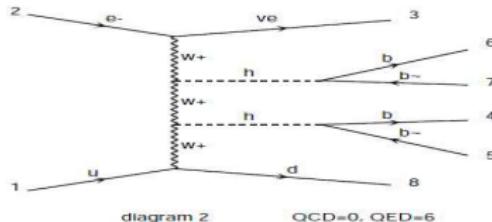
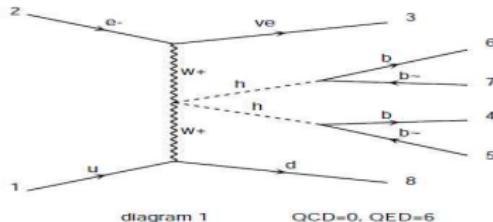
# Higgs at LHeC

- ▶ "Higgs boson searches and the  $Hb\bar{b}$  coupling at the LHeC", B. Mellado, Tao Han, PRD **82** 016009 (2010)
  - ▶ use of forward jet tagging as a means to secure the observation and to significantly improve the purity of the Higgs boson signal in  $H \rightarrow b\bar{b}$
- ▶ "Azimuthal angle probe of Anomalous  $HWW$  couplings at a High energy e p Collider", B. Mellado et al, PRL 109, 261801 (2012)
  - ▶  $\Gamma_{\mu\nu}^{SM} = -gM_V g_{\mu\nu}$
  - ▶  $\Gamma_{\mu\nu}^{BSM}(p, q) = \frac{g}{M_V} [\lambda(p \cdot q g_{\mu\nu} - p_\nu q_\mu) + \lambda' \epsilon_{\mu\nu\rho\sigma} p^\rho q^\sigma]$



# Di-higgs production at $e^- p$ Collider

CC production channel:  $e^- p \rightarrow \nu_e h h j, h \rightarrow b\bar{b}$



# Lagrangian and Effective vertices

- $\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{hhh}^{(3)} + \mathcal{L}_{hWW}^{(3)} + \mathcal{L}_{hhWW}^{(4)}$ , where

$$\mathcal{L}_{hhh}^{(3)} = \frac{m_h^2}{2v} (1 - g_{hhh}^{(1)}) h^3 + \frac{1}{2} g_{hhh}^{(2)} h \partial_\mu h \partial^\mu h,$$

$$\mathcal{L}_{hWW}^{(3)} = -\frac{g}{2m_W} g_{hWW}^{(1)} W^{\mu\nu} W_{\mu\nu}^\dagger h - \frac{g}{m_W} \left[ g_{hWW}^{(2)} W^\nu \partial^\mu W_{\mu\nu}^\dagger h + \text{h.c.} \right] - \frac{g}{2m_W} \tilde{g}_{hWW} W^{\mu\nu} \tilde{W}_{\mu\nu}^\dagger h,$$

$$\mathcal{L}_{hhWW}^{(4)} = -\frac{g^2}{4m_W^2} g_{hhWW}^{(1)} W^{\mu\nu} W_{\mu\nu}^\dagger h^2 - \frac{g^2}{2m_W^2} \left[ g_{hhWW}^{(2)} W^\nu \partial^\mu W_{\mu\nu}^\dagger h^2 + \text{h.c.} \right] - \frac{g^2}{4m_W^2} \tilde{g}_{hhWW} W^{\mu\nu} \tilde{W}_{\mu\nu}^\dagger h^2$$

- Effective Vertices:

$$i\Gamma_{hhh} = -6iv\lambda_{SM}g_{hhh}^{(1)} - ig_{hhh}^{(2)}(p_1 \cdot p_2 + p_2 \cdot p_3 + p_3 \cdot p_1)$$

$$i\Gamma_{hW-W^+} = i \left[ \left\{ \frac{g^2}{2} v + \frac{g}{m_W} g_{hWW}^{(1)} p_2 \cdot p_3 + \frac{g}{m_W} g_{hWW}^{(2)} (p_2^2 + p_3^2) \right\} \eta^{\mu_2 \mu_3} \right.$$

$$\left. - \frac{g}{m_W} g_{hWW}^{(1)} p_2^{\mu_3} p_3^{\mu_2} - \frac{g}{m_W} g_{hWW}^{(2)} (p_2^{\mu_2} p_2^{\mu_3} + p_3^{\mu_2} p_3^{\mu_3}) - i \frac{g}{m_W} \tilde{g}_{hWW} \epsilon_{\mu_2 \mu_3 \mu \nu} p_2^\mu p_3^\nu \right]$$

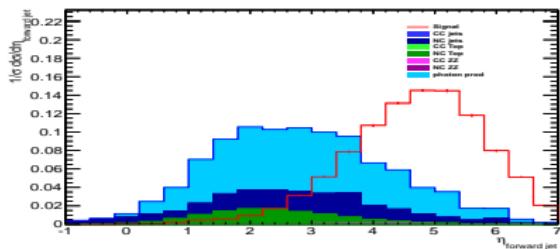
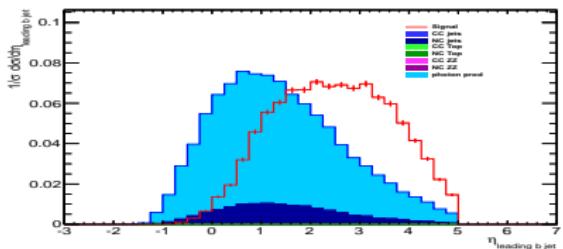
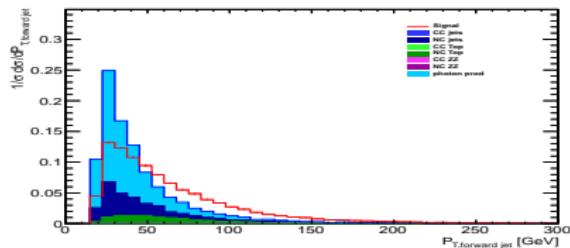
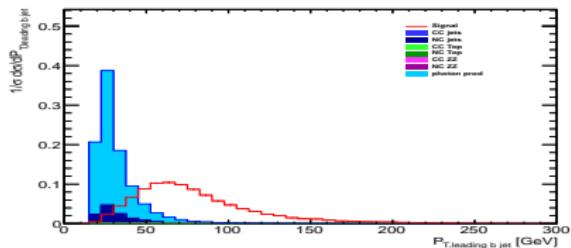
$$i\Gamma_{hhW-W^+} = i \left[ \left\{ \frac{g^2}{2} + \frac{g^2}{m_W^2} g_{hhWW}^{(1)} p_3 \cdot p_4 + \frac{g^2}{m_W^2} g_{hhWW}^{(2)} (p_3^2 + p_4^2) \right\} \eta^{\mu_3 \mu_4} \right.$$

$$\left. - \frac{g^2}{m_W^2} g_{hhWW}^{(1)} p_3^{\mu_4} p_4^{\mu_3} - \frac{g^2}{m_W^2} g_{hhWW}^{(2)} (p_3^{\mu_3} p_3^{\mu_4} + p_4^{\mu_3} p_4^{\mu_4}) - i \frac{g^2}{m_W^2} \tilde{g}_{hhWW} \epsilon_{\mu_3 \mu_4 \mu \nu} p_3^\mu p_4^\nu \right]$$

# Cross section and Distributions

Process	cc (fb)	nc (fb)	PHOTO (fb)
Signal:	2.40e-01		
$bbbbj$ :	8.20e-01	3.60e+03	2.85e+03
$bbjjj$ :	6.50e+03	2.50e+04	1.94e+06
$zzj(z \rightarrow bb)$ :	7.40e-01	1.65e-02	1.73e-02
$ttj$ (hadronic):	3.30e-01	1.40e+02	3.27e+02
$ttj$ (semi-leptonic):	1.22e-01	4.90e+01	1.05e+02

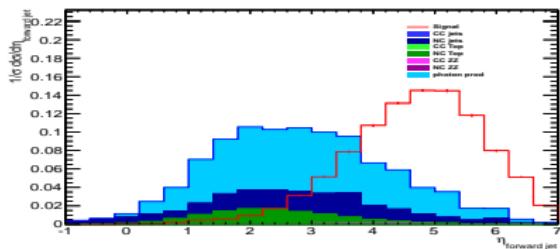
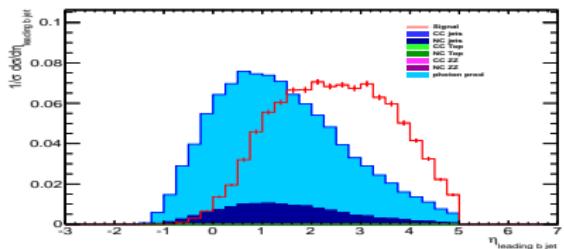
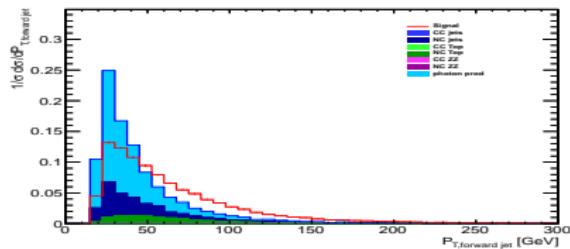
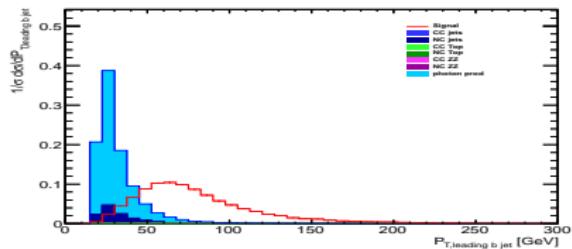
**Table :** Cross sections (in fb):  $E_e = 60$  GeV,  $E_p = 50$  TeV,  $j = g u \bar{u} d \bar{d} s \bar{s} c \bar{c}$ . Initial cuts:  $|\eta| \leq 10$  for jets, leptons and  $b$ ,  $P_T \geq 10$  GeV,  $\Delta R_{\min} = 0.4$  for all particles.



# Cross section and Distributions

Process	cc (fb)	nc (fb)	PHOTO (fb)
Signal:	2.40e-01		
$bbbbj$ :	8.20e-01	3.60e+03	2.85e+03
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$zzj(z \rightarrow bb)$ :	7.40e-01	1.65e-02	1.73e-02
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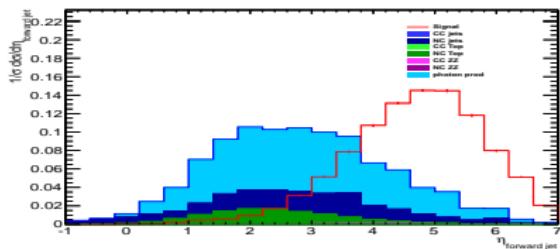
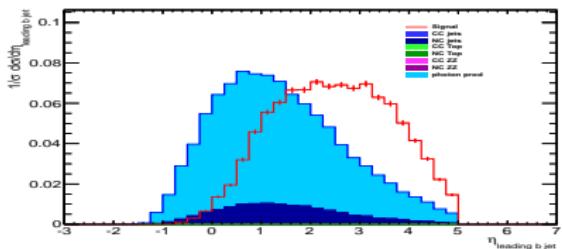
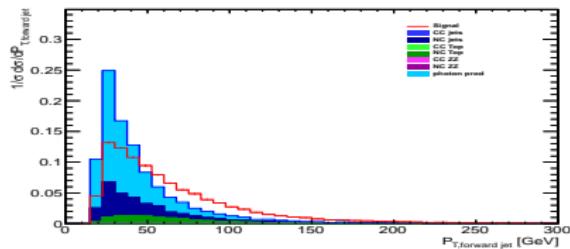
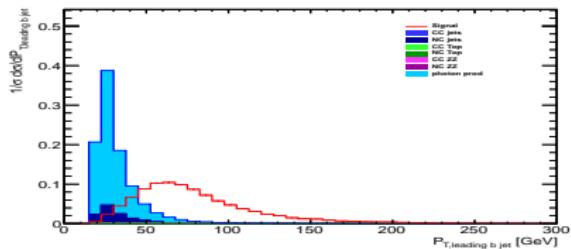
**Table :** Cross sections (in fb):  $E_e = 60$  GeV,  $E_p = 50$  TeV,  $j = g u \bar{u} d \bar{d} s \bar{s} c \bar{c}$ . Initial cuts:  $|\eta| \leq 10$  for jets, leptons and  $b$ ,  $P_T \geq 10$  GeV,  $\Delta R_{\min} = 0.4$  for all particles.



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## Cut-based Analysis

- ▶ Select 4  $b$  + 1-jet:  $p_T^{jet} > 20 \text{ GeV}$ ,  $|\eta| < 7$  for *non-b*-jets,  $|\eta| < 5$  for  $b$ -jets. The four  $b$  jets must be well separated within  $\Delta R > 0.7$  in case of the overlapped truth matching in the  $b$ -tagging.
- ▶ Rejecting leptons with  $p_T^{e^-} > 10 \text{ GeV}$  (suppress the NC process)
- ▶  $\eta_{forward-jet} > 4.0$ , the forward jet as defined as the *non-b*-jet which has the largest  $p_T$  after selecting at least 4  $b$ -jets.
- ▶  $E_T^{miss} > 40 \text{ GeV}$  and  $\Delta\Phi_{E_T^{miss}, leadingjet} > 0.4$ ,  $\Delta\Phi_{E_T^{miss}, subleadingjet} > 0.4$ .
- ▶ Pair the four  $b$ -jets into two pairs and calculate the invariant masses of each pair. The composition of the pairs which has the smallest variance of mass to  $(m_H - 40) \text{ GeV}$  is chosen. The first pair is defined as  $90 < M_1 < 125$ , which must have the leading  $b$ -jet. The other pair is defined as  $75 < M_2 < 125$ .
- ▶ Choosing the invariant mass of all four  $b$ -jets  $> 280 \text{ GeV}$ .

Significance:  $s = \sqrt{2((S+B)\log(1+S/B)-S)}$

Expected relative error:  $\frac{\Delta S}{S} = \frac{\sqrt{2 \times S + 2 \times B + (0.05 \times S)^2 + (0.05 \times B)^2}}{S}$ , where S and B are expected signal and background yields in  $\mathcal{L} = 10 ab^{-1}$  with 5% systematic error.

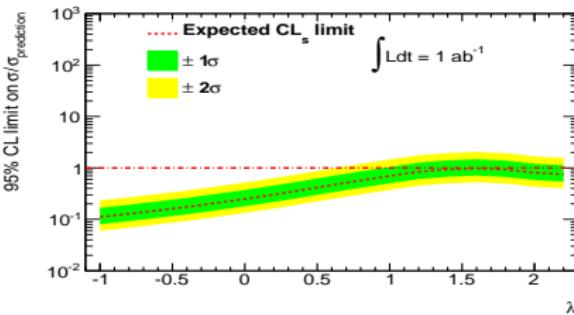
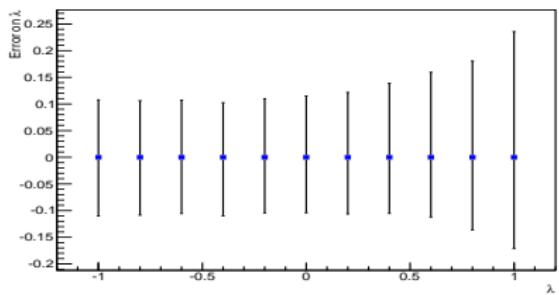
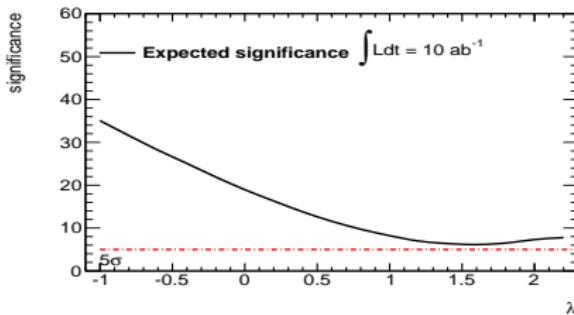
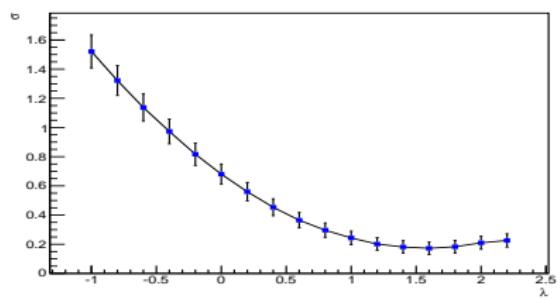
# Cut-based Analysis

Samples	Signal	CCJet	NCJet	CCTop	NCTop
Initial	$2.36e+03 \pm 4.82$	$6.45e+06 \pm 9.3e+03$	$2.5e+08 \pm 4.26e+05$	$4.49e+03 \pm 5.03$	$7.4e+06 \pm 6.86e+03$
4 b and 1 light jets	$299 \pm 1.16$	$293 \pm 7.56$	$2.23e+04 \pm 678$	$5.72 \pm 0.023$	$9.87e+03 \pm 31.1$
Electron rejection	$299 \pm 1.16$	$293 \pm 7.56$	$6.84e+03 \pm 385$	$5.66 \pm 0.0229$	$6.43e+03 \pm 28$
Forward jet	$224 \pm 1.01$	$22.9 \pm 1.39$	$864 \pm 65.1$	$0.399 \pm 0.00537$	$307 \pm 5.8$
$E_T^{\text{miss}}$	$149 \pm 0.823$	$18.7 \pm 0.981$	$93.9 \pm 26.7$	$0.372 \pm 0.00524$	$85.4 \pm 2.86$
$E_T^{\text{miss}} - \phi$ rejection	$128 \pm 0.76$	$16.8 \pm 0.957$	$45.3 \pm 14$	$0.326 \pm 0.00493$	$63.6 \pm 2.48$
$M_1 M_2$	$71 \pm 0.568$	$1.49 \pm 0.216$	$0.151 \pm 0.0866$	$0.06 \pm 0.00212$	$11.1 \pm 1.08$
$M_{4b}$	$63.4 \pm 0.536$	$0.849 \pm 0.191$	$0.151 \pm 0.0866$	$0.0346 \pm 0.00141$	$5.4 \pm 0.776$
Samples	CCZZj	NCZZj	NCPhotoProd	Total background	Significance
Initial	$7.36e+03 \pm 10.6$	$338 \pm 0.426$	$2.1e+09 \pm 3.43e+06$	$2.36e+09 \pm 3.5e+06$	$0.049$
4 b and 1 light jets	$678 \pm 2.19$	$21.7 \pm 0.0707$	$7.36e+04 \pm 4.21e+03$	$1.07e+05 \pm 4.3e+03$	$0.92$
Electron rejection	$678 \pm 2.19$	$14 \pm 0.0614$	$6.23e+04 \pm 1.29e+03$	$7.65e+04 \pm 1.4e+03$	$1.1$
Forward jet	$380 \pm 1.64$	$1.04 \pm 0.014$	$1.43e+04 \pm 297$	$1.59e+04 \pm 3e+02$	$1.8$
$E_T^{\text{miss}}$	$342 \pm 1.55$	$0.18 \pm 0.00575$	$980 \pm 21.9$	$1.52e+03 \pm 35$	$3.8$
$E_T^{\text{miss}} - \phi$ rejection	$287 \pm 1.42$	$0.1 \pm 0.00427$	$440 \pm 10.4$	$853 \pm 18$	$4.3$
$M_1 M_2$	$16.8 \pm 0.344$	$0.00613 \pm 0.00117$	$54.4 \pm 1.21$	$84.00 \pm 1.68$	$6.9$
$M_{4b}$	$7.43 \pm 0.229$	$0.00239 \pm 0.000661$	$21.9 \pm 0.63$	$35.78 \pm 1.05$	$8.7$

**Table :** Number of events after optimization and weighted with luminosity  $\mathcal{L} = 10 \text{ ab}^{-1}$ . The abbreviations CC(NC)Jet and CC(NC)Top accounts for the weighted sum of CC(NC) backgrounds 1, 2 and 4, 5 as given in Table 1. NCPhotoProd refer to weighted sum of all photo-production.

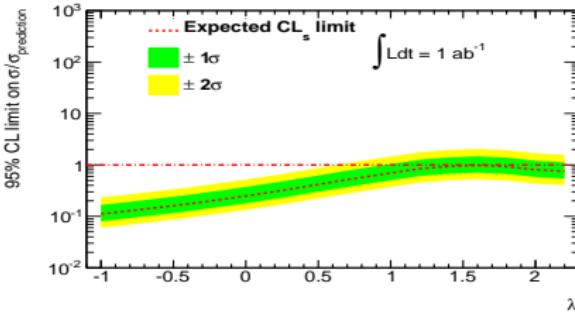
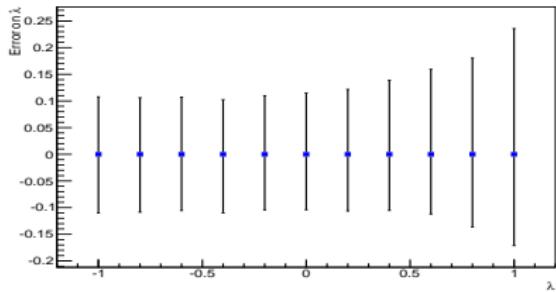
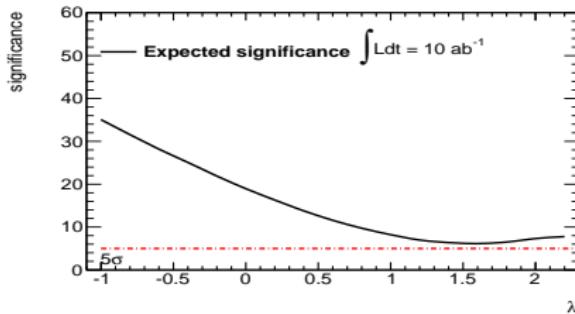
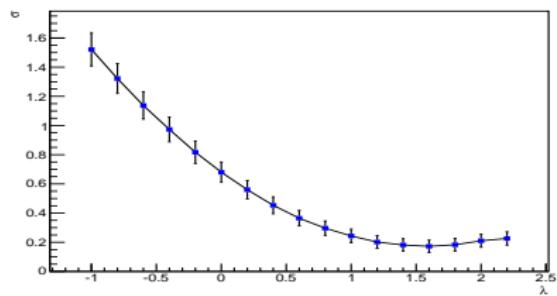
# Statistical Analysis

- ▶  $g_{hhh}^{(1)} \rightarrow \lambda, g_{hhh}^{(2)} \sim 10^{-4} - 10^{-3},$
- ▶  $g_{hWW}^{(1)} \sim 10^{-1}, g_{hWW}^{(2)} \sim 10^{-3} - 10^{-2},$
- ▶  $g_{hhWW}^{(1)} \sim 10^{-2}, g_{hhWW}^{(2)} \sim 10^{-3} - 10^{-2},$
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