

# New Rare Decay Results from KTeV

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Data from the KTeV experiment have provided many opportunities for studies of fundamental symmetries in nature, not just CP. We present new limits on lepton flavor violation and a new result concerning the parity of the  $\pi^0$ . We also present studies relevant to the underlying contributions to the decays  $K_L \rightarrow \pi^0 ll$ .

## 1. Introduction

Fundamental symmetries have yielded a significant number of insights into the interactions of fundamental particles. While CP violation has been intensely studied for signs of new physics, only recently has lepton flavor violation exposed cracks in the Standard Model. It is not presently clear what kind of mechanism is responsible for the violation of lepton flavor symmetry, and the situation is not helped by the fact that the violation of this symmetry has thus far appeared in only the neutrino sector, where experiments are extremely challenging. New limits on other manifestations of LFV may be very useful in constraining models, while the kaon sector provides a landscape where backgrounds to such searches are quite manageable. However, heavily suppressed CP violating decays, such as  $K_L \rightarrow \pi^0 ll$ , remain sensitive probes of physics beyond the Standard Model owing to the ease with which the SM predictions can be produced. Finally, CPT remains one of the few conserved symmetries, and as such is an excellent place in which to look for new physics.

## 2. The KTeV Experiment

KTeV is the culmination of a series of kaon experiments at Fermilab. The project consisted of two different experiments sharing a common detector. E799-II focused on rare  $K_L$  decays. E832 was designed to establish the existence of Direct CP violation in  $K \rightarrow \pi\pi$ . The KTeV detector,

described more fully in [6] consisted of a long vacuum decay volume followed by a magnetic spectrometer, a very high performance CsI crystal calorimeter and finally a muon veto. KTeV, when operating in E799 configuration, also included a transition radiation detection (TRD) system, designed to improve the detector's already excellent particle ID capability. In this mode, two nearly parallel  $K_L$  beams were produced. On the other hand, the E832 configuration inserted an active regenerator, consisting of a series of plastic scintillator blocks instrumented with PMTs, into the beam. This regenerator alternated between the two kaon beams, and had the effect of transforming the relevant beam into a coherent  $K_L$ - $K_S$  beam.

## 3. The parity of the $\pi^0$

There has been considerable direct [1] and indirect [3,2] evidence of the pseudo-scalar nature of the  $\pi^0$  for some time. While the fact that the  $\pi^0$  is a pseudo-scalar is not in doubt, it is interesting to re-examine the issue by studying the decay  $\pi^0 \rightarrow e^+e^-e^+e^-$ . In this decay, each electron-positron pair act as an analyzer that reveals the polarization of the virtual photon from the underlying decay  $\pi^0 \rightarrow \gamma^*\gamma^*$ , and thus expose the parity of the  $\pi^0$ .

Data from the 4-track trigger of KTeV's E799 phase were filtered in order to expose events consistent with the decays  $K_L \rightarrow \pi^0\pi^0\pi^0_{DD}$ ,  $\pi^0_{DD} = \pi^0 \rightarrow e^+e^-e^+e^-$ . The first requirement was that two pairs of electromag-

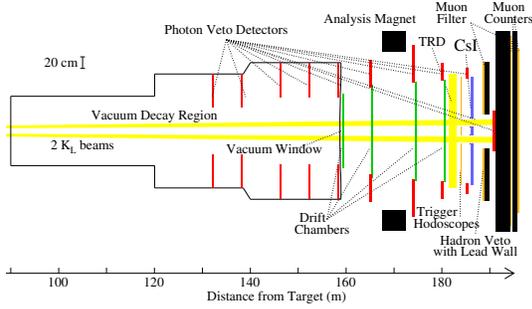


Figure 1. A cartoon of the KTeV detector in the E799 configuration. The relative positions of the major detector components are shown, including the drift chambers and CsI calorimeter. Notice the twin kaon beams entering the detector.

netic clusters in the CsI calorimeter, unassociated with charged tracks, reconstruct with an invariant masses consistent with a  $\pi^0$ . The second requirement was that there are also four charged tracks in the detector whose energy deposition in the calorimeter are consistent with electrons/positrons. The momenta of the four tracks must yield a combined invariant mass also consistent with a  $\pi^0$ . Finally, the invariant mass of the entire system was required to be equal to that of the parent  $K_L$ . The summed momentum of all the daughter particles was also required to point back to the kaon production target. After these cuts and additional cuts detailed in [7] there are 30511 candidate events with an estimated background of 0.6%. The main background was from  $K_L \rightarrow \pi^0_D \pi^0_D \pi^0$  where  $\pi^0_D = \pi^0 \rightarrow e^+e^-\gamma$

Once the  $\pi^0 \rightarrow e^+e^-e^+e^-$  sample has been isolated, we can begin to analyze the kinematics of the decay. The plane of each Dalitz pair reveals the polarization of the parent virtual photon. It is thus necessary to determine how to form the Dalitz pairs. We choose the pairing of the particles in such that  $x_1 < x_2$  and the product  $x_1 \times x_2$  is minimized, where  $x_1$  and  $x_2$  are kinematic vari-

ables defined by:

$$x_i = \left( \frac{m_{e_i^+ e_i^-}}{M_{\pi^0}} \right)^2 \quad (1)$$

and are thus proportional to the invariant mass of each Dalitz pair. Note that there will be mispairings introduced using this method, however this mispairing effect is minimized in the full treatment as detailed in [7] by utilizing a matrix element method. Once the  $e^+e^-$  pairs are formed, the angle  $\phi$  is defined as the angle between the normal to the plane formed by  $e_1^+e_1^-$  and the plane formed by  $e_2^+e_2^-$  as shown in Figure 2. The resulting distribution of the angle  $\phi$  is shown in Figure 3.

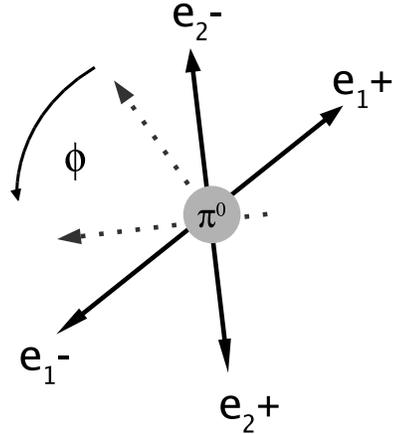


Figure 2. A graphical representation of the angle  $\phi$  between the planes of the Dalitz pairs in  $\pi^0 \rightarrow e^+e^-e^+e^-$ .

In addition to inspecting the distribution of the angle  $\phi$ , a detailed analysis of the form factor of the  $\pi^0 \rightarrow e^+e^-e^+e^-$  decay was carried out. For

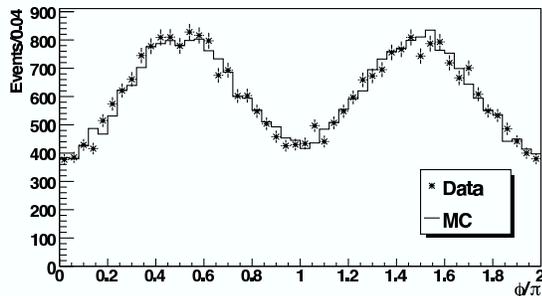


Figure 3. The distribution of angle between the planes defined by the two Dalitz pairs. There is a strong preference for the planes to be orthogonal, consistent with the parent being a pseudo-scalar particle. The non-zero number of events in the regions near  $\phi = 0, \pi, 2\pi$  are a result of mispairing of the Dalitz pairs.

this study, a maximum likelihood fit was carried out using the DIP model [4] and various additional terms which allow for scalar and CPT couplings [5]. The fit yields a value for the DIP parameter

$$\alpha = 1.3 \pm 1.0(stat) \pm 0.9(syst) \quad (2)$$

which compares favorably to the standard slope parameter from  $\pi^0 \rightarrow e^+e^-\gamma$ . In addition, the results of the fit constrain the presence of a scalar component in the decay to  $< 12.1\%$  ( $3.3\%$ ) at 90% confidence when CPT is assumed to be violated (conserved).

In order to measure the branching ratio of this decay, we must also select an additional sample in order to obtain a normalization sample. The decay  $K_L \rightarrow \pi^0_D \pi^0_D \pi^0$  where  $\pi^0_D = \pi^0 \rightarrow e^+e^-\gamma$  is selected as a normalization mode due to the similar final state. After all cuts, 141251 normalization events remain with a background of 0.5%. The main background was  $K_L \rightarrow \pi^0 \pi^0 \pi^0_{DD}$ . Using the number of  $K_L \rightarrow \pi^0 \pi^0 \pi^0_{DD}$  events to the number of  $K_L \rightarrow \pi^0_D \pi^0_D \pi^0$  events, along with the previously measured value of the Dalitz

branching ratio ( which is a leading contribution to the systematic error) we obtain:

$$Br(\pi^0 \rightarrow e^+e^-e^+e^-) = (3.26 \pm 0.18) \times 10^{-5} \quad (3)$$

The above result also includes a detailed treatment of radiative corrections [5]. It should be noted that the KTeV collaboration intends to release a new measurement of  $Br(\pi^0 \rightarrow e^+e^-\gamma)$  in the near future, at which point the above branching ratio can be recomputed and the systematic error reduced.

#### 4. Search for Lepton Flavor Violation

With the observation of neutrino oscillation [8] it is now known that lepton flavor is not a perfectly conserved symmetry of nature. With the root mechanism of neutrino oscillation still unknown, it is important to search for other manifestations of this symmetry violation. Neutral kaon decays can offer an alternative probe of LFV. The experimental signature is simple: the presence of a lepton pair  $\mu e$  in any kaon decay.

##### 4.1. Search for $K_L \rightarrow \pi^0 \mu^\pm e^\mp$

One decay mode which would exhibit LFV is  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$ . The E799 data set is filtered [9] to look for events in which there is a charged track which matches hits in the muon detector, implying that a muon is indeed present. The other charged track must then have a CsI cluster whose energy is equal to the momentum as measured using magnetic deflection, implying that the shower in the CsI was electromagnetic in origin and thus due to an electron. Additionally, the TRD info for the electron-like track must also be consistent with an electron. Only events with two charged tracks are accepted. Additionally, there must be two more CsI clusters not associated with any tracks, which come from the two  $\gamma$ s from the  $\pi^0$ . With these requirements, the signal is dominated by  $K_e3$  and/or  $K_e4$  decays where the pion either decays ( and thus produces an muon ) or punches through the CsI calorimeter to the muon detector. Making a tight cut on accidental activity in the detector eliminates extra CsI clusters which are needed for  $K_e3$  events to be accepted, while  $K_e4$  events can be reduced by calculating  $|p_\nu|$ , the

magnitude of the neutrino momentum assuming that the decay was actually a  $K_{e4}$  event, and then retaining events for which  $|p_\nu| < 0$ , which is the case when the  $K_{e4}$  hypothesis is incorrect.

Using a detailed Monte Carlo simulation of the decay and the detector, we define contours as a function of the  $\pi^0\mu e$  invariant mass and  $p_T^2$  (the squared component of the summed momentum which is transverse to the neutral kaon beam) which would enclose either 99% or 95% of the total  $\pi^0 \rightarrow \mu^\pm e^\mp$  sample. The 99% region is defined as the control region while the 95% region is defined as the signal region, and is blinded. Monte Carlo studies of all possible sources of backgrounds indicate that the background expected in the control region is  $4.21 \pm 0.53$  events while for the control region the expected number is  $0.66 \pm 0.23$  events. Unblinding the signal region, we observe no events, while we observe 5 events in the control region. This leads to a limit on the branching ratio of

$$Br(K_L \rightarrow \pi^0 \mu^\pm e^\mp) < 7.56 \times 10^{-11} \quad (4)$$

at 90% confidence, which is a factor of 83 lower than the previous limit [10].

#### 4.2. Search for $K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$

Very similar to  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$  is  $K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$ . The additional  $\pi^0$  requires the presence of two more CsI photon clusters for reconstruction, the side effect of which is a strong suppression of the accidental background which was an issue for  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$ . Due to the lower accidental background, it is possible to relax cuts relative to  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$  in order to raise the sensitivity—in this case the tight cut on accidental activity in the detector is removed, as is the TRD cut on the electron track. After applying these cuts, and others as detailed in [9], the primary background is  $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$  events. In order for  $K_L \rightarrow \pi^0 \pi^0 \pi^0_D$  events to contribute to the background, one electron must fail to deposit a significant amount of energy into the CsI calorimeter, and at the same time, there must be an accidental hit in the muon detector which matches the electron track. In order to prevent this, we place a loose requirement on the TRD information for the muon-like track, requir-

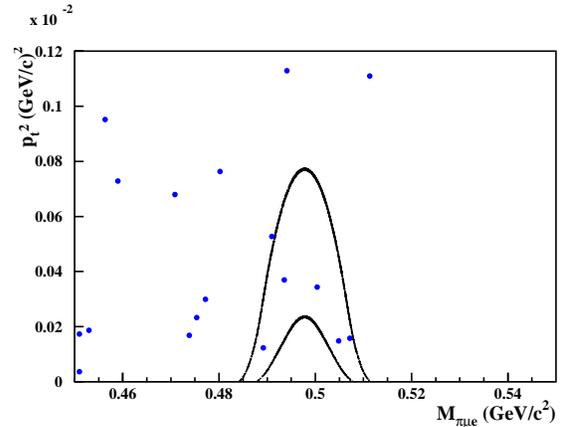


Figure 4. A plot of the invariant  $\pi^0\mu e$  mass versus transverse momentum squared for the  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$  sample. The larger (smaller) contour defines the region which encloses 99% (95%) of  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$  Monte Carlo events.

ing that the track is *not* electron-like. After this cut is added, there are an expected  $0.44 \pm 0.23$  background events in the signal region. In the data, after all cuts, there are no events in the signal region, leading to a branching ratio limit of:

$$Br(K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp) < 1.7 \times 10^{-10} \quad (5)$$

at 90 % confidence. This is the first limit placed on this decay.

#### 4.3. Search for $\pi^0 \rightarrow \mu^\pm e^\mp$

The  $K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$  search can be easily extended by noticing that the decay  $K_L \rightarrow \pi^0 \pi^0 \pi^0$ ,  $\pi^0 \rightarrow \mu^\pm e^\mp$  has the same final state. All that is required to constrain the rate at which this decay occurs is the additional requirement that the  $\mu e$  pair reconstruct near the  $\pi^0$  invariant mass. After enforcing this additional cut, we are led to the branching ratio limit of:

$$Br(\pi^0 \rightarrow \mu^\pm e^\mp) < 3.59 \times 10^{-10} \quad (6)$$

at 90 % confidence. This is a factor of 10 (2) times lower than the previous best limits on  $\pi^0 \rightarrow \mu^- e^+$

( $\pi^0 \rightarrow \mu^+ e^-$ ) [11,12]. Note that this analysis is equally sensitive to both charge modes.

#### 4.4. Final Note

It should be emphasized that all of the lepton flavor violating searches detailed here are background free. Specifically, the estimated background for  $K_L \rightarrow \pi^0 \mu^\pm e^\mp$  is 0.66, for  $K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$  the estimate is 0.44 and the expected background for  $\pi^0 \rightarrow \mu^\pm e^\mp$  is 0.03 events. This implies that a KTeV style experiment with additional beam intensity can further lower these limits, especially  $\pi^0 \rightarrow \mu^\pm e^\mp$  due to the multiplicity of neutral pions produced via  $K_L \rightarrow \pi^0 \pi^0 \pi^0$ .

### 5. CP conserving contributions to $K_L \rightarrow \pi^0 ll$

While lepton flavor violation is a direct gateway to new physics, various extensions to the Standard Model result in a multitude of new or enhanced CP violation effects. The suite of decays that comprise  $K_L \rightarrow \pi^0 ll$  are especially attractive targets for further study due to the heavily suppressed standard model predictions and the precision with which the SM predictions can be made.

#### 5.1. $K_L \rightarrow \pi^0 \gamma \gamma$

The vector meson exchange amplitude  $A_V$  can be used to determine the size of the CP conserving component of  $K_L \rightarrow \pi^0 ll$  [18] In order to produce a sample of  $K_L \rightarrow \pi^0 \gamma \gamma$  events, data from the E832 dataset is searched for events containing four CsI clusters, and no charged tracks. The energy of each of the CsI clusters is required to be above 2 GeV. The distribution of these photon clusters is also required to be consistent with a kaon decay within the E832 configuration's pure  $K_L$  beam. The clusters are then paired such that one pair yields an invariant mass within 3 MeV of the mass of the  $\pi^0$ , while the other pair is required to *not* reconstruct into a  $\pi^0$ . This last requirement suppresses the background due to  $K \rightarrow \pi \pi$ . After these cuts and others are applied [13] we are left with 1982 events with an expected background level of approximately 30%.

The decay  $K_L \rightarrow \pi^0 \pi^0$  was chosen as the normalization mode, as it has the same final state.

The resulting branching ratio is:

$$Br(K_L \rightarrow \pi^0 \gamma \gamma) = (1.29 \pm 0.06) \times 10^{-6} \quad (7)$$

which is consistent with the result from NA48 [15] and supersedes the previous KTeV result [14].

After having obtained a sample of  $K_L \rightarrow \pi^0 \gamma \gamma$  the resulting events were used to perform a likelihood fit using the model developed in [19] and the Dalitz variables  $Z_{Dalitz} = M_{34}^2/M_K^2$  and  $Y_{Dalitz} = (E_{\gamma 3} - E_{\gamma 4})/M_K$  where  $M_{34}$  is the invariant mass of the two photons which are not daughters of the  $\pi^0$ . The result is:

$$A_V = -0.31 \pm 0.05_{stat} \pm 0.07_{syst} \quad (8)$$

The distributions of the Dalitz plot variables for both data and Monte Carlo, generated using the best fit value of  $A_V$ , are shown in Figures 5 and 6.

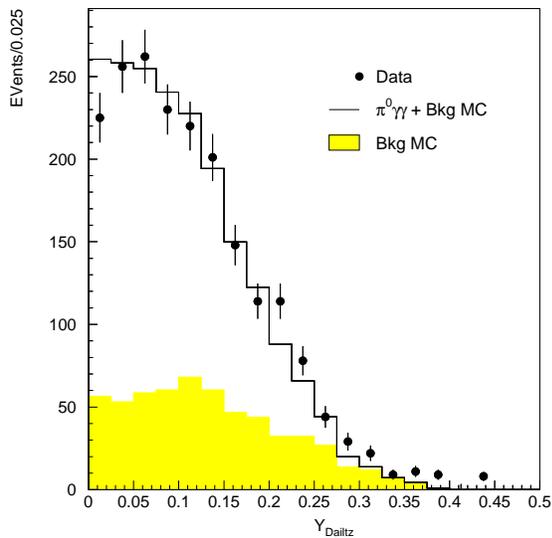


Figure 5. Distribution of the variable  $Y_{Dalitz}$  used in the analysis of  $K_L \rightarrow \pi^0 \gamma \gamma$ .

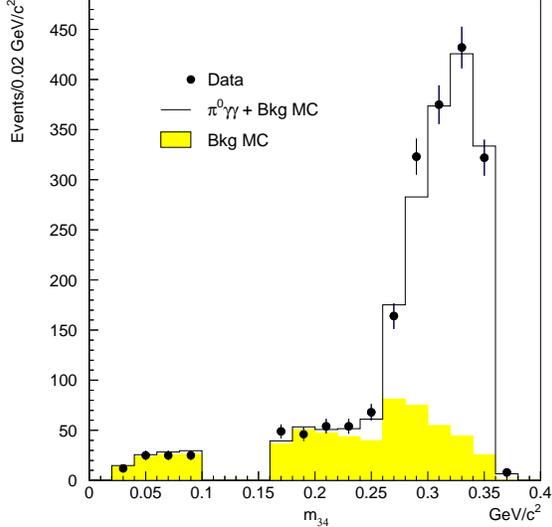


Figure 6. Distribution of the variable  $Z_{Dalitz}$  used in the analysis of  $K_L \rightarrow \pi^0 \gamma \gamma$ .

### 5.2. $K_L \rightarrow \pi^0 e^+ e^- \gamma$

This decay, which can be thought of as  $K_L \rightarrow \pi^0 \gamma^* \gamma$  also sees contributions from the vector meson exchange process, and as such can also be used to measure  $A_V$ . Reconstruction begins by looking for two charged tracks and three neutral CsI clusters, which are not associated with any tracks. Two of the three neutral CsI clusters are required to reconstruct with an invariant mass near the mass of the  $\pi^0$ . The decay vertex obtained from the  $\pi^0$  reconstruction is then used to compute both  $M_{ee\gamma}$  and  $M_{ee\gamma\gamma}$ . In this case the decay vertex obtained from the extrapolation of the two charged tracks is not used as the two electron trajectories are nearly parallel and overlapping in this decay. Finally an additional constraint is applied that requires that no combination of charged tracks and a photon may reconstruct near the invariant mass of the  $\pi^0$ . After application of these and additional cuts [16] we are left with 139 events with an estimated background of approximately 14.4 events.

Isolating the decay  $K_L \rightarrow \pi^0 \pi^0_D$ , which has the same final state and utilizing it as a normalization mode, we then obtain the branching ratio:

$$Br(K_L \rightarrow \pi^0 e^+ e^- \gamma) = (1.62 \pm 0.17) \times 10^{-8} \quad (9)$$

which supersedes the older KTeV result [17] which was affected by an older value of the  $K_L \rightarrow \pi^0 \pi^0_D$  branching ratio. This branching ratio measurement also compares favorably to the value obtained using Chiral Perturbation Theory, which is  $Br(K_L \rightarrow \pi^0 e^+ e^- \gamma)_{ChPT} = 1.51 \times 10^{-8}$  [20,16]. This value of the branching ratio also informs searches for  $K_L \rightarrow \pi^0 e^+ e^-$ , as the low value implies that this decay mode will not be a sizable contribution to the background for  $K_L \rightarrow \pi^0 e^+ e^-$ . Furthermore, the distribution of  $M_{\pi^0 ee}$  peaks well away from the kaon mass in this decay.

The sample of  $K_L \rightarrow \pi^0 e^+ e^- \gamma$  events can also be used to extract  $A_V$  much in the same way as  $K_L \rightarrow \pi^0 \gamma \gamma$ . Performing a likelihood fit using the model from Reference [19] and the kinematic variables  $Z_{Dalitz} = M_{ee\gamma}^2 / M_K^2$ ,  $Y_{Dalitz} = (E_\gamma - E_{ee}) / M_K$  and  $Q_{Dalitz} = M_{ee}^2 / M_K^2$ . Note that  $Z_{Dalitz}$  and  $Y_{Dalitz}$  are analogues of the same variables in  $K_L \rightarrow \pi^0 \gamma \gamma$ . The resulting fit produces

$$A_V = -0.76 \pm 0.16_{stat} \pm 0.07_{syst} \quad (10)$$

The distributions of the three kinematic variables, for data and Monte Carlo generated with the fitted value of  $A_V$ , are shown in Figure 7. This value is consistent with the value obtained from the KTeV analysis of  $K_L \rightarrow \pi^0 \gamma \gamma$  in addition to the value obtained by the NA48 collaboration [15] as shown in Figure 8.

These values for  $A_V$  indicate that CP violating terms will be the dominant contribution to  $K_L \rightarrow \pi^0 e^+ e^-$ .

## 6. Summary

The KTeV collaboration has recently produced a new determination of the parity of the  $\pi^0$  using the decay  $\pi^0 \rightarrow e^+ e^- e^+ e^-$  in addition to placing new limits on the presence of scalar and CPT violating contributions to its decay. In the lepton flavor violating sector, limits on the decays

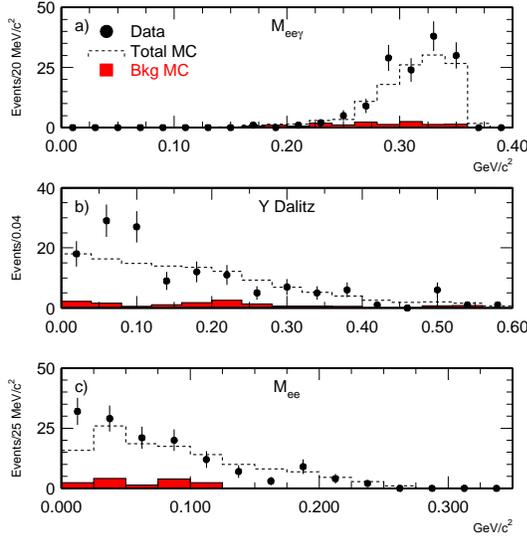


Figure 7. Distributions of the three Dalitz variables used in the analysis of  $K_L \rightarrow \pi^0 e^+ e^- \gamma$ .

$K_L \rightarrow \pi^0 \mu^\pm e^\mp$  and  $\pi^0 \rightarrow \mu^\pm e^\mp$  have been improved while the first limit has been set for the decay  $K_L \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$ . There were no expected backgrounds for all three decays, indicating that these limits could be improved in the future. Finally, the branching ratios for the related decays  $K_L \rightarrow \pi^0 \gamma \gamma$  and  $K_L \rightarrow \pi^0 e^+ e^- \gamma$  were measured. A Dalitz analysis of both decays was also carried out in order to produce two new estimates of the vector meson exchange amplitude  $A_V$ .

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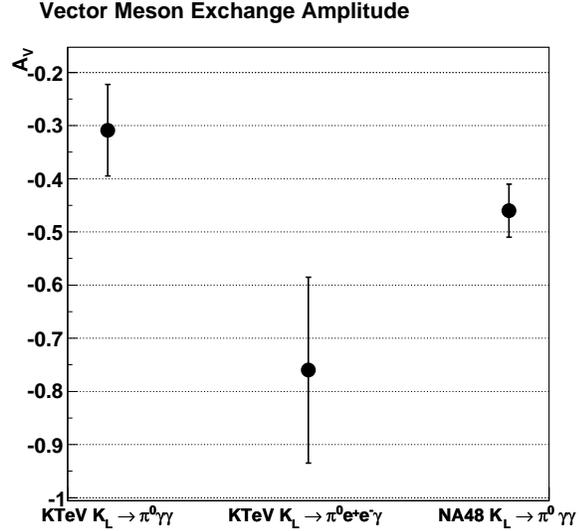


Figure 8. Recent measurements of the vector meson exchange amplitude  $A_V$

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