

# Introduction to hadron collider physics

## ***Theory challenges for LHC Physics***

*Dubna International Advanced School of Theoretical Physics*

*Helmholtz International Summer School*

**July 20-30 2015**

## **Lecture 3**

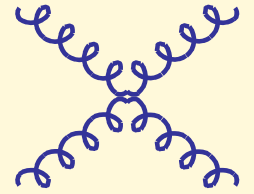
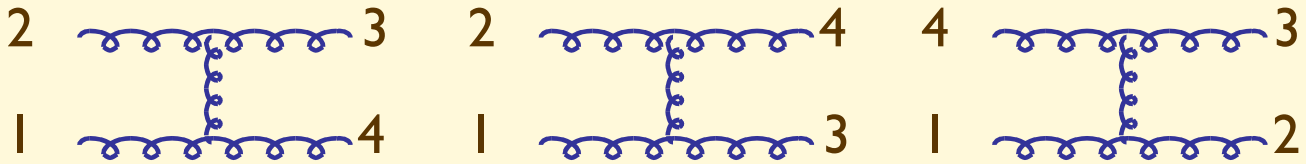
**Michelangelo L. Mangano**

TH Unit, Physics Department, CERN

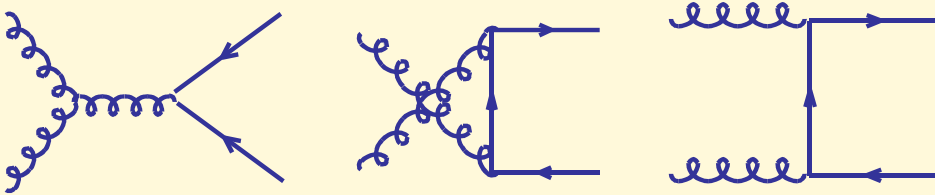
[michelangelo.mangano@cern.ch](mailto:michelangelo.mangano@cern.ch)

- Inclusive production of jets is the largest component of high- $Q$  phenomena in hadronic collisions
- QCD predictions are known up to NLO accuracy
- Intrinsic theoretical uncertainty (at NLO) is approximately 10%
- Uncertainty due to knowledge of parton densities varies from 5-10% (at low transverse momentum,  $p_T$  to 100% (at very high  $p_T$  corresponding to high- $x$  gluons)
- Jet are used as probes of the quark structure (possible substructure implies departures from point-like behaviour of cross-section), or as probes of new particles (peaks in the invariant mass distribution of jet pairs)

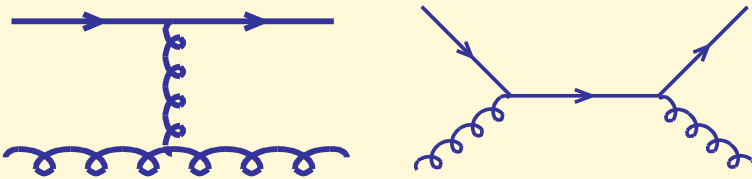
$gg \rightarrow gg$



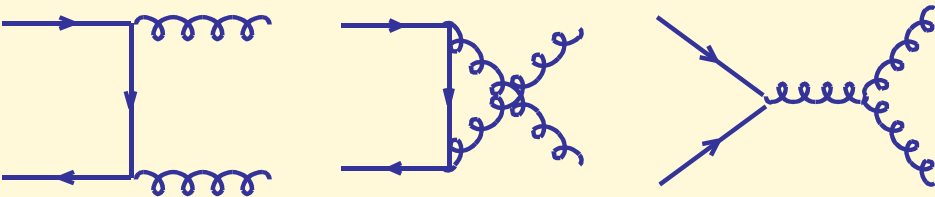
$gg \rightarrow q\bar{q}$



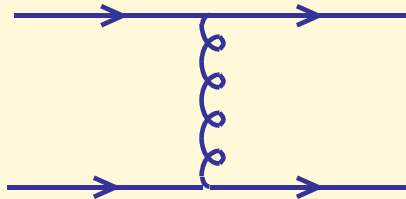
$qg \rightarrow qg$



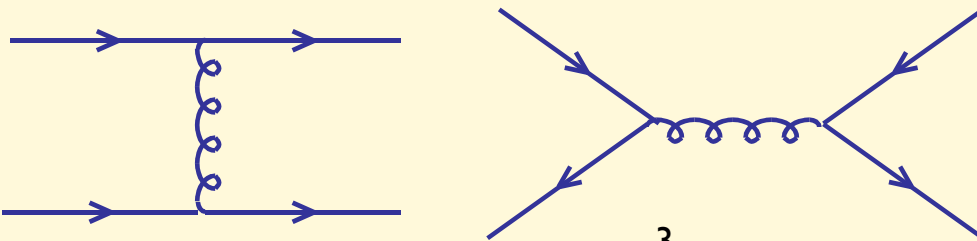
$q\bar{q} \rightarrow gg$



$qq' \rightarrow qq'$



$q\bar{q} \rightarrow q\bar{q}$

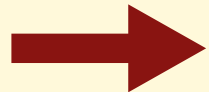


# Phase space and cross-section for LO jet production

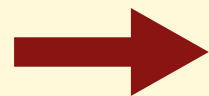
$$d[PS] = \frac{d^3 p_1}{(2\pi)^2 2p_1^0} \frac{d^3 p_2}{(2\pi)^2 2p_2^0} (2\pi)^4 \delta^4(P_{in} - P_{out}) dx_1 dx_2$$

$$(a) \quad \delta(E_{in} - E_{out}) \delta(P_{in}^z - P_{out}^z) dx_1 dx_2 = \frac{1}{2E_{beam}^2}$$

$$(b) \quad \frac{dp^z}{p^0} = dy \equiv d\eta$$



$$d[PS] = \frac{1}{4\pi S} p_T dp_T d\eta_1 d\eta_2$$



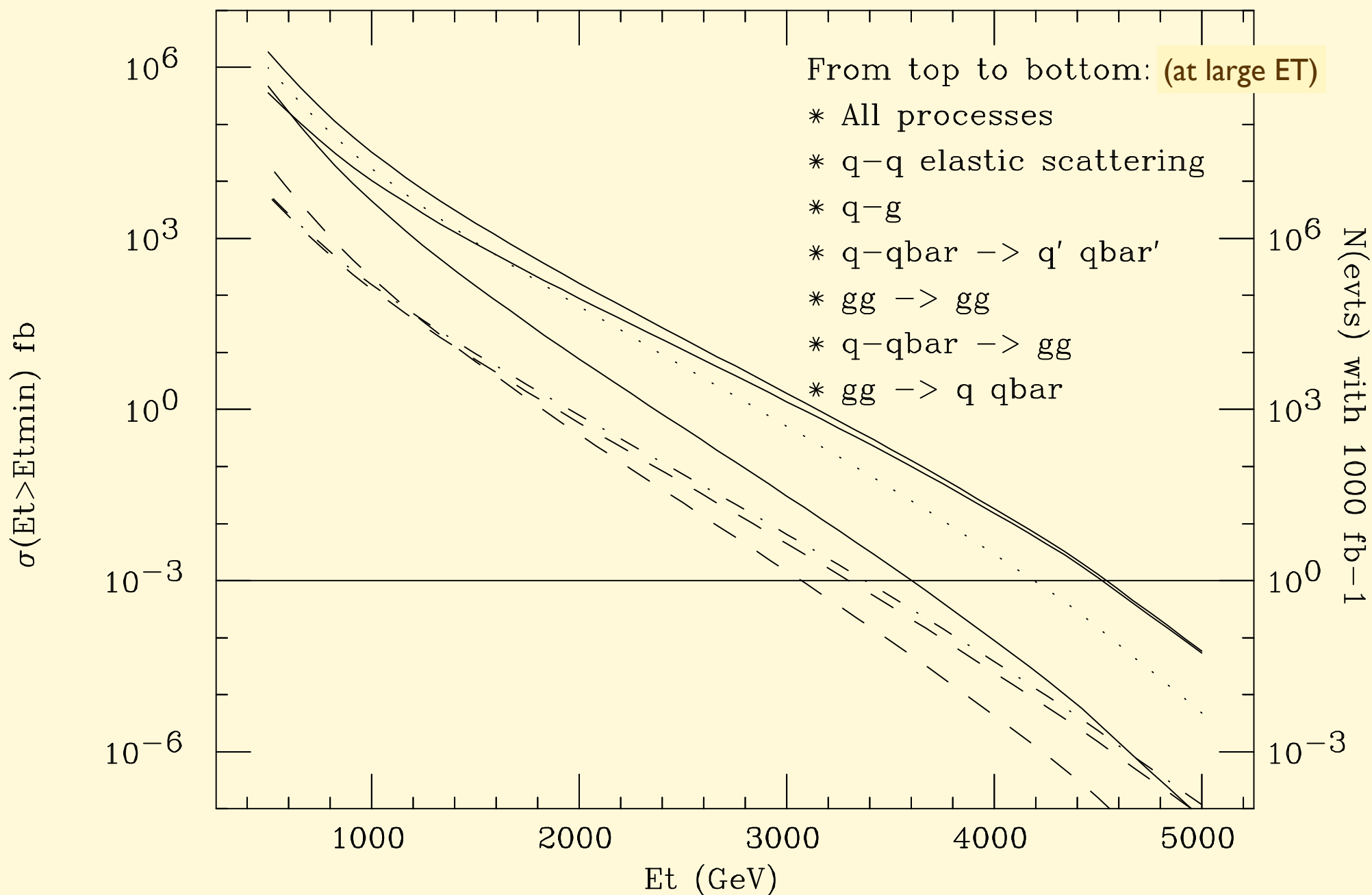
$$\frac{d^3 \sigma}{dp_T d\eta_1 d\eta_2} = \frac{p_T}{4\pi S} \sum_{i,j} f_i(x_1) f_j(x_2) \frac{1}{2\hat{s}} \sum_{kl} |M(ij \rightarrow kl)|^2$$

The measurement of  $p_T$  and rapidities for a dijet final state uniquely determines the parton momenta  $x_1$  and  $x_2$ . Knowledge of the partonic cross-section allows therefore the determination of partonic densities  $f(x)$

Process	$\frac{d\hat{\sigma}}{d\Phi_2}$	at 90°
$qq' \rightarrow qq'$	$\frac{4}{9} \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$	2.22
$qq \rightarrow qq$	$\left[ \frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{s}^2 + \hat{t}^2}{\hat{u}^2} \right) - \frac{8}{27} \frac{\hat{s}^2}{\hat{u}\hat{t}} \right]$	3.26
$q\bar{q} \rightarrow q'\bar{q}'$	$\frac{4}{9} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2}$	0.22
$q\bar{q} \rightarrow q\bar{q}$	$\left[ \frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2} \right) - \frac{8}{27} \frac{\hat{u}^2}{\hat{s}\hat{t}} \right]$	2.59
$q\bar{q} \rightarrow gg$	$\left[ \frac{32}{27} \frac{\hat{t}^2 + \hat{u}^2}{\hat{t}\hat{u}} - \frac{8}{3} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2} \right]$	1.04
$gg \rightarrow q\bar{q}$	$\left[ \frac{1}{6} \frac{\hat{t}^2 + \hat{u}^2}{\hat{t}\hat{u}} - \frac{3}{8} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2} \right]$	0.15
$gg \rightarrow qq$	$\left[ -\frac{4}{9} \frac{\hat{s}^2 + \hat{u}^2}{\hat{s}\hat{u}} + \frac{\hat{u}^2 + \hat{s}^2}{\hat{t}^2} \right]$	6.11
$gg \rightarrow gg$	$\frac{9}{2} \left( 3 - \frac{\hat{t}\hat{u}}{\hat{s}^2} - \frac{\hat{s}\hat{u}}{\hat{t}^2} - \frac{\hat{s}\hat{t}}{\hat{u}^2} \right)$	30.4

# Jet production rates at the LHC, subprocess composition

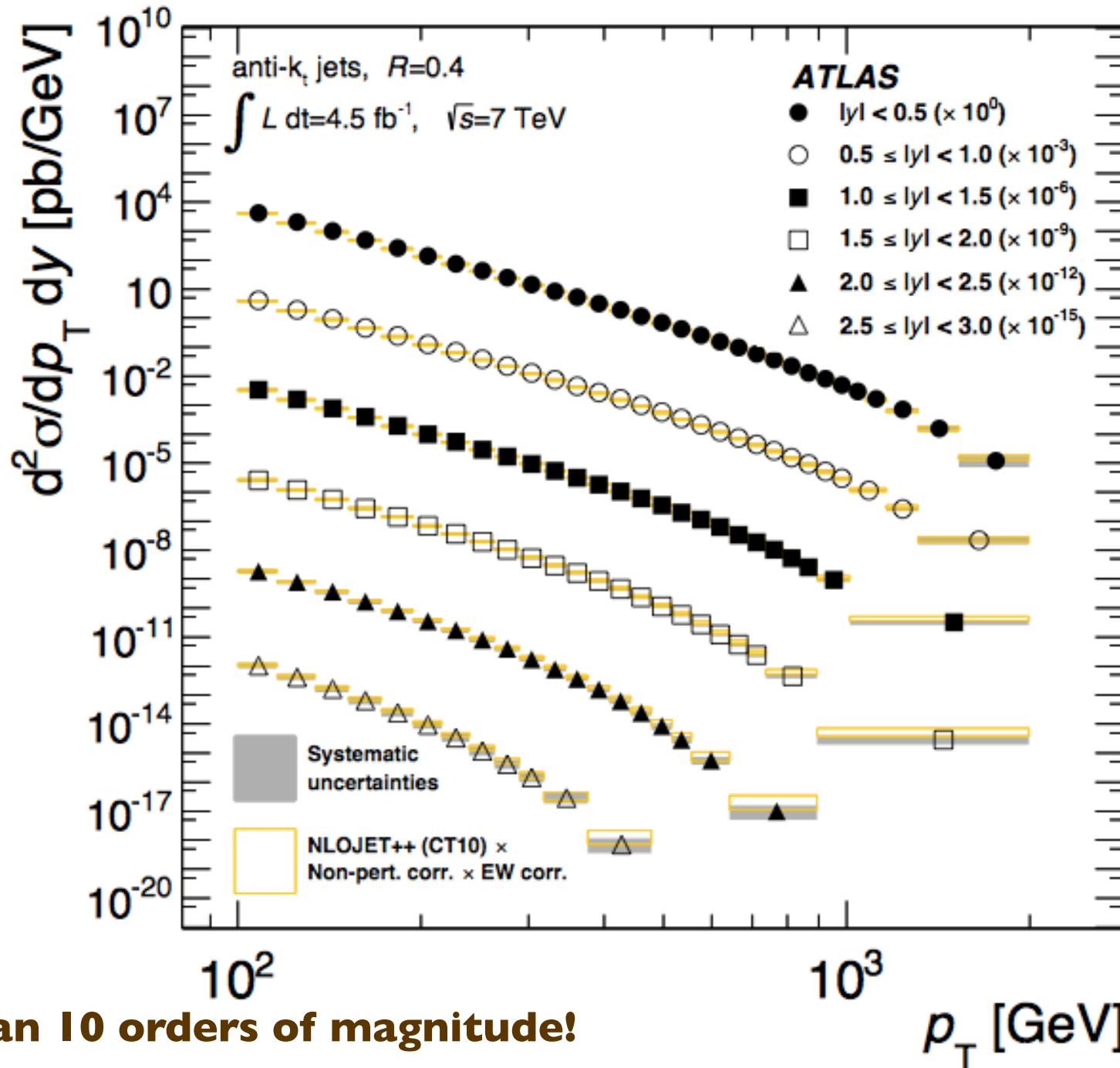
(this is at 14 TeV: results at 7 TeV are ~obtained by rescaling ET by 0.5)



# Some LHC results in jet physics

# Example: Jet cross section

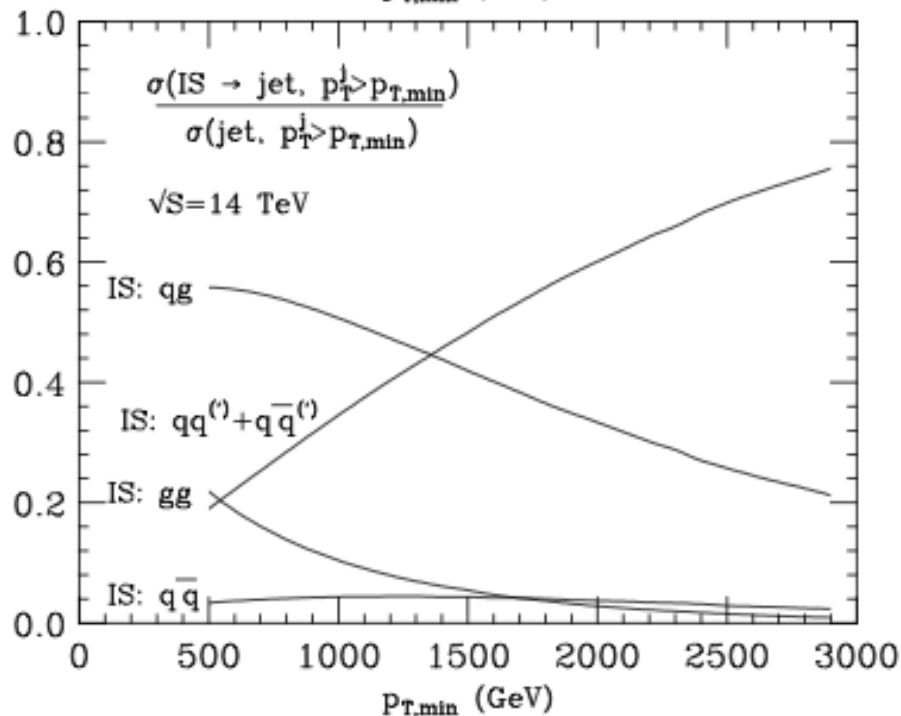
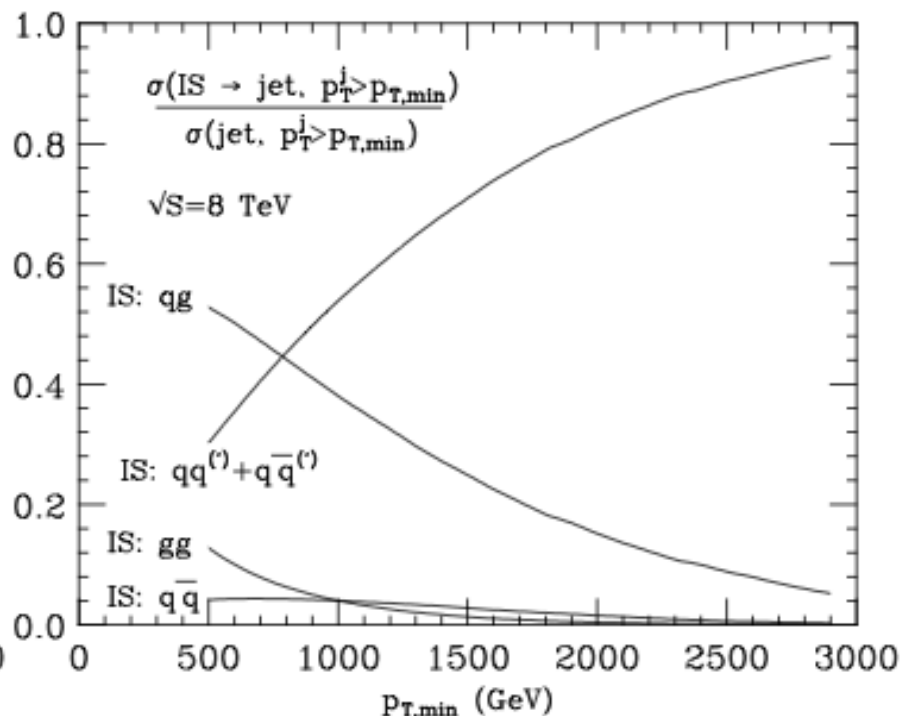
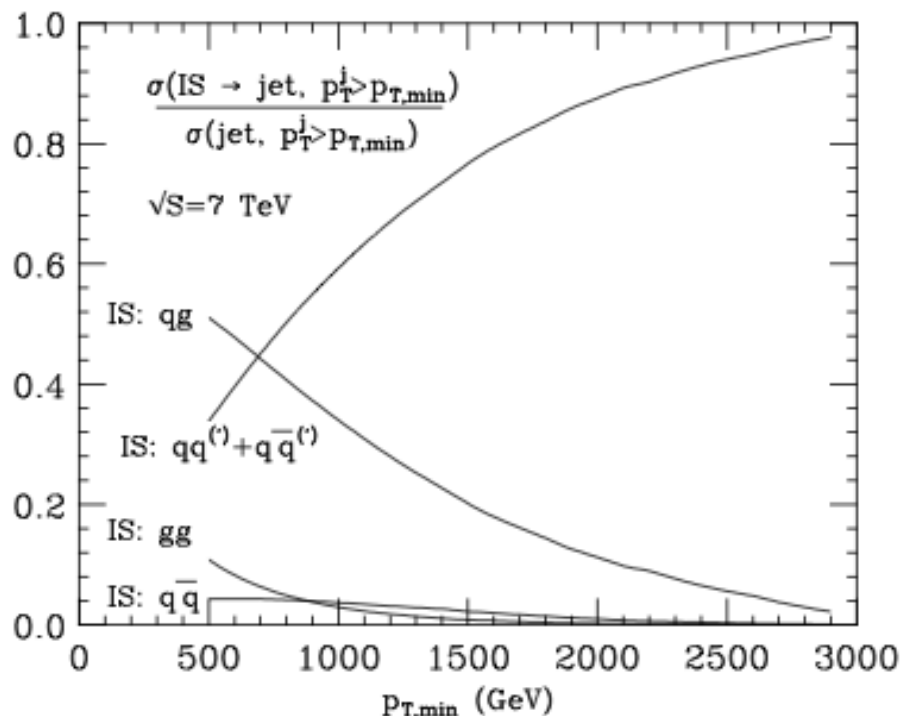
ATLAS, arXiv:1410.8857



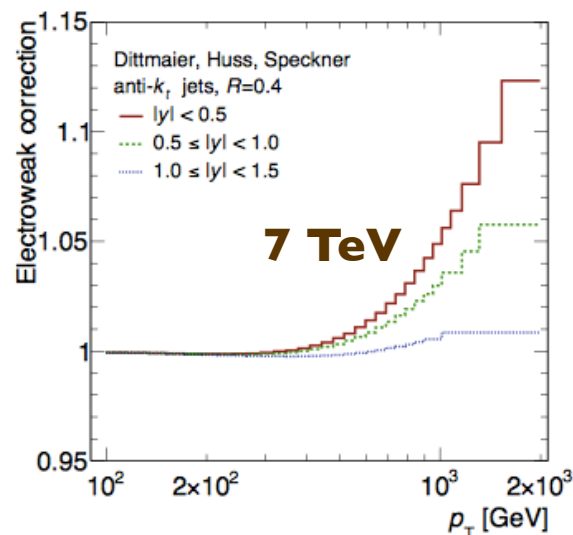
Rates span 10 orders of magnitude!



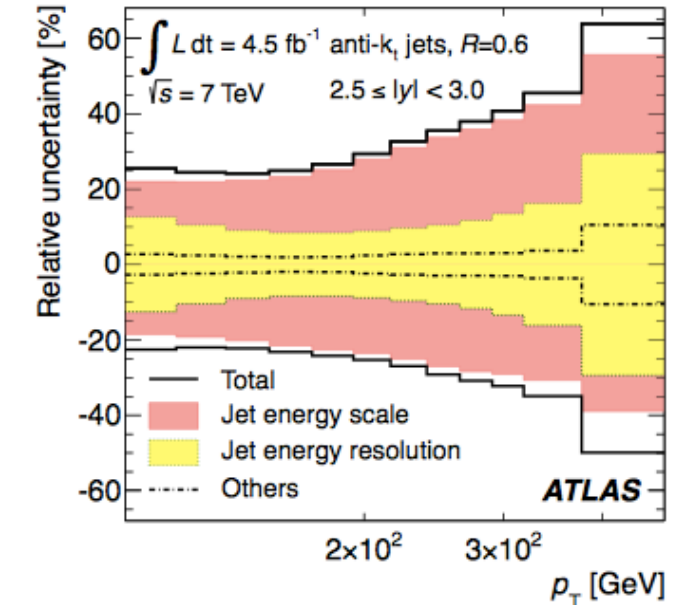
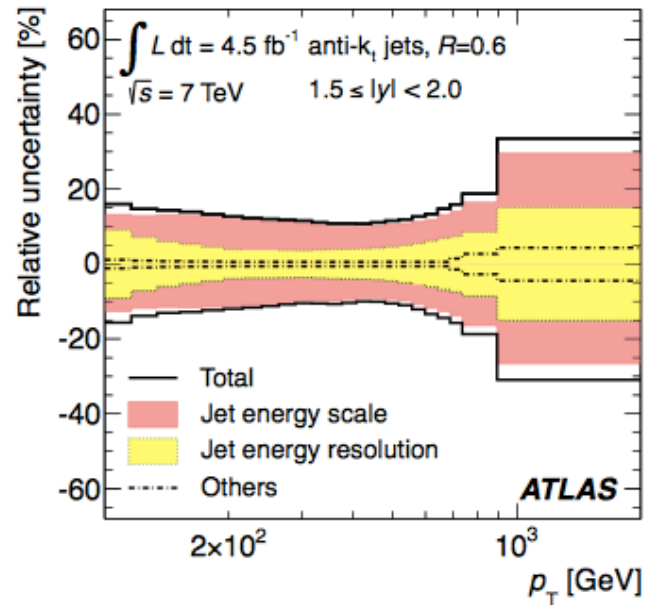
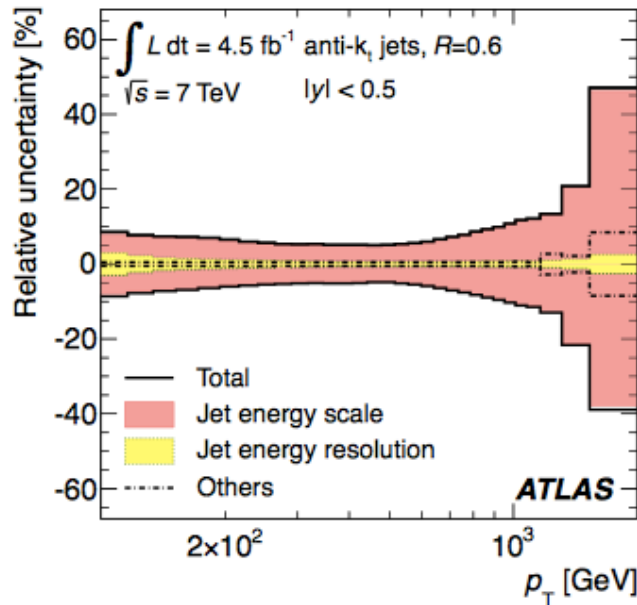
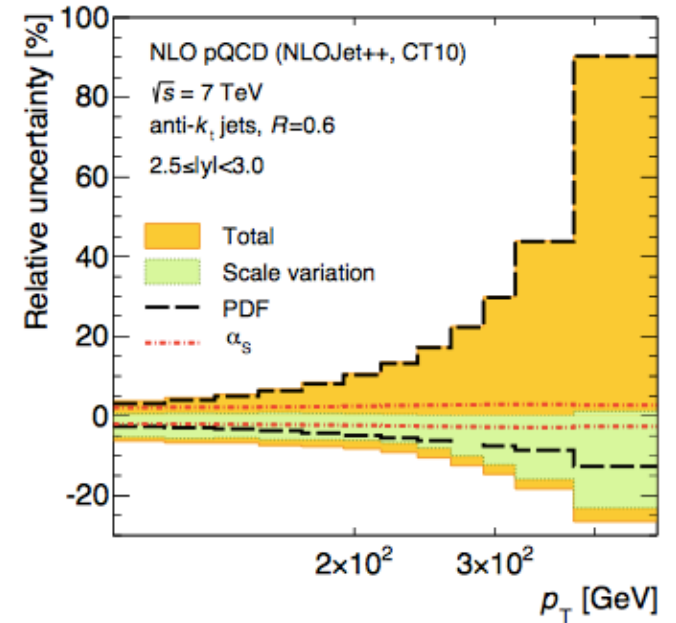
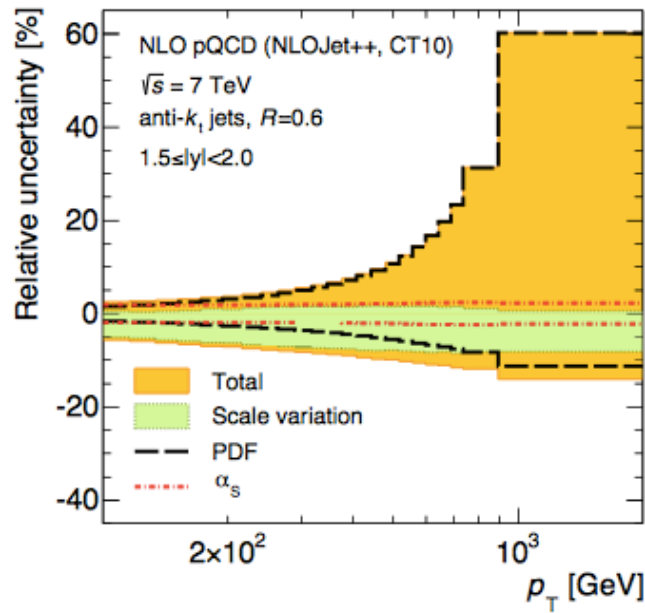
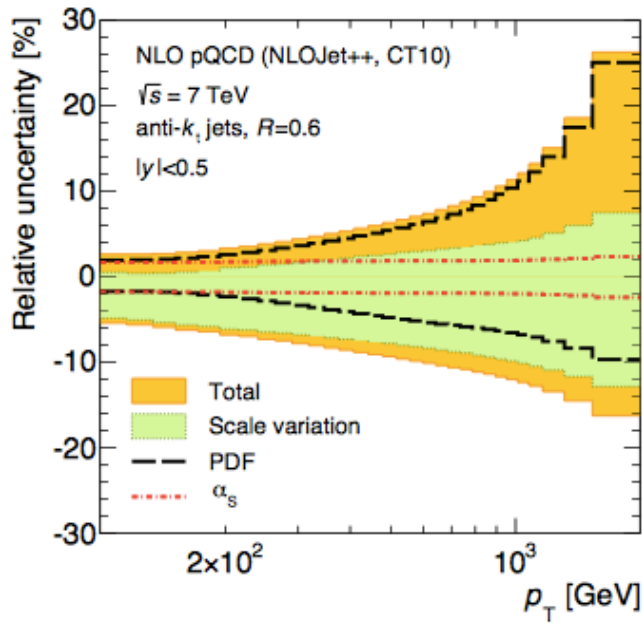
# Initial state composition of inclusive jet events



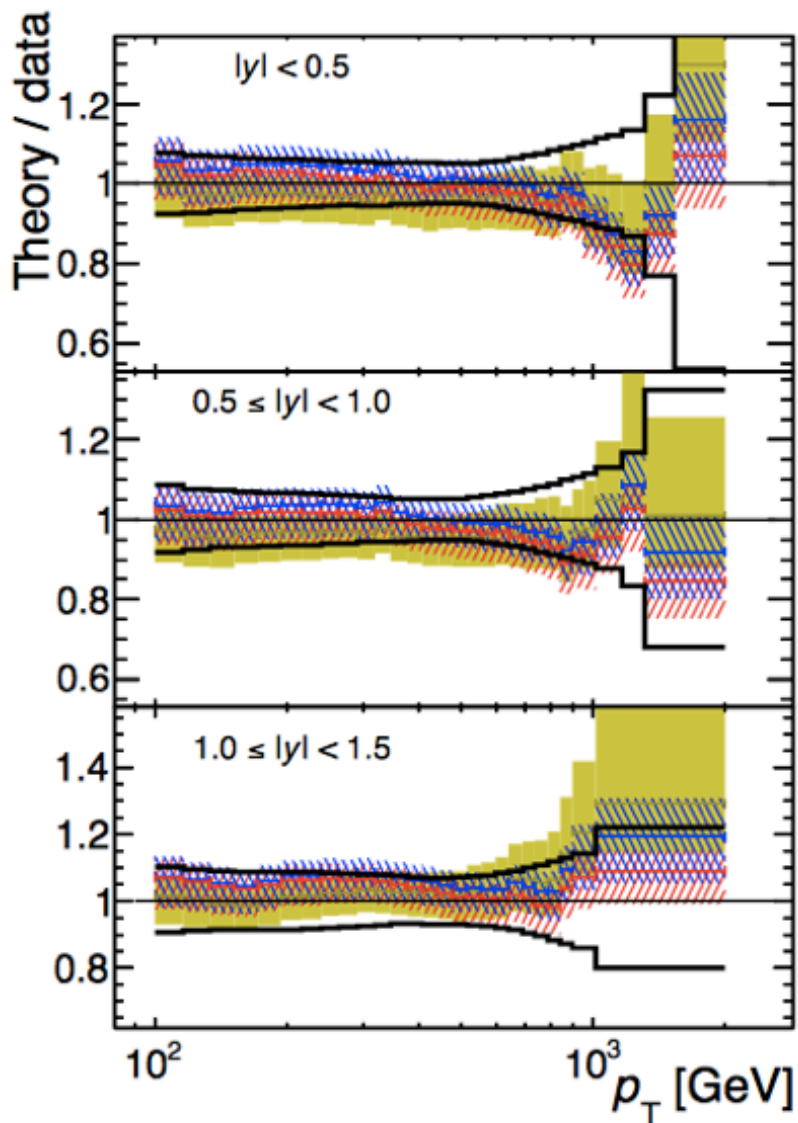
**NB: Impact of virtual EW corrections:**



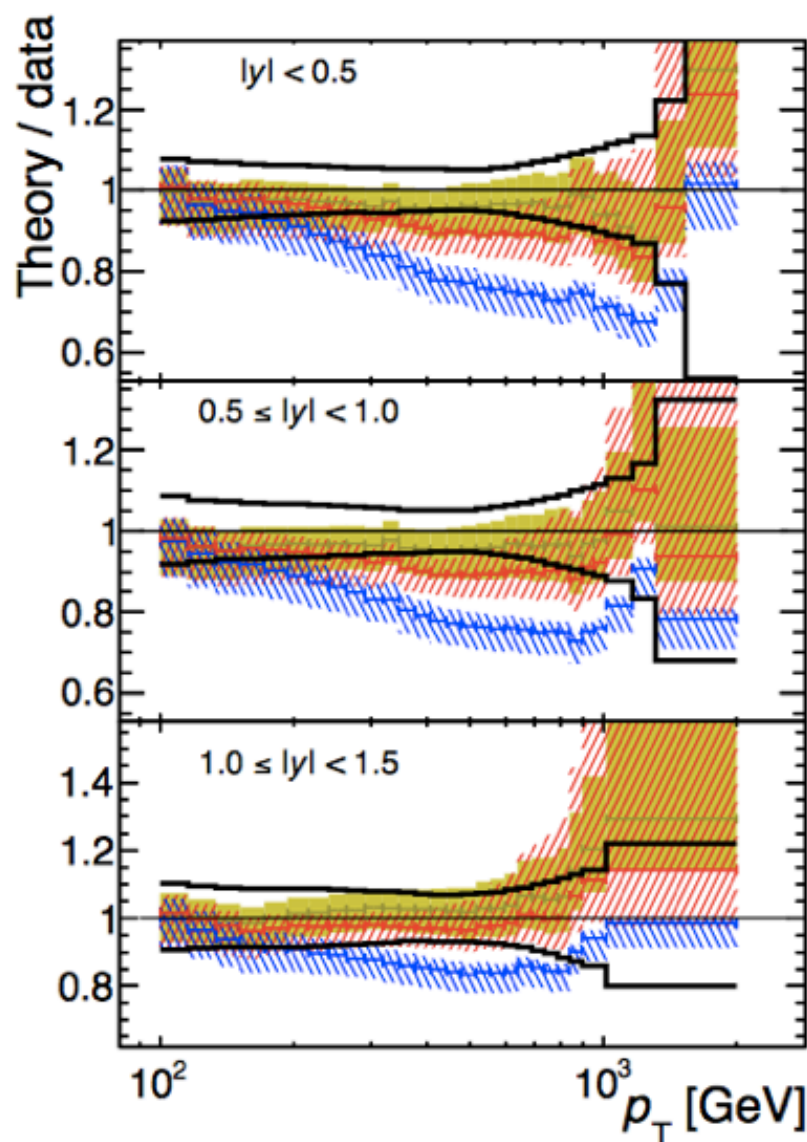
**at  $p_T \sim 2 \text{ TeV}$  it's larger than  $qg$  contribution**



**Central production, TH vs data**  
**(TH: absolute prediction for both shape and normalization)**



**ATLAS**  
 $\int L dt = 4.5 \text{ fb}^{-1}$   
 $\sqrt{s} = 7 \text{ TeV}$   
 anti- $k_r$  jets,  $R=0.4$

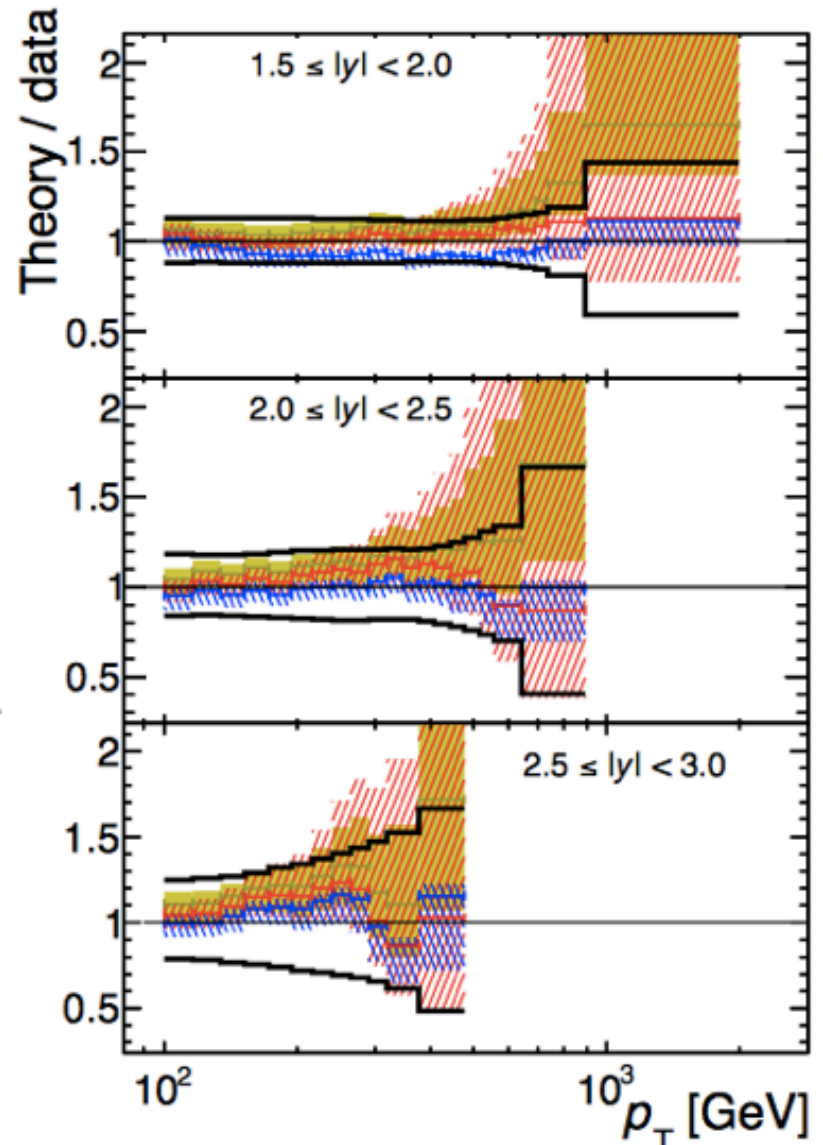
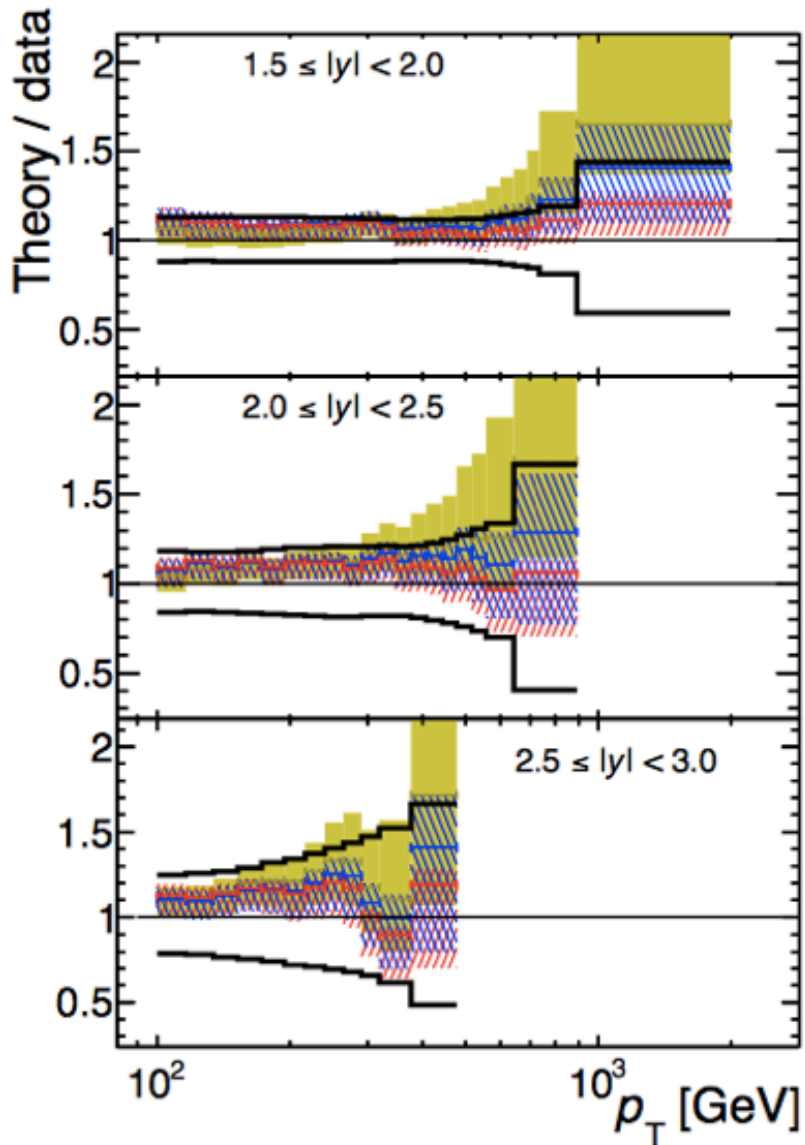


NLOJET++  
 $\mu_F = \mu_R = p_T^{\text{max}}$   
 Non-pert and  
 EW corr.

CT10  
 MSTW 2008  
 NNPDF 2.1

CT10  
 HERAPDF  
 1.5  
 ABM11  
 $n_f = 5$

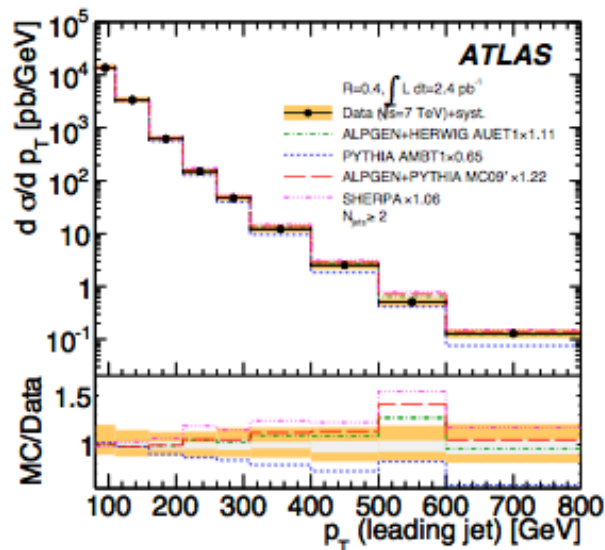
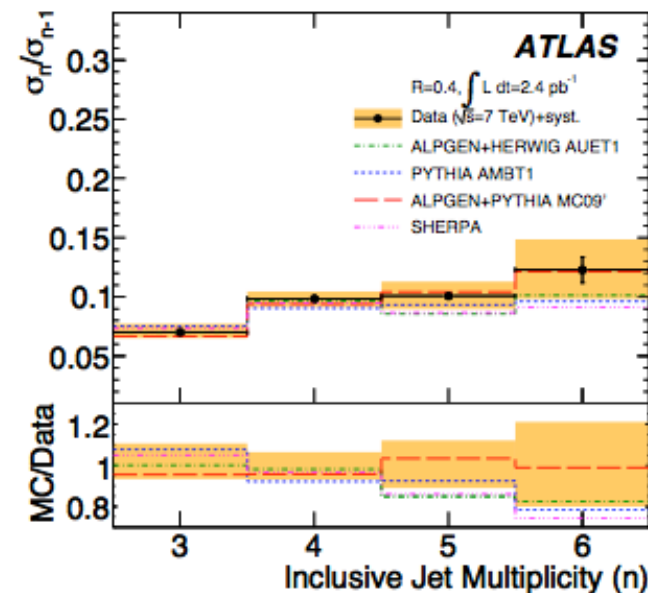
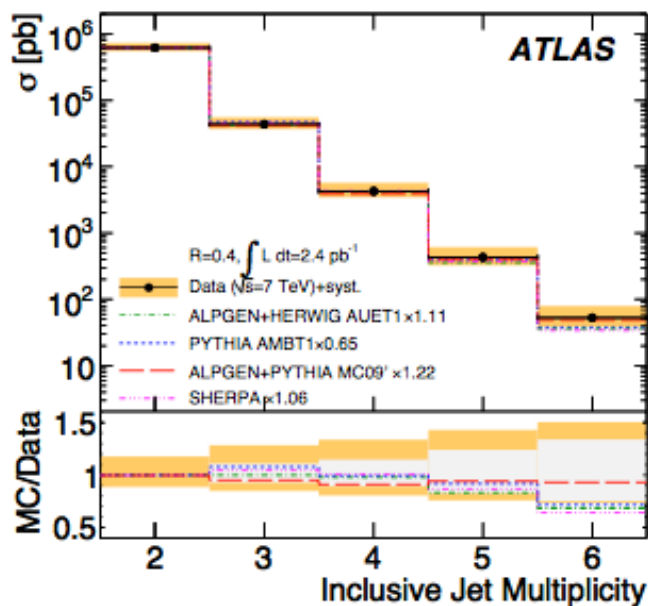
**Forward production, TH vs data**  
**(TH: absolute prediction for both shape and normalization)**



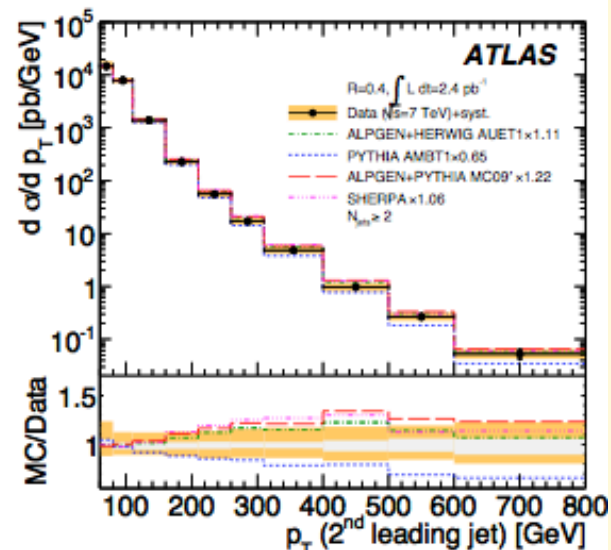
NLOJET++  
 $\mu_F = \mu_R = p_T^{\max}$   
 Non-pert and  
 EW corr.

CT10  
 MSTW 2008  
 NNPDF 2.1

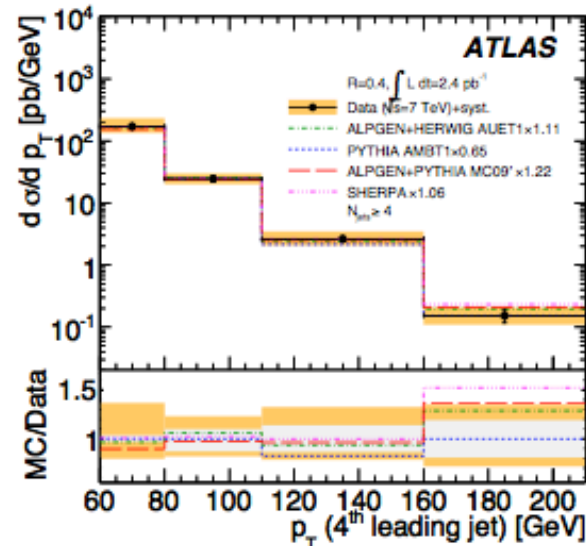
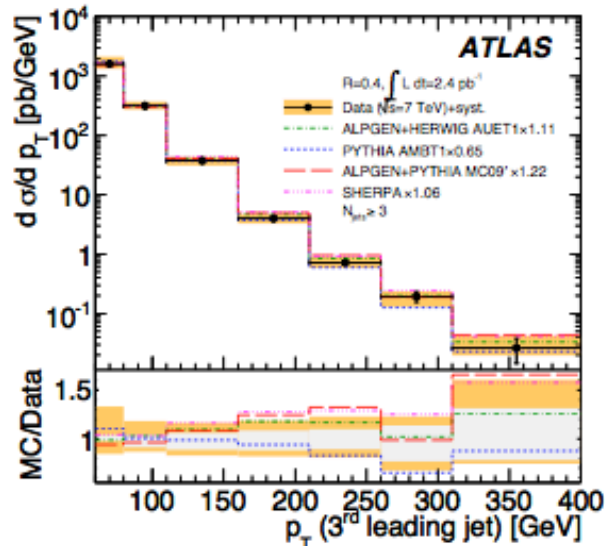
CT10  
 HERAPDF  
 1.5  
 ABM11  
 $n_f = 5$



(a)

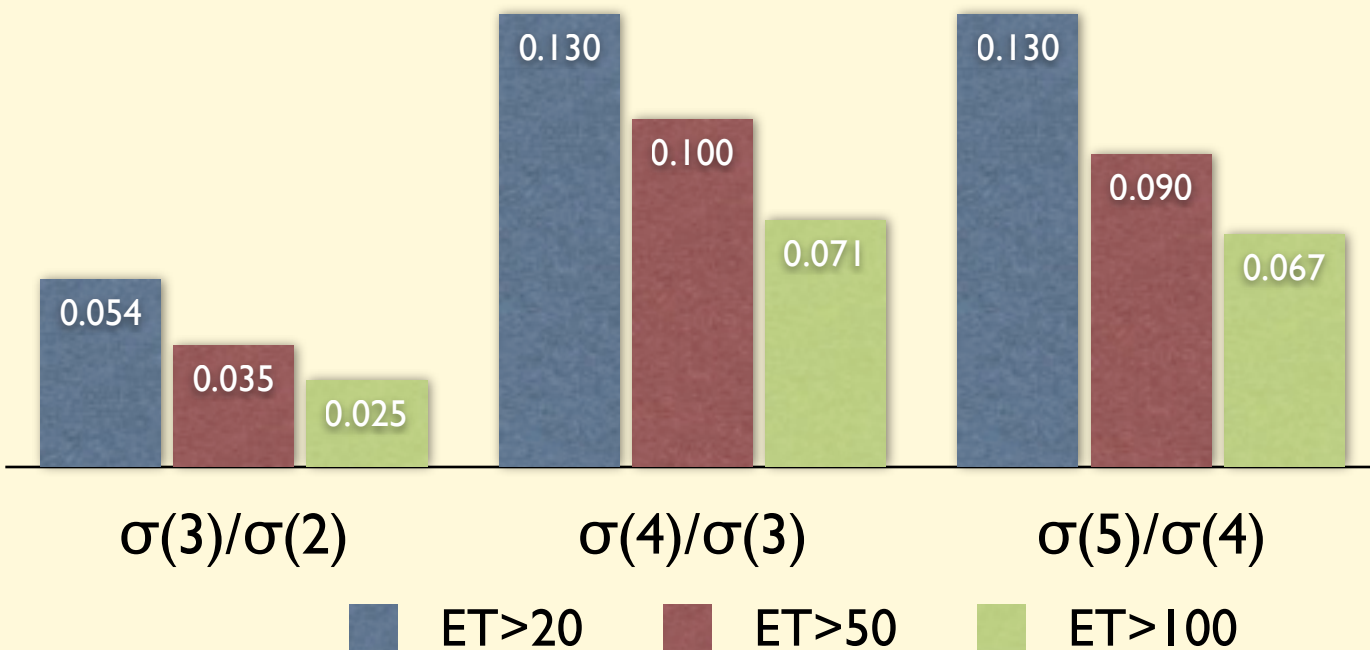


(b)



# Multijet rates

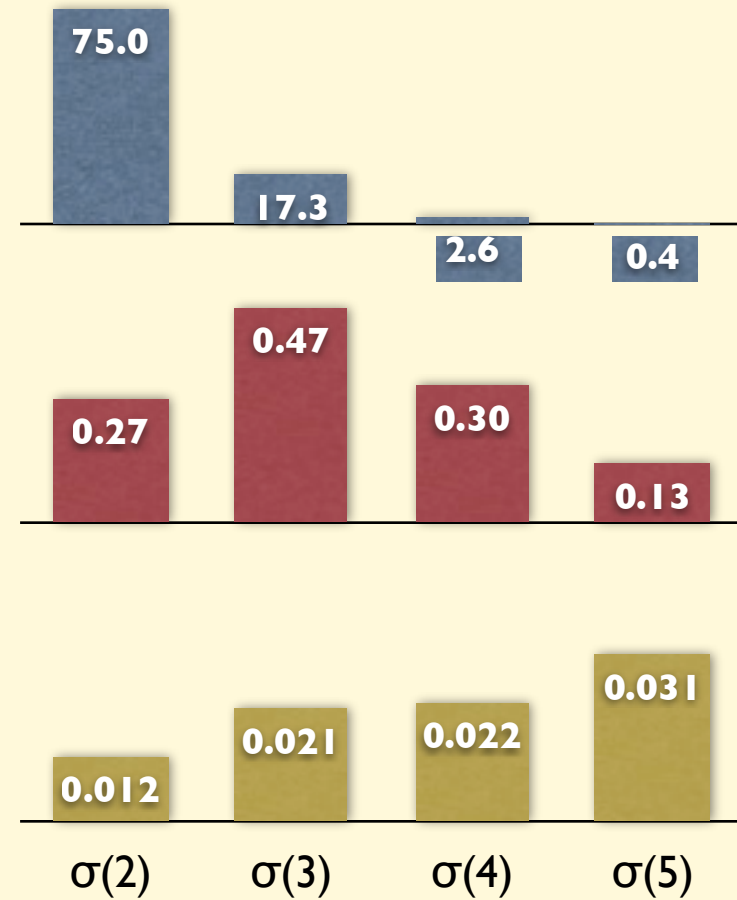
$\sigma$ [ $\mu\text{b}$ ]	<b>N jet=2</b>	<b>N jet=3</b>	<b>N jet=4</b>	<b>N jet=5</b>
<b><math>E_T^{\text{jet}} &gt; 20</math> GeV</b>	350	19	2.6	0.35
<b><math>E_T^{\text{jet}} &gt; 50</math> GeV</b>	12.7	0.45	0.045	0.004
<b><math>E_T^{\text{jet}} &gt; 100</math> GeV</b>	0.85	0.021	0.0015	0.0001



- The higher the jet  $E_T$  threshold, the harder to emit an extra jet
- When several jets are already present, however, emission of an additional one is less suppressed

# Multijet rates, vs $\sqrt{s}$ , with $E_T^{\text{jet}} > 20 \text{ GeV}$

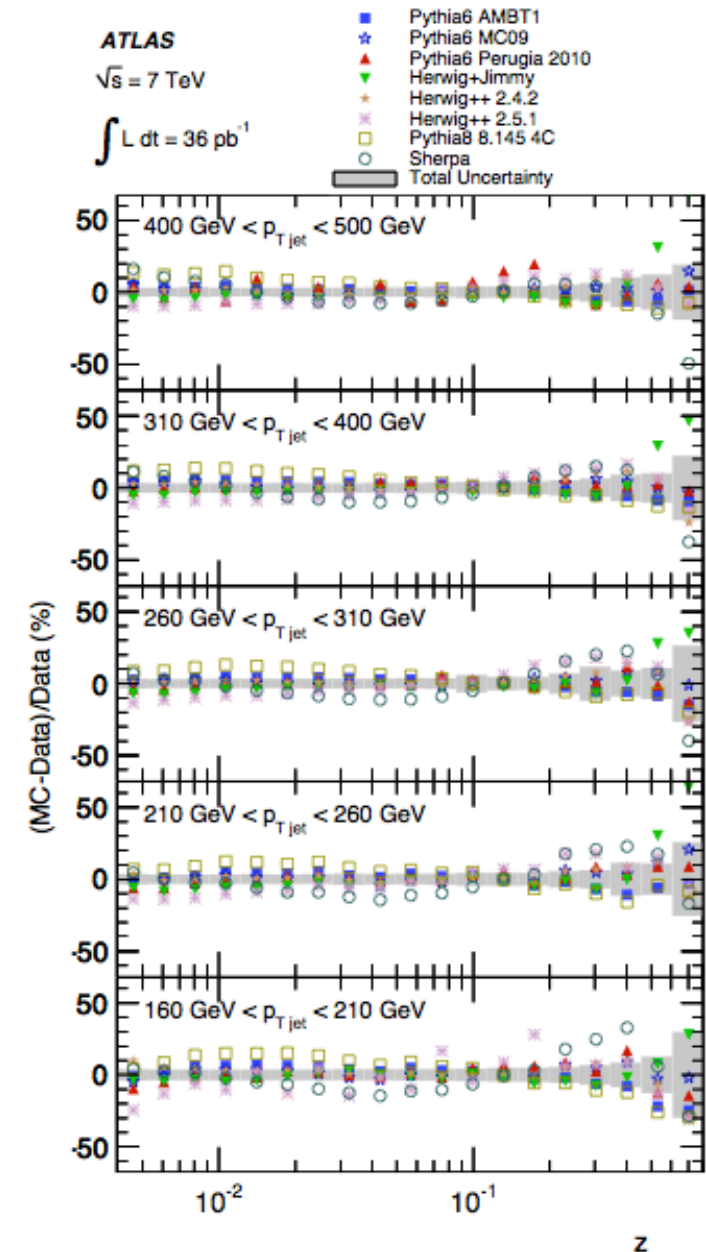
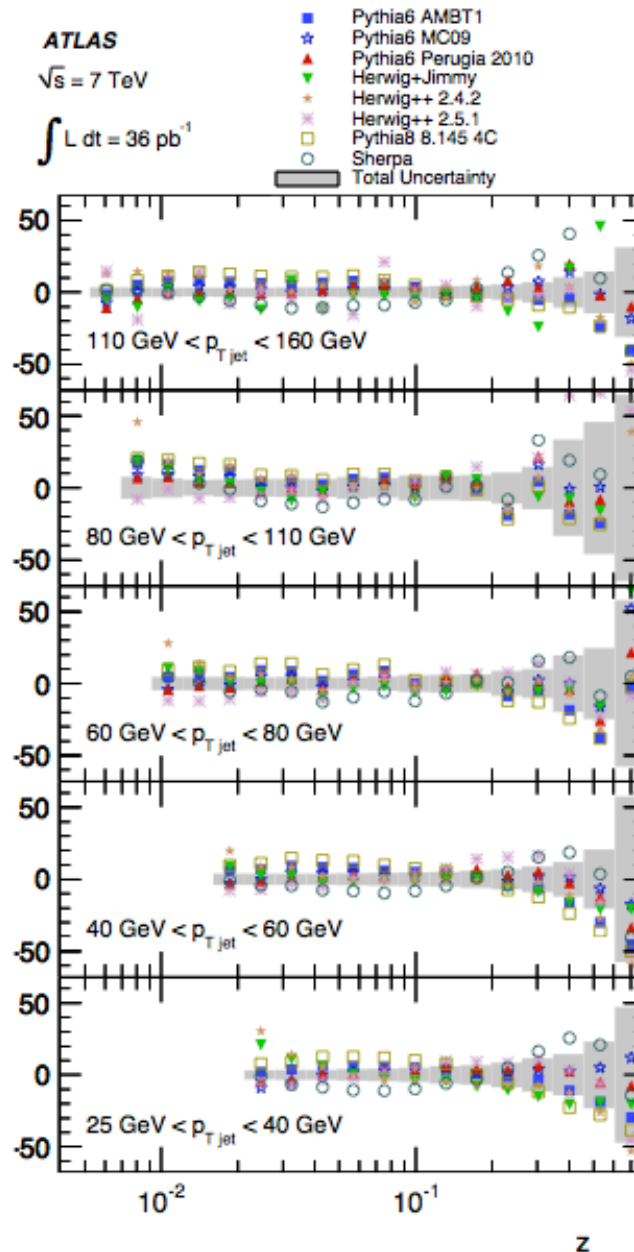
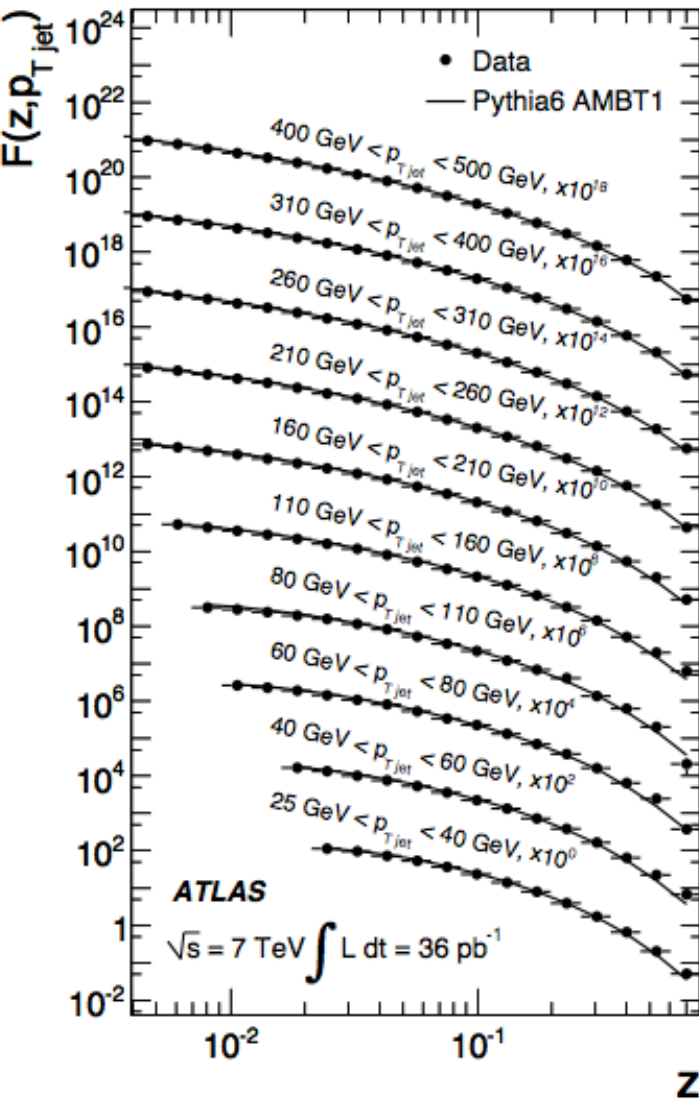
$\sigma$ [ $\mu\text{b}$ ]	N jet=2	N jet=3	N jet=4	N jet=5
$\sqrt{s} > 100 \text{ GeV}$	75	17.3	2.6	0.37
$\sqrt{s} > 500 \text{ GeV}$	0.27	0.47	0.30	0.13
$\sqrt{s} > 1000 \text{ GeV}$	0.012	0.021	0.022	0.031



**High mass final states are dominated by multijet configurations**

# Jet fragmentation function

ATLAS, arXiv:1109.5816



- plus
- jet shapes
- p<sub>T</sub>rel spectra
- <N<sub>ch</sub>> and <z> distributions,
- ....

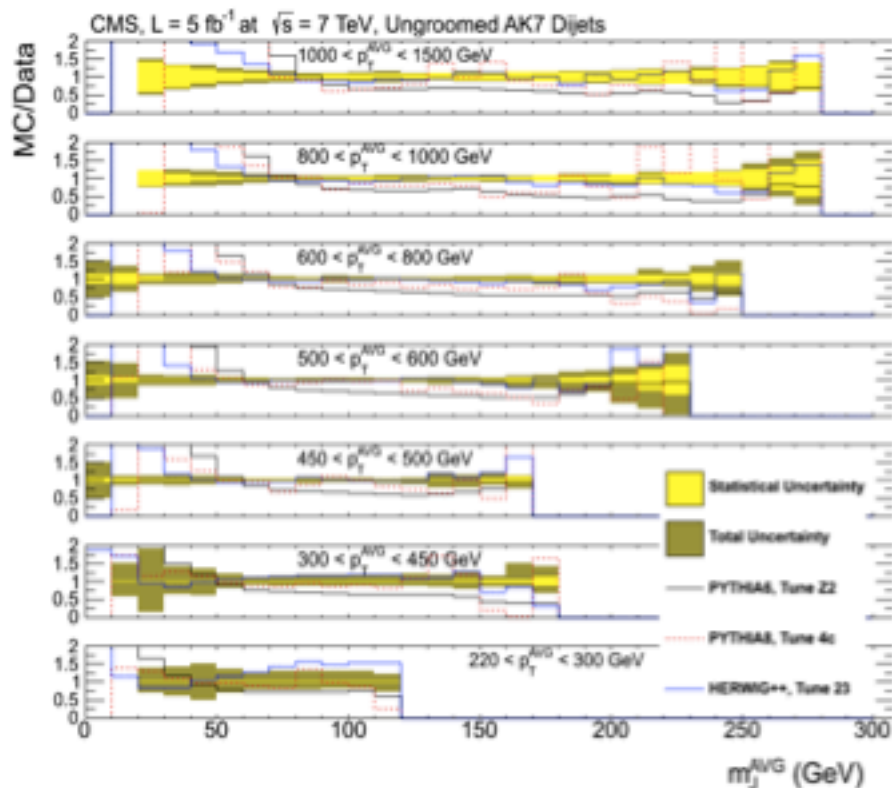
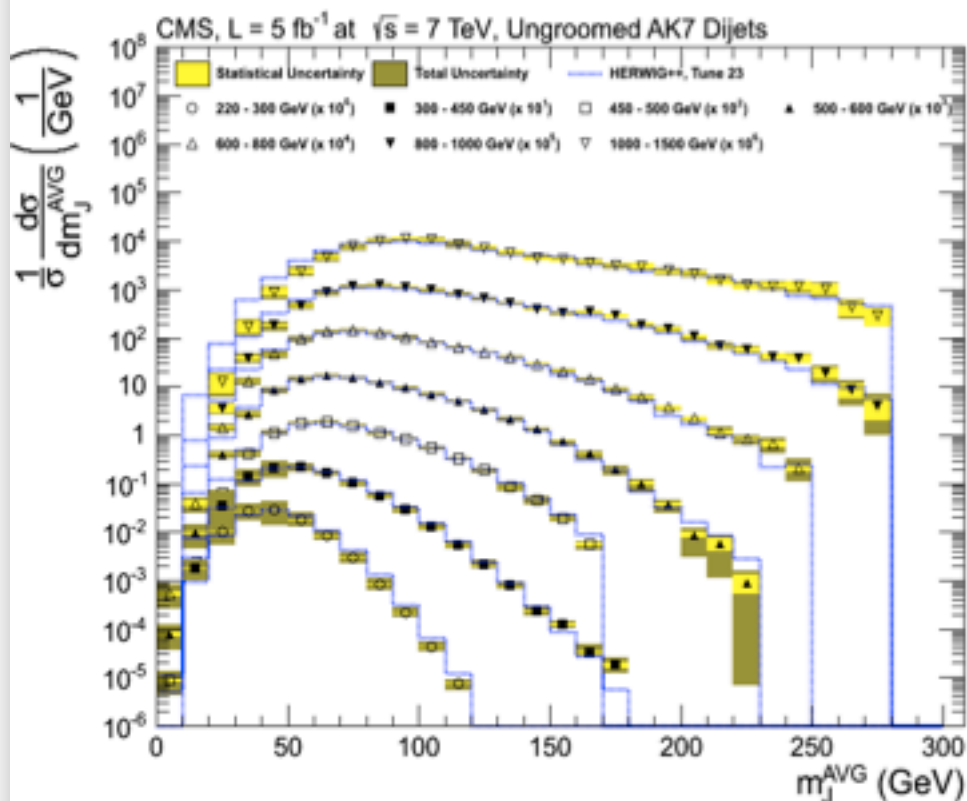




# QCD jet mass measurement



Processes with high mass jets (q/g initiated) are important backgrounds for many analyses in the boosted topology.

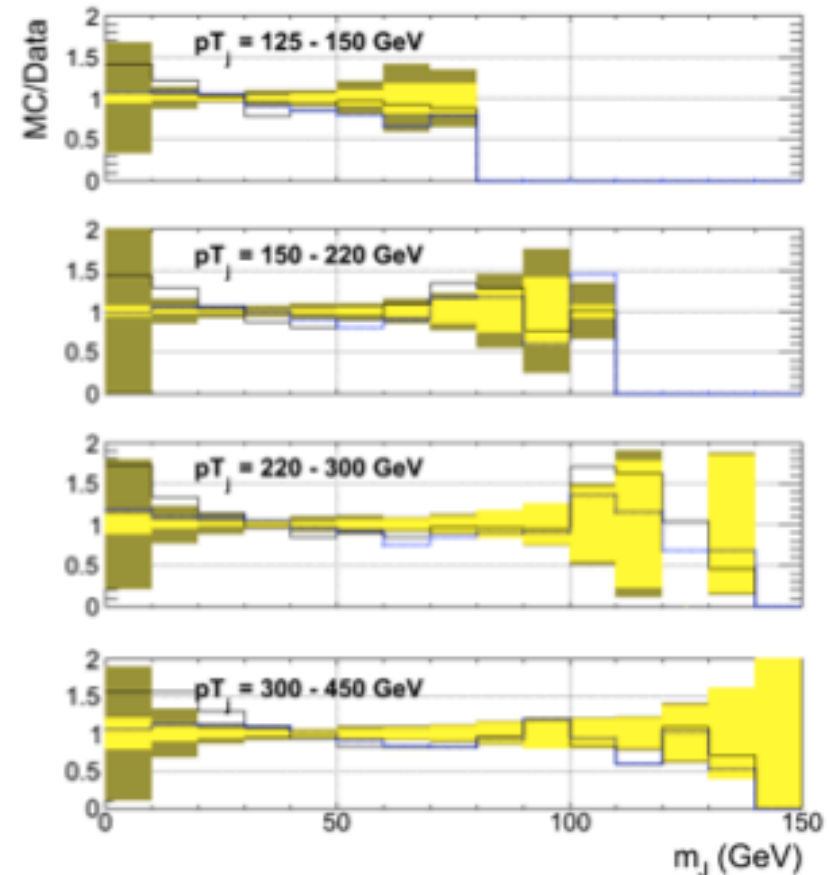
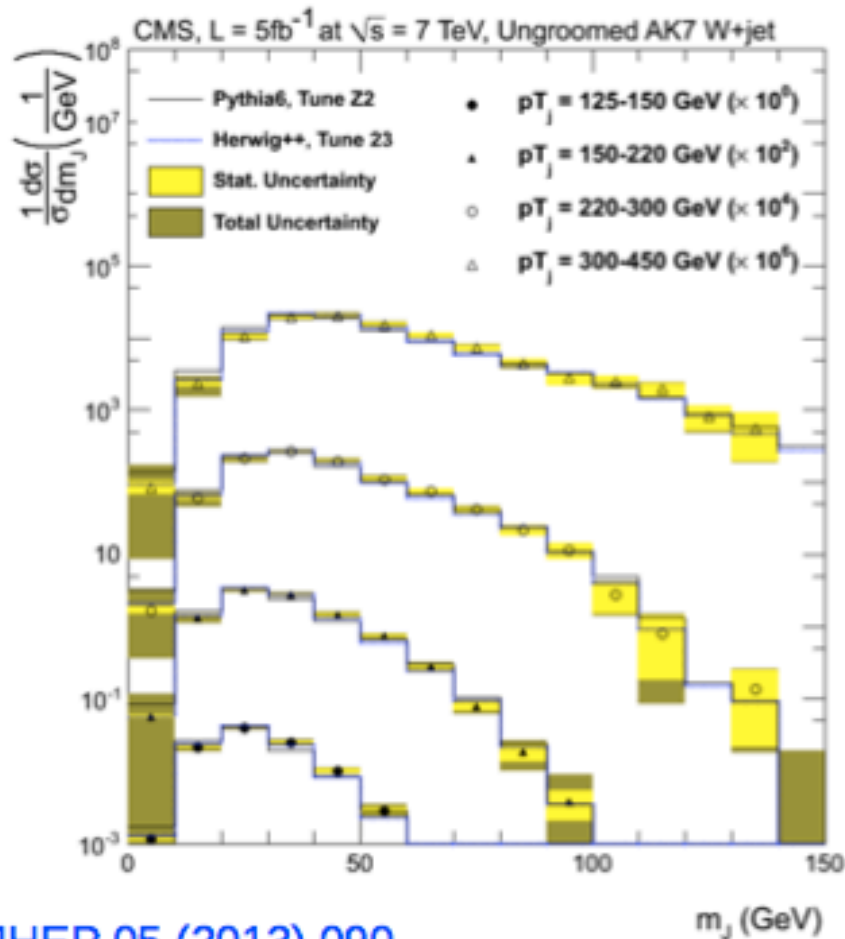


JHEP 05 (2013) 090  
CMS-SMP-12-019

Dijet typology (gluon enriched)



# QCD jet mass measurement



JHEP 05 (2013) 090  
CMS-SMP-12-019

**V+jet typology (quark enriched):  
agreement with data is slightly better**

# Reconstruct $W/Z \rightarrow jj$ from broad jets at large $p_T$

Likelihood discriminant using (i) thrust minor (ii) sphericity (iii) aplanarity

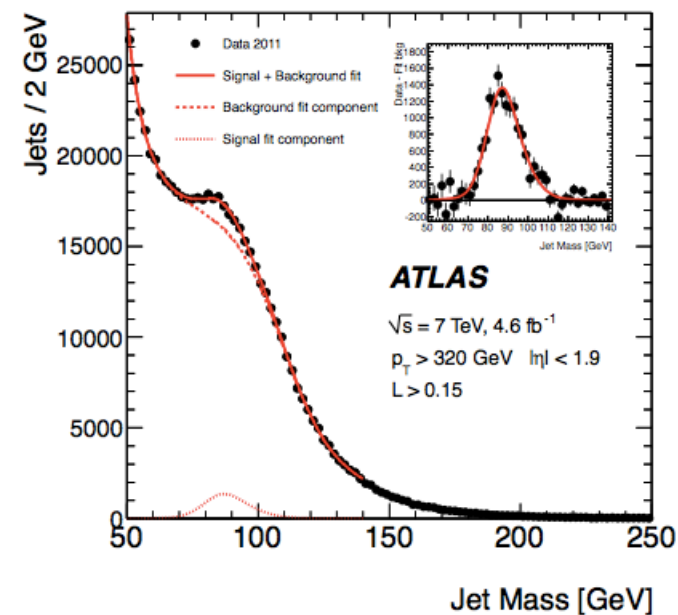
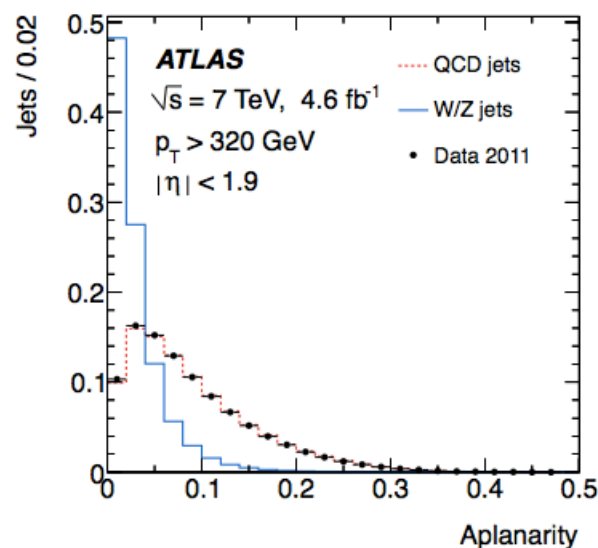
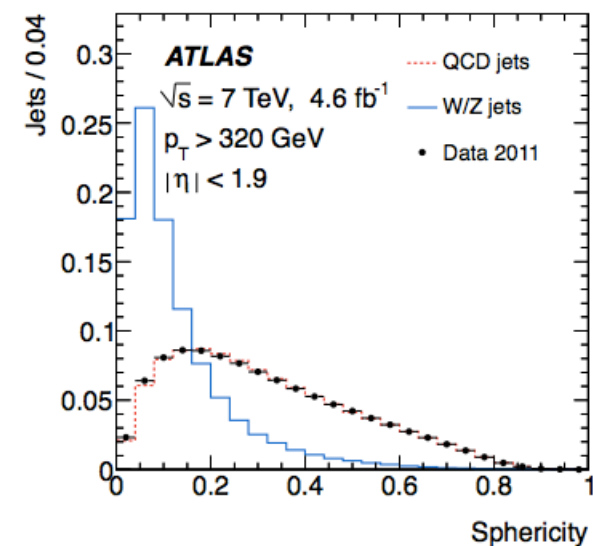
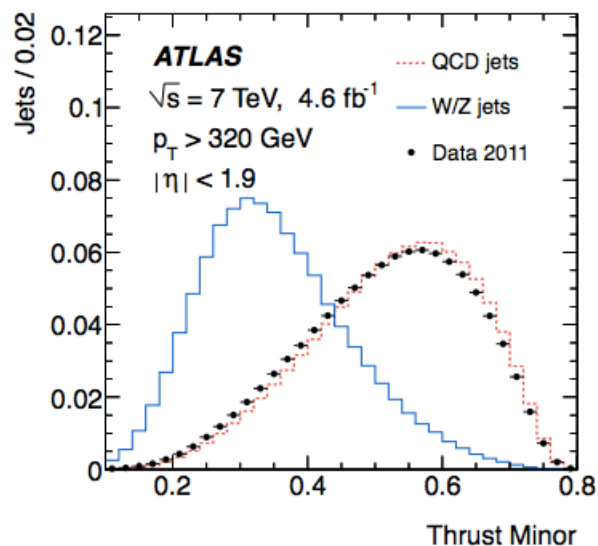
Extract

$$\sigma_{W+Z} = 8.5 \pm 0.8(\text{stat}) \pm 1.5(\text{syst}) \text{ pb}$$

ATLAS, *J.Phys.* **16** (2014) 113013

NLO:

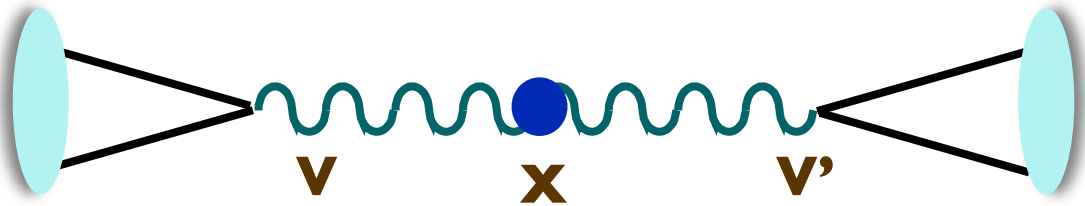
$$\sigma_{W+Z} = 5.1 \pm 0.5 \text{ pb}$$



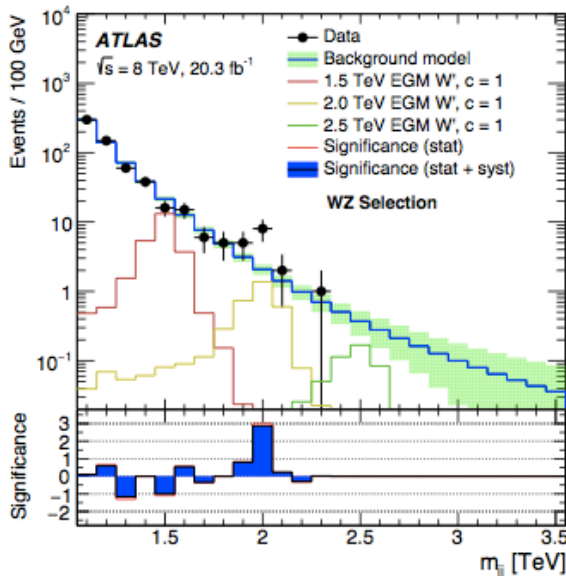
# Example in use of $W/Z \rightarrow jj$

ATLAS, arXiv:1506.00962

$pp \rightarrow X \rightarrow VV' \rightarrow \text{jet jet}$ , with  $V^{(\prime)} = W, Z$  fully hadronic decays

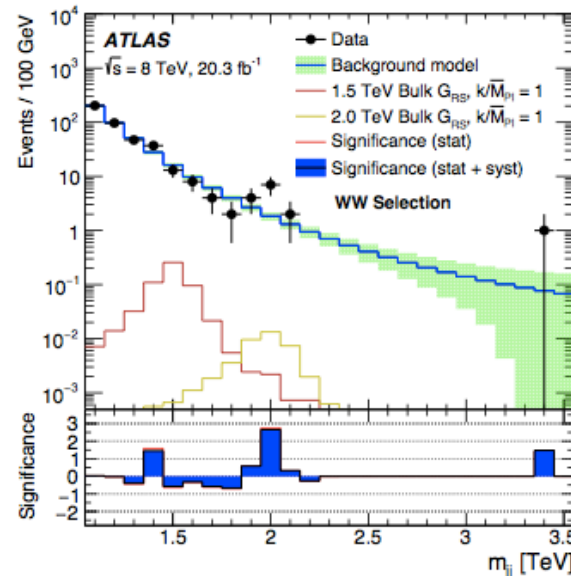


$$|m_j - m_{V'}| < 13 \text{ GeV}$$



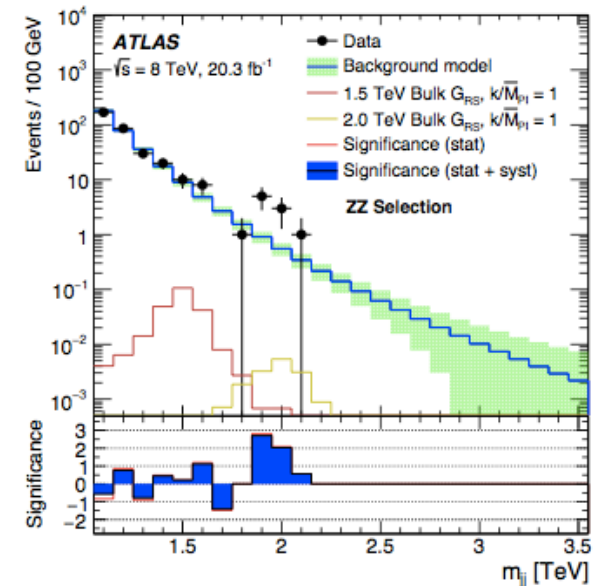
**3.5 $\sigma$  local**

$\rightarrow$  **2.4 $\sigma$  global**, accounting for the whole range of  $m_{jj}$  and for ZZ, WW, WZ modes



**2.6 $\sigma$**

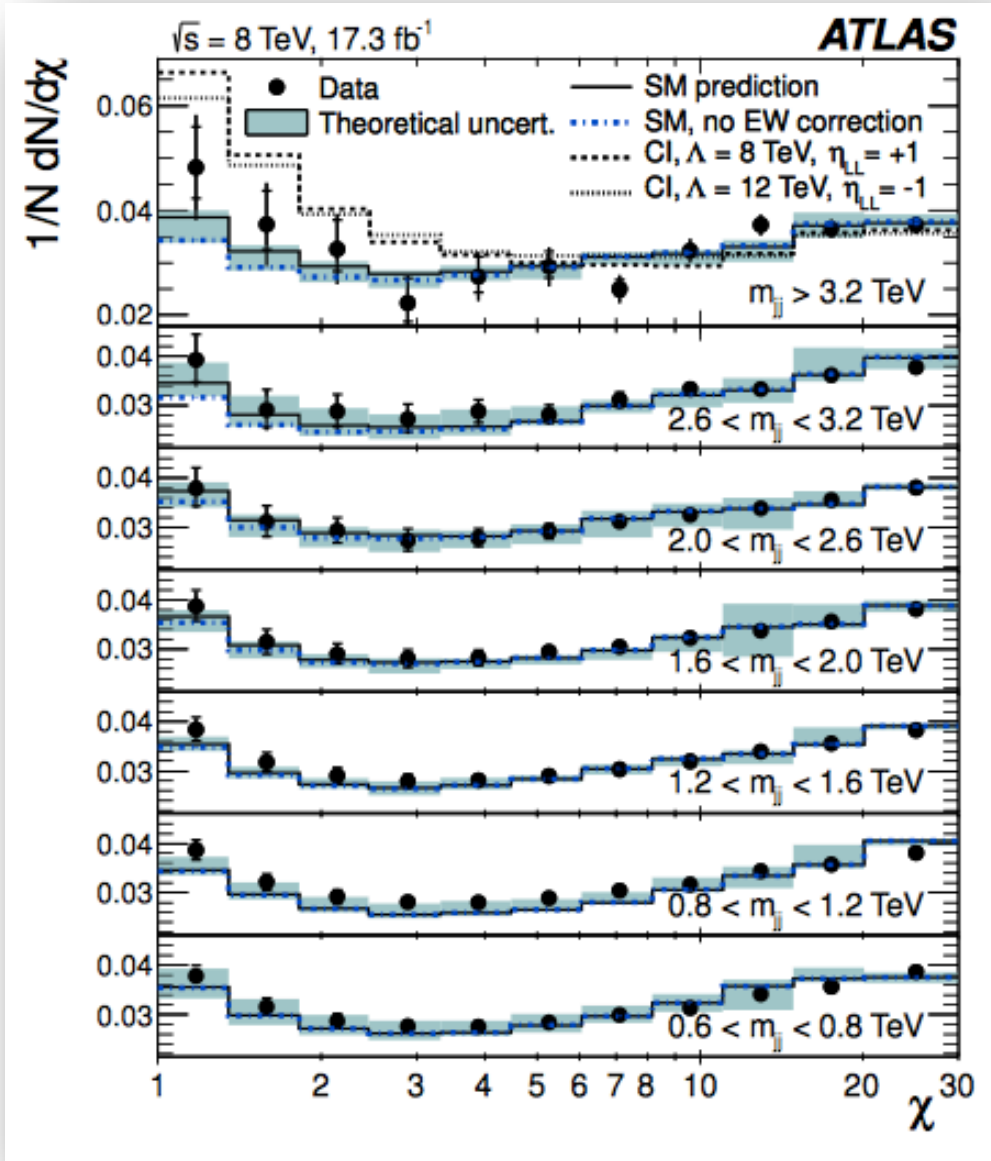
NB: the excesses are strongly correlated:  $|m_j - m_{V'}| < 13 \text{ GeV}$  allows the same event to belong to more than one selection among WZ, WW and ZZ



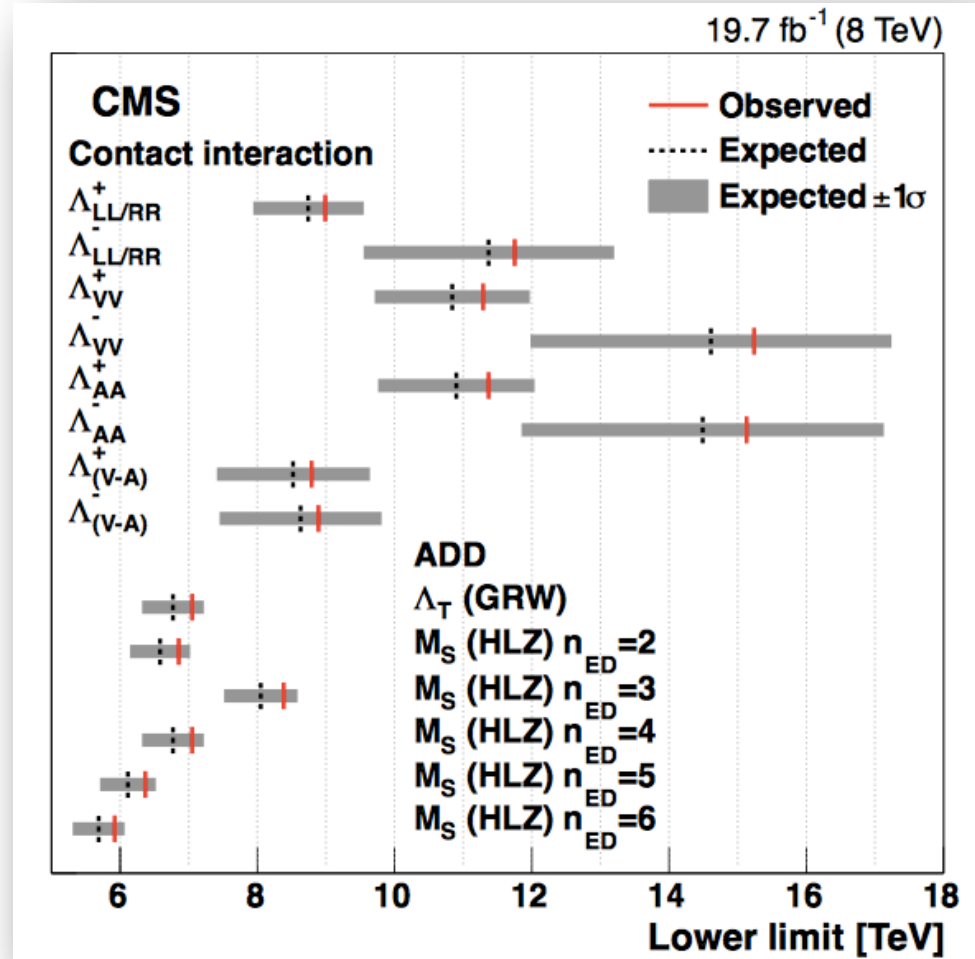
**2.9 $\sigma$**

# Constraints on quark contact interactions

ATLAS, <http://arxiv.org/abs/1504.00357>



CMS, <http://arxiv.org/abs/1411.2646>

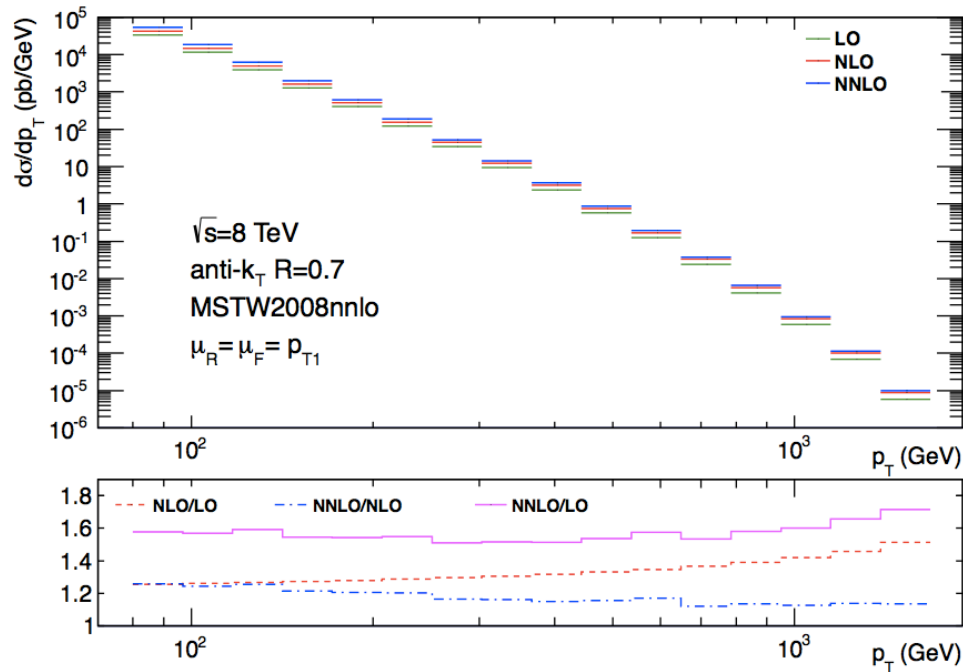


$$\chi = \frac{1 + |\cos \theta^*|}{1 - |\cos \theta^*|} \quad \mathbf{NB:} \quad d\chi = 2 \frac{d \cos \theta}{\sin^4(\theta/2)}$$

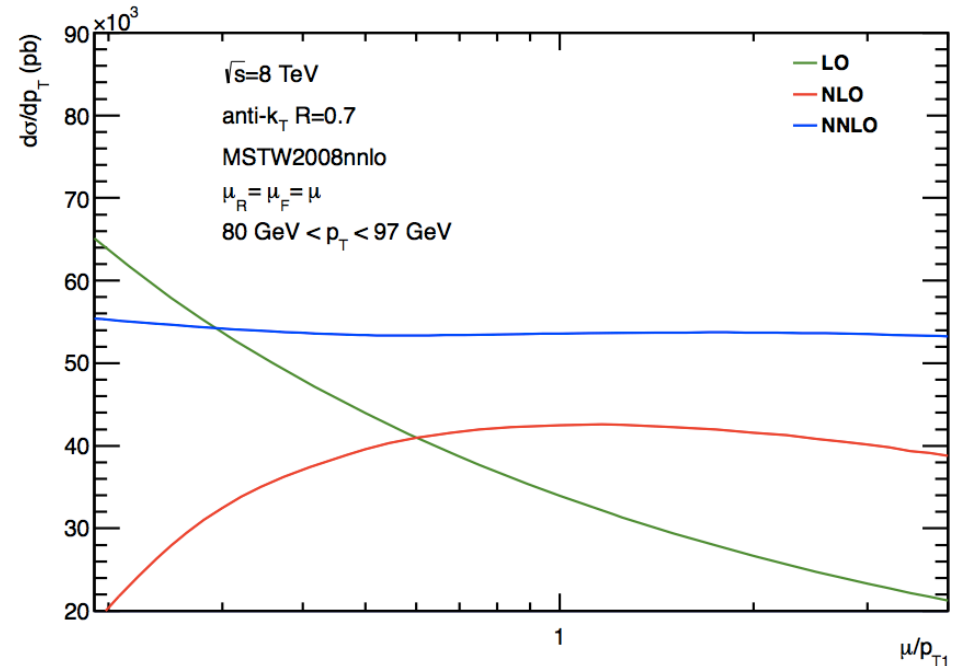
Quarks appear pointlike even at the distances probed by the LHC, up to scales in the range of (10 TeV)<sup>-1</sup>

# Inclusive jet cross section at NNLO

“Second order QCD corrections to jet production at hadron colliders: the all-gluon contribution”, A. Gehrmann-De Ridder, T. Gehrmann, E.W.N. Glover, J. Pires, arXiv:1301.7310



**NNLO/NLO ~ 1.2**

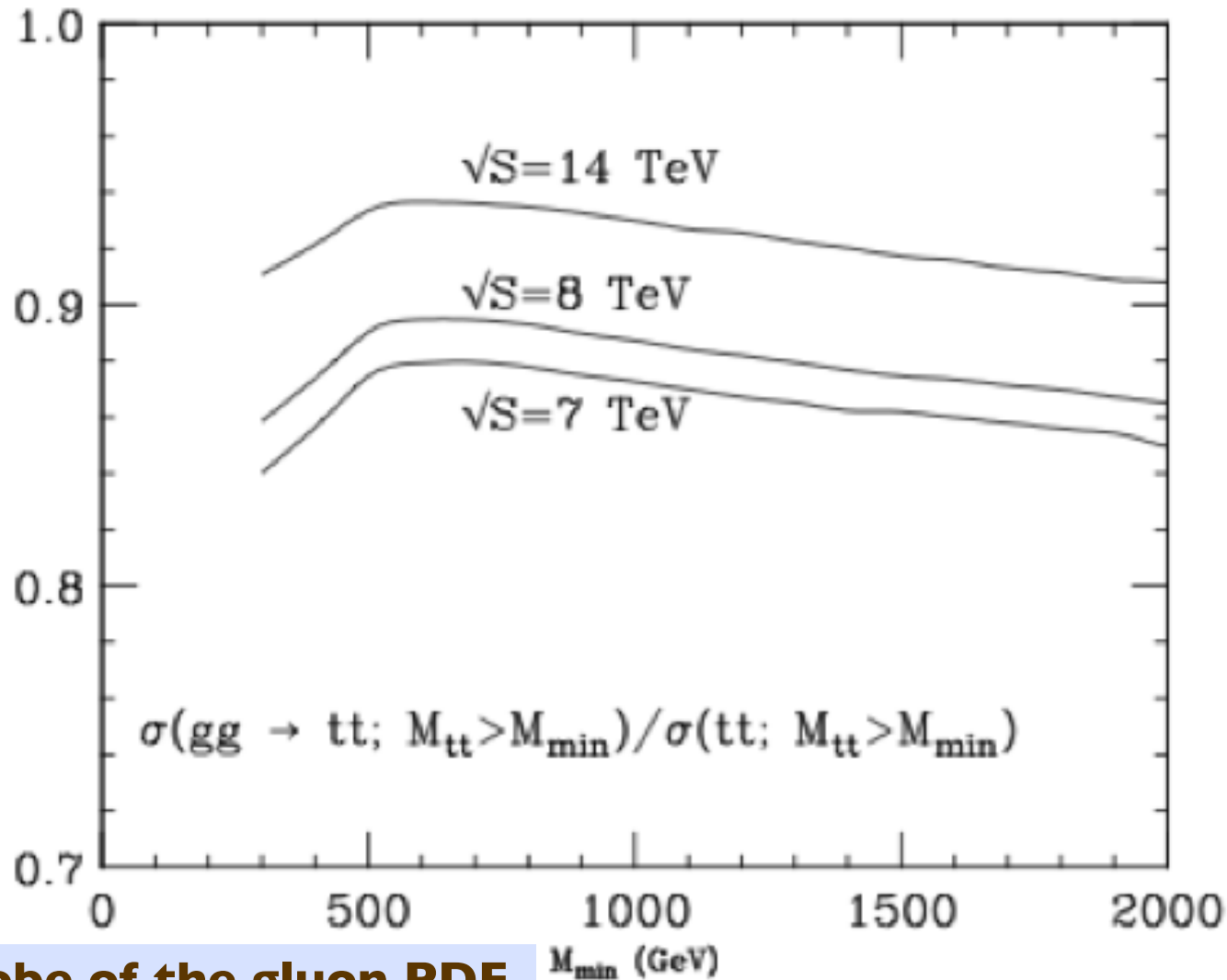
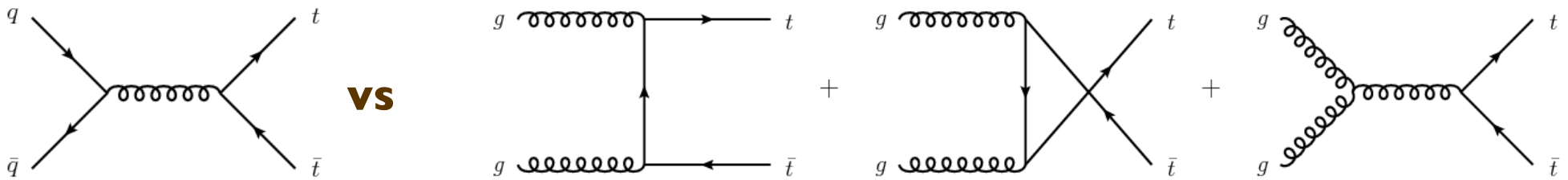


**NNLO scale systematics ~ few % ...**  
**- does this survive if  $\mu_F \neq \mu_R$  ?**

**Notice that NNLO outside the NLO scale-variation band**

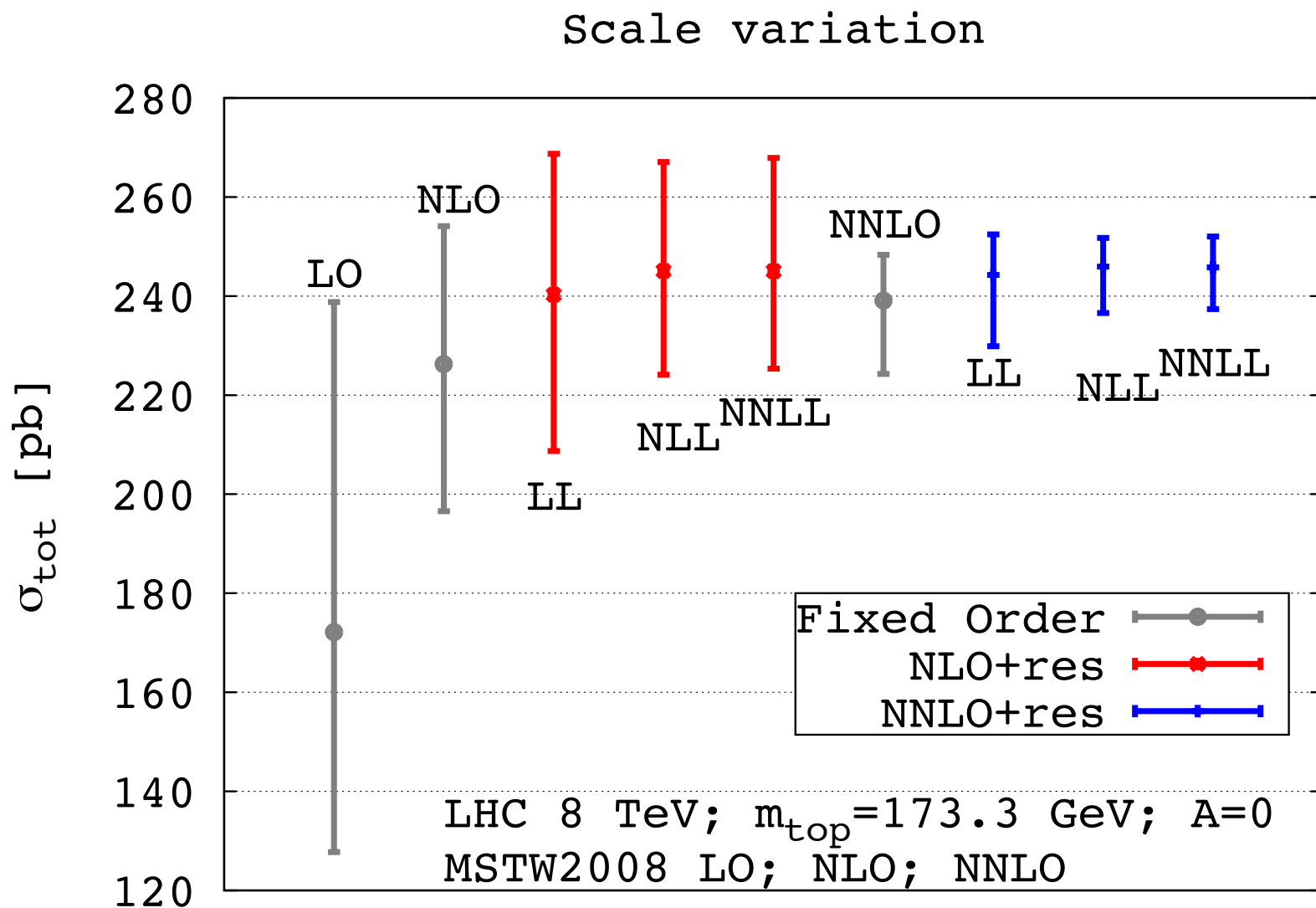
# Top quark production

Production dominated by  $gg$  initial state up to very large  $p_T$



⇒ sensitive probe of the gluon PDF

# Great precision reached with the completion of the NNLO calculation



Independent  $\mu_R$ ,  $\mu_F$  variation, with  $\mu_0 = m_{\text{top}}$ ,  
 $0.5 \mu_0 < \mu_{R,F} < 2 \mu_0$  and  
 $0.5 < \mu_R / \mu_F < 2$

Baernreuther, Czakon, Mitov arXiv:1204.5201  
Czakon, Mitov arXiv:1207.0236  
Czakon, Mitov arXiv:1210.6832  
Czakon, Fiedler, Mitov arXiv:1303.6254



# Phenomenological study of $t\bar{t}$ production at NNLO

M. Czakon, M. Mangano, A. Mitov, J. Rojo arXiv:1303.7215

LHC 8 TeV

PDF set	$\sigma_{t\bar{t}}$ (pb)	$\delta_{\text{scale}}$ (pb)	$\delta_{\text{PDF}}$ (pb)	$\delta_{\alpha_s}$ (pb)	$\delta_{m_t}$ (pb)	$\delta_{\text{tot}}$ (pb)
ABM11	198.6	+5.0 (+2.5%) -6.2 (-3.1%)	+8.5 (+4.3%) -8.5 (-4.3%)	+0.0 (+0.0%) -0.0 (-0.0%)	+6.1 (+3.1%) -5.9 (-3.0%)	+15.5 (+7.8%) -16.6 (-8.4%)
CT10	246.3	+6.4 (+2.6%) -8.6 (-3.5%)	+10.1 (+4.1%) -8.2 (-3.3%)	+4.9 (+2.0%) -4.9 (-2.0%)	+7.4 (+3.0%) -7.1 (-2.9%)	+19.8 (+8.1%) -20.5 (-8.3%)
HERA1.5	252.7	+6.5 (+2.6%) -5.9 (-2.3%)	+5.4 (+2.1%) -8.6 (-3.4%)	+4.0 (+1.6%) -4.0 (-1.6%)	+7.5 (+3.0%) -7.3 (-2.9%)	+16.6 (+6.6%) -17.8 (-7.1%)
MSTW08	245.8	+6.2 (+2.5%) -8.4 (-3.4%)	+6.2 (+2.5%) -6.2 (-2.5%)	+4.0 (+1.6%) -4.0 (-1.6%)	+7.4 (+3.0%) -7.1 (-2.9%)	+16.6 (+6.8%) -18.7 (-7.6%)
NNPDF2.3	248.1	+6.4 (+2.6%) -8.7 (-3.5%)	+6.6 (+2.7%) -6.6 (-2.7%)	+3.7 (+1.5%) -3.7 (-1.5%)	+7.5 (+3.0%) -7.2 (-2.9%)	+17.1 (+6.9%) -19.1 (-7.7%)
ATLAS	241.0					$\pm 32.0$ ( 13.3%)
CMS	227.0					$\pm 15.0$ ( 6.6%)

**TH and parametric uncertainties are all of similar size:**

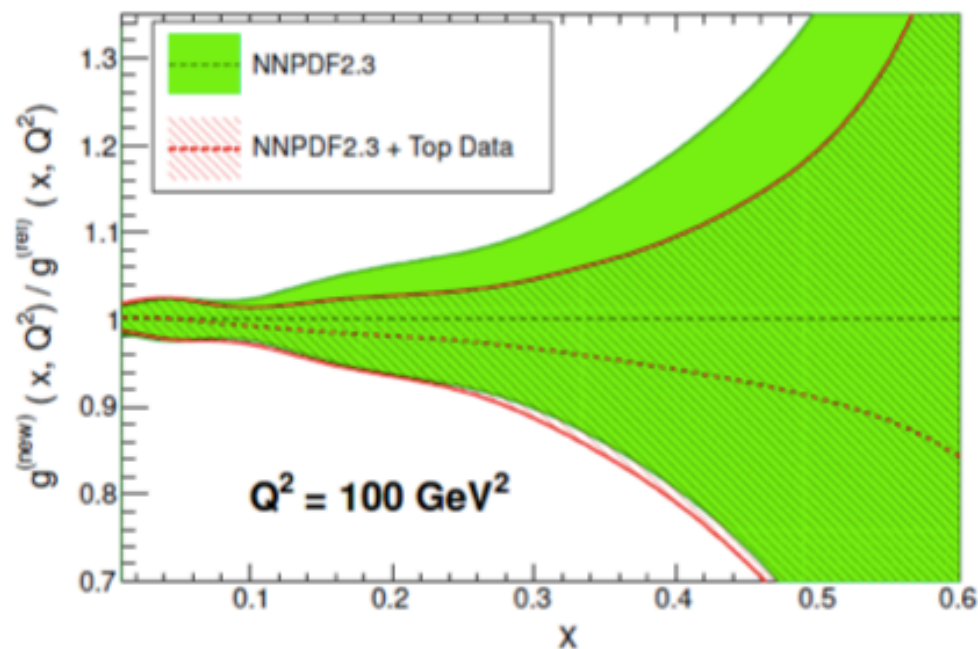
	scales (i.e. missing yet-higher order corrections)	$\sim 3\%$
	pdf (at 68%cl)	$\sim 2\text{-}3\%$
$\Delta\alpha_s = \pm 0.0007 \Rightarrow$	$\alpha_s$ (parametric)	$\sim 1.5\%$
$\Delta m_{\text{top}} = \pm 1 \text{ GeV} \Rightarrow$	$m_{\text{top}}$ (parametric)	$\sim 3\%$

# Constraining the gluon PDF with $\sigma(t\bar{t})$

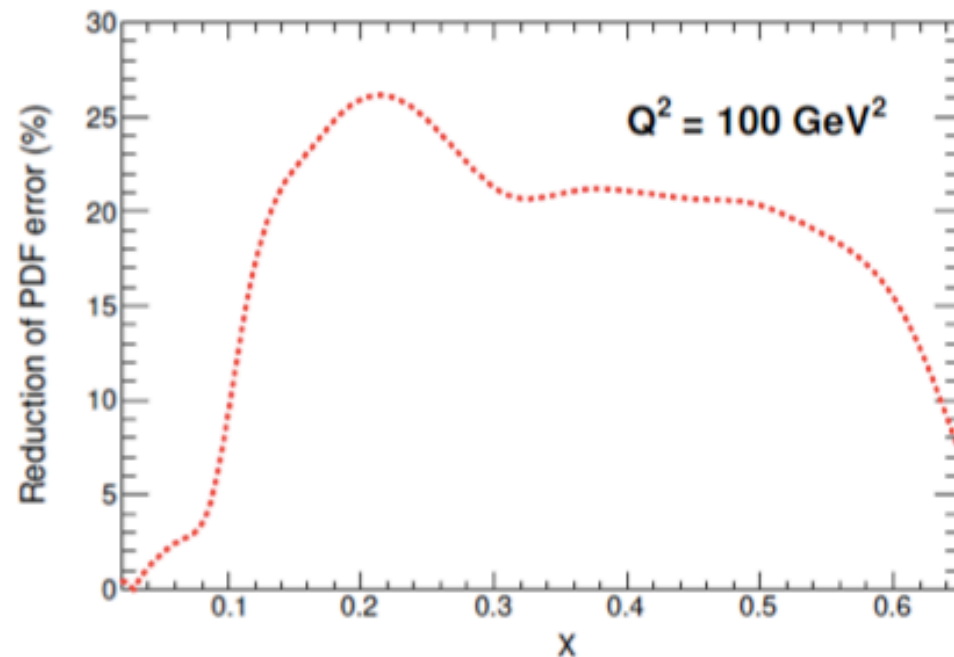
M. Czakon et al arXiv:1303.7215

- Top quark cross-section data **discriminates between PDF sets**
- In addition, it can also be used to **reduce the PDF uncertainties** within a single PDF set
- We included the most precise top quark data into the **NNPDF2.3** global PDF analysis

Ratio to NNPDF2.3 NNLO,  $\alpha_s = 0.118$



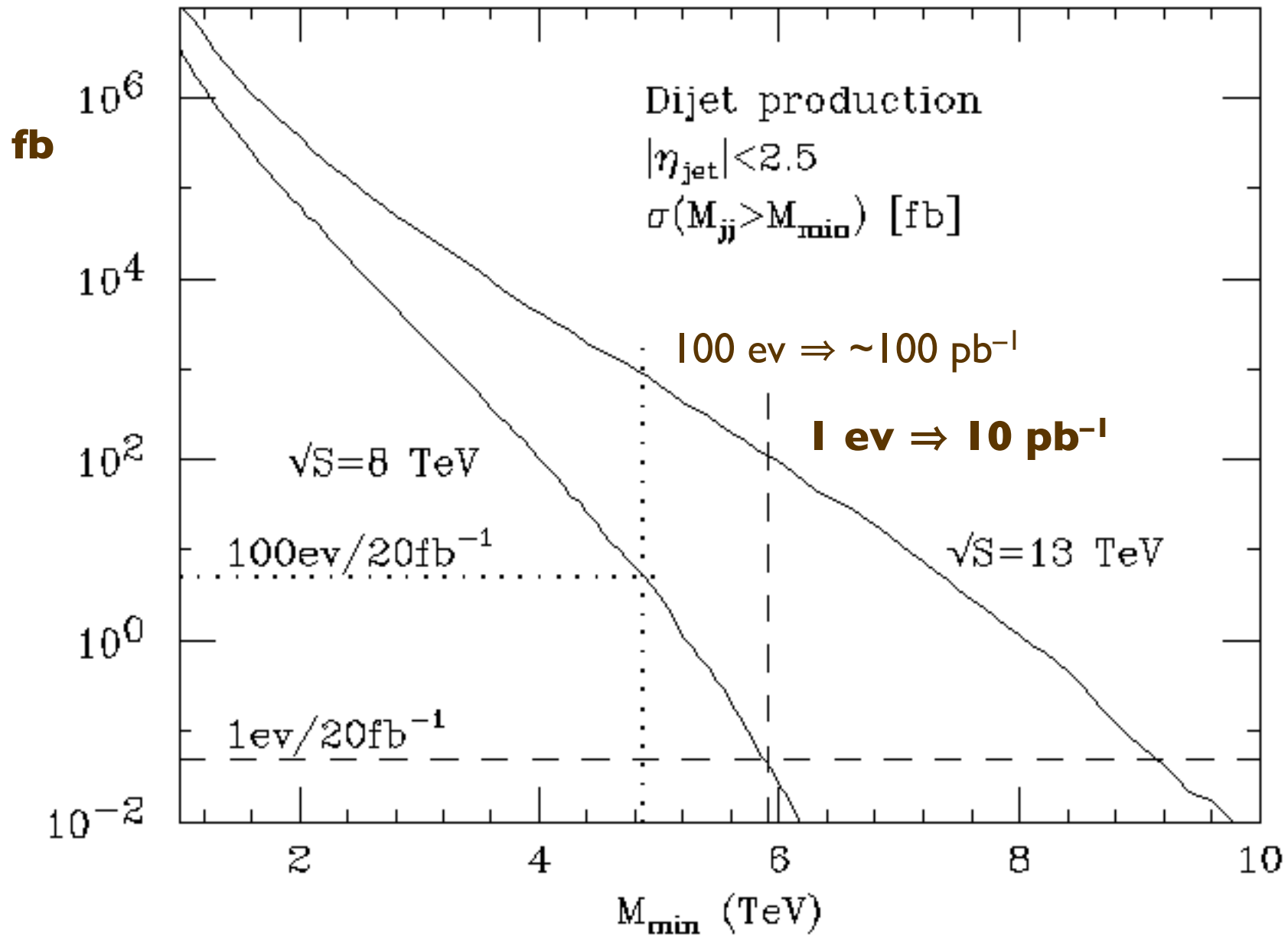
NNPDF2.3 NNLO + TeV,LHC Top Quark Data



Collider	Ref	Ref+TeV	Ref +TeV+LHC7	Ref+TeV+LHC7+8
Tevatron	$7.26 \pm 0.12$	-	-	-
LHC 7 TeV	$172.5 \pm 5.2$	$172.7 \pm 5.1$	-	-
LHC 8 TeV	$247.8 \pm 6.6$	$248.0 \pm 6.5$	$245.0 \pm 4.6$	-
LHC 14 TeV	$976.5 \pm 16.4$	$976.2 \pm 16.3$	$969.8 \pm 12.0$	$969.6 \pm 11.6$

**How long before run 2  
extends the discovery  
reach of run 1?**

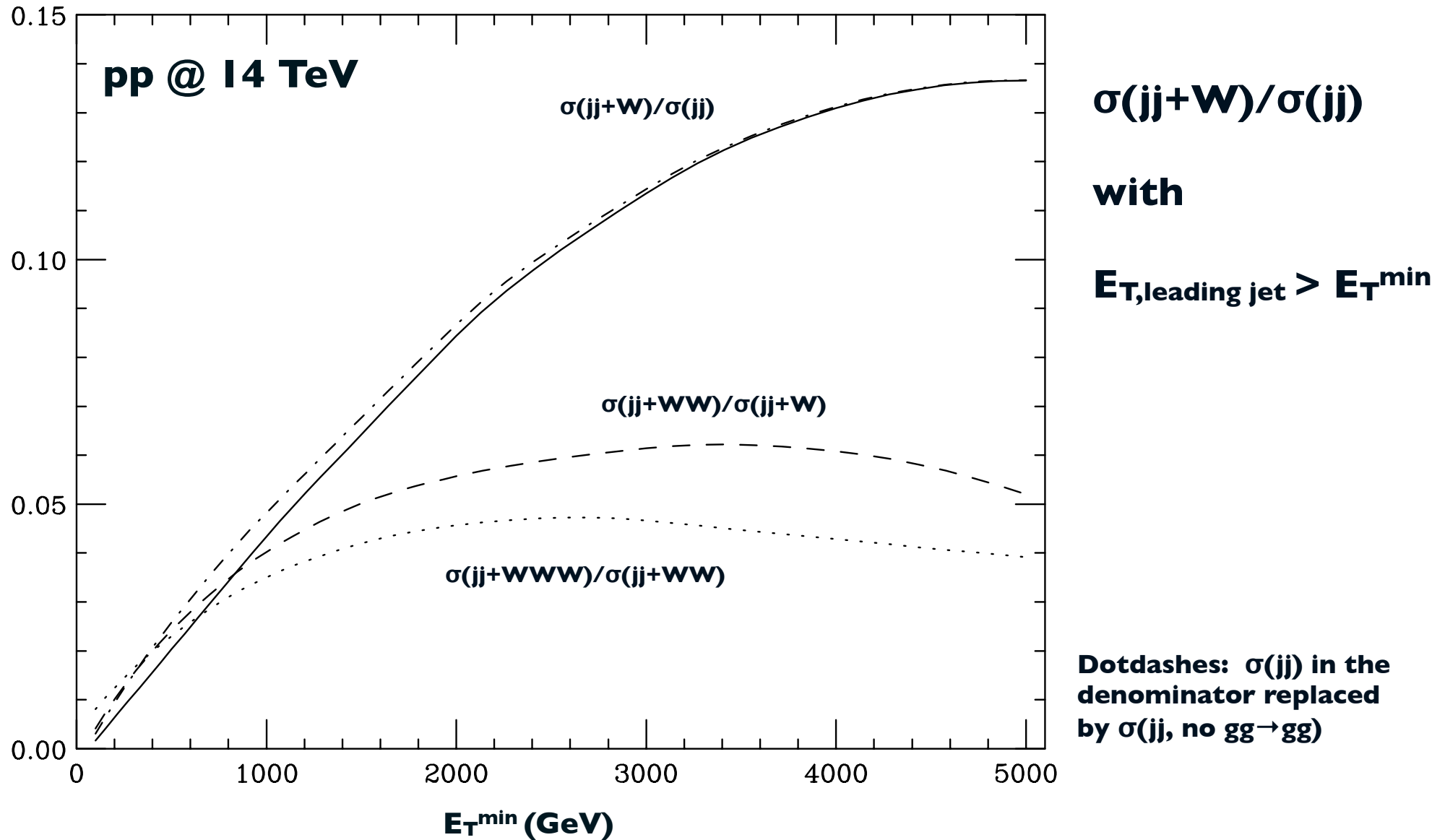
# Rate comparison 8 vs 13 TeV: dijet production



# Remarks

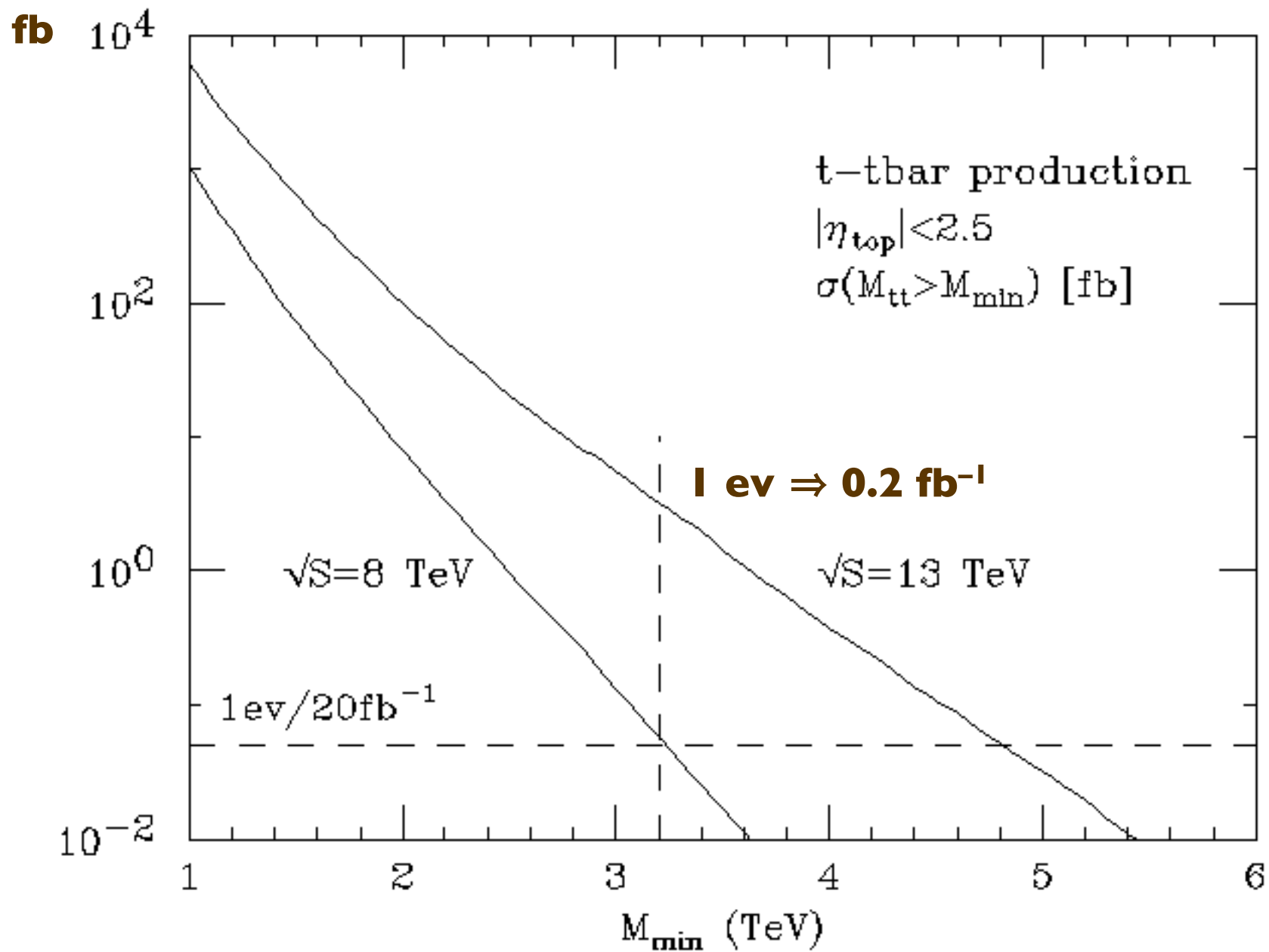
- Large statistics of jets with  $E_T$  in the multi-TeV range =>
  - start measurements of large EW effects

# W production in dijet events



- **Substantial increase of W production at large energy: over 10% of high-ET events have a W or Z in them!**
- **It would be interesting to go after these W and Zs, and verify their emission properties**

# Rate comparison 8 vs 13 TeV: $t\bar{t}$ production

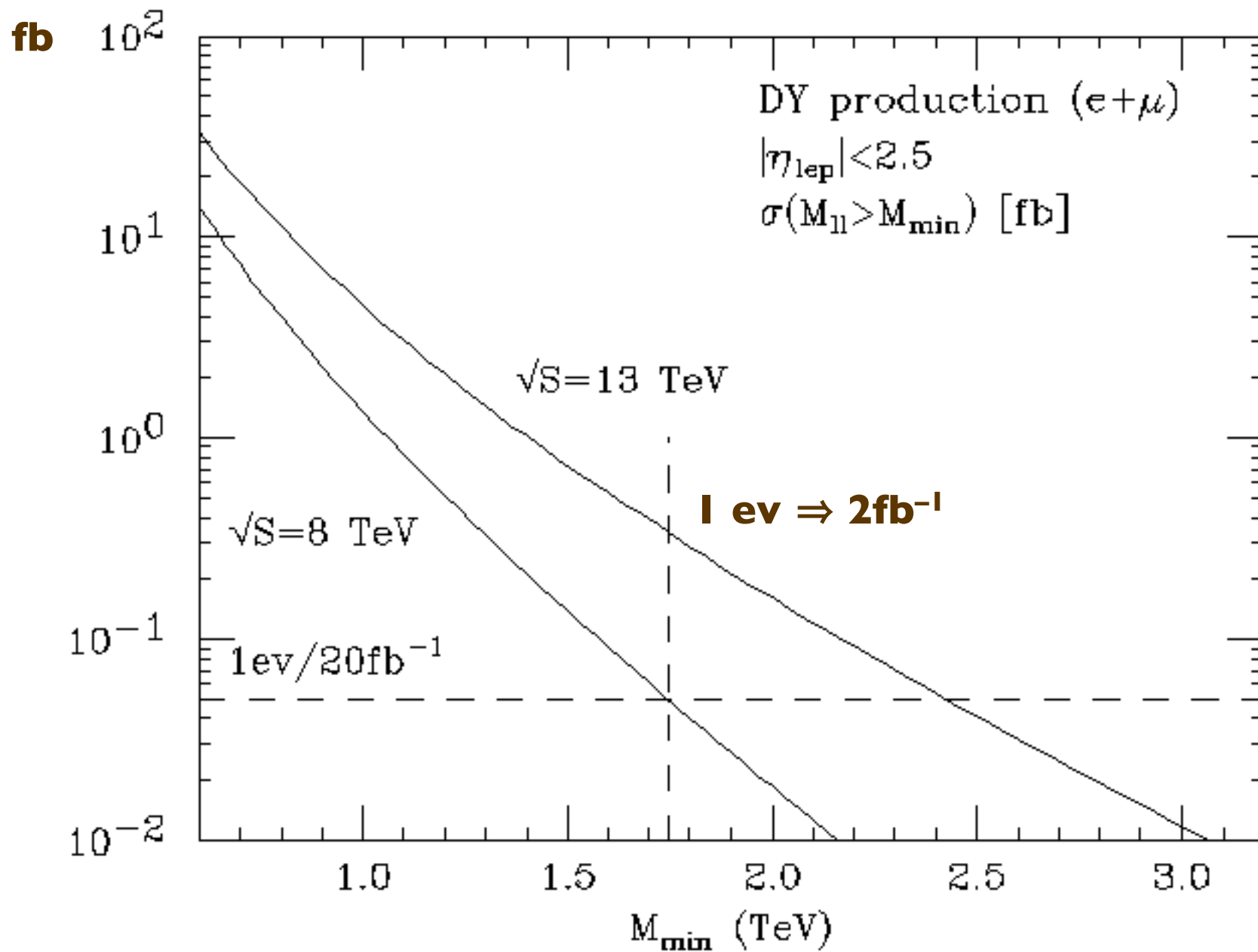


# Remarks

- After  $\sim 20 \text{ fb}^{-1}$  top quark  $E_T$  probed above 2-3 TeV =>
  - Lorentz factor  $\gamma$  larger than 10:
    - top jet  $\sim$  b jet at LEP !
  - all top decay products within a cone with  $R < 0.1$ 
    - “hyper”-boosted regime for top tagging ...



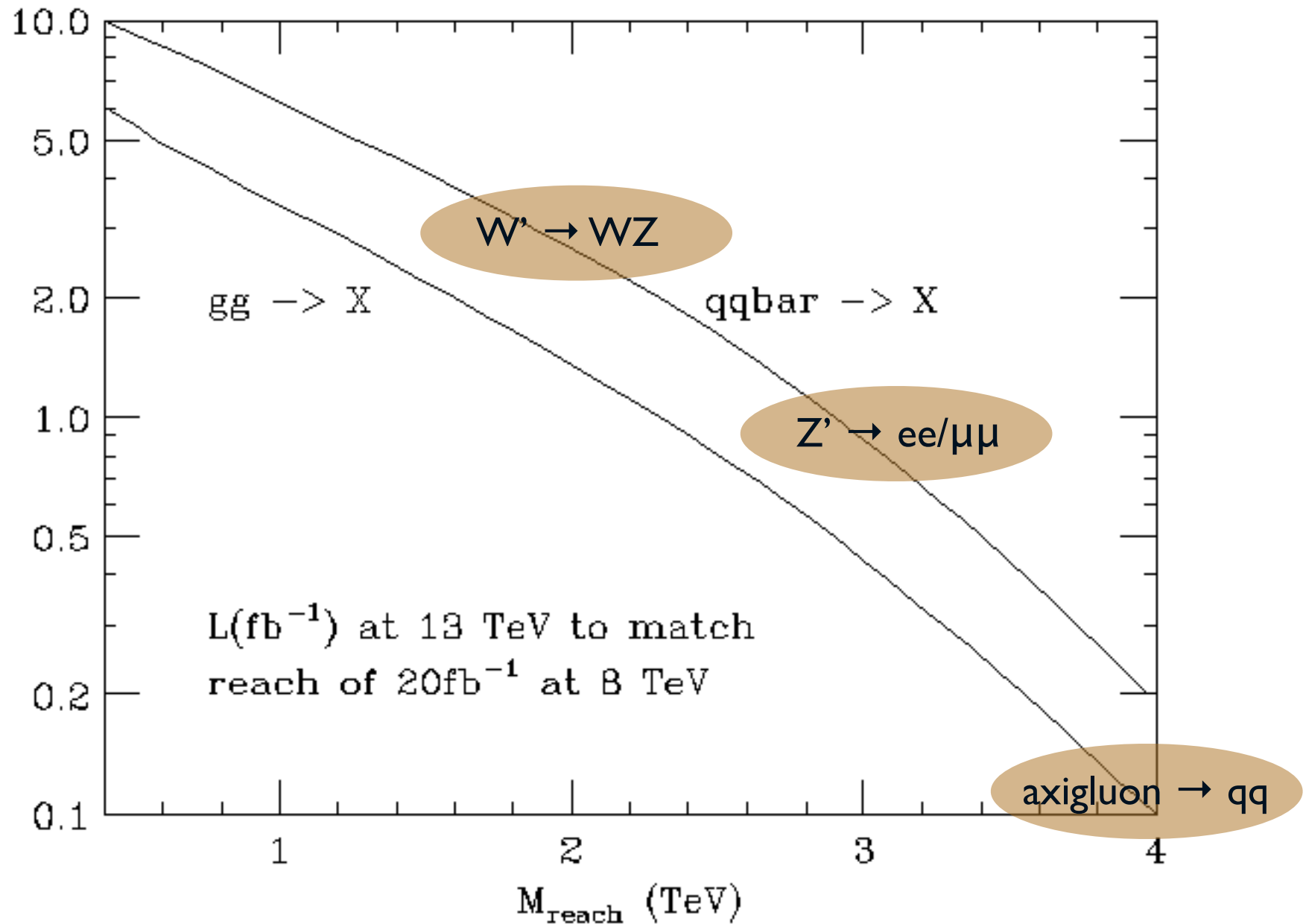
# Rate comparison 8 vs 13 TeV: Drell-Yan production



## ***the rule of thumb ....***

- The more strongly coupled is a process,
  - ➡ the larger is the mass scale that was explored/  
constrained during Run 1,
  - ➡ the larger is the cross section gain from 8→13 TeV,
    - ➡ the sooner Run 2 will catch up and extend the  
search potential

# 13 TeV luminosity required to match BSM sensitivity reached so far ( $20\text{fb}^{-1}$ ) at 8 TeV



See also <http://collider-reach.web.cern.ch>, by Salam and Weiler

# Observation

- For what concerns the extension of the discovery reach at high mass, nothing in the future of the LHC programme will match the step forward from  $20 \text{ fb}^{-1}$  at 8 TeV to  $100 \text{ fb}^{-1}$  at 13 TeV