

# Concept for a compact low emittance cell Plans for an upgrade of the Swiss Light Source

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Antoni Gaudí (1852-1926): *"buttresses are the crutches of the Gothic"* ⇒ follow nature (i.e. the directions of force):

- inclined columns and walls
- cosh-shaped ("parabolic") arcs





Sagrada Familia → Barcelona

which constraints may be released to get new solutions?



# The theoretical minium emittance (TME) cell

Conditions for minimum emittance

$$\beta_o^{\min} = \frac{L}{2\sqrt{15}} \quad \eta_o^{\min} = \frac{hL^2}{24} \implies \varepsilon_{xo}^{\min}[\text{pm} \cdot \text{rad}] = \frac{7.8}{12\sqrt{15}} (E[\text{GeV}])^2 \frac{(\phi[^\circ])^3}{J_x}$$

- periodic/symmetric cell:  $\alpha = \eta' = 0$  at ends
- $\Rightarrow$  over-focusing of  $\beta_x \Rightarrow$  phase advance  $\mu^{\min} = 284.5^{\circ}$ 
  - 2<sup>nd</sup> focus, useless
     overstrained optics, huge chromaticity...
  - Iong cell
  - ⇒ better have two relaxed cells of  $\phi/2$
  - ➡ MBA concept...



#### **Relaxed TME cells**

 Deviations from TME conditions

$$F = \frac{\varepsilon_{xo}}{\varepsilon_{xo}^{\min}} \quad b = \frac{\beta_o}{\beta_o^{\min}} \quad d = \frac{\eta_o}{\eta_o^{\min}}$$

 Ellipse equations for emittance

$$\frac{5}{4}(d-1)^2 + (b-F)^2 = F^2 - 1$$

• Cell phase advance  

$$\tan \frac{\mu}{2} = \frac{6}{\sqrt{15}} \frac{b}{(d-3)}$$



is this what we really wanted ?

# what would Gaudí do ?

- 1. disentangle dispersion  $\eta$  and beta function  $\beta_x$ 
  - ⇒ release constraint: focusing is done with quads.
  - ⇒ use "anti-bend" (AB) out of phase with main bend
  - suppress dispersion ( $\eta_{o} \approx 0$ ) in main bend center.
  - allow modest  $\beta_{xo}$  for low cell phase advance.
- 2. optimize bending field for minimum emittance
  - ⇒ release constraint: bend field is homogeneous.
  - ⇒ use "longitudinal gradient bend" (LGB)
  - highest field at bend center  $(h_o = (e/p) B_o)$
  - reduce field h(s) as dispersion  $\eta(s)$  grows
- $\Rightarrow$  sub-TME cell (F < 1) at moderate phase advance

### step 1: the anti-bend (AB)

- General problem of dispersion matching:
  - dispersion is a horizontal trajectory
  - dispersion production in dipoles  $\rightarrow$  "defocusing":  $\eta$ " > 0
- Quadrupoles in conventional cell:
  - over-focusing of beta function  $\beta_x$
  - insufficient focusing of dispersion  $\eta_{\Xi^{^{16}}}$
- $\Rightarrow$  disentangle  $\eta$  and  $\beta_x$
- use negative dipole: anti-bend
  - kick  $\Delta \eta' = \psi$ , angle  $\psi < 0$
  - out of phase with main dipole
  - negligible effect on  $\beta_x$ ,  $\beta_y$



relaxed TME cell, 5°, 2.4 GeV,  $J_x \approx 2$ Emittance: **500 pm / 200 pm** 

#### **AB** emittance effects

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AB emittance contribution

$$\varepsilon \propto I_5 = \int_L |h|^3 \mathcal{H} ds \xrightarrow{AB} \approx |h|^3 \frac{\eta^2}{\beta}$$

- η is large and ≈constant at AB
   ⇒ low field, long magnet
- Cell emittance (2×AB +main bend)
  - main bend angle to be increased by 2  $|\psi|$  ⇒ in total, still lower emittance
- AB as combined function magnet
  - Increase of damping partition  $J_x$ 
    - vertical focusing in normal bend
    - horizontal focusing in anti-bend.
  - horizontal focusing required anyway at AB
  - AB = off-centered quadrupole ⇒ half quadrupole







#### **AB impact on chromaticity**

• Anti-bend  $\Rightarrow$  negative momentum compaction  $\alpha$ 

$$\alpha = \frac{1}{C} \left( \int_{\text{LGB}}^{\text{small}} \eta h \, ds + \int_{\text{AB}}^{\text{large}} \eta h \, ds \right) < 0$$

⇒ Head-tail stability for negative chromaticity!

- First simulations on transverse instabilities (Eirini Koukovini-Platia @CERN)
  - SLS candidate lattice :  $\alpha = -10^{-4}$  ; 100 MHz, 5 mA/bunch
  - resistive wall: 10~mm radius Cu-pipe,  $1~\mu m$  NEG
  - broad band resonanter: 8 GHz, Q = 1,  $R = 500 \text{ k}\Omega/\text{m}$
  - transverse instability from HEADTAIL code
  - $\Rightarrow$  unstable for  $\xi = 0$ , stability for  $\xi < -4$

## step 2: the longitudinal gradient bend (LGB)

$$\mathcal{E} \propto I_5 = \int_L |h(s)|^3 \mathcal{H}(s) ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \text{orbit curvature} \\ \frac{h(s) = B(s)}{h(s)} ds \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta')^2}{\beta} \qquad \mathcal{H} = \frac{\eta^2 + (\alpha \eta + \beta \eta'$$

- Longitudinal field variation h(s) to compensate  $\mathcal{H}(s)$  variation
- Beam dynamics in bending magnet
  - Curvature is source of dispersion:  $\eta''(s) = h(s) \rightarrow \eta'(s) \rightarrow \eta(s)$
  - Horizontal optics ~ like drift space:  $\beta(s) = \beta_0 2\alpha_0 s + \frac{1 + \alpha_0^2}{\beta_0} s^2$
  - Assumptions: no transverse gradient (k = 0); rectangular geometry
- Variational problem: find extremal of  $\eta(s)$  for  $I_5 = \int_L f(s,\eta,\eta',\eta'') ds \rightarrow \min$  with functional  $f = \mathcal{H}(s,\eta,\eta',\eta'') |\eta''|^3$ 
  - too complicated to solve
    - mixed products up to  $\eta^{'''}$  in Euler-Poisson equation...
- → special functions h(s), simple (few parameters): variational problem → minimization problem
- $\rightarrow$  numerical optimization

(p/e)

#### LGB numerical optimization

- Half bend in N slices: curvature  $h_i$ , length  $\Delta s_i$
- Knobs for minimizer:  $\{h_i\}, \beta_0, \eta_0$
- Objective:  $I_5$
- Constraints:
  - length:  $\Sigma \Delta s_i = L/2$
  - angle:  $\Sigma h_i \Delta s_i = \Phi/2$
  - [field:  $h_{\rm i} < h_{\rm max}$ ]
  - [optics:  $\beta_0, \eta_0$  ]
- Results:
  - hyperbolic field variation
     (for symmetric bend, dispersion suppressor bend is different)

Ι

• Trend:  $h_0 \to \infty$ ,  $\beta_0 \to 0$ ,  $\eta_0 \to 0$ 



#### LGB optimization with optics constraints

- Numerical optimization of field profile for fixed  $\beta_0$ ,  $\eta_0$ 
  - Emittance (F) vs.  $\beta_0$ ,  $\eta_0$  normalized to data for TME of hom. bend



small (~0) dispersion at centre required, but tolerant to large beta function

#### The LGB/AB cell ("Gaudí cell")

- Conventional cell vs. longitudinal-gradient bend/anti-bend cell
  - both: angle 6.7°, E = 2.4 GeV, L = 2.36 m,  $\Delta \mu_x = 160^\circ$ ,  $\Delta \mu_y = 90^\circ$ ,  $J_x \approx 1$



1<sup>st</sup> Workshop on Low Emittance Lattice Design, Barcelona, Apr. 23-24, 2015



#### **SLS lattice and history**



#### SLS upgrade constraints and challenges

- Constraints
  - get factor 20...50 lower emittance (100...250 pm)
  - keep circumference & footprint: hall & tunnel.
  - re-use injector: booster & linac.
  - keep beam lines: avoid shift of source points.
  - "dark period" for upgrade 6...9 months
- Main challenge: *small circumference* (288 m)
  - Multi bend achromat:  $\epsilon \propto (number of bends)^{-3}$
  - Damping wigglers (DW):  $\varepsilon \propto \frac{\text{ring}}{\text{ring} + \text{DW}}$  radiated power
  - ⇒ Low emittance from MBA and/or DW requires space !
  - $\Rightarrow$  Scaling MAX IV to SLS size and energy gives  $\epsilon \approx 1 \ nm$  \*
  - $\Rightarrow$  LGB/AB-cell based MBA  $\Rightarrow$  ε ≈ 100...200 pm ✓

#### SLS-2 lattice design



Various concept lattice designs for 100-200 pm

(factor 25...50 compared to SLS-1)

- based on a 7-bend achromat arc.
- Iongitudinal gradient bends and anti-bends.
- period-3 lattice: 12 arcs and 3 different straight types.
- beam pipe / magnet bore  $\varnothing$  20 / 26 mm.

#### 60 s.c. superbend LGB/AB lattice



#### n.c. bend LGB/AB lattice



#### s.c./n.c. hybrid MBA lattice



#### **SLS-2** design priorities

- Dynamic aperture optimization
  - Non-linear optics optimization to provide sufficient lifetime and injection efficiency.
  - → Mike Ehrlichman's talk
- Injection scheme
  - off-axis and on-axis schemes using existing SLS injector.
  - → Angela Saa Hernandez' talk
- Impedances and instabilities
  - Interaction of beam with narrow, NEG coated beam pipe.
- Alignment and orbit correction
  - Magnet/girder integration, dynamic alignment, photon BPMs.
  - Rely on beam based alignment methods.

#### **Time schedule**

#### Jan. 2014 Letter of Intent submitted to SERI (SERI = State secretariat for Education, Research and Innovation)

#### schedule and budget

- 2017-20 studies & prototypes 2 MCHF
- 2021-24 new storage ring 63 MCHF beamline upgrades 20 MCHF
- Oct. 2014 positive evaluation by SERI: SLS-2 is on the "roadmap".
- Concept decisions fall 2015.
- Conceptual design report end 2016.

#### Conclusion

- Anti bends (AB) disentangle horizontal beta and dispersion functions.
- Longitudinal gradient bends (LGB) provide minimum emittance by adjusting the field to the dispersion.
- The new LGB/AB cell provides low emittance at modest cell phase advance.
- Upgrade of the Swiss Light Source SLS has to cope with a rather compact lattice footprint.
- Draft designs for an SLS upgrade are based on LGB/AB-MBAs and on hybrid MBAs, and promise an emittance in the 100..200 pm range.
- A conceptual design report is scheduled for end 2016.