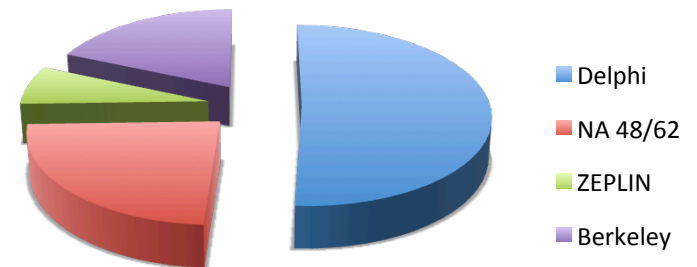
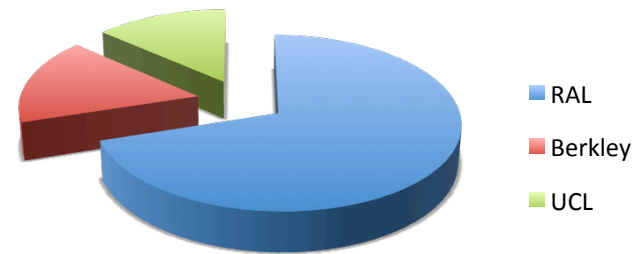
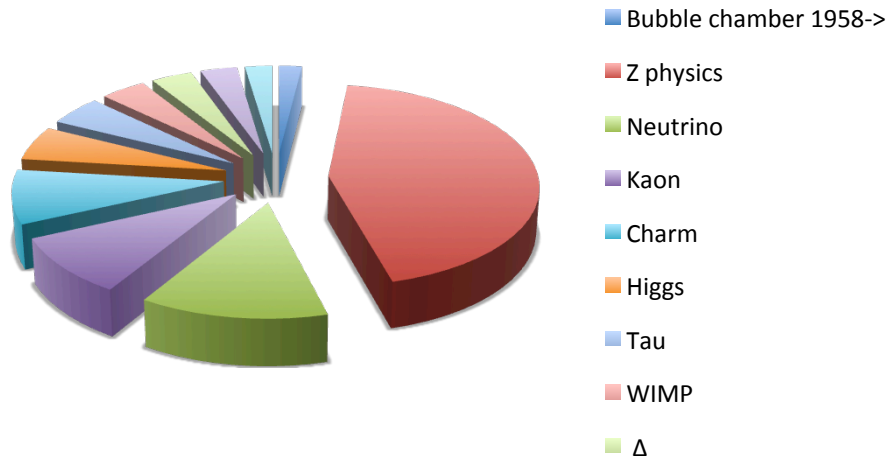


From Regge poles to the Higgs, and beyond

Graham Ross,
Meeting in honour of George@80,
RAL,
April 2015



George @ 80



RAL theory
1969-74

Roger Phillips
Hong Mo Chan
Richard Roberts
Gordon Ringland
D.P.Roy
Hannu Miettinen
Gordy Kane
G.V.Dass

Regge physics,
Veneziano model,..

David Morgan
Mike Pennington
A.N.Kamal

$\pi\pi..$

Pasha Kabir

CP,CPT,C..

A.Love
GGR

Field theory

Particle Theory ~1969

The analytic S-matrix, ELOP, 1966
..., S. Mandelstam

Bootstrap model, G. Chew, 1968

Crossing symmetry + Regge

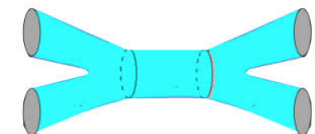


Finite energy sum rules, R. Dolen, D.Horn,
C. Schmidt, 1967

Duality

Construction of a crossing-symmetric, Regge-behaved amplitude
for linearly rising trajectories, G.Veneziano, 1968

Quantum dynamics of a massless relativistic string,
P.Goddard, J. Goldstone, C. Rebbi and C.B.Thorne, 1973



Field theory ~1969

Harvard,
Oxford (J.C.Taylor),..

Electroweak theory:

A model of leptons, S. Weinberg, 1967

Broken symmetries and the masses of gauge bosons, P.Higgs, 1964

Field theory ~1969

Harvard,
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A model of leptons, S. Weinberg, 1967

Broken symmetries and the masses of gauge bosons, P.Higgs, 1964

Alex Love -> S.Weinberg (1970)

(Electromagnetic and weak masses, S. Weinberg, 1972)

Purely hadronic weak interactions in unified field theories of the weak and electromagnetic interactions,

D.Bailin, A.Love, D.Nanopoulos, *GGR*, 1973

$SU(2) \times U(1)$ afterthought

(Just before Gargamelle)

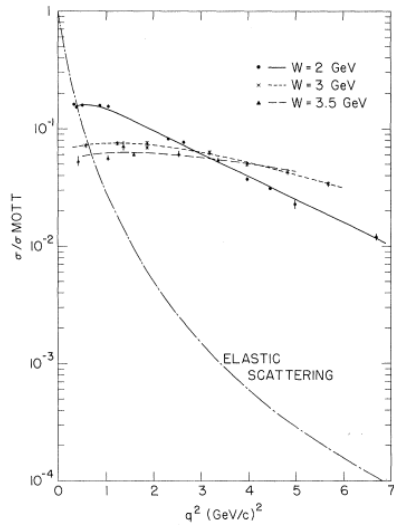
Polarised scattering as test for Z parity violating coupling

Quarks and QCD

Quark model for the elementary particles, R.H.Dalitz, 1965, 1973... (F.E.Close)

QCD, Fritzsche, Gell-Mann, Leutwyler 1972-73

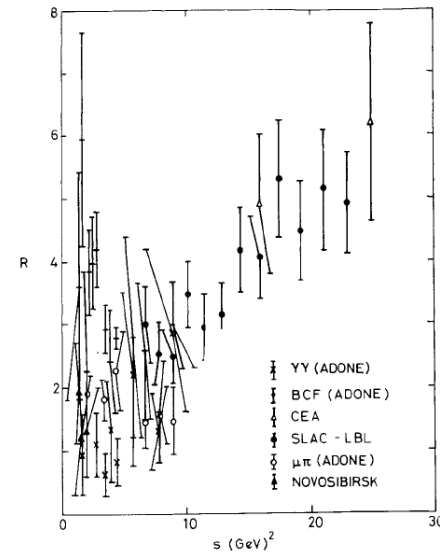
Asymptotic freedom, H.D. Politzer; D.J.Gross, F. Wilczek (1973).



Breidenbach et al 1969

Bjorken scaling

$$\frac{\sigma_{e^+e^- \rightarrow \text{hadrons}}}{\sigma_{e^+e^- \rightarrow \mu^+\mu^-}}$$



1974

Ambiguous

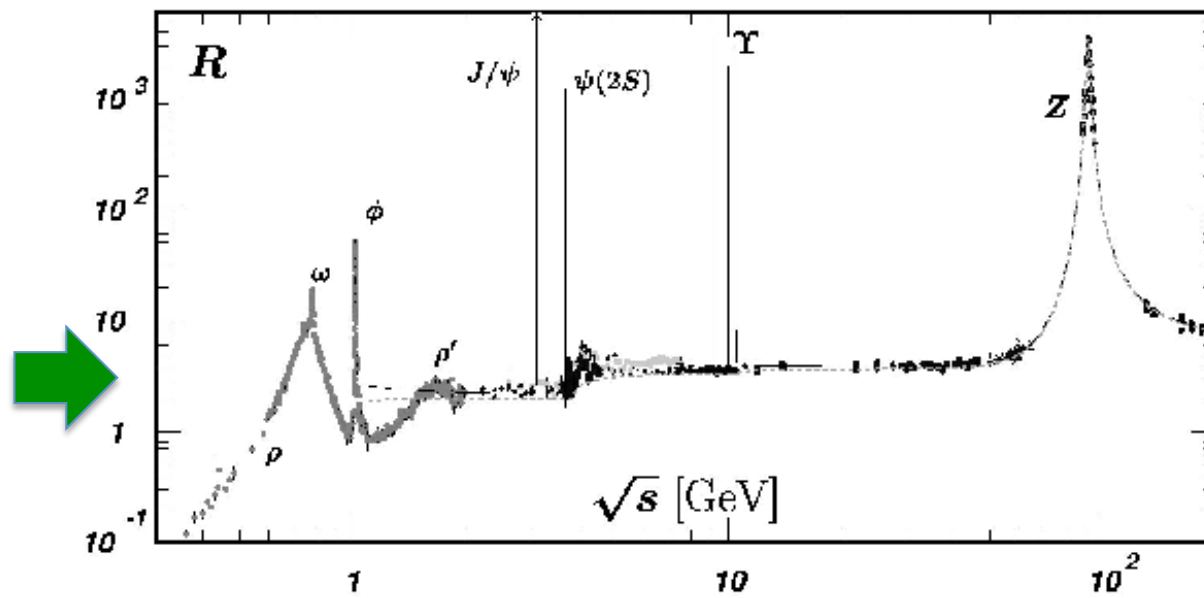
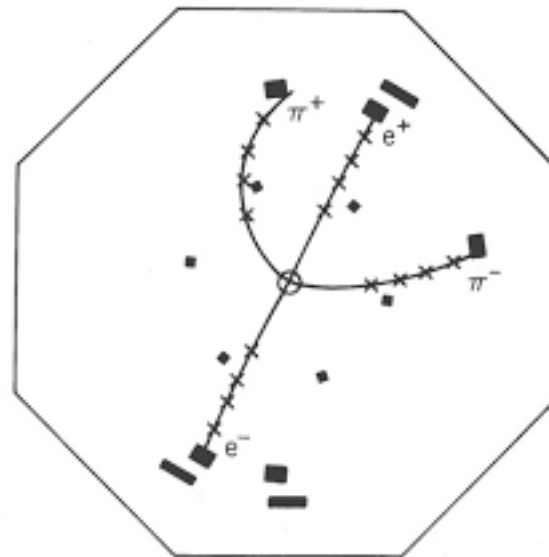
...by 1974 : theoretical elements of Standard Model in place

...but community not convinced

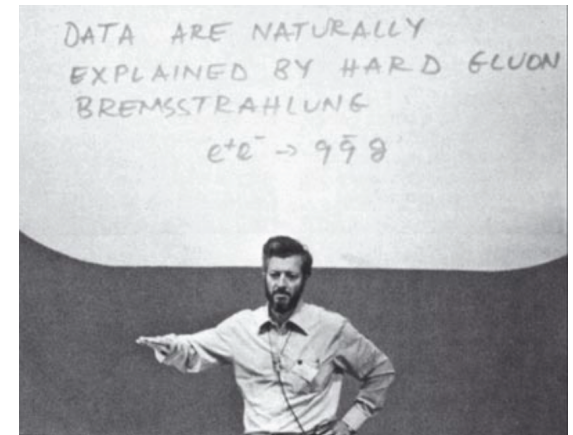
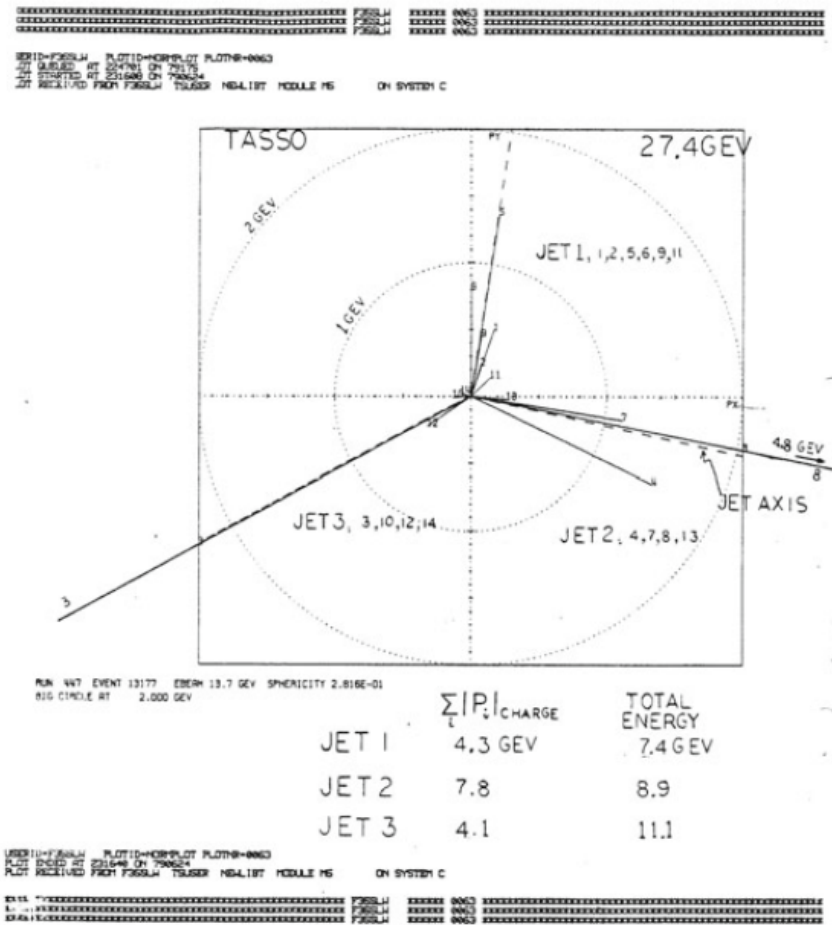
J/ ψ discovery

November 1974

Physics telegrams:
Z?, H?, ...



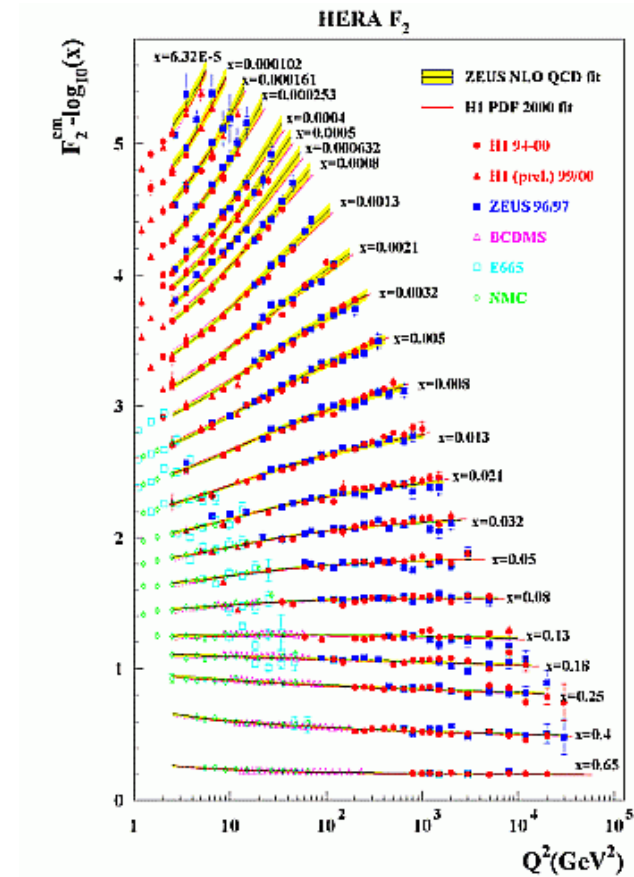
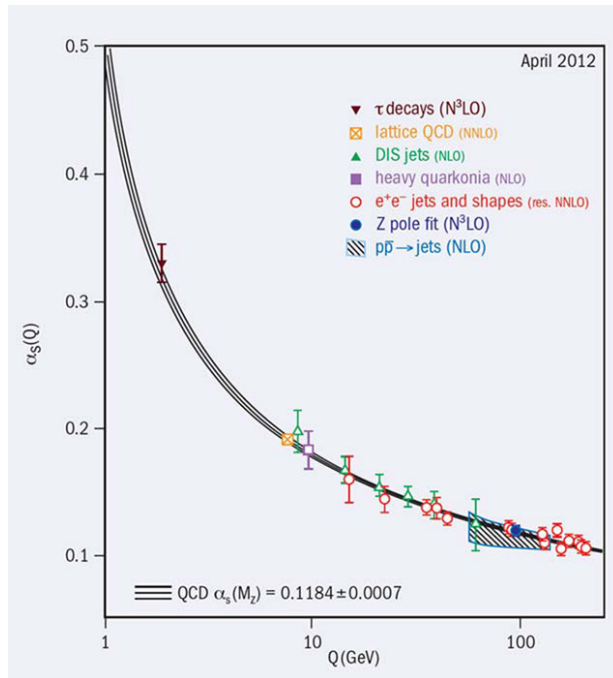
DESY: JADE, Mark-J, PLUTO, TASSO - Lepton-Photon symposium Fermilab, Aug 1979



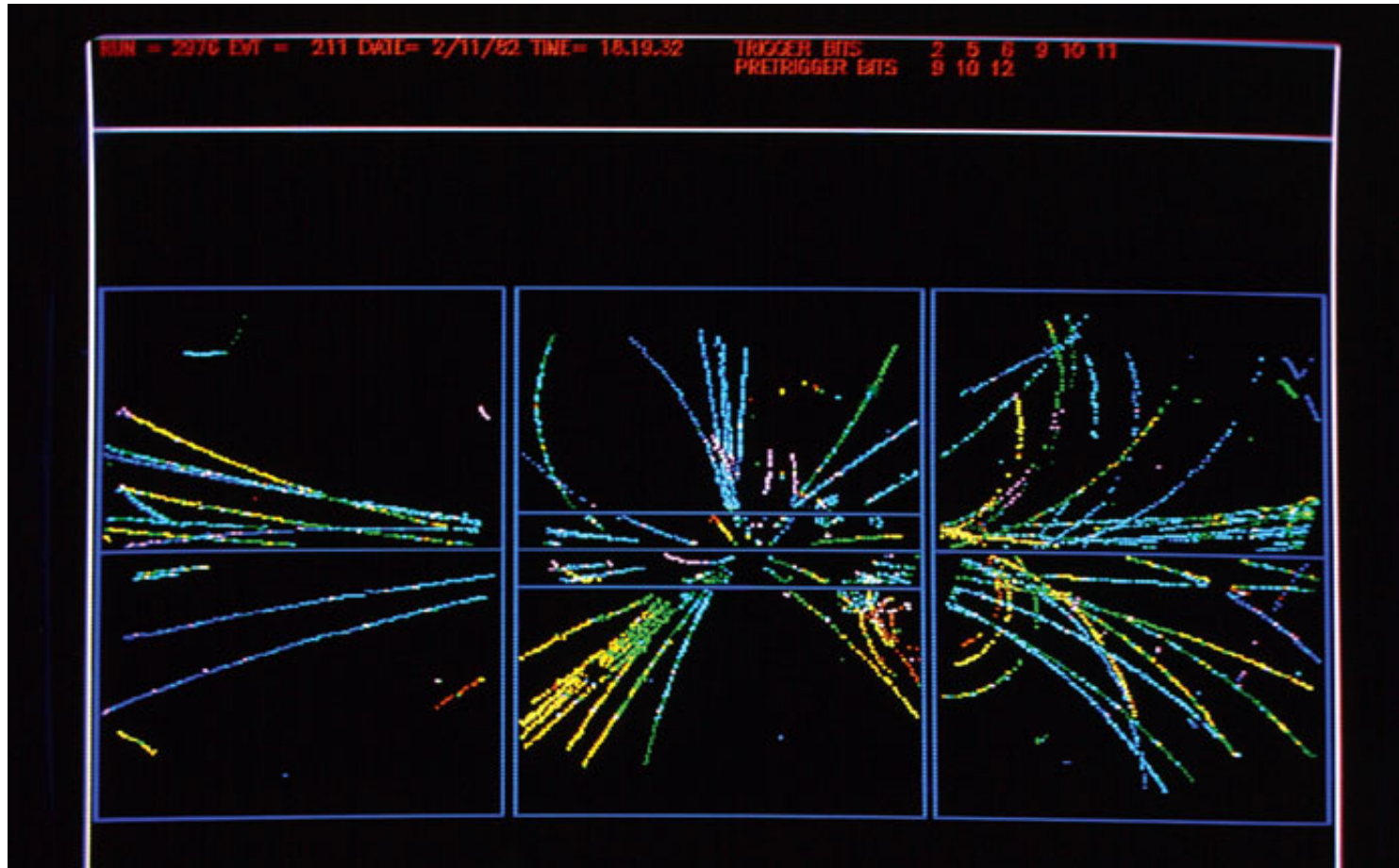
The computer printout of the first three-jet event found in June 1979

Second force particle(s) discovered!

QCD predictions confirmed



UA1, UA2 W, Z discovery (1983)



$$SU(3) \times SU(2) \times U(1)$$

τ (1975), b (1977), t (1995), ν_τ (2000) discoveries

complete the Standard Model

... apart from the Higgs

τ (1975), b (1977), t (1995), ν_τ (2000) discoveries

complete the Standard Model

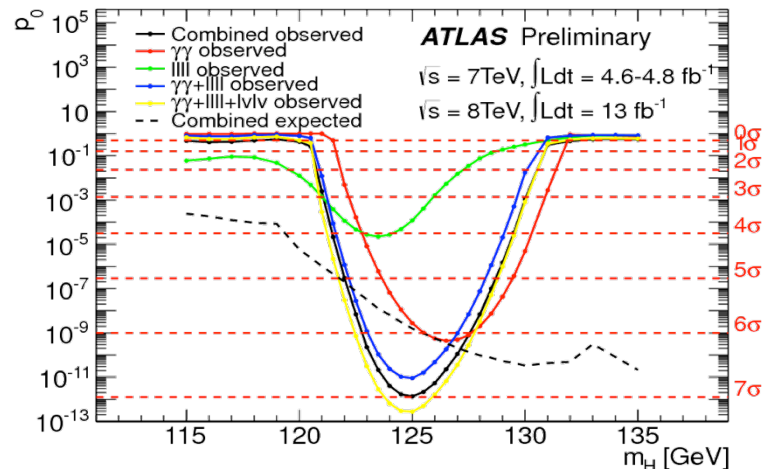
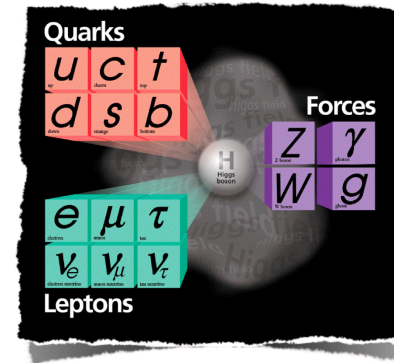
... apart from the Higgs

...fast forward

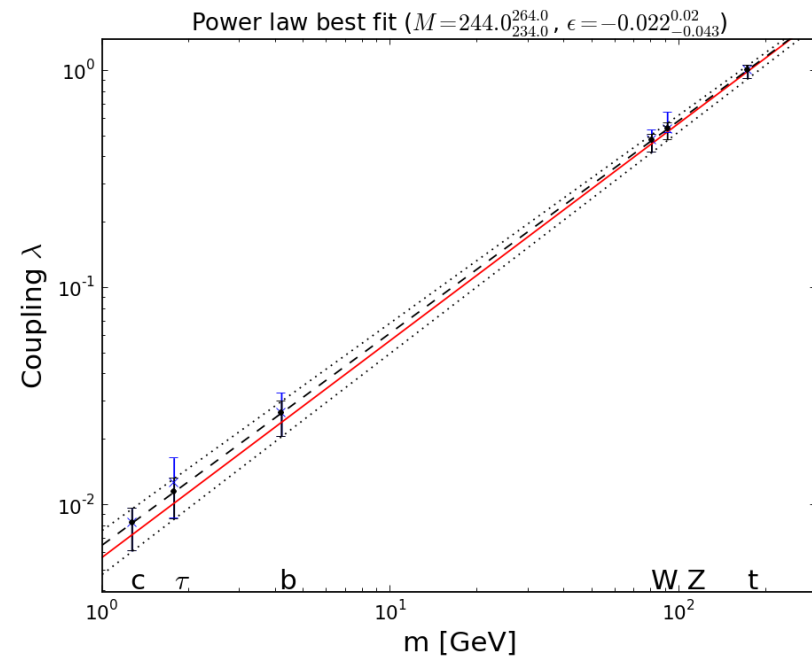
LHC

Higgs discovery (2012)!

...completes the Standard Model



$m_H = 125.09 \pm 0.24$ (0.21 stat. \pm 0.11 syst.) GeV

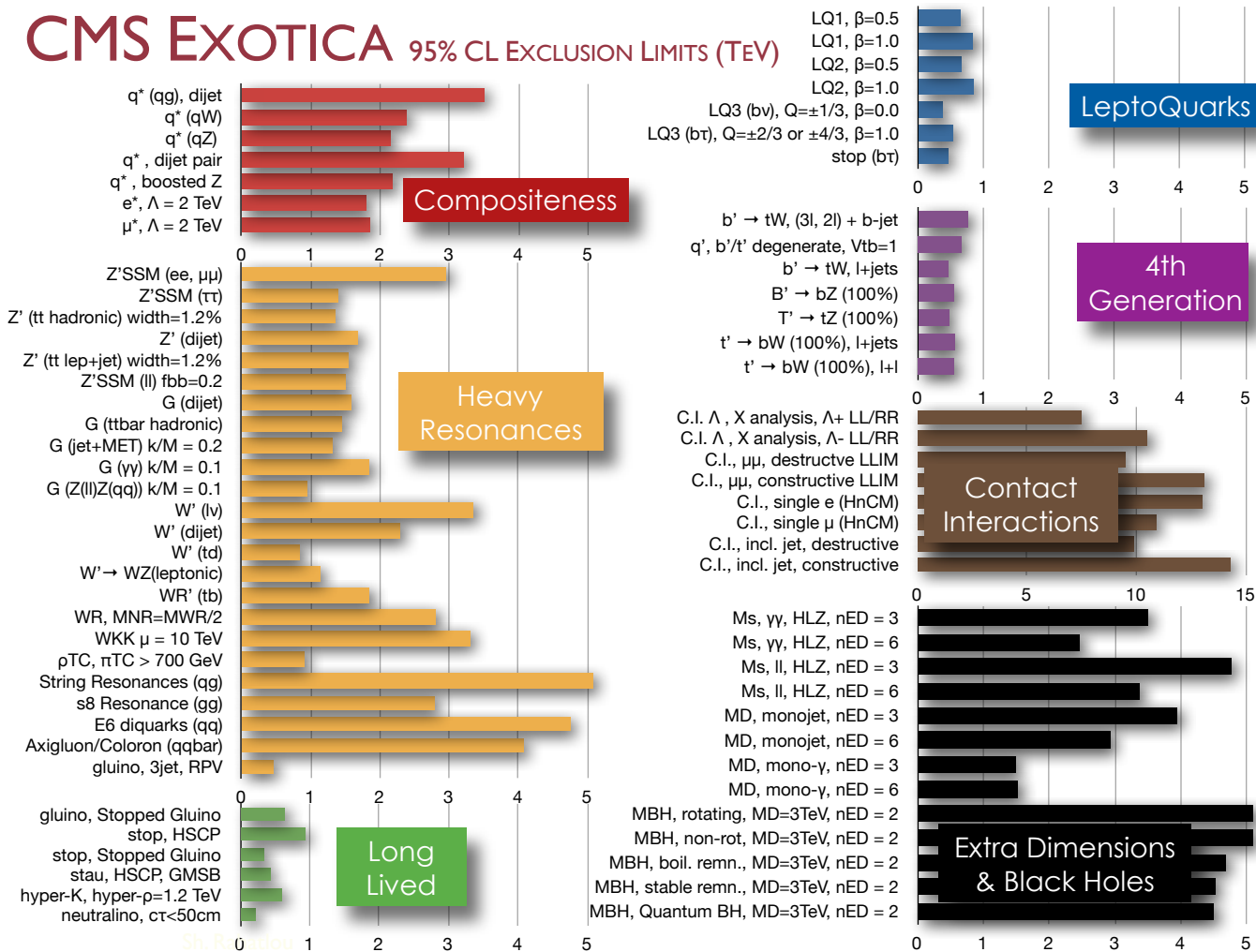


- Strong exclusion of a spin-1 resonance
- 0^- excluded at $> 3\sigma$ level
- Graviton-like resonances excluded at $> 3\sigma$

LHC 8

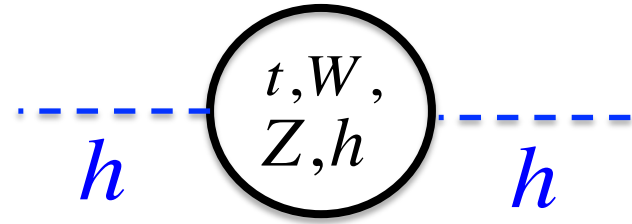
No evidence (yet) for BSM

CMS EXOTICA 95% CL EXCLUSION LIMITS (TeV)



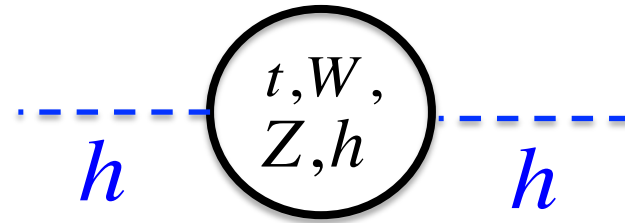
... and beyond

The Hierarchy problem



$$\delta m_h^2 |_{SM} = \frac{3G_F}{4\sqrt{2}\pi^2} (4m_t^2 - 2m_W^2 - m_Z^2 - m_h^2) \Lambda^2 = \left(\frac{\Lambda}{500 \text{ GeV}} \right)^2 m_h^2$$

The Hierarchy problem

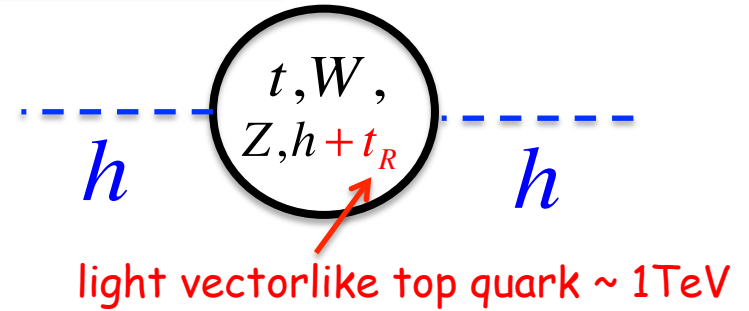


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Light Higgs \Rightarrow Symmetry protection

- Composite models - Higgs as Pseudo-Goldstone boson
- Supersymmetric models - Higgs as chiral superpartner
- Scale invariant models - $m_0^2 + \delta m^2 = 0$

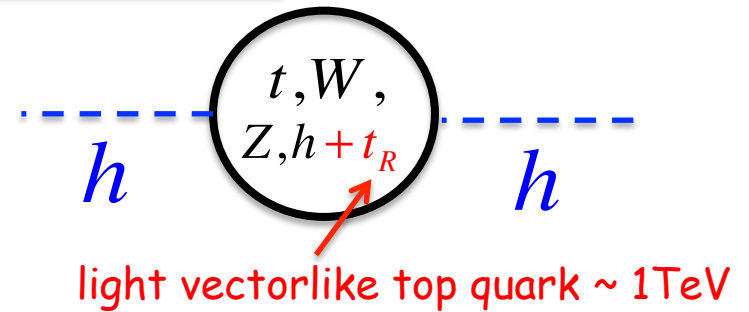
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Partial compositeness \Rightarrow Technifermion top quark resonance $\sim 1\text{TeV}$

● Composite models - Higgs as Pseudo-Goldstone boson



$$\delta m_h^2 |_{SM} = \frac{3G_F}{4\sqrt{2}\pi^2} (4m_t^2 - 2m_W^2 - m_Z^2 - m_h^2) \Lambda^2 = \left(\frac{\Lambda}{500\text{GeV}} \right)^2 m_h^2$$

Partial compositeness \Rightarrow Technifermion top quark resonance $\sim 1\text{TeV}$

LHC discovery potential:

QCD pair production: $\sigma_{m_t=500\text{GeV}} = 570\text{fb}$, $\sigma_{m_t=1\text{TeV}} = 1.3\text{fb}$ (8TeV CM)

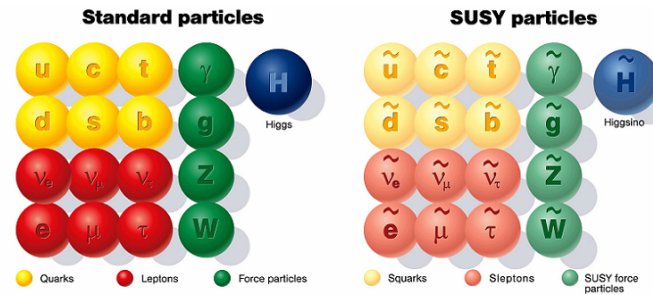
$BR(Q_{5/3(8/3)} \rightarrow l^+l^+ ..) = 5(6)\%$, $BR(Q_{5/3(8/3)} \rightarrow lll..) = 3(6.5)\%$

LHC₈ $m_t > 770\text{GeV}$ (95%)

Panico et al
1201.7114
Pappadopulo et al
1303.3062

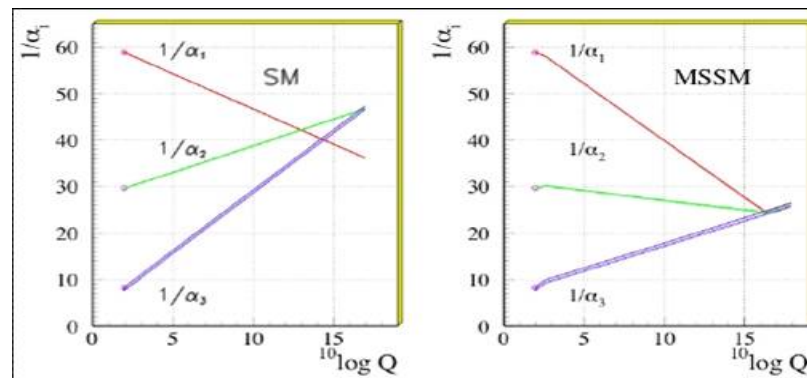
- Supersymmetric models - Higgs as chiral superpartner

e.g. MSSM:



$$\begin{pmatrix} \tilde{H}_u \\ H_u \end{pmatrix}, \begin{pmatrix} \tilde{H}_d \\ H_d \end{pmatrix}$$

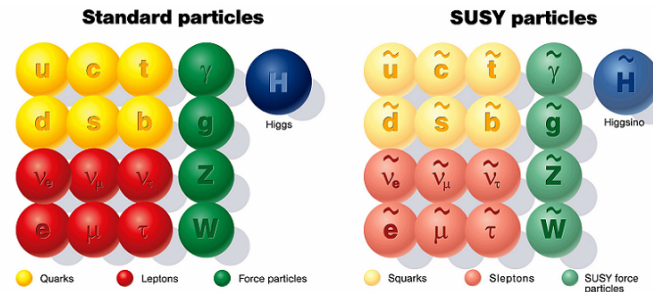
$$\mu \tilde{H}_u \tilde{H}_d, \quad \tilde{H}_u \rightarrow e^{i\alpha} \tilde{H}_u \Rightarrow \mu = 0$$



U. Amaldi, W. deBoer, and H. Furstenau
Ibanez, GGR

- Supersymmetric models - Higgs as chiral superpartner

e.g. MSSM:



$$m_h^2 = M_Z^2 + \frac{3m_t^2 h_t^2}{4\pi^2} \left(\ln \left(m_{stop}^2 / m_t^2 \right) + \delta_t \right) + \dots \approx 126 \text{ GeV}$$

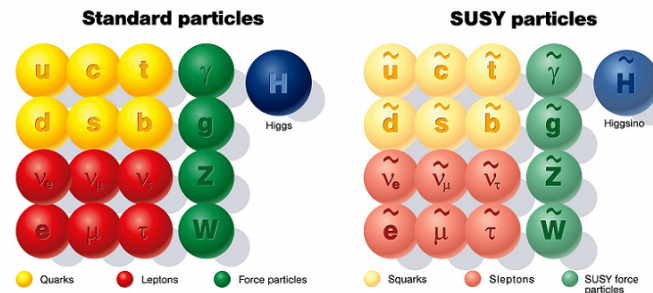
$$\delta m_{H_u}^2 \approx -\frac{3y_t^2}{4\pi^2} \left(m_{stop}^2 + \frac{g_s^2}{3\pi^2} m_{gluino}^2 \log \left(\frac{\Lambda}{m_{gluino}} \right) \right) \log \left(\frac{\Lambda}{m_{stop}} \right)$$

LHC Higgs discovery $\implies \Delta_{\min}^{MSSM} > 350, \quad m_h = 125.6 \pm 3 \text{ GeV}$

↗
Fine tuning measure ($\Delta < 100$ acceptable)

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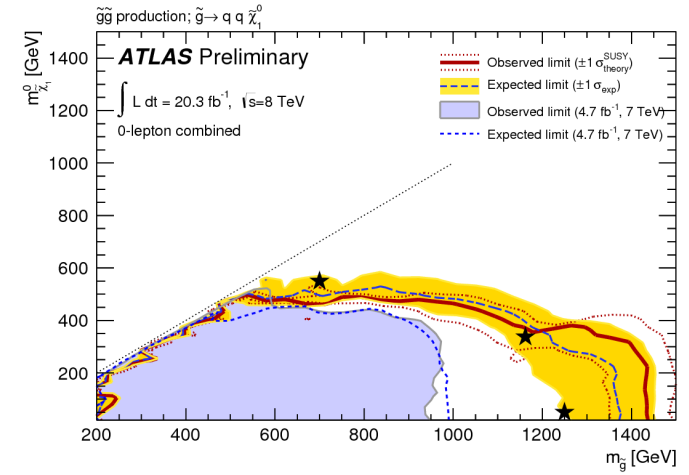
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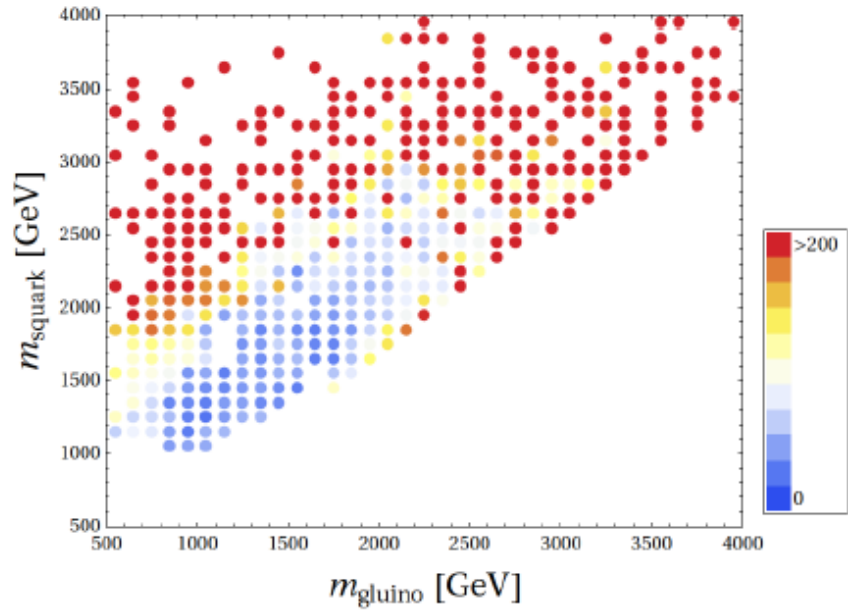
...but generalisations still viable

e.g. NMSSM with non-universal gaugino masses:

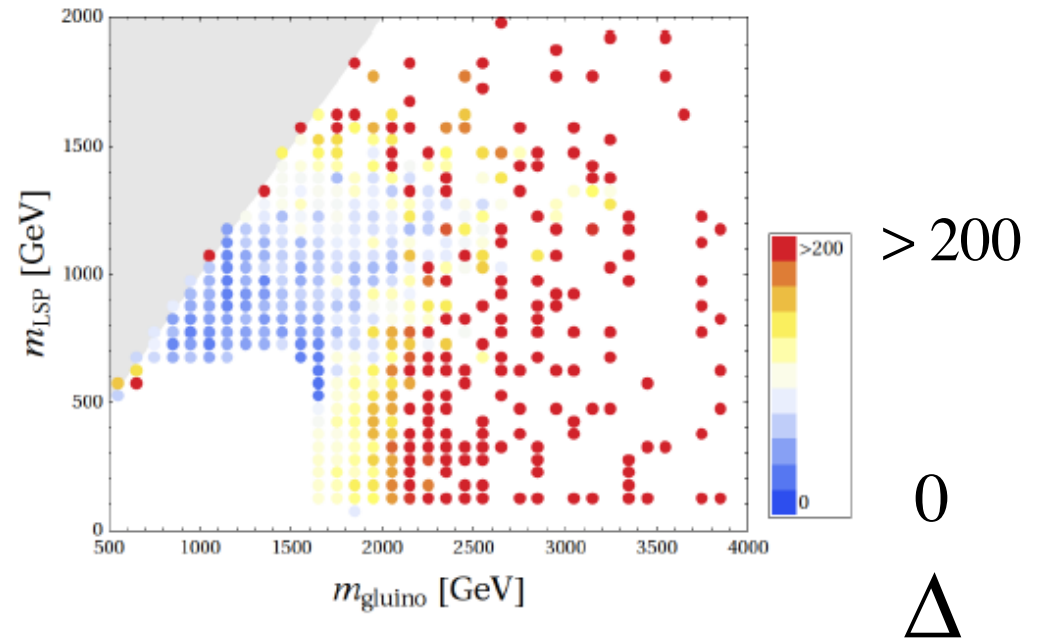
Masses v/s fine tuning



m_{squark}

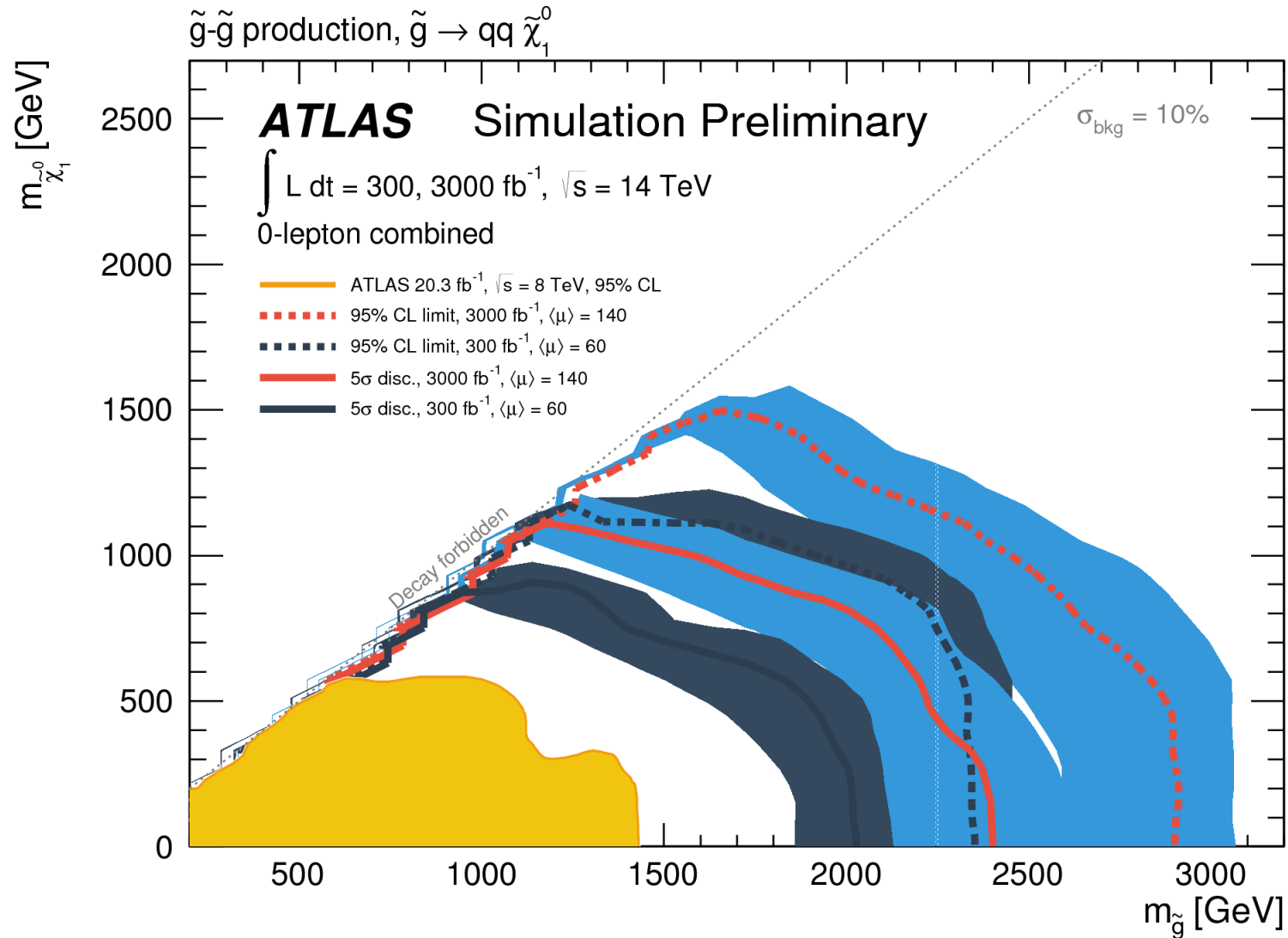


m_{LSP}

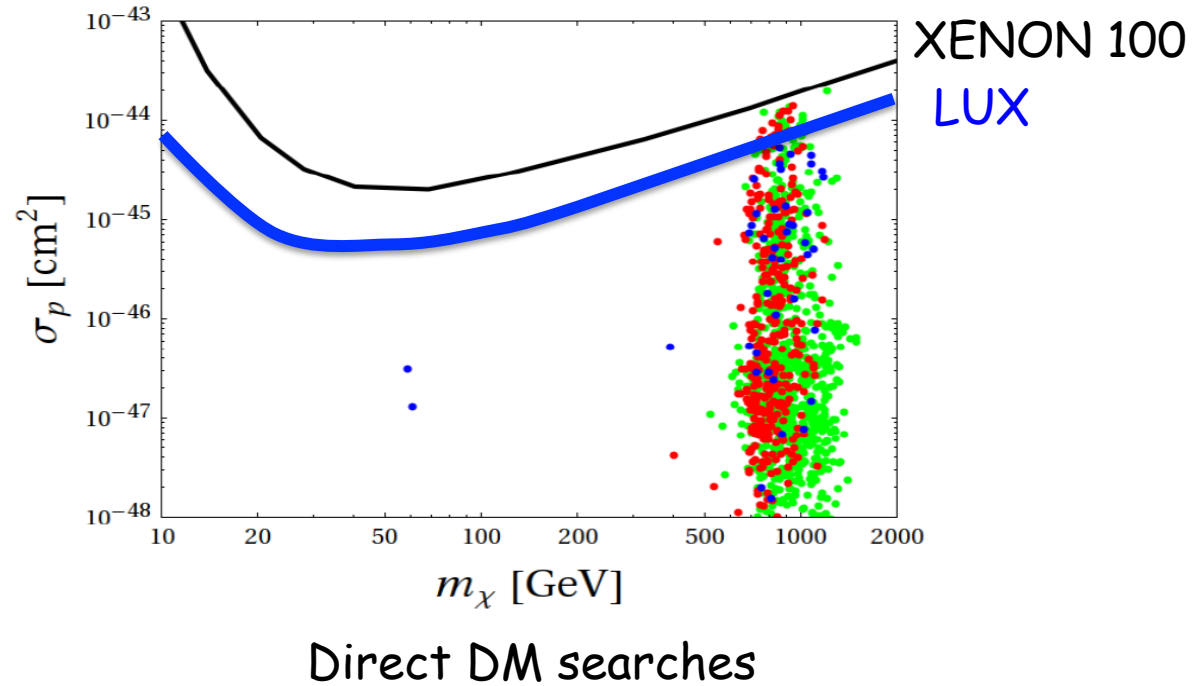
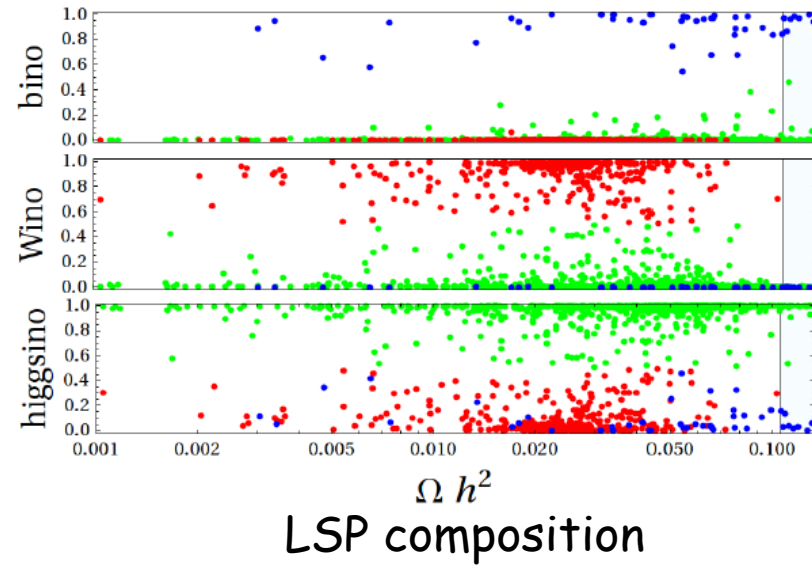


M_{gluino}

Heavy LSP reach



Dark matter



- Scale invariant models:

(SM in absence of Higgs mass is scale invariant)

Field theory: δm^2 not measurable

...only $m^2 = m_0^2 + \delta m^2$ "physical"

Only $m^2 = 0$ special

$$\Rightarrow \frac{d m_H^2}{d \ln \mu} = \frac{3m_H^2}{8\pi^2} \left(2\lambda + y_t^2 - \frac{3g_2^2}{4} - \frac{3g_1^2}{20} \right)$$

...no hierarchy problem for SM!

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(SM in absence of Higgs mass is scale invariant)

Field theory: δm^2 not measurable

...only $m^2 = m_0^2 + \delta m^2$ "physical"

Only $m^2 = 0$ special ... origin of EW breaking ?

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Dimensional transmutation:

Coleman Weinberg

$V(h)$

$$V(h) = \lambda(h)h^4$$

$|h|$

"real" hierarchy problem



..... many models with new **light** states interacting with the Higgs

No heavy thresholds? (real hierarchy problem)

● Neutrino masses?
$$L_{mass} = h_a \bar{l}_a \nu_{Ra} H + \frac{M_{ab}}{2} \nu_{Ra}^T C \nu_{Rb}$$

e.g. $h_A^2 = 5 \cdot 10^{-14}, h_B^2 = 5 \cdot 10^{-15}, M_a = 20 GeV$

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● Baryogenesis?

e.g. ν_{Ra} oscillate

$$\cancel{CP}, \quad L_{A,B,C} \neq 0, \quad L_A + L_B + L_C = 0$$

$$\Delta_{LAB} = L_A + L_B \xrightarrow{\text{Sphalerons}} \Delta B = \Delta_{LAB} / 2$$

No heavy thresholds? (real hierarchy problem)

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● Strong CP problem?

$\frac{\theta}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$, $\theta \leq 10^{-10} ??$

$S = (|S| + f_a) e^{i \frac{a}{f_a}}$, $10^{10} GeV \leq f_a \leq 10^{12} GeV$

● Strong CP problem: $\frac{\theta}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}, \quad \theta \leq 10^{-10} ??$

$$S = (|S| + f_a) e^{i\frac{a}{f_a}}, \quad 10^{10} \text{ GeV} \leq f_a \leq 10^{12} \text{ GeV}$$

DFSZ axion: 2 Higgs doublets $H_{1,2}$, complex singlet, S

$$V(H_1, H_2) = \frac{\lambda_1}{2} |H_u|^4 + \frac{\lambda_2}{2} |H_d|^4 + \lambda_3 |H_u|^2 |H_d|^2 + \lambda_4 |H_u^\dagger H_d|^2 \\ + \zeta_1 |S|^2 |H_u|^2 + \zeta_2 |S|^2 |H_d|^2 + \zeta_3 S^2 H_u H_d + h.c.$$

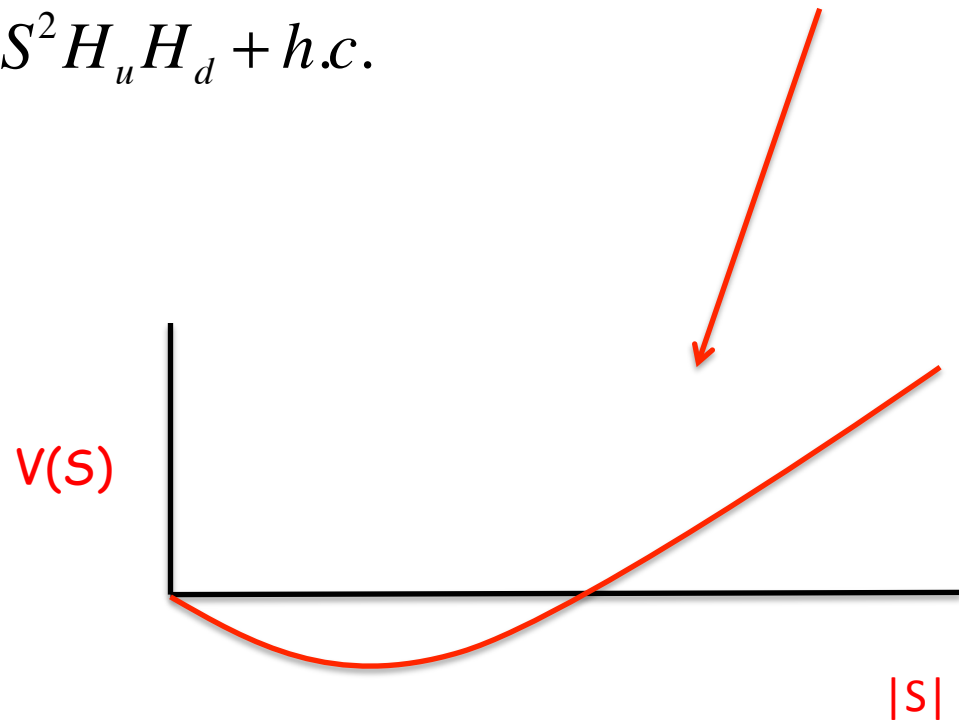
Requires two Higgs doublets (type II couplings) + light pseudo-dilaton

$$m_{H_2^0}^2, m_{H^\pm}^2 \leq O(\text{TeV})$$

Coleman Weinberg in DFSZ model

$$V_{DFSZ}(H_1, H_2, S) \approx \frac{\lambda_1}{2} \left(|H_u|^2 + \frac{\zeta_1}{\lambda_1} |S|^2 \right)^2 + \frac{1}{64\pi^2} (\zeta_2 |S|^2)^2 \left(-\frac{1}{2} + \ln \frac{|S|^2}{f_a^2} \right) + \frac{\lambda_2}{2} |H_d|^4 + \zeta_3 S^2 H_u H_d + h.c.$$

$\zeta_2 S^2 |H_d|^2$



$$\langle H_u^2 \rangle = -\frac{\zeta_1}{\lambda_1} \langle S^2 \rangle \text{ triggers EW breaking}$$

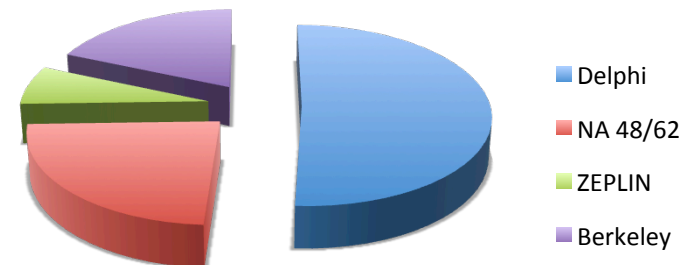
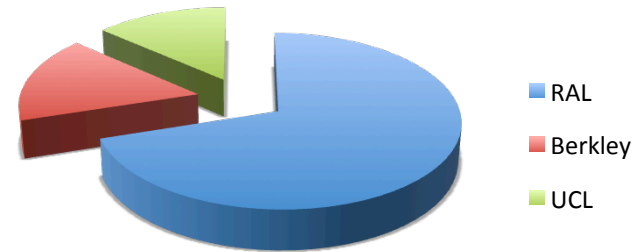
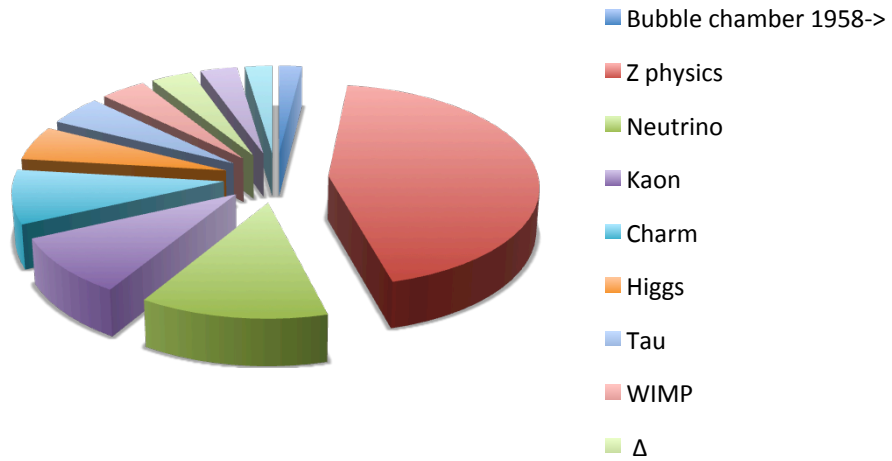
...and beyond

Field theory corrections to Higgs mass inevitable:

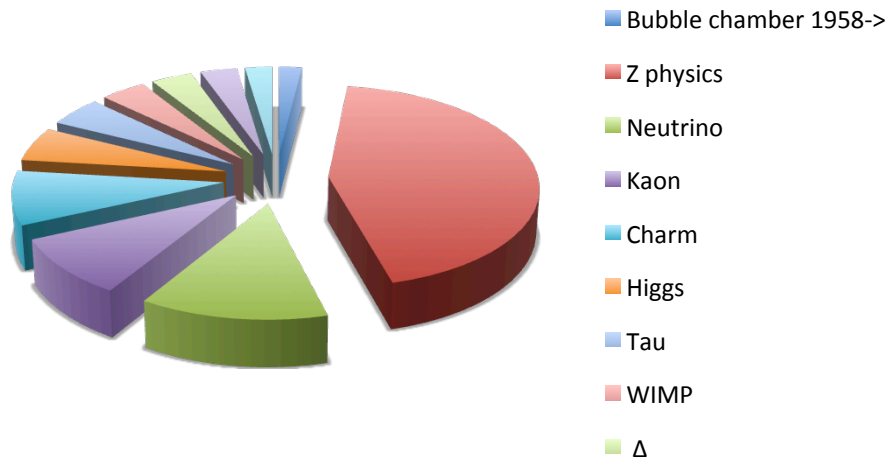
if don't appeal to anthropics need symmetry to keep Higgs light

⇒ BSM physics visible at LHC 13/14

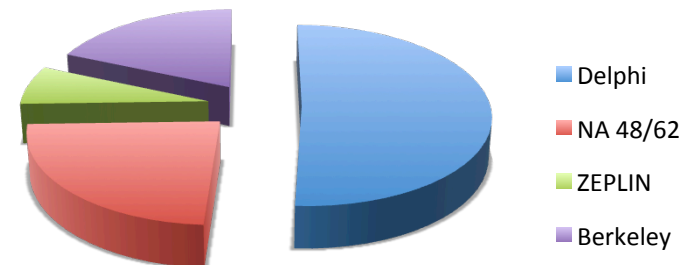
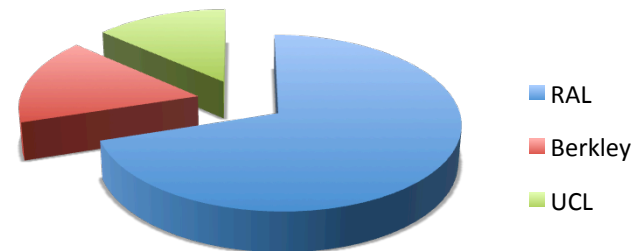
George @ 80



George @ 80, and beyond

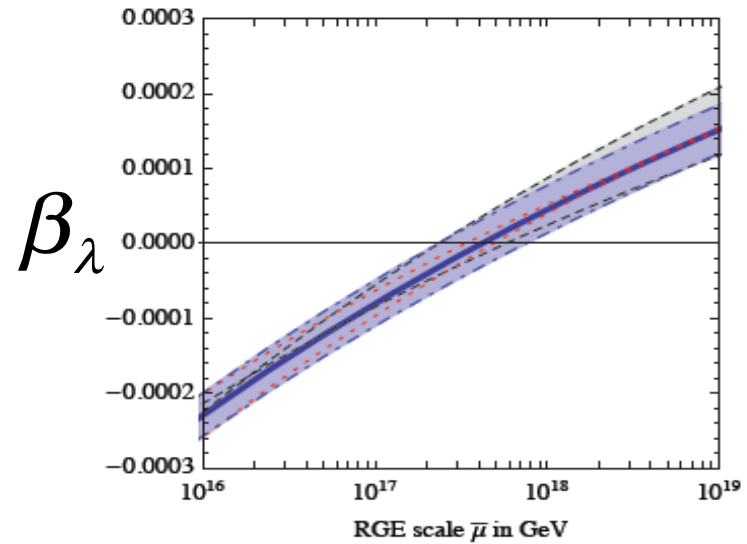
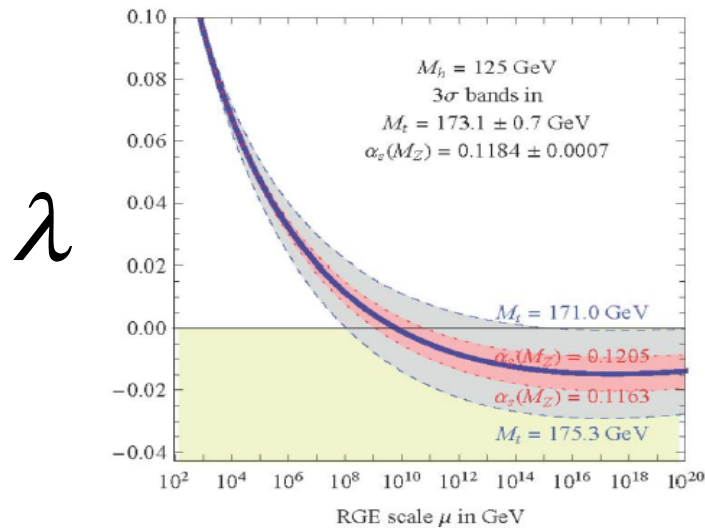


● SUSY discovery?



LHC 8

Higgs discovery!



DeGrassi et al,...

$$V(H) = -m^2 |\phi|^2 + \lambda |\phi|^4$$

$$m^2 \simeq (89 \text{ GeV}^2), \lambda \simeq 0.13$$

