

Resummation effects within k_T -factorization for $c\bar{c}$ and $c\bar{c}c\bar{c}$ production

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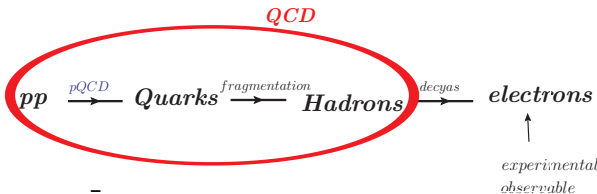


Outline

- 1 Production of $c\bar{c}$
- 2 D meson production
- 3 Production of $c\bar{c}c\bar{c}$ in DPS
- 4 Collinear SPS production of $c\bar{c}c\bar{c}$
- 5 SPS $c\bar{c}c\bar{c}$ production in k_T -factorization
- 6 Perturbative parton splitting
- 7 Multiple $c\bar{c}$ production
- 8 Conclusions

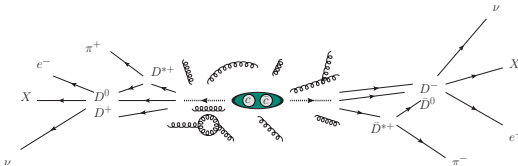


3-step process



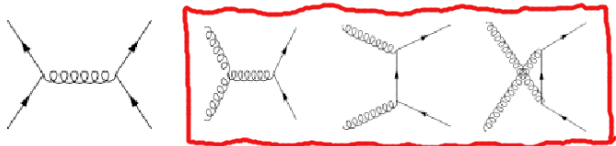
- 1 Heavy quarks $Q\bar{Q}$ pairs production
 - $m_c = 1.5 \text{ GeV}, m_b = 4.75 \text{ GeV} \rightarrow$ perturbative QCD
- 2 Heavy quarks hadronization (fragmentation)
- 3 Semileptonic decays of D and B mesons

$$\frac{d\sigma^e}{dyd^2p} = \frac{d\sigma^Q}{dyd^2p} \otimes D_{Q \rightarrow H} \otimes f_{H \rightarrow e}$$

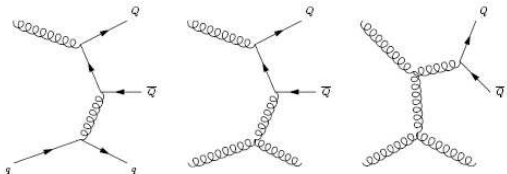


Dominant mechanisms of $Q\bar{Q}$ production

- Leading order processes contributing to $Q\bar{Q}$ production:



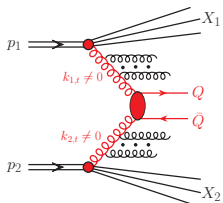
- gluon-gluon fusion** dominant at high energies
- $q\bar{q}$ annihilation important only near the threshold
- some of next-to-leading order diagrams:



NLO contributions \rightarrow K-factor



k_T -factorization (semihard) approach



- charm and bottom quarks production at high energies
→ gluon-gluon fusion
- QCD collinear approach → only inclusive one particle distributions, total cross sections

LO k_T -factorization approach → $\kappa_{1,t}, \kappa_{2,t} \neq 0$
 ⇒ $Q\bar{Q}$ correlations

- multi-differential cross section

$$\frac{d\sigma}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \sum_{ij} \int \frac{d^2\kappa_{1,t}}{\pi} \frac{d^2\kappa_{2,t}}{\pi} \frac{1}{16\pi^2(x_1 x_2 s)^2} \overline{|\mathcal{M}_{j \rightarrow Q\bar{Q}}|^2} \times \delta^2(\bar{\kappa}_{1,t} + \bar{\kappa}_{2,t} - \bar{p}_{1,t} - \bar{p}_{2,t}) F_i(x_1, \kappa_{1,t}^2) F_j(x_2, \kappa_{2,t}^2)$$

- off-shell $\overline{|\mathcal{M}_{gg \rightarrow Q\bar{Q}}|^2}$ → Catani, Ciafaloni, Hautmann (rather long formula)
- major part of **NLO corrections automatically included**
- $F_i(x_1, \kappa_{1,t}^2), F_j(x_2, \kappa_{2,t}^2)$ - unintegrated parton distributions

- $x_1 = \frac{m_{1,t}}{\sqrt{s}} \exp(y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(y_2),$
 $x_2 = \frac{m_{1,t}}{\sqrt{s}} \exp(-y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(-y_2),$ where $m_{i,t} = \sqrt{p_{i,t}^2 + m_Q^2}.$



Unintegrated parton distribution functions

- k_T -factorization \rightarrow replacement: $p_k(x, \mu_F^2) \rightarrow \mathcal{F}_k(x, \kappa_T^2, \mu_F^2)$
- PDFs \rightarrow UPDFs

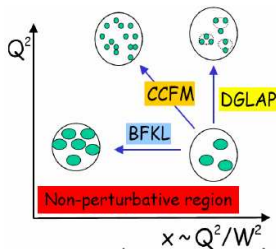
$$x p_k(x, \mu_F^2) = \int_0^\infty d\kappa_T^2 \mathcal{F}(x, \kappa_T^2, \mu_F^2)$$

- UPDFs - needed in less inclusive measurements which are sensitive to the transverse momentum of the parton

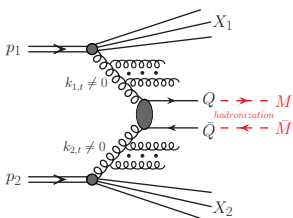
gg-fusion dominance \Rightarrow **great test of existing unintegrated gluon densities!**
especially at LHC (small- x)

several models:

- Jung, Kwiecinski (CCFM, wide x -range)
- Kimber-Martin-Ryskin (higher x -values)
- Kutak-Stasto (small- x , saturation effects)
- Ivanov-Nikolaev, GBW, Karzeev-Levin, etc.



Fragmentation functions technique



- fragmentation functions extracted from e^+e^- data
- often used: Braaten et al., Kartvelishvili et al., Peterson et al.
- rescaling transverse momentum at a constant rapidity (angle)

- from heavy quarks to heavy mesons:

$$\frac{d\sigma(y, p_t^M)}{dyd^2p_t^M} \approx \int \frac{D_{Q \rightarrow M}(z)}{z^2} \cdot \frac{d\sigma(y, p_t^Q)}{dyd^2p_t^Q} dz$$

where: $p_t^Q = \frac{p_t^M}{z}$ and $z \in (0, 1)$

- **approximation:**

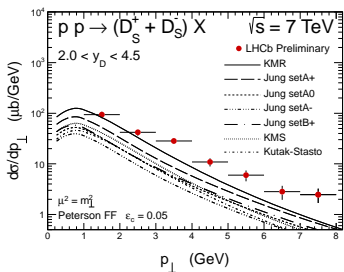
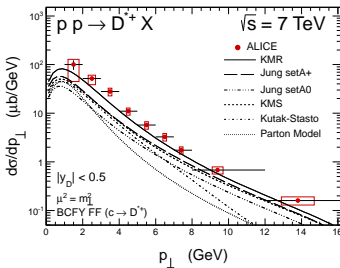
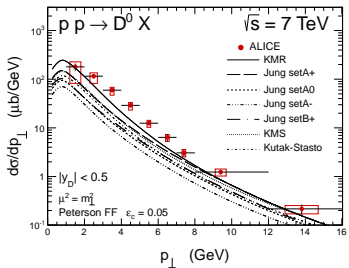
rapidity unchanged in the fragmentation process $\rightarrow y_Q \approx y_M$

Production of D mesons in this framework:

Maciula, Szczurek, Phys. Rev. **D87** (2013) 094022.



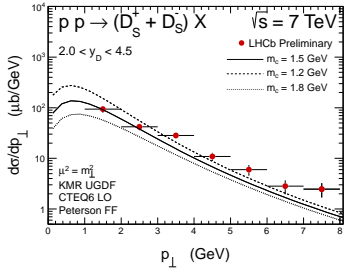
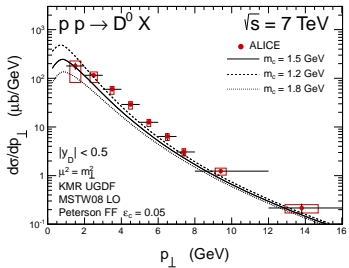
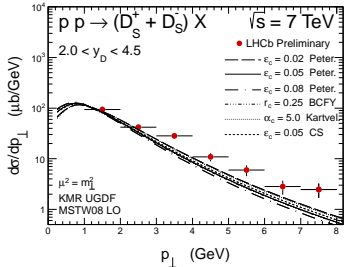
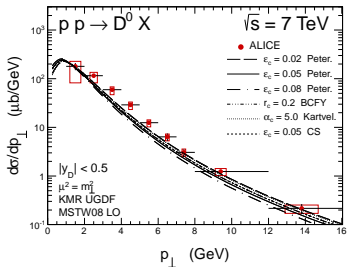
D mesons, different UGDFs



- various UGDFs models → crucial test of their applicability at high energies and small x -values
- only **KMR model** gives good description of the ALICE and LHCb data
- significant difference between LO parton model and LO k_T -factorization



Effects of hadronization and quark mass uncertainty for KMR UGDF



RHIC, different UGDFs

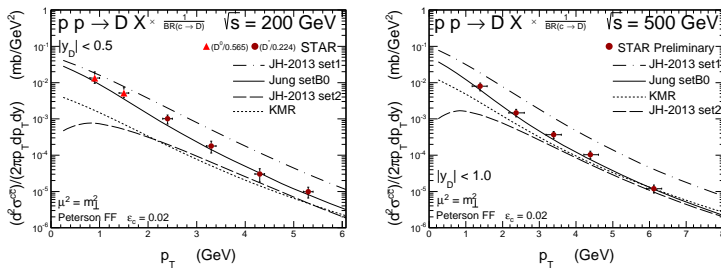


Figure: D mesons cross section normalized to the parton-level cross section. KMR (dotted line), the JH2013 set1 (long-dashed-dotted line), set2 (long-dashed line) and the Jung setB0 (solid line) UGDFs.

R. Maciula, A. Szczurek and M. Luszczak, arXiv:1505.05038



RHIC, uncertainties for Jung setB0 UGDF

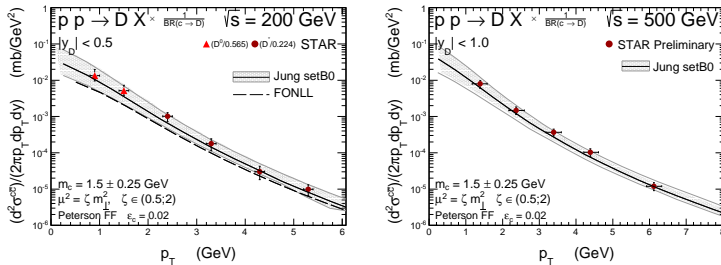


Figure: Uncertainties due to the choice of the factorization and/or renormalization scales and charm quarks mass are summed in quadrature. For $\sqrt{s} = 200$ GeV also results of FONLL.

R. Maciula, A. Szczurek and M. Luszczak, arXiv:1505.05038



Semileptonic decay functions

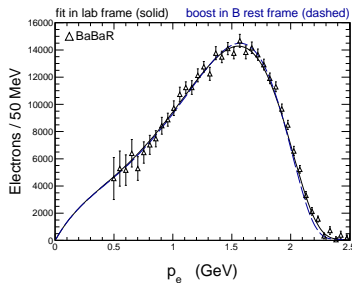
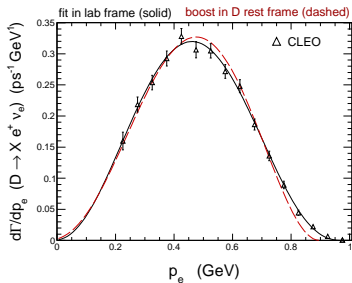


Figure: Fits to the **CLEO** (left) and **BABAR** (right) data. The solid lines correspond to the parametrizations in the laboratory frames and the dashed lines to the meson rest frames.



Non-photonic electrons at RHIC

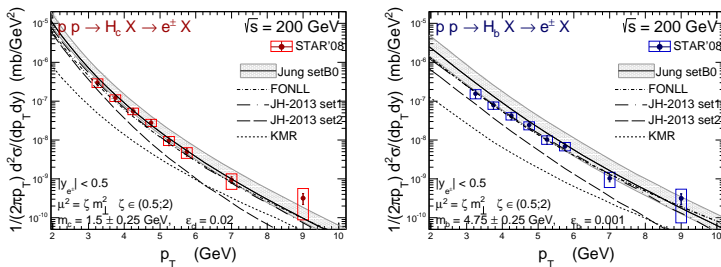


Figure: Electrons from semileptonic decays of charm (left) and bottom hadrons (right). Theoretical uncertainties due to quark mass and scales variation are also shown.



Non-photonic electrons at RHIC

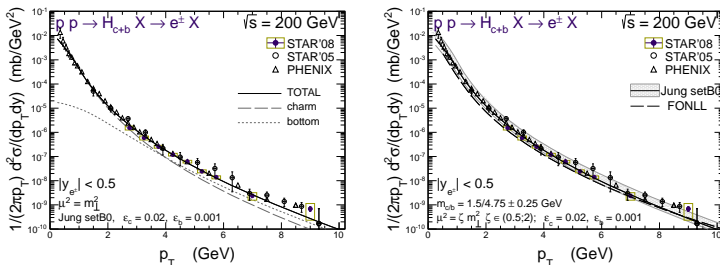


Figure: Electrons coming from both charm and bottom hadrons summed together H_{c+b} . The STAR and PHENIX experimental data are compared to the predictions with the Jung setB0 UGDF.

Separated charm and bottom contributions (left) and theoretical uncertainties due to quark mass and scales variation (right).

The FONLL predictions are drawn for comparison.

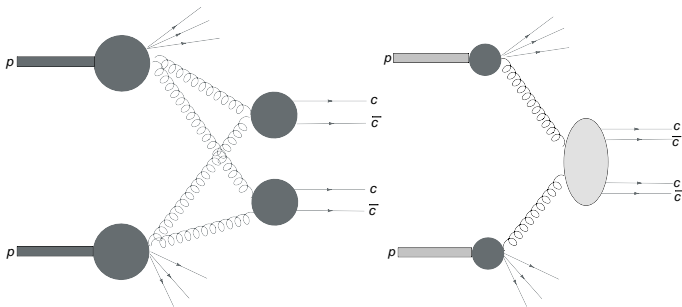


Introduction to DPS

- Cross section for MPI grows fast with energy both for
 - soft processes (e.g. multiplicities)
 - hard processes (mostly DPS)
- Cross section for DPS grows much faster than that for SPS.
- Problems with some processes at the LHC
 - missing strength for charmed mesons
 - missing strength for four jets
 - missing strength for $J/\psi J/\psi$
 - missing strength for $W^+ W^-$
- Already at the LHC there is a **competition between DPS and SPS**
- **Fastly developing field.** We are on the way to better control them.
- MPI and DPS effects at FCC would be much bigger than ever so far



Production of $c\bar{c}c\bar{c}$



Łuszczak, Maciuła, Szczurek, Phys. Rev. **D85** (2012) 014905.



Formalism

Consider reaction: $pp \rightarrow c\bar{c}c\bar{c}X$

Modeling double-parton scattering

Factorized form:

$$\sigma^{DPS}(pp \rightarrow c\bar{c}c\bar{c}X) = \frac{1}{2\sigma_{eff}} \sigma^{SPS}(pp \rightarrow c\bar{c}X_1) \cdot \sigma^{SPS}(pp \rightarrow c\bar{c}X_2).$$

The simple formula can be generalized to include differential distributions

$$\frac{d\sigma}{dy_1 dy_2 d^2p_{1t} dy_3 dy_4 d^2p_{2t}} = \frac{1}{2\sigma_{eff}} \cdot \frac{d\sigma}{dy_1 dy_2 d^2p_{1t}} \cdot \frac{d\sigma}{dy_3 dy_4 d^2p_{2t}}.$$

σ_{eff} is a model parameter (15 mb).

Found e.g. from experimental analysis of four jets (see also [Siódmok et al.](#))

In principle does not need to be universal



Formalism

$$d\sigma^{DPS} = \frac{1}{2\sigma_{eff}} F_{gg}(x_1, x_2, \mu_1^2, \mu_2^2) F_{gg}(x'_1 x'_2, \mu_1^2, \mu_2^2) d\sigma_{gg \rightarrow c\bar{c}}(x_1, x'_1, \mu_1^2) d\sigma_{gg \rightarrow c\bar{c}}(x_2, x'_2, \mu_2^2) dx_1 dx_2 dx'_1 dx'_2.$$

$$F_{gg}(x_1, x_2, \mu_1^2, \mu_2^2), F_{gg}(x'_1 x'_2, \mu_1^2, \mu_2^2)$$

are called **double parton distributions**

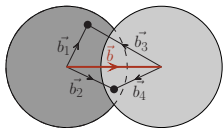
dPDF are subjected to special **evolution equations**

single scale evolution: **Snigirev**

double scale evolution: **Ceccopieri, Gaunt-Stirling**



Factorized Ansatz and double-parton distributions (DPDFs)



DPDF - emission of parton i with assumption that second parton j is also emitted:

$$\Gamma_{i,j}(b, x_1, x_2; \mu_1^2, \mu_2^2) = F_i(x_1, \mu_1^2) F_j(x_2, \mu_2^2) F(b; x_1, x_2, \mu_1^2, \mu_2^2)$$

- correlations between two partons

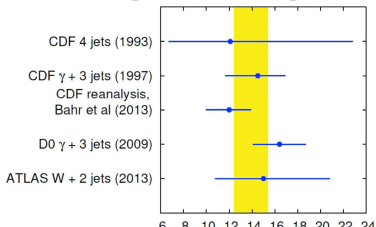
C. Flensburg et al., JHEP 06, 066 (2011)

in general:

$$\sigma_{\text{eff}}(x_1, x_2, x'_1, x'_2, \mu_1^2, \mu_2^2) = \left(\int d^2b F(b; x_1, x_2, \mu_1^2, \mu_2^2) F(b; x'_1, x'_2, \mu_1^2, \mu_2^2) \right)^{-1}$$

factorized Ansatz:

- additional limitations: $x_1 + x_2 < 1$ oraz $x'_1 + x'_2 < 1$
- DPDF in multiplicative form: $F_{ij}(b; x_1, x_2, \mu_1^2, \mu_2^2) = F_i(x_1, \mu_1^2) F_j(x_2, \mu_2^2) F(b)$
- $\sigma_{\text{eff}} = \left[\int d^2b (F(b))^2 \right]^{-1}$, $F(b)$ - energy and process independent



phenomenology: $\sigma_{\text{eff}} \Rightarrow$ nonperturbative quantity with a dimension of cross section, connected with transverse size of overlapping protons

$$\sigma_{\text{eff}} \approx 15 \text{ mb} \quad (p_{\perp}\text{-independent})$$

a detailed analysis of σ_{eff} :

Seymour, Siódmok, JHEP 10, 113 (2013)



Exact LO calculation of SPS $c\bar{c}c\bar{c}$ contribution

- Till recently only **approximate** (high-energy approx.) SPS contribution to $gg \rightarrow c\bar{c}c\bar{c}$
- Recently **full calculation** of leading-order $2 \rightarrow 4$ diagrams for SPS $gg \rightarrow c\bar{c}c\bar{c}$ and $q\bar{q} \rightarrow c\bar{c}c\bar{c}$ (small)
- **Automatic calculation** with exact LO matrix elements and full phase space integration (**van Hameren code**, similar to HELAC)
- Generation of **unweighted events** and building quark/antiquark distributions
- Hadronization with fragmentation functions
- **No K-factor** (relatively small for $b\bar{b}b\bar{b}$)

van Hameren, Maciuła, Szczurek, Phys. Rev. **D89** (2014) 054907.



SPS cross section for $c\bar{c}c\bar{c}$

$$d\hat{\sigma} = \frac{1}{2\hat{s}} \overline{|\mathcal{M}_{gg \rightarrow c\bar{c}c\bar{c}}|^2} d^4PS. \quad (1)$$

where

$$d^4PS = \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{d^3p_4}{2E_4(2\pi)^3} (2\pi)^4 \delta^4(p_1 + p_2 + p_3 + p_4). \quad (2)$$

Above p_1, p_2, p_3, p_4 are four-momenta of final c, \bar{c}, c, \bar{c} quarks and antiquarks, respectively.

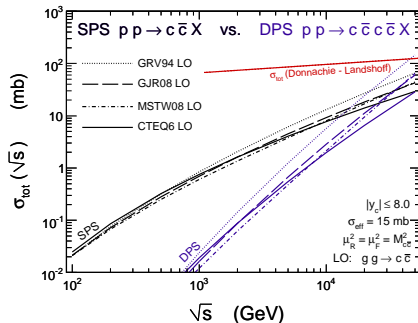
Neglecting small electroweak corrections, the hadronic cross section is

$$\begin{aligned} d\sigma &= \int dx_1 dx_2 (g(x_1, \mu_F^2) g(x_2, \mu_F^2) d\sigma_{gg \rightarrow c\bar{c}c\bar{c}} \\ &+ \sum_f q_f(x_1, \mu_F^2) \bar{q}_f(x_2, \mu_F^2) d\sigma_{q\bar{q} \rightarrow c\bar{c}c\bar{c}} \\ &+ \sum_f \bar{q}_f(x_1, \mu_F^2) q_f(x_2, \mu_F^2) d\sigma_{\bar{q}q \rightarrow c\bar{c}c\bar{c}}). \end{aligned}$$

In the calculation below we include $u\bar{u}, \bar{u}u, d\bar{d}, \bar{d}d, s\bar{s}, \bar{s}s$ annihilation terms.



Energy dependence of $c\bar{c}c\bar{c}$ production



Luszczak, Maciula, Szczurek, Phys. Rev. **C86** (2012) 014905

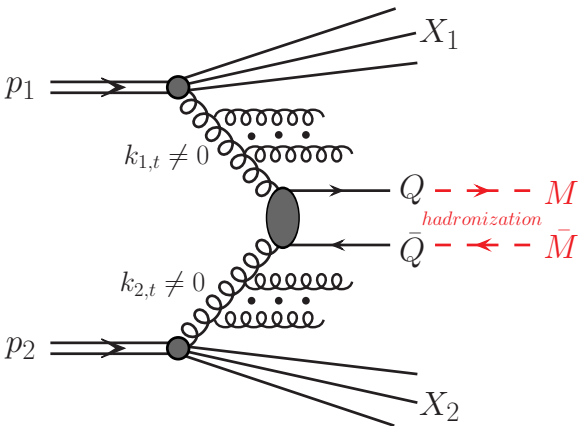
spectacular result:

Already at the LHC production of two pairs as probable as production of one pair.



DPS in k_T -factorization

each step:



DPS in k_T -factorization

Generalize the [LO collinear](#) approach to k_T -factorization approach.

More complicated (**more kinematical variables**) as momenta of outgoing partons are less correlated

We need information about each quark and antiquark

$$\frac{1}{2\sigma_{\text{eff}}} \cdot \frac{\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}}}{d\sigma} \cdot \frac{\frac{d\sigma}{dy_3 dy_4 d^2 p_{3,t} d^2 p_{4,t}}}{d\sigma} = \quad (4)$$



DPS in k_T -factorization

Each individual scattering in the k_T -factorization approach

$$\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}} = \frac{1}{16\pi^2 \hat{s}^2} \int |\overline{\mathcal{M}}_{\text{off}}|^2 \delta(\vec{k}_{1t} + \vec{k}_{2t} - \vec{p}_{1t} - \vec{p}_{2t}) \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2) \frac{d^2 k_{1t}}{\pi} \frac{d^2 k_{2t}}{\pi}$$

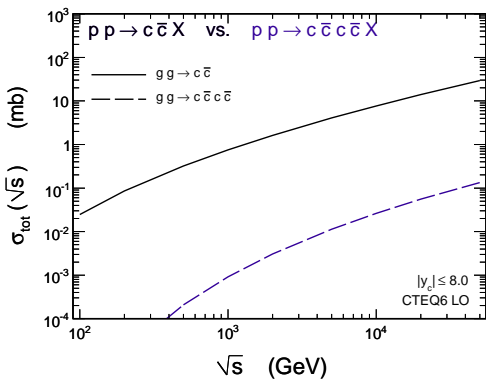
$$\frac{d\sigma}{dy_3 dy_4 d^2 p_{3,t} d^2 p_{4,t}} = \frac{1}{16\pi^2 \hat{s}^2} \int |\overline{\mathcal{M}}_{\text{off}}|^2 \delta(\vec{k}_{3t} + \vec{k}_{4t} - \vec{p}_{3t} - \vec{p}_{4t}) \mathcal{F}(x_3, k_{3t}^2, \mu^2) \mathcal{F}(x_4, k_{4t}^2, \mu^2) \frac{d^2 k_{3t}}{\pi} \frac{d^2 k_{4t}}{\pi}$$

Effectively **16 dimensions**, Monte Carlo method

Maciula-Szczurek, hep-ph-1301.4469, Phys. Rev. **D87** (2013) 074039.



Single parton scattering $2 \rightarrow 4$ process?

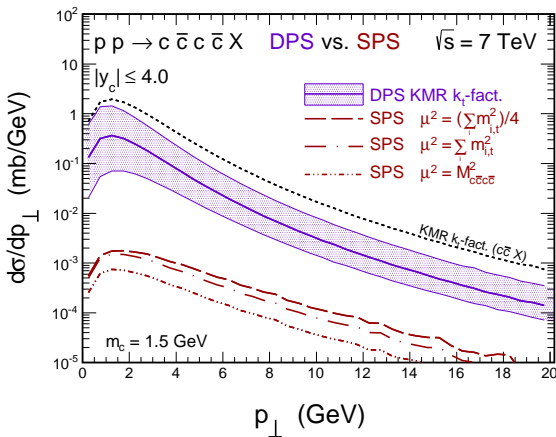


Only about 1 % at high energies

Much smaller than DPS production of $c\bar{c}c\bar{c}$



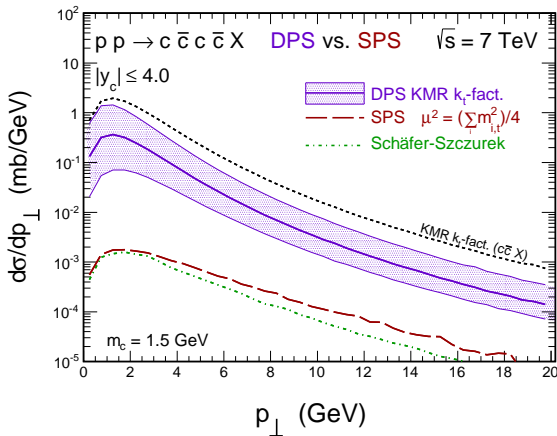
Exact collinear SPS, quark level



dependence on renormalization and factorization scale of SPS



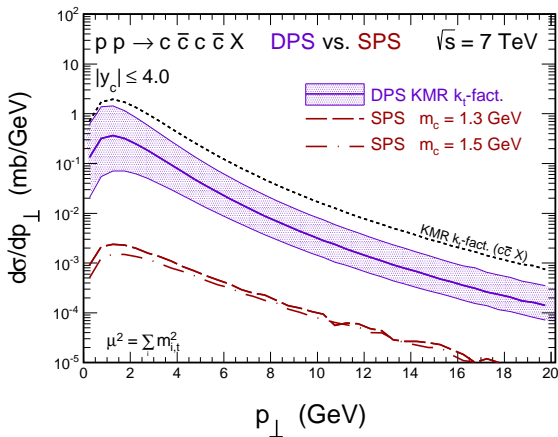
Exact collinear SPS, quark level



similar shape of SPS and DPS



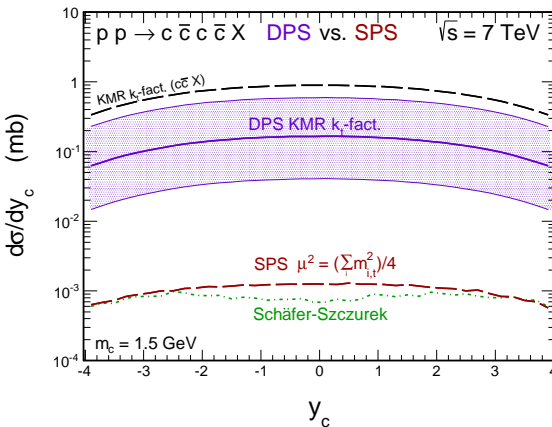
Exact collinear SPS, quark level



weak dependence on the quark mass for SPS



Exact collinear SPS, quark level

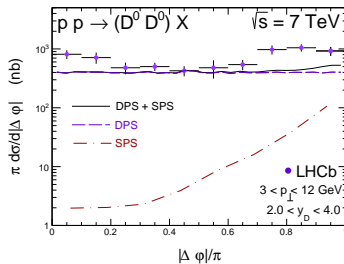
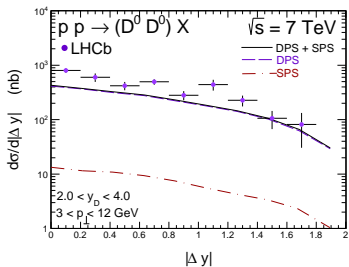


Agreement of high-energy approx. and exact at large quark rapidities



Comparison to LHCb data

After hadronization

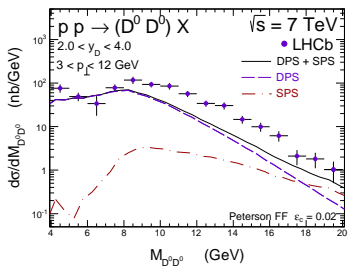


single-parton $c\bar{c}c\bar{c}$ production:

van Hameren, Maciula, Szczurek, Phys. Rev. **D89** (2014) 094019; Schafer, Szczurek, Phys. Rev. **D85** (2012) 094029.



Comparison to LHCb data



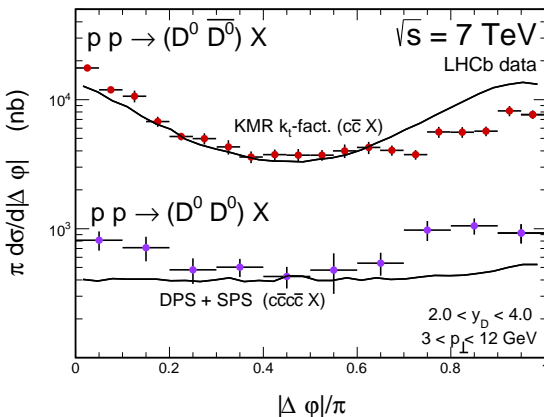
single-parton $c\bar{c}c\bar{c}$ production:

van Hameren, Maciuła, Szczurek, Phys. Rev. **D89** (2014) 094019.

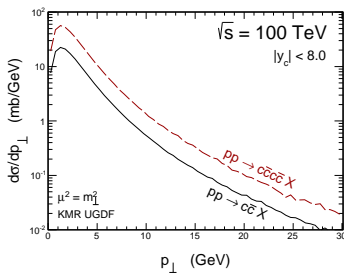
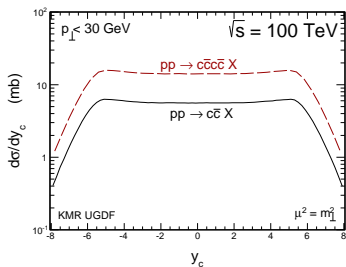


Exact collinear SPS, D meson level

colorblue $D^0 D^0$ versus $D^0 \bar{D}^0$ correlations



Double charm production at FCC

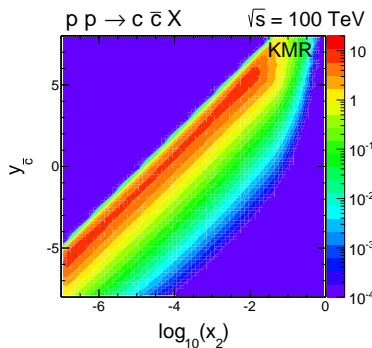
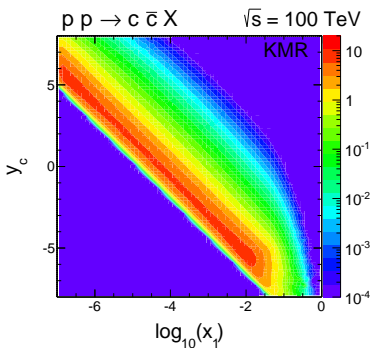


within k_T -factorization approach.

gluon distributions extrapolated to smaller x -values



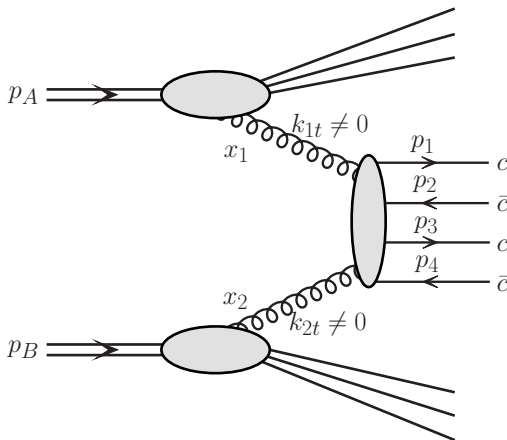
Charm production at FCC



very small x values available !



SPS in k_t -factorization approach



include gluon transverse momenta

A. van Hameren, R. Maciula and A. Szczurek, arXiv:1504.06490



Basic formulae

Within the k_T -factorization approach the SPS cross section for $pp \rightarrow c\bar{c}c\bar{c}X$ reaction can be written as

$$d\sigma_{pp \rightarrow c\bar{c}c\bar{c}} = \int dx_1 \frac{d^2 k_{1t}}{\pi} dx_2 \frac{d^2 k_{2t}}{\pi} \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2) d\hat{\sigma}_{gg \rightarrow c\bar{c}c\bar{c}} \quad (5)$$

The elementary cross section in Eq. (5) can be written somewhat formally as:

$$d\hat{\sigma} = \frac{d^3 p_1}{2E_1(2\pi)^3} \frac{d^3 p_2}{2E_2(2\pi)^3} \frac{d^3 p_3}{2E_3(2\pi)^3} \frac{d^3 p_4}{2E_4(2\pi)^3} (2\pi)^4 \delta^4(p_1 + p_2 + p_3 + p_4 - k_1 - k_2) \times \frac{1}{\text{flux}} |\overline{\mathcal{M}_{g^*g^* \rightarrow c\bar{c}c\bar{c}}(k_1, k_2)}|^2, \quad (6)$$

where only dependence of the matrix element on four-vectors of gluons k_1 and k_2 is made explicit.



Matrix element squared

Denoting by \mathcal{M}^a the amplitude with the color of one off-shell gluon highlighted explicitly we have

$$\sum_a |\mathcal{M}^a|^2 = \sum_a \left| \sqrt{2} \sum_{i,j} \mathcal{M}_{ij} T_{ij}^a \right|^2 = \sum_{i,j,k,l} \mathcal{M}_{ij} \mathcal{M}_{kl}^* \left(\delta_{ik} \delta_{lj} - \frac{1}{N_C} \delta_{ij} \delta_{kl} \right) = \sum_{i,j} |\mathcal{M}_{ij}|^2 \quad (7)$$

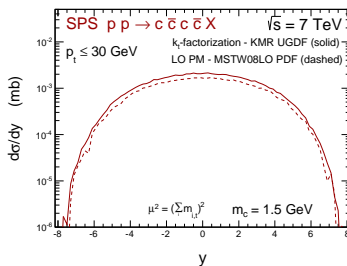
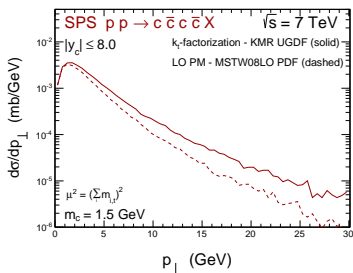
Matrix element squared with **off-shell initial gluons** calculated with an **automated code** of **A. van Hameren**

(Dyson-Schwinger recursion method, JHEP. 01 (2013) 078.)

Monte Carlo generation of events and constructing distributions from the kinematically complete weighted events



First results for k_t -factorization approach



$$\mu_f^2 = \left(\sum_i^4 m_{i,t} \right)^2$$

k_t -factorization and collinear results similar



First results for k_t -factorization approach

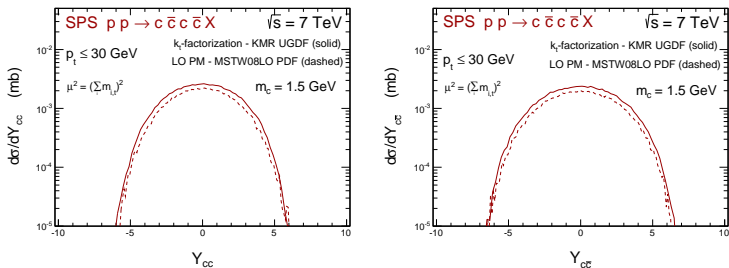


Figure: $Y_{cc} = (y_c + y_{\bar{c}})/2$ (left panel) and $Y_{c\bar{c}} = (y_c + y_{\bar{c}})/2$ (right panel).

$$\mu_f^2 = \left(\sum_i^4 m_{i,t} \right)^2$$

k_t -factorization and collinear results similar



First results for k_t -factorization approach

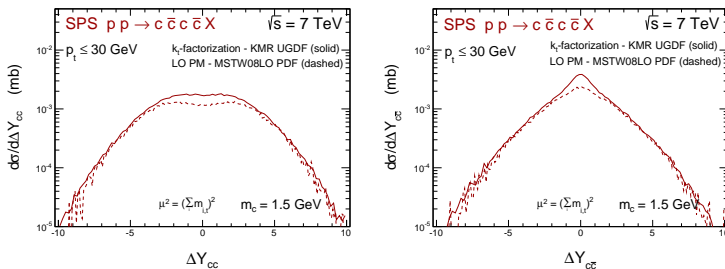


Figure: $\Delta Y_{cc} = y_c - y_{\bar{c}}$ (left panel) and $\Delta Y_{c\bar{c}} = y_c - y_{\bar{c}}$ (right panel).

$$\mu_f^2 = \left(\sum_i^4 m_{i,t} \right)^2$$



First results for k_T -factorization approach

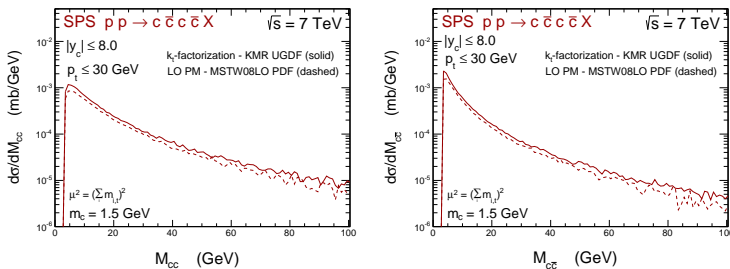


Figure: M_{cc} (left panel) and $M_{c\bar{c}}$ (right panel).

$$\mu_f^2 = \left(\sum_i^4 m_{i,t} \right)^2$$



First results for k_T -factorization approach

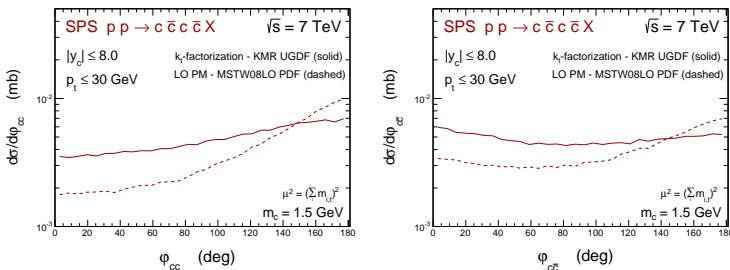


Figure: Azimuthal angle correlations between two c quarks (left panel) and between c and \bar{c} (right panel).

$$\mu_f^2 = \left(\sum_i^4 m_{i,t} \right)^2$$

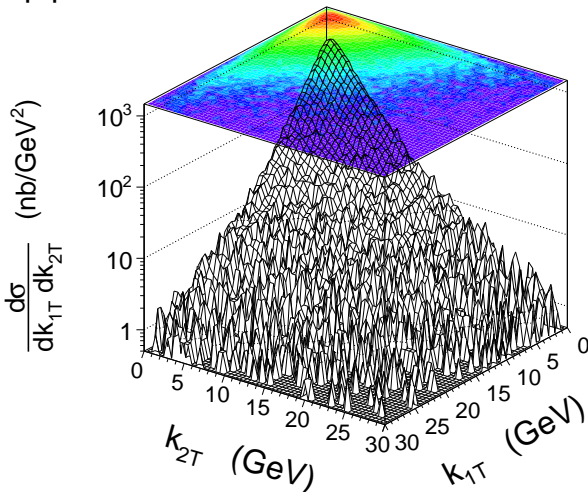
k_T -factorization gives more decorrelation than collinear-factorization



First results for k_t -factorization approach

$$pp \rightarrow c\bar{c}c\bar{c}X$$

$$\sqrt{s} = 7 \text{ TeV}$$



First results for k_T -factorization approach

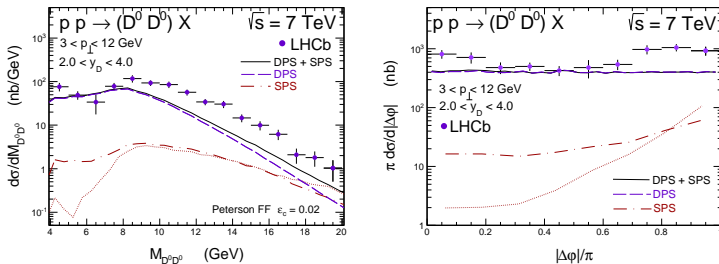
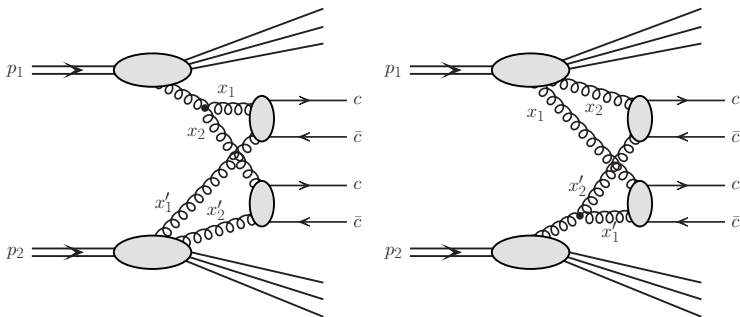


Figure: Distributions in $D^0 D^0$ invariant mass (left) and in azimuthal angle between both D^0 's (right) within the LHCb acceptance. The DPS contribution (dashed line) and the SPS contribution within the k_T -factorization approach (dashed-dotted line). The collinear SPS result from our previous studies (dotted line).



Parton splitting mechanism

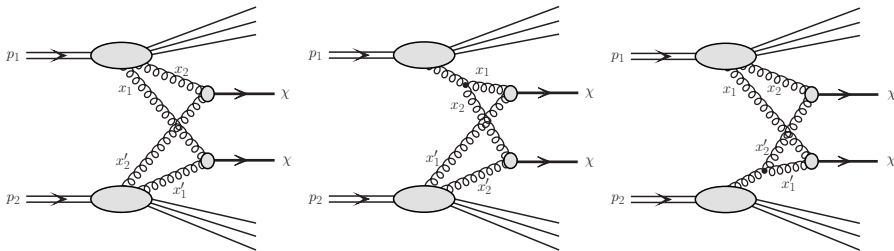
There are perturbative mechanisms not included in **conventional DPS**.



Gaunt, Maciuła, Szczurek, Phys. Rev. **D90** (2014) 054017.



Double quarkonium production



Gaunt, Maciuła, Szczurek, Phys. Rev. **D90** (2014) 054017.



A bit of formalism for parton splitting

Conventional DPS:

$$\sigma(2v2) = \frac{1}{2} \frac{1}{\sigma_{\text{eff},2v2}} \int dy_1 dy_2 d^2 p_{1\perp} dy_3 dy_4 d^2 p_{2\perp} \frac{1}{16\pi\hat{s}^2} \overline{|\mathcal{M}(gg \rightarrow c\bar{c})|^2} x_1 x'_1 x_2 x'_2 \times D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2) D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2)$$

Parton splitting DPS

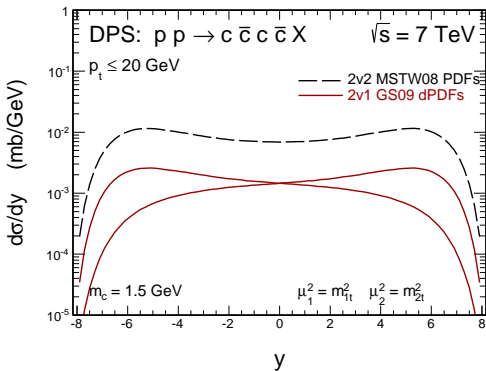
$$\sigma(2v1) = \frac{1}{2} \frac{1}{\sigma_{\text{eff},2v1}} \int dy_1 dy_2 d^2 p_{1\perp} dy_3 dy_4 d^2 p_{2\perp} \frac{1}{16\pi\hat{s}^2} \overline{|\mathcal{M}(gg \rightarrow c\bar{c})|^2} x_1 x'_1 x_2 x'_2 \times \left(\hat{D}^{gg}(x'_1, x'_2, \mu_1^2, \mu_2^2) D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2) + D^{gg}(x'_1, x'_2, \mu_1^2, \mu_2^2) \hat{D}^{gg}(x_1, x_2, \mu_1^2, \mu_2^2) \right)$$

There are two different normalization parameters. They are related in a geometrical picture.

Presence of the two components leads to a dependence of effective parameter on different kinematical variables.



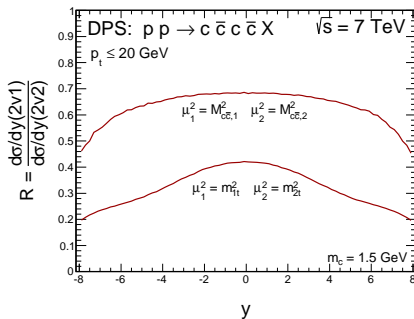
Parton splitting vs conventional DPS



Asymmetric 1v2 and 2v1 contributions



Parton splitting vs conventional DPS

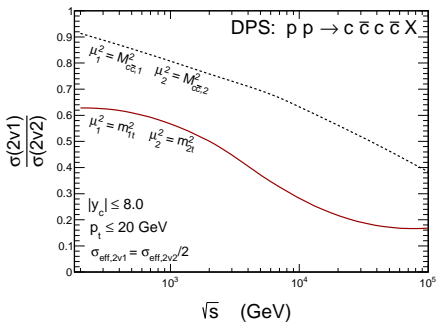


Rapidity and factorization scale dependence

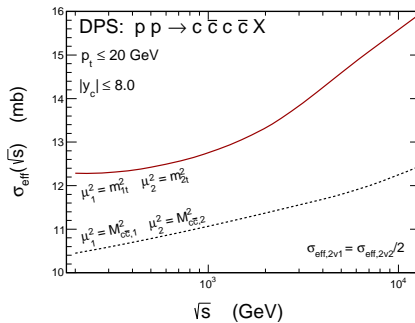
There could be also transverse momentum dependence.



Parton splitting vs conventional DPS



Parton splitting vs conventional DPS



σ_{eff} is no longer a constant



Multiple $c\bar{c}$ production

We consider the following simple **eikonal model** of uncorrelated multiple production of charm.

$$\sigma_{c\bar{c}}^{(k)}(s^{1/2}) = \int d^2b \frac{\left(T_{NN}(b)\sigma_{c\bar{c}}(s^{1/2})\right)^k}{k!} \exp\left(-T_{NN}(b)\sigma_{c\bar{c}}(s^{1/2})\right) \quad (10)$$

The nucleon-nucleon thickness function T_{NN}

$$T_{NN}(b) = \int t_N(\vec{B} - \vec{b}/2) t_N(\vec{B} + \vec{b}/2) d^2B, \quad (11)$$

where $t_N(b_i)$ are partonic profile functions in the nucleon $i = 1, 2$.

We have tested three different **profile functions**:

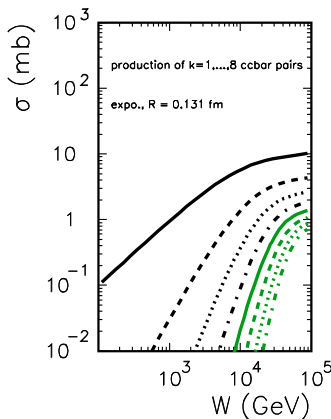
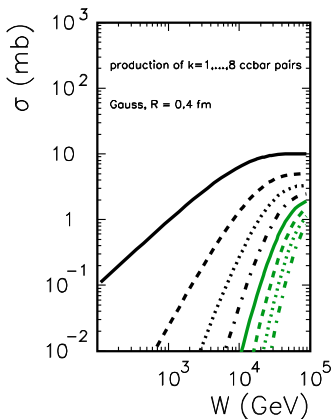
$$t_N(b_i) = \frac{\pi R_G^2}{\exp} \left(-b_i^2/R_G^2\right),$$

$$t_N(b_i) = \frac{1}{4\pi} \mu_e^3 b_i K_1(\mu_e b_i),$$

$$t_N(b_i) = \text{const } \partial(b_i - R_s).$$



Multiple $c\bar{c}$ production

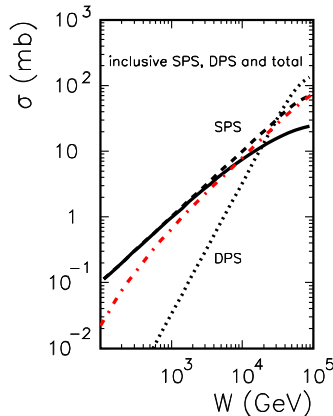
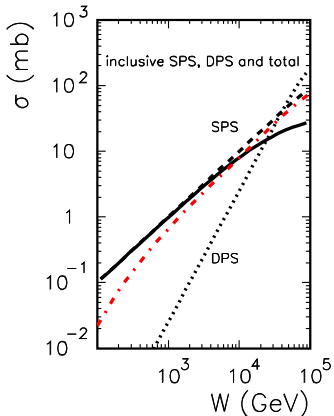


gaussian (left), exponential (right)

Large cross section for multiple charm



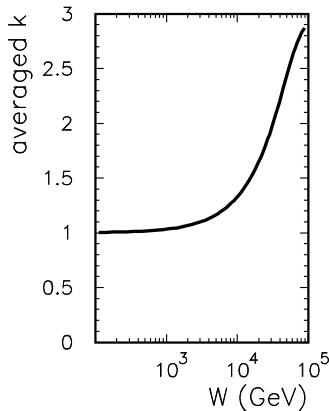
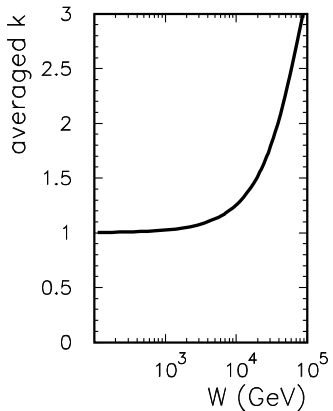
Multiple $c\bar{c}$ production



gaussian (left), exponential (right)



Multiple $c\bar{c}$ production



gaussian (left), exponential (right)



Conclusions

- k_T -factorization provides good description of charm production at RHIC and LHC.
- Surprisingly large cross sections for inclusive $c\bar{c}c\bar{c}$ due to DPS.
- Relatively small cross sections for SPS $c\bar{c}c\bar{c}$.
- **Multiple $c\bar{c}$ pairs** can be produced in p p collisions at the LHC and FCC.
- Look at correlations between **same flavour charmed mesons** such as D^0D^0 .
- Look at correlations between $e^+\mu^+$ or $e^-\mu^-$ from semileptonic decays (ALICE, CMS).
- **Enhancement of the number of $c\bar{c}$ pairs in AA collisions**
 - important for recombination/coalescence
 - further **enhancement of hidden-charm meson production** ($J/\psi, \psi'$) at higher energies.



Conclusions

- The effect of **DPS growing with center-of-mass energy**.
- At LHC and even more at FCC many hard processes with **DPS contamination**.
- We start to better understand the DPS processes.
- DPS's are backgrounds to other processes **but are interesting per se**.
- Let us set a systematic program to study DPS.

