

# Jets at high multiplicity

**Peter Schichtel**



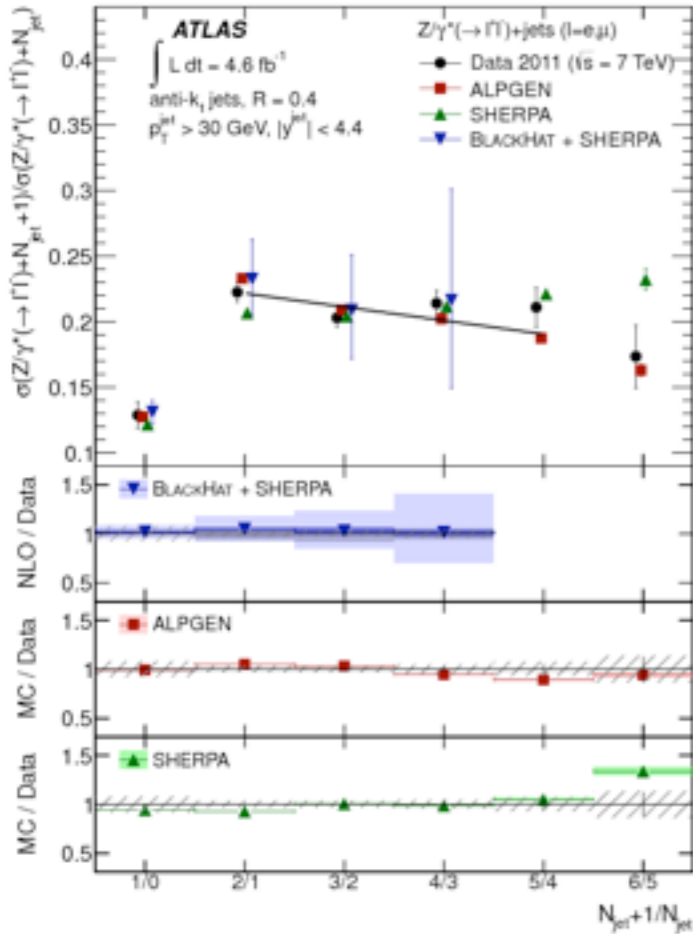
@ Pheno 2015

with: Englert, Gerwick, Plehn, Schumann

# Scaling patterns

## staircase scaling

[Steve Ellis, Kleis, Stirling (1985); Berends (1989)]

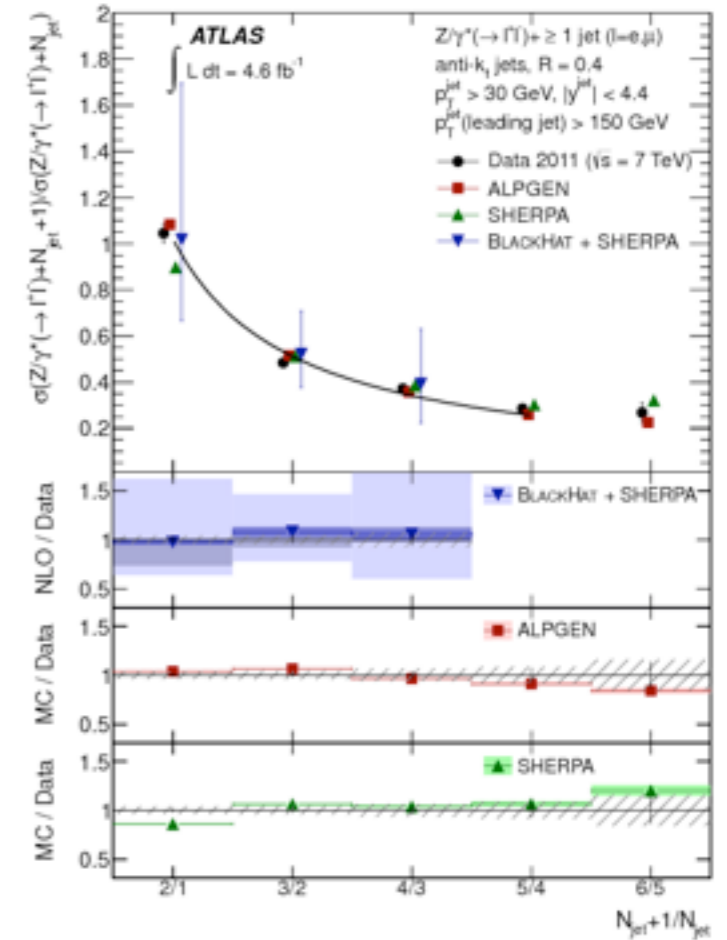


observed at: UAI, Tevatron  
 confirmed at LHC [1304.7098]  
 → staircase small tilt  
 → Poisson flattens out  
 needs high  $p_T$  jet

phase space

## Poisson scaling

[Peskin & Schroeder; Rainwater, Zeppenfeld (1997)]



QED:

resolvable

$n$  independent emissions

$$P(n) = \frac{\bar{n}^n e^{-\bar{n}}}{n!}$$

bosonic phase space

normalization

unresolvable  
resummed

falling ratios

$$R_{\frac{n+1}{n}} = \frac{\sigma_{n+1}}{\sigma_n} = \frac{\bar{n}}{n+1}$$

constant ratios

$$R_{\frac{n+1}{n}} = \frac{\sigma_{n+1}}{\sigma_n} = R_0$$

same for exclusive and inclusive

[Englert, Plehn, PS, Schumann (2011)]

# Bremsstrahlung in QCD

[Konishi et al. (1979); Ellis, Stirling, Webber (1996); Gerwick, Gripaos, Schumann, Webber (2012) ]

**generating functional formalism**

$$\Phi_i(t) = u \exp \left[ \int_{t_0}^t dt' \sum_{jl} \Gamma_{i \rightarrow jl} \left( \frac{\Phi_j(t') \Phi_l(t')}{\Phi_i(t')} - 1 \right) \right]$$

democratic limit

$t \rightarrow t_0$   
high multiplicities

$$\Phi_g \sim \frac{1}{1 + \frac{1-u}{u\Delta_g}} \mathcal{R}(u)$$

→ staircase scaling

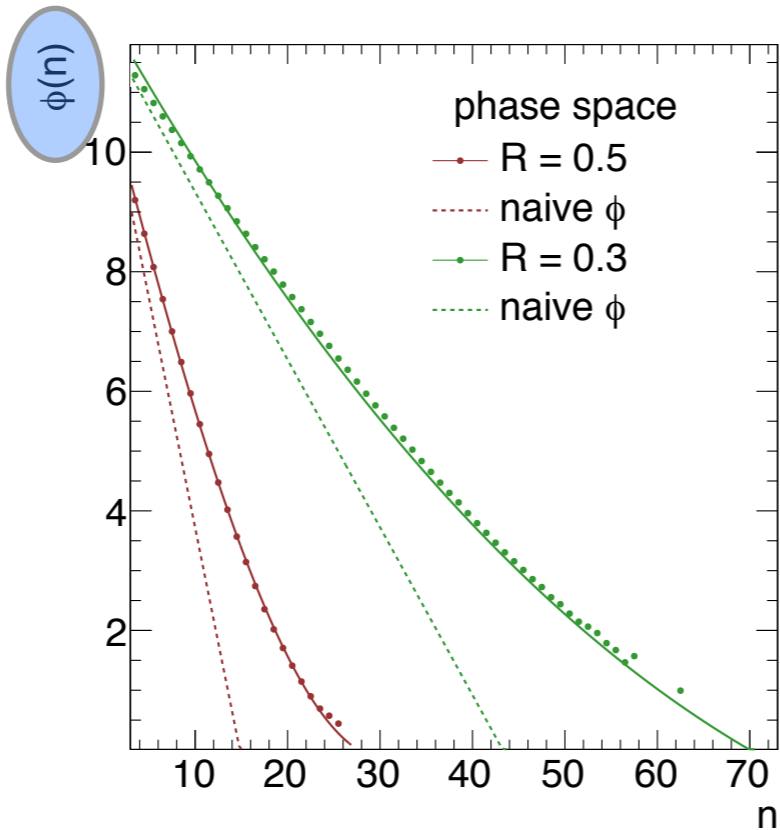
large log limit:

$t \gg t_0$   
low multiplicities

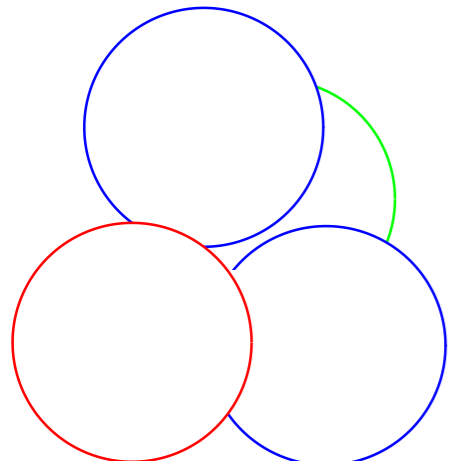
$$\Phi_i(t) = \frac{u\Delta_i(t)}{\Delta_i(t)u}$$

→ Poisson scaling

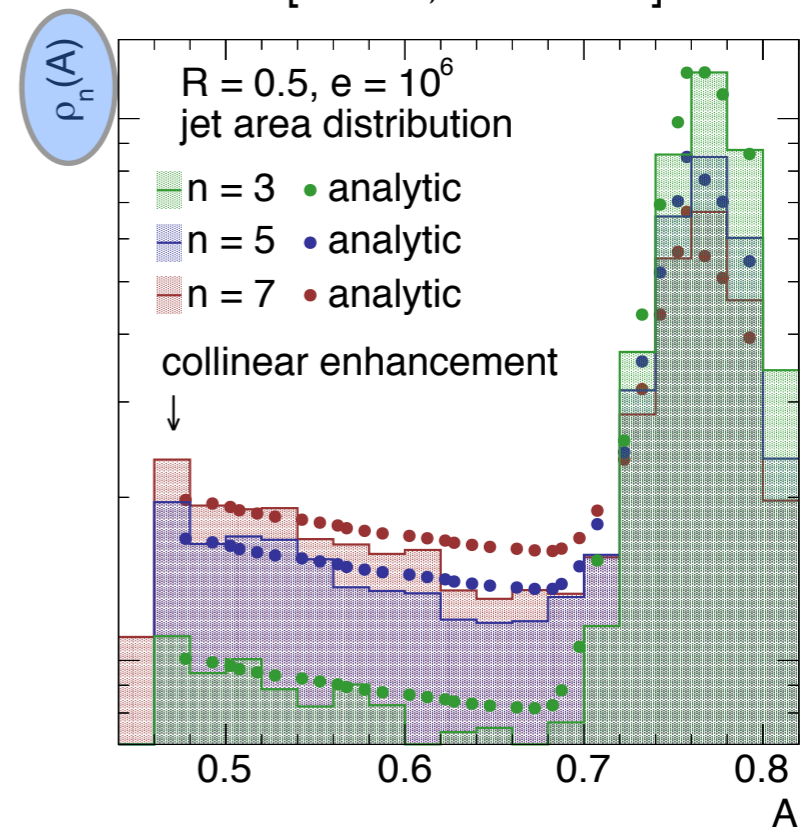
**non-trivial geometry**



anti- $k_T$  algorithm



[Gerwick, PS: 1412.1806]



overlay effects → area depletion  
 collinear & circular → exact area model  
 study very high multiplicities in MC  
 iteratively good for moderate jet numbers

# Summary

[Gerwick, PS: 1412.1806]

$$R_{\frac{n+1}{n}} = \left( R_0 \left[ 1 + \frac{1}{B + (n+1)} \right] + \frac{dR_0}{dn} (n+1) \right) \times \frac{\phi(n+1)}{\phi(n)}$$

small & vanishing as  $R \rightarrow 0$

jet spectra follow simple scaling patterns

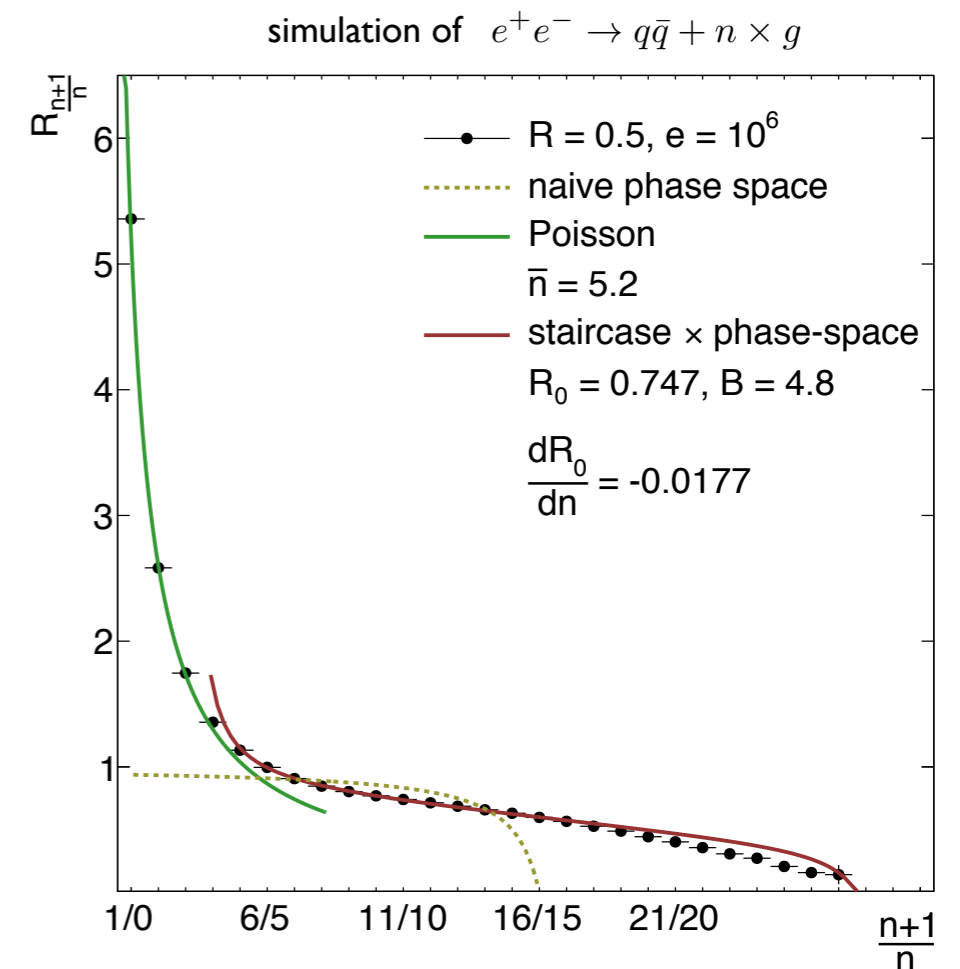
staircase scaling is a firm QCD prediction (& observed)

@ LHC: low multiplicities due to PDF effects

three sources for deviations

- breaking terms ✓
- phase space ✓
- finite jet radius ✗

QCD high multiplicity predictions possible [difficult with NLO]



Experiment: [Ellis,Kleis,Stirling(1985), Alioli et al, JHEP (2011) 095, Aad et al. Phys. Rev. D **85** 092002 (2012) and 1304.7098]

Generating functional: [Konishi et al. (1979); Ellis, Stirling, Webber (1996); Gerwick, Gripaos, Schumann, Webber (2012)]

Scaling patterns: [Englert, Plehn, PS, Schumann PRD 83 (2011) and JHEP 030 (2012), Gerwick, Plehn, Schumann PRL 108 (2012), Gerwick, Plehn, PS, Schumann JHEP 162 (2012), Gerwick, PS arxiv: 1412.1806]