

Matching NNLO calculations with parton showers in GENEVA



Simone Alioli

PSR 2015

Krakow - 27 May 2015

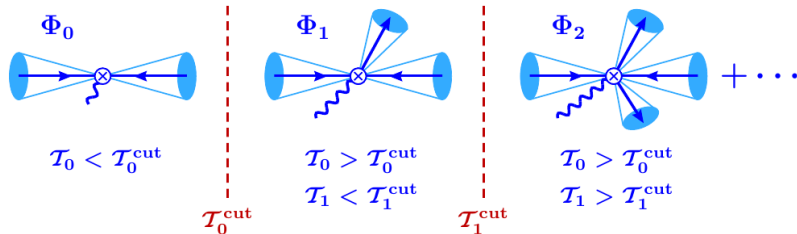
SA, C. Bauer, C. Berggren, A. Hornig, F. Tackmann, C. Vermilion, J. Walsh, S. Zuberi JHEP09(2013)120

SA, C. Bauer, C. Berggren, F. Tackmann, J. Walsh, S. Zuberi JHEP06(2014)089

SA, C. Bauer, F. Tackmann, J. Walsh (in preparation)

IR-safe event definition beyond LO

- ▶ Only generate “physical events”, i.e. events to which one can assign an IR-finite cross section $d\sigma^{\text{MC}}$.
- ▶ Introduce a resolution parameter \mathcal{T}_N , $\mathcal{T}_N \rightarrow 0$ in the IR region. Emissions below $\mathcal{T}_N^{\text{cut}}$ are unresolved (i.e. integrated over) and the kinematic considered is the one of the event before the emission.
- ▶ An M -parton event is thus really defined as an N -jet event, $N \leq M$, fully differential in Φ_N (standard “jet-algo” not needed)
 - Price to pay: power corrections in $\mathcal{T}_N^{\text{cut}}$ due to PS projection.
 - Advantage: vanish for IR-safe observables as $\mathcal{T}_N^{\text{cut}} \rightarrow 0$
- ▶ Iterating the procedure, the phase space is sliced into jet-bins



IR-safe event definition beyond LO

- ▶ Only generate “physical events”, i.e. events to which one can assign an IR-finite cross section $d\sigma^{\text{MC}}$.
- ▶ Introduce a resolution parameter \mathcal{T}_N , $\mathcal{T}_N \rightarrow 0$ in the IR region. Emissions below $\mathcal{T}_N^{\text{cut}}$ are unresolved (i.e. integrated over) and the kinematic considered is the one of the event before the emission.
- ▶ An M -parton event is thus really defined as an N -jet event, $N \leq M$, fully differential in Φ_N (standard “jet-algo” not needed)
 - Price to pay: power corrections in $\mathcal{T}_N^{\text{cut}}$ due to PS projection.
 - Advantage: vanish for IR-safe observables as $\mathcal{T}_N^{\text{cut}} \rightarrow 0$
- ▶ Iterating the procedure, the phase space is sliced into jet-bins

Inclusive N -jet bin

$$\frac{d\sigma_{\geq N}^{\text{MC}}}{d\Phi_N}$$

$\mathcal{T}_0^{\text{cut}}$

$\mathcal{L}_1 < \mathcal{L}_1$

$\mathcal{T}_1^{\text{cut}}$

$\mathcal{L}_1 > \mathcal{L}_1$



IR-safe event definition beyond LO

- ▶ Only generate “physical events”, i.e. events to which one can assign an IR-finite cross section $d\sigma^{\text{MC}}$.
- ▶ Introduce a resolution parameter \mathcal{T}_N , $\mathcal{T}_N \rightarrow 0$ in the IR region. Emissions below $\mathcal{T}_N^{\text{cut}}$ are unresolved (i.e. **integrated over**) and the kinematic considered is the one of the event before the emission.
- ▶ An M -parton event is thus really defined as an N -jet event, $N \leq M$, fully differential in Φ_N (**standard “jet-algo” not needed**)
 - **Price to pay:** power corrections in $\mathcal{T}_N^{\text{cut}}$ due to PS projection.
 - **Advantage:** vanish for IR-safe observables as $\mathcal{T}_N^{\text{cut}} \rightarrow 0$
- ▶ Iterating the procedure, **the phase space is sliced into jet-bins**

Exclusive N -jet bin

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})$$

Inclusive $(N + 1)$ -jet bin

$$\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$$

$\mathcal{T}_0^{\text{cut}}$

$\mathcal{T}_1 < \mathcal{T}_1^{\text{cut}}$

$\mathcal{T}_1^{\text{cut}}$

$\mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}$



IR-safe event definition beyond LO

- ▶ Only generate “physical events”, i.e. events to which one can assign an IR-finite cross section $d\sigma^{\text{MC}}$.
- ▶ Introduce a resolution parameter \mathcal{T}_N , $\mathcal{T}_N \rightarrow 0$ in the IR region. Emissions below $\mathcal{T}_N^{\text{cut}}$ are unresolved (i.e. integrated over) and the kinematic considered is the one of the event before the emission.
- ▶ An M -parton event is thus really defined as an N -jet event, $N \leq M$, fully differential in Φ_N (standard “jet-algo” not needed)
 - Price to pay: power corrections in $\mathcal{T}_N^{\text{cut}}$ due to PS projection.
 - Advantage: vanish for IR-safe observables as $\mathcal{T}_N^{\text{cut}} \rightarrow 0$
- ▶ Iterating the procedure, the phase space is sliced into jet-bins

Exclusive N -jet bin

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})$$

Excl. $(N+1)$ -jet

$$\frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}})$$

Inclusive $(N+2)$ -jet bin

$$\frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

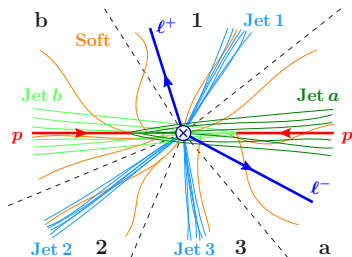
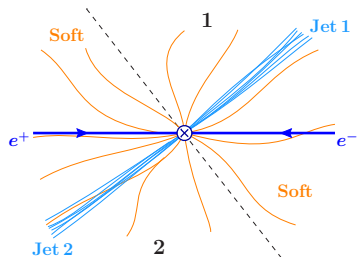
$\mathcal{T}_0^{\text{cut}}$

$\mathcal{T}_1^{\text{cut}}$

N-Jettiness as jet-resolution variable

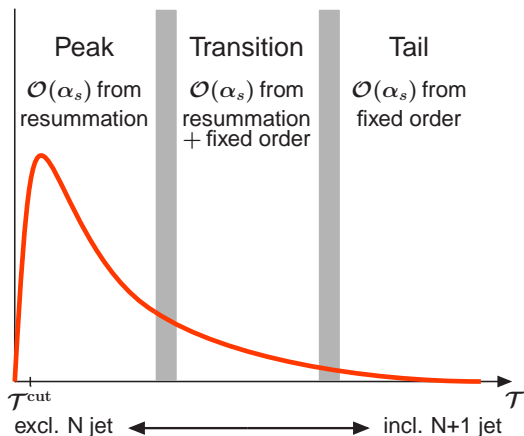
- ▶ Use N -jettiness as resolution parameter. Global physical observable with straightforward definitions for hadronic colliders, in terms of beams $q_{a,b}$ and jet-directions q_j

$$\mathcal{T}_N = \frac{2}{Q} \sum_k \min\{q_1 \cdot p_k, \dots, q_N \cdot p_k\} \Rightarrow \mathcal{T}_N = \frac{2}{Q} \sum_k \min\{q_a \cdot p_k, q_b \cdot p_k, q_1 \cdot p_k, \dots, q_N \cdot p_k\}$$



- ▶ N -jettiness has good factorization properties, IR safe and resumable at all orders. Resummation known at NNLL for any N in SCET [Stewart et al. 1004.2489, 1102.4344]
- ▶ $\mathcal{T}_N \rightarrow 0$ for N pencil-like jets, $\mathcal{T}_N \gg 0$ spherical limit.
- ▶ $\mathcal{T}_N < \mathcal{T}_N^{\text{cut}}$ acts as jet-veto, e.g. CJV $\mathcal{T}_0 = \frac{2}{Q} \sum_k \min\{q_a \cdot p_k, q_b \cdot p_k\} < \mathcal{T}_0^{\text{cut}}$

Perturbative accuracy



- ▶ Fixed NLO_{N+1} (MCFM, BH, ...) is insufficient outside FO region
- ▶ Resummation OK in peak region, fails to describe FO region
- ▶ Lowest accuracy across the whole spectrum in MEPS: CKKW, MLM
- ▶ Standard NLO+PS (POWHEG, MC@NLO) improve total rate, not spectrum

(Notation: $\tau = \mathcal{T}/Q$, $L = \ln \tau$, $L_{\text{cut}} = \ln \tau^{\text{cut}}$)

$$\begin{aligned}
 \frac{\sigma(\tau^{\text{cut}})}{\sigma_B} &= \begin{array}{cccc} \text{LL}_\sigma & \text{NLL}_\sigma & \text{NLL}'_\sigma & \text{NNLL}_\sigma \end{array} && \text{LO}_N \\
 &+ \alpha_s \left[\frac{c_{11}}{2} L_{\text{cut}}^2 + c_{10} L_{\text{cut}} + c_{1,-1} + F_1(\tau^{\text{cut}}) \right] && \text{NLO}_N \\
 &+ \alpha_s^2 \left[\begin{array}{cccc} \vdots & \vdots & \vdots & \vdots \end{array} \right] \\
 \\
 \frac{1}{\sigma_B} \frac{d\sigma}{d\tau} &= \alpha_s/\tau \left[c_{11} L + c_{10} + \tau f_1(\tau) \right] && \text{LO}_{N+1} \\
 &+ \alpha_s^2/\tau \left[c_{23} L^3 + c_{22} L^2 + c_{21} L + c_{20} + \tau f_2(\tau) \right] && \text{NLO}_{N+1} \\
 &+ \alpha_s^3/\tau \left[\begin{array}{cccc} \vdots & \vdots & \vdots & \vdots \end{array} \right]
 \end{aligned}$$

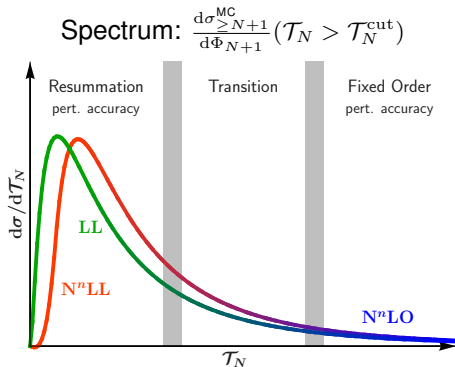
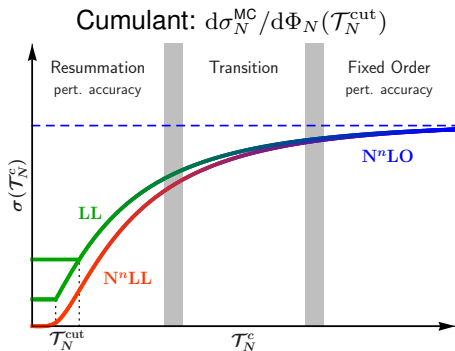
- ▶ Lowest pert. accuracy everywhere requires $\text{NLL}_\tau + \text{LO}_{N+1}$
 - NLL because $\alpha_s(\alpha_s^n L^{2n}) \approx \alpha_s$ in the peak.
- ▶ Next-to-Lowest pert. accuracy everywhere requires $\text{NNLL}_\tau + \text{NLO}_{N+1}$

Relation between cumulant and spectrum

- ▶ Consistency between $d\sigma_N^{\text{MC}}, d\sigma_{\geq N+1}^{\text{MC}}$ is required to push $\mathcal{T}_N^{\text{cut}}$ dependence to high-enough order to ensure spectrum is total derivative of the cumulant

$$\frac{d}{d\mathcal{T}_N^{\text{cut}}} \left[\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) \right]_{\mathcal{T}_N^{\text{cut}}=\mathcal{T}_N} = \int \frac{d\Phi_{N+1}}{d\Phi_N} \delta[\mathcal{T}_N - \mathcal{T}_N(\Phi_{N+1})] \frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$$

- ▶ If this is not satisfied, claimed accuracy might be spoiled by log of $\mathcal{T}_N^{\text{cut}}$.



- ▶ Introduce an unphysical infrared regulator \mathcal{T}^{cut} and separate inclusive and exclusive regions: \mathcal{T}^{cut} dependence drops out to the order we are working.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$



- ▶ Introduce an unphysical infrared regulator \mathcal{T}^{cut} and separate inclusive and exclusive regions: \mathcal{T}^{cut} dependence drops out to the order we are working.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$

- ▶ Cumulant: \mathcal{T} integral over exclusive N -jets bin up to \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) = \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \left[\frac{d\sigma^{\text{FO}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) - \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) \right]_{\text{FO}}$$



- ▶ Introduce an unphysical infrared regulator \mathcal{T}^{cut} and separate inclusive and exclusive regions: \mathcal{T}^{cut} dependence drops out to the order we are working.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$

- ▶ Cumulant: \mathcal{T} integral over exclusive N -jets bin up to \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) = \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \left[\frac{d\sigma^{\text{FO}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) - \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) \right]_{\text{FO}}$$

- ▶ Spectrum: \mathcal{T} distribution of inclusive $N + 1$ -jets sample above \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) = \frac{d\sigma^{\text{FO}}}{d\Phi_{N+1}}(\mathcal{T}) \left[\frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} / \frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} \right]_{\text{FO}}$$



- ▶ Introduce an unphysical infrared regulator \mathcal{T}^{cut} and separate inclusive and exclusive regions: \mathcal{T}^{cut} dependence drops out to the order we are working.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$

- ▶ Cumulant: \mathcal{T} integral over exclusive N -jets bin up to \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) = \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \left[\frac{d\sigma^{\text{FO}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) - \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) \right]_{\text{FO}}$$

- ▶ Spectrum: \mathcal{T} distribution of inclusive $N + 1$ -jets sample above \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) = \frac{d\sigma^{\text{FO}}}{d\Phi_{N+1}}(\mathcal{T}) \left[\frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} / \frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} \right]_{\text{FO}}$$

- ▶ Correctly reproduces the expected limits for $\mathcal{T} \rightarrow 0$ and $\mathcal{T} \sim Q$.



- ▶ Introduce an unphysical infrared regulator \mathcal{T}^{cut} and separate inclusive and exclusive regions: \mathcal{T}^{cut} dependence drops out to the order we are working.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$

- ▶ Cumulant: \mathcal{T} integral over exclusive N -jets bin up to \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) = \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \left[\frac{d\sigma^{\text{FO}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) - \frac{d\sigma^{\text{resum}}}{d\Phi_N}(\mathcal{T}^{\text{cut}}) \right]_{\text{FO}}$$

- ▶ Spectrum: \mathcal{T} distribution of inclusive $N + 1$ -jets sample above \mathcal{T}^{cut}

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) = \frac{d\sigma^{\text{FO}}}{d\Phi_{N+1}}(\mathcal{T}) \left[\frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} \Big/ \frac{d\sigma^{\text{resum}}}{d\Phi_N d\mathcal{T}} \Big|_{\text{FO}} \right]$$

- ▶ Correctly reproduces the expected limits for $\mathcal{T} \rightarrow 0$ and $\mathcal{T} \sim Q$.
- ▶ Additive approach in spectrum better suited for Monte Carlo programs.



Additive matching

- ▶ Theoretically, both the multiplicative and additive approach are valid, the difference being **higher order terms** present in the multiplicative approach.

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) = \frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} \left[\frac{d\sigma^{NLO1}}{d\Phi_{N+1}} / \frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} \Big|_{NLO1} \right]$$

$$\frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) = \left[\frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} - \frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} \Big|_{NLO1} \right] + \frac{d\sigma^{NLO1}}{d\Phi_{N+1}}$$

- ▶ However, one must be careful these higher order terms do not spoil the accuracy after integration of the spectrum against the cumulant.

$$\sigma_{\geq N} = \int d\Phi_N \frac{d\sigma}{d\Phi_N}(\mathcal{T}^{\text{cut}}) + \int d\Phi_{N+1} \frac{d\sigma}{d\Phi_{N+1}}(\mathcal{T}) \theta(\mathcal{T} > \mathcal{T}^{\text{cut}})$$

Example: $\alpha_S \mathcal{T}_0^{\text{cut}} \log(\mathcal{T}_0^{\text{cut}}) * \alpha_S^2 \log(\mathcal{T}_0^{\text{cut}})^4 \approx \alpha_S \mathcal{T}_0^{\text{cut}} \log(\mathcal{T}_0^{\text{cut}}) * 1$

- ▶ Additive approach requires instead resummed and resummed expanded to be made more differential.

$$\frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} \implies \frac{d\sigma^{NNLL'}}{d\Phi_{N+1}} \equiv \frac{d\sigma^{NNLL'}}{d\Phi_N d\mathcal{T}} P(z, \varphi)$$

- ▶ Using splitting-function $P(z, \varphi)$ that integrates to 1 for each \mathcal{T} , automatically preserving \mathcal{T} distribution at given log accuracy .

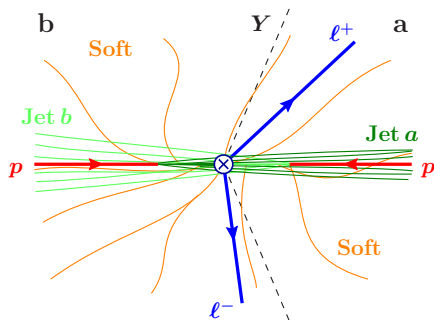


Hadronic collisions: $pp \rightarrow (Z \rightarrow \ell^+ \ell^-) + \text{jets}$

- ▶ To extend GENEVA approach to Drell-Yan we need :
 - A factorizable and resumable resolution parameter: Beam Thrust $\mathcal{T}_0 = \sum_i p_{T,i} e^{-|\eta_i - y_V|}$. Resummation known to NNLL

$$\frac{d\sigma^s}{dx_a dx_b d\mathcal{T}_B} = \sigma_B \cdot H(\mu_H) \otimes U_H(\mu_H, \mu) \cdot B(x_a, \mu_{B_a}) \otimes U_B(\mu_{B_a}, \mu) \\ \otimes B(x_b, \mu_{B_b}) \otimes U_B(\mu_{B_b}, \mu) \otimes S(\mathcal{T}_B, \mu_S) \otimes U_S(\mu_S, \mu)$$

- We use NNLL **Soft S**, **Beam B** and Hard **H** functions. **Evolution kernels U** are obtained by RGE running at NNLL in SCET.

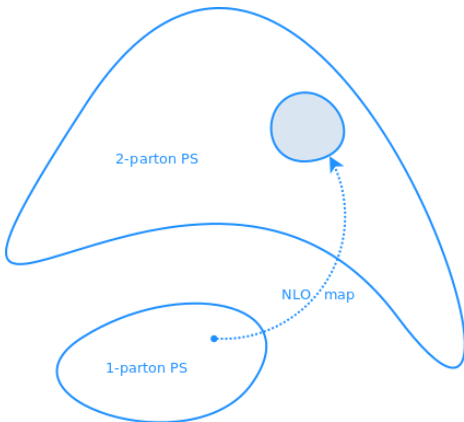


- Beam Functions convolutions with PDFs
- Preserving Beam Thrust and full V kinematics in $V + 1 \rightarrow V + 2$
- Efficient Pythia8 showering without changing \mathcal{T}_0 for ISR
- Proper framework to deal with MPI
- Re-tuning of GENEVA+PYTHIA ...

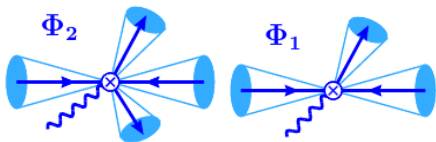
Preserving the \mathcal{T}_0 value in $V + 1 \rightarrow V + 2$ partons splittings

$$\frac{d\sigma^{\text{NLO}}}{d\Phi_1}(\mathcal{T}_0) = [B_1(\Phi_1) + V_1(\Phi_1)] \delta(\mathcal{T}(\Phi_1) - \mathcal{T}_0) + \int \frac{d\Phi_2}{d\Phi_1} B_2(\Phi_2) \delta(\mathcal{T}(\Phi_1(\Phi_2)) - \mathcal{T}_0)$$

- ▶ When calculating NLO_1 we must preserve $d\Phi_1$. Cannot re-use existing calculations.
- ▶ Real emissions must preserve both $d^4q\delta(q^2 - M_{\ell^+\ell^-}^2)$ and $\mathcal{T}_0 \equiv \bar{p}_{T,1} e^{-|y_V - \bar{\eta}_1|} = p_{T,1} e^{-|y_V - \eta_1|} + p_{T,2} e^{-|y_V - \eta_2|}$.



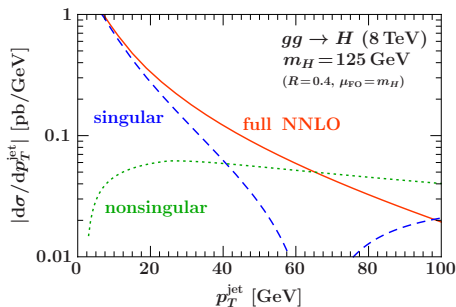
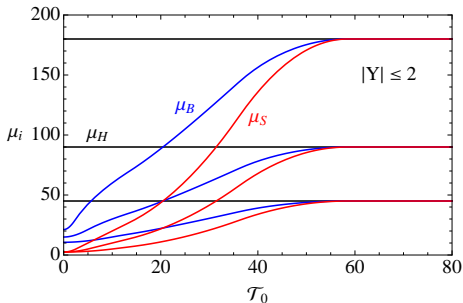
- ▶ Standard FKS or CS don't do this. They are design to preserve other quantities. We had to design our own map



- ▶ This map makes \mathcal{T}_0 -subtraction local in \mathcal{T}_0 . Better numerical convergence. Still averaged over $d\Omega_2$

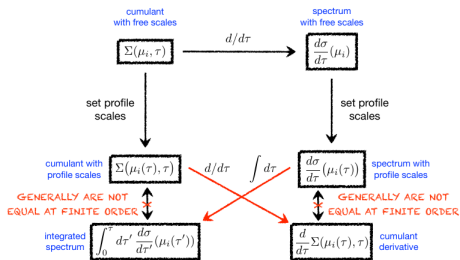
Scale profiles and theoretical uncertainties

- ▶ Theoretical uncertainties in resum. are evaluated by independently varying each μ .
- ▶ Range of variations is tuned to turn off the resummation before the nonsingular dominates (Y_V -dependent) and to respect SCET scaling $\mu_H \gtrsim \mu_B \gtrsim \mu_S$
- ▶ FO unc. are usual $\{2\mu_H, \mu_H/2\}$ variations.
- ▶ Final results added in quadrature.



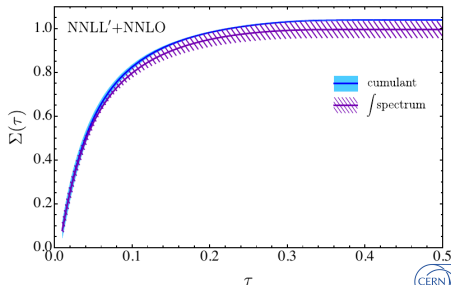
Preserving the total cross-section

- ▶ Different advantages in resumming the cumulant (better cross-section and correlated unc.) or the spectrum (better profiles in trans and tail region and better point-by-point unc.)
- ▶ The two approaches only agree at all order. When the series is truncated results are incompatible.
- ▶ Similar problem in preserving total xsec in matched QCD resummation solved with ad-hoc smoother.
- ▶ We add higher-order term to the spectrum such that integral get closer to cumulant. Add the exact difference to central to restore it completely.
- ▶ Correlations now enforced by hand, automatic method to select profile scale enforcing correlations under investigation.



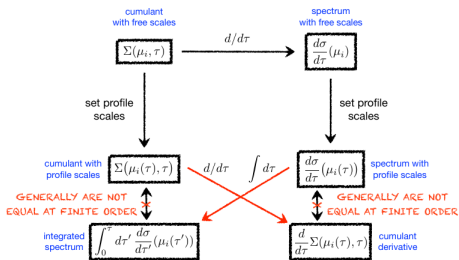
[slide from J. Walsh]

cumulant vs. integrated spectrum

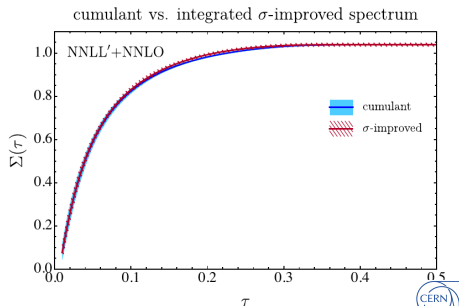


Preserving the total cross-section

- ▶ Different advantages in resumming the cumulant (better cross-section and correlated unc.) or the spectrum (better profiles in trans and tail region and better point-by-point unc.)
- ▶ The two approaches only agree at all order. When the series is truncated results are incompatible.
- ▶ Similar problem in preserving total xsec in matched QCD resummation solved with ad-hoc smoother.
- ▶ We add higher-order term to the spectrum such that integral get closer to cumulant. Add the exact difference to central to restore it completely.
- ▶ Correlations now enforced by hand, automatic method to select profile scale enforcing correlations under investigation.



[slide from J. Walsh]



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC.

[1311.0286]



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{\text{C-S}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{\text{B-C}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^C}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{C-S}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{B-C}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- Singular part of NNLO cross-section, contains all $\log(\mathcal{T}_N^{\text{cut}})$

Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^C}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{C-S}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{B-C}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- Singular part of NNLO cross-section, contains all $\log(\mathcal{T}_N^{\text{cut}})$
- Sudakov factor, provides (at least) LL resummation of $\mathcal{T}_N^{\text{cut}}$

$$\Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}}) = \exp \left\{ - \int \frac{d\Phi_{N+1}}{d\Phi_N} \frac{S_{N+1}(\Phi_{N+1})}{B_N(\hat{\Phi}_N)} \theta[\mathcal{T}_N(\Phi_{N+1}) > \mathcal{T}_N^{\text{cut}}] \right\}$$

Combining fully exclusive NNLO with LL resummation.

- We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- Exclusive N -jet cross section

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^C}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{C-S}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{B-C}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- Singular part of NNLO cross-section, contains all $\log(\mathcal{T}_N^{\text{cut}})$
- Sudakov factor, provides LL resummation of $\mathcal{T}_N^{\text{cut}}$
- Corrects singular $\mathcal{T}_N^{\text{cut}}$ dependence from Sudakov expansion.

Combining fully exclusive NNLO with LL resummation.

- We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- Exclusive N -jet cross section

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{\text{C-S}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{\text{B-C}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- Singular part of NNLO cross-section, contains all $\log(\mathcal{T}_N^{\text{cut}})$
- Sudakov factor, provides LL resummation of $\mathcal{T}_N^{\text{cut}}$
- Corrects singular $\mathcal{T}_N^{\text{cut}}$ dependence from Sudakov expansion.
- **Corrects the finite terms to the exact inclusive cross section.**

Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section (NNLO+LL)

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{\text{C-S}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{\text{B-C}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section (NNLO+LL)

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{\text{C-S}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{\text{B-C}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- ▶ Inclusive $N+1$ -jet cross section (NLO+LL)

$$\begin{aligned} \frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) &= \frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Big|_{\Phi_N = \hat{\Phi}_N} \frac{S_{N+1}(\Phi_{N+1})}{B_N(\hat{\Phi}_N)} \Delta_N(\hat{\Phi}_N; \mathcal{T}_N) \theta(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) \\ &+ \frac{d\sigma_{\geq N+1}^{\text{C-S}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) + \frac{d\sigma_{\geq N+1}^{\text{B-C}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) \end{aligned}$$



Combining fully exclusive NNLO with LL resummation.

- ▶ We have worked out analytically the ingredients (and the recipe) needed to achieve NNLO accuracy in LL accurate SMC. $\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$ [1311.0286]

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}), \quad \frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}), \quad \frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ Exclusive N -jet cross section (NNLO+LL)

$$\frac{d\sigma_N^{\text{MC}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = \underbrace{\frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}})}_{\text{resummed}} + \underbrace{\frac{d\sigma_N^{\text{C-S}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_N^{\text{B-C}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}})}_{\text{FO nonsingular matching}}$$

- ▶ Inclusive $N+1$ -jet cross section (NLO+LL)

$$\frac{d\sigma_{\geq N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) = \frac{d\sigma_{\geq N}^{\text{C}}}{d\Phi_N} \Big|_{\Phi_N = \hat{\Phi}_N} \frac{S_{N+1}(\hat{\Phi}_{N+1})}{B_N(\hat{\Phi}_N)} \Delta_N(\hat{\Phi}_N; \mathcal{T}_N) \theta(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) \\ + \frac{d\sigma_{\geq N+1}^{\text{C-S}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) + \frac{d\sigma_{\geq N+1}^{\text{B-C}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}})$$

- ▶ Inclusive N -jet cross-section correct by construction, since they are related by exact derivative.



Combining fully exclusive NNLO with LL resummation.

- ▶ Split up **inclusive $N+1$ -jet cross section** using resolution scale $\mathcal{T}_{N+1}^{\text{cut}}$
- ▶ **Exclusive $N+1$ -jet cross section (NLO+LL)** resummed

$$\frac{d\sigma_{N+1}^{\text{MC}}}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}}) = \overbrace{\frac{d\sigma'_{\geq N+1}{}^C}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) \Delta_{N+1}(\Phi_{N+1}; \mathcal{T}_{N+1}^{\text{cut}})}^{\text{resummed}}$$

$$+ \left(\underbrace{\frac{d\sigma_{N+1}^{C-S}}{d\Phi_{N+1}}}_{\text{FO singular matching}} + \underbrace{\frac{d\sigma_{N+1}^{B-C}}{d\Phi_{N+1}}}_{\text{FO nonsing. matching}} \right) (\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}; \mathcal{T}_{N+1}^{\text{cut}})$$

- ▶ **Inclusive $N+2$ -jet cross section (LO+LL)**

$$\frac{d\sigma_{\geq N+2}^{\text{MC}}}{d\Phi_{N+2}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}}) = \frac{d\sigma'_{\geq N+1}{}^C}{d\Phi_{N+1}}(\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}) \Big|_{\Phi_{N+1} = \hat{\Phi}_{N+1}}$$

$$\times \frac{S_{N+2}(\Phi_{N+2})}{B_{N+1}(\hat{\Phi}_{N+1})} \Delta_{N+1}(\hat{\Phi}_{N+1}; \mathcal{T}_{N+1}) \theta(\mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$

$$+ \left(\frac{d\sigma_{\geq N+2}^{C-S}}{d\Phi_{N+2}} + \frac{d\sigma_{\geq N+2}^{B-C}}{d\Phi_{N+2}} \right) (\mathcal{T}_N > \mathcal{T}_N^{\text{cut}}, \mathcal{T}_{N+1} > \mathcal{T}_{N+1}^{\text{cut}})$$



Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.



Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:



Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:
 - 1) Any exclusive observable must be (at least) LL in resummation regions; maintain logarithmic accuracy of \mathcal{T}_N and \mathcal{T}_{N+1} from MC cross sections.



Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:
 - 1) Any exclusive observable must be (at least) LL in resummation regions; maintain logarithmic accuracy of \mathcal{T}_N and \mathcal{T}_{N+1} from MC cross sections.
 - 2) NNLO accuracy for N -jet obs. , NLO for $N+1$ -jet and LO for $N+2$ -jet, in respective resolved regions. No FO requirements for unresolved regions, only filled by shower.



Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:
 - 1) Any exclusive observable must be (at least) LL in resummation regions; maintain logarithmic accuracy of \mathcal{T}_N and \mathcal{T}_{N+1} from MC cross sections.
 - 2) NNLO accuracy for N -jet obs. , NLO for $N+1$ -jet and LO for $N+2$ -jet, in respective resolved regions. No FO requirements for unresolved regions, only filled by shower.
 - 3) Any leftover dependence on $\mathcal{T}_N^{\text{cut}}$ and $\mathcal{T}_{N+1}^{\text{cut}}$ only enters at higher orders.



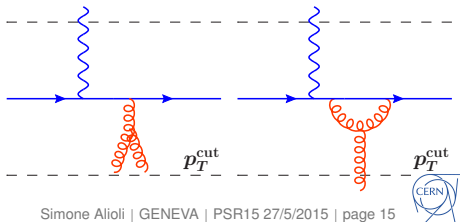
Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:
 - 1) Any exclusive observable must be (at least) LL in resummation regions; maintain logarithmic accuracy of \mathcal{T}_N and \mathcal{T}_{N+1} from MC cross sections.
 - 2) NNLO accuracy for N -jet obs. , NLO for $N+1$ -jet and LO for $N+2$ -jet, in respective resolved regions. No FO requirements for unresolved regions, only filled by shower.
 - 3) Any leftover dependence on $\mathcal{T}_N^{\text{cut}}$ and $\mathcal{T}_{N+1}^{\text{cut}}$ only enters at higher orders.
- ▶ Conditions above also ensure double-counting is avoided.

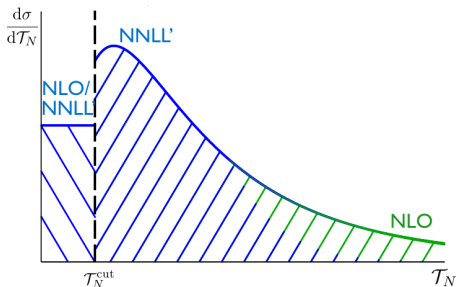


Adding the parton shower.

- ▶ Use the NNLO+LL fully-exclusive results $d\sigma_N^{\text{MC}}$, $d\sigma_{N+1}^{\text{MC}}$, $d\sigma_{>N+2}^{\text{MC}}$ as event weights and their kinematics as starting point for showering.
- ▶ Three conditions have to be satisfied for the shower matching:
 - 1) Any exclusive observable must be (at least) LL in resummation regions; maintain logarithmic accuracy of \mathcal{T}_N and \mathcal{T}_{N+1} from MC cross sections.
 - 2) NNLO accuracy for N -jet obs. , NLO for $N+1$ -jet and LO for $N+2$ -jet, in respective resolved regions. No FO requirements for unresolved regions, only filled by shower.
 - 3) Any leftover dependence on $\mathcal{T}_N^{\text{cut}}$ and $\mathcal{T}_{N+1}^{\text{cut}}$ only enters at higher orders.
- ▶ Conditions above also ensure double-counting is avoided.
- ▶ **Caveat:** when showering the NNLO N -jet bin care must be taken.
 - Single parton variables not IR-safe at NNLO
 - Conditions above could be applied after showering as a global veto



- ▶ What do we need need to make a NNLO+PS out of GENEVA ?



- ▶ Inclusive cross section NNLL' + NLO accurate
- ▶ Perturbative $\mathcal{O}(\alpha_s)$ everywhere
- ▶ Logarithms of merging scale ($\mathcal{T}_N^{\text{cut}}$) cancel at NNLL' by construction: merging of 2 NLOs is a by-product

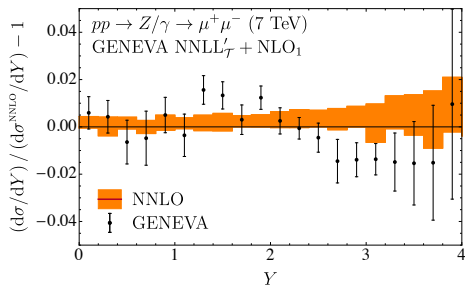
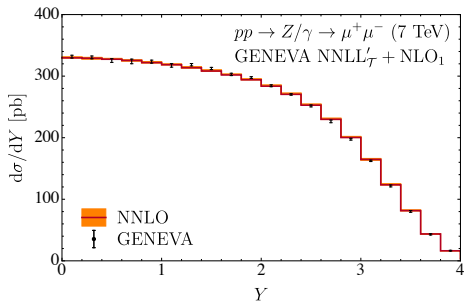
- ▶ Starting from NNLL' resummation, NNLO singular is automatically included

$$\checkmark \frac{d\sigma_{\geq N}^C}{d\Phi_N} \Delta_N(\Phi_N; \mathcal{T}_N^{\text{cut}}) \rightarrow \frac{d\sigma_N^{\text{resummed}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) \quad \checkmark \frac{d\sigma_N^{C-S}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) = 0$$

$$\times \frac{d\sigma_N^{B-C}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) \rightarrow \frac{d\sigma_N^{\text{nonsingular}}}{d\Phi_N}(\mathcal{T}_N^{\text{cut}}) \text{ suppressed by powers of } \mathcal{T}_N^{\text{cut}}$$

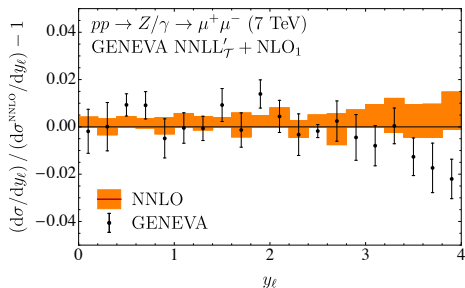
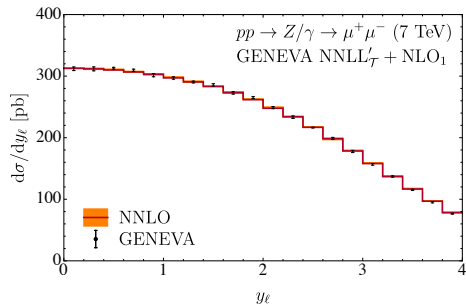
- ▶ Only non-singular power-suppressed contribution stemming from RV and RR are missing. Their effect can be made negligible by lowering $\mathcal{T}_N^{\text{cut}}$.
- ▶ Adding the NNLO non-singular terms back to 0-jet bin allows to raise $\mathcal{T}_N^{\text{cut}}$ to more moderate values.

- ▶ NNLO xsec and inclusive distributions validated against DYNMLO. Also checked against VRAP



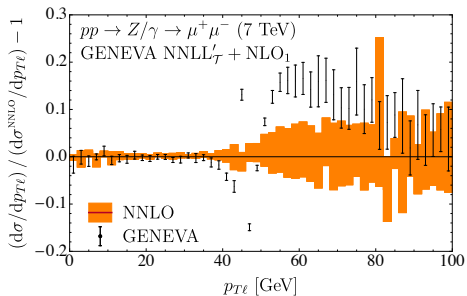
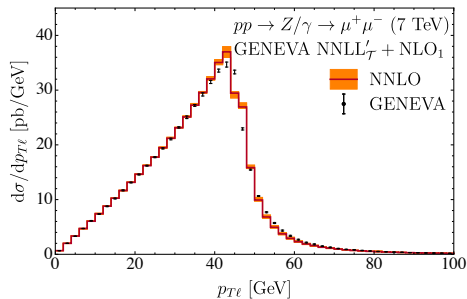
- ▶ Comparison for 7 TeV LHC, $\mathcal{T}_0^{\text{cut}} = 1$. Very good agreement for NNLO quantities, both central scale and variations.
- ▶ Non-trivial correlations for outer scales, ad-hoc procedure to ensure exact reproducibility of fixed-order variations.

- ▶ NNLO xsec and inclusive distributions validated against DYNMLO. Also checked against VRAP



- ▶ Comparison for 7 TeV LHC, $\mathcal{T}_0^{\text{cut}} = 1$. Very good agreement for NNLO quantities, both central scale and variations.
- ▶ Non-trivial correlations for outer scales, ad-hoc procedure to ensure exact reproducibility of fixed-order variations.

- ▶ NNLO xsec and inclusive distributions validated against DYNNLO. Also checked against VRAP



- ▶ Comparison for 7 TeV LHC, $\mathcal{T}_0^{\text{cut}} = 1$. Very good agreement for NNLO quantities, both central scale and variations.
- ▶ Non-trivial correlations for outer scales, ad-hoc procedure to ensure exact reproducibility of fixed-order variations.

Including \mathcal{T}_1 resummation

- Define separately excl. 1-jet and incl. 2-jets using $\mathcal{T}_1^{\text{cut}}$

$$\frac{d\sigma_0^{\text{MC}}}{d\Phi_0}(\mathcal{T}_0^{\text{cut}}) = \frac{d\sigma_0^{\text{resum}}}{d\Phi_0}(\mathcal{T}_0^{\text{cut}}) + \frac{d\sigma_0^{\text{nons}}}{d\Phi_0}(\mathcal{T}_0^{\text{cut}}),$$

$$\frac{d\sigma_1^{\text{MC}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}) = \frac{d\sigma_1^{\text{resum}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}) + \frac{d\sigma_1^{\text{nons}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}),$$

$$\begin{aligned} \frac{d\sigma_{\geq 2}^{\text{MC}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}, \mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}) &= \frac{d\sigma_{\geq 2}^{\text{resum}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) \theta(\mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}) \\ &+ \frac{d\sigma_{\geq 2}^{\text{nons}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}, \mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}). \end{aligned}$$

- We also perform a Sudakov-like LL resummation of $\mathcal{T}_1^{\text{cut}}$ to obtain a sensible separation between 1 and 2 jets, always enforcing unitarity

$$\frac{d\sigma_1^{\text{resum}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}) = \frac{d\sigma_{\geq 1}^{\text{C}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) U_1(\Phi_1, \mathcal{T}_1^{\text{cut}}),$$

$$\frac{d\sigma_{\geq 2}^{\text{resum}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) = \frac{d\sigma_{\geq 1}^{\text{C}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) U_1'(\Phi_1, \mathcal{T}_1) \Big|_{\Phi_1 = \Phi_1^{\mathcal{T}}(\Phi_2)} \mathcal{P}(\Phi_2),$$

- ▶ Some freedom in choice of what gets exponentiated by the U_1 Sudakov

$$\frac{d\sigma_{\geq 1}^C}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) = \frac{d\sigma_{\geq 1}^{\text{resum}}}{d\Phi_1} \theta(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) + \left[\frac{d\sigma_{\geq 1}^C}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) \right]_{\text{NLO}_1} - \frac{d\sigma_{\geq 1}^s}{d\Phi_1} \theta(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}),$$

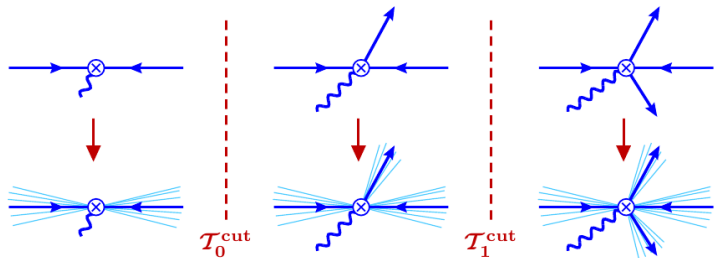
$$\left[\frac{d\sigma_{\geq 1}^C}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) \right]_{\text{NLO}_1} = (B_1 + V_1)(\Phi_1) \theta(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) + \int \frac{d\Phi_2}{d\tilde{\Phi}_1} C_2(\Phi_2) \theta(\tilde{\mathcal{T}}_0 > \mathcal{T}_0^{\text{cut}}).$$

- ▶ The complement gets automatically taken care of by the non-singular contributions. Dependence on $\mathcal{T}_1^{\text{cut}}$ cancels by construction.

$$\frac{d\sigma_1^{\text{nons}}}{d\Phi_1}(\mathcal{T}_1^{\text{cut}}) = \int d\Phi_2 \left[\frac{B_2(\Phi_2)}{d\Phi_1^T} \theta(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}) \theta(\mathcal{T}_1 < \mathcal{T}_1^{\text{cut}}) - \frac{C_2(\Phi_2)}{d\tilde{\Phi}_1} \theta(\tilde{\mathcal{T}}_0 > \mathcal{T}_0^{\text{cut}}) \right] - B_1(\Phi_1) U_1^{(1)}(\Phi_1, \mathcal{T}_1^{\text{cut}}),$$

$$\frac{d\sigma_{\geq 2}^{\text{nons}}}{d\Phi_2}(\mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}) = \{ B_2(\Phi_2) [1 - \Theta^{\mathcal{T}}(\Phi_2) \theta(\mathcal{T}_1 < \mathcal{T}_1^{\text{cut}})] - B_1(\Phi_1^T) U_1^{(1)'}(\Phi_1^T, \mathcal{T}_1) \mathcal{P}(\Phi_2) \theta(\mathcal{T}_1 > \mathcal{T}_1^{\text{cut}}) \} \theta(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}).$$

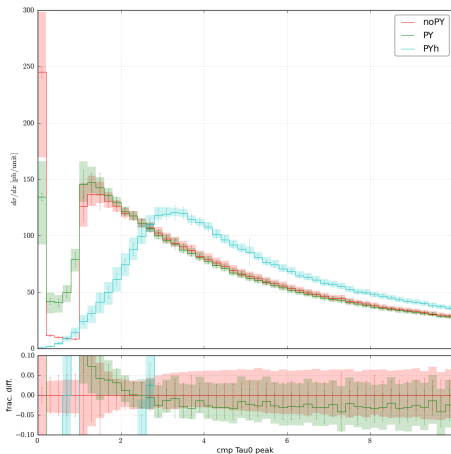
Showering and Hadronization



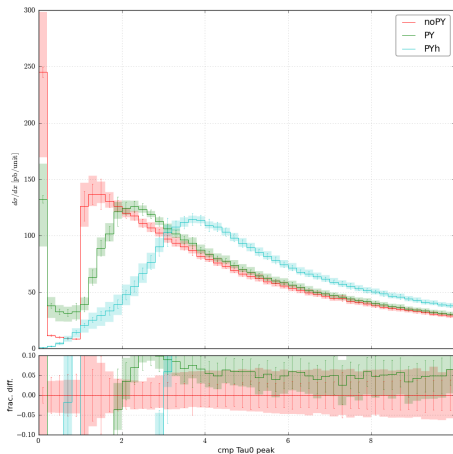
- ▶ Push $\mathcal{T}_0^{\text{cut}}$ towards zero allows to replace as much of the shower as possible with GENEVA higher logarithmic resummation.
- ▶ However, ultimately non-perturbative effects have to take over.
- ▶ Shower fills in $\mathcal{T}_0 < \mathcal{T}_0^{\text{cut}}$ from 0-jet events and $\mathcal{T}_1 < \mathcal{T}_1^{\text{cut}}$ from 1-jet ones. Small spill-over parameter $\lambda > \frac{|\mathcal{T}_0^{\text{GE+PY}} - \mathcal{T}_0^{\text{GE}}|}{\mathcal{T}_0^{\text{GE}}}$.
- ▶ Internal shower machinery untouched. Running shower repeatedly until conditions are met. Choice of starting scale can make showering quite efficient.

Showering and hadronization

\mathcal{T}_0 – constrained

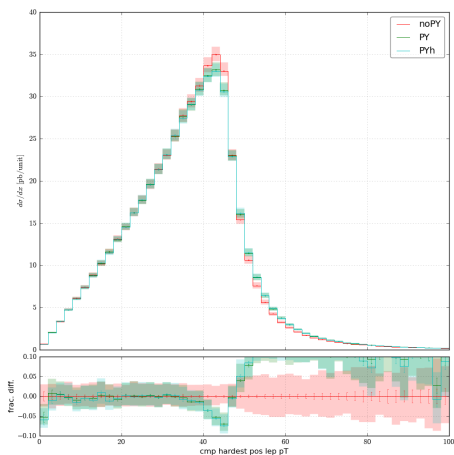
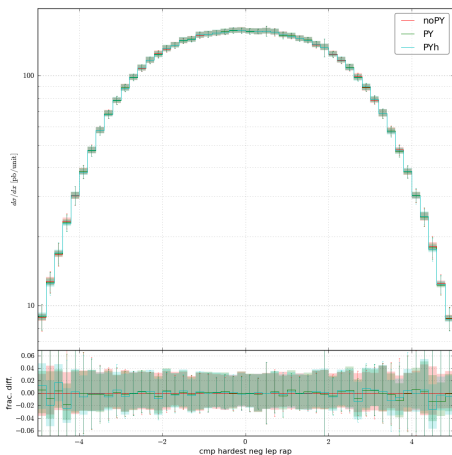


\mathcal{T}_0 – unconstrained



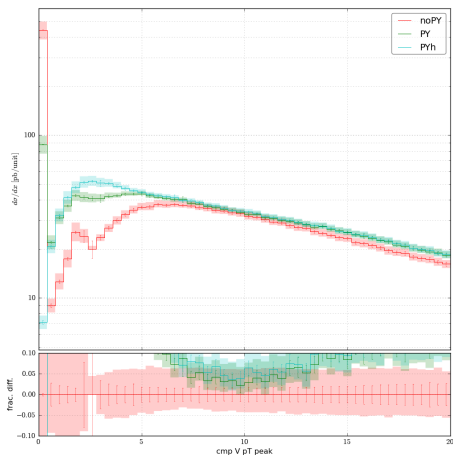
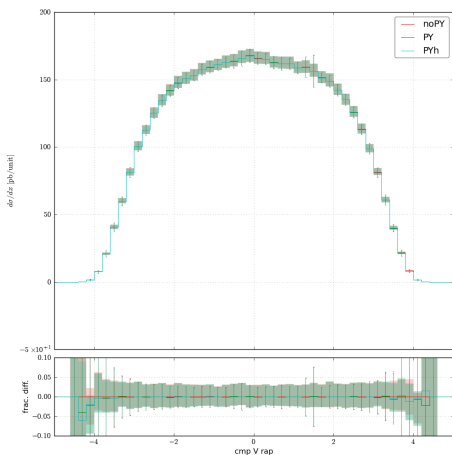
- ▶ At small \mathcal{T}_0 , large shift from unconstrained shower even when $\mathcal{T}_1^{\text{cut}}$ small.
- ▶ Hadronization completely unconstrained and left to Pythia.
- ▶ As expected, $\mathcal{O}(1)$ shift in peak region. At larger \mathcal{T}_0 it only reduces to power corrections

Showering and hadronization



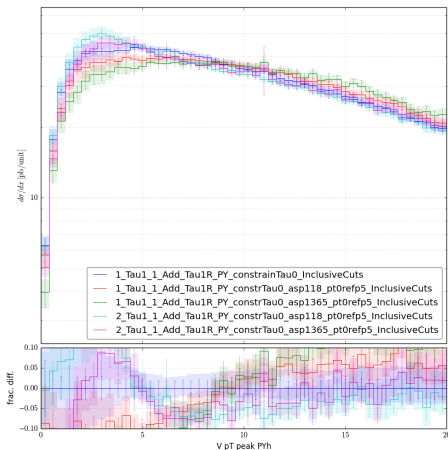
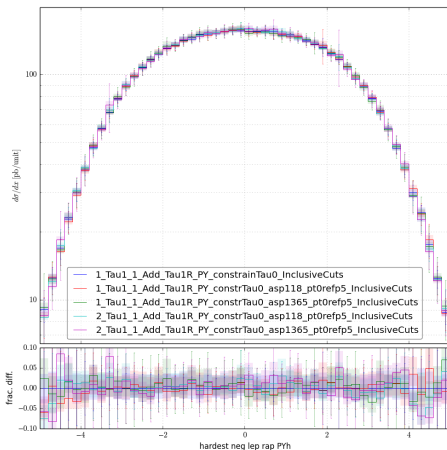
- ▶ Inclusive quantities not modified
- ▶ PYTHIA 8 tuning to data includes tuning of the shower parameters → replacing PYTHIA by GENEVA showering could imply re-tuning is necessary

Showering and hadronization



- ▶ PYTHIA8 includes variations of perturbative parameters into tunes.
- ▶ Some distributions particularly sensitive to PYTHIA8 choices.

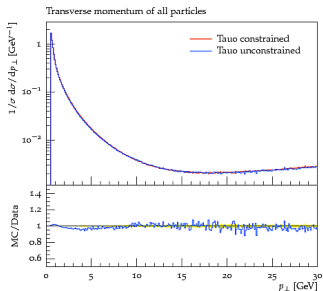
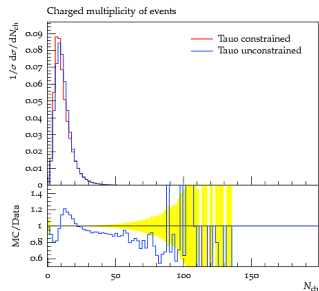
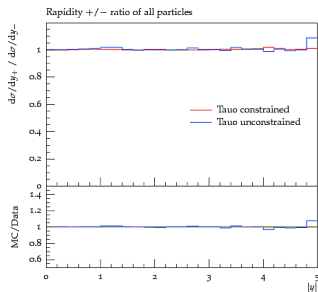
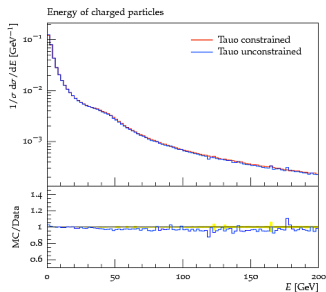
Showering and hadronization



- ▶ First study to determine freedom in selection of particular PYTHIA8 parameters governing the shower, like $p_{T_0}^{\text{ref}}$ or $\alpha_s(M_Z)$
- ▶ Adopted approach much more conservative than standard ranges suggested in PYTHIA manual.
- ▶ Trying to leave only true non-perturbative effects to further tuning.

Showering and Hadronization

- ▶ How much is \mathcal{T}_0 constrain affecting the shower ?

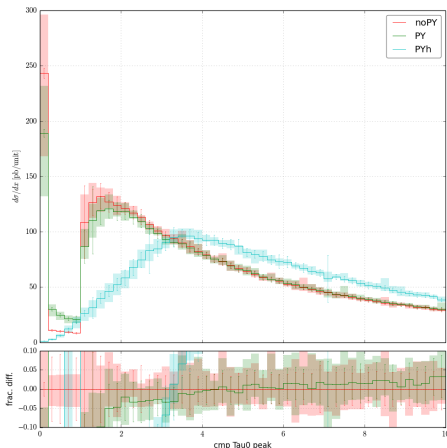


Showering and Hadronization

- ▶ How can we relax the \mathcal{T}_0 constrain ?

We need the shower to fill back the phase space that we consider unresolved. This specifically **depends on the map** we have used in the calculation. **Pythia uses a very different map.**

- ▶ Do the first $1 \rightarrow 2$ splitting ourselves with out \mathcal{T}_0 -preserving map and using a LL $U_1(\Phi_1; \mathcal{T}_1^{\text{cut}}, \mathcal{T}_1^{\text{IR}})$ Sudakov.
- ▶ PYTHIA will then start after our first emission, no further constraint on it.
- ▶ One could use NLL $U_1(\Phi_1; \mathcal{T}_1^{\text{cut}}, \mathcal{T}_1^{\text{IR}})$ or use POWHEG/MC@NLO method to do this splitting with higher accuracy.



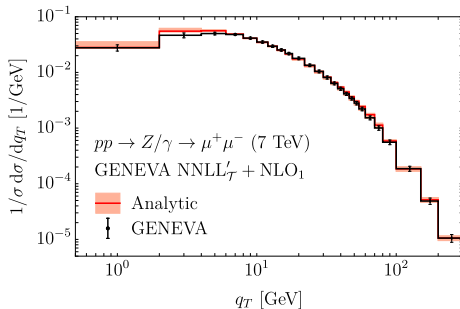
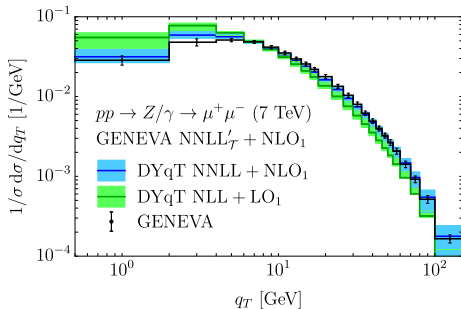
$$\frac{d\sigma_1^{\text{MC}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}; \mathcal{T}_1^{\text{IR}}) = \frac{d\sigma_1^{\text{MC}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}) U_1(\Phi_1; \mathcal{T}_1^{\text{cut}}, \mathcal{T}_1^{\text{IR}}),$$

$$\frac{d\sigma_{\geq 2}^{\text{MC}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}, \mathcal{T}_1 > \mathcal{T}_1^{\text{IR}}) = \frac{d\sigma_{\geq 2}^{\text{MC}}}{d\Phi_2}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}, \mathcal{T}_1 > \mathcal{T}_1^{\text{cut}})$$

$$+ \frac{d\sigma_1^{\text{MC}}}{d\Phi_1}(\mathcal{T}_0 > \mathcal{T}_0^{\text{cut}}; \mathcal{T}_1^{\text{cut}}) U_1'(\Phi_1; \mathcal{T}_1^{\text{cut}}, \mathcal{T}_1) \Big|_{\Phi_1 = \Phi \mathcal{T}(\Phi_2)} \mathcal{P}(\Phi_2).$$

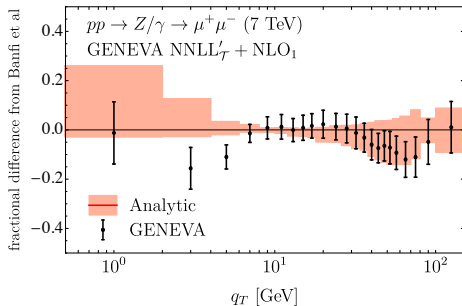
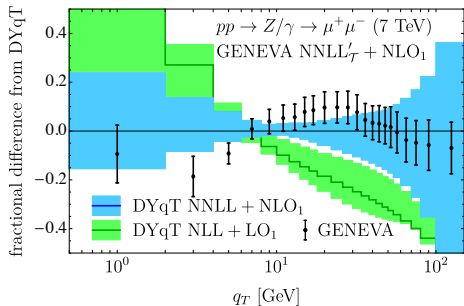
Predictions for other observables : q_T and ϕ^*

- ▶ Comparison with **DYqT** Bozzi et al. arXiv:1007.2351 and **BDMT** results Banfi et al. arXiv:1205.4760
- ▶ Inclusive cuts for DYqT, ATLAS cuts for BDMT. Each normalized to own XS.
- ▶ Analytic predictions formally higher log accuracy than GENEVA
- ▶ PYTHIA8 provides non-perturbative hadronization corrections



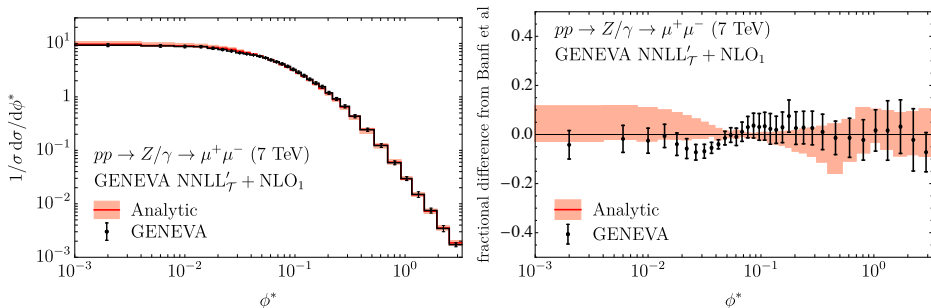
Predictions for other observables : q_T and ϕ^*

- ▶ Comparison with **DYqT** Bozzi et al. arXiv:1007.2351 and **BDMT** results Banfi et al. arXiv:1205.4760
- ▶ Inclusive cuts for DYqT, ATLAS cuts for BDMT. Each normalized to own XS.
- ▶ Analytic predictions formally higher log accuracy than GENEVA
- ▶ PYTHIA8 provides non-perturbative hadronization corrections



Predictions for other observables : q_T and ϕ^*

- ▶ Comparison with **DYqT** Bozzi et al. arXiv:1007.2351 and **BDMT** results Banfi et al. arXiv:1205.4760
- ▶ Inclusive cuts for DYqT, ATLAS cuts for BDMT. Each normalized to own XS.
- ▶ Analytic predictions formally higher log accuracy than GENEVA
- ▶ PYTHIA8 provides non-perturbative hadronization corrections

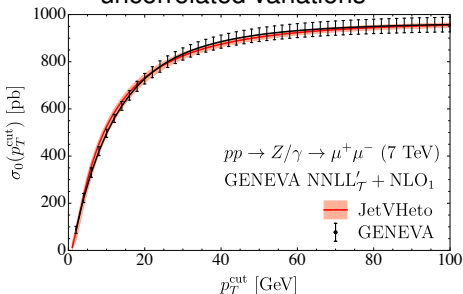


- ▶ ϕ^* strongly correlated to q_T , $\phi^* = \tan\left(\frac{\pi - \Delta\phi}{2}\right) \sin\theta^* \approx \left|\sum_i \frac{k_{T,i}}{Q} \sin\phi_i\right|$

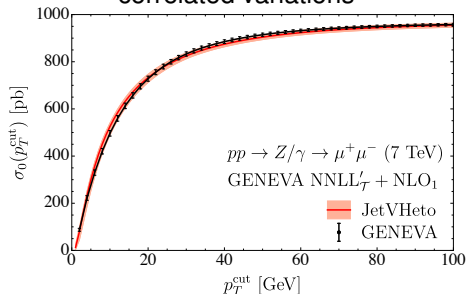
Predictions for other observables : jet-veto acceptance

- ▶ Comparison with **JetVHeto** results Banfi et al. arXiv:1308.4634
- ▶ Analytic predictions at NNLL formally higher log accuracy than GENEVA
- ▶ Must reduce to total xsec in the tail. Small differences due to different hard-scale and NWA.
- ▶ Non-trivial propagation of spectrum uncertainties to cumulant result. Neglected correlations yield larger uncertainties.
- ▶ Imposing total XS hard variations only results in small uncertainties in peak region.

uncorrelated variations

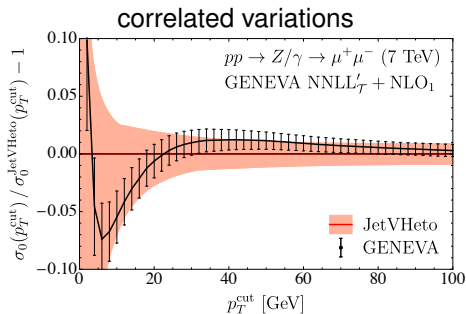
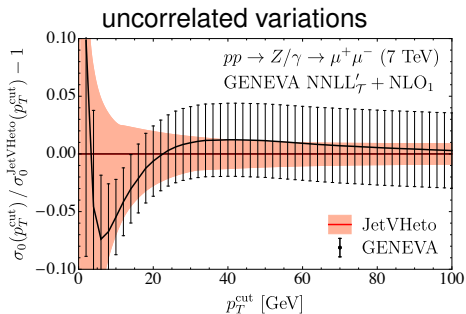


correlated variations



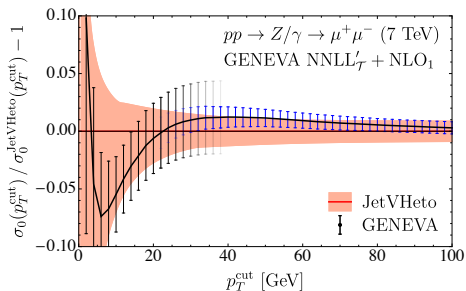
Predictions for other observables : jet-veto acceptance

- ▶ Comparison with **JetVHeto** results Banfi et al. arXiv:1308.4634
- ▶ Analytic predictions at NNLL formally higher log accuracy than GENEVA
- ▶ Must reduce to total xsec in the tail. Small differences due to different hard-scale and NWA.
- ▶ Non-trivial propagation of spectrum uncertainties to cumulant result. Neglected correlations yield larger uncertainties.
- ▶ Imposing total XS hard variations only results in small uncertainties in peak region.



Predictions for other observables : jet-veto acceptance

- ▶ Comparison with **JetVHeto** results Banfi et al. arXiv:1308.4634
- ▶ Analytic predictions at NNLL formally higher log accuracy than GENEVA
- ▶ Must reduce to total xsec in the tail. Small differences due to different hard-scale and NWA.
- ▶ Non-trivial propagation of spectrum uncertainties to cumulant result. Neglected correlations yield larger uncertainties.
- ▶ Imposing total XS hard variations only results in small uncertainties in peak region.

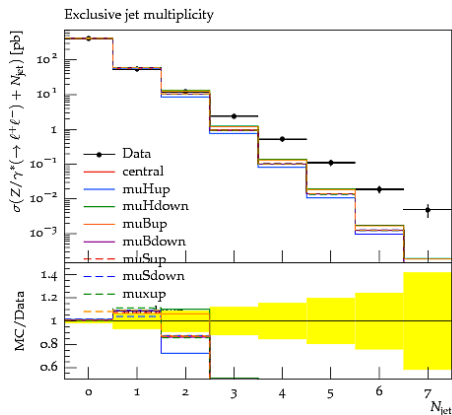
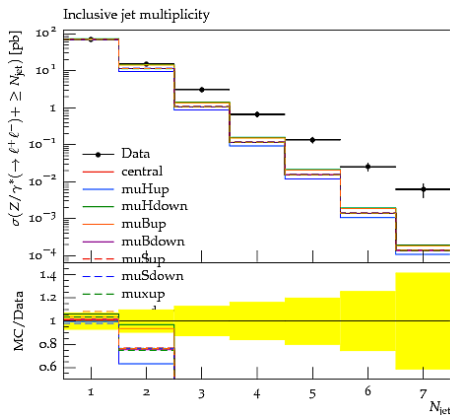


- ▶ Testing new profile scales that correctly capture the right uncertainty.

see J. Walsh talk at SCET '15



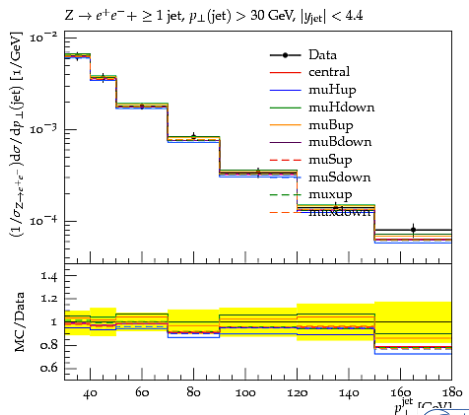
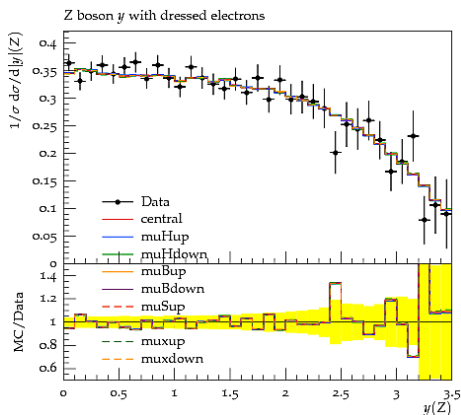
Comparisons with data



- ▶ First preliminary results for 7 TeV LHC .
- ▶ Results consistent with NNLO₀ MC expectations
- ▶ Higher multiplicities could be improved at LO with standard CKKW /MLM approaches
- ▶ Provided sufficient resummation available for \mathcal{T}_N further NLO matrix elements could be included.

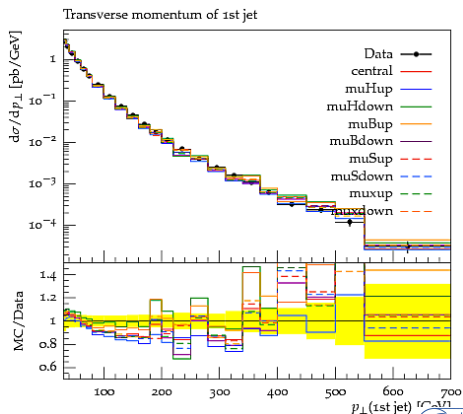
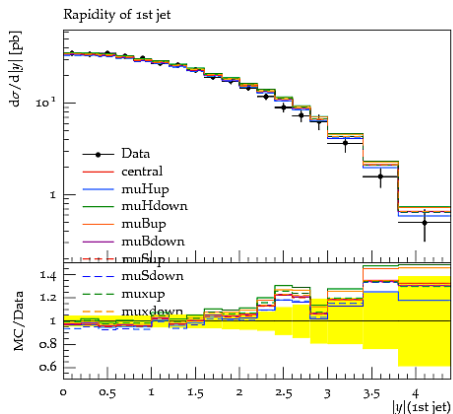
Comparisons with data

- ▶ Preliminary comparisons. All scale variations show to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.
- ▶ For inclusive quantities, fixed order scale variations including correlations provide the best estimate of theory uncertainty



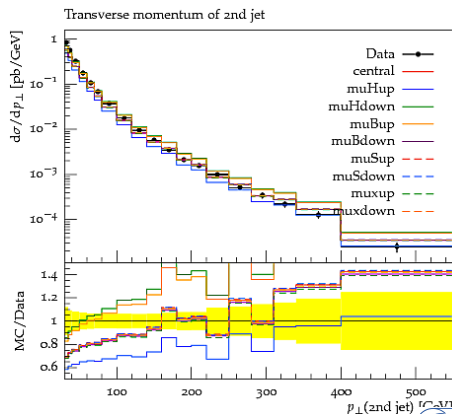
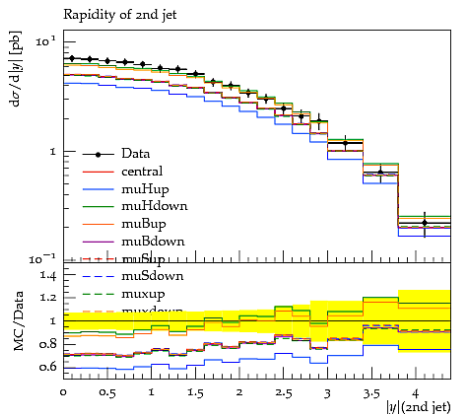
Comparisons with data

- ▶ Preliminary comparisons. All scale variations show to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.
- ▶ For inclusive quantities, fixed order scale variations including correlations provide the best estimate of theory uncertainty



Comparisons with data

- ▶ Preliminary comparisons. All scale variations show to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.
- ▶ For inclusive quantities, fixed order scale variations including correlations provide the best estimate of theory uncertainty



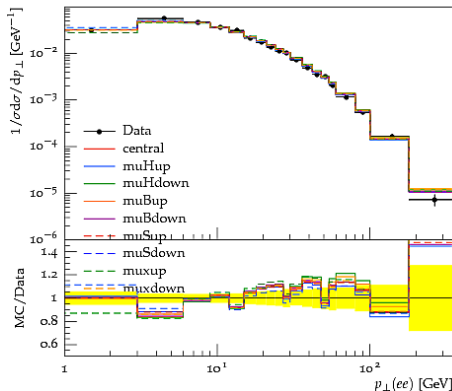
Comparisons with Z/γ^*p_T LHC 7 TeV data

- ▶ Preliminary comparisons. All scale variations shown to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.

ATLAS 2011

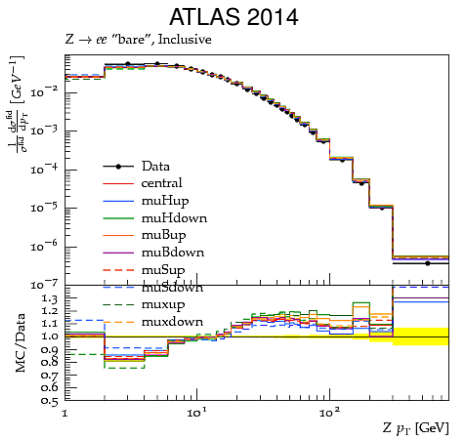
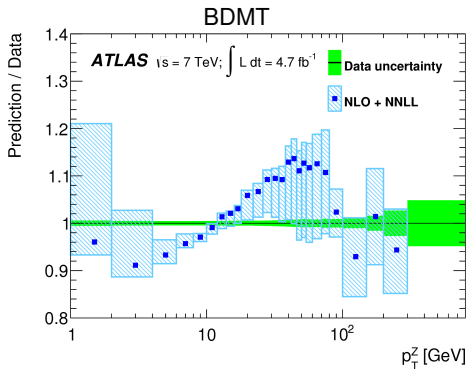
ATLAS 2014

$Z p_{\perp}$ reconstructed from bare electrons



Comparisons with Z/γ^*p_T LHC 7 TeV data

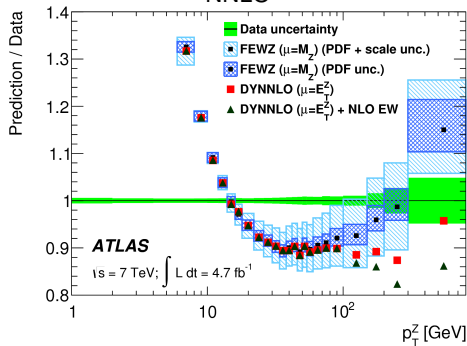
- ▶ Preliminary comparisons. All scale variations shown to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.



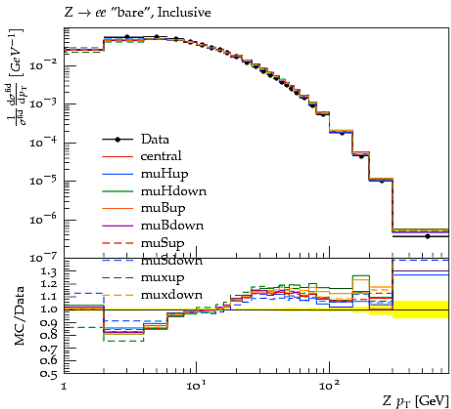
Comparisons with Z/γ^*p_T LHC 7 TeV data

- ▶ Preliminary comparisons. All scale variations shown to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.

NNLO



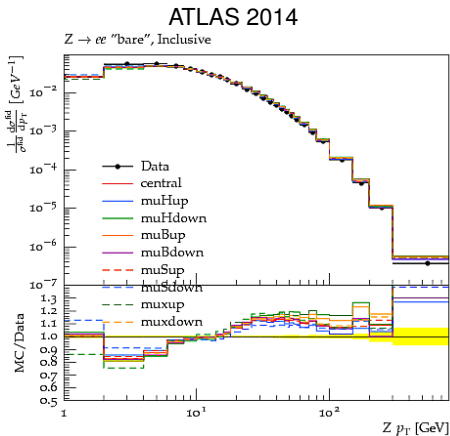
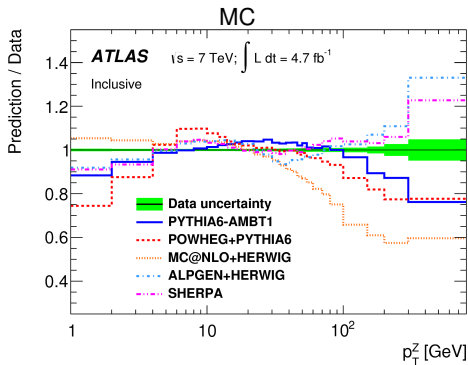
ATLAS 2014



- ▶ NNLO $Z + 1$ -jet required to reduce theory uncertainty in the tail.

Comparisons with $Z/\gamma^* p_T$ LHC 7 TeV data

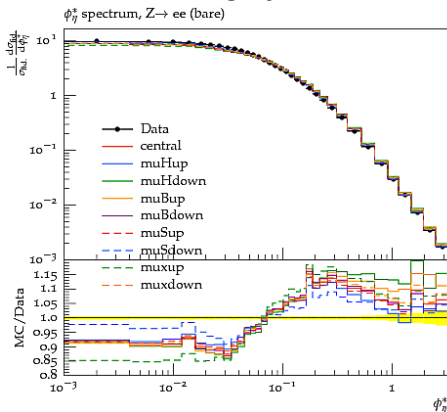
- ▶ Preliminary comparisons. All scale variations shown to provide breakdown on uncertainties.
- ▶ More accurate uncertainty requires the envelope of resummation scales added in quadrature to hard scale variations.



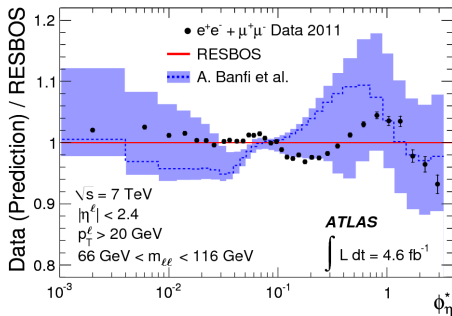
- ▶ NNLO $Z + 1$ -jet required to reduce theory uncertainty in the tail.

- ▶ Similar good agreement in ϕ^* distribution

ATLAS 2012

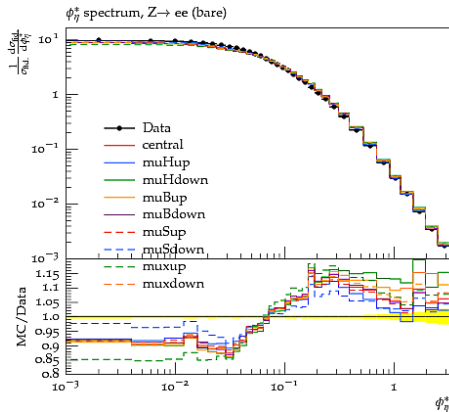


BDMT / RESBOS

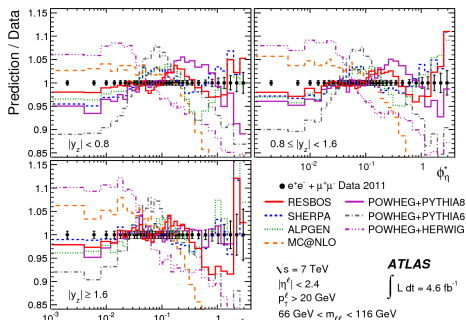


- ▶ Similar good agreement in ϕ^* distribution

ATLAS 2012



MC



Conclusions and outlook



is NNLO event generator that can be interfaced with shower/hadronization.

- ▶ Based on **IR-safe, jet-like** definitions of events.
- ▶ Uses a physics observable, N -jettiness, factorizable and whose resummation is known to NNLL as jet resolution parameter. e^+e^- and Drell-Yan results extremely encouraging.
- ▶ Worked out **theoretical framework for NNLO+PS**: given formulas for jet cross section at the necessary accuracy in both fixed order ($\text{NNLO}_N, \text{NLO}_{N+1}, \text{LO}_{N+2}$) and resummation regions (LL). Discussed shower matching.
- ▶ POWHEG, MC@NLO, GENEVA and MiNLO-NNLOPS re-derived as special limits. **GENEVA** also immediately follows, imposing NNLL' accuracy .
- ▶ Good agreement with analytical calculation / tools and with LHC data.

Future directions:

- Adding more jets, e.g. $pp \rightarrow V + 0, 1, 2$ and validation with LHC data.
- Next process is $gg \rightarrow H + 0, 1, 2$ jets.
- Investigate resummation of different resolution parameters / double resummation
- Study interface to other SMC: HERWIG++, SHERPA ...
- Comprehensive tuning program of GENEVA + SMC.

Thank you for your attention!

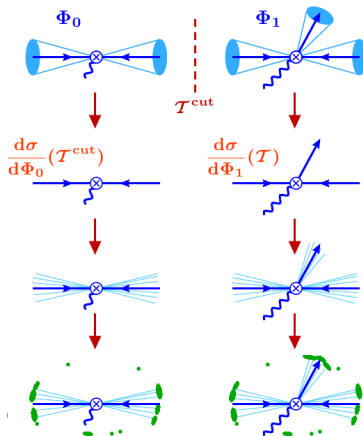


Backup

GENEVA: quick overview

Combines 3 key ingredients in a single framework:

1. Fully Exclusive NLO Calculations
 - ▶ $\text{NLO}_N, \text{NLO}_{N+1}, \dots$
2. Higher-order Resummation (using SCET, but not limited to it)
 - ▶ $\text{LL}_\mathcal{O}, \text{NLL}_\mathcal{O}, \text{NLL}'_\mathcal{O}, \text{NNLL}_\mathcal{O} \dots$
3. Parton Shower and Hadronization
 - ▶ Pythia8, Herwig++, ...



GENEVA guiding principle

Give a coherent description at the **Next-to-Lowest perturbative accuracy** in both fixed-order perturbation theory and logarithmic resummation, including **event-by-event theoretical uncertainties**, and combine it with parton shower and hadronization.

First application: $e^+e^- \rightarrow \text{jets}$

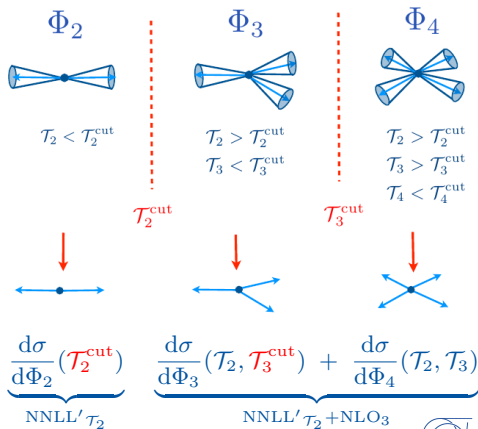
- ✓ Simpler process to test our construction.
- ✓ Thrust spectrum known to $N^3LL'_{\mathcal{T}} + NNLO_3$.
- ✓ Several 2-jet shapes known to $NNLL_{\mathcal{O}} + NNLO_3$.
- ✓ LEP data available for validation.

- Use 2- and 3-jettiness.

$$\mathcal{T}_2 = E_{\text{cm}} \left(1 - \max_{\hat{n}} \frac{\sum_k |\hat{n} \cdot \vec{p}_k|}{\sum_k |\vec{p}_k|} \right)$$

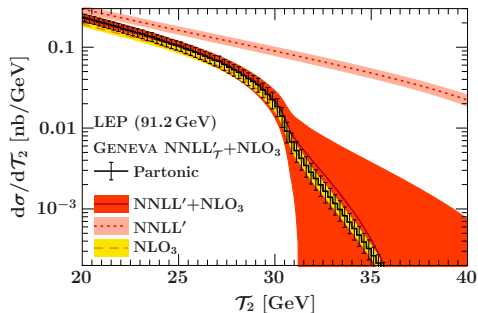
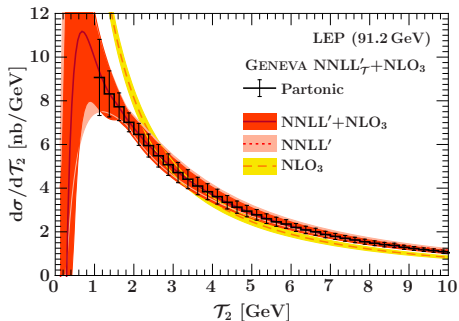
$$= E_{\text{cm}} (1 - T)$$

- Opportunely partitioning the phase-space
- Perturbatively calculating NLO/Resumm. jet-cross sections.



Resummation of \mathcal{T}_2

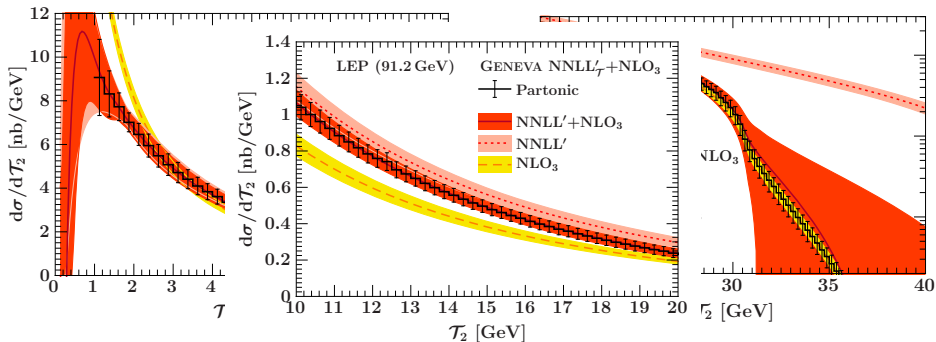
- ▶ GENEVA precisely reproduces full NNLL'+NLO3 analytic result :
simply getting out what we put in!



- Error bars are always theory uncertainties, obtained via scale variations. Statistical uncertainties negligible and not shown.
- Resummation unc. obtained via quadrature sum of single scale variations (μ_S, μ_J) inside profile scale bands plus direct sum of FO uncertainties (μ_H).
- GENEVA $\mathcal{T}_2^{\text{cut}} = 1$ GeV above
- Theoretical uncertainties agree across most of the spectrum, differences after kinematic 3-body endpoint consequence of different matching procedure (multiplicative vs. additive).

Resummation of \mathcal{T}_2

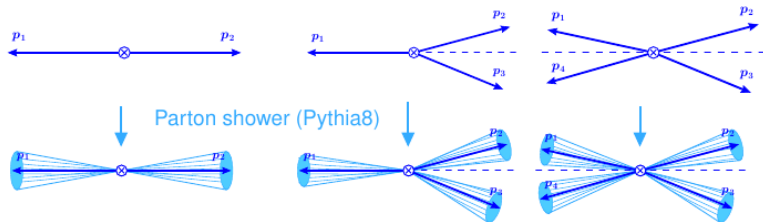
- ▶ GENEVA precisely reproduces full NNLL'+NLO3 analytic result :
simply getting out what we put in!



- Error bars are always theory uncertainties, obtained via scale variations. Statistical uncertainties negligible and not shown.
- Resummation unc. obtained via quadrature sum of single scale variations (μ_S, μ_J) inside profile scale bands plus direct sum of FO uncertainties (μ_H).
- GENEVA $\mathcal{T}_2^{\text{cut}} = 1$ GeV above
- Theoretical uncertainties agree across most of the spectrum, differences after kinematic 3-body endpoint consequence of different matching procedure (multiplicative vs. additive).

Interface with the parton shower

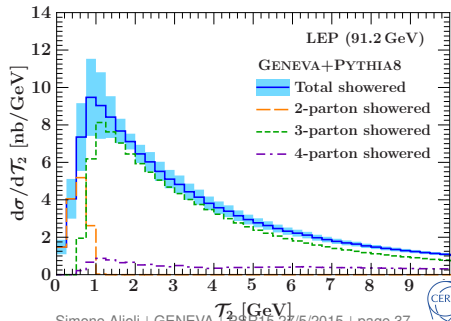
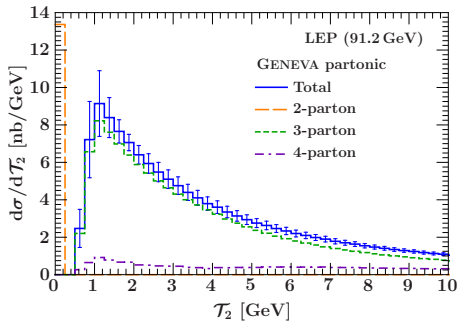
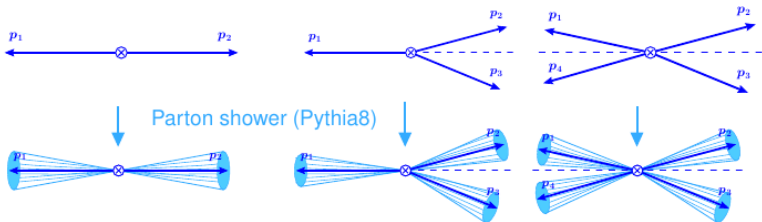
- ▶ The shower must not be allowed to spoil NNLL' \mathcal{T} accuracy of GENEVA, but only used to fill out jets.



- ▶ \mathcal{T}_2 spectrum for 3 and 4-parton events constrained by higher-order resummation. Only allow small variations $\Delta\mathcal{T}_2 < \mathcal{T}_2^{\text{cut}}(1 + \epsilon)$.
- ▶ 2-parton events must remain in 2-jets bin, up to small corrections
- ▶ Similarly for $\mathcal{T}_3(\Phi_4)$ spectrum and 3-jets bin. Proxy for \mathcal{T} -ordered PS.
- ▶ Shower unconstrained in the far tail at the moment, since only LO $_4$ there.

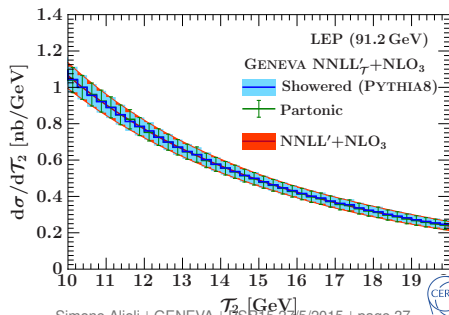
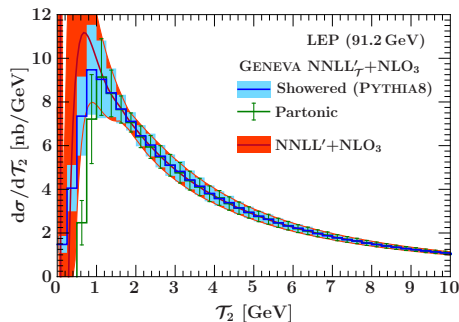
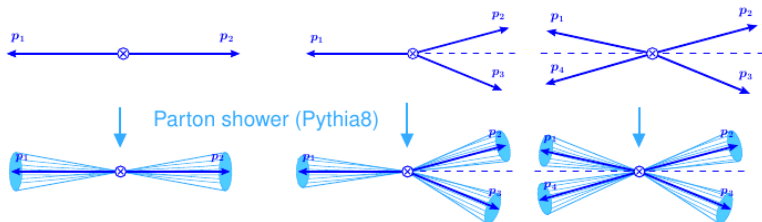
Interface with the parton shower

- ▶ The shower must not be allowed to spoil NNLL' τ accuracy of GENEVA, but only used to fill out jets.



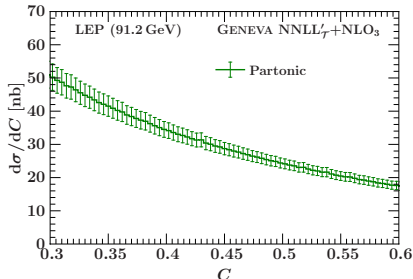
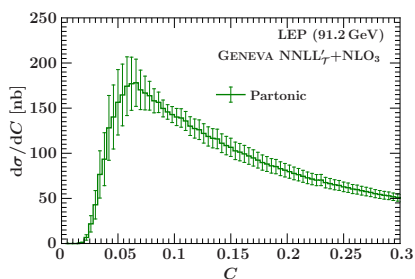
Interface with the parton shower

- ▶ The shower must not be allowed to spoil NNLL' $_{\tau}$ accuracy of GENEVA, but only used to fill out jets.



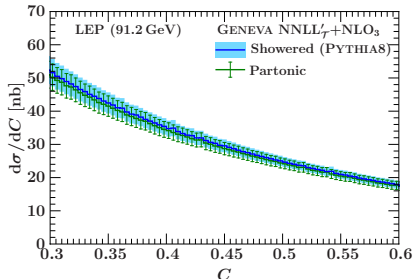
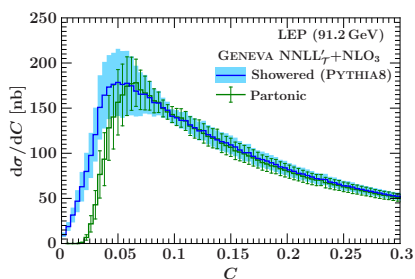
Accuracy of observables different from resolution parameter

- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_E$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ C -parameter – perturbative structure very similar to \mathcal{T}_2



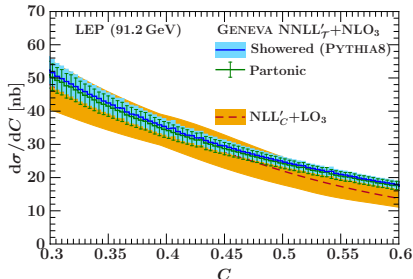
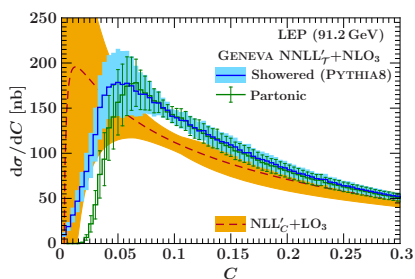
Accuracy of observables different from resolution parameter

- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_E$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ C -parameter – perturbative structure very similar to \mathcal{T}_2



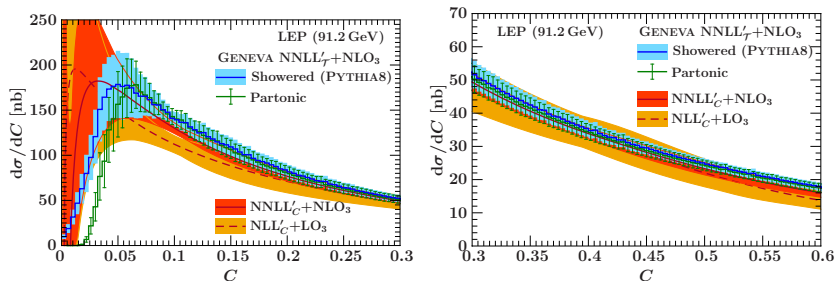
Accuracy of observables different from resolution parameter

- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_E$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ C -parameter – perturbative structure very similar to \mathcal{T}_2



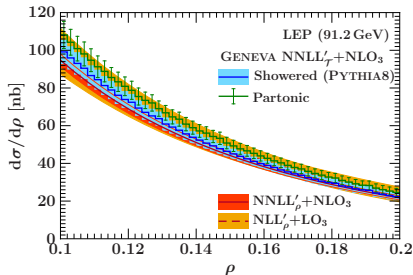
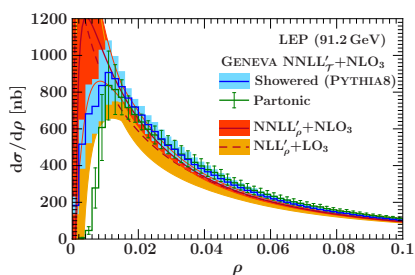
Accuracy of observables different from resolution parameter

- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_E$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ C -parameter – perturbative structure very similar to \mathcal{T}_2



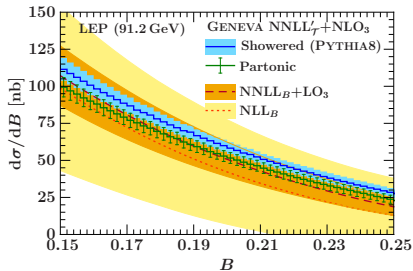
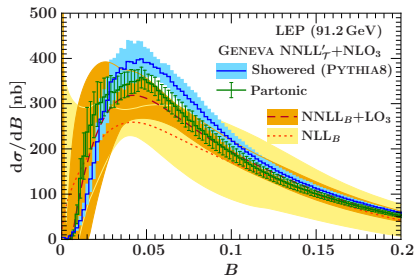
Accuracy of observables different from resolution parameter

- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_\epsilon$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ Heavy jet mass – perturbative structure partially related to \mathcal{T}_2



Accuracy of observables different from resolution parameter

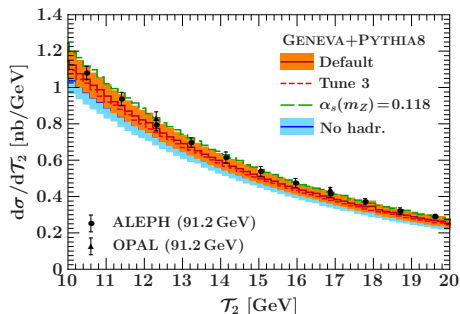
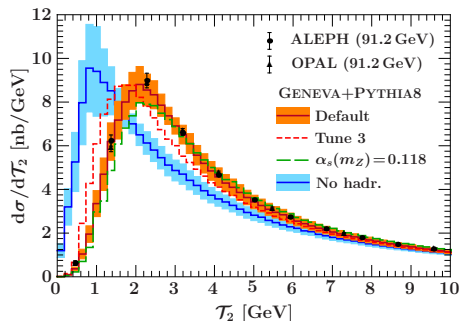
- ▶ After showering we are formally limited by shower resummation for generic observables $\mathcal{O} \neq \mathcal{T}_\epsilon$. Naively, (N)LL is expected.
- ▶ What is the perturbative accuracy we obtain for other \mathcal{O} ?
- ▶ Jet Broadening – perturbative structure completely different from \mathcal{T}_2



- ▶ Good agreement in central values and scale uncertainties envelopes at NNLL, also for observables with a very different resummation structure.
- ▶ NNLL resummation allows to push $\mathcal{T}_2^{\text{cut}}$ to very small values, effectively replacing the shower evolution.
- ▶ Ultimately, we rely on Pythia8 hadronization model for non-pert. physics

Hadronization and comparison with LEP data.

- Two-jettiness = $E_{\text{cm}}(1 - T)$



- ▶ Hadronization (non-perturbative effect) is unconstrained.
- ▶ No ad-hoc tune yet, default Pythia8 Tune1 with $\alpha_s(m_Z) = 0.1135$ from τ fits.

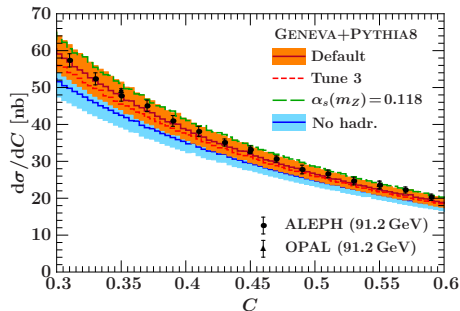
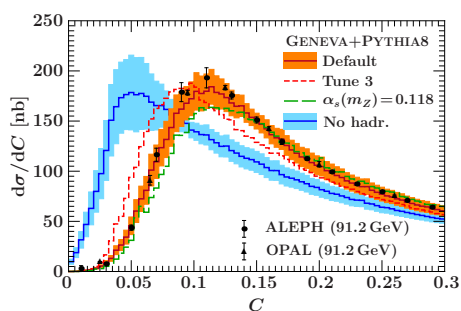
[Abbate et al. 1006.3080]

- ▶ Large shift due to hadronization, $\mathcal{O}(1)$, in the peak.
- ▶ Power suppressed effects elsewhere, as expected.



Hadronization and comparison with LEP data.

• C -parameter



- ▶ Hadronization (non-perturbative effect) is unconstrained.
- ▶ No ad-hoc tune yet, default Pythia8 Tune1 with $\alpha_s(m_Z) = 0.1135$ from τ fits.

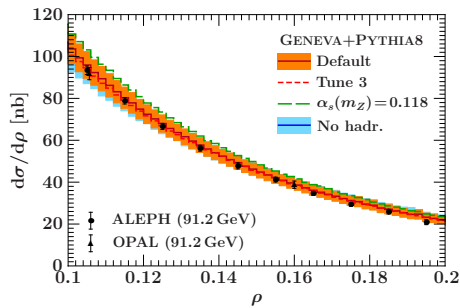
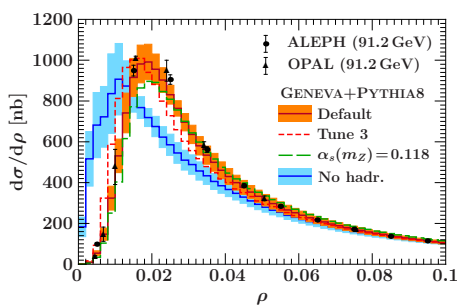
[Abbate et al. 1006.3080]

- ▶ Large shift due to hadronization, $\mathcal{O}(1)$, in the peak.
- ▶ Power suppressed effects elsewhere, as expected.



Hadronization and comparison with LEP data.

- Heavy jet mass

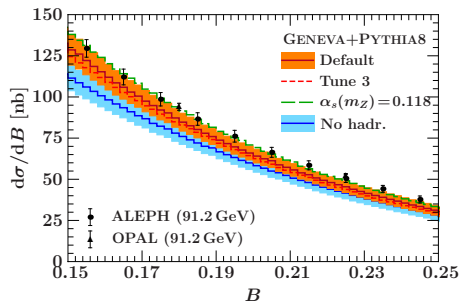
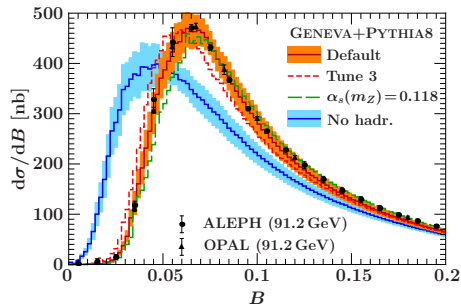


- ▶ Hadronization (non-perturbative effect) is unconstrained.
- ▶ No ad-hoc tune yet, default Pythia8 Tune1 with $\alpha_s(m_Z) = 0.1135$ from τ fits.

[Abbate et al. 1006.3080]

- ▶ Large shift due to hadronization, $\mathcal{O}(1)$, in the peak.
- ▶ Power suppressed effects elsewhere, as expected.

• Jet Broadening



- ▶ Hadronization (non-perturbative effect) is unconstrained.
- ▶ No ad-hoc tune yet, default Pythia8 Tune1 with $\alpha_s(m_Z) = 0.1135$ from τ fits.
- ▶ Large shift due to hadronization, $\mathcal{O}(1)$, in the peak.
- ▶ Power suppressed effects elsewhere, as expected.

[Abbate et al. 1006.3080]

Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales.

[Hamilton et al. 1206.3572]



Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales. [Hamilton et al. 1206.3572]
- ▶ Like CKKW, it also includes LL Sudakovs factors, that regulate IR divergencies (e.g. H+1 jets finite $p_T^j \rightarrow 0$)



Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales. [Hamilton et al. 1206.3572]
- ▶ Like CKKW, it also includes LL Sudakovs factors, that regulate IR divergencies (e.g. H+1 jets finite $p_T^j \rightarrow 0$)
- ▶ NLO accuracy for inclusive sample not achieved in MiNLO v1
 - The reason is that resumming $q_{T\text{cut}}$ with LL Sudakov generates terms $\mathcal{O}(\alpha_s^{1.5})$



Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales. [Hamilton et al. 1206.3572]
- ▶ Like CKKW, it also includes LL Sudakovs factors, that regulate IR divergencies (e.g. H+1 jets finite $p_T^j \rightarrow 0$)
- ▶ NLO accuracy for inclusive sample not achieved in MiNLO v1
 - The reason is that resumming $q_{T\text{cut}}$ with LL Sudakov generates terms $\mathcal{O}(\alpha_s^{1.5})$
- ▶ By carefully comparing with NNLL resummation and including missing terms (B_2) in MiNLO Sudakovs, NLO accuracy for inclusive sample can be restored \rightarrow MiNLO v2 . [Hamilton et al. 1212.4504]



Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales. [Hamilton et al. 1206.3572]
- ▶ Like CKKW, it also includes LL Sudakovs factors, that regulate IR divergencies (e.g. H+1 jets finite $p_T^j \rightarrow 0$)
- ▶ NLO accuracy for inclusive sample not achieved in MiNLO v1
 - The reason is that resumming $q_{T\text{cut}}$ with LL Sudakov generates terms $\mathcal{O}(\alpha_s^{1.5})$
- ▶ By carefully comparing with NNLL resummation and including missing terms (B_2) in MiNLO Sudakovs, NLO accuracy for inclusive sample can be restored \rightarrow MiNLO v2 . [Hamilton et al. 1212.4504]
- ▶ Merging scale can be basically pushed to Λ_{QCD} : achieves NLO merging without merging scale (H+0 jets is never present)



Comparison with existing approaches: MiNLO NNLO+PS.

- ▶ MiNLO v1 is CKKW-inspired recipe to set *a priori* the scales of a NLO calculation involving multiple scales. [Hamilton et al. 1206.3572]
- ▶ Like CKKW, it also includes LL Sudakovs factors, that regulate IR divergencies (e.g. $H+1$ jets finite $p_T^j \rightarrow 0$)
- ▶ NLO accuracy for inclusive sample not achieved in MiNLO v1
 - The reason is that resumming $q_{T\text{cut}}$ with LL Sudakov generates terms $\mathcal{O}(\alpha_s^{1.5})$
- ▶ By carefully comparing with NNLL resummation and including missing terms (B_2) in MiNLO Sudakovs, NLO accuracy for inclusive sample can be restored \rightarrow MiNLO v2. [Hamilton et al. 1212.4504]
- ▶ Merging scale can be basically pushed to Λ_{QCD} : achieves NLO merging without merging scale ($H+0$ jets is never present)
- ▶ For simple processes (e.g. $gg \rightarrow H$), using **HNNLO** [Catani et al. 0801.3232] for **event-by-event reweighting** results in a **NNLO+PS** [Hamilton,Nason,Re,Zanderighi 1309.0017]

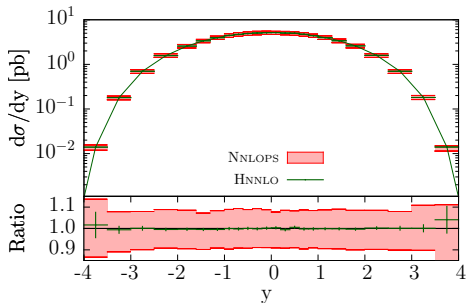
$$\mathcal{W}(y) = \frac{\left(\frac{d\sigma}{dy}\right)_{\text{HNNLO}}}{\left(\frac{d\sigma}{dy}\right)_{\text{HJ-MiNLO}}} = \frac{c_2\alpha_S^2 + c_3\alpha_S^3 + c_4\alpha_S^4}{c_2\alpha_S^2 + c_3\alpha_S^3 + c'_4\alpha_S^4 + \dots} = 1 + \frac{c_4 - c'_4}{c_2} \alpha_S^2 + \dots$$

- Integrates back to the total NNLO cross-section
- NLO accuracy of H_j not spoiled
- Need to reweight after generation

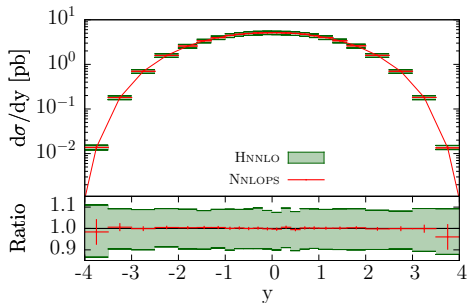


Comparison with existing approaches: MiNLO NNLO+PS.

► Hj -MiNLO NNLO+PS results

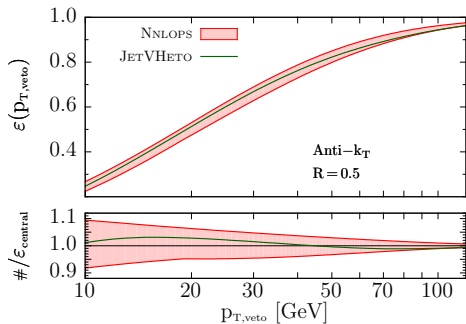


[Hamilton,Nason,Re,Zanderighi 1309.0017]

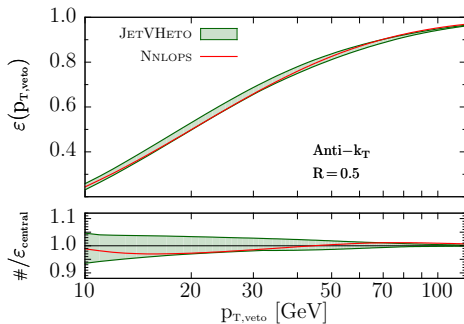


Comparison with existing approaches: MiNLO NNLO+PS.

► Hj -MiNLO NNLO+PS results

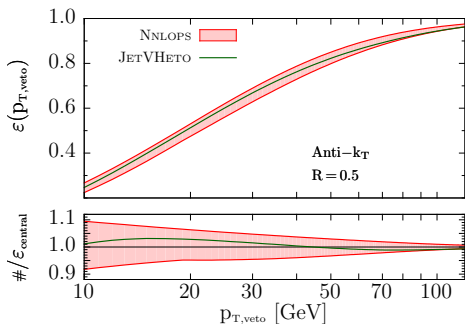


[Hamilton,Nason,Re,Zanderighi 1309.0017]

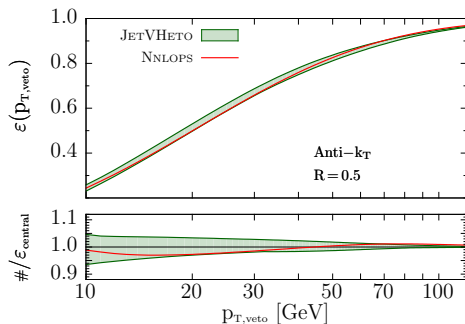


Comparison with existing approaches: MiNLO NNLO+PS.

► H_j -MiNLO NNLO+PS results



[Hamilton,Nason,Re,Zanderighi 1309.0017]

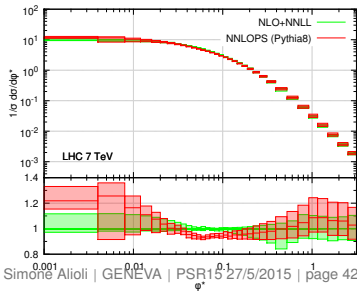
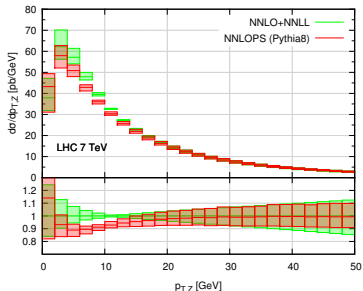
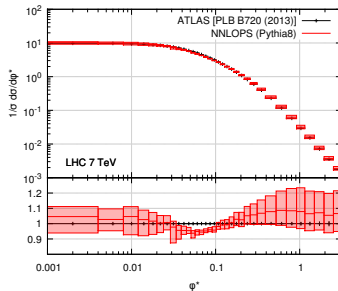
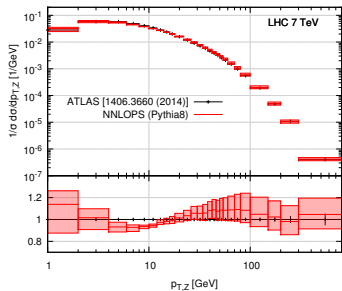


- We have re-derived MiNLO NNLO+PS formula as a check of our framework. It follows directly with a specific choice of splitting functions.
- Alternative choice of splitting functions proposed in [1311.0286] has pros and cons:
 - ✓ No need to know NLL resummation for NNLO+PS
 - ✓ No need to reweight after generation
 - ✗ Can't just simply run NNLO code as is . . .

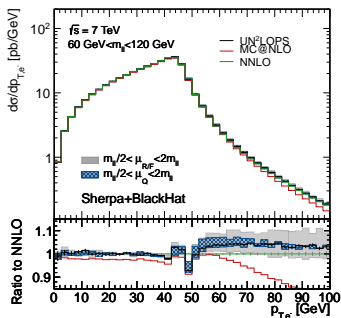
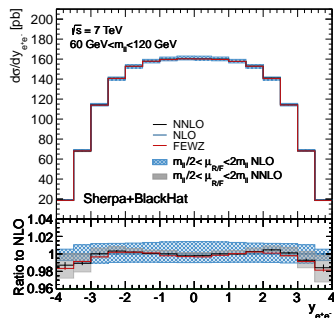


Comparison with existing approaches: MiNLO NNLO+PS.

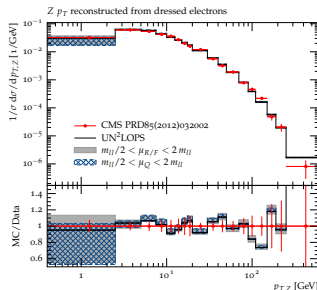
- ▶ Also available for Z production [Karlberg et al. 1407.2949]



Comparison with existing approaches: UNNLOPS.



- ▶ Recent results from SHERPA+BlackHat [1405.3607]
- ▶ Uses q_T -subtraction for zero jet bin (phase-space slicing)
- ▶ NNLO accuracy is maintained via UNNLOPS approach, basically enforcing spectrum is derivative of the cumulant via unitarity



N-jettiness subtractions

- ▶ Basic idea very much resemble q_T -subtraction. Divide phase space into NNLO $_N$ and NLO $_{N+1}$, only apply extra subtraction to NNLO $_N$.
- ▶ N-jettiness more powerful than q_T of the colorless system (or massive colored system). Any number of massless leg could in principle be dealt with.
- ▶ Simplest approach is to just use slicing. This amounts to approximate the α_S^2 terms by their singular counterpart, neglecting α_S^2 non-singular
- ▶ First example of N-jettiness like slicing $\tau = (p_b + p_X)^2/m_t^2$ in top-decay Gao et al. [1210.2808]
- ▶ 1-jettiness slicing recently applied to $W + 1$ -jet and $H + 1$ -jet production. Boughezal et al. [1504.02131, 1505.03893].
- ▶ Proper subtraction requires instead to use the singular to regulate the (integrated) divergencies left over by the NLO subtraction (as done in q_T -subtraction).

$$\begin{aligned}\sigma(X) &= \sigma^s(X, \mathcal{T}_{\text{off}}) + \int_{\mathcal{T}_\delta} d\mathcal{T}_N \left[\frac{d\sigma(X)}{d\mathcal{T}_N} - \frac{d\sigma^s(X)}{d\mathcal{T}_N} \theta(\mathcal{T}_N < \mathcal{T}_{\text{off}}) \right] + \mathcal{O}(\delta_{\text{IR}}) \\ &= \sigma^s(X, \mathcal{T}_{\text{off}}) + \int_{\mathcal{T}_\delta}^{\mathcal{T}_{\text{off}}} d\mathcal{T}_N \frac{d\sigma^{\text{non-s}}(X)}{d\mathcal{T}_N} + \int_{\mathcal{T}_{\text{off}}} \frac{d\sigma(X)}{d\mathcal{T}_N} + \mathcal{O}(\delta_{\text{IR}}).\end{aligned}$$

- ▶ Method used in GENEVA for NNLO results SA et al. [1311.0286].
- ▶ General method formalized in Gaunt et al. [1505.04794]. Also discussed how to make the subtraction more differential for better numerical stability.



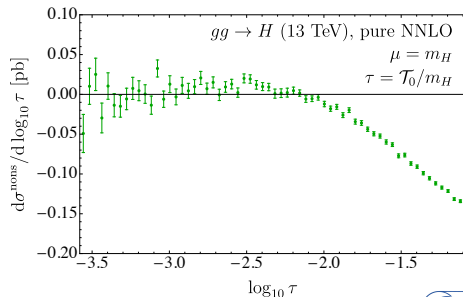
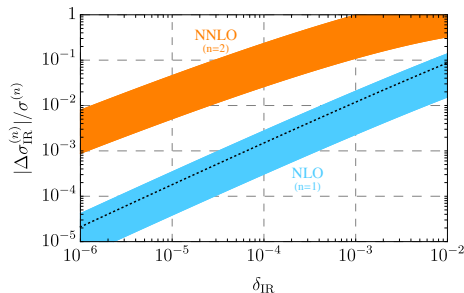
N-jettiness subtractions

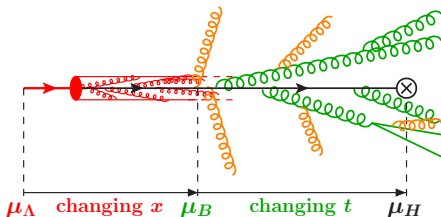
- ▶ The error can be estimated considering dominant missing non-singulars at $\mathcal{O}(\alpha_s)$ and $\mathcal{O}(\alpha_s^2)$ go as

$$\Delta\sigma^{(1)}(\delta_{IR})/\sigma^{(1)} \approx c \delta_{IR} \log \delta_{IR}$$

$$\Delta\sigma^{(2)}(\delta_{IR})/\sigma^{(2)} \approx c \delta_{IR} \log^3 \delta_{IR}$$

- ▶ When $\sigma^{(2)}$ is small, a larger $\Delta\sigma^{(2)}(\delta_{IR})$ could be tolerated.
- ▶ In any case, the correct behaviour of the non-singular towards zero should always be checked.
- ▶ This results from very delicate cancellations between 2 divergent quantities $\sigma(\tau) - \sigma^{\text{sing.}}(\tau)$, so their ratio going to 1 does not necessarily imply $\sigma^{\text{non-sing.}}(\tau)$ being zero.





- ▶ **Beam** functions are perturbative objects, connected to **PDF** via OPE in SCET

$$B_i(t, x; \mu_B) = \sum_k \int_x^1 \frac{d\xi}{\xi} \mathcal{I}_{ik}(t, \frac{x}{\xi}; \mu_B) f_k(\xi; \mu_B)$$

- ▶ Calculating these integral on-the-fly is computationally intensive
- ▶ We have prepared interpolation grids for all convolutions, will distribute them independently from GENEVA
- ▶ These grids are essentially LHAPDF6 grids, we use the LHAPDF6 log-bicubic interpolator to get the values on-the-fly

Beam Functions

- ▶ **Beam** functions are perturbative objects, connected to **PDF** via OPE in SCET

$$B_i(t, x; \mu_B) = \sum_k \int_x^1 \frac{d\xi}{\xi} \mathcal{I}_{ik}(t, \frac{x}{\xi}; \mu_B) f_k(\xi; \mu_B)$$

- ▶ Calculating these integral on-the-fly is computationally intensive
- ▶ We have prepared interpolation grids for all convolutions, will distribute them independently from GENEVA
- ▶ These grids are essentially LHAPDF6 grids, we use the LHAPDF6 log-bicubic interpolator to get the values on-the-fly
- ▶ Results have been validated against direct integration, e.g. CT10NNLO $P_{gg} \otimes g$

