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Comparison of sea-quark contributions to electromagnetic and axial form factors

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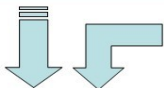
OUTLINE

- Perturbative chiral quark model
- EM and axial form factors
- Sea-quark contributions
- Summary & Outlook

Perturbative chiral quark model (PCQM)

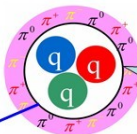
PRD22 2838(1980); NPA426 456(1984); PLB229 333(1989);PRC64 065203(2001); PRD63 054026(2001);

MIT bag model



Chiral symmetry: meson cloud

Cloudy bag model



including interaction of confined quarks with the pion fields on the bag surface

unphysical sharp bag boundary



Static quark potential

Effective Lagrangian of the PCQM

$$\begin{aligned}
 \mathcal{L}_{\text{inv}}(x) = & \underbrace{\bar{\psi}(x)[i\cancel{\partial} - \gamma^0 \mathbf{V}(\mathbf{r})]\psi(x)}_{\mathcal{L}_q} + \underbrace{\frac{F^2}{4} \text{Tr}[\partial_\mu U \partial^\mu U^\dagger]}_{\mathcal{L}_\Phi} \\
 & - \underbrace{\bar{\psi}(x) \mathbf{S}(\mathbf{r}) \left[\frac{U + U^\dagger}{2} + \gamma^5 \frac{U - U^\dagger}{2} \right] \psi(x)}_{\mathcal{L}_{\text{int}}}
 \end{aligned}$$

- Model potential

$\mathbf{V}(\mathbf{r})$: vector potential, $\mathbf{S}(\mathbf{r})$: scalar potential.

- Model parameter

$F = 88 \text{ MeV}$.

- In SU(3) flavor symmetry

$$\text{q - field : } \psi(x) = \begin{pmatrix} u(x) \\ d(x) \\ s(x) \end{pmatrix}, \quad \chi \text{ - field : } U = \exp \left[i \frac{\hat{\Phi}}{F} \right] \simeq 1 + i \frac{\hat{\Phi}}{F} + o \left(\frac{\hat{\Phi}}{F} \right),$$

$$\text{meson field : } \hat{\Phi} = \sum_{i=1}^8 \Phi_i \lambda_i = \begin{pmatrix} \pi^0 + \frac{1}{\sqrt{3}}\eta & \sqrt{2}\pi^+ & \sqrt{2}K^+ \\ \sqrt{2}\pi^- & -\pi^0 + \frac{1}{\sqrt{3}}\eta & \sqrt{2}K^0 \\ \sqrt{2}K^- & \sqrt{2}\bar{K}^0 & -\frac{2}{\sqrt{3}}\eta \end{pmatrix}.$$

Chiral symmetry

$\mathcal{L}_{\text{inv}}(x)$ is invariant under transformation

$$\psi_L \rightarrow U_L \psi_L$$

$$\psi_R \rightarrow U_R \psi_R$$

$$U \rightarrow U_R U U_L^\dagger$$

where

$$\psi_{L/R} = \frac{1}{2}(1 \mp \gamma^5)\psi$$

$$U_L = \exp\left(-i \sum_{a=1}^8 \Theta_a^L \frac{\lambda_a}{2}\right)$$

$$U_R = \exp\left(-i \sum_{a=1}^8 \Theta_a^R \frac{\lambda_a}{2}\right)$$

Previous works

PRC**64** 065203(2001); PRD**63** 054026(2001); PLB**520** 204(2001); PRC**65** 025202(2002); PRC**66** 055204(2002); PRC**68** 015205(2003); EPJA**20** 317(2004); JPG**30** 793(2004); JPG**35** 025005(2008).

- electromagnetic properties of baryons
- low-energy meson-baryon scattering
- strange nucleon form factors
- electromagnetic excitation of nucleon resonances
- axial form factor of the nucleon
-

Quark Wavefunction

- The radial parts $g(r)$ and $f(r)$ are expanded in Sturmian basis

$$g(r) = \sum_n A_n \frac{S_{n0}(r)}{r},$$
$$f(r) = \sum_n B_n S_{n0}(r),$$

where Sturmian functions

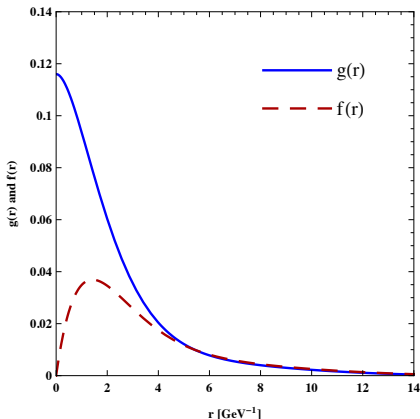
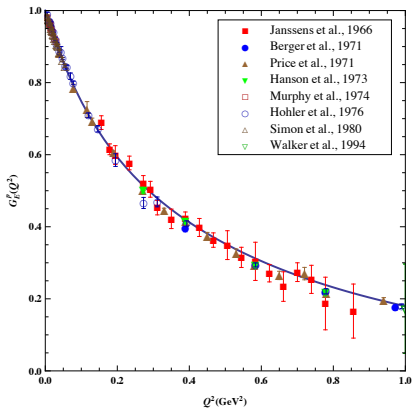
$$S_{nl} = \left[\frac{n!}{(n+2l+1)!} \right]^{1/2} (2br)^{l+1} e^{-br} L_n^{2l+1}(2br),$$

A_n , B_n , and b are free expansion parameters.

- Quark WF will be determined by fitting theoretical results of p charge form factor to the experimental data.

Quark wavefunctions

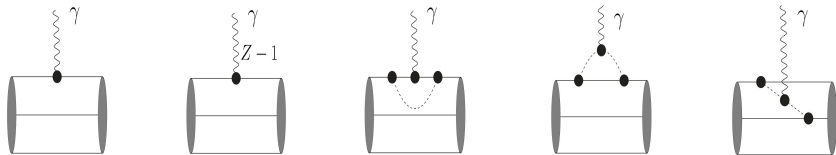
X. Y. Liu *et al*, J. Phys. G: Nucl. Part. Phys. **41** (2014) 055008.



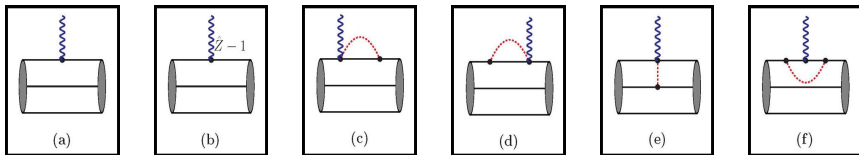
- 5-term ($n=5$), by fitting with experimental data of $G_E^p(Q^2)$

Feynman Diagrams

- Diagrams contributing to EM form factor

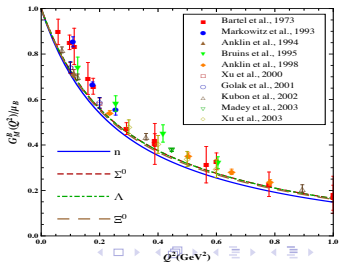
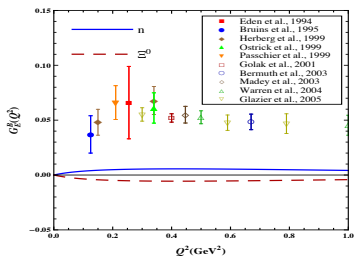
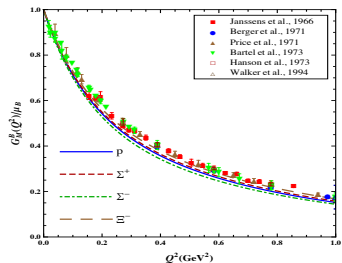
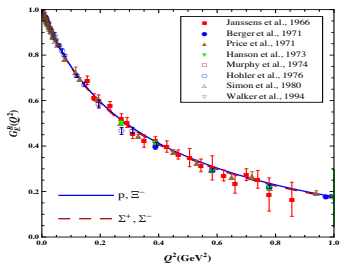


- Diagrams contributing to axial form factor



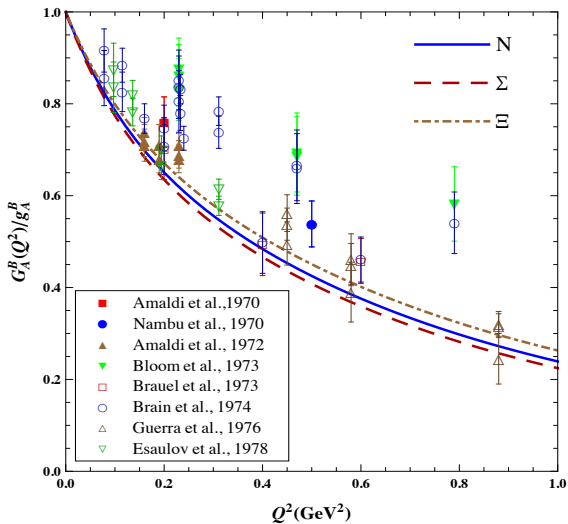
Electromagnetic form factors

X. Y. Liu *et al*, J. Phys. G: Nucl. Part. Phys. **41** (2014) 055008.

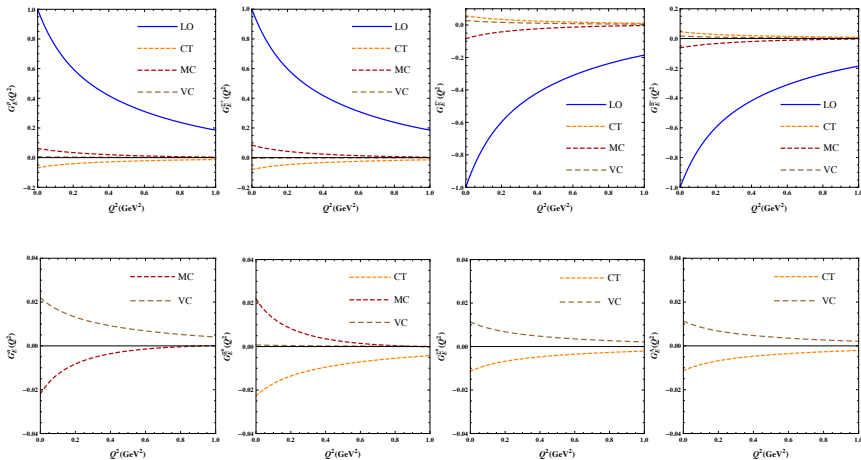


Axial form factors

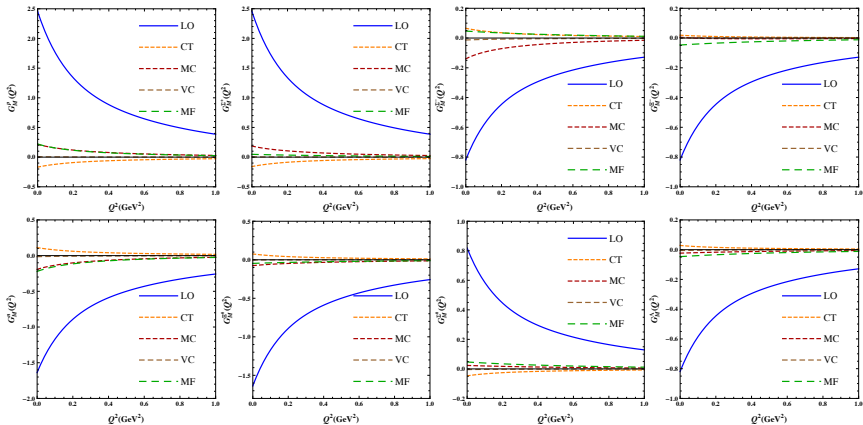
X. Y. Liu *et al*, Phys. Rev. D **91** (2015) 034022.



The individual contributions of charge form factors



The individual contributions of magnetic form factors



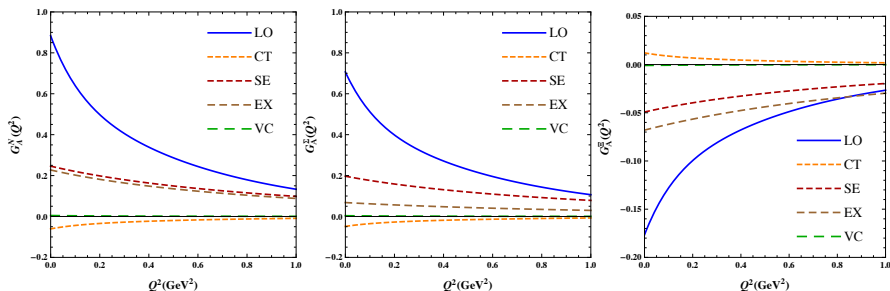
- Meson cloud contributing to EM form factors is less than 10%.
- The LO diagram results in a dipole-like form factor.
- The meson cloud leads to a flat contribution to EM form factor.

π , K and η mesons contribute to the μ_B

	Meson loops		
	π	K	η
μ_p	0.281	0.002	-0.006
μ_n	-0.339	0.018	0.004
μ_{Σ^+}	0.032	0.055	-0.008
μ_{Σ^0}	-0.039	-0.062	-0.004
μ_{Σ^-}	-0.109	0.068	0
μ_{Λ}	0	-0.052	0.004
μ_{Ξ^0}	-0.008	-0.055	0.012
μ_{Ξ^-}	-0.027	-0.058	0.010

- π -meson dominates nucleon magnetic moments.
- K -meson contributions to hyperons are in the same order.
- η -meson contributions are negligible.

The individual contributions of axial form factors



- Meson cloud contributing to axial form factor is about 30%
- The LO diagram results in a dipole-like form factor
- The meson cloud leads to a flat contribution to axial form factor

π , K and η mesons contribute to the g_A^B

	Meson loops		
	π	K	η
g_A^N	0.375	0.045	-0.002
g_A^Σ	0.118	0.104	-0.002
g_A^Ξ	-0.030	-0.077	-0.001

- π -meson dominates nucleon axial charges.
- K -meson contributions to hyperons axial charges are in the same order as the π ones.
- η -meson contributions are negligible.

Summary

- Sea-quark contributions to EM form factors are about 10%.
- Sea-quark contributions to axial form factors are about 30%.
- π meson dominates the contribution of nucleon form factor, K meson has a considerable contribution to the form factors of hyperons while η meson contribution is suppressed.

Outlook

- The flat meson contributions may indicate the sea-quark distribute mainly in a very small region.
The form factor distribution in r -space could be obtained by inverse Fourier transform as

$$\rho(r) = \frac{1}{(2\pi)^3} \int F(q^2) e^{iqr} d^3q.$$

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