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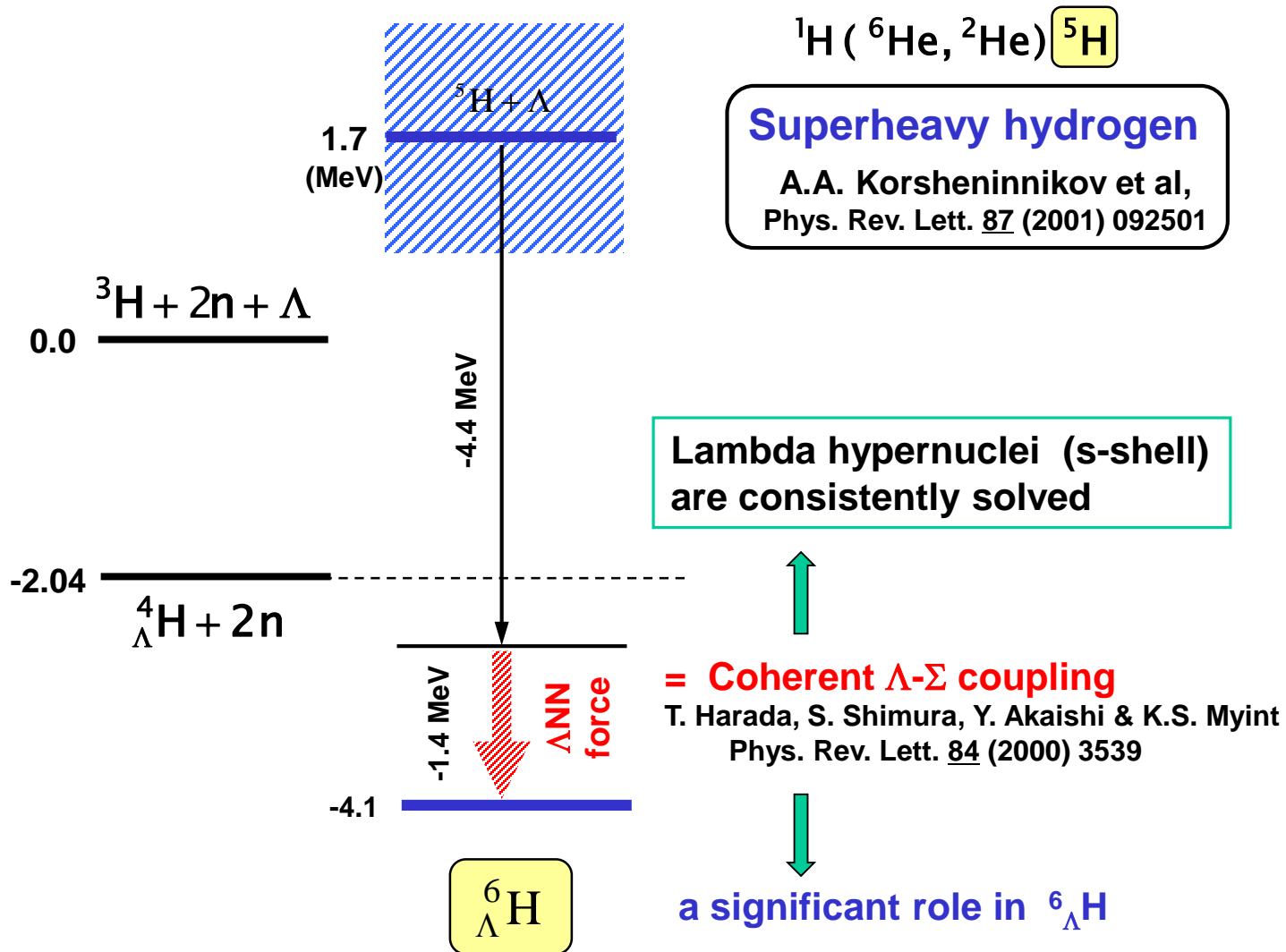
Analysis of Heavy Hyperhydrogen ${}^6_{\Lambda}H$

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Our Previous Work



“Hyperheavy hydrogen”

Our Group
 Prog. Theor. Phys. Suppl. 146 (2002) 599

More than ten years before
 the experimental observation

✚ Structure of p-shell hypernuclei, ${}_{\Lambda}^6\text{H}(0^+)$ ground state and

${}_{\Lambda}^6\text{H}(1^+)$ excited state by using **Brueckner-Hartree-Fock** method

Spin-isospin weight

Projection operator, $P_{\text{YN}}^+(S, T)P_{\text{YN}}(S, T)$

Λ -channel (I)

$$|I\rangle = |{}_{\Lambda}^6\text{H}\rangle_{00} = \sqrt{\frac{1}{2}} \Lambda_{\uparrow}^+ p_{\downarrow}^+ n_{\uparrow}^+ n_{\downarrow}^+ v^+ |0\rangle - \sqrt{\frac{1}{2}} \Lambda_{\downarrow}^+ p_{\uparrow}^+ n_{\uparrow}^+ n_{\downarrow}^+ v^+ |0\rangle$$

Σ -channel (II)

$$v^+ = \sqrt{\frac{1}{2}} \left\{ n_{3/2}^+ n_{-3/2}^+ - n_{1/2}^+ n_{-1/2}^+ \right\}$$

$$|II\rangle = |{}_{\Sigma}^6\text{H}\rangle_{00} = \sqrt{\frac{1}{6}} \Sigma_{\uparrow}^{0+} p_{\downarrow}^+ n_{\uparrow}^+ n_{\downarrow}^+ v^+ |0\rangle - \sqrt{\frac{1}{6}} \Sigma_{\downarrow}^{0+} p_{\uparrow}^+ n_{\uparrow}^+ n_{\downarrow}^+ v^+ |0\rangle + \sqrt{\frac{1}{3}} \Sigma_{\uparrow}^{-+} p_{\uparrow}^+ p_{\downarrow}^+ n_{\downarrow}^+ v^+ |0\rangle - \sqrt{\frac{1}{3}} \Sigma_{\downarrow}^{-+} p_{\uparrow}^+ p_{\downarrow}^+ n_{\uparrow}^+ v^+ |0\rangle$$

Spin-isospin weight of YN interactions

$$\langle V_{ij} \rangle = \sum_{i,j} \langle i | P_{ij}^+(S, T) P_{ij}(S, T) V_{ij}(S, T) | j \rangle \quad \mathbf{i, j=I, II}$$

Spin-isospin weights of ΥN interaction in s-shell

 ${}^6_{\Lambda} \text{H}(0^+)$
 ${}^6_{\Lambda} \text{H}(1^+)$

| | S=0,T=1/2 | S=0,T=3/2 | S=1,T=1/2 | S=1,T=3/2 | | S=0,T=1/2 | S=0,T=3/2 | S=1,T=1/2 | S=1,T=3/2 |
|---------------------------|----------------|---------------|---------------|-----------|---------------------------|---------------|-----------|---------------|---------------|
| $V_{\Lambda N-\Lambda N}$ | $\frac{3}{2}$ | 0 | $\frac{3}{2}$ | 0 | $V_{\Lambda N-\Lambda N}$ | $\frac{1}{2}$ | 0 | $\frac{5}{2}$ | 0 |
| $V_{\Sigma N-\Sigma N}$ | $\frac{1}{6}$ | $\frac{4}{3}$ | $\frac{3}{2}$ | 0 | $V_{\Sigma N-\Sigma N}$ | $\frac{1}{2}$ | 0 | $\frac{7}{6}$ | $\frac{4}{3}$ |
| $V_{\Sigma N-\Lambda N}$ | $-\frac{1}{2}$ | 0 | $\frac{3}{2}$ | 0 | $V_{\Sigma N-\Lambda N}$ | $\frac{1}{2}$ | 0 | $\frac{1}{2}$ | 0 |

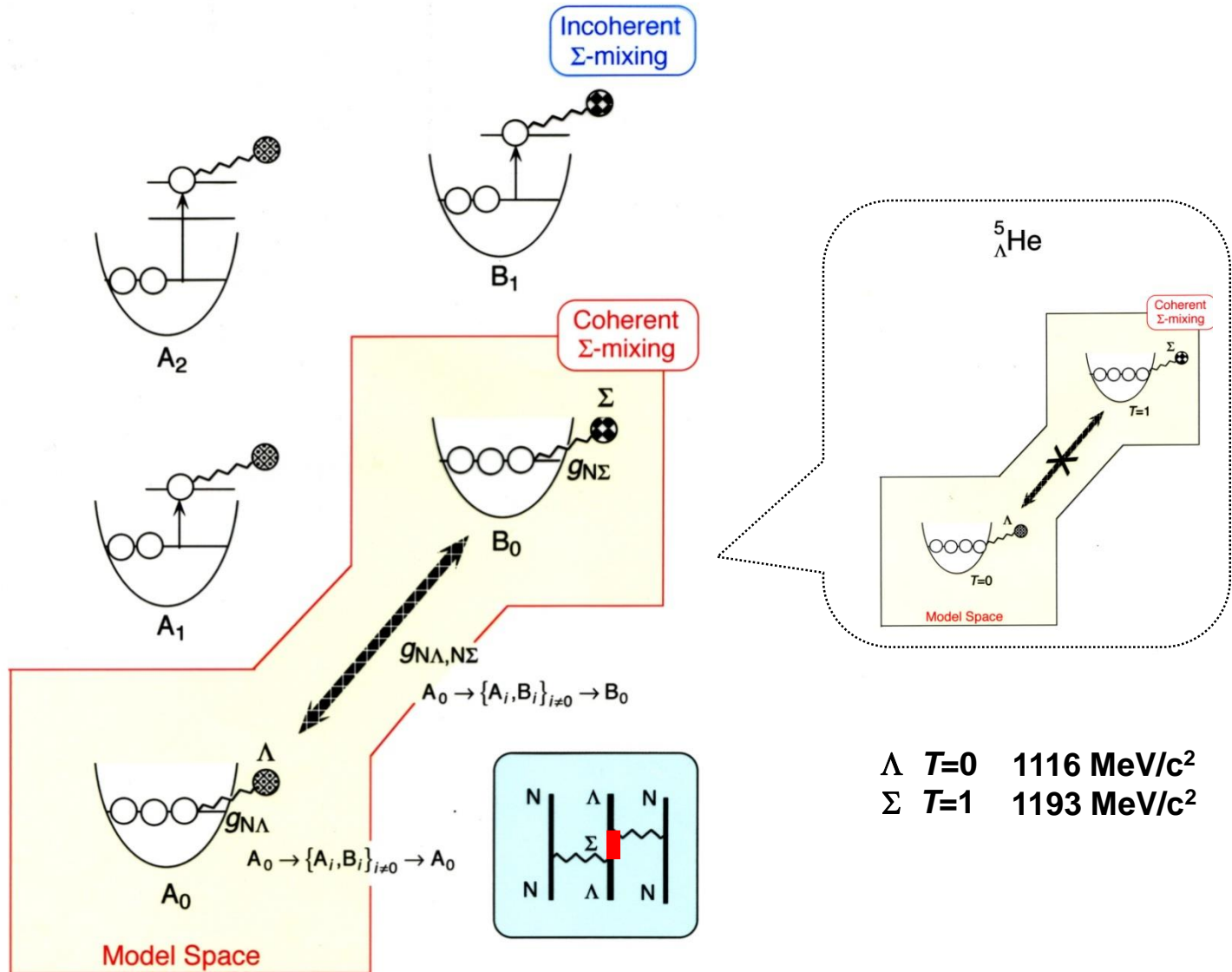
In ${}^6_{\Lambda} \text{H}(0^+)$ state, $V_{\Sigma N-\Lambda N} = 3/2$ and In ${}^6_{\Lambda} \text{H}(1^+)$ state, $V_{\Sigma N-\Lambda N} = 1/2$

❖ Λ - Σ coupling effect in ${}^6_{\Lambda} \text{H}(0^+)$ is about 3^2 times larger than that of ${}^6_{\Lambda} \text{H}(1^+)$ state.

Spin-isospin weights of YN interaction in p-shell

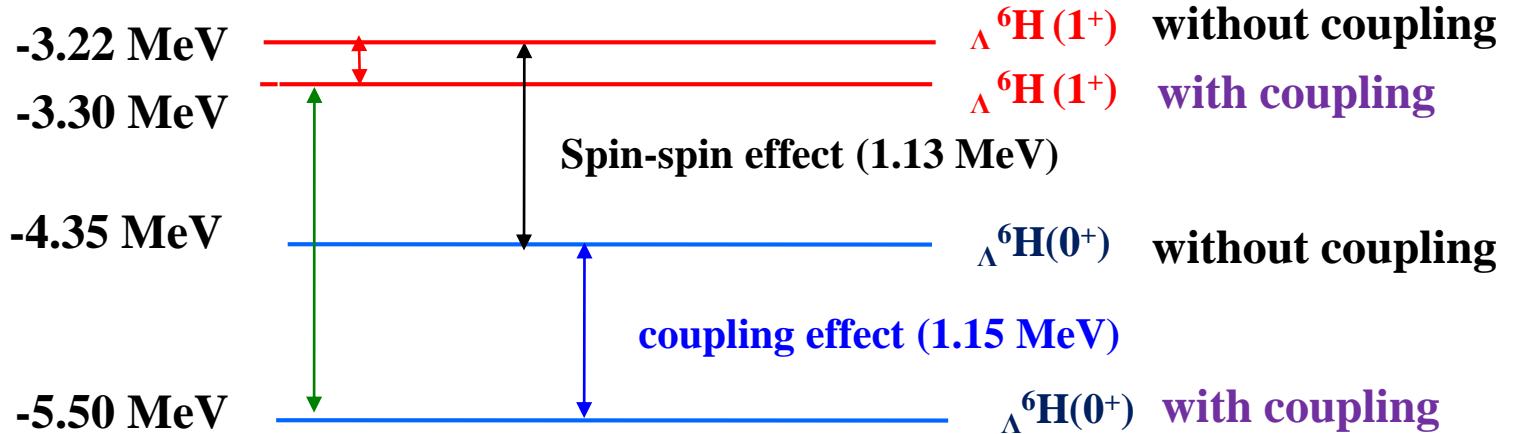
| | $S=0, T=\frac{1}{2}$ | $S=0, T=\frac{3}{2}$ | $S=1, T=\frac{1}{2}$ | $S=1, T=\frac{3}{2}$ |
|---------------------------|----------------------|----------------------|----------------------|----------------------|
| $V_{\Lambda N-\Lambda N}$ | $\frac{1}{4}$ | 0 | $\frac{3}{4}$ | 0 |
| $V_{\Sigma N-\Sigma N}$ | $\frac{1}{36}$ | $\frac{2}{9}$ | $\frac{1}{12}$ | $\frac{2}{3}$ |
| $V_{\Sigma N-\Lambda N}$ | $\frac{1}{12}$ | 0 | $\frac{1}{4}$ | 0 |

Coherent Λ - Σ coupling



0 MeV ————— $\Lambda^+{}^5\text{H}$

coupling effect (0.08 MeV)



Energy levels for $\Lambda^6\text{H}(0^+)$ and $\Lambda^6\text{H}(1^+)$

Level splitting = spin-spin effect + coupling effect

(2.20 MeV) (1.13 MeV) + (1.07 MeV)

The coupling effect is significant in $\Lambda^6\text{H}$ system.

➤ By using Brueckner-Hartree-Fock method with Shinmura's Y-N interactions which are phase shift equivalent potential of Nijmegen model NSC97f(S).

$$V_{t(nn)} = -13.3 \text{ MeV exp} \left\{ - \left(\frac{r}{2.2 \text{ fm}} \right)^2 \right\}$$

$$E = -0.35 \text{ MeV}$$

$$V_{t\Lambda} = -45.4 \text{ MeV exp} \left\{ - \left(\frac{r}{1.53 \text{ fm}} \right)^2 \right\}$$

$$E = -2.4 \text{ MeV}$$

$$V_{(nn)\Lambda} = -11.5 \text{ MeV exp} \left\{ - \left(\frac{r}{1.8 \text{ fm}} \right)^2 \right\}$$

$$E_{t(nn)\Lambda} = -4.54 \text{ MeV}$$

Evidence for ${}^6_{\Lambda}\text{H}$

M. Agnello et al,
Nucl. Phys. A 881(2012) 269

$$V_{t(nn)} = -10.5 \text{ MeV exp} \left\{ - \left(\frac{r}{2.2 \text{ fm}} \right)^2 \right\}$$

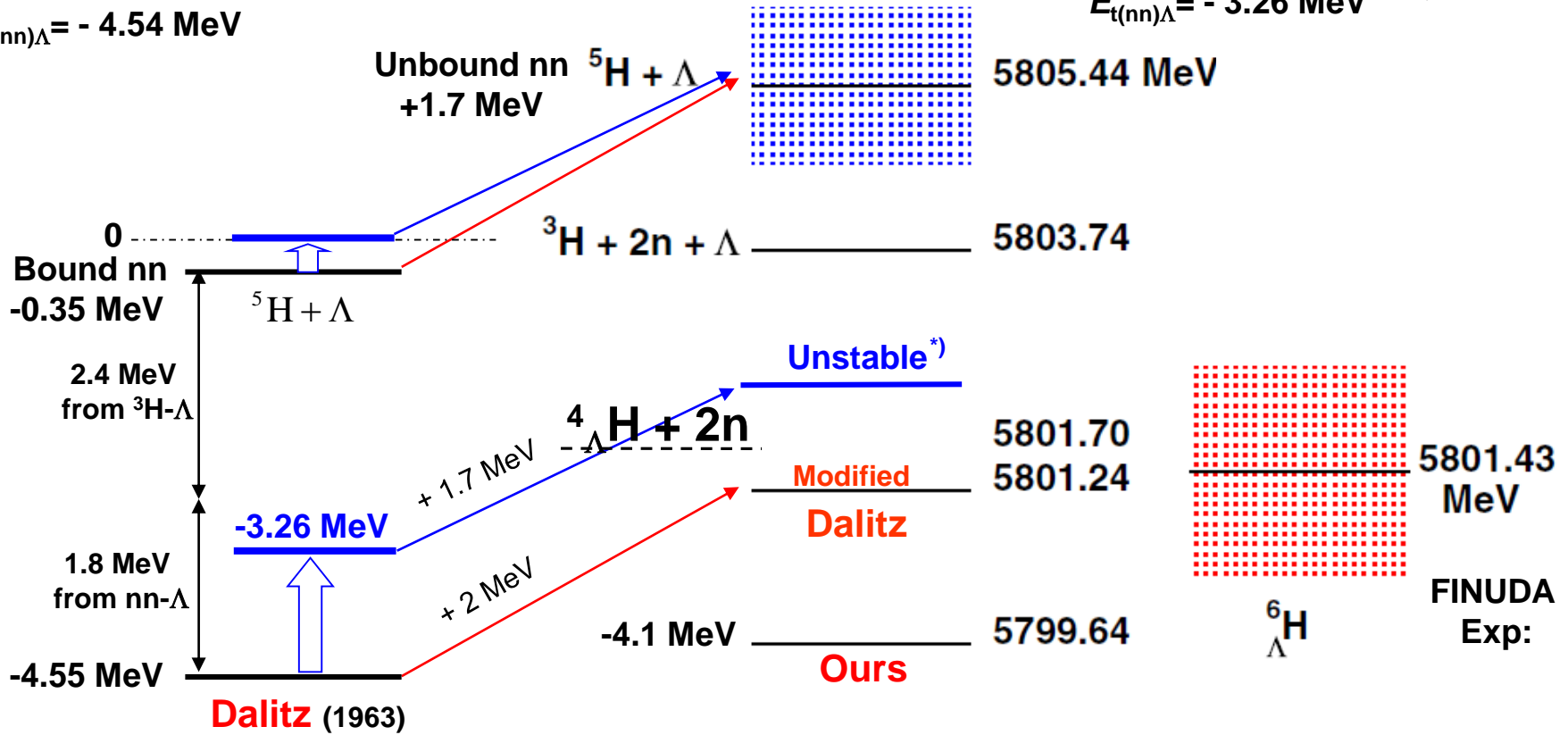
$$E = 0$$

$$V_{t\Lambda} = -43.8 \text{ MeV exp} \left\{ - \left(\frac{r}{1.53 \text{ fm}} \right)^2 \right\}$$

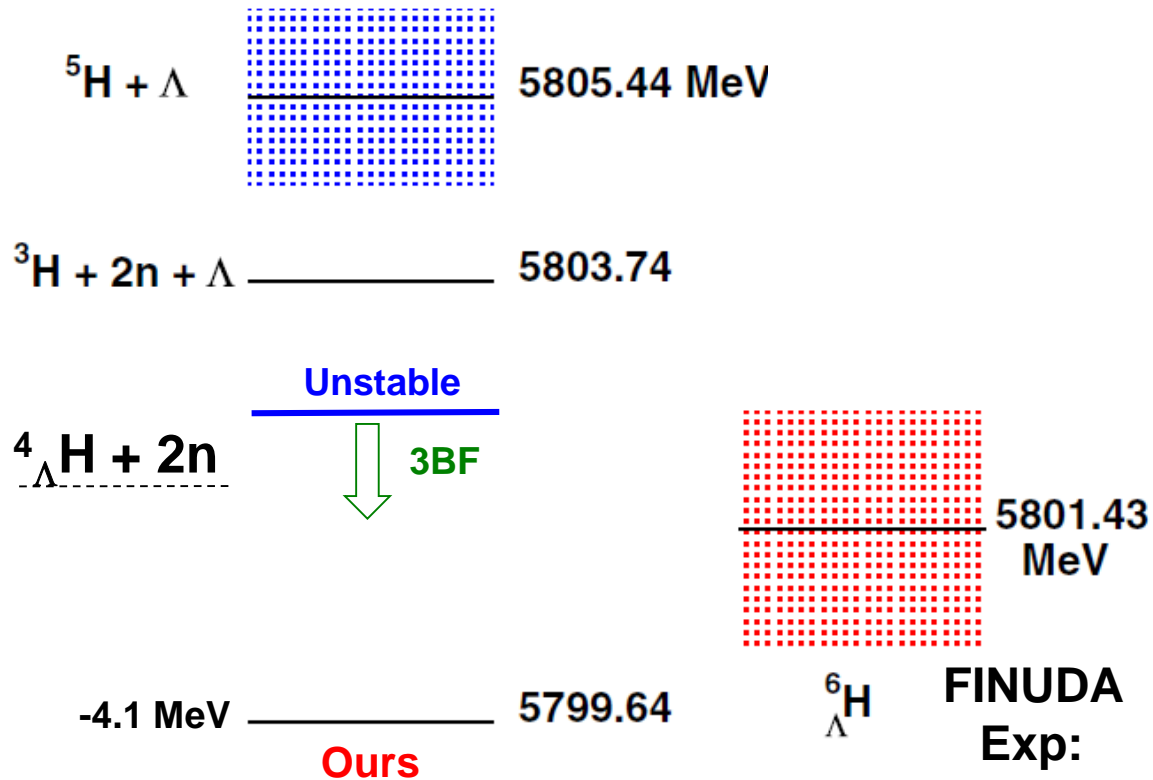
$$E = -2.04 \text{ MeV}$$

$$V_{(nn)\Lambda} = -11.5 \text{ MeV exp} \left\{ - \left(\frac{r}{1.8 \text{ fm}} \right)^2 \right\}$$

$$E_{t(nn)\Lambda} = -3.26 \text{ MeV}$$



*) This state comes above the threshold and cannot survive till weak decay.

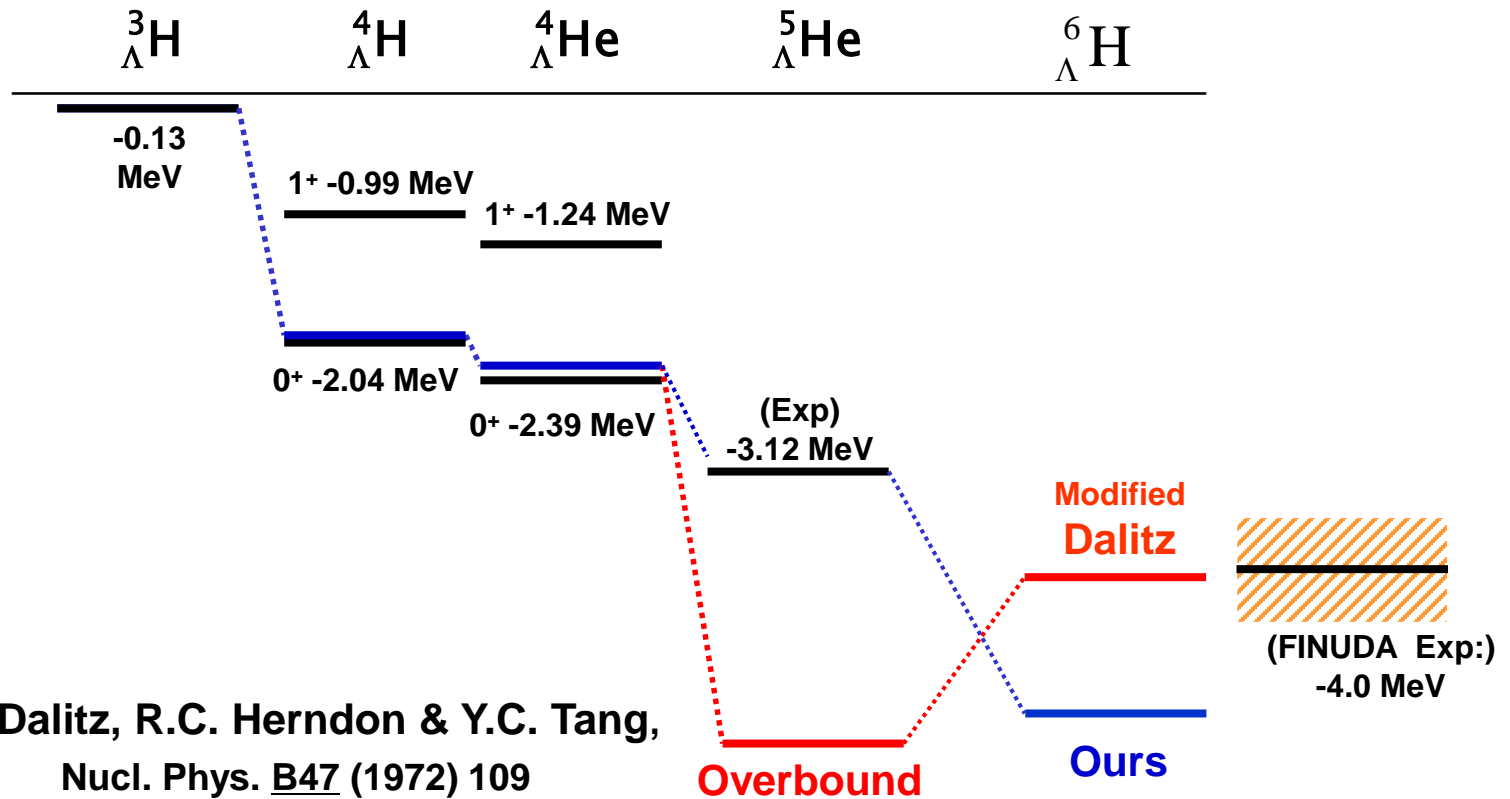


Thus, the coherent Λ - Σ coupling is necessitated.

J-PARC E-10 showed that there is no peak structure corresponding to the ${}^6_{\Lambda}\text{H}$

$$\sigma({}^6_{\Lambda}\text{H}) = 1.2 \text{ nb/sr at 90\% confidence level}$$

The overbinding problem



Conclusions

- **Significance of coherent Λ - Σ coupling**
- **Spin-spin is half and Λ - Σ coupling effect is half**
- **More experimental data are awaited**

Thank you very much

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