



# HADRON NUCLEAR PHYSICS 2015

*July 7- 11, 2015 @Krabi, Thailand*



มหาวิทยาลัยเทคโนโลยีสุรนารี  
Suranaree University of Technology

**Strangeness configurations of the  
proton for  $\phi$  meson production in  
 $p\bar{p}$  annihilation**

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# Outline

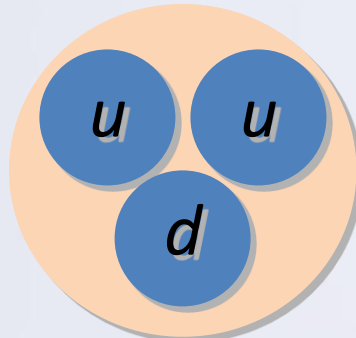
- Introduction
- Proton wave functions with pentaquark components
- The transition amplitude and the branching ratios for the reactions

$$p\bar{p} \rightarrow X\phi \quad (X = \pi^0, \eta, \rho, \omega)$$

- Summary and Conclusions

# 1. Introduction

Baryons being bound states of three quarks.



*proton*

*The proton might contain a substantial strange quark-antiquark component*

The apparent OZI rule violation  $\phi(s\bar{s})$  production nucleon-antinucleon annihilation reactions suggests the existence of strange quarks in the nucleon.

### Deep Inelastic Scattering

The non-zero strange spin of the proton

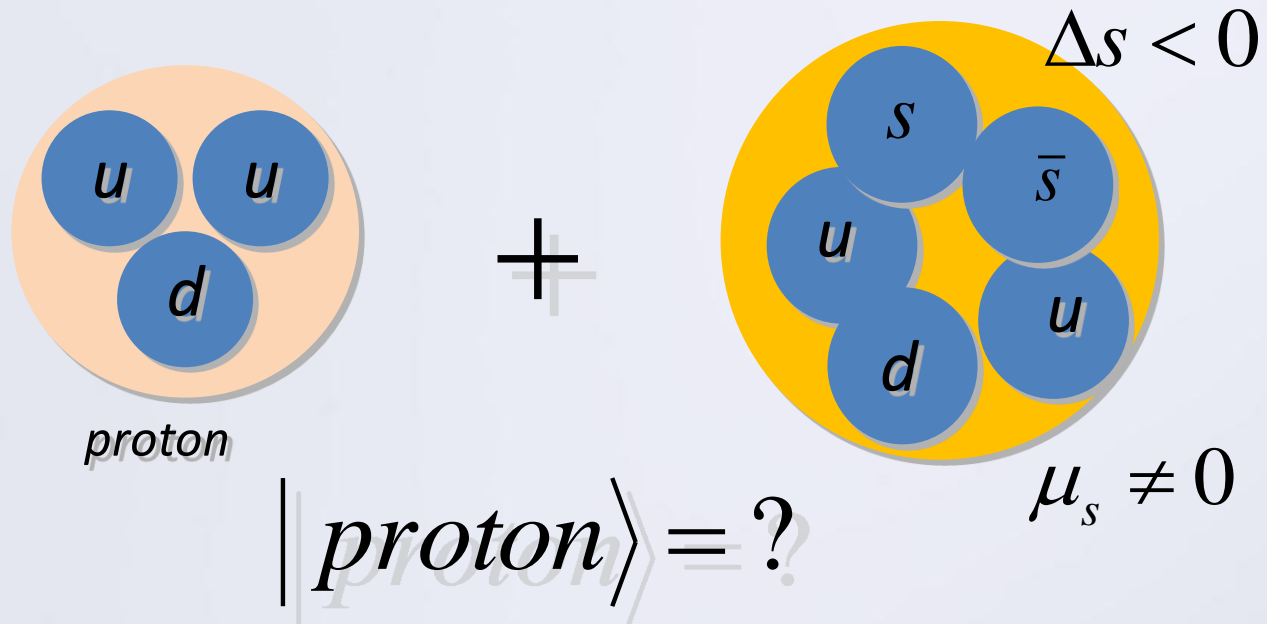
$$\Delta s = -0.10 \pm 0.03$$



The strangeness magnetic moment can be extrapolated from the strange magnetic form factor

$$G_M^S(Q=0) \equiv \mu_s \neq 0$$

The presence of  $uuds\bar{s}$  piece in the proton wave function.



Some experimental measurements suggest a positive value for  $\mu_s$

But most theoretical calculations of the proton derive a negative value for this observable !

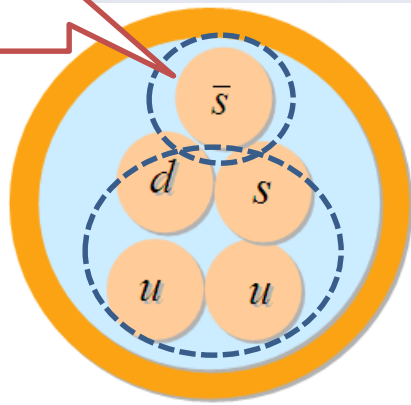
$$|p\rangle = A|uud\rangle + B|uuds\bar{s}\rangle \quad A^2 \gg B^2$$

PHYSICAL REVIEW C 73, 035207 (2006)

## Strangeness spin, magnetic moment, and strangeness configurations of the proton

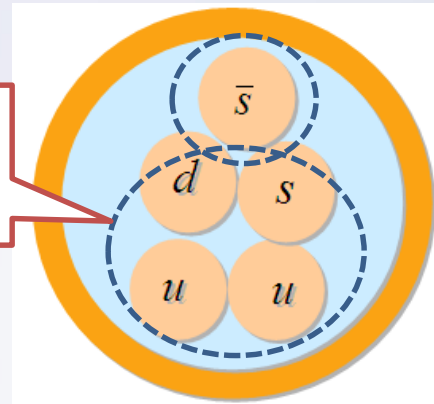
C. S. An,<sup>1,\*</sup> D. O. Riska,<sup>2,†</sup> and B. S. Zou<sup>1,3,‡</sup>

*P*-state

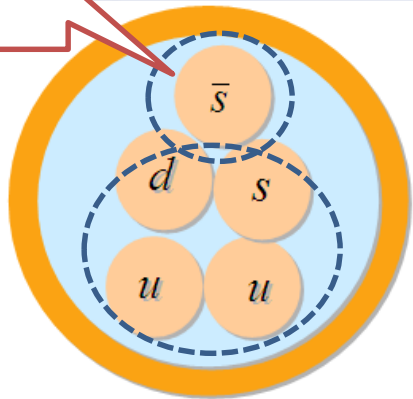


***pentaquark***

*P*-state



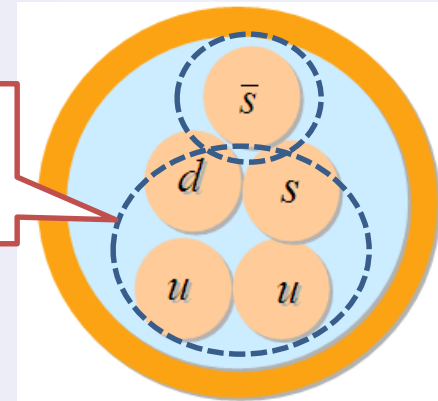
*P*-state



$$\Delta s < 0 \quad \mu_s < 0$$

***2 configurations***

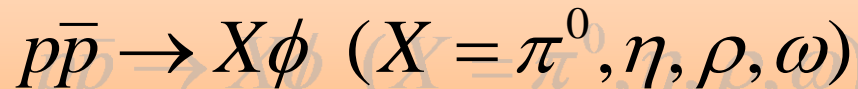
*P*-state



$$\Delta s < 0 \quad \mu_s > 0$$

***15 configurations!***

The branching ratios for the reactions



## 2. Proton wave functions with pentaquark components

$$|p\rangle = A|uud\rangle + B|uuds\bar{s}\rangle$$

$$|uuds\rangle \otimes |\bar{s}\rangle$$

*spatial*  $\otimes$  *spin*  $\otimes$  *flavor*  $\otimes$  *color*

$$S_{5q} = \frac{1}{2}$$

*proton*

color singlet

***P***-state

$$|\bar{s}\rangle, |uuds\rangle$$

$$|uuds\bar{s}\rangle$$

## color singlet

The color state of the antiquark in pentaquarks is a  $[11]$  antitriplet

$$\bar{s} \rightarrow [11]$$

$$uuds \equiv [211] \otimes \bar{s} \equiv [11] \rightarrow uuds\bar{s} \equiv [222]$$

color singlet

The color wave function of the four-quark configuration must be a  $[211]_3$  triplet

$$uuds \rightarrow [211]$$

$$\chi_{[211]_\lambda}^c(q^4) = \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & \\ \hline 4 & \\ \hline \end{array}$$

$$\chi_{[211]_\rho}^c(q^4) = \begin{array}{|c|c|} \hline 1 & 3 \\ \hline 2 & \\ \hline 4 & \\ \hline \end{array}$$

$$\chi_{[211]_\eta}^c(q^4) = \begin{array}{|c|c|} \hline 1 & 4 \\ \hline 2 & \\ \hline 3 & \\ \hline \end{array}$$

The color wave functions can be derived by applying the  $\lambda$ ,  $\rho$ ,  $\eta$  type projection operators of the irreducible representation IR[211] of the permutation group  $S_4$  in Yamanouchi basis, onto single particle color states

$$\begin{aligned} \chi_{[211]_\lambda}^c(R) = & \frac{1}{\sqrt{16}}(2|RRGB\rangle - 2|RRBG\rangle \\ & -|GRRB\rangle - |RGRB\rangle - |BRGR\rangle - |RBGR\rangle \\ & +|BRRG\rangle + |GRBR\rangle + |RBRG\rangle + |RGBR\rangle) \end{aligned}$$

The corresponding singlet color wave function of the pentaquark at color symmetry pattern  $\lambda$ ,  $\rho$ ,  $\eta$  is given by

$$\chi_{[222]_j}^C = \frac{1}{\sqrt{3}} \left[ \chi_{[211]_j}^c(R) \bar{R} + \chi_{[211]_j}^c(G) \bar{G} + \chi_{[211]_j}^c(B) \bar{B} \right]$$

The total wave function of the four quark configuration is antisymmetric

$$|uuds\rangle^{OSFC} \rightarrow [1111]$$

the spatial-spin-flavor part must be a [31] state

$$\begin{array}{|c|c|} \hline & \\ \hline & \\ \hline & \\ \hline \end{array}
 \text{ color } [211]
 \quad \otimes \quad
 \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}
 \text{ spatial-flavor-spin } [31]$$

$$\psi_{[1111]} = \sum_{i,j=\lambda,\rho,\eta} a_{ij} \chi_{[211]_i}^c \chi_{[31]_j}^{osf}$$

Applying the IR[31] and IR[211] of the permutation group  $S_4$  in Yamanouchi basis

$$\psi_{[1111]} = \frac{1}{\sqrt{3}} \left( \chi_{[211]_\lambda}^c \chi_{[31]_\rho}^{osf} - \chi_{[211]_\rho}^c \chi_{[31]_\lambda}^{osf} + \chi_{[211]_\eta}^c \chi_{[31]_\eta}^{osf} \right)$$

$$\psi_{[1111]} = \frac{1}{\sqrt{3}} \left( \chi_{[211]_\lambda}^c \chi_{[31]_\rho}^{osf} - \chi_{[211]_\rho}^c \chi_{[31]_\lambda}^{osf} + \chi_{[211]_\eta}^c \chi_{[31]_\eta}^{osf} \right)$$

The spatial-spin-flavor of the  $q^4$

$$\chi_{[31]}^{osf} = \sum_{i,j} a_{ij} \chi_{[X]_i}^o \chi_{[Y]_j}^{sf}$$

$$\chi_{[Z]}^{sf} = \sum_{i,j} a_{ij} \chi_{[X]_i}^f \chi_{[Y]_j}^s$$

The spin-flavor of the  $q^4$

$[31]_{OSF}$	
$[4]_O$	$[31]_{SF}$
$[1111]_O$	$[211]_{SF}$
$[22]_O$	$[31]_{SF}, [211]_{SF}$
$[211]_O$	$[31]_{SF}, [211]_{SF}, [22]_{SF}$
$[31]_O$	$[4]_{SF}, [31]_{SF}, [211]_{SF}, [22]_{SF}$

$[4]_{FS}$			
$[31]_{FS}$			
$[22]_{FS}$			
$[211]_{FS}$			
$[211]_F [22]_S$	$[211]_F [31]_S$	$[211]_F [4]_S$	$[22]_F [31]_S$
$[31]_F [22]_S$	$[31]_F [31]_S$		

*spin*

$$|[22]_s\rangle = |[22]_{s_1}\rangle, |[22]_{s_2}\rangle \quad \begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array} \quad \rightarrow \quad |[22]_{s_1}\rangle = \left[ \left[ \begin{array}{c} 1 \\ \frac{1}{2} \otimes \frac{1}{2} \\ 2 \end{array} \right]_0 \otimes \left[ \begin{array}{c} 3 \\ \frac{1}{2} \otimes \frac{1}{2} \\ 2 \end{array} \right]_0 \right]_0$$

*flavor*

$$\begin{array}{|c|c|} \hline 1 & 4 \\ \hline 2 & \\ \hline 3 & \\ \hline \end{array} \quad \rightarrow \quad |[211]_{F_1}\rangle = \frac{1}{\sqrt{24}} \{ 2uuds + 2uusd + 2dsuu + 2sduu \\ - duus - udus - sudu - usdu \\ - suud - dusu - usud - udsu \}$$

*spatial*

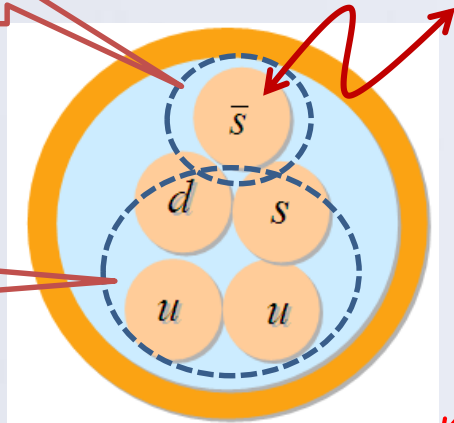
$[4]_O$  symmetry

$$\begin{array}{|c|c|c|c|} \hline 1 & 2 & 3 & 4 \\ \hline \end{array} \quad \rightarrow \quad \vec{\xi}_s = \frac{\vec{q}_2 + \vec{q}_3 + \vec{q}_4 + \vec{q}_5 - 4\vec{q}_1}{\sqrt{20}}$$

According to the requirement of positive parity for the proton wave function

P-state

$$\ell = 1 \Rightarrow P = (-1)^{\ell+1}$$



S-state

	$[31]_{OSF}$
$[4]_O$	$[31]_{SF}$
$[1111]_O$	$[211]_{SF}$
$[22]_O$	$[31]_{SF}, [211]_{SF}$
$[211]_O$	$[31]_{SF}, [211]_{SF}, [22]_{SF}$
$[31]_O$	$[4]_{SF}, [31]_{SF}, [211]_{SF}, [22]_{SF}$

the spatial part takes the  $[4]_O$  symmetry

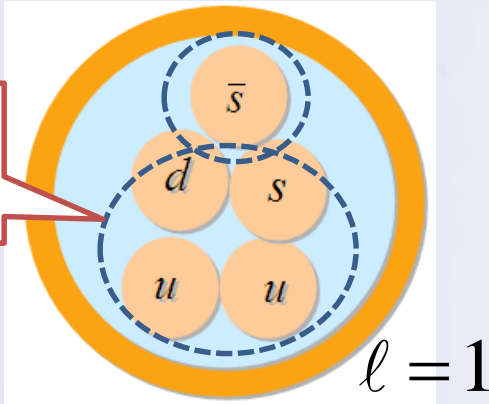
$[31]_{FS}$		
$[31]_F[22]_S$	$[31]_F[31]_S$	$[31]_F[4]_S$
$[211]_F[31]_S$	$[22]_F[31]_S$	$[4]_F[31]_S$

$$\Delta s < 0$$

$$\mu_s < 0$$

$$|uuds\bar{s}\rangle = [|\frac{1}{2}, m_{\bar{s}}\rangle \otimes |1, \mu\rangle]_{\frac{1}{2}, m_{5q}} \frac{1}{\sqrt{3}} (\chi_{[222]_{\lambda}}^C(\bar{s}\chi_{[31]_{\rho}}^{FS}) - \chi_{[222]_{\rho}}^C(\bar{s}\chi_{[31]_{\lambda}}^{FS}) + \chi_{[222]_{\eta}}^C(\bar{s}\chi_{[31]_{\eta}}^{FS}))$$

P-state



$[31]_{OSF}$	
$[4]_O$	$[31]_{SF}$
$[1111]_O$	$[211]_{SF}$
$[22]_O$	$[31]_{SF}, [211]_{SF}$
$[211]_O$	$[31]_{SF}, [211]_{SF}, [22]_{SF}$
$[31]_O$	$[4]_{SF}, [31]_{SF}, [211]_{SF}, [22]_{SF}$

the spatial wave function of the subsystem has the mixed symmetry  $[31]_O$

$$\psi_{uuds\bar{s}} = \sum_{J_{4q}} \left[ \left| \frac{1}{2}, m_{\bar{s}} \right\rangle \otimes \left[ \bar{s} \chi_{[31]_{S_{4q}, m_{4q}}}^{FS} (uuds) \otimes \chi_{\ell, \mu}^{OC} \right]_{J_{4q}, m_{4q}} \right]$$

orbital

1	3	4	$\vec{\xi}_\rho \Rightarrow Y_{1, \mu} \left( \frac{\vec{q}_1 - \vec{q}_2}{\sqrt{2}} \right)$
2			

1	2	4	$\vec{\xi}_\lambda \Rightarrow Y_{1, \mu} \left( \frac{\vec{q}_1 + \vec{q}_2 - 2\vec{q}_3}{\sqrt{6}} \right)$
3			

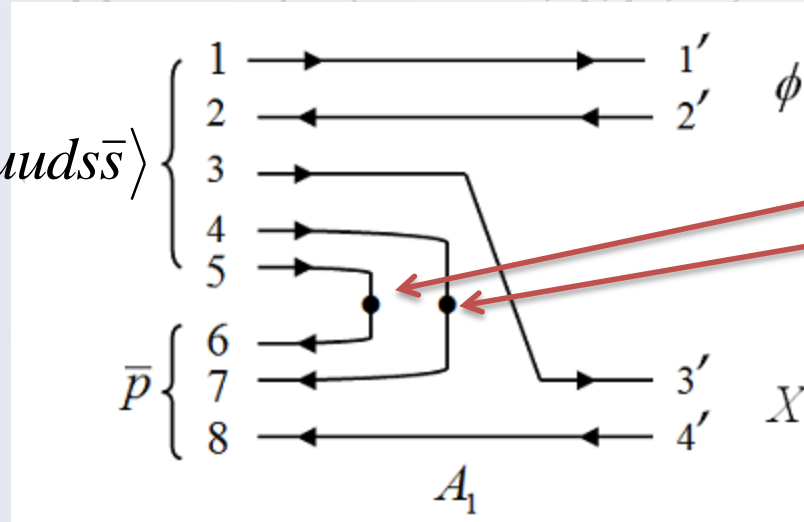
1	2	3	$\vec{\xi}_\eta \Rightarrow Y_{1, \mu} \left( \frac{\vec{q}_1 + \vec{q}_2 + \vec{q}_3 - 3\vec{q}_4}{\sqrt{12}} \right)$
4			

**15 configurations**  
 $\Delta s < 0 \quad \mu_s > 0$

# 3. The $p\bar{p}$ transition amplitude and branching ratios

$$p\bar{p} \rightarrow X\phi \quad (X = \pi^0, \eta, \rho, \omega)$$

$$|p\rangle = A|uud\rangle + B|uuds\bar{s}\rangle$$



${}^3P_0$

$$|\psi_{p\bar{p}}\rangle = |uuds\bar{s}\rangle \otimes |\bar{u}\bar{u}\bar{d}\rangle$$

$$T = \langle \psi_{\phi X} | \hat{O}_{A_1} | \psi_{p\bar{p}} \rangle$$

$$A^2 \gg B^2$$

$$T = 2AB \langle \phi X | \hat{O}_{A_1} | uuds\bar{s} \otimes \bar{u}\bar{u}\bar{d} \rangle$$

$T_{A_1}$

$$\langle \phi X | \hat{O} | uuds\bar{s} \otimes \bar{u}\bar{u}\bar{d} \rangle = T_{A_1} = \int d^3 q_1 \dots d^3 q_8 d^3 q'_1 \dots d^3 q'_4 \langle \phi X | \bar{q}'_1 \dots \bar{q}'_4 \rangle$$

$$\langle \bar{q}'_1 \dots \bar{q}'_4 | \hat{O}_{A_1} | \bar{q}_1 \dots \bar{q}_8 \rangle \langle \bar{q}_1 \dots \bar{q}_8 | (uuds\bar{s}) \otimes (\bar{u}\bar{u}\bar{d}) \rangle$$

The internal spatial wave functions are approximated as the harmonic oscillator forms

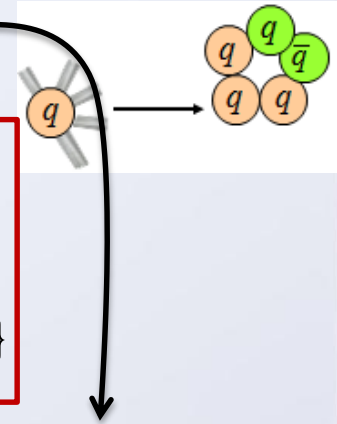
$$\langle uuds\bar{s} | \bar{q}_1 \dots \bar{q}_5 \rangle = \varphi_{uuds\bar{s}}(\bar{q}_1, \dots, \bar{q}_5) \psi_{uuds\bar{s}}$$

$$\varphi_{uuds\bar{s}}(\bar{q}_1, \dots, \bar{q}_5) = N_{uuds\bar{s}} \exp \left\{ -\frac{R_{5q}^2}{4} [(\bar{q}_2 - \bar{q}_3)^2 + \frac{1}{3}(\bar{q}_2 + \bar{q}_3 - 2\bar{q}_4)^2 + \frac{1}{6}(\bar{q}_2 + \bar{q}_3 + \bar{q}_4 - 3\bar{q}_5)^2 + (\frac{\bar{q}_2 + \bar{q}_3 + \bar{q}_4 + \bar{q}_5 - 4\bar{q}_1}{10})^2] \right\}$$

$$\psi_{uuds\bar{s}} = \sum_{J_{4q}} \left[ \left| \frac{1}{2}, m_{\bar{s}} \right\rangle \otimes \left[ \bar{s} \chi_{[ ]_{S_{4q}, m_{4q}}}^{FS}(uuds) \otimes \chi_{l, \mu}^{OC} \right]_{J_{4q}, m_{4q}} \right]_{\frac{1}{2}, m_{5q}}$$

$$[4]_{SF}, [31]_{SF}, [211]_{SF}, [22]_{SF}$$

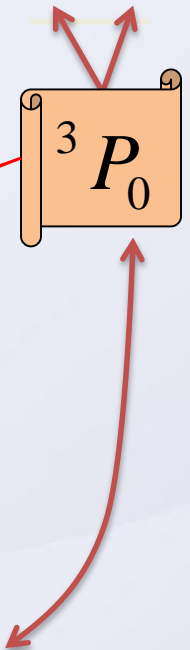
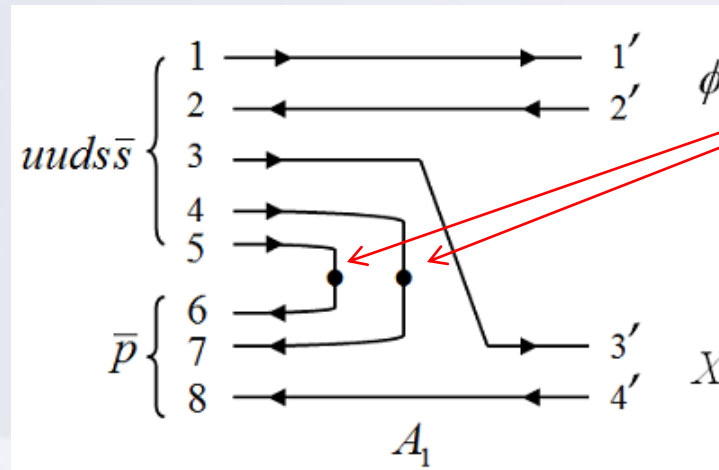
$$\chi_{1, \mu}^{OC} = \frac{1}{\sqrt{3}} \left[ \chi_{[222]_{\lambda}}^C Y_{1\mu} \left( \frac{\bar{q}_2 - \bar{q}_3}{\sqrt{2}} \right) - \chi_{[222]_{\rho}}^C Y_{1\mu} \left( \frac{\bar{q}_2 + \bar{q}_3 - 2\bar{q}_4}{\sqrt{6}} \right) + \chi_{[222]_{\eta}}^C Y_{1\mu} \left( \frac{\bar{q}_2 + \bar{q}_3 + \bar{q}_4 - 3\bar{q}_5}{\sqrt{12}} \right) \right]$$



# The effective operators

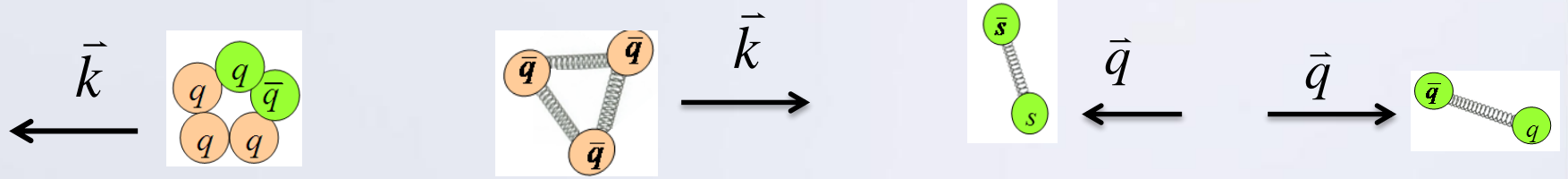
$$O_{A_1} = \lambda_{A_1} \delta^{(3)}(\vec{q}_1 - \vec{q}_{1'}) \delta^{(3)}(\vec{q}_2 - \vec{q}_{2'}) \delta^{(3)}(\vec{q}_3 - \vec{q}_{3'}) \delta^{(3)}(\vec{q}_8 - \vec{q}_{4'}) V^{56} V^{47}$$

↑  
the effective strength parameter



$$V^{ij} = \sum_{\gamma} \sigma_{-\gamma}^{ij} Y_{1\gamma} (\vec{q}_i - \vec{q}_j) \delta^{(3)}(\vec{q}_i + \vec{q}_j) (-1)^{1+\gamma} 1_F^{ij} 1_C^{ij}$$

## Choosing the plane wave basis for the relative motion of the proton and antiproton



$$\delta^{(3)}(\vec{q}_1 + \vec{q}_2 + \vec{q}_3 + \vec{q}_4 + \vec{q}_5 - \vec{k}) \quad \delta^{(3)}(\vec{q}_6 + \vec{q}_7 + \vec{q}_8 + \vec{k}) \quad \delta^{(3)}(\vec{q} - \vec{q}_1 + \vec{q}_2) \quad \delta^{(3)}(\vec{q} + \vec{q}_3 + \vec{q}_4)$$

In the low-momentum approximation, we have the transition amplitude

$$T_{fi}(\vec{q}, \vec{k}) = \lambda_{A_1} \exp\{-Q_q^2 q^2 - Q_k^2 k^2\} \langle f | O_{A_1} | i \rangle$$

the spin-color-flavor weight

$$\langle f | O_{A_1} | i \rangle = \langle f | \sum_{\nu, \lambda} (-1)^{\nu+\lambda} \sum_{m, n} \Omega_{m, n}^{SP(PS)} f_{m, n}^{SP(PS)} \sigma_{-\nu}^{56} \sigma_{-\lambda}^{47} 1_F^{56} 1_F^{47} 1_C^{56} 1_C^{47} f(\nu, \lambda, \mu, m_f, M) | i \rangle$$

$Q_q^2, Q_k^2$  and  $\Omega_{m, n}^{SP(PS)}$  are geometrical constants  
depending on the radial parameters  $R_B, R_M$

$$T_{fi}(\vec{q}, \vec{k}) = \lambda_{A_i} \exp\{-Q_q^2 q^2 - Q_k^2 k^2\} \langle f | O_{A_i} | i \rangle$$

the spin-color-flavor weight

$$\langle f | O_{A_i} | i \rangle = \langle f | \sum_{\nu, \lambda} (-1)^{\nu+\lambda} \sum_{m, n} \Omega_{m, n}^{SP(PS)} f_{m, n}^{SP(PS)} \sigma_{-\nu}^{56} \sigma_{-\lambda}^{47} 1_F^{56} 1_F^{47} 1_C^{56} 1_C^{47} f(\nu, \lambda, \mu, m_f, M) | i \rangle$$

The spin-angular momentum functions

$$\begin{aligned} f_{1,1}^{SP} &= f_{1,2}^{SP} = f_{1,3}^{SP} = (-1)^\nu \delta_{\lambda, -\nu} \delta_{\mu, m_f} \\ f_{2,1}^{SP} &= f_{2,2}^{SP} = f_{2,3}^{SP} = (-1)^\mu \delta_{\mu, -\nu} \delta_{\lambda, m_f} \\ f_{3,1}^{SP} &= f_{3,2}^{SP} = f_{3,3}^{SP} = (-1)^\mu \delta_{\mu, -\lambda} \delta_{\nu, m_f} \\ f_{1,1}^{PS} &= f_{1,2}^{PS} = f_{1,3}^{PS} = (-1)^{\lambda+\mu} \delta_{\lambda, -\nu} \delta_{\mu, -M} \\ f_{2,1}^{PS} &= f_{2,2}^{PS} = f_{2,3}^{PS} = (-1)^{\lambda+\mu} \delta_{\mu, -\nu} \delta_{\lambda, -M} \\ f_{3,1}^{PS} &= f_{3,2}^{PS} = f_{3,3}^{PS} = (-1)^{\nu+\mu} \delta_{\mu, -\lambda} \delta_{\nu, -M} \end{aligned}$$

$$|i\rangle = |\{\chi_{\frac{1}{2}, m_{5q}}(uuds\bar{s}) \otimes \chi_{\frac{1}{2}, m_{\bar{p}}}(\bar{u}\bar{u}\bar{d})\}_{S, S_z} \otimes (L, M)\rangle_{J, J_z}$$

$$|f\rangle = |\{\chi_{1, m_\alpha}(\phi) \otimes \chi_{j m, m_{3', 4'}}(X)\}_{j, m_\epsilon} \otimes (\ell_f, m_f)\rangle_{J, J_z}$$



Including the initial state interaction for the atomic state of the  $p\bar{p}$  system

$$T_{if}(\vec{q}, \vec{k}) \Rightarrow T_{f,LSJ}(\vec{q}) = \int d^3k T_{fi}(\vec{q}, \vec{k}) \phi_{LSJ}^I(\vec{k})$$

The protonium wave function in momentum space for fixed isospin  $I$

The partial decay width for the transition of the state to the two-meson state

$$\Gamma_{p\bar{p} \rightarrow \phi X} = \int \frac{d^3 p_\phi}{2E_\phi} \frac{d^3 p_X}{2E_X} \delta^{(3)}(\vec{p}_\phi + \vec{p}_X) \delta(E - E_\phi - E_X) |T_{f,LSJ}(\vec{q})|^2$$

**Branching ratio**



the partial decay width divided by the total width

$$J = 0 \rightarrow |0,0\rangle$$

$$J = 1 \begin{cases} \nearrow |1,1\rangle \\ \rightarrow |1,0\rangle \\ \searrow |1,-1\rangle \end{cases}$$

$$BR(\phi, X) = W(J) \frac{\Gamma_{p\bar{p} \rightarrow \phi, X}}{\Gamma_{total}(J)}$$

statistical weight  $W(J) = (2J + 1)$

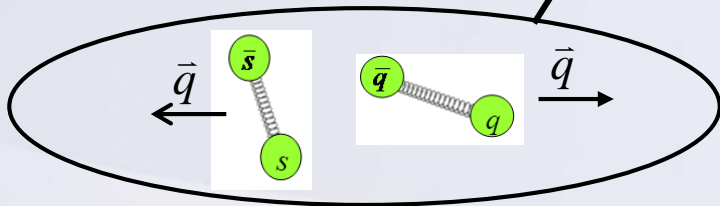
## Reducing the model dependence

$$BR(\phi, X) = \frac{W(J)}{\Gamma_{total}(J)} \lambda_{A_i}^2 f(\phi, X) \langle f | O_{A_i} | i \rangle^2 \gamma(I, J)$$

*Choosing a simplified phenomenological approach that has been applied in studies of two-meson branching ratios in nucleon-antinucleon and radiative protonium annihilation.*

A. Kercek, T. Gutsche and A. Faessler, J. Phys. G **25**, 2271 (1999)

T. Gutsche, R. Vinh Mau, M. Strohmeier-Presicek and A. Faessler, Phys. Rev. C **59**, 630 (1999)



we use a kinematical phase-space factor of the phenomenological form

$$f(\phi, X) = q \exp \{-1.2 \text{ GeV}^{-1} (s - s_{\phi X})^{1/2}\}$$

$$\sqrt{s} = (m_\phi^2 + q^2)^{1/2} + (m_X^2 + q^2)^{1/2}$$

The initial-state interaction coefficients

$$\gamma(I, J) \propto \int d^3k \phi_{LSJ}^I(\vec{k}) \exp\{-Q_k^2 k^2\}$$

*are related to the probability for a protonium state to have isospin I and spin J*

State $i$	$\gamma_0(i)$	$\gamma_1(i)$	$\Gamma_{tot}(i)$
$^1S_0$	0.56	0.44	1.0
$^3S_1$ - $^3D_1$	0.56	0.44	0.9

# Results

	$^{11}S_0 \rightarrow \omega\phi$	$^{33}S_1 \rightarrow \pi^0\phi$	$^{31}S_0 \rightarrow \rho^0\phi$	$^{13}S_1 \rightarrow \eta\phi$
BR <sup>exp</sup>	$6.3 \pm 2.3$	$5.5 \pm 0.7$	$3.4 \pm 1.0$	$0.9 \pm 0.3$
[4][22][22]	6.3★	5.4	3.8	1.4 - 1.8
[4][31][31]	6.3★	5.4	3.8	1.4 - 1.8
[31][211][22]	6.3★	4.3	3.8	1.9 - 2.5
[31][211][31]	6.3★	3.8	2.7	1.2 - 1.5
[31][22][31]	6.3★	5.9	4.9	1.0 - 1.4
[31][31][22]	6.3★	7.3	3.9	0.90 - 1.0
[22][211][31]	6.3★	181.2	97.5	44.0 - 57.6

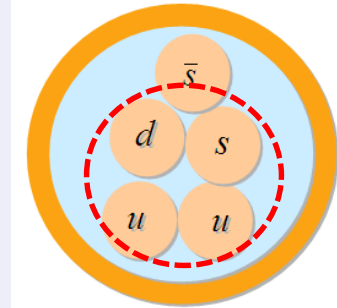
	$^{11}S_0 \rightarrow \omega\phi$	$^{33}S_1 \rightarrow \pi^0\phi$	$^{31}S_0 \rightarrow \rho^0\phi$	$^{13}S_1 \rightarrow \eta\phi$
BR <sup>exp</sup>	$6.3 \pm 2.3$	$5.5 \pm 0.7$	$3.4 \pm 1.0$	$0.9 \pm 0.3$
[22][22][22]	6.3★	0.85	3.4	5.3 - 6.9
[211][211][22]	6.3★	0.85	3.5	5.3 - 6.7
[211][211][31]	6.3★	7.7	4.0	3.2 - 4.2
[22][31][31]	6.3★	4.5	2.3	2.2 - 2.9
[211][22][31]	6.3★	181.2	97.5	44.0 - 57.6
[211][31][22]	6.3★	0.85	3.5	5.3 - 6.9
[211][31][31]	6.3★	0.24	0.17	0.090 - 0.11

	$^{33}P_{0,1,2} \rightarrow \rho^0 \phi$	$^{31}P_1 \rightarrow \pi^0 \phi$	$^{13}P_{0,1,2} \rightarrow \omega \phi$	$^{11}P_1 \rightarrow \eta \phi$
BR <sup>exp</sup>	$3.7 \pm 0.9$	$0 + 0.3$	$2.9 \pm 1.4$	$0.4 \pm 0.2$
[4][22][22]	3.7★	0.31	1.6	0.10 - 0.14
[4][31][31]	3.7★	1.1	5.3	0.36 - 0.47
[31][211][22]	3.7★	0.48	1.3	0.17 - 0.22
[31][211][31]	3.7★	1.4	6.1	0.55 - 0.71
[31][22][31]	3.7★	0.65	5.1	0.18 - 0.23
[31][31][22]	3.7★	0.22	2.5	0.067 - 0.087
[22][211][31]	3.7★	0.012	0.23	$1.2-1.5 (\times 10^{-5})$

	$^{33}P_{0,1,2} \rightarrow \rho^0 \phi$	$^{31}P_1 \rightarrow \pi^0 \phi$	$^{13}P_{0,1,2} \rightarrow \omega \phi$	$^{11}P_1 \rightarrow \eta \phi$
[31][31][31]	3.7★	0.76	2.4	0.26 - 0.34
[22][22][22]	3.7★	0.0029	13	0.0061 - 0.0080
[211][211][22]	3.7★	0.0029	13	0.0061 - 0.0080
[211][211][31]	3.7★	0.0029	3.6	0.23 - 0.30
[22][31][31]	3.7★	$5.1 \times 10^{-4}$	2.2	0.16 - 0.20
[211][22][31]	3.7★	0.012	0.23	1.2-1.5 ( $\times 10^{-5}$ )
[211][31][22]	3.7★	0.0029	13	0.0061 - 0.0080
[211][31][31]	3.7★	$7.4 \times 10^{-4}$	0.63	0.0062 - 0.0081

# Conclusions

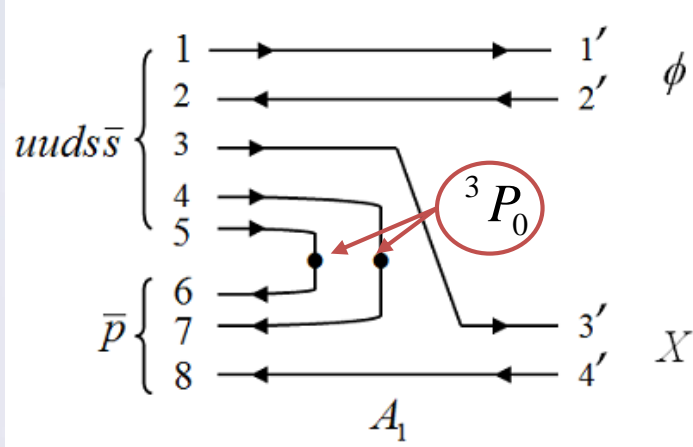
$$|p\rangle = A|uud\rangle + B|uuds\bar{s}\rangle$$



15 configurations

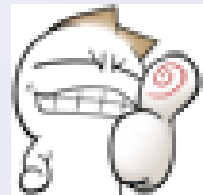


## Branching ratios $p\bar{p} \rightarrow X\phi$ ( $X = \pi^0, \eta, \rho, \omega$ )



The best agreement of theoretical results with the experimental data is found in the pentaquark configuration with the flavor-spin symmetry

$$[4]_{FS} [22]_F [22]_S$$



**Thank you  
for your attention**

