



# Hadron structure in the covariant confined quark model

T h o m a s G u t s c h e

I n s t i t u t f ü r T h e o r e t i s c h e P h y s i k  
U n i v e r s i t ä t T ü b i n g e n

---



# Overview

- Covariant confined quark model
- Applications in the meson sector
- (Light baryons and their electromagnetic structure)
- Semileptonic decays of heavy baryons
- Summary



# Recent Coworkers

- Tübingen: V. Lyubovitskij
- Dubna: M. Ivanov
- Mainz: J. Körner
- Napoli: P. Santorelli
- Almaty: N. Habyl



# Covariant quark model

- main assumption: hadrons interact by quark exchange
- quantum field theory tool: interaction Lagrangian for coupling between composite hadron and its constituents

Coupling of a meson  $M(x)$  to the  $q\bar{q}$  constituents

$$\mathcal{L}_{\text{int}}^{\text{str}}(x) = g_M M(x) \cdot J_M(x)$$

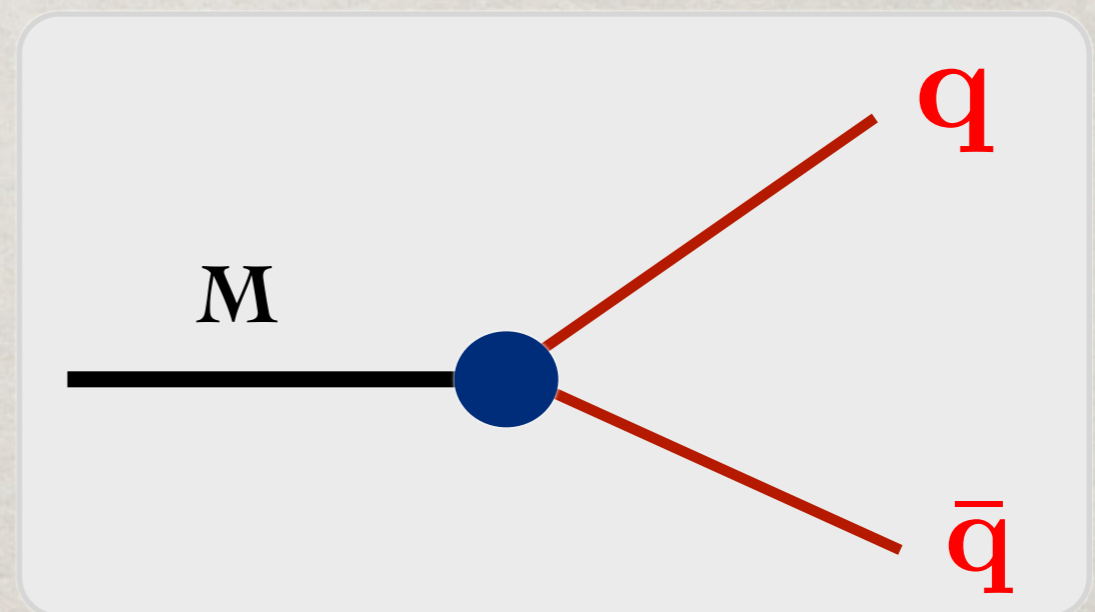
with the non-local quark current

$$J_M(x) = \int dx_1 \int dx_2 F_M(x, x_1, x_2) \bar{q}_1(x_1) \Gamma_M \lambda_M q_2(x_2) + \text{h.c.}$$

Vertex function

Spin

Flavor





# compositeness condition

Salam 1962, Weinberg 1963

- composite field  $M$  and quarks are introduced as elementary particles
- non-local interaction between  $M$  and its constituents
- field renormalization constant  $Z$ :  
matrix element between physical and bare state
- Quasi-particle  $M$  is a stable composite bound state with

$$Z_M^{1/2} = \langle M_{bare} | M_{dressed} \rangle = 0$$



# compositeness condition

compositeness condition leads to self-consistent determination of the hadron-constituents coupling.

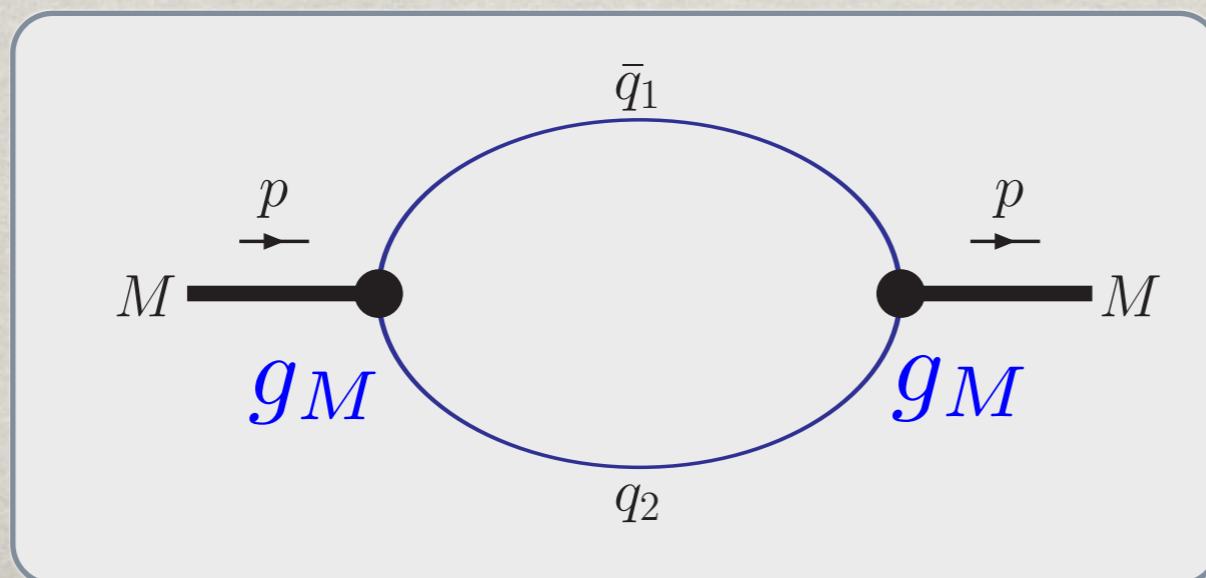
coupling  $g_M$  is determined by the condition

$$Z_M = 1 - \Sigma'_M(m_M^2) = 0$$

with the derivative of the mass operator

$$\Sigma'_M(m_M^2) = g_M^2 \Pi'_M(m_M^2) = g_M^2 \frac{d\Pi_M(p^2)}{dp^2} \Big|_{p^2=m_M^2}$$

Exp. input





# vertex function and propagators

- vertex function characterizes finite size of hadron:

$$F_M(x, x_1, x_2) = \delta^{(4)}\left(x - \sum_{i=1}^2 w_i x_i\right) \Phi_M\left((x_1 - x_2)^2\right)$$

with  $w_i = m_i / \sum m_i$  and

translational invariance for any 4-vector  $a$  with

$$F_M(x + a, x_1 + a, x_2 + a) = F_M(x, x_1, x_2)$$

often choose simple Gaussian form with

$$\Phi_M(y^2) = \int \frac{d^4 k}{(2\pi)^4} e^{-ik \cdot y} \tilde{\Phi}(-k^2), \quad \tilde{\Phi}(-k_E^2) = \exp(-k_E^2 / \Lambda_M^2)$$

- constituent quark propagator

$$S_q(k) = \frac{1}{m_q - \not{k} - i\epsilon}$$

with effective mass  $m_q$



# inclusion of photons or gauging the non-local Lagrangian

Strong interaction Lagrangian is non-local

Gauged by applying gauge field exponential with

$$q_i(x_i) \rightarrow e^{-ie_{q_i} I(x_i, x, P)} q_i(x_i) \text{ with } I(x_i, x, P) = \int_x^{x_i} dz_\mu A^\mu$$

Mandelstam (1961), Terning (1991)

Expansion of gauged Lagrangian with

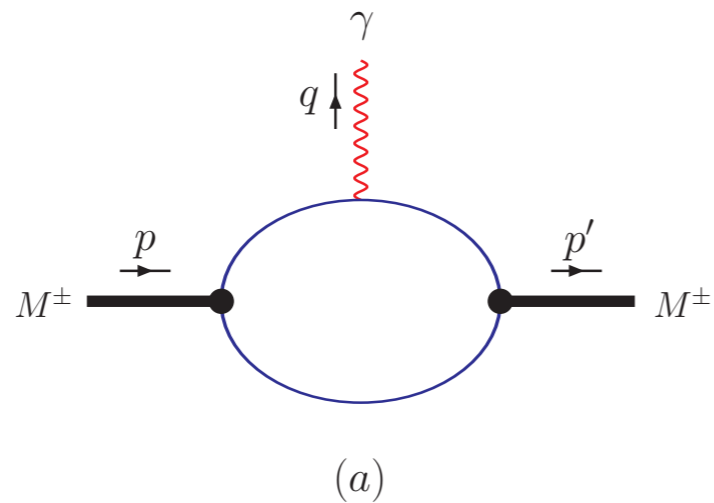
$$\mathcal{L}_{\text{int}}^{\text{str;em}}(x) = g_M M(x) \int dx_1 \int dx_2 F_M(x, x_1, x_2)$$

$$\times \bar{q}_1(x_1) e^{ie_{q_1} I(x_1, x, P)} \Gamma_M \lambda_M e^{-ie_{q_2} I(x_2, x, P)} q_2(x_2)$$

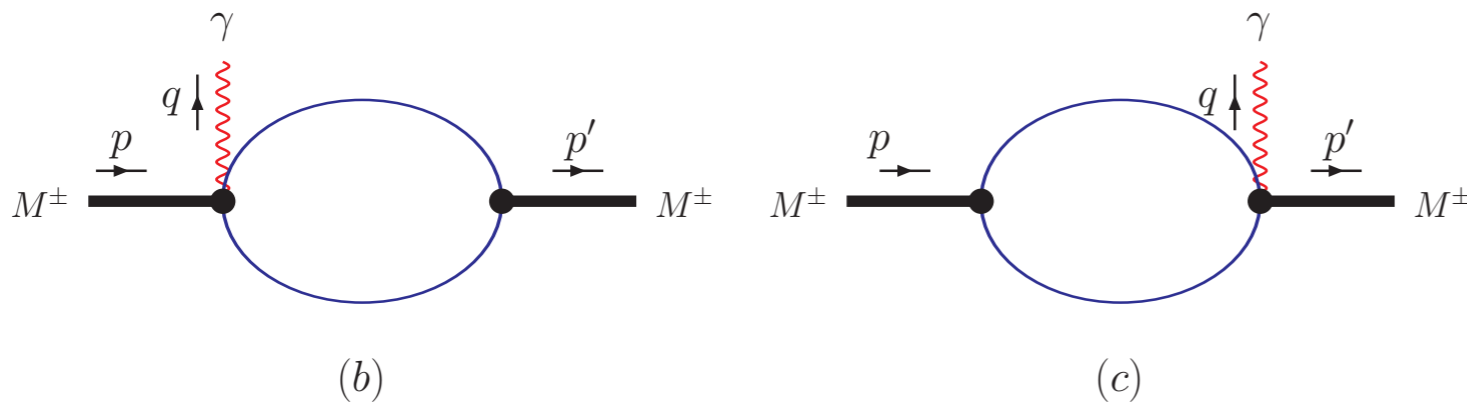
in powers of  $A_\mu$  leads to:



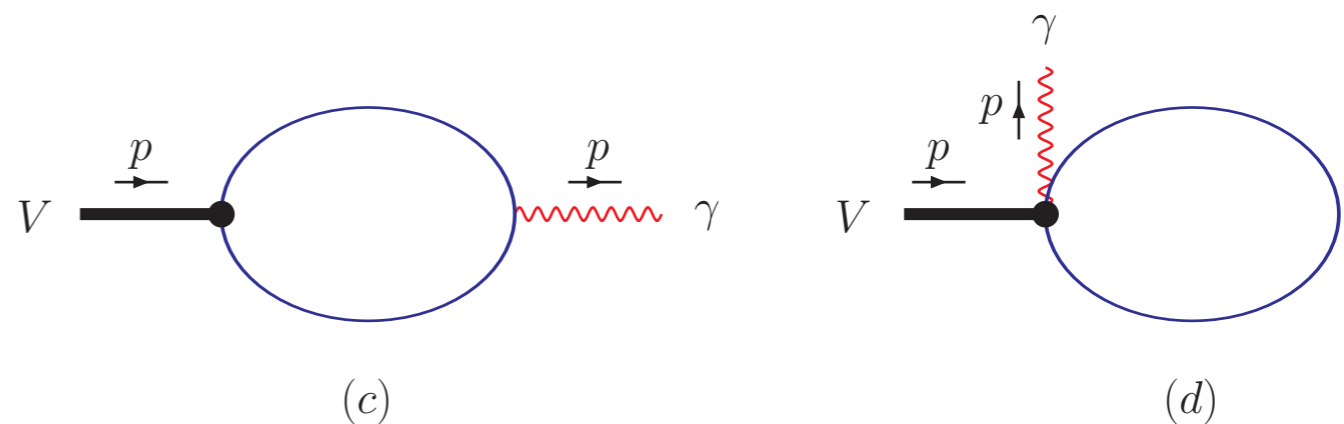
# inclusion of photons or gauging the non-local Lagrangian



electromagnetic  
vertex function



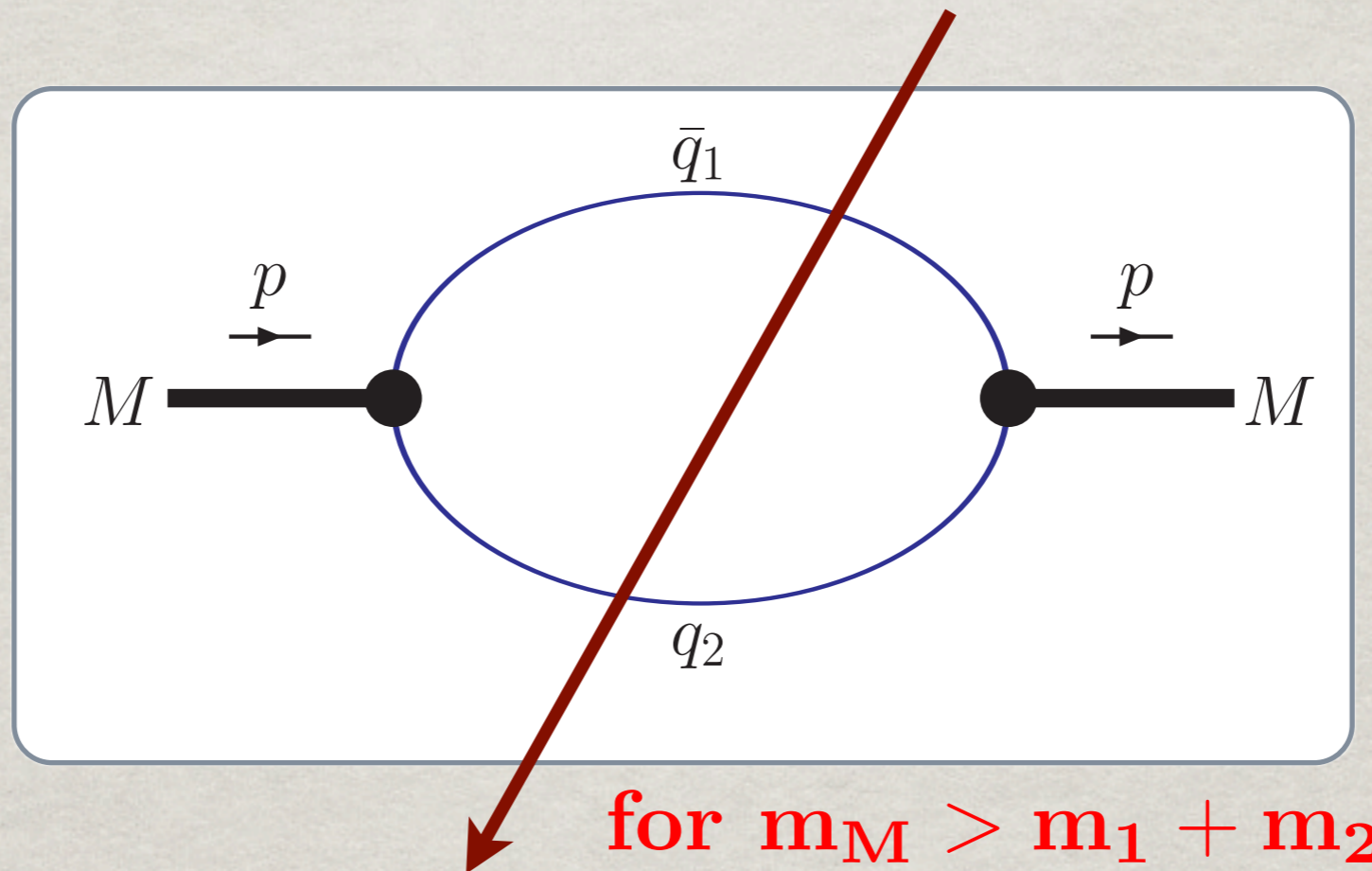
vector meson  
 $V \rightarrow \gamma$  transition





# infrared confinement

up to now applications limited to hadrons with  $m_M < m_1 + m_2$ .



for  $m_M > m_1 + m_2$

reason: free quark propagator,  
threshold singularities with free quarks

---> confinement = absence of quark poles



# infrared confinement

**Idea:** consider scalar one-pole propagator

$$\frac{1}{m^2 - p^2} = \int_0^{\infty} d\alpha \exp[-\alpha(m^2 - p^2)]$$

in the Schwinger representation.

Introduce integration limit with the

infrared confinement scale:  $\lambda$  with mass dimension (m)

$$\int_0^{1/\lambda^2} d\alpha \exp[-\alpha(m^2 - p^2)] = \frac{1 - \exp[-(m^2 - p^2)/\lambda^2]}{m^2 - p^2}$$

**entire function, confined propagator**  
(similar to NJL (Ebert 1996), constant  
self-dual field Leutwyler/Efimov (1995))



Consider general l-loop diagram with n propagators:

$$\Pi(p_1, \dots, p_n) = \int_0^\infty d^n \alpha \int [d^4 k]^l \Phi \exp\left[-\sum_{i=1}^n \alpha_i (m_i^2 - p_i^2)\right]$$

numerator: product of propagators and vertices

after loop integration

$$\Pi = \int_0^\infty d^n \alpha F(\alpha_1, \dots, \alpha_n)$$

complete structure  
of diagram

with the identity  $1 = \int_0^\infty dt \delta\left(t - \sum_{i=1}^n \alpha_i\right)$  we get

$$\Pi = \int_0^\infty dt t^{n-1} \int_0^1 d^n \alpha \delta\left(1 - \sum_{i=1}^n \alpha_i\right) F(t\alpha_1, \dots, t\alpha_n)$$



confinement: introduce infrared cut-off at  $1/\lambda^2$

$$\Pi^c = \int_0^{1/\lambda^2} dt t^{n-1} \int_0^1 d^n \alpha \delta\left(1 - \sum_{i=1}^n \alpha_i\right) F(t\alpha_1, \dots, t\alpha_n)$$

consequences:

- all thresholds are removed in the quark-loop diagram
- infrared cut-off  $1/\lambda^2$  is universal -- same for all physical processes

T. Branz, A. Faessler, TG, M. Ivanov, J. Körner, V. Lyubovitskij,  
PRD D81, 034010 (2010)

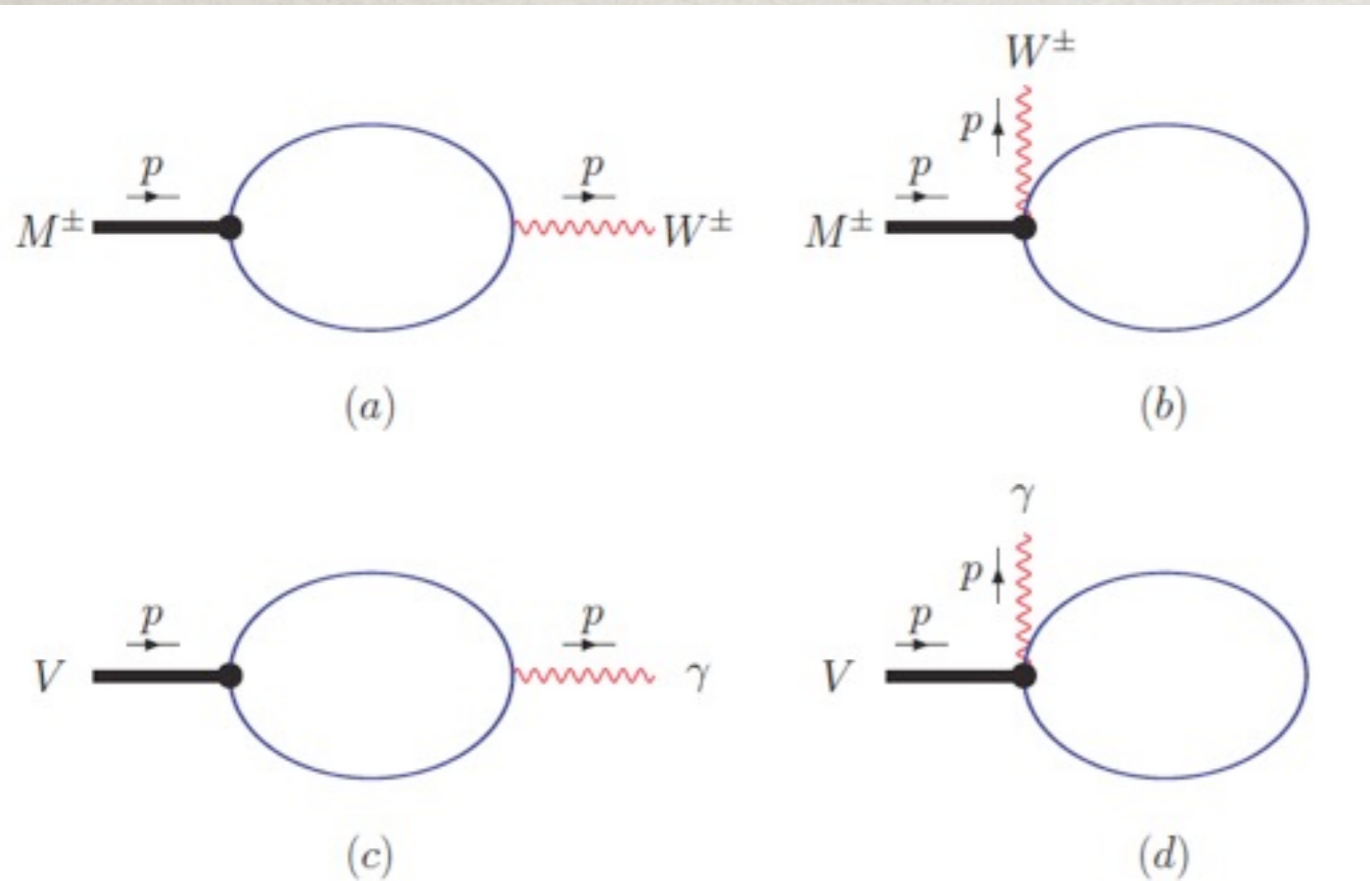


# first fits and parameters

see T. Branz, A. Faessler, TG, M. Ivanov, J. Körner, V. Lyubovitskij, PRD D81, 034010 (2010)

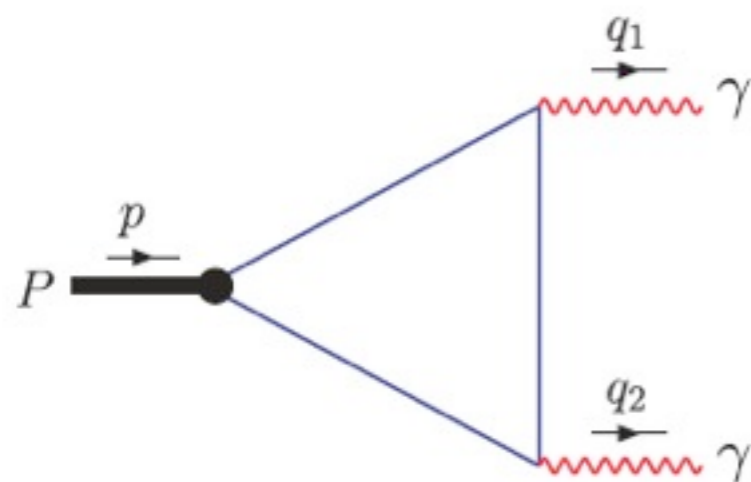
update in M. Ivanov et al., PRD D85, 034004 (2012)

$\pi$  and  $\rho$  properties:

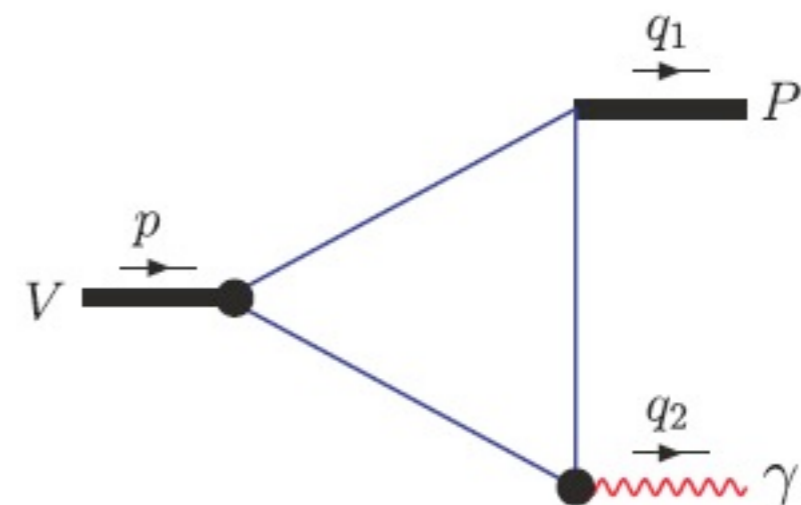


$\rightarrow \mathbf{f}_\pi$

$\rightarrow \mathbf{g}_{\rho\gamma}$



$\rightarrow \mathbf{g}_{\pi\gamma\gamma}$



$\rightarrow \mathbf{g}_{\rho\pi\gamma}$



# first fits and parameters

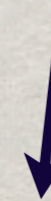
see T. Branz, A. Faessler, TG, M. Ivanov, J. Körner, V. Lyubovitskij, PRD D81, 034010 (2010)

update in M. Ivanov et al., PRD D85, 034004 (2012)

$\pi$  and  $\rho$  properties:

Quantity	Our	Data (PDG)
$f_\pi$ , MeV	130.2	$130.4 \pm 0.04 \pm 0.2$
$g_{\pi\gamma\gamma}$ , $\text{GeV}^{-1}$	0.23	0.276
$g_{\rho\gamma}$	0.2	0.2
$g_{\rho\pi\gamma}$ , $\text{GeV}^{-1}$	0.75	$0.723 \pm 0.037$

Infrared cut-off



$$m_u = m_d$$

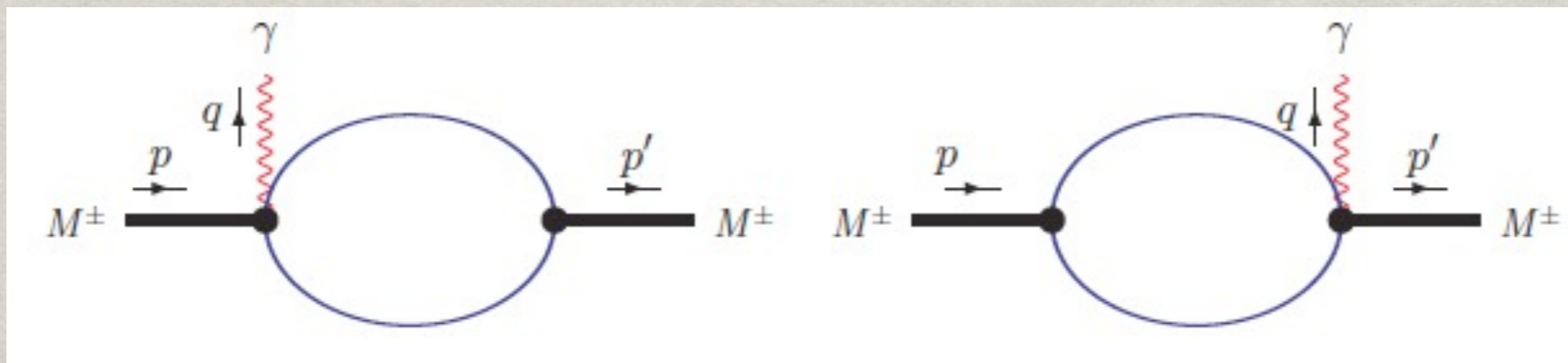
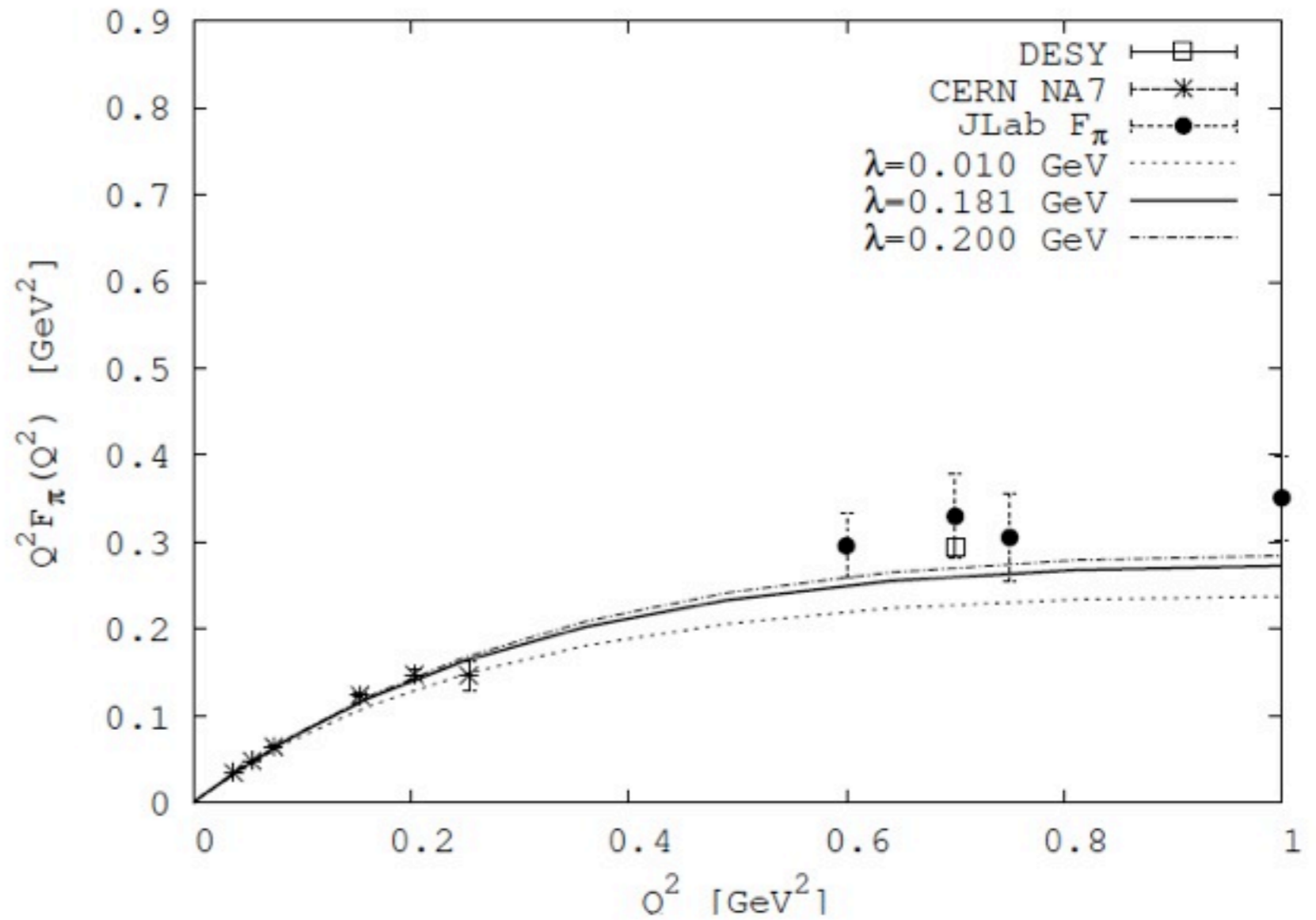
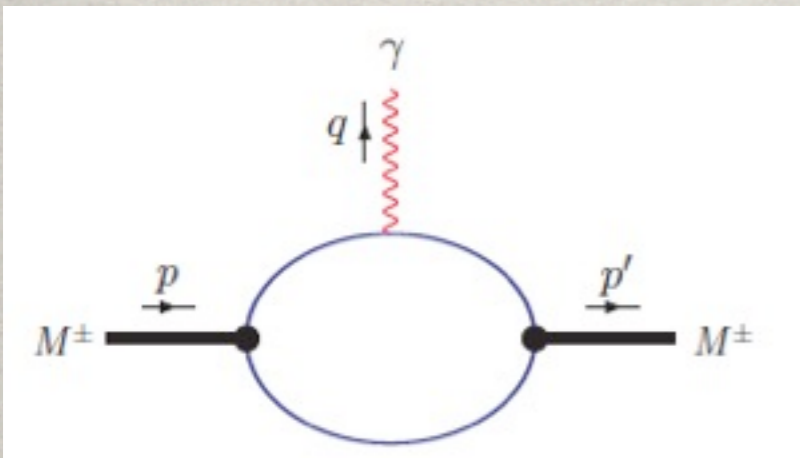
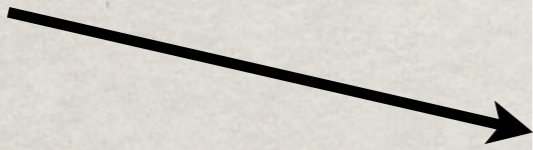
$m$	$\Lambda_\pi$	$\Lambda_\rho$	$\lambda$	
0.217	0.711	0.295	0.181	GeV

parameters



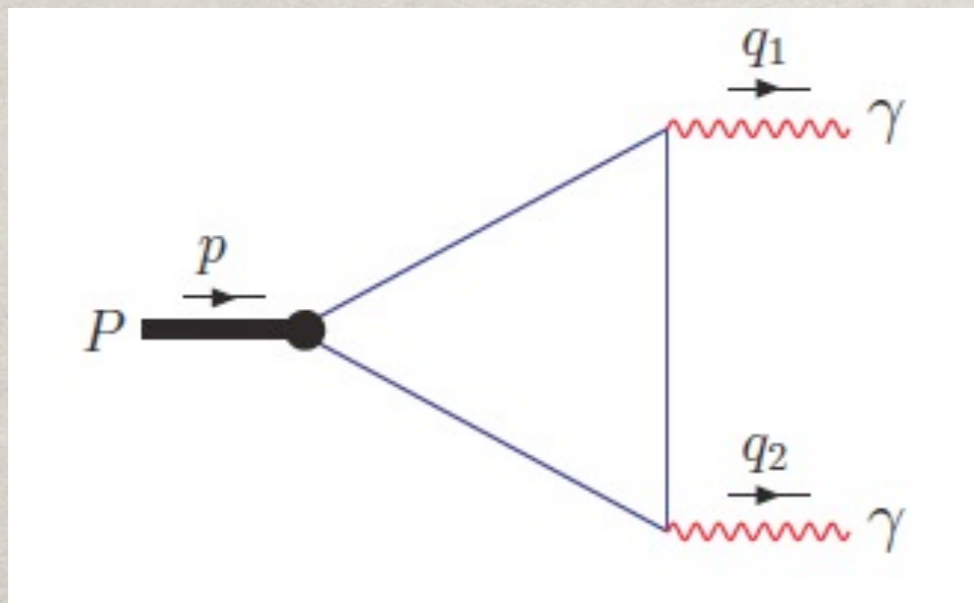
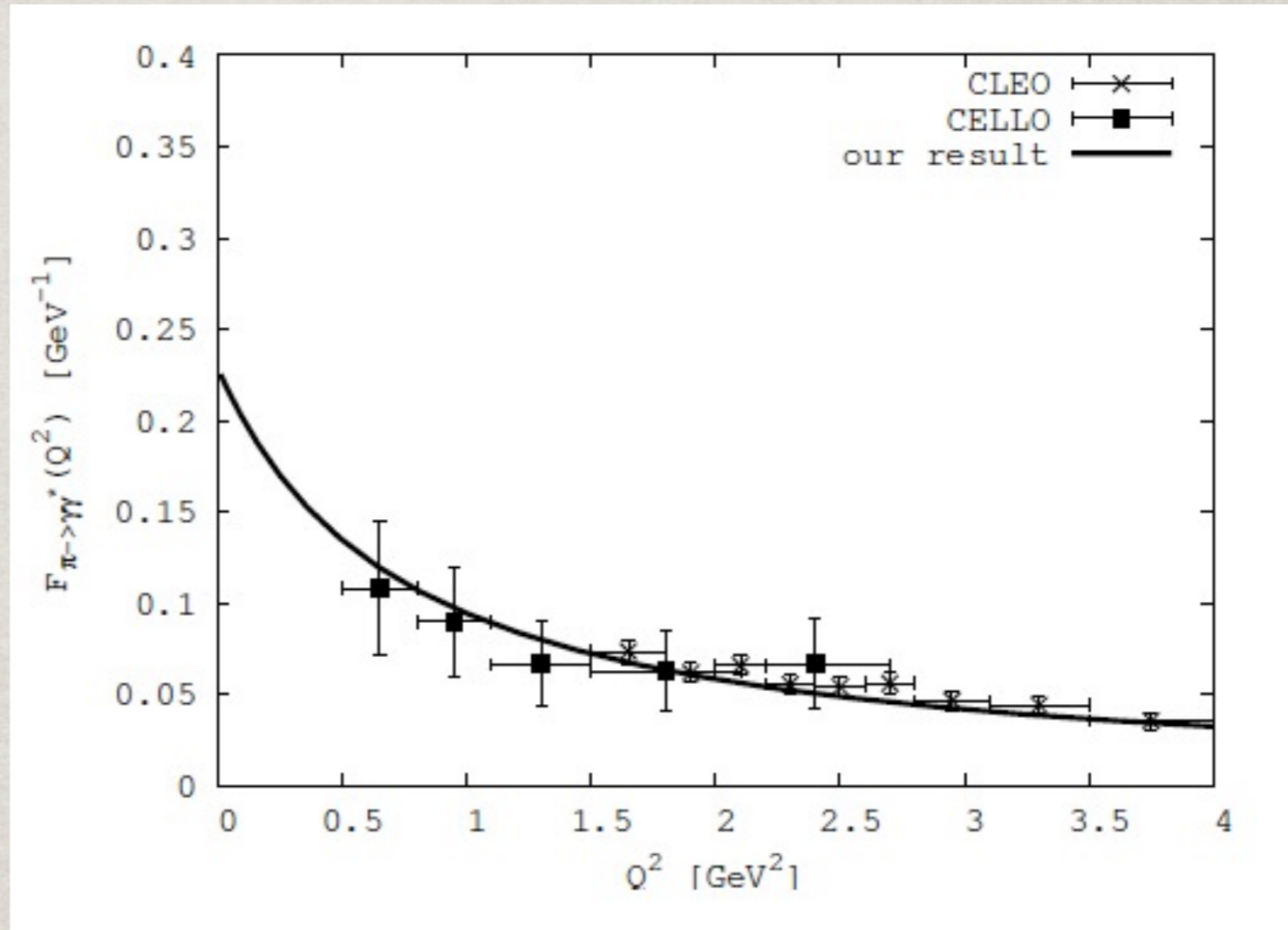
form factor  $\pi^\pm \rightarrow \pi^\pm \gamma^*$  for space-like photon momentum  $Q^2$

variation in  
infrared cut-off





transition form factor  $\gamma\gamma^* \rightarrow \pi^0$  for space-like photon momentum  $Q^2$



+ „nonlocal“ graphs



# further model parameters: basic electroweak properties

$$\begin{array}{ccc} m_s & m_c & m_b \\ \hline 0.360 & 1.6 & 4.8 \text{ GeV} \end{array}$$

$\Lambda_{\rho/\omega/\phi}$	$\Lambda_{\eta}$	$\Lambda_{\eta^s}$	$\Lambda_{\eta'}$	$\Lambda_{\eta'^s}$	$\Lambda_K$	$\Lambda_{K^*}$	$\Lambda_D$	$\Lambda_{D^*}$	$\Lambda_{D_s}$	$\Lambda_{D_s^*}$	$\Lambda_{B/B^*}$	$\Lambda_{B_s/B_s^*}$	$\Lambda_{J/\psi}$	$\Lambda_{\eta_c/B_c}$	$\Lambda_{\Upsilon}$	$\Lambda_{\eta_b}$
0.295	0.70	0.85	0.27	0.45	0.87	0.30	1.4	2.3	1.95	2.6	3.35	4.4	3.3	3.0	5.07	5.0 GeV

TABLE II: Weak leptonic decay constants  $f_{P(V)}$  in MeV.

Meson	Our	Data [15]
$\pi^-$	130.2	$130.4 \pm 0.04 \pm 0.2$
$K^-$	155.4	$155.5 \pm 0.2 \pm 0.8$
$D^+$	206.2	$205.8 \pm 8.9$
$D_s^+$	273.7	$273 \pm 10$
$B^-$	216.4	$216 \pm 22$
$B_s^0$	250.2	$253 \pm 8 \pm 7$
$B_c$	485.2	$489 \pm 5 \pm 3$ [23]
$\rho^+$	209.3	$210.5 \pm 0.6$ [15]
$D^{*+}$	187.0	$245 \pm 20_{-2}^{+3}$ [24]
$D_s^{*+}$	213	$272 \pm 16_{-20}^{+3}$ [25]
$B^{*+}$	210.6	$196 \pm 24_{-2}^{+39}$ [24]
$B_s^{*0}$	264.6	$229 \pm 20_{-16}^{+41}$ [24]

## Electromagnetic leptonic decay constants $f_V$

Meson	Our	Data [15]
$\rho^0$	148.0	$154.7 \pm 0.7$
$\omega$	51.7	$45.8 \pm 0.8$
$\phi$	76.3	$76 \pm 1.2$
$J/\psi$	277.4	$277.6 \pm 4$
$\Upsilon(1s)$	238.4	$238.5 \pm 5.5$

in MeV.



TABLE IV. Electromagnetic and leptonic decay widths in keV.

Process	Ours	Data [15]
$\pi^0 \rightarrow \gamma\gamma$	$5.40 \times 10^{-3}$	$(7.7 \pm 0.6) \times 10^{-3}$
$\eta \rightarrow \gamma\gamma$	0.51	$0.510 \pm 0.026$
$\eta' \rightarrow \gamma\gamma$	4.27	$4.28 \pm 0.19$
$\eta_c \rightarrow \gamma\gamma$	4.55	$7.2 \pm 0.7 \pm 2.0$
$\eta_b \rightarrow \gamma\gamma$	0.43	
$\rho^0 \rightarrow e^+e^-$	6.33	$7.04 \pm 0.06$
$\omega \rightarrow e^+e^-$	0.76	$0.60 \pm 0.02$
$\phi \rightarrow e^+e^-$	1.27	$1.27 \pm 0.04$
$J/\psi \rightarrow e^+e^-$	5.54	$5.55 \pm 0.14 \pm 0.02$
$\Upsilon \rightarrow e^+e^-$	1.34	$1.34 \pm 0.018$

further predictions  
in the meson sector

$\rho^\pm \rightarrow \pi^\pm \gamma$	72.42	$68 \pm 7$
$\rho^0 \rightarrow \eta \gamma$	63.25	$62 \pm 17$
$\omega \rightarrow \pi^0 \gamma$	682.71	$703 \pm 25$
$\omega \rightarrow \eta \gamma$	7.63	$6.1 \pm 2.5$
$\eta' \rightarrow \omega \gamma$	12.44	$9.06 \pm 2.87$
$\phi \rightarrow \eta \gamma$	51.72	$58.9 \pm 0.5 \pm 2.4$
$\phi \rightarrow \eta' \gamma$	0.41	$0.27 \pm 0.01$
$K^{*\pm} \rightarrow K^\pm \gamma$	40.86	$50 \pm 5$
$K^{*0} \rightarrow K^0 \gamma$	122.04	$116 \pm 10$
$D^{*\pm} \rightarrow D^\pm \gamma$	0.62	$1.5 \pm 0.8$
$D^{*0} \rightarrow D^0 \gamma$	20.27	$< 0.9 \times 10^3$
$D_s^{*\pm} \rightarrow D_s^\pm \gamma$	0.30	$< 1.8 \times 10^3$
$B^{*\pm} \rightarrow B^\pm \gamma$	0.36	
$B^{*0} \rightarrow B^0 \gamma$	0.12	
$B_s^{*0} \rightarrow B_s^0 \gamma$	0.12	
$J/\psi \rightarrow \eta_c \gamma$	1.89	$1.58 \pm 0.37$
$\Upsilon \rightarrow \eta_b \gamma$	0.02	



## physics of heavy baryons: motivation

- origin of flavor and CP violations
- determination of CKM matrix elements
- weak decays of heavy hadrons containing a b- or c-quark
- experimental possibilities at LHCb
- signals for new physics beyond the Standard Model
- models of heavy flavor decays (nonperturbative hadronic effects)
- new exotic states



## recent work on heavy baryons:

TG, M. Ivanov, J. Körner, V. Lyubovitskij, P. Santorelli and N.Habyl:

PRD 91, 074001 (2015)  $\Lambda_b \rightarrow \Lambda_c + \tau^- + \bar{\nu}_\tau$

PRD 90, 114033 (2014)  $\Lambda_b \rightarrow \mathbf{p} + \ell^- + \bar{\nu}_\ell$  and  $\Lambda_c \rightarrow \mathbf{n} + \ell^+ + \nu_\ell$

PRD 88, 114018 (2013)  $\Lambda_b \rightarrow \Lambda(\rightarrow \mathbf{p}\pi^-) + \mathbf{J}/\Psi(\rightarrow \ell^+\ell^-)$

PRD 87, 074031 (2013)  $\Lambda_b \rightarrow \Lambda\ell^+\ell^-$  ( $\ell = \mathbf{e}, \mu, \tau$ ) and  $\Lambda_b \rightarrow \Lambda\gamma$

PRD 86, 074013 (2012) el.magn. structure of light baryons



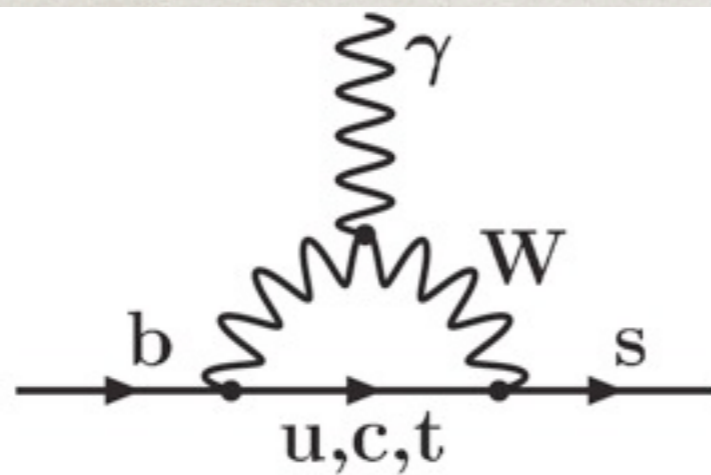
## Rare baryon decays:

$$\Lambda_b \rightarrow \Lambda \ell^+ \ell^- \quad (\ell = e, \mu, \tau) \quad \text{and} \quad \Lambda_b \rightarrow \Lambda \gamma$$

TG, M. Ivanov, J. Körner, V. Lyubovitskij, P. Santorelli, PRD 87, 074031 (2013)

- flavor-changing neutral currents - FCNC, like

$$b \rightarrow s \gamma$$



(forbidden at tree level,  
=0 for degenerate up-type  
masses)

- loop induced processes: sensitivity to „new physics“
- extraction of CKM matrix elements
- exclusive and inclusive decays of the form

$$b \rightarrow s \gamma \quad \text{and} \quad b \rightarrow s \ell^+ \ell^-$$

- rare baryon decays complementary to  $B \rightarrow K^{(*)} \ell^+ \ell^-$



## Rare baryon decays:

$$\Lambda_b \rightarrow \Lambda \ell^+ \ell^- \quad (\ell = e, \mu, \tau) \quad \text{and} \quad \Lambda_b \rightarrow \Lambda \gamma$$

- naive factorization, based on OPE in local operators
- separation of short-distance SM dynamics from long-distance hadronic effects
- nonperturbative determination of hadronic matrix elements  $\rightarrow$  form factors
- $b \rightarrow s \ell^+ \ell^-$  contains lots of information through
  - lepton invariant mass
  - lepton energy spectra
  - forward-backward asymmetries .....

### • data

$\Gamma(\Lambda \mu^+ \mu^-) / \Gamma_{\text{total}}$	<i>DOCUMENT ID</i>	<i>TECN</i>	<i>COMMENT</i>
<b>10.8 ± 2.8 OUR AVERAGE</b>			
9.6 ± 1.6 ± 2.5	<sup>40</sup> AAIJ	13AJ LHCb	$pp$ at 7 TeV
17.3 ± 4.2 ± 5.5	AALTONEN	11AI CDF	$p\bar{p}$ at 1.96 TeV



# Lagrangian and 3-quark current

$$\mathcal{L}_{\text{int}}^{\Lambda}(x) = g_{\Lambda} \bar{\Lambda}(x) \cdot J_{\Lambda}(x) + g_{\Lambda} \bar{J}_{\Lambda}(x) \cdot \Lambda(x)$$

$$J_{\Lambda}(x) = \int dx_1 \int dx_2 \int dx_3 F_{\Lambda}(x; x_1, x_2, x_3) J_{3q}^{(\Lambda)}(x_1, x_2, x_3)$$

$$J_{3q}^{(\Lambda)}(x_1, x_2, x_3) = \epsilon^{a_1 a_2 a_3} Q^{a_1}(x_1) u^{a_2}(x_2) C \gamma^5 d^{a_3}(x_3)$$

$$Q = s, c, b$$

$$(ud)_1 S_0$$

Vertex function of the form

$$F_{\Lambda}(x; x_1, x_2, x_3) = \delta^{(4)}\left(x - \sum_{i=1}^3 w_i x_i\right) \Phi_{\Lambda}\left(\sum_{i<j} (x_i - x_j)^2\right)$$

$$\text{with } w_i = m_i / (m_1 + m_2 + m_3)$$



# Effective Hamiltonian for the quark amplitudes

see Buchalla, Buras, Lautenbacher, Rev. Mod. Phys. 68 (1996)

$b \rightarrow s \ell^+ \ell^-$

$$M(b \rightarrow s \ell^+ \ell^-) = \frac{G_F}{\sqrt{2}} \frac{\alpha \lambda_t}{2\pi} \left\{ C_9^{\text{eff}} (\bar{s} O^\mu b) (\bar{\ell} \gamma_\mu \ell) + C_{10} (\bar{s} O^\mu b) (\bar{\ell} \gamma_\mu \gamma_5 \ell) - \frac{2}{q^2} C_7^{\text{eff}} [m_b (\bar{s} i \sigma^{\mu q} (1 + \gamma^5) b) + m_s (\bar{s} i \sigma^{\mu q} (1 - \gamma^5) b)] (\bar{\ell} \gamma_\mu \ell) \right\}$$

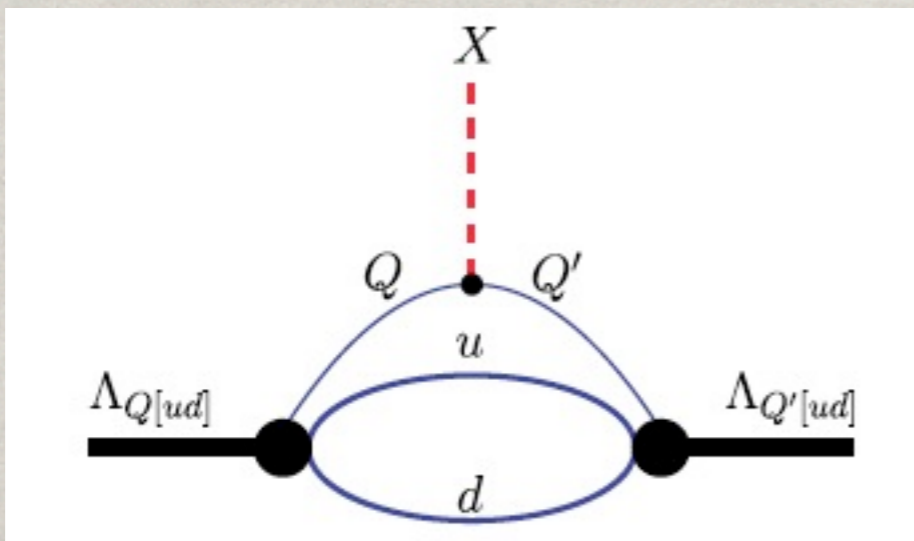
$b \rightarrow s \gamma$

long-distance  $c\bar{c}$  contributions

$$\sigma^{\mu q} = \sigma^{\mu\nu} q_\nu$$

$$\lambda_t \equiv V_{ts}^\dagger V_{tb}$$

$$M(b \rightarrow s \gamma) = -\frac{G_F}{\sqrt{2}} \frac{e \lambda_t}{4\pi^2} C_7^{\text{eff}} [m_b (\bar{s} i \sigma^{\mu q} (1 + \gamma^5) b) + m_s (\bar{s} i \sigma^{\mu q} (1 - \gamma^5) b)] \epsilon_\mu$$



$$\Lambda_{Q[ud]} \rightarrow \Lambda_{Q'[ud]} + X$$

$$X = \ell^- \bar{\nu}_\ell, \ell^+ \ell^- \text{ or } \gamma$$



# Hadronic matrix elements and form factors

$$\langle B_2 | \bar{s} \gamma^\mu b | B_1 \rangle = \bar{u}_2(p_2) [f_1^V(q^2) \gamma^\mu - f_2^V(q^2) i \sigma^{\mu q} / M_1 + f_3^V(q^2) q^\mu / M_1] u_1(p_1),$$

$$\langle B_2 | \bar{s} \gamma^\mu \gamma^5 b | B_1 \rangle = \bar{u}_2(p_2) [f_1^A(q^2) \gamma^\mu - f_2^A(q^2) i \sigma^{\mu q} / M_1 + f_3^A(q^2) q^\mu / M_1] \gamma^5 u_1(p_1),$$

$$\langle B_2 | \bar{s} i \sigma^{\mu q} / M_1 b | B_1 \rangle = \bar{u}_2(p_2) [f_1^{TV}(q^2) (\gamma^\mu q^2 - q^\mu \not{q}) / M_1^2 - f_2^{TV}(q^2) i \sigma^{\mu q} / M_1] u_1(p_1),$$

$$\langle B_2 | \bar{s} i \sigma^{\mu q} \gamma^5 / M_1 b | B_1 \rangle = \bar{u}_2(p_2) [f_1^{TA}(q^2) (\gamma^\mu q^2 - q^\mu \not{q}) / M_1^2 - f_2^{TA}(q^2) i \sigma^{\mu q} / M_1] \gamma^5 u_1(p_1)$$

with  $q = p_1 - p_2$  and  $q_1 = q / M_1$



# Fit parameters

- quark masses and infrared cut-off as in meson sector
- set of size parameters:

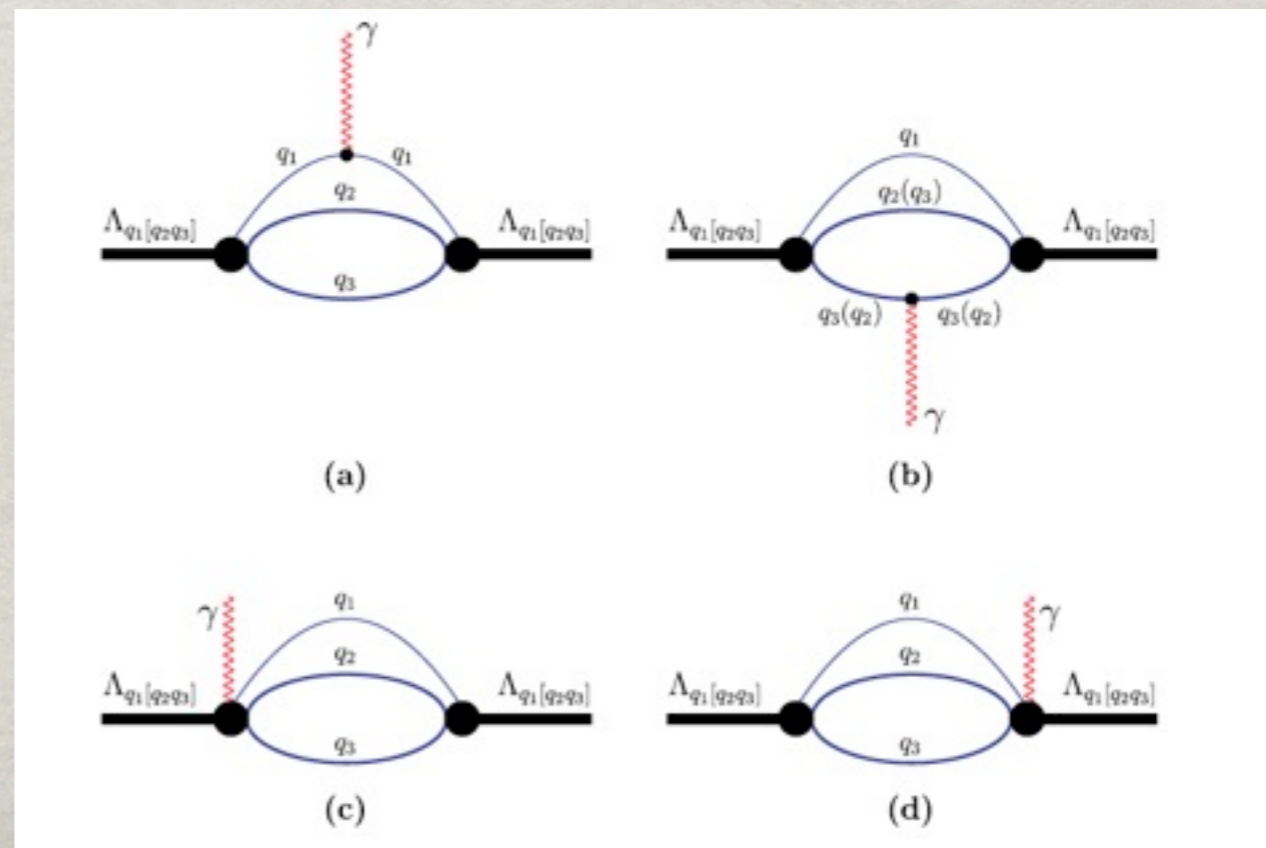
$$\Lambda_{\Lambda_s} = 0.490 \text{ GeV}, \quad \Lambda_{\Lambda_c} = 0.864 \text{ GeV} \text{ and } \Lambda_{\Lambda_b} = 0.569 \text{ GeV}$$

- fit to magnetic moments of Lambda-hyperon:

$$\mu_{\Lambda_s} = -0.73, \quad \mu_{\Lambda_c} = 0.39, \quad \mu_{\Lambda_b} = -0.06,$$

in n.m.

$$\mu_{\Lambda_s}^{\text{expt}} = -0.613 \pm 0.004$$





- and to leading semileptonic decays

TABLE IV. Branching ratios of semileptonic decays of heavy baryons (in %).

Mode	Our results	Data [52]
$\Lambda_c \rightarrow \Lambda e^+ \nu_e$	2.0	$2.1 \pm 0.6$
$\Lambda_c \rightarrow \Lambda \mu^+ \nu_\mu$	2.0	$2.0 \pm 0.7$
$\Lambda_b \rightarrow \Lambda_c e^- \bar{\nu}_e$	6.6	$6.5^{+3.2}_{-2.5}$
$\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu$	6.6	
$\Lambda_b \rightarrow \Lambda_c \tau^- \bar{\nu}_\tau$	1.8	

TABLE V. Asymmetry parameter  $\alpha$  in the semileptonic decays of heavy baryons.

Mode	Our results	Data [52]
$\Lambda_c \rightarrow \Lambda e^+ \nu_e$	0.828	$0.86 \pm 0.04$
$\Lambda_c \rightarrow \Lambda \mu^+ \nu_\mu$	0.825	
$\Lambda_b \rightarrow \Lambda_c e^- \bar{\nu}_e$	0.831	
$\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu$	0.831	
$\Lambda_b \rightarrow \Lambda_c \tau^- \bar{\nu}_\tau$	0.731	



## Rare baryon decays:

$$\Lambda_b \rightarrow \Lambda \ell^+ \ell^- \quad (\ell = e, \mu, \tau) \quad \text{and} \quad \Lambda_b \rightarrow \Lambda \gamma$$

our result:  $\text{BR}(\Lambda_b \rightarrow \Lambda \mu^+ \mu^-) = 1.0 \cdot 10^{-6}$

recent LHCb result:

$\Gamma(\Lambda \mu^+ \mu^-) / \Gamma_{\text{total}}$	<i>DOCUMENT ID</i>	<i>TECN</i>	<i>COMMENT</i>
<i>VALUE</i> (units $10^{-7}$ )			
<b><math>10.8 \pm 2.8</math> OUR AVERAGE</b>			
$9.6 \pm 1.6 \pm 2.5$	<sup>40</sup> AAIJ	13AJ LHCb	$pp$ at 7 TeV
$17.3 \pm 4.2 \pm 5.5$	AALTONEN	11AI CDF	$p\bar{p}$ at 1.96 TeV

and the prediction:  $\text{BR}(\Lambda_b \rightarrow \Lambda \gamma) = 0.4 \cdot 10^{-5}$

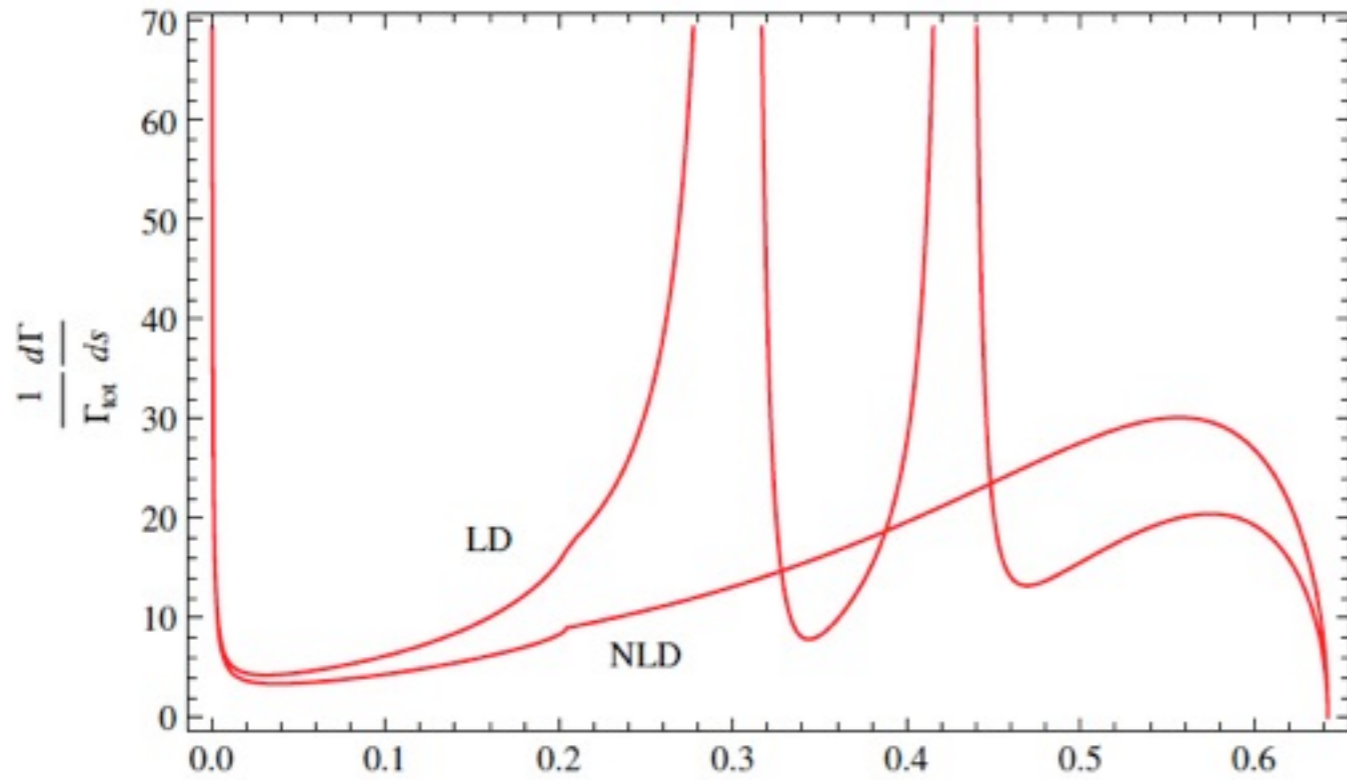
compared to:

$\Gamma(\Lambda \gamma) / \Gamma_{\text{total}}$	<i>CL%</i>	<i>DOCUMENT ID</i>	<i>TECN</i>	<i>COMMENT</i>
<i>VALUE</i>				
<b><math>&lt; 1.3 \times 10^{-3}</math></b>	90	ACOSTA	02G CDF	$p\bar{p}$ at 1.8 TeV



differential rate

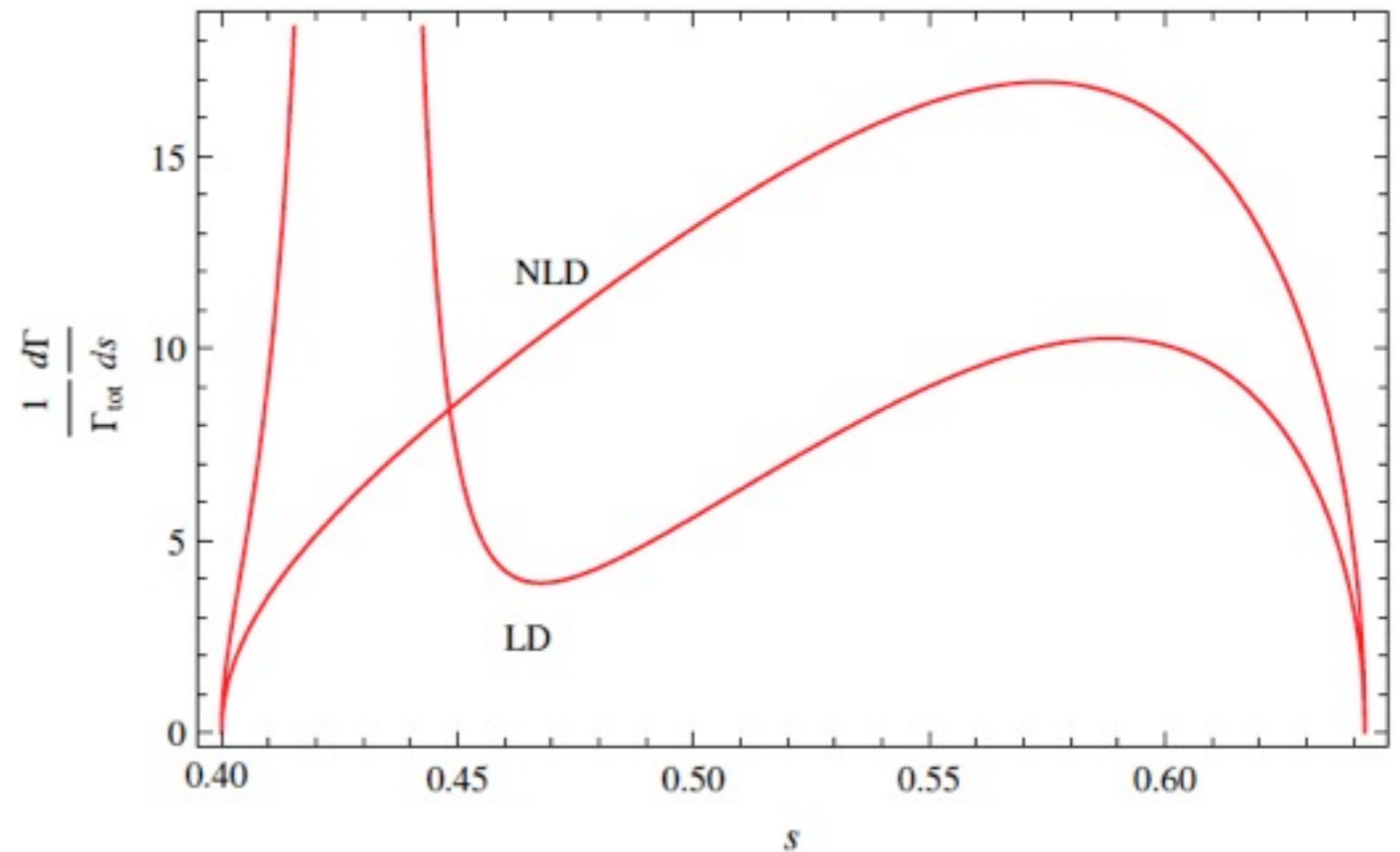
$$\frac{1}{\Gamma_{\text{Tot}}} \frac{d\Gamma(\Lambda_b \rightarrow l^+ l^-)}{ds}$$



$e^+ e^-$

$$s \equiv q^2 / M_{\Lambda_b}^2$$

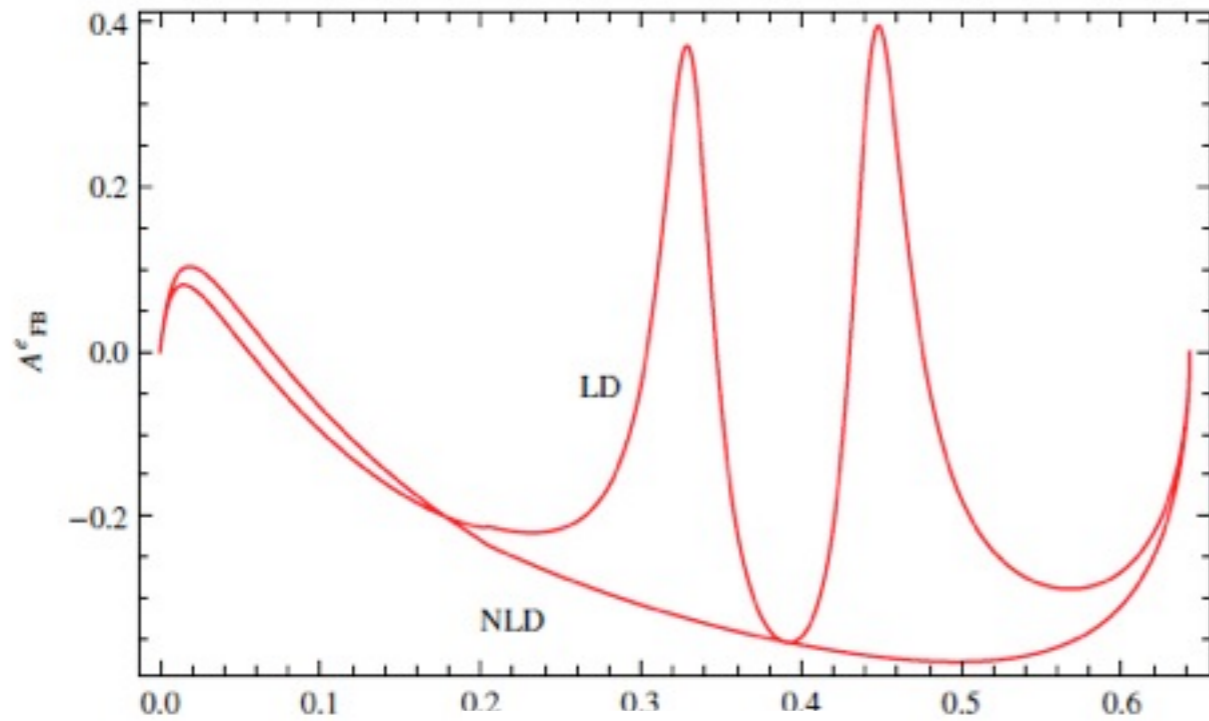
$\tau^+ \tau^-$





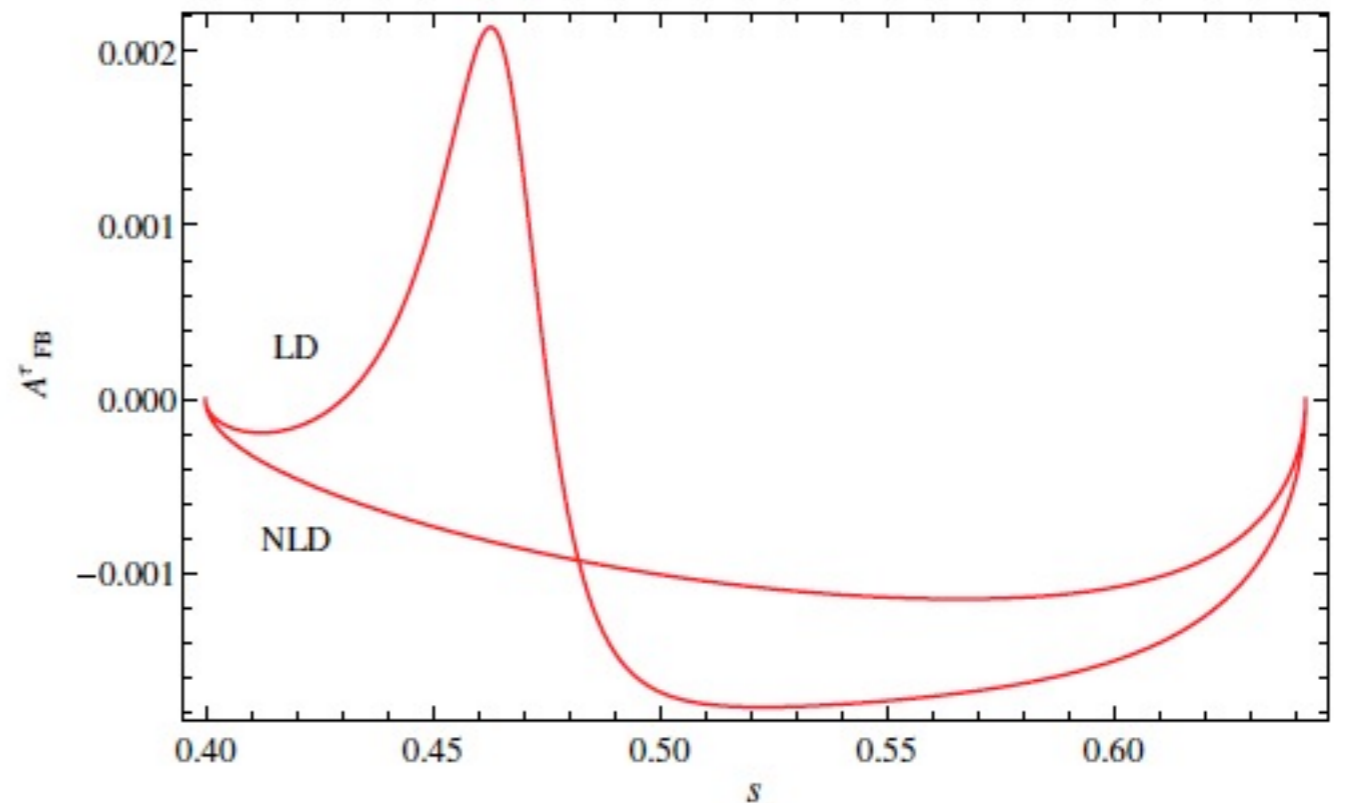
# forward-backward asymmetry

$$A_{\text{FB}} = \frac{\int_0^1 d(\cos\vartheta) - \int_{-1}^0 d(\cos\vartheta)}{\int_0^1 d(\cos\vartheta) + \int_{-1}^0 d(\cos\vartheta)}$$



$$s \equiv q^2 / M_{\Lambda_b}^2$$

$e^+e^-$



$\tau^+ \tau^-$



## Focus on semileptonic decay:

$$\Lambda_b \rightarrow \Lambda_c + \tau^- + \bar{\nu}_\tau$$

TG, M. Ivanov, J. Körner, V. Lyubovitskij, P. Santorelli, N. Habyl, PRD 91, 074001 (2015)

- tests of a key property of the SM: lepton flavor universality
- deviations would signal possible NP
- constraints on NP are weaker for the third generation
- discrepancies with SM results in B decays:

$$R(\mathcal{D}) \equiv \frac{\text{Br}(\bar{B} \rightarrow \mathcal{D}\tau^-\bar{\nu}_\tau)}{\text{Br}(\bar{B} \rightarrow \mathcal{D}\ell^-\bar{\nu}_\ell)}$$

$$(\mathcal{D} = D, D^*; \ell = e, \mu)$$

$$R(D) = \begin{cases} 0.305 \pm 0.012 & \text{SM} \\ 0.421 \pm 0.058 & \text{BABAR \& Belle,} \end{cases}$$

$$R(D^*) = \begin{cases} 0.252 \pm 0.004 & \text{SM} \\ 0.337 \pm 0.025 & \text{BABAR \& Belle.} \end{cases}$$

$$0.336 \pm 0.027 \pm 0.030$$

LHCb 2015



# $\Lambda_b$ with spin 1/2 has a complex angular distribution

Mode	Our results	Data
$\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu_e$	2.72	$2.74 \pm 0.82$
$\Lambda_b^0 \rightarrow \Lambda_c^+ e^- \bar{\nu}_e$	6.9	$6.5^{+3.2}_{-2.5}$
$\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau$	2.0	

rates in %

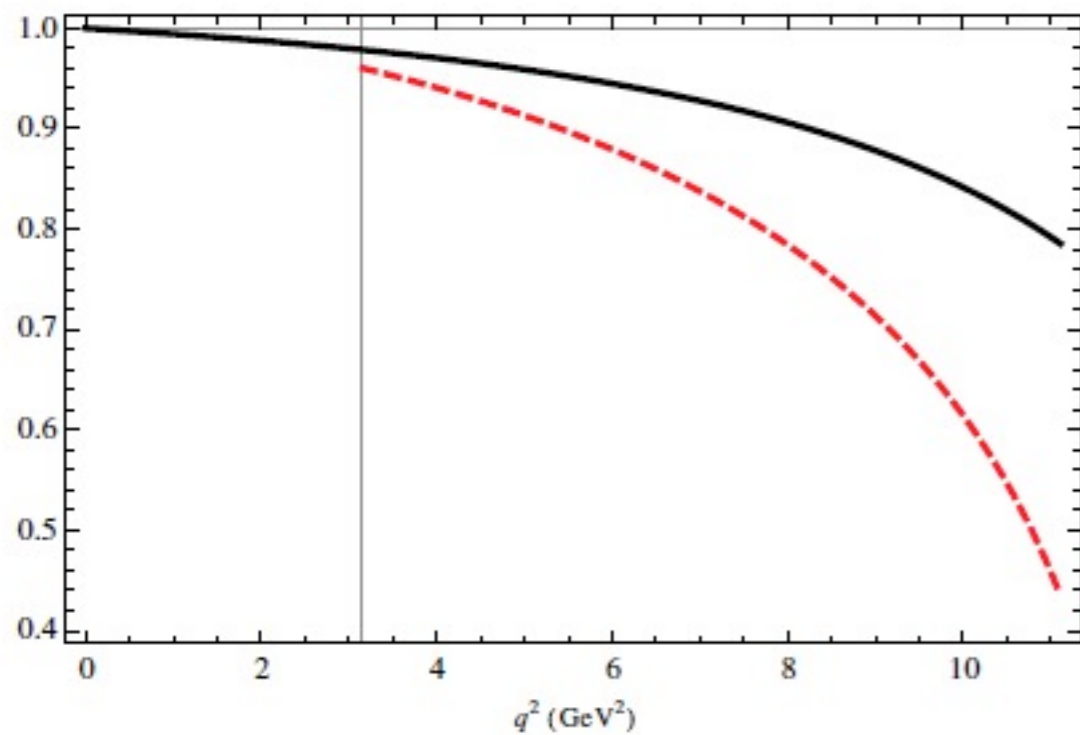


FIG. 9 (color online). The  $q^2$  dependence of the total  $\Lambda_c$  polarization  $|\vec{P}^h|(q^2) = \sqrt{(P_x^h)^2 + (P_z^h)^2}$  for the  $e^-$  (solid) and  $\tau^-$  (dashed) modes.

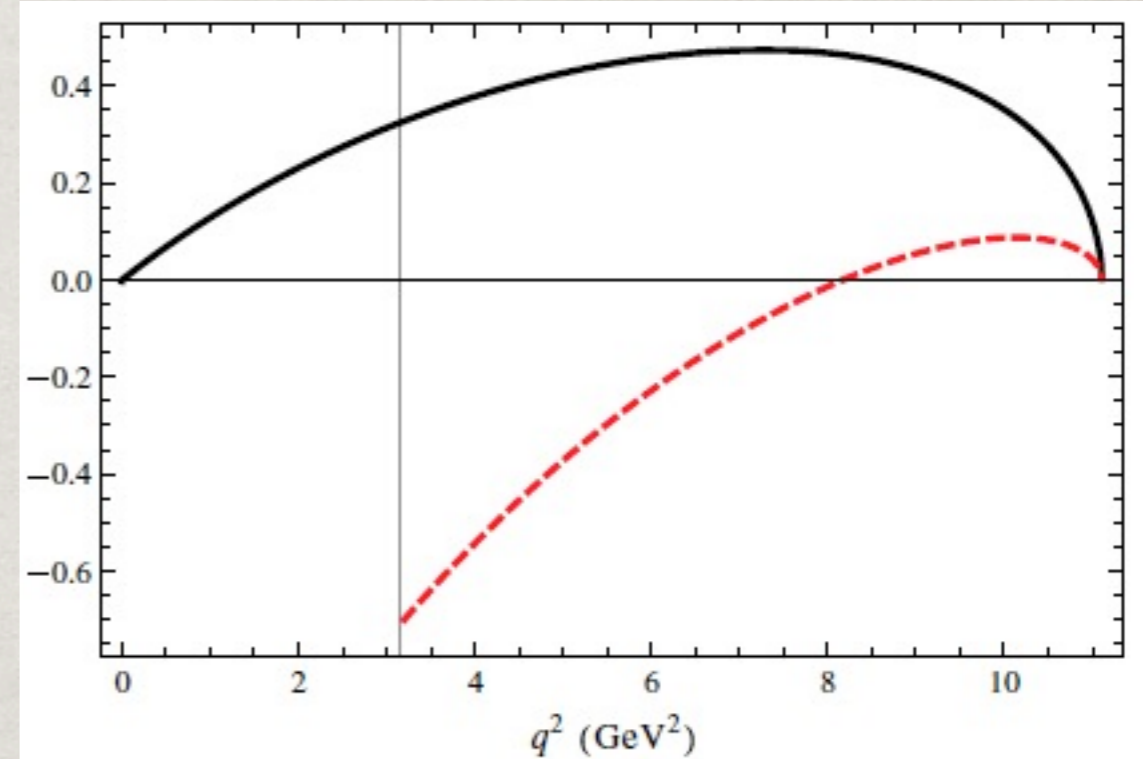


FIG. 5 (color online). The  $q^2$  dependence of the lepton-side forward-backward asymmetry  $A_{FB}^\ell(q^2)$  for the  $e^-$  (solid) and  $\tau^-$  (dashed) modes.

forward-backward  
asymmetries

polarization  
observables



# finally

- quark model: „old-fashioned“ but reliable tool in describing conventional hadron structure
- here: covariant confined quark model, quantum field theory tool for analyzing hadronic properties
- light hadron sector
- heavy hadrons -- lab to constrain SM and BSM physics
- looking forward to LHCb among others
- extension to multiquark configurations