

# Inflating with Goldstone bosons

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& Veronica Sanz, Jack Setford; arXiv:1503.08097

& Veronica Sanz JCAP 02 (2015) 008; arXiv:1411.7809

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# What I'll talk about

- Challenges for inflationary model building:
  - Exceptionally flat potential (\*)
  - Robustness against UV corrections (\*\*)
- Pseudo Goldstone (pGB) modes make attractive inflaton candidates as they are (or can be) natural
  - Automatically explain (\*)
  - Particular models also satisfy (\*\*)
- CMB data motivate a minimal single field model with a unique potential

# Inflation recap

- Experimentally supported paradigm still lacking fundamental understanding
- Solves traditional problems in cosmology + offers framework for structure formation
- CMB data: power spectrum of density fluctuations  $\Delta(k)$   
$$n_s - 1 = \frac{d \log \Delta_s^2}{d \log k} \quad r = \frac{\Delta_t^2(k)}{\Delta_s^2(k)}$$
- Popular: single scalar field slow roll models

# CMB data: power spectrum of density fluctuations

$$\Delta_{s,t}(k) = A_{s,t} \left( \frac{k}{k_*} \right)^{(n_{s,t}-1) + \frac{1}{2} dn_{s,t}/d \log k \log(k/k_*) + \dots}$$

# CMB data: power spectrum of density fluctuations

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$\mathbf{r}$

$\mathbf{n}_s$

# Inflation recap

- Single field slow roll inflation (SRA)

$$\epsilon = \frac{\tilde{M}_p^2}{2} \left( \frac{V'(\phi)}{V(\phi)} \right)^2 \ll 1 \text{ and } \eta = \tilde{M}_p^2 \frac{V''(\phi)}{V(\phi)} \ll 1$$

- Amount of inflation (CMB:  $N \approx 60$ )

$$N = \log \frac{a(t_e)}{a(t_i)} = \int_{t_i}^{t_e} H dt \rightarrow N = \frac{1}{\sqrt{2}M_p} \int_{\phi_E}^{\phi_I} \frac{1}{\sqrt{\epsilon}}$$

- Observables can be expressed in SRA

$$n_s = 1 - 6\epsilon + 2\eta \quad r = 16\epsilon$$

# The hierarchy problem (\*)

- Sufficient inflation + amplitudes of CMB anisotropy:  $V(\phi)$  width  $\gg$  height
  - Scale of inflation ( $\sim$ height):  $\sim$ GUT scale
  - Field excursion (width):  $\sim$ Planck scale (Lyth bound)

$$\Lambda^4 = (2.2 \times 10^{16} \text{ GeV})^4 \frac{r}{.2} \quad \Delta\phi \geq M_p \sqrt{\frac{r}{4\pi}}$$

- Flat potential generically unstable under radiative corrections

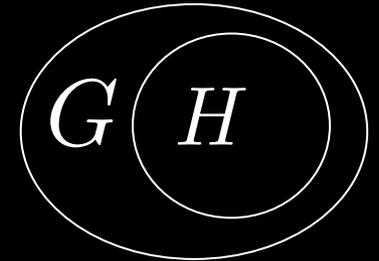
# Why a pGB?

- A shift symmetry can protect the potential

$$\phi = \phi + C$$

- The inflaton is the Goldstone boson of the breaking of a global symmetry  $G$  to subgroup  $H$  at scale  $f$

– Potential forbidden by shift symmetry



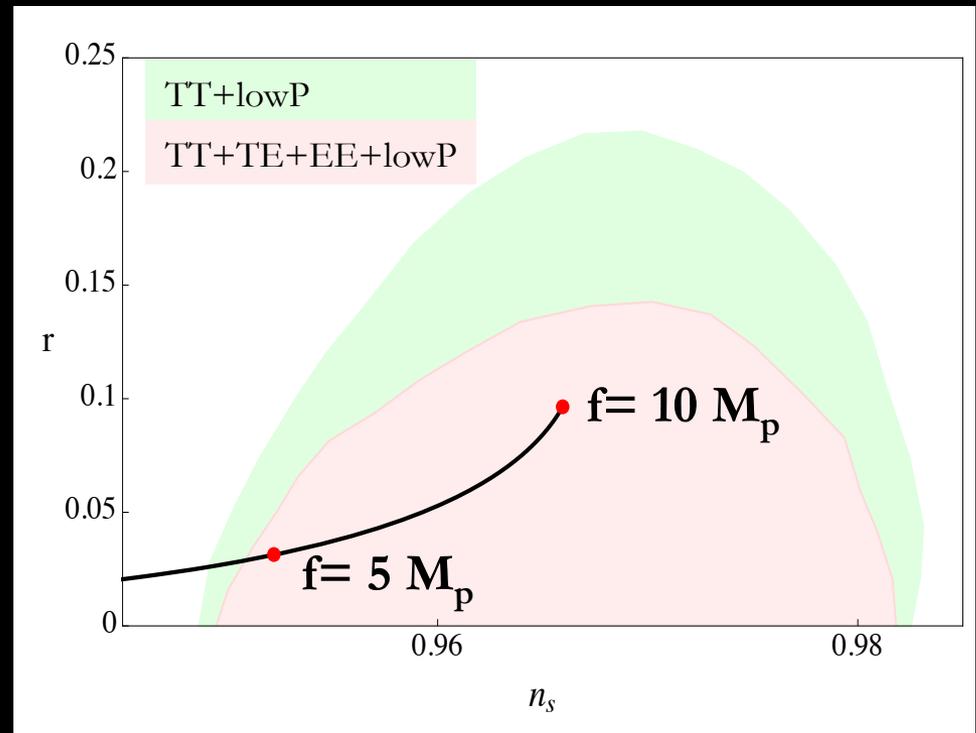
- Small potential generated when  $G$  is not exact
  - Well known examples: axions, pions, ...

# The pGB inflaton we already knew...

- Natural Inflation<sup>TM</sup>
  - pGB is an axion

$$V(\phi) = \Lambda^4 \left( 1 + \cos \frac{\phi}{f} \right)$$

- NI<sup>TM</sup> + CMB:



Freese, Frieman, Olinto (PRL, 1990)

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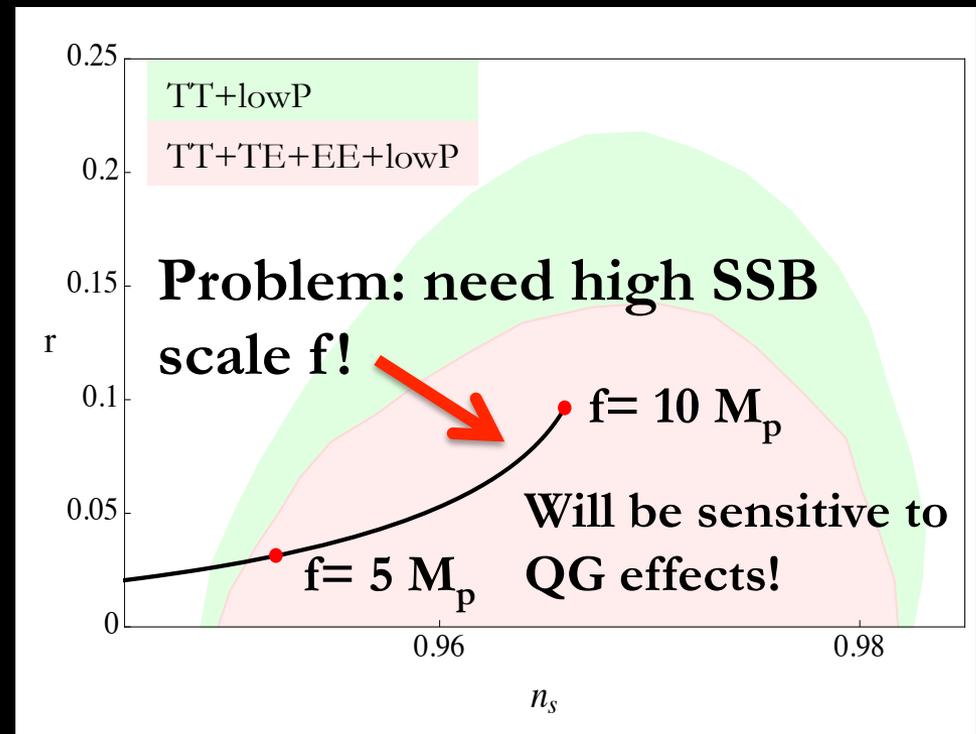
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– (\*) ✓

– (\*\*) ✗



Freese, Frieman, Olinto (PRL, 1990)

# UV Robustness (\*\*)

- Quantum Gravity **does not preserve global symmetries (explicitly break G)**
  - Realistic potential will have large UV corrections
  - Demonstrated explicitly

Kallosh, Linde, Linde,  
Susskind, arXiv:9502069

Montero, Uranga, Valenzuela,  
arXiv:1503.03886
- Not robust against UV corrections
- pGB inflation (such as  $\text{NI}^{\text{TM}}$ ) with  $f > M_p$  is not a good effective theory, i.e. **predictivity is lost**

Can we find models with a  
pGB inflaton and with sub-Planckian scales?

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pGB inflaton and with sub-Planckian scales?

Exceptionally flat  
potential (\*)



Robustness against  
UV corrections (\*\*)



# Yes!

We show that the minimal cosmologically motivated<sup>Ⓢ</sup> potential for a pGB inflaton is:

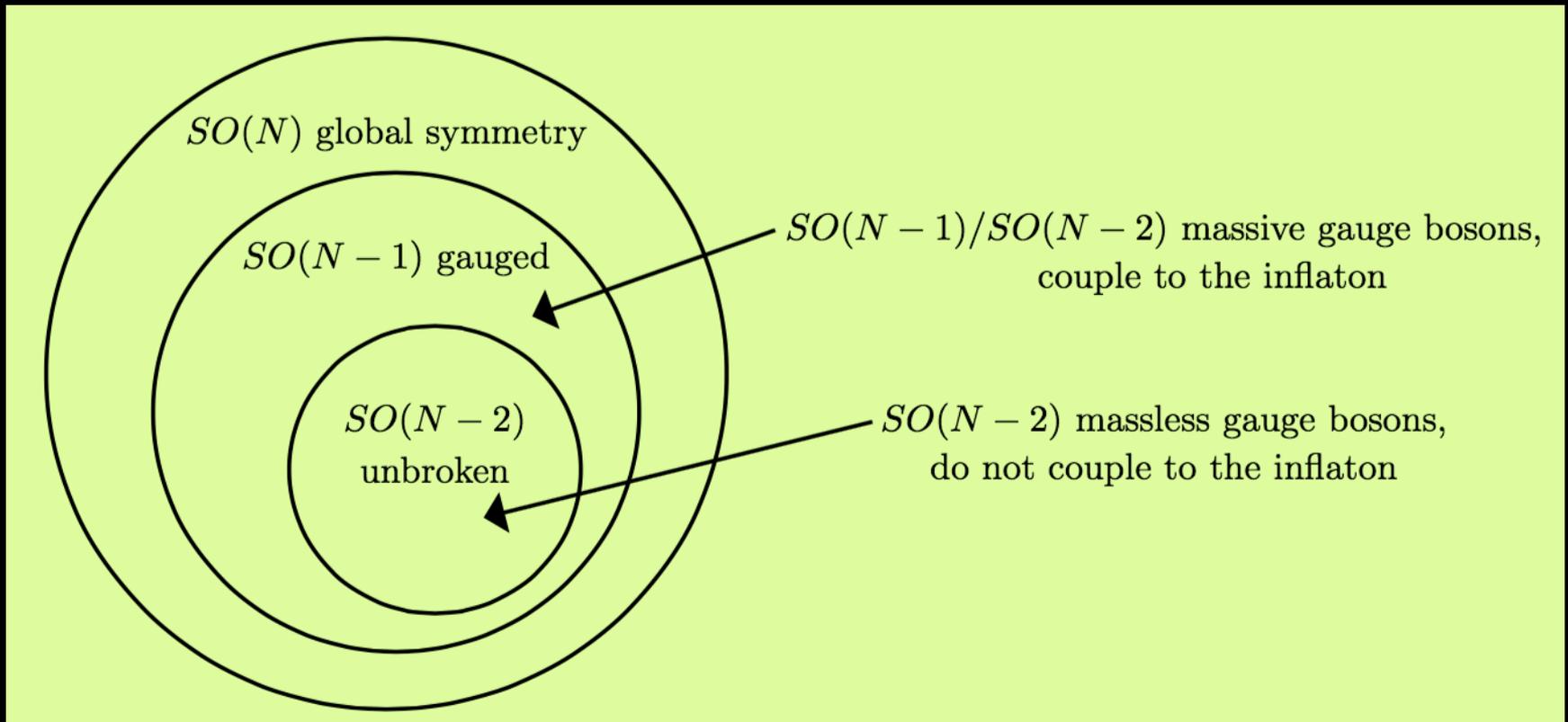
$$V(\phi) = \Lambda^4 \left( C_\Lambda + \alpha \cos \phi/f + \beta \sin^2 \phi/f \right)$$

With  $f$  and  $\Lambda$  sub-Planckian.

<sup>Ⓢ</sup>Hilltop models are preferred by CMB data  
(Martin, Ringeval, Trota, Vennin JCAP 1403 (2014) 039)

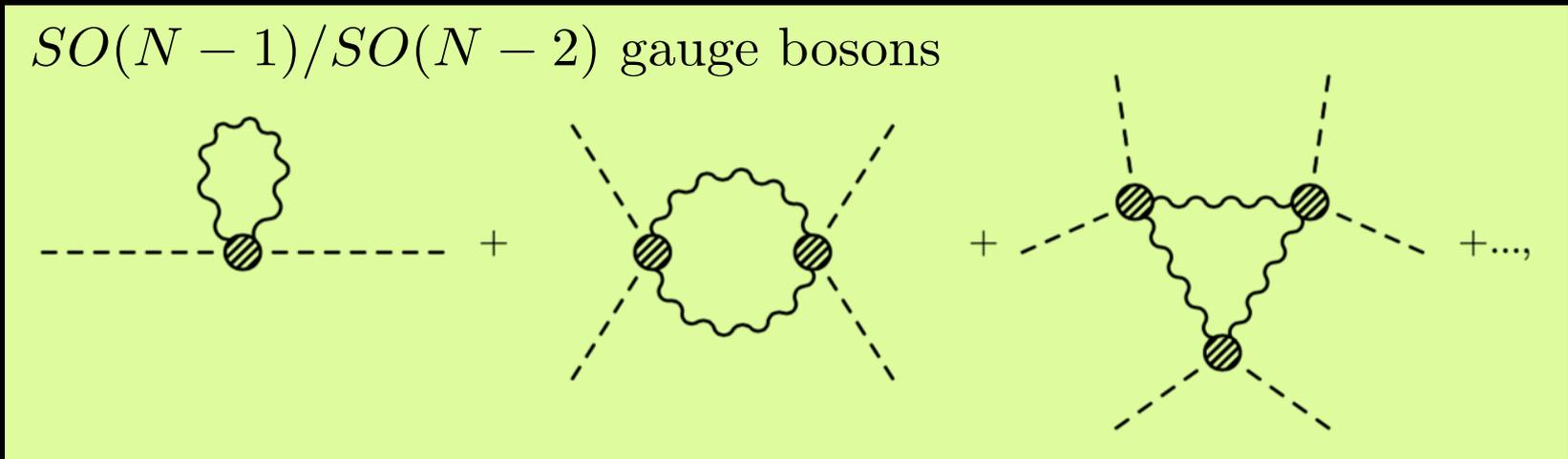
# EFT for pGBs: CCWZ

Callan, Coleman, Wess and Zumino (CCWZ), PRL 1969



# CCWZ (gauge fields)

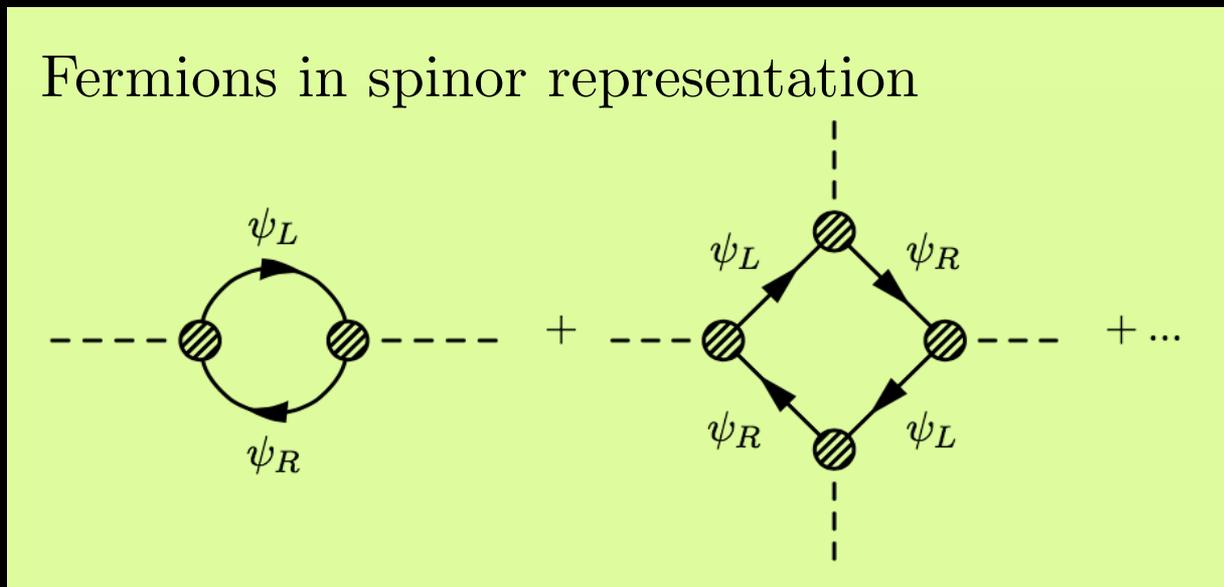
- Coleman Weinberg potential at 1-loop



- Resumming diagrams:  $V(\phi) = \beta_b \sin^2 \phi / f$

# CCWZ (fermions)

- Coleman Weinberg potential at 1-loop

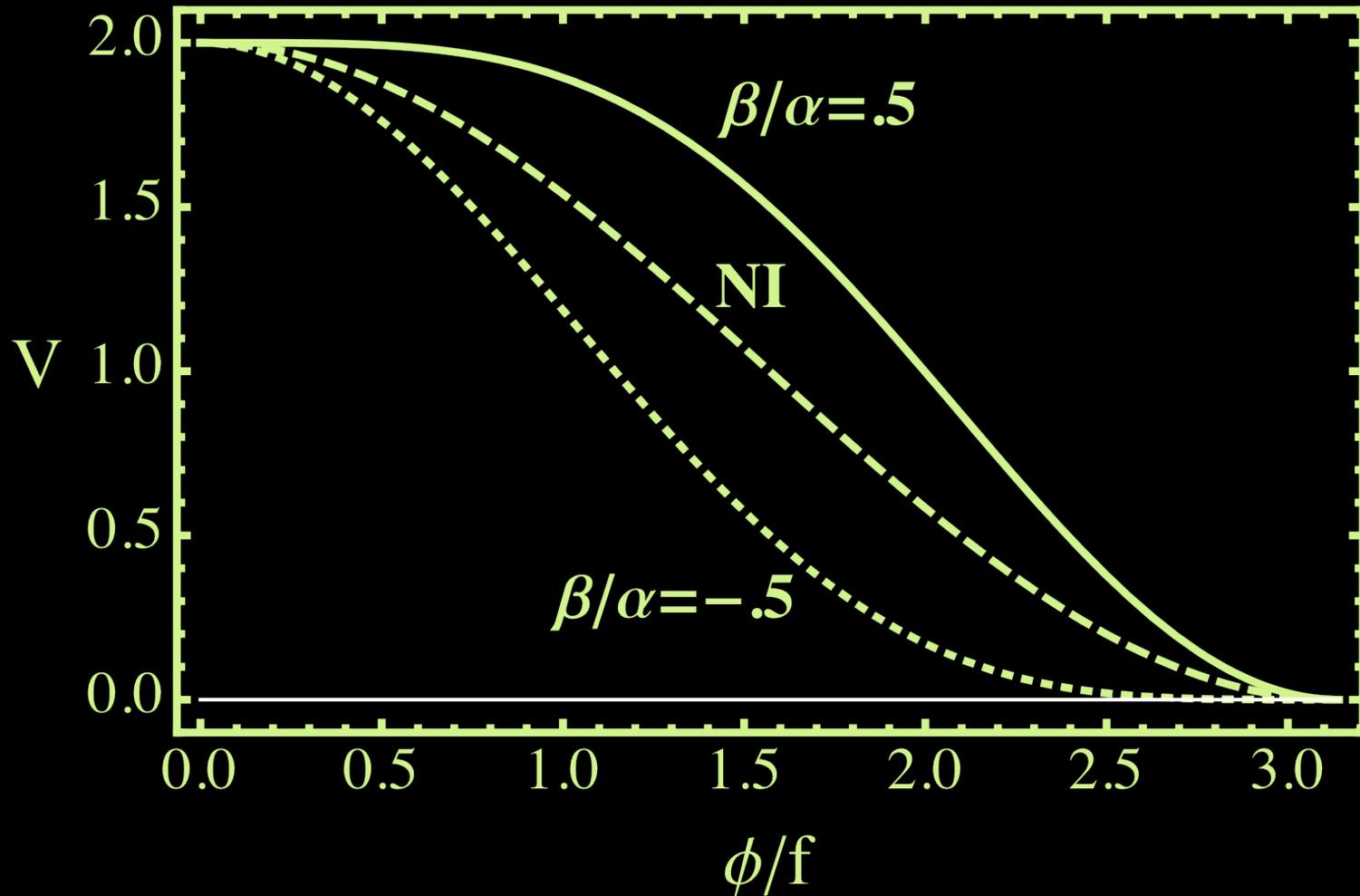


- Resumming diagrams:

$$V(\phi) = \alpha \cos \phi/f + \beta_f \sin^2 \phi/f$$

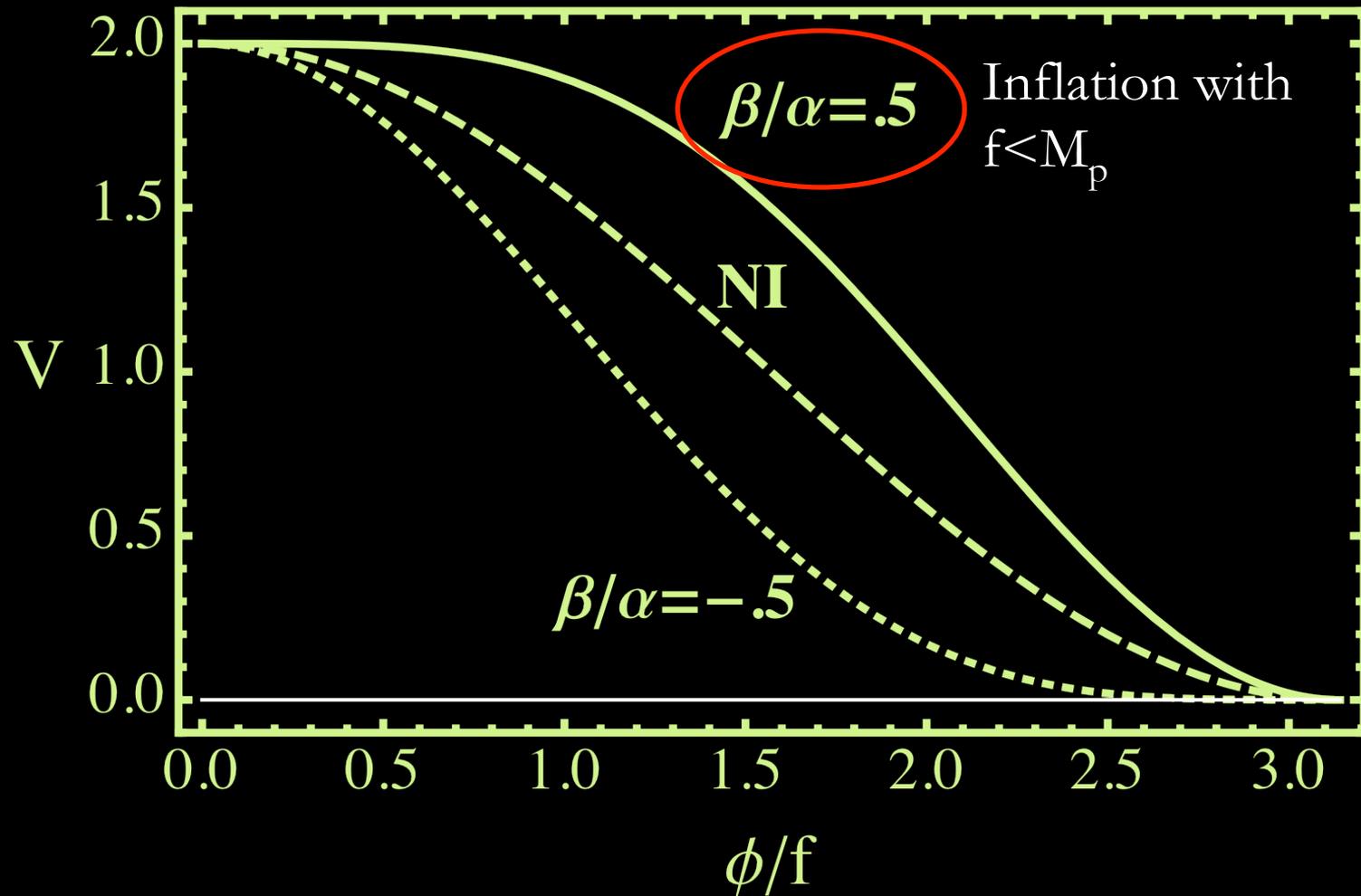
Bosonic + Fermionic contributions:

$$V(\phi) = \Lambda^4 \left( C_\Lambda + \alpha \cos \phi/f + \beta \sin^2 \phi/f \right)$$

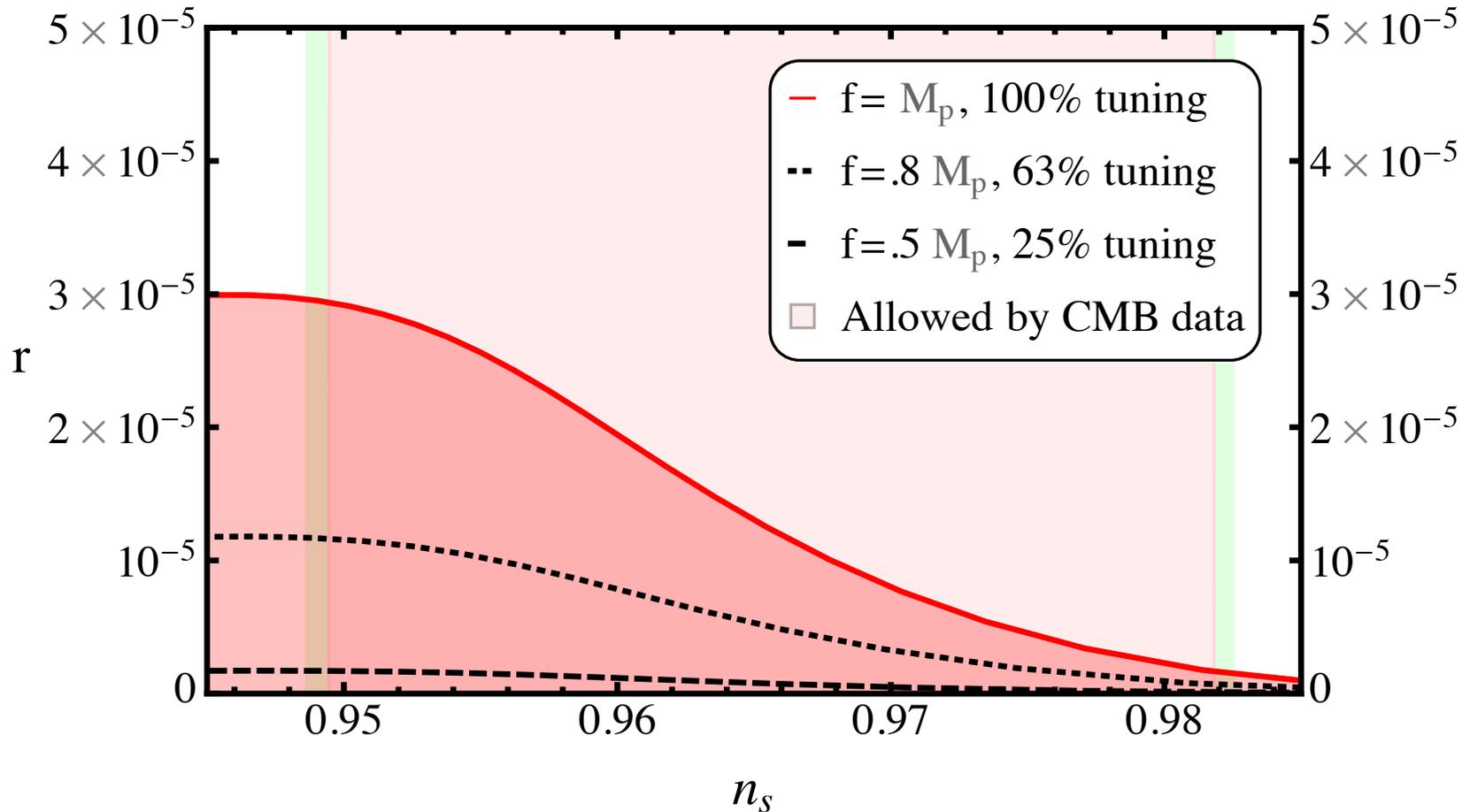


Bosonic + Fermionic contributions:

$$V(\phi) = \Lambda^4 \left( C_\Lambda + \alpha \cos \phi/f + \beta \sin^2 \phi/f \right)$$



# $V(\phi)$ and Planck (2015) data



# Portal to the UV theory

- $\beta / \alpha \approx 1/2$  is a relation between fermions and bosons of the UV sector:

$$\alpha = \alpha \left( \frac{\Pi_1^L}{\Pi_0^L}, \frac{\Pi_1^R}{\Pi_0^R} \right) \quad \beta = \beta \left( \frac{\Pi_1^A}{\Pi_0^A}, \frac{M^2}{\Pi_0^L \Pi_0^R} \right)$$

- Indicates a symmetry in the UV sector
  - Similar example: cancelations between resonances in walking Technicolor models
  - Can think of inflation as a BC for the UV theory

(Hirn & Sanz, arXiv:0807.2465;  
Agashe, Csaki, Grojean & Reece,  
arXiv:0704.1821)

# To Conclude

- Goldstone models solve the hierarchy problem of inflation (\*): a flat potential is natural
- A good effective theory also has sub-Planckian scales (\*\*)

- The unique form of single field pGB inflation satisfying (\*) and (\*\*) is

$$V(\phi) = \Lambda^4 \left( C_\Lambda + \alpha \cos \phi/f + \beta \sin^2 \phi/f \right)$$

- Compatible with CMB data

Thank you!

Please ask me questions!

# Backup slides

CCWZ

Fine-tuning

Non-Gaussianity

Uniqueness of  $V(\phi)$

# CCWZ (gauge fields)

Parameterize GBs as  $\Sigma(x)$

$$\Sigma(x) = \Sigma_0 \exp(iT^{\hat{a}} \phi^{\hat{a}}(x)/f)$$



SO(N) GB Lagrangian (low energy)

$$\mathcal{L}_{eff} = \frac{1}{2}(P_T)^{\mu\nu} [\Pi_0^A(p^2) \text{Tr}(A_\mu A_\nu) + \Pi_1^A(p^2) \Sigma^T A_\mu A_\nu \Sigma]$$



Set to zero unphysical fields

$$\mathcal{L}_{eff} = \frac{1}{2}(P_T)^{\mu\nu} \left[ \Pi_0^A(p^2) + \frac{1}{2} \Pi_1^A(p^2) \sin^2(\phi/f) \right] A_\mu^{\tilde{a}} A_\nu^{\tilde{a}}$$

# Fine-tuning

- Customary definition

$$\Delta = \left| \frac{\partial \log n_s}{\partial \log \tilde{\beta}} \right| = \left| \frac{\tilde{\beta}}{n_s} \frac{\partial n_s}{\partial \tilde{\beta}} \right| \approx [1.02 - 1.05] \left( \frac{f}{M_p} \right)^{-2}$$

- In percentage,

$$\text{Percentage tuning} = \frac{100}{\Delta} \% \approx 95 \left( \frac{f}{M_p} \right)^2 \%$$



# Speed of sound / non Gaussianity

- Goldstone modes have strong momentum dependent self-couplings

- $\chi$ PT:

$$\mathcal{L} = \sum_n \frac{c_n}{f^{2n-4}} X^n, \quad \text{with } X = \frac{1}{2} \partial_\mu \Sigma \partial^\mu \Sigma^\dagger$$

- Implies a nontrivial speed of sound  $\left( f_{NL}^{eq} \sim \frac{1}{c_s^2} \right)$ 
  - Imprinted in the CMB as non-Gaussianity

# Speed of sound / non Gaussianity

- Inflation breaks Lorentz invariance. Non-canonical kinetic term implies

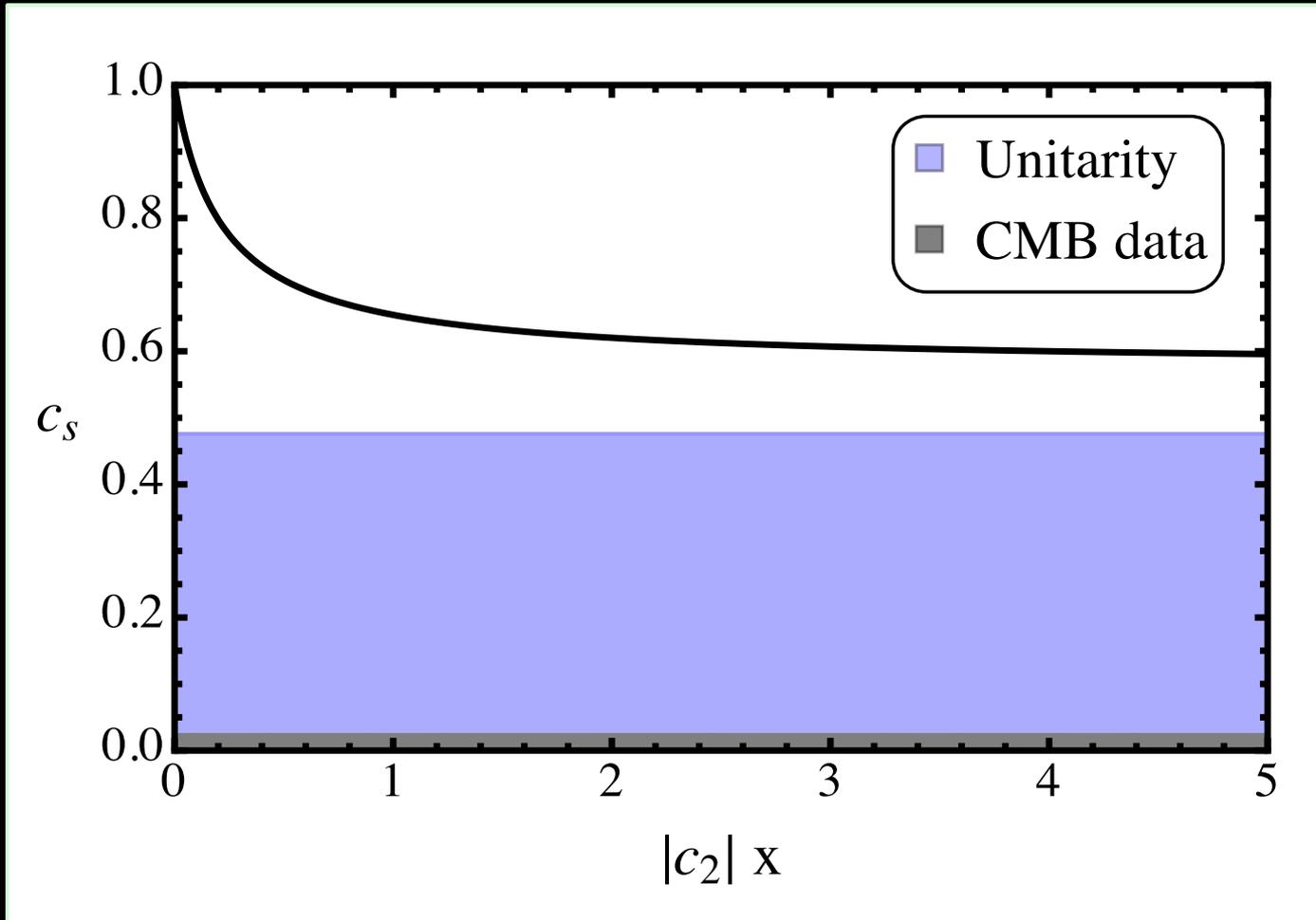
$$(\partial_\mu\phi)^2 = (\partial_t\phi)^2 - (\partial_i\phi)^2 \rightarrow (\partial_t\phi)^2 - c_s^2(\partial_i\phi)^2$$

$$c_s = \left(1 + 2\frac{2c_2x}{1 + 2c_2x}\right)^{-1/2} \quad \text{with } x = X/f^2$$

- EFT breaks down for:

$$\Lambda_u^4 = \frac{24\pi}{5} \left( \frac{2M_p^2 |\dot{H}| (c_s)_*^5}{1 - (c_s)_*^2} \right) < f^4$$

# Speed of sound prediction



# Uniqueness of $V(\phi)$

- Instead using fermions in a vector representation of  $SO(N)$  yields

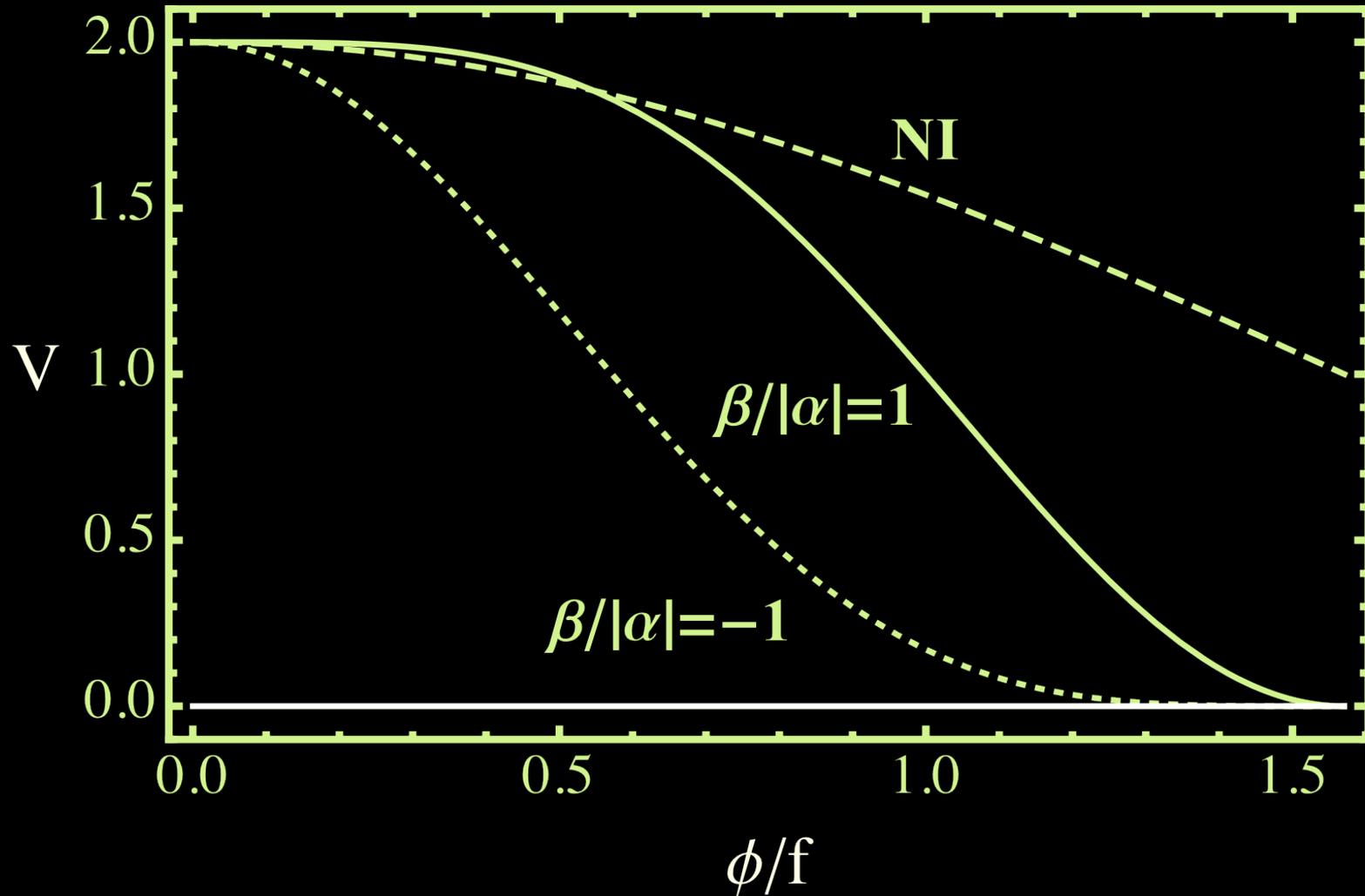
$$V(\phi) = \alpha \sin^2(\phi/f) + \beta \sin^2(\phi/f) \cos^2(\phi/f)$$

- Hilltop model (good!) for  $\beta > 0$ , but:

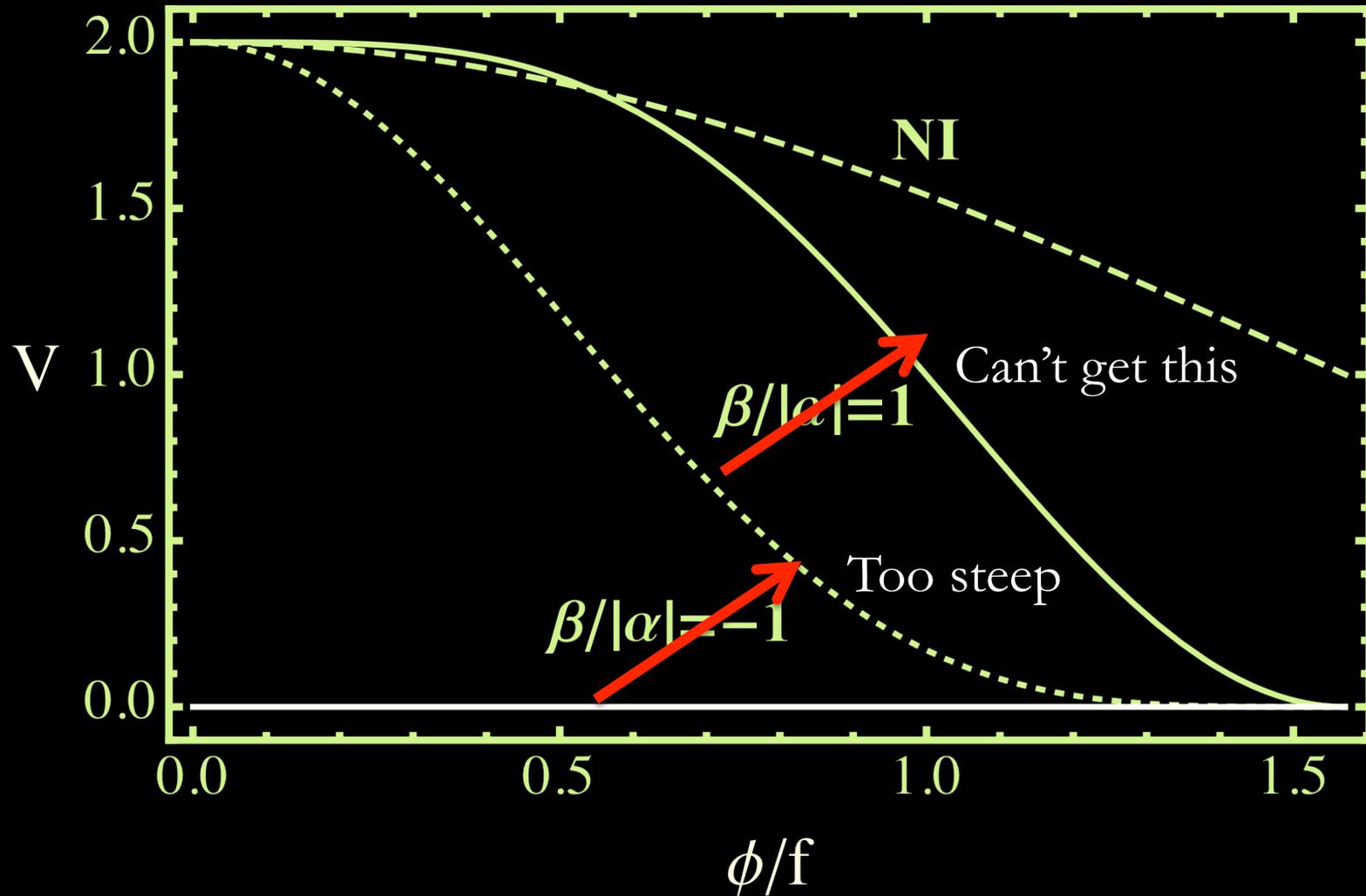
$$\beta = -2N_c \int \frac{d^4 p_E}{(2\pi)^4} \left( \frac{\Pi_1^L \Pi_1^R}{\Pi_0^L \Pi_0^R} + \frac{M^2}{p_E^2 \Pi_0^L \Pi_0^R} \right) < 0$$

- Not good.

Not good.



Not good.



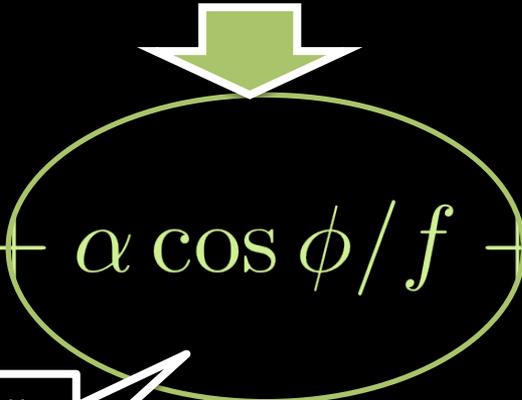
# Inflation?

Not finding a hilltop potential turns out to be generic for models with fermions in vector (or tensor) representations: all invariants in the Lagrangian are with even powers of  $\Sigma(x)$ .

One has to use a spinor representation to get couplings  $\Gamma^a \Sigma^a(x)$ .

# Spinor representations

- With fermions in a spinor rep one finds that the fermions and gauge bosons contribute to terms in the potential at different orders in  $\Sigma(\mathbf{x})$
- As advertised, with fermions in a spinor rep:


$$V(\phi) = \Lambda^4 \left( C_\Lambda + \alpha \cos \phi/f + \beta \sin^2 \phi/f \right)$$

Looking at the group theory in detail one can convince herself that the first term will be a cos (not a sin).