



Weighting Neutrinos



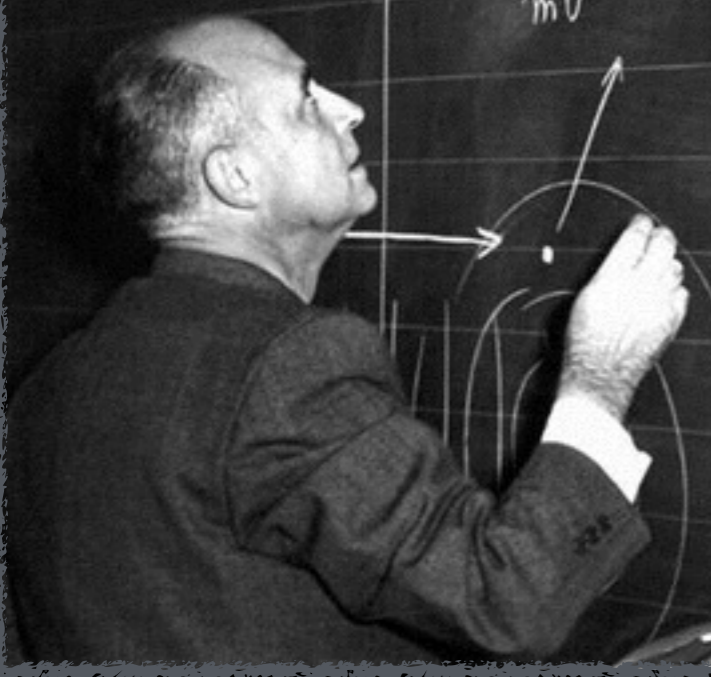
SLAC Summer Institute

August 14th 2015

Joseph A. Formaggio
MIT

onda incidente e^{ikx}

$$\lambda = \frac{h}{mv} = 1,8 \times 10^{-8} \text{ cm}$$



Neutrino mass measurements have a long history in physics, predating the Standard Model itself.

LA MASSA DEL NEUTRINO.

probabilità di transizione (32) determina tra l'altro la forma continuo dei raggi β . Discuteremo qui come la forma di questo spettro dipende dalla massa di quiete del neutrino, in modo da poter determinare questa massa da un confronto con la forma sperimentale dello spettro stesso. La massa μ interviene in (32) tra l'altro nel fattore p^2/v_e . La dipendenza della forma della curva di distribuzione dell'energia da μ , è marcata specialmente in vicinanza della energia massima E_0 dei raggi β . Si riconosce facilmente che la curva di distribuzione per energie E prossime al valore massimo E_0 , si comporta, a meno di un fattore indipendente da E , come

$$(36) \quad \frac{dN}{dE} = \frac{1}{2} (\mu^2 + E_0 - E) \sqrt{(E_0 - E)^2 + 2\mu^2(E_0 - E)}$$

Nella fig. 1 la fine della curva di distribuzione è rappresentata per $\mu = 0$, e per un valore piccolo e uno grande di μ . La maggiore somiglianza con le

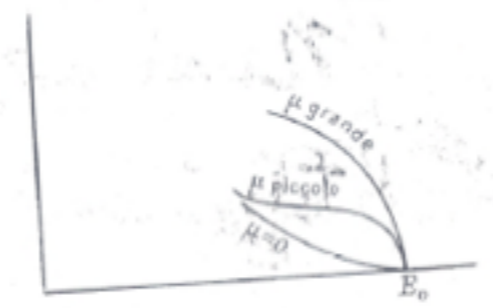


Fig. 1.

$\frac{1}{\alpha} (\mu c^2 + E_0 - E) \sqrt{(E_0 - E)^2 + 2\mu c^2 (E_0 - E)}$
 La fine della curva di distribuzione è rappresentata per $\mu = 0$,
 piccolo e uno grande di μ . La maggiore somiglianza con le

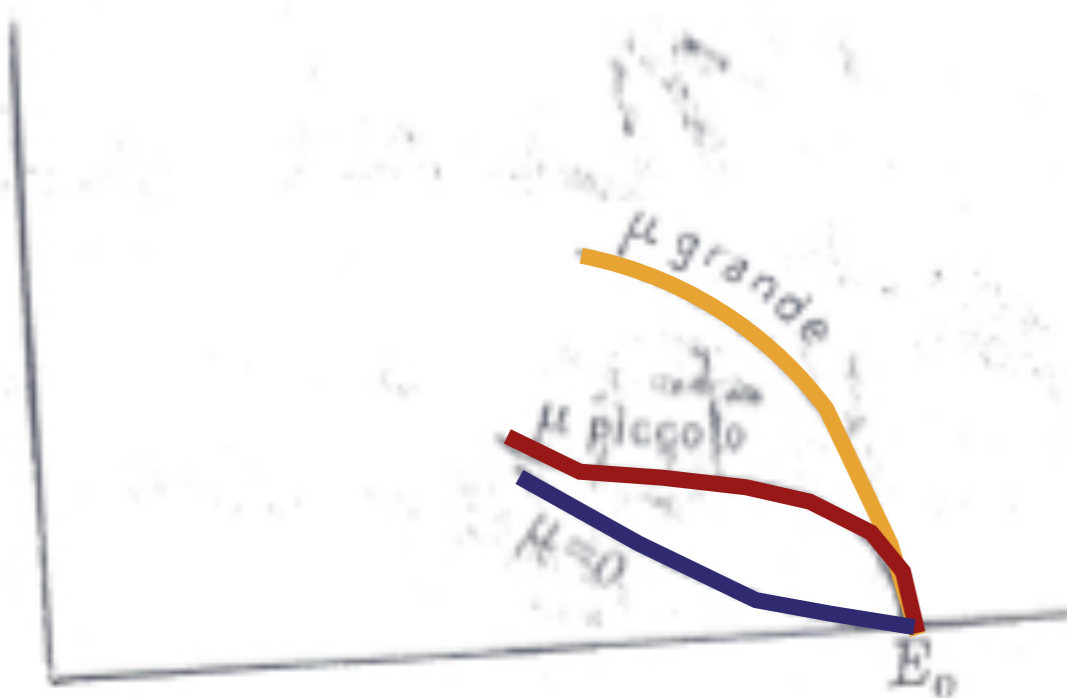
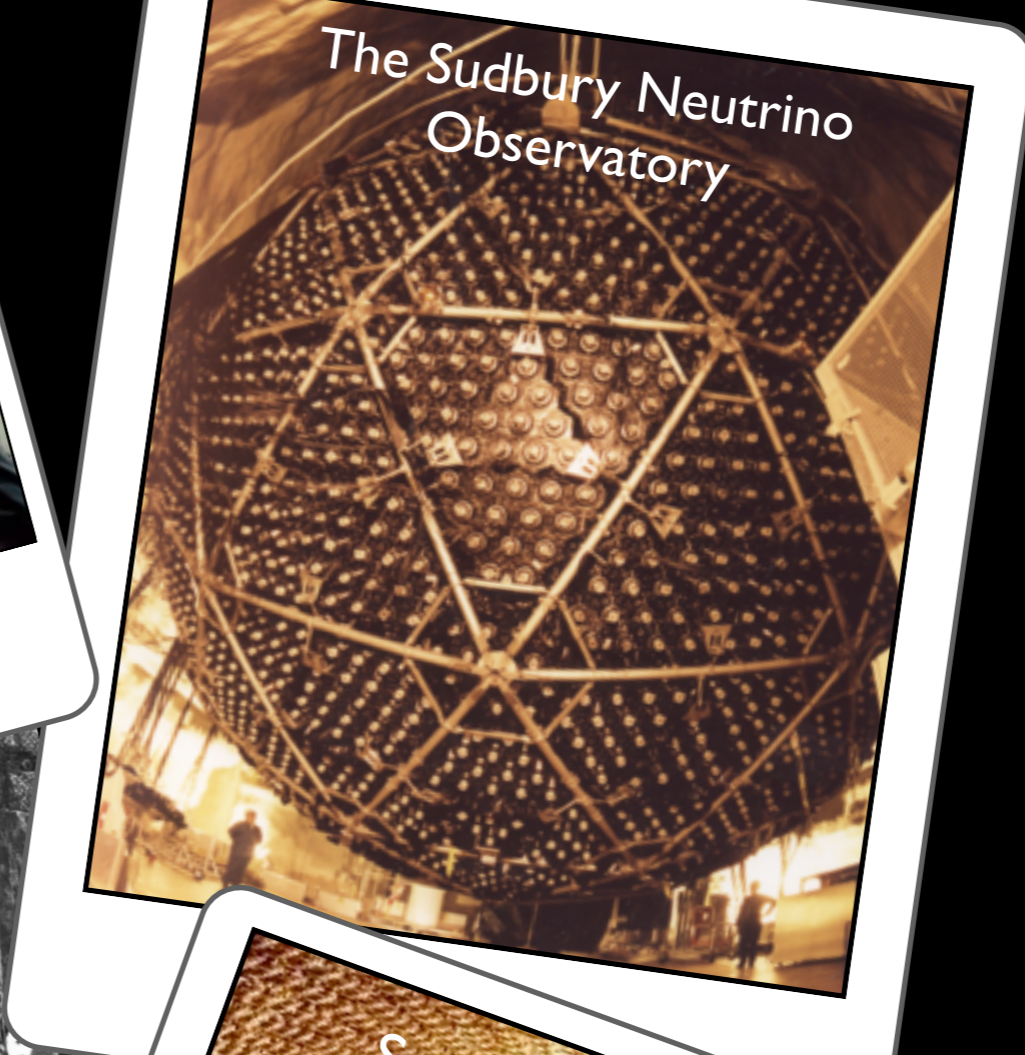


Fig. 1.

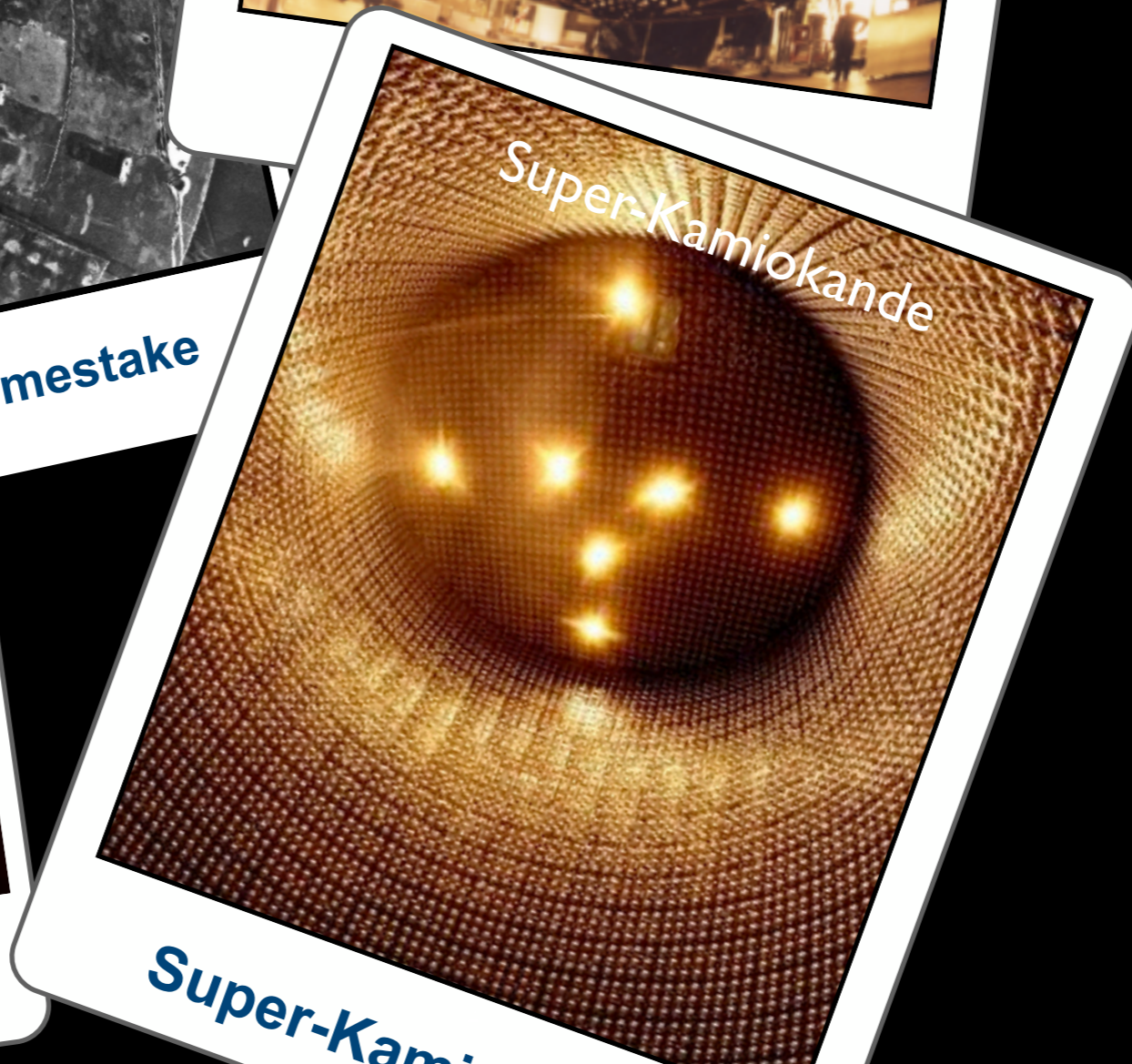
We have learned one thing
in this time.

"Grande" is ruled out.

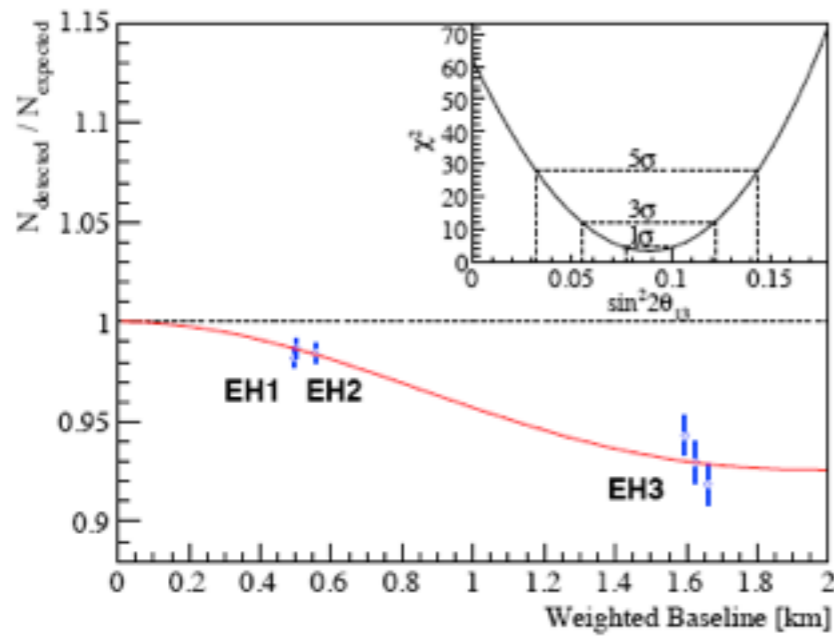
And so is "Zero".



With oscillations firmly in place, we at least understand that the neutrino has a mass



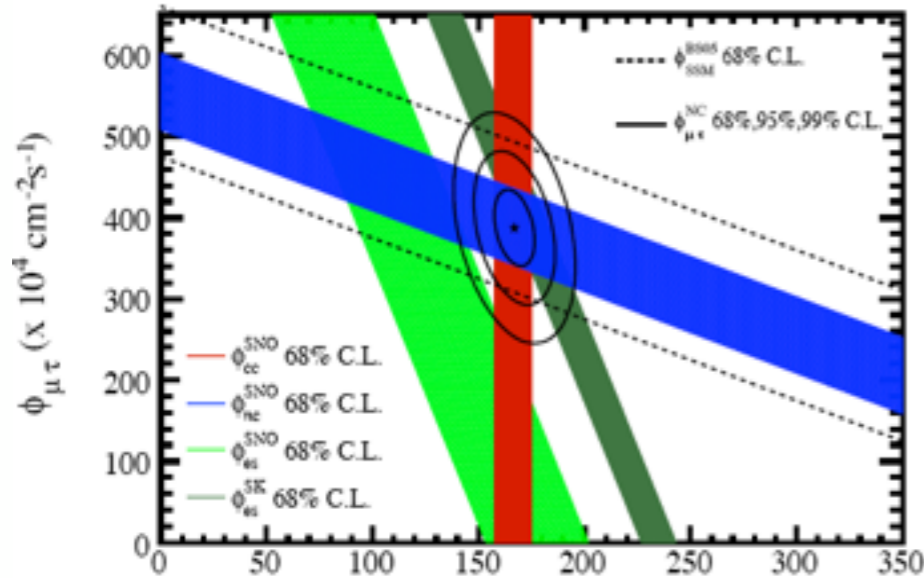
As such, oscillation measurements place a lower limit on the neutrino mass scale.



$$\sin^2(2\theta_{13}) = 0.093 \pm 0.008$$

Reactor & Long Baseline

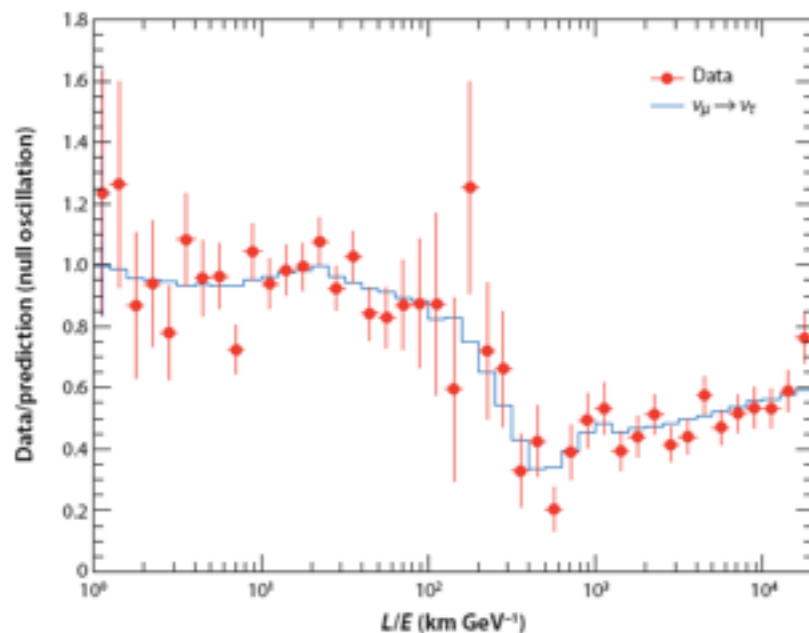
With oscillations firmly in place, we at least understand that the neutrino has a mass



$$\sin^2(2\theta_{12}) = 0.846 \pm 0.021$$

$$\Delta m_{21}^2 = (7.53 \pm 0.18) \times 10^{-5} \text{ eV}^2$$

Solar



$$\sin^2(2\theta_{23}) = 0.999^{+0.001}_{-0.018}$$

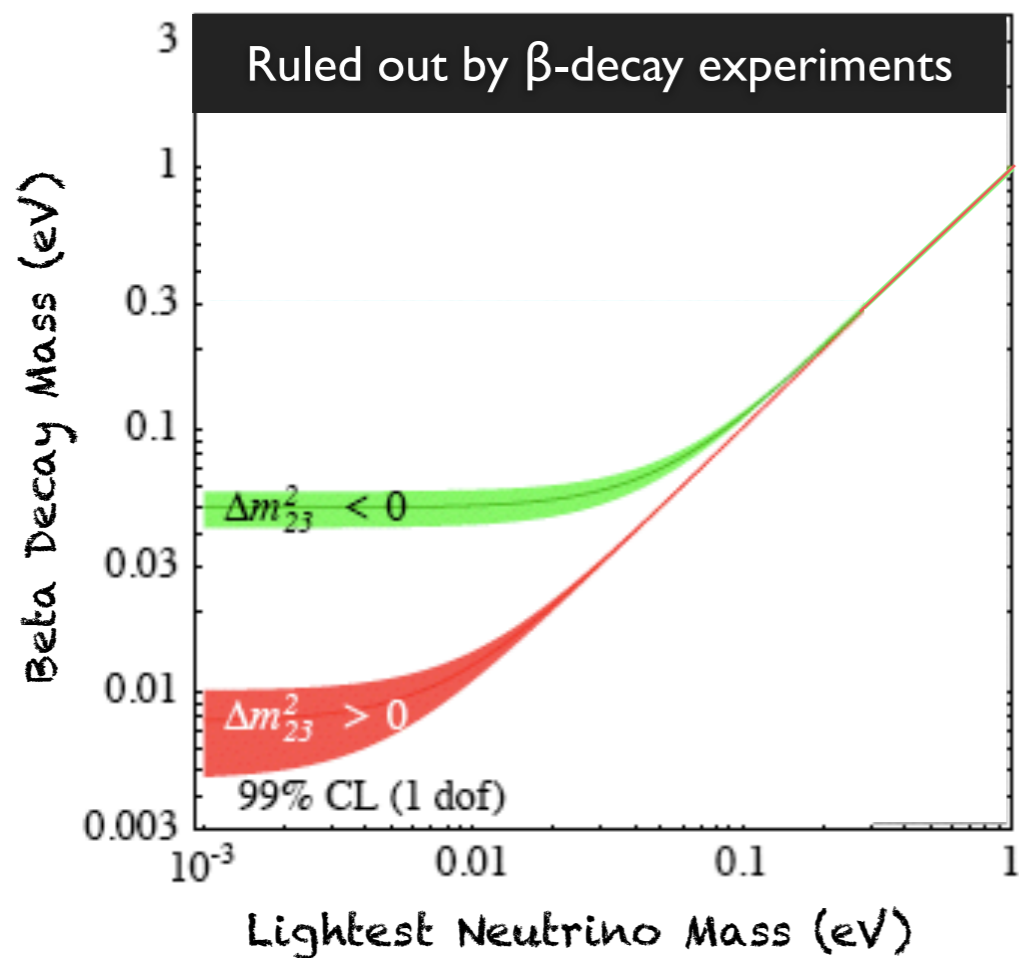
$$\Delta m_{32}^2 = 0.00244 \pm 0.00006 \text{ eV}^2$$

Atmospheric

As such, oscillation measurements place a lower limit on the neutrino mass scale.

Measuring Neutrino Masses

Oscillations now make a prediction upon other measurements.



$$M = \sum_i^{n_\nu} m_{\nu,i}$$

Cosmological Measurements

$$\langle m_{\beta\beta}^2 \rangle = \left| \sum_i^{n_\nu} U_{ei}^2 m_{\nu,i} \right|^2$$

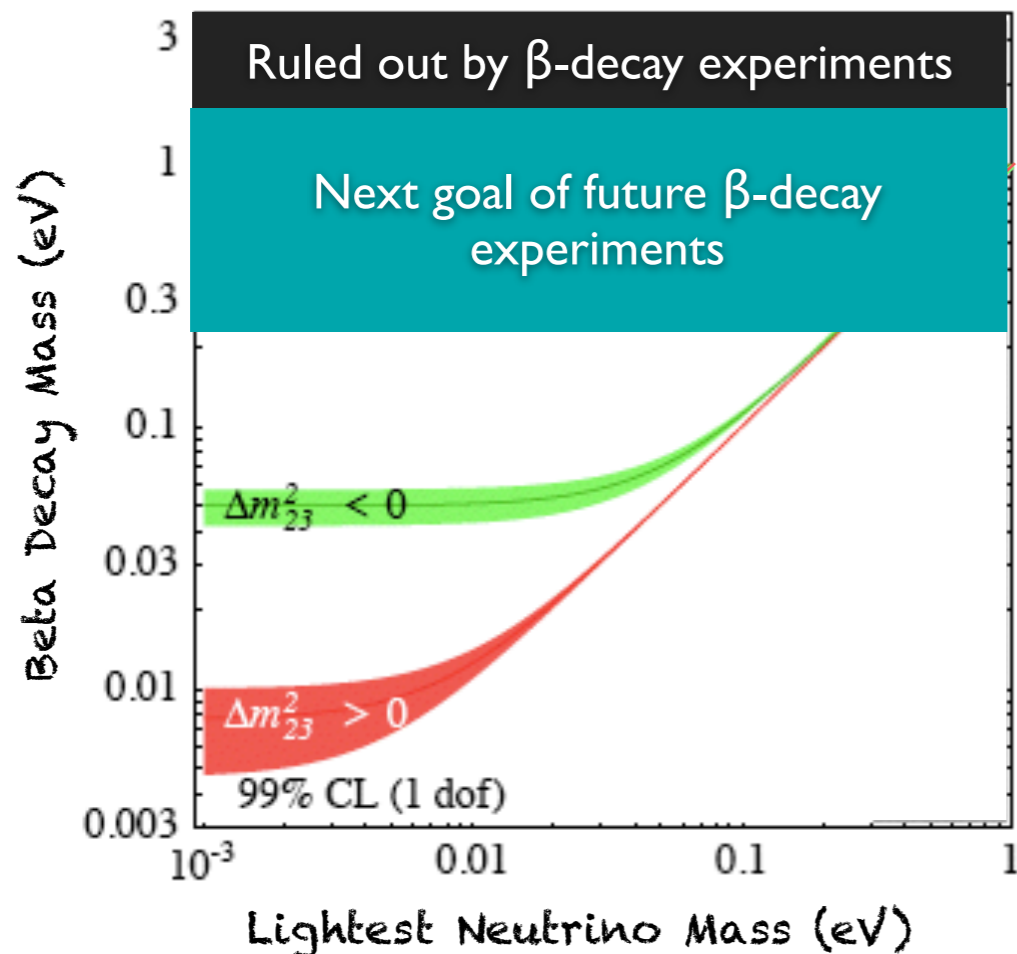
$0\nu\beta\beta$ Measurements

$$\langle m_\beta \rangle^2 = \sum_i^{n_\nu} |U_{ei}|^2 m_{\nu,i}^2$$

Beta Decay Measurements

The Neutrino Mass Scale

- The neutrino mass scale remains one of the essential “unknowns” of the Standard Model.
- Knowledge of neutrino masses can have a significant impact on many different arenas, including cosmology, the mass hierarchy, sterile neutrinos, and even relic neutrino detection.



$m_\nu > 2 \text{ eV}$ (eV scale, current)

Neutrinos ruled out as dark matter

$m_\nu > 0.2 \text{ eV}$ (degeneracy scale)

Impact on cosmology and $\sigma_{\nu\beta\beta}$ reach

$m_\nu > 0.05 \text{ eV}$ (inverted hierarchy)

Resolve hierarchy if null result

$m_\nu > 0.01 \text{ eV}$ (normal hierarchy)

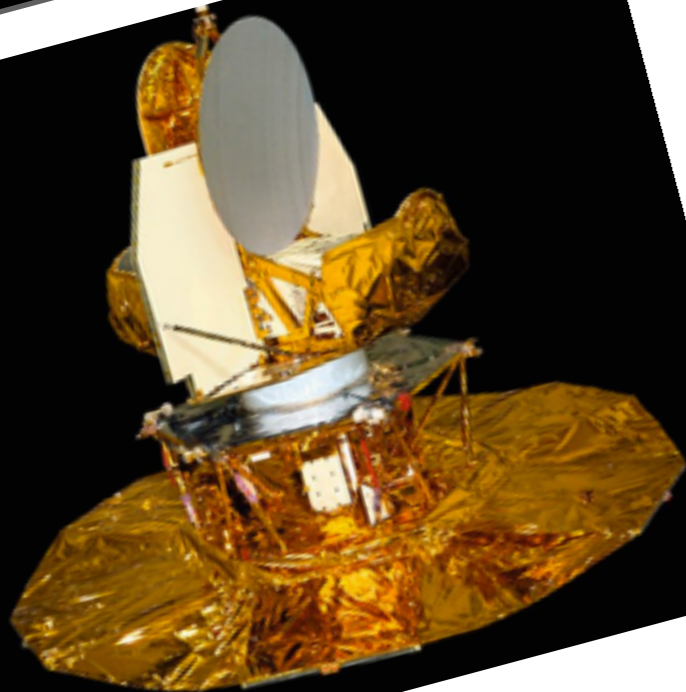
Oscillation limit; possible $C\nu\beta$ detection



$$M = \sum_i^{n_\nu} m_{\nu,i}$$

Cosmological Measurements

The Era of Precision Cosmology



WMAP



Wil



**Atacama
Cosmology Telescope**

Cosmology has had a similar trajectory as neutrino physics, from inception to present day



Sloan Digital Sky Survey

The Triumph of Cosmology

- The combination of the standard model of particle physics and general relativity allows us to relate events taking place at different epochs together.
- Observation of the cosmological neutrinos would then provide a window into the 1st second of creation

Microwave Background

400 kyr
 $z=1100$

Nucleosynthesis

3-30 min
 $z=5 \times 10^8$

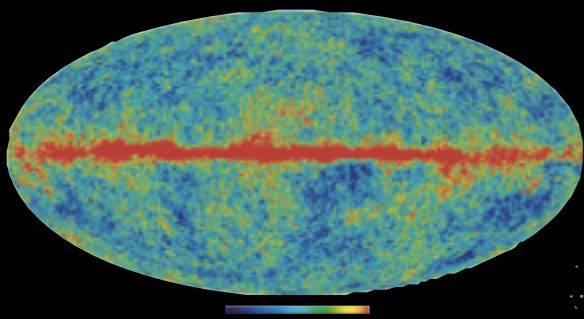
Relic Neutrinos

0.18 s
 $z=1 \times 10^{10}$

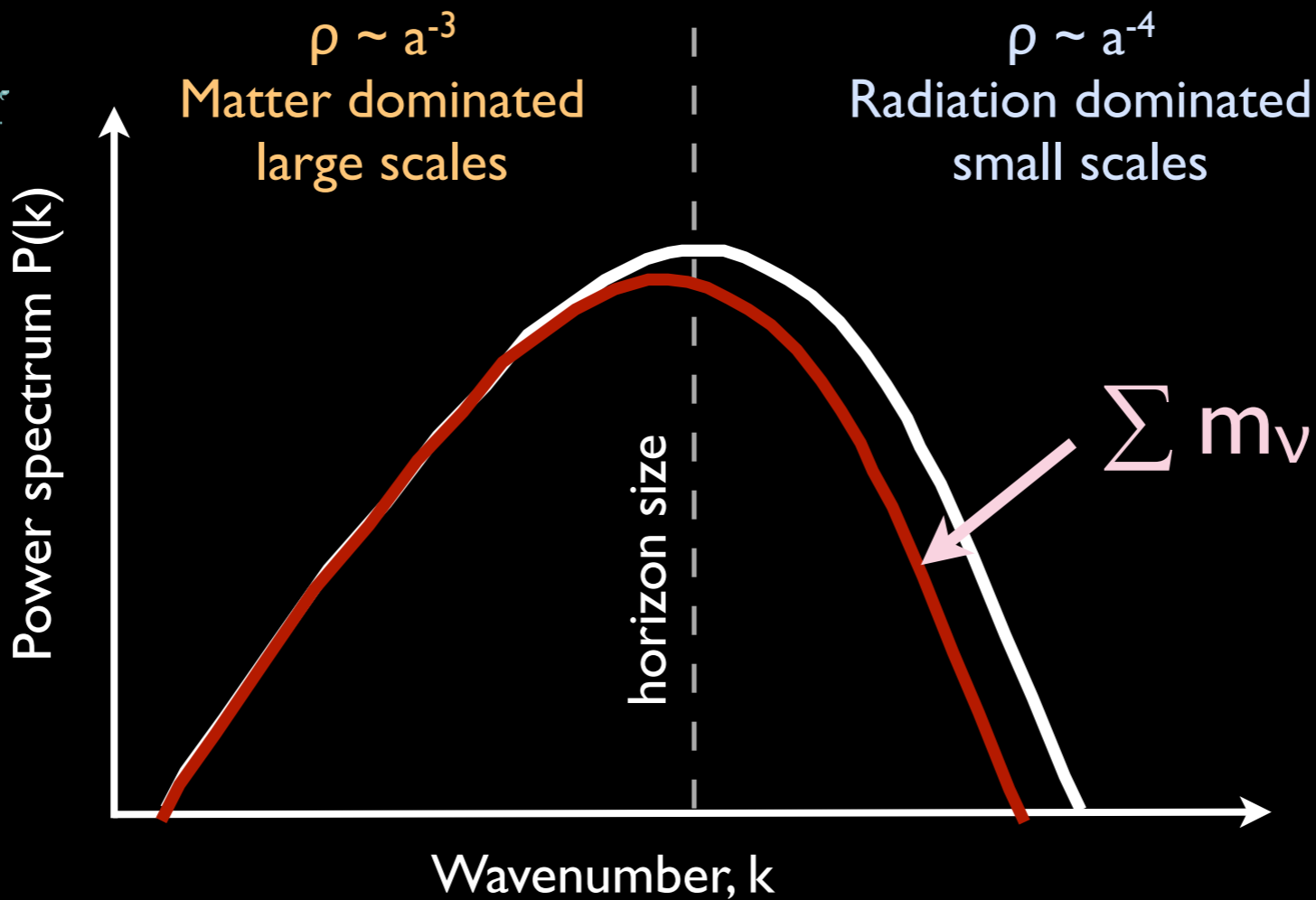
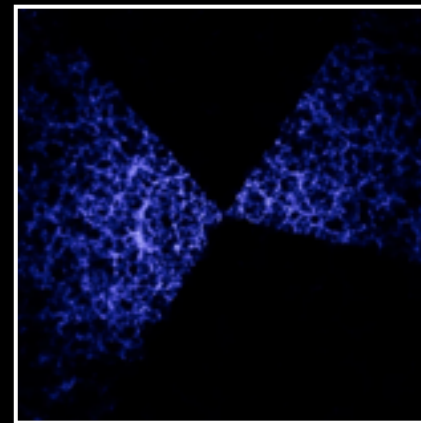


The Strategy (a naive view)

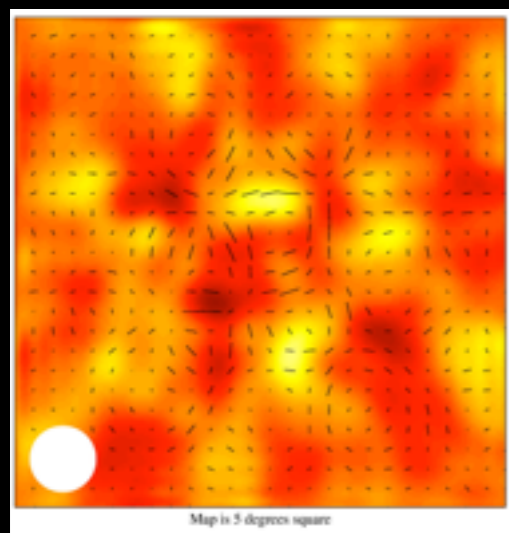
WMAP Temperature Map



Galaxy Surveys



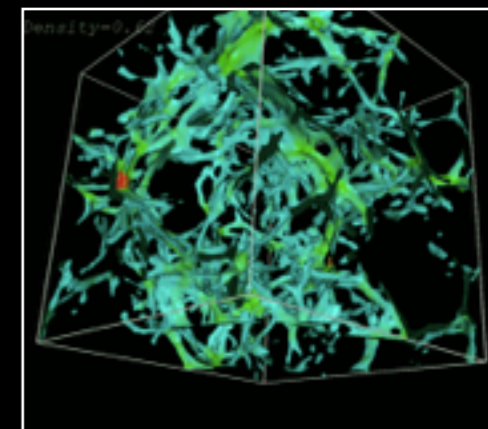
Weak lensing



CMB Polarization

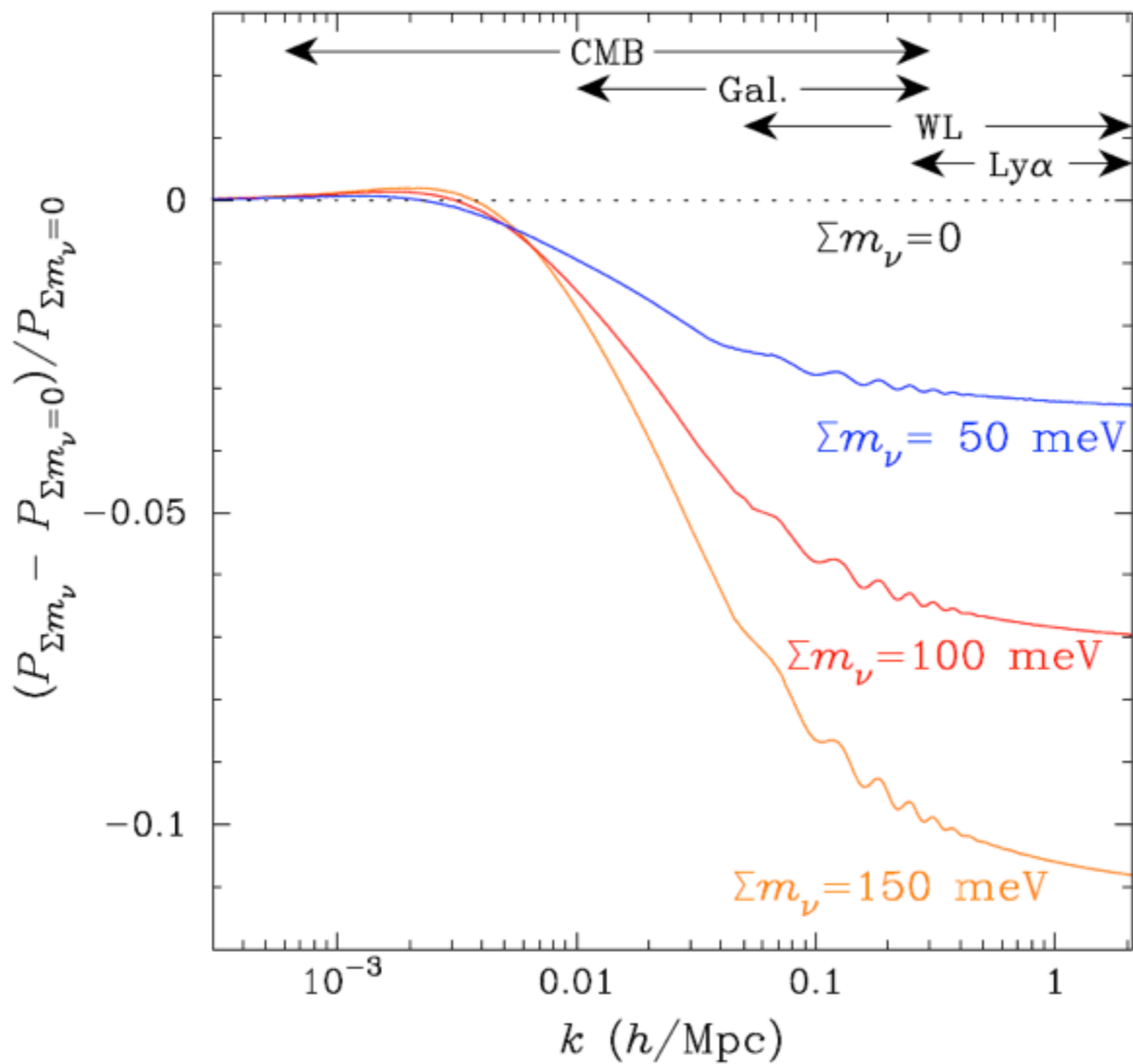
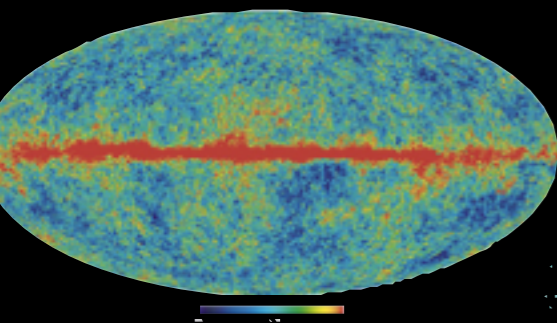
$\delta(x) = (\rho(x) - \bar{\rho}) / \bar{\rho}$
 Neutrinos come to affect the power spectrum,

particularly at small distance scales
 $P(k) = \langle |\delta(k)|^2 \rangle$

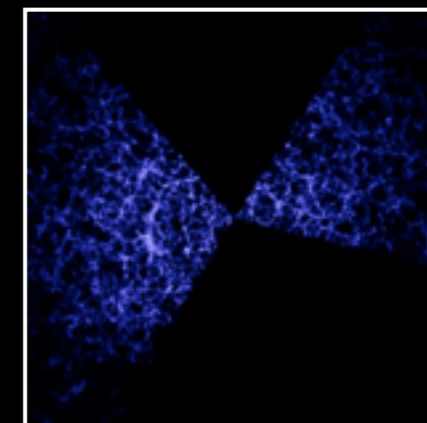


Lyman α

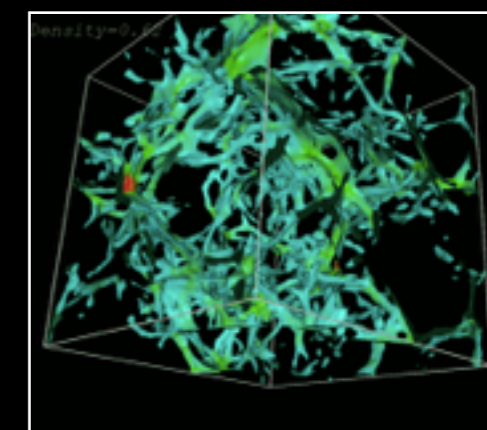
Temperature Map



Galaxy Surveys



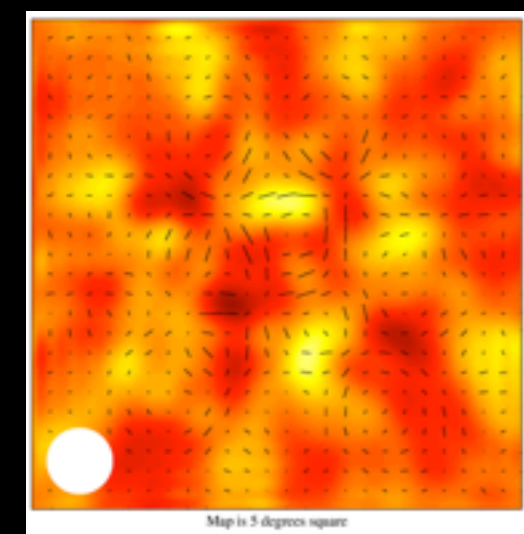
Weak lensing



Lyman α

Large scale structure tends to weaken power spectrum at small wavelengths...

CMB Polarization



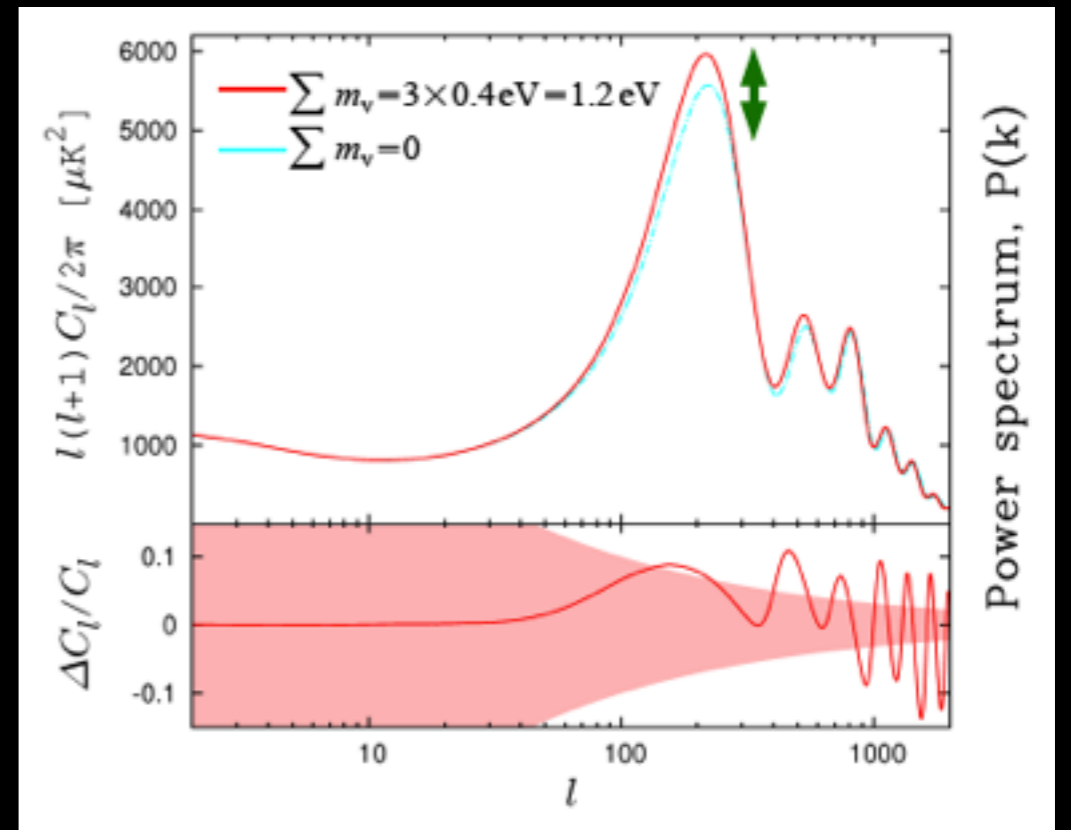
Neutrino Physics & Cosmology

- Two primary cosmology measurements that link directly to neutrino physics:

(1) Number of neutrino species

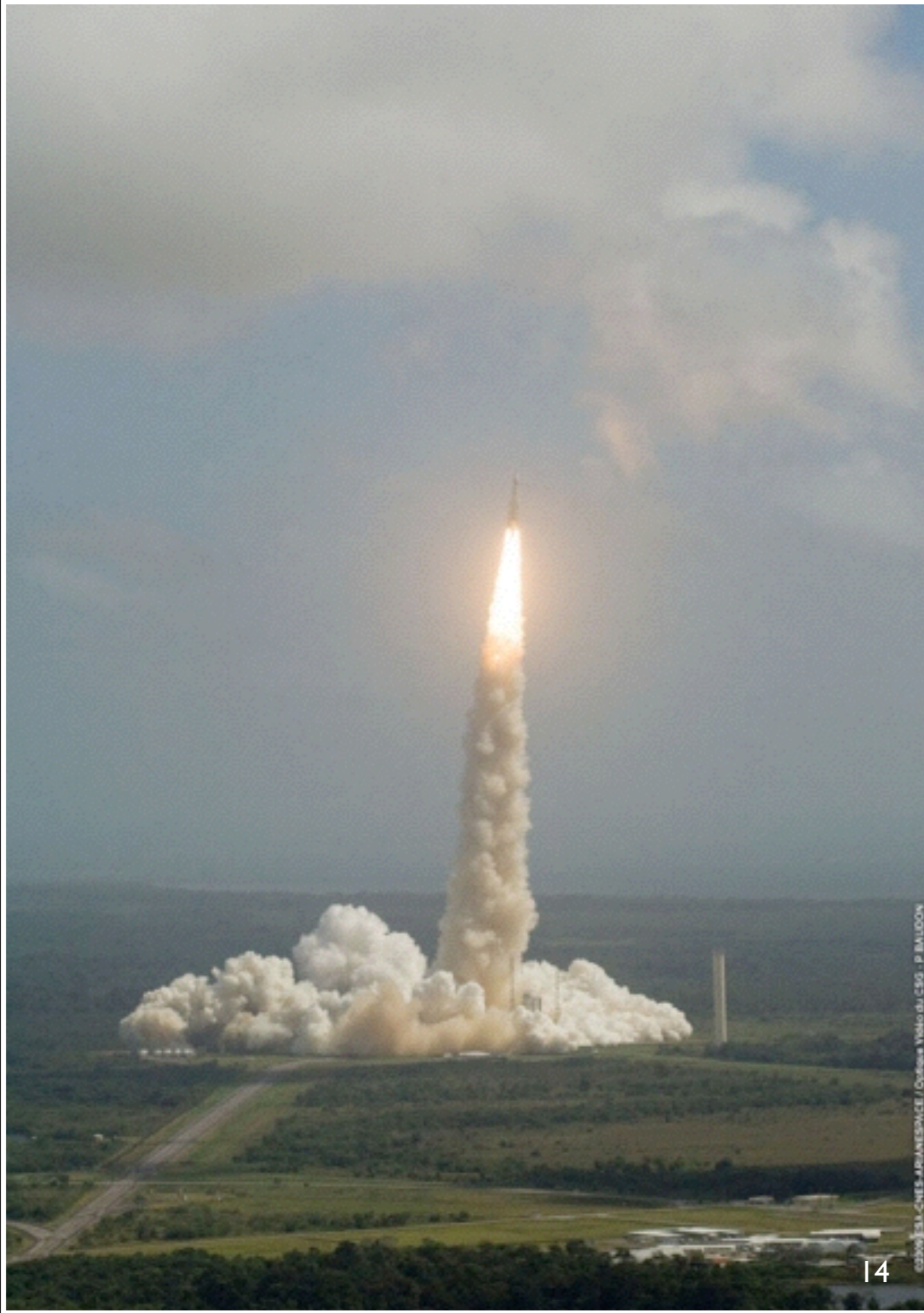
(2) Sum of neutrino masses

- Both large scale structure (LSS) and CMB anisotropies (CMB), particularly CMB gravitational lensing, can be used to measure these quantities.



$$\Omega_R h^2 = \left[1 + N_{\text{eff}} \frac{7}{8} \left(\frac{4}{11} \right)^{\frac{4}{3}} \right] \Omega_\gamma h^2$$

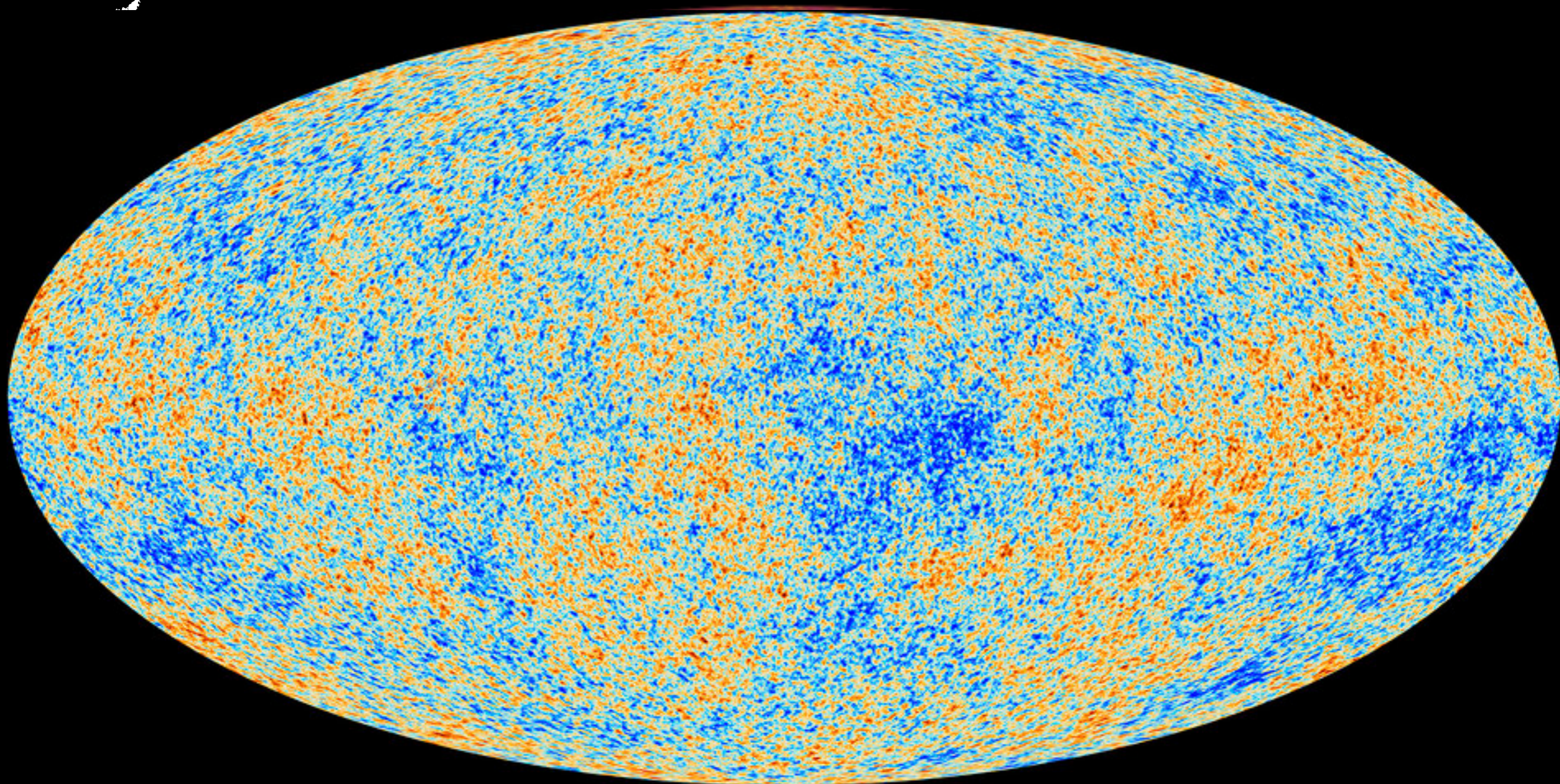
$$\Omega_\nu = \frac{\rho_\nu}{\rho_{\text{critical}}} = \frac{\sum_i^{n_\nu} m_{\nu,i}}{\rho_{\text{critical}}}$$



Planck Satellite:

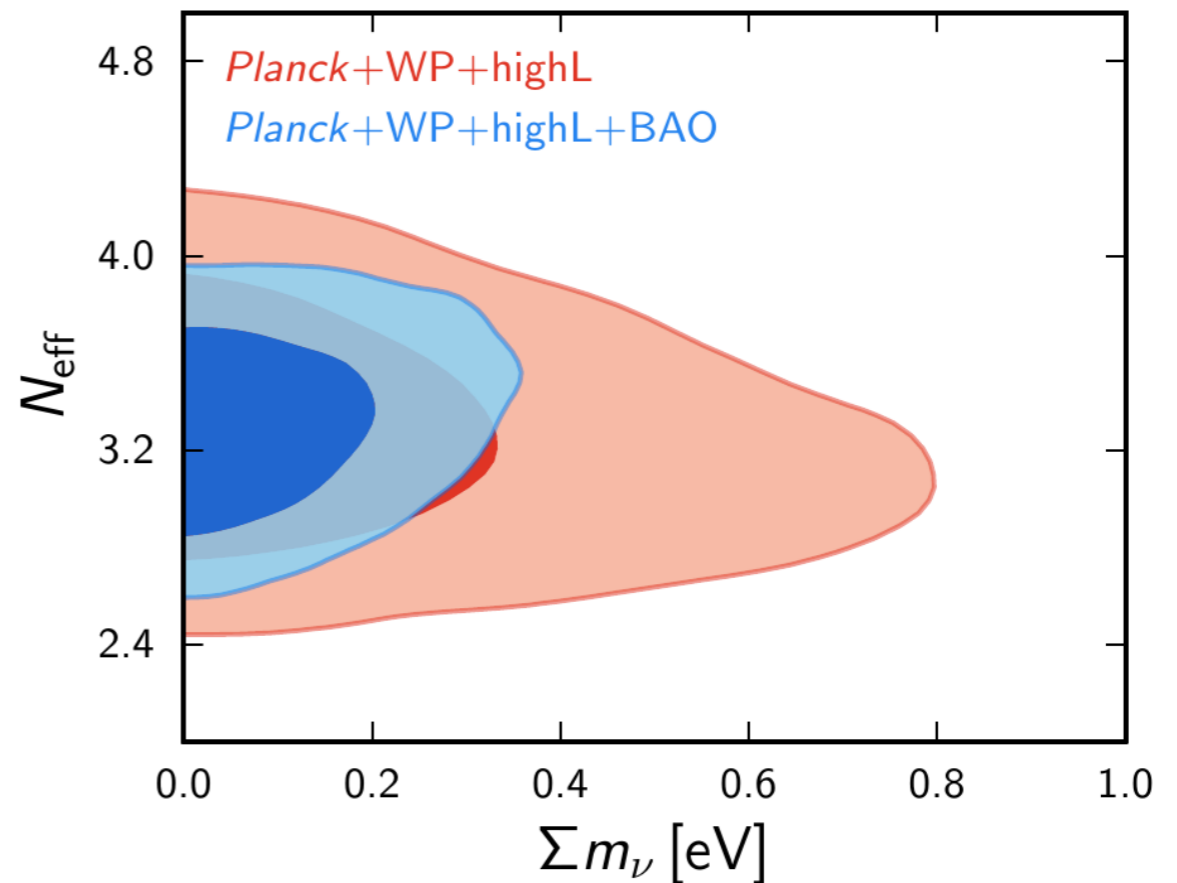
Launched May 14th, 2009

The Microwave
sky...

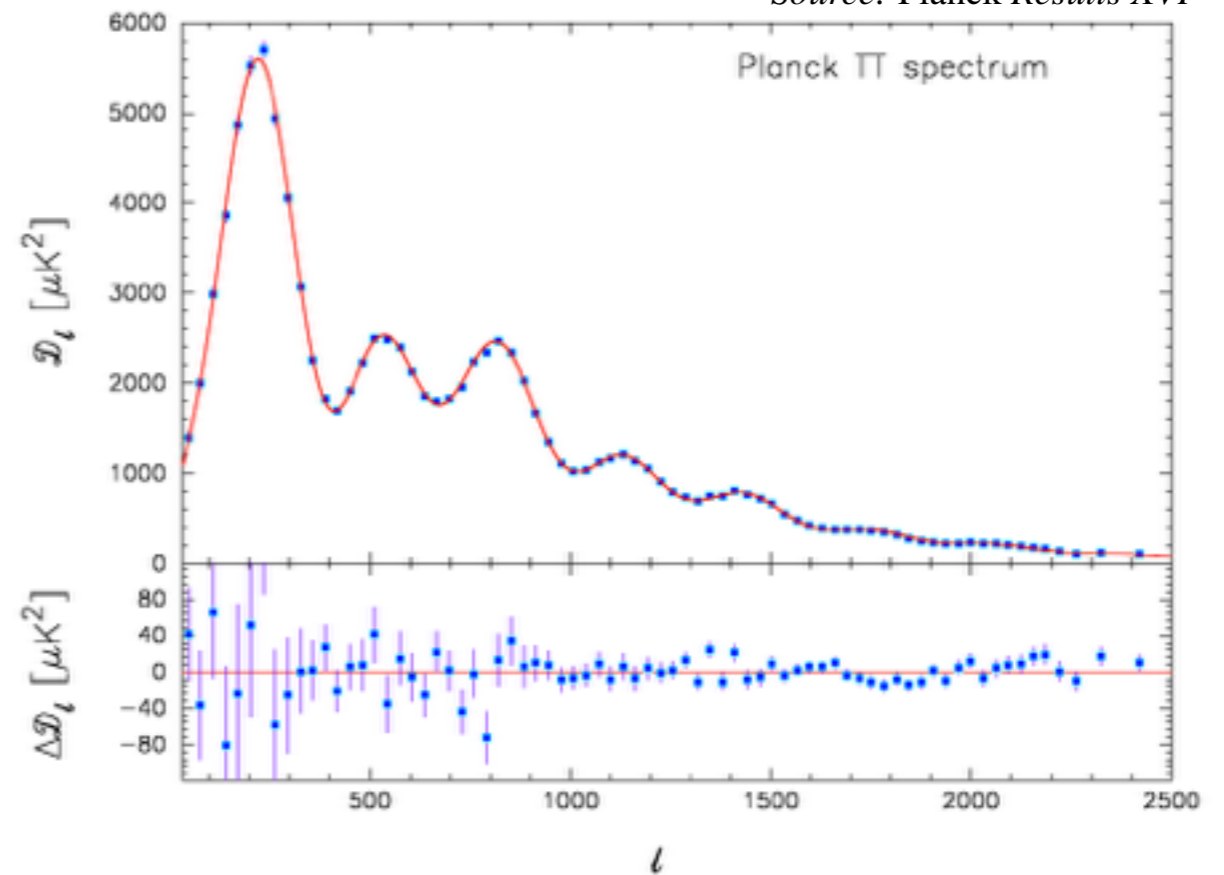


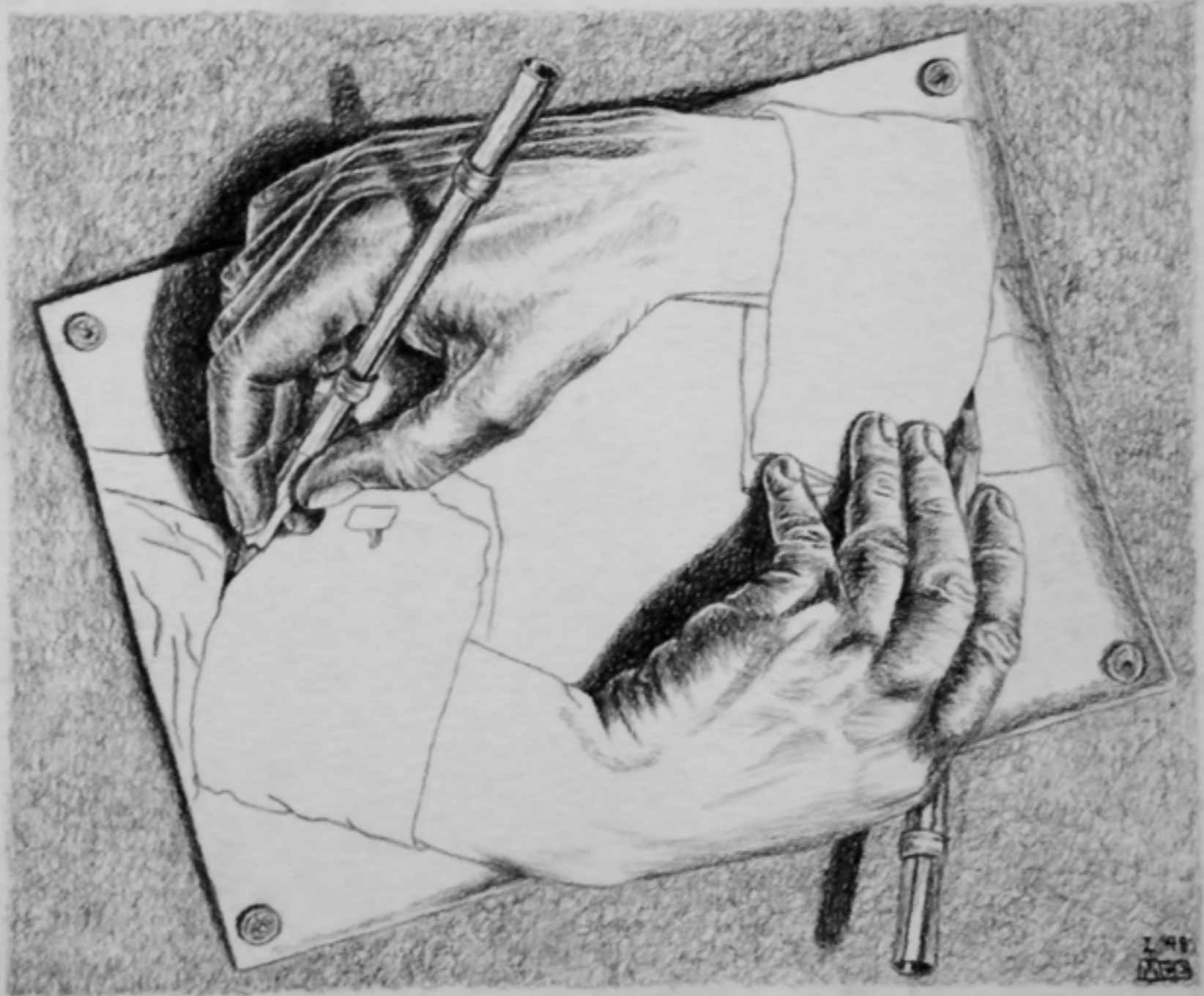
PLANCK Results

- The basic PLANCK analysis looks at 6 main cosmological parameters. Neutrino masses are added as extensions to that model.
- Most conservative data combinations see no evidence for neutrino masses.
- Certainly tension exists with certain parameters (SZ clusters, Hubble constant, BICEP2) that alter the fits or in some cases favor finite masses.



Source: Planck Results XVI

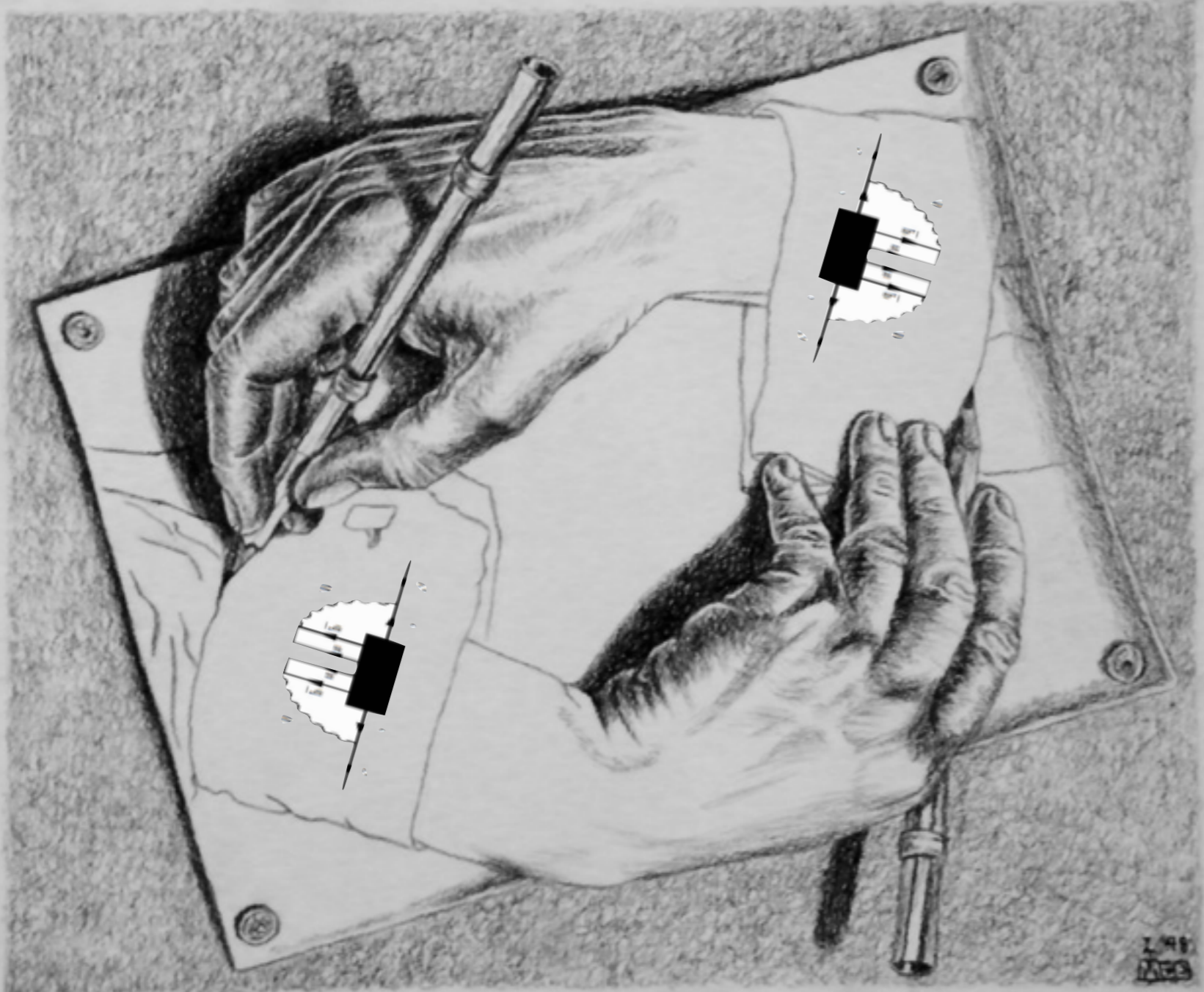




Neutrinoless Double
Beta Decay

$$\langle m_{\beta\beta}^2 \rangle = \left| \sum_i^{n_\nu} U_{ei}^2 m_{\nu,i} \right|^2$$

$0\nu\beta\beta$ Measurements



What would a positive signal mean?

A lot, actually, since the Standard Model conserves B-L.

- Demonstrate that neutrinos are Majorana fermions.
- Shed light on the neutrino mechanism
- Probe into the causes for the matter anti-matter asymmetry in the universe

$$(N, Z) \rightarrow (N - 2, Z + 2) + e^- + e^-$$

$$\Delta L = 2$$

Simple in principle...

① Clean Signature

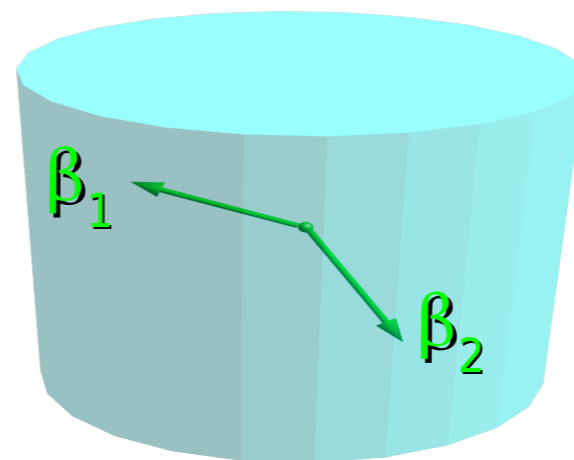
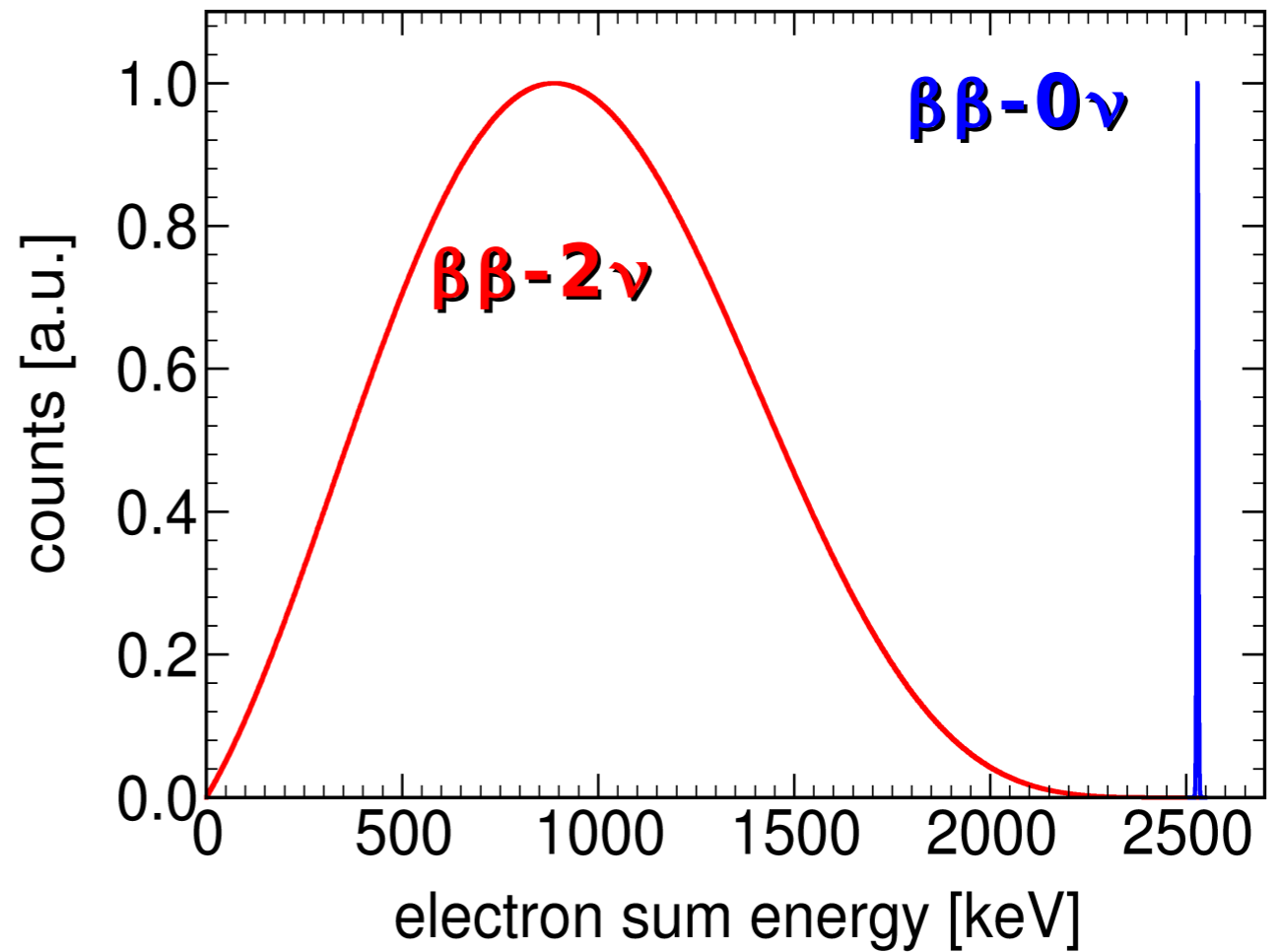
Sum of electrons is at a single energy

② Know where to look

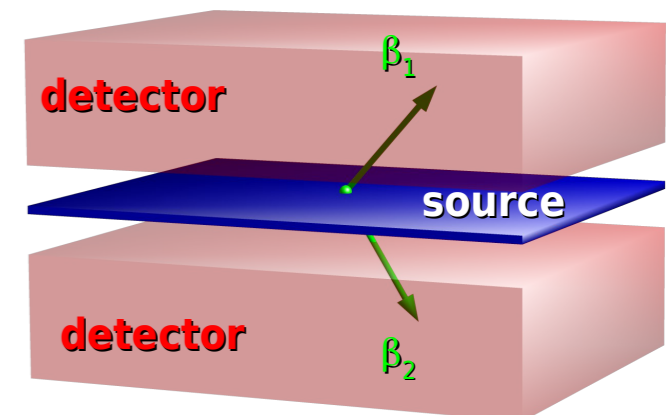
Occurs at endpoint of the allowed decay, well-separated from bulk $\beta\beta\nu\nu$.

③ Particle detection

(we know how to detect electrons well)



Source = detector



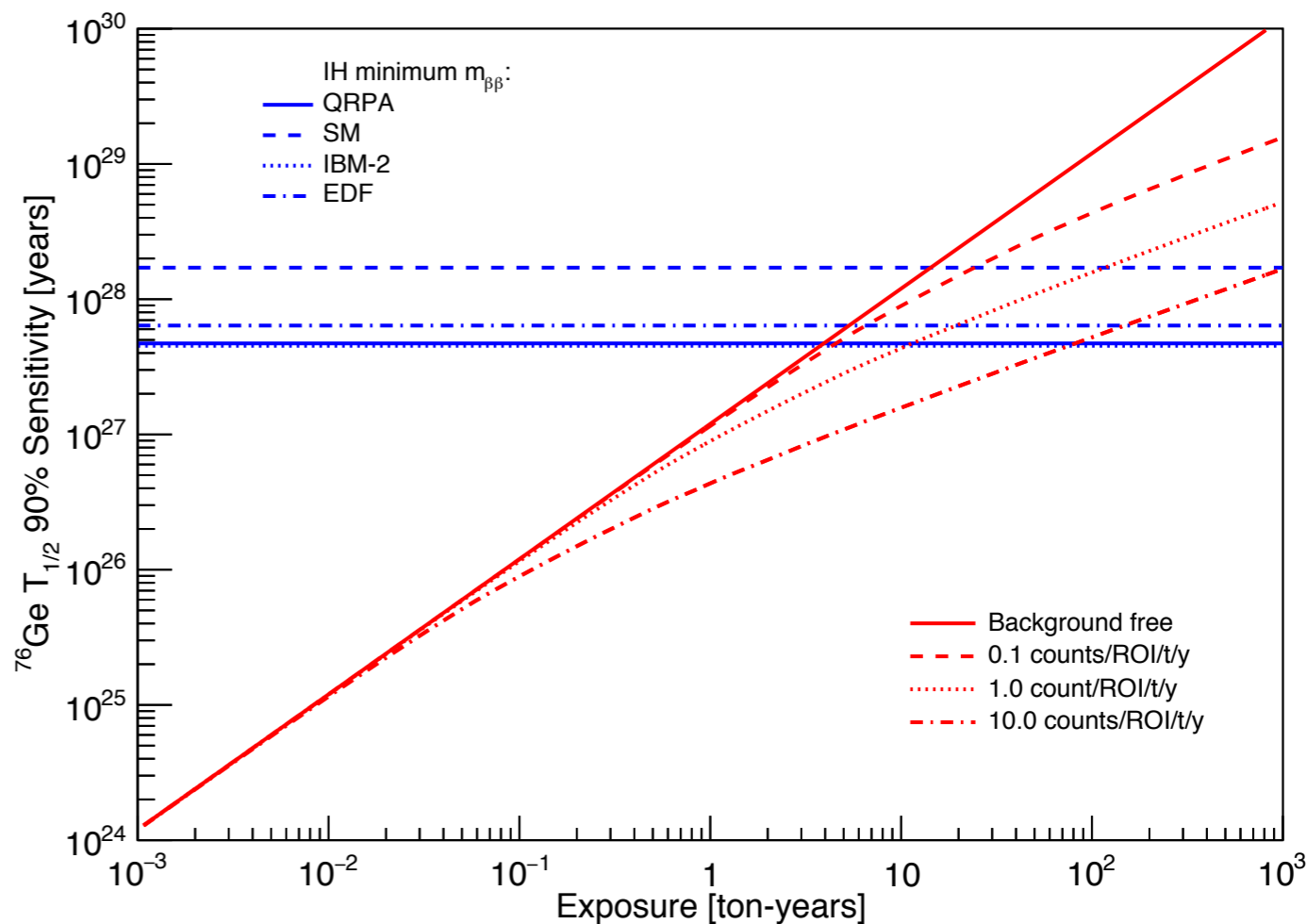
Source ≠ detector

...but not in practice

Background Suppression
The key to success in all these experiments is background suppression

Isotope Abundance
Often trading high Q value for poor abundance

Rarity of Process
Rarest process (yet) to be measured.



⁷⁶Ge example, but similar sensitivities for other $0\nu\beta\beta$ isotopes.

Background free

$$\left[T_{1/2}^{0\nu} \right] \propto \epsilon_{ff} \cdot I_{abundance} \cdot \text{Source Mass} \cdot \text{Time}$$

Background limited

$$\left[T_{1/2}^{0\nu} \right] \propto \epsilon_{ff} \cdot I_{abundance} \cdot \sqrt{\frac{\text{Source Mass} \cdot \text{Time}}{\text{Bkg} \cdot \Delta E}}$$

CUORE



(AMORE, LUCIFER)

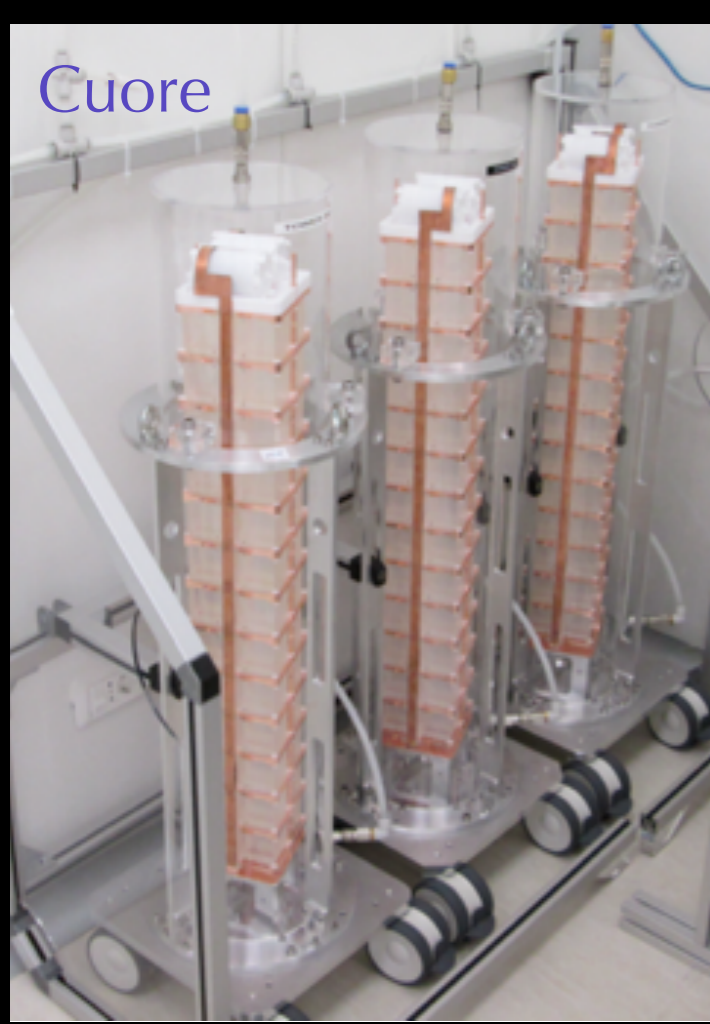


(EXO, NEXT)

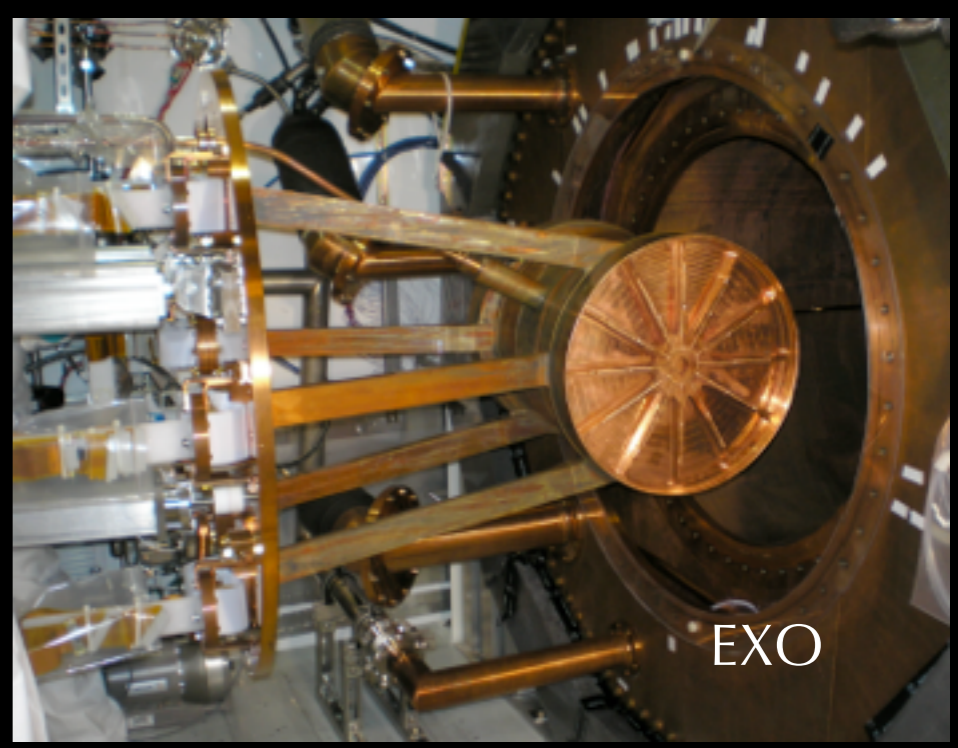
GERDA,
MAROJANA,
SUPERNEMO

SNO+
KAMLAND ZEN
CANDLES

Cuore

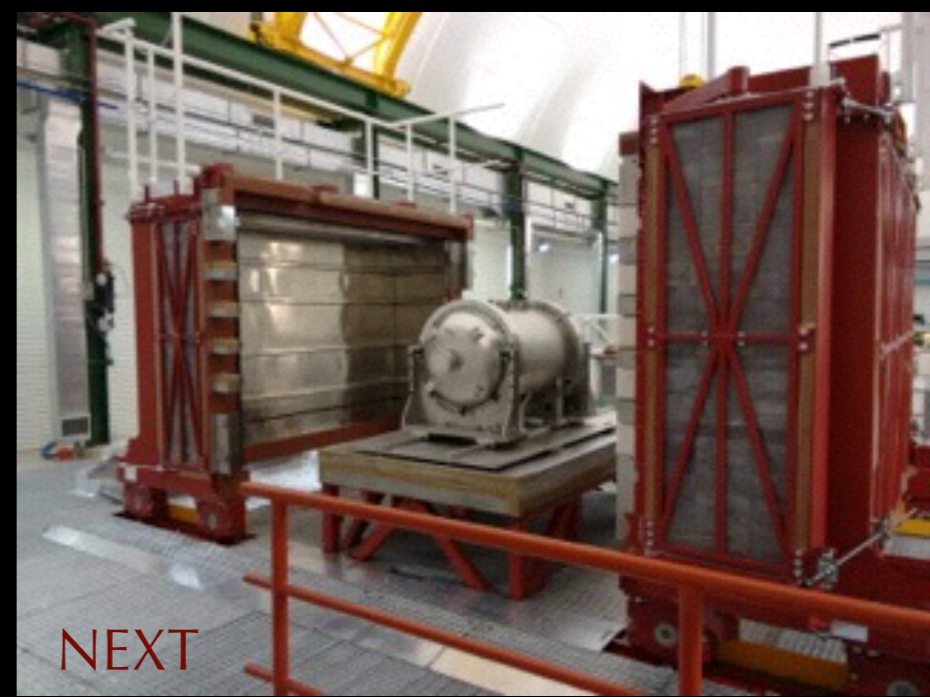


SNO+



EXO

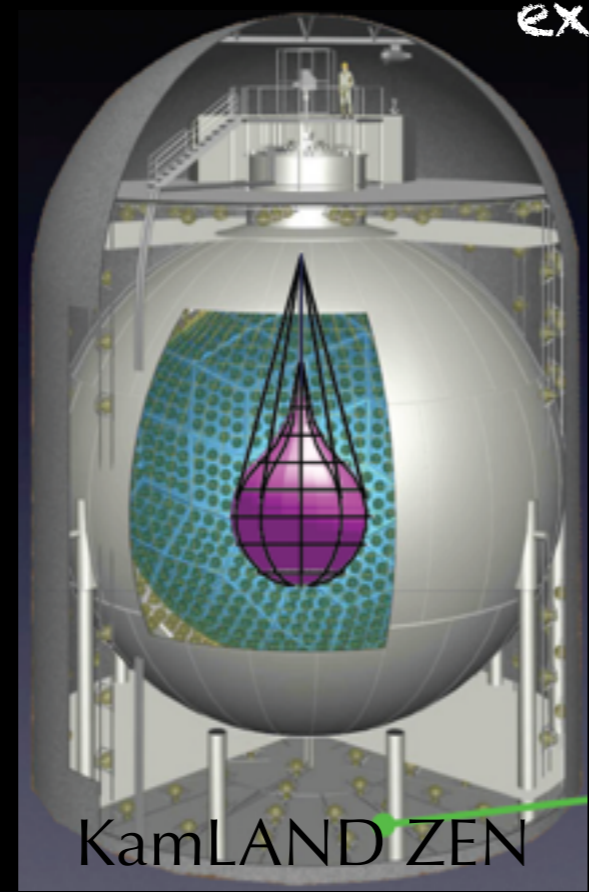
Many, many experiments...



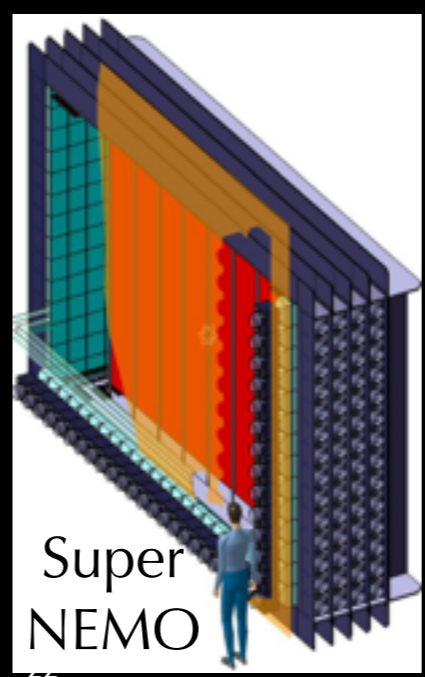
NEXT



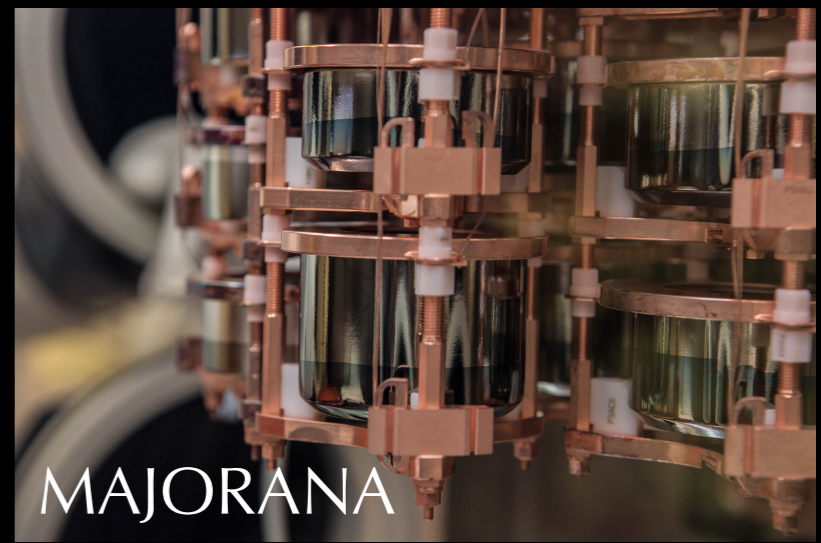
GERDA



KamLAND ZEN



Super NEMO



MAJORANA

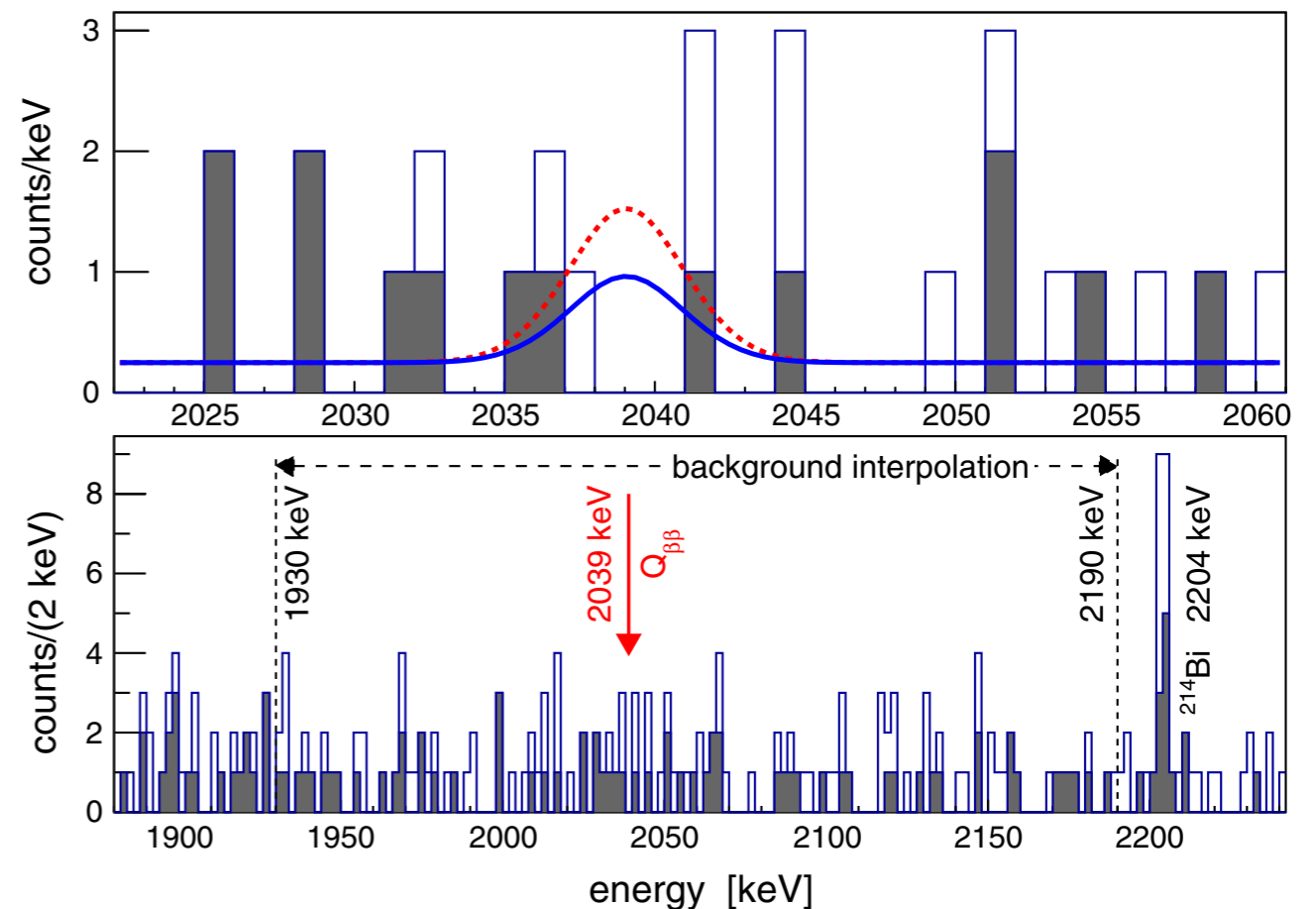


With so many choices, how does any one experiment stand out !?

Ionization: GERDA

others ionization detectors:
MAJORANA, SuperNEMO

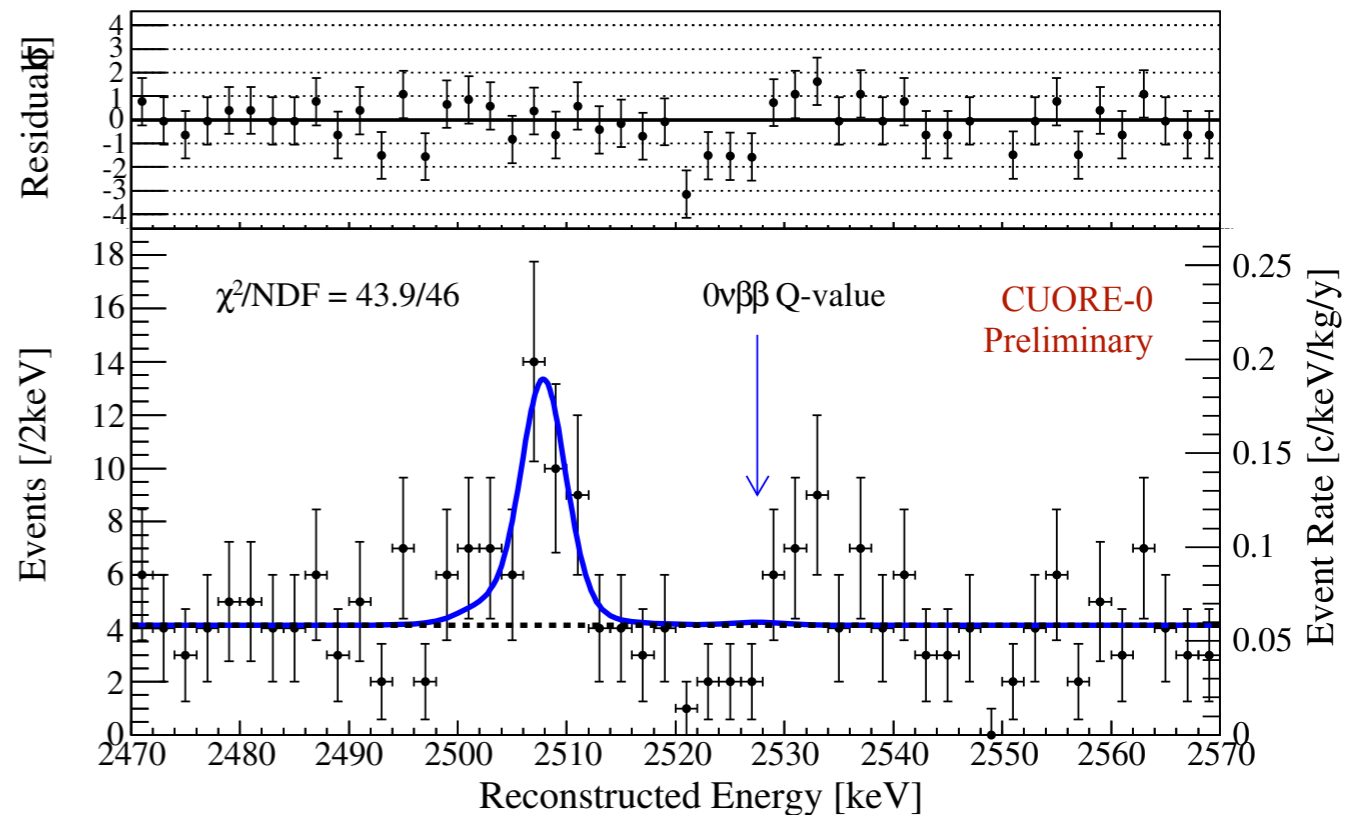
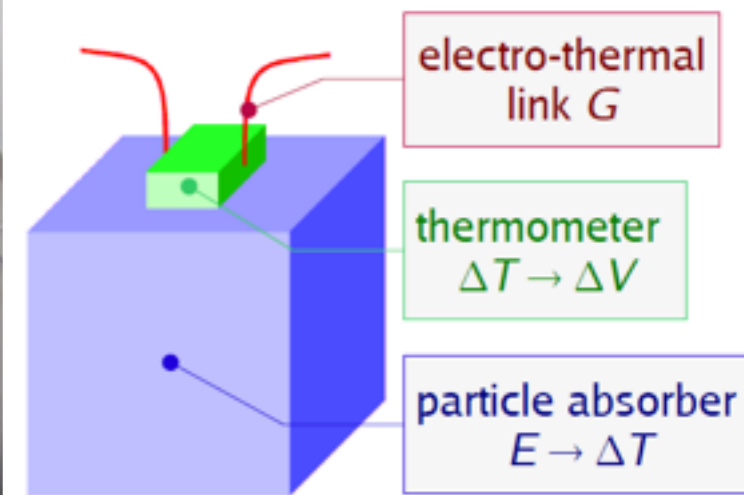
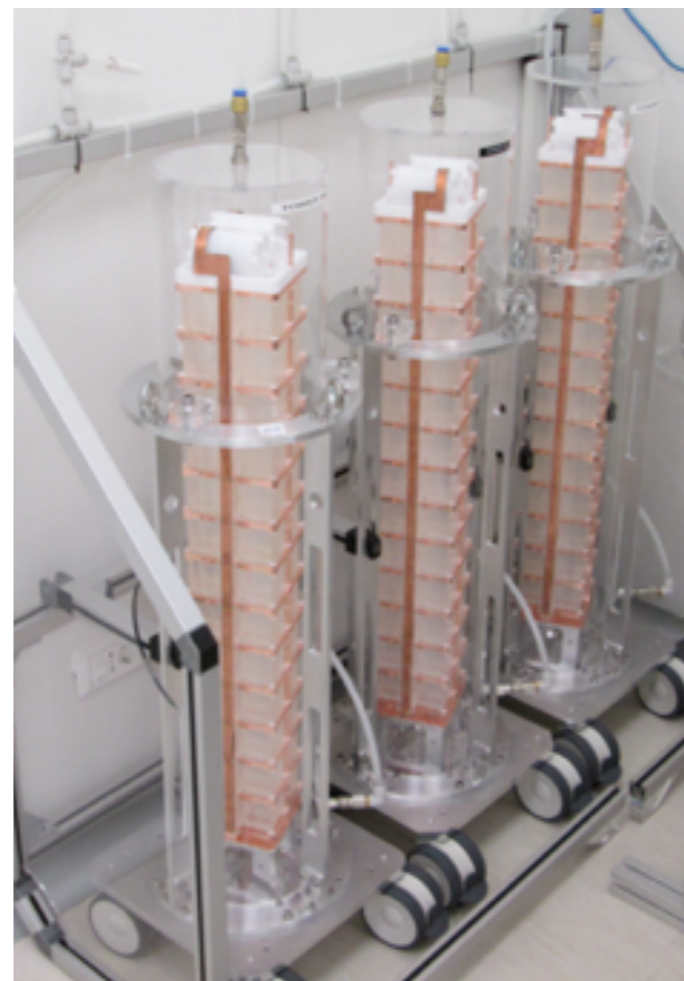
- 87% enriched ^{76}Ge detectors (crystals) in liquid argon
- 14.6 kg of 86% enriched ^{76}Ge (6 p-type semi-coax detectors from H-M & IGEX). (4.8 keV FWHM @ $Q_{\beta\beta}$)
- 3 kg of 87% enriched BEGe enriched detectors (5 detectors)
- Single-site, multi-site pulse shape discrimination



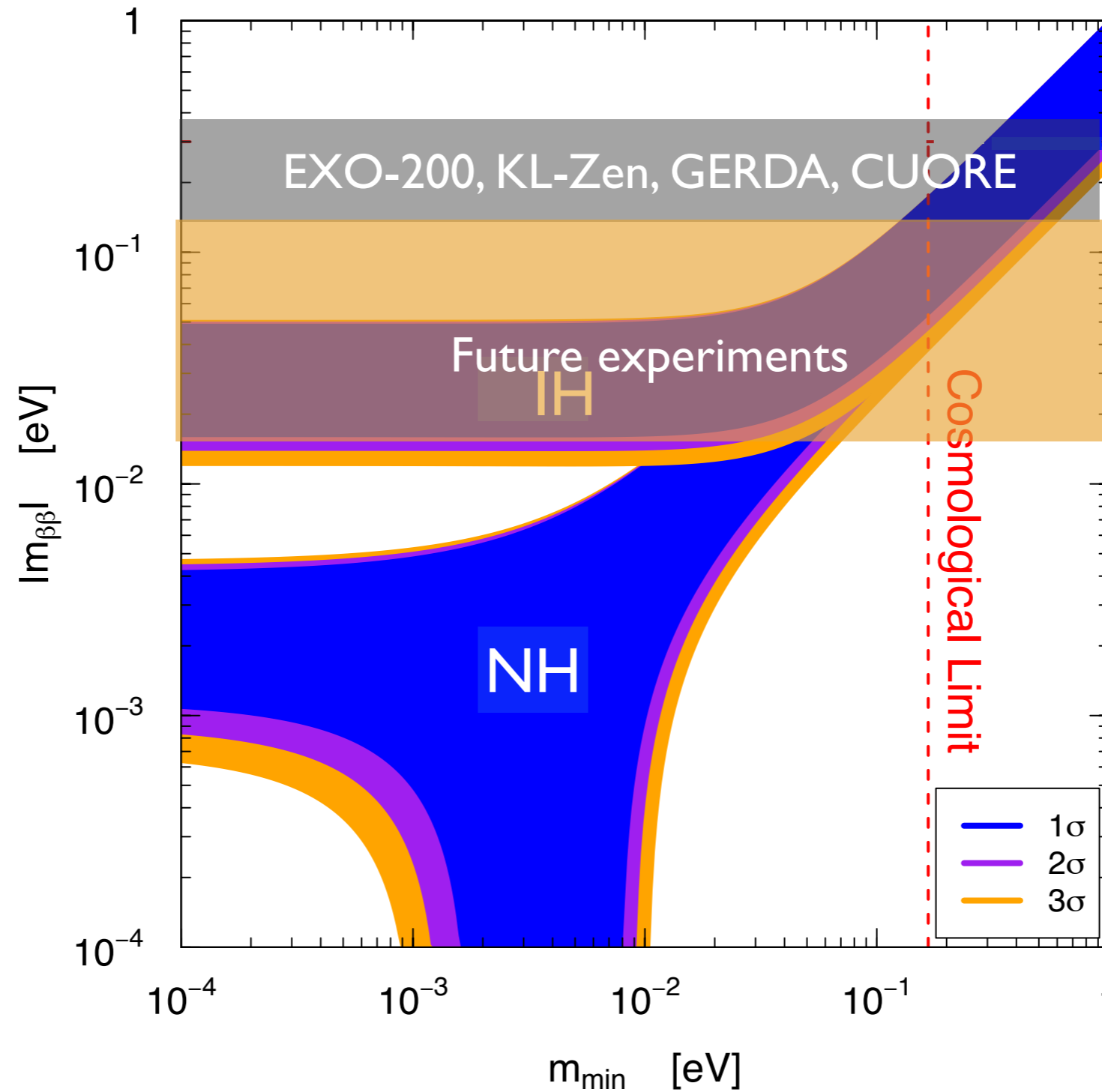
$T_{1/2} > 2.1 \times 10^{25}$ y (90% CL) ^{76}Ge

PHONONS: CUORE

- Towers of 11 kg of ^{130}Te (34% nat.) bolometers
- Array of 52 $5 \times 5 \times 5 \text{ cm}^3$ TeO_2 crystals held at 10 mK
- FWHM of 5.1 keV



$T_{1/2} > 4.0 \times 10^{24} \text{ y}$ (90% CL) ^{130}Te



Current limits essential rule out long-standing claim for observation of the neutrinoless decay mode in ^{76}Ge .

Next generation will push into the inverted Sacle

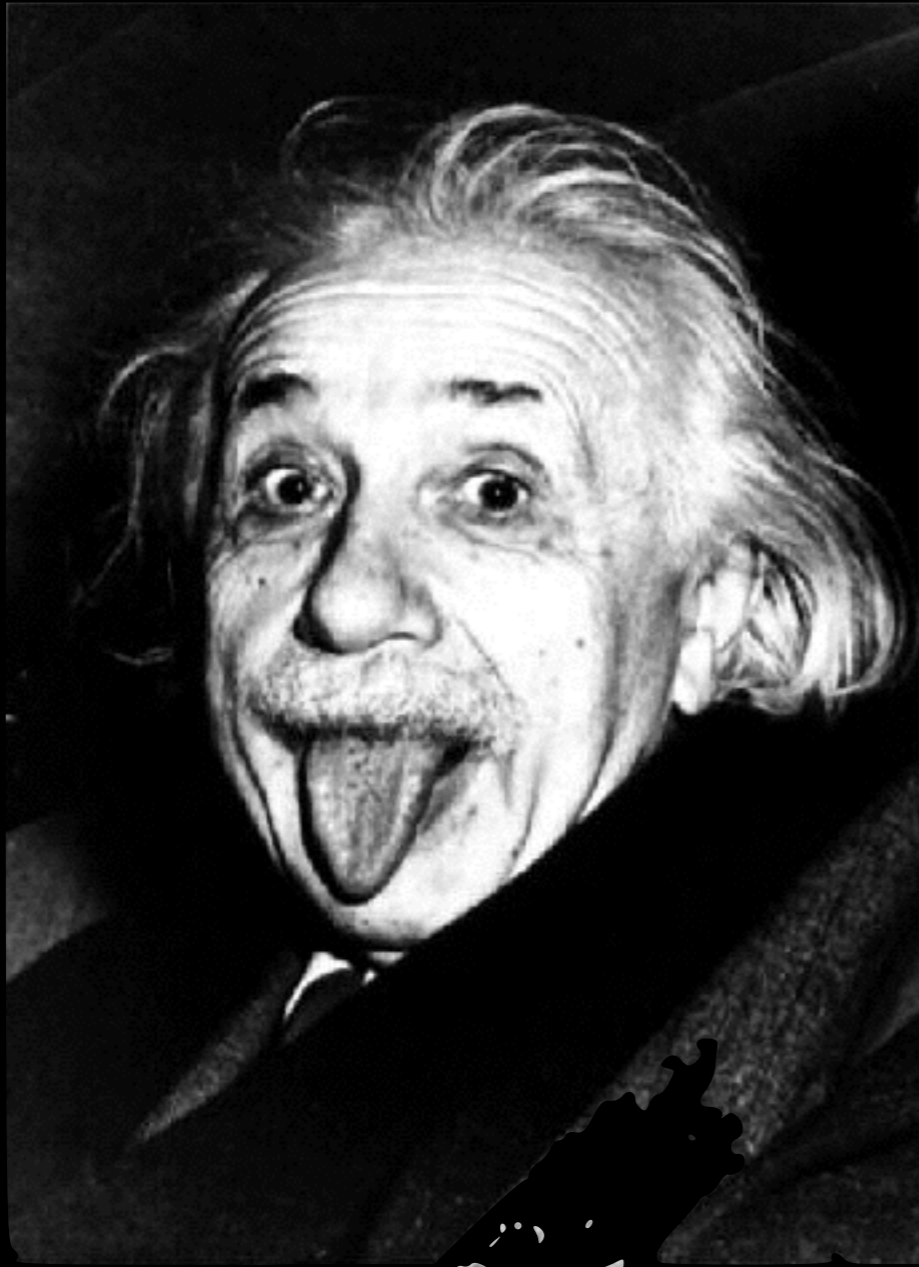


Current stage: ~10-100 kg



Upcoming: ~100-1000 kg

Far future: multi ton??



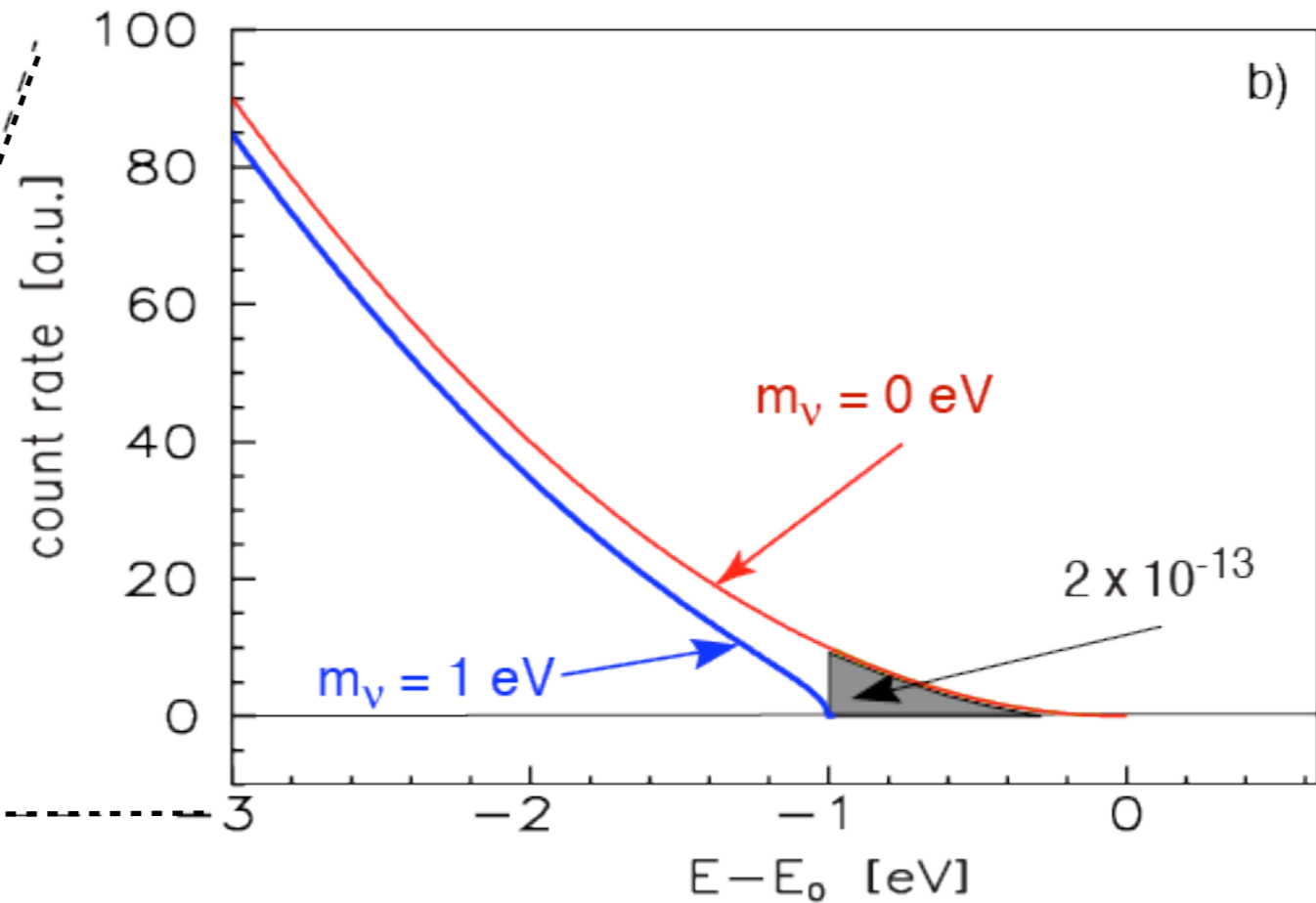
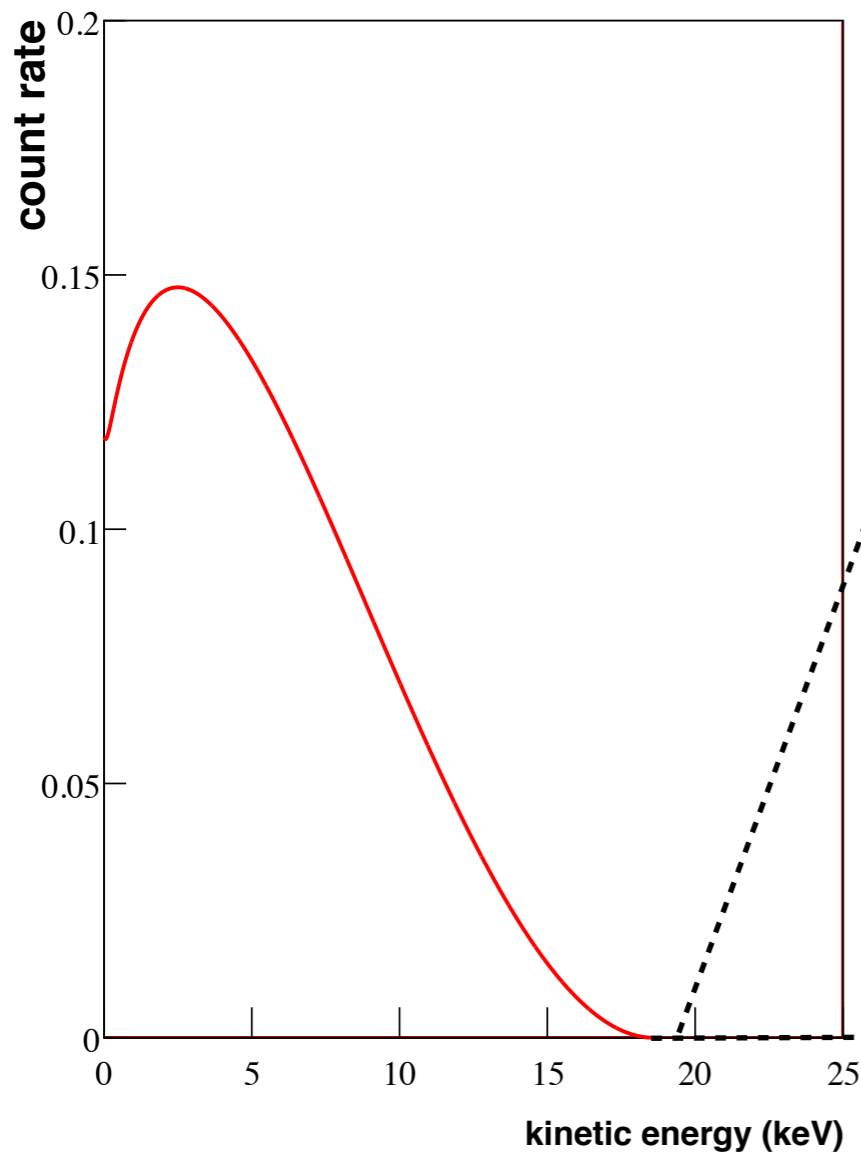
$$\langle m_\beta \rangle^2 = \sum_i^{n_\nu} |U_{ei}|^2 m_{\nu,i}^2$$

Beta Decay Measurements

Direct Probes

$$\dot{N} \sim p_e (K_e + m_e) \sum_i |U_{ei}|^2 \sqrt{E_0^2 - m_{\nu i}^2}$$

Electron Energy



Beta Decay

A kinematic determination of the neutrino mass
No model dependence on cosmology or nature of mass

Neutrinos from Radioactivity

- The phase space of the decay (i.e. how many different states can occupy a particular momentum).
- Corrections due to the Coulomb field, or Fermi function.
- The matrix element related to the initial and final states of the decay.

Transition	ΔI	Parity change?
Superallowed	$0, \pm 1$	No
Allowed	$0, \pm 1$	No
1 st Forbidden	$0, \pm 1$	Yes
Unique 1 st Forbidden	± 2	Yes
2nd Forbidden	± 2	No
3rd Forbidden	± 3	Yes

Spin of states govern type of exchange
 E.g.: $0^+ \rightarrow 0^+$ is superallowed

$$\frac{dN}{dE} = C \times \underbrace{|M|^2}_{\text{Matrix Element}} \underbrace{F(Z, E) p_e(E + m_e^2) (E_0 - E)}_{\text{Phase space}} \sum_i |U_{ei}|^2 \sqrt{(E_0 - E)^2 - m_i^2}$$

Fermi Function
Matrix Element Phase space

The $\pi\sqrt{2}$ Magnetic Spectrometer

- Bergkvist constructs first tritium source experiment in Stockholm.
- Double focusing spectrometer; first to fully tackle energy resolution, energy loss and final states coherently.
- Achieved best limit of the time ($m_\nu < 55 \text{ eV}$).

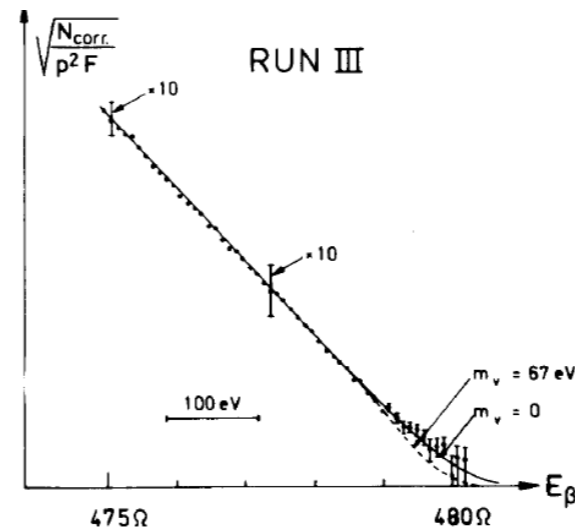


Fig. 20. Kurie plots of data from runs I–III. The data exhibited have been subjected to a very slight correction for distortion in the measured spectrum. The theoretical curves have been fitted to the data in the way discussed in connection with fig. 18.

Nuclear Physics B39 (1972) 317–370. North-Holland Publishing Company

A HIGH-LUMINOSITY, HIGH-RESOLUTION STUDY OF THE END-POINT BEHAVIOUR OF THE TRITIUM β -SPECTRUM (I). BASIC EXPERIMENTAL PROCEDURE AND ANALYSIS WITH REGARD TO NEUTRINO MASS AND NEUTRINO DEGENERACY

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Received 23 September 1971
(Revised 13 December 1971)

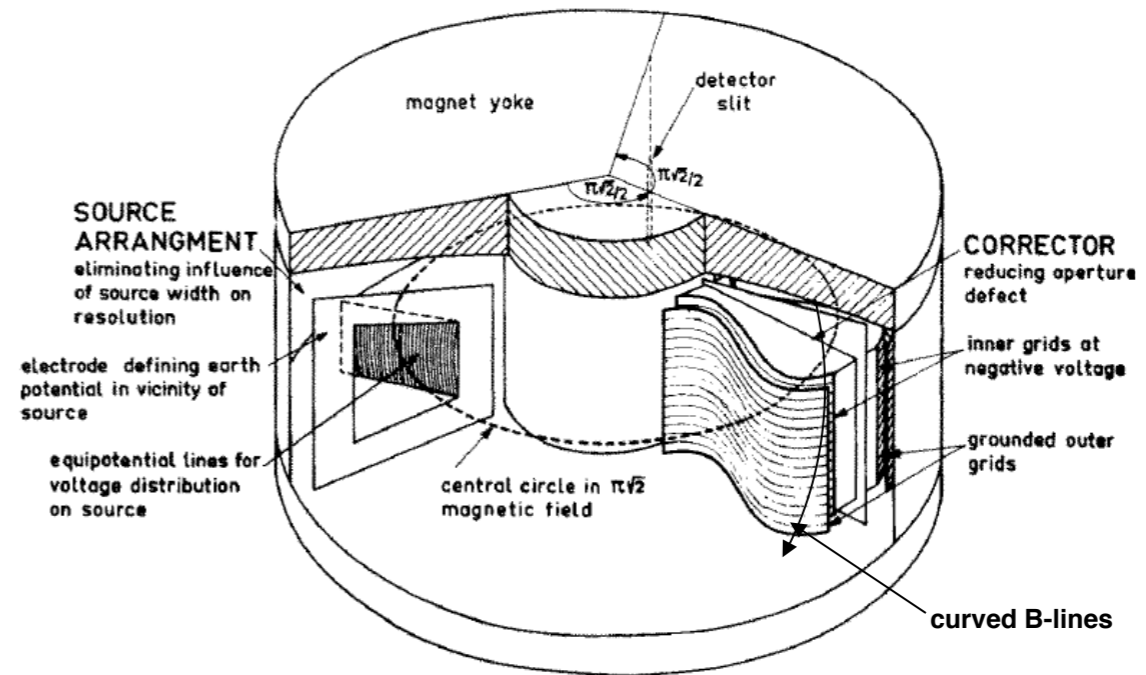
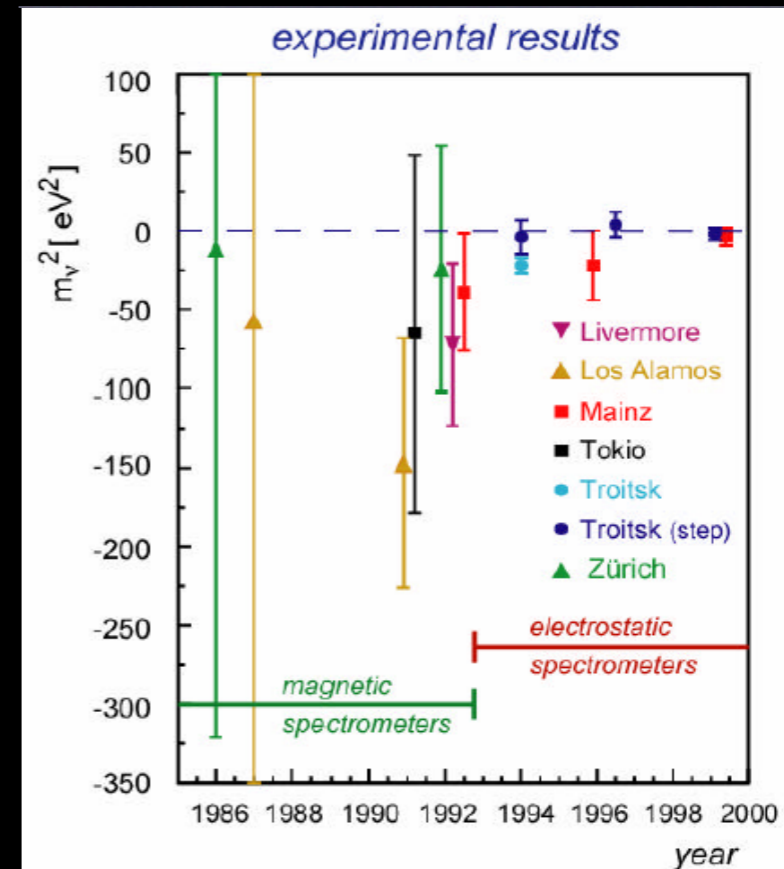
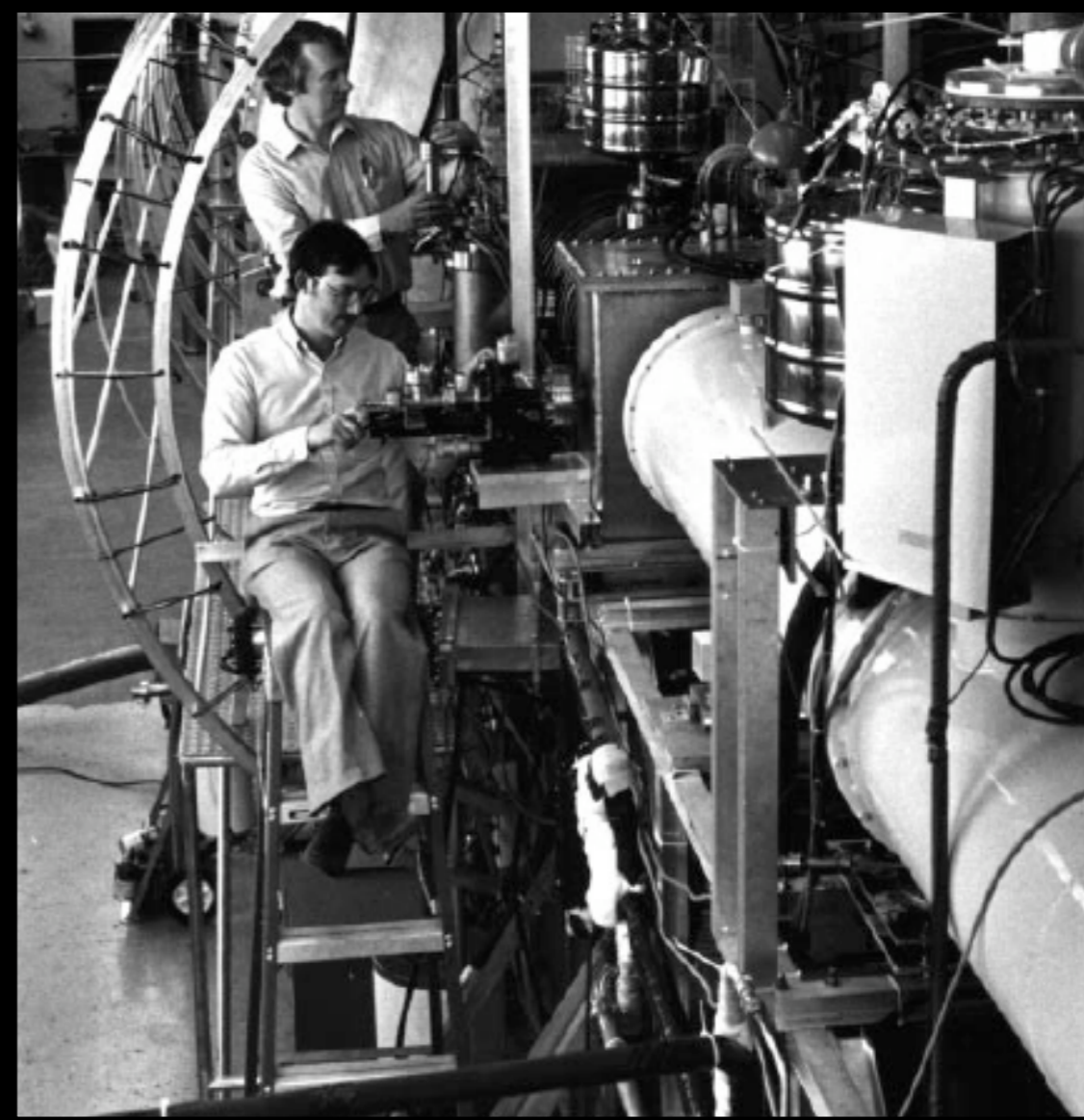
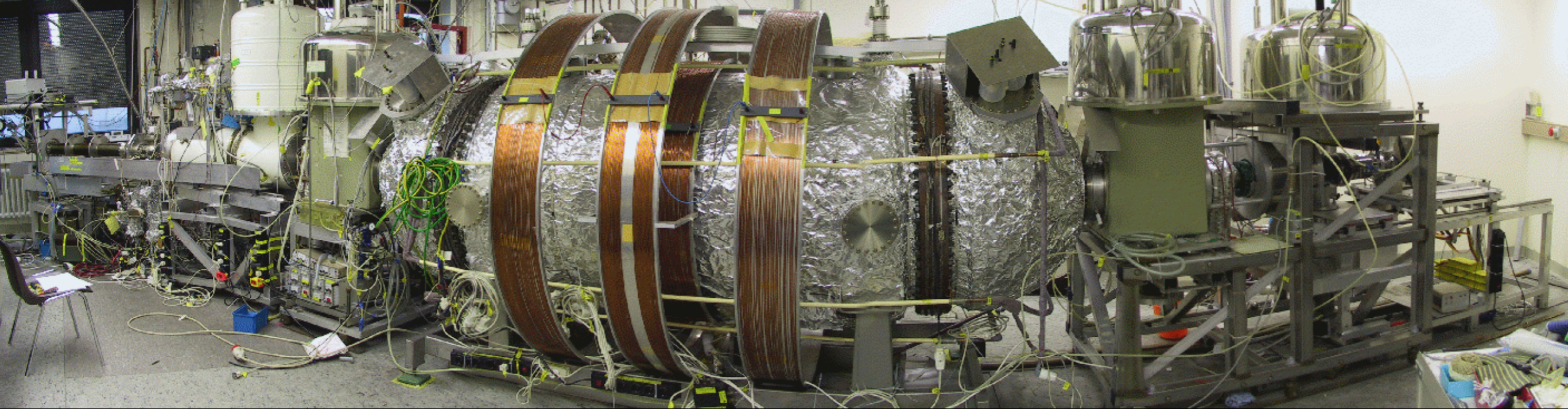


Fig. 3. Basic components of electrostatic-magnetic spectrometer employed in the present investigation of the end-point region of the tritium β -spectrum.

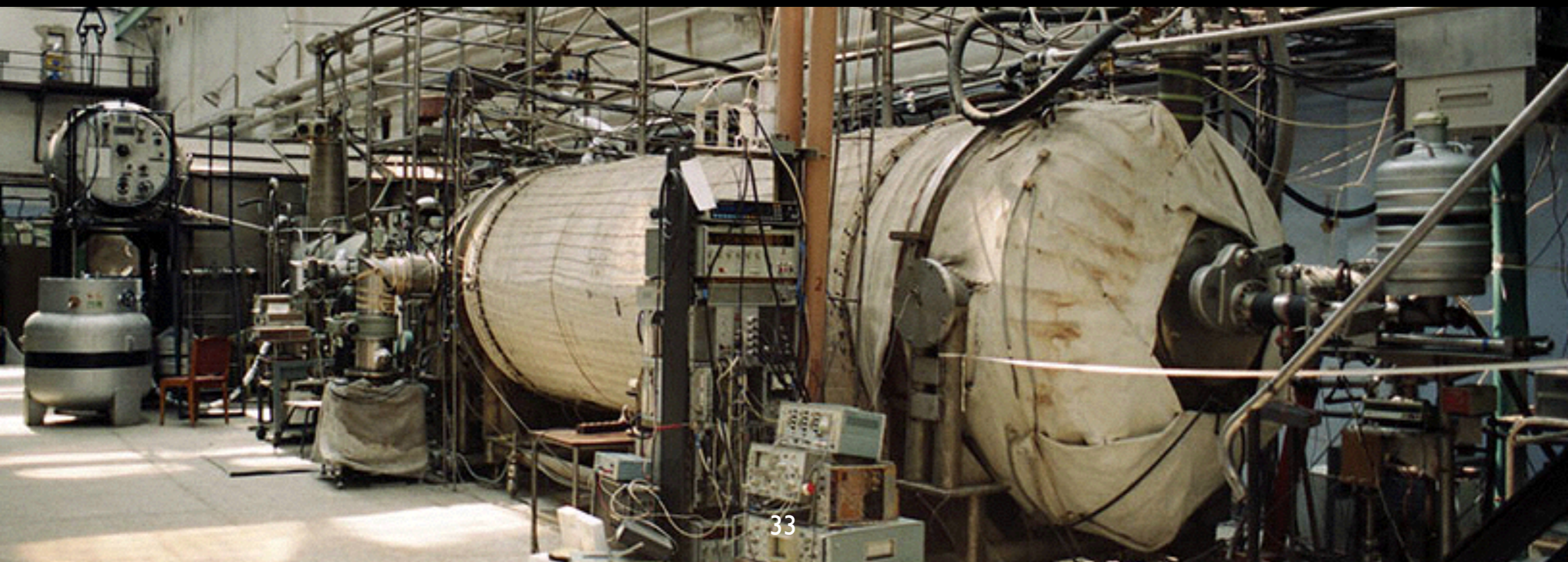
Los Alamos

- Robertson, Bowles, Wilkerson and others at Los Alamos devise the first gaseous tritium source experiment to circumvent earlier issues seen with solid state sources.
- Their limit of 27 eV rules out a previous signal for neutrino mass. Sets stage for gaseous sources in future designs.





Mainz & Troitsk



Current Techniques

Spectroscopy (KATRIN)

Magnetic Adiabatic
Collimation with
Electrostatic Filtering

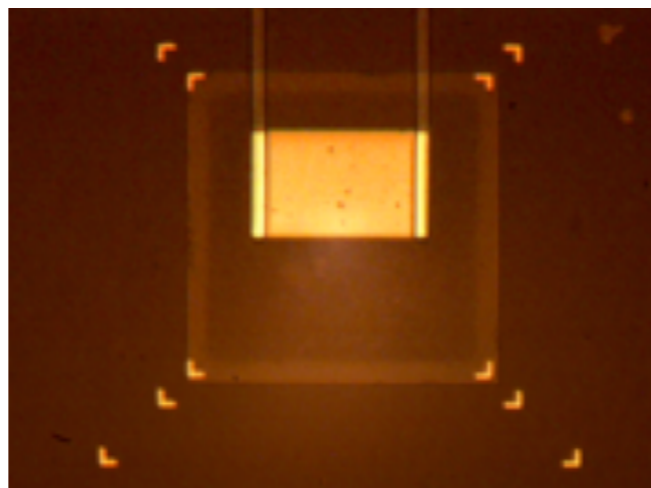
State-of-the-Art technique



Calorimetry (HOLMES, ECHO & NUMECS)

Technique highly
advanced.

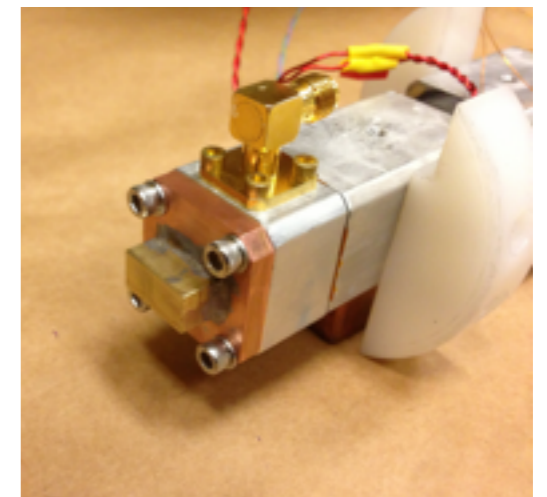
New experiment(s)
planned to reach
 $\sim eV$ scale.



Frequency (Project 8)

Radio-frequency
spectroscopy for beta decay

R&D phase (new results)

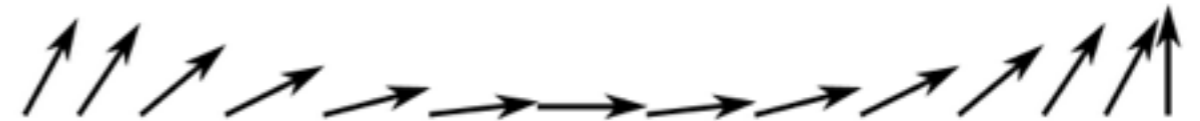
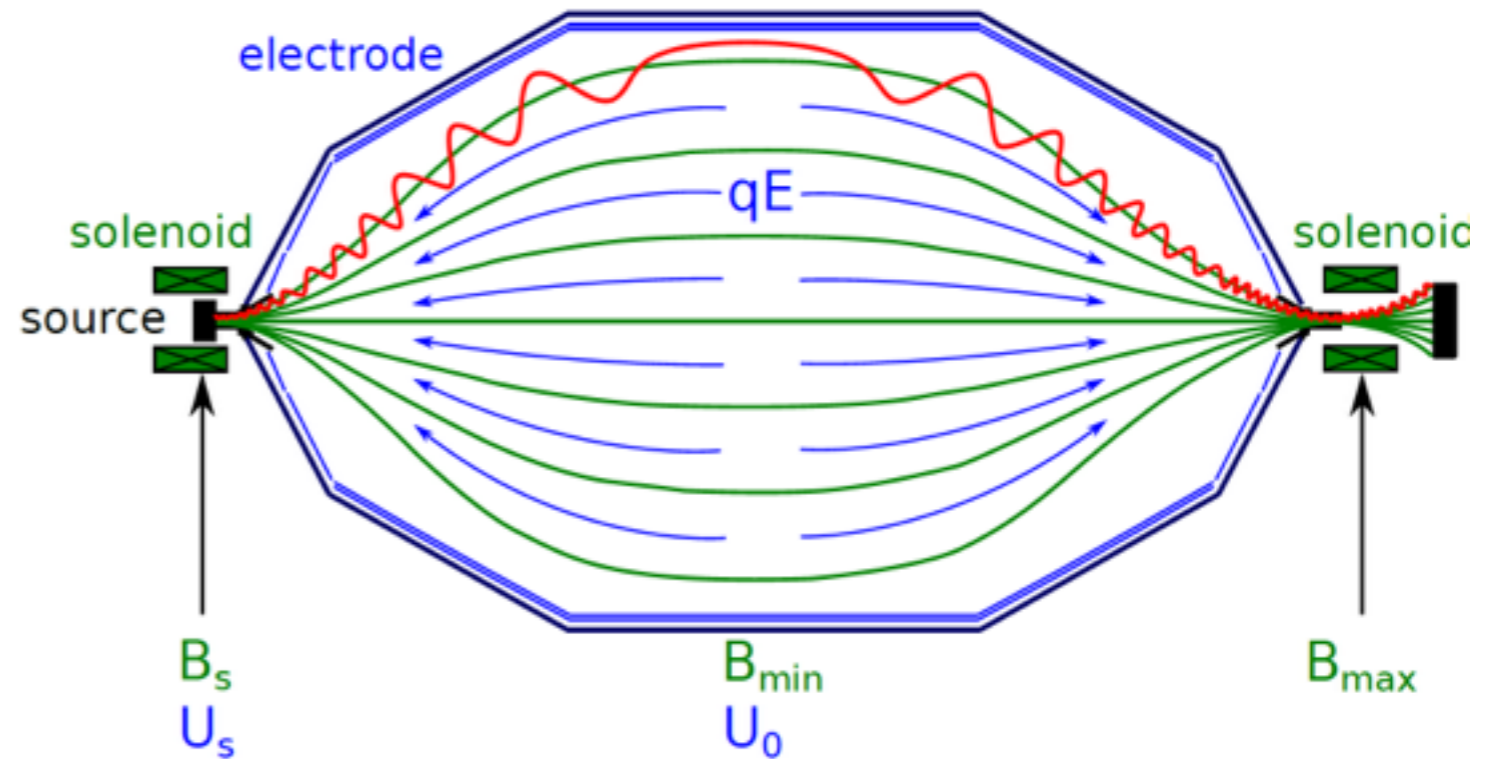


MAC-E Filter Technique

KATRIN



Spectroscopic: MAC-E Filter



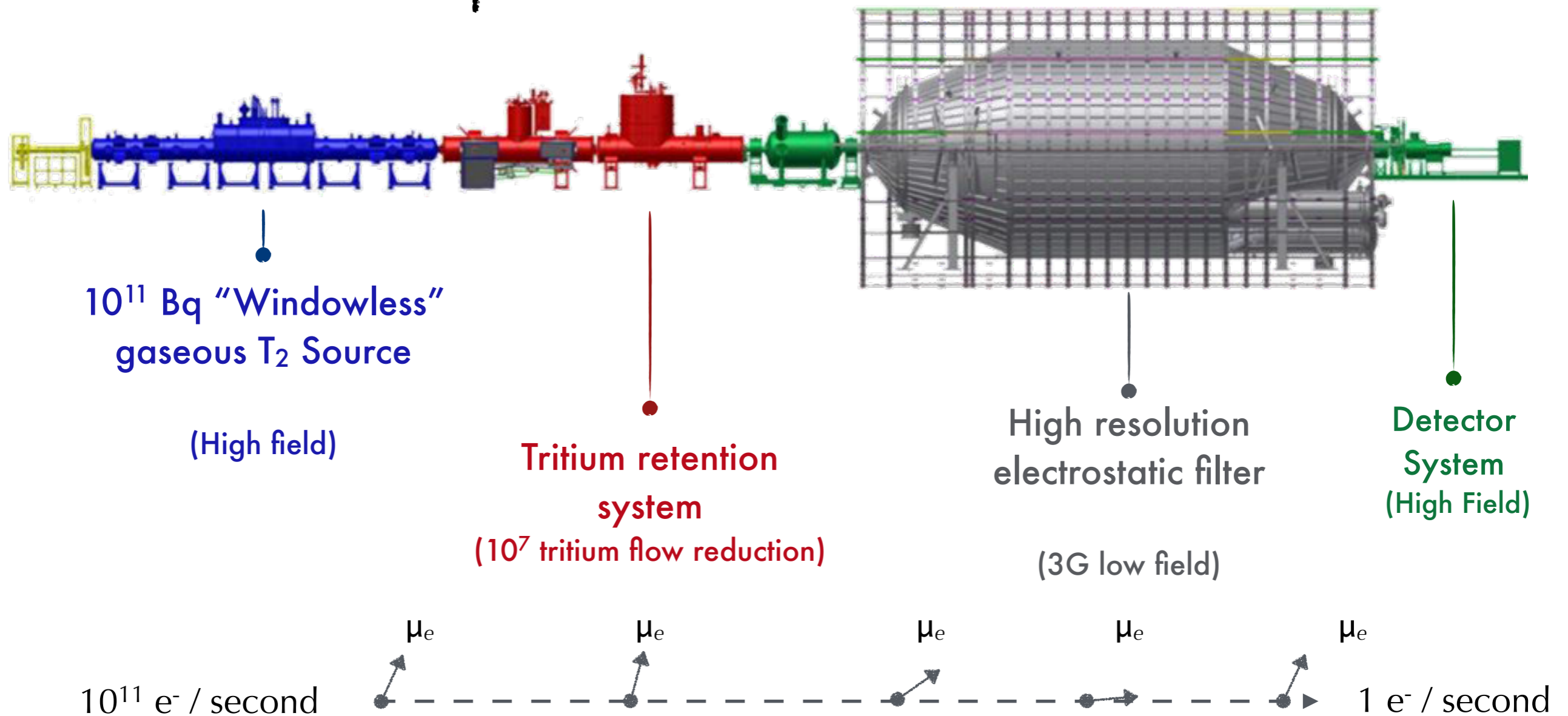
adiabatic transformation of e^- momentum

Inhomogeneous magnetic guiding field.
Retarding potential acts as high-pass filter

High energy resolution

$$(\Delta E/E = B_{\min}/B_{\max} = 0.93 \text{ eV})$$

The KATRIN Setup



Adiabatic transport ensures high retention of phase space for decay

$$\frac{\Delta E}{E} = \frac{B_{\min}}{B_{\max}} \rightarrow 0.93 \text{ eV}$$

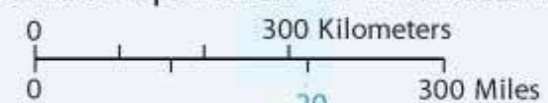
Energy resolution scales as the ratio of minimum / maximum fields

The Journey...



Scale 1: 19,500,000

Lambert Conformal Conic Projection,
standard parallels 40°N and 56°N



...and the arrival.





Field- Compensation Air Coils

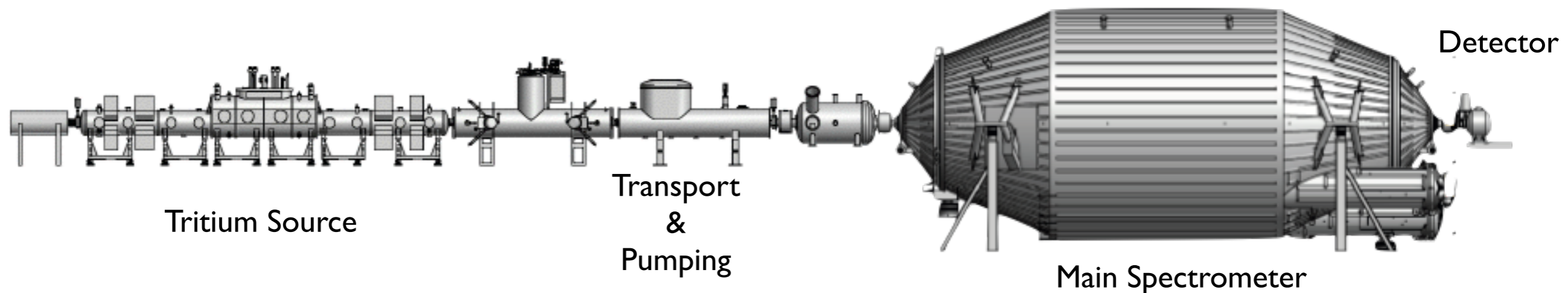


Inner electrode wire mesh



High Voltage Divider

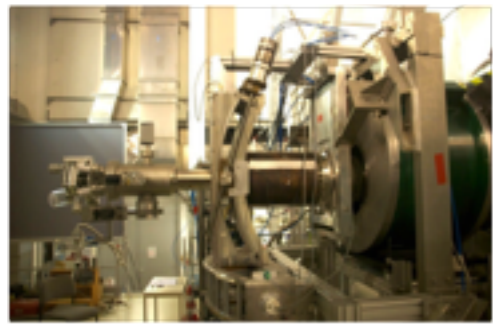
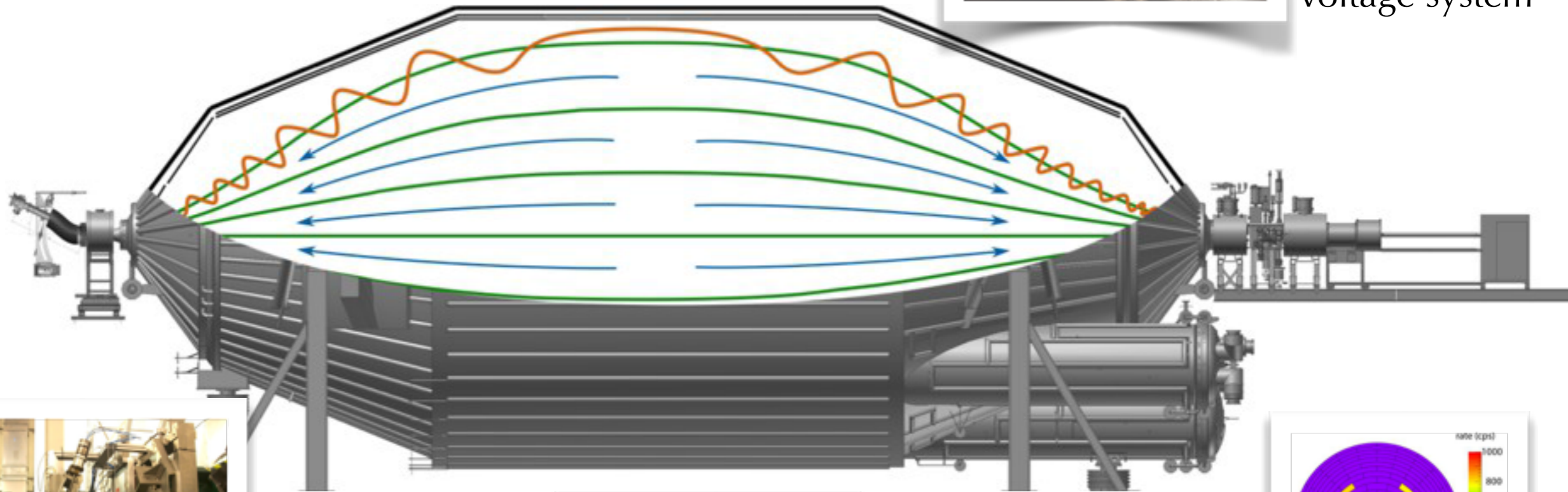
- A 10 m diameter analyzing spectrometer with 1:2000 energy resolution (0.93 eV)
- Extremely stable high voltage of main vessel.
- Few \sim ppm precision divider and monitoring spectrometer.



Spectrometer Commissioning



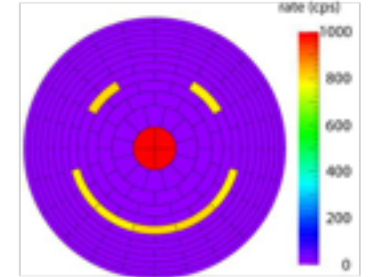
Precision high
voltage system



High precision
electron gun



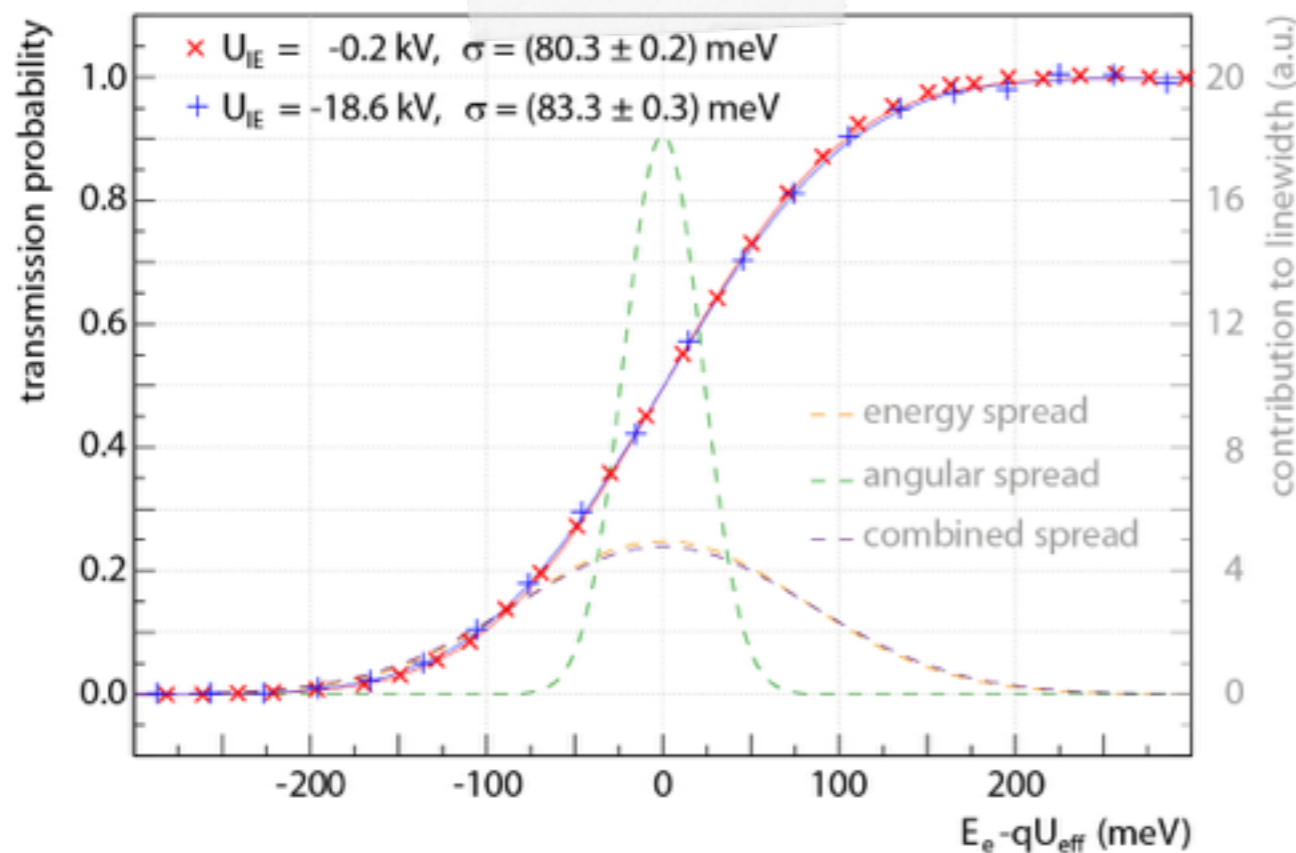
Ultra high vacuum
system



Full detector
system

Summer 2013 saw "first light" from the KATRIN.
Spectrometer and detector system fully integrated.
Allowed for test of transmission₄₀ function and background levels.

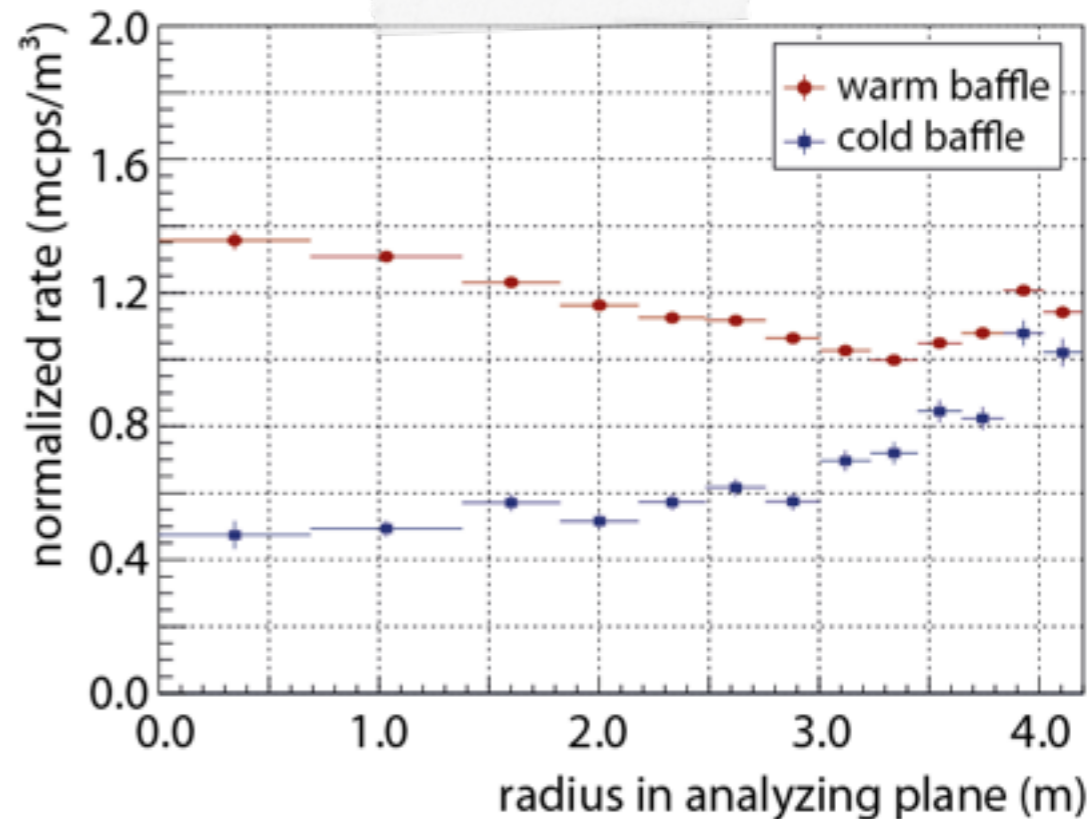
Transmission Function



At -18.6 keV, better than 100 meV resolution

Sharpest transmission function for a MAC-E filter

Background Rates



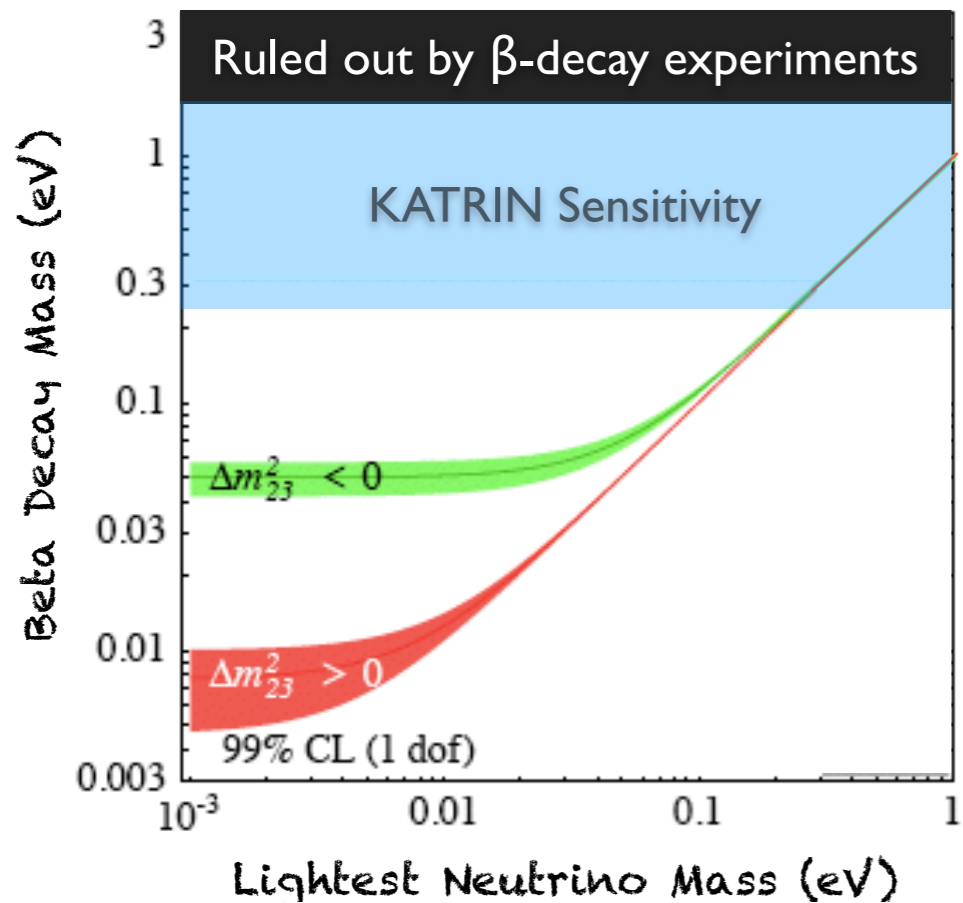
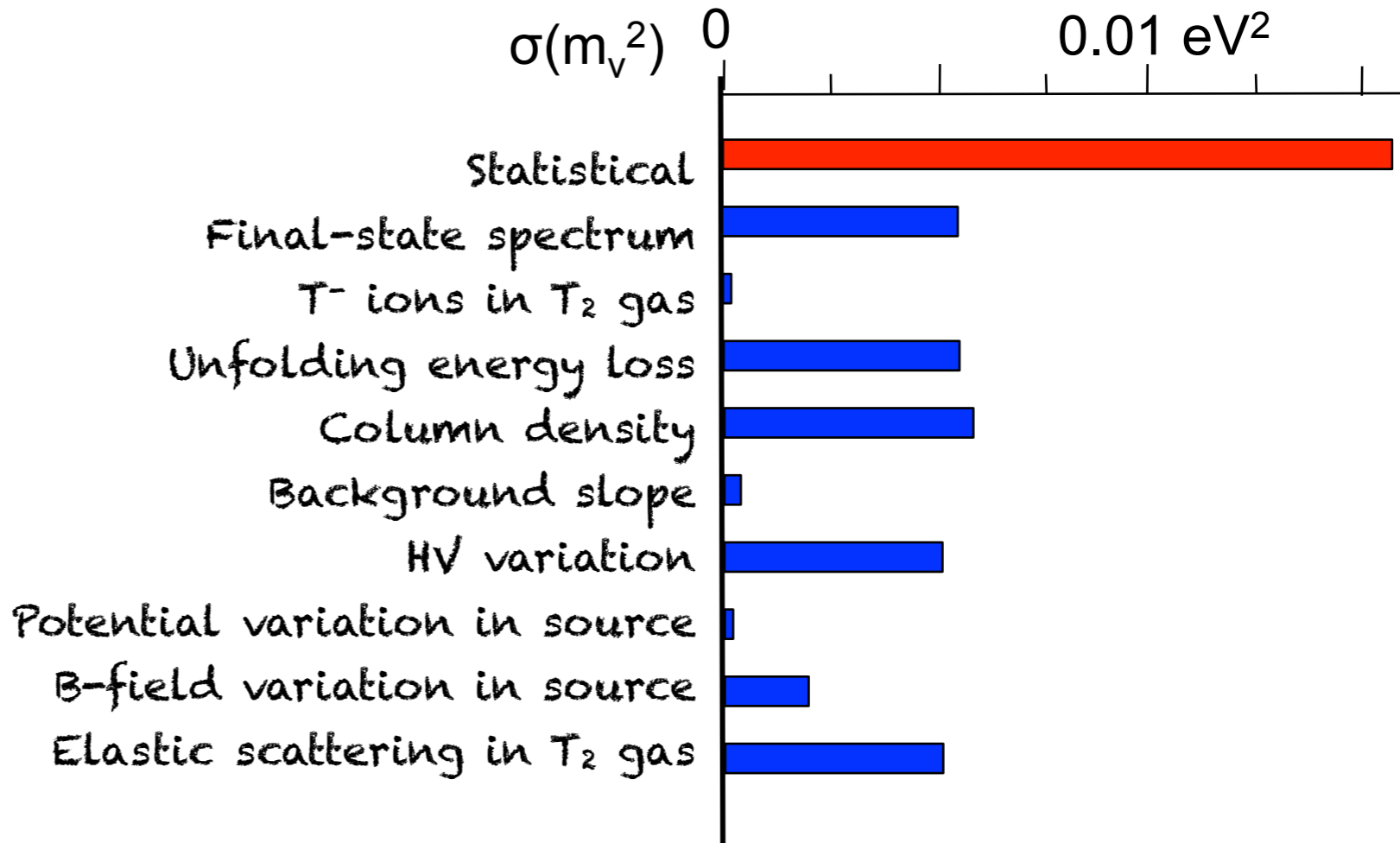
Background rate of order Hz (radon-dominated)

Greater reduction of backgrounds to come

Commissioning showed excellent behavior of MAC-E Filter response.

Next round of commissioning meant to study background levels.

Projected Sensitivity



Neutrino Mass Goals

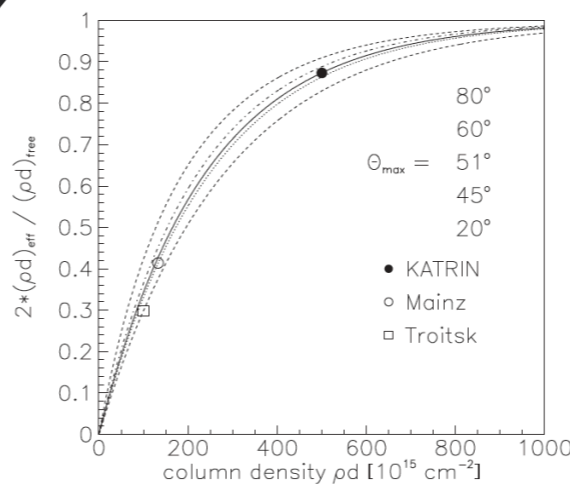
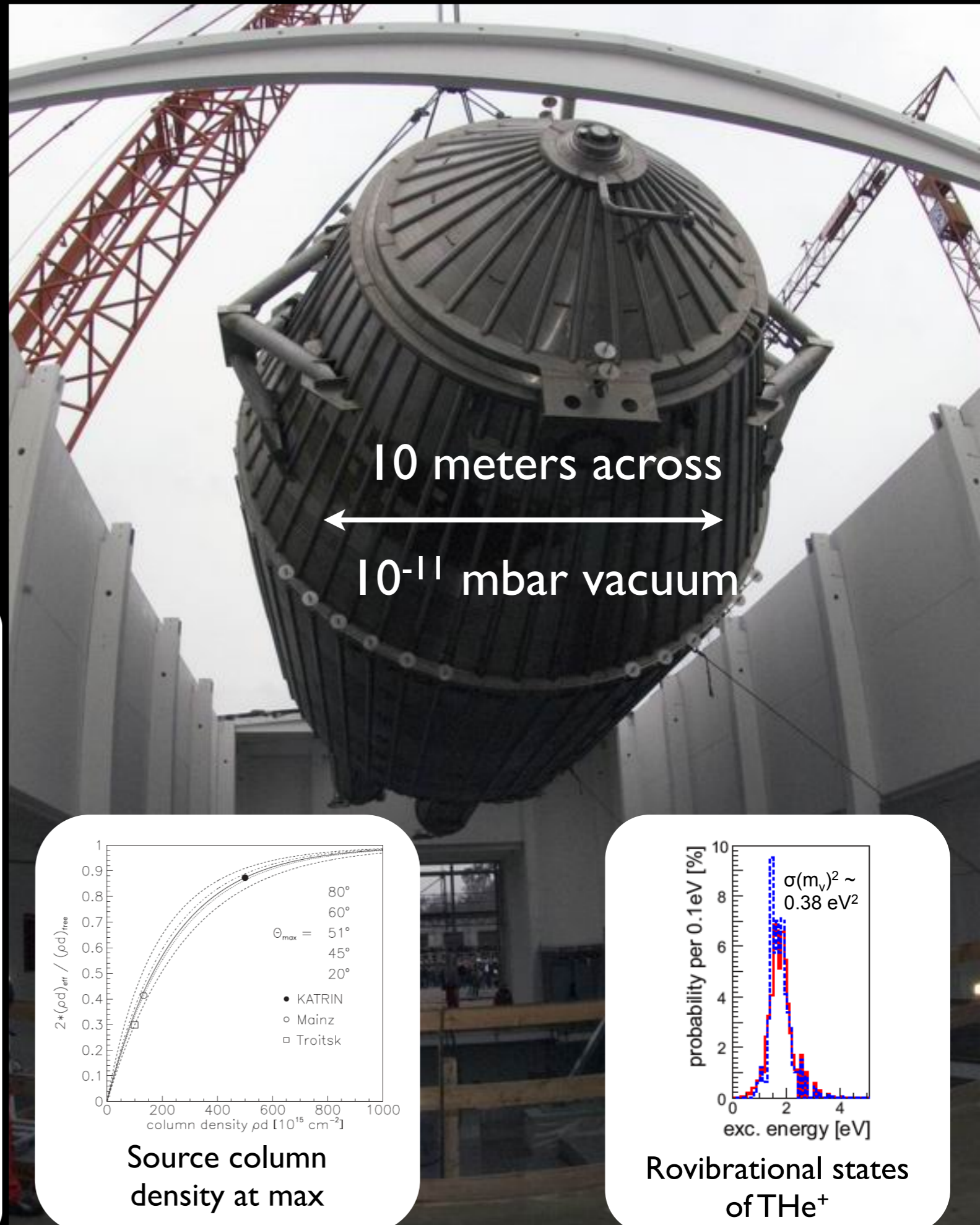
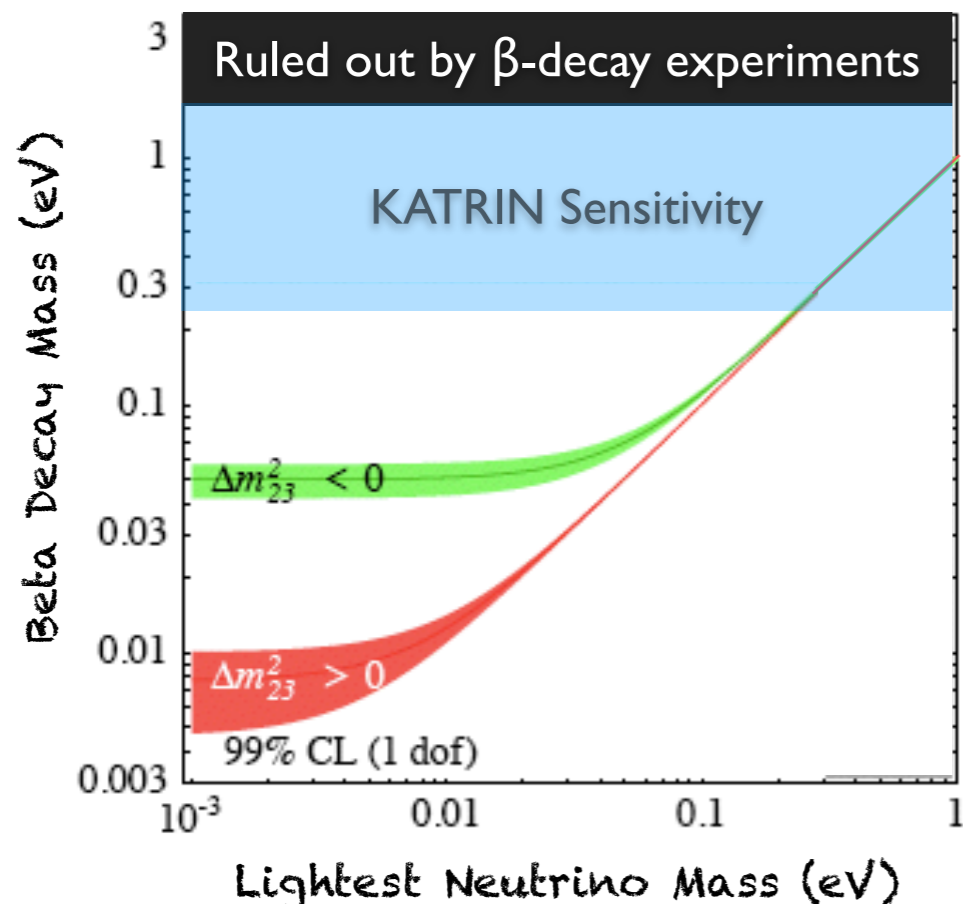
Discovery: 350 meV (at 5 σ)

Sensitivity: 200 meV (at 90% C.L.)

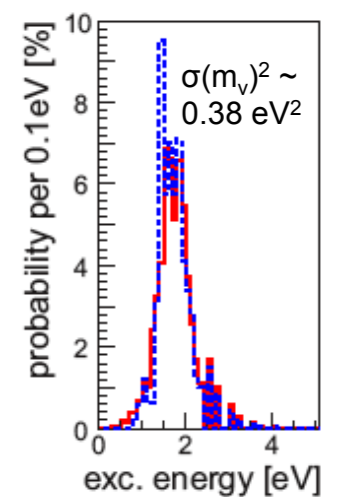
Data taking to
commence in 2016.

Can we push further?

- Can direct measurements push to the inverted ordering scale?
- To do so, they must have better scaling law.

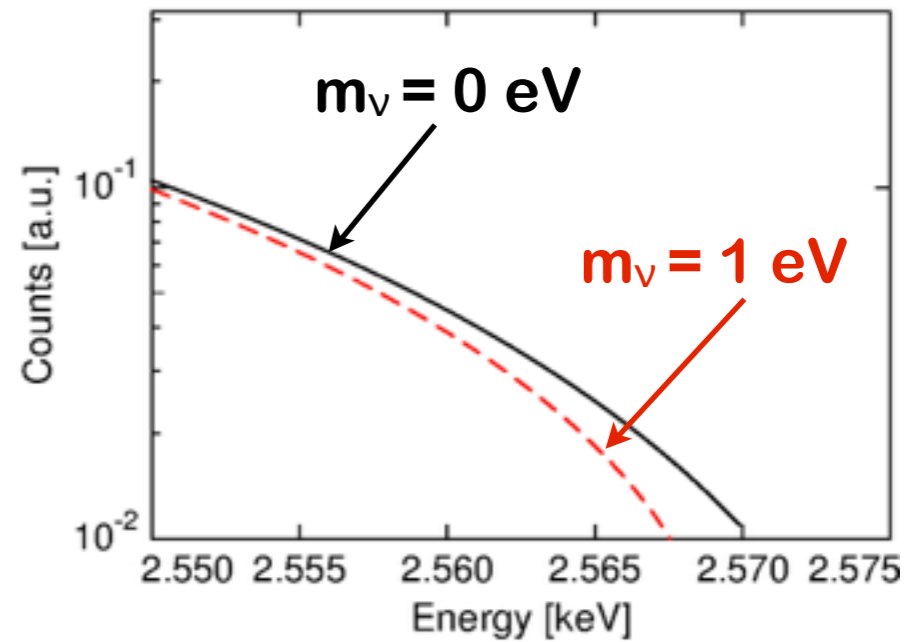
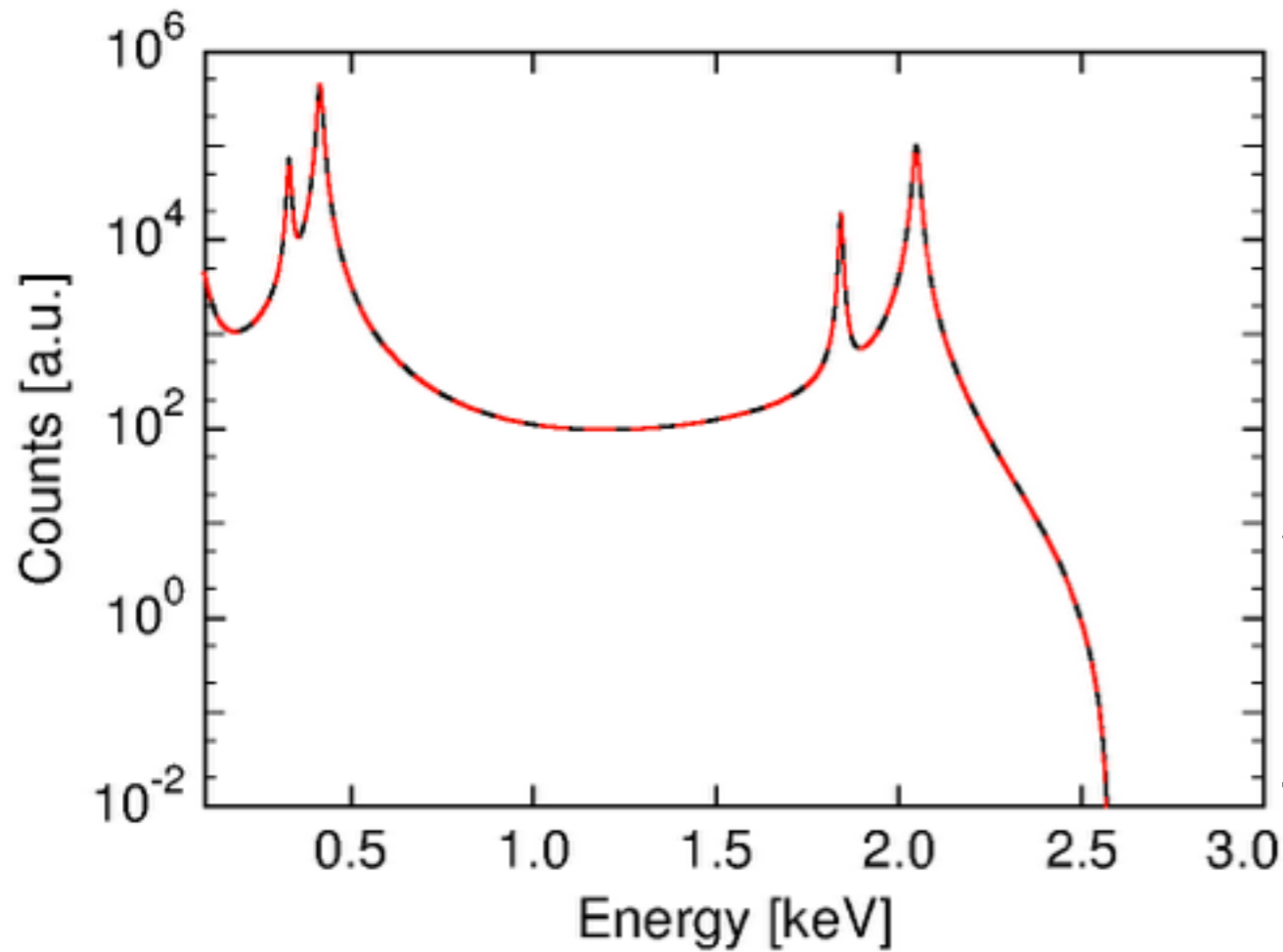


Source column density at max



Rovibrational states of THe^+

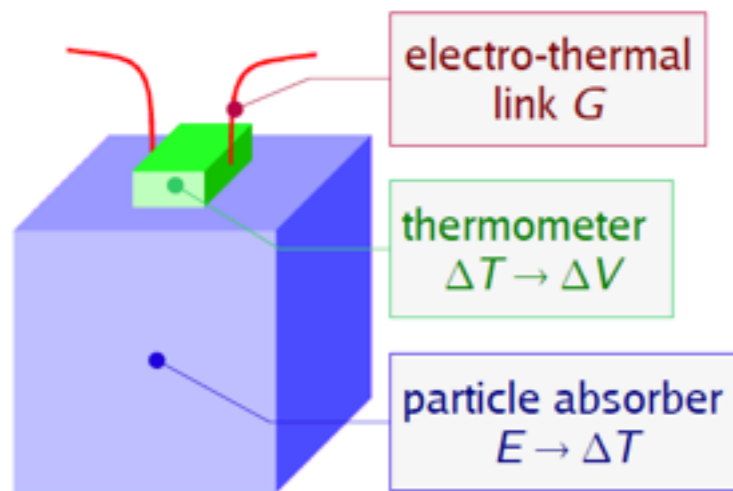
$$\dot{N} \sim (Q_{EC} - E_C)^2 \sum_i |U_{ei}|^2 \sqrt{1 - \frac{m_{\nu i}^2}{(Q_{EC} - E_C)^2}} \sum_H B_H \psi_H^2(0) \frac{\frac{\Gamma_H}{2\pi}}{(E_{EC} - E_H)^2 + \frac{\Gamma_H^2}{4}}$$



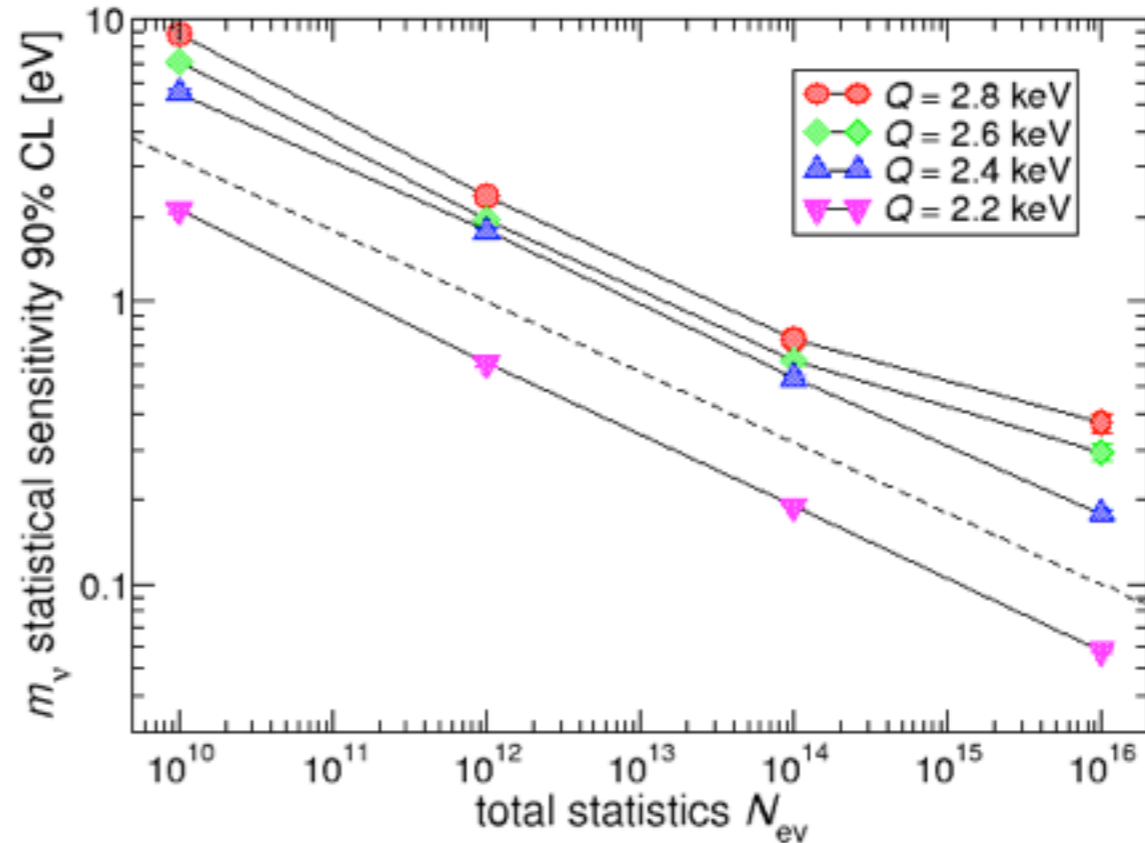
isotope
 New ~~kid~~ on the block:
 Electron Capture

Advantages & Challenges

Calorimetry



Challenges:



Source Activity

$N_{ev} > 10^{14}$ to reach sub-eV level

Advantages:

- Source = detector
- No backscattering
- No molecular final state effects.
- Self-calibrating

Detector Response

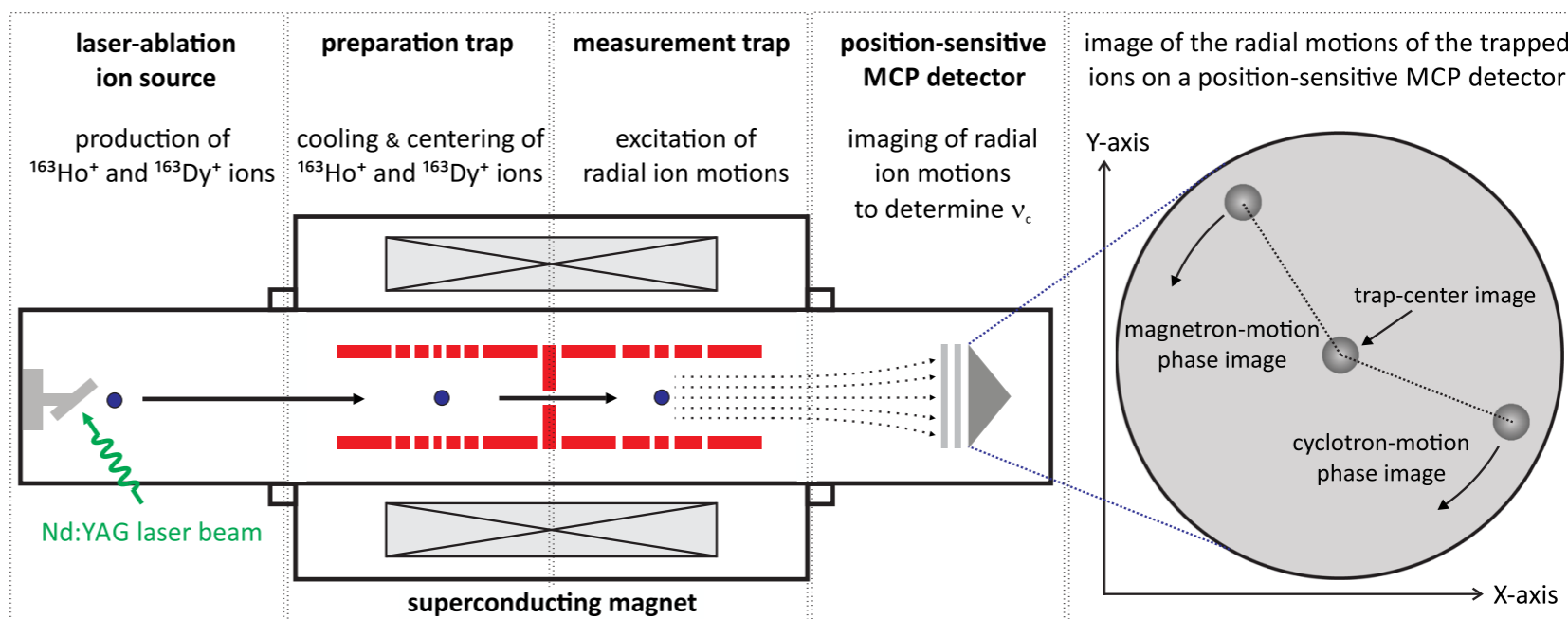
$\Delta E_{FWHM} < 10$ eV
Trisetime < 1 μ s

Experimental Challenges:

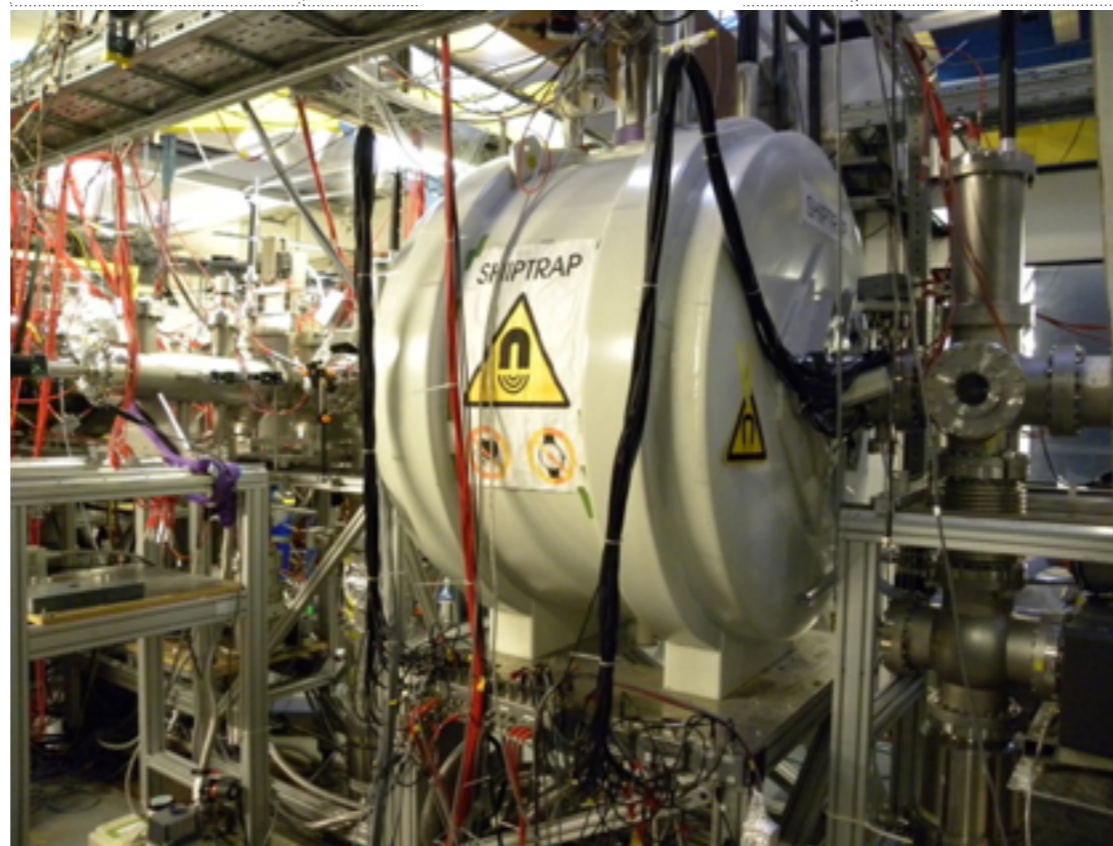
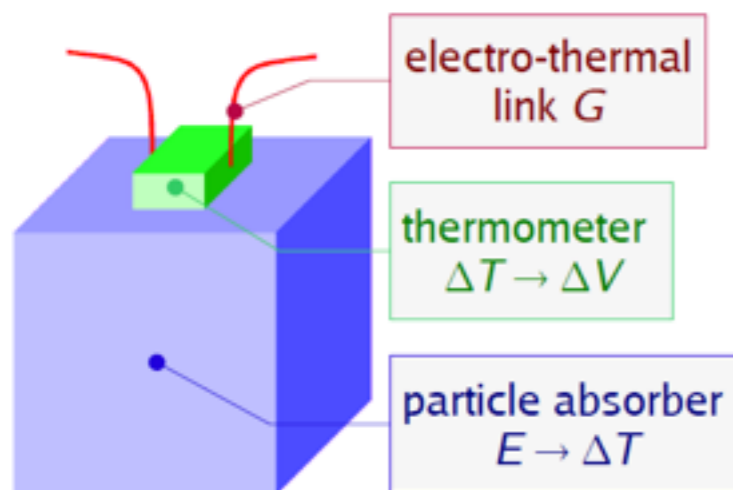
- Fast rise times to avoid pile-up effects.
- Good energy resolution & linearity
- Sufficient isotope production

New results!

SHIPTRAP



Calorimetry

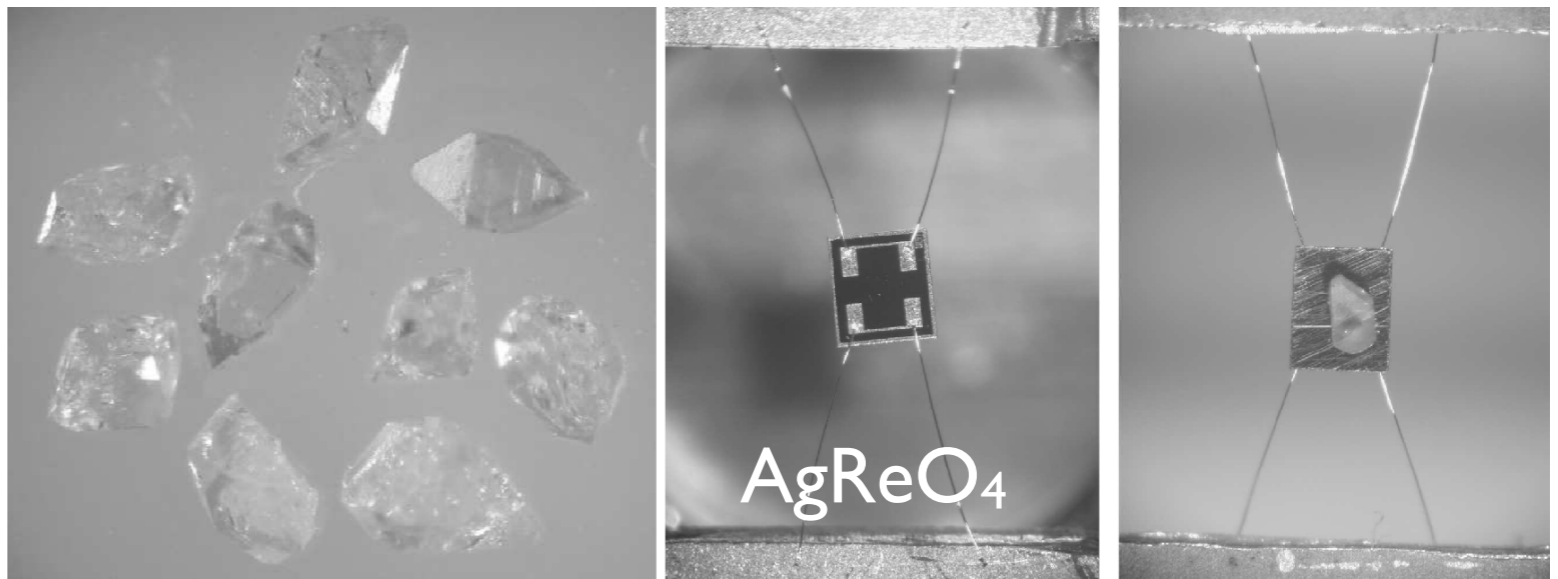


Latest results with Penning traps show improved resolution on the Ho-Dy mass difference.

/PhysRevLett.115.062501

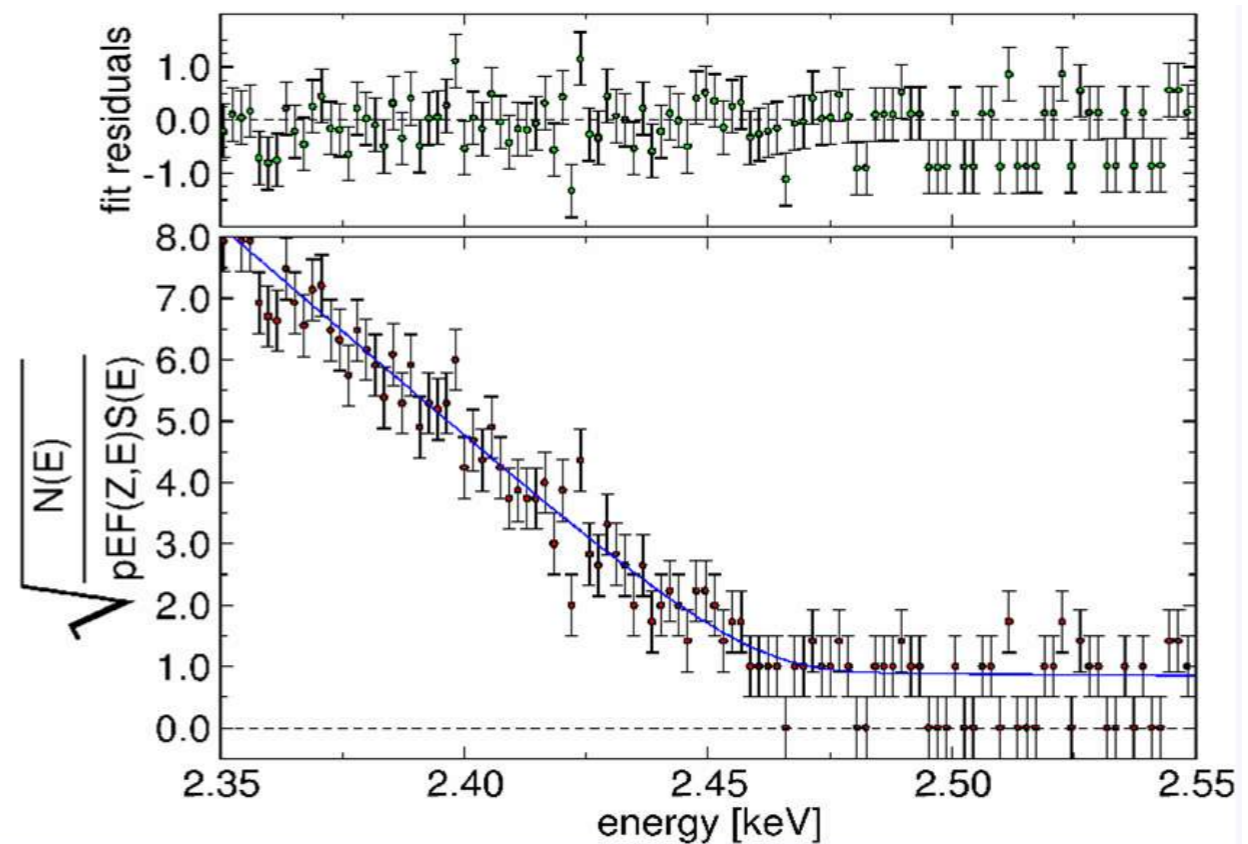
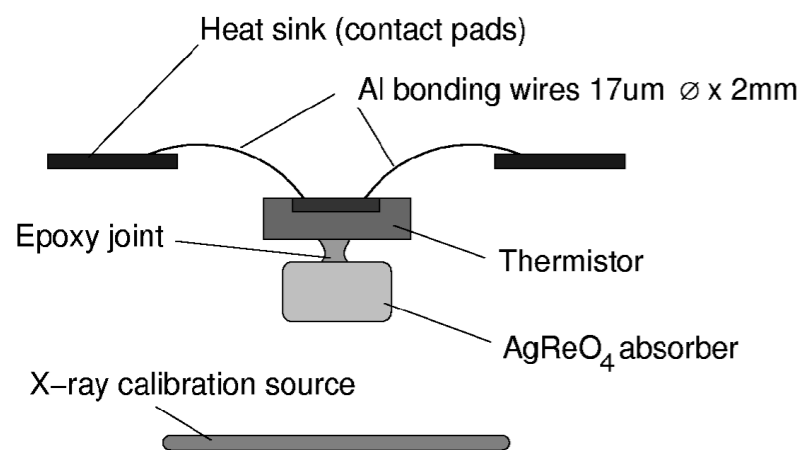
Their Predecessor

MARE



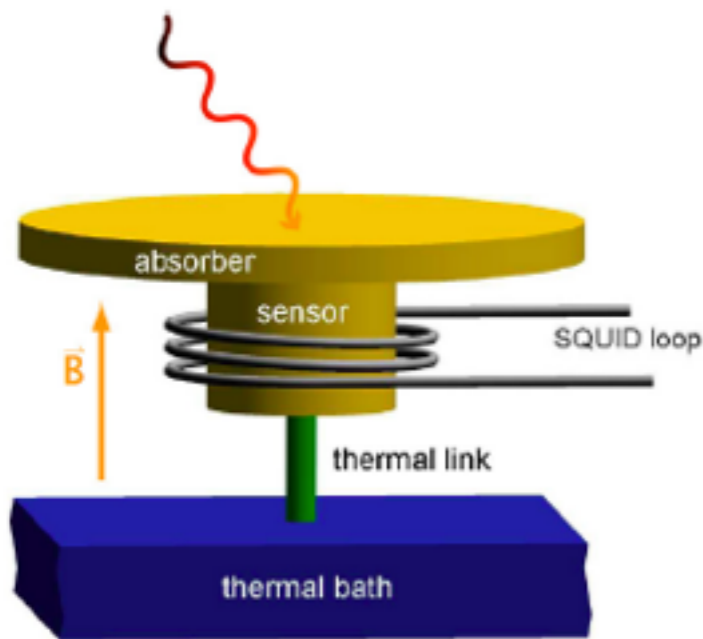
MARE provides the first β decay measurement of ^{187}Re using calorimetry

Calorimetry

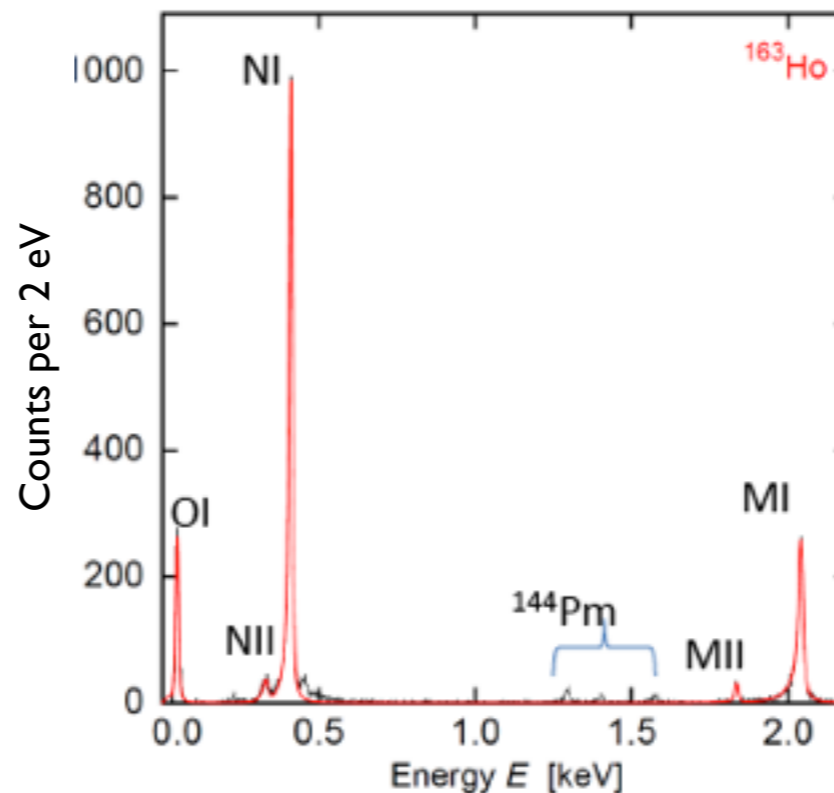
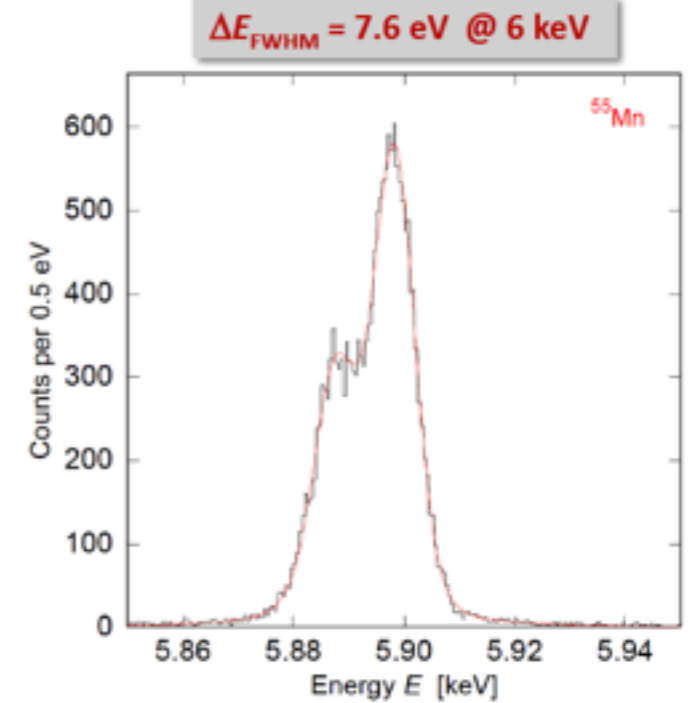
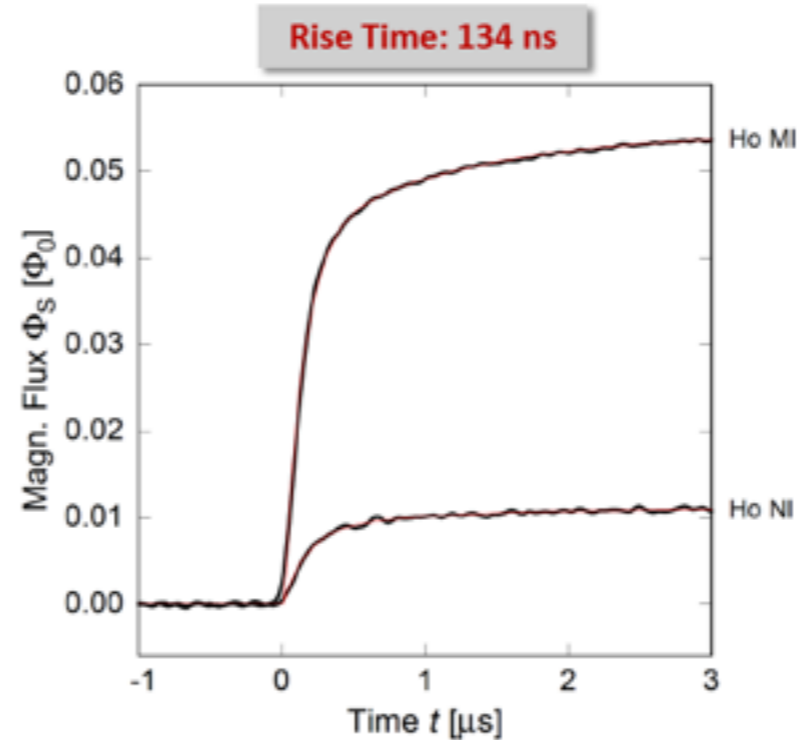


The ECHO Experiment

Technology:



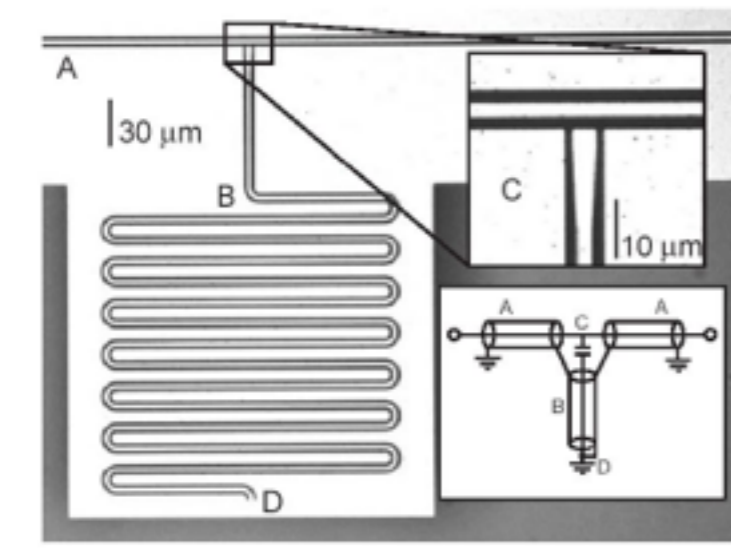
Metallic Magnetic Calorimeters



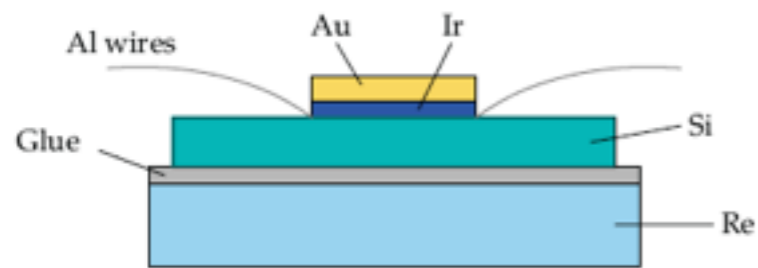
- The ECHO experiment uses metallic magnetic calorimeters to achieve goals.
- Fast rise times and good energy resolutions and linearity demonstrated.
- Endpoint measured at 2.80 ± 0.08 keV.

The HOLMES Experiment

Technologies:



Superconducting Resonators

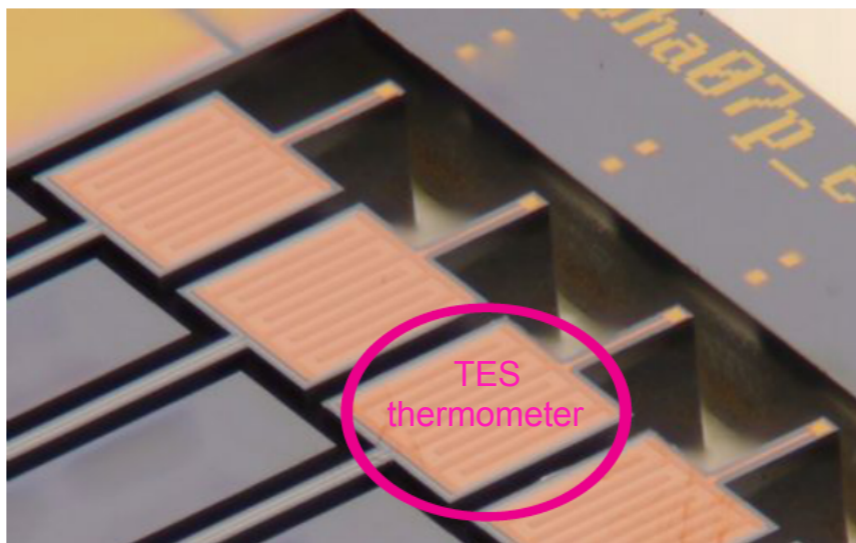
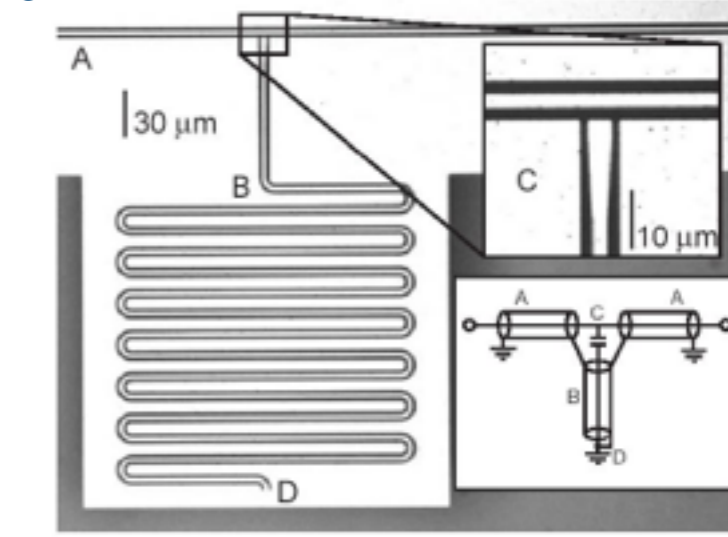
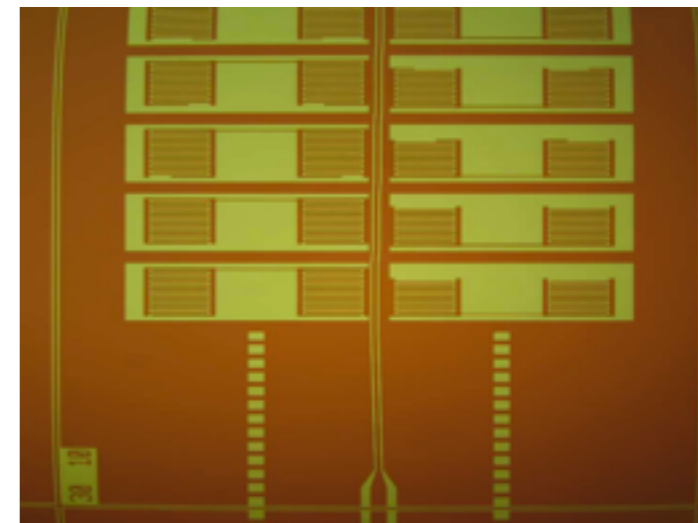


Transition Edge Sensors



HOLMES (Italy)

*transition edge
sensors / MKIDs*



NuMECS (USA)

transition edge sensors

Project 8

Coherent radiation emitted can be collected and used to measure the energy of the electron in non-destructively.

PROJECT 8

Frequency Approach



I. I. Rabi



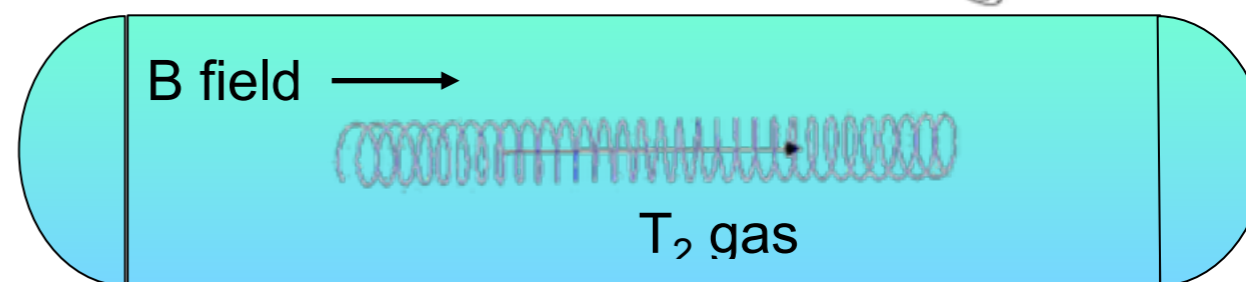
A. L. Schawlow

“Never measure anything but frequency.”

- Use cyclotron frequency to extract electron energy.

$$\omega(\gamma) = \frac{\omega_0}{\gamma} = \frac{eB}{K + m_e}$$

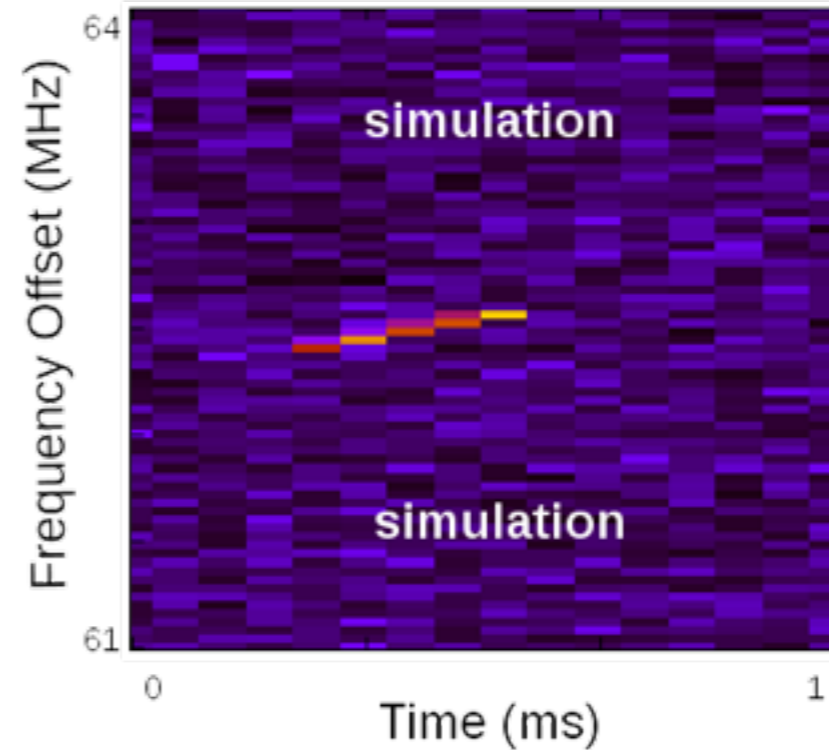
- Non-destructive measurement of electron energy.



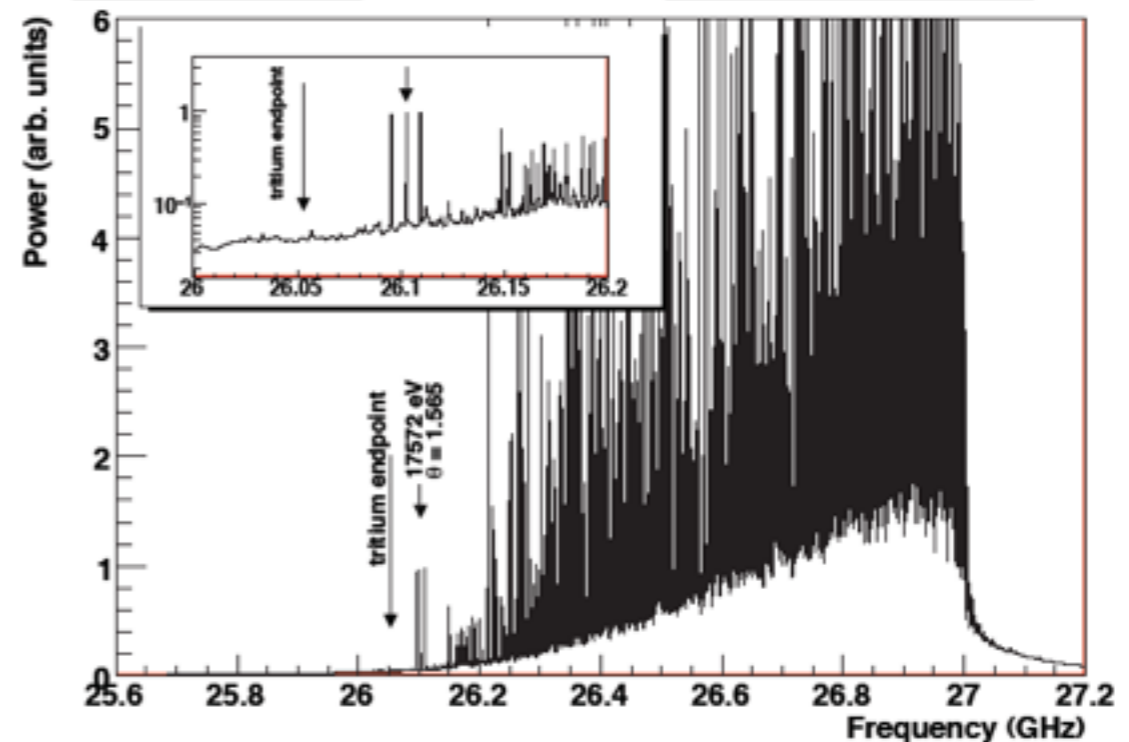
Unique Advantages

- ① **Source = Detector**
(no need to extract the electrons from the tritium)
- ② **Frequency Measurement**
(can pin electron energies to well-known frequency standards)
- ③ **Full Spectrum Sampling**
(full spectrum measured at once, large leverage for stability and statistics)

Signal Simulation
Power vs Time, Frequency



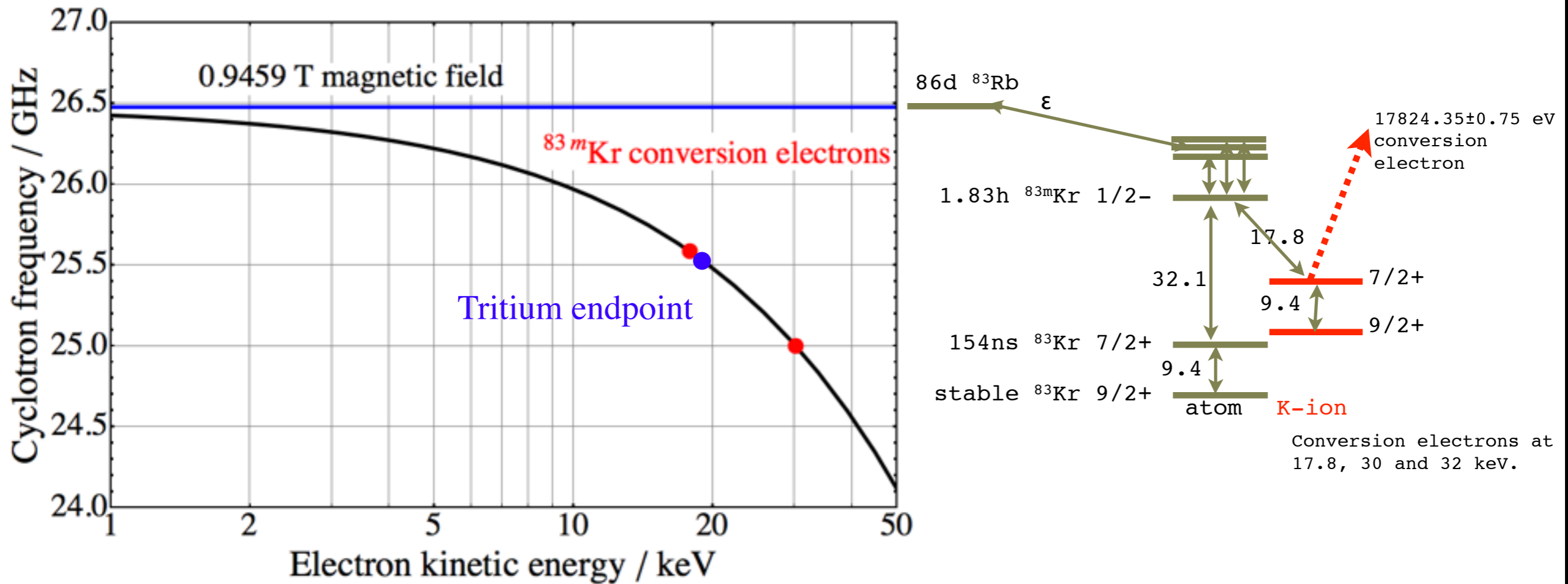
rare high-energy electrons ↔ many overlapping low-energy electrons



100,000 tritium decays in 30 μ s

Simulation of beta (frequency) spectrum

Initial Demonstration: ^{83m}Kr

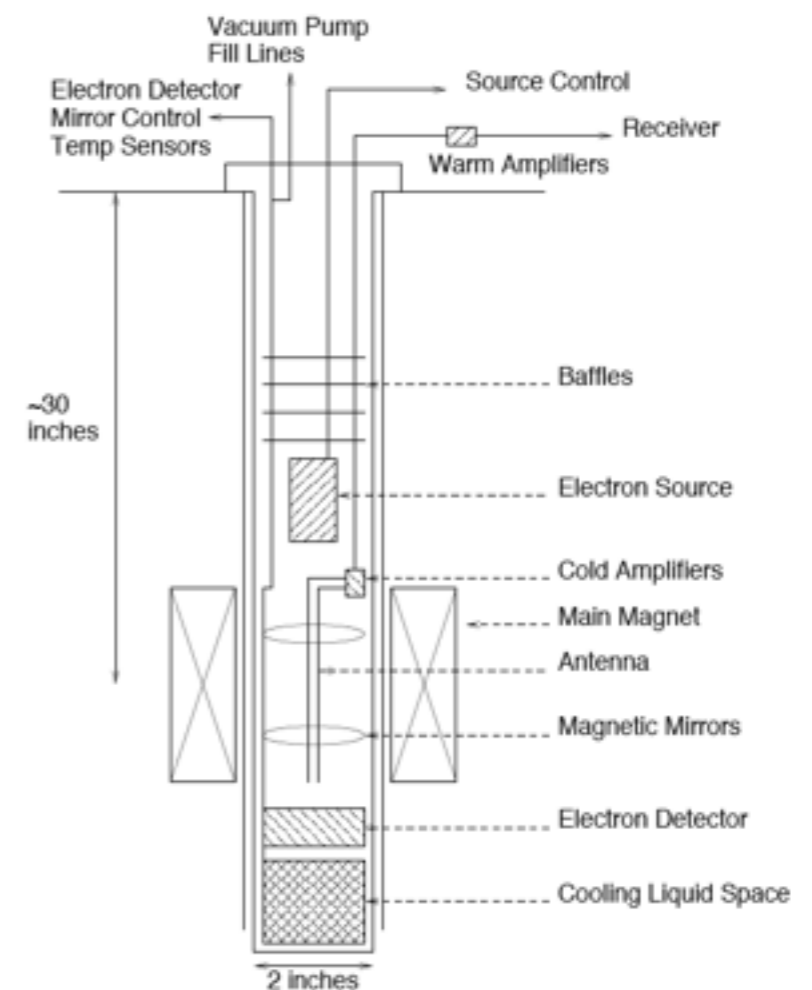


Phase I : Use mono-energetic source to determine single electron detection.

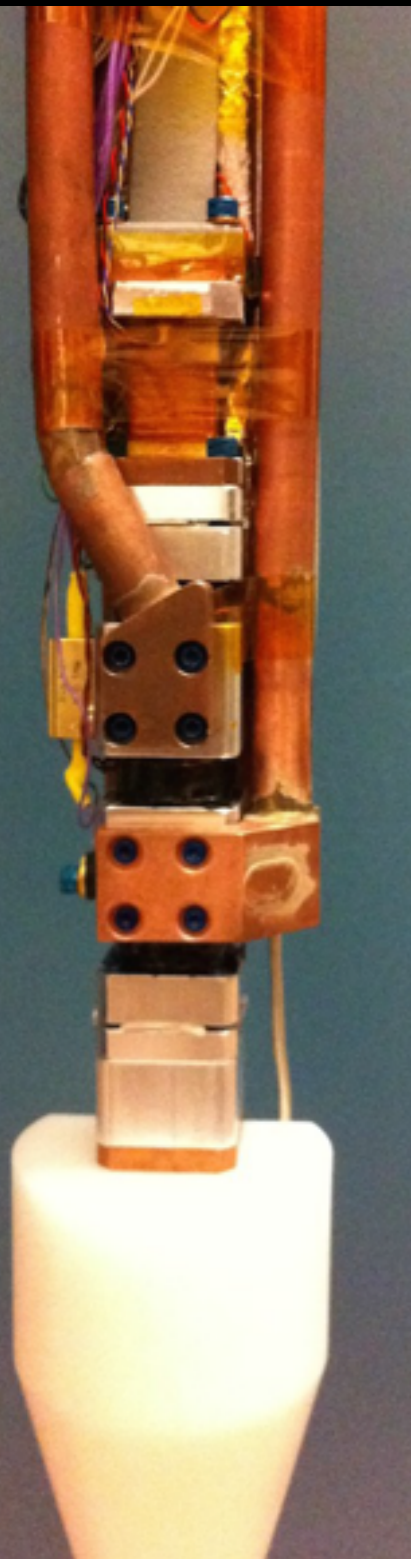
Use of standard gaseous ^{83m}Kr source allows quantification of energy resolution and linearity.

Basic Layout of Phase I

- ① **Gas/Electron System**
Provides mono-energetic electrons for signal detection.
- ② **Magnet System**
Provides magnetic field and trapping of electrons.
- ③ **RF Detection/Calibration System**
Detection of microwave signal.



The Apparatus



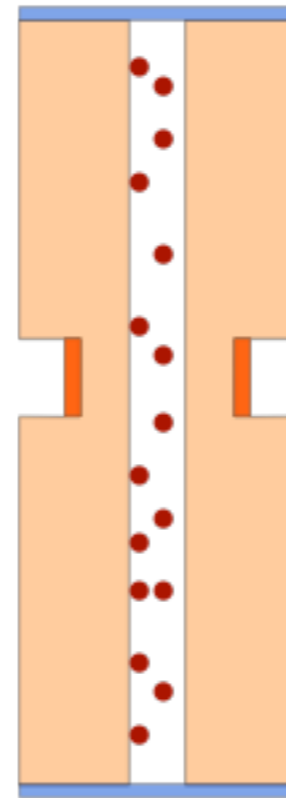
Copper waveguide

Kr gas lines

Magnetic bottle coil

Gas cell

Test signal injection port



Waveguide
Cut-away

B-Field trap profile

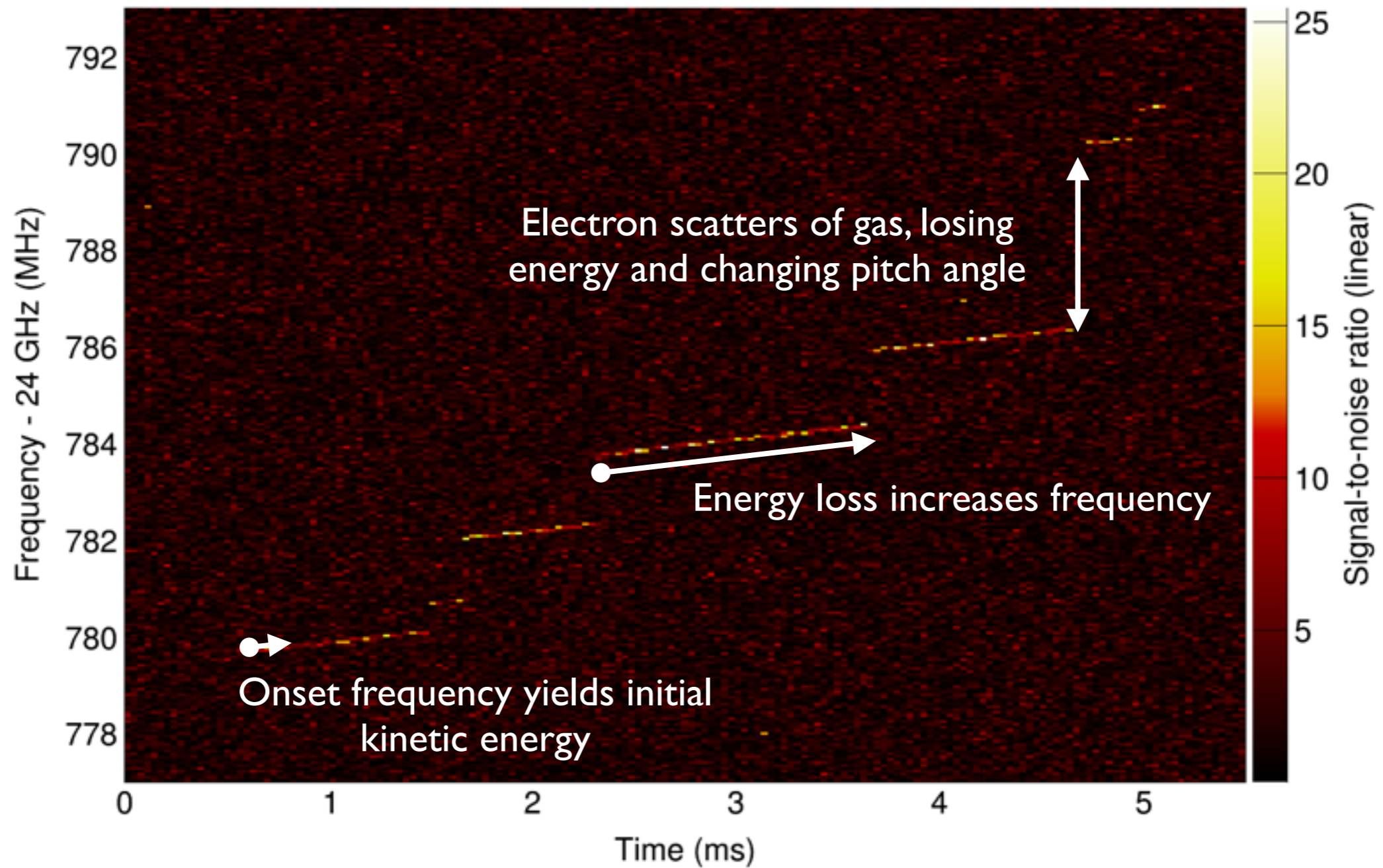


Photo of apparatus

Cyclotron frequency coupled directly to standard waveguide at 26 GHz, located inside bore of NMR 1 Tesla magnet.

Magnetic bottle allows for trapping of electron within cell for measurement.

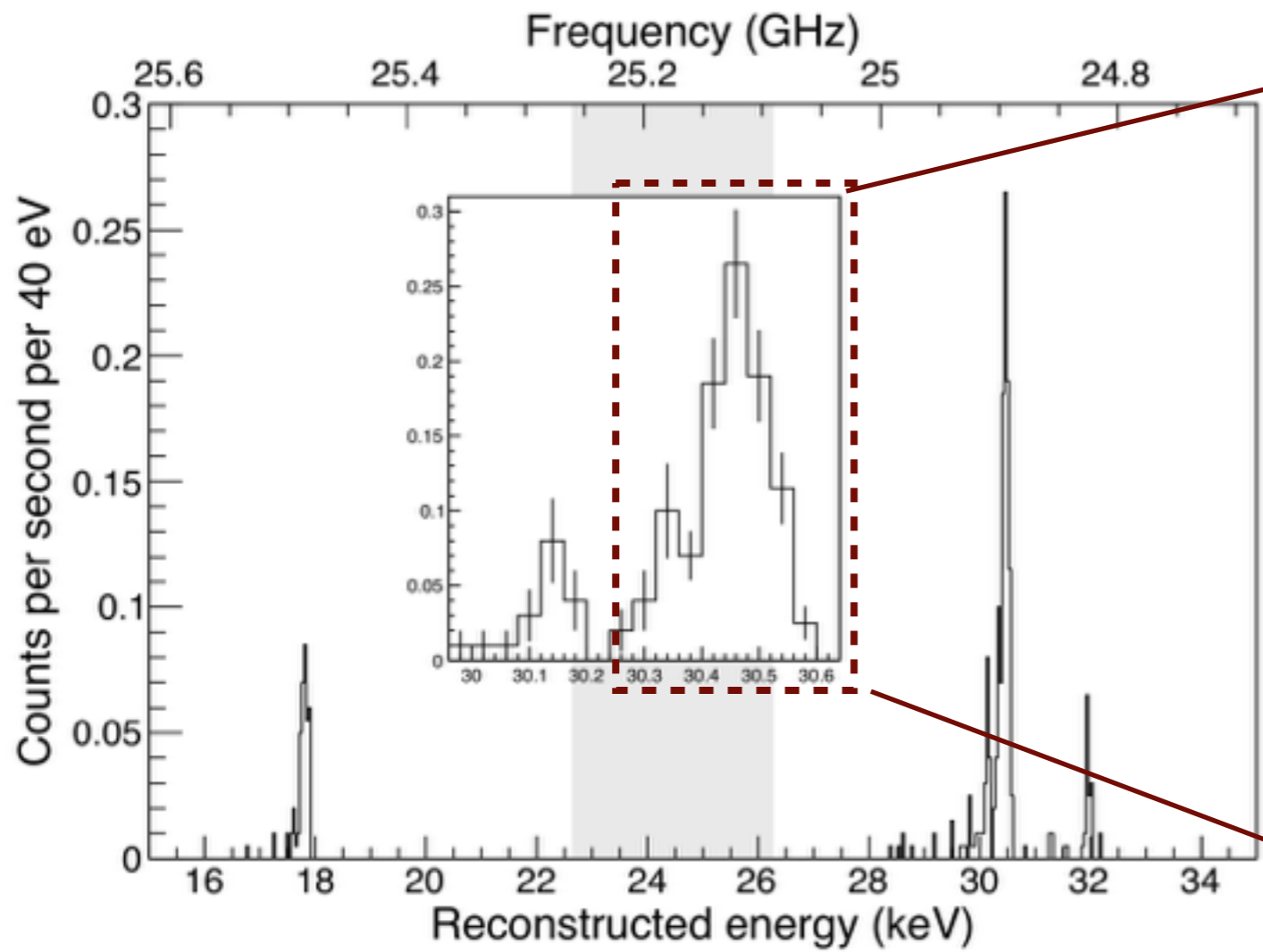
Project 8 "Event Zero"



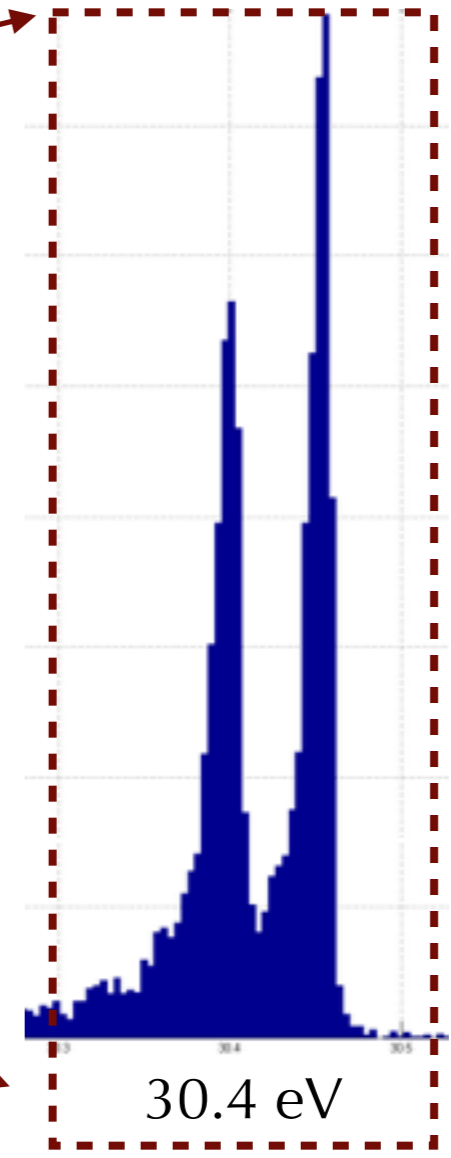
Clear detection of single electrons from their emitted cyclotron frequency.

All predicted features present (sudden onset, energy loss, scattering loss)

Image Reconstruction & Energy Resolution



FWHM ~ 140 eV



FWHM ~15 eV
(and improving)

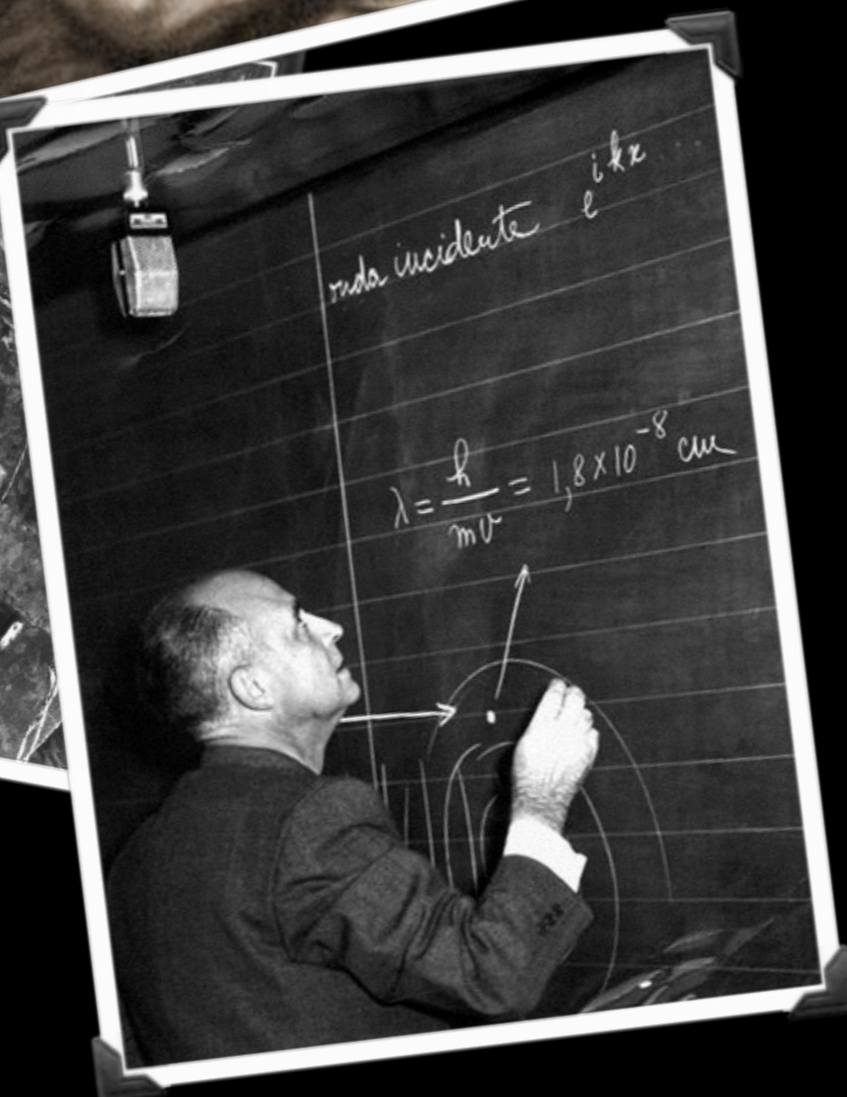
Event reconstruction from image reconstruction allows detailed analysis
(energy & scattering all extractable)



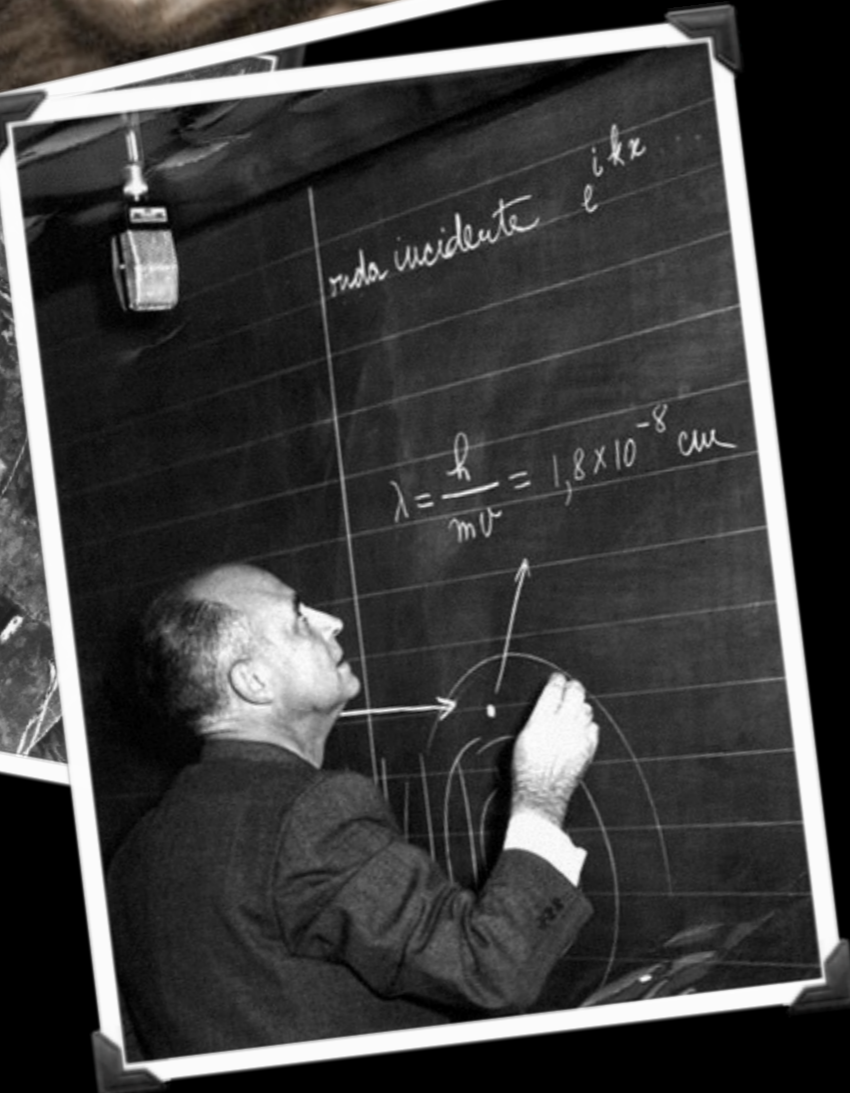
• The quest for neutrino mass has a long and very rich history, filled with remarkable people possessing remarkable ingenuity.



• We are by no means done. Oscillations provide a prediction that can and should be tested.



• Frontiers in beta decay, neutrinoless double beta decay and cosmology can now all feed into this remarkable measurement.

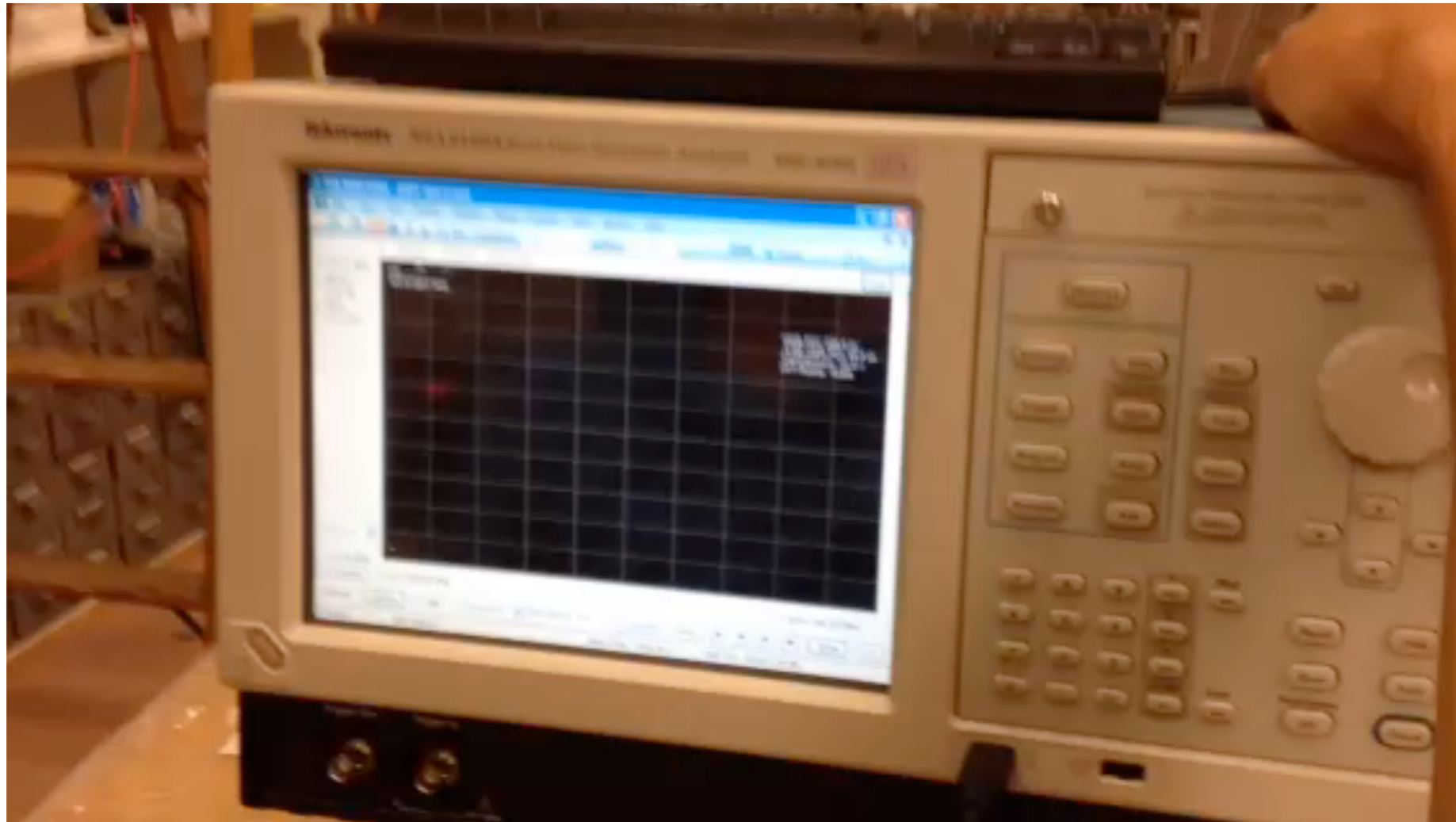


Thank you for
your attention

I'm sorry, we are out of time

(Backup slides)

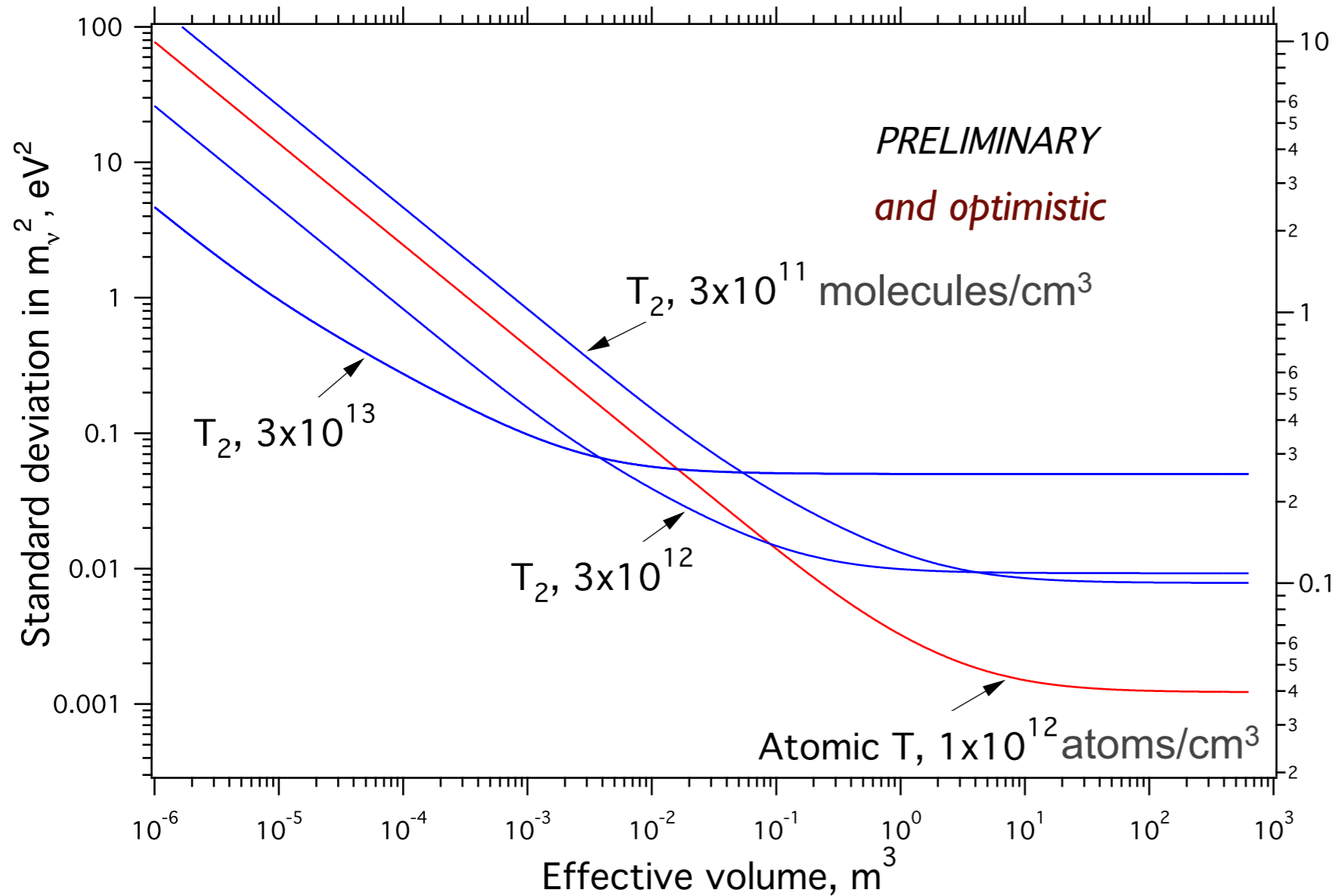
Eureka moment



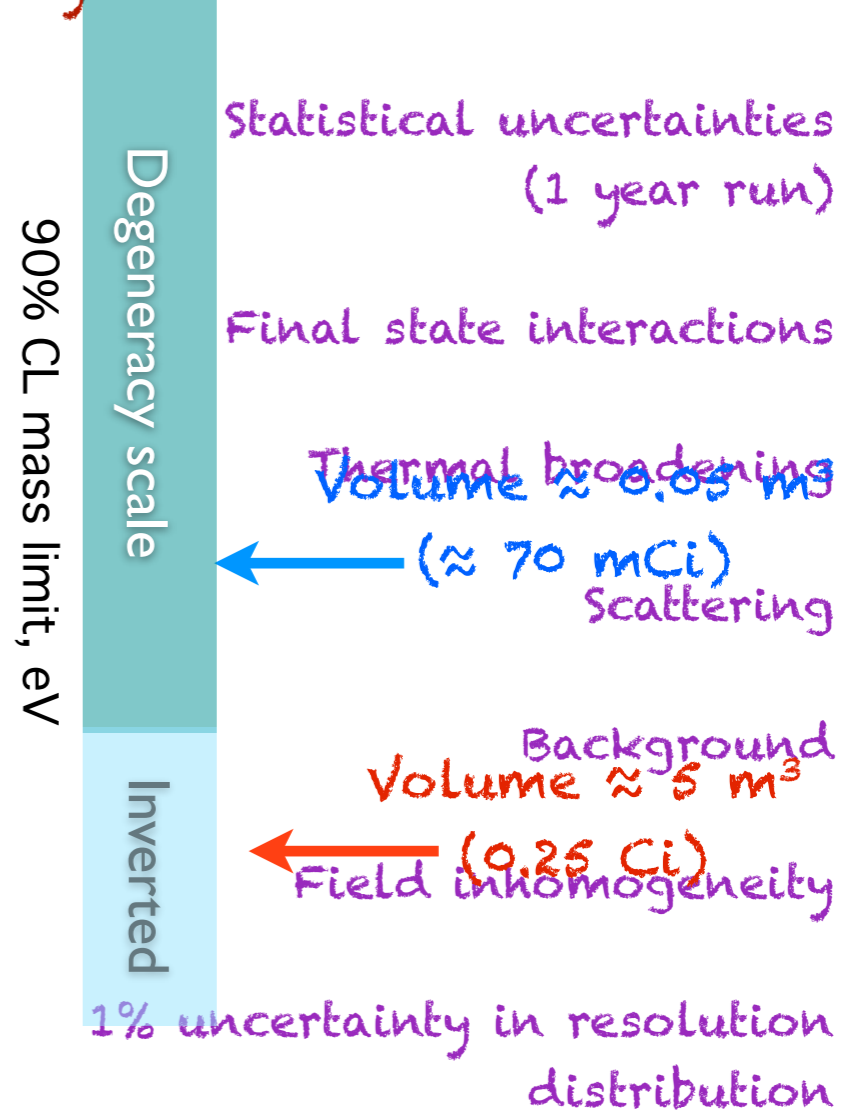
First detection of single-electron cyclotron radiation.

Data taking on June 6th, 2014 immediately shows trapped electrons.

Projected Sensitivity (Molecular & Atomic)



Systematics include:



Systematics include final state interactions, thermal broadening, statistical uncertainties, and scattering.

Backgrounds in experiments

Experiment		Mass [kg] (total/FV*)	Bkg (cnts/ROI -t-y) [†]	Width (FWHM)
CUORE0	^{130}Te	32/11	300	5.1 keV ROI
EXO-200	^{136}Xe	170/76	130	88 keV ROI
GERDA I	^{76}Ge	16/13	40	4 keV ROI
KamLAND-Zen (Phase 2)	^{136}Xe	383/88	210 per t(Xe)	400 keV ROI
CUORE	^{130}Te	600/206	50	5 keV ROI
GERDA II	^{76}Ge	35/27	4	4 keV ROI
MAJORANA DEMONSTRATOR	^{76}Ge	30/24	4	4 keV ROI
NEXT 100	^{136}Xe	100/80	9	17 keV ROI
SNO+	^{130}Te	2340/160	45 per t(Te)	240 keV ROI

↑ Measured
 ↓
 ↑ Projected
 ↓

* FV = $0\nu\beta\beta$ isotope mass in fiducial volume (includes enrichment factor)

† Region of Interest (ROI) can be single or multidimensional (E, spatial, ...)