

The physics of the FLUKA code: hadronic models

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FLUKA

Interaction and Transport Monte Carlo code

Main Authors

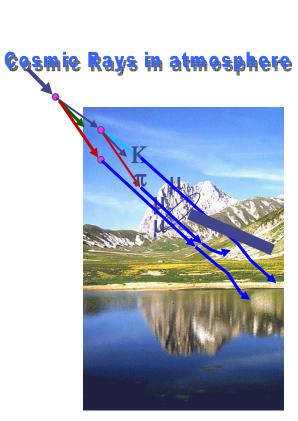
A. Fassò

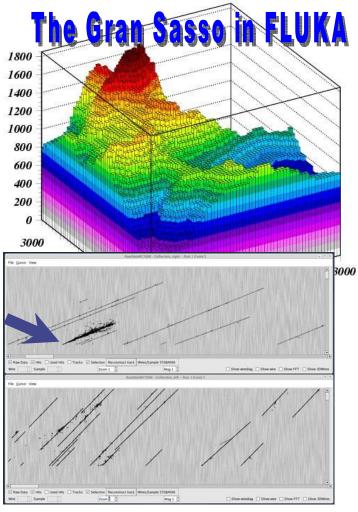
SLAC Stanford

A. Ferrari CERN

J. Ranft Siegen University

P.R. Sala INFN Milan





Fluka History:

The early days

The beginning:

1962: Johannes Ranft (Leipzig) and Hans Geibel (CERN): Monte Carlo for high-energy proton beams

The name:

1970: study of event-by-event fluctuations in a Nal calorimeter (FLUktuierende KAskade)

Early 70's to ≈1987: J. Ranft and coworkers (Leipzig University)
with contributions from Helsinki University of Technology (J. Routti, P. Aarnio)
and CERN (G.R. Stevenson, A. Fassò)
Link with EGS4 in 1986, later abandoned

The modern code: some dates

Since 1989: mostly INFN Milan (A. Ferrari, P.R. Sala): little or no remnants of older versions. Link with the past: J. Ranft and A. Fassò

1990: LAHET / MCNPX: high-energy hadronic FLUKA generator No further update

1993: G-FLUKA (the FLUKA hadronic package in GEANT3). No further update, used by G-Calor

1998: FLUGG, interface to GEANT4 geometry

2000: grant from NASA to develop heavy ion interactions and transport

2001: the INFN FLUKA Project

2003: official CERN-INFN collaboration to develop, maintain and distribute FLUKA

2005: release of the source code and definition of the FLUKA license

FLUKA collaboration

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Fluka applications:

FLUKA is a well established tool in HEP for:

- Particle physics: calorimetry, tracking and detector simulation $(\rightarrow ALICE, ICARUS, ...)$
- Accelerator design (→ LHC systems)
- Radioprotection (standard tool at CERN and SLAC)
- Dosimetry
- Cosmic ray physics

FLUKA is also used for:

- > Neutronics simulations
- > ADS (Accelerator DrivenSystems)

FLUKA applications to Medicine/radiobiology are growing, thanks to

- Mixed field capability, including ion transport and interactions
- ✓ Accuracy
- Reliability

Download, papers and documentation: www.fluka.org

FLUKA Description

FLUKA is a general purpose tool for calculations of particle transport and interactions with matter, covering an extended range of applications spanning from proton and electron accelerator shielding to target design, calorimetry, activation, dosimetry, detector design, Accelerator Driven Systems, cosmic rays, neutrino physics, radiotherapy etc.

- 60 different particles + Heavy Ions
 - Hadron-hadron and hadron-nucleus interactions 0-10000 TeV
 - Electromagnetic and μ interactions 1 keV 10000 TeV
 - Nucleus-nucleus interactions 0-10000 TeV/n
 - Charged particle transport ionization energy loss
 - Neutron multi-group transport and interactions 0-20 MeV
 - v interactions
 - Transport in magnetic field
 - Combinatorial (boolean) and Voxel geometry
 - Double capability to run either fully analogue and/or biased calculations
- Maintained and developed under INFN-CERN agreement and copyright 1989-2006
- More than 1000 users all over the world

http://www.fluka.org

The FLUKA hadronic Models

Elastic, exchange Phase shifts data, eikonal	se shifts Resonance proc		ial	gh Energy DPM dronization
Hadron-Nucleus PEANUT Sophisticated GINC Gradual onset of Glauber-Gribov multiple interactions Preequilibrium Coalescence		E< 0.1GeV/u BME Complete fusion+ peripheral	0.1< E< 5 GeV/u rQMD-2.4 modified new QMD	E> 5 GeV/u DPMJET DPM+ Glauber+ GINC
The state of the s	Evaporation/Fis	ssion/Fermi breal	k-up	

Inelastic hN interactions

Intermediate Energies

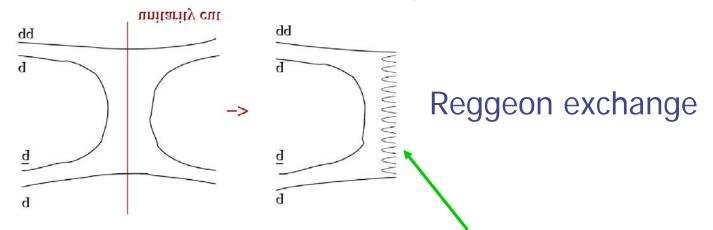
- $N_1 + N_2 \rightarrow N_1' + N_2' + \pi$ threshold around 290 MeV important above 700 MeV
- $\pi + N \rightarrow \pi' + \pi'' + N'$ opens at 170 MeV
- Dominance of the $\Delta(1232)$ resonance and of the N* resonances \rightarrow reactions treated in the framework of the isobar model \rightarrow all reactions proceed through an intermediate state containing at least one resonance
- Resonance energies, widths, cross sections, branching ratios from data and conservation laws, whenever possible

High Energies: Dual Parton Model/Quark Gluon String Model etc

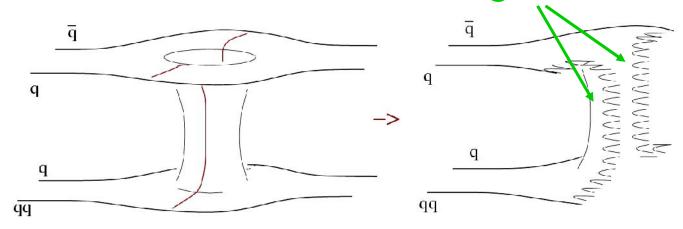
- Interacting strings (quarks held together by the gluon-gluon interaction into the form of a string)
- Interactions treated in the Reggeon-Pomeron framework
- each of the two hadrons splits into 2 colored partons \rightarrow combination into 2 colourless chains \rightarrow 2 back-to-back jets
- each jet is then hadronized into physical hadrons

Inelastic hN at high energies (DPM)

Parton and color concepts, Topological expansion of QCD, Duality

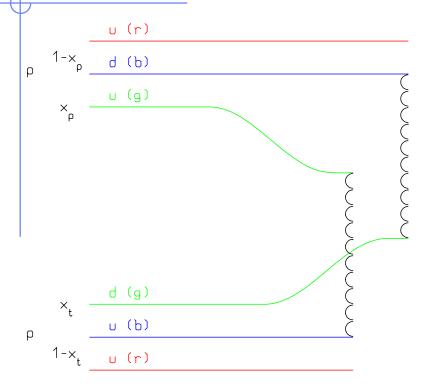


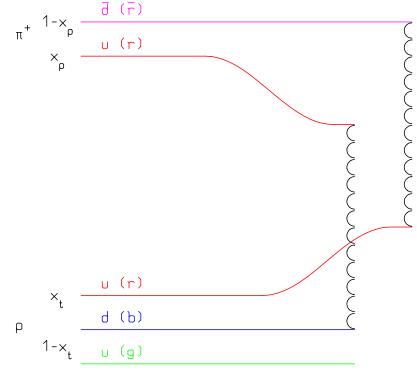
color strings to be "hadronized"



Pomeron exchange

Hadron-hadron collisions: chain examples



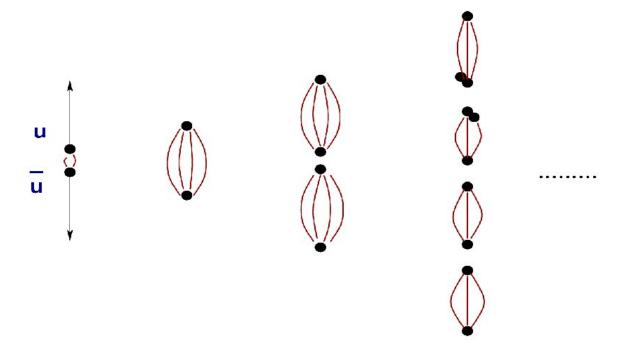


Leading two-chain diagram in DPM for p-p scattering. The color (red, blue, and green) and quark combination shown in the figure is just one of the allowed possibilities

Leading two-chain diagram in DPM for π^+ -p scattering. The color (red, blue, and green) and quark combination shown in the figure is just one of the allowed possibilities

The "hadronization" of color strings

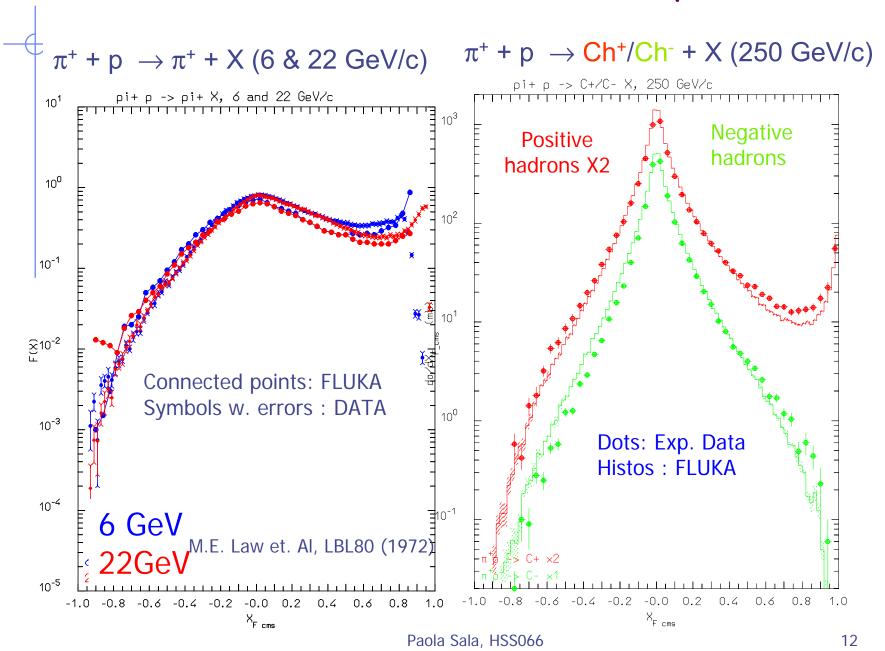
An example:



ud $d\overline{\mathbf{u}}$ uud udd us sd ud . . .

du

Inelastic hN interactions: examples



PEANUT

PreEquilibrium Approach to NUclear Thermalization

 PEANUT handles hadron-nucleus interactions from threshold (or 20 MeV neutrons) to 5 GeV up

Sophisticated Generalized IntraNuclear Cascade

Smooth transition (all non-nucleons emitted/absorbed/decayed + all secondaries below 30-50 MeV)

Prequilibrium stage

Standard Assumption on exciton number or excitation energy

Common FLUKA Evaporation model

Extension of PEANUT

- Peanut has proven to be a precise and reliable tool for intermediate energy hadron-nucleus reactions
- Its "nuclear environment" is also used in the modelization of (real and virtual) photonuclear reactions, neutrino interactions, nucleon decays, muon captures..

The goal was to extend it to cover all the energy range, and substitute the high energy h-A generator with the following advantages:

- Sophisticated (G)INC ⇒ better nuclear physics, particularly for residual production
- Smooth transition from intermediate to high energies
- Preequilibrium stage
- Explicit formation zone
- Possibility to account explicitly for QuasiElastic

Only two ingredients were missing:

- 1. The treatment of Glauber multiple scattering
- 2. A continuous and self consistent approach to the Quasi-Elastic reaction component

(Generalized) IntraNuclear Cascade

- Primary and secondary particles moving in the nuclear medium
- Target nucleons motion and nuclear well according to the Fermi gas model
- Interaction probability σ_{free} + Fermi motion × $\rho(r)$ + exceptions (ex. π)
- Glauber cascade at higher energies
- Classical trajectories (+) nuclear mean potential (resonant for π)
- Curvature from nuclear potential \rightarrow refraction and reflection
- Interactions are incoherent and uncorrelated
- Interactions in projectile-target nucleon $CMS \rightarrow Lorentz$ boosts
- Multibody absorption for π , μ^{-} , K^{-}
- Quantum effects (Pauli, formation zone, correlations...)
- Exact conservation of energy, momenta and all addititive quantum numbers, including nuclear recoil

hA at high energies: Glauber-Gribov cascade

Glauber cascade

- Quantum mechanical method to compute Elastic, Quasi-elastic and Absorption hA cross sections from Free hadron-nucleon scattering + nuclear ground state
- Multiple Collision expansion of the scattering amplitude
- Glauber-Gribov
 - Field theory formulation of Glauber model
 - Multiple collisions ↔ Feynman diagrams
 - High energies: exchange of one or more Pomerons with one or more target nucleons (a closed string exchange)

Glauber Cascade

Quantum mechanical method to compute all relevant hadron-nucleus cross sections from hadron-nucleon scattering: $S_{hN}(\overline{b},s) = e^{i\chi_{hN}(b,s)} = \eta_{hN}(b,s)e^{2i\delta_{hN}(b,s)}$

and nuclear ground state wave function Ψ_i

Total
$$\sigma_{hAT}(s) = 2\int d^2\vec{b} \int d^3\vec{u} \left| \Psi_i(\vec{u})^2 \right| 1 - \prod_{j=1}^A \operatorname{Re} S_{hN}(\vec{b} - \vec{r}_{j\perp}, s)$$
Elastic
$$\sigma_{hAel}(s) = \int d^2\vec{b} \left| \int d^3\vec{u} \left| \Psi_i(\vec{u})^2 \right| 1 - \prod_{j=1}^A S_{hN}(\vec{b} - \vec{r}_{j\perp}, s) \right|^2$$

Scattering
$$\sigma_{hA \Sigma f}(s) \equiv \sum_{f} \sigma_{hA fi}(s) = \int d^{2}\vec{b} \int d^{3}\vec{u} |\Psi_{i}(\vec{u})|^{2} \left[1 - \prod_{j=1}^{A} S_{hN}(\vec{b} - \vec{r}_{j\perp}, s) \right]^{2}$$

Absorption (particle prod.)

Absorption probability over a given b and nucleon configuration

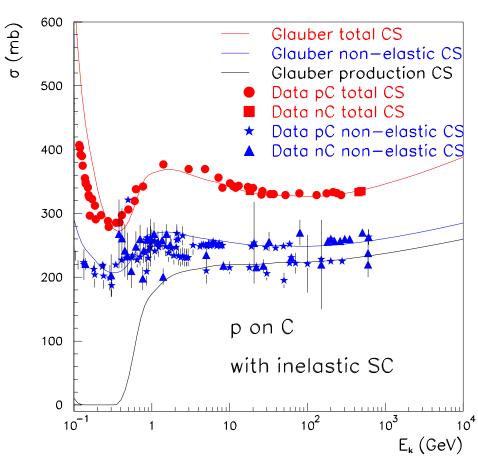
$$\sigma_{hA abs}(s) \equiv \sigma_{hA T}(s) - \sigma_{hA \Sigma f}(s)$$

$$= \int d^{2} \vec{b} \int d^{3} \vec{u} |\Psi_{i}(\vec{u})|^{2} \left\{ 1 - \left\{ \prod_{j=1}^{A} 1 - \left[1 - \left| S_{hN}(\vec{b} - \vec{r}_{j\perp}, s) \right|^{2} \right] \right\} \right\}$$

Glauber cross section calculations

Self-consistent calculation including "a priori" inelastic screening through the substitution where λ is the ratio of the single diffractive amplitude, 1 side only, over the elastic amplitude

$$\Gamma(s,\vec{b}) \rightarrow \widehat{\Gamma}_{hN}(s,\vec{b}) = \begin{bmatrix} 1 & \lambda \\ \lambda & 1 \end{bmatrix} \Gamma_{hN}(s,\vec{b})$$



Proton Carbon cross sections with inelastic screening accounted for

Please note the ambiguity of the non-elastic exp. results, almost 2-population like

Gribov interpretation of Glauber multiple collisions

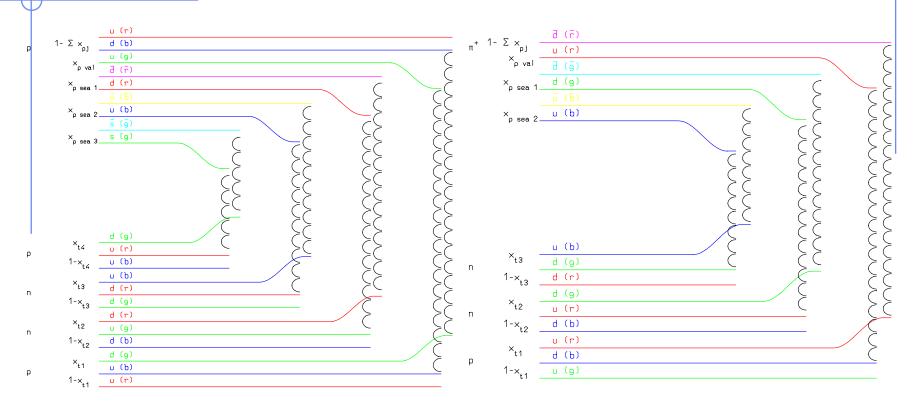
Therefore the absorption cross section is just the integral in the impact parameter plane of the probability of getting at least one non-elastic hadron-nucleon collision

and the overall average number of collision is given by

$$\langle \nu \rangle = \frac{Z\sigma_{hpr} + N\sigma_{hnr}}{\sigma_{hAabs}}$$

- Glauber-Gribov model = Field theory formulation of Glauber model
- Multiple collision terms ⇒ Feynman graphs
- At high energies: exchange of one or more pomerons with one or more target nucleons
- In the Dual Parton Model language: (neglecting higher order diagrams): Interaction with n target nucleons $\Rightarrow 2n$ chains
 - Two chains from projectile valence quarks + valence quarks of one target nucleon ⇒valence-valence chains
 - 2(n-1) chains from sea quarks of the projectile + valence quarks of target nucleons \Rightarrow 2(n-1) sea-valence chains

Glauber-Gribov: chain examples



Leading two-chain diagrams in DPM for p-A Glauber scattering with 4 collisions. The color (red blue green) and quark combinations shown in the figure are just one of the allowed possibilities

Leading two-chain diagrams in DPM for $\pi^{+-}A$ Glauber scattering with 3 collisions.

Formation zone

Naively: "materialization" time (originally proposed by Stodolski).

Qualitative estimate:

In the frame where
$$p//=0$$

$$\bar{t} = \Delta t \approx \frac{\hbar}{E_T} = \frac{\hbar}{\sqrt{p_T^2 + M^2}}$$

Particle proper time

$$\tau = \frac{M}{E_T}\bar{t} = \frac{\hbar M}{p_T^2 + M^2}$$

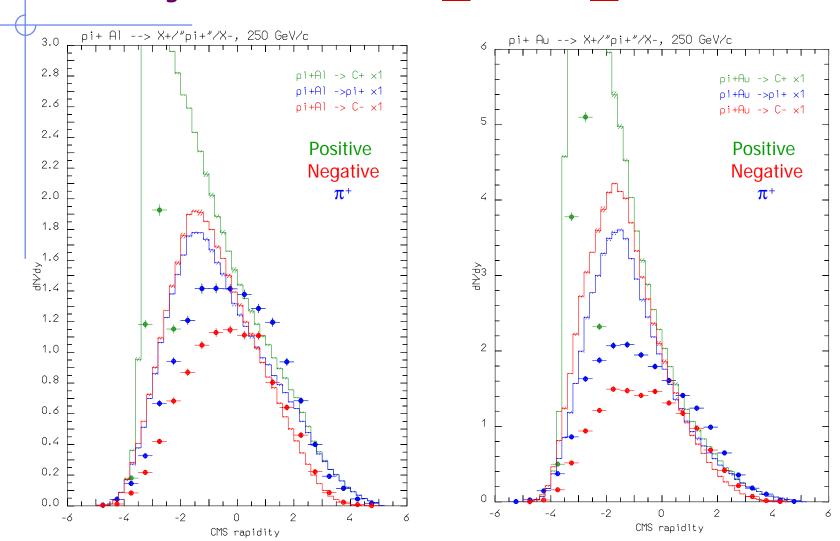
Going to the nucleus system

$$\Delta x_{for} \equiv \beta \ c \cdot t_{lab} \approx \frac{p_{lab}}{E_T} \bar{t} \approx \frac{p_{lab}}{M} \tau = k_{for} \frac{\hbar p_{lab}}{p_T^2 + M^2}$$

Condition for possible reinteraction inside a nucleus:

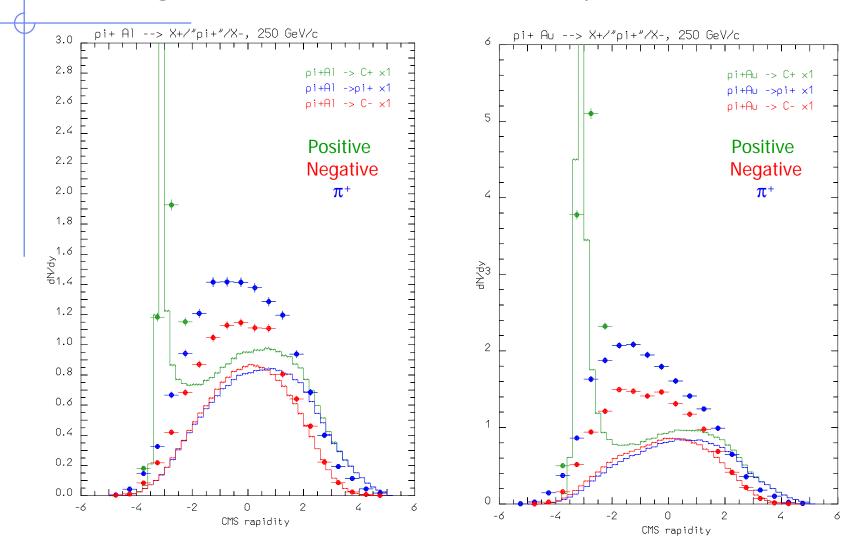
$$\Delta x_{for} \le R_A \approx r_0 A^{\frac{1}{3}}$$

Setting the formation zone: no Glauber, no formation zone



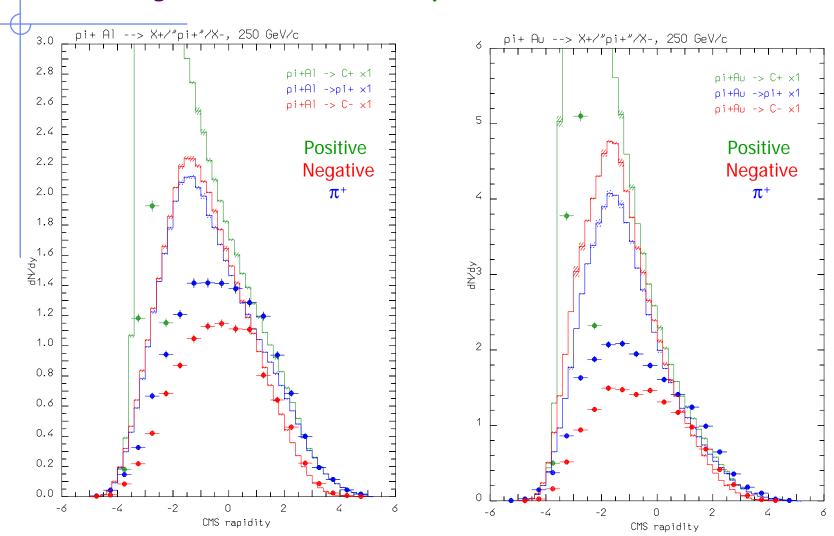
Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on Aluminum (left) and Gold (right) Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

Setting the formation zone: no Glauber, yes formation zone



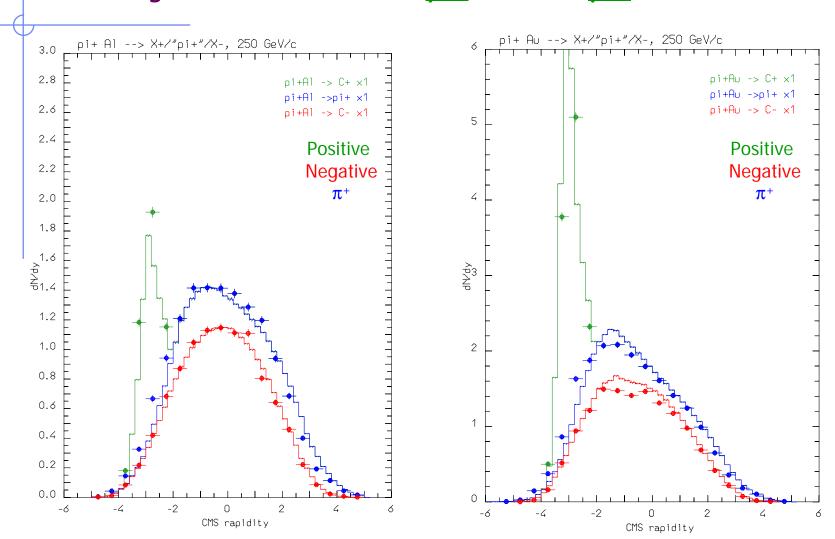
Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on Aluminum (left) and Gold (right) Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

Setting the formation zone: yes Glauber, no formation zone



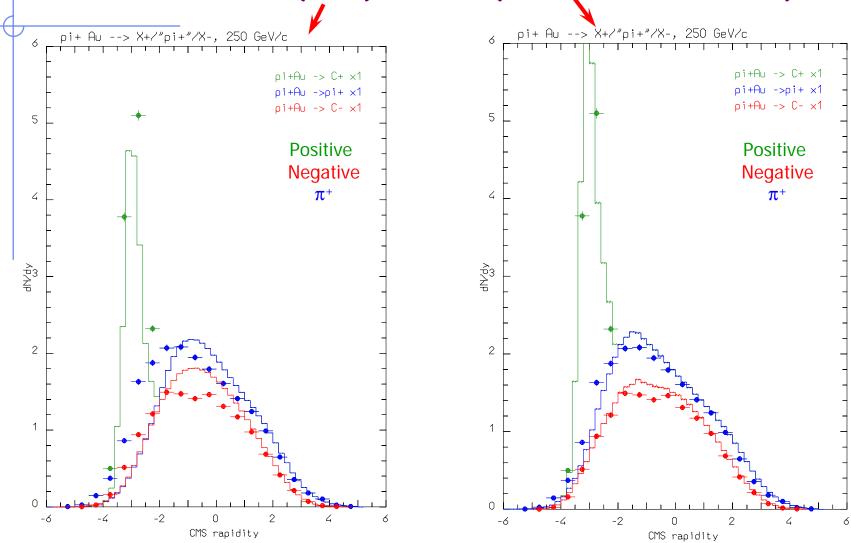
Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on Aluminum (left) and Gold (right) Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

Setting the formation zone: yes Glauber, yes formation zone



Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on Aluminum (left) and Gold (right) Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

Old HE model (left) vs new (PEANUT extended)



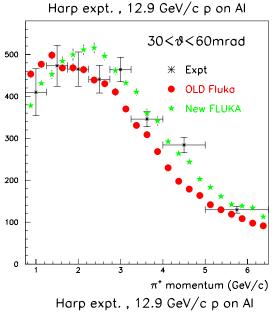
Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on Gold Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

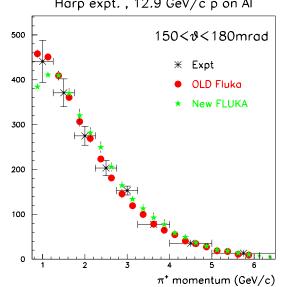
Comparison with the HARP experiment

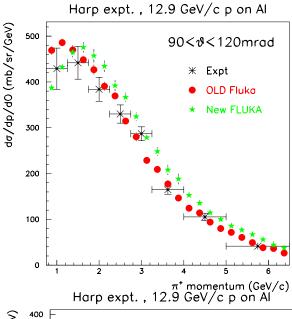
Data from the HARP experiment at CERN

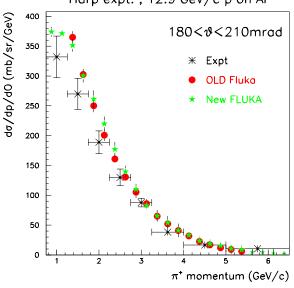
particle production with p beams in the 1.5-15 GeV/c range on several targets

First published results: 12.9 GeV/c protons on Aluminum, π^+ production cross section as a function of emission energy and angle









presented at COSPAr2006, Beijing july 006

Preequilibrium emission

For E > π production threshold \rightarrow only (G)INC models At lower energies a variety of preequilibrium models

Two leading approaches

The quantum-mechanical multistep model:

Very good theoretical background Complex, difficulties for multiple emissions The semiclassical exciton model Statistical assumptions Simple and fast Suitable for MC

Statistical assumption:

any partition of the excitation energy E^* among N, $N = N_h + N_p$, excitons has the same probability to occur

Step: nucleon-nucleon collision with $N_{n+1}=N_n+2$ ("never come back approximation)

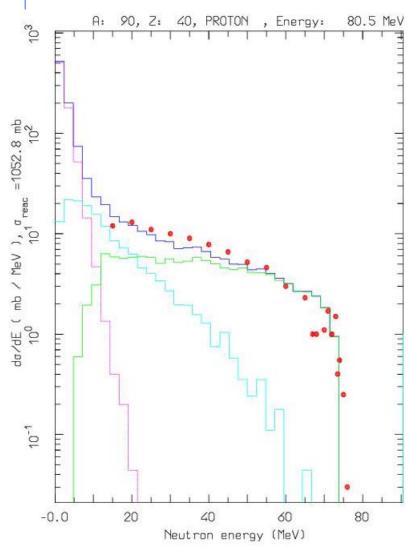
Chain end = equilibrium = N_n sufficiently high or excitation energy below threshold

N₁ depends on the reaction type and cascade history

Preequilibrium in FLUKA

- FLUKA preequilibrium is based on GDH (M. Blann et al.) cast in a MonteCarlo form
- GDH: Exciton model, r, E_f are "local" averages on the trajectory and constrained state densities are used for the lowest lying configurations.
- Modification of GDH in FLUKA:
 - \bullet cross section σ_{inv} from systematics
 - Correlation /coherence length/ hardcore effect on reinteractions
 - Constrained exciton state densities configurations 1p-ih, 2p-ih, 1p-2h, 2p-2h, 3p-1h and 3p-2h
 - True local r, E_f for the initial configuration, evolving into average
 - Non-isotropic angular distribution (fast particle approximation)

Thin target example

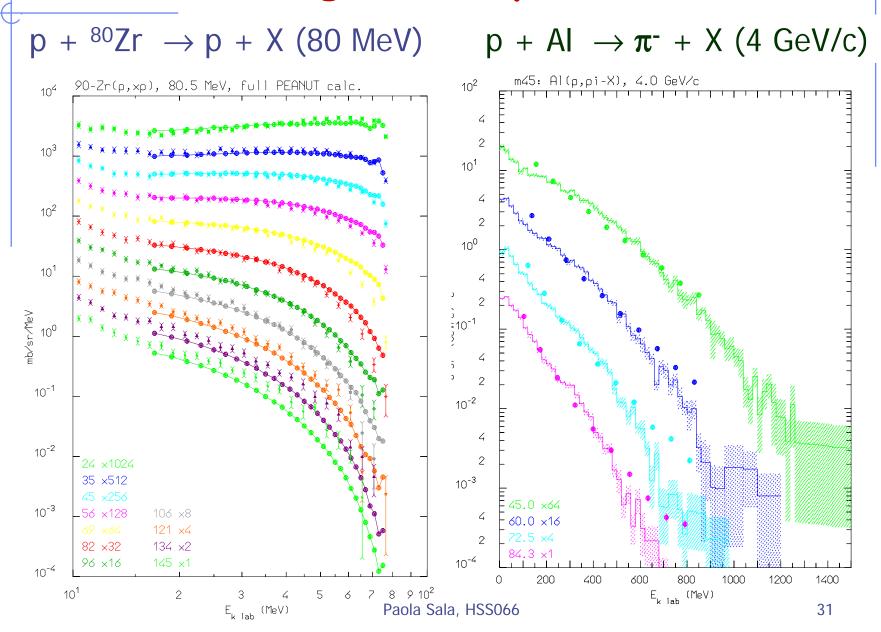


Angle-integrated 90 Zr(p,xn) at 80.5 MeV

The various lines show the total, INC, preequilibrium and evaporation contributions

Experimental data from M. Trabandt et al., Phys. Rev. C39, 452 (1989)

Thin target examples



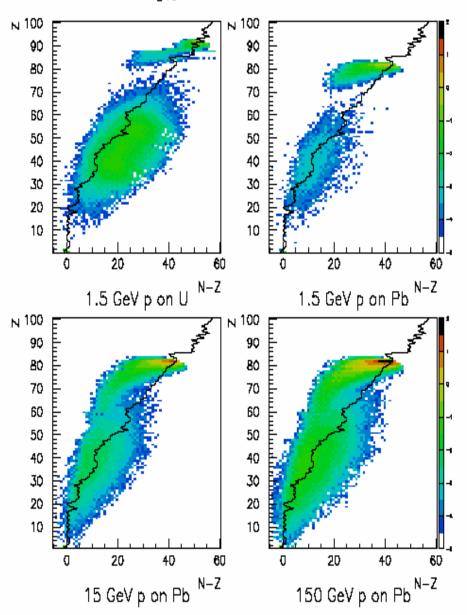
Equilibrium particle emission

- Evaporation: Weisskopf-Ewing approach
 - 600 possible emitted particles/states (A<25) with an extended evaporation/fragmentation formalism
 - Full level density formula
 - Inverse cross section with proper sub-barrier
 - Analytic solution for the emission widths
 - Emission energies from the width expression with no. approx.
 - New energy dependent self-consistent evaporation level densities (RIPL-2/IAEA recommendations)
 - Mew pairing energies consistent with the above point
 - mExtension of mass tables till A=330 using available offline calculations
 - Mew shell corrections coherent with the new masses
- Fission:
 - **Actinide fission done on first principles
 - New fission barrier calculations (following Myers & Swiatecki)
 - Fission level density enhancement at saddle point washing out with excitation energy (following IAEA recommendations)
 - Fission product widths and asymmetric versus symmetric probabilities better parameterized
- Fermi Break-up for A<18 nuclei
 - ~ 50000 combinations included with up to 6 ejectiles
- γ de-excitation: statistical + rotational + tabulated levels

Residual Nuclei

- The production of residuals is the result of the last step of the nuclear reaction, thus it is influenced by all the previous stages
- Residual mass distributions are very well reproduced
- Residuals near to the compound mass are usually well reproduced
- However, the production of specific isotopes may be influenced by additional problems which have little or no impact on the emitted particle spectra (Sensitive to details of evaporation, Nuclear structure effects, Lack of spin-parity dependent calculations in most MC models)

Log₁₀ N of residual nuclei

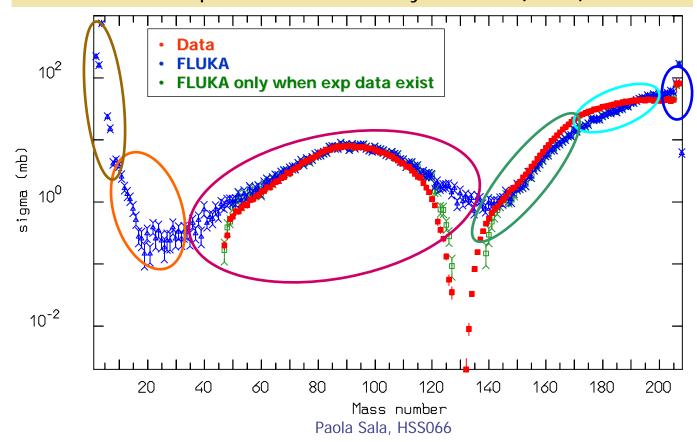


Example of fission/evaporation

- Quasi-elastic products
- Spallation products
- Deep spallation products

- Fission products
- Fragmentation products
- Evaporation products

1 A GeV ²⁰⁸Pb + p reactions Nucl. Phys. A 686 (2001) 481-524



Low-energy neutron transport in FLUKA performed by a multigroup algorithm:





- Widely used in low-energy neutron transport codes (not only Monte Carlo, but also Discrete Ordinate codes)
- Energy range of interest is divided in a given number of discrete intervals "energy groups"
- Elastic and inelastic reactions simulated not as exclusive process, but by group-to-group transfer probabilities (downscattering matrix)
- The scattering transfer probability between different groups represented by a Legendre polynomial expansion truncated at the (N+1)th term:

$$\sigma_s(g \to g', \mu) = \sum_{i=0}^N \frac{2i+1}{4\pi} P_i(\mu) \sigma_s^i(g \to g')$$

 μ = scattering angle

N = chosen Legendre order of anisotropy

FLUKA Implementation

- Both fully biased and semi-analog approaches available
- Energy range up to 19.6 MeV divided in 72 energy groups of approximately equal logarithmic width, and one thermal
- Prepared using a specialized code (NJOY) and ad-hoc programs
- Continuously enriched and updated on the basis of the most recent evaluations (ENDF/B, JEF, JENDL, etc.)
- The library contains 140 different materials/temperatures
- Cross sections of some materials are available at 2 or 3 different temperatures (0, 87 and 293° K) + Doppler broadening
- Hydrogen cross sections available for different types of molecular binding (free, H₂O, CH₂)
- Neutron energy deposition calculated by means of kerma factors
- However, H recoil protons, protons from $^{14}N(n,p)$ and $(\alpha,\,^3H)$ from neutron capture in 6Li and ^{10}B can be produced and transported explicitly
- Pointwise cross sections available for reactions in H, ⁶Li , Ar

The new library

A new library is in preparation, based on 260 n and 40 γ groups including 30 thermal groups at different temperatures and different self-shielding

Paola Sala, HSS066

Other features

Gamma Generation

- In general, gamma generation by low energy neutrons (but not gamma transport) is treated also in the frame of a multigroup scheme
- A downscattering matrix provides the probability, for a neutron in a given energy group, to generate a photon in each of 22 gamma energy groups, covering the range from 10 keV to 20 MeV.
- The actual energy of the photon is sampled randomly in the energy interval corresponding to its gamma group. With the exception of a few important gamma lines, such as the 2.2 MeV transition of Deuterium and the 478 keV photon from $^{10}\text{B}(n,\gamma)$ reaction, all ^{40}Ar lines, and the capture lines for Cd and Xe
- The gamma generation matrix apart from capture gammas, includes also gammas produced by other inelastic reactions such as (n,n')

Residual Nuclei

- For many materials (not for all), group-dependent information on the residual nuclei produced by low-energy neutron interactions is available in the FLUKA library
- This information can be used to score residual nuclei, but the user must check its availability before requesting scoring

Heavy ion interaction models

- DPMJET-III for energies ≥ 5 GeV/n
 - DPMJET (R. Engel, J. Ranft and S. Roesler) Nucleus-Nucleus interaction model
 - Energy range: from 5-10 GeV/n up to the highest Cosmic Ray energies (1018-1020 eV)
 - Used in many Cosmic Ray shower codes
 - Based on the Dual Parton Model and the Glauber model, like the high-energy FLUKA hadron-nucleus event generator
- Modified and improved version of rQMD-2.4 for 0.1 < E < 5 GeV/n
 - rQMD-2.4 (H. Sorge et al.) Cascade-Relativistic QMD model
 - Energy range: from 0.1 GeV/n up to several hundred GeV/n
 - Successfully applied to relativistic A-A particle production
- BME (Boltzmann Master Equation) for E < 0.1 GeV/n
 - FLUKA implementation of BME from E.Gadioli et al (Milan)
 - Now under test for light ions
- Developemnt of new QMD codes
 - Non relativistic in Milan: 0.1-≈0.7 GeV/n Poster TC3-0194
 - Relativistic in Houston:
 Poster TC3-0195
- Standard FLUKA evaporation/fission/fragmentation used in both Target/Projectile final de-excitation
- Electromagnetic dissociation

Real and Virtual Photonuclear Interactions

Photonuclear reactions

- Giant Dipole Resonance interaction (special database)
- Quasi-Deuteron effect
- Delta Resonance energy region
- Vector Meson Dominance in the high energy region
- (G)INC, preequilibrium and evaporation like for hadron-nucleus

Virtual photon reactions

- Muon photonuclear interactions
- Electromagnetic dissociation

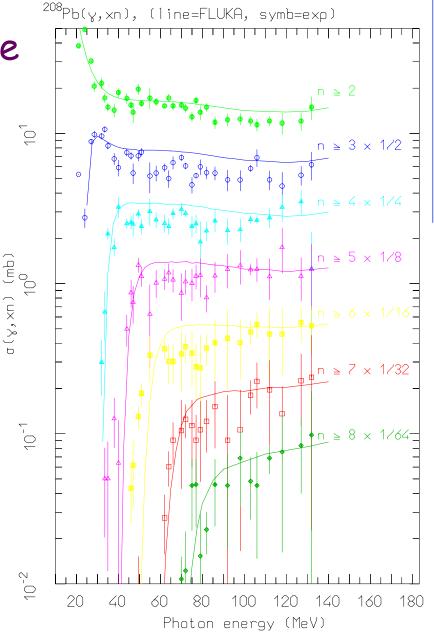
Photonuclear int.: example

Reaction: 208 Pb(γ , \times n) $20 \le E\gamma \le 140$ MeV

Cross section for multiple neutron emission as a function of photon energy, Different colors refer to neutron multiplicity $\geq n$, with $2 \leq n \leq 8$

Symbols: exp data (NPA367, 237 (1981); NPA390, 221 (1982))

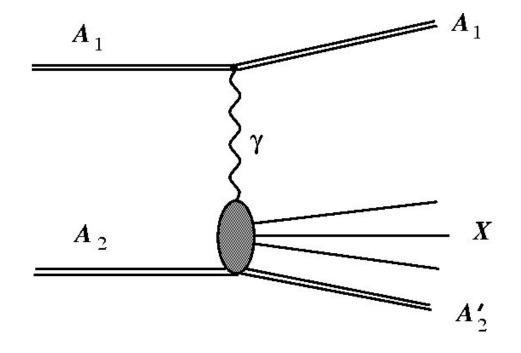
Lines: FLUKA



Electromagnetic dissociation

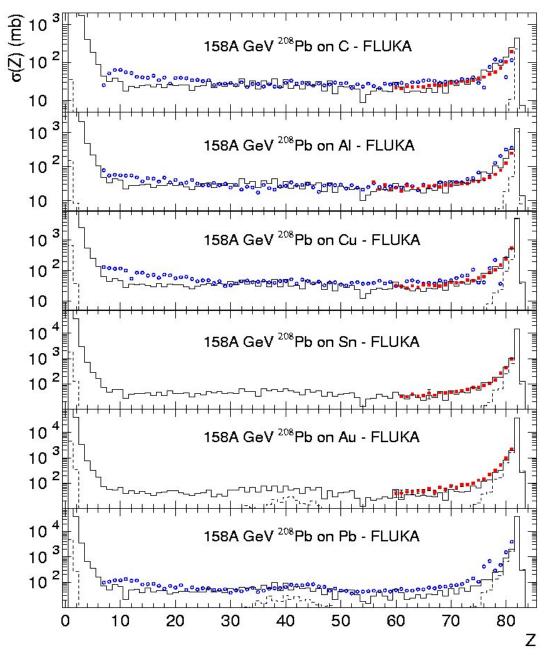
Electromagnetic dissociation: σ_{EM} increasingly large with (target) Z's and energy. Already relevant for few GeV/n ions on heavy targets (σ_{EM} ~ 1 b vs σ_{nucl} ~ 5 b for 1 GeV/n Fe on Pb)

$$\sigma_{1\gamma} = \int \frac{d\omega}{\omega} n_{A_1}(\omega) \sigma_{\gamma} n_{A_2}(\omega) \propto Z_1^2$$



158 GeV/n fragmentation

Fragment charge cross section for 158 AGeV Pb ions on various targets. Data (symbols) from NPA662, 207 (2000), NPA707, 513 (2002) (blue circles) and from C.Scheidenberger et al. PRC, in press (red squares), histos are FLUKA (with DPMJET-III) predictions: the dashed histo is the electromagnetic dissociation contribution



EMF ElectroMagneticFluka

- *Photoelectric: fluorescence, angular distribution, Auger, polarization
- Compton and Rayleigh: atomic bonds, polarization
- •Pair production correlated angular and energy distribution; also for μ
- •Photonuclear interactions; also for μ
- •Bremsstrahlung : LPM, angular distribution, ... also for μ
- ·Bhabha and Möller scattering
- Positron annihilation at rest and in flight
- ·µ capture at rest
- Optical photon (Cherenkov) production
 and transport
 Paola Sala, HSS066

PHOTONS

- cross sections from EPDL97
- new coherent scattering
- updated photoelectric
- updated pair production
- Compton profile