## **Comparative Quantum Gravity – a brief survey**

Windows into Quantum Gravity, Madrid, 28 - 31 October 2015

Hermann Nicolai MPI für Gravitationsphysik, Potsdam (Albert Einstein Institut)

See also: arXiv:1301.5481

## Why Quantum Gravity?

#### • Singularities in General Relativity (GR)

- Black holes: gravitational collapse generically unavoidable
- Singularity theorems: space and time 'end' at the singularity
- Cosmological ("big bang") singularity: what 'happened' at t = 0?
- Structure of space-time at the smallest distances?

### Why Quantum Gravity?

#### • Singularities in General Relativity (GR)

- Black holes: gravitational collapse generically unavoidable
- Cosmological ("big bang") singularity: what 'happened' at t = 0?
- Singularity theorems: space and time 'end' at the singularity
- Structure of space-time at the smallest distances?

#### • Singularities in Quantum Field Theory (QFT)

- Perturbation theory: UV divergences in Feynman diagrams
- Can be removed by infinite renormalizations order by order
- Standard Model (or its extensions) unlikely to exist as rigorous QFT(s)
- Therefore must look for an UV completion of the theory!

## Why Quantum Gravity?

#### • Singularities in General Relativity (GR)

- Black holes: gravitational collapse generically unavoidable
- Singularity theorems: space and time 'end' at the singularity
- Cosmological ("big bang") singularity: what 'happened' at t = 0?
- Structure of space-time at the smallest distances?

#### • Singularities in Quantum Field Theory (QFT)

- Perturbation theory: UV divergences in Feynman diagrams
- Can be removed by infinite renormalizations order by order
- Standard Model (or its extensions) unlikely to exist as rigorous QFT(s)
- Therefore must look for an UV completion of the theory!

#### • Difficulties probably have common origin:

- Space-time as a continuum (differentiable manifold)
- Elementary Particles as exactly *pointlike* excitations
- Expect something to happen at  $\ell_{Planck} \sim 10^{-33} cm$  !

## **Different Attitudes**

#### • Hypothesis 1:

Quantum Gravity essentially *is* the (non-perturbative) quantization of Einstein Gravity (in metric/connection/loop or discrete formalism). Thus GR, suitably treated and eventually complemented by the Standard Model of Particle Physics or its possible extensions, correctly describes the physical degrees of freedom also at the very smallest distances.

#### • Hypothesis 2:

GR is an effective (low energy) theory arising at large distances from a more fundamental Planck scale theory whose basic degrees of freedom are very different from either GR or QFT, and as yet unknown. GR, and with it, space-time itself as well as general covariance, are thus assumed to be 'emergent', much like macroscopic physics 'emerges' from the quantum world of atoms and molecules.

## A Basic Fact

Perturbative quantum gravity is non-renormalizable

$$\Gamma_{div}^{(2)} = \frac{1}{\varepsilon} \frac{209}{2880} \frac{1}{(16\pi^2)^2} \int dV C_{\mu\nu\rho\sigma} C^{\rho\sigma\lambda\tau} C_{\lambda\tau}{}^{\mu\nu}$$

[Goroff& Sagnotti(1985); van de Ven(1992)]

Two possible conclusions:

- Consistent quantization of gravity requires a radical modification of Einstein's theory at short distances, in particular inclusion of supersymmetric matter; or
- UV divergences are artefacts of perturbative treatment ⇒ disappear upon a proper *non-perturbative* quantization of Einstein's theory.

## A Basic Fact

Perturbative quantum gravity is non-renormalizable

$$\Gamma_{div}^{(2)} = \frac{1}{\varepsilon} \frac{209}{2880} \frac{1}{(16\pi^2)^2} \int dV C_{\mu\nu\rho\sigma} C^{\rho\sigma\lambda\tau} C_{\lambda\tau}{}^{\mu\nu}$$

[Goroff& Sagnotti(1985); van de Ven(1992)]

Two possible conclusions:

- Consistent quantization of gravity requires a radical modification of Einstein's theory at short distances, in particular inclusion of supersymmetric matter; or
- UV divergences are articlated of perturbative treatment  $\Rightarrow$  disappear upon a proper *non-perturbative* quantization of Einstein's theory.

No approach to quantum gravity can claim complete success that does not explain *in detail* the ultimate fate of this divergence and other divergences!

### Gravity and Matter [ $\rightarrow$ Hermann Weyl (1918)]

Einstein's equations according to Einstein:

$$\underbrace{R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R}_{\mathbf{Marble}} = \underbrace{\kappa T_{\mu\nu}}_{\mathbf{Timber}?}$$

**Question:** can we understand the r.h.s. geometrically?

- Kaluza-Klein theories?
- Supersymmetry and Supergravity?

Gravity vs. quantum mechanics: do we need to change the rules of quantum mechanics?

- Black hole evaporation and information loss?
- Emergent space and time vs. quantum non-locality?

### **Scales and Hierarchies**

Gravitational force is much weaker than matter interactions  $\Rightarrow$  the 'Hierarchy Problem'.

This fact is reflected in the relevant mass scales

• Known elementary particles cover a large mass range:

- Light neutrinos  $\sim 0.01 \,\mathrm{eV}$ , electron  $\sim 0.5 \,\mathrm{MeV}$ 

- Light quarks  $\sim 1 \,\mathrm{MeV}$ , top quark  $\sim 173 \,\mathrm{GeV}$ 

- Electroweak scale  $\sim m_Z \sim 90 \,\mathrm{GeV}$ 

• ... but still tiny vis-à-vis Planck Scale  $M_{Pl} \sim 10^{19} \,\mathrm{GeV}$  !

A key challenge for any proposed theory of Quantum Gravity: offer *quantifiable* criteria to confirm or falsify the theory. These must in particular allow to discriminate the given proposal against alternative ones!

## **Approaches to Quantum Gravity**

- Supergravity, Superstrings and M Theory
- AdS/CFT and Holography
- Path integrals: Euclidean, Lorentzian, matrix models,...
- Canonical Quantization (metric formalism)
- Loop Quantum Gravity
- Discrete Quantum Gravity: Regge calculus, (C)DT
- Discrete Quantum Gravity: spin foams, group field theory,...
- Non-commutative geometry and non-commutative space-time
- Asymptotic Safety and RG Fixed Points
- Causal Sets, emergent (Quantum) Gravity
- Cellular Automata ('computing quantum space-time')

# Asymptotic Safety: is standard QFT enough?

[Weinberg(1979), Reuter (1995), Percacci(2006), Niedermaier(2007), Reuter&Saueressig(2012)]

Approach is closest in spirit to conventional QFT ideas (RG flow, RG group, etc.), but does not require anything special to happen to continuum space-time below  $\ell_{Pl}$ ! More specifically:

- Is the UV limit of gravity determined by a non-Gaussian fixed point (NGFP) of the gravitational renormalisation group (RG) flow which controls the behaviour of theory at high energies and renders it safe from unphysical divergences?
- Aim: construct scale dependent effective action  $\Gamma_k$

 $\lim_{k\to\infty} \Gamma_k = \text{bare action} , \quad \lim_{k\to0} \Gamma_k = \text{effective low energy action}$   $\Rightarrow \text{ approach is essentially agnostic about microscopic theory,}$ all the information is in *universality classes* of RG flows.

•  $M_{Planck}$  analogous to  $\Lambda_{QCD}$ : *lower end* of asymptotic scaling regime  $\Rightarrow$  observable effects only if some prediction can be made about IR limit as theory flows down from NGFP.

## **Canonical Quantum Gravity**

Non-perturbative and background independent approach: quantum metric fluctuations and quantum geometry.

- Hamiltonian approach: manifest space-time covariance is lost through split ('foliation') of space-time as  $\mathcal{M} = \Sigma \times \mathbb{R}$ .
- $\rightarrow$  Space-time geometry is viewed as the *evolution of spatial* geometry in time according to Einstein's equations.
- Geometrodynamics: canonical dynamical degrees of freedom  $g_{mn}(t, \mathbf{x}) \quad \text{and} \quad \Pi^{mn}(t, \mathbf{x}) = \frac{\delta S_{\text{Einstein}}}{\delta \dot{a}_{mn}(t, \mathbf{x})}$
- Dynamics defined by *constraints* (via shift and lapse): Hamiltonian constraint  $\mathcal{H}(\mathbf{x})$  and diffeomorphism constraints  $\mathcal{D}_m(\mathbf{x})$
- Quantum Constraint Algebra from classical Poisson algebra:

$$\{\mathcal{D},\mathcal{D}\}\sim\mathcal{D}\qquad \{\mathcal{D},\mathcal{H}\}\sim\mathcal{H}\qquad \{\mathcal{H},\mathcal{H}\}\sim\mathcal{D}\ ,$$

possibly modulo anomalies (cf. Witt vs. Virasoro algebra).

 $\Rightarrow$  Quantum space-time covariance must be proven!

### New Variables, New Perspectives?

• New canonical variables: replace  $g_{mn}$  by connection

$$A_m{}^a = -\frac{1}{2}\epsilon^{abc}\omega_{m\,bc} + \gamma K_m{}^a$$

 $[\omega_{m bc} =$ spatial spin connection,  $K_m{}^a =$ extrinsic curvature]

• New canonical brackets [Ashtekar (1986)]

$$\{A_m{}^a(\mathbf{x}), E_b{}^n(\mathbf{y})\} = \gamma \delta_b^a \delta_m^n \delta^{(3)}(\mathbf{x}, \mathbf{y}) , \{A_m{}^a(\mathbf{x}), A_n{}^b(\mathbf{y})\} = \{E_a{}^m(\mathbf{x}), E_b{}^n(\mathbf{y})\} = 0$$

with conjugate variable  $E_a{}^m$  = inverse densitized dreibein  $\Rightarrow$  for  $\gamma = \pm i$  constraints become polynomial

 $E_a{}^n F_{mn}{}^a(A) \approx 0$ ,  $\epsilon^{abc} E_a{}^m E_b{}^n F_{mnc}(A) \approx 0$ ,  $D_m(A) E_a{}^m \approx 0$ 

with SU(2) field strength  $F_{mna} \equiv \partial_m A_{na} - \partial_n A_{ma} + \varepsilon_{abc} A_m{}^b A_n{}^c$ .

• But reality constraint difficult to elevate to quantum theory  $\rightarrow \gamma$  is nowadays taken real ('Barbero-Immirzi parameter')

## Loop Quantum Gravity (LQG)

• Modern canonical variables: holonomy (along edge e)

$$h_e[A] = \mathcal{P} \exp \int_e A$$

• Conjugate variable = flux through area element S

$$F_S^a[E] := \int_S dF^a = \int_S \epsilon_{mnp} E_a^{\ m} dx^n \wedge dx^p$$

- act on wave functionals  $\Psi_{\{\Gamma,C\}}[A] = f_C(h_{e_1}[A], \dots, h_{e_n}[A])$  with spin network  $\Gamma$  (graph consisting of edges e and vertices v).
- New feature: Kinematical Hilbert space H<sub>kin</sub> can be defined, but is non-separable ⇒ operators not weakly continuous.
   Cf. ordinary quantum mechanics: replace ⟨x|x'⟩ = δ(x x') by ⟨x|x'⟩ = 1 if x = x' and = 0 if x ≠ x' → 'pulverize' real line!
- $\Rightarrow$  No UV divergences (and thus no anomalies)?
- $\Rightarrow$  No negative norm states? [cf. Narnhofer&Thirring (1992)]

### Status of Hamiltonian constraint

- Diffeomorphism constraint solved formally:  $\mathcal{X}_{\Gamma} = \sum_{\phi \in \text{Diff}} \Psi_{\Gamma \circ \phi}$
- $\Rightarrow$  Hamiltonian constraint not defined on  $\mathcal{H}_{kin}$ , but on distribution space  $\mathcal{S}$  ('habitat') = dual of dense subspace  $\subset \mathcal{H}_{kin}$ .
- Main success: definition of regulated Hamiltonian (with  $\epsilon > 0$ ) by means of kinematical operators (volume, etc.) [Thiemann(2000)]

$$\hat{H}[N,\epsilon] = \sum_{\alpha} N(v_{\alpha}) \,\epsilon^{mnp} \mathrm{Tr}\left(\left(h_{\partial P_{mn}(\epsilon)} - h_{\partial P_{mn}(\epsilon)}^{-1}\right) h_{p}^{-1}\left[h_{p},V\right]\right)$$
$$+ \frac{1}{2}(1+\gamma^{2}) \sum_{\alpha} N(v_{\alpha}) \,\epsilon^{mnp} \mathrm{Tr}\left(h_{m}^{-1}\left[h_{m},\bar{K}\right] h_{n}^{-1}\left[h_{n},\bar{K}\right] h_{p}^{-1}\left[h_{p},V\right]\right)$$

- Proper definition relies on diffeomeorphism invariance of states  $\mathcal{X} \in \mathcal{S} \Rightarrow \text{ limit } \epsilon \rightarrow 0 \text{ exists (at best) as a weak limit:}$  $\langle H^*[N]\mathcal{X}|\Psi \rangle = \lim_{\epsilon \rightarrow 0} \langle \mathcal{X}|\hat{H}[N,\epsilon]\Psi \rangle , \quad \mathcal{X} \in \mathcal{S}$
- Ultralocal action of unregulated Hamiltonian adds 'spiderwebs' (of size  $\epsilon \to 0$ ) to spin network  $\Gamma$ , but cumbersome to evaluate (on S) even for the simplest examples.

# **Summary and Critique**

Non-perturbative approaches (LQG, spin foams,...) put main emphasis on general concepts underlying GR:

- (Spatial) Background Independence
- Diffeomorphism Invariance

However, these approaches so far do not incorporate essential insights and successes of standard QFT:

- Consistency restrictions from anomalies?
- Quantization ambiguities?
- Matter couplings: anything goes?

These issues will be hard to settle without a detailed understanding of how standard QFT and the semiclassical limit (Einstein equations, *etc.*) emerge.

## The Superworld

Basic strategy: render gravity perturbatively consistent (i.e. finite) by modifying GR at short distances.

- Supersymmetry: matter (fermions) vs. forces (bosons)
- (Partial) cancellation of UV infinities
- The *raison d'etre* for matter to exist?
- Maximally symmetric point field theories
  - -D = 4, N = 8 Supergravity
  - -D = 11 Supergravity
- Supersymmetric extended objects
  - No point-like interactions  $\Rightarrow$  no UV singularities?
  - IIA/IIB und heterotic superstrings (D = 10)
  - Supermembranes and M(atrix)-Theory (D = 11)

# String Theory

Very much modelled on concepts from particle physics (hence no problem with semi-classical limit):

- Not simply a theory of one-dimensional extended objects: D-branes, M-branes, ...
- Microscopic BH Entropy:  $S = \frac{1}{4}A$  (+ corrections)
- Holography: the key to quantum gravity?
- New ideas for physics beyond the Standard Model:
  - Low energy supersymmetry and the MSSM
  - Large extra dimensions and brane worlds (but D = 4??)
  - Multiverses and the string landscape
  - $\rightarrow$  a new El Dorado for experimentalists?

## String Theory: open questions

- Struggling to reproduce SM as is
- Struggling to incorporate  $\Lambda > 0$
- Perturbative finiteness: obvious, but unprovable?
- Role of maximally extended N = 8 supergravity?

Recent advances transcend perturbation theory, but

- No convincing scenario for resolution of space-time singularities in GR (e.g. via AdS/CFT ?)
- Or: what 'happens' to space and time at  $\ell_{PL}$ ?
- The real question: what *is* string theory?

## A Key Issue: Non-Uniqueness

Existing approaches suffer from a very large number of ambiguities, so far preventing any kind of prediction with which the theory will stand or fall:

- Superstrings: 10<sup>500</sup> 'consistent' vacua and the multiverse?
- LQG: 10<sup>500</sup> 'consistent' Hamiltonians/spin foam models?
- Discrete Gravity: 10<sup>500</sup> 'consistent' lattice models?
- Asymptotic Safety: 10<sup>500</sup> 'consistent' RG flows?

Question: does Nature pick the 'right' answer at random from a huge variety of possibilities, or are there criteria to narrow down the number of choices?

## A Key Issue: Non-Uniqueness

Existing approaches suffer from a very large number of ambiguities, so far preventing any kind of prediction with which the theory will stand or fall:

- Superstrings: 10<sup>500</sup> 'consistent' vacua and the megaverse?
- LQG: 10<sup>500</sup> 'consistent' Hamiltonians/spin foam models?
- Discrete Gravity: 10<sup>500</sup> 'consistent' lattice models?
- Asymptotic Safety: 10<sup>500</sup> 'consistent' RG flows?

Question: does Nature pick the 'right' answer at random from a huge variety of possibilities, or are there criteria to narrow down the number of choices?

In order to discriminate between a growing number of diverging ideas on quantum gravity better to start looking for *inconsistencies*...

... or else ansätze may remain 'fantasy' [G.W. Gibbons]!

# Forward to the Past: N = 8 Supergravity?

... most symmetric field theoretic extension of Einstein's theory of gravitation [Cremmer, Julia(1979); deWit, HN(1981)]

 $\rightarrow$  a promising candidate for the unification of all interactions with gravity? But:

- Existence of supersymmetric counter terms suggests non-renormalizable divergences from three loops onwards ⇒ no improvement over Einstein?
- Properties of theory (no chiral fermions, huge negative cosmological constant) in obvious contradiction to experiment and observation?

Last but not least: Superstring theory seemed to do much better in both regards...

## N = 8 Supergravity

```
[Cremmer, Julia(1979); B. deWit, HN (1981)]
```

Unique theory (modulo 'gauging'), most symmetric known field theoretic extension of Einstein's theory!

# $1 \times [2] \oplus 8 \times \left[\frac{3}{2}\right] \oplus 28 \times [1] \oplus 56 \times \left[\frac{1}{2}\right] \oplus 70 \times [0]$

- Diffeomorphisms and local Lorentz symmetry
- N = 8 local supersymmetry
- SU(8) R symmetry (local or rigid)
- Linearly or non-linearly realized duality symmetry  $E_{7(7)}$

70 scalar fields described by 56-bein  $\mathcal{V}(x) \in E_{7(7)}/SU(8)$ 28 vectors + 28 'dual' vectors transform in 56 of  $E_{7(7)}$ . NB: complete breaking of N = 8 supersymmetry  $\rightarrow$  $\#(\text{spin-}\frac{1}{2} \text{ fermions}) = 56 - 8 = 48 = 3 \times 16 !$ 

## N = 8 Supergravity: new perspectives

Very recent work has shown that N = 8 supergravity

• is much more finite than expected (behaves like N = 4 super-Yang-Mills up to four loops)

[Bern, Carrasco, Dixon, Johansson, Roiban, PRL103(2009)081301]

- ... and could thus be finite to all orders!
- However: efforts towards five loops seem to be stuck.

In string theory as well there appear difficulties starting *at five loops*: super-moduli space is no longer 'split' [Grushevsky,Witten,...] But even if N=8 Supergravity is finite:

- what about *non-perturbative* quantum gravity?
- is there any relation to *real physics*?

If no new spin- $\frac{1}{2}$  degrees of freedom are found at LHC, the following curious fact could also become relevant:

## A strange coincidence?

 $SO(8) \rightarrow SU(3) \times U(1)$  breaking and 'family color locking'

$(u,c,t)_L$ :	${f 3}_c imesar{f 3}_f o {f 8}\oplus{f 1}\;,$	$Q = \frac{2}{3} - q$
$(ar{u},ar{c},ar{t})_L$ :	$ar{f 3}_c imes {f 3}_f o {f 8}\oplus {f 1}\;,$	$Q = -\frac{2}{3} + q$
$(d,s,b)_L$ :	$3_c  imes 3_f  ightarrow 6 \oplus ar{3} \; ,$	$Q = -\frac{1}{3} + q$
$(ar{d},ar{s},ar{b})_L$ :	$ar{f 3}_c  imes ar{f 3}_f  o ar{f 6} \oplus f 3 \; ,$	$Q = \frac{1}{3} - q$
$(e^-,\mu^-, au^-)_L$ :	$1_c  imes 3_f  ightarrow 3 \; ,$	Q = -1 + q
$(e^+,\mu^+,\tau^+)_L$ :	${f 1}_c  imes ar{f 3}_f  o ar{f 3} \;,$	Q = 1 - q
$( u_e, u_\mu, u_ au)_L$ :	$1_c  imes ar{3}_f  ightarrow ar{3} \ ,$	Q = -q
$(ar u_e,ar u_\mu,ar u_ au)_L$ :	$1_c  imes 3_f  ightarrow 3 \; ,$	Q = q

N = 8 Supergravity and Standard Model assignments agree if spurion charge is chosen as  $q = \frac{1}{6}$  [Gell-Mann (1983)] Realized at SU(3) × U(1) stationary point! [Warner,HN: NPB259(1985)412] Mismatch of  $\pm \frac{1}{6}$  can be fixed by deforming U(1) [Meissner,HN:1412.1715]

## **Uniqueness from Symmetry?**

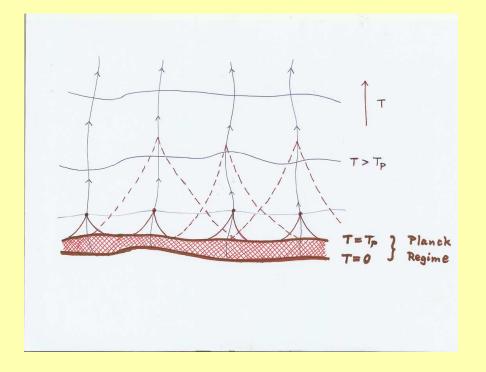
- N = 8 Supergravity possesses an unexpected ('hidden') duality symmetry:  $E_{7(7)}$  [Cremmer, Julia, 1979]
- An unexpected link with the *exceptional groups*  $G_2, F_4, E_6, E_7, E_8$ , the solitary members of the Lie group classification.
- 'Dimensional reduction'  $\equiv$  metamorphoses spacetime symmetries into internal symmetries:

 $\cdots \subset E_6 \subset E_7 \subset E_8 \subset E_9 \subset E_{10}$ 

with the  $\infty$ -dimensional 'prolongations'  $E_9$  and  $E_{10}$ 

- $E_{10}$  = maximally extended hyperbolic Kac–Moody Symmetry – a mathematical ENIGMA!
- $\Rightarrow$  'De-Emergence' of space (and time) ?!?

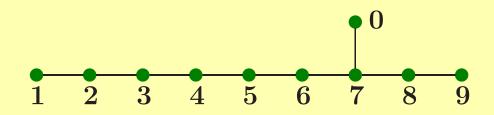
## Another hint: BKL and Spacelike Singularities



For  $T \rightarrow 0$  spatial points decouple and the system is effectively described by a continuous superposition of one-dimensional systems  $\rightarrow$  effective dimensional reduction to D = 1! [Belinski,Khalatnikov,Lifshitz (1972)]

A candidate symmetry:  $G = E_{10}$ ?

 $E_{10}$  is the 'group' associated with the Kac-Moody Lie algebra  $\mathfrak{g} \equiv \mathfrak{e}_{10}$  defined via the Dynkin diagram [e.g. Kac]



Defined by generators  $\{e_i, f_i, h_i\}$  and relations via Cartan matrix  $A_{ij}$  ('Chevalley-Serre presentation')

$$\begin{array}{ll} [h_i, h_j] &= 0, & [e_i, f_j] = \delta_{ij} h_i, \\ [h_i, e_j] &= A_{ij} e_j, & [h_i, f_j] = -A_{ij} f_j \\ (\operatorname{ad} e_i)^{1 - A_{ij}} e_j &= 0 & (\operatorname{ad} f_i)^{1 - A_{ij}} f_j = 0. \end{array}$$

 $\mathfrak{e}_{10}$  is the free Lie algebra generated by  $\{e_i, f_i, h_i\}$  modulo these relations  $\rightarrow$  infinite dimensional as  $A_{ij}$  is *indefinite*  $\rightarrow$  Lie algebra of *exponential growth* !

## Habitat of Quantum Gravity?

• Cosmological evolution as one-dimensional motion in the moduli space of 3-geometries [Wheeler, DeWitt,...]

$$\mathcal{M} \equiv \mathcal{G}^{(3)} = \frac{\{\text{spatial metrics } g_{ij}(\mathbf{x})\}}{\{\text{spatial diffeomorphisms}\}}$$

- Formal canonical quantization leads to WDW equation ("Schrödinger equation of quantum gravity")
- Unification of space-time, matter and gravitation: configuration space  $\mathcal{M}$  for quantum gravity should consistently incorporate matter degrees of freedom.
- Can we understand and 'simplify'  $\mathcal{M}$  by means of embedding into a group theoretical coset G/K(G)?
- Proposal:  $G = E_{10}$  with involutory subgroup  $K(E_{10})$ . [Damour, Henneaux, Kleinschmidt, HN (since 2002)]

# SL(10) level decomposition of $E_{10}$

• Decomposition w.r.t. to SL(10) subgroup in terms of SL(10) tensors  $\rightarrow$  *level expansion* 

$$\alpha = \ell \alpha_0 + \sum_{j=1}^{9} m^j \alpha_j \quad \Rightarrow \quad E_{10} = \bigoplus_{\ell \in \mathbb{Z}} E_{10}^{(\ell)}$$

• Up to  $\ell \leq 3$  basic fields of D = 11 SUGRA together with their magnetic duals (spatial components)

$\ell = 0$	$G_{mn}$	Graviton
$\ell = 1$	$A_{mnp}$	3-form
$\ell = 2$	$A_{m_1\dots m_6}$	dual 6-form
$\ell = 3$	$h_{m_1\dots m_8 n}$	dual graviton

- Analysis up to level  $\ell \leq 28$  yields 4 400 752 653 representations (Young tableaux) of SL(10) [Fischbacher,HN:0301017]
- Lie algebra structure (structure constants, etc.) understood only up to  $\ell \leq 4$ . Also: no matter where you stop it will get even more complicated beyond!

# The $E_{10}/K(E_{10})$ $\sigma$ -model

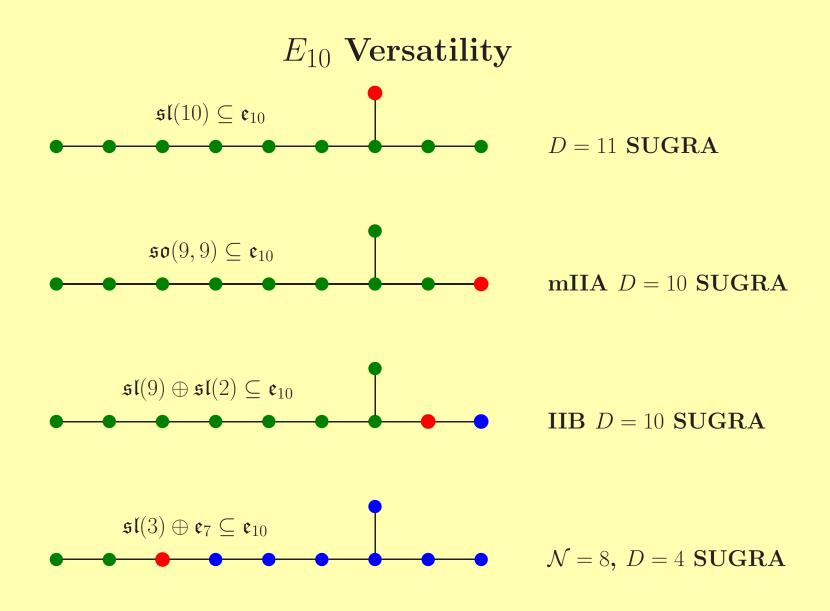
Basic Idea: map evolution according to D = 11 SUGRA equations of motion onto null geodesic motion of a point particle on  $E_{10}/K(E_{10})$  coset manifold [DHN:0207267]

$$\mathcal{V}(t) = \exp\left(h_{ab}(t)S^{ab} + \frac{1}{3!}A_{abc}(t)E^{abc} + \frac{1}{6!}A_{abcdef}(t)E^{abcdef} + \cdots\right)$$

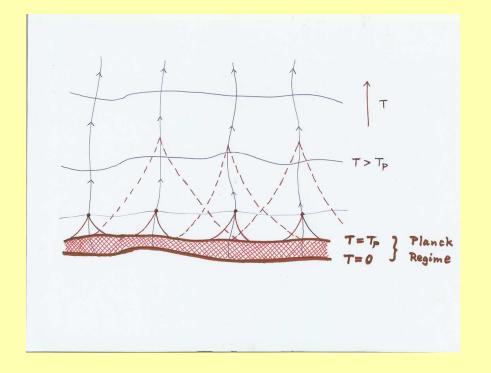
and then work out Cartan form  $\mathcal{V}^{-1}\partial_t \mathcal{V} = Q + P \rightarrow \sigma$ -model dynamics up to  $\ell \leq 3$  matches with supergravity equations of motion when truncated to first order spatial gradients.

Conjecture: information about spatial dependence gets 'spread' all over  $E_{10}$  Lie algebra  $\Leftrightarrow$  level expansion contains complete set of gradient representations for all D = 11 fields and their duals.

Last but not least:  $U(1)_q$  deformation required to match quark and lepton charges with N = 8 supergravity belongs to  $K(E_{10})$ ! [Kleinschmidt,HN, arXiv:1504.01586]



## $E_{10}$ : The Basic Picture



Conjecture: for  $0 < T < T_P$  space-time 'de-emerges', and space-time based (quantum) field theory is replaced by quantised 'spinning'  $E_{10}/K(E_{10}) \sigma$ -model.

[Damour, Henneaux, Kleinschmidt, HN: since 2002]

# Outlook

- Incompleteness of the SM and GR are strongest arguments in favor of quantizing gravity.
- Main Question: how are short distance singularities resolved in GR and QFT, and how can this resolution be reconciled with classical Einstein equations in continuum space-time?
  - Dissolving pointlike interactions (strings, branes,...)
  - Cancellation of UV infinities (e.g. N = 8 supergravity)?
  - Fundamental discreteness (LQG, discrete gravity)?
  - Other mechanism (e.g. AS, non-commutative space-time)?
- Symmetry-based approach offers new perspectives: N=8 supergravity and  $E_{10}$  are uniquely distinguished.
- ... but there is still a long way to go!

### Coming up: www.einsteinconference2015.org

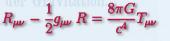
#### A Century of General Relativity November 30 - December 2, 2015 Harnack House Berlin

The year 2015 marks the 100th anniversary of Einstein's field equations. To celebrate this event, the Max Planck Institute for Gravitational Physics (or Albert Einstein Institute) will host a conference during the week of November 30, 2015, exactly one hundred years after the publication of Einstein's paper. The conference will take place in the recently renovated Harnack House in Berlin, where Albert Einstein regularly lectured between 1915 and 1931. On December 3.5 the Max Planck Institute for the History of Science will conclude the celebratory events with a workshop on the history of Einstein's theory.

Abhay Ashtekar Penn State University, University Park







Zvi Bern University of California, Los Angeles Thibault Damour IHES, Buressur-Vvette Reinhard Genzel Max Planck Institute for Extraterrestial Physics, Munich Andrea Ghez University of California, Los Angeles David Gross Kavli Institute for Theoretical Physics, Santa Barbara Hanoch Gutfreund Hebrew University, Perusalem Ted Jacobson University of Maryland, College Park Sergiu Klainerman Princeton University, Princeton Joseph Polchinski Kavli Institute for Theoretical Physics, Santa Barbara Frans Pretorius Princeton University, Princeton Harvey Reall DMMTP Cambridge David Spergel Princeton University, Princeton Ingrid Stairs University of British Columbia, Vancouver Paul Steinhardt Princeton University, Princeton Rai Weiss Massachusetts Institute of Technology, Cambridge

Scientific Organization Committee: Bruce Allen, Alessandra Buonanno, Karsten Danzmann, Hermann Nicolai (Chair), Beinard Schutz Max Planck Institute for Gravitational Physics (Albert Einstein Institute) For more information and program details please visit: www.einsteinconference2015.org

www.einsteinconference2015.org

