



Charm Physics

— Recent Experimental Progress —

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XXXV Physics in Collision 2015, 15-19th September,

University of Warwick, Coventry, United Kingdom

SM predictions :

- a rather dull EW phenomenology of CKM parameters
- a low frequency for the $D\bar{D}$ oscillations
- tiny CP asymmetries
- extremely rare FCNC decay

**Challenging
experimental
measurement**

Motivations for dedicated and comprehensive studies :

- Provide an unique and powerful laboratory for studying the impact of non-pQCD dynamics and for testing the validity of theoretical methods
- Provides a calibration of the theoretical tools for the B decays
- Provide a novel window on NP search

**Charming
Promising**

- D^0 - \bar{D}^0 Oscillation and CP Violation
- Quantum-Correlated Charm @ threshold
- (Semi-) Leptonic Decay
- Hadronic Decay
- Rare Decay

For each I will highlight recent progress and speculate on future developments

Apology I can not cover all of results



Charm facilities



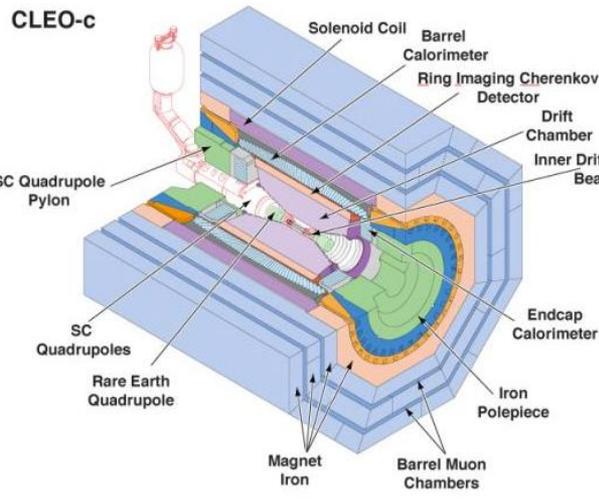
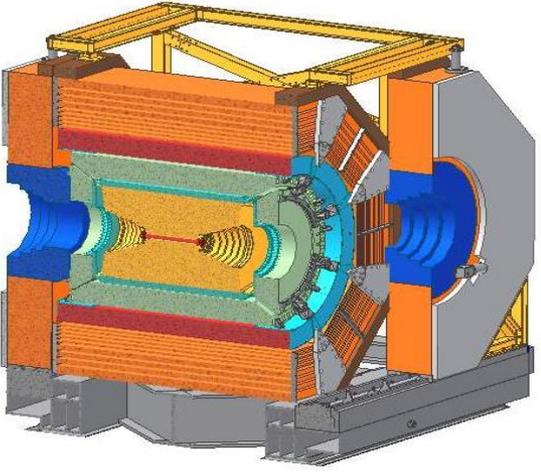
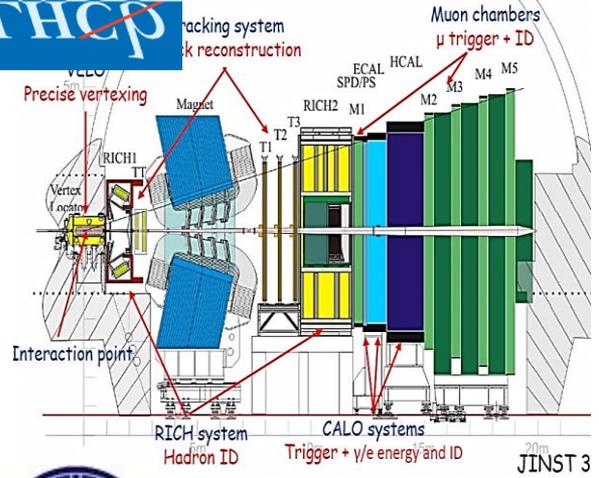
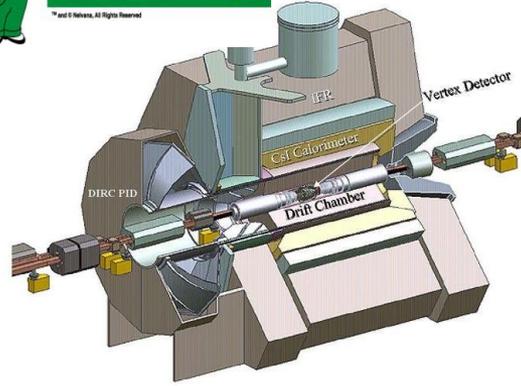
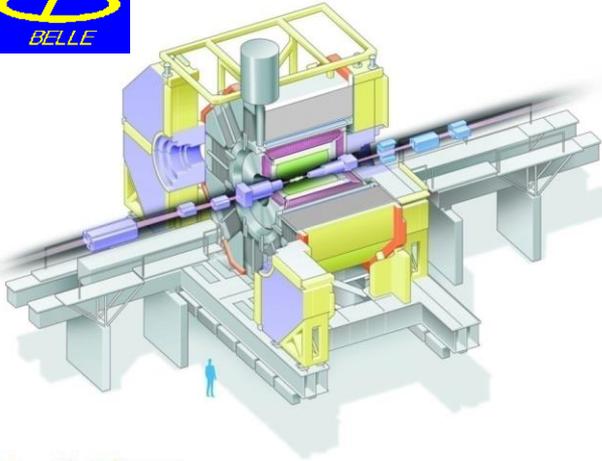
Hadron Colliders (Huge cross-section, energy boost)

- Tevetron (CDF, D0)
- LHC (LHCb, CMS, ATLAS)

e^+e^- Collider (more kine. constrains, clean envir., $\sim 100\%$ trigger eff.)

- B-Factories (Belle, BaBar)
 - Prompt D^* decay : slow pion tag D flavor, $D^{*+} \rightarrow D^0 \pi^+$ or $D^{*-} \rightarrow D^0 \pi^-$
 - Semileptonic B decay : muon tag D flavor, $B \rightarrow D^0 \mu^+ \nu_\mu X$ or $B \rightarrow D^0 \mu^- \nu_\mu X$
- Threshold Production (CLEOc, BESIII)
 - **Can not compete in statistics with Hadron colliders & B-Factories**
 - Only D meson pairs, no extra CM energy for pions
 - Quantum correlations (QC) and CP-tagging are unique
 - Systematic uncertainties cancellations while applying double tag technique

Results from These Experiments





D^0 - \bar{D}^0 Oscillation and CPV

- D^0 is the only mixing meson with up-type quarks
- Neutral D mass eigenstates are linear combination of flavor states

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle & |p|^2 + |q|^2 &= 1 \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle & \phi &= \arg(q/p) \end{aligned}$$

- Mixing parameters :

$$x = \frac{m_2 - m_1}{\Gamma} \sim \text{Mixing frequency}$$

$$y = \frac{\Gamma_2 - \Gamma_1}{2\Gamma} \sim \text{Lifetime difference}$$

$$P(D^0 \rightarrow \bar{D}^0, t) = \frac{1}{2} \left| \frac{q}{p} \right|^2 e^{-\Gamma t} \{-\cos(x\Gamma t) + \cosh(y\Gamma t)\}$$

- Short distance is highly suppressed by the GIM mechanism and the matrix elements within the SM. $x \sim \mathcal{O}(10^{-5})$, $y \sim \mathcal{O}(10^{-7})$

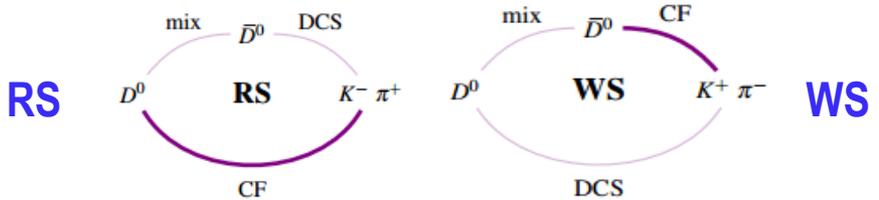
(NP, e.g. FCNC processes with up-type quark, might manifest in the loop)

- Long distance is dominant, but theoretical uncertainty is large $x, y \sim \mathcal{O}(10^{-3})$
- Improving the constraints on the charm mixing parameters is important to testing the SM, such as long-distance effect.

- CP Violation occurs if $|q/p| \neq 1$ or CPV phase $\phi \neq 0$
- In SM, CPV is expected to be small for charm, theory calculation is challenging.
- Enhancement hits at NP, and CPV search in charm provide probe for NP
- CPV in decay : $A_d \equiv (|A_f|^2 - |\bar{A}_{\bar{f}}|) / (|A_f|^2 + |\bar{A}_{\bar{f}}|)$
- CPV in mixing : $A_m \equiv (|q/p|^2 - |p/q|^2) / (|q/p|^2 + |p/q|^2)$
- CPV in interference through : $\phi = \arg \left(\frac{q\bar{A}_{\bar{f}}}{pA_f} \right)$
- No strong evidence for CPV in charm

D⁰-D̄⁰ Mixing in D⁰→Kπ

- Measurement of time-dependent ratio of D⁰→K⁻π⁺ (RS) and D⁰→K⁺π⁻ (WS) decays



PRL 110 (2013) 101802

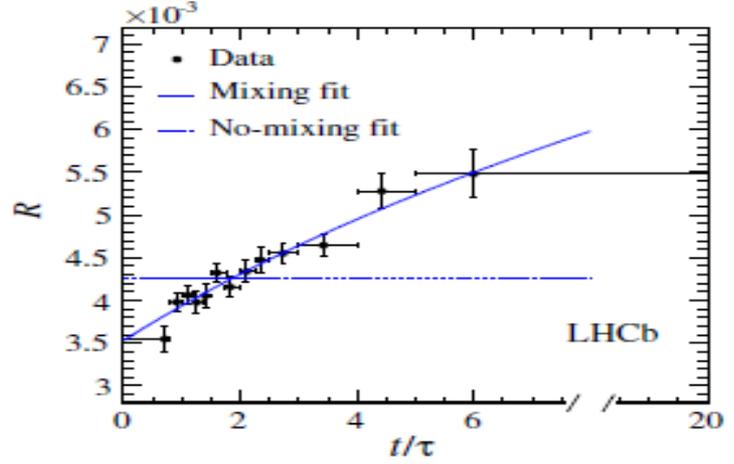
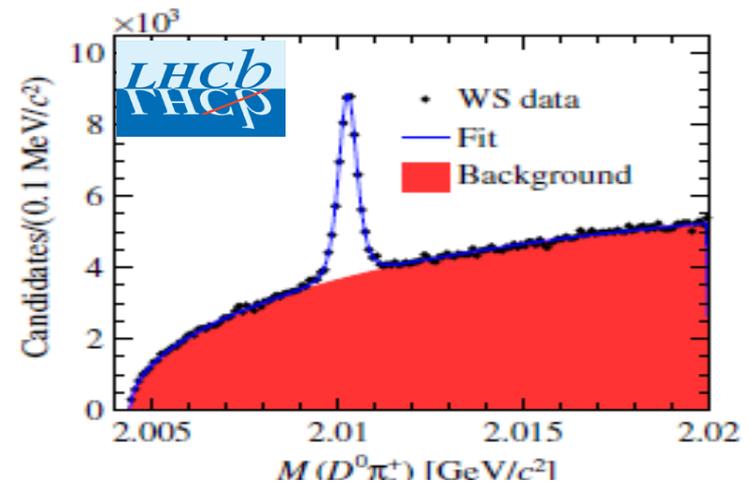
- In limit of small mixing and negligible CPV

$$R(t) \approx R_D + \sqrt{R_D} y' \frac{t}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{t}{\tau}\right)^2$$

$$A(D^0 \rightarrow K^+ \pi^-) / A(D^0 \rightarrow K^- \pi^+) = \sqrt{R_D} e^{-i\delta}$$

$$x' \equiv x \cos \delta_{K\pi} + y \sin \delta_{K\pi}, \quad y' \equiv y \cos \delta_{K\pi} - x \sin \delta_{K\pi}$$

- LHCb 1 fb⁻¹ data @ 7 TeV :
 - D⁰ flavor tagged by slow π⁺ charge from D^{*+}→D⁰π⁺
 - Extract the x', y' and R_D by bin χ² fit to R(t)
 - No mixing hypothesis excluded at 9.1σ

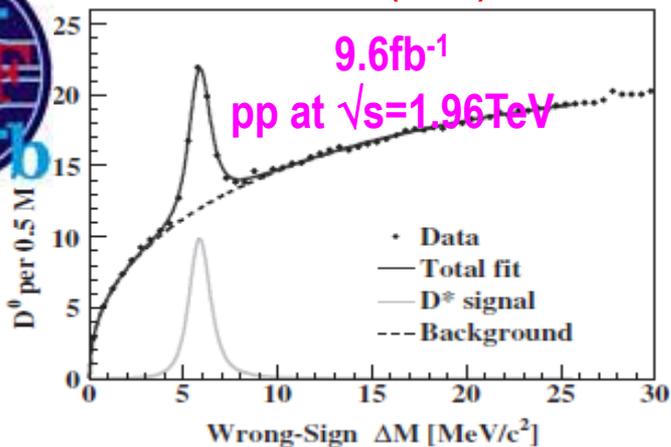


First observation of D⁰-D̄⁰ mixing in a single measurement

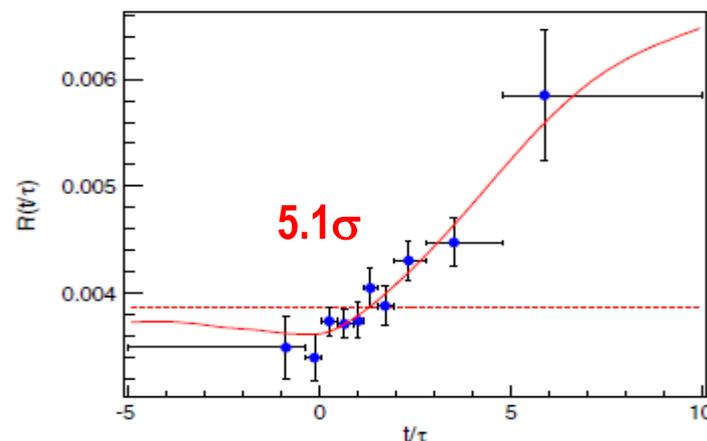
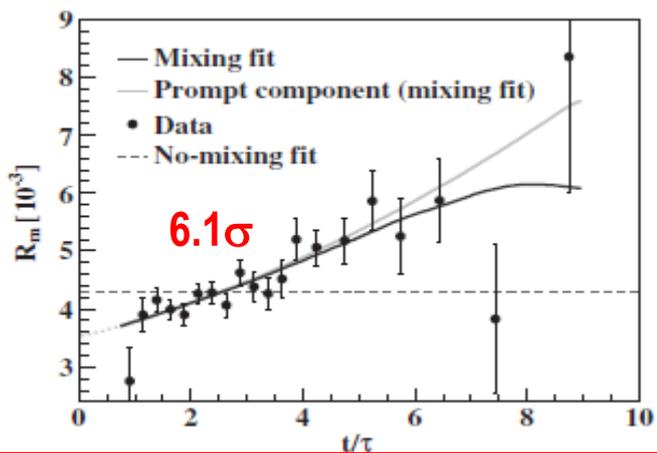
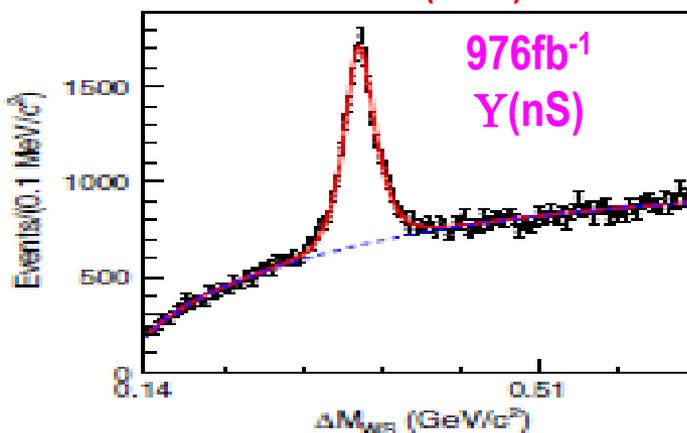
D⁰- \bar{D}^0 Mixing in D⁰→Kπ



PRL 111 (2013) 231802



PRL 112 (2014) 111801



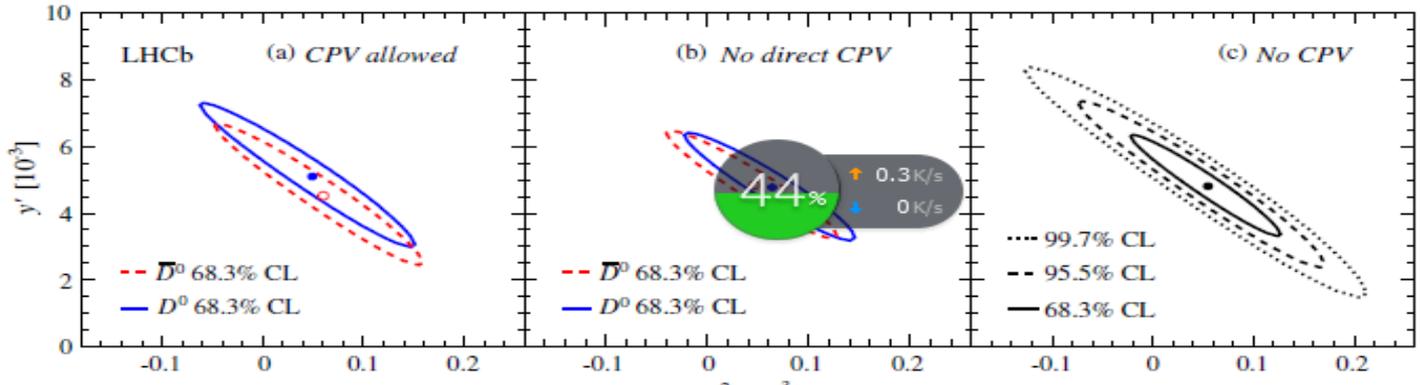
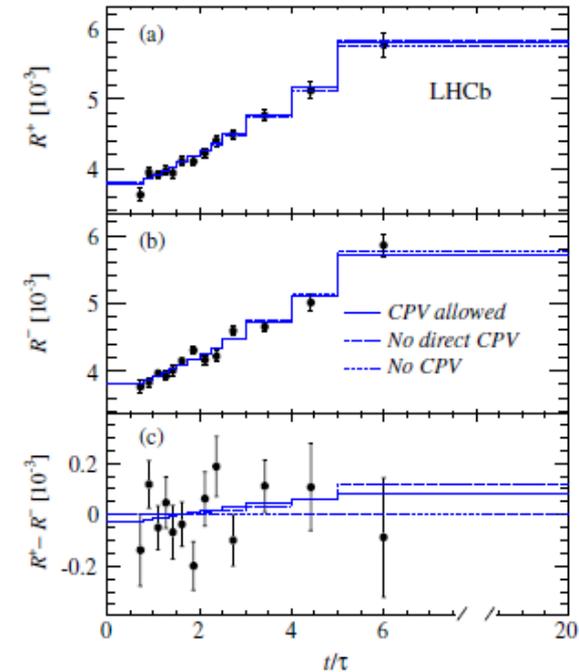
D⁰- \bar{D}^0 mixing is confirmed by hadron collider CDF and e⁺e⁻ collider Belle

D⁰- \bar{D}^0 Mixing & CPV in D⁰→Kπ

- LHCb updated results with 3fb⁻¹ pp collision data
- CPV search : splitting D⁰ and \bar{D}^0 samples, fit to R[±](t)
 - Same parameters : **no CPV**
 - Different in R_D[±] : **direct CPV**
 - Different in (x'²⁺, y'⁺) and (x'²⁻, y'⁻) : **indirect CPV**
- **Results compatible with CP conservation :**

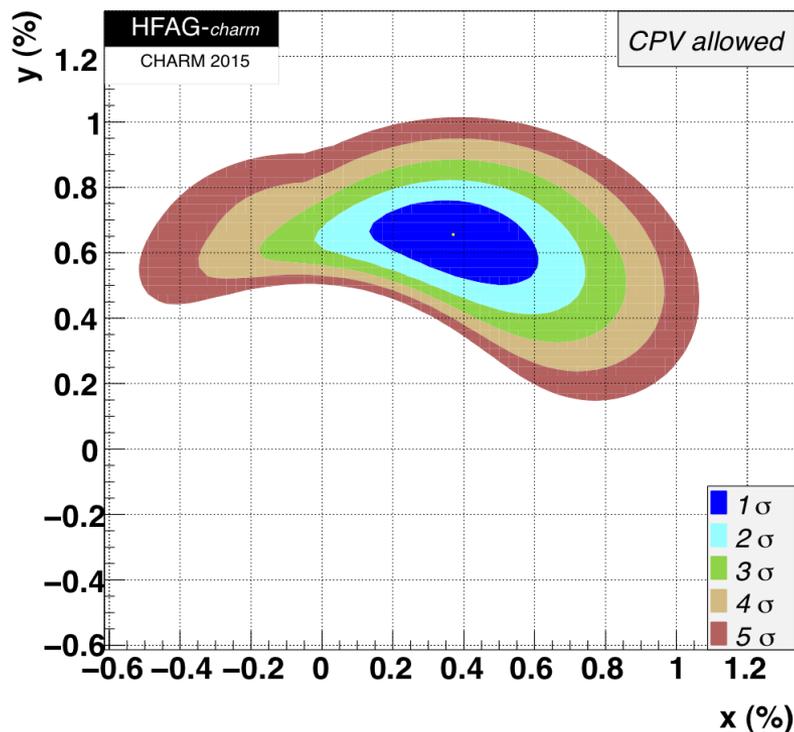
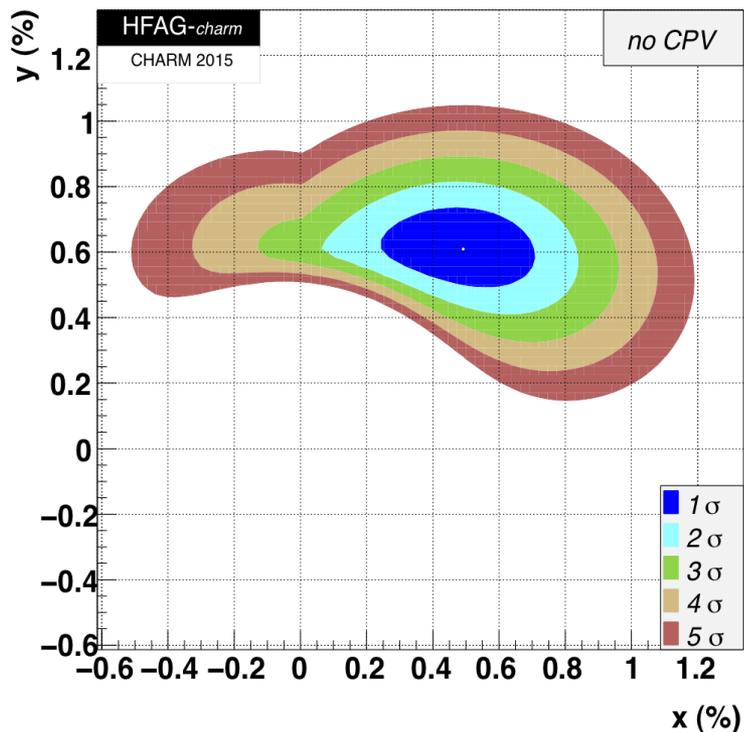
$$A_D \equiv \frac{R_D^+ - R_D^-}{R_D^+ + R_D^-} = (-0.7 \pm 1.9)\%$$
- The mixing Parameters are consistent with, 2.5 times more precise than previous results

PRL 111 (2013) 251801



D⁰- \bar{D}^0 Mixing

http://www.slac.stanford.edu/xorg/hfag/charm/CHARM15/results_mix_cpv.html



D⁰- \bar{D}^0 mixing is well established in different experiments

Indirect CPV in $D^0 \rightarrow h^+ h^-$

- Time-dependent CP asymmetry for a neutral D meson decay to a CP eigenstate :

$$A_{CP}(t) = \frac{\Gamma(D^0 \rightarrow f; t) - \Gamma(\bar{D}^0 \rightarrow f; t)}{\Gamma(D^0 \rightarrow f; t) + \Gamma(\bar{D}^0 \rightarrow f; t)}$$

- Approximated as linear-time dependence :

$$A_{CP}(t) \approx A_{CP}^{dir} - A_{\Gamma} \frac{t}{\tau}$$

$$A_{\Gamma} \equiv \frac{\hat{\Gamma} - \bar{\Gamma}}{\hat{\Gamma} + \bar{\Gamma}} \approx (A_{CP}^{mix}/2 - A_{CP}^{dir}) y \cos \phi - x \sin \phi$$

- D^0 flavor tagged by the muon from SL b-hadron decay.
- Consistent with no indirect CPV hypothesis

$$A_{\Gamma}(K^+ K^-) = (-0.134 \pm 0.077_{-0.034}^{+0.025})\%$$

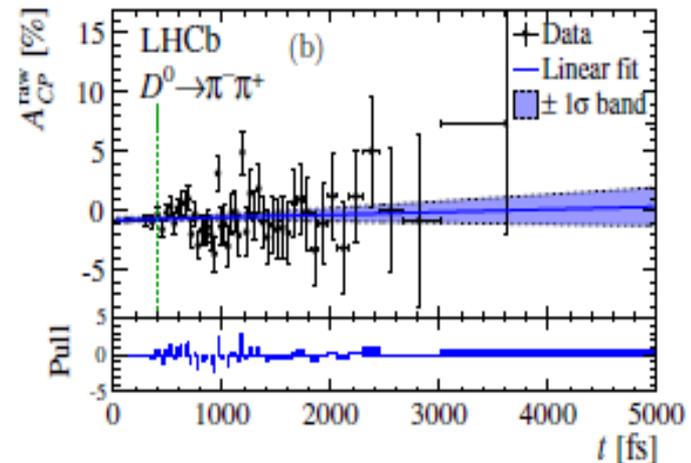
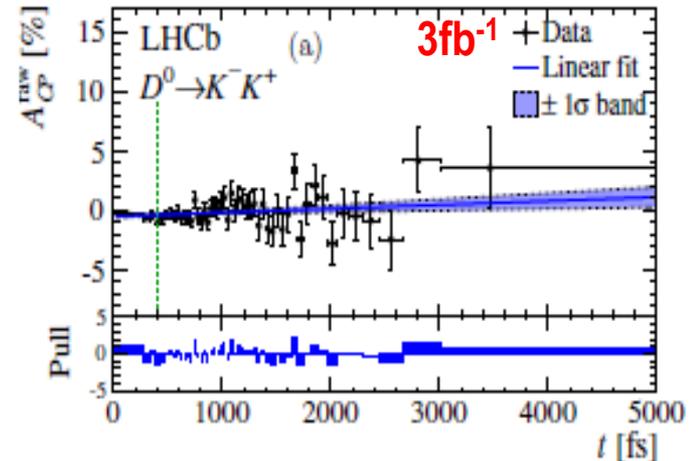
$$A_{\Gamma}(\pi^+ \pi^-) = (-0.092 \pm 0.145_{-0.034}^{+0.025})\%$$

Assume indirect CPV is universal:

$$A_{\Gamma} = (-0.125 \pm 0.072)\%$$

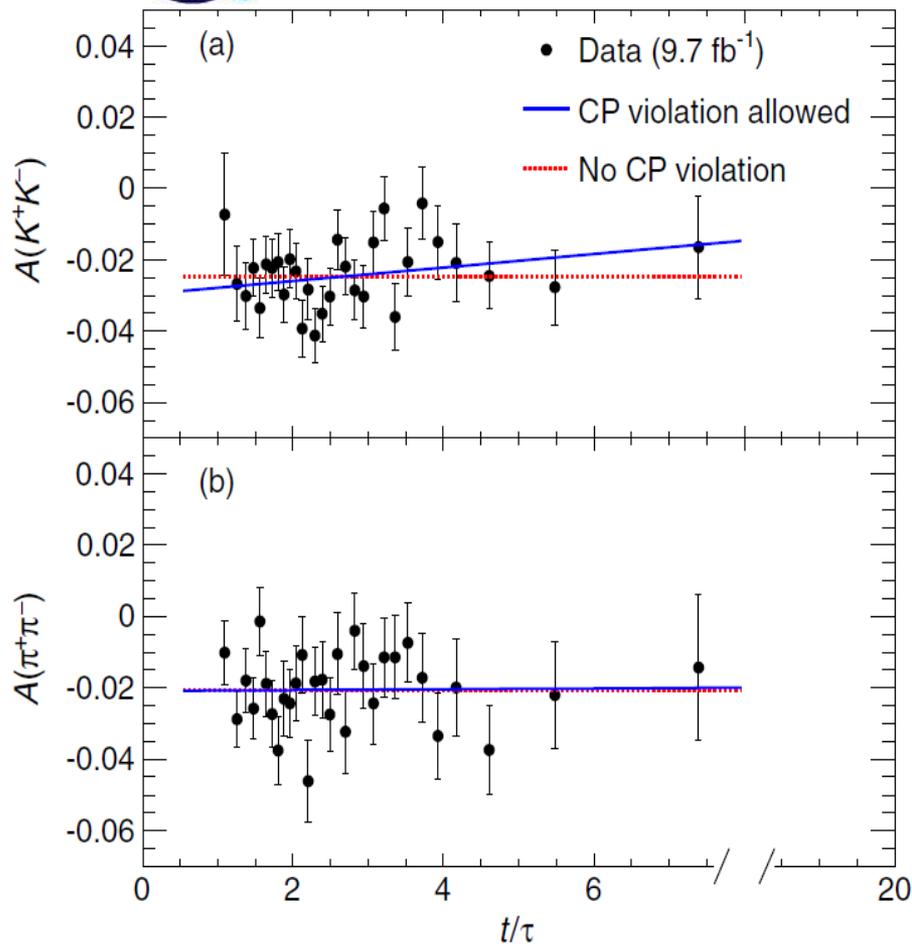


JHEP 04 (2015) 043





9.7fb⁻¹ 1.96TeV ppbar collision
PRD 90 (2014) 111103 (R)



- D^0 is tagged with slow π in $D^{*+} \rightarrow D^0 \pi^+$

- CDF Results :

$$A_{\Gamma}(K^+K^-) = (-0.19 \pm 0.15(\text{stat}) \pm 0.04(\text{syst}))\%$$

$$A_{\Gamma}(\pi^+\pi^-) = (-0.01 \pm 0.18(\text{stat}) \pm 0.03(\text{syst}))\%$$

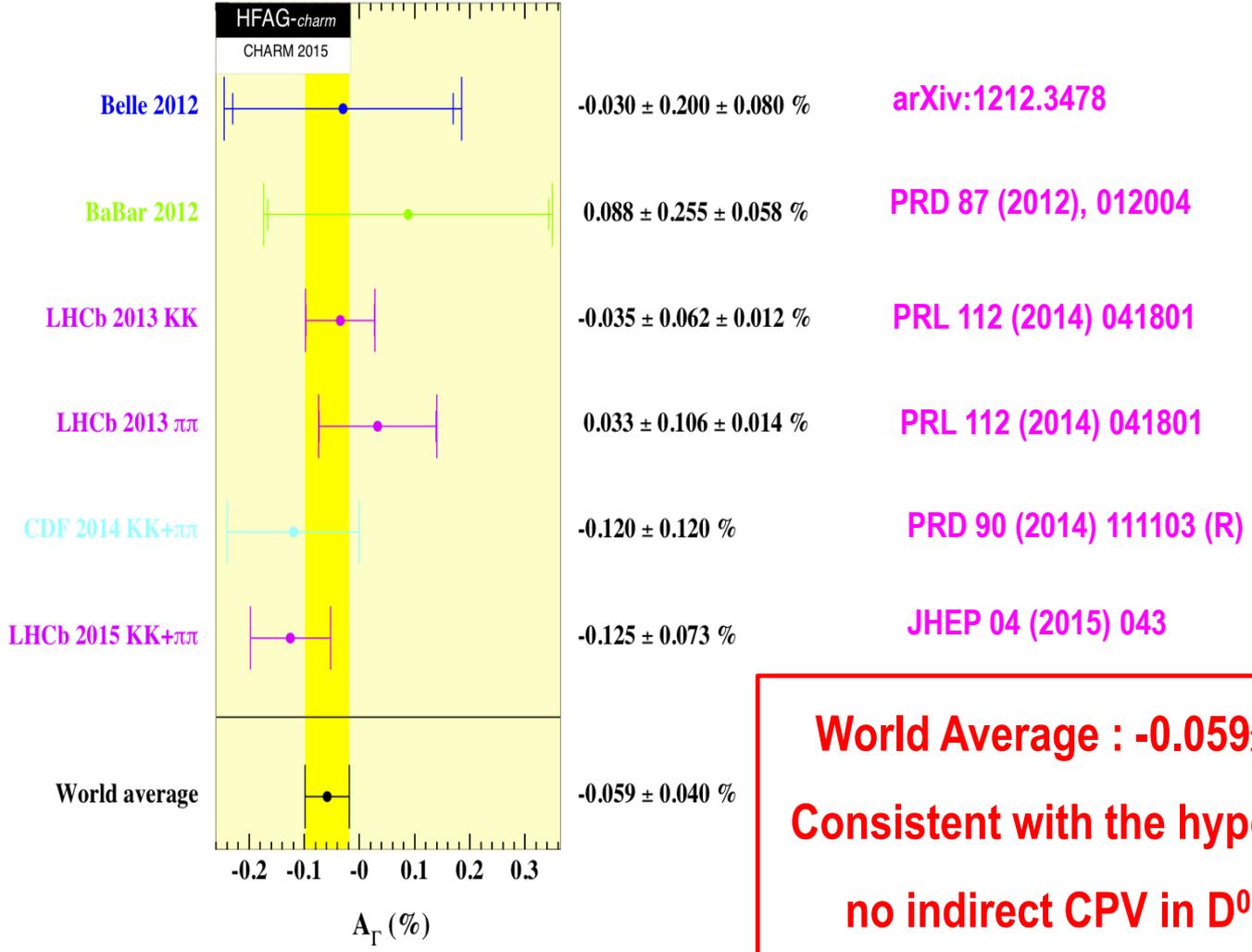
- Compatible with the absence of CPV
- Consistent with determination from other experiments
- Among the world's best results



Indirect CPV in $D^0 \rightarrow h^+ h^-$



http://www.slac.stanford.edu/xorg/hfag/charm/CHARM15/results_mixing.html



World Average : -0.059 ± 0.040 %
Consistent with the hypothesis of
no indirect CPV in $D^0 \rightarrow h^+ h^-$

- Time integrated CP asymmetry receives contributions from both direct and indirect CPV

$$A_{CP} = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)} = a_{CP}^{dir}(f) + \frac{\langle t \rangle}{\tau} a_{CP}^{ind}$$

- Assuming ind. CPV is decay mode independent,

Only the effect of direct CPV remain in ΔA_{CP}

$$\begin{aligned} \Delta A_{CP} &= A_{CP}(K^- K^+) - A_{CP}(\pi^- \pi^+) \\ &= [a_{CP}^{dir}(K^- K^+) - a_{CP}^{dir}(\pi^- \pi^+)] + \frac{\Delta \langle t \rangle}{\tau} a_{CP}^{ind} \end{aligned}$$

Vanish in the limit

- LHCb 3fb^{-1} data, muon flavor tagged D^0 in B hadron SL decay

- The raw asymmetry for a D meson decay :

$$A_{raw} = \frac{N(D \rightarrow f) - N(\bar{D} \rightarrow f)}{N(D \rightarrow f) + N(\bar{D} \rightarrow f)} = A_{CP} + A_D(\mu^-) + A_P(\bar{B})$$

- And ΔA_{CP}

$$\Delta A_{CP} = A_{raw}(K^+ K^-) - A_{raw}(\pi^+ \pi^-) = A_{CP}(K^+ K^-) - A_{CP}(\pi^+ \pi^-)$$

- No significant CPV in SCS decay at the level 10^{-3}

$$\Delta A_{CP} = (+0.14 \pm 0.16 \pm 0.08)\%$$

$$A_{CP}(K^+ K^-) = (-0.06 \pm 0.15 \pm 0.10)\%$$

$$A_{CP}\pi^+ \pi^- = (-0.20 \pm 0.19 \pm 0.10)\%$$

Most precise measurement of time-integrated CPV $A_{CP}(K^+ K^-)$ and $A_{CP}(\pi^+ \pi^-)$

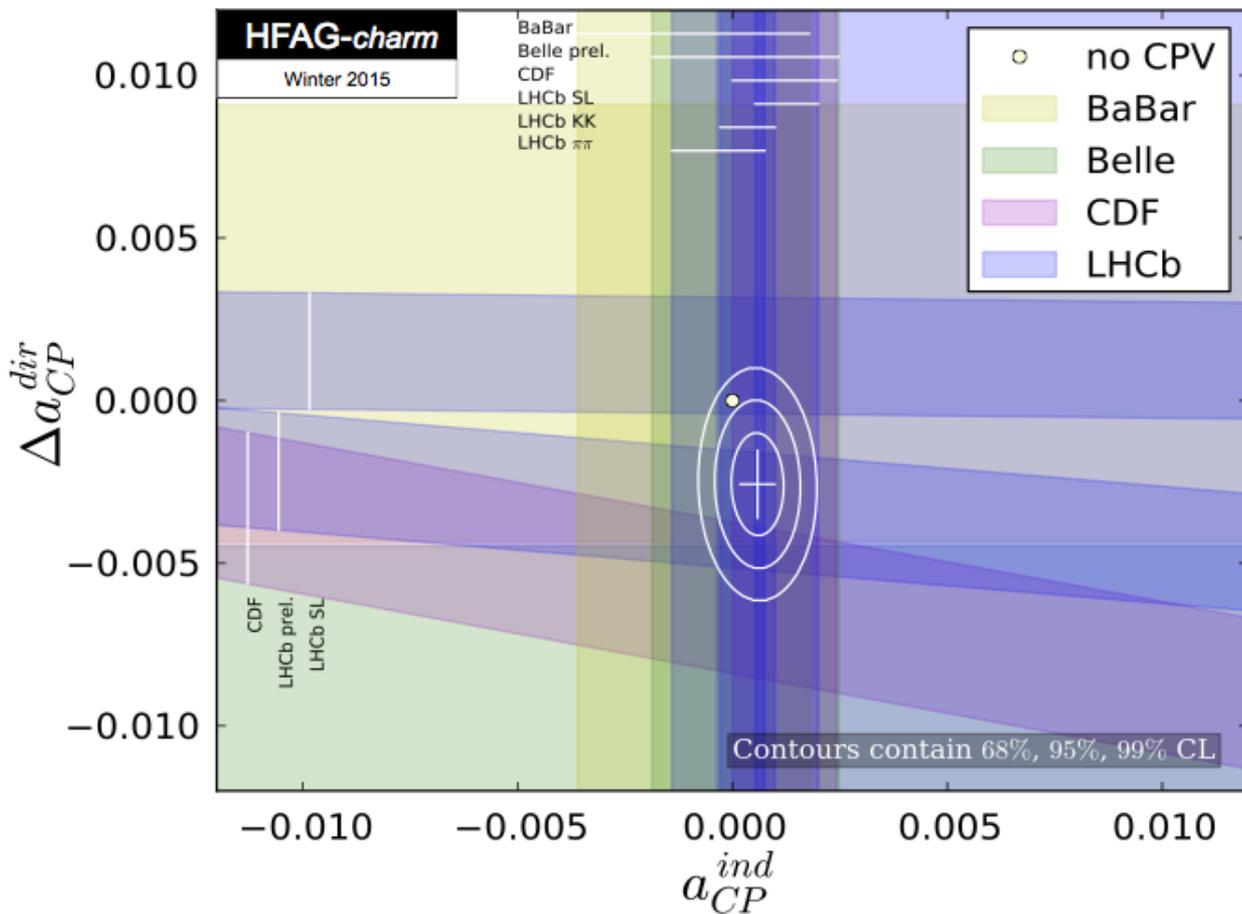
Belle update the results of similar analysis with full data set, please see Tara's talk at Charm 2015

<http://belle.kek.jp/belle/talks/CHARM15/nanut.pdf>

CPV in $D^0 \rightarrow h^+ h^-$

http://www.slac.stanford.edu/xorg/hfag/charm/April15/DCPV/direct_indirect_cpv.html

Combine time-dependent and time-integrated CPV results



$$a_{CP}^{ind} = (0.058 \pm 0.040)\%$$

$$\Delta a_{CP}^{dir} = (-0.257 \pm 0.104)\%$$

P = 0.018 of no CPV

- D^0 decay into a neutral mesons pair is particular interest for the search of NP and the understanding of penguin contributions.
- CPV is expected larger if CPV exists in D^0 decay to charge meson pair
- SM predicts a 95% CL UL of 1.1% for direct CPV in decay $D^0 \rightarrow K_s K_s$

- LHCb performed the search of time integrated CP asymmetry with 3 fb^{-1} data

$$A_{CP} = \frac{N^+ - N^-}{N^+ + N^-}$$

- The D^0 flavor is tagged by the slow π^+ from $D^{*+} \rightarrow D^0 \pi^+$
- The CP asymmetry is obtained in four $K_s K_s$ reconstruction categories



$$A_{CP} = -0.029 \pm 0.052 \pm 0.022$$

arXiv:1508.06087
LHCb-PAPER-2015-030

- Consistent with no CP Violation and with SM expectation
- Three times smaller for uncertainty than previous measurement (PRD 63, 2001, 071101)

CP Asymmetry in $D^0 \rightarrow \pi^0 \pi^0$

- Search for the time integrated CPV using data sample 966 fb⁻¹
- The flavor of D⁰ is tagged with the slow π⁺ in decay D^{*+} → D⁰π⁺
- The reconstructed asymmetry :

$$A_{rec} = \frac{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} - N_{rec}^{D^{*-} \rightarrow \bar{D}^0 \pi_s^-}}{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} + N_{rec}^{D^{*-} \rightarrow \bar{D}^0 \pi_s^-}}$$

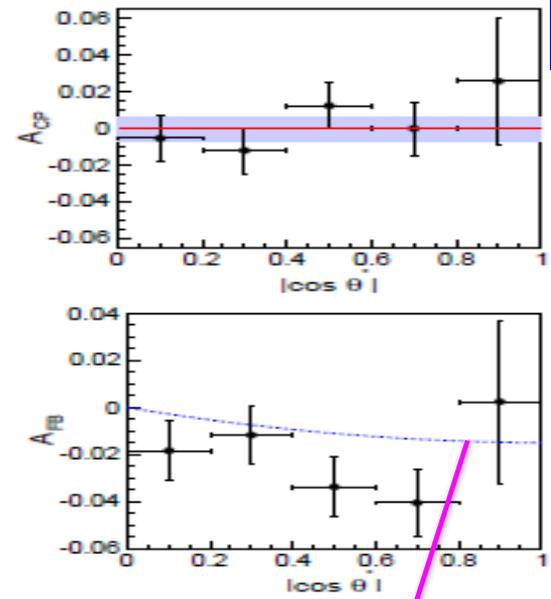
$$= A_{CP} + A_{FB} + A_{\epsilon}^{\pi_s}$$

The underlying CP asymmetry

Estimated with CF decay
D^{*+} → D⁰π_s → K⁻π⁺π_s

The Forward-backward asymmetry due to γ-Z⁰ interference and High order QED effects
Is an odd function of the cosine of D^{*+} polar angle

PRL 112 (2014) 211601



Lower than leading order QED prediction, High-order correction may bring better agreement

- Corrected A_{rec}^{cor} :

$$A_{rec}^{cor} = A_{CP} + A_{FB}(\cos \theta^*)$$

$$A_{CP} = |A_{rec}^{cor}(\cos \theta^*) + A_{rec}^{cor}(-\cos \theta^*)|/2$$

$$A_{FB} = |A_{rec}^{cor}(\cos \theta^*) - A_{rec}^{cor}(-\cos \theta^*)|/2$$

$A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = (-0.03 \pm 0.64 \pm 0.10)\%$
No evidence for CP Violation
An order of magnitude improvement in precision

Two-body Final States :

- Search for direct CPV in SCS $D_{(s)}^{\pm} \rightarrow K_S h^{\pm}$
(LHCb, 3fb⁻¹, JHEP 1410 (2014) 025, BaBar, 469fb⁻¹, PRD 87 (2013), 052012)

Multi-body Final States :

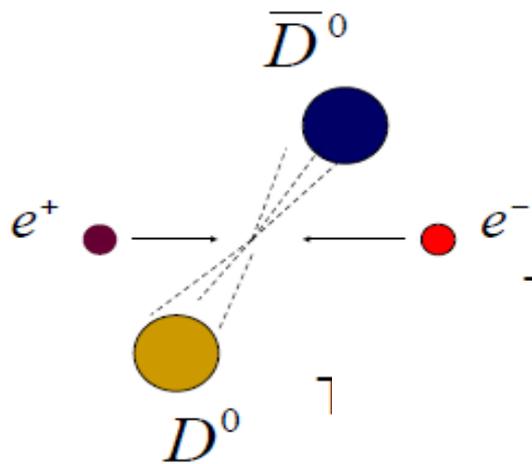
- Model-independent searches for CPV in $D^+ \rightarrow \pi^+ \pi^- \pi^+$ (LHCb, 1fb⁻¹, PLB 728 (2014) 585)
- Search for direct CPV in SCS decay $D^{\pm} \rightarrow K^+ K^- \pi^{\pm}$ with Model-(in)dependent Dalitz analysis
(BaBar, 476fb⁻¹, PRD 87 (2013), 052010)
- Search for indirect CPV using $D^+ \rightarrow \pi^+ \pi^- \pi^+$ with a time-dependent amplitude analysis
(Belle, 921fb⁻¹, PRD 89 (2014), 091103)
- Time-integrated CPV in SCS process $D^0 \rightarrow \pi^+ \pi^- \pi^0$ (LHCb, 2fb⁻¹, PLB 740 (2015) 158)
- Time-dependent Dalitz analysis in $D^0 \rightarrow K_S \pi^- \pi^+$
(LHCb, 1fb⁻¹, LHCb-Paper-2015-042, see Canto's talks at LHCP 2015 meeting)
- CPV via T-odd moments in $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ (LHCb, 3fb⁻¹, JHEP 10 (2015) 005)
-

No CPV observation, more results are expected soon



Quantum-Correlated Charm @ Threshold

Quantum Correlated $D^0\bar{D}^0$ States



For a physical process producing $D^0\bar{D}^0$, such as :

$$e^+e^- \rightarrow \psi'' \rightarrow D^0\bar{D}^0$$

The $D^0\bar{D}^0$ pair should be a quantum-correlated state

The J^{PC} of ψ'' is 1^{--} , a definite $C = -1$ state for $D^0\bar{D}^0$ pair

D^0 mesons will have **opposite CP**

The quantum coherence of $D^0\bar{D}^0$ pairs play an unique way to study :

- Strong phase, $\cos\delta$: Double tag events, e.g. $K^-\pi^+$ VS. CP_{\pm}
- Strong phase c_i, s_i (Dalitz) : $K_S\pi^+\pi^-$ VS. CP_{\pm} , $K_S\pi^+\pi^-$ VS. Flavor Tag, $K_S\pi^+\pi^-$ VS. $K_S\pi^+\pi^-$
- Charm mixing, y_{CP} : Flavor tag VS. CP_{\pm}
- Mixing parameters, (x^2+y^2) : $(K^-\ell^+\nu)^2, (K^-\pi^+)^2$
- DCS : Wrong sign decay $K^-\pi^+$ VS. $K^-\ell^+\nu$

Typical kinematic variables :

$$\Delta E = E_D - E_{Beam}$$

$$M_{BC} = \sqrt{E_{Beam}^2 - \vec{p}_D^2}$$

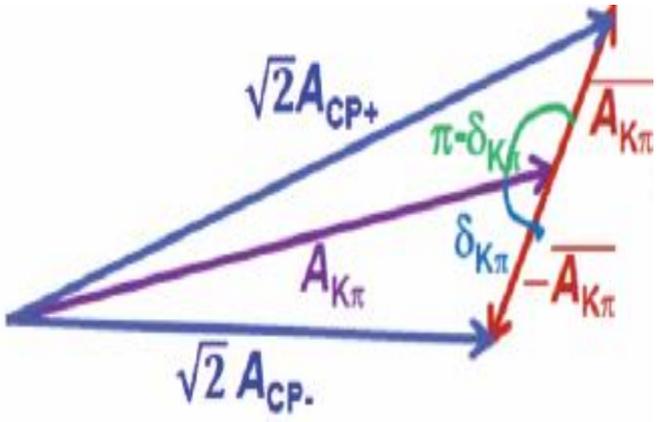
Strong Phase $\delta_{K\pi}$ in $D^0 \rightarrow K\pi$

Time-dependent decay rate of WS process $D^0 \rightarrow K^+\pi^-$, $x' \equiv x \cos \delta_{K\pi} + y \sin \delta_{K\pi}$
 most precise measurement for the mixing parameter, sensitive to : $y' \equiv y \cos \delta_{K\pi} - x \sin \delta_{K\pi}$

Strong phase $\delta_{K\pi}$: Difference between the DCS and CF amplitude

$$\frac{\langle K^-\pi^+ | \bar{D}^0 \rangle^{DCS}}{\langle K^-\pi^+ | D^0 \rangle^{CF}} = -r_{K\pi} e^{-i\delta_{K\pi}}$$

Important for extracting x and y from x' and y'



$$\langle K\pi | D_{CP\pm}^0 \rangle = (\langle K\pi | D^0 \rangle \pm \langle K\pi | \bar{D}^0 \rangle) / \sqrt{2} \Rightarrow \sqrt{2} A_{CP\pm} = A_{K\pi} \pm \bar{A}_{K\pi}$$

$$2r_{K\pi} \cdot \cos \delta_{K\pi} \approx A_{CP \rightarrow K\pi} \equiv \frac{|A_{CP-}|^2 + |A_{CP+}|^2}{|A_{CP-}|^2 + |A_{CP+}|^2} = \frac{Br(D_{CP-} \rightarrow K\pi) - Br(D_{CP+} \rightarrow K\pi)}{Br(D_{CP-} \rightarrow K\pi) + Br(D_{CP+} \rightarrow K\pi)}$$

Ignore the mixing effect

Strong Phase $\delta_{K\pi}$ in $D^0 \rightarrow K\pi$

Signal reconstruction :

- Single Tag (ST) : CP Tags (5 modes CP+, 3 modes CP-)
- Double Tag (DT) : $K\pi$ + CP Tag

Type	Mode
Flavored	$K^-\pi^+, K^+\pi^-$
S+	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$
S-	$K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

BESIII 2.9 fb⁻¹ ψ'' data PLB 734 (2014) 227

Branching Ratio Measurement :

$$Br(D_{CP\pm} \rightarrow K\pi) = \frac{N_{K\pi,CP\pm}}{N_{CP\pm}} \cdot \frac{\varepsilon_{CP\pm}}{\varepsilon_{K\pi,CP\pm}}$$

Asymmetry of CP tagged D decay rate : $A_{CP \rightarrow K\pi} = (12.7 \pm 1.3 \pm 0.7) \times 10^{-2}$

Consider the mixing effect

$$2r_{K\pi} \cdot \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot A_{CP \rightarrow K\pi}$$

External input from HFAG2013 and PDG

- $r_{K\pi}^2 = (0.347 \pm 0.006)\%$
- $y = (0.66 \pm 0.09)\%$
- $R_{WS} = (0.380 \pm 0.005)\%$

$$\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

- World best precision
- The statistical errors dominant the precision
- BESIII 20 fb⁻¹ data, precision will reach 0.05

CLEO-c results [*Phys. Rev. D* 86 (2012) 112001]

$$\cos \delta_{K\pi} = 0.81_{-0.18-0.05}^{+0.22+0.07}$$

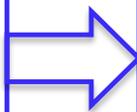
$$\cos \delta_{K\pi} = 1.15_{-0.17-0.08}^{+0.19+0.00} \quad (\text{globalfit})$$

The mixing parameters extracted from time-dependent decay $D^0 \rightarrow K\pi$ is highly corrected, it is important to access the mixing parameters directly.

$$y_{CP} = \frac{1}{2} \left[y \cos \phi \left(\left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) - x \sin \phi \left(\left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \right]$$

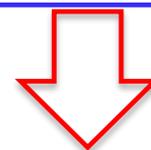
In absence of CPV, $|P/q|=1$ and $\phi=0$, leading to $y_{CP} = y$

- The D^0 semileptonic decay is sensitive to flavor content and does not depend on the CP eigenvalue
- The total decay width of the $D_{CP\pm}$ depend on its CP eigenvalue : $\Gamma_{CP\pm} = \Gamma(1 \pm y_{CP})$



The semileptonic decay of the CP eigenstates $D_{CP\pm}$

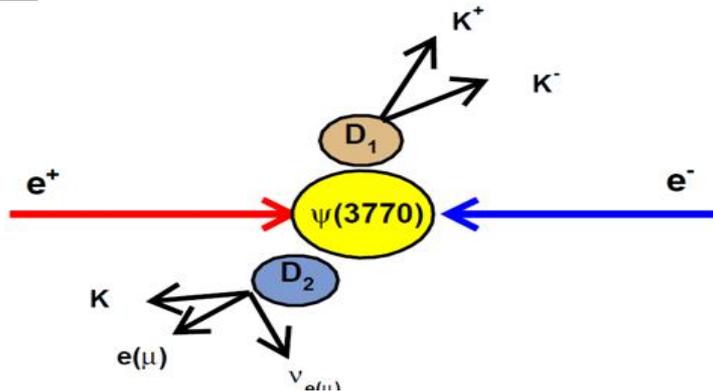
$$B_{D_{CP\pm} \rightarrow l} \approx B_{D \rightarrow l} (1 \mp y_{CP})$$



$$y_{CP} \approx \frac{1}{4} \left(\frac{B_{D_{CP-} \rightarrow l}}{B_{D_{CP+} \rightarrow l}} - \frac{B_{D_{CP+} \rightarrow l}}{B_{D_{CP-} \rightarrow l}} \right)$$

y_{CP} Measurement

BESIII 2.9 fb⁻¹ ψ'' data PLB 744 (2015) 339



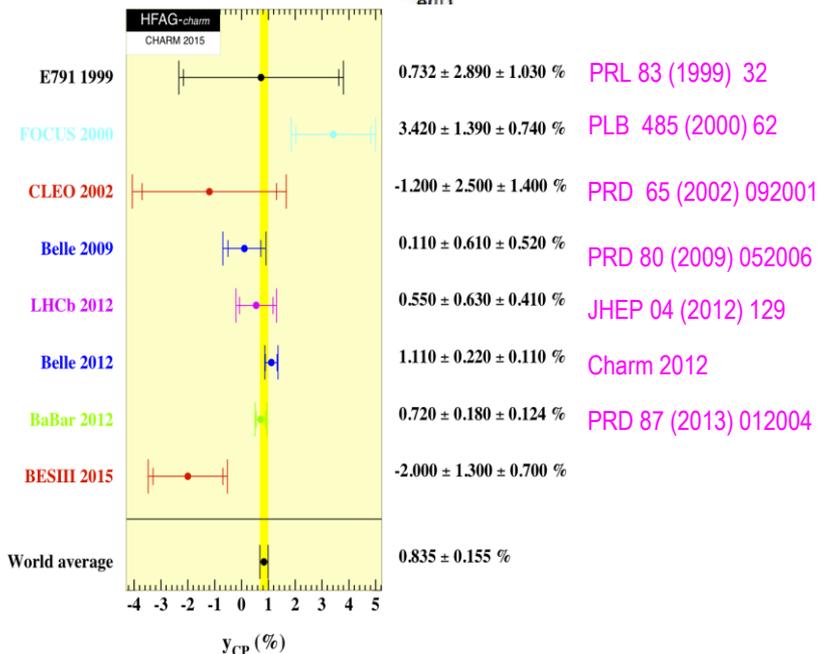
Measure y_{CP} using CP-tagged semi-leptonic D decay

- Single Tag : 3 modes from CP+ and CP-
- Double Tag : CP Tag + Semi-leptonic D

Type	Mode
CP+	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0$
CP-	$K_S^0\pi^0, K_S^0\omega, K_S^0\eta$
Semileptonic	$K^\mp e^\pm\nu, K^\mp \mu^\pm\nu$

- Branching fraction measurement

$$B_{D_{CP^\mp} \rightarrow l} = \frac{N_{CP^\pm;l}}{N_{CP^\pm}} \cdot \frac{\epsilon_{CP^\pm}}{\epsilon_{CP^\pm;l}}$$



BESIII Results

$$y_{CP} = (-2.0 \pm 1.3 \pm 0.7)\%$$

- Compatible with previous measurement
- Statistically limited, less precise than average
- More data may help

CKM direct Measurement

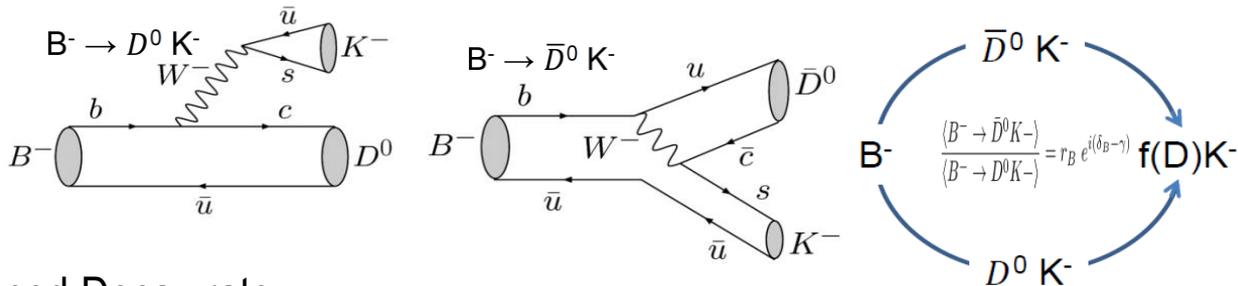
$$\alpha/\phi_2 = (87.6^{+3.5}_{-3.3})^\circ$$

$$\beta/\phi_1 = (21.85^{+0.68}_{-0.67})^\circ$$

$$\gamma/\phi_3 = (73.2^{+6.3}_{-7.0})^\circ$$

Least precisely measure angle

The most sensitive method to constrain γ/ϕ_3 nowadays
 Determine γ/ϕ_3 through the measurement of the interference between $b \rightarrow c$ and $b \rightarrow u$ transitions when D^0 and \bar{D}^0 both decay to the same final state $f(D)$



Binned Decay rate :

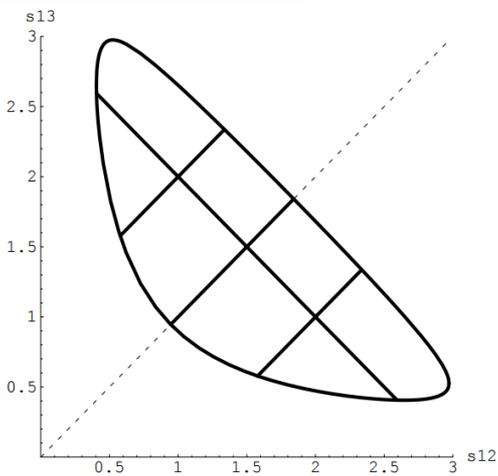
$$\Gamma(B^\pm \rightarrow \bar{D}(K_S \pi^+ \pi^-)K^\pm)_i = T_i + r_B^2 T_{\bar{i}} + 2r_B \sqrt{T_i T_{\bar{i}}} \cos(\delta_B \pm \gamma - \Delta\delta_D)$$

$$= T_i + r_B^2 T_{\bar{i}} + 2r_B \sqrt{T_i T_{\bar{i}}} \{c_i \cos(\delta_B \pm \gamma) + s_i \sin(\delta_B \pm \gamma)\}$$

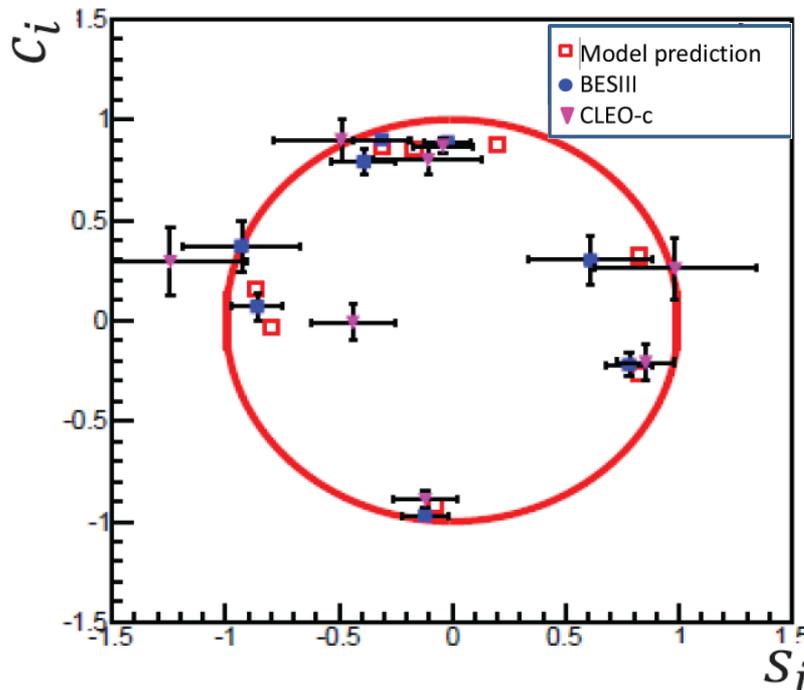
- T_i : Bin yield measured in flavor decays
- r_B : color suppression factor ~ 0.1
- δ_B : strong phase of B decay
- c_i, s_i : weighted average of $\cos(\Delta\delta_D)$ and $\sin(\Delta\delta_D)$ respectively where $\Delta\delta_D$ is the difference between phase of D^0 and \bar{D}^0

Measured at B-Factories

Through $D^0 \rightarrow K_S \pi^+ \pi^-$ analysis



Mirrored binning over $x=y$ makes it so $c_i = c_{\bar{i}}$ and $s_i = -s_{\bar{i}}$



BESIII 2.9 fb⁻¹ ψ'' data

$D^0 \rightarrow K_S \pi^+ \pi^-$

- Still statistical limited, only Statistical errors are shown
- Consistent with CLEO-c measurements, but superior in statistical errors

- The reduction in c_i, s_i contribution to the uncertainty in γ/ϕ_3 of $\sim 40\%$ ($\sim 80\%$ for 20fb⁻¹ data)

BELLE, Model-Independent Dalitz,
PRD 85, 112014 (2012)

$$\gamma/\phi_3 = (77.3_{-14.9}^{+15.1}(\text{stat.}) \pm 4.1(\text{syst.}) \pm 4.3(c_i/s_i))^{\circ}$$

$$\downarrow$$

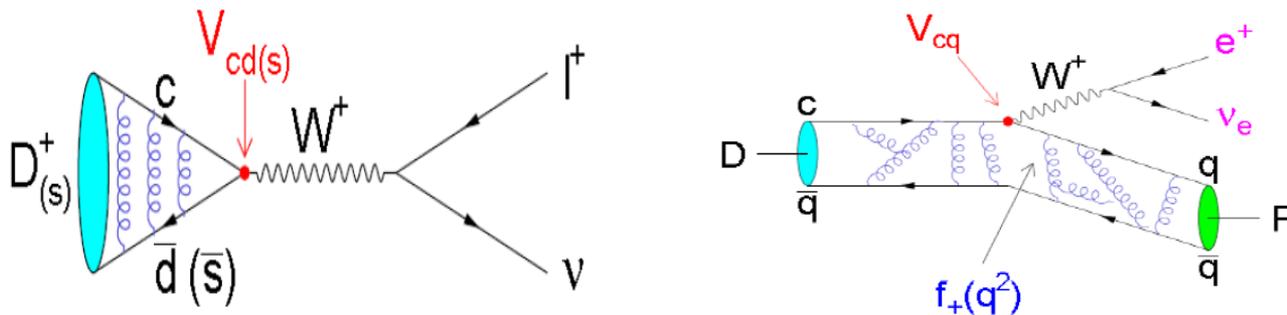
$$\pm 2.5(0.9)(c_i/s_i)$$

- Crucial inputs for the future analysis carried out in the LHCb and BELLE II experiment (stat. sensitivity reaches 1~2%)



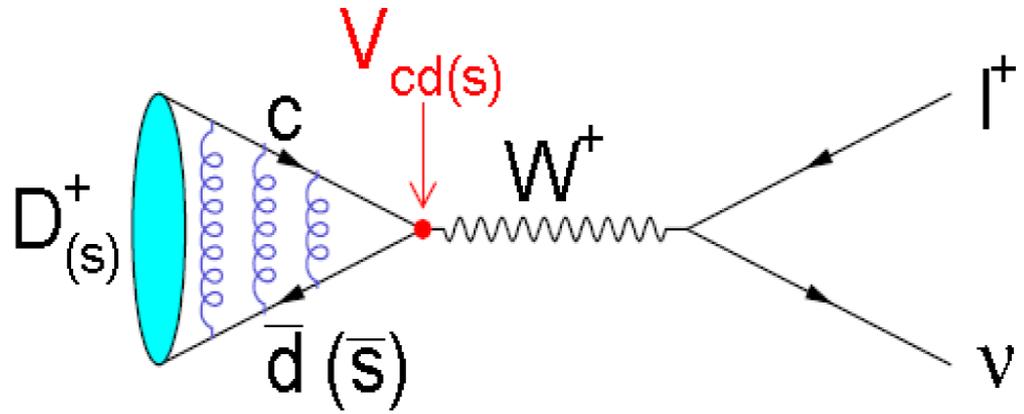
(Semi-) Leptonic Decay

D leptonic and semi-lepton decay are ideal window to probe for weak and strong effects



- In CKM, the uncertainty is dominated by the uncertainty of $f_{B(s)}$ and $f_+^{b \rightarrow \pi}(q^2)$ of B meson calculated in LQCD
- Precision measurement of (semi-) leptonic decay rates can be used to validate $f_{D(s)+}$ and $f_+^{D \rightarrow K(\pi)}(q^2)$ calculated in LQCD, and then improve LQCD calculation of $f_{B(s)}$ and $f_+^{b \rightarrow \pi}(q^2)$ for B meson.
- Recent improved LQCD calculation on $f_{D(s)+}$ (0.5%) and $f_+^{D \rightarrow K(\pi)}(q^2)$ (1.7%, 4.4%) provide good chance to constrain the CKM matrix element $|V_{cs(d)}|$, test the unitarity of CKM and search for NP

D⁺_(s) Leptonic Decay



In SM :
$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

Bridge to precisely measure :

- Decay constants $f_{D_{(s)}^+}$ with input $|V_{cd(s)}|$ of CKMfit
- CKM matrix element $|V_{cd(s)}|$ with input $f_{D_{(s)}^+}$ from LQCD

Search for new physics

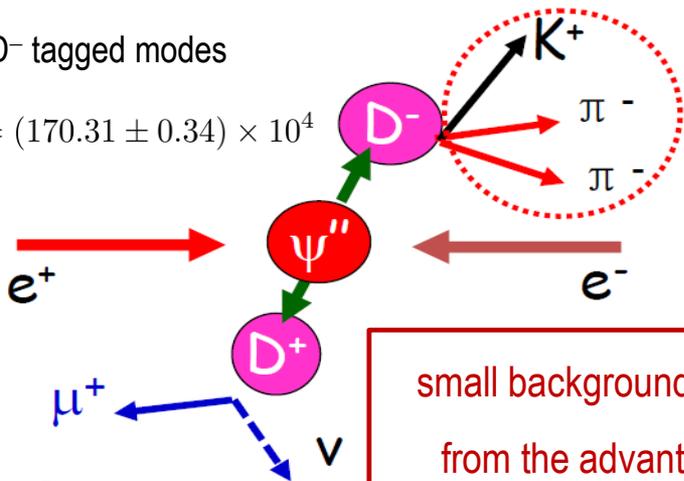
D⁺ Leptonic Decay

$$e^+e^- \rightarrow \psi'' \rightarrow D^+D^-$$

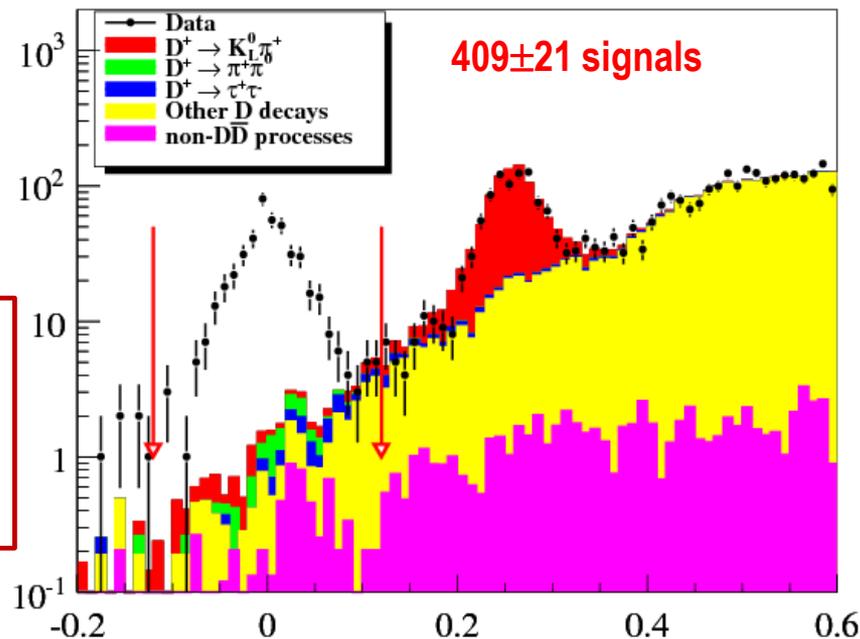
BESIII 2.9 fb⁻¹ ψ'' data PRD 89 (2014) 051104

9 D⁻ tagged modes

$$N_{D_{tag}^-} = (170.31 \pm 0.34) \times 10^4$$



small background benefit
from the advantage of
threshold production



$$B(D^+ \rightarrow \mu^+\nu) = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

|V_{cd}| of CKM-Fitter

Others from PDG

f_{D⁺} of LQCD

Most precise measurement,

but statistical uncertainty dominant

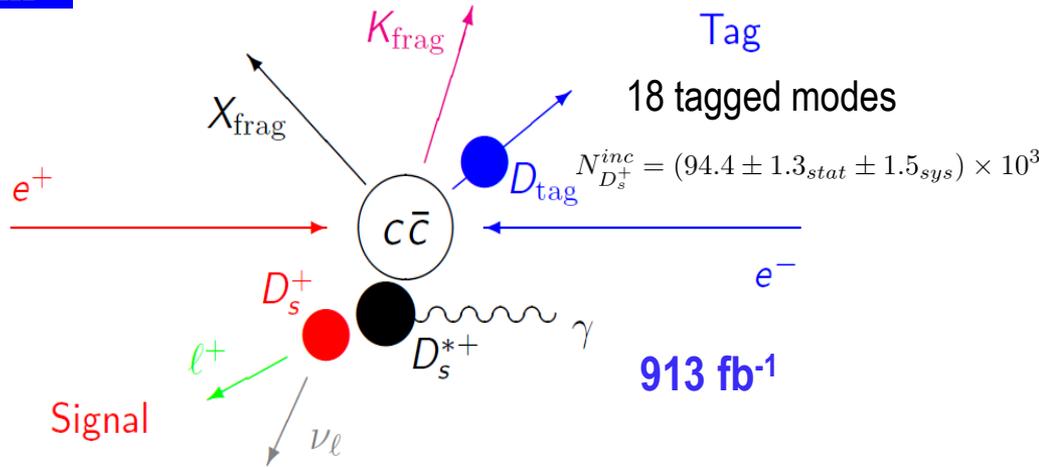
$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

D_s^+ Leptonic Decay



$$e^+e^- \rightarrow c\bar{c} \rightarrow D_{tag}K_{frag}X_{frag}D_s^{*+}, D_s^{*+} \rightarrow D_s^+\gamma$$

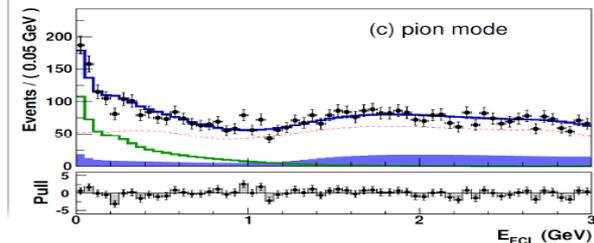
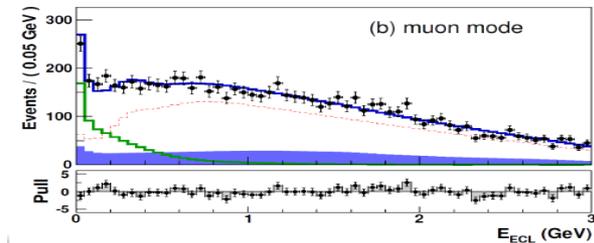
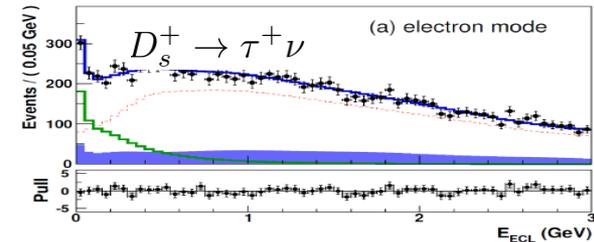
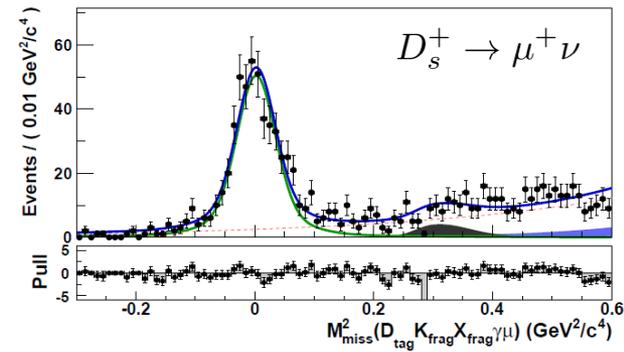


JHEP 1309 (2013) 139

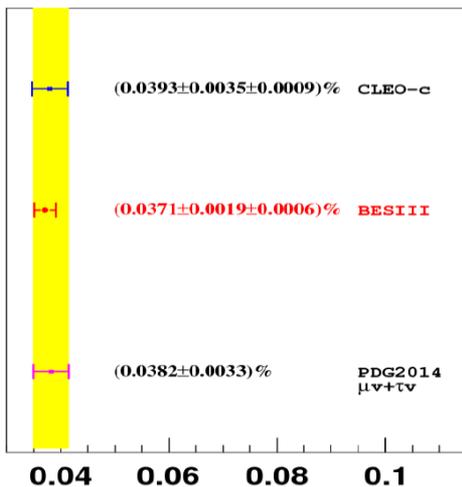
$$B(D_s^+ \rightarrow \mu^+ \nu_\mu) = (0.531 \pm 0.028 \pm 0.020)\%$$

$$B(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.70 \pm 0.21 \pm_{-0.30}^{+0.31})\%$$

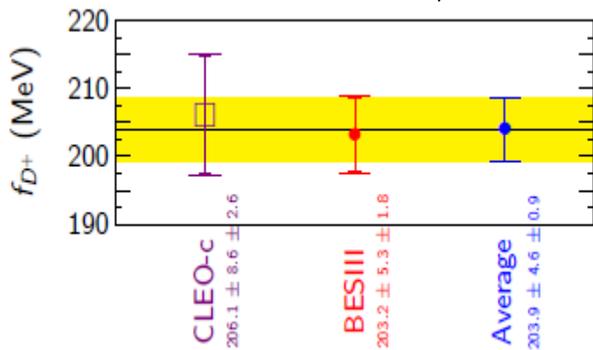
$D_s^+ \rightarrow l^+ \nu_l$	$f_{D_s^+}$ (MeV)
$\mu^+ \nu_\mu$	$249.8 \pm 6.6(\text{stat.}) \pm 4.7(\text{syst.}) \pm 1.7(\tau_{D_s})$
$\tau^+ \nu_\tau$	$261.9 \pm 4.9(\text{stat.}) \pm 7.0(\text{syst.}) \pm 1.8(\tau_{D_s})$
Combination	$255.5 \pm 4.2(\text{stat.}) \pm 4.8(\text{syst.}) \pm 1.8(\tau_{D_s})$



Comparison BR and $f_{D(s)^+}$

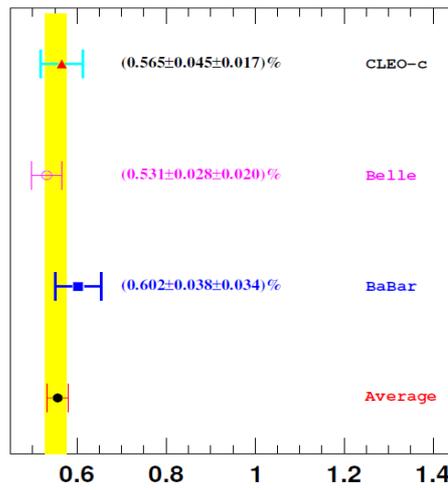


$B(D^+ \rightarrow \mu^+ \nu_\mu)$ (%)

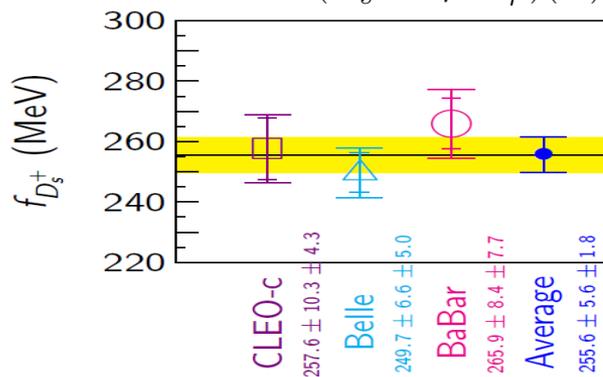


BESIII : 2.7% with 2.92fb^{-1}

Expected: 1.5% with 10fb^{-1}

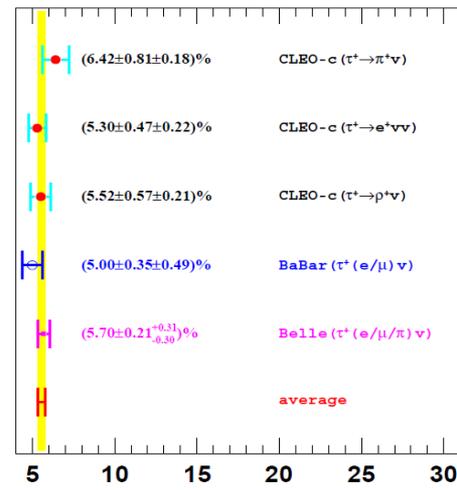


$B(D_s^+ \rightarrow \mu^+ \nu_\mu)$ (%)

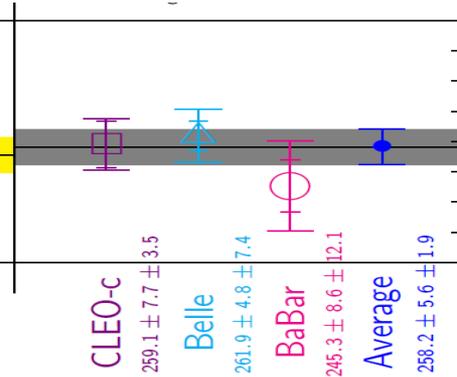


CLEO-c : 2.5% with 0.68fb^{-1}

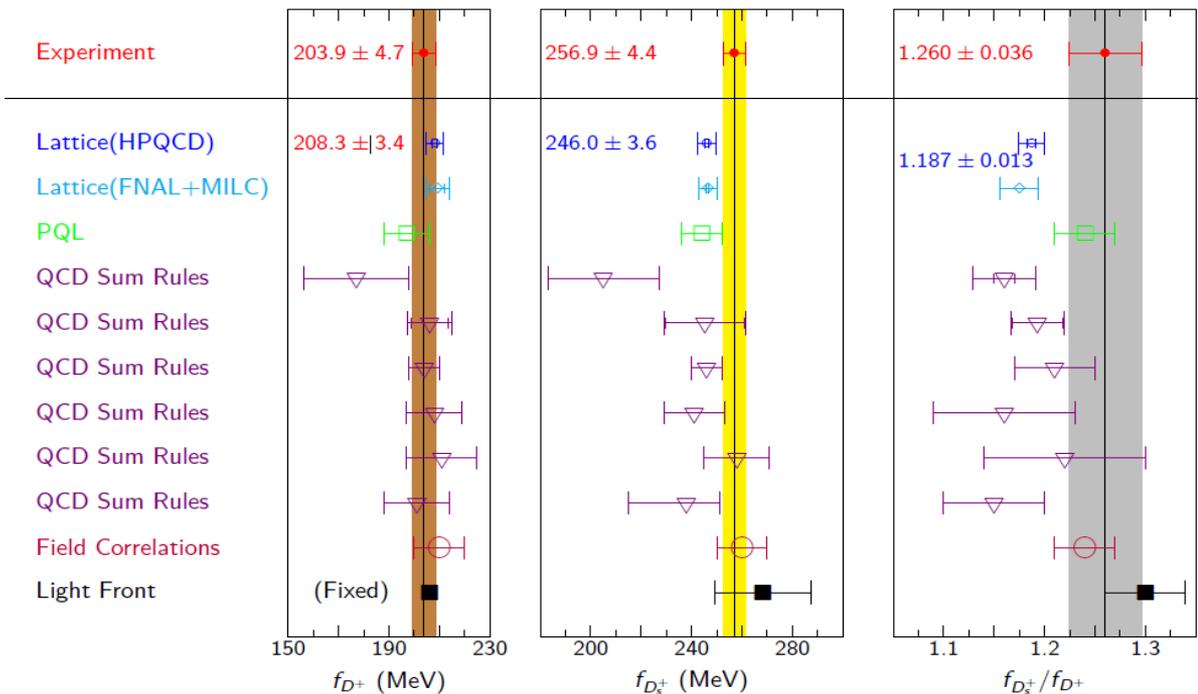
BESIII expected: 1.25% with 5fb^{-1}



$B(D_s^+ \rightarrow \tau^+ \nu_\tau)$ (%)



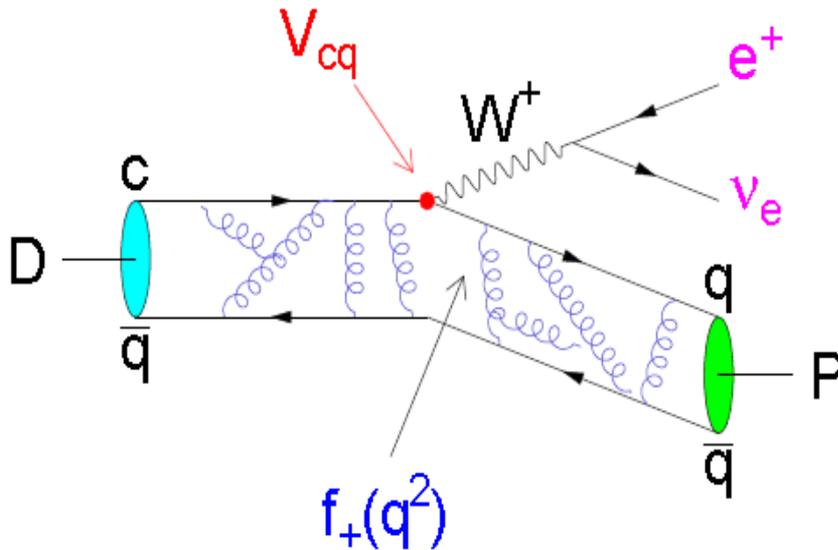
The plots taken from Gang's talk at CMK2014



- The experiment have worse precision
- Precision of the LQCD calculation of f_{D^+} , $f_{D_s^+}$, $f_{D^+}/f_{D_s^+}$ reach $\sim 0.5\%$, are really challenging the experiments
- The experimental measured and the LQCD calculation different by $\sim 2\sigma$ for $f_{D^+}/f_{D_s^+}$
- Improving measurement with larger data samples is expected

	Experiments	Femilab Lattice+MILC (2014)	HPQCD (2012)
	Averaged	Expected	Expected
f_{D^+} (MeV)	203.9 ± 4.7	$212.6 \pm 0.4^{+1.0}_{-1.2}$	208.3 ± 3.4
$f_{D_s^+}$ (MeV)	256.9 ± 4.4	$249.0 \pm 0.3^{+1.1}_{-1.5}$	246.0 ± 3.6
$f_{D^+}/f_{D_s^+}$	1.260 ± 0.036	$1.1712 \pm 0.0010^{+0.0029}_{-0.0032}$	1.187 ± 0.013

D Semi-leptonic Decay



In SM, the differential rates :

$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

Bridge to precisely measure :

- Form factors $f_{+}^{D \rightarrow K(\pi)}(q^2)$ with input $|V_{cd(s)}|$ of CKMfit
 - Validate $f_{+}^{K(\pi)}(q^2)$ calculated in LQCD
 - Improve $f_{+}^{B \rightarrow \pi}(0)$ calculated in LQCD, then improve $|V_{ub}|$
 - Improve the precision of the unitarity triangle
- CKM matrix element $|V_{cd(s)}|$ with input $f_{+}^{D \rightarrow K(\pi)}(0)$ from LQCD

Different FF parameterization

Simple Pole Model	$f_+(q^2) = \frac{f_+(0)}{(1 - q^2/M_{\text{pole}}^2)}$
Modified Pole Model	$f_+(q^2) = \frac{f_+(0)}{(1 - q^2/M_{\text{pole}}^2)(1 - \alpha q^2/M_{\text{pole}}^2)}$
ISGW2 Model	$f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r^2}{12} (q_{\text{max}}^2 - q^2)\right)^{-2}$
Series Expansion	$f_+(q^2) = \frac{1}{P(q^2)\Phi(q^2, t_0)} \sum_{k=0}^{\infty} a_k(t_0) [z(q^2, t_0)]^k$

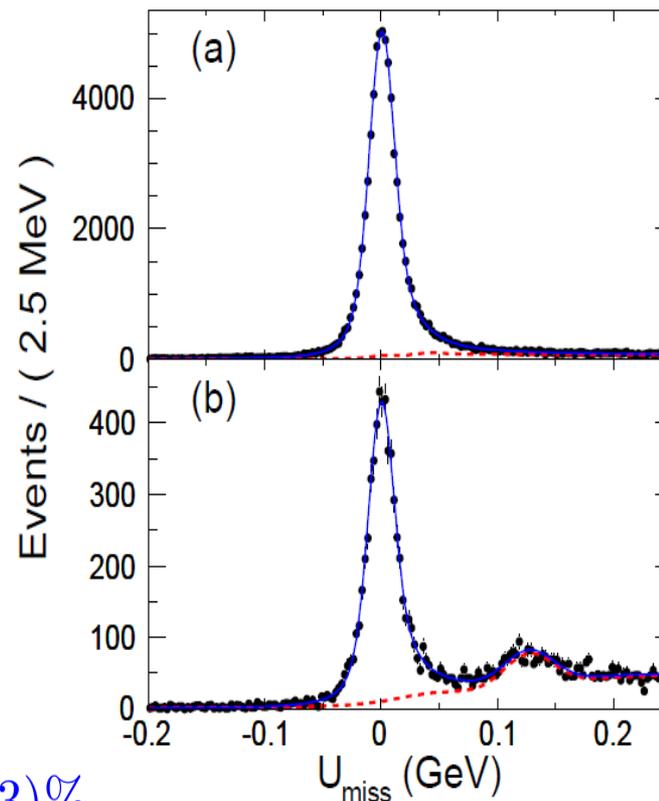
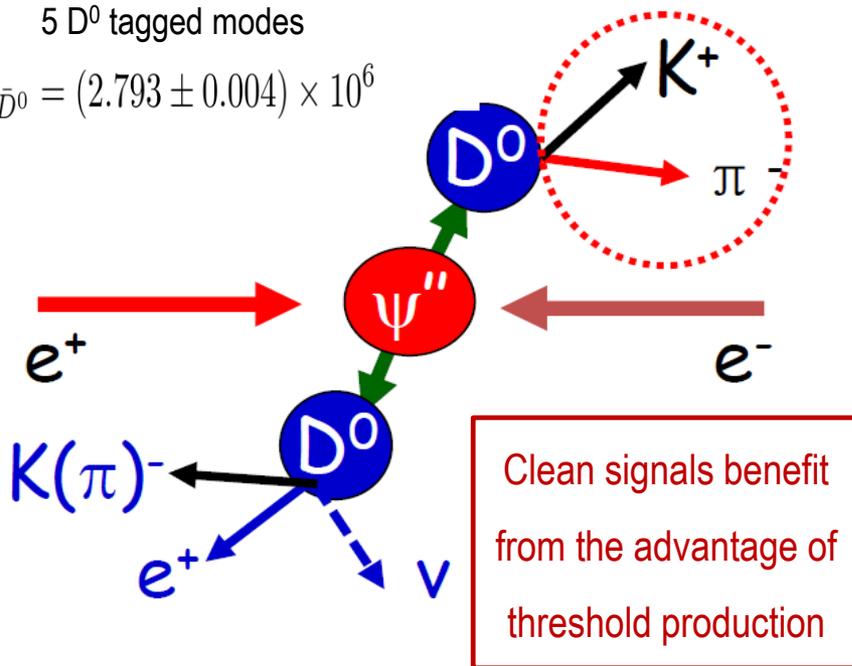
$D^0 \rightarrow K(\pi)^- e^+ \nu_e$ Decay @ BESIII

$$e^+ e^- \rightarrow \psi'' \rightarrow D^0 \bar{D}^0$$

BESIII 2.9 fb⁻¹ ψ'' data [arXiv:1508.07560](https://arxiv.org/abs/1508.07560)

5 D^0 tagged modes

$$N_{\bar{D}^0} = (2.793 \pm 0.004) \times 10^6$$

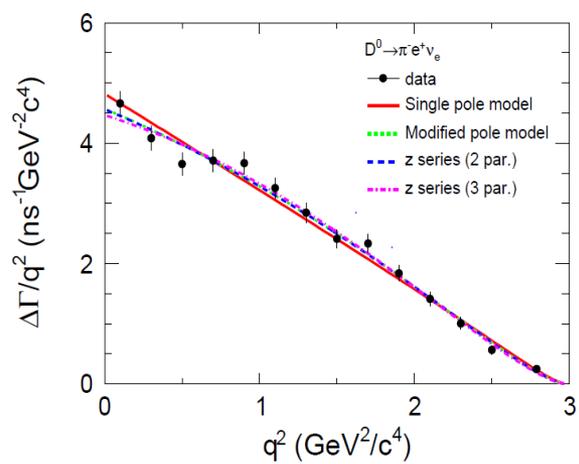
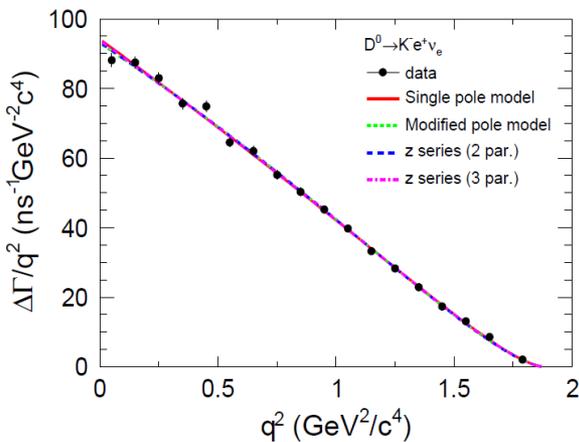


$$B(D^0 \rightarrow K^- e^+ \nu_e) = (3.505 \pm 0.014 \pm 0.033)\%$$

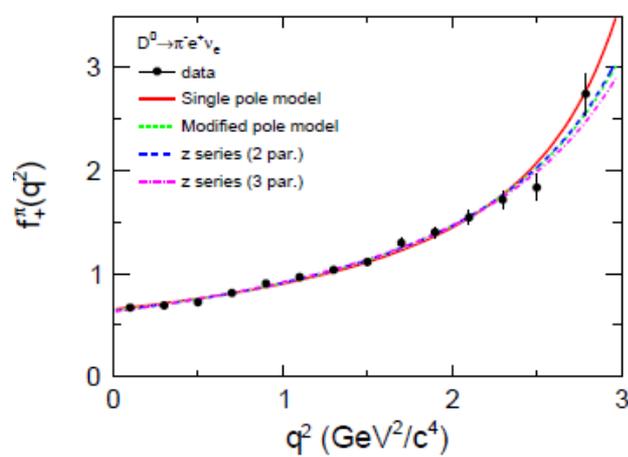
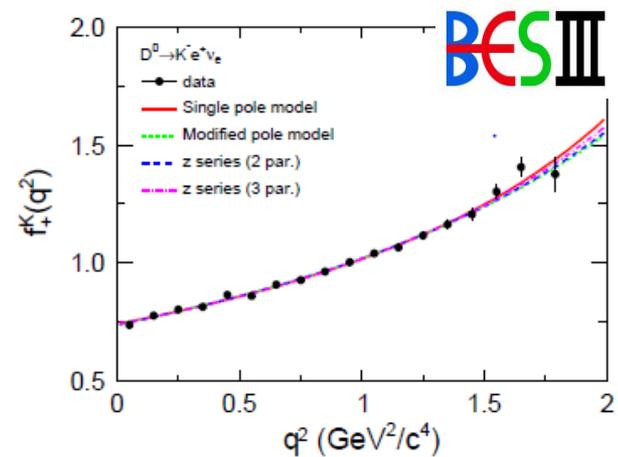
$$B(D^0 \rightarrow \pi^- e^+ \nu_e) = (0.295 \pm 0.004 \pm 0.003)\%$$

Most precise measurements

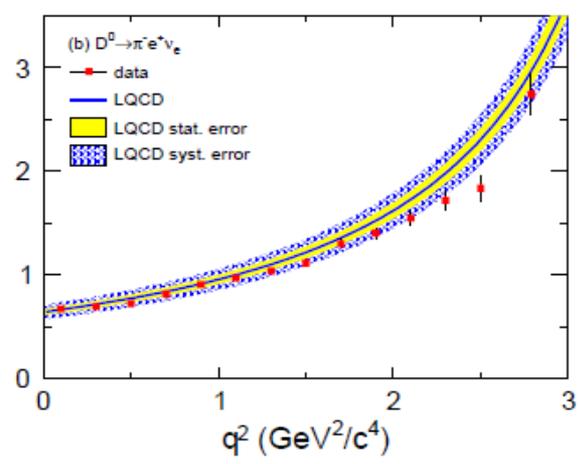
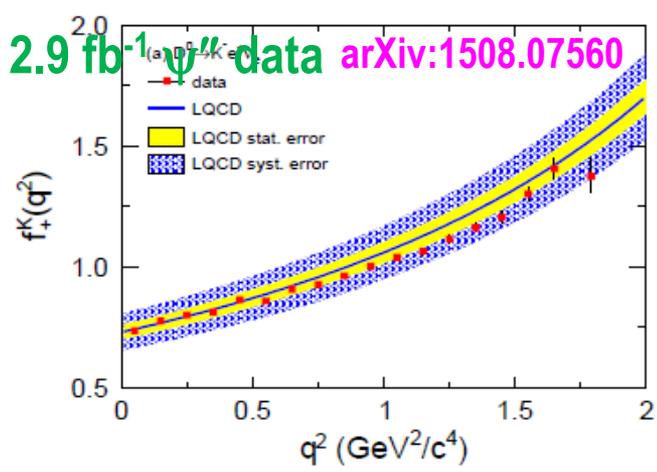
Measurement of $f_+^{K(\pi)}(q^2)$



Fit with different FF parameterization

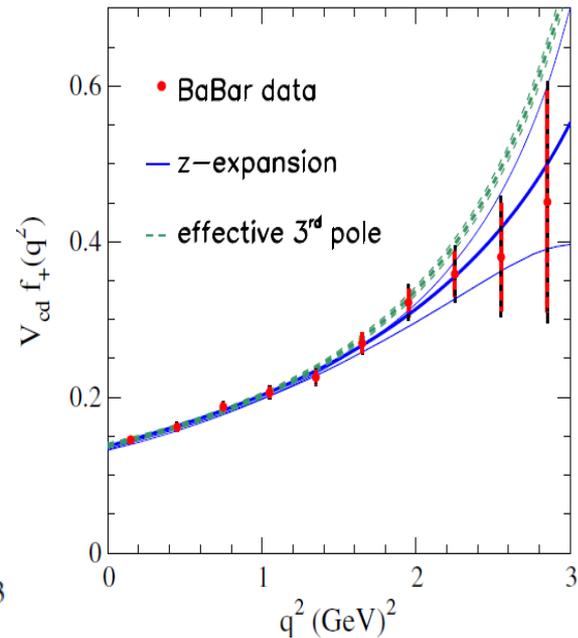
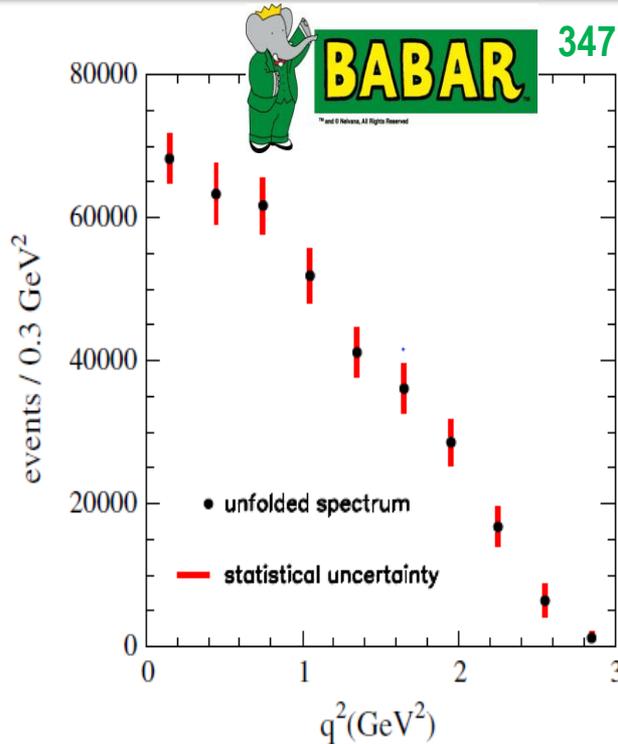
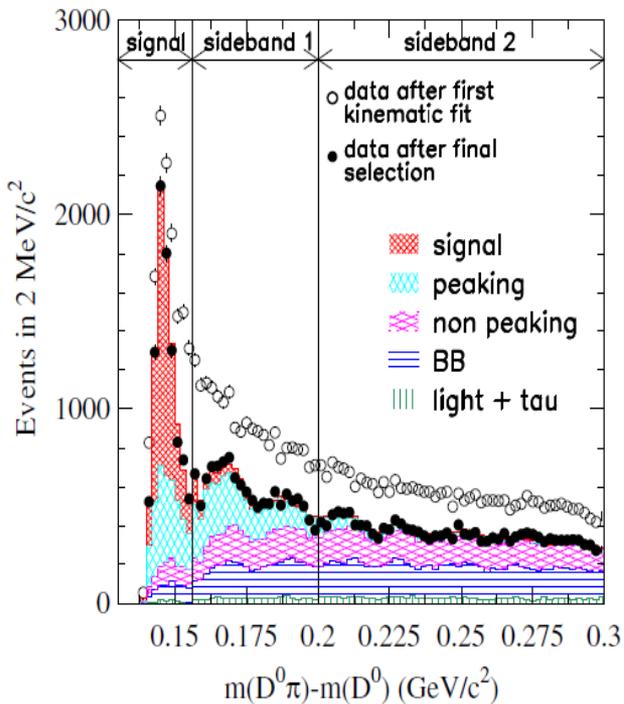


Projection on FF with $|V_{cd(s)}|$ from CKMfiter



Comparisons of measured FF with LQCD predictions

$D^0 \rightarrow \pi^- e^+ \nu_e$ Decay @ BABAR



$$B(D^0 \rightarrow \pi^- e^+ \nu_e) = (0.2770 \pm 0.0068_{stat} \pm 0.0092_{syst} \pm 0.0037_{ext})\%$$

LQCD calculation

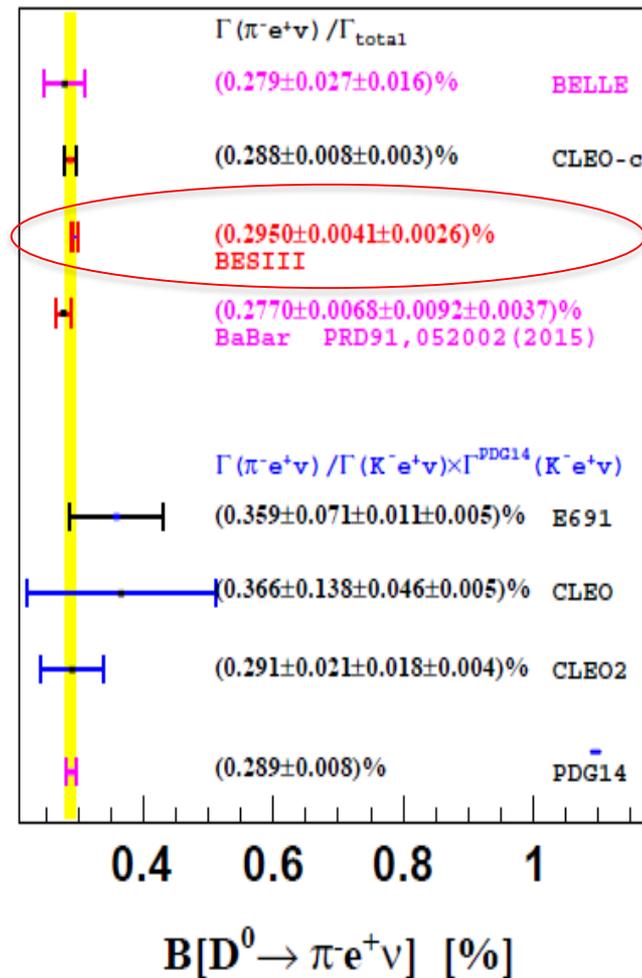
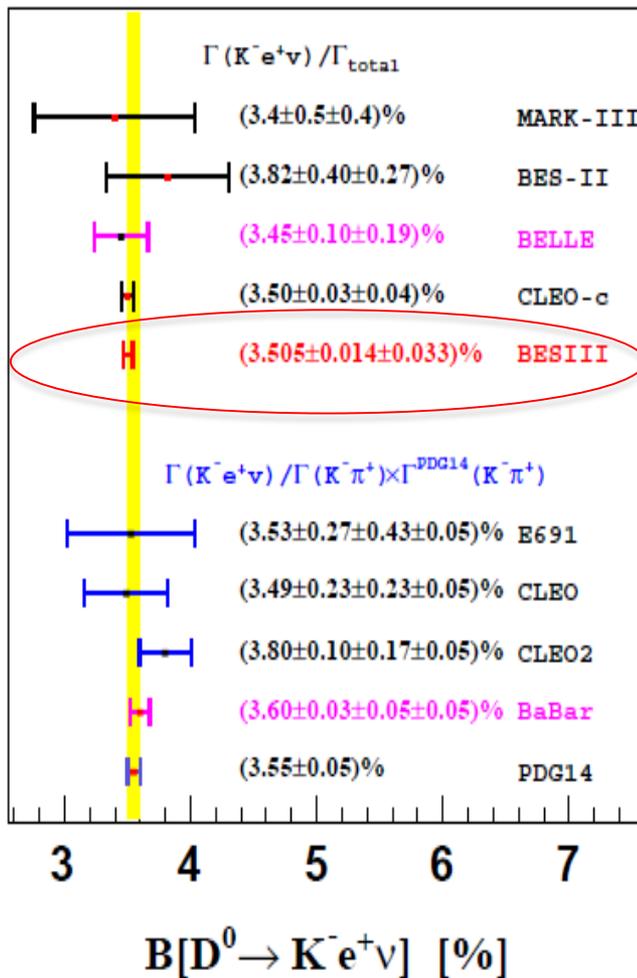
$$f_+^\pi(0) = 0.610 \pm 0.029_{exp}$$

$$|V_{cd}| = |V_{us}| = 0.2252 \pm 0.0009$$

$$|V_{cd}| = 0.206 \pm 0.007_{exp} \pm 0.009_{LQCD}$$

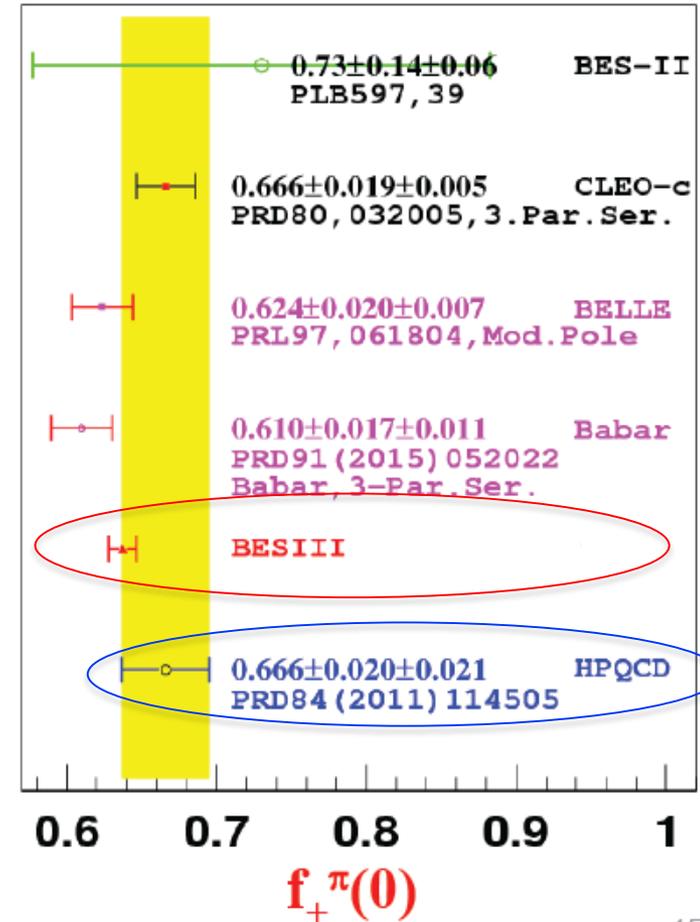
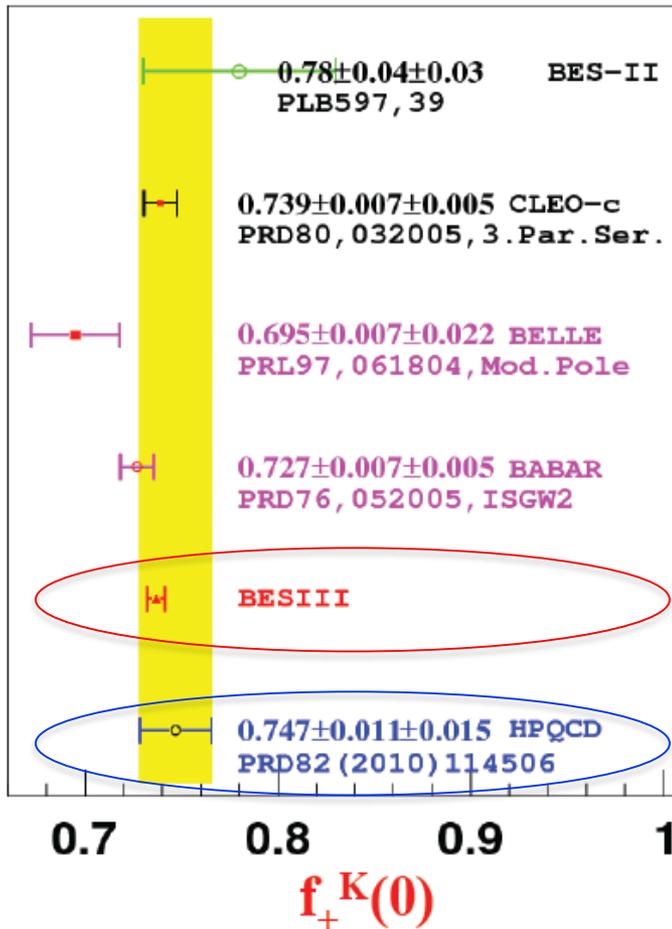
$$f_+^\pi(0) = 0.610 \pm 0.020_{exp} \pm 0.005_{ext}$$

Comparisons of BR



BESIII experiment achieved most precise measurement.

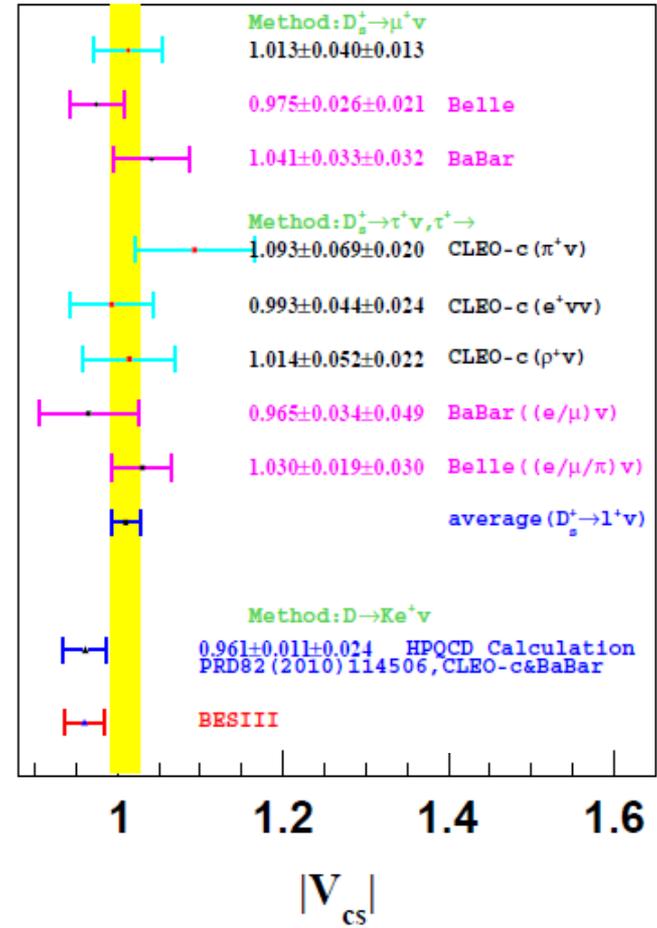
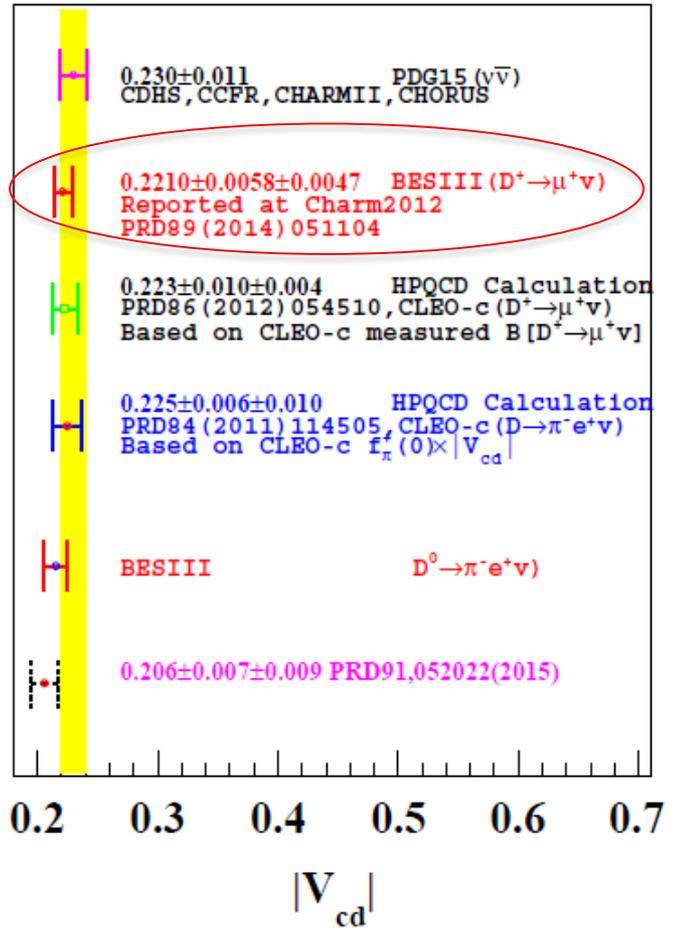
Comparisons of FF



15

- BESIII experiment achieved most precise measurement.
- The experimental accuracy is better than that of theoretical predictions

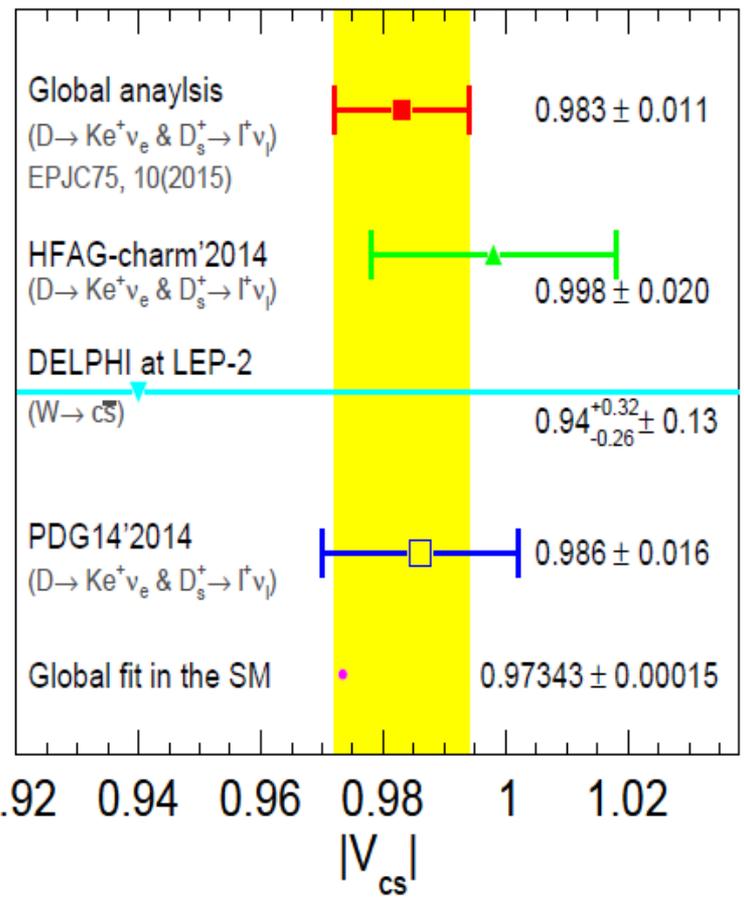
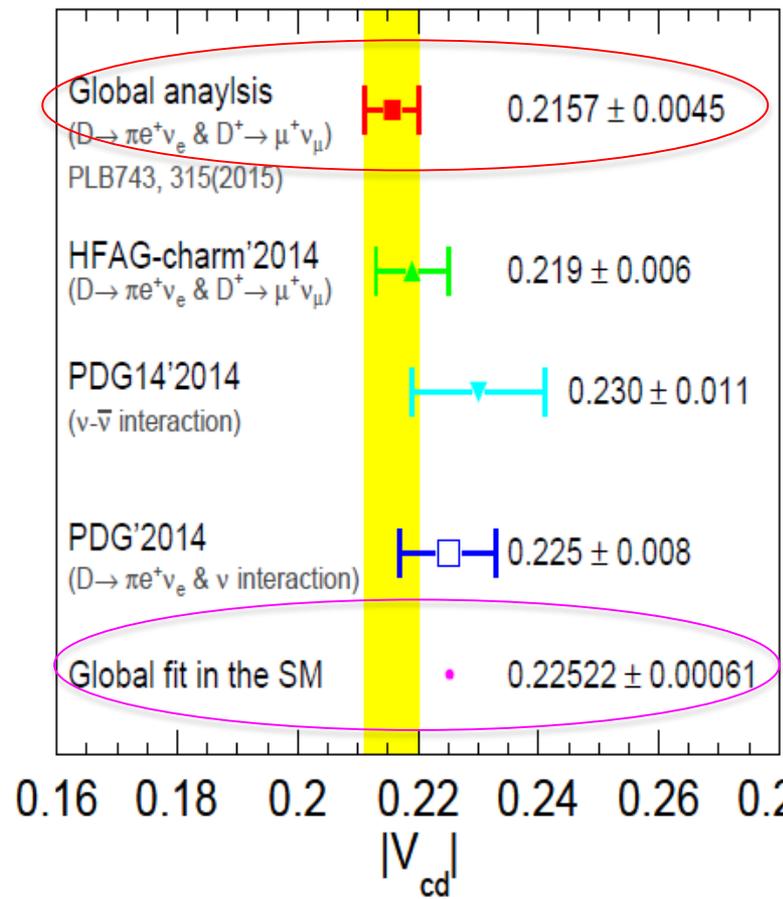
Extraction of $|V_{cd}|$ and $|V_{cs}|$



BES used the leptonic $D^+ \rightarrow \mu^+ \nu_{\mu}$ to extract the $|V_{cd}|$ for the first time

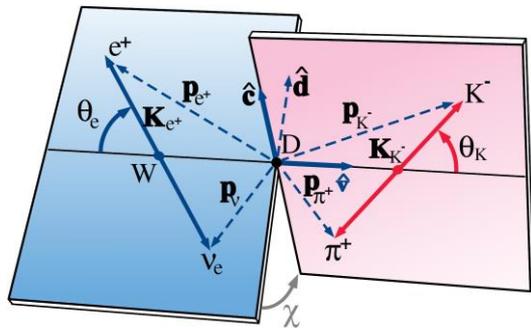
The accuracy is better than that of PDG2015 average from $\nu\nu$ interactions

Comparisons of $|V_{cd}|$ and $|V_{cs}|$



Comparison between the PDG 2014, HFAG-Charm 2014, Global analysis and Global fit in SM
 The values from the global analysis deviates from that obtained from the SM global fit by 2.1σ

Semileptonic $D \rightarrow V \ell^+ \nu_\ell$ Decay



- $m^2 = (p_{\pi^+} + p_{K^-})^2$
- $\cos(\theta_K) = \frac{\hat{\nu} \cdot \mathbf{K}_{K^-}}{|\mathbf{K}_{K^-}|}$
- $\cos(\chi) = \hat{\mathbf{c}} \cdot \hat{\mathbf{d}}$
- $q^2 = (p_{e^+} + p_{\nu_e})^2$
- $\cos(\theta_e) = -\frac{\hat{\nu} \cdot \mathbf{K}_{e^+}}{|\mathbf{K}_{e^+}|}$
- $\sin(\chi) = (\hat{\mathbf{c}} \times \hat{\nu}) \cdot \hat{\mathbf{d}}$

Decay rates depend on 5 variables and 3 form factors

$$d^5\Gamma = \frac{G_F^2 |V_{cs}|^2}{(4\pi)^6 m_D^2} X \beta \mathcal{I}(m^2, q^2, \theta_K, \theta_e, \chi) dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi$$

- $X = p_{K\pi} m_D$, $p_{K\pi}$ is the momentum of the $K\pi$ system in the D rest frame
- $\beta = 2p^*/m$, p^* is the breakup momentum of the $K\pi$ system in its rest frame
- \mathcal{I} can be expressed in terms of helicity amplitudes $H_{0,\pm}$:

$$H_0(q^2) = \frac{1}{2m_q} \left[(m_D^2 - m^2 - q^2)(m_D + m) A_1(q^2) - 4 \frac{m_D^2 p_{K\pi}^2}{m_D + m} A_2(q^2) \right]$$

$$H_{\pm}(q^2) = (m_D + m) A_1(q^2) \mp \frac{2m_D p_{K\pi}}{m_D + m} V(q^2)$$

- Vector form factor: $V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}$; or: FF ratio $r_V = V(0)/A_1(0)$
- Axial-vector form factor: $A_1(q^2) = \frac{A_1(0)}{1 - q^2/m_A^2}$, $A_2(q^2) = \frac{A_2(0)}{1 - q^2/m_A^2}$; or: FF ratio $r_2 = A_2(0)/A_1(0)$

- BESIII : 2.92fb^{-1} , PWA of $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$,

Preliminary results, see Fenfen's talk at CHARM 2015

- BESIII : 2.92fb^{-1} , Study of $D^+ \rightarrow \omega/\phi e^+ \nu_e$,

ArXiv:1508.00151

- CLEO-C : 818pb^{-1} , $D^0 \rightarrow \rho^- l^+ \nu_l$, $D^+ \rightarrow \rho^0/\omega l^+ \nu_l$

PRL 110 (2013) 131802

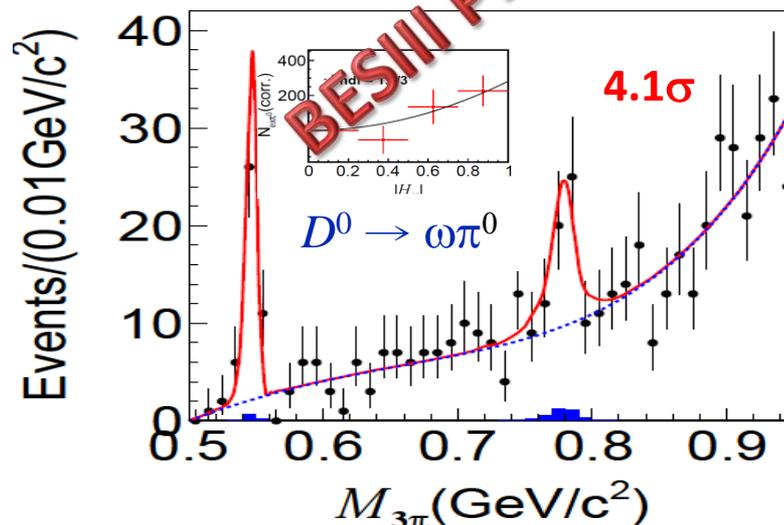
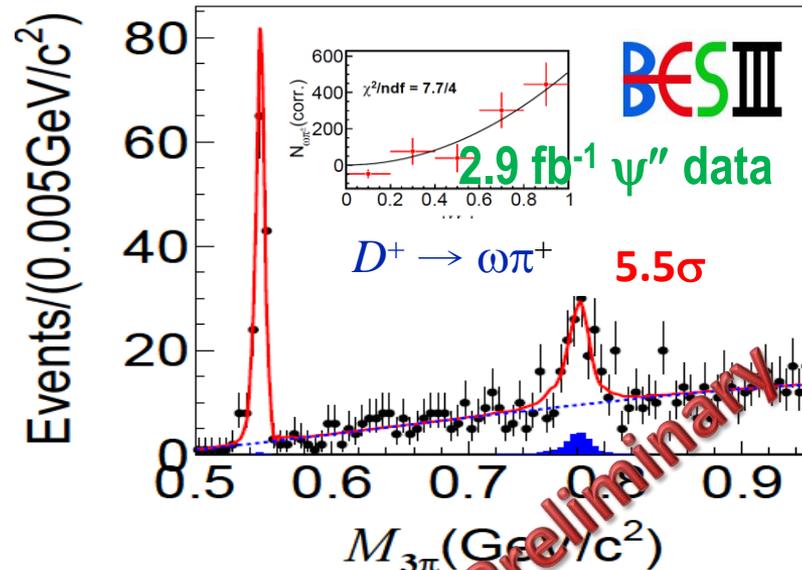


Hadronic Decay

- CLEO-c (281 pb^{-1}) ψ'' data did not observe CSC decay $D^{\pm 0} \rightarrow \omega \pi^{\pm 0}$ [PRL 96, 081802 (2006)]
- Theory predicts $D^{\pm 0} \rightarrow \omega \pi^{\pm 0} \sim 1.0 \times 10^{-4}$ due to the destructive interference between color-suppressed diagrams [PRD 81, 074021 (2010)]
- **BESIII first observation :**
 - Consistent with theory prediction in BR
 - ω helicity angle $\sim \cos^2\theta$ distribution
 - BR($D \rightarrow \eta \pi$) consistent previous measurement

Decay mode	This work	Previous measurements
$D^+ \rightarrow \omega \pi^+$	$(2.74 \pm 0.58 \pm 0.17) \times 10^{-4}$	$< 3.4 \times 10^{-4}$ at 90% C.L.
$D^0 \rightarrow \omega \pi^0$	$(1.05 \pm 0.41 \pm 0.09) \times 10^{-4}$	$< 2.6 \times 10^{-4}$ at 90% C.L.
$D^+ \rightarrow \eta \pi^+$	$(3.13 \pm 0.22 \pm 0.19) \times 10^{-3}$	$(3.53 \pm 0.21) \times 10^{-3}$
$D^0 \rightarrow \eta \pi^0$	$(0.67 \pm 0.10 \pm 0.05) \times 10^{-3}$	$(0.68 \pm 0.07) \times 10^{-3}$

See Peter's talk at CHARM2015 for details





Absolute BR of Λ_c^+ hadron decays



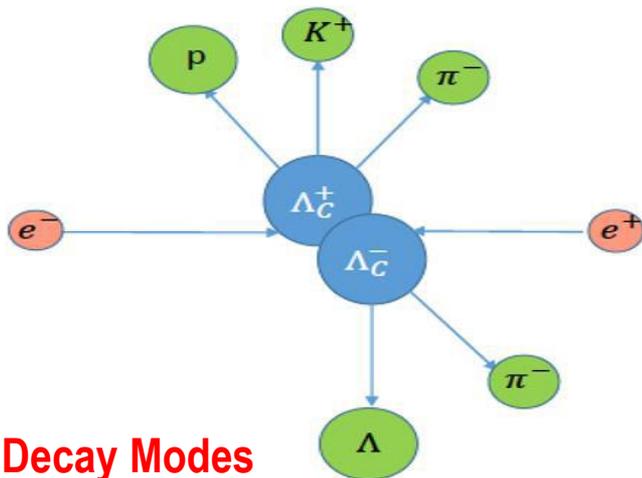
- **Absolute branching fraction of Λ_c^+ are not well determined since its discovery**
 - BFs of $\sim 85\%$ decay modes are measured relative to $\Lambda_c^+ \rightarrow pK^-\pi^+$
 - However, no completely model-independent measurements of the absolute BF of $\Lambda_c^+ \rightarrow pK^-\pi^+$ (from Argus and CLEO very old results)
 - The uncertainties of BFs of Λ_c^+ decays are 25%~40% in PDG2014
- **Until Belle's first "model-independent" measurement:**
 - $B(\Lambda_c^+ \rightarrow pK^-\pi^+) = (6.84 \pm 0.24 - 0.27 + 0.21)\%$ precision reaches to 4.7% [PRL 113 (2014) 042002]
- **Measurement using the threshold pair-productions via e^+e^- annihilations**
 $(e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-)$ is unique: the most simple and straightforward
 - BESIII preliminary analysis based on 567pb^{-1} data @ 4.6GeV
 - Kinematics does not allow additional particles, clean
 - Fully reconstruct the pairs and double tagged method

Absolute BR of Λ_c^+ hadron decays

BESIII 567 pb⁻¹ @ 4.6 GeV

See Xiaorui's talk at CHARM2015 for detail

A least square global fitter [CPC 37, 106201 (2013)]



12 Decay Modes

Mode
pK_S^0
$pK^- \pi^+$
$pK_S^0 \pi^0$
$pK_S^0 \pi^+ \pi^-$
$pK^- \pi^+ \pi^0$
$\Lambda \pi^+$
$\Lambda \pi^+ \pi^0$
$\Lambda \pi^+ \pi^- \pi^+$
$\Sigma^0 \pi^+$
$\Sigma^+ \pi^0$
$\Sigma^+ \pi^+ \pi^-$
$\Sigma^+ \omega$

BESIII Preliminary

Decay modes	Global fit \mathcal{B}	PDG \mathcal{B}	Belle \mathcal{B}
pK_S	1.48 ± 0.08	1.15 ± 0.30	
$pK^- \pi^+$	5.77 ± 0.27	5.0 ± 1.3	$6.84 \pm 0.24^{+0.21}_{-0.27}$
$pK_S^0 \pi^0$	1.77 ± 0.12	1.65 ± 0.50	
$pK_S^0 \pi^+ \pi^-$	1.43 ± 0.10	1.30 ± 0.35	
$pK^- \pi^+ \pi^0$	4.25 ± 0.22	3.4 ± 1.0	
$\Lambda \pi^+$	1.20 ± 0.07	1.07 ± 0.28	
$\Lambda \pi^+ \pi^0$	6.70 ± 0.35	3.6 ± 1.3	
$\Lambda \pi^+ \pi^- \pi^+$	3.67 ± 0.23	2.6 ± 0.7	
$\Sigma^0 \pi^+$	1.28 ± 0.08	1.05 ± 0.28	
$\Sigma^+ \pi^0$	1.18 ± 0.11	1.00 ± 0.34	
$\Sigma^+ \pi^+ \pi^-$	3.58 ± 0.22	3.6 ± 1.0	
$\Sigma^+ \omega$	1.47 ± 0.18	2.7 ± 1.0	

Global fit :
Stat. Err. only

- $B(\Lambda_c^+ \rightarrow pK^- \pi^+)$:
 - BESIII have comparable precision of Belle's results, but smaller rate
- Improved precision of the other 11 modes significantly (mostly $\leq 8\%$)

Others Hadronic Decay

**A lot of others progress on multi-body hadronic decay
(Amplitude/Daltiz) analysis (e.g. $D^0 \rightarrow K_S K^+ K^-$, $/K_S K^+ \pi^-$),**

please see the talks :

- Peter Weidenkaff's talk at Charm2015
- Angelo Di Canto's talk at LHCP2015
-



Rare Decay

How rare of rare Charm Decay

Charm provide a unique environment for testing the SM rare/forbidden decays and searching for NP

10⁻⁰
10⁻¹
10⁻²
10⁻³
10⁻⁴
10⁻⁵
10⁻⁶
10⁻⁷
10⁻⁸
10⁻⁹
10⁻¹⁰
10⁻¹¹
10⁻¹²
10⁻¹³
10⁻¹⁴
10⁻¹⁵

Cabibbo favor

Single Cabibbo suppressed

Doubly Cabibbo suppressed

Radiative decays

Long distance:
Vector meson Dominance

Short distance FCNC

Forbidden decays: LNV, LFV, BNV

SM predictions and experimental reaches

$$D^0 \rightarrow K^{*0} \gamma / \phi \gamma / \omega \gamma / \rho \gamma$$

$$D^+_{(s)} \rightarrow K^{*+} \gamma / \rho^+ \gamma$$

CLEO-c

BESIII

BESIII final/B factory

$$D^{0+} \rightarrow \gamma \gamma / V V' (I^+ I^-) / h V (I^+ I^-) / h h' V (I^+ I^-)$$

LHCb

Super-B

Super- τ -charm

$$D^{0+} \rightarrow \gamma \gamma / V I^+ I^- / h I^+ I^- / h h' I^+ I^-$$

$$D^0 \rightarrow \mu^+ \mu^- / e^+ e^-$$

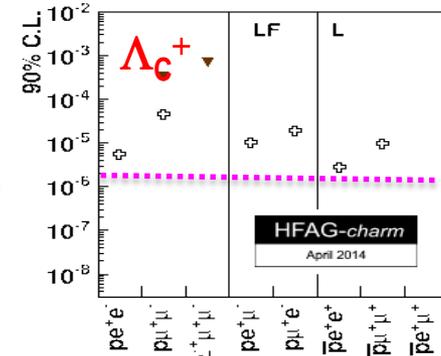
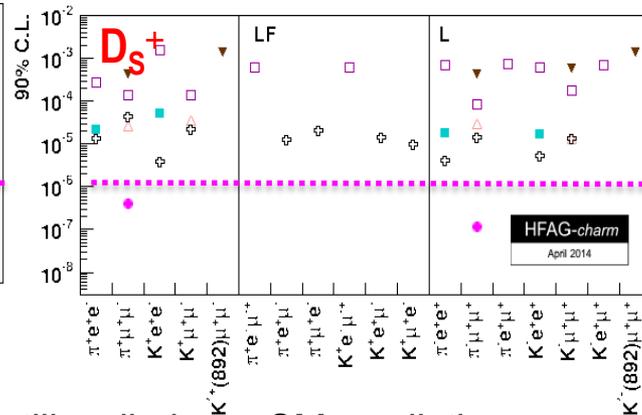
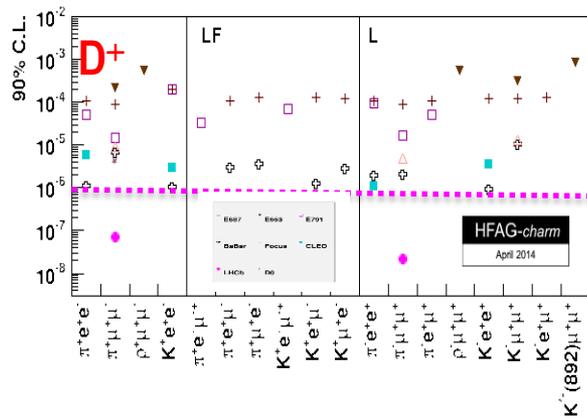
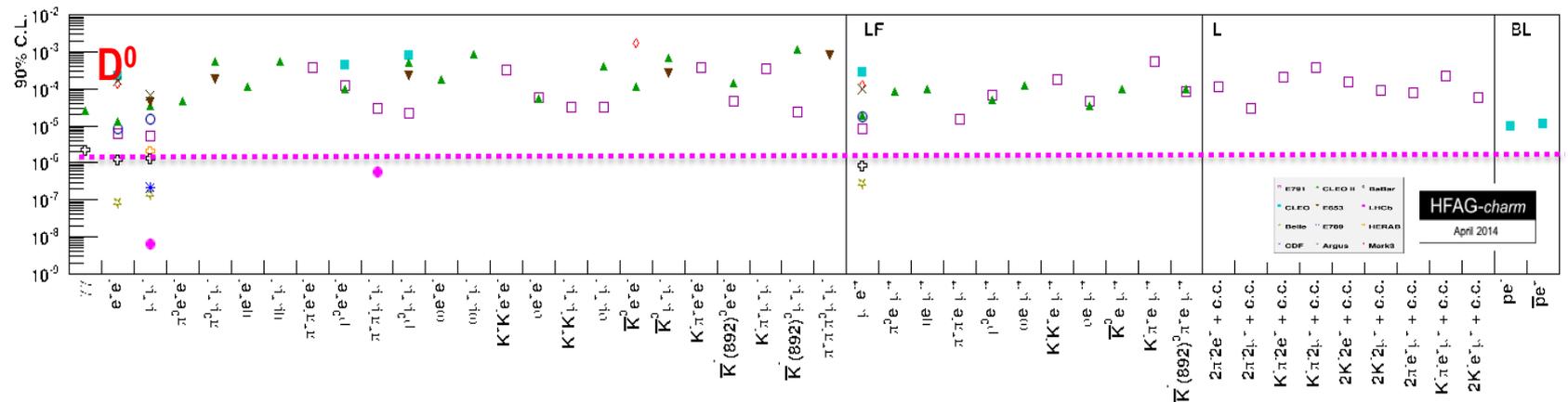
$$D \rightarrow (h h) \mu^+ \mu^- / (h h) e^+ e^-$$

$$D \rightarrow (h) \mu^+ e^-$$

$$D \rightarrow (h) p e^-$$

Charm Rare Decay

HFAG : http://www.slac.stanford.edu/xorg/hfag/charm/April14/Rare/rare_charm.html



- Very few limit below 10^{-6} , are still well above SM prediction
- Many channels studies more than a decade ago
- LHCb shows great potential in several process, (e.g. $D^0 \rightarrow \mu^+ \mu^-$, but still $100 \times \text{SM}$ and $10 \times \text{NP}$)



Summary & Prospects



- Charm physics provide a unique environment for the testing SM and searching from new physics, very broad topics
 - **D^0 - \bar{D}^0 Mixing** : is well established in a single experiment
 - **CPV** : no CPV observed at 10^{-3} level, need more data and new method
 - **Quantum-Correlated @ threshold** : unique input for testing CKM, mixing and searching for CPV
 - **Semilepton decay** : Validate LQCD calculation and improve the CKM matrix elements measurement. LQCD prediction is precise, and challenge experimental measurement.
 - **Hadronic decay** : more precise measurement are necessary
 - **Rare decay** : lots of measurements, but limits are still well above SM prediction



Summary & Prospects



- Results still coming in from Belle with full data set ($\sim 950\text{fb}^{-1}$)
- BESIII team has built and developed technology with charm at threshold, and more and wide results are coming
- LHCb is producing a wide new results, including Dalitz plot/amplitude analyses
- Perspectives :
 - BESIII will continue to run 6-8 years, will continue play role with the data produced at threshold.
 - LHCb runII (2015-2018), 10 times charm data ($2 \times \sigma(cc)_{7\text{TeV}}$, 2×better trigger, 50fb^{-1}) will play the key role for charm in next few years.
 - BELLE-II will collect 50ab^{-1} from e^+e^- collision
 - Super τ -Charm Factory (Russia, China)?

Thanks



Backup Slides



CPV in $D_{(s)}^+ \rightarrow K_S h^+$ @ LHCb



Paras Naik's talk at Charm 2015

JHEP 1410 (2014) 25
3fb⁻¹

- Search for direct CP asymmetry in the **SCS** decays
- Measured asymmetries are affected by other asymmetries

$$\mathcal{A}_{\text{meas}}^{D_{(s)}^\pm \rightarrow K_S^0 h^\pm} \approx \mathcal{A}_{CP}^{D_{(s)}^\pm \rightarrow K_S^0 h^\pm} + \mathcal{A}_{\text{prod}}^{D_{(s)}^\pm} + \mathcal{A}_{\text{det}}^{h^\pm} + \mathcal{A}_{K^0/\bar{K}^0}$$

measure

want

Production asymmetry

f's detection asymmetry

Correction due to CPV in kaon system

- Combine with **CF** decays where CPV is not expected. Take asymmetries to isolate CP asymmetries e.g.

$$\mathcal{A}_{CP}^{D_s^\pm \rightarrow K_S^0 \pi^\pm} = \mathcal{A}_{\text{meas}}^{D_s^\pm \rightarrow K_S^0 \pi^\pm} - \mathcal{A}_{\text{meas}}^{D_s^\pm \rightarrow \phi \pi^\pm} - \mathcal{A}_{K^0}$$

$\mathcal{A}_{K^0} = (+0.07 \pm 0.02)\%$
calculation described in
JHEP 07 (2014) 041

- Results: $\mathcal{A}_{CP}^{D_s^\pm \rightarrow K_S^0 K^\pm} = (+0.03 \pm 0.17 \pm 0.14)\%$

$$\mathcal{A}_{CP}^{D_s^\pm \rightarrow K_S^0 \pi^\pm} = (+0.38 \pm 0.46 \pm 0.17)\%$$



- Can also get a sum of both **SCS** asymmetries using **CF** $D_{(s)}^+ \rightarrow K_S h^+$

$$\mathcal{A}_{CP}^{D_s^\pm \rightarrow K_S^0 K^\pm} + \mathcal{A}_{CP}^{D_s^\pm \rightarrow K_S^0 \pi^\pm} = (+0.41 \pm 0.49 \pm 0.26)\%$$

Paras Naik's talk at Charm 2015

- Search for CPV in the **SCS** decay $D \rightarrow KK\pi\pi$ using triple products

$$C_T = \mathbf{p}_{K^+} \cdot (\mathbf{p}_{\pi^+} \times \mathbf{p}_{\pi^-}) \quad \bar{C}_T = \mathbf{p}_{K^-} \cdot (\mathbf{p}_{\pi^-} \times \mathbf{p}_{\pi^+})$$

- These are non-vanishing since there are four distinct final state particles
- These triple products are odd under T (hence the name "T-odd")
 - We cannot reverse the decay, their P-odd nature is more important
- In the absence of final state interactions (FSI) due to long-distance strong interaction effects, if the number of decays with $C_T < 0$ is different from the number of decays with $C_T > 0$ this implies parity violation.
- We form triple-product asymmetries for both D flavors:

$$A_{C_T} = \frac{\Gamma(C_T > 0) - \Gamma(C_T < 0)}{\Gamma(C_T > 0) + \Gamma(C_T < 0)}, \quad \bar{A}_{\bar{C}_T} = \frac{\Gamma(-\bar{C}_T > 0) - \Gamma(-\bar{C}_T < 0)}{\Gamma(-\bar{C}_T > 0) + \Gamma(-\bar{C}_T < 0)}$$

CKM Fitter 2015 Summer

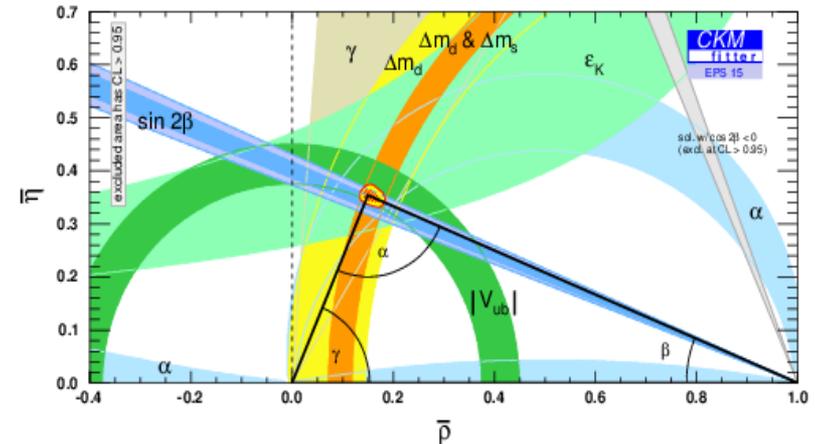
Direct Measurement

$$\alpha/\phi_2 = (87.6^{+3.5}_{-3.3})^\circ$$

$$\beta/\phi_1 = (21.85^{+0.68}_{-0.67})^\circ$$

$$\gamma/\phi_3 = (73.2^{+6.3}_{-7.0})^\circ$$

- γ/ϕ_3 is the least precisely measured angle
- Precision is statistically limited
- Precise measurement of γ/ϕ_3 is needed to test the UT of CKM
- Any difference between tree measurement to loop measurement might be a sign of NP in flavor sector



$$\gamma = \arg(-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)$$

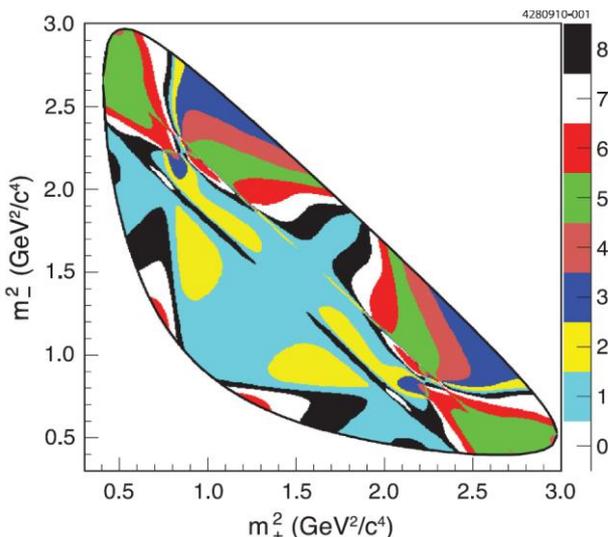
- GGSZ (Dalitz) method in $B^- \rightarrow D^0 K$ is Most sensitive method to constrain γ/ϕ_3 nowadays
- With the amount of data LHCb collecting, γ/ϕ_3 measurement soon will be systematically limit
- BESIII can help reducing the systematics with providing more information on $D^0 \rightarrow K^0 \pi^+ \pi^-$

Binning in Dalitz plots

BESIII performing analysis with $2.9\text{fb}^{-1} \psi''$ data

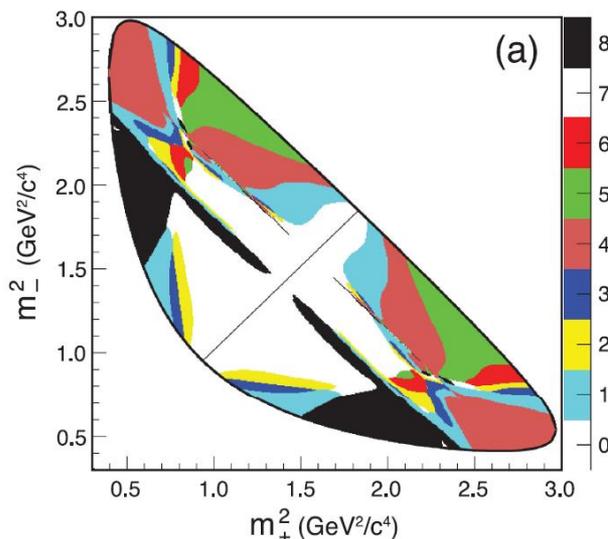
Same method as CLEO-c (PRD 82 (2010) 112006)

BaBar 2008 Equal Distance Bins



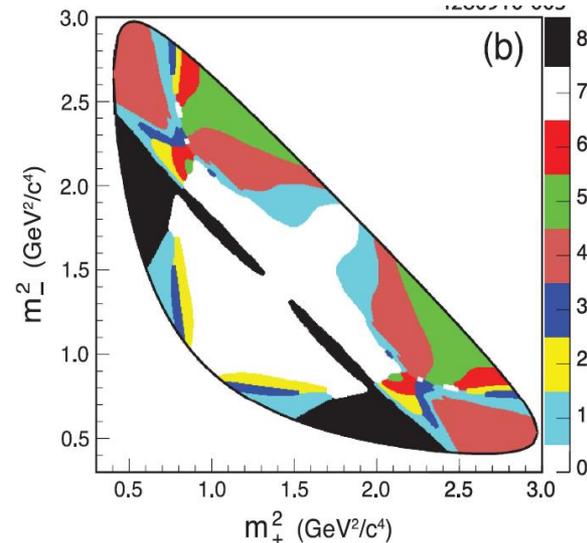
Result of splitting the Dalitz PHSP into 8 equally spaced phase bins base on BaBar 2008 Model

BaBar 2008 Optimal Bins



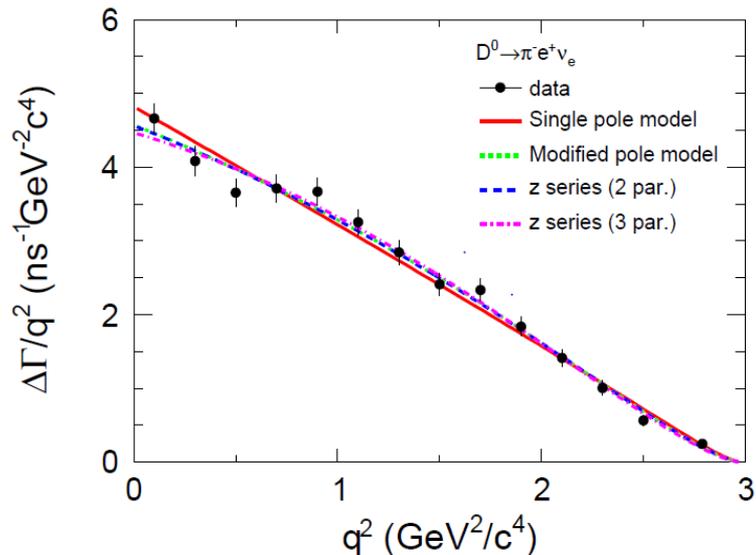
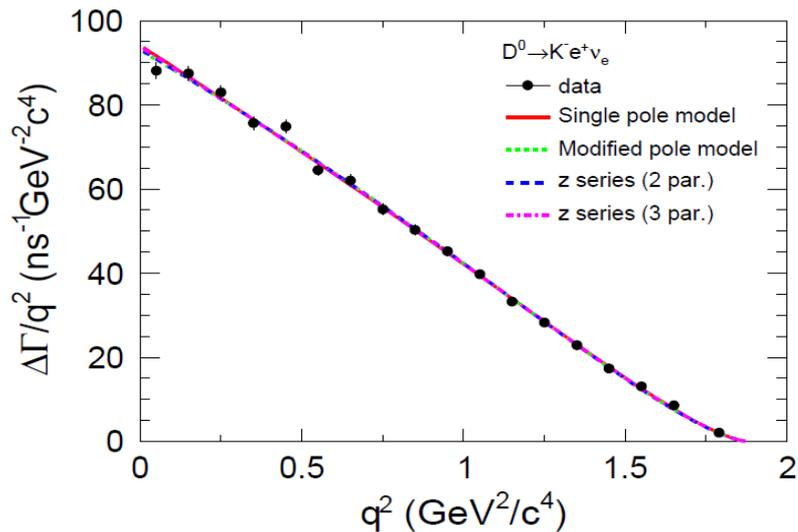
Starting with the equally spaced bins, bins are adjusted to optimize the sensitivity to γ . A secondary adjustment smooths binned areas smaller than detector resolution

BaBar 2008 Modified Optimal Bins



Similar to the "optimal binning" except the expected background is taken into account before optimizing to γ sensitivity

Measurement of $f_+^{K(\pi)}(q^2)$



		Single pole model	
Decay mode	$f_+^{K(\pi)}(0) V_{cs(d)} $	$M_{\text{pole}} \text{ (GeV}^2/c^2\text{)}$	
$D^0 \rightarrow K^- e^+ \nu_e$	$0.7209 \pm 0.0022 \pm 0.0035$	$1.921 \pm 0.010 \pm 0.007$	
$D^0 \rightarrow \pi^- e^+ \nu_e$	$0.1475 \pm 0.0014 \pm 0.0005$	$1.911 \pm 0.012 \pm 0.004$	
		Modified pole model	
Decay mode	$f_+^{K(\pi)}(0) V_{cs(d)} $	α	
$D^0 \rightarrow K^- e^+ \nu_e$	$0.7163 \pm 0.0024 \pm 0.0034$	$0.309 \pm 0.020 \pm 0.013$	
$D^0 \rightarrow \pi^- e^+ \nu_e$	$0.1437 \pm 0.0017 \pm 0.0008$	$0.279 \pm 0.035 \pm 0.011$	
		Two-parameter series expansion	
Decay mode	$f_+^{K(\pi)}(0) V_{cs(d)} $	r_1	
$D^0 \rightarrow K^- e^+ \nu_e$	$0.7172 \pm 0.0025 \pm 0.0035$	$-2.2286 \pm 0.0864 \pm 0.0573$	
$D^0 \rightarrow \pi^- e^+ \nu_e$	$0.1435 \pm 0.0018 \pm 0.0009$	$-2.0365 \pm 0.0807 \pm 0.0257$	
		Three-parameter series expansion	
Decay mode	$f_+^{K(\pi)}(0) V_{cs(d)} $	r_1	r_2
$D^0 \rightarrow K^- e^+ \nu_e$	$0.7195 \pm 0.0035 \pm 0.0041$	$-2.3338 \pm 0.1587 \pm 0.0804$	$3.4188 \pm 3.9090 \pm 2.4098$
$D^0 \rightarrow \pi^- e^+ \nu_e$	$0.1420 \pm 0.0024 \pm 0.0010$	$-1.8432 \pm 0.2212 \pm 0.0690$	$-1.3874 \pm 1.4615 \pm 0.4680$

Study of $D^+ \rightarrow K_L e^+ \nu_e$

- Never been studied **BESIII Preliminary, 2.9 fb⁻¹ ψ'' data, see Fenfen's talk at Charm2015**
- A CP asymmetry with magnitude of about $\sim -3.3 \times 10^{-3}$ due to K^0 - \bar{K}^0 mixing

[PLB 353(1995) 31, 363 (1995) 266]

- K_L reconstruction :
 - Get position of the K_L in EMC by fining a neutral cluster
 - Use the constraint of $U_{miss}=0$ to get the momentum of K_L

Simultaneous fit to event density
with 2-parameters series FF

BESIII Preliminary Results

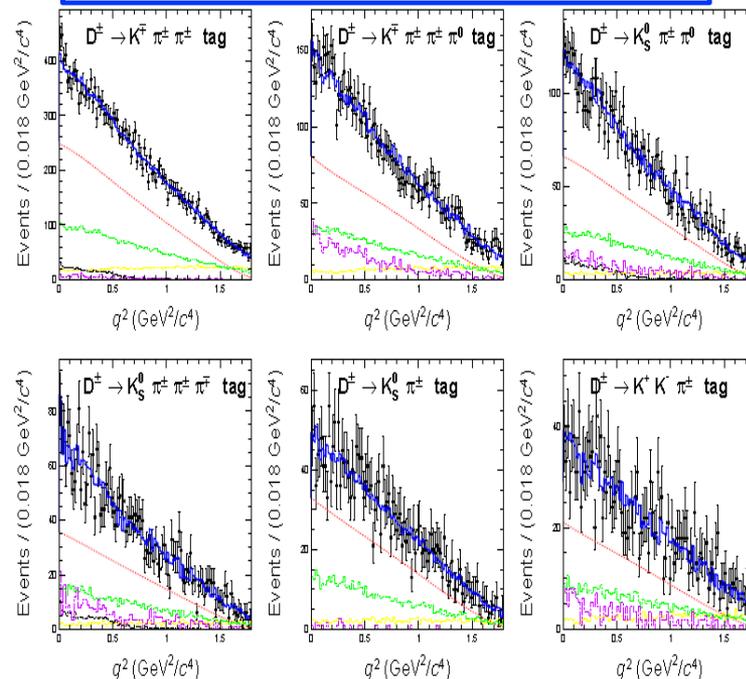
$$A_{CP}(D^+ \rightarrow K_L e^+ \nu_e) = (-0.59 \pm 0.60_{stat} \pm 1.48_{syst})\%$$

$$B(D^+ \rightarrow K_L e^+ \nu_e) = (4.482 \pm 0.027_{stat} \pm 0.103_{syst})\%$$

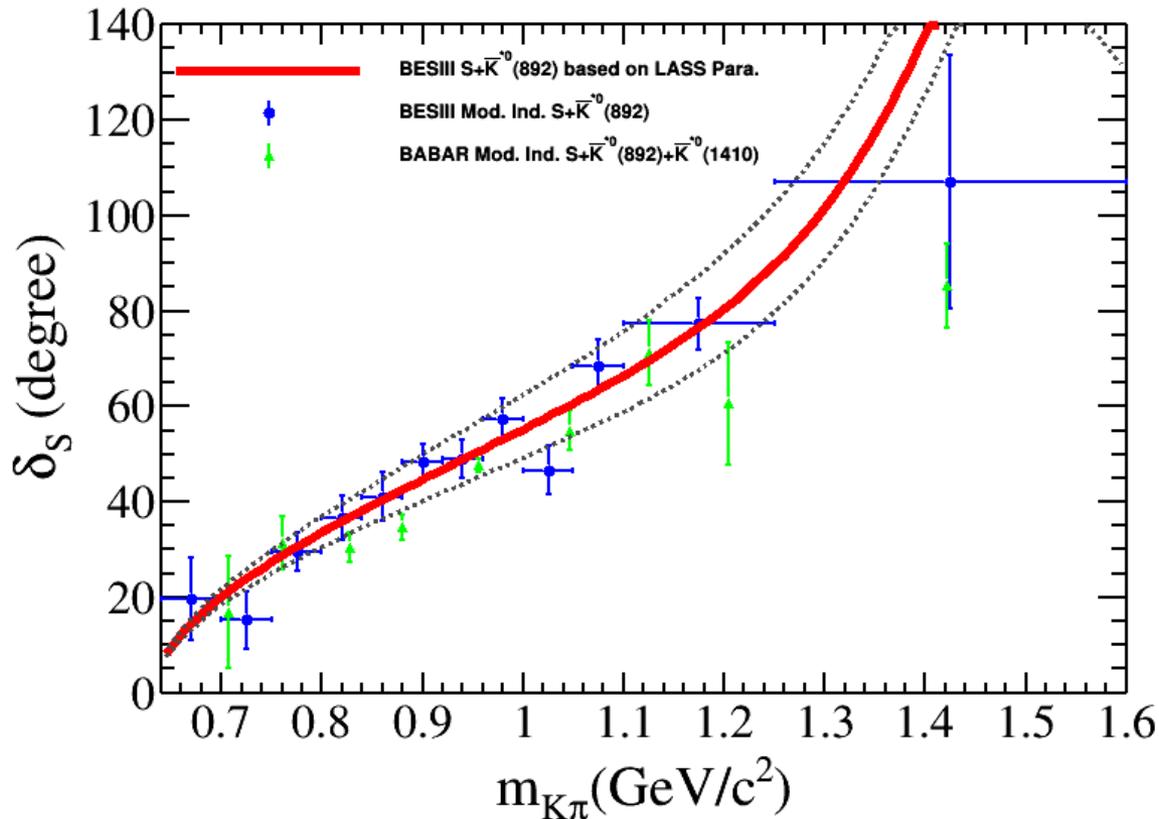
$$f_+^K(0)|V_{cs}| = 0.728 \pm 0.006 \pm 0.011$$

$$|V_{cs}| = 0.975 \pm 0.008 \pm 0.015 \pm 0.025$$

$$\text{With } f_+^K(0) = 0.747 \pm 0.019 \quad (PRD82, 114506)$$



BESIII 2.9 fb⁻¹ ψ'' data, see Fenfen's talk at Charm2015



Model-independent measurement of BESIII are consistent with its result from amplitude analysis within 1σ .

Paras Naik's talk at Charm 2015

JHEP 10 (2015) 005, 3.0fb⁻¹

- To eliminate the effects of FSI, which conserve P, we form an asymmetry of asymmetries which cancels out the FSI; any remaining asymmetry implies that either C or P is violated, i.e. we have CPV

$$a_{CP}^{T\text{-odd}}(D^0) = \frac{1}{2} (A_{C_T} - \bar{A}_{\bar{C}_T})$$

- LHCb measured these asymmetries using SL flavor-tagged D decays.

$$A_{C_T} = (-71.8 \pm 4.1(\text{stat}) \pm 1.3(\text{syst})) \times 10^{-3}$$

$$\bar{A}_{\bar{C}_T} = (-75.5 \pm 4.1(\text{stat}) \pm 1.2(\text{syst})) \times 10^{-3}$$

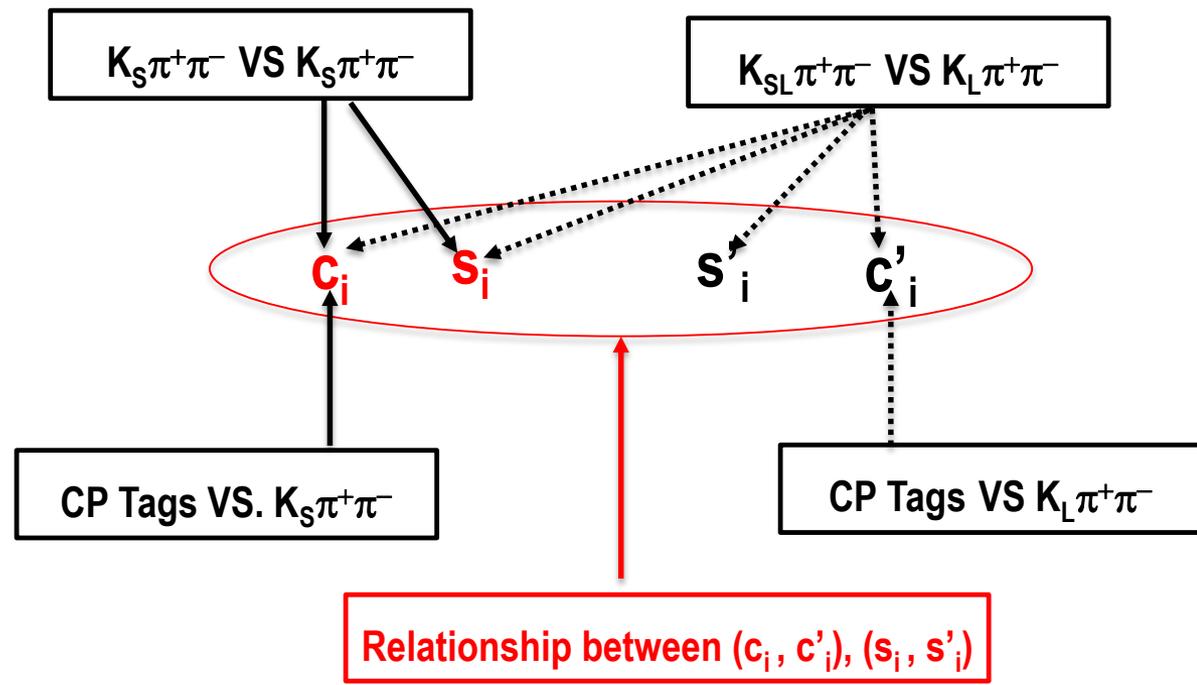


$$a_{CP}^{T\text{-odd}}(D^0) = (1.8 \pm 2.9(\text{stat}) \pm 0.4(\text{syst})) \times 10^{-3}$$

- We also searched for local CPV in bins of phase space, and evidence of CPV in bins of proper time. No CPV was found.

c_i/s_i in $D^0 \rightarrow K_{S/L} \pi^+ \pi^-$ Analysis

c_i and s_i can be calculated from double tags of $D^0 \rightarrow K_S \pi^+ \pi^-$ VS. $D^0 \rightarrow (K_{S/L} \pi^+ \pi^- \text{ or CP eigenstates})$

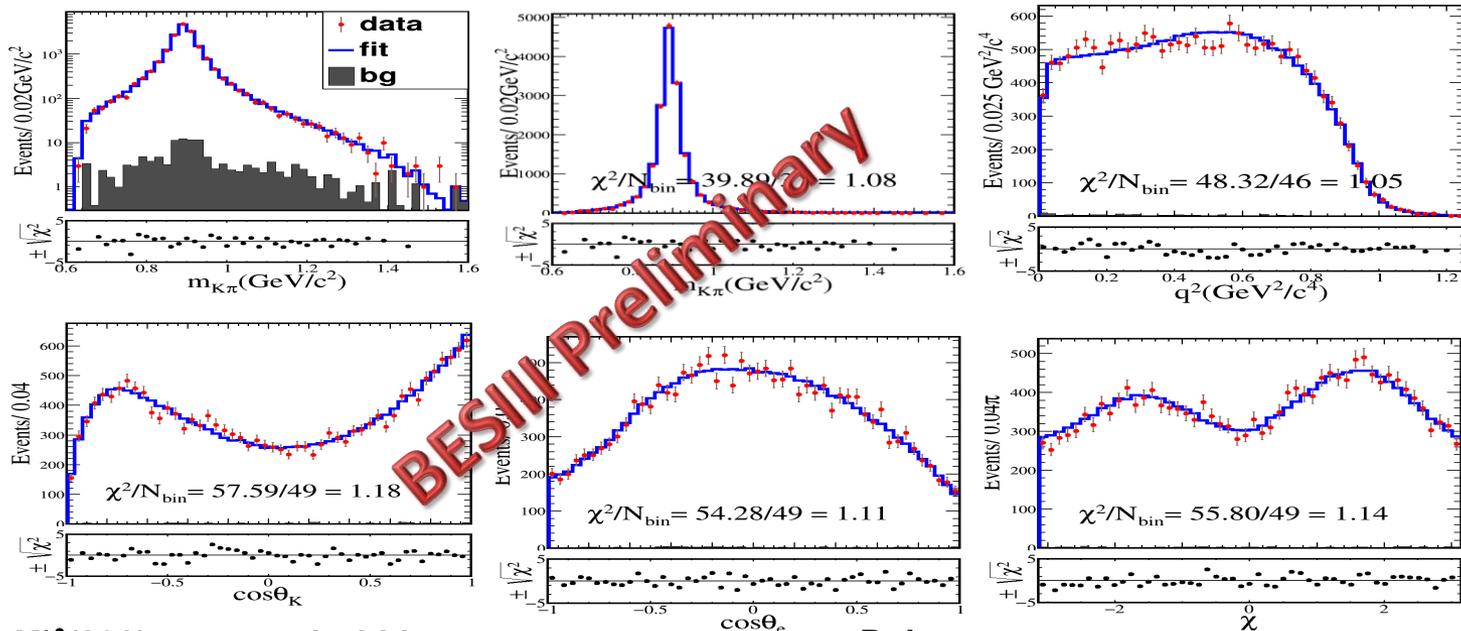


Only c_i, s_i from $D^0 \rightarrow K_S \pi^+ \pi^-$ is used to calculate γ .

However adding in $D^0 \rightarrow K_L \pi^+ \pi^-$ to calculate c_i', s_i' and use the relationship to c_i, s_i to further constrain the results in a global fit

PWA of $D^+ \rightarrow K^- \pi^+ e^+ \nu_e$

BESIII 2.9 fb⁻¹ ψ'' data, see Fenfen's talk at Charm2015



- $K^{*0}(892)$ mass and width

$$M_{K^{*0}(892)} = (894.60 \pm 0.25 \pm 0.08) \text{MeV}/c^2$$

$$\Gamma_{K^{*0}(892)} = (46.42 \pm 0.56 \pm 0.15) \text{MeV}/c^2$$

- The fractions of components

$$f(D^+ \rightarrow (K^- \pi^+)_{K^{*0}(892)} e^+ \nu_e) = (93.93 \pm 0.22 \pm 0.18)\%$$

$$f(D^+ \rightarrow (K^- \pi^+)_{S\text{-wave}} e^+ \nu_e) = (6.05 \pm 0.22 \pm 0.18)\%$$

- Pole mass

$$m_V = (1.81_{-0.17}^{+0.25} \pm 0.02) \text{GeV}/c^2$$

$$m_A = (2.61_{-0.17}^{+0.22} \pm 0.03) \text{GeV}/c^2$$

- Form factor and ratios :

$$A_1(0) = 0.573 \pm 0.011 \pm 0.020$$

$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_A = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

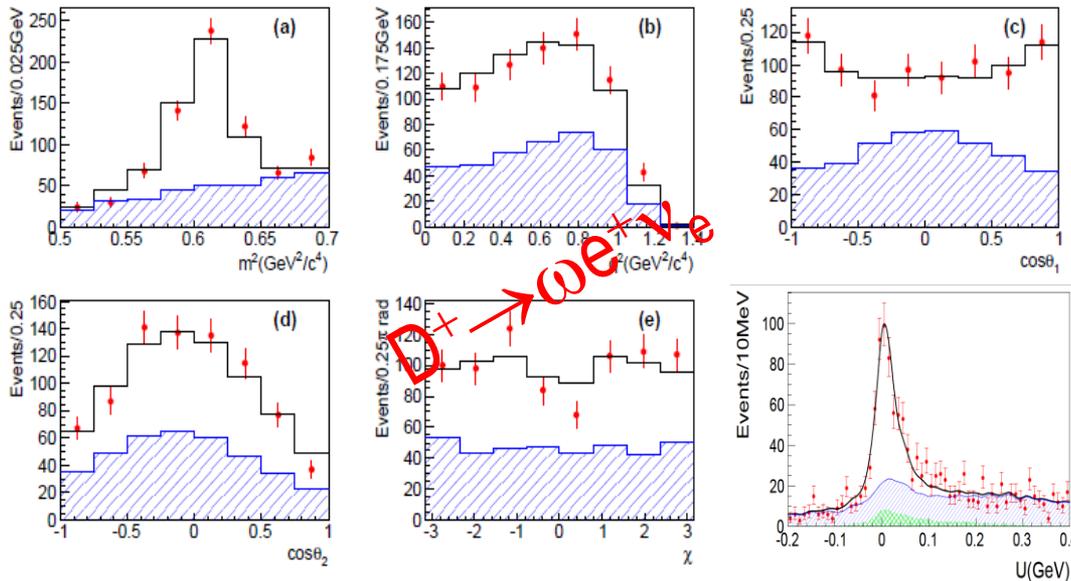
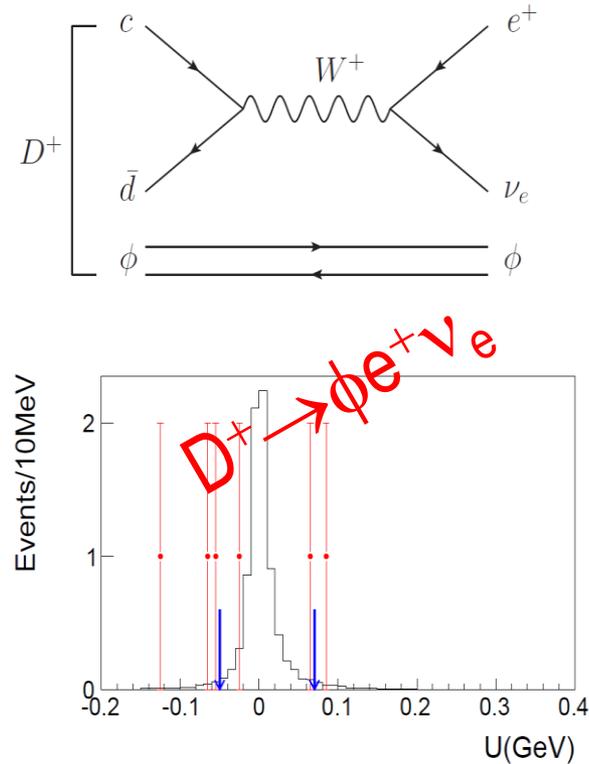


Study of $D^+ \rightarrow \omega/\phi e^+ \nu_e$



- Form factor of decay $D^+ \rightarrow \omega e^+ \nu_e$ have never been measured
- $D^+ \rightarrow \phi e^+ \nu_e$ proceeds only by ω - ϕ mixing or non-perturbative “Weak Annihilation” (WA) process, measure of its BR can help to judge the dominant process

BESIII 2.9 fb⁻¹ ψ'' data [arXiv:1508.00151](https://arxiv.org/abs/1508.00151)

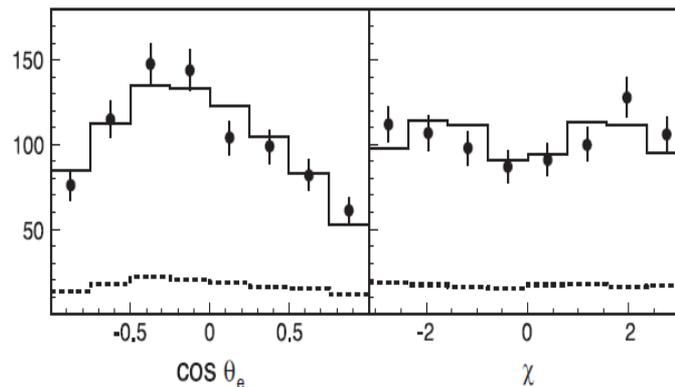
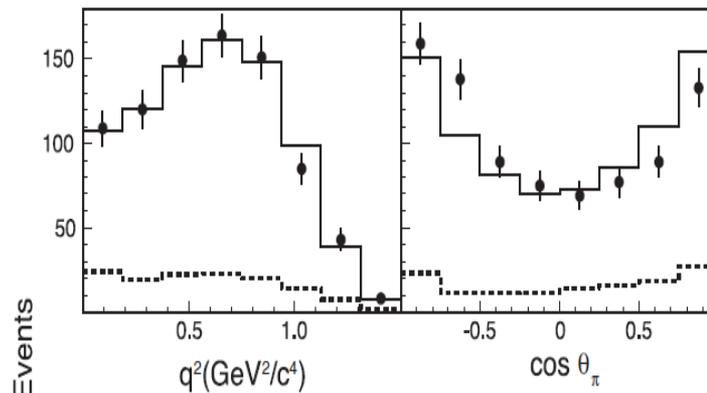
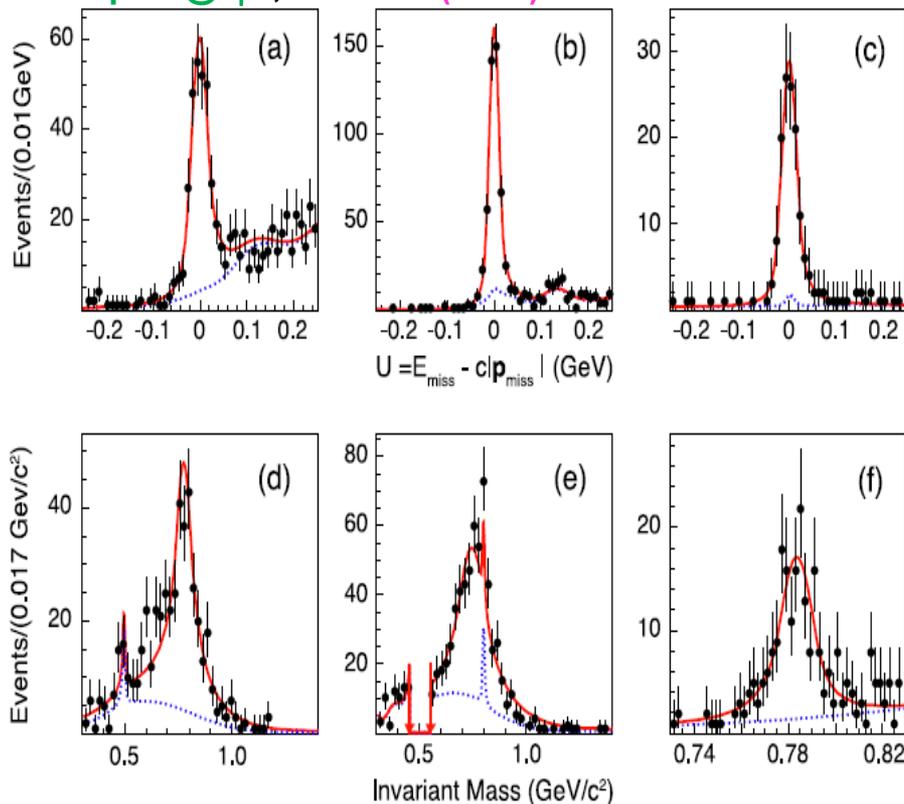


$$r_V = V(0)/A_1(0) = 1.24 \pm 0.09 \pm 0.06$$

$$r_A = A_2(0)/A_1(0) = 1.06 \pm 0.15 \pm 0.05$$

Mode	This work	Previous
$\omega e^+ \nu_e$	$(1.63 \pm 0.11 \pm 0.08) \times 10^{-3}$	$(1.82 \pm 0.18 \pm 0.07) \times 10^{-3}$
$\phi e^+ \nu_e$	$< 1.3 \times 10^{-5}$ (@90% C.L.)	$< 9.0 \times 10^{-5}$ (@90% C.L.)

818 pb⁻¹ @ ψ'' , PRL 110 (2013) 131802



$$B(D^0 \rightarrow \rho^- \ell \nu_\ell) = (1.77 \pm 0.12 \pm 0.10)\%$$

$$B(D^+ \rightarrow \rho^0 \ell \nu_\ell) = (2.17 \pm 0.12^{+0.12}_{-0.22})\%$$

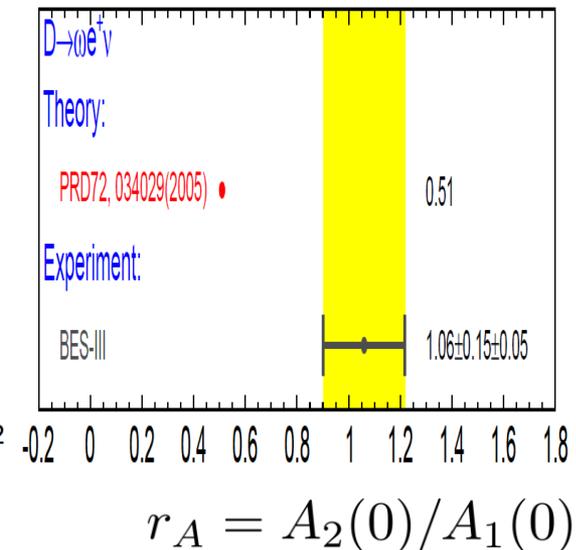
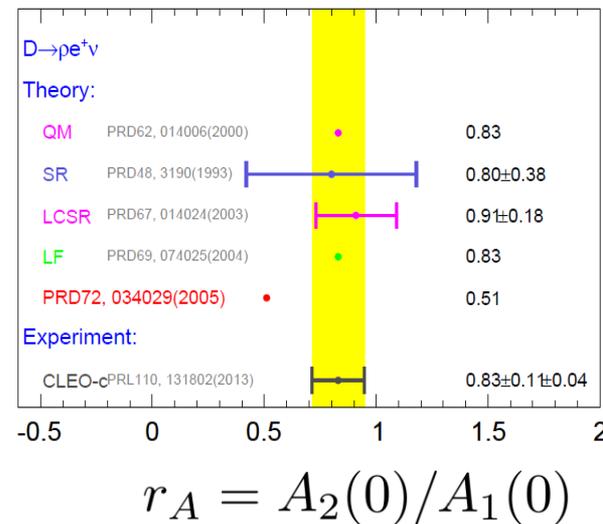
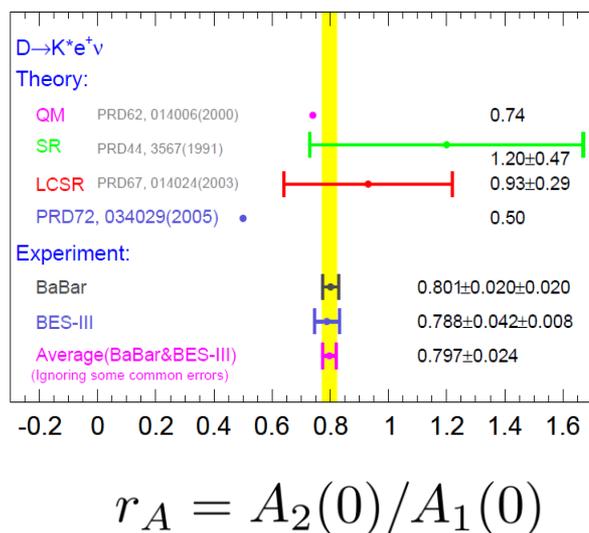
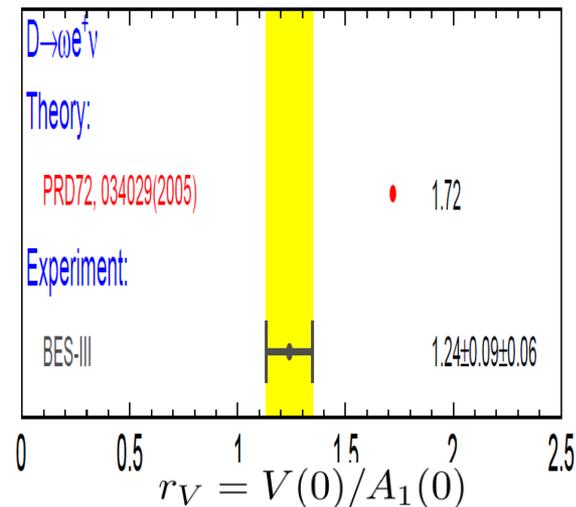
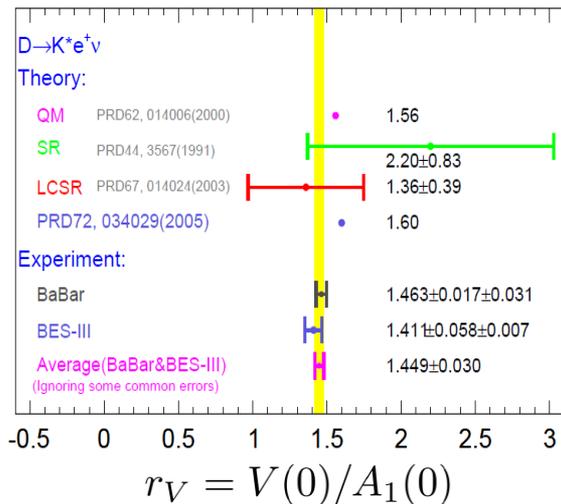
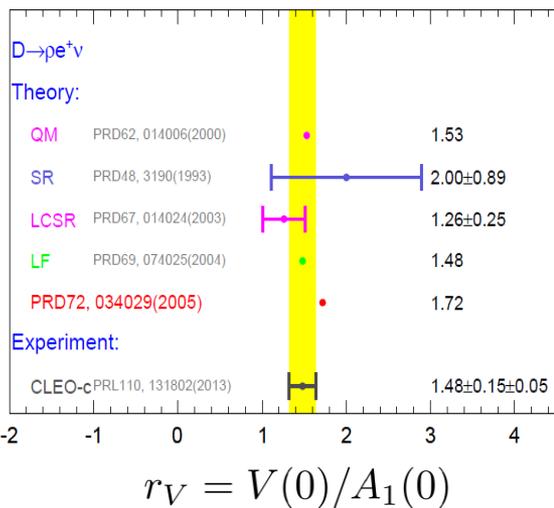
$$B(D^+ \rightarrow \omega \ell \nu_\ell) = (1.82 \pm 0.18 \pm 0.07)\%$$

$$\frac{\Gamma(D^0 \rightarrow \rho^- \ell \nu_\ell)}{2\Gamma(D^0 \rightarrow \rho^- \ell \nu_\ell)} = 1.03 \pm 0.09^{+0.08}_{-0.02}$$

$$r_V = V(0)/A_1(0) = 1.48 \pm 0.15 \pm 0.05$$

$$r_A = A_2(0)/A_1(0) = 0.83 \pm 0.11 \pm 0.04$$

Comparison of $r_{V/A}$ in $D \rightarrow V e^+ v_e$

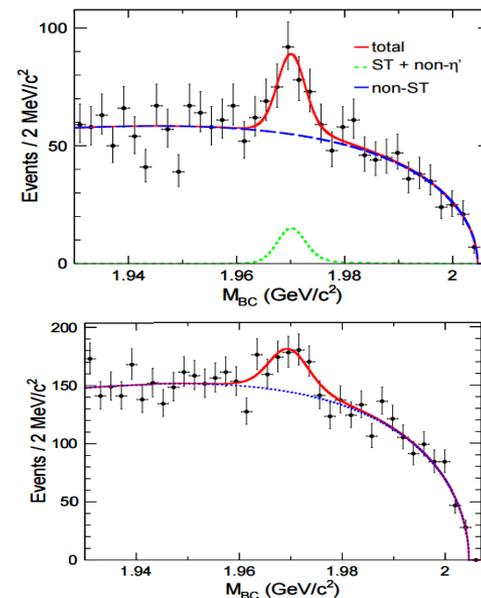


Measurement of $D_S^+ \rightarrow \eta' X / \eta' \rho^+$

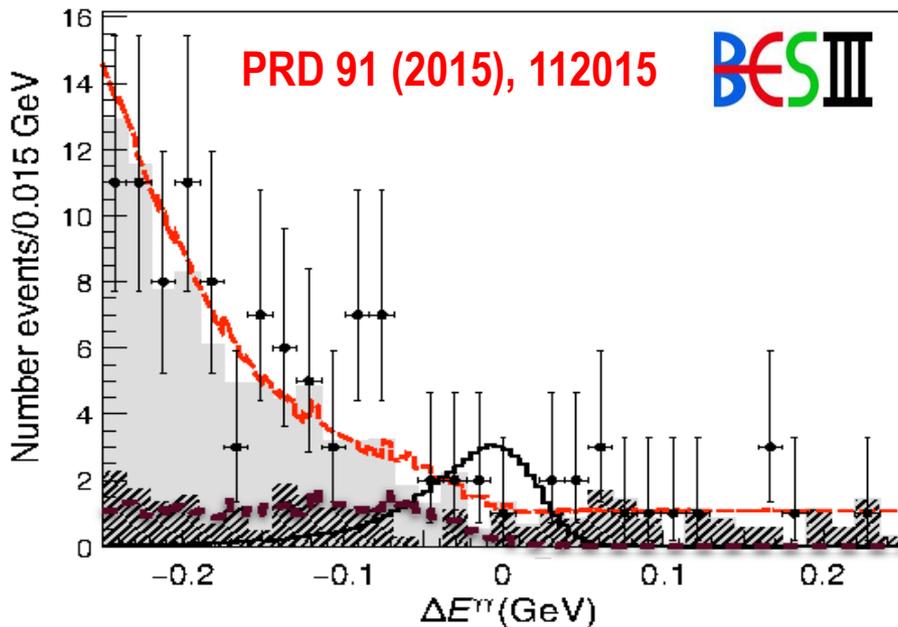
BESIII 482 pb⁻¹ @ 4.009 GeV arXiv:1506.08952

- Inclusive measurement on BR :
 - BR($D_S^+ \rightarrow \eta' X$) = $(11.7 \pm 1.8)\%$ [CLEO-c, PRD79, 112008 (2009)]
 - BR($D_S^+ \rightarrow \eta' X$) = $(18.6 \pm 2.3)\%$ [sum over all exclusive measurement in PDG]
- Exclusive measurement on BR :
 - BR($D_S^+ \rightarrow \eta' \rho^+$) = $(12.5 \pm 2.2)\%$ [CLEO2, PRD58, 052002 (1998)]
 - BR($D_S^+ \rightarrow \eta' \pi^+ \pi^0(\rho^+)$) = $(5.6 \pm 0.5 \pm 0.6)\%$ [CLEO-c, PRD88, 032009 (2013)]
- A factorization method predicts :
 - BR($D_S^+ \rightarrow \eta' \pi^+ \pi^0(\rho^+)$) = $(3.0 \pm 0.5)\%$ [F. S. Yu et al, PRD84, 074019 (2011)]
- **BESIII Measurement based on 482 pb⁻¹ data at 4.009 GeV**
 - BR($D_S^+ \rightarrow \eta' X$) = $(8.8 \pm 1.8 \pm 0.5)\%$
 - BR($D_S^+ \rightarrow \eta' \rho^+$) = $(5.8 \pm 1.4 \pm 0.4)\%$
 - BR($D_S^+ \rightarrow \eta' \pi^+ \pi^0(\rho^+)$) $\leq 5.1\%$ @ 90% C.L.

A interesting situation
on BR measurement



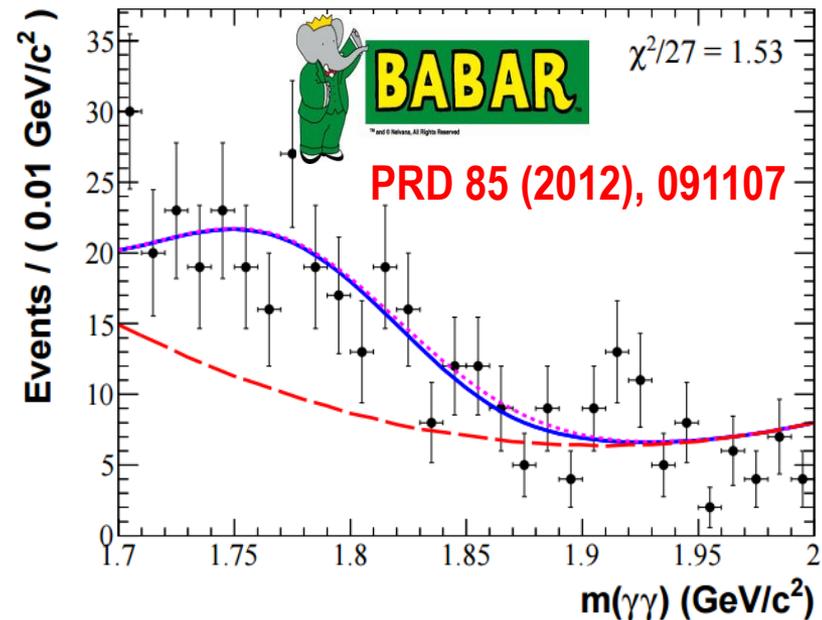
Consistent with CLEO-c recent measurement,
Reconcile the tension between experimental data and theoretical prediction



BESIII Double tagged method (5 tag modes)

- 2.9 fb⁻¹ results: $B(D^0 \rightarrow \gamma\gamma) < 3.8 \times 10^{-6}$ @ 90% C.L.
- 10.0 fb⁻¹ expected: $B(D^0 \rightarrow \gamma\gamma) < 1.0 \times 10^{-6}$ @ 90% C.L.

**BESIII has much smaller bkg than that at B factory,
peaking bkg from $D^0 \rightarrow \pi^0 \pi^0$ is under control**



Belle II (470.5fb-1) :

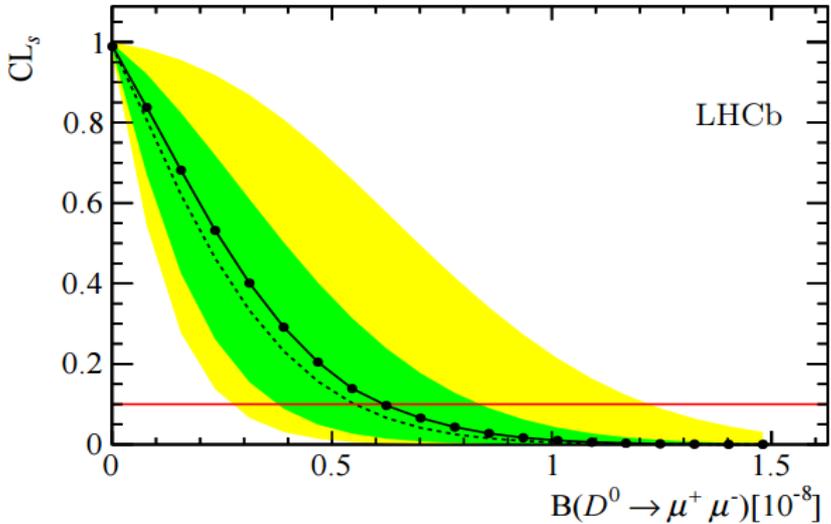
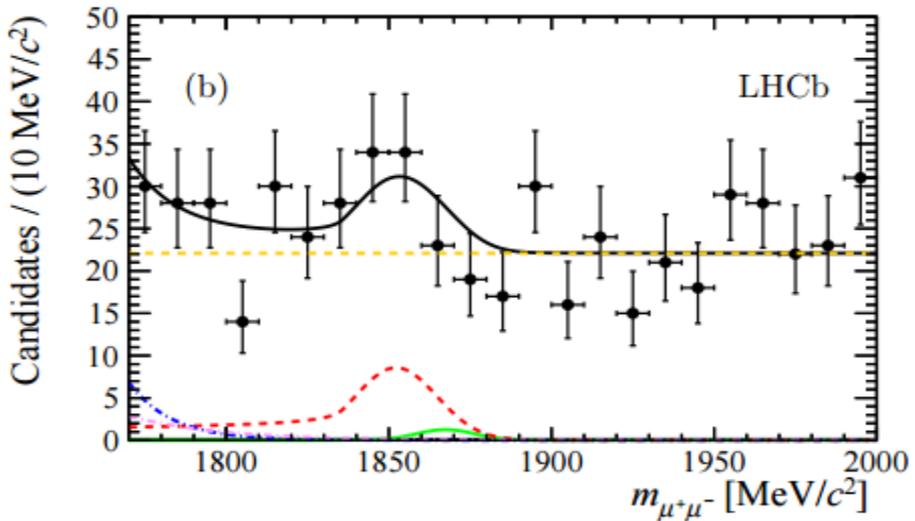
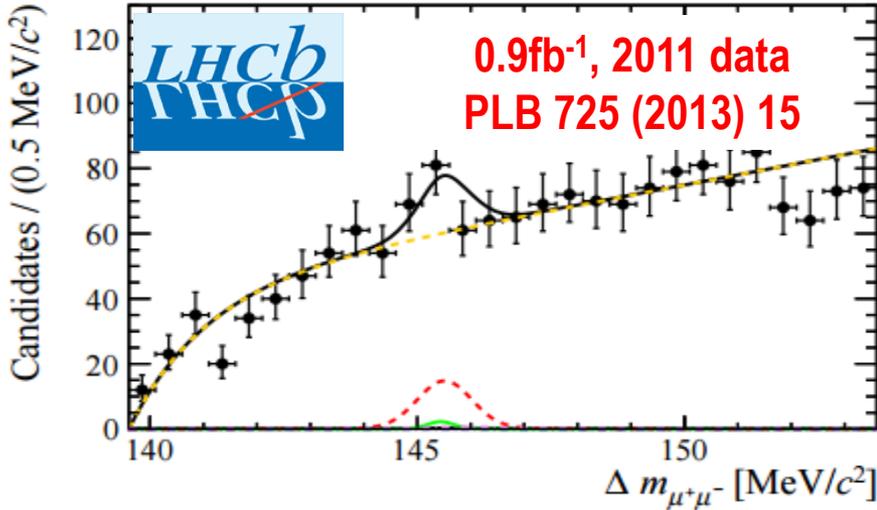
$$B(D^0 \rightarrow \gamma\gamma) < 2.2 \times 10^{-6} \text{ @ 90\% C.L.}$$

Theory prediction :

$$B(D^0 \rightarrow \gamma\gamma)^{VM D} \simeq (3.5_{-2.6}^{+4.0}) \times 10^{-8}$$

$$B(D^0 \rightarrow \gamma\gamma)^{SD} \simeq 3 \times 10^{-11}$$

D⁰ → μ⁺μ⁻ Measurement



- Using D* chain : D⁺ → D⁰(μ⁺μ⁻)π_s⁺ :
 $B(D^0 \rightarrow \mu^+ \mu^-) \leq 6.2(7.6) \times 10^{-9}$ @ 90 (95)% C. L.
- Current best limit
- But still 100×SM or 10×NP prediction
- Also best limit for FCNC in charm

LHCb :

- For run II (2015–2018) expect mild improvements wrt run I
- LHCb upgrade:
 $\sigma(c\bar{c})_{14\text{ TeV}} \sim 2\sigma(c\bar{c})_{7\text{ TeV}}$, trigger $\sim 2\times$ better, $\sim 50\text{ fb}^{-1}$
- $10\times$ charm per year

Modes	Run I	Run II	Upgrade
$D^0 \rightarrow \mu^+\mu^-$	few 10^{-9}	fewer 10^{-9}	few 10^{-10}
$D^+ \rightarrow \pi^+\mu^+\mu^-$	few 10^{-8}	fewer 10^{-8}	few 10^{-9}
$D_s^+ \rightarrow K^+\mu^+\mu^-$	few 10^{-7}	fewer 10^{-7}	few 10^{-8}
$D^0 \rightarrow h^+h^{(\prime)\pm}\mu^+\mu^-$	few 10^{-7}	fewer 10^{-7}	few 10^{-8}

- Rare charm program in LHCb includes/foresee:

$D^0 \rightarrow \ell^+\ell'^-$, $\Lambda_c \rightarrow p\ell^+\ell^-$, $D \rightarrow h(h')\ell\ell'$, $D^0 \rightarrow \phi\gamma$
with $\ell = \mu, e$ (FCNC, LFV and LNV modes)

BELLE-II

- Should collect 50 ab^{-1} from e^+e^-
low background, excellent γ and π^0 reconstruction
- Simple projections from BaBar $X_c \rightarrow h\ell\ell$ analysis [PRD 84 (2011) 072006]
 $\sim 100\times$ statistics
 \Rightarrow should achieve U.L. of $\sim 10^{-7}$ for D^+ and 10^{-6} for D_s^+, Λ_c^+ on semileptonic FCNC, LNV and LFV
- also extrapolating from BaBar, could reach $\mathcal{B}(D^0 \rightarrow \gamma\gamma) \lesssim 10^{-7}$
- Can do a great job in $h\ell\ell$ with $h = \pi^0, \eta, \omega$

Super τ -charm Factory

- Assuming to collect $\sim 10^{10}$ D pairs $\Rightarrow 10^4\times$ Cleo-c
- can achieve U.L. of few 10^{-8} for 3-body D^+ and 10^{-7} for 4-body D^0
- could reach $\mathcal{B}(D^0 \rightarrow \gamma\gamma) \lesssim 10^{-7}$

Carla's Talk at CHARM2015