# Towards an Understanding of the Correlations in Jet Substructure

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D. Adams<sup>1</sup>, A. Arce<sup>2</sup>, L. Asquith<sup>3</sup>, M. Backovic<sup>4</sup>, T. Barillari<sup>5</sup>, P. Berta<sup>6</sup>, D. Bertolini<sup>7</sup>, D. Adams<sup>1</sup>, A. Arce<sup>2</sup>, L. Asquith<sup>2</sup>, M. Backovic<sup>4</sup>, T. Barillari<sup>9</sup>, P. Berta<sup>6</sup>, D. Bertolini<sup>7</sup>,
A. Buckley<sup>8</sup>, J. Butterworth<sup>9</sup>, R. C. Camacho Toro<sup>10</sup>, J. Caudron<sup>11</sup>, Y.-T. Chien<sup>12</sup>, J. Cogan<sup>13</sup>,
B. Cooper<sup>9</sup>, D. Curtin<sup>14</sup>, C. Debenedetti<sup>15</sup>, J. Dolen<sup>16</sup>, M. Eklund<sup>17</sup>, S. El Hedri<sup>11</sup>,
S. D. Ellis<sup>18</sup>, T. Embry<sup>17</sup>, D. Ferencek<sup>19</sup>, J. Ferrando<sup>8</sup>, S. Fleischmann<sup>20</sup>, M. Freytsis<sup>21</sup>,
M. Giulini<sup>22</sup>, Z. Han<sup>23</sup>, D. Hare<sup>24</sup>, P. Harris<sup>25</sup>, A. Hinzmann<sup>26</sup>, R. Hoing<sup>27</sup>, A. Hornig<sup>12</sup>,
M. Jankowiak<sup>28</sup>, K. Johns<sup>17</sup>, G. Kasieczka<sup>29</sup>, R. Kogler<sup>27</sup>, W. Lampl<sup>17</sup>, A. J. Larkoski<sup>30</sup>,
C. Lee<sup>12</sup>, R. Leone<sup>17</sup>, P. Loch<sup>17</sup>, D. Lopez Mateos<sup>21</sup>, H. K. Lou<sup>31</sup>, M. Low<sup>32</sup>,
P. Maksimovic<sup>33</sup>, I. Marchesini<sup>27</sup>, S. Marzani<sup>30</sup>, L. Masetti<sup>11</sup>, R. McCarthy<sup>34</sup>, S. Menke<sup>5</sup>,
D. W. Miller<sup>32</sup>, K. Michar<sup>24</sup>, P. Nachmarl<sup>13</sup>, P. Mafl<sup>3</sup>, F. T. O'Conchul<sup>7</sup>, A. Overharma<sup>35</sup> D. W. Miller<sup>32</sup>, K. Mishra<sup>24</sup>, B. Nachman<sup>13</sup>, P. Nef<sup>13</sup>, F. T. O'Grady<sup>17</sup>, A. Ovcharova<sup>35</sup>, A. Picazio<sup>10</sup>, C. Pollard<sup>8</sup>, B. Potter-Landua<sup>25</sup>, C. Potter<sup>25</sup>, S. Rappoccio<sup>16</sup>, J. Rojo<sup>36</sup>, J. Rutherfoord<sup>17</sup>, G. P. Salam<sup>25,37</sup>, J. Schabinger<sup>38</sup>, A. Schwartzman<sup>13</sup>, M. D. Schwartz<sup>21</sup> B. Shuve<sup>39</sup>, P. Sinervo<sup>40</sup>, D. Soper<sup>23</sup>, D. E. Sosa Corral<sup>22</sup>, M. Spannowsky<sup>41</sup>, E. Strauss<sup>13</sup>,
M. Swiatlowski<sup>13</sup>, J. Thaler<sup>30</sup>, C. Thomas<sup>25</sup>, E. Thompson<sup>42</sup>, N. V. Tran<sup>24</sup>, J. Tseng<sup>36</sup>,
E. Usai<sup>27</sup>, L. Valery<sup>43</sup>, J. Veatch<sup>17</sup>, M. Vos<sup>44</sup>, W. Waalewijn<sup>45</sup>, J. Wacker<sup>13</sup>, and C. Young<sup>25</sup> <sup>1</sup>Brookhaven National Laboratory, Upton, NY 11973, USA <sup>2</sup>Duke University, Durham, NC 27708, USA <sup>3</sup>Argonne National Laboratory, Lemont, IL 60439, USA <sup>4</sup>CP3, Universite catholique du Louvain, B-1348 Louvain-la-Neuve, Belgium <sup>5</sup>Max-Planck-Institute fuer Physik, 80805 Muenchen, Germany <sup>6</sup>Charles University in Prague, FMP, V Holesovickach 2, Prague, Czech Republic <sup>7</sup>University of California, Berkeley, CA 94720, USA <sup>8</sup>University of Glasgow, Glasgow, G12 8QQ, UK <sup>9</sup>University College London, WC1E 6BT, UK <sup>10</sup>University of Geneva, CH-1211 Geneva 4, Switzerland <sup>11</sup>Universitaet Mainz, DE 55099, Germany <sup>12</sup>Los Alamos National Laboratory, Los Alamos, NM 87545, USA <sup>13</sup>SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA <sup>14</sup>University of Maryland, College Park, MD 20742, USA <sup>15</sup>University of California, Santa Cruz, CA 95064, USA <sup>16</sup>University at Buffalo, Buffalo, NY 14260, USA <sup>17</sup>University of Arizona, Tucson, AZ 85719, USA <sup>18</sup>University of Washington, Seattle, WA 98195, USA <sup>19</sup>Rutgers University, Piscataway, NJ 08854, USA <sup>20</sup>Bergische Universitaet Wuppertal, Wuppertal, D-42097, Germany <sup>21</sup>Harvard University, Cambridge, MA 02138, USA <sup>22</sup>Universitaet Heidelberg, DE-69117, Germany <sup>23</sup>University of Oregon, Eugene, OR 97403, USA <sup>24</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA <sup>25</sup>CERN, CH-1211 Geneva 23, Switzerland <sup>26</sup>Universitaet Zuerich, 8006 Zuerich, Switzerland <sup>27</sup>Universitaet Hamburg, DE-22761, Germany <sup>28</sup>New York University, New York, NY 10003, USA <sup>29</sup>ETH Zuerich, 8092 Zuerich, Switzerland <sup>30</sup>Massachusetts Institute of Technology, Cambridge, MA 02139, USA <sup>31</sup>Princeton University, Princeton, NJ 08544, USA <sup>32</sup>University of Chicago, IL 60637, USA <sup>33</sup>Johns Hopkins University, Baltimore, MD 21218, USA <sup>34</sup>YITP, Stony Brook University, Stony Brook, NY 11794-3840, USA <sup>35</sup>Berkeley National Laboratory, University of California, Berkeley, CA 94720, USA <sup>36</sup>University of Oxford, Oxford, OX1 3NP, UK <sup>37</sup>LPTHE, UPMC Univ. Paris 6 and CNRS UMR 7589, Paris, France <sup>38</sup>Universidad Autonoma de Madrid, 28049 Madrid, Spain <sup>39</sup>Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada <sup>40</sup>University of Toronto, Toronto, Ontario M5S 1A7, Canada <sup>41</sup>IPPP, University of Durham, Durham, DH1 3LE, UK <sup>42</sup>Columbia University, New York, NY 10027, USA <sup>43</sup>LPC Clermont-Ferrand, 63177 Aubiere Cedex, France <sup>44</sup>Instituto de Física Corpuscular, IFIC/CSIC-UVEG, E-46071 Valencia, Spain <sup>45</sup>University of Amsterdam, 1012 WX Amsterdam, Netherlands

<sup>1</sup>Address(es) of author(s) should be given Received: date / Accepted: date

Abstract Over the past five or so years a large number of 51 1 observables have been proposed in the literature, and ex-52 2 plored at the LHC experiments, that attempt to utilise the in-53 3 ternal structure of highly boosted jets in order to distinguish54 4 those that have been initiated by a quark, a gluon or by as5 5 heavier particle, such as a Top quark or W boson. This reports6 6 of the BOOST2013 workshop presents original particle-levels7 7 studies that attempt to improve our understanding of the re-58 8 lationship between these observables, their complementarity 59 g and overlap, and the dependence of this on the underlying jet 60 10 parameters, especially the jet radius R and jet  $p_T$ . This is ex-61 11 plored in the context of quark/gluon discrimination, boosted 62 12 W-boson tagging and boosted Top quark tagging. 13 63 64

Keywords boosted objects · jet substructure · beyondthe-Standard-Model physics searches · Large Hadron
Collider

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#### 17 1 Introduction

A characteristic feature of the proton-proton collisions at the<sup>71</sup> 18 LHC is a center-of-mass energy, 7 TeV in 2010 and 2011,72 19 8 TeV in 2012, and 13TeV with the start of the second phase<sup>73</sup> 20 of operation in 2015, that, even after accounting for par-74 21 ton desity functions, is large compared to the heaviest of75 22 the known particles. Thus these particles (and potentially<sup>76</sup> 23 also previously unknown ones) will often be produced at77 24 the LHC with substantial boosts. As a result, when decaying<sup>78</sup> 25 hadronically, these particles will not be observed as multi-79 26 ple jets in the detector, but rather as a single hadronic jet<sup>80</sup> 27 with distinctive internal substructure. This realization has<sup>81</sup> 28 led to a new era of sophistication in our understanding of<sup>82</sup> 29 both standard QCD jets and jets containing the decay of a<sup>83</sup> 30 heavy particle, with an array of new jet observables and de-84 31 tection techniques introduced and studies. To allow the ef-85 32 ficient sharing of results from these jet substructure studies<sup>86</sup> 33 a series of BOOST Workshops have been held on a yearly<sup>87</sup> 34 basis: SLAC (2009, [1]), Oxford University (2010, [2]),88 35 Princeton University University (2011, [3]), IFIC Valencia<sup>89</sup> 36 (2012 [4]), University of Arizona (2013 [5]), and, most re-90 37 cently, University College London (2014 [6]). After each of<sup>91</sup> 38 these meetings Working Groups have functioned during the<sup>92</sup> 30 following year to generate reports highlighting the most in-93 40 teresting new results, including studies of ever maturing de-94 41 95 tails. Previous BOOST reports can be found at [7–9]. 42 This report from BOOST 2013 thus views the study and 96 43 implementation of jet substructure techniques as a fairly ma-97 44 ture field, and focuses on the question of the correlations98 45 between the plethora of observables that have been devel-99 46 oped and employed, and their dependence on the underly<sub>100</sub> 47

ing jet parameters, especially the jet radius *R* and jet  $p_{T101}$ Samples of quark-, gluon-, W- and Top-initiated jets are re-102 constructed at the particle-level using FASTJET [10], and the03 performance, in terms of separating signal from background, of various groomed jet masses and jet substructure observables investigated through Receiver Operating Characteristic (ROC) curves, which show the efficiency to "tag" the signal as a function of the efficiency (or rejection, being 1/efficiency) to "tag" the background. In new analyses developed for the report, we investigate the separation of a quark signal from a gluon background (q/g tagging), a W signal from a gluon background (W-tagging) and a Top signal from a mixed quark/gluon QCD background (Top-tagging). In the case of Top-tagging, we also investigate the performance of dedicated Top-tagging algorithms, the HepTopTagger [11] and the Johns Hopkins Tagger [12]. Using multivariate techniques, we study the degree to which the discriminatory information provided by the observables and taggers overlaps, by examining in particular the extent to which the signalbackground separation performance increases when two or more variables/taggers are combined, via a Boosted Decision Tree (BDT), into a single discriminant. Where possible, we provide a discussion of the physics behind the structure of the correlations and the  $p_T$  and R scaling that we observe.

We present the performance of observables in idealized simulations without pile-up and detector resolution effects, with the primary goal of studying the correlations between observables and the dependence on jet radius and  $p_T$ . The relationship between substructure observables, their correlations, and how these depend on the jet radius *R* and jet  $p_T$  should not be too sensitive to pile-up and resolution effects; conducting studies using idealized simulations allows us to more clearly elucidate the underlying physics behind the observed performance, and also provides benchmarks for the development of techniques to mitigate pile-up and detector effects. A full study of the performance of pile-up and detector mitigation strategies is beyond the scope of the current report, and will be the focus of upcoming studies.

The report is organized as follows. In Section 2 we describe the generation of the Monte Carlo event samples that we use in the studies that follow. In Section 3 we detail the jet algorithms, observables and taggers investigated in each section of the report, and in Section 4 the multivariate techniques used to combine the one or more of the observables into single discriminants. In Section 5 we describe the q/g-tagging studies, in Section 6 we describe the W-tagging studies, and in Section 7 we describe the Top-tagging studies. Finally we offer some summary of the studies and general conclusions in Section 8.

This report presents original analyses and discussions pertaining to the performance of and correlations between various jet substructure techniques applied to quark/gluon discrimination, W-boson tagging, and Top tagging. The principal organizers of and contributors to the analyses presented in the report are: B. Cooper, S. D. Ellis, M. Freyt149
sis, A. Hornig, A. Larkoski, D. Lopez Mateos, B. Shuve, and
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#### **107** 2 Monte Carlo Samples

In the below sections the Monte Carlo samples used in thq<sub>55</sub> q/g tagging, W tagging and Top tagging sections of this re<sub>156</sub> port are described. Note that in all cases the samples used contain no additional proton-proton interactions beyond the hard scatter (no pile-up), and there is no attempt to emulatq<sub>57</sub> the degradation in angular and  $p_T$  resolution that would result when reconstructing the jets inside a real detector. 158

#### 115 2.1 Quark/gluon and W tagging

Samples were generated at  $\sqrt{s} = 8$  TeV for QCD dijets, and<sub>63</sub> 116 for  $W^+W^-$  pairs produced in the decay of a (pseudo) scalar<sub>64</sub> 117 resonance and decaying hadronically. The QCD events were 455 118 split into subsamples of gg and  $q\bar{q}$  events, allowing for tests 119 of discrimination of hadronic W bosons, quarks, and gluons. 120 Individual gg and  $q\bar{q}$  samples were produced at leading 121 order (LO) using MADGRAPH5 [13], while  $W^+W^-$  sam-122 ples were generated using the JHU GENERATOR [14-16] 123 to allow for separation of longitudinal and transverse polar-124 izations. Both were generated using CTEQ6L1 PDFs [17]<sub>iss</sub> 125 The samples were produced in exclusive  $p_T$  bins of width<sub>169</sub> 126 100 GeV, with the slicing parameter chosen to be the  $p_T$  of  $p_T$ 127 any final state parton or W at LO. At the parton-level the 128  $p_T$  bins investigated were 300-400 GeV, 500-600 GeV and 129 1.0-1.1 TeV. The samples were then all showered through 130 PYTHIA8 (version 8.176) [18] using the default tune 4C 131 [19]. For each of the various samples (W,q,g) and  $p_T$  bins, 132 500,000 events were simulated. 133

### 134 2.2 Top tagging

Samples were generated at  $\sqrt{s} = 14$  TeV. Standard Model<sub>174</sub> 135 dijet and top pair samples were produced with SHERPA 2.0.Q<sub>75</sub> 136 [20–25], with matrix elements of up to two extra partons  $_{76}$ 137 matched to the shower. The top samples included only hadronic 138 decays and were generated in exclusive  $p_T$  bins of width<sub>78</sub> 139 100 GeV, taking as slicing parameter the maximum of the<sub>179</sub> 140 top/anti-top  $p_T$ . The QCD samples were generated with  $a_{so}$ 141 cut on the leading parton-level jet  $p_T$ , where parton-level<sub>181</sub> 142 jets are clustered with the anti- $k_t$  algorithm and jet radii of 143 R = 0.4, 0.8, 1.2. The matching scale is selected to be  $Q_{\text{cut}} =$ 144 40,60,80 GeV for the  $p_{T \min} = 600, 1000$ , and 1500 GeV bin<sub>f82</sub> 145 respectively. For the top samples, 100k events were gener-146

ated in each bin, while 200k QCD events were generated ineach bin.

#### 3 Jet Algorithms and Substructure Observables

In this section, we define the jet algorithms and observables used in our analysis. Over the course of our study, we considered a larger set of observables, but for the final analysis, we eliminated redundant observables for presentation purposes. In Sections 3.1, 3.2, 3.3 and 3.4 we first describe the various jet algorithms, groomers, taggers and other substructure variables used in these studies.

#### 3.1 Jet Clustering Algorithms

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**Jet clustering:** Jets were clustered using sequential jet clustering algorithms [26] implemented in FASTJET 3.0.3. Final state particles *i*, *j* are assigned a mutual distance  $d_{ij}$  and a distance to the beam,  $d_{iB}$ . The particle pair with smallest  $d_{ij}$  are recombined and the algorithm repeated until the smallest distance is instead the distance to the beam,  $d_{iB}$ , in which case *i* is set aside and labelled as a jet. The distance metrics are defined as

$$d_{ij} = \min(p_{T_i}^{2\gamma}, p_{T_j}^{2\gamma}) \frac{\Delta R_{ij}^2}{R^2},$$
(1)

$$d_{i\mathrm{B}} = p_{Ti}^{2\gamma},\tag{2}$$

where  $\Delta R_{ij}^2 = (\Delta \eta)^2 + (\Delta \phi)^2$ . In this analysis, we use the anti- $k_t$  algorithm ( $\gamma = -1$ ) [27], the Cambridge/Aachen (C/A) algorithm ( $\gamma = 0$ ) [28, 29], and the  $k_t$  algorithm ( $\gamma = 1$ ) [30, 31], each of which has varying sensitivity to soft radiation in defining the jet.

**Qjets:** We also perform non-deterministic jet clustering [32, 33]. Instead of always clustering the particle pair with smallest distance  $d_{ij}$ , the pair selected for combination is chosen probabilistically according to a measure

$$P_{ij} \propto e^{-\alpha (d_{ij} - d_{\min})/d_{\min}},\tag{3}$$

where  $d_{\min}$  is the minimum distance for the usual jet clustering algorithm at a particular step. This leads to a different cluster sequence for the jet each time the Qjet algorithm is used, and consequently different substructure properties. The parameter  $\alpha$  is called the rigidity and is used to control how sharply peaked the probability distribution is around the usual, deterministic value. The Qjets method uses statistical analysis of the resulting distributions to extract more information from the jet than can be found in the usual cluster sequence.

#### 3.2 Jet Grooming Algorithms

**Pruning:** Given a jet, re-cluster the constituents using the C/A algorithm. At each step, proceed with the merger as

usual unless both

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Tij}} < z_{\text{cut}} \text{ and } \Delta R_{ij} > \frac{2m_j}{p_{Tj}} R_{\text{cut}}, \tag{4}$$

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in which case the merger is vetoed and the softer branchaid 183 discarded. The default parameters used for pruning [34] inp15 184 this study are  $z_{\text{cut}} = 0.1$  and  $R_{\text{cut}} = 0.5$ . One advantage of £16 185 pruning is that the thresholds used to veto soft, wide-angle17 186 radiation scale with the jet kinematics, and so the algorithm<sup>18</sup> 187 is expected to perform comparably over a wide range of mo219 188 menta. 220 189 221

Trimming: Given a jet, re-cluster the constituents into sub=222 jets of radius  $R_{\text{trim}}$  with the  $k_t$  algorithm. Discard all subjets<sup>223</sup> i with 224

$$p_{Ti} < f_{\rm cut} \, p_{TJ}. \tag{5}_{226}$$

The default parameters used for trimming [35] in this study<sup>227</sup> 191 are  $R_{\text{trim}} = 0.2$  and  $f_{\text{cut}} = 0.03$ . 192

Filtering: Given a jet, re-cluster the constituents into sub-<sup>230</sup> 194 jets of radius  $R_{\text{filt}}$  with the C/A algorithm. Re-define the jet<sup>231</sup> 195 to consist of only the hardest N subjets, where N is deter-196 mined by the final state topology and is typically one more<sup>233</sup> 197 than the number of hard prongs in the resonance decay (to<sup>234</sup> 198 include the leading final-state gluon emission) [36]. While<sup>235</sup> 199 we do not independently use filtering, it is an important step<sup>236</sup> 200 of the HEPTopTagger to be defined later. 201 238

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Soft drop: Given a jet, re-cluster all of the constituents using<sup>239</sup> the C/A algorithm. Iteratively undo the last stage of the  $C/A^{240}$ 241 clustering from j into subjets  $j_1$ ,  $j_2$ . If 242

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} < z_{\text{cut}} \left(\frac{\Delta R_{12}}{R}\right)^{\beta}, \qquad (6)_{244}^{243}$$

discard the softer subjet and repeat. Otherwise, take j to be<sub>246</sub> 203 the final soft-drop jet [37]. Soft drop has two input param<sub>247</sub> 204 eters, the angular exponent  $\beta$  and the soft-drop scale  $z_{\text{cut}_{248}}$ 205 with default value  $z_{\text{cut}} = 0.1$ . 206 249

#### 3.3 Jet Tagging Algorithms 207

Modified Mass Drop Tagger: Given a jet, re-cluster all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A clustering from j into subjets  $j_1, j_2$ with  $m_{j_1} > m_{j_2}$ . If either

$$m_{j_1} > \mu m_j \text{ or } \frac{\min(p_{T1}^2, p_{T2}^2)}{m_j^2} \Delta R_{12}^2 < y_{\text{cut}},$$
 (7)<sup>24</sup>

then discard the branch with the smaller transverse masses  $m_T = \sqrt{m_i^2 + p_{T_i}^2}$ , and re-define j as the branch with these

larger transverse mass. Otherwise, the jet is tagged. If declustering continues until only one branch remains, the jet is considered to have failed the tagging criteria [38]. In this study we use by default  $\mu = 1.0$  (i.e. implement no mass drop criteria) and  $y_{\text{cut}} = 0.1$ .

Johns Hopkins Tagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if its  $p_{\rm T}$  is less than  $\delta_p p_{\rm Tjet}$ . This continues until both prongs are harder than the  $p_{\rm T}$  threshold, both prongs are softer than the  $p_{\rm T}$  threshold, or if they are too close  $(|\Delta \eta_{ij}| + |\Delta \phi_{ij}| < \delta_R)$ ; the jet is rejected if either of the latter conditions apply. If both are harder than the  $p_{\rm T}$  threshold, the same procedure is applied to each: this results in 2, 3, or 4 subjets. If there exist 3 or 4 subjets, then the jet is accepted: the top candidate is the sum of the subjets, and W candidate is the pair of subjets closest to the W mass [12]. The output of the tagger is  $m_t$ ,  $m_W$ , and  $\theta_h$ , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the Wdecay products. The two free input parameters of the John Hopkins tagger in this study are  $\delta_p$  and  $\delta_R$ , defined above.

**HEPTopTagger:** Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if  $m_1/m_{12} > \mu$  (there is not a significant mass drop). Otherwise, both prongs are kept. This continues until a prong has a mass  $m_i < m$ , at which point it is added to the list of subjets. Filter the jet using  $R_{\text{filt}} = \min(0.3, \Delta R_{ij})$ , keeping the five hardest subjets (where  $\Delta R_{ij}$  is the distance between the two hardest subjets). Select the three subjets whose invariant mass is closest to  $m_t$  [11]. The output of the tagger is  $m_t$ ,  $m_W$ , and  $\theta_h$  (defined above). The two free input parameters of the HEPTopTagger in this study are m and  $\mu$ , defined above.

Top Tagging with Pruning or Trimming: For comparison with the other top taggers, we add a W reconstruction step to the pruning and trimming algorithms described above. A W candidate is found as follows: if there are two subjets, the highest-mass subjet is the W candidate (because the W prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the W candidate. In the case of only one subjet, no W is reconstructed.

#### 3.4 Other Jet Substructure Observables

Jet substructure observables are calculated using jet constituents prior to any grooming.

Qjet mass volatility: As described above, Qjet algorithms re-cluster the same jet non-deterministically to obtain a collection of interpretations of the jet. For each jet interpretation, the pruned jet mass is computed with the default pruning parameters. The mass volatility,  $\Gamma_{Qjet}$ , is defined as [32]

$$\sqrt{\langle m_J^2 \rangle - \langle m_J \rangle^2}$$

$$\Gamma_{\text{Qjet}} = \frac{\sqrt{m_J}}{\langle m_J \rangle}, \qquad (8)^{-1}$$

where averages are computed over the Qjet interpretations. 260

We use a rigidity parameter of  $\alpha = 0.1$  (although other stud<sub>280</sub> 261 ies suggest a smaller value of  $\alpha$  may be optimal [32, 33]), 262 and 25 trees per event for all of the studies presented here. 281 263 264 282

N-subjettiness: N-subjettiness [39] quantifies how well the283 radiation in the jet is aligned along N directions. To compute<sub>84</sub> N-subjettiness,  $\tau_N^{(\beta)}$ , one must first identify N axes within  $s_{s_s}$ the jet. Then, 286

$$\tau_N = \frac{1}{d_0} \sum_i p_{Ti} \min\left(\Delta R_{1i}^{\beta}, \dots, \Delta R_{Ni}^{\beta}\right), \qquad (9)_{289}^{289}$$

where distances are between particles i in the jet and the<sub>291</sub> axes, 292

$$d_0 = \sum_i p_{Ti} R^\beta \tag{10}^{293}$$

and R is the jet clustering radius. The exponent  $\beta$  is a free  $\beta_{96}$ 265 parameter. There is also some choice in how the axes used to27 266 compute N-subjettiness are determined. The optimal config<sub>298</sub> 267 uration of axes is the one that minimizes N-subjettiness; re<sub>299</sub> 268 cently, it was shown that the "winner-takes-all" (WTA) axesoo 269 can be easily computed and have superior performance com-270 pared to other minimization techniques [40]. We use both<sup>301</sup> 271 the WTA and one-pass  $k_t$  optimization axes in our analyses.<sup>302</sup> 272 303

A more powerful discriminant is often the ratio,

$$\tau_{N,N-1} \equiv \frac{\tau_N}{\tau_{N-1}}.\tag{11}^{305}$$

While this is not an infrared-collinear (IRC) safe observable<sub>306</sub> 273 it is calculable [41] and can be made IRC safe with a loose 274 lower cut on  $\tau_{N-1}$ . 275 307 276 308

Energy correlation functions: The transverse momentumos version of the energy correlation functions are defined as10 [42]: 311

where *i* is a particle inside the jet. It is preferable to work in terms of dimensionless quantities, particularly the energy correlation function double ratio:

$$C_N^{(\beta)} = \frac{\text{ECF}(N+1,\beta) \text{ECF}(N-1,\beta)}{\text{ECF}(N,\beta)^2}.$$
(13)

This observable measures higher-order radiation from leadingorder substructure. Note that  $C_2^{(0)}$  is identical to the variable PTD introduced by CMS in [43].

#### **4** Multivariate Analysis Techniques

Multivariate techniques are used to combine variables into an optimal discriminant, and the extent to which the discrimination power increases when this is done is used to indicate how much the discriminatory information present in the variables overlaps. An alternative strategy for studying correlations in discrimination power that is not explored here is "truth matching" [44].

In all cases the multivariate technique used to combine variables is a boosted decision tree (BDT) as implemented in the TMVA package [45]. We use the BDT implementation including gradient boost. An example of the BDT settings are as follows:

- Shrinkage=0.1

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- UseBaggedGrad=F
- nCuts=10000
- MaxDepth=3
- UseYesNoLeaf=F
- nEventsMin=200

Exact parameter values are chosen to best reduce the effect of overtraining. Additionally, the simulated data were split into training and testing samples and comparisons of the BDT output were compared to reduced the effect of overtraining as well.

#### **5** Quark-Gluon Discrimination

In this section, we examine the differences between quarkand gluon-initiated jets in terms of substructure variables, and to determine to what extent these variables are correlated. Along the way, we provide some theoretical understanding of these observables and their performance. The motivation for these studies comes not only from the desire to "tag" a jet as originating from a quark or gluon, but also to improve our understanding of the quark and gluon components of the QCD backgrounds relative to boosted resonances. While recent studies have suggested that quark/gluon

tagging efficiencies depend highly on the Monte Carlo gen366 317 erator used [46, 47], we are more interested in understanding. 318 the scaling performance with  $p_T$  and R, and the correlation **S68** 319 between observables, which are expected to be treated con-320 sistently within a single shower scheme. 370 321

#### 5.1 Methodology 322

374 These studies use the qq and gg MC samples, described pre-323 viously in Section 2. The showered events were clustered 324 with FASTJET 3.03 using the anti- $k_{\rm T}$  algorithm with jet radii 325 of R = 0.4, 0.8, 1.2. In both signal (quark) and background 326 (gluon) samples, an upper and lower cut on the leading jet 327  $p_T$  is applied after showering/clustering, to ensure similar 328  $p_T$  spectra for signal and background in each  $p_T$  bin. The 329 bins in leading jet  $p_T$  that are considered are 300-400 GeV,<sup>370</sup> 330 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 331 GeV, 1.0-1.1 TeV parton  $p_T$  slices respectively. Various jet 332 grooming approaches are applied to the jets, as described  $in_{382}^{382}$ 333 Section 3.4. Only leading and subleading jets in each sam-334 ple are used. The following observables are studied in this 335 section: 336 385

- The number of constituents  $(N_{\text{constits}})$  in the jet. 337
- The pruned Qjet mass volatility,  $\Gamma_{Qjet}$ . 338
- 339

 1-point energy correlation functions, C<sub>1</sub><sup>β</sup> with β = 0, 1, 2<sup>388</sup>
 1-subjettiness, τ<sub>1</sub><sup>β</sup> with β = 1, 2. The *N*-subjettiness axe<sup>389</sup> are computed using one-pass k<sub>t</sub> axis optimization. 340

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The ungroomed jet mass, m. 342

We will see below that, in terms of their jet-by-jet corre<sup>393</sup> 343 lations and their ability to separate quark initiated jets from<sup>394</sup> 344 gluon initiated jets (hereafter called simply quark jets and 345 gluon jets), these observables fall into five classes. The  $\mathsf{first}_{\mathtt{96}}$ 346 three,  $N_{\text{constits}}$ ,  $\Gamma_{\text{Qjet}}$  and  $C_1^{\beta=0}$ , form classes by themselves<sub>97</sub> 347 (Classes I to III) in the sense that they each carry some inde398 348 pendent information about a jet and, when combined, pro399 349 vide substantially better quark jet and gluon jet separation. 350 than either observable by itself. Of the remaining  $observ_{401}$ 351 ables,  $C_1^{\beta=1}$  and  $\tau_1^{\beta=1}$  comprise a single class (Class IV)<sub>02</sub> in the sense that they exhibit similar distributions when ap<sub>403</sub> 352 353 plied to a sample of jets, their jet-by-jet values are highly 104 354 correlated, they exhibit very similar power to separate quarkos 355 jets and gluon jets (with very similar dependence on the jeto6 356 parameters R and  $p_T$ ) and this separation power is essentator 357 tially unchanged when they are combined. The fifth classos 358 (Class V) is composed of  $C_1^{\beta=2}$ ,  $\tau_1^{\beta=2}$  and the (ungroomed)<sup>99</sup> 359 jet mass. Again the issue is that jet-by-jet correlations are10 360 strong (even though the individual observable distributions11 361 are somewhat different), quark versus gluon separation power2 362 is very similar (including the R and  $p_T$  dependence) and lit<sup>413</sup> 363 tle is achieved by combining more than one of these ob#14 364 servables. This class structure is not surprising given that15 365

within a class the observables exhibit very similar dependence on the kinematics of the underlying jet constituents. For example, the members of Class V are constructed from of a sum over pairs of constituents using products of the energy of each member of the pair times the angular separation squared for the pair (for the mass case think in terms of mass squared with small angular separations). By the same argument the Class IV and Class V observables will be seen to be more similar than any other pair of classes, differing only in the power  $(\beta)$  of the dependence on the angular separations, which will produce small but detectable differences. We will return to a more complete discussion of jet masses at the end of Section 5.

#### 5.2 Single Variable Discrimination

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The quark and gluon distributions of different substructure observables are shown in Figure 1, which already illustrates at least some of the points about the Classes made above. At a fundamental level the primary difference between quark jets and gluon jets is the color charge of the initiating parton, typically expressed in terms of the ratio of the corresponding Casimir factors  $C_F/C_A = 4/9$ . Since the quark has the smaller color charge, it will radiate less than a corresponding gluon and the resulting jet will contain fewer constituents. This difference is clearly indicated in Figure 1(a), suggesting that simply counting constituents will provide good separation between quark and gluon jets. In fact, among the observables considered, one can see by eye that N<sub>constits</sub> should provide the highest separation power, i.e., the quark and gluon distributions are most distinct, as was originally noted in [47, 48]. Figure 1 further suggests that  $C_1^{\bar{\beta}=0}$  should provide the next best separation followed by  $C_1^{\beta=1}$ , as was also found by the CMS and ATLAS Collaborations[46, 49].

To more quantitatively study the power of each observable as a discriminator for quark/gluon tagging, ROC curves are built by scanning each distribution and plotting the background efficiency (to select gluon jets) vs. the signal efficiency (to select quark jets). Figure 2 shows these ROC curves for all of the substructure variables shown in Figure 1, along with the ungroomed mass, representing the best performing mass variable, for R=0.4, 0.8 and 1.2 jets in the  $p_T = 300 - 400$  GeV bin. In addition, the ROC curve for a tagger built from a BDT combination of all the variables (see Section 4) is shown. Clearly, and as suggested earlier,  $n_{\text{constits}}$  is the best performing variable for all Rs, even though  $C_1^{\beta=0}$  is close, particularly for R=0.8. Most other variables have similar performance, except  $\Gamma_{\text{Oiet}}$ , which shows significantly worse discrimination (this may be due to our choice of rigidity  $\alpha = 0.1$ , with other studies suggesting that a smaller value, such as  $\alpha = 0.01$ , produces better results[32, 33]). The combination of all variables shows somewhat bet-

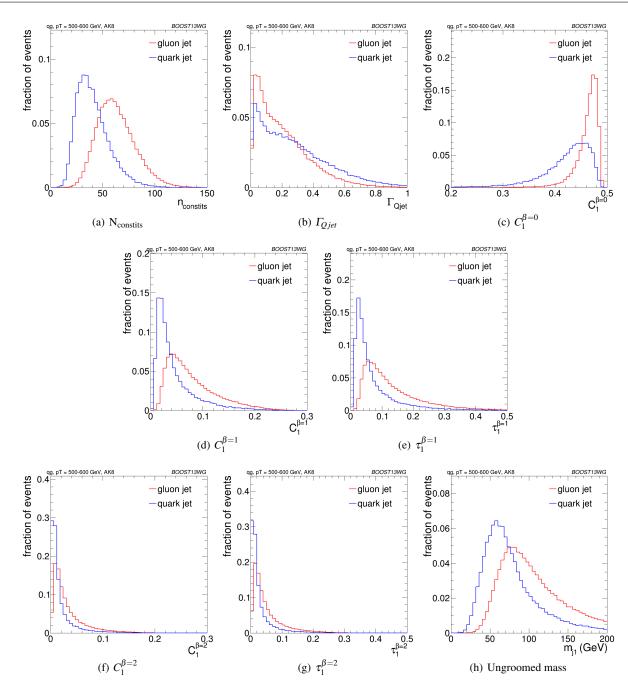


Fig. 1 Comparisons of quark and gluon distributions of different substructure variables (organized by Class) for leading jets in the  $p_T = 500 - 600$  GeV bin using the anti- $k_T R = 0.8$  algorithm.

ter discrimination, and we will discuss in more detail belowi25
the correlations between the observables and their impact on 26
the combined discrimination power. 427

We now examine how the performance of the substructure observables changes with  $p_T$  and R. To present the results in a "digestible" fashion we will focus on the gluon jet "rejection" factor,  $1/\varepsilon_{bkg}$ , for a quark signal efficiency,  $\varepsilon_{sig}$ , of 50%. We can use the values of  $1/\varepsilon_{bkg}$  generated for the 9 kinematic points introduced above (R = 0.4, 0.8, 1.2 and the 100 GeV  $p_T$  bins with lower limits  $p_T = 300$  GeV, 500 GeV, 1000 GeV) to generate surface plots. The surface plots in Figure 3 indicate both the level of gluon rejection and the variation with  $p_T$  and R for each of the studied single observable. The color shading is defined so that a change in color corresponds to a change of about 0.4 in  $1/\varepsilon_{bkg}$ . The colors have the same correlation with the magnitude of  $1/\varepsilon_{bkg}$  in all of the plots, but repeat after a change of about 4. Thus "blue" corresponds to a value of about 2.5 in Fig-

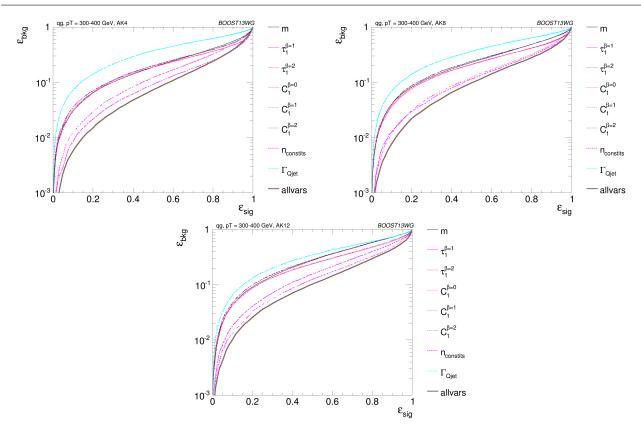


Fig. 2 The ROC curve for all single variables considered for quark-gluon discrimination in the  $p_T$  300-400 GeV bin using the anti- $k_T$  R=0.4, 0.8 and 1.2 algorithm.

ure 3(b) and the values 6.5 and 10.5 in Figure 3(a), while 30 "yellow" corresponds to about 5 in Figures 3(c) to (h) and 60 about 9 in Figure 3(a).

We see, as expected, that the numerically largest rejec-462 437 tion rates occur for the observable  $N_{\text{constits}}$  in Figure 3(a),<sup>463</sup> 438 where the rejection factor is in the range 6 to 11 and varies 439 rather dramatically with R. As R increases the jet collects 440 more constituents from the underlying event, which are the  $^{\rm 466}$ 441 same for quark and gluon jets, and the separation power de-467 442 creases. At large R, there is some improvement with increas-443 ing  $p_T$  due to the enhanced radiation, which does distinguish 444 quarks from gluons. Figure 3(b) confirms the limited effi469 445 cacy of the single observable  $\Gamma_{Qjet}$  (at least for our parame<sub>470</sub> 446 ter choices) with a rejection rate only in the range 2.5 to 2.8471 447 On the other hand, this observable probes a very different<sub>72</sub> 448 property of jet substructure, *i.e.*, the sensitivity to detailed<sub>73</sub> 449 changes in the grooming procedure, and this difference is74 450 suggested by the distinct R and  $p_T$  dependence illustrated<sub>475</sub> 451 in Figure 3(b). The rejection rate increases with increasing<sub>476</sub> 452 R and decreasing  $p_T$ , since the distinction between quark<sub>177</sub> 453 and gluon jets for this observable arises from the relative<sub>78</sub> 454 importance of the one "hard" gluon emission configuration479 455 The role of this contribution is enhanced for both decreasing 456  $p_T$  and increasing R. Figure 3(c) indicates that the observ<sub>281</sub> 457 able  $C_1^{\beta=0}$  can, by itself, provide a rejection rate in the range 458

7.8 to 8.6 (intermediate between the two previous observables) and again with distinct *R* and  $p_T$  dependence. In this case the rejection rate decreases slowly with increasing *R* ( $\beta = 0$  explicitly means that the angular dependence is much reduced), while the rejection rate peaks at intermediate  $p_T$  values (an effect visually enhanced by the limited number of  $p_T$  values included). Both the distinct values of the rejection rates and the differing *R* and  $p_T$  dependence serve to confirm that these three observables tend to probe independent features of the quark and gluon jets.

Figures 3(d) and (e) serve to confirm the very similar properties of the Class IV observables  $C_1^{\beta=1}$  and  $\tau_1^{\beta=1}$  (as already suggested in Figures 1(d) and (e)) with essentially identical rejection rates (4.1 to 5.4) and identical *R* and  $p_T$ dependence (a slow decrease with increasing *R* and an even slower increase with increasing  $p_T$ ). A similar conclusion for the Class V observables  $C_1^{\beta=2}$ ,  $\tau_1^{\beta=2}$  and *m* with similar rejection rates in the range 3.5 to 5.3 and very similar *R* and  $p_T$  dependence (a slow decrease with increasing *R* and an even slower increase with increasing  $p_T$ ). Arguably, drawing a distinction between the Class IV and Class V observables, is a fine point, but the color shading does suggest some distinction from the slightly smaller rejection rate in Class V. Again the strong similarities between the plots

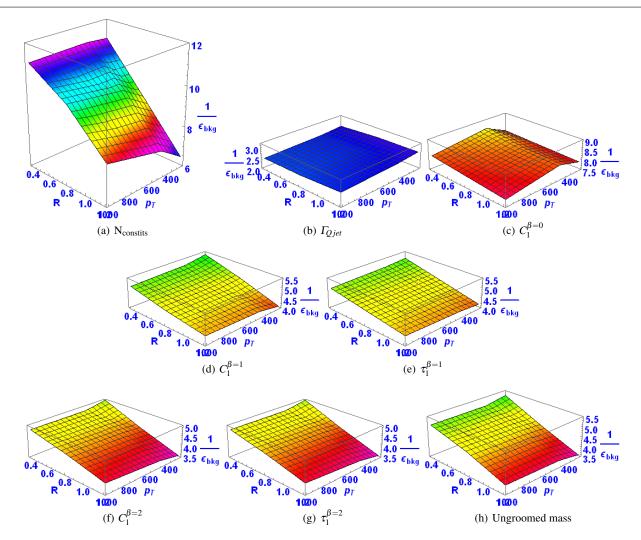


Fig. 3 Surface plots of  $1/\varepsilon_{bkg}$  for all single variables considered for quark-gluon discrimination as functions of R and  $p_T$ .

within the second and third rows in Figure 3 speaks to thas common properties of the observables within the two classes.

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In summary, the overall discriminating power between<sub>503</sub> 485 quark and gluon jets tends to decrease with increasing  $R_{504}$ 486 except for the  $\Gamma_{Qjet}$  observable, presumably primarily due 505487 to the increasing contamination from the underlying event<sub>506</sub> 488 Since the construction of the  $\Gamma_{Qjet}$  observable explicitly in **507** 489 volves pruning away the soft, large angle constituents, it isos 490 not surprising that it exhibits different R dependence. In gen<sub>509</sub> 491 eral the discriminating power increases slowly and mono<sub>B10</sub> 492 tonically with  $p_T$  (except for the  $\Gamma_{Qjet}$  and  $C_1^{\beta=0}$  observ<sub>511</sub> 493 ables) presumably because there is overall more (color charge2 494 related) radiation as  $p_T$  increasing providing some increase13 495 in discrimination (except for the  $\Gamma_{Qjet}$  observable). We turn<sub>14</sub> 496 now to the question of the impact of employing more than15 497 one observable at a time. 516 498

5.3 Combined Performance and Correlations

The quark/gluon tagging performance can be further improved over cuts on single observables by combining multiple observables in a BDT; due to the challenging nature of q/g-tagging, any improvement in performance with multivariable techniques could be critical for certain analyses, and the improvement could be more substantial in data than the marginal benefit found in MC and shown in Fig. 2. Furthermore, insight can be gained into the features allowing for quark/gluon discrimination if the origin of the improvement is understood. To quantitatively study this improvement, we build quark/gluon taggers from every pair-wise combination of variables studied in the previous section for comparison with the all-variable combination. To illustrate the results achieved in this way we will exhibit the same sort 2D of surface plots as in Figure 3. Based on our discussion of the correlated properties of observables within a single class, we expect little improvement in the rejection

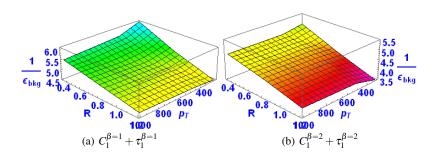


Fig. 4 Surface plots of  $1/\epsilon_{bkg}$  for the indicated pairs of variables from Classes IV and V considered for quark-gluon discrimination as functions of *R* and  $p_T$ .

rate when combining observables from the same class and **5**18 substantial improvement when combining observables from **5**18 different classes. **5**58

Figure 4 shows pairwise plots for (a) Class IV and (b)<sup>559</sup> 520 Class V. Comparing to the corresponding plots in Figure 3<sup>60</sup> 521 we see that combining  $C_1^{\beta=1} + \tau_1^{\beta=1}$  provides a small im-522 provement in the rejection rate of about 10% (0.5 out of 523 5) with essentially no change in the *R* and  $p_T$  dependence,<sup>563</sup> 524 while combining  $C_1^{\beta=2} + \tau_1^{\beta=2}$  yields a rejection rate that is 525 essentially identical to the single observable rejection rate 526 for all R and  $p_T$  values (with a similar conclusion if one of 527 these observables is replaced with the ungroomed jet mass 528 *m*). This again confirms that expectation that the observables 569529 within a single class effectively probe the *same* jet proper-530 ties. 531 571

Next we consider the cross-class pairs of observables in 572 532 dicated in Figure 5, where only one member of Classes IV573 533 and V is included. As expected the largest rejection rates are 534 obtained from combining another observable with N<sub>constits</sub> 535 (Figures 5(a) to (d)). In general, the rates are larger than<sub>74</sub> 536 for the single variable case with similar R and  $p_T$  depen-537 dence. In particular, the pair  $N_{constits} + C_1^{\beta=1}$  yields rejection  $\mathbf{F75}$ 538 rates in the range 6.4 to 14.7 (6.4 to 15 for the similar case<sup>76</sup> 539  $N_{\text{constits}} + \tau_1^{\beta=1}$  with the largest values at small *R* and large<sup>77</sup> 540  $p_T$ . The other pairings with N<sub>constits</sub> (except with  $\tau_1^{\beta=1}$ ) yield<sup>578</sup> 541 smaller rejection rates and smaller dynamic range. The pair<sup>579</sup> 542  $N_{\text{constits}} + C_1^{\beta=0}$  (Figure 5(d)) exhibits the smallest range of 543 rates (8.3 to 11.3) suggesting that the differences between the substantial three the  $p^{582}$ 544 these two observables serve to substantially reduce the R545 and  $p_T$  dependence for the pair, but this also reduces the 546 possible optimization. The other pairs indicated exhibit sim-547 ilar behavior. The pair rejection rates are somewhat better 548 than either observable alone (since we are always combin-549 ing from different classes), and the R and  $p_T$  dependence is 550 generally similar to the more variant single observable case. 551 The smallest *R* and  $p_T$  variation always occurs when pairing 552 with  $C_1^{\beta=0}$ . Changing any of the observables in these pairs 553 with a different observable in the same class (*e.g.*,  $C_1^{\beta=2}$  for  $f_{92}$ 554  $\tau_1^{\beta=2}$  produces very similar results (at the few percent level) 593 555

Figure 5(k) shows the result of a BDT analysis including all of the current observables with rejection rates in the range 10.5 to 17.1. This is a somewhat narrower range than in Figure 5(b) but with somewhat larger maximum values.

Another way to present the same data but by fixing R and  $p_T$  and showing all single observables and pairs of observables at once is in terms of the "matrices" indicated in Figures 6 and 7. The numbers in each cell are the now familiar rejection factor values of  $1/\varepsilon_{bkg}$  (gluons) for  $\varepsilon_{sig} = 50\%$  (quarks). Figure 6 corresponds  $p_T = 1 - 1.1$  TeV and R = 0.4, 0.8, 1.2, while Figure 7 is for R = 0.4 and the 3  $p_T$  bins. The actual numbers should be familiar from the discussion above with the single observable rejections rates appearing on the diagonal and the pairwise results off the diagonal. The correlations indicated by the shading should be largely understood as indicating the organization of the observables into the now familiar classes. The all-observable (BDT) result appears as the number at the lower right in each plot.

#### 5.4 QCD Jet Masses

To close the discussion of the tagging of jets as either quark jets or gluon jets we provide some insight into the behavior of the masses of such QCD jets, both with and without grooming. Recall that, in practice, an identified jet is simply a list of constituents, *i.e.*, final state particles. To the extent that the masses of these individual constituents are irrelevant, typically because the detected constituents are relativistic, each constituent has a "well" defined 4-momentum. It follows that the 4-momentum of the jet is simply the sum of the 4-momenta of the constituents and its square is the jet mass squared. We have already seen one set of jet mass distributions in Figure 1(h) for quark and gluon jets found with the anti- $k_{\rm T}$  algorithm with R = 0.8 and  $p_T$  in the bin 500-600 GeV. If we consider the mass distributions for other kinematic points (other values of R and  $p_T$ ), we observe considerable variation but that variation can largely be removed by plotting versus the scaled variable  $m/p_T/R$ . Simply on dimensional grounds we know that jet mass must scale essentially linearly with  $p_T$ , with the remaining  $p_T$ 

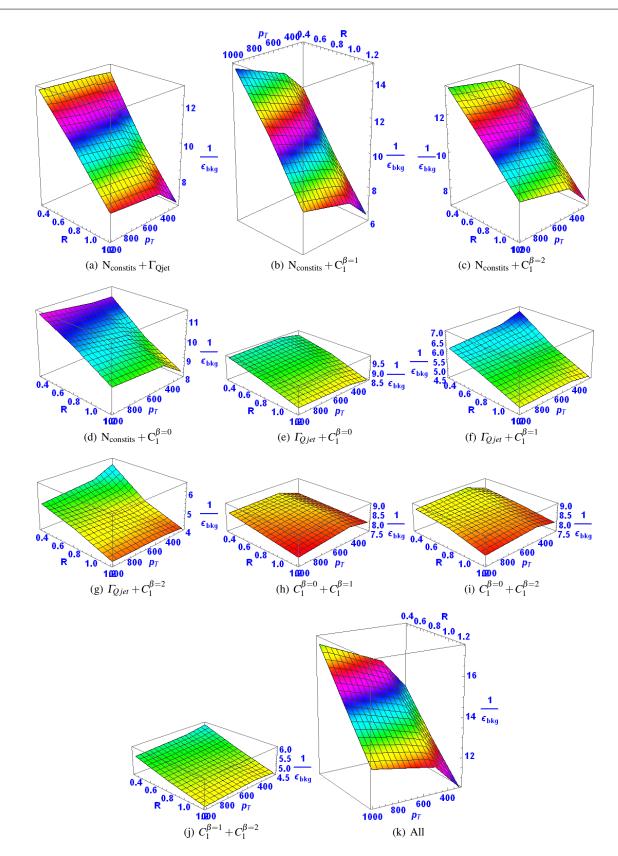


Fig. 5 Surface plots of  $1/\varepsilon_{\text{bkg}}$  for the indicated pairs of variables from different classes considered for quark-gluon discrimination as functions of R and  $p_T$ .

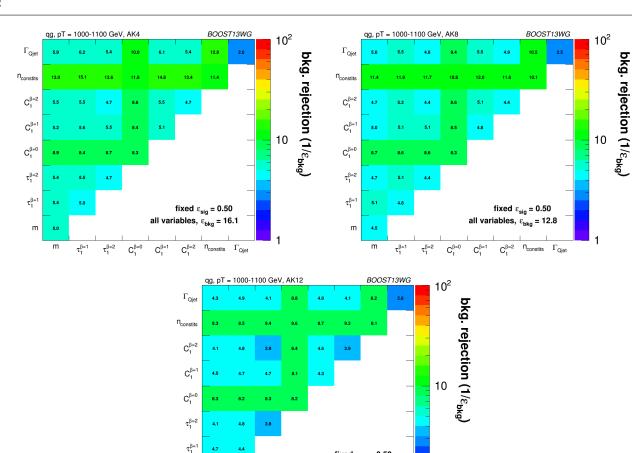


Fig. 6 Gluon rejection defined as  $1/\varepsilon_{gluon}$  when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for jets with  $p_T = 1 - 1.1$  TeV and for (top left) R = 0.4; (top right) R = 0.8; (bottom) R = 1.2. The rejection obtained with a tagger that uses all variables is also shown in the plots.

fixed  $\varepsilon_{sig} = 0.50$ 

 $\epsilon_{bkg}$  = 11.5

n<sub>constits</sub> Γ<sub>Qjet</sub>

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variables.

 $C_1^{\beta=2}$ 

dependence arising predominantly from the running of the12 594 coupling,  $\alpha_s(p_T)$ . The R dependence is also crudely lin<sub>513</sub> 595 ear as the mass scales approximately with the largest anoia 596 gular opening between any 2 constituents and that is seti15 597 by R. The mass distributions for quark and gluon jets versis 598 sus  $m/p_T/R$  for all of our kinematic points are indicated in 17 599 Figure 8, where we use a logarithmic scale on the y-axis18 600 to clearly exhibit the behavior of these distributions over a19 601 large dynamic range. We observe that the distributions for E20 602 the different kinematic points do approximately scale, *i.e.*<sup>621</sup> 603 the simple arguments above do capture most of the variation22 604 with R and  $p_T$ . We will consider shortly an explanation of  $p_{23}$ 605 the residual non-scaling. A more quantitative understanding24 606 607 of jet mass distributions requires all-orders calculations in25 QCD, which have been performed for ungroomed jet massage 608 spectra at high logarithmic accuracy, both in the context of 27 609 direct QCD resummation [50, 51] and Soft Collinear Effec 628 610 tive Theory [52, 53]. 611 629

m 4.0

m

 $\tau_1^{\beta=1}$   $\tau_1^{\beta=2}$   $C_1^{\beta=0}$   $C_1^{\beta=1}$ 

Several features of Figure 8 can be easily understood. The distributions all cut-off rapidly for  $m/p_T/R > 0.5$ , which is understood as the precise limit (maximum mass) for a jet composed of just 2 constituents. As expected from the soft and collinear singularities in QCD, the mass distribution peaks at small mass values. The actual peak is "pushed" away from the origin by the so-called Sudakov form factor. Summing the corresponding logarithmic structure (singular in both  $p_T$  and angle) to all orders in perturbation theory yields a distribution that is highly damped as the mass vanishes. In words, there is precisely zero probability that a color parton emits no radiation (and the resulting jet has zero mass). The large mass "shoulder"  $(0.3 < m/p_T/R < 0.5)$  is driven largely by the presence of a single large angle, energetic emission in the underlying QCD shower, *i.e.*, this regime is quite well described by low-order perturbation theory. (The shoulder label will be more clear after we groom the jet.) In contrast, we should think of the peak region as corresponding to multiple soft emissions. This simple (ap-

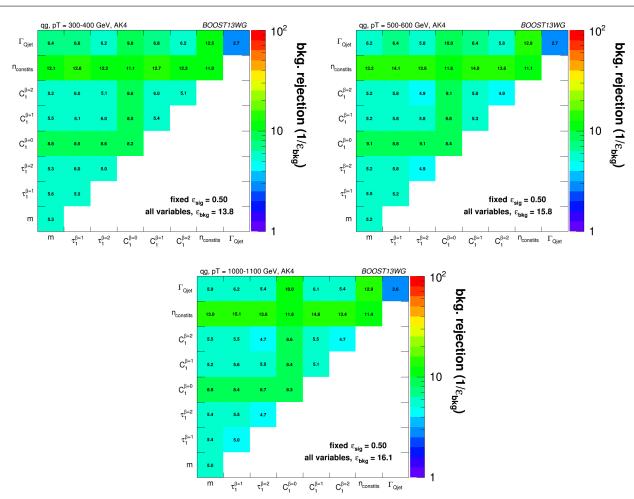


Fig. 7 Gluon rejection defined as  $1/\varepsilon_{gluon}$  when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for R=0.4 jets with (top left)  $p_T = 300 - 400$  GeV, (top right)  $p_T = 500 - 600$  GeV and (bottom)  $p_T = 1 - 1.1$  TeV. The rejection obtained with a tagger that uses all variables is also shown in the plots.

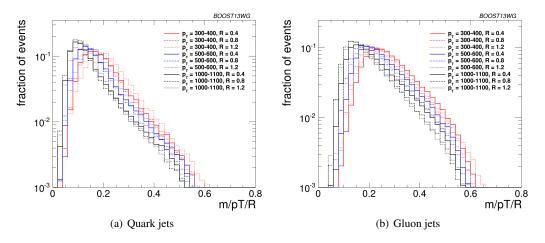


Fig. 8 Comparisons of quark and gluon ungroomed mass distributions versus the scaled variable  $m/p_T/R$ .

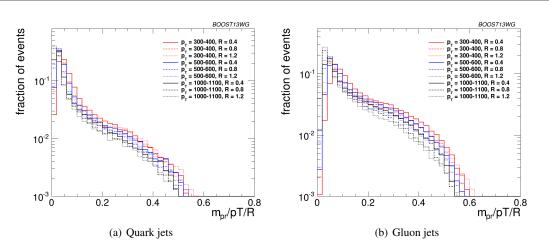


Fig. 9 Comparisons of quark and gluon pruned mass distributions versus the scaled variable  $m_{pr}/p_T/R$ .

proximate) picture provides an understanding of the bulk of 677 631 the differences between the quark and gluon jet mass distrisos 632 butions. Since the probability of the single large angle, ener-633 getic emission is proportional to the color charge, the gluonaro 634 distribution should be enhanced in this region by a factor 635 of about  $C_A/C_F = 9/4$ , consistent with what is observed in 72 636 Figure 8. Similarly the exponent in the Sudakov damping 637 factor for the gluon jet mass distribution is enhanced by the 638 same factor, leading to a peak "pushed" further from the 674 639 origin. So the gluon jet mass distribution exhibits a larger<sup>675</sup> 640 average jet mass than the quark jet, with a larger relative 641 contribution arising from the perturbative shoulder region.<sup>677</sup> 642 Recall also that the number of constituents in the jet is also<sup>678</sup> 643 larger (on average) for the gluon jet simply because a gluon<sup>679</sup> 644 will radiate more than a quark. These features explain much<sup>680</sup> 645 of what we observed earlier in terms of the effectiveness<sup>681</sup> 646 of the various observable to separate quark jets from gluons 647 jets. Note in particular that the enhanced role of the shoulder 648 for gluon jet explains, at least qualitatively, the difference in 649 the distributions for the observable  $\Gamma_{Qjet}$ . Since the shoul-650 der is dominated by a single large angle, hard emission, it 651 is minimally impacted by pruning, which removes the large 652 angle, soft constituents (as illustrated just below). Thus jets 653 in the shoulder exhibit small volatility and they are a larger 654 component in the gluon jet distribution. Hence gluon jets, 655 on average, have smaller values of  $\Gamma_{Qjet}$  than quark jets as 656 in Figure 1(b). Further this feature of gluon jets is distinct<sup>692</sup> 657 from fact that there are more constituents, which explains 658 why  $\Gamma_{Qjet}$  and N<sub>constits</sub> supply largely independent informa-659 tion for distinguishing quark and gluon jets. 660 696

To illustrate some of these points in more detail, Fig597 ure 9 exhibits the jet mass distributions (of Figure 8) *af*598 *ter pruning* [34, 54]. Removing the large angle, soft con599 stituents moves the peak in both of the distributions from500 *m*/*p*<sub>T</sub>/*R* ~ 0.1 - 0.2 to the region around *m*/*p*<sub>T</sub>/*R* ~ 0.05701 This explains why pruning works to reduce the QCD back702 ground when looking for a signal in a specific jet mass bin. The "shoulder" feature is much more apparent after pruning, as is the larger shoulder for the gluon jets. A quantitative (all-orders) understanding of groomed mass distributions is also possible. For instance, resummation of the pruned mass distribution was achieved in [38, 55].

Our final topic in this section is the residual R and  $p_T$ dependence exhibited in Figures 8 and 9, where we are using the scaled variable  $m/p_T/R$ . As already suggested, the residual  $p_T$  dependence can be understood as arising primarily from the slow decrease of the strong coupling  $\alpha_s(p_T)$  as  $p_T$  increases. This will lead to a corresponding decrease in the (largely perturbative) shoulder regime for both distributions as  $p_T$  increases. At the same time, and for the same reason, the Sudakov damping is less strong with increasing  $p_T$  and the peak moves towards the origin. Thus the overall impact of increasing  $p_T$  for both distributions is a (slow) shift to smaller values of  $m/p_T/R$ . This is just what is observed in Figures 8 and 9, although the numerical size of the effect is reduced in the pruned case. The R dependence is more complicated as there are effectively three different contributions to the mass distribution. The perturbative large angle, energetic single emission contribution largely scales in the variable  $m/p_T/R$ , which is why we see little residual R dependence in either figure for  $m/p_T/R > 0.4$ . The large angle soft emissions can both contribute at mass values that scale like R and increase in number as R increases (*i.e.*, as the area of the jet grows as  $R^2$ ). Such contributions can yield a distribution that moves to the right as R increases and presumably explain the behavior at small  $p_T$  in Figure 8. Since pruning largely removes this contribution, we observe no such behavior in Figure 9. The contribution of small angle, soft emissions will be at fixed m values and thus shift to the left versus the scaled variable as R increases. This presumably explains the small shifts in this direction observed in both figures.

#### 703 5.5 Conclusions

In Section 5 we have seen that a variety of jet observables<sub>51</sub> 704 provide information about the jet that can be employed ef752 705 fectively to separately tag quark and gluon jets. Further, whena 706 used in combination, these observables can provide events 707 better separation. We saw that the best performing single<sub>55</sub> 708 observable is simply the number of constituents in the jet<sub>756</sub> 709  $N_{constits}$ , while the largest further improvement comes from  $_{57}$ 710 combining with  $C_1^{\beta=1}$  (or  $\tau_1^{\beta=1}$ ), but the smallest *R* and  $p_{T^{58}}$ 711 dependence arises from combining with  $C_1^{\beta=0}$ . On the other<sup>59</sup> 712 hand, some of the commonly used observables are highly<sup>60</sup> 713 correlated and do not provide extra information and enhanced 714 tagging when used together. We have both demonstrated these<sup>1</sup> 715 correlations and provided a discussion of the physics behind<sup>62</sup> 716 the structure of the correlation. In particular, using the jet<sup>63</sup> 717 mass as a specific example observable we have tried to ex<sup>764</sup> 718 plicitly explain the differences between jets initiated by both<sup>65</sup> 719 quarks and gluons. 766 720

#### 721 6 Boosted W-Tagging

In this section, we study the discrimination of a boosted<sup>71</sup> 722 hadronically decaying W signal against a gluon background,772 723 comparing the performance of various groomed jet masses,773 724 substructure variables, and BDT combinations of groomed 725 mass and substructure. A range of different distance param-726 eters R for the anti- $k_{\rm T}$  jet algorithm are explored, as well as<sub>74</sub> 727 a variety of kinematic regimes (lead jet  $p_T$  300-400 GeV, 728 500-600 GeV, 1.0-1.1 TeV). This allows us to determiners 729 the performance of observables as a function of jet radius76 730 and jet boost, and to see where different approaches mayrr 731 break down. The groomed mass and substructure variables78 732 are then combined in a BDT as described in Section 4, and 79 733 the performance of the resulting BDT discriminant explored<sub>80</sub> 734 through ROC curves to understand the degree to which vari781 735 ables are correlated, and how this changes with jet boost and 82 736 jet radius. 737 783

### 738 6.1 Methodology

These studies use the WW samples as signal and the dijetese 739 gg as background, described previously in Section 2. Whilstes 740 only gluonic backgrounds are explored here, the conclusions90 741 as to the dependence of the performance and correlations on<sup>91</sup> 742 the jet boost and radius are not expected to be substantially 32 743 different for quark backgrounds; we will see that the dif793 744 ferences in the substructure properties of quark- and gluon794 745 initiated jets, explored in the last section, are significantly'95 746 smaller than the differences between W-initiated and gluon796 747 initiated jets. 797 748

As in the q/g tagging studies, the showered events were stared with EASTLET 3.03 using the anti  $k_{\rm T}$  algorithm

clustered with FASTJET 3.03 using the anti- $k_T$  algorithm with jet radii of R = 0.4, 0.8, 1.2. In both signal and background samples, an upper and lower cut on the leading jet  $p_T$  is applied after showering/clustering, to ensure similar  $p_T$  spectra for signal and background in each  $p_T$  bin. The bins in leading jet  $p_T$  that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton  $p_T$  slices respectively. The jets then have various grooming approaches applied and substructure observables reconstructed as described in Section 3.4. The substructure observables studied in this section are:

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- The ungroomed, trimmed (*m*<sub>trim</sub>), and pruned (*m*<sub>prun</sub>) jet masses.
- The mass output from the modified mass drop tagger  $(m_{\rm mmdt})$ .
- The soft drop mass with  $\beta = -1, 2 (m_{sd})$ .
- 2-point energy correlation function ratio  $C_2^{\beta=1}$  (we also studied  $\beta = 2$  but do not show its results because it showed poor discrimination power).
- *N*-subjettiness ratio  $\tau_2/\tau_1$  with  $\beta = 1$  ( $\tau_{21}^{\beta=1}$ ) and with axes computed using one-pass  $k_t$  axis optimization (we also studied  $\beta = 2$  but did not show its results because it showed poor discrimination power).
- The pruned Qjet mass volatility,  $\Gamma_{Qjet}$ .

#### 6.2 Single Variable Performance

In this section we will explore the performance of the various groomed jet mass and substructure variables in terms of discriminating signal and background. Since we have not attempted to optimise the grooming parameter settings of each grooming algorithm, we do not want to place too much emphasis here on the relative performance of the groomed masses, but instead concentrate on how their performance changes depending on the kinematic bin and jet radius considered.

Figure 10 the compares the signal and background in terms of the different groomed masses explored for the anti- $k_{\rm T}$  R=0.8 algorithm in the  $p_T$  500-600 bin. One can clearly see that in terms of separating signal and background the groomed masses will be significantly more performant than the ungroomed anti- $k_{\rm T}$  R=0.8 mass. Figure 11 compares signal and background in the different substructure variables explored for the same jet radius and kinematic bin.

Figures 12, 13 and 14 show the single variable ROC curves compared to the ROC curve for a BDT combination of all the variables (labelled "allvars"), for each of the anti- $k_{\rm T}$  distance parameters considered in each of the kinematic bins. One can see that, in all cases, the "allvars" option is considerably better performant than any of the individual

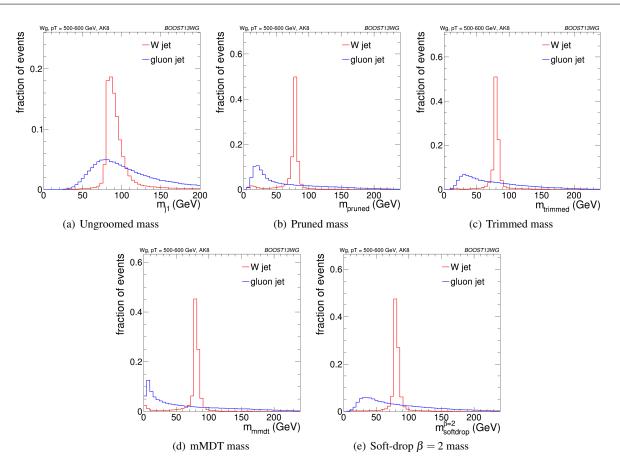


Fig. 10 Comparisons of the QCD background to the WW signal in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm: leading jet mass distributions.

single variables considered, indicating that there is considered
erable complementarity between the variables, and this will
be explored further in the next section.

Although the ROC curves give all the relevant informa<sup>824</sup> 801 tion, it is hard to compare performance quantitatively. In225 802 Figures 15, 16 and 17 are shown matrices which give the26 803 background rejection for a signal efficiency of 70% when27 804 two variables (that on the x-axis and that on the y-axis) ar@28 805 combined in a BDT. These are shown separately for each29 806  $p_T$  bin and jet radius considered. In the final column of 30807 these plots are shown the background rejection performance31 808 for three-variable BDT combinations of  $m_{sd}^{\beta=2} + C_2^{\beta=1} + X^{832}$ 809 These results will be discussed later in Section 6.3.3. The<sup>33</sup> 810 diagonal of these plots correspond to the background rejec<sup>834</sup> 811 tions for a single variable BDT, and can thus be examined to35 812 get a quantitative measure of the individual single variable<sup>36</sup> 813 performance, and to study how this changes with jet radius<sup>37</sup> 814 and momenta. 815

One can see that in general the most performant single<sup>39</sup> variables are the groomed masses. However, in certain kine<sup>940</sup> matic bins and for certain jet radii,  $C_2^{\beta=1}$  has a background<sup>41</sup> rejection that is comparable to or better than the groomed<sup>42</sup> masses.

By comparing Figures 15(a), 16(a) and 17(b), we can see how the background rejection performance evolves as we increase momenta whilst keeping the jet radius fixed to R=0.8. Similarly, by comparing Figures 15(b), 16(b) and 17(c) we can see how performance evolves with  $p_T$  for R=1.2. For both R=0.8 and R=1.2 the background rejection power of the groomed masses increases with increasing  $p_T$ , with a factor 1.5-2.5 increase in rejection in going from the 300-400 GeV to 1.0-1.1 TeV bins. In Figure 18 we show the Soft-drop  $\beta = 2$  groomed mass and the pruned mass for signal and background in the  $p_T$  300-400 and  $p_T$  1.0-1.1 TeV bins for R=1.2 jets. Two effects result in the improved performance of the groomed mass at high  $p_T$ . Firstly, as is evident from the figure, the resolution of the signal peak after grooming improves, because the groomer finds it easier to pick out the hard signal component of the jet against the softer components of the underlying event when the signal is boosted. Secondly, one can see from Figure 9 that as  $p_T$ increases the perturbative shoulder of the gluon distribution decreases in size, as discussed in Section 5.4, and thus there is a slight decrease (or at least no increase) in the level of background in the signal mass region  $(m/p_T/R \sim 0.5)$ .

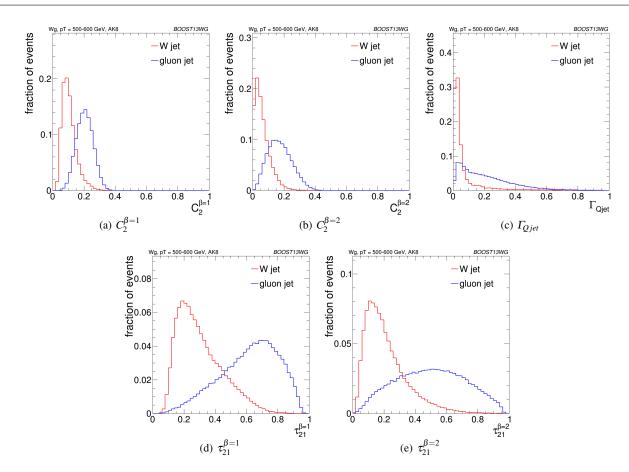


Fig. 11 Comparisons of the QCD background to the WW signal in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm: substructure variables.

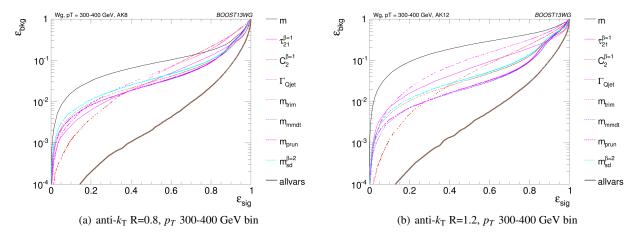


Fig. 12 The ROC curve for all single variables considered for W tagging in the  $p_T$  300-400 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.

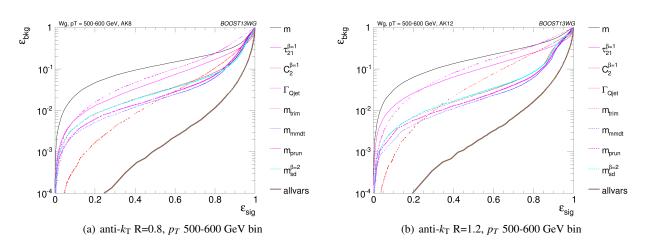


Fig. 13 The ROC curve for all single variables considered for W tagging in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.

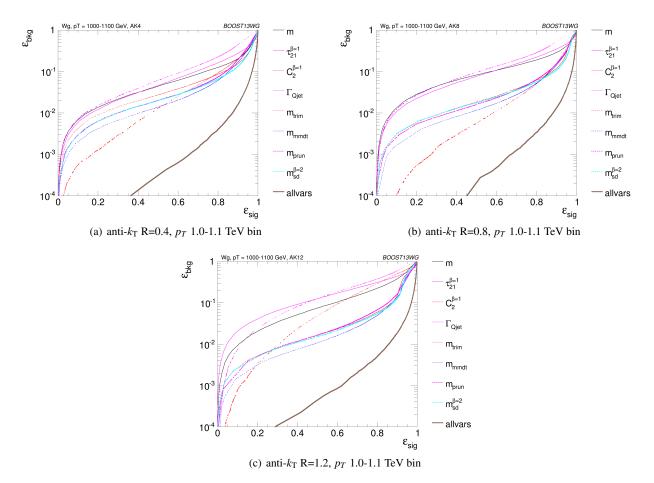
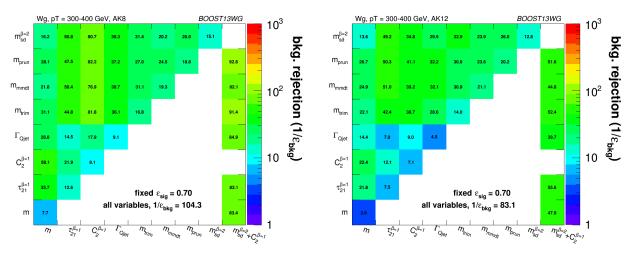


Fig. 14 The ROC curve for all single variables considered for W tagging in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4 algorithm, anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.





(a) anti- $k_{\rm T}$  R=0.8,  $p_T$  300-400 GeV bin

(b) anti- $k_T$  R=1.2,  $p_T$  300-400 GeV bin

Fig. 15 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the  $p_T$ 300-400 GeV bin using the anti-k<sub>T</sub> R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

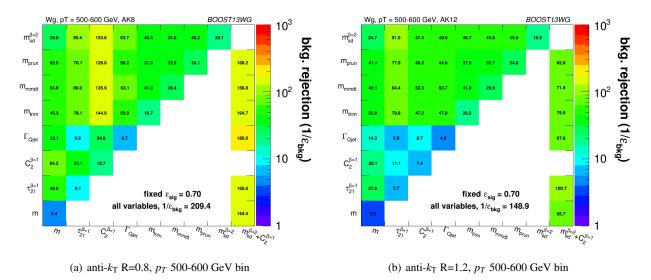
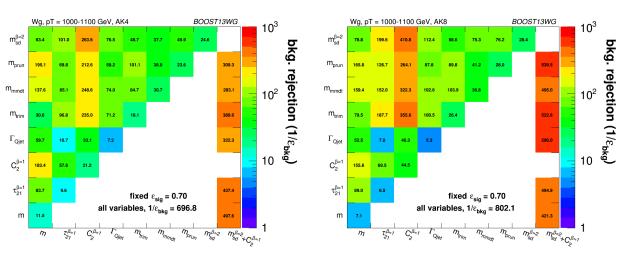


Fig. 16 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the p<sub>T</sub> 500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

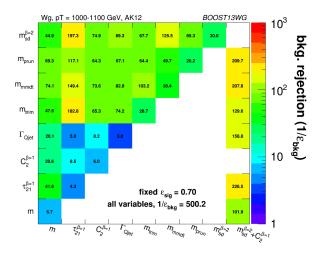
However, one can see from the Figures 15(b), 16(b) and  $\mathbf{k}_{\mathbf{z}}(\mathbf{c})$  ing from the lower to the higher  $p_T$  bin, the signal peak re-that the  $C_2^{\beta=1}$ ,  $\Gamma_{Qjet}$  and  $\tau_{21}^{\beta=1}$  substructure variables behavess somewhat differently. The background rejection power of  $\mathbf{k}_{\mathbf{z}}$  to smaller  $\tau_{21}^{\beta=1}$  values, reducing the discrimination power of 843 844 845 the  $\Gamma_{Qjet}$  and  $\tau_{21}^{\beta=1}$  variables both decrease with increasing 846  $p_T$ , by up to a factor two in going from the 300-400 GeVese 847 to 1.0-1.1 TeV bins. Conversely the rejection power of  $C_2^{\beta=l_{859}}$ 848 dramatically increases with increasing  $p_T$  for R=0.8, but 500 849 does not improve with  $p_T$  for the larger jet radius R=1.2<sup>801</sup> In Figure 19 we show the  $\tau_{21}^{\beta=1}$  and  $C_2^{\beta=1}$  distributions for signal and background in the  $p_T$  300-400 and  $p_T$  1.0-1.<sup>863</sup> TeV bins for R=0.8 jets. For  $\tau_{21}^{\beta=1}$  one can see that in mov<sup>364</sup> 850 851 852 853

the variable. This is expected, since jet substructure methods explicitly relying on identifying hard prongs would expect to work better at low  $p_T$ , where the prongs would tend to be more separated. However,  $C_2^{\beta=1}$  does not rely on the explicit identification of subjets, and one can see from Figure 19 that the discrimination power visibly increases with increasing  $p_T$ . This is in line with the observation in [42] that  $C_2^{\beta=1}$ performs best when  $m/p_T$  is small.



(a) anti- $k_{\rm T}$  R=0.4,  $p_T$  1.0-1.1 TeV bin

(b) anti- $k_{\rm T}$  R=0.8,  $p_T$  1.0-1.1 TeV bin



(c) anti- $k_T$  R=1.2,  $p_T$  1.0-1.1 TeV bin

Fig. 17 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4, R=0.8 and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

By comparing the individual sub-figures of Figures 15, 1600 865 and 17 we can see how the background rejection perfor\*\*\* 866 mance depends on jet radius within the same  $p_T$  bin. To<sub>82</sub> 867 within  $\sim 25\%$ , the background rejection power of the groomed 868 masses remains constant with respect to the jet radius. Fig<sub>384</sub> 869 ure 20 shows how the groomed mass changes for varying. 870 jet radius in the  $p_T$  1.0-1.1 TeV bin. One can see that the 871 signal mass peak remains unaffected by the increased ra<sub>887</sub> 872 dius, as expected, since grooming removes the soft contam<sub>388</sub> 873 ination which could otherwise increase the mass of the jet 874 as the radius increased. The gluon background in the sig-nal mass region also remains largely unaffected, as expected 875 876 from Figure 9, which shows very little dependence of the 877 groomed gluon mass distribution on R in the signal region<sup>892</sup> 878  $(m/p_T/R \sim 0.5)$ . This is discussed further in Section 5.4. 879 894

However, we again see rather different behaviour versus R for the substructure variables. In all  $p_T$  bins considered the most performant substructure variable,  $C_2^{\beta=1}$ , performs best for an anti- $k_T$  distance parameter of R=0.8. The performance of this variable is dramatically worse for the larger jet radius of R=1.2 (a factor seven worse background rejection in the 1.0-1.1 TeV bin), and substantially worse for R=0.4. For the other jet substructure variables considered,  $\Gamma_{Qjet}$  and  $\tau_{21}^{\beta=1}$ , their background rejection power also reduces for larger jet radius, but not to the same extent. Figure 21 shows the  $\tau_{21}^{\beta=1}$  and  $C_2^{\beta=1}$  distributions for signal and background in the 1.0-1.1 TeV  $p_T$  bin for R=0.8 and R=1.2 jet radii. One can clearly see that for the larger jet radius the  $C_2^{\beta=1}$  distribution of both signal and background get wider, and consequently the discrimination power decreases. For  $\tau_{21}^{\beta=1}$  there

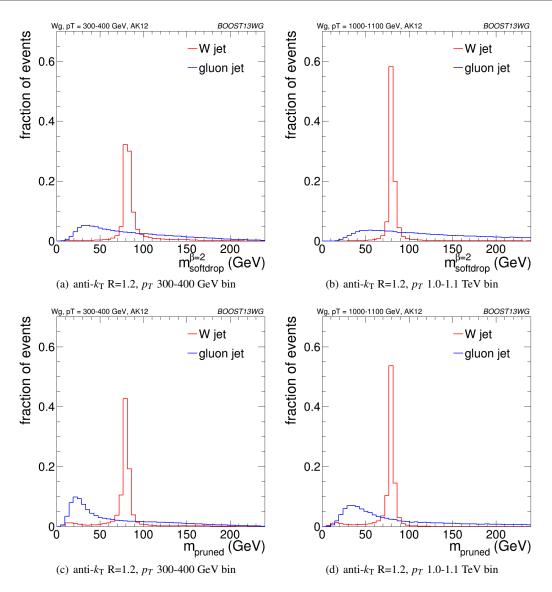


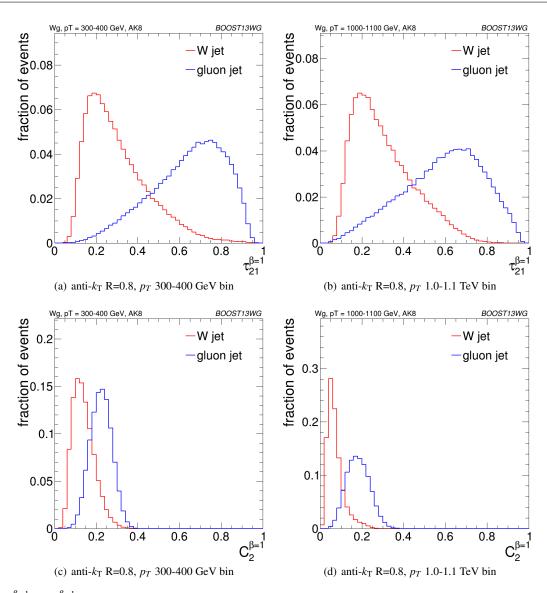
Fig. 18 The Soft-drop  $\beta = 2$  and pruned groomed mass distribution for signal and background R=1.2 jets in two different  $p_T$  bins.

is comparitively little change in the distributions with in 907 895 creasing jet radius. The increased sensitivity of  $C_2$  to soft 896 wide angle radiation in comparison to  $\tau_{21}$  is a known feature 897 of this variable [42], and a useful feature in discriminating 898 coloured versus colour singlet jets. However, at very large909 899 jet radii (R $\sim$ 1.2), this feature becomes disadvantageous; the<sup>910</sup> 900 jet can pick up a significant amount of initial state or other<sup>911</sup> 901 uncorrelated radiation, and  $C_2$  is more sensitive to this than<sup>912</sup> 902 is  $\tau_{21}$ . This uncorrelated radiation has no (or very little) de<sup>913</sup> 903 pendence on whether the jet is W- or gluon-initiated, and<sup>914</sup> 904 so sensitivity to this radiation means that the discrimination<sup>915</sup> 905 power will decrease. 906 916

#### 6.3 Combined Performance

The off-diagonal entries in Figures 15, 16 and 17 can be used to compare the performance of different BDT two-variable combinations, and see how this varies as a function of  $p_T$  and R. By comparing the background rejection achieved for the two-variable combinations to the background rejection of the "all variables" BDT, one can understand how much more discrimination is possible by adding further variables to the two-variable BDTs.

One can see that in general the most powerful two-variable combinations involve a groomed mass and a non-mass substructure variable  $(C_2^{\beta=1}, \Gamma_{Qjet} \text{ or } \tau_{21}^{\beta=1})$ . Two-variable combinations of the substructure variables are not powerful in comparison. Which particular mass + substructure variable



**Fig. 19** The  $\tau_{21}^{\beta=1}$  and  $C_2^{\beta=1}$  distributions for signal and background R=0.8 jets in two different  $p_T$  bins.

combination is the most powerful depends strongly on the  $p_T$  and R of the jet, as discussed in the sections that follow.  $p_T$  and R of the jet, as discussed in the sections that follow.  $p_T$  and  $p_T$ 

There is also modest improvement in the background re939 923 jection when different groomed masses are combined, com-924 pared to the single variable groomed mass performance, in-925 dicating that there is complementary information between 926 the different groomed masses. In addition, there is an im<sub>341</sub> 927 provement in the background rejection when the groomed<sub>42</sub> 928 masses are combined with the ungroomed mass, indicating43 929 that grooming removes some useful discriminatory informa 930 tion from the jet. These observations are explored further in<sub>45</sub> 931 the section below. 932 946

Generally one can see that the R=0.8 jets offer the bestar two-variable combined performance in all  $p_T$  bins explored we here. This is despite the fact that in the highest 1.0-1.1 GeV  $p_T$  bin the average separation of the quarks from the W650 decay is much smaller than 0.8, and well within 0.4. This conclusion could of course be susceptible to pile-up, which is not considered in this study.

#### 6.3.1 Mass + Substructure Performance

As already noted, the largest background rejection at 70% signal efficiency are in general achieved using those two variable BDT combinations which involve a groomed mass and a non-mass substructure variable. For both R=0.8 and R=1.2 jets, the rejection power of these two variable combinations increases substantially with increasing  $p_T$ , at least within the  $p_T$  range considered here.

For a jet radius of R=0.8, across the full  $p_T$  range considered, the groomed mass + substructure variable combinations with the largest background rejection are those which



= 1000-1100 GeV. AK12

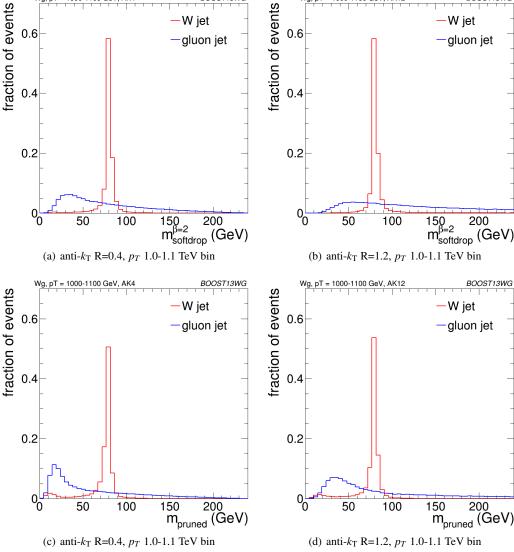


Fig. 20 The Soft-drop  $\beta = 2$  and pruned groomed mass distribution for signal and background R=0.4 and R=1.2 jets in the 1.0-1.1 TeV  $p_T$  bin.

involve  $C_2^{\beta=1}$ . For example, in combination with  $m_{sd}^{\beta=2}$ , thises produces a five-, eight- and fifteen-fold increase in backsor 951 952 ground rejection compared to using the groomed mass alone, 953 In Figure 22 the low degree of correlation between  $m_{sd}^{\beta=2}$ 954 versus  $C_2^{\beta=1}$  that leads to these large improvements in back•••• 955 ground rejection can be seen. One can also see that what 956 little correlation exists is rather non-linear in nature, chang972 957 ing from a negative to a positive correlation as a function of 73 958 the groomed mass, something which helps to improve the 959 background rejection in the region of the W mass peak. 960

Wg, pT = 1000-1100 GeV, AK4

However, when we switch to a jet radius of R=1.2 the<sup>976</sup> picture for  $C_2^{\beta=1}$  combinations changes dramatically. These<sup>977</sup> become significantly less powerful, and the most powerful<sup>778</sup> variable in groomed mass combinations becomes  $\tau_{21}^{\beta=1}$  for all jet  $p_T$  considered. Figure 23 shows the correlation between  $m_{sd}^{\beta=2}$  and  $C_2^{\beta=1}$  in the  $p_T$  1.0 - 1.2 TeV bin for the various jet radii considered. Figure 24 is the equivalent set of distributions for  $m_{sd}^{\beta=2}$  and  $\tau_{21}^{\beta=1}$ . One can see from Figure 23 that, due to the sensitivity of the observable to to soft, wide-angle radiation, as the jet radius increases  $C_2^{\beta=1}$  increases and becomes more and more smeared out for both signal and background, leading to worse discrimination power. This does not happen to the same extent for  $\tau_{21}^{\beta=1}$ . We can see from Figure 24 that the negative correlation between  $m_{sd}^{\beta=2}$  and  $\tau_{21}^{\beta=1}$  that is clearly visible for R=0.4 decreases for larger jet radius, such that the groomed mass and substructure variable are far less correlated and  $\tau_{21}^{\beta=1}$  offers improved discrimination within a  $m_{sd}^{\beta=2}$  mass window.

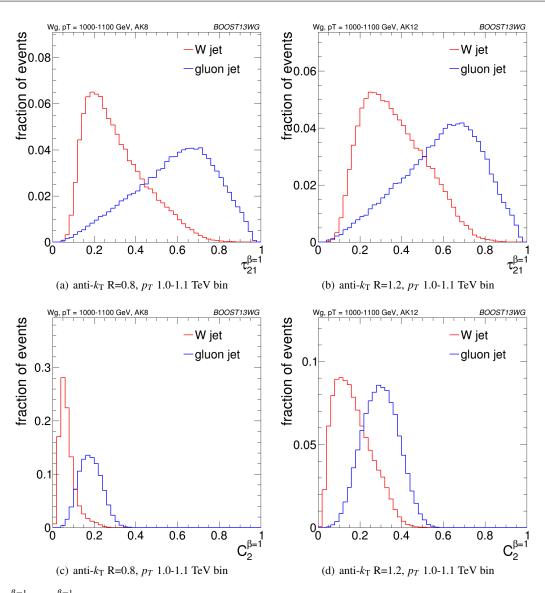


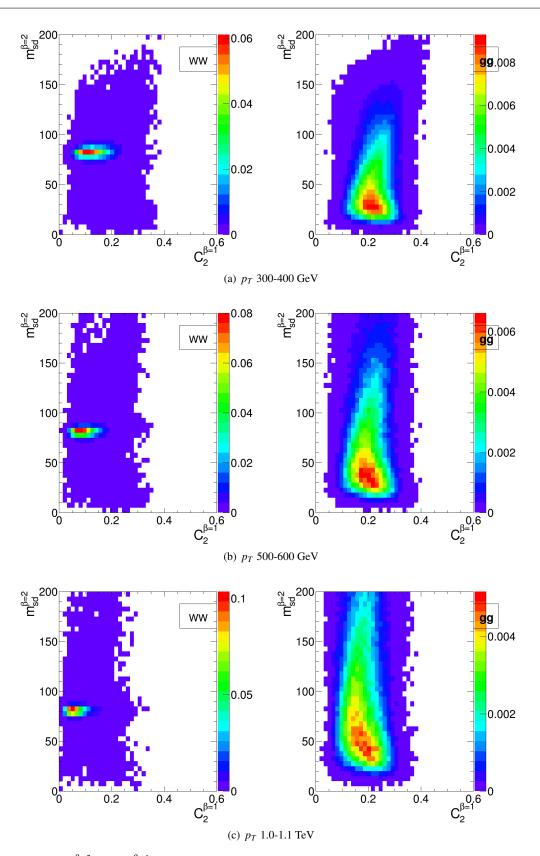
Fig. 21 The  $\tau_{21}^{\beta=1}$  and  $C_2^{\beta=1}$  distributions for signal and background R=0.8 and R=1.2 jets in the 1.0-1.1 TeV  $p_T$  bin.

#### 979 6.3.2 Mass + Mass Performance

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The different groomed masses and the ungroomed mass are 980 of course not fully correlated, and thus one can always see"97 981 some kind of improvement in the background rejection (rel<sup>998</sup> 982 ative to the single mass performance) when two different<sup>99</sup> 983 mass variables are combined in the BDT. However, in some 984 cases the improvement can be dramatic, particularly at higher1 985  $p_T$ , and particularly for combinations with the ungroomet<sup>002</sup> 986 mass. For example, in Figure 17 we can see that in the  $p_1^{1003}$ 987 1.0-1.1 TeV bin the combination of pruned mass with untool 988 groomed mass produces a greater than eight-fold improve2005 989 ment in the background rejection for R=0.4 jets, a greater06 990 than five-fold improvement for R=0.8 jets, and a factor ~twoor 991 improvement for R=1.2 jets. A similar behaviour can be seetf08 992 for mMDT mass. In Figures 25, 26 and 27 is shown the 2-D'09 993

correlation plots of the pruned mass versus the ungroomed mass separately for the WW signal and gg background samples in the  $p_T$  1.0-1.1 TeV bin, for the various jet radii considered. For comparison, the correlation of the trimmed mass with the ungroomed mass, a combination that does not improve on the single mass as dramatically, is shown. In all cases one can see that there is a much smaller degree of correlation between the pruned mass and the ungroomed mass in the backgrounds sample than for the trimmed mass and the ungroomed mass. This is most obvious in Figure 25, where the high degree of correlation between the trimmed and ungroomed mass is expected, since with the parameters used (in particular  $R_{trim} = 0.2$ ) we cannot expect trimming to have a significant impact on an R=0.4 jet. The reduced correlation with ungroomed mass for pruning in the background means that, once we have made the requirement that



**Fig. 22** 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $C_2^{\beta=1}$  for R=0.8 jets in the various  $p_T$  bins considered.

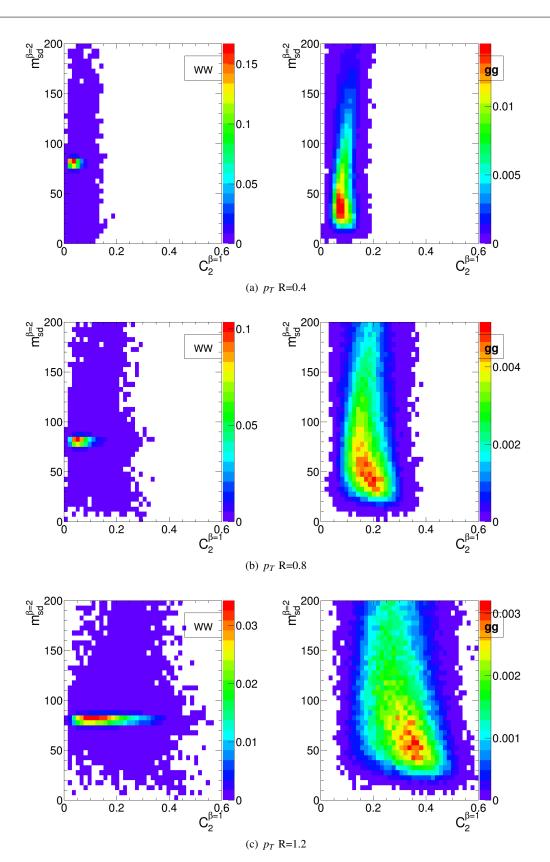


Fig. 23 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $C_2^{\beta=1}$  for R=0.4, 0.8 and 1.2 jets in the  $p_T$  1.0-1.1 TeV bin.

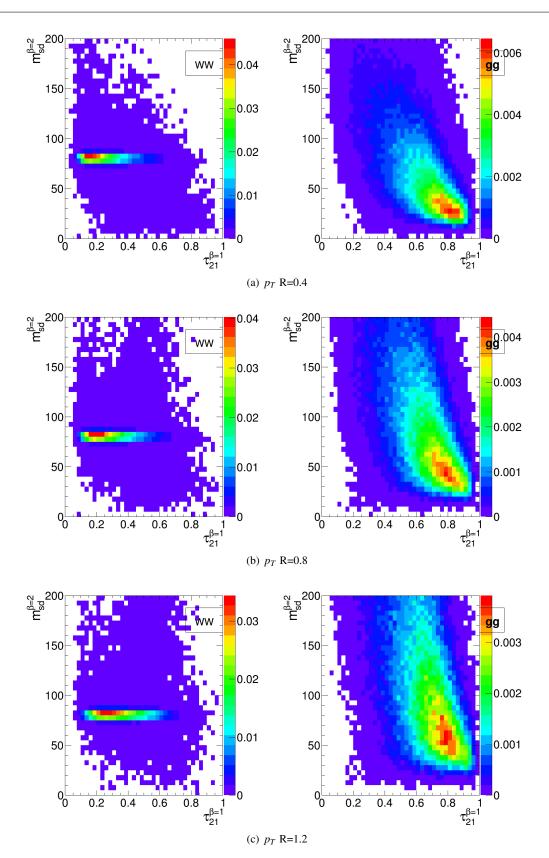


Fig. 24 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $\tau_{21}^{\beta=1}$  for R=0.4, 0.8 and 1.2 jets in the  $p_T$  1.0-1.1 TeV bin.

the pruned mass is consistent with a W (i.e.  $\sim$ 80 GeV), 10611010 relatively large difference between signal and background62 1011 in the ungroomed mass still remains, and can be exploited 1012 to improve the background rejection further. In other words 1013 many of the background events which pass the pruned masses 1014 requirement do so because they are shifted to lower mass ( $t_{\Omega_{66}}$ 1015 be within a signal mass window) by the grooming, but these 1016 events still have the property that they look very much likeos background events before the grooming. A single require 1018 ment on the groomed mass only does not exploit this. Of 1019 course, the impact of pile-up, not considered in this study, 1020 could significantly limit the degree to which the ungroomed 1021 mass could be used to improve discrimination in this way. 1070 1022

### 1023 6.3.3 "All Variables" Performance

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As well as the background rejection at a fixed 70% sigura 1024 nal efficiency for two-variable combinations, Figures 15, 1974 1025 and 17 also report the background rejection achieved by 75 1026 a combination of all the variables considered into a single<sup>76</sup> 1027 BDT discriminant. One can see that, in all cases, the re-077 1028 jection power of this "all variables" BDT is significantly78 1029 larger than the best two-variable combination. This indicates79 1030 that beyond the best two-variable combination there is stilleso 1031 significant complementary information available in the re-1032 maining variables in order to improve the discrimination of 1033 signal and background. How much complementary informaess 1034 tion is available appears to be  $p_T$  dependent. In the lower  $p_{\frac{1}{2}084}$ 1035 300-400 and 500-600 GeV bins the background rejection of 1036 the "all variables" combination is a factor  $\sim 1.5$  greater than the second se 1037 the best two-variable combination, but in the highest  $p_T$  bines 1038 it is a factor  $\sim 2.5$  greater. 1039 1088

The final column in Figures 15, 16 and 17 allows uses 1040 to explore the all variables performance a little further. Ib90 1041 shows the background rejection for three variable BDT compositions of  $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$ , where X is the variable only the y-axis. For jets with R=0.4 and R=0.8, the combination  $m_{sd}^{\beta=2} = R_{sd}^{\beta=1}$ 1042 1043 1044  $m_{sd}^{\beta=2} + C_2^{\beta=1}$  is the best performant (or very close to the bester performant) two-variable combination in every  $p_T$  bin contract 1045 1046 sidered. For R=1.2 this is not the case, as  $C_2^{\beta=1}$  is superceded. 1047 by  $\tau_{21}^{\beta=1}$  in performance, as discussed earlier. Thus, in conference 1048 sidering the three-variable combination results it is best two 1049 focus on the R=0.4 and R=0.8 cases. Here we see that, fatos 1050 the lower  $p_T$  300-400 and 500-600 GeV bins, adding theorem 1051 third variable to the best two-variable combination brings uso1 1052 to within  $\sim 15\%$  of the "all variables" background rejection<sub>102</sub> 1053 However, in the highest  $p_T$  1.0-1.1 TeV bin, whilst adding<sub>03</sub> 1054 the third variable does improve the performance considering 1055 ably, we are still  $\sim 40\%$  from the observed "all variables" as 1051056 background rejection, and clearly adding a fourth or maybeing 1057 even fifth variable would bring considerable gains. In terms<sub>107</sub> 1058 of which variable offers the best improvement when  $added_{08}$ 1059 to the  $m_{sd}^{\beta=2} + C_2^{\beta=1}$  combination, it is hard to see an obvious 1060

pattern; the best third variable changes depending on the  $p_T$  and R considered.

In conclusion, it appears that there is a rich and complex structure in terms of the degree to which the discriminatory information provided by the set of variables considered overlaps, with the degree of overlap apparently decreasing at higher  $p_T$ . This suggests that in all  $p_T$  ranges, but especially at higher  $p_T$ , there are substantial performance gains to be made by designing a more complex multivariate W tagger.

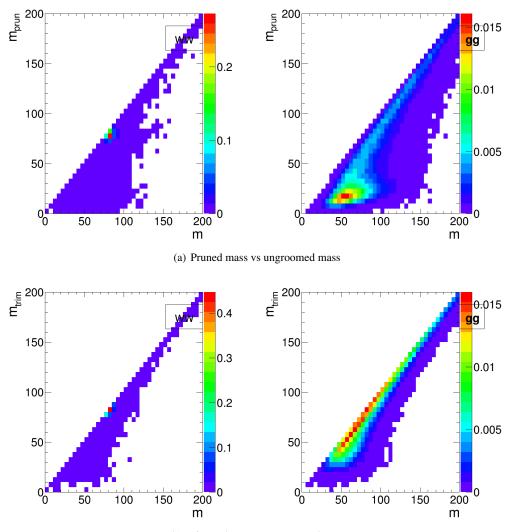
#### 6.4 Conclusions

We have studied the performance, in terms of the degree to which a hadronically decaying W boson can be separated from a gluonic background, of a number of groomed jet masses, substructure variables, and BDT combinations of the above. We have used this to build a picture of how the discriminatory information contained in the variables overlaps, and how this complementarity between the variables changes with  $p_T$  and anti- $k_T$  distance parameter R.

In terms of the performance of individual variables, we find that, in agreement with other studies [56], in general the groomed masses perform best, with a background rejection power that increases with increasing  $p_T$ , but which is more constant with respect to changes in R. We have explained the dependence of the groomed mass performance on  $p_T$  and R using the understanding of the QCD mass distribution gleaned in Section 5.4. Conversely, the performance of other substructure variables, such as  $C_2^{\beta=1}$  and  $\tau_{21}^{\beta=1}$  is more susceptible to changes in radius, with background rejection power decreasing with increasing R. This is due to the inherent sensitivity of these observables to soft, wide angle radiation.

The best two-variable performance is obtained by combining a groomed mass with a substructure variable. Which particular substructure variable works best in combination is strongly dependent on  $p_T$  and R.  $C_2^{\beta=1}$  offers significant complimentarity to groomed mass at smaller R, owing to the small degree of correlation between the variables. However, the sensitivity of  $C_2^{\beta=1}$  to soft, wide-angle radiation leads to worse discrimination power at large R, where  $\tau_{21}^{\beta=1}$  performs better in combination. Our studies also demonstrate the potential for enhanced discrimination by combining groomed and ungroomed mass information, although the use of ungroomed mass in this may in practice be limited by the presence of pile-up that is not considered in these studies.

By examining the performance of a BDT combination of all the variables considered, it is clear that there are potentially substantial performance gains to be made by designing a more complex multivariate W tagger, especially at higher  $p_T$ .



(b) Trimmed mass vs ungroomed mass

Fig. 25 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4 algorithm.

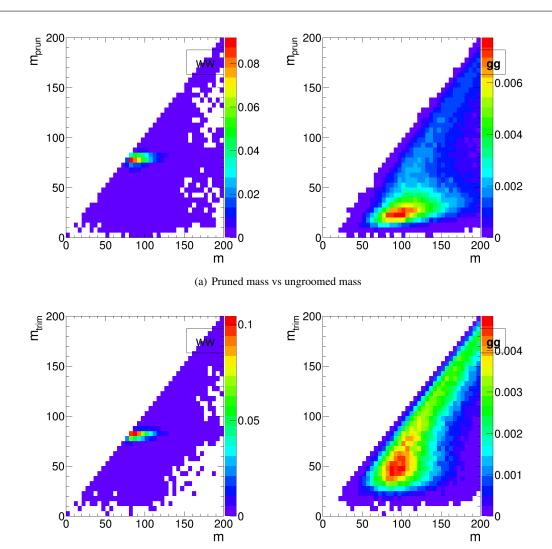
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#### 1110 7 Top Tagging

In this section, we study the identification of boosted to<sup>jj27</sup> 1111 quarks at Run II of the LHC. Boosted top quarks result ill<sup>28</sup> 1112 large-radius jets with complex substructure, containing a  $B^{\pm 29}$ 1113 subjet and a boosted W. The additional kinematic handles<sup>30</sup> 1114 coming from the reconstruction of the W mass and b-tagging<sup>31</sup> 1115 allow a very high degree of discrimination of top quark jets 1116 from QCD backgrounds. We study fully hadronic decays of 1117 Л 1133 the top quark. 1118 1134

<sup>1119</sup> We consider top quarks with moderate boost (600-100Ω<sub>35</sub> <sup>1120</sup> GeV), and perhaps most interestingly, at high boost ( $\gtrsim 150$ Ω<sub>36</sub> <sup>1121</sup> GeV). Top tagging faces several challenges in the high- $p_{T_{137}}$ <sup>1122</sup> regime. For such high- $p_T$  jets, the *b*-tagging efficiencies arΩ<sub>38</sub> <sup>1123</sup> no longer reliably known. Also, the top jet can also accom<sub>139</sub> <sup>1124</sup> panied by additional radiation with  $p_T \sim m_t$ , leading to com<sub>140</sub> binatoric ambiguities of reconstructing the top and W, and the possibility that existing taggers or observables shape the background by looking for subjet combinations that reconstruct  $m_t/m_W$ . To study this, we examine the performance of both mass-reconstruction variables, as well as shape observables that probe the three-pronged nature of the top jet and the accompanying radiation pattern.

We use the top quark MC samples for each bin described in Section 2.2. The analysis relies on FASTJET 3.0.3 for jet clustering and calculation of jet substructure observables. Jets are clustered using the anti- $k_t$  algorithm. An upper and lower  $p_T$  cut are applied after jet clustering to each sample to ensure similar  $p_T$  spectra in each bin. The bins in leading jet  $p_T$  that are investigated for top tagging are 600-700 GeV, 1-1.1 TeV, and 1.5-1.6 TeV. Jets are clustered with radii R = 0.4, 0.8, and 1.2; R = 0.4 jets are only studied in the 1.5-



(b) Trimmed mass vs ungroomed mass

Fig. 26 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.8 algorithm.

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1141 1.6 TeV bin because for top quarks with this boost, the top 53 1142 decay products are all contained within an R = 0.4 jet. 1154

1143	7.1 Methodology	1157
	, ii iii iii ii ii ii ii ii ii ii ii ii	1158

- We study a number of top-tagging strategies, in particular:<sup>1159</sup>
- 1145 1. HEPTopTagger 1161

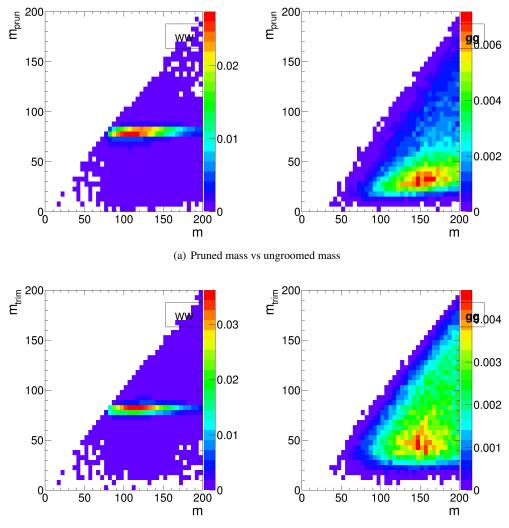
- 1147 3. Trimming
- 1148 4. Pruning

The top taggers have criteria for reconstructing a top and WW candidate, and a corresponding top and W mass, as denois scribed in Section 3.3, while the grooming algorithms (trimnee ming and pruning) do not incorporate a W-identification step for

For a level playing field, where grooming is used we construct a W candidate mass,  $m_W$ , from the three leading subjets by taking the mass of the pair of subjets with the smallest invariant mass; in the case that only two subjets are reconstructed, we take the mass of the leading subjet. The top mass,  $m_t$ , is the mass of the groomed jet. All of the above taggers and groomers incorporate a step to remove pile-up and other soft radiation.

We also consider the performance of the following jet shape observables:

- The ungroomed jet mass.
- *N*-subjettiness ratios  $\tau_2/\tau_1$  and  $\tau_3/\tau_2$  with  $\beta = 1$  and the "winner-takes-all" axes.
- 2-point energy correlation function ratios  $C_2^{\beta=1}$  and  $C_3^{\beta=1}$ .
- The pruned Qjet mass volatility,  $\Gamma_{Qjet}$ .



(b) Trimmed mass vs ungroomed mass

Fig. 27 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=1.2 algorithm.

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In addition to the jet shape performance, we combine thas jet shapes with the mass-reconstruction methods described above to determine the optimal combined performance.

For determining the performance of multiple variables,185 1171 we combine the relevant tagger output observables and/or jet 1172 shapes into a boosted decision tree (BDT), which determines 1173 the optimal cut. Additionally, because each tagger has twb87 1174 input parameters, as described in Section 3.3, we scan over 1175 reasonable values of the parameters to determine the optimal<sup>89</sup> 1176 value that gives the largest background rejection for each to<sup>jj90</sup> tagging signal efficiency. This allows a direct comparisoliter 1178 of the optimized version of each tagger. The input values 1179 1193 scanned for the various algorithms are: 1180 1194

**HEPTopTagger:** 
$$m \in [30, 100]$$
 GeV,  $\mu \in [0.5, 1]$ 

**1182** – **JH Tagger:** 
$$\delta_p \in [0.02, 0.15], \delta_R \in [0.07, 0.2]$$

**Trimming:** 
$$f_{\text{cut}} \in [0.02, 0.14], R_{\text{trim}} \in [0.1, 0.5]$$

- **Pruning:**  $z_{\text{cut}} \in [0.02, 0.14], R_{\text{cut}} \in [0.1, 0.6]$ 

#### 7.2 Single-observable performance

We start by investigating the behaviour of individual jet substructure observables. Because of the rich, three-pronged structure of the top decay, it is expected that combinations of masses and jet shapes will far outperform single observables in identifying boosted tops. However, a study of the toptagging performance of single variables facilitates a direct comparison with the *W* tagging results in Section 6, and also allows a straightforward examination of the performance of each observable for different  $p_T$  and jet radius.

Fig. 28 shows the ROC curves for each of the top-tagging observables, with the bare (ungroomed) jet mass also plotted for comparison. The jet shape observables all perform sub-

stantially worse than jet mass, unlike W tagging for which 51 1198 several observables are competitive with or perform betters 1199 than jet mass (see, for example, Fig. 10). To understands 1200 why this is the case, consider N-subjettiness. The W is two 2541201 pronged and the top is three-pronged; therefore, we expegies 1202  $\tau_{21}$  and  $\tau_{32}$  to be the best-performant N-subjettiness ratio, re256 1203 spectively. However,  $\tau_{21}$  also contains an implicit cut on the 1204 denominator,  $\tau_1$ , which is strongly correlated with jet mass<sub>258</sub> 1205 Therefore,  $\tau_{21}$  combines both mass and shape information  $\tau_{259}$ 1206 to some extent. By contrast, and as is clear in Fig. 28(a), these 1207 best shape for top tagging is  $\tau_{32}$ , which contains no informa<sub>261</sub> 1208 tion on the mass. Therefore, it is unsurprising that the shapes 1209 most useful for top tagging are less sensitive to the jet mass<sub>2263</sub> 1210 and under-perform relative to the corresponding observable 1211 for W tagging. 1212 1265

Of the two top tagging algorithms, we can see from Fig266 1213 ure 28 that the Johns Hopkins (JH) tagger out-performs theor 1214 HEPTopTagger in terms of its signal-to-background separa-208 1215 tion power in both the top and W candidate masses; this isso 1216 expected, as the HEPTopTagger was designed to reconstruct<sup>70</sup> 1217 moderate  $p_T$  top jets in *ttH* events (for a proposal for a high<sub>271</sub> 1218  $p_T$  variant of the HEPTopTagger, see [57]). In Figure 29 wer2 1219 show the histograms for the top mass output from the JH73 1220 and HEPTopTagger for different R in the  $p_T$  1.5-1.6 TeV<sub>274</sub> 1221 bin, and in Figure 30 for different  $p_T$  at at R =0.8, optimized<sub>75</sub> 1222 at a signal efficiency of 30%. One can see from these fig276 1223 ures that the likely reason for the better performance of the77 1224 JH tagger is that, in the HEPTopTagger algorithm, the jet is78 1225 filtered to select the five hardest subjets, and then three sub279 1226 jets are chosen which reconstruct the top mass. This require280 1227 ment tends to shape a peak in the QCD background aroundes 1228  $m_t$  for the HEPTopTagger, while the JH tagger has no suches 1229 requirement. It has been suggested [58] that performance in283 1230 the HEPTopTagger may be improved by selecting the threes4 1231 subjets reconstructing the top only among those that pass these 1232 W mass constraints, which somewhat reduces the shaping  $o_{\text{Es6}}$ 1233 the background. The discrepancy between the JH and HEP+287 1234 TopTaggers is more pronounced at higher  $p_T$  and larger jetses 1235 radius (see Figs. 33 and 36). 1289 1236

We also see in Figure 28(b) that the top mass from the 1237 JH tagger and the HEPTopTagger has superior performances 1238 relative to either of the grooming algorithms; this is because92 1239 the pruning and trimming algorithms do not have inherenteo3 1240 W-identification steps and are not optimized for this put294 1241 pose. Indeed, because of the lack of a W-identification step395 1242 grooming algorithms are forced to strike a balance betweenp96 1243 under-grooming the jet, which broadens the signal peak due 1244 to UE contamination and features a larger background rate, 1245 and over-grooming the jet, which occasionally throws outer 1246 the b-jet and preserves only the W components inside the 1247 jet. We demonstrate this effect in Figures 29 and 30, showi298 1248 ing that with  $\varepsilon_{sig} = 0.3 - 0.35$ , the optimal performance at  $\varepsilon_{sig}$ 1249 the tagger over-grooms a substantial fraction of the jets (2300 1250

20-30%), leading to a spurious second peak at the *W* mass. This effect is more pronounced at large *R* and *p<sub>T</sub>*, since more aggressive grooming is required in these limits to combat the increased contamination from UE and QCD radiation.

In Figures 31 and 33 we directly compare ROC curves for jet shape observable performance and top mass performance respectively in the three different  $p_T$  bins considered whilst keeping the jet radius fixed at R=0.8. The input parameters of the taggers, groomers and shape variables are separately optimized in each  $p_T$  bin. One can see from Figure 31 that the tagging performance of jet shapes do not change substantially with  $p_T$ . The observables  $\tau_{32}^{(\beta=1)}$  and Qjet volatility  $\Gamma$  have the most variation and tend to degrade with higher  $p_T$ , as can be seen in Figure 32. This makes sense, as higher- $p_T$  QCD jets have more, harder emissions within the jet, giving rise to substructure that fakes the signal. By contrast, from Figure 33 we can see that most of the top mass observables have superior performance at higher  $p_T$  due to the radiation from the top quark becoming more collimated. The notable exception is the HEPTopTagger, which degrades at higher  $p_T$ , likely in part due to the backgroundshaping effects discussed earlier.

In Figures 34 and 36 we directly compare ROC curves for jet shape observable performance and top mass performance respectively for the three different jet radii considered within the  $p_T$  1.5-1.6 TeV bin. Again, the input parameters of the taggers, groomers and shape variables are separately optimized for each jet radius. We can see from these figures that most of the top tagging variables, both shape and reconstructed top mass, perform best for smaller radius. This is likely because, at such high  $p_T$ , most of the radiation from the top quark is confined within R = 0.4, and having a larger jet radius makes the observable more susceptible to contamination from the underlying event and other uncorrelated radiation. In Figure 35, we compare the individual top signal and QCD background distributions for each shape variable considered in the  $p_T$  1.5-1.6 TeV bin for the various jet radii. One can see that the distributions for both signal and background broaden with increasing R, degrading the discriminating power. For  $C_2^{(\beta=1)}$  and  $C_3^{(\beta=1)}$ , the background distributions are shifted upward as well. Therefore, the discriminating power generally gets worse with increasing *R*. The main exception is for  $C_3^{(\beta=1)}$ , which performs optimally at R = 0.8; in this case, the signal and background coincidentally happen to have the same distribution around R = 0.4, and so R = 0.8 gives better discrimination.

#### 7.3 Performance of multivariable combinations

We now consider various BDT combinations of the observables from Section 7.2, using the techniques described in Section 4. In particular, we consider the performance of in-

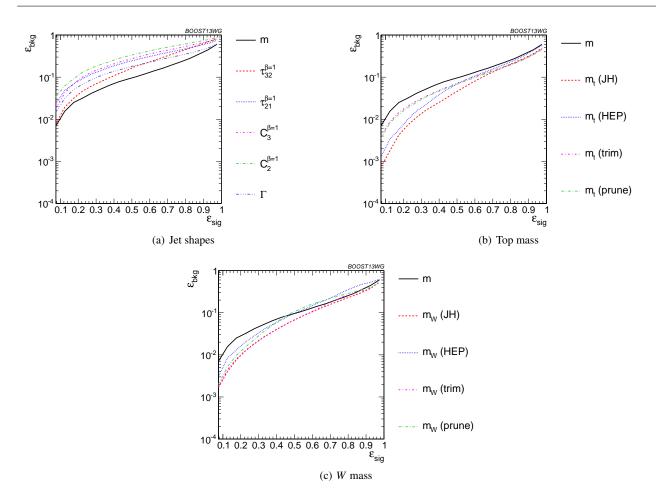


Fig. 28 Comparison of single-variable top-tagging performance in the  $p_T = 1 - 1.1$  GeV bin using the anti- $k_T$ , R=0.8 algorithm.

dividual taggers such as the JH tagger and HEPTopTagger323 1301 which output information about the top and W candidate<sub>24</sub> 1302 masses and the helicity angle; groomers, such as trimming25 1303 and pruning, which remove soft, uncorrelated radiation from 26 1304 the top candidate to improve mass reconstruction, and to27 1305 which we have added a W reconstruction step; and the com-s28 1306 bination of the outputs of the above taggers/groomers, both29 1307 with each other, and with shape variables such as N-subjettiness 1308 ratios and energy correlation ratios. For all observables with31 1309 tuneable input parameters, we scan and optimize over reals32 1310 istic values of such parameters, as described in Section 7.1. 1311

In Figure 37, we directly compare the performance of 34 1312 the HEPTopTagger, the JH tagger, trimming, and pruning335 1313 in the  $p_T = 1 - 1.1$  TeV bin using jet radius R=0.8, where R=0.8, 1314 both  $m_t$  and  $m_W$  are used in the groomers. Generally, WB37 1315 find that pruning, which does not naturally incorporate sub338 1316 jets into the algorithm, does not perform as well as the oth339 1317 ers. Interestingly, trimming, which does include a subjets40 1318 identification step, performs comparably to the HEPTopTag341 1319 ger over much of the range, possibly due to the background<sub>342</sub> 1320 shaping observed in Section 7.2. By contrast, the JH tag343 1321 ger outperforms the other algorithms. To determine whether 1322

there is complementary information in the mass outputs from different top taggers, we also consider in Figure 37 a multivariable combination of all of the JH and HEPTopTagger outputs. The maximum efficiency of the combined JH and HEPTopTaggers is limited, as some fraction of signal events inevitably fails either one or other of the taggers. We do see a 20-50% improvement in performance when combining all outputs, which suggests that the different algorithms used to identify the top and *W* for different taggers contains complementary information.

In Figure 38 we present the results for multivariable combinations of the top tagger outputs with and without shape variables. We see that, for both the HEPTopTagger and the JH tagger, the shape observables contain additional information uncorrelated with the masses and helicity angle, and give on average a factor 2-3 improvement in signal discrimination. We see that, when combined with the tagger outputs, both the energy correlation functions  $C_2 + C_3$  and the *N*subjettiness ratios  $\tau_{21} + \tau_{32}$  give comparable performance, while the Qjet mass volatility is slightly worse; this is unsurprising, as Qjets accesses shape information in a more indirect way from other shape observables. Combining all

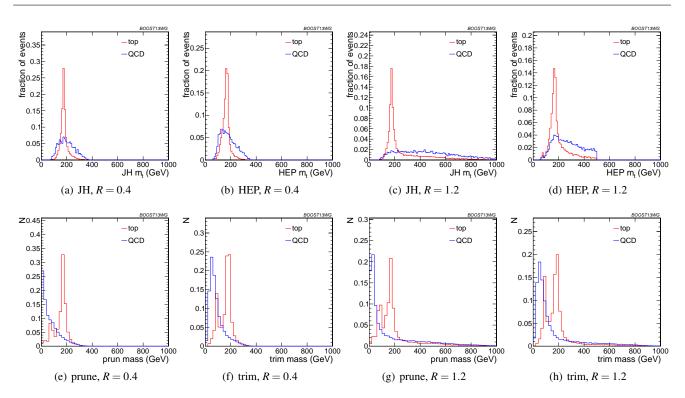


Fig. 29 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different *R* using the anti- $k_T$  algorithm,  $p_T = 1.5 - 1.6$  TeV. Each histogram is shown for the working point optimized for best performance with  $m_t$  in the 0.3 - 0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger. In this and subsequent plots, the HEPTopTagger distribution cuts off at 500 GeV because the tagger fails to tag jets with a larger mass.

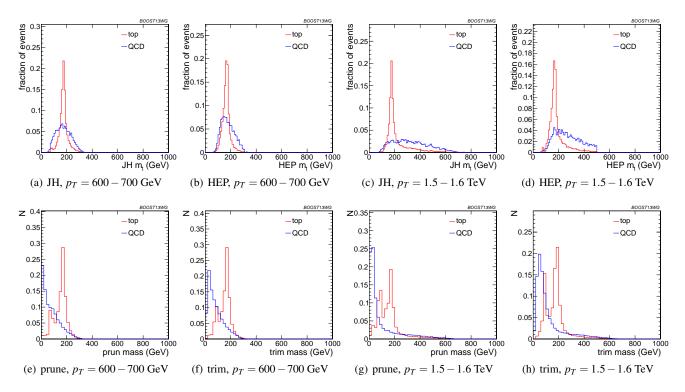


Fig. 30 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different  $p_T$  using the anti- $k_T$  algorithm, R = 0.8. Each histogram is shown for the working point optimized for best performance with  $m_t$  in the 0.3 – 0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger.

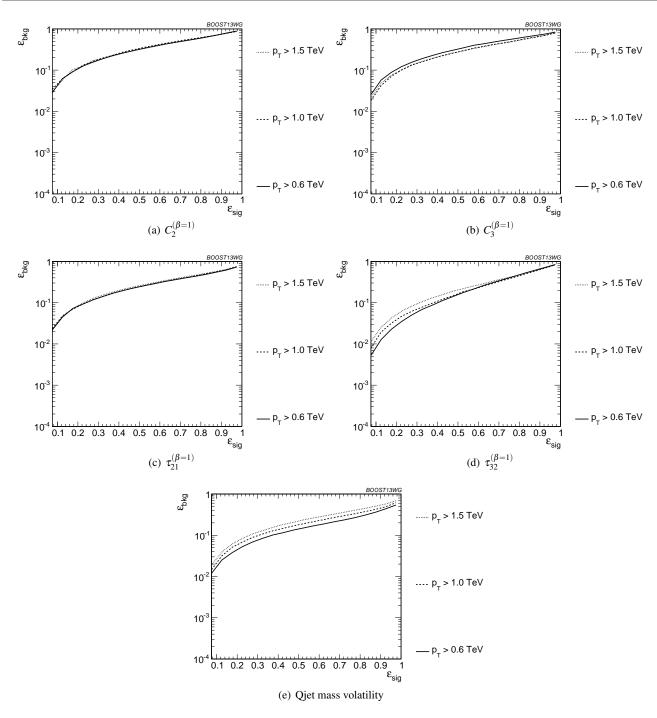


Fig. 31 Comparison of individual jet shape performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

shape observables with a single top tagger provides events
greater enhancement in discrimination power. We directly
compare the performance of the JH and HEPTopTaggers ints
Figure 38(c). Combining the taggers with shape informasse
tion nearly erases the difference between the tagging meth-

ods observed in Figure 37; this indicates that combining th<sup>257</sup>
 shape information with the HEPTopTagger identifies the dif<sup>358</sup>
 ferences between signal and background missed by the tag<sup>1359</sup>

ger alone. This also suggests that further improvement to discriminating power may be minimal, as various multivariable combinations are converging to within a factor of 20% or so.

In Figure 39 we present the results for multivariable combinations of groomer outputs with and without shape variables. As with the tagging algorithms, combinations of groomers with shape observables improves their discriminating power;

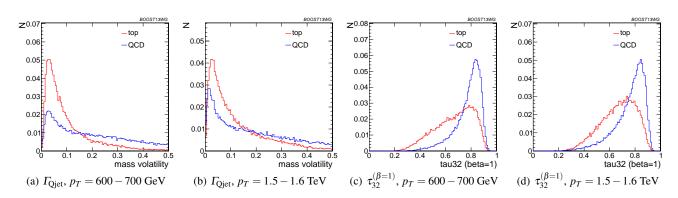


Fig. 32 Comparison of  $\Gamma_{\text{Qjet}}$  and  $\tau_{32}^{\beta=1}$  at R = 0.8 and different values of the  $p_T$ . These shape observables are the most sensitive to varying  $p_T$ .

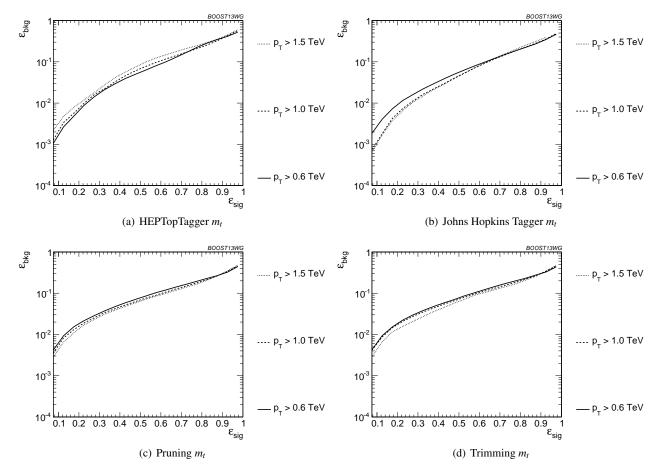


Fig. 33 Comparison of top mass performance of different taggers at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

combinations with  $au_{32} + au_{21}$  perform comparably to those to the second sec 1361 with  $C_3 + C_2$ , and both of these are superior to combina<sub>370</sub> 1362 tions with the mass volatility,  $\Gamma$ . Substantial improvement is 1363 further possible by combining the groomers with all shape 1364 observables. Not surprisingly, the taggers that lag behind 1365 in performance enjoy the largest gain in signal-background 1366 discrimination with the addition of shape observables. Once 1367 again, in Figure 39(c), we find that the differences between  $\frac{1}{1376}$ 1368

pruning and trimming are erased when combined with shape information.

Finally, in Figure 40, we compare the performance of each of the tagger/groomers when their outputs are combined with all of the shape observables considered. One can see that the discrepancies between the performance of the different taggers/groomers all but vanishes, suggesting perhaps that we are here utilising all available signal-background discrmination information, and that this is the optimal top

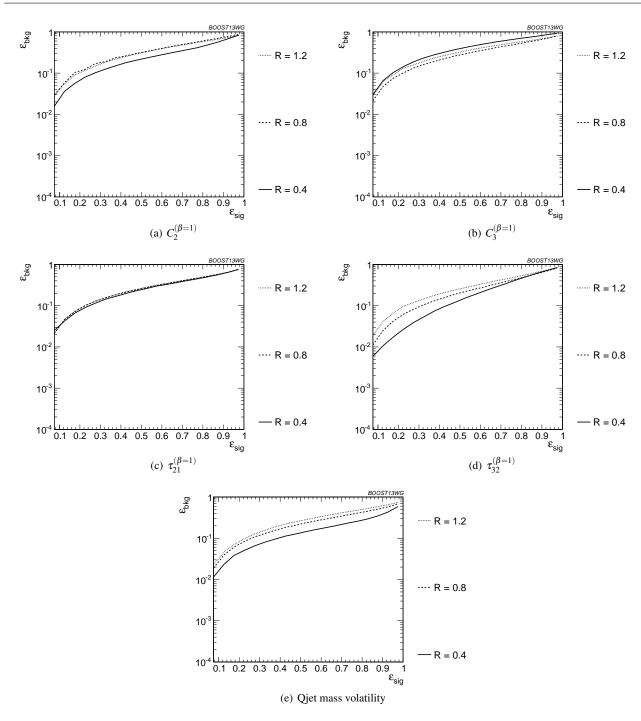


Fig. 34 Comparison of individual jet shape performance at different R in the  $p_T = 1.5 - 1.6$  TeV bin.

tagging performance that could be achieved in these condisestions.

<sup>1380</sup> Up to this point we have just considered the combined <sup>1381</sup> multivariable performance in the  $p_T$  1.0-1.1 TeV bin with <sup>1382</sup> jet radius R=0.8. We now compare the BDT combination <sup>1383</sup> of tagger outputs, with and without shape variables, at dif <sup>1384</sup> ferent  $p_T$ . The taggers are optimized over all input parame <sup>1385</sup> ters for each choice of  $p_T$  and signal efficiency. As with the single-variable study, we consider anti- $k_T$  jets clustered with R = 0.8 and compare the outcomes in the  $p_T = 500 - 600$  GeV,  $p_T = 1 - 1.1$  TeV, and  $p_T = 1.5 - 1.6$  TeV bins. The comparison of the taggers/groomers is shown in Figure 41. The behaviour with  $p_T$  is qualitatively similar to the behaviour of the  $m_t$  observable for each tagger/groomer shown in Figure 33; this suggests that the  $p_T$  behaviour of the taggers is dominated by the top mass reconstruction. As before,

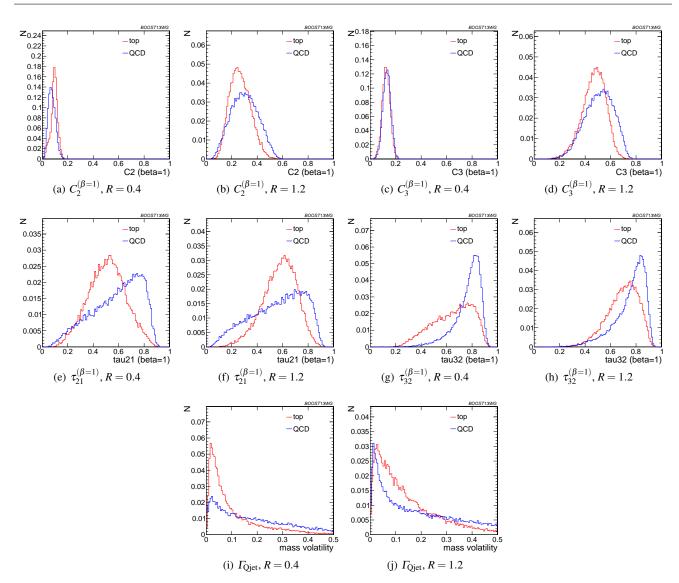


Fig. 35 Comparison of various shape observables in the  $p_T = 1.5 - 1.6$  TeV bin and different values of the anti- $k_T$  radius R.

the HEPTopTagger performance degrades slightly with interaction creased  $p_T$  due to the background shaping effect, while the JI JH tagger and groomers modestly improve in performance 1412

In Figure 42, we show the  $p_T$  dependence of BDT com-1397 binations of the JH tagger output combined with shape oba14 1398 servables. We find that the curves look nearly identical: theas 1399  $p_T$  dependence is dominated by the top mass reconstruc<sub>416</sub> 1400 tion, and combining the tagger outputs with different shape 1401 observables does not substantially change this behaviour418 1402 The same holds true for trimming and pruning. By contrast 1403 HEPTopTagger ROC curves, shown in Figure 43, do change 420 1404 somewhat when combined with different shape observables 1405 due to the suboptimal performance of the HEPTopTagger ata22 1406 high  $p_T$ , we find that combining the HEPTopTagger with<sub>23</sub> 1407  $C_3^{(\beta=1)}$ , which in Figure 31(b) is seen to have some model 1408 est improvement at high  $p_T$ , can improve its performance425 1409

Combining the HEPTopTagger with multiple shape observables gives the maximum improvement in performance at high  $p_T$  relative to at low  $p_T$ .

In Figure 44 we compare the BDT combinations of tagger outputs, with and without shape variables, at different jet radius *R* in the  $p_T = 1.5 - 1.6$  TeV bin. The taggers are optimized over all input parameters for each choice of *R* and signal efficiency. We find that, for all taggers and groomers, the performance is always best at small *R*; the choice of *R* is sufficiently large to admit the full top quark decay at such high  $p_T$ , but is small enough to suppress contamination from additional radiation. This is not altered when the taggers are combined with shape observable. For example, in Figure 45 is shown the depedence on *R* of the JH tagger when combined with shape observables, where one can see that the

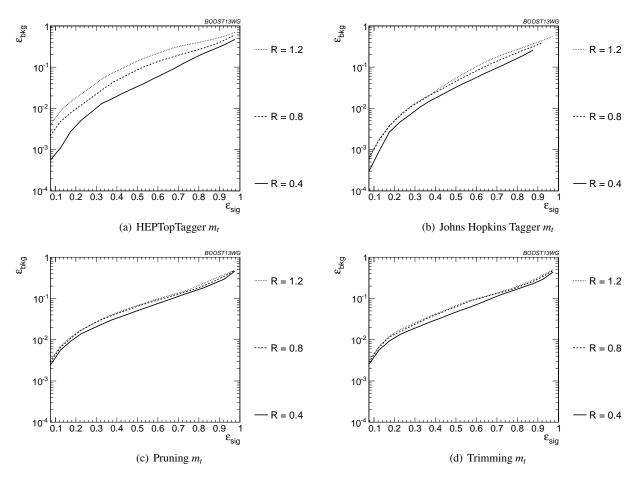


Fig. 36 Comparison of top mass performance of different taggers at different R in the  $p_T = 1.5 - 1.6$  TeV bin.

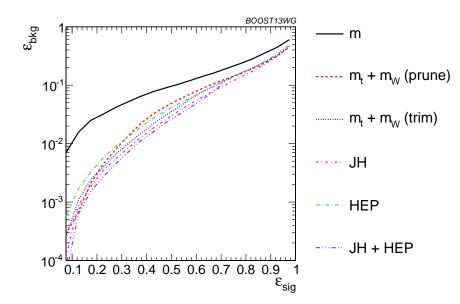
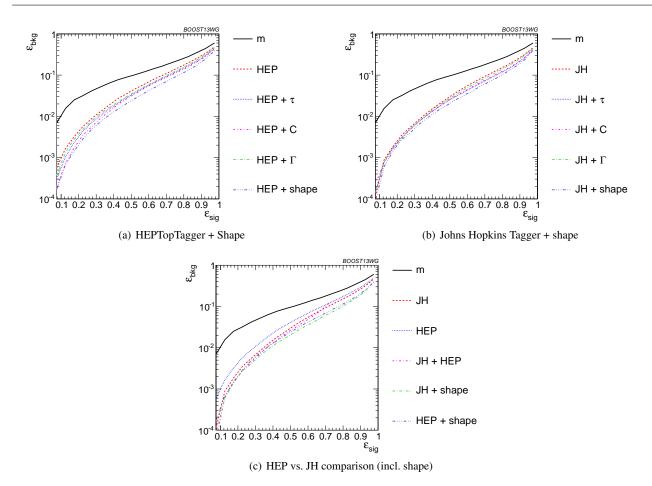


Fig. 37 The performance of the various taggers in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. For the groomers a BDT combination of the reconstructed  $m_t$  and  $m_W$  are used. Also shown is a multivariable combination of all of the JH and HEPTopTagger outputs. The ungroomed mass performance is shown for comparison.



**Fig. 38** The performance of BDT combinations of the JH and HepTopTagger outputs with various shape observables in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Taggers are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{Qjet}$ , and all of the above (denoted "shape").

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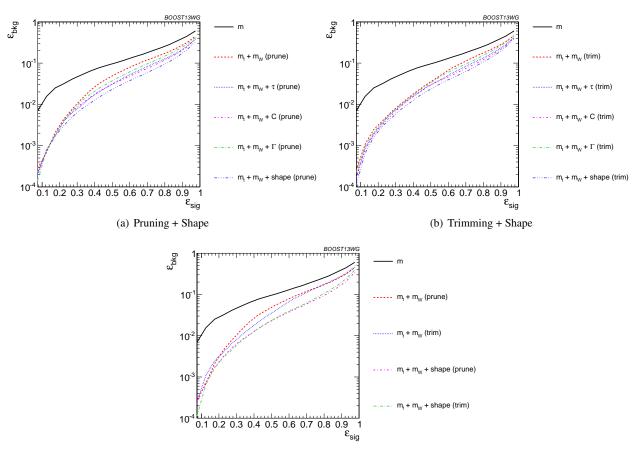
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*R*-dependence is identical for all combinations. The samaa
holds true for the HEPTopTagger, trimming, and pruning. 1444

1428 7.4 Performance at Sub-Optimal Working Points

Up until now, we have re-optimized our tagger and groomenso 1429 parameters for each  $p_T$ , R, and signal efficiency working<sup>51</sup> 1430 point. In reality, experiments will choose a finite set of work452 1431 ing points to use. How do our results hold up when thisss 1432 is taken into account? To address this concern, we replies 1433 cate our analyses, but only optimize the top taggers for as5 1434 particular  $p_T/R$ /efficiency and apply the same parameters<sup>56</sup> 1435 to other scenarios. This allows us to determine the extents 1436 to which re-optimization is necessary to maintain the highs 1437 signal-background discrimination power seen in the top tag. 1438 ging algorithms we study. The shape observables typicall<sup>1460</sup> 1439 do not have any input parameters to optimize. Therefore, was 1440 focus on the taggers and groomers, and their combinations 1441 with shape observables, in this section. 1463 1442

**Optimizing at a single**  $p_T$ : We show in Figure 46 the performance of the top taggers, using just the reconstructed top mass as the discriminating variable, with all input parameters optimized to the  $p_T = 1.5 - 1.6$  TeV bin, relative to the performance optimized at each  $p_T$ . We see that while the performance degrades by about 50% when the high- $p_T$ optimized points are used at other momenta, this is only an order-one adjustment of the tagger performance, with trimming and the Johns Hopkins tagger degrading the most. The jagged behaviour of the points is due to the finite resolution of the scan. We also observe a particular effect associated with using suboptimal taggers: since taggers sometimes fail to return a top candidate, parameters optimized for a particular efficiency  $\varepsilon_S$  at  $p_T = 1.5 - 1.6$  TeV may not return enough signal candidates to reach the same efficiency at a different  $p_T$ . Consequently, no point appears for that  $p_T$  value. This is not often a practical concern, as the largest gains in signal discrimination and significance are for smaller values of  $\varepsilon_S$ , but it is something that must be considered when selecting benchmark tagger parameters and signal efficiencies.



(c) Trim vs. Prune comparison (incl. shape)

**Fig. 39** The performance of the BDT combinations of the trimming and pruning outputs with various shape observables in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Groomer mass outputs are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $r_{Qjet}$ , and all of the above (denoted "shape").

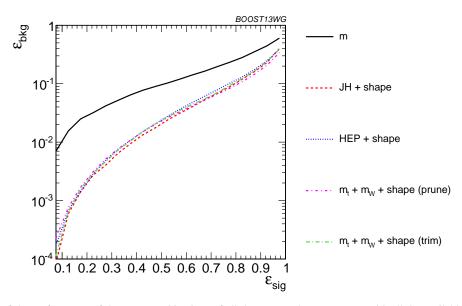


Fig. 40 Comparison of the performance of the BDT combinations of all the groomer/tagger outputs with all the available shape observables in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Tagger/groomer outputs are combined with all of the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{Qjet}$ .

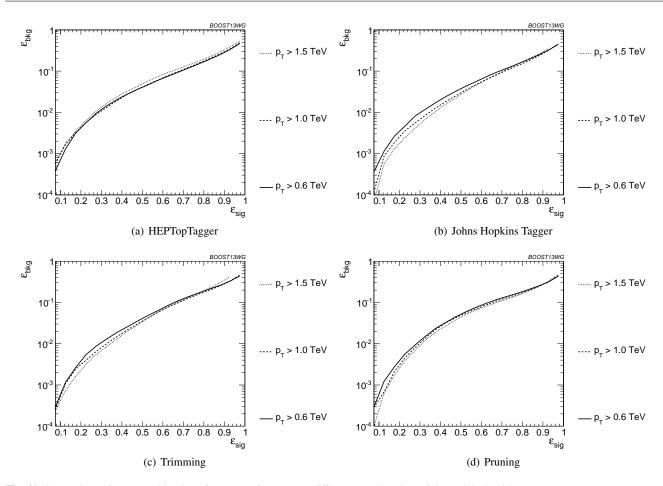


Fig. 41 Comparison of BDT combination of tagger performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

The degradation in performance is more pronounced fourse 1464 the BDT combinations of the full tagger outputs, shown inar 1465 Figure 47), particularly at very low signal efficiency where 1466 the optimization picks out a cut on the tail of some distri-1467 bution that depends precisely on the  $p_T/R$  of the jet. Once 1468 again, trimming and the Johns Hopkins tagger degrade more 1469 markedly. Similar behaviour holds for the BDT combina-1470 tions of tagger outputs plus all shape observables. 1472 1494

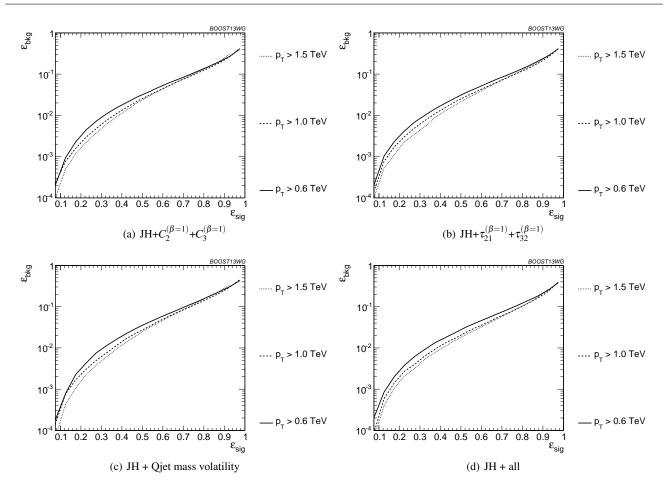
**Optimizing at a single** *R***:** We perform a similar analysis 1473 optimizing tagger parameters for each signal efficiency at 1474 R = 1.2, and then use the same parameters for smaller R, ilf<sup>97</sup> 1475 the  $p_T$  1.5-1.6 TeV bin. In Figure 48 we show the ratio of the 1476 performance of the top taggers, using just the reconstructet?" 1477 top mass as the discriminating variable, with all input pation 1478 rameters optimized to the R = 1.2 values compared to input for 1479 parameters optimized separately at each radius. While theo2 1480 performance of each observable degrades at small  $\mathcal{E}_{sig}$  conf<sup>503</sup> 1481 pared to the optimized search, the HEPTopTagger fares the504 1482 worst as the observed is quite sensitive to the selected value<sup>505</sup> 1483 of R. It is not surprising that a tagger whose top mass reconso 1484 struction is susceptible to background-shaping at large R and or 1485

 $p_T$  would require a more careful optimization of parameters to obtain the best performance.

The same holds true for the BDT combinations of the full tagger outputs, shown in Figure 49). The performance for the sub-optimal taggers is still within an O(1) factor of the optimized performance, and the HEPTopTagger performs better with the combination of all of its outputs relative to the performance with just  $m_t$ . The same behaviour holds for the BDT combinations of tagger outputs and shape observables.

**Optimizing at a single efficiency:** The strongest assumption we have made so far is that the taggers can be reoptimized for each signal efficiency point. This is useful for making a direct comparison of the power of different top tagging algorithms, but is not particularly practical for the LHC analyses. We now consider the effects when the tagger inputs are optimized once, in the  $\varepsilon_S = 0.3 - 0.35$  bin, and then used to determine the full ROC curve. We do this in the  $p_T 1 - 1.1$  TeV bin and with R = 0.8.

The performance of each tagger, normalized to its performance optimized in each bin, is shown in Figure 50 for



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Fig. 42 Comparison of BDT combination of JH tagger + shape at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

cuts on the top mass and W mass, and in Figure 51 for BDIE28 1508 combinations of tagger outputs and shape variables. In both29 1509 plots, it is apparent that optimizing the taggers in the 0.3530 0.35 efficiency bin gives comparable performance over efisit 1511 ficiencies ranging from 0.2-0.5, although performance des32 1512 grades at small and large signal efficiencies. Pruning appears 33 1513 to give especially robust signal-background discrimination34 1514 without re-optimization, possibly due to the fact that thereas 1515 are no absolute distance or  $p_T$  scales that appear in the algosse 1516 rithm. Figures 50 and 51 suggest that, while optimization at 37 1517 all signal efficiencies is a useful tool for comparing differsas 1518 ent algorithms, it is not crucial to achieve good top-tagging39 1519 performance in experiments. 1540 1520

We have studied the performance of various jet substructure observables, groomed masses, and top taggers to study the performance of top tagging at different  $p_T$  and jet radius passe rameter. At each  $p_T$ , R, and signal efficiency working point we optimize the parameters for those observables with tunes able inputs. Overall, we have found that these techniques sea individually and in combination, continue to perform well at high  $p_T$ , which is important for future LHC running. In general, the John Hopkins tagger performs best, while jet grooming algorithms under-perform relative to the best top taggers due to the lack of an optimized W-identification step; as expected from its design, the HEPTopTagger performance degrades at high  $p_T$ . Tagger performance can be improved by a further factor of 2-4 through combination with jet substructure observables such as  $\tau_{32}$ ,  $C_3$ , and Qjet mass volatility; when combined with jet substructure observables, the performance of various groomers and taggers becomes very comparable, suggesting that, taken together, the observables studied are sensitive to nearly all of the physical differences between top and QCD jets. A small improvement is also found by combining the Johns Hopkins and HEPTopTaggers, indicating that different taggers are not fully correlated.

Comparing results at different  $p_T$  and R, top tagging performance is generally better at smaller R due to less contamination from uncorrelated radiation. Similarly, most observables perform better at larger  $p_T$  due to the higher degree of collimation of radiation. Some observables fare worse at higher  $p_T$ , such as the *N*-subjettiness ratio  $\tau_{32}$  and the Qjet

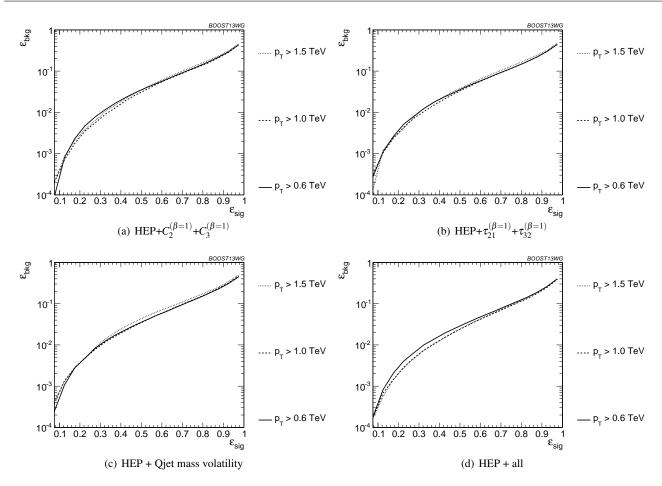


Fig. 43 Comparison of BDT combination of HEP tagger + shape at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

mass volatility  $\Gamma$ , as higher- $p_T$  QCD jets have more, hardebro emissions that fake the top jet substructure. The HEPTop-Tagger is also worse at large  $p_T$  due to the tendency of the tagger to shape backgrounds around the top mass. The  $p_T$ - and *R*-dependence of the multivariable combinations is dominated by the  $p_T$ - and *R*-dependence of the top mass reconstruction component of the tagger/groomer.

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Finally, we consider the performance of various observ-1557 able combinations under the more realistic assumption that  $t^{279}$ 1558 the input parameters are only optimized at a single  $p_T$ , R, or 1559 signal efficiency, and then the same inputs are used at other 1560 working points. Remarkably, the performance of all observ-1561 ables is typically within a factor of 2 of the fully optimized 1562 inputs, suggesting that while optimization can lead to sub-584 1563 stantial gains in performance, the general behaviour found<sup>1685</sup> 1564 in the fully optimized analyses extends to more general ap586 1565 plications of each variable. In particular, the performance of 1566 pruning typically varies the least when comparing suboptisse 1567 mal working points to the fully optimized tagger due to these 1568 scale-invariant nature of the pruning algorithm. 1590 1569

## 8 Summary & Conclusions

Furthering our understanding of jet substructure is crucial to improving our understanding of QCD and enhancing the prospects for the discovery of new physical processes at Run II of the LHC. In this report we have studied the performance of jet substructure techniques over a wide range of kinematic regimes that will be encountered in Run II of the LHC. The performance of observables and their correlations have been studied by combining the variables into BDT discriminants, and comparing the background rejection power of this discriminant to the rejection power achieved by the individual variables. The performance of "all variables" BDT discriminants has also been investigated, to understand the potential of the "ultimate" tagger where "all" available information (at least, all of that provided by the variables considered) is used.

We focused on the discrimination of quark jets from gluon jets, and the discrimination of boosted W bosons and top quarks from the QCD backgrounds. For each, we have identified the best-performing jet substructure observables, both individually and in combination with other observables. In

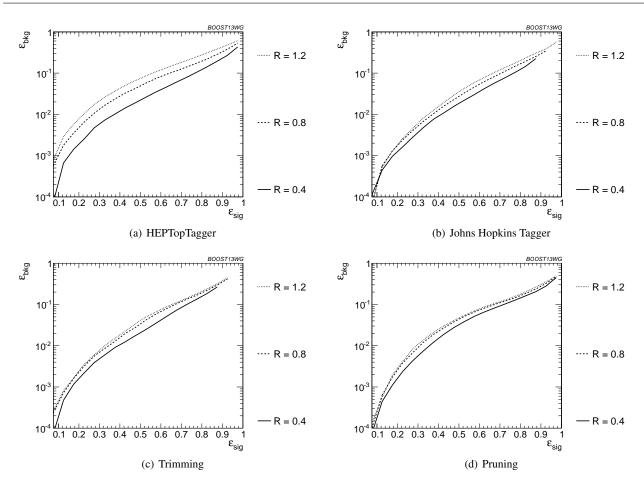
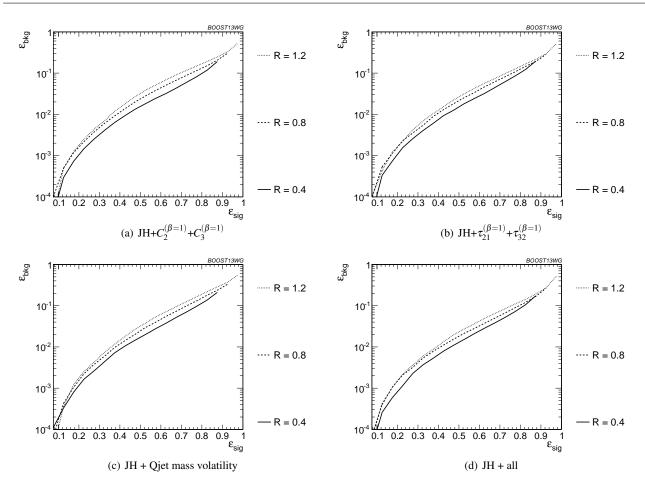


Fig. 44 Comparison of tagger and jet shape performance at different radius at  $p_T = 1.5-1.6$  TeV.

doing so, we have also provided a physical picture of why 1591 certain sets of observables are (un)correlated. Additionally, 14 1592 we have investigated how the performance of jet substruction 1593 ture observables varies with R and  $p_T$ , identifying observation 1594 ables that are particularly robust against or susceptible to17 1595 these changes. In the case of q/g tagging, it seems that close18 1596 to the ultimate performance can be achieved by combining19 1597 the most powerful discriminant, the number of constituents20 1598 of a jet, with just one other variable,  $C_1^{\beta=1}$  (or  $\tau_1^{\beta=1}$ ). Man<sub>1,2,2</sub> 1599 of the other variables considered are highly correlated anter-1600 provide little additional discrimination. For both top and W623 1601 tagging, the groomed mass is a very important discriminate24 1602 ing variable, but one that can be substantially improved inses 1603 combination with other variables. There is clearly a ricts<sup>26</sup> 1604 and complex relationship between the variables considered 1605 for W and top tagging, and the performance and correld<sup>627</sup> 1606 tions between these variables can change considerably withf28 1607 changing jet  $p_T$  and R. In the case of W tagging, even af<sup>629</sup> 1608 ter combining groomed mass with two other substructure 1609 observables, we are still some way short of the ultimate tage51 1610 ger performance, indicating the complexity of the informates 1611 tion available, and the complementarity between the observ<sup>1633</sup> 1612 1634

ables considered. In the case of top tagging, we have shown that the performance of both the John Hopkins and Hep Top Tagger can be improved when their outputs are combined with substructure observables such as  $\tau_{32}$  and  $C_3$ , and that the performance of a discriminant built from groomed mass information plus substructure observables is very comparable to the performance of the taggers. We have optimized the top taggers for a particular value of  $p_T$ , R, and signal efficiency, and studied their performance at other working points. We have found that the performance of observables remains within a factor of two of the optimized value, suggesting that the performance of jet substructure observables is not significantly degraded when tagger parameters are only optimized for a few select benchmark points.

Our analyses were performed with ideal detector and pile-up conditions in order to most clearly elucidate the underlying physical scaling with  $p_T$  and R. At higher boosts, detector resolution effects will become more important, and with the higher pile-up expected at Run II of the LHC, pileup mitigation will be crucial for future jet substructure studies. Future studies will be needed to determine which of the observables we have studied are most robust against pile-up



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Fig. 45 Comparison of BDT combination of JH tagger + shape at different radius at  $p_T = 1.5-1.6$  TeV.

and detector effects, and our analyses suggest particularly useful combinations of observables to consider in such studies ies.

At the new energy frontier of Run II of the LHC booster 1638 jet substructure techniques will be more central to our searches 1639 for new physics than ever before, and by achieving a deeperso 1640 understanding of the underlying structure of quark, gluon<sup>500</sup> 1641 W and Top initiated jets, and how the observables that trues 1642 to elucidate this structure are related, the hope is that more 1643 sophisticated taggers can be commissioned that will extendos 1644 the reach for new physics as far as possible. 1645 1664

## 1646 References

- 1647
   1. Boost2009, SLAC National Accelerator Laboratory, 9-10 July, 2009,
   1670
- [http://www-conf.slac.stanford.edu/Boost2009].
- Boost2010, University of Oxford, 22-25 June 2010, [http://www.physics.ox.ac.uk/boost2010].
- 3. Boost2011, Princeton University, 22-26 May 2011,
   [https://indico.cern.ch/event/138809/].

- Boost2012, IFIC Valencia, 23-27 July 2012, [http://ific.uv.es/boost2012].
- Boost2013, University of Arizona, 12-16 August 2013, [https://indico.cern.ch/event/215704/].
- 6. *Boost2014*, University College London, 18-22 August 2014,
- [http://http://www.hep.ucl.ac.uk/boost2014/].
  7. A. Abdesselam, E. B. Kuutmann, U. Bitenc,
  G. Brooijmans, J. Butterworth, et al., *Boosted objects:* A Probe of beyond the Standard Model physics, Eur.Phys.J. C71 (2011) 1661, [arXiv:1012.5412].
- A. Altheimer, S. Arora, L. Asquith, G. Brooijmans, J. Butterworth, et al., *Jet Substructure at the Tevatron* and LHC: New results, new tools, new benchmarks, J.Phys. G39 (2012) 063001, [arXiv:1201.0008].
- A. Altheimer, A. Arce, L. Asquith, J. Backus Mayes, E. Bergeaas Kuutmann, et al., *Boosted objects and jet* substructure at the LHC, arXiv:1311.2708.
- M. Cacciari, G. P. Salam, and G. Soyez, *FastJet User Manual*, *Eur.Phys.J.* C72 (2012) 1896, [arXiv:1111.6097].

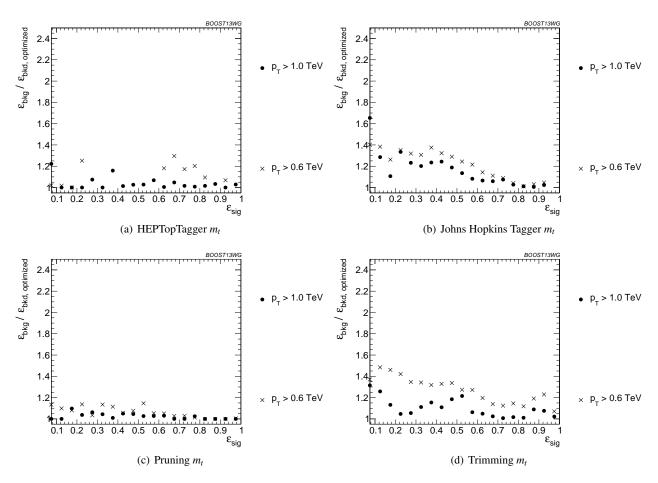


Fig. 46 Comparison of top mass performance of different taggers at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm; the tagger inputs are set to the optimum value for  $p_T = 1.5 - 1.6$  TeV.

1698

1699

- 1675 11. T. Plehn, M. Spannowsky, M. Takeuchi, and
- 1676
   D. Zerwas, Stop Reconstruction with Tagged Tops,

   1677
   JHEP 1010 (2010) 078, [arXiv:1006.2833].
- 107812. D. E. Kaplan, K. Rehermann, M. D. Schwartz, and<br/>B. Tweedie, Top Tagging: A Method for Identifying<br/>Boosted Hadronically Decaying Top Quarks,<br/>Phys.Rev.Lett. 101 (2008) 142001,<br/>[arXiv:0806.0848].1700
- 1683
   13. J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer, and
   1705

   1684
   T. Stelzer, MadGraph 5 : Going Beyond, JHEP 1106
   1706

   1685
   (2011) 128, [arXiv:1106.0522].
   1707
- 1686 14. Y. Gao, A. V. Gritsan, Z. Guo, K. Melnikov, 1708
- 1687
   M. Schulze, et al., Spin determination of
   1709

   1688
   single-produced resonances at hadron colliders,
   1710

   1689
   Phys.Rev. D81 (2010) 075022, [arXiv:1001.3396]. 1711
- 1500
   15. S. Bolognesi, Y. Gao, A. V. Gritsan, K. Melnikov,
   1712

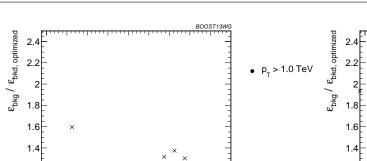
   1691
   M. Schulze, et al., On the spin and parity of a
   1713

   1692
   single-produced resonance at the LHC, Phys.Rev. D86714

   1693
   (2012) 095031, [arXiv:1208.4018].
   1715
- 169416. I. Anderson, S. Bolognesi, F. Caola, Y. Gao, A. V.17161695Gritsan, et al., Constraining anomalous HVV17171696interactions at proton and lepton colliders, Phys.Rev.1718

**D89** (2014) 035007, [arXiv:1309.4819].

- J. Pumplin, D. Stump, J. Huston, H. Lai, P. M. Nadolsky, et al., New generation of parton distributions with uncertainties from global QCD analysis, JHEP 0207 (2002) 012, [hep-ph/0201195].
- T. Sjostrand, S. Mrenna, and P. Z. Skands, A Brief Introduction to PYTHIA 8.1, Comput.Phys.Commun. 178 (2008) 852–867, [arXiv:0710.3820].
- A. Buckley, J. Butterworth, S. Gieseke, D. Grellscheid, S. Hoche, et al., *General-purpose event generators for LHC physics, Phys.Rept.* 504 (2011) 145–233, [arXiv:1101.2599].
- T. Gleisberg, S. Hoeche, F. Krauss, M. Schonherr,
   S. Schumann, et al., *Event generation with SHERPA* 1.1, JHEP 0902 (2009) 007, [arXiv:0811.4622].
- 21. S. Schumann and F. Krauss, *A Parton shower* algorithm based on Catani-Seymour dipole factorisation, JHEP **0803** (2008) 038, [arXiv:0709.1027].
- F. Krauss, R. Kuhn, and G. Soff, *AMEGIC++ 1.0: A Matrix element generator in C++, JHEP* 0202 (2002) 044, [hep-ph/0109036].



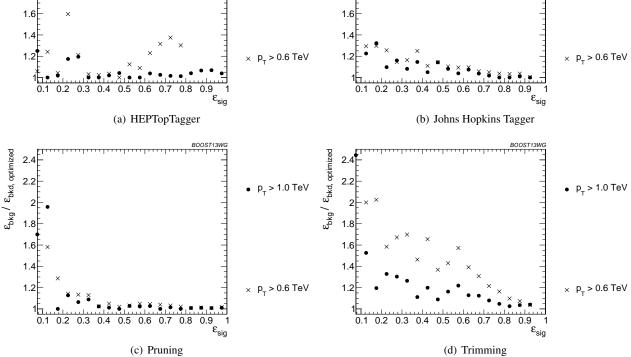


Fig. 47 Comparison of BDT combination of tagger performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm; the tagger inputs are set to the optimum value for  $p_T = 1.5 - 1.6$  TeV.

1742

1743

- 1719
   23. T. Gleisberg and S. Hoeche, Comix, a new matrix

   1720
   element generator, JHEP 0812 (2008) 039,

   1721
   [arXiv:0808.3674].
- 1722
   24. S. Hoeche, F. Krauss, S. Schumann, and F. Siegert,
   1744

   1723
   QCD matrix elements and truncated showers, JHEP
   1745

   1724
   0905 (2009) 053, [arXiv:0903.1219].
   1746
- 1725
   25. M. Schonherr and F. Krauss, Soft Photon Radiation in1747

   1726
   Particle Decays in SHERPA, JHEP **0812** (2008) 018, 1748

   1727
   [arXiv:0810.5071].
- 172826. JADE Collaboration Collaboration, S. Bethke et al., 17501729Experimental Investigation of the Energy Dependence17511730of the Strong Coupling Strength, Phys.Lett. B2131731(1988) 235.
- 1732
   27. M. Cacciari, G. P. Salam, and G. Soyez, *The Anti-k(t)* 1754

   1733
   *jet clustering algorithm*, *JHEP* 0804 (2008) 063, 1755

   1734
   [arXiv:0802.1189]. 1756
- 1735
   28. Y. L. Dokshitzer, G. Leder, S. Moretti, and B. Webber‡757

   1736
   Better jet clustering algorithms, JHEP **9708** (1997)

   1737
   001, [hep-ph/9707323].
- 173829. M. Wobisch and T. Wengler, Hadronization17601739corrections to jet cross-sections in deep inelastic17611740scattering, hep-ph/9907280.1762

 S. Catani, Y. L. Dokshitzer, M. Seymour, and B. Webber, *Longitudinally invariant Kt clustering algorithms for hadron hadron collisions*, *Nucl.Phys.* B406 (1993) 187–224.

p > 1.0 TeV

- S. D. Ellis and D. E. Soper, Successive combination jet algorithm for hadron collisions, Phys.Rev. D48 (1993) 3160–3166, [hep-ph/9305266].
- 32. S. D. Ellis, A. Hornig, T. S. Roy, D. Krohn, and M. D. Schwartz, *Qjets: A Non-Deterministic Approach to Tree-Based Jet Substructure*, *Phys.Rev.Lett.* **108** (2012) 182003, [arXiv:1201.1914].
- 33. S. D. Ellis, A. Hornig, D. Krohn, and T. S. Roy, On Statistical Aspects of Qjets, JHEP 1501 (2015) 022, [arXiv:1409.6785].
- 34. S. D. Ellis, C. K. Vermilion, and J. R. Walsh, *Recombination Algorithms and Jet Substructure: Pruning as a Tool for Heavy Particle Searches*, *Phys.Rev.* D81 (2010) 094023, [arXiv:0912.0033].
- 35. D. Krohn, J. Thaler, and L.-T. Wang, *Jet Trimming*, *JHEP* **1002** (2010) 084, [arXiv:0912.1342].
- 36. J. M. Butterworth, A. R. Davison, M. Rubin, and G. P. Salam, *Jet substructure as a new Higgs search channel*

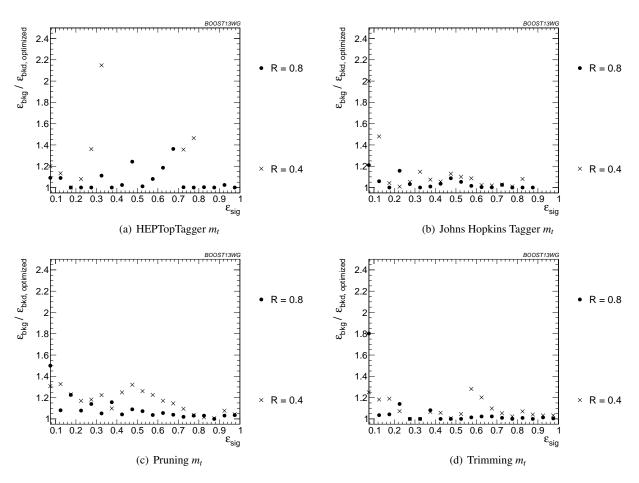


Fig. 48 Comparison of top mass performance of different taggers at different *R* in the  $p_T = 1500 - 1600$  GeV bin; the tagger inputs are set to the optimum value for R = 1.2.

1786

- at the LHC, Phys.Rev.Lett. 100 (2008) 242001,

   [arXiv:0802.2470].
- 1765
   37. A. J. Larkoski, S. Marzani, G. Soyez, and J. Thaler,
   1787

   1766
   Soft Drop, JHEP 1405 (2014) 146,
   1788

   1767
   [arXiv:1402.2657].
   1789
- 1768
   38. M. Dasgupta, A. Fregoso, S. Marzani, and G. P. Salam790

   1769
   Towards an understanding of jet substructure, JHEP

   1770
   1309 (2013) 029, [arXiv:1307.0007].
- 1771
   39. J. Thaler and K. Van Tilburg, Identifying Boosted
   1793

   1772
   Objects with N-subjettiness, JHEP **1103** (2011) 015,
   1794

   1773
   [arXiv:1011.2268].
   1795
- 1774
   40. A. J. Larkoski, D. Neill, and J. Thaler, Jet Shapes with 1796

   1775
   the Broadening Axis, JHEP 1404 (2014) 017, 1797

   1776
   [arXiv:1401.2158]. 1798
- 1777
   41. A. J. Larkoski and J. Thaler, Unsafe but Calculable:
   1709

   1778
   Ratios of Angularities in Perturbative QCD, JHEP
   1800

   1779
   1309 (2013) 137, [arXiv:1307.1699].
   1801
- 1780
   42. A. J. Larkoski, G. P. Salam, and J. Thaler, *Energy* 1802

   1781
   *Correlation Functions for Jet Substructure, JHEP* 1306.03

   1782
   (2013) 108, [arXiv:1305.0007].
   1804
- 178343. CMS Collaboration Collaboration, S. Chatrchyan18051784et al., Search for a Higgs boson in the decay channel H

to ZZ(\*) to q qbar  $\ell^- l$ + in pp collisions at  $\sqrt{s} = 7$ TeV, JHEP **1204** (2012) 036, [arXiv:1202.1416].

- 44. A. J. Larkoski, J. Thaler, and W. J. Waalewijn, Gaining (Mutual) Information about Quark/Gluon Discrimination, JHEP 1411 (2014) 129, [arXiv:1408.3122].
- A. Hoecker, P. Speckmayer, J. Stelzer, J. Therhaag, E. von Toerne, and H. Voss, *TMVA: Toolkit for Multivariate Data Analysis*, *PoS* ACAT (2007) 040, [physics/0703039].
- 46. ATLAS Collaboration Collaboration, G. Aad et al., Light-quark and gluon jet discrimination in pp collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector, Eur.Phys.J. C74 (2014), no. 8 3023, [arXiv:1405.6583].
- J. Gallicchio and M. D. Schwartz, *Quark and Gluon Jet Substructure*, *JHEP* 1304 (2013) 090, [arXiv:1211.7038].
- J. Gallicchio and M. D. Schwartz, *Quark and Gluon Tagging at the LHC*, *Phys.Rev.Lett.* **107** (2011) 172001, [arXiv:1106.3076].



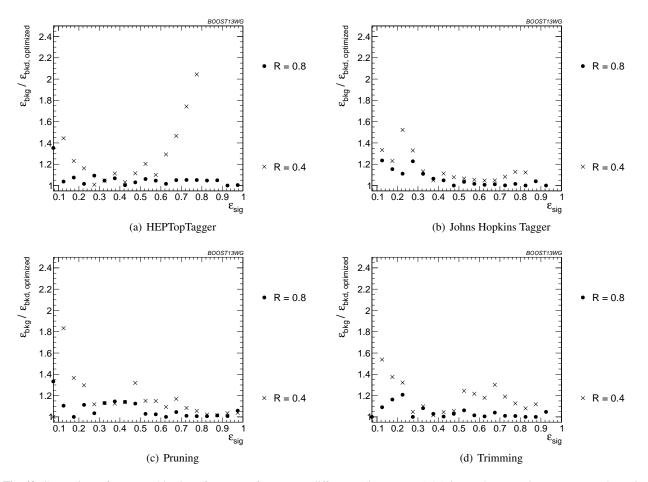


Fig. 49 Comparison of BDT combination of tagger performance at different radius at  $p_T = 1.5$ -1.6 TeV; the tagger inputs are set to the optimum value for R = 1.2.

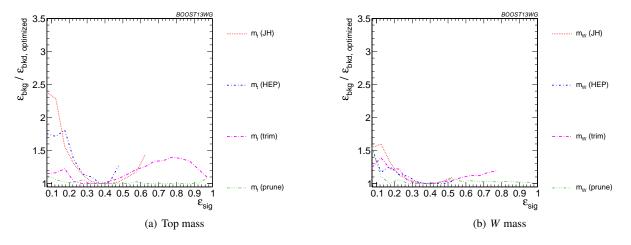
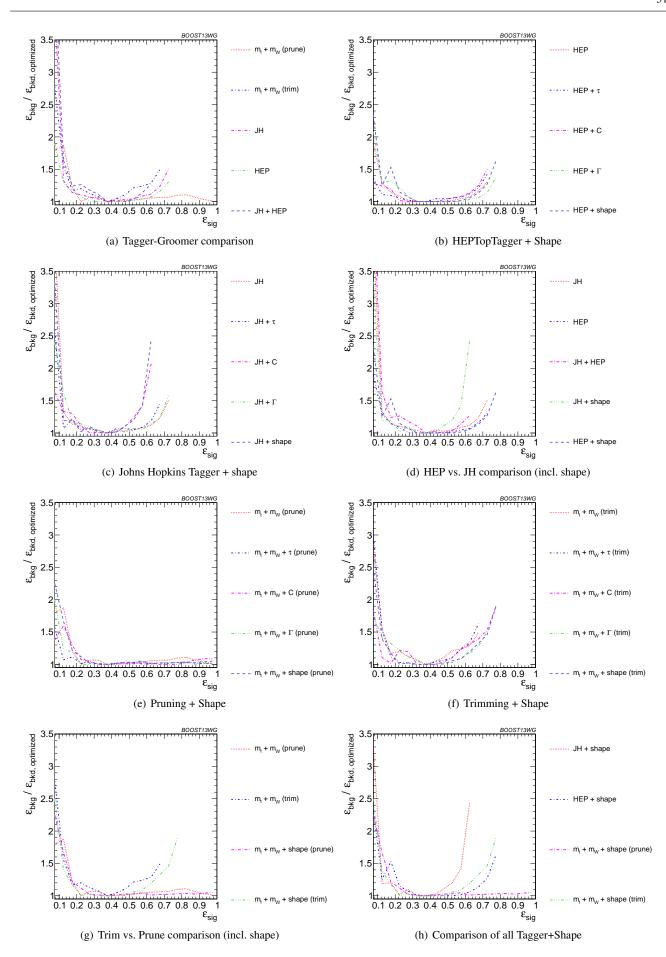


Fig. 50 Comparison of single-variable top-tagging performance in the  $p_T = 1 - 1.1$  GeV bin using the anti- $k_T$ , R=0.8 algorithm; the inputs for each tagger are optimized for the  $\varepsilon_{sig} = 0.3 - 0.35$  bin.



**Fig. 51** The BDT combinations in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Taggers are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{Qjet}$ , and all of the above (denoted "shape"). The inputs for each tagger are optimized for the  $\varepsilon_{sig} = 0.3 - 0.35$  bin.

1806	49.	CMS Collaboration Collaboration, C. Collaboration,
1807		Performance of quark/gluon discrimination in 8 TeV pp
1808		data, .
1809	50.	Hn. Li, Z. Li, and CP. Yuan, QCD resummation for
1810		light-particle jets, Phys.Rev. D87 (2013) 074025,
1811		[arXiv:1206.1344].
1812	51.	M. Dasgupta, K. Khelifa-Kerfa, S. Marzani, and
1813		M. Spannowsky, On jet mass distributions in Z+jet and
1814		dijet processes at the LHC, JHEP 1210 (2012) 126,
1815		[arXiv:1207.1640].
1816	52.	YT. Chien, R. Kelley, M. D. Schwartz, and H. X. Zhu,
1817		Resummation of Jet Mass at Hadron Colliders,
1818		Phys.Rev. D87 (2013), no. 1 014010,
1819		[arXiv:1208.0010].
1820	53.	T. T. Jouttenus, I. W. Stewart, F. J. Tackmann, and W. J.
1821		Waalewijn, Jet mass spectra in Higgs boson plus one
1822		jet at next-to-next-to-leading logarithmic order,
1823		<i>Phys.Rev.</i> <b>D88</b> (2013), no. 5 054031,
1824		[arXiv:1302.0846].
1825	54.	S. D. Ellis, C. K. Vermilion, and J. R. Walsh,
1826		Techniques for improved heavy particle searches with
1827		jet substructure, Phys.Rev. D80 (2009) 051501,
1828		[arXiv:0903.5081].
1829	55.	M. Dasgupta, A. Fregoso, S. Marzani, and A. Powling,
1830		Jet substructure with analytical methods, Eur.Phys.J.
1831		<b>C73</b> (2013), no. 11 2623, [arXiv:1307.0013].
1832	56.	Performance of Boosted W Boson Identification with
1833		the ATLAS Detector, Tech. Rep.
1834		ATL-PHYS-PUB-2014-004, CERN, Geneva, Mar,
1835		2014.
1836	57.	S. Schaetzel and M. Spannowsky, <i>Tagging highly</i>
1837		boosted top quarks, Phys.Rev. D89 (2014), no. 1
1838		014007, [arXiv:1308.0540].
1839	58.	C. Anders, C. Bernaciak, G. Kasieczka, T. Plehn, and
1840		T. Schell, <i>Benchmarking an Even Better</i>
1841		<i>HEPTopTagger</i> , <i>Phys.Rev.</i> <b>D89</b> (2014) 074047,
1842		[arXiv:1312.1504].