

F-theory phenomenology

Fernando Marchesano



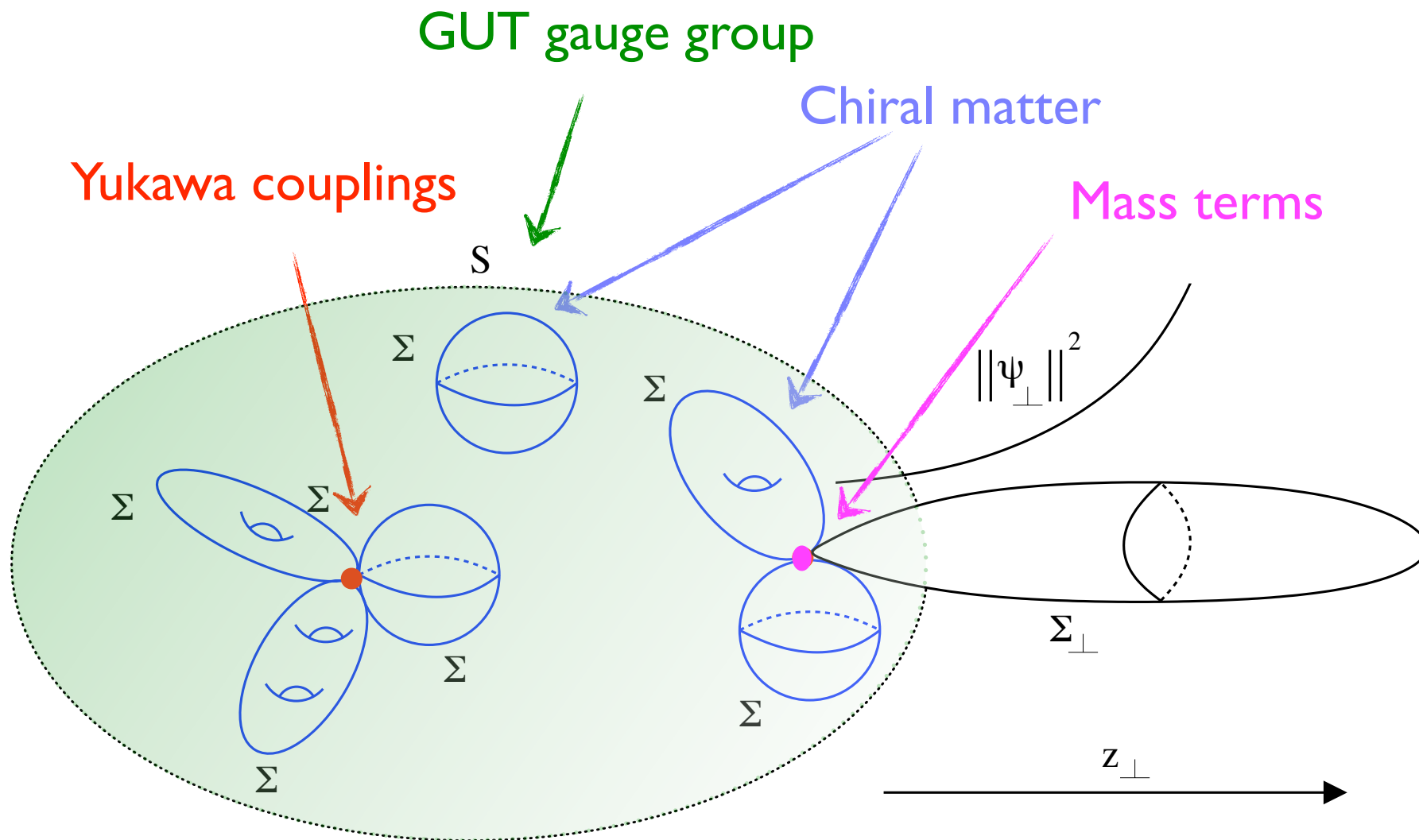
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Block II:
From GUTs to the
MSSM

GUT's from F-theory

- ✿ We have just seen how to engineer a 4D GUT local model via F-theory, and to achieve a number of essential model building ingredients



GUT's from F-theory

- ❖ We have just seen how to engineer a 4D GUT local model via F-theory, and to achieve a number of essential model building ingredients
- ❖ However, it remains to be seen if we can obtain acceptable physics below M_{GUT}
- ❖ In particular, in the range $M_{\text{SUSY}} \ll M \ll M_{\text{GUT}}$ we would like to have

SM gauge group

MSSM matter content

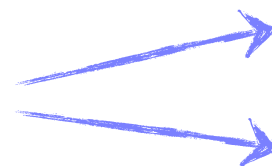
No exotic matter

Acceptable Yukawas and μ -term

Acceptable proton lifetime

R-parity

No 5D & 6D operators
(No Higgs triplets)



MSSM from GUT's

- ❖ In the following we will see **how F-theory GUT's can realize all these phenomenological features**
- ❖ We will also see that **each item** in our “wish list” translates into a topological or **geometrical condition** to be satisfied by our model
- ❖ In fact, such geometrical picture will provide **new mechanisms** to deal with typical problems that arise in classical 4D field theory GUT models

Bibliography:

Beasley, Heckman, Vafa - 0806.0102

Donagi & Wijnholt - 0808.2223

Font & Ibáñez - 0811.2157

Basic Assumptions

- ❖ $M_{\text{GUT}} \ll M_{\text{Planck}}$, and in principle there is the limit $M_{\text{GUT}}/M_{\text{Planck}} \rightarrow 0$

Hence, we can formally **decouple gravity** from our gauge theory, as usually assumed in 4D field theory GUT model building

- ❖ $M_{\text{GUT}} \gg M_{\text{SUSY}} (\sim \text{TeV})$

At this level of the construction **everything is supersymmetric** (see next block for SUSY-breaking)

Decoupling Limit

✿ $M_{\text{GUT}} \ll M_{\text{Planck}}$, and in principle there is the limit $M_{\text{GUT}}/M_{\text{Planck}} \rightarrow 0$

Hence, we can formally **decouple gravity** from our gauge theory, as usually assumed in 4D field theory GUT model building

- ◆ This implies that **the volume of the 4-cycle S and the volume of the compact manifold B_3 are not linked**, so that we can take $M_{\text{Planck}} \rightarrow \infty$ while keeping M_{GUT} fixed
- ◆ This imposes a strong constraint on S , namely that it should be a **del Pezzo surface dP_N**

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

- ✿ An important question is how the gauge group G_{GUT} is broken down to $G_{\text{MSSM}} = \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y$ below M_{GUT}
- ✿ In usual 4D GUT's this is essentially realized via adjoint Higgsing

$$\text{SU}(5) \xrightarrow{24} \text{SU}(3) \times \text{SU}(2) \times \text{U}(1) \xrightarrow{5} \text{SU}(3) \times \text{U}(1)_{\text{em}}$$
$$\langle \Phi \rangle = \text{diag}(2V, 2V, 2V, -3V, -3V), \quad \langle H \rangle = (0, 0, 0, 0, v)^t$$

$$\text{SO}(10) \longrightarrow \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$$

$$\text{SO}(10) \longrightarrow \text{SU}(5) \times \text{U}(1) \longrightarrow \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$$

$$\text{SO}(10) \longrightarrow \text{SU}(3) \times \text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{\text{B-L}} \longrightarrow \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$$



We need a field Φ in the adjoint of G_{GUT}
as well as a way to generate a potential for it

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

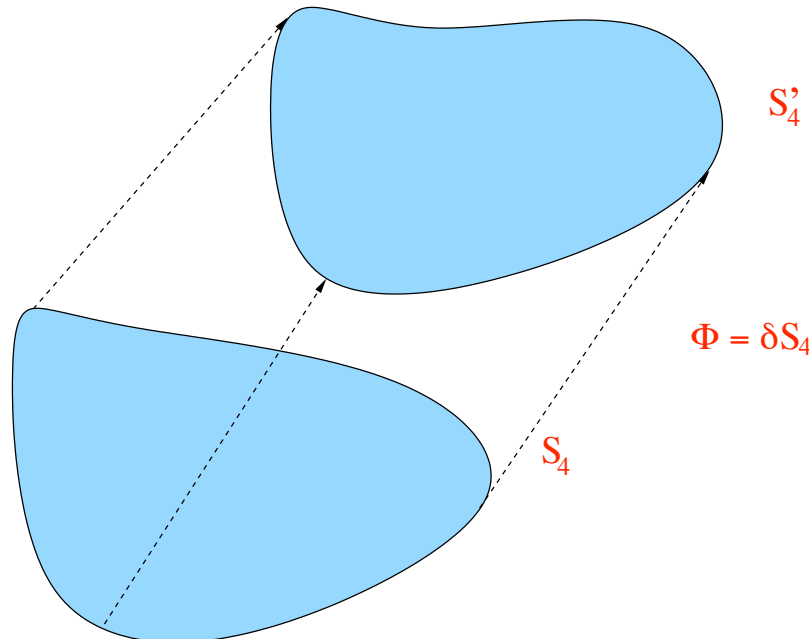
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- ❖ In usual 4D GUT's this is essentially realized via adjoint Higgsing
- ❖ Just like for a D7-brane wrapping a 4-cycle S , adjoint fields appear if

$h^{(0,1)}(S) \neq 0 \Rightarrow$ Wilson lines

$h^{(0,2)}(S) \neq 0 \Rightarrow$ Geometric deformations of S



No potential



Potential generated by
background fluxes

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$h^{(0,2)}(S) \neq 0 \Rightarrow$ Geometric deformations of S

- ✦ However, for a del Pezzo surface $h^{(0,1)} = h^{(0,2)} = 0 \Rightarrow$ No adjoints



The usual 4D GUT model is incompatible
with decoupling gravity

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

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- ❖ Adjoint Higgsing **X**
- ❖ An alternative mechanism relies on turning on **discrete Wilson lines**, available whenever $h^{(0,1)}(S) = 0$ but $\pi_1(S) \neq 0$
- ◆ However for $S = \text{del Pezzo}$ $\pi_1(S) = 0 \Rightarrow$ **No discrete Wilson lines**

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

- ❖ An important question is how the gauge group G_{GUT} is broken down to $G_{\text{MSSM}} = \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y$ below M_{GUT}
- ❖ Adjoint Higgsing ✗
- ❖ Discrete Wilson lines ✗
- ❖ Finally, one can turn on a $F_{\text{U}(1)}$ flux along S , so that $G_{\text{new}} = [G_{\text{GUT}}, \text{U}(1)]$

◆ In particular $\text{SU}(5) \xrightarrow{F_Y} \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y$

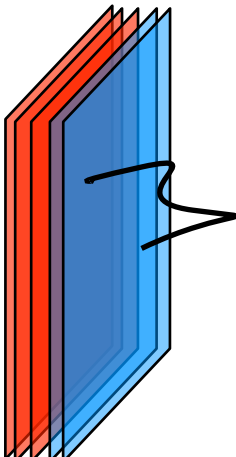
$$F_Y = \begin{pmatrix} -2 & & & & \\ & -2 & & & \\ & & -2 & & \\ & & & 3 & \\ & & & & 3 \end{pmatrix}$$

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

- ❖ An important question is how the gauge group G_{GUT} is broken down to $G_{\text{MSSM}} = \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y$ below M_{GUT}
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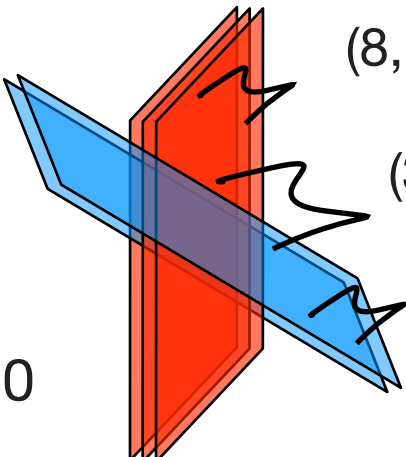
◆ Dual picture of intersecting D-branes



24

$F_Y=0$

⇒



$F_Y \neq 0$

$$F_Y = \begin{pmatrix} -2 & & & & \\ & -2 & & & \\ & & -2 & & \\ & & & 3 & \\ & & & & 3 \end{pmatrix}$$

(8,1)

(3,2)₋₅

(1,3)

← unwanted matter

$G_{\text{GUT}} \rightarrow G_{\text{MSSM}}$ breaking

- ❖ An important question is how the gauge group G_{GUT} is broken down to $G_{\text{MSSM}} = \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y$ below M_{GUT}
- ❖ Adjoint Higgsing ❌
- ❖ Discrete Wilson lines ❌
- ❖ Hypercharge flux F_Y ✓

Caveats:

- ◆ If F_Y couples to RR bulk fields, $\text{U}(1)_Y$ will get a **Stückelberg mass**
- ◆ In general F_Y will generate reps. $(\bar{3}, 2)_5, (3, \bar{2})_{-5}$ that mediate proton decay
- ◆ Just as F_Y modifies the gauge group on S , it can modify the matter content on $\Sigma \Rightarrow$ we could induce **MSSM exotics**

Massless Hypercharge

- ❖ In type IIB, a D7-brane with gauge group U(1) contains the coupling

$$\int_{\mathbb{R}^{1,3} \times S} F^2 \wedge C_4 = \sum_i \int_{\mathbb{R}^{1,3}} F \wedge B_2^i \int_S F_{U(1)} \wedge \alpha_2^i$$

where α_2 are harmonic forms of the bulk. If $\int_S (\alpha_2^i) \neq 0$ for any i , the 4D coupling renders the U(1) massive via a Stückelberg mechanism

- ❖ One can achieve that $\int_S (\alpha_2^i) = 0 \forall i$, by taking the P.D. ($F_{U(1)}$) a non-trivial 2-cycle of S which is nevertheless trivial in the homology of B_3

Buican et al. - hep-th/0610007

- ❖ The same happens in F-theory, so a viable F-theory GUT model is based on a del Pezzo surface $S \subset B_3$, where some 2-cycles of S are trivial in B_3

- ❖ Such setup is impossible if B_3
 \downarrow \mathbb{P}^1 \Rightarrow
 S

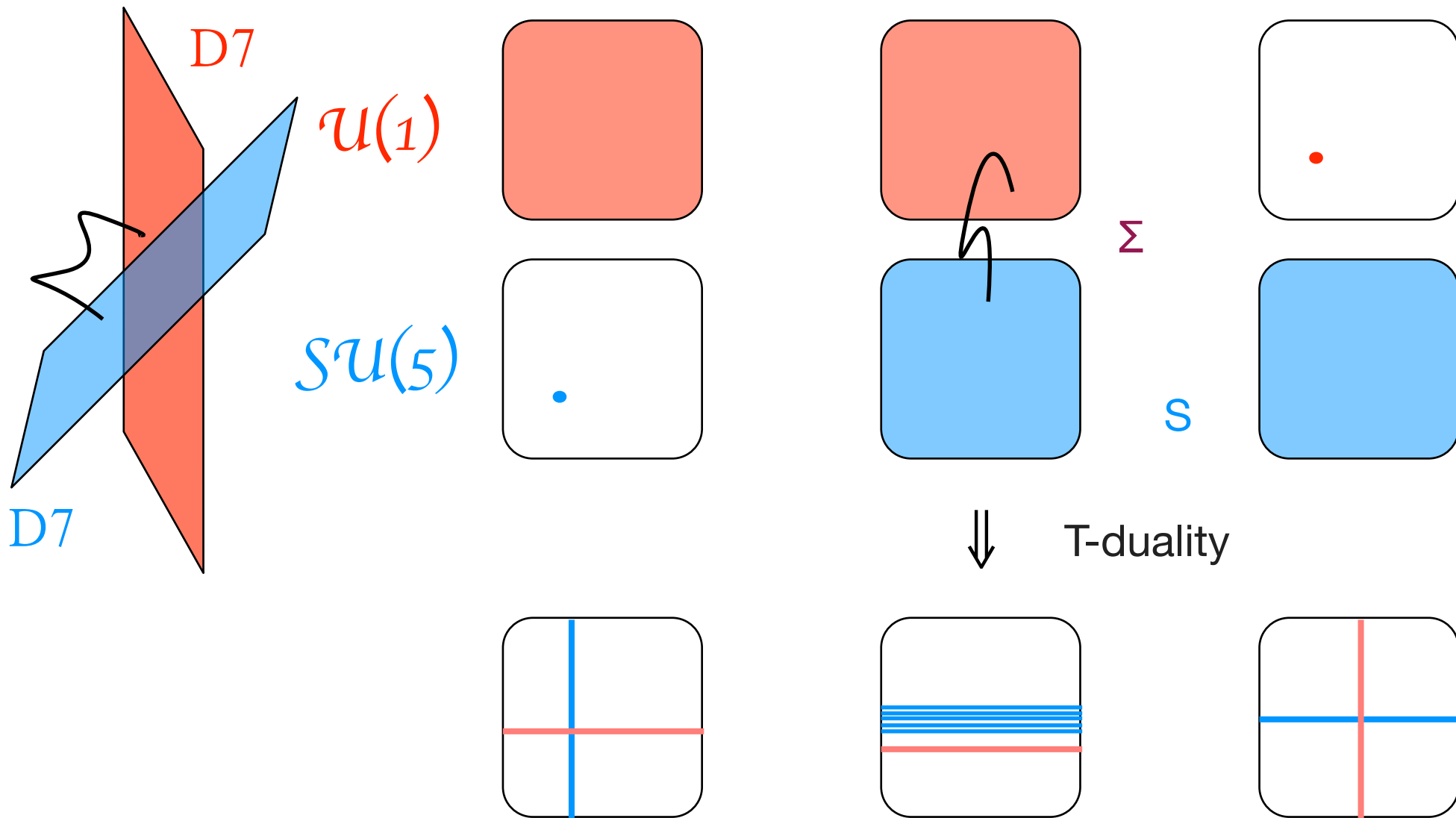
No obvious
heterotic dual

Avoiding Exotics

- ❖ An extra condition is that **no** $(3,2)_{-5} + (\bar{3},2)_5$ should appear upon introducing F_Y , not even in vector-like pairs, since that could mediate **proton decay**
- ❖ In terms of the topology of dP_N , this means that $5F_Y$ **must live in** a specific set of $H_2(dP_N, \mathbb{Z})$, that correspond to the **simple roots of the Lie algebra $E_N \Rightarrow N$ choices**
- ❖ It turns that $F_Y \notin H_2(dP_N, \mathbb{Z})$ but only $5F_Y$ does. This is **not incompatible with Dirac quantization**, since all the fields are also charged under some extra $U(1)$'s that should be turned on for consistency

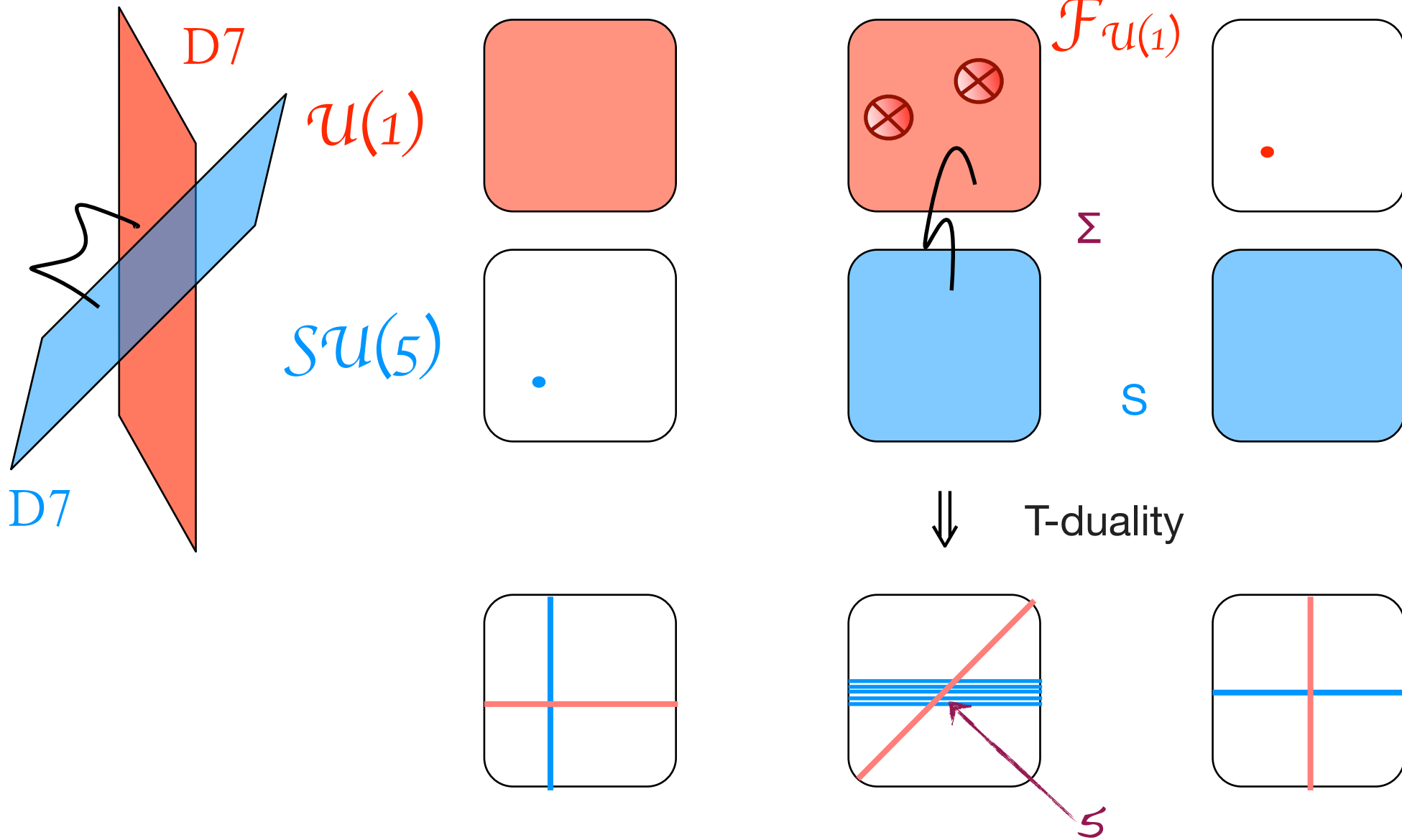
Avoiding Triplets

✿ In flat space:



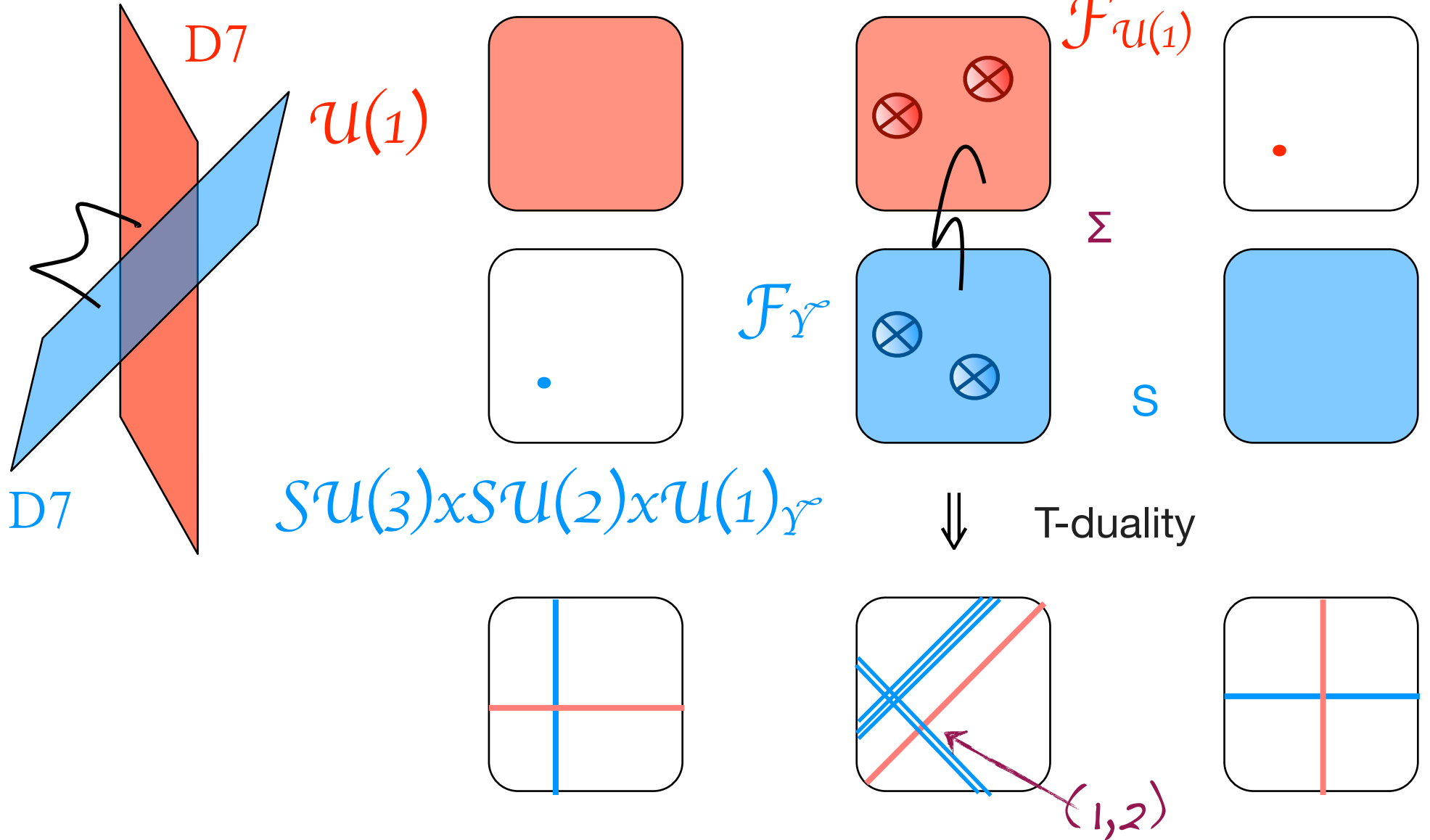
Avoiding Triplets

✿ In flat space:



Avoiding Triplets

✿ In flat space:



Avoiding Exotics

- ❖ In general, whenever $\int_{\Sigma} F_Y \neq 0$, Σ will **no longer** contain **full GUT multiplets**
- ❖ This can be **positive for the Higgs curve Σ_H** , since we may get rid of the triplet Higgses, but potentially **dangerous for the rest** of the matter curves, since no exotics are contained there
- ❖ Indeed, for **SU(5) each family = $10 + \bar{5}$** \Rightarrow anomaly free combination

$$\bar{5} = \begin{pmatrix} d_R^1 \\ d_R^2 \\ d_R^3 \\ e \\ \nu_e \end{pmatrix}, \quad 10 = \begin{pmatrix} 0 & u_R^3 & -u_R^2 & u_L^1 & d_L^1 \\ & 0 & u_R^1 & u_L^2 & d_R^2 \\ & & 0 & u_L^3 & d_L^3 \\ & & & 0 & e_R \\ & & & & 0 \end{pmatrix}$$

- ❖ For SO(10):

$$16 = (\nu_L, u_L^1, u_L^2, u_L^3; e_L, d_L^1, d_L^2, d_L^3; d_R^3, d_R^2, d_R^1, e_R; u_R^3, u_R^2, u_R^1, \nu_R)$$

Avoiding Exotics

- ❖ In general, whenever $\int_{\Sigma} F_Y \neq 0$, Σ will no longer contain full GUT multiplets
- ❖ This can be positive for the Higgs curve Σ_H , since we may get rid of the triplet Higgses, but potentially dangerous for the rest of the matter curves, since no exotics are contained there
- ❖ A simple way to avoid exotics is then to impose

$$\int_{\Sigma_H} F_Y \neq 0 \quad \text{For the Higgs curve}$$

$$\int_{\Sigma_i} F_Y = 0 \quad \text{For the matter curves}$$

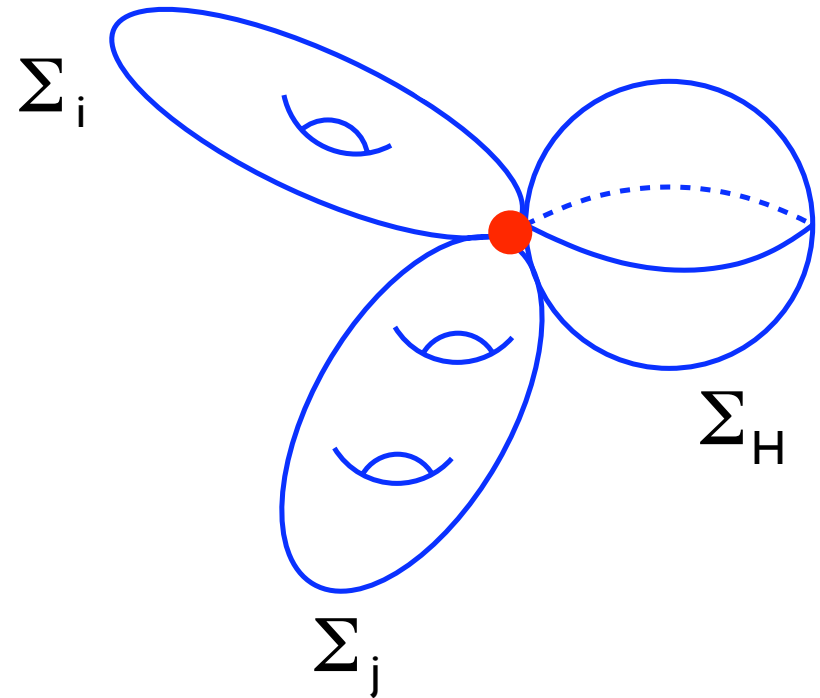
- ➔ allows to define R-parity in terms of the flux G_4
- ➔ favors that H_u and H_d arise from different curves Σ_H , which in turn suppresses 5D operators violating Baryon number

Yukawas and textures

- ❖ In the simplest GUT models, all MSSM matter localizes on curves
- ❖ Hence all Yukawas arise from triple intersections
- ❖ As each curve typically contains a different family of (up-like) quarks, we find a texture of the form

$$\lambda_{ij}^u = \begin{pmatrix} 0 & A & B \\ A & 0 & C \\ B & C & 0 \end{pmatrix}$$

that rather suggests one light family and two heavy ones

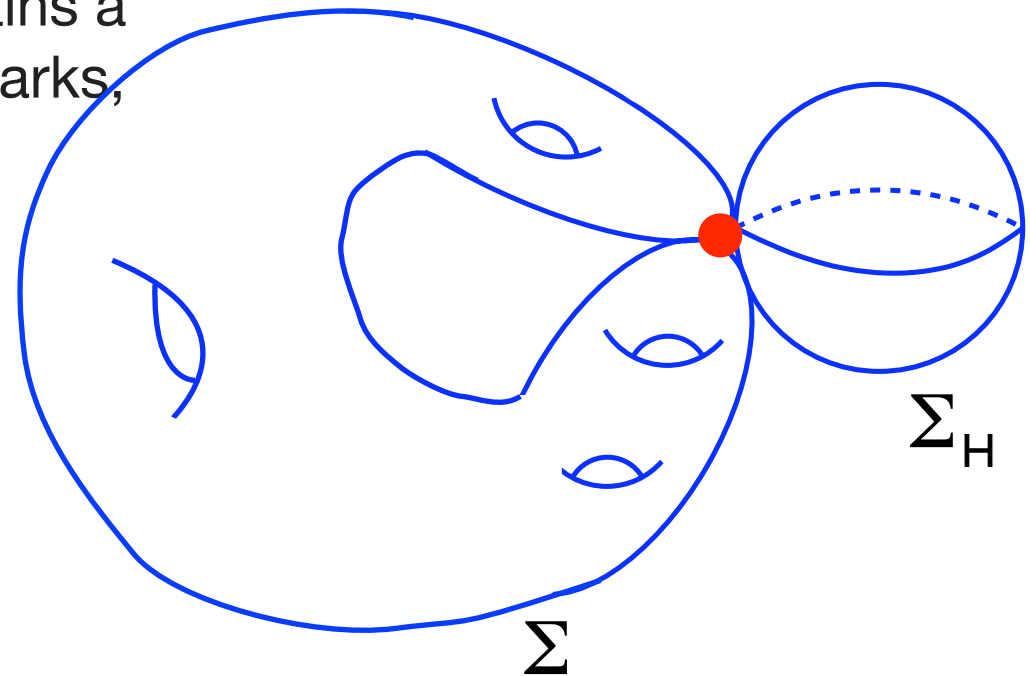


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- ❖ A possibility to allow diagonal entries is to consider self-intersecting curves

Yukawas and textures

- ❖ In the simplest GUT models, **all MSSM matter localizes on curves**
- ❖ Hence all **Yukawas** arise from **triple intersections**
- ❖ Another possibility is to **weaken the condition**

$$\int_{\Sigma_i} F_Y = 0 \quad \forall i \quad \text{to} \quad \sum_i \int_{\Sigma_i} F_Y = 0$$

Ibáñez & Font - 0811.2157

- ❖ If this is done, each matter curve Σ_i **will not contain** the usual **GUT multiplets**, but those will be **unequally distributed** among all the curves
- ❖ The total spectrum is however the same and the Yukawas present **more interesting textures**. Neat example: SO(10) model

quarks

$$\lambda_{ij}^Q \sim \begin{pmatrix} x & x & 0 \\ x & x & 0 \\ 0 & 0 & x \end{pmatrix}$$

leptons

$$\lambda_{ij}^l \sim \begin{pmatrix} x & x & x \\ x & x & x \\ x & x & x \end{pmatrix}$$

Yukawas and textures

- ✿ In conventional 4D GUT's there are **very few independent Yukawas**

$$L_{YUK}^{SU(5)} = Y_U^{ij} \bar{\psi}_{10}^i \psi_{10}^j H_5^* + Y_{D,L}^{ij} \bar{\psi}_5^i \psi_{10}^j H_5 + h.c.$$

- $Y_D(M_{GUT}) = Y_L(M_{GUT})$
 - **At M_{EW} : $m_b/m_\tau \sim 3$** (good for the 3rd family, bad for 1st and 2nd)
 - For **SO(10)** there is **only one Yukawa** coupling
- ✿ In models with extra dimensions we have **more freedom**.

In the case at hand:

$$m_Q = m_l \left| \frac{\psi_Q(0)}{\psi_l(0)} \right| \quad \leftarrow \text{different } \psi\text{'s expected from different hyperch.}$$

- ✿ Such **discrepancy** will in average be **bigger for larger $\text{Vol}(\Sigma)$** , which usually contain the **lightest generations!!**

Further couplings

- ❖ Another important class of cubic couplings are those that involve a **singlet Φ under G_{GUT}**

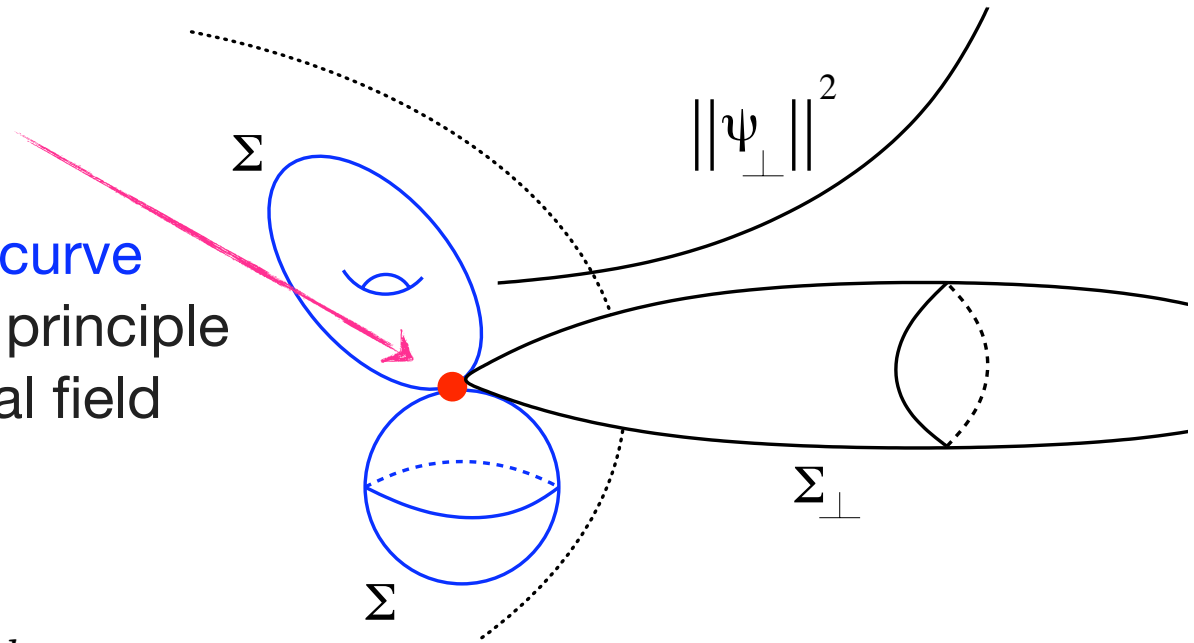
$$W_{\perp} = \lambda \Phi XY$$

- ❖ Such singlet lives in a **curve transverse to S** and in principle will be a non-dynamical field

Example: **μ -term**

$$W_{\mu} = \lambda \Phi H_u H_d$$

- ❖ This coupling will be **enhanced or suppressed** depending on the behavior of the **singlet wavefunction near S**



Singlet wavefunctions

- ❖ Singlet wavefunctions satisfy the following **Laplace equation** in the coordinate z transverse to S

$$4 \frac{\partial^2 \psi}{\partial z \partial \bar{z}} = \left(\frac{1}{2} \mathcal{R} - \mathcal{F} \right) \psi \quad \Rightarrow \quad \psi = e^{\frac{1}{4} \left(\frac{1}{2} \mathcal{R} - \mathcal{F} \right) |z|^2} + \dots$$

- ❖ In this frame the norm of ψ is given by

$$\|\psi\|^2 = M_*^2 \int_{\Sigma_\perp} e^{2\phi(z, \bar{z})} |\psi|^2 \quad e^{2\phi(z, \bar{z})} |\psi|^2 \sim e^{-\frac{1}{2} \left(\frac{1}{2} \mathcal{R} + \mathcal{F} \right) |z|^2}$$

$$\mathcal{R} \sim -M_{GUT}^2$$

$$\mathcal{F} \sim \pm \text{Vol}^{-1}(\Sigma_X) \pm \text{Vol}^{-1}(\Sigma_Y) \sim \pm M_{GUT}^2$$

➔ Everything depends on the **sign of $\mathcal{F} + \mathcal{R}/2$**

- **positive** \Rightarrow coupling **enhancement** $\Rightarrow \|\psi\|^2 \sim M_*^2 / M_{GUT}^2$
- **negative** \Rightarrow coupling **suppression** (μ -term)