

POETIC VI - École Polytechnique

Intrinsic bottom and its impact on heavy new  
physics at the LHC

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Florian Lyonnet

with T. Ježo, K. Kovařík, A. Kusina, F. Olness, I. Schienbein, J. Yu

Southern Methodist University



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# Introduction

- **Heavy quarks parton distribution function** play an important role in several SM and BSM processes
  - ▶  $b$  plus jet, associated  $tW$ ,  $tH^+$
- In the Standard approach, HQ PDF:
  - ▶ **DGLAP**+ perturbatively calculable boundary condition
- Purely perturbative treatment:  $m_c = 1.3$  GeV?  $m_b = 4.5$  GeV?
  - ▶ **Light-cone** and **meson cloud** models predict a **non-perturbative** heavy quark component
- Global analysis for **IC** by CTEQ and Jimenez-Delgado et al.  
⇒ set *significantly different limits*

# Motivations

## Our approach

- (II) Intrinsic heavy quark evolution can be **decoupled**
  - ▶ Quantify our approximation
- (III) Fill the gap by providing **IB(IC)** PDF
  - ▶ Well suited because the normalization can be **adjusted freely**
- (IV) Study the impact of IC and IB on parton-parton luminosities at the **LHC**
  - ▶ Assess the impact on **SM** and **NP** processes

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II) Evolution of intrinsic heavy quarks

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IV) Parton-parton Luminosities and intrinsic heavy quarks at the LHC 14 TeV

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# Evolution equation

## Definition

- $Q_1(x, \mu_0) := Q(x, \mu_0) - Q_0(x, \mu_0)$ ,
  - ▶ in  $\overline{\text{MS}}$  (only NLO),  $Q_0(x, \mu_0) = 0$  if  $\mu_0 = m_Q$
- Any non-zero boundary condition  $Q(x, m_Q) \neq 0$  can be attributed to intrinsic component
- Light quark  $q$ , heavy quark ( $c$  or  $b$ )  $Q$ , and gluon  $g$

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$$\dot{g} = P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q,$$

$$\dot{q} = P_{qq} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q,$$

$$\dot{Q} = P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q.$$

- $Q = Q_0 + Q_1$ 
  - ▶  $Q_0$  is the usual radiatively generated extrinsic heavy quark
  - ▶  $Q_1$  is the **non-perturbative** intrinsic heavy quark



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$$\begin{aligned} \dot{g} &= P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q_0 + \cancel{P_{gQ} \otimes Q_1}, \\ \dot{q} &= P_{qq} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q_0 + \cancel{P_{qQ} \otimes Q_1}, \\ \dot{Q}_0 + \dot{Q}_1 &= P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q_0 + P_{QQ} \otimes Q_1. \end{aligned}$$

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- $(q, g, Q_0) \Rightarrow$  usual DGLAP eq. without intrinsic
  - $Q_1$  Standalone **non-singlet** evolution equation
    - ▶  $\dot{Q}_1 = P_{QQ} \otimes Q_1$ .

## Sum rule

### Full-fledge analysis:

- Modified **sum rule** in global analysis:

$$\int_0^1 dx x \left( g + \sum_i (q_i + \bar{q}_i) + Q_0 + \bar{Q}_0 + Q_1 + \bar{Q}_1 \right) = 1.$$

- Allowing for a small **violation** of the sum rule we can completely decouple the analysis of **intrinsic heavy quarks**

$$\Rightarrow \left\{ \begin{array}{l} \bullet \text{ Can take } \mathbf{\text{any PDF set}} \text{ for } (q, g, Q_0) \\ \bullet \text{ Add the standalone intrinsic heavy quark} \end{array} \right.$$

- Violation of the sum rule:  $\int_0^1 dx x (Q_1 + \bar{Q}_1)$

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## Different matching conditions

### BHPS Intrinsic charm:

$$c_1(x) = \bar{c}_1(x) \propto x^2 [6x(1+x) \ln x + (1-x)(1+10x+x^2)]$$

- **Normalization** and **precise energy scale** are not specified
- $b$ -quark expected to be **very similar** with **normalization suppressed**  $m_c^2/m_b^2 \simeq 0.1$
- Matching scale is “unknown”:
  - ▶  $b_1(x, m_b) = \frac{m_c^2}{m_b^2} c_1(x, m_c)$
  - ▶  $b_1(x, m_c) = \frac{m_c^2}{m_b^2} c_1(x, m_c) \Rightarrow$  our ansatz
- **Remains valid** at all scales
- Note that **asymmetric boundary conditions**,  $c_1(x) \neq \bar{c}_1(x), b_1(x) \neq \bar{b}_1(x)$  could be accommodated (like in meson cloud models)

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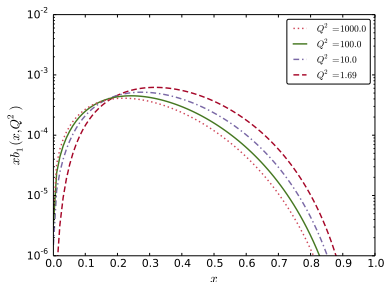
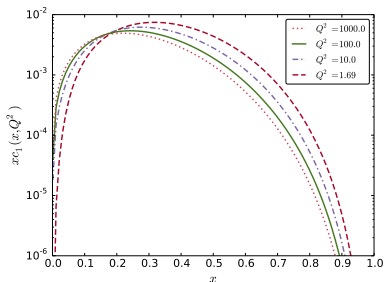
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## $c_1(x)$ , $b_1(x)$ @NLO

- $b_1(x, m_c) = \frac{m_c^2}{m_b^2} c_1(x, m_c)$ ,  $\int_0^1 c_1(x) = 0.01$ ,  $m_c = 1.3$  GeV,  
 $m_b = 4.5$  GeV

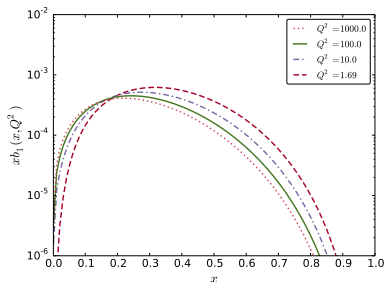
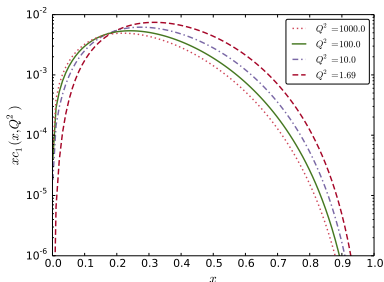


- The normalization can be changed by **simple rescaling**



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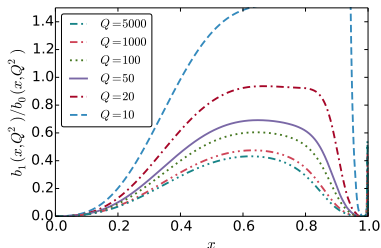
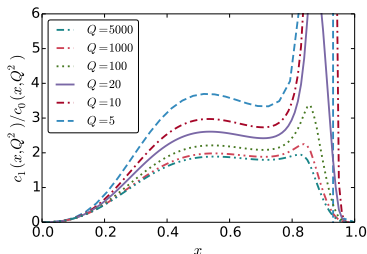
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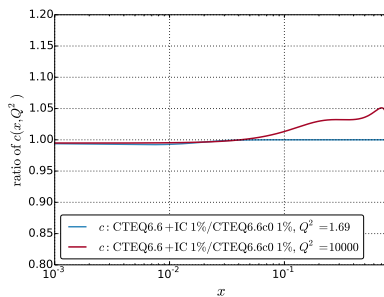
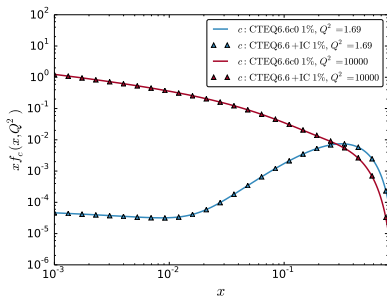
## $c_1(x)$ , $b_1(x)$ @NLO

- Modifications in **BHPS** models are essentially at **large- $x$**
- IB effects less **pronounced**:
  - ▶ Still, observables dominated by  $b$  initiated processes could be enhanced by a factor up to  $\sim 1.6$
  - ▶ For constraining intrinsic bottom  $\Rightarrow$  low  $Q$  and high- $x$  e.g. AFTER@LHC



## Goodness of the approximation

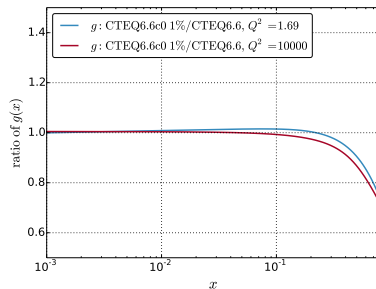
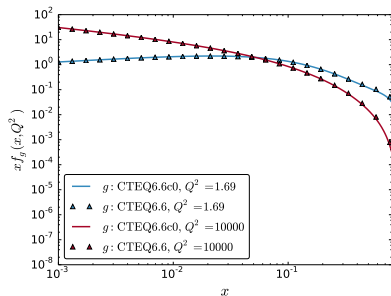
- Comparison of  $c_1(x) + \text{CTEQ6.6}$  and  $c(x)$  of  $\text{CTEQ6.6c0}$  with the **same normalization**
  - ▶  $\int_0^1 dx c(x) = 0.01$
  - ▶  $\int_0^1 dx x [c(x) + \bar{c}(x)] = 0.0057$
- **Charm-quark** with 1% normalization



- The error is under control and reaches at worst 5%.

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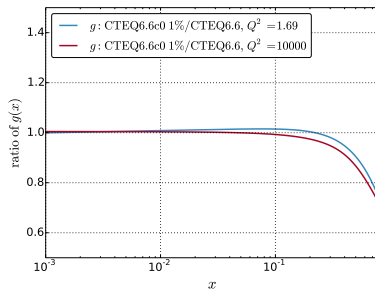
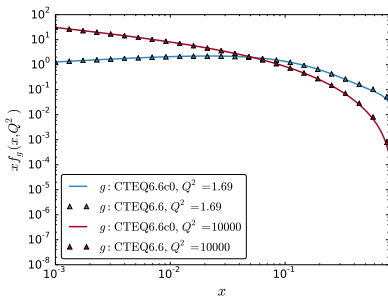
- Comparison of  $g(x)$  of CTEQ6.6 and  $g(x)$  of CTEQ6.6c0 with 1% normalization



- The error is larger at high  $x$  but the gluon is very small and the uncertainties large in this region.

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- Comparison of  $g(x)$  of CTEQ6.6 and  $g(x)$  of CTEQ6.6c0 with 1% normalization



- Also looked at how this affect luminosities
- For **IB** the errors will be 10 times smaller !

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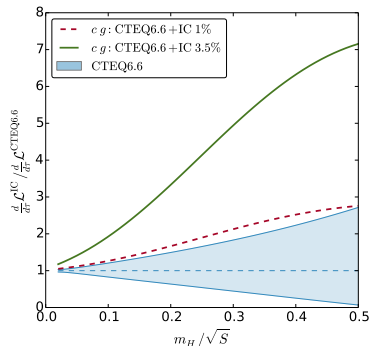
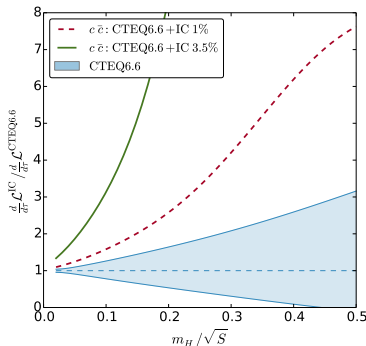
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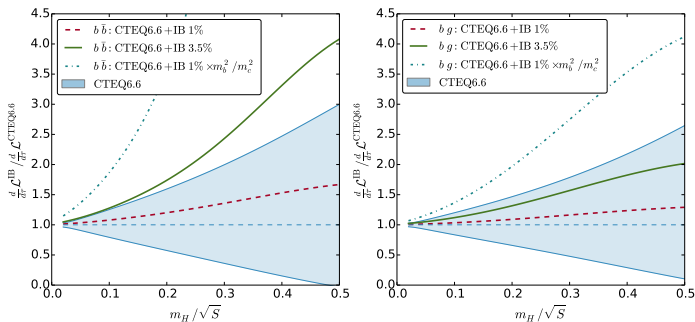


■  $\sqrt{\tau} = m_H/\sqrt{S}$



- The impact of the intrinsic charm is clearly visible and outside the uncertainty band from PDF for both  $c\bar{c}$  and  $cg$ .





- Also include an *extreme* scenario with the **first moment** of IB at 1%.
- Effects smaller than for IC as expected
- 3.5% normalization is distinguishable

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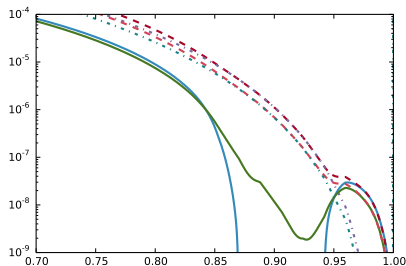
V) Conclusion

- Intrinsic heavy quarks can be decoupled  $\Rightarrow$  **non-singlet** evolution
  - ▶ Can generate matched **IC/IB** distributions for any PDF set **without** re-doing a global analysis  $\Rightarrow$  Produced **IB** set!
  - ▶ The normalization can be chosen **freely**
- The Approximation holds to a **very good** level for all relevant applications:
  - ▶ For **IB**, it is very good
  - ▶ For **IC**:
    - (i) 1-2% normalization  $\Rightarrow$  error smaller than **PDF uncertainty** at large- $x$
    - (ii) For **larger norms**, the error **grows** but the effect also such that it can easily be separated from the *without IC case*.
- Need a low  $Q$  large- $x$  machine to constrain IB
  - ▶ Electron Ion Collider (EIC)
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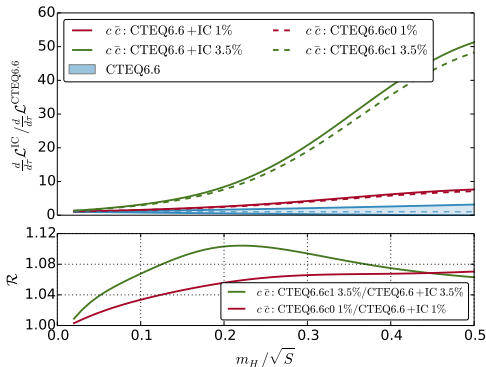
- the  $c$  PDF of CTEQ66.c0 goes negative at large- $x$  small  $Q$



## Definition

$$\blacksquare \frac{d\mathcal{L}_{ij}}{d\tau}(\tau, \mu) = \frac{1}{1+\delta_{ij}} \int_{\tau}^1 \frac{dx}{x} \left[ f_i(x, \mu) f_j(\tau/x, \mu) + (i \leftrightarrow j) \right]$$

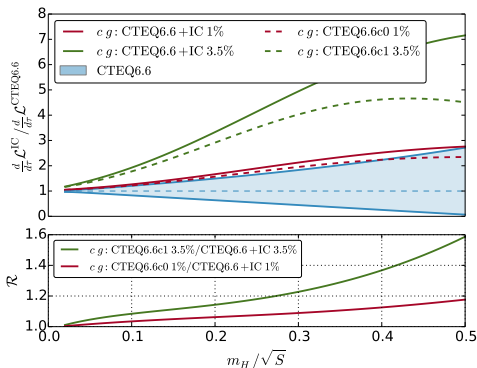
- Validity of the approximation on the Luminosities:



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### Validit



$\blacksquare$  Note that for the intrinsic bottom the error is **smaller**