

# Revealing transversity GPDs through the production of a rho meson and a photon

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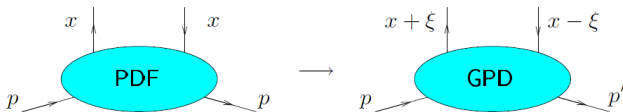
# Transversity of the nucleon using hard processes

## What is transversity?

- Transverse spin content of the proton:

$$\begin{array}{lcl}
 |\uparrow\rangle(x) & \sim & |\rightarrow\rangle + |\leftarrow\rangle \\
 |\downarrow\rangle(x) & \sim & |\rightarrow\rangle - |\leftarrow\rangle \\
 \text{spin along } x & & \text{helicity states}
 \end{array}$$

- Observables which are sensitive to helicity flip thus give access to transversity  $\Delta_T q(x)$ . Poorly known.
- Transversity GPDs are completely unknown experimentally.

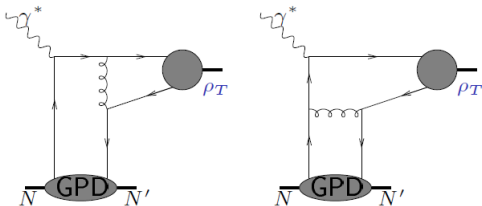


- For massless (anti)particles, chirality = (-)helicity
- Transversity is thus a chiral-odd quantity
- Since (in the massless limit) QCD and QED are chiral even ( $\gamma^\mu, \gamma^\mu \gamma^5$ ), the chiral odd quantities ( $1, \gamma^5, [\gamma^\mu, \gamma^\nu]$ ) which one wants to measure should appear in pairs

# Transversity of the nucleon using hard processes: using a two body final state process?

## How to get access to transversity GPDs?

- the dominant DA of  $\rho_T$  is of twist 2 and chiral odd ( $[\gamma^\mu, \gamma^\nu]$  coupling)
- unfortunately  $\gamma^* N^\uparrow \rightarrow \rho_T N' = 0$ 
  - This cancellation is true at any order : such a process would require a helicity transfer of 2 from a photon.
  - lowest order diagrammatic argument:



$$\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha \rightarrow 0$$

[Diehl, Gousset, Pire], [Collins, Diehl]

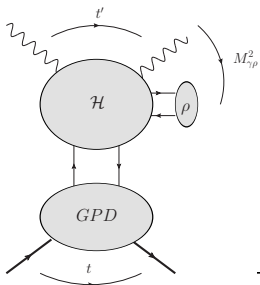
# Transversity of the nucleon using hard processes: using a two body final state process?

Can one circumvent this vanishing?

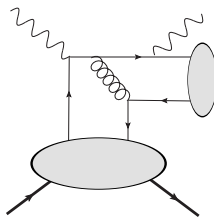
- This vanishing only occurs at [twist 2](#)
- At twist 3 this process does not vanish [[Ahmad, Goldstein, Liuti](#)], [[Goloskokov, Kroll](#)]
- However processes involving [twist 3 DAs](#) may face problems with factorization (end-point singularities)
- One can also consider a 3-body final state process [[Ivanov, Pire, Szymanowski, Teryaev](#)], [[Enberg, Pire, Szymanowski](#)], [[El Beiyad, Pire, Segond, Szymanowski, Wallon](#)]

# Probing transversity using $\rho$ meson + photon production

- Processes with **3 body final states** can give access to **all GPDs**
- We consider the process  $\gamma N \rightarrow \gamma \rho N'$
- Collinear factorization of the amplitude for  $\gamma + N \rightarrow \gamma + \rho + N'$  at large  $M_{\gamma\rho}^2$



Factorized amplitude

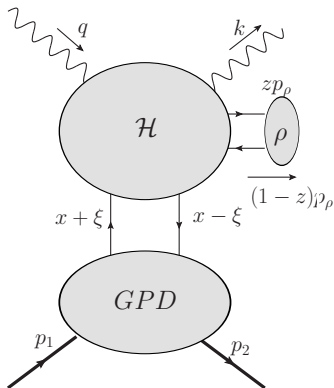


Typical non-zero diagram for a **transverse**  $\rho$  meson

# Master formula based on leading twist 2 factorization

$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) \times H(x, \xi, t) \Phi_\rho(z) + \dots$$

- Both the DA and the GPD can be either **chiral even** or **chiral odd**.
- At twist 2 the **longitudinal  $\rho$  DA** is **chiral even** and the **transverse  $\rho$  DA** is **chiral odd**.
- Hence we will need both **chiral even** and **chiral odd** non-perturbative building blocks and hard parts.



Non perturbative **chiral odd** building blocks

- Helicity flip GPD at twist 2 :

$$\begin{aligned}
 & \int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) i\sigma^{+i} \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle \\
 = & \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H_T^q(x, \xi, t) i\sigma^{+i} + \tilde{H}_T^q(x, \xi, t) \frac{P^+ \Delta^i - \Delta^+ P^i}{M_N^2} \right. \\
 + & \left. E_T^q(x, \xi, t) \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2M_N} + \tilde{E}_T^q(x, \xi, t) \frac{\gamma^+ P^i - P^+ \gamma^i}{M_N} \right] u(p_1, \lambda_1)
 \end{aligned}$$

- We will consider the simplest case when  $\Delta_\perp = 0$ .
- In that case and in the forward limit  $\xi \rightarrow 0$  only the  $H_T^q$  term survives.
- Transverse  $\rho$  DA at twist 2 :

$$\langle 0 | \bar{u}(0) \sigma^{\mu\nu} u(x) | \rho^0(p, s) \rangle = \frac{i}{\sqrt{2}} (\epsilon_\rho^\mu p^\nu - \epsilon_\rho^\nu p^\mu) f_\rho^\perp \int_0^1 du e^{-iup \cdot x} \phi_\perp(u)$$

Non perturbative **chiral even** building blocks

- Helicity conserving GPDs at twist 2 :

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) \frac{i\sigma^{\alpha+} \Delta_\alpha}{2m} \right]$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left( -\frac{1}{2}z^- \right) \gamma^+ \gamma^5 \psi \left( \frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[ \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \frac{\gamma^5 \Delta^+}{2m} \right]$$

- Helicity conserving (vector) DA at twist 2 :

$$\langle 0 | \bar{u}(0) \gamma^\mu u(x) | \rho^0(p, s) \rangle = \frac{p^\mu}{\sqrt{2}} \frac{\epsilon \cdot x}{p \cdot x} f_\rho m_\rho \int_0^1 du e^{-iup \cdot x} \phi_\parallel(u)$$



## Kinematics

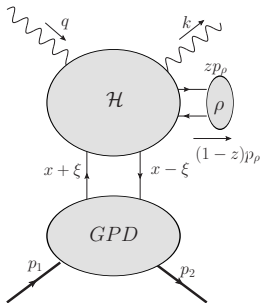
## Kinematics to handle GPD in a 3-body final state process

- use a **Sudakov** basis :  
light-cone vectors  $p$ ,  $n$  with  $2p \cdot n = s$
- assume the following kinematics:
  - $\Delta_{\perp} \sim 0$
  - $M^2, m_{\pi}^2, m_{\rho}^2 \ll M_{\pi\rho}^2$

- initial state particle momenta:

$$q^{\mu} = n^{\mu}, \quad p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{M^2}{s(1 + \xi)} n^{\mu}$$

- final state particle momenta:



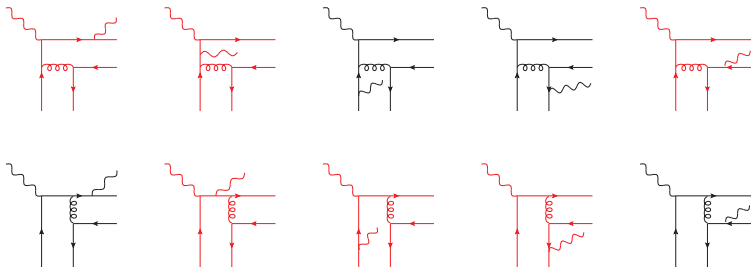
$$p_2^{\mu} = (1 - \xi) p^{\mu} + \frac{M^2}{s(1 - \xi)} n^{\mu}$$

$$k^{\mu} = \alpha n^{\mu} + \frac{\vec{k}_t^2}{\alpha s} p^{\mu} + k_{\perp}^{\mu}$$

$$p_{\rho}^{\mu} = \alpha_{\rho} n^{\mu} + \frac{\vec{p}_t^2 + m_{\rho}^2}{\alpha_{\rho} s} p^{\mu} - k_{\perp}^{\mu}$$

# Computation of the hard part

20 diagrams to compute



The other half can be deduced by  $q \leftrightarrow \bar{q}$  (anti)symmetry  
Red diagrams cancel in the chiral odd case

## Chiral odd amplitude

## The chiral odd case

The  $z$  and  $x$  dependence of the amplitude can be factorized

$$\mathcal{A} = \mathcal{N}(z, x) T^i$$

$$\begin{aligned} T^i &= (1 - \alpha) [(\epsilon_{q\perp} \cdot k_{\perp}) (\epsilon_{k\perp} \cdot \epsilon_{\rho\perp}) - (\epsilon_{k\perp} \cdot k_{\perp}) (\epsilon_{q\perp} \cdot \epsilon_{\rho\perp})] k_{\perp}^i \\ &- (1 + \alpha) (\epsilon_{\rho\perp} \cdot k_{\perp}) (\epsilon_{k\perp} \cdot \epsilon_{q\perp}) k_{\perp}^i + \alpha (\alpha^2 - 1) \xi s (\epsilon_{q\perp} \cdot \epsilon_{k\perp}) \epsilon_{\rho}^i \\ &- \alpha (\alpha^2 - 1) \xi s [(\epsilon_{q\perp} \cdot \epsilon_{\rho\perp}) \epsilon_{k\perp}^i - (\epsilon_{k\perp} \cdot \epsilon_{\rho\perp}) \epsilon_{q\perp}^i] \end{aligned}$$

Hence calculating differential cross sections is simple :

$$d\sigma \propto \left| \int_0^1 dz \int_{-1}^1 dx \mathcal{N}(z, x) \phi_{\rho}(z) H_T^q(x) \right|^2 \sum_{\text{helicities}, (i, j)} T^i T^j$$

# The chiral even case

## The chiral even case

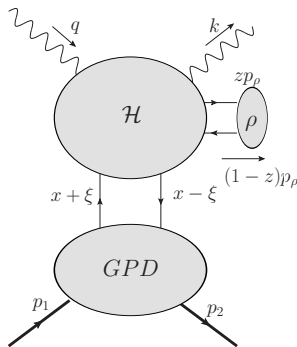
- All 20 (10) diagrams are computed, both with **vector** and **axial** coupling
- The  $z$  and  $x$  dependences do not factorize but they are known.

## Final computation

## Final computation

$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) \times H(x, \xi, t) \Phi_\rho(z) + \dots$$

- One performs the  $z$  integration **analytically** using an asymptotic DA  $\propto z(1-z)$
- One then plugs a GPD model into the formula and performs the integral wrt  $x$  numerically.



# A model based on Double Distribution

## Realistic Parametrization of GPDs

- GPDs can be represented in terms of **Double Distribution** [Radyushkin] based on **Schwinger** representation of a toy model for GPDs which has the structure of a triangle diagram in scalar  $\phi^3$  theory

$$H^q(x, \xi, t = 0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) f^q(\beta, \alpha)$$

- ansatz for these Double Distribution [Radyushkin]:
  - $f^q(\beta, \alpha) = \Pi(\beta, \alpha) q(\beta)$  in the chiral even case
  - $f_T^q(\beta, \alpha) = \Pi(\beta, \alpha) \Delta_T q(\beta)$  in the chiral odd case
  - $q(x)$  : PDF [MSTW, GRV...],  $\Delta_T q(x)$  : Chiral odd PDF [Anselmino *et al.*]
  - $\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$  : profile function

# Conclusion

- This calculation is still being done but predictions for **cross sections** and **counting rates** will be ready very soon.
- Our result will also be applied to **electroproduction** ( $Q^2 \neq 0$ ) after adding **Bethe-Heitler** contributions and interferences.
- This mechanism will give us access to **transversity GPDs** but also to the **usual GPDs** by analogy with **Timelike Compton Scattering**, the  $\gamma\rho$  pair playing the role of the  $\gamma^*$ .
- Possible measurement in **JLAB** and in **COMPASS**