

GPDs in heavy mesons production and Compton scattering

Jakub Wagner

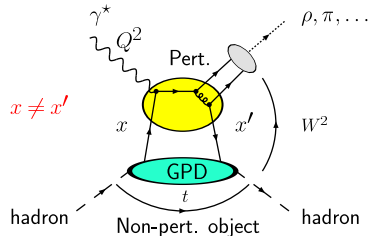
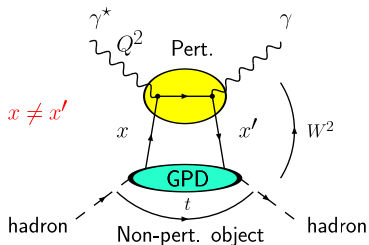
Theoretical Physics Department
National Center for Nuclear Research
Warsaw, Poland

POETIC6, Palaiseau

timelike-DVCS: B.Pire, L.Szymanowski, H.Moutarde, F.Sabatié

J/Ψ photoproduction: D.Ivanov, L.Szymanowski

Processes



- ▶ Universality of GPDs,
- ▶ Meson production - additional difficulties,

So, in addition to spacelike DVCS ...

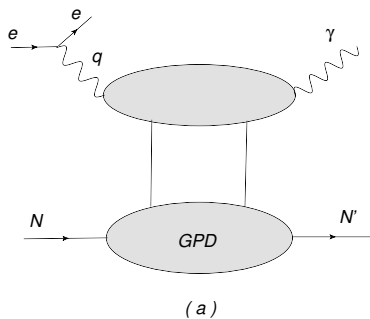


Figure : Deeply Virtual Compton Scattering (DVCS) : $lN \rightarrow l'N'\gamma$

we can also study **timelike DVCS (TCS)**

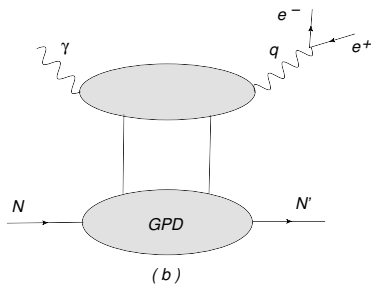


Figure : Timelike Compton Scattering (**TCS**): $\gamma N \rightarrow l^+ l^- N'$

Why **TCS**:

- ▶ universality of the GPDs,
- ▶ another source for GPDs (special sensitivity on real part of GPD H),
- ▶ spacelike-timelike crossing,
- ▶ more in M.Boer talk on Friday morning.

General Compton Scattering:

$$\gamma^*(q_{in})N(p) \rightarrow \gamma^*(q_{out})N'(p')$$

variables, describing the processes of interest in this generalized Bjorken limit, are the **scaling variable** ξ and **skewness** $\eta > 0$:

$$\xi = -\frac{q_{out}^2 + q_{in}^2}{q_{out}^2 - q_{in}^2}\eta, \quad \eta = \frac{q_{out}^2 - q_{in}^2}{(p + p') \cdot (q_{in} + q_{out})}.$$

- ▶ DDVCS: $q_{in}^2 < 0$, $q_{out}^2 > 0$, $\eta \neq \xi$
- ▶ DVCS: $q_{in}^2 < 0$, $q_{out}^2 = 0$, $\eta = \xi > 0$
- ▶ TCS: $q_{in}^2 = 0$, $q_{out}^2 > 0$, $\eta = -\xi > 0$

Coefficient functions and Compton Form Factors

CFFs are the GPD dependent quantities which enter the amplitudes. They are defined through relations:

$$\mathcal{A}^{\mu\nu}(\xi, \eta, t) = -e^2 \frac{1}{(P+P')^+} \bar{u}(P') \left[g_T^{\mu\nu} \left(\mathcal{H}(\xi, \eta, t) \gamma^+ + \mathcal{E}(\xi, \eta, t) \frac{i\sigma^{+\rho} \Delta_\rho}{2M} \right) + i\epsilon_T^{\mu\nu} \left(\tilde{\mathcal{H}}(\xi, \eta, t) \gamma^+ \gamma_5 + \tilde{\mathcal{E}}(\xi, \eta, t) \frac{\Delta^+ \gamma_5}{2M} \right) \right] u(P),$$

,where:

$$\begin{aligned} \mathcal{H}(\xi, \eta, t) &= + \int_{-1}^1 dx \left(\sum_q T^q(x, \xi, \eta) H^q(x, \eta, t) + T^g(x, \xi, \eta) H^g(x, \eta, t) \right) \\ \tilde{\mathcal{H}}(\xi, \eta, t) &= - \int_{-1}^1 dx \left(\sum_q \tilde{T}^q(x, \xi, \eta) \tilde{H}^q(x, \eta, t) + \tilde{T}^g(x, \xi, \eta) \tilde{H}^g(x, \eta, t) \right). \end{aligned}$$

▶ DVCS vs TCS

$$\begin{aligned}
 DVCS T^q &= -e_q^2 \frac{1}{x+\eta-i\varepsilon} - (x \rightarrow -x) = (TCS T^q)^* \\
 DVCS \tilde{T}^q &= -e_q^2 \frac{1}{x+\eta-i\varepsilon} + (x \rightarrow -x) = -(TCS \tilde{T}^q)^*
 \end{aligned}$$

$$DVCS \operatorname{Re}(\mathcal{H}) \sim P \int \frac{1}{x \pm \eta} H^q(x, \eta, t), \quad DVCS \operatorname{Im}(\mathcal{H}) \sim i\pi H^q(\pm\eta, \eta, t)$$

▶ DDVCS

$$DDVCS T^q = -e_q^2 \frac{1}{x+\xi-i\varepsilon} - (x \rightarrow -x)$$

$$DDVCS \operatorname{Re}(\mathcal{H}) \sim P \int \frac{1}{x \pm \xi} H^q(x, \eta, t), \quad DVCS \operatorname{Im}(\mathcal{H}) \sim i\pi H^q(\pm\xi, \eta, t)$$

But this is only true at LO. At NLO all GPDs hidden in the convolutions.

Coefficient functions

Renormalized coefficient functions for DVCS are given by

$$T^q(x) = \left[C_0^q(x) + C_1^q(x) + \ln\left(\frac{Q^2}{\mu_F^2}\right) \cdot C_{coll}^q(x) \right] - (x \rightarrow -x),$$

$$T^g(x) = \left[C_1^g(x) + \ln\left(\frac{Q^2}{\mu_F^2}\right) \cdot C_{coll}^g(x) \right] + (x \rightarrow -x),$$

$$\tilde{T}^q(x) = \left[\tilde{C}_0^q(x) + \tilde{C}_1^q(x) + \ln\left(\frac{Q^2}{\mu_F^2}\right) \cdot \tilde{C}_{coll}^q(x) \right] + (x \rightarrow -x),$$

$$\tilde{T}^g(x) = \left[\tilde{C}_1^g(x) + \ln\left(\frac{Q^2}{\mu_F^2}\right) \cdot \tilde{C}_{coll}^g(x) \right] - (x \rightarrow -x).$$

The results for DVCS and TCS cases are simply related:

$${}^{TCS}T(x, \eta) = \pm \left({}^{DVCS}T(x, \xi = \eta) + i\pi \cdot C_{coll}(x, \xi = \eta) \right)^*,$$

D.Mueller, B.Pire, L.Szymanowski, J.Wagner, Phys.Rev.D86, 2012.

where + (−) sign corresponds to vector (axial) case.

Compton Form Factors - DVCS - $Re(\mathcal{H})$

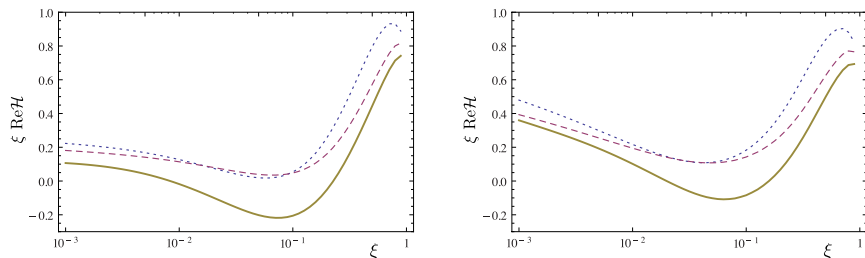


Figure : The **real** part of the **spacelike** Compton Form Factor $\mathcal{H}(\xi)$ multiplied by ξ , as a function of ξ in the double distribution model based on **Kroll-Goloskokov** (upper left) and **MSTW08** (upper right) parametrizations, for $\mu_F^2 = Q^2 = 4 \text{ GeV}^2$ and $t = -0.1 \text{ GeV}^2$, at the Born order (dotted line), including the NLO quark corrections (dashed line) and including both quark and gluon NLO corrections (solid line).

Compton Form Factors - DVCS - $Im(\mathcal{H})$

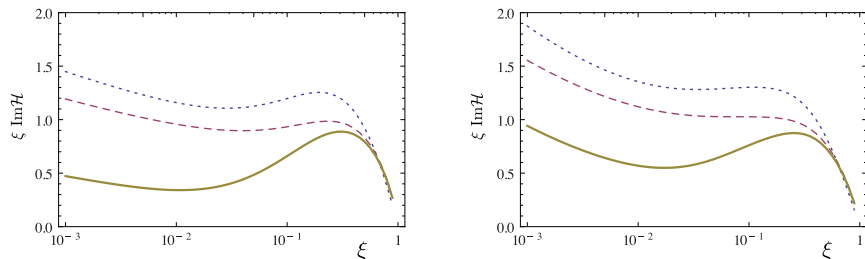


Figure : The **imaginary** part of the **spacelike** Compton Form Factor $\mathcal{H}(\xi)$ multiplied by ξ , as a function of ξ in the double distribution model based on **Kroll-Goloskokov** (upper left) and **MSTW08** (upper right) parametrizations, for $\mu_F^2 = Q^2 = 4 \text{ GeV}^2$ and $t = -0.1 \text{ GeV}^2$, at the Born order (dotted line), including the NLO quark corrections (dashed line) and including both quark and gluon NLO corrections (solid line).

Compton Form Factors - TCS - $Re(\mathcal{H})$

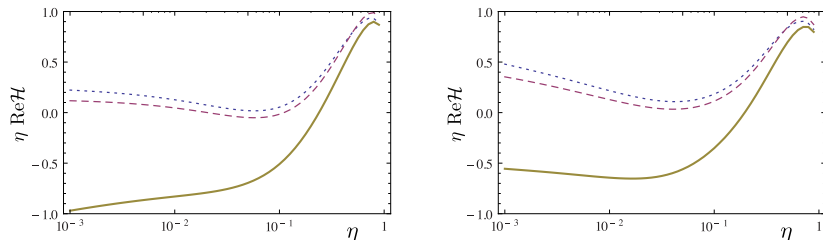


Figure : The **real** part of the **timelike** Compton Form Factor \mathcal{H} multiplied by η , as a function of η in the double distribution model based on **Kroll-Goloskokov** (upper left) and **MSTW08** (upper right) parametrizations, for $\mu_F^2 = Q^2 = 4 \text{ GeV}^2$ and $t = -0.1 \text{ GeV}^2$. Below the ratios of the NLO correction to LO result of the corresponding models.

Compton Form Factors - TCS - $Im(\mathcal{H})$

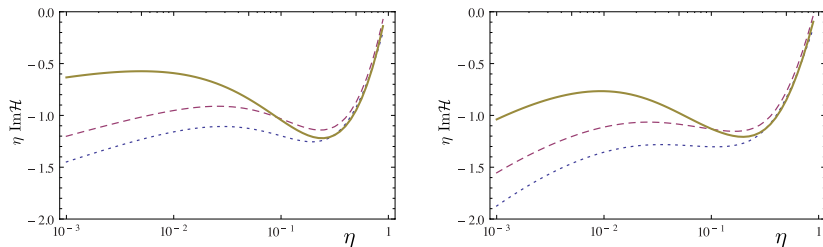


Figure : The **imaginary** part of the **timelike** Compton Form Factor \mathcal{H} multiplied by η , as a function of η in the double distribution model based on **Kroll-Goloskokov** (upper left) and **MSTW08** (upper right) parametrizations, for $\mu_F^2 = Q^2 = 4 \text{ GeV}^2$ and $t = -0.1 \text{ GeV}^2$. Below the ratios of the NLO correction to LO result of the corresponding models.

Few words about factorization scale

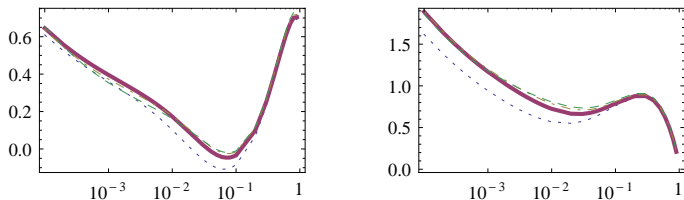


Figure : Full NLO result. Left column - $\xi \cdot \text{Re}(\mathcal{H}(\xi))$, right column - $\xi \cdot \text{Im}(\mathcal{H}(\xi))$,
 $Q^2 = 4\text{gev}^2$, $\mu_F^2 = Q^2, Q^2/2, Q^2/3$

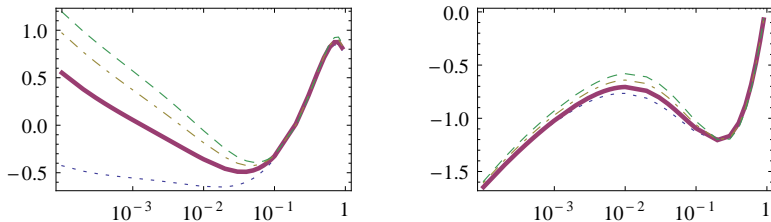
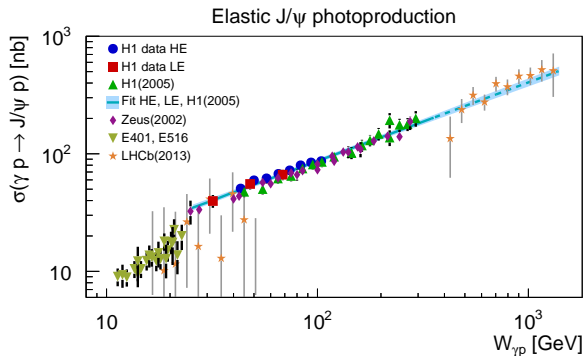


Figure : Full NLO result. Left column - $\xi \cdot \text{Re}(\mathcal{H}(\xi))$, right column - $\xi \cdot \text{Im}(\mathcal{H}(\xi))$

Heavy Vector Mesons Photoproduction

We have good data! See H1 2013 paper:



Heavy Vector Mesons Photoproduction

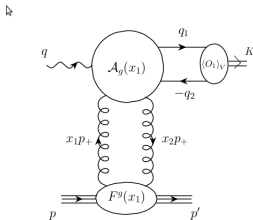


Figure 1: Kinematics of heavy vector meson photoproduction.

$$\mathcal{M} \sim \left(\frac{\langle O_1 \rangle_V}{m^3} \right)^{1/2} \int_{-1}^1 dx \left[T_g(x, \xi) F^g(x, \xi, t) + T_q(x, \xi) F^{q,S}(x, \xi, t) \right],$$

$$F^{q,S}(x, \xi, t) = \sum_{q=u,d,s} F^q(x, \xi, t).$$

$F^{g(q)}(x, \xi, t; \mu_F^2)$ – the gluon (quark) GPDs, m is a pole mass of heavy quark, $\xi = M^2/(2W^2 - M^2)$ is the skewedness parameter.

NRQCD – all information about the quarkonium structure is encoded in the NRQCD matrix element $\langle O_1 \rangle_V$ which enters the leptonic decay rate

$$\Gamma[V \rightarrow l^+ l^-] = \frac{2e_q^2 \pi \alpha^2}{3} \frac{\langle O_1 \rangle_V}{m^2} \left(1 - \frac{8\alpha_S}{3\pi} \right)^2.$$

Hard scattering kernels:

$$T_g(x, \xi) = \frac{\xi}{(x - \xi + i\varepsilon)(x + \xi - i\varepsilon)} \mathcal{A}_g \left(\frac{x - \xi + i\varepsilon}{2\xi} \right),$$
$$T_q(x, \xi) = \mathcal{A}_q \left(\frac{x - \xi + i\varepsilon}{2\xi} \right).$$

► LO

$$\mathcal{A}_g^{(0)}(y) = \alpha_S \quad \mathcal{A}_q^{(0)}(y) = 0.$$

► NLO

D. Yu. Ivanov , A. Schafer , L. Szymanowski and G. Krasnikov - **Eur.Phys.J. C34 (2004)**
297-316

$$T_q(x, \xi) = \frac{\alpha_S^2(\mu_R) C_F}{2\pi} f_q \left(\frac{x - \xi + i\varepsilon}{2\xi} \right),$$

$$f_q(y) = \ln \left(\frac{4m^2}{\mu_F^2} \right) (1 + 2y) \left(\frac{\ln(-y)}{1 + y} - \frac{\ln(1 + y)}{y} \right) - \pi^2 \frac{13(1 + 2y)}{48y(1 + y)} + \frac{2 \ln 2}{1 + 2y}$$
$$+ \frac{\ln(-y) + \ln(1 + y)}{1 + 2y} + (1 + 2y) \left(\frac{\ln^2(-y)}{1 + y} - \frac{\ln^2(1 + y)}{y} \right)$$
$$+ \frac{3 - 4y + 16y(1 + y)}{4y(1 + y)} Li_2(1 + 2y) - \frac{7 + 4y + 16y(1 + y)}{4y(1 + y)} Li_2(-1 - 2y)$$

Photoproduction amplitude and cross section - LO

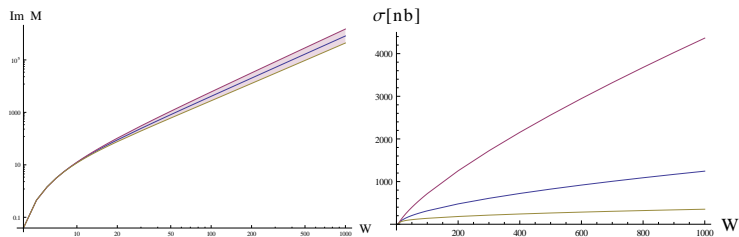


Figure : (left) Imaginary part of the amplitude \mathcal{M} and (right) photoproduction cross section as a function of $W = \sqrt{s_{\gamma p}}$ for $\mu_F^2 = M_{J/\psi}^2 \times \{0.5, 1, 2\}$.

Photoproduction cross section - LO and NLO

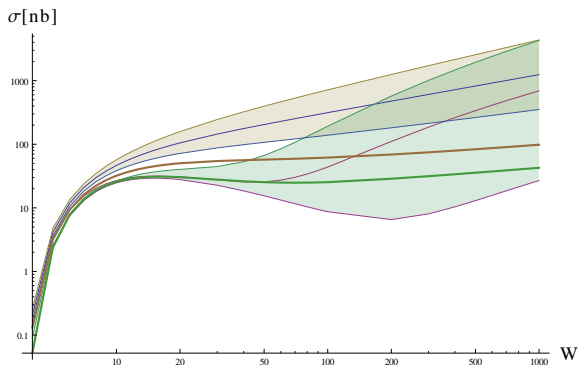
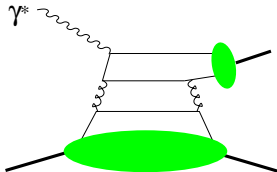
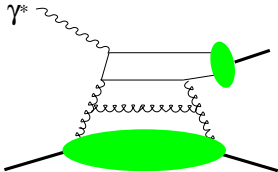


Figure : Photoproduction cross section as a function of $W = \sqrt{s_{\gamma p}}$ for $\mu_F^2 = M_{J/\psi}^2 \times \{0.5, 1, 2\}$ - LO and NLO. Thick lines for LO and NLO for $\mu_F^2 = 1/4 M_{J/\psi}^2$.

- ▶ Jones & Martin & Ryskin & Teubner, arXiv:1507.06942. Choice of the factorization scale.
- ▶ Why NLO corrections are large at small x_B ?
large contribution comes from

$$ImA^g \sim H^g(\xi, \xi) + \frac{3\alpha_s}{\pi} \left[\log \frac{M_V^2}{\mu_F^2} - \log 4 \right] \int_{\xi}^1 \frac{dx}{x} H^g(x, \xi)$$

$H^g(x, \xi) \sim xg(x) \sim const$, therefore $\int dx/x H^g(x, \xi) \sim \log(1/\xi) H^g(\xi, \xi)$



At higher orders powers of energy log are generated

$$\mathcal{I}m A^g \sim H^g(\xi, \xi) + \int_{\xi}^1 \frac{dx}{x} H^g(x, \xi) \sum_{n=1} C_n(L) \frac{\bar{\alpha}_s^n}{(n-1)!} \log^{n-1} \frac{x}{\xi}$$

$C_n(L)$ - polynomials of $L = \log \frac{Q^2}{\mu_F^2}$, maximum power is L^n

- ▶ for DIS a technique suggested by Catani, Ciafaloni and Hautmann; [Catani, Hautmann '94]
- ▶ One can calculate $C_n(L)$ in $D = 4 + 2\epsilon$ dimensions.
- ▶ Consistently with collinear factorization, in terms of corrections to coeff. functions and anomalous dimensions, in \overline{MS} scheme
- ▶ The method used in DIS can be generalized to exclusive, nonforward processes.

Coeff. functions at small x / their Mellin moments at $N \rightarrow 0$

$$L = \log \left(\frac{Q^2}{\mu_F^2} \right), \quad x = \frac{\bar{\alpha}_s}{N}$$

Result for $J/\Psi, \Upsilon$

$$1 + x(L - \log 4) + \frac{x^2}{6} (\pi^2 + 3 \log^2 4 + 3L(L - \log 16)) + \dots + \mathcal{O}(x^{10})$$

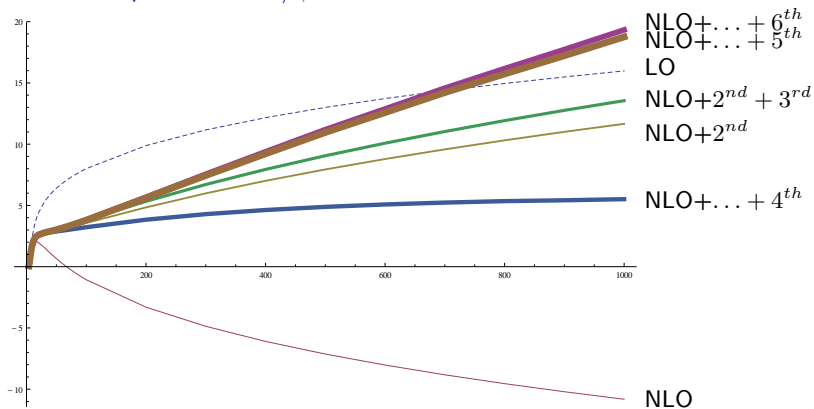
F_L - [Catani, Hautmann '94]

$$\mu_F^2 = Q^2$$

$$F_L: \quad 1 - \frac{1}{3} x + 2.13 x^2 + 2.27 x^3 + 0.434 x^4 + \dots$$

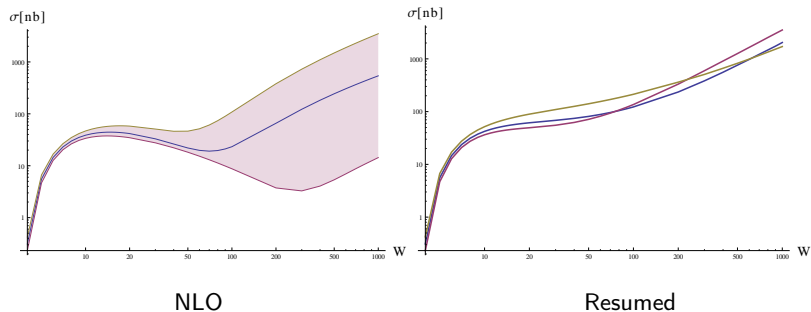
$$J/\Psi, \Upsilon: \quad 1 - 1.39 x + 2.61 x^2 + 0.481 x^3 - 4.96 x^4 + \dots$$

Resummed amplitude for J/ψ



Imaginary part of the amplitude for photoproduction of heavy mesons as a function of $W = \sqrt{s_{\gamma p}}$ for $\mu_F^2 = M_{J/\psi}^2$

Resummed cross section for J/ψ

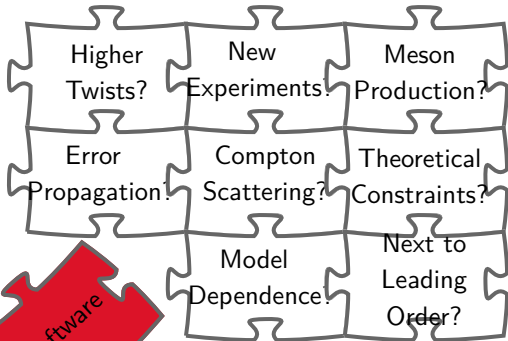


Photoproduction cross section as a function of $W = \sqrt{s_{\gamma p}}$ for
 $\mu_F^2 = M_{J/\psi}^2 \times \{0.5, 1, 2\}$

Summary

- ▶ GDPs enter factorization theorems for hard exclusive reactions in a similar manner as PDFs enter factorization theorem for DIS
- ▶ DVCS is a golden channel, a lot of new DVCS experiments planned - JLAB 12, COMPASS, EIC(?)
- ▶ GPDs in other exclusive processes - TCS, DVMP, photoproduction of heavy mesons...
- ▶ TCS already measured at JLAB 6 GeV, but much richer and more interesting kinematical region available after upgrade to 12 GeV
- ▶ Ultraperipheral collisions at hadron colliders opens a new way to measure GPDs,
- ▶ NLO corrections are very important: large for TCS; dramatic for VM photoproduction.
- ▶ High energy resummation needed for VM photoproduction (in progress).

PARTONS Project



PARTONS Project



PARtonic
Tomography
Of
Nucleon
Software

PARTONS
Project

Computing chain

Example

Team

Experimental
data and
phenomenology

Full processes

Computation
of amplitudes

Small distance
contributions

First
principles and
fundamental
parameters

Large distance
contributions

PARTONS
Project

Computing chain

Example

Team

Experimental
data and
phenomenology

Full processes

Computation
of amplitudes

Small distance
contributions

First
principles and
fundamental
parameters

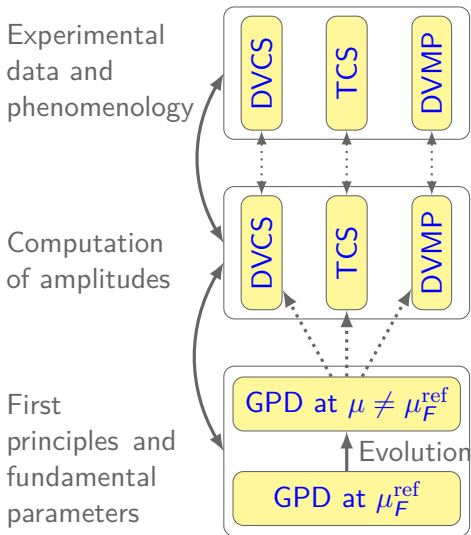
Large distance
contributions

PARTONS
Project

Computing chain

Example

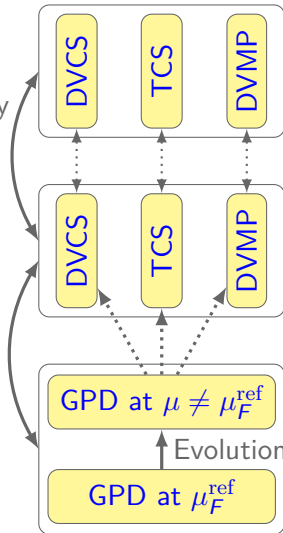
Team



Experimental
data and
phenomenology

Computation
of amplitudes

First
principles and
fundamental
parameters



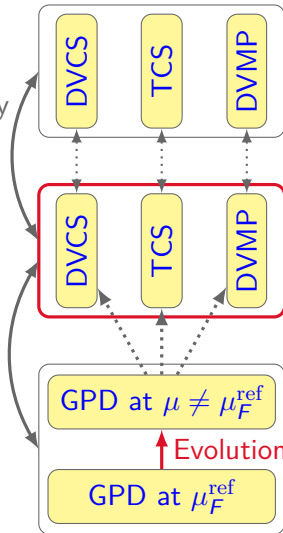
- Many observables.
- Kinematic reach.

Experimental
data and
phenomenology

Need for
modularity

Computation
of amplitudes

First
principles and
fundamental
parameters



- Many observables.
- Kinematic reach.

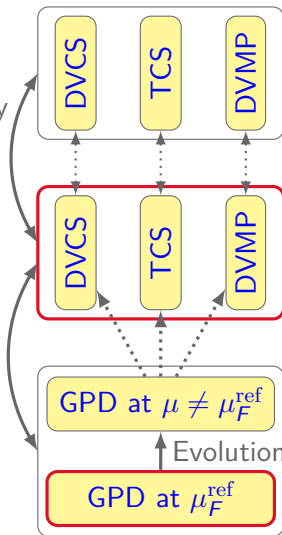
- **Perturbative approximations.**
- Physical models.
- Fits.
- Numerical methods.
- Accuracy and speed.

Experimental data and phenomenology

Need for modularity

Computation of amplitudes

First principles and fundamental parameters



- Many observables.
- Kinematic reach.

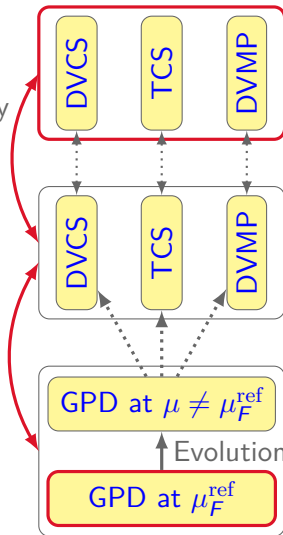
- Perturbative approximations.
- **Physical models.**
- Fits.
- Numerical methods.
- Accuracy and speed.

Experimental data and phenomenology

Need for modularity

Computation of amplitudes

First principles and fundamental parameters



- Many observables.
- Kinematic reach.

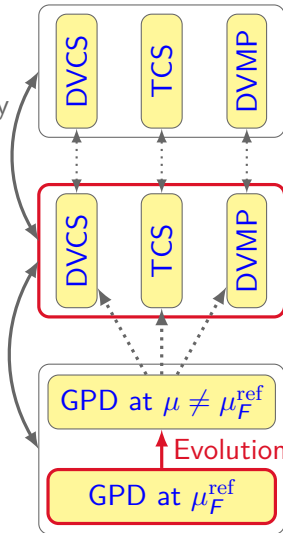
- Perturbative approximations.
- Physical models.
- Fits.
- Numerical methods.
- Accuracy and speed.

Experimental data and phenomenology

Need for modularity

Computation of amplitudes

First principles and fundamental parameters



- Many observables.
- Kinematic reach.

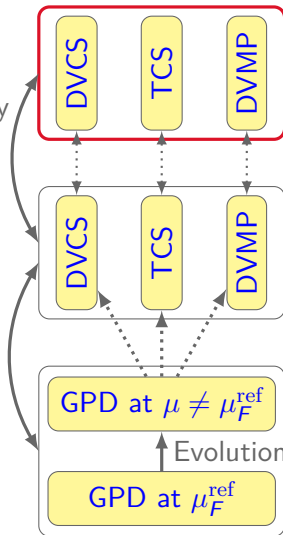
- Perturbative approximations.
- Physical models.
- Fits.
- Numerical methods.
- Accuracy and speed.

Experimental
data and
phenomenology

Need for
modularity

Computation
of amplitudes

First
principles and
fundamental
parameters



- Many observables.
- Kinematic reach.

- Perturbative approximations.
- Physical models.
- Fits.
- Numerical methods.
- Accuracy and speed.

PARTONS

Project

Computing chain

Example

Team

- 3 stages:
 - 1 Design.
 - 2 Integration and validation.
 - 3 Production.

- Flexible software architecture.

- 1 new physical development = 1 new module.

- What *can* be automated *will be* automated.

- Get ready for 12 GeV!

GPD computing made simple.

Each line of code corresponds to a physical hypothesis.

 gpdEvolutionExample()

```

1 // Load QCD evolution module
2 EvolQCDModule* pEvolQCDModule = pModuleObjectFactory->
3 getEvolQCDModule( VinnikovEvolQCDModel::moduleID );
4
5 // Configure QCD evolution module
6 pEvolQCDModule->setQcdOrderType( QCDOOrderType::LO );
7
8 // Load GPD module
9 GPDModule* pGK11Module =
10 pModuleObjectFactory->getGPDModule( GK11Model::moduleID );
11
12 // Create kinematic configuration ( x, xi, t, MuF, MuR )
13 GPDKinematic gpdKinematic( 0.25, 0.29, -0.28, 1.82, 1.82 );
14
15 // Compute GPD and store results
16 GPDOutputData results = pGPDSerivce->
17 computeGPDModelWithEvolution( gpdKinematic, pGK11Module,
18 pEvolQCDModule, GPDComputeType::H );
19
20 // Print results
21 std::cout << results.toString() << std::endl ;

```

PARTONS
Project

Computing chain

Example

Team

GPD computing made simple.

Each line of code corresponds to a physical hypothesis.

gpdEvolutionExample()

```

1 // Load QCD evolution module
2 EvolQCDModule* pEvolQCDModule = pModuleObjectFactory->getEvolQCDModule( VinnikovEvolQCDModel::n
3 getEvolQCDModule( VinnikovEvolQCDModel::n
4
5 // Configure QCD evolution module
6 pEvolQCDModule->setQcdOrderType( QCDO
7
8 // Load GPD module
9 GPDModule* pGK11Module =
10 pModuleObjectFactory->getGPDModule( GK1
11
12 // Create kinematic configuration ( x, xi, t, M
13 GPDKinematic gpdKinematic( 0.25, 0.29, -0.2
14
15 // Compute GPD and store results
16 GPDOutputData results = pGPDSerice->
17 computeGPDModelWithEvolution( gpdKinemat
18 pEvolQCDModule, GPDComputeType::H );
19
20 // Print results
21 std :: cout << results.toString() << std::endl ;

```

Preliminary

$$H_u = 1.5435$$

$$H_u(-) = 2.04736$$

$$H_u(+) = 1.03964$$

$$H_d = 0.524068$$

$$H_d(-) = 1.00457$$

$$H_d(+) = 0.0435651$$

$$H_s = -0.539675$$

$$H_s(-) = 0$$

$$H_s(+) = -1.07935$$

$$H_g = -0.3086$$

Development team



B. Berthou



C. Mezrag



H. Moutarde



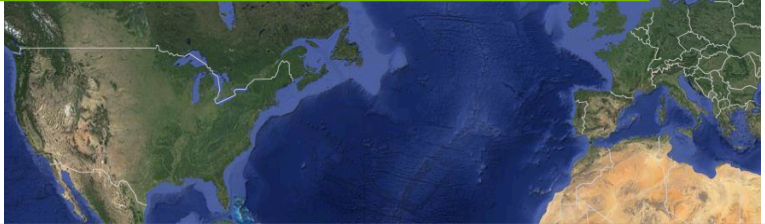
F. Sabatié



J. Wagner



P. Sznajder



IPN and LPT (Orsay), Irfu (Saclay) and CPhT (Polytechnique)



Experimental data analysis Perturbative QCD
World data fits GPD modeling