

# Frontiers of QCD with Precision nPDFs

*What lessons can we extract from the last 20 years?*

*What might the future bring?*

Fred Olness

SMU

Thanks to:

A. Kusina, I. Schienbein, F. Lyonnet, K. Kovarik, J.Y. Yu, T. Stavreva, T. Jezo,  
J.G. Morfin, J.F. Owens, P. Nadolsky, V. Radescu, C. Keppel, B. Clark, E. Godat

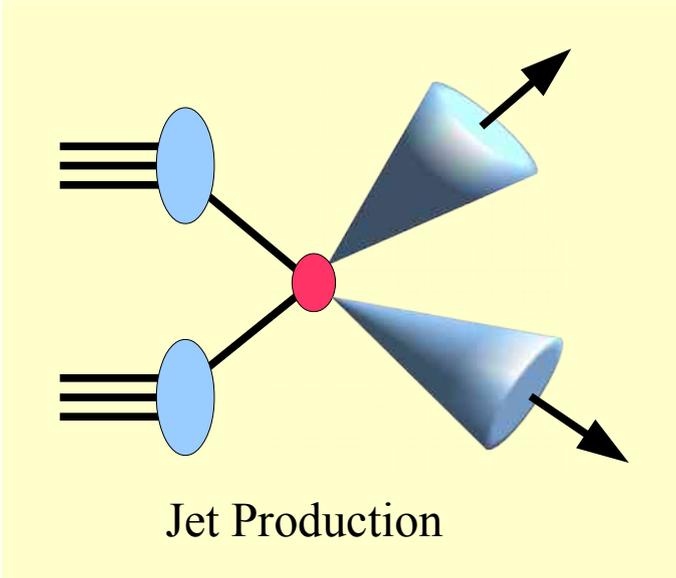
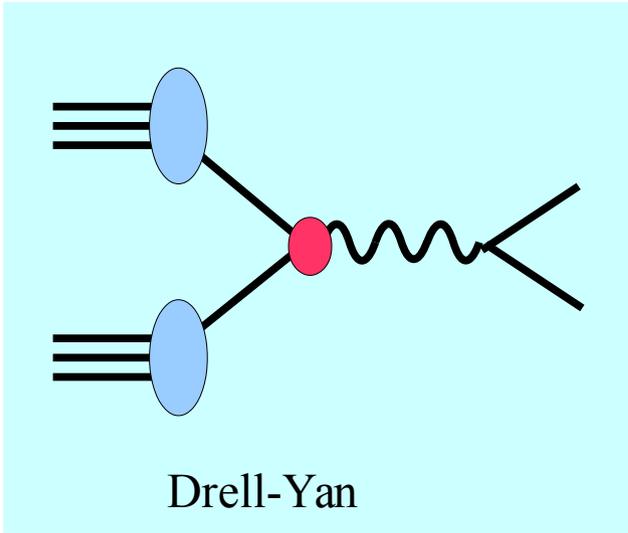
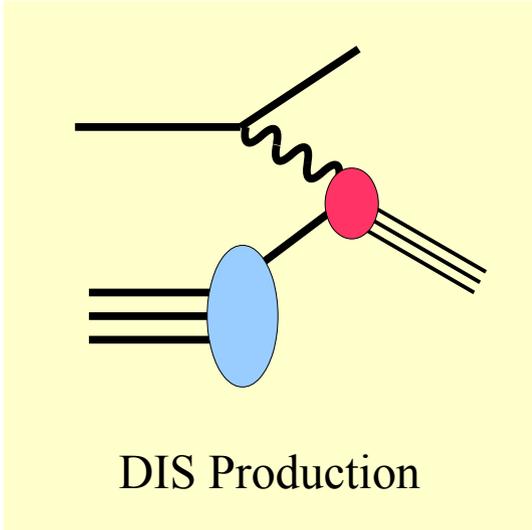
POETIC6  
9 September 2015

$$\sigma_{P \gamma \rightarrow c} = f_{P \rightarrow a} \otimes \hat{\sigma}_{a \gamma \rightarrow c}$$

Experimental Observables

**Parton Distribution Function (PDF)**

Theoretical Calculations

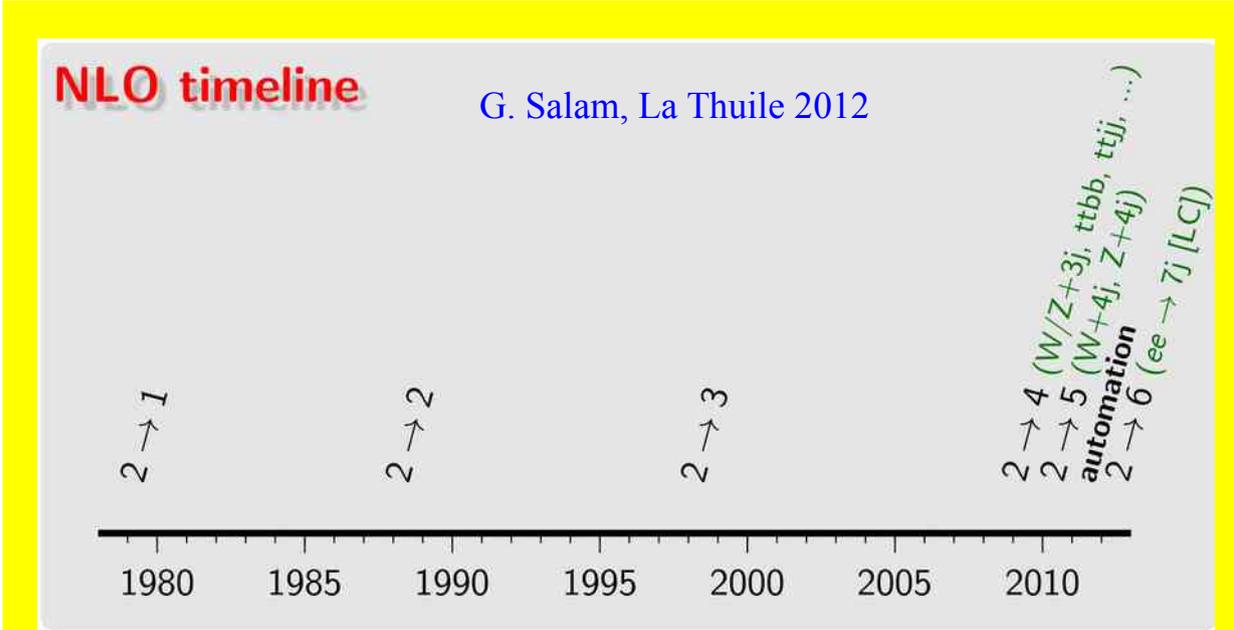
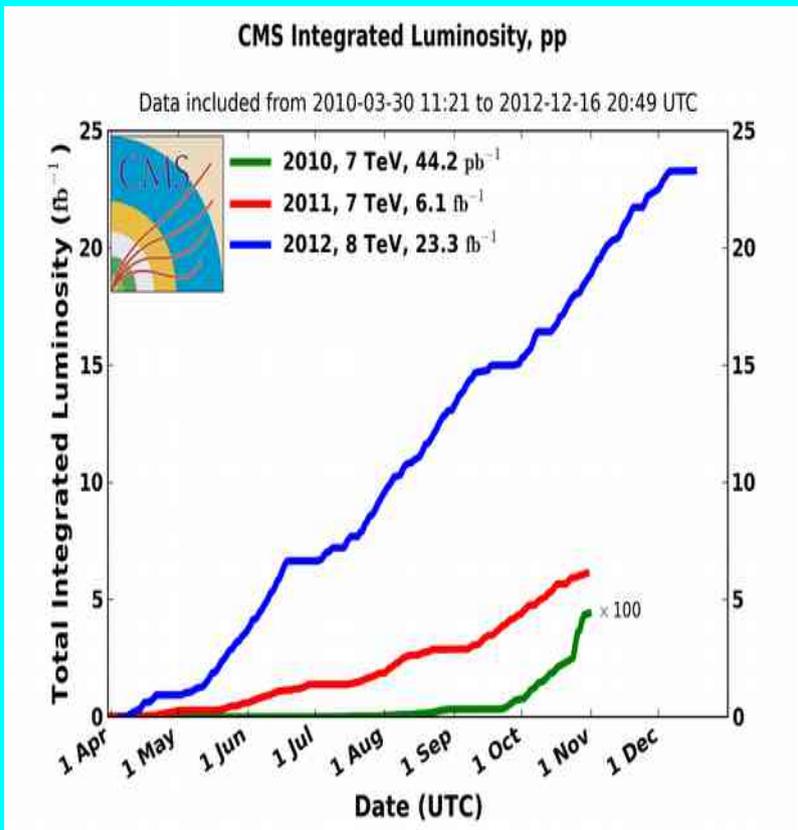


$$\sigma_{P \gamma \rightarrow c} = f_{P \rightarrow a} \otimes \hat{\sigma}_{a \gamma \rightarrow c}$$

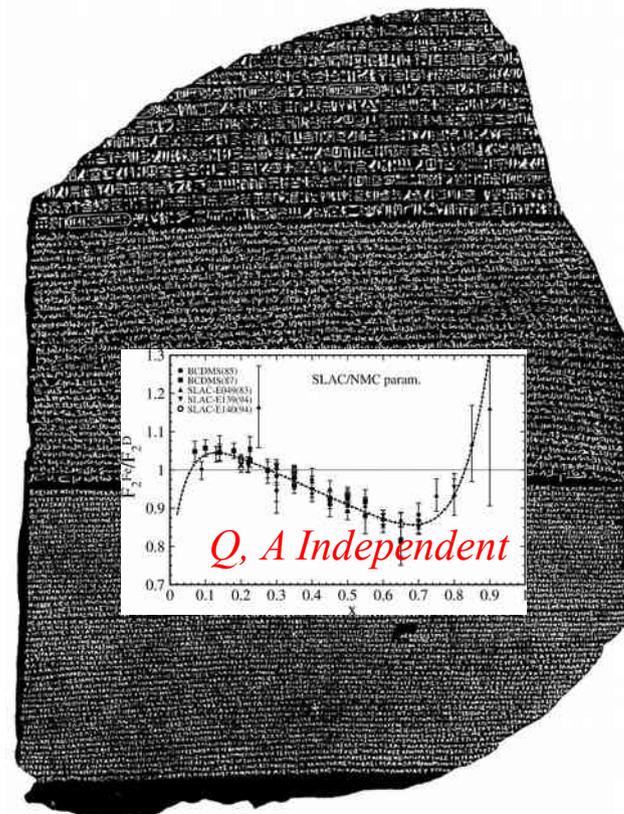
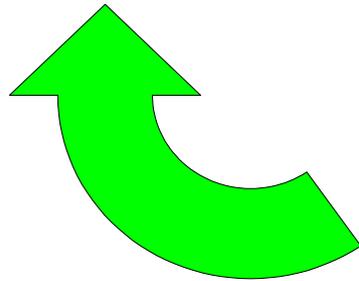
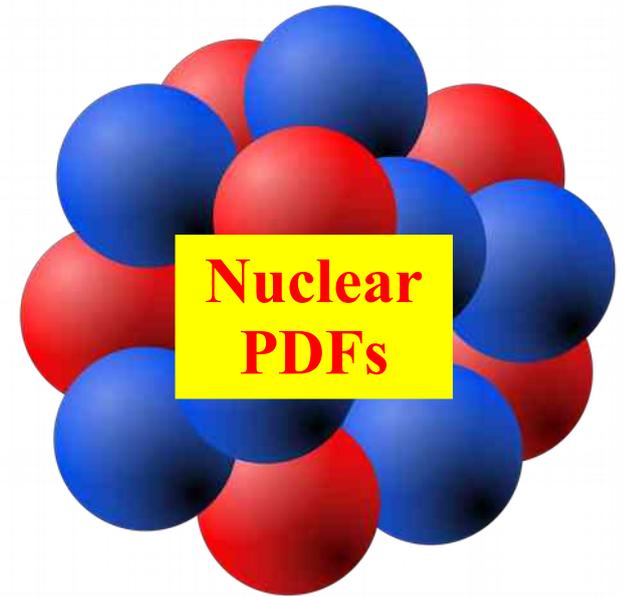
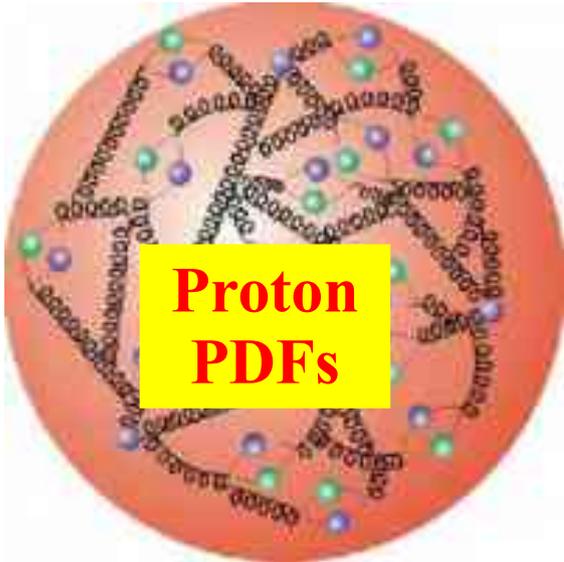
Experimental Observables

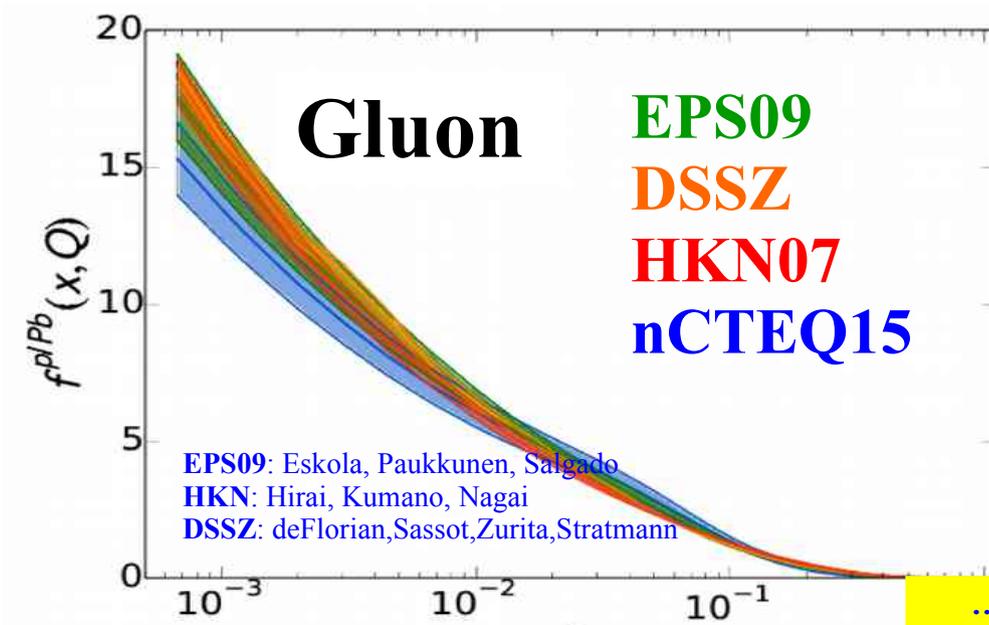
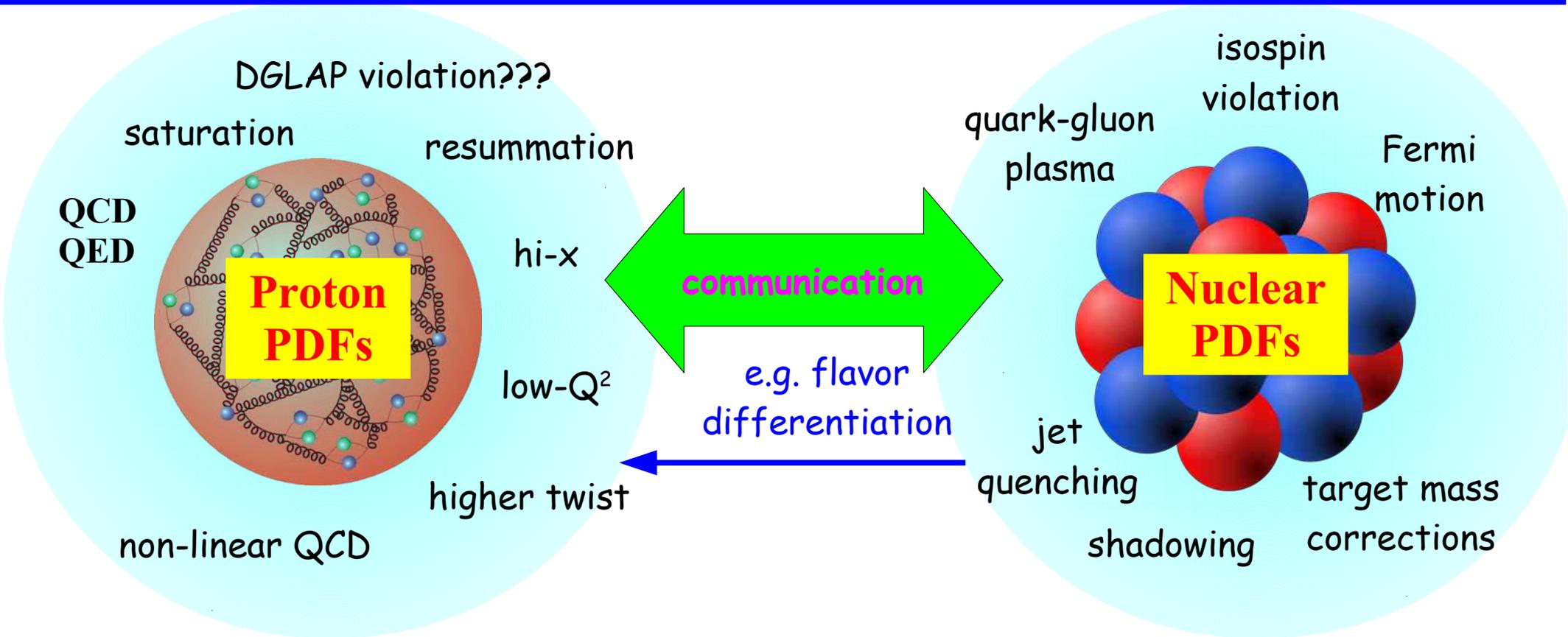
WHAT ABOUT PDF'S ???

Theoretical Calculations



... there was a time when nuclear corrections were carved in stone ...





... the original motivation for nCTEQ15

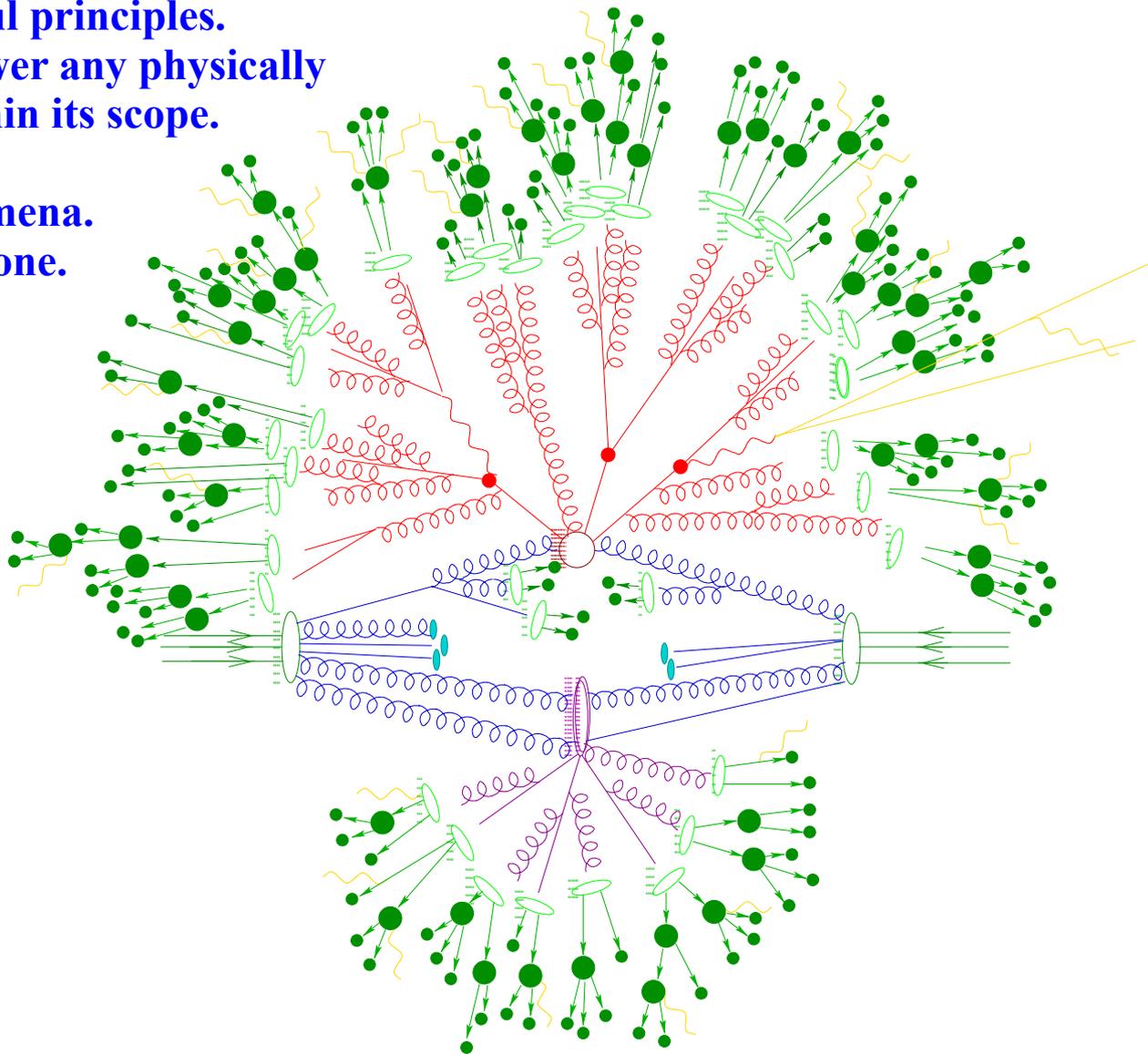
# What QCD Tells Us About Nature – and Why We Should Listen

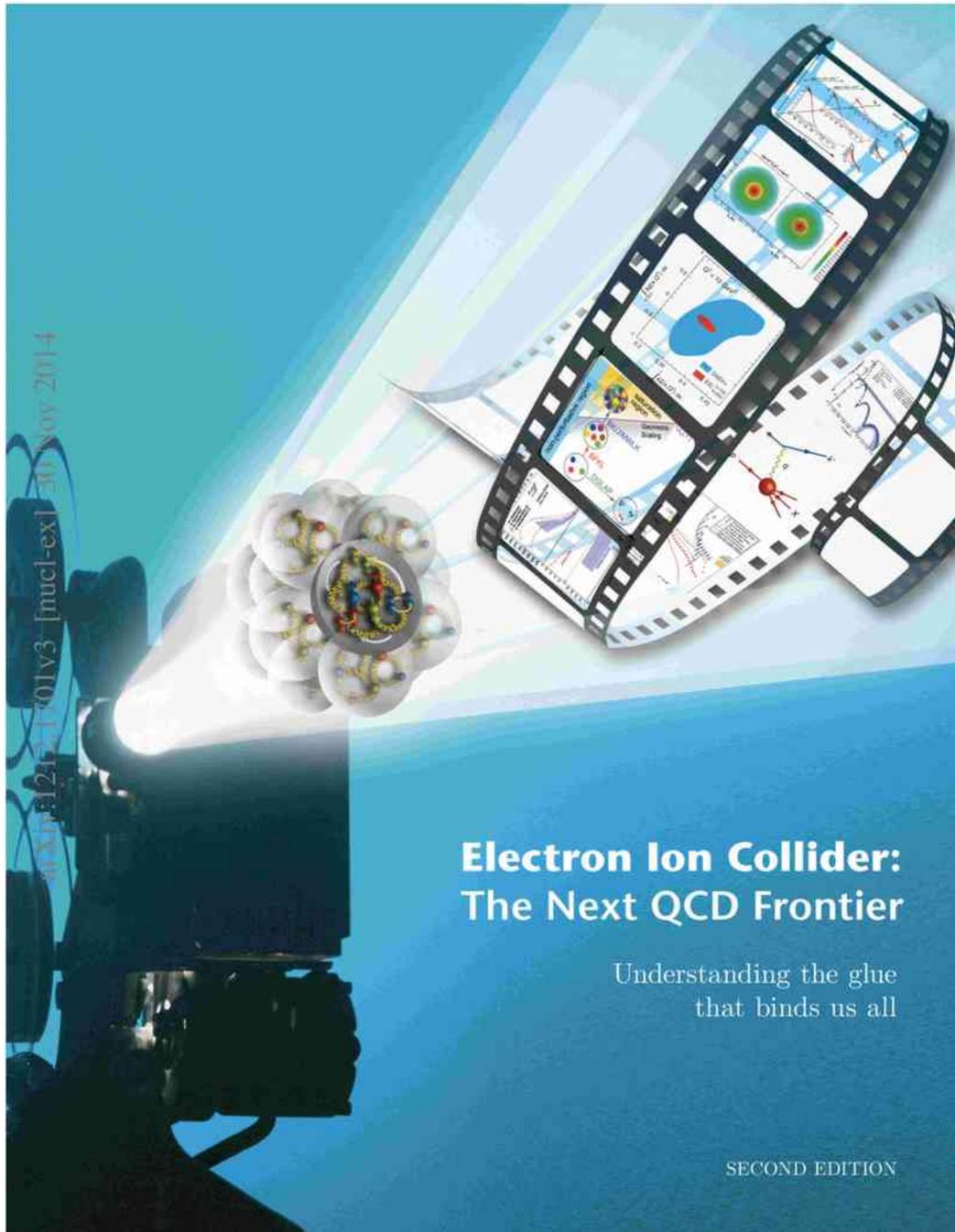
Frank Wilczek (*arXiv:hep-ph/9907340*)

## QCD is our most perfect physical theory

- It embodies deep and beautiful principles.
- It provides algorithms to answer any physically meaningful question within its scope.
- Its scope is wide.
- It contains a wealth of phenomena.
- It has few parameters ... or none.
- It is true.
- It lacks flaws.

Lessons: The Nature of Nature  
... alien, simple, beautiful, weird,  
& comprehensible





# Electron Ion Collider: The Next QCD Frontier

Understanding the glue  
that binds us all

SECOND EDITION

arXiv:1211.01v3 [nucl-ex] 30 Nov 2014

# Workshop on the LHeC

Electron-proton and electron-ion collisions at the LHC

**24 June 2015** CERN

**25-26 June 2015** Chavannes-de-Bogis, Switzerland



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## The CTEQ List of Challenges in Perturbative QCD

**~1995**

Welcome to the CTEQ List of Challenges in Perturbative QCD! Although QCD has successfully passed many tests, there are still areas where there are problems when comparing theory and experiment or where additional data or calculations are needed. Here is our current list of Challenges in Perturbative QCD. This is expected to be a dynamic list, so check back often. It is expected that existing entries will be periodically updated and that new entries will be added.

1. Direct photon production
2. Heavy quark production cross sections
3. Jet cross sections and  $x_T$  scaling
4. Determining the gluon distribution
5. Large- $x$  behavior of parton distributions
6. Determining the flavor dependence of pdf's
7. Extracting Charged & Neutral Current Cross Sections

[http://www.hep.fsu.edu/~owens/qcd/QCD\\_list.html](http://www.hep.fsu.edu/~owens/qcd/QCD_list.html)

**1) Flavor Differentiation  
& Nuclear Corrections**

**2) Multi-scale problems:  
Heavy Quarks  
Resummation**

**3) Hi-Order Corrections**

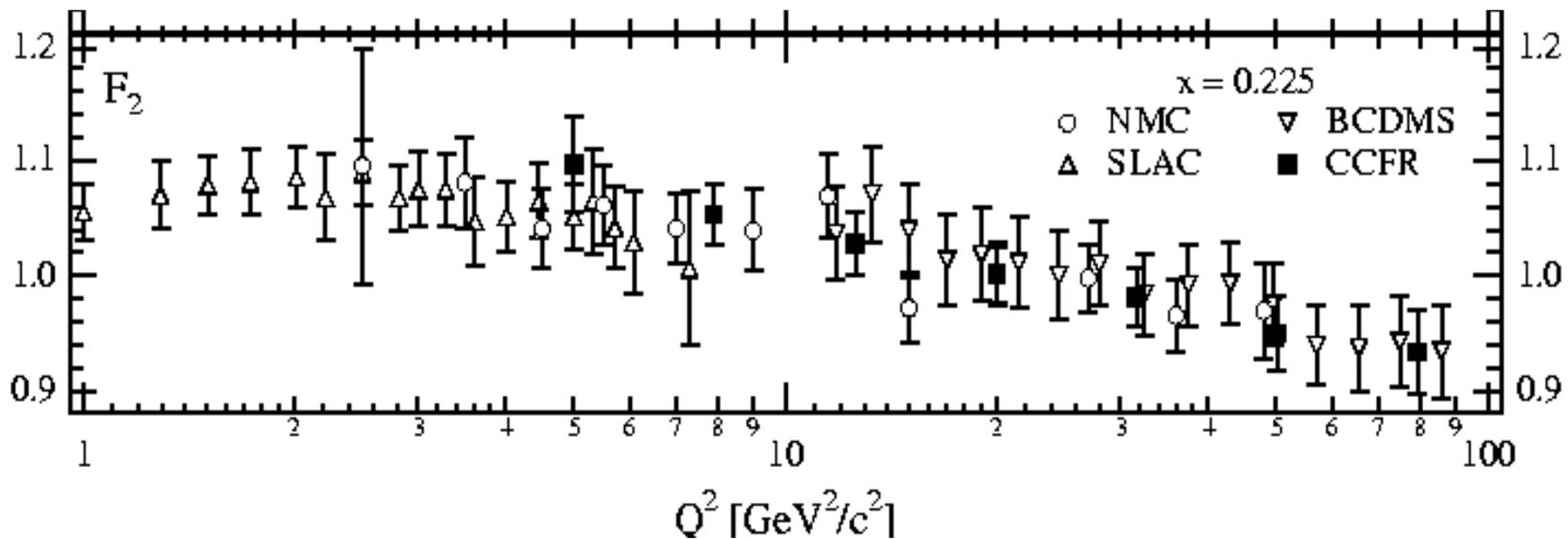
# FLAVOR DIFFERENTIATION

# Di-muon production $\Rightarrow$ Extract $s(x)$ Parton Distribution

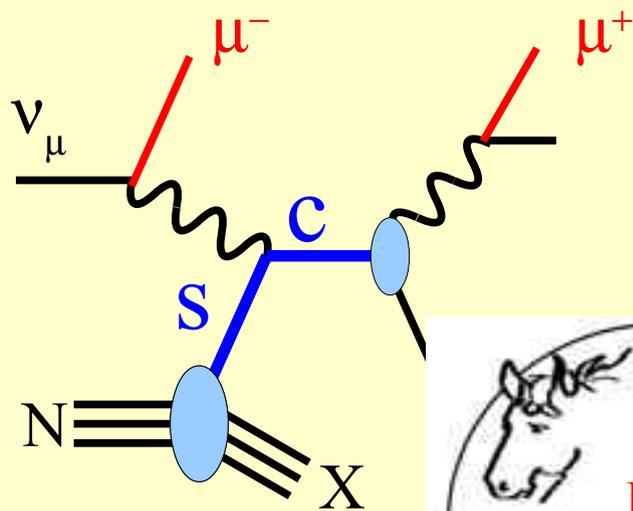
The CTEQ List of Challenges in Perturbative QCD

**~1995**

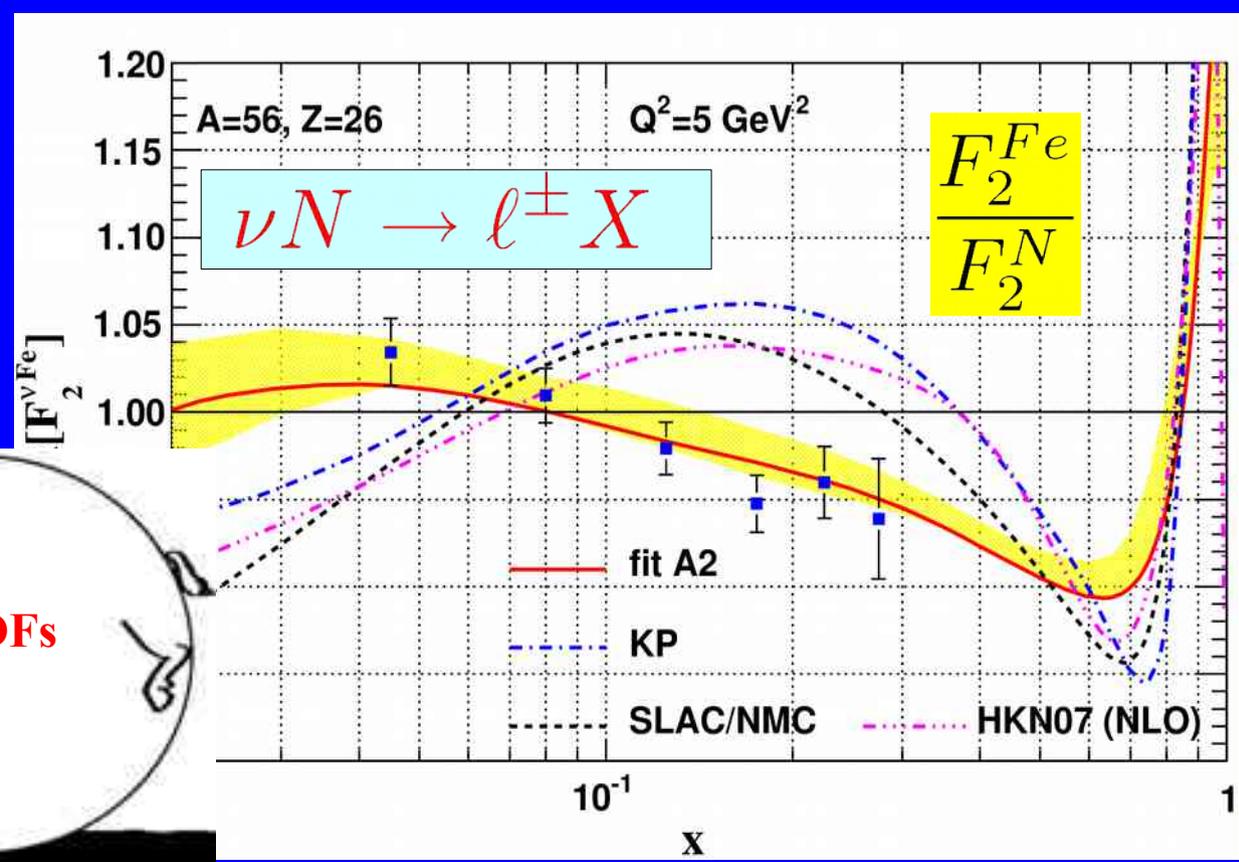
**CTEQ**



Extract  $s(x)$



**Depends on nuclear corrections**

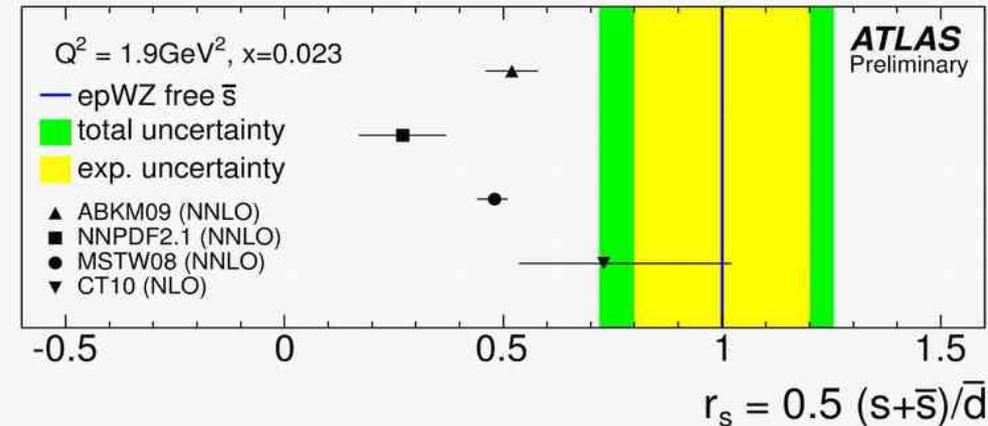


# Use LHC data to constrain Strange Quark

## W, Z data sensitivity to strange sea

- ATLAS performed NNLO QCD fit to  $Z, W^+, W^-$  + HERA  $ep$  DIS cross sections: significant tension for  $Z$  observed when suppressing strange by 50% at low scale  $1.9 \text{ GeV}^2$
- Fit with free strange sea gives no suppression

$$r_s = 1.00 \pm 0.20_{\text{exp}} \begin{matrix} +0.16 \\ -0.20 \text{ sys} \end{matrix}$$



**DIY: Do It Yourself: Strange Quark from LHC Data**

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**Welcome to HERAFitter Project**  
 HERAFitter is a QCD Fit Package used to determine HERAPDFs and it is part of the

*... what about the*

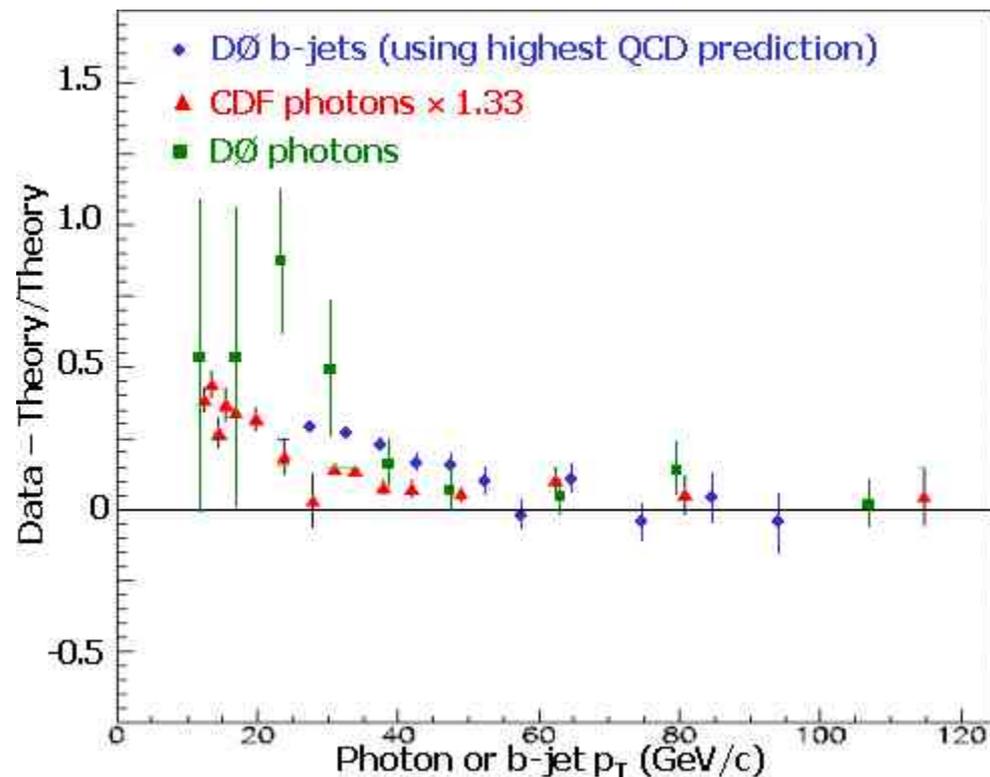
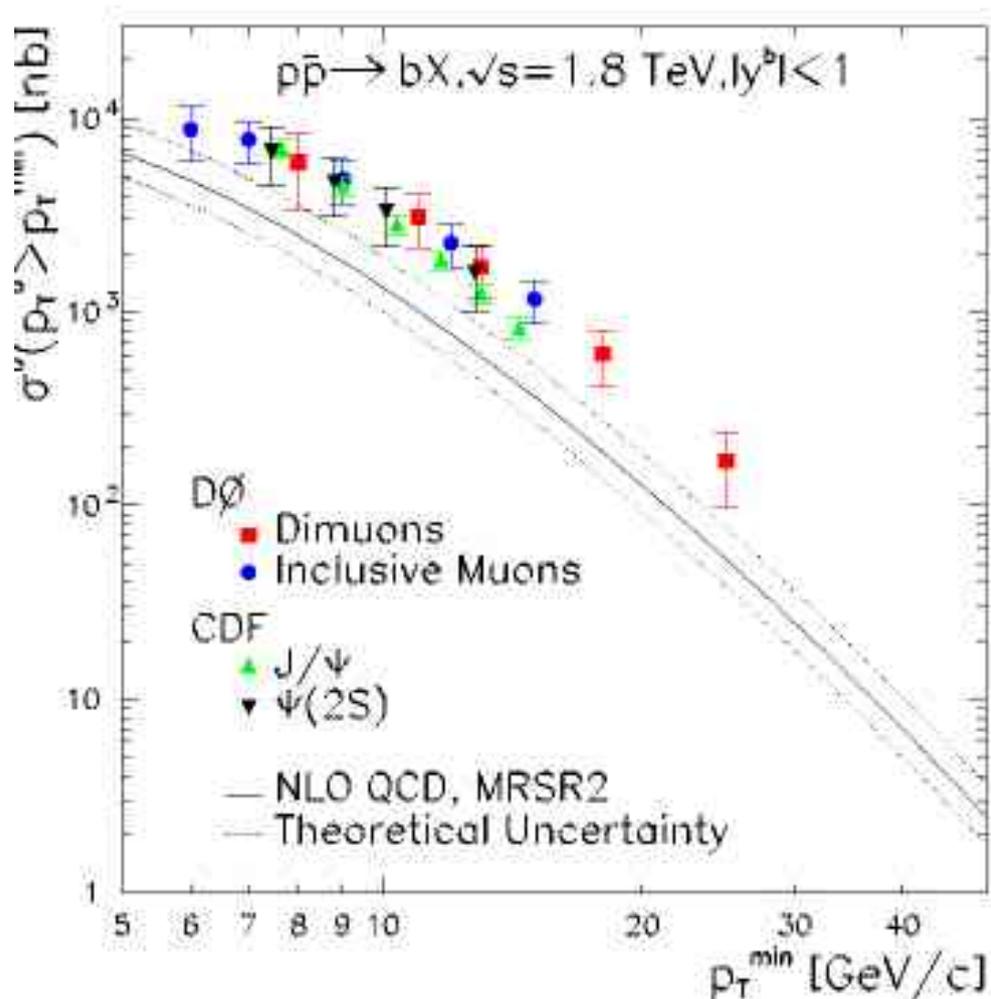
# Heavy Quarks

*c & b: Extrinsic & Intrinsic*

*Historically, these have been a challenge because  $Q \sim m_{c,b}$*

## The CTEQ List of Challenges in Perturbative QCD

Calculating b-quark production cross sections at hadron-hadron colliders



~1995

# Multi-Scale Problems are Challenging

## Two-Loop Total Cross Section: One Scale

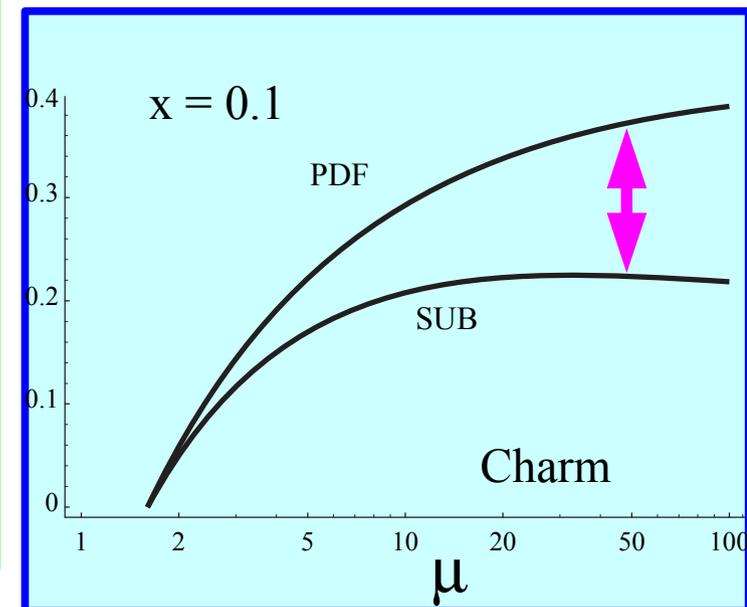
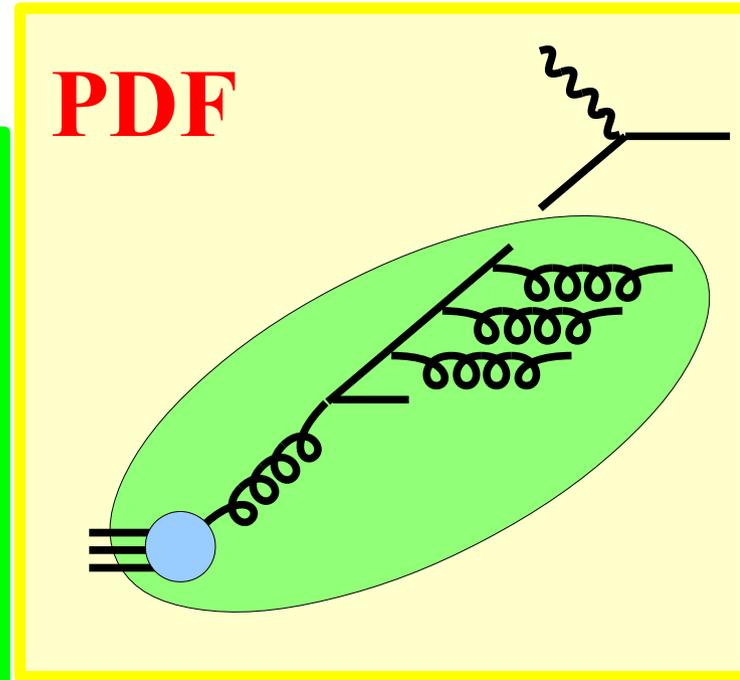
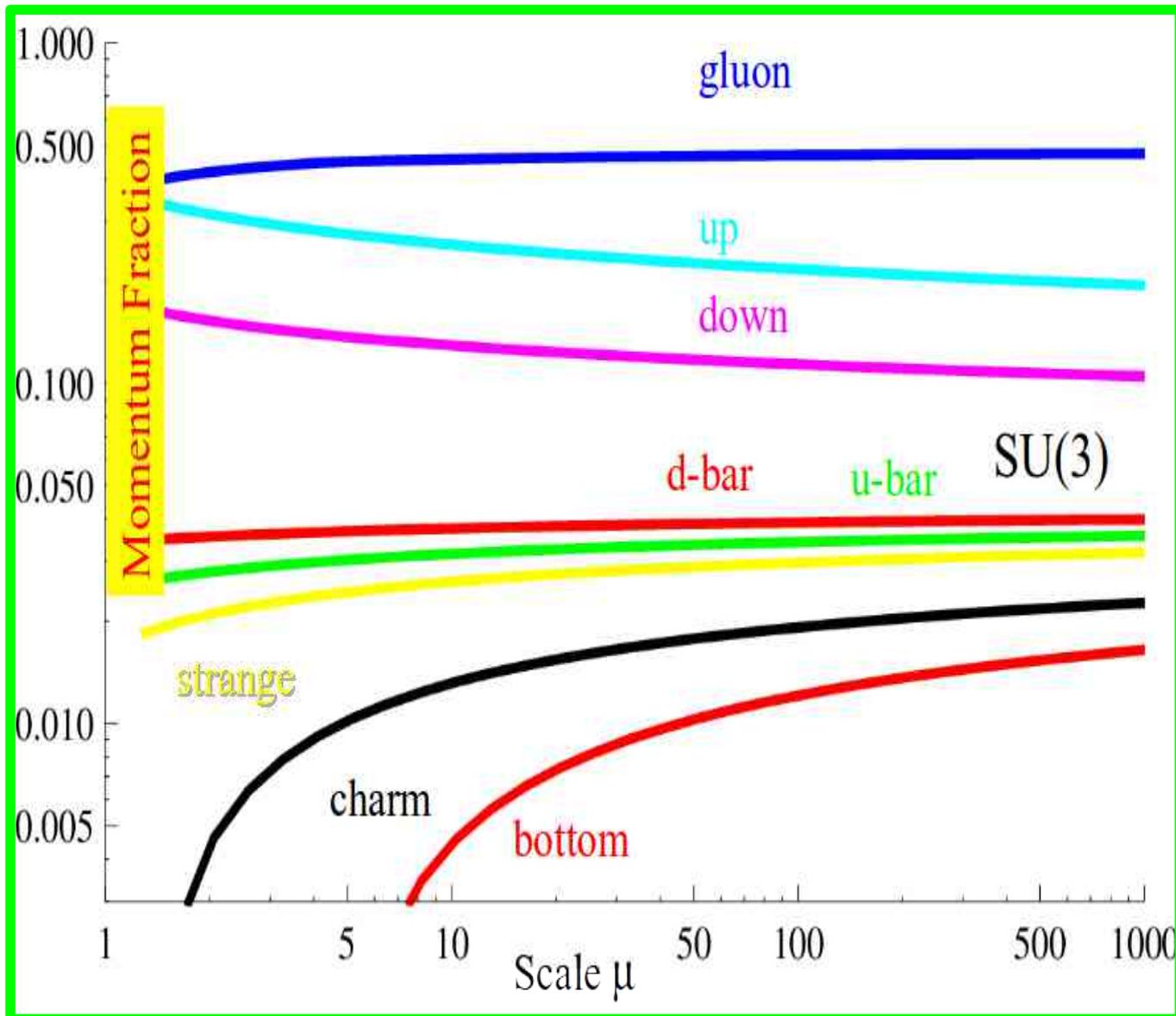
$$\sigma(Q^2) = \sigma_0 \left\{ 1 + \frac{\alpha_s(Q^2)}{4\pi} (3C_F) + \left[ \frac{\alpha_s(Q^2)}{4\pi} \right]^2 \left[ -C_F^2 \left[ \frac{3}{2} \right] + C_F C_A \left[ \frac{123}{2} - 44\zeta(3) \right] + C_F T n_f (-22 + 16\zeta(3)) \right] \right\}$$

## Two-Loop Drell-Yan Cross Section: Two Scales

$$\begin{aligned} H_{q\bar{q}}^{(2),S+V}(z) = & \left[ \frac{\alpha_s}{4\pi} \right]^2 \delta(1-z) \left\{ C_A C_F \left[ \left[ \frac{193}{3} - 24\zeta(3) \right] \ln \left[ \frac{Q^2}{M^2} \right] - 11 \ln^2 \left[ \frac{Q^2}{M^2} \right] - \frac{12}{5} \zeta(2)^2 + \frac{592}{9} \zeta(2) + 28\zeta(3) - \frac{1535}{12} \right] \right. \\ & + C_F^2 \left[ [18 - 32\zeta(2)] \ln^2 \left[ \frac{Q^2}{M^2} \right] + [24\zeta(2) + 176\zeta(3) - 93] \ln \left[ \frac{Q^2}{M^2} \right] \right. \\ & \left. \left. + \frac{8}{5} \zeta(2)^2 - 70\zeta(2) - 60\zeta(3) + \frac{511}{4} \right] \right. \\ & \left. + n_f C_F \left[ 2 \ln^2 \left[ \frac{Q^2}{M^2} \right] - \frac{34}{3} \ln \left[ \frac{Q^2}{M^2} \right] + 8\zeta(3) - \frac{112}{9} \zeta(2) + \frac{127}{6} \right] \right\} \\ & + C_A C_F \left[ -\frac{44}{3} \mathcal{D}_0(z) \ln^2 \left[ \frac{Q^2}{M^2} \right] + \left\{ \left[ \frac{536}{9} - 16\zeta(2) \right] \mathcal{D}_0(z) - \frac{176}{3} \mathcal{D}_1(z) \right\} \ln \left[ \frac{Q^2}{M^2} \right] \right. \\ & \left. - \frac{176}{3} \mathcal{D}_2(z) + \left[ \frac{1072}{9} - 32\zeta(2) \right] \mathcal{D}_1(z) + [56\zeta(3) + \frac{176}{3} \zeta(2) - \frac{1616}{27}] \mathcal{D}_0(z) \right] \\ & + C_F^2 \left[ [64\mathcal{D}_1(z) + 48\mathcal{D}_0(z)] \ln^2 \left[ \frac{Q^2}{M^2} \right] + \left\{ 192\mathcal{D}_2(z) + 96\mathcal{D}_1(z) - [128 + 64\zeta(2)] \mathcal{D}_0(z) \right\} \ln \left[ \frac{Q^2}{M^2} \right] \right. \\ & \left. + 128\mathcal{D}_3(z) - (128\zeta(2) + 256)\mathcal{D}_1(z) + 256\zeta(3)\mathcal{D}_0(z) \right] \\ & + n_f C_F \left[ \frac{8}{3} \mathcal{D}_0(z) \ln^2 \left[ \frac{Q^2}{M^2} \right] + \left[ \frac{32}{3} \mathcal{D}_1(z) - \frac{80}{9} \mathcal{D}_0(z) \right] \ln \left[ \frac{Q^2}{M^2} \right] + \frac{32}{3} \mathcal{D}_2(z) - \frac{160}{9} \mathcal{D}_1(z) + \left[ \frac{224}{27} - \frac{32}{3} \zeta(2) \right] \mathcal{D}_0(z) \right] . \end{aligned}$$

# Charm & Bottom PDFs Resum Logs

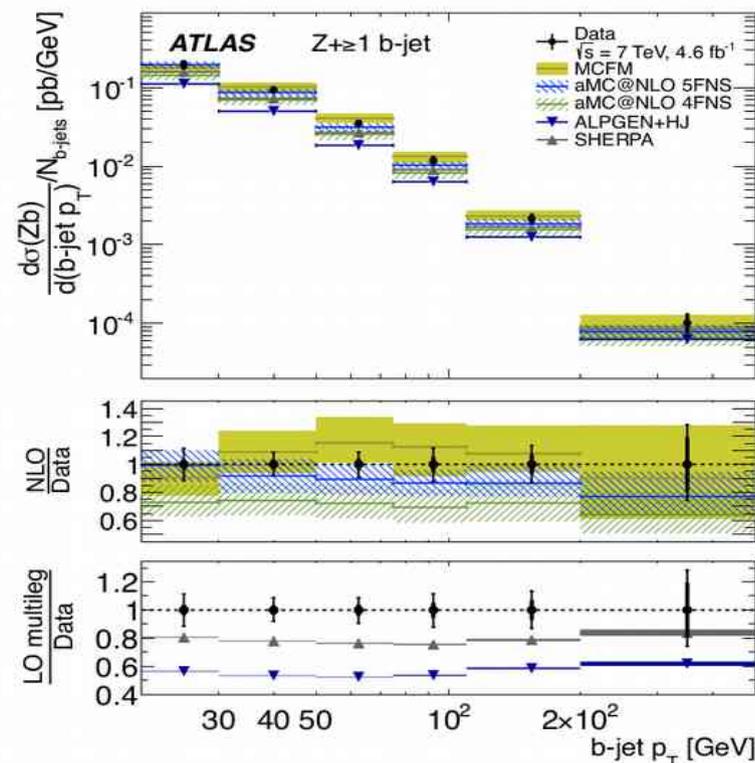
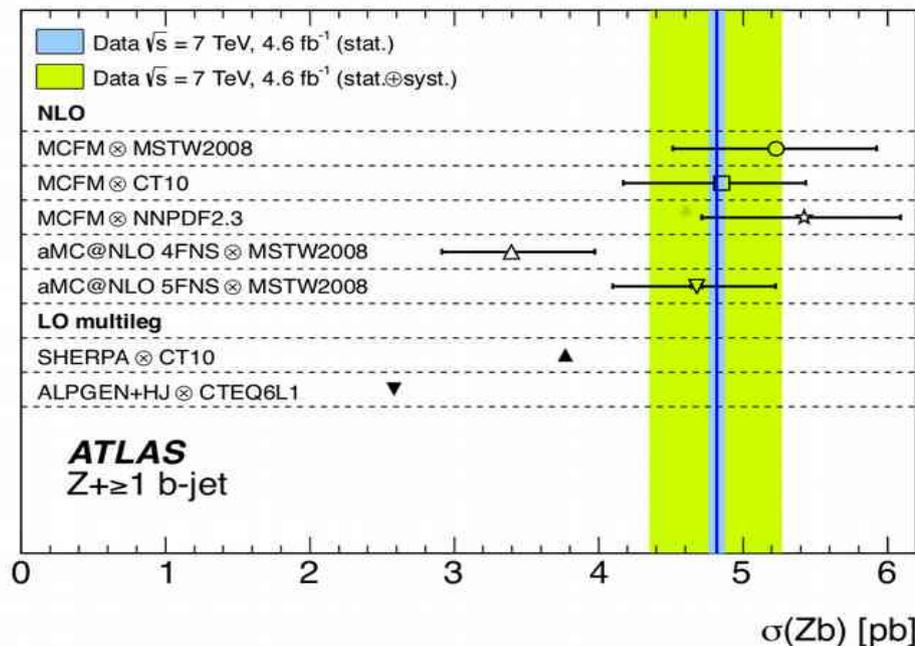
Resum  $\alpha_s \ln(m/Q)$



## Heavy flavor: Z+b-jets

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- + Good agreement with NLO MCFM and aMC@NLO
  - Seems to favor scheme where b-quark is taken from PDF (5 FNS)
  - LO+PS generators are underestimating the cross section
  - Can't constrain PDF yet due to too large uncertainty
  
- + Good description of b-jet  $p_T$  shape
  - Normalization is off



# $W/Z/\gamma$ Production

“Benchmark Calculations”

*Recall Direct Photon*

*... the fine print:*

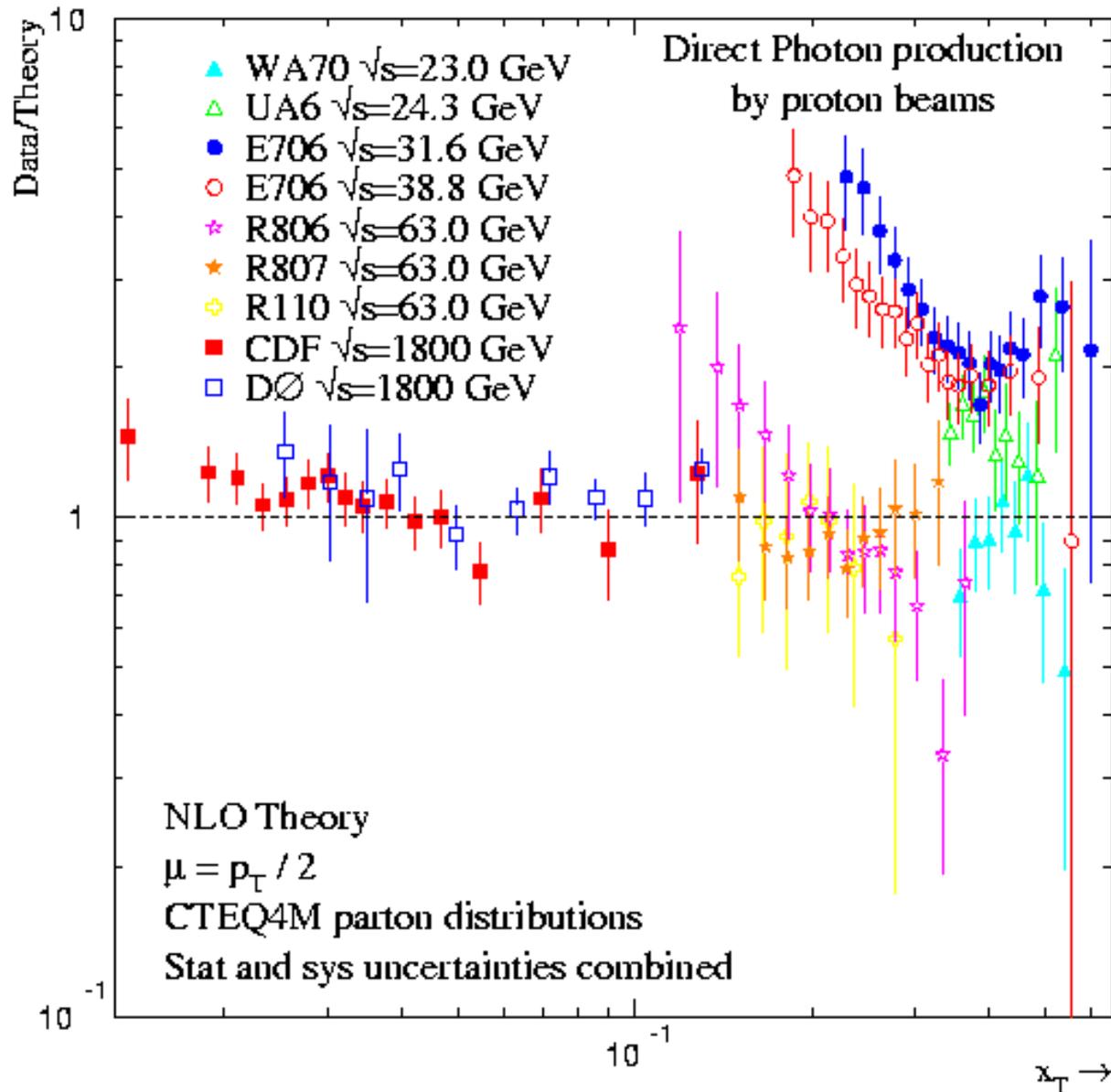
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# The CTEQ List of Challenges in Perturbative QCD

## Understanding Direct Photon Production



~1995

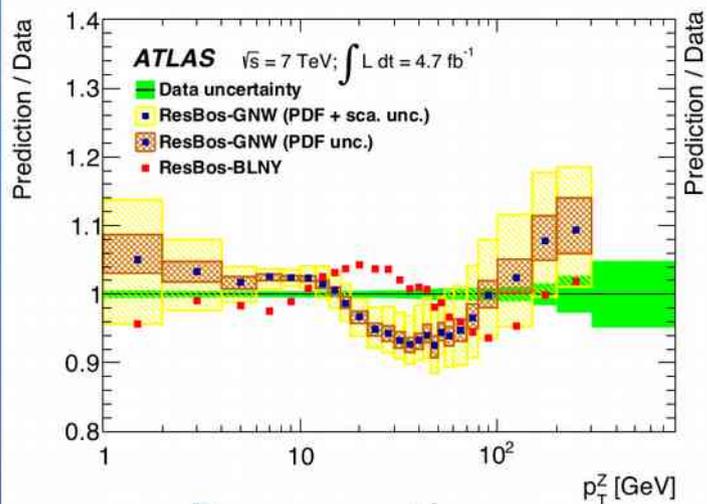
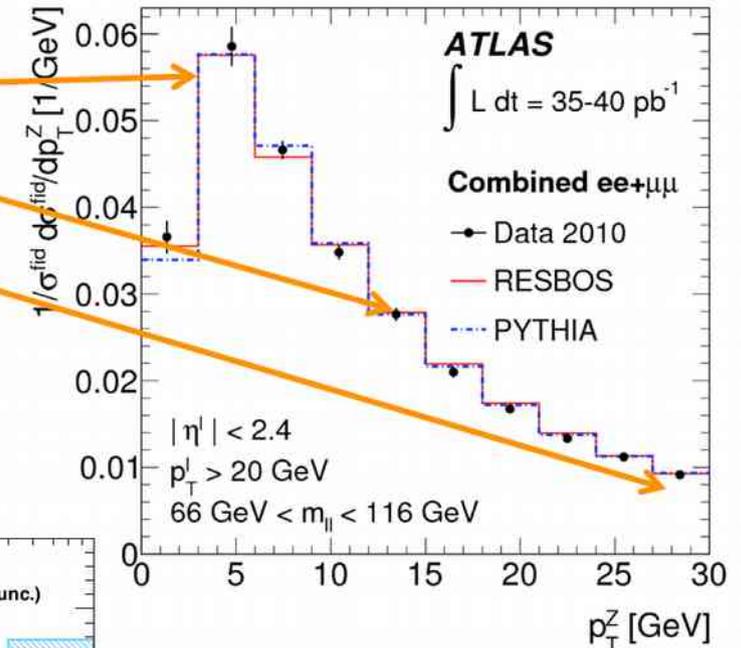


# QCD bremsstrahlung: Vector Boson $P_T$

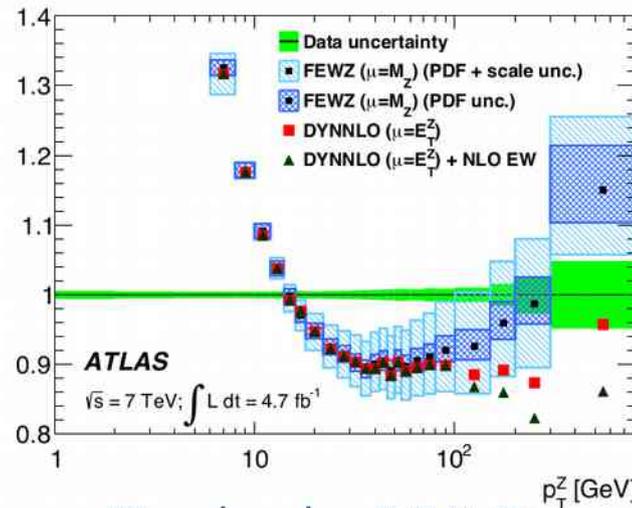
Phys. Lett. B705 (2011) 415-434

JHEP 09 (2014) 145

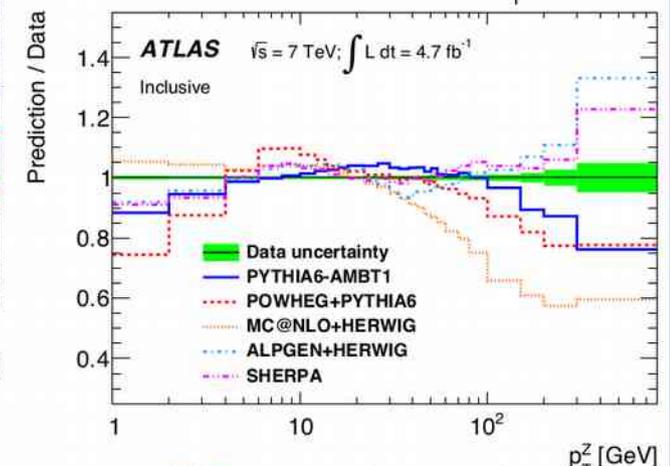
- + Test multiple aspect of QCD predictions
  - Intrinsic- $K_T$
  - Low-PT (W,Z): logarithmic resummations
  - High-PT (W,Z): (N)NLO perturbative QCD
  - Important test of parton shower tuning
    - No color flow between initial and final state



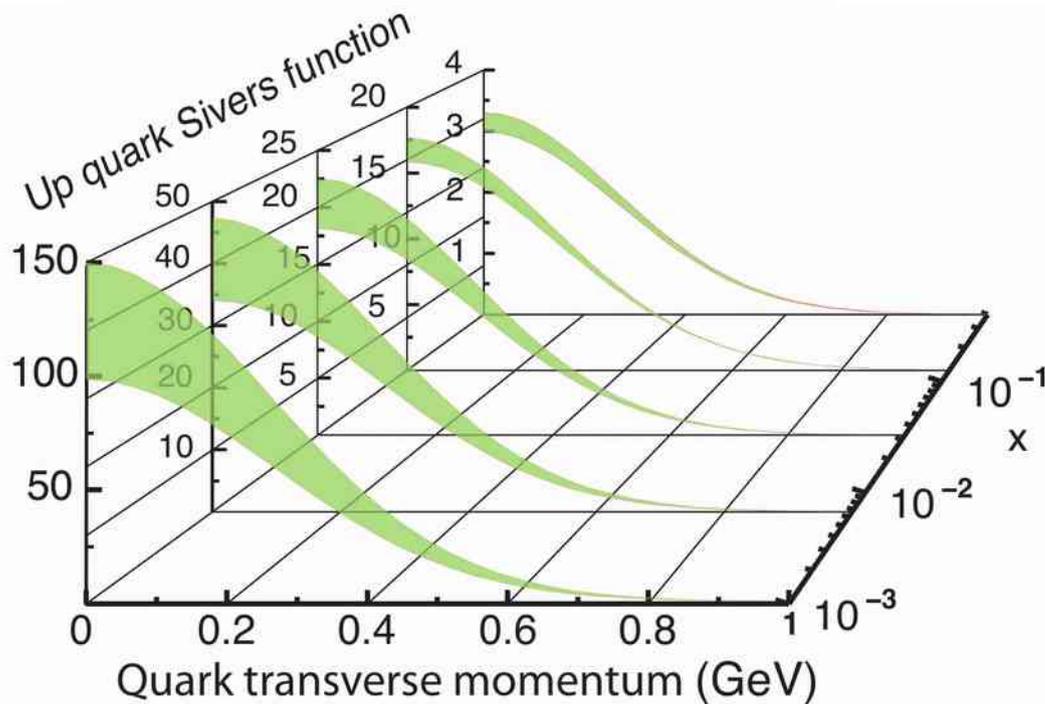
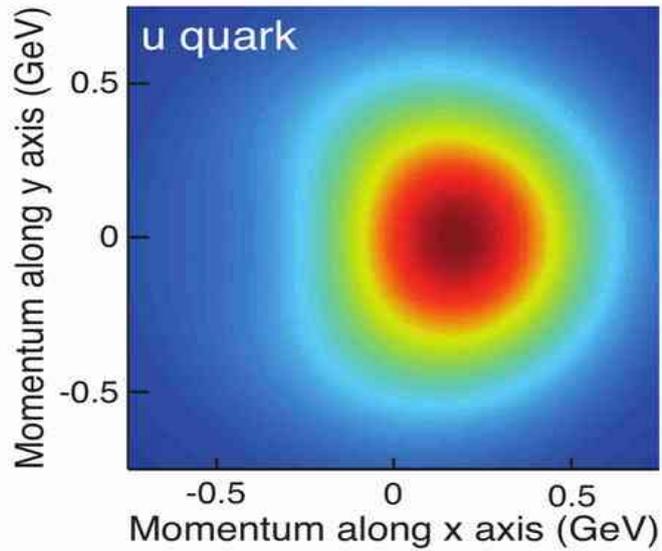
Resummation:  
Good description at  
low and average  $P_T$



Fixed order (NNLO):  
Poor description at  
average  $P_T$



PS more important  
than NLO ME



previously discussed by: Rolf Ent & Michael Engelhardt

## Lattice Calculations

Kresimir Kumericki  
Curse of dimensionality

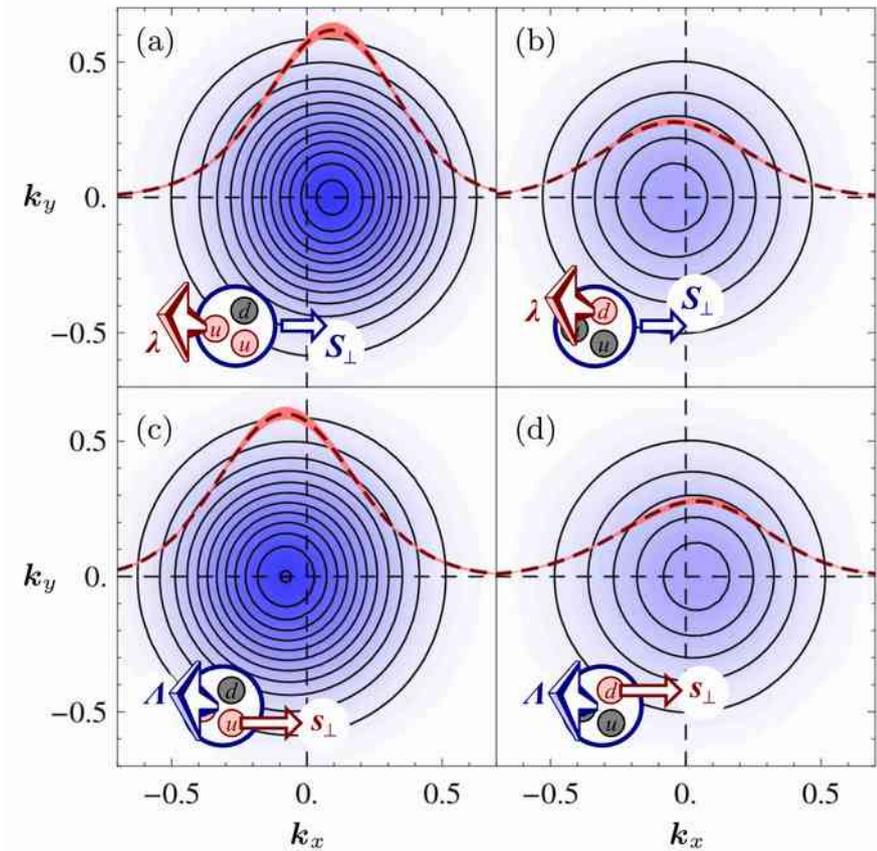


FIG. 3: Quark densities in the  $k_{\perp}$ -plane, for  $m_{\pi} \approx 500$  MeV. (a)  $\rho_L$  for u-quarks and  $\lambda = 1$ ,  $S_{\perp} = (1, 0)$ , (b) the same for d-quarks, (c)  $\rho_T$  for u-quarks and  $\Lambda = 1$ ,  $s_{\perp} = (1, 0)$ , (d) the same for d-quarks. The error bands show the density profile at  $k_y = 0$  as a function of  $k_x$  (scale not shown).

# Higher Orders

*An example...*

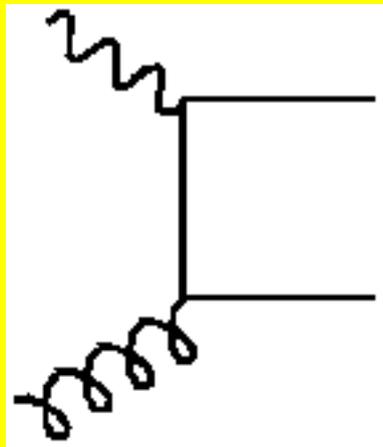
ACOT@ NNLO + N<sup>3</sup>LO

## LO

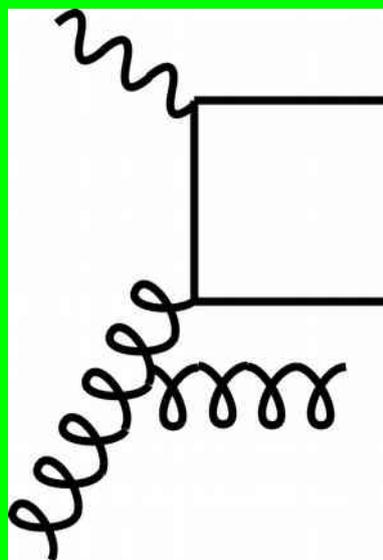


~1995

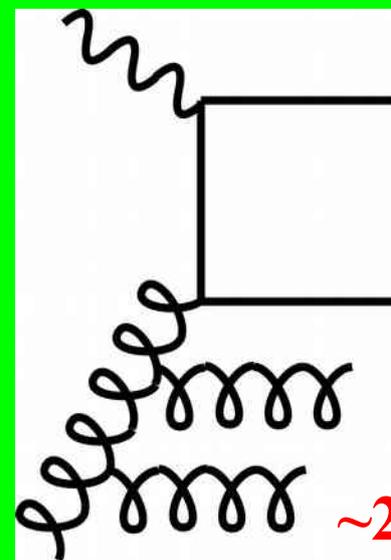
## NLO



## N2LO



## N3LO



~2015

## Full ACOT

Based on the Collins-Wilczek-Zee (CWZ) Renormalization Scheme  
*... hence, extensible to all orders*

DGLAP kernels & PDF evolution are pure  $\overline{\text{MS}}$ -Bar  
*Subtractions are  $\overline{\text{MS}}$ -Bar*

ACOT:  $m \rightarrow 0$  limit yields  $\overline{\text{MS}}$ -Bar  
*with no finite renormalization*

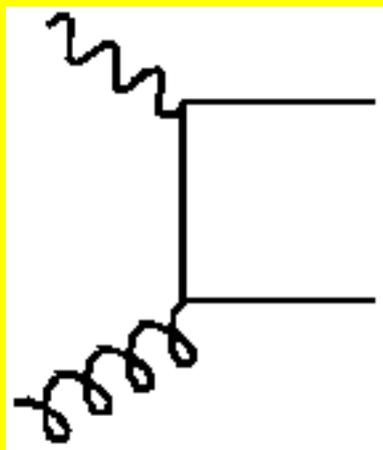
PDFs Discontinuous at N2LO

$\alpha_s$  Discontinuous at  $\alpha_s^3$

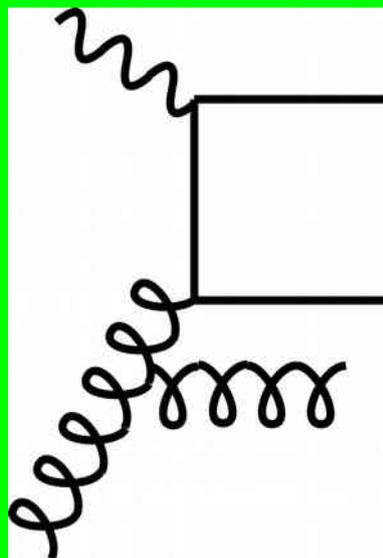
**LO**



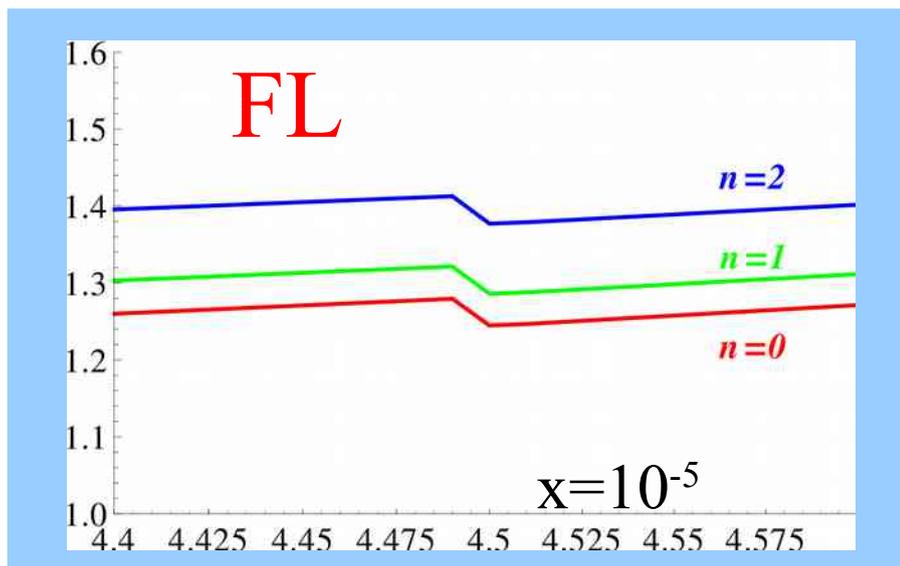
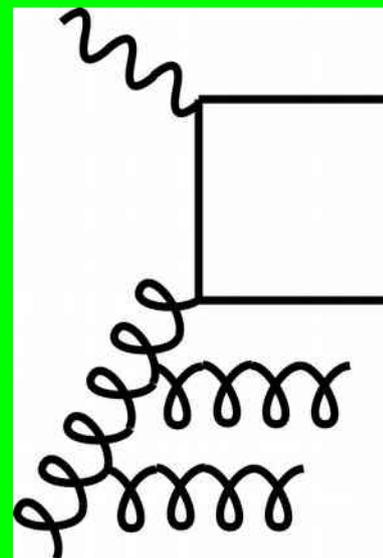
**NLO**



**N2LO**



**N3LO**



**PDFs Discontinuous at N2LO**  
 $\alpha_s$  Discontinuous at  $\alpha_s^3$

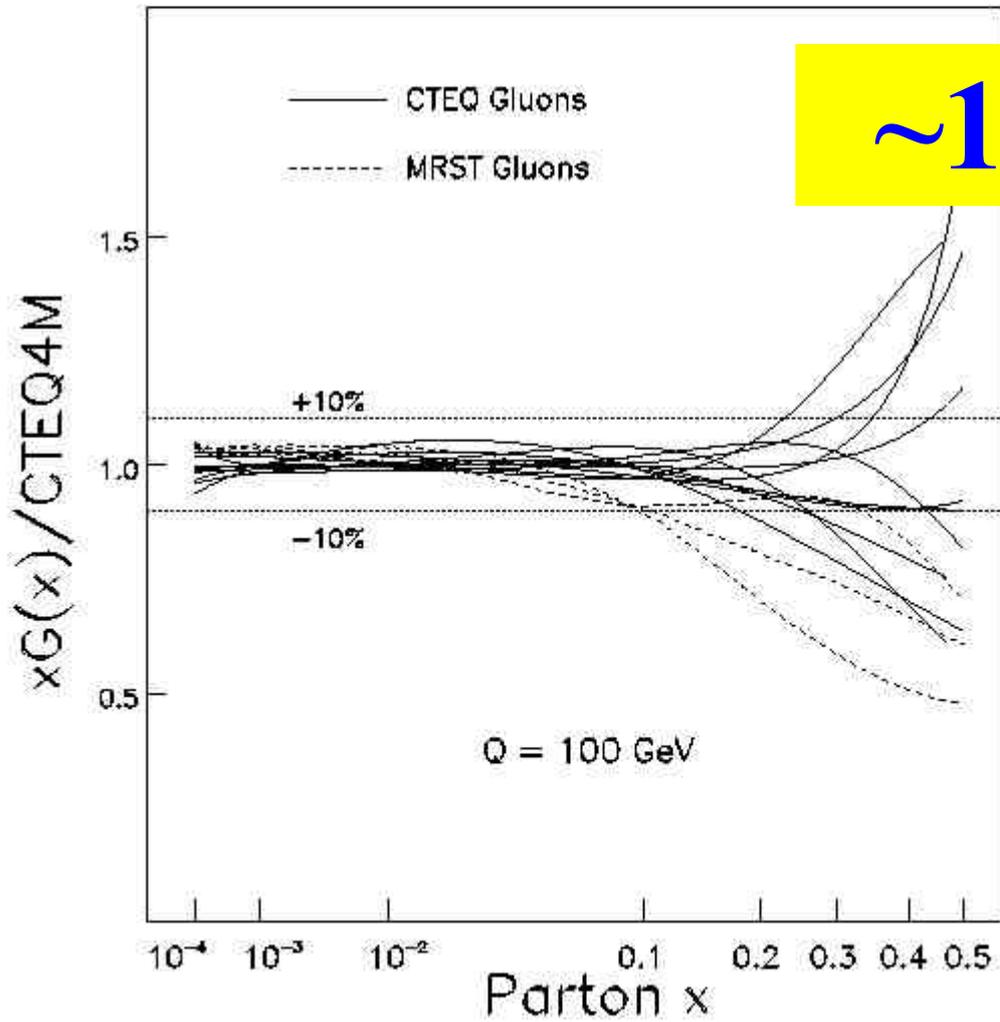
$$\sigma_{TOT}^{N_F+1} = \sigma_{TOT}^{N_F} + \mathcal{O}(\alpha_S^{m+1})$$

Quark & Gluon have opposite discontinuities

*... this is really cool!!!*

# The CTEQ List of Challenges in Perturbative QCD

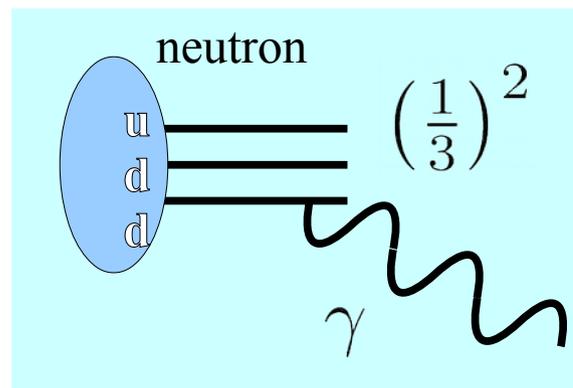
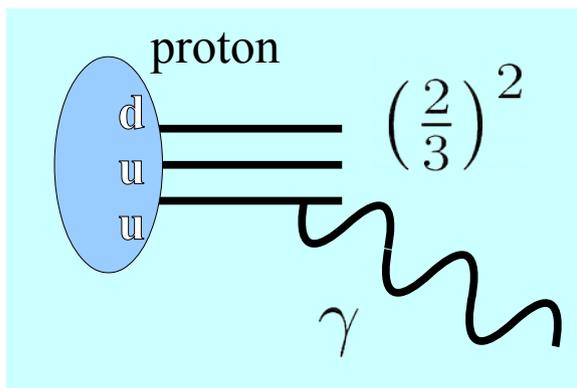
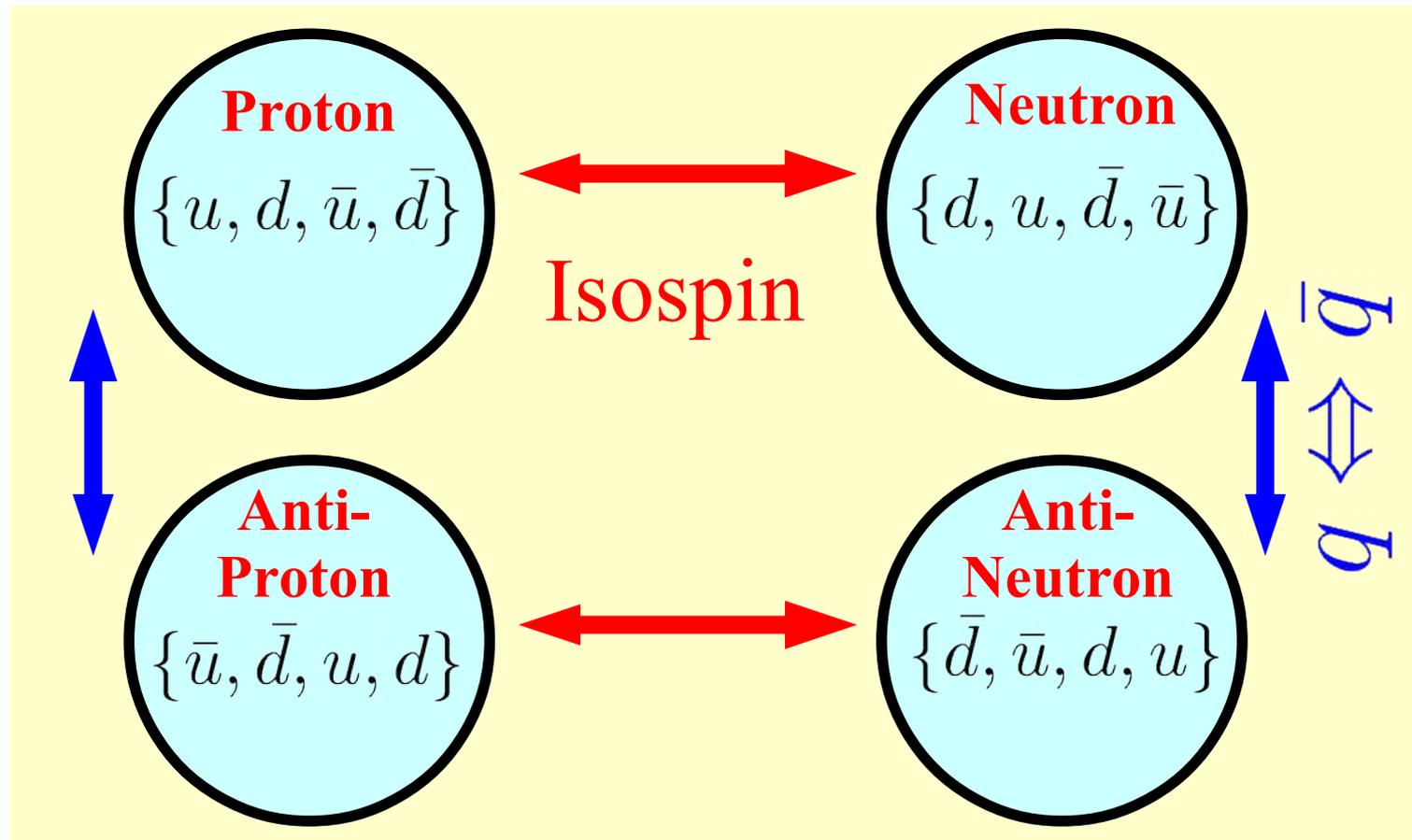
Large-x behavior of parton distributions



**~1995**

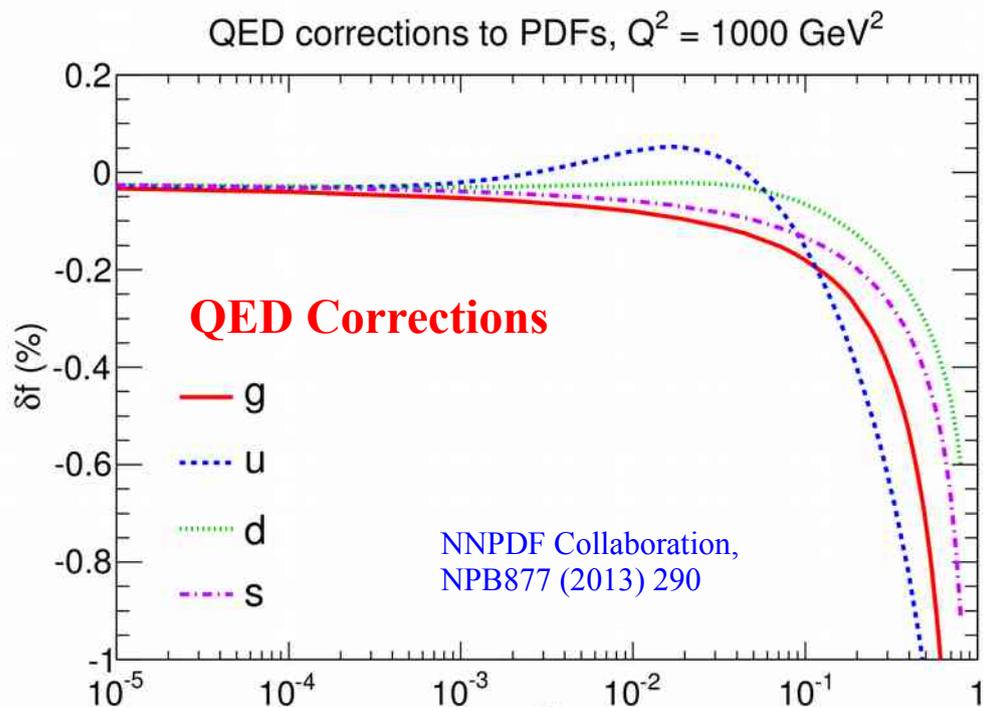
# Isospin Symmetry

*... taken for granted*

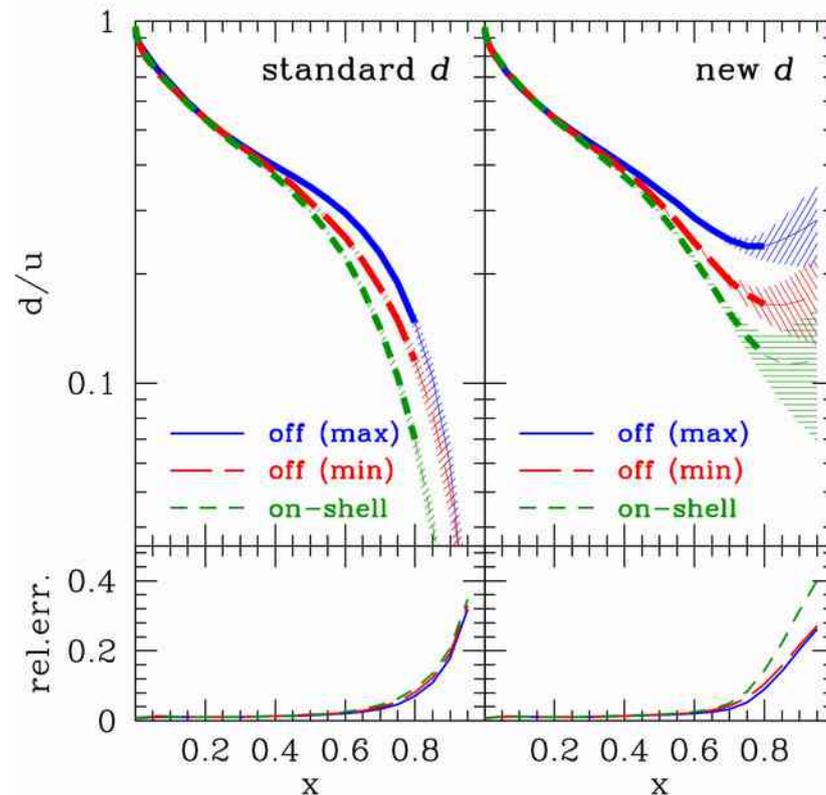


**Isospin terms are comparable to NNLO QCD**

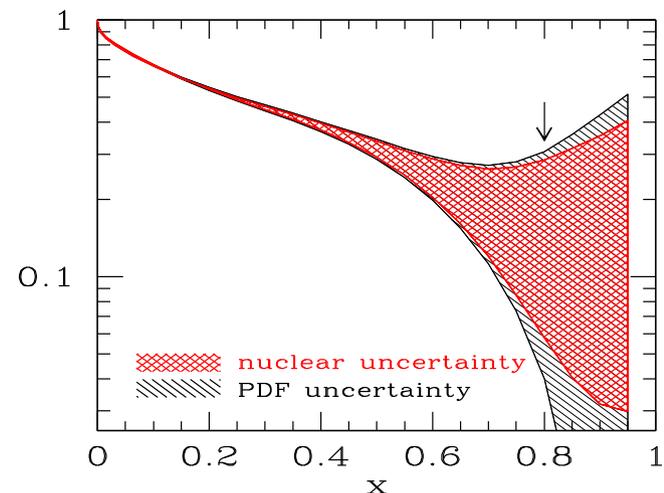
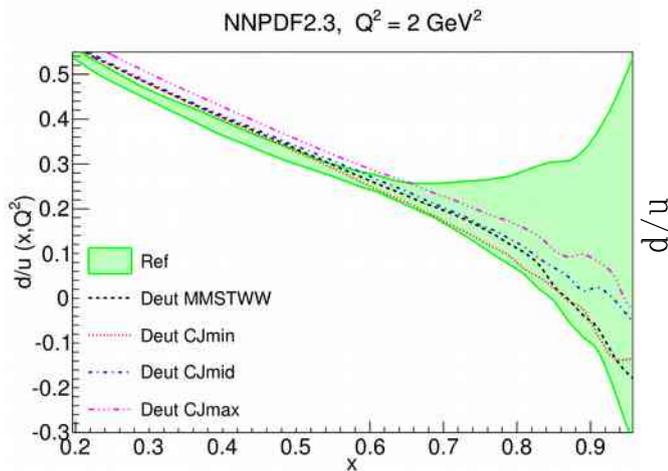
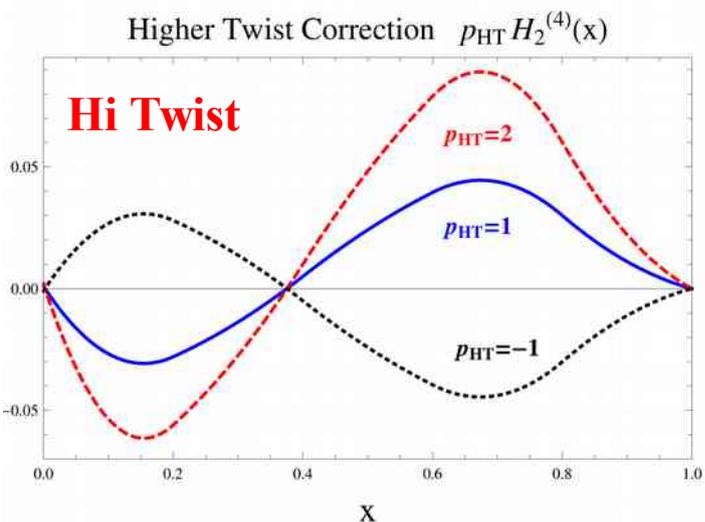
**QCD & EW Corrections do NOT factorize**



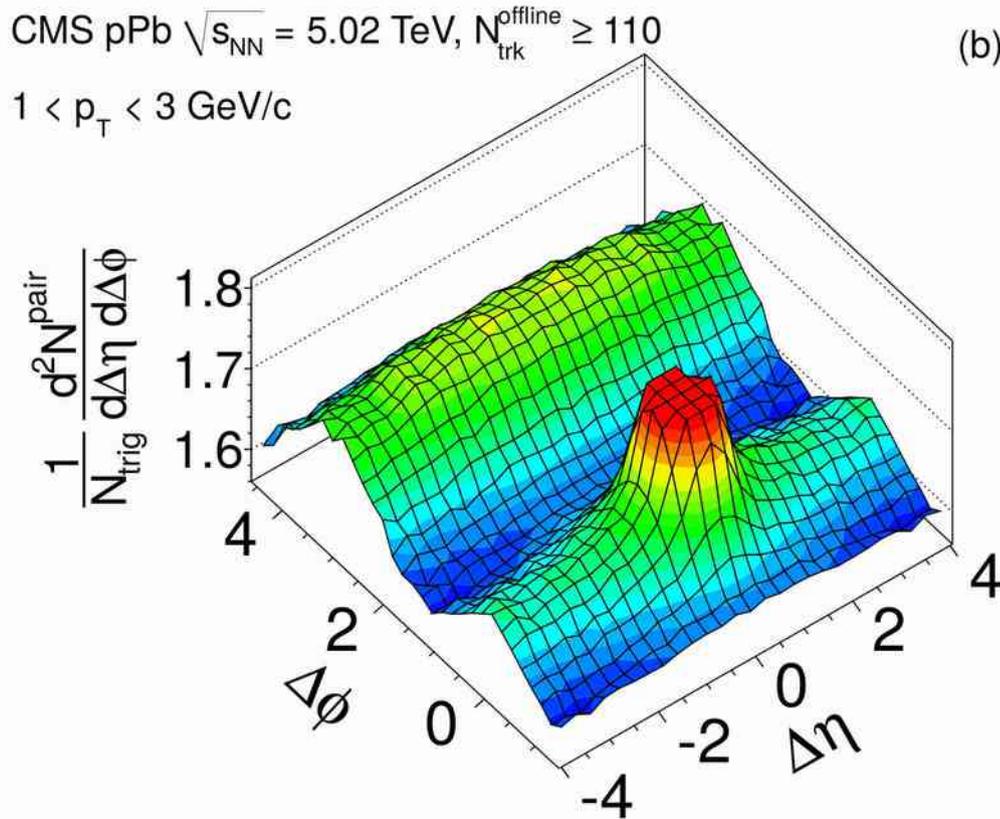
Hi-x is a “Gold Mine” for EIC



*Nuclear Corrections or Parameterization???*

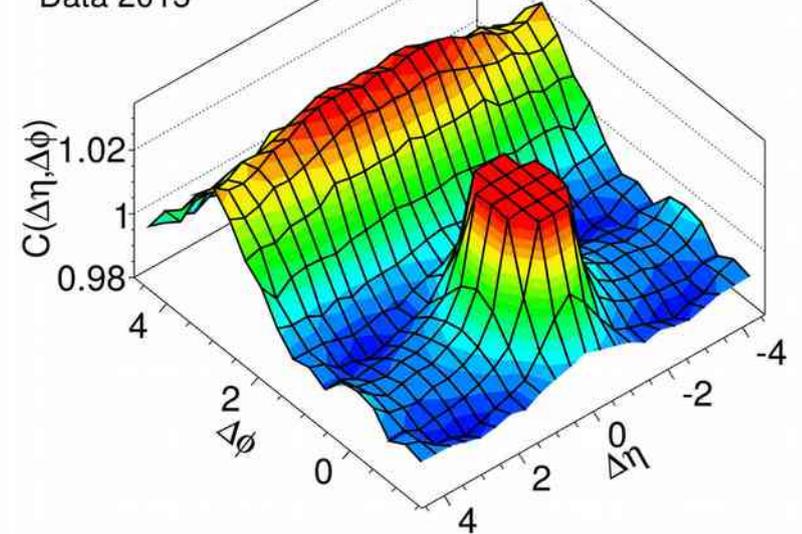


other  
effects



(b)

**ATLAS Preliminary**  
 $\sqrt{s} = 13$  TeV,  $L_{\text{int}} \approx 14$  nb $^{-1}$   
 Data 2015  
 $0.5 < p_T^{a,b} < 5.0$  GeV  
 $N_{\text{ch}}^{\text{rec}} \geq 120$



**ALICE**  
 p-Pb  $\sqrt{s_{NN}} = 5.02$  TeV  
 V0S: (0-20%)-(60-100%)  
 $0.5 < p_T^{\pm} (\text{GeV}/c) < 1$   
 Assoc. tracks  
 $-q$   
 $0V$

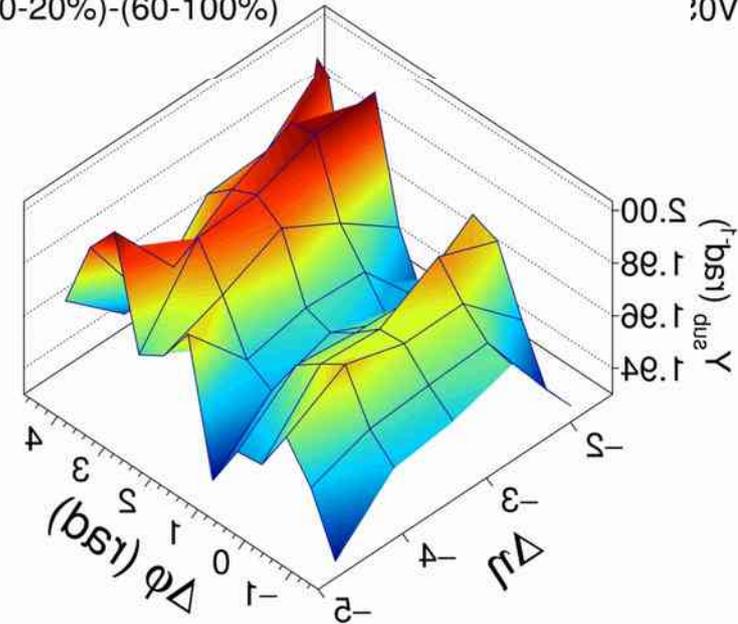
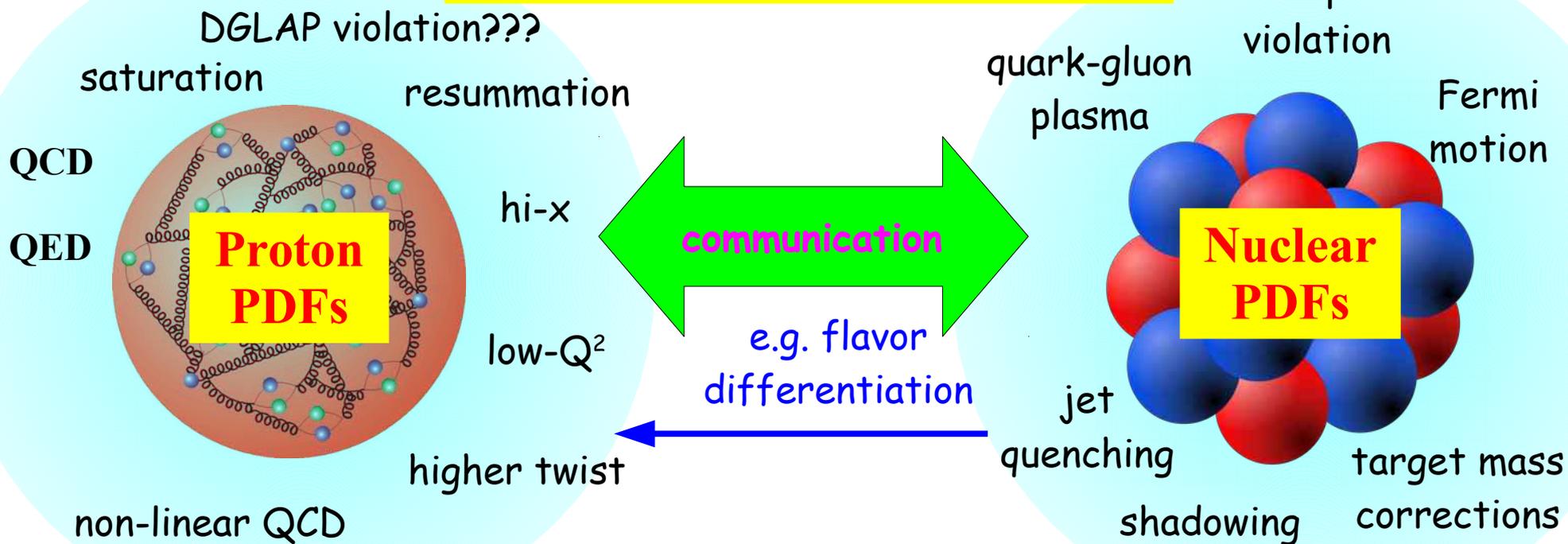


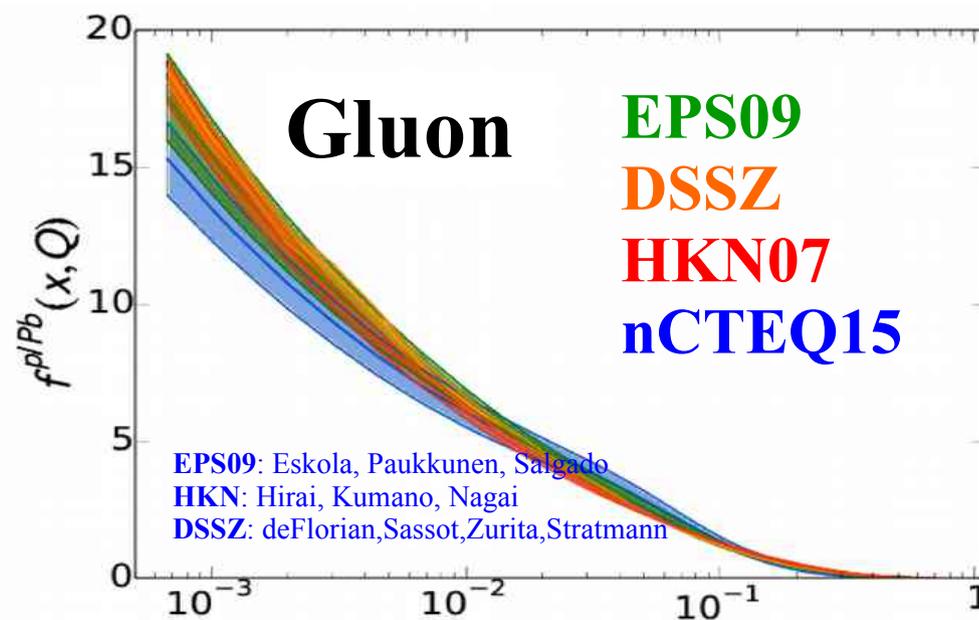
Figure 3.33: The two-particle correlation function in high-multiplicity  $p$ +Pb collisions as a function of  $\Delta\phi$  and  $\Delta\eta$  reported by the CMS collaboration [252]. The 'ridge' structure is seen as a correlation near  $\Delta\phi = 0$  stretching over many units of rapidity  $\Delta\eta$ .

# Conclusion

**“QCD is our most perfect physical theory”**



- 1) Flavor Differentiation & Nuclear Corrections
- 2) Multi-scale problems: Heavy Quarks Resummation
- 3) Hi-Order Corrections



**Lessons: The Nature of Nature ... alien, simple, beautiful, weird, & comprehensible**





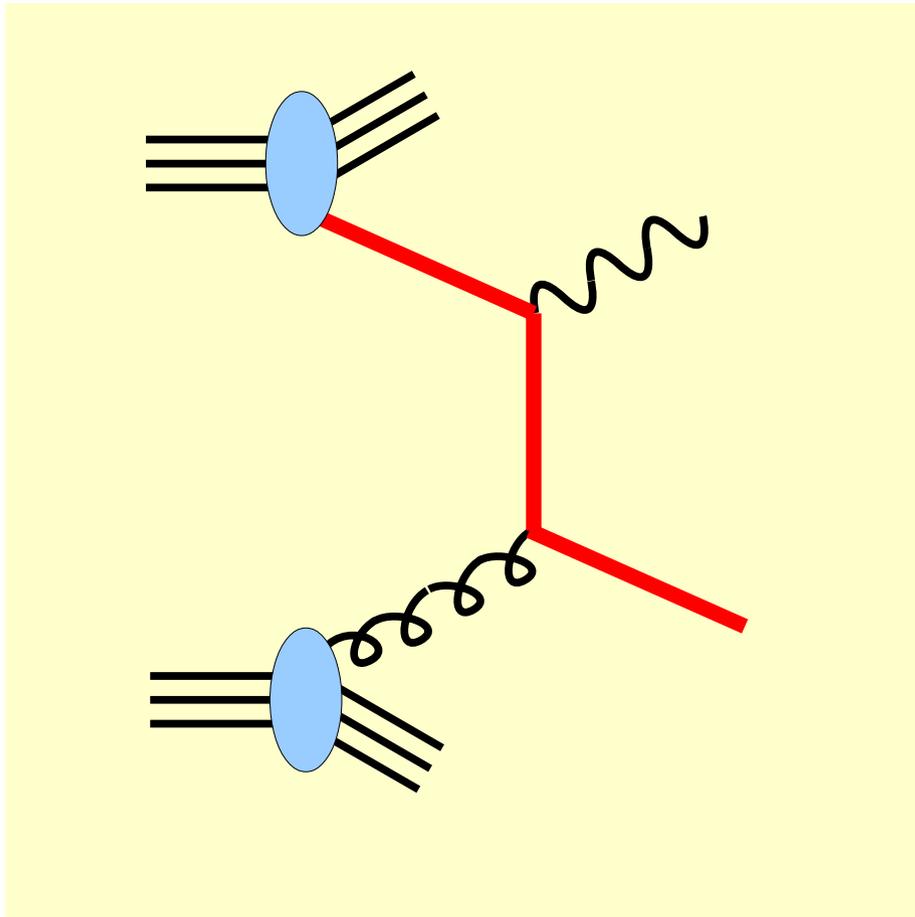
# $W/Z/\gamma$ Production

“Benchmark Calculations”

*... how stable are these*

*... the fine print:*

.....

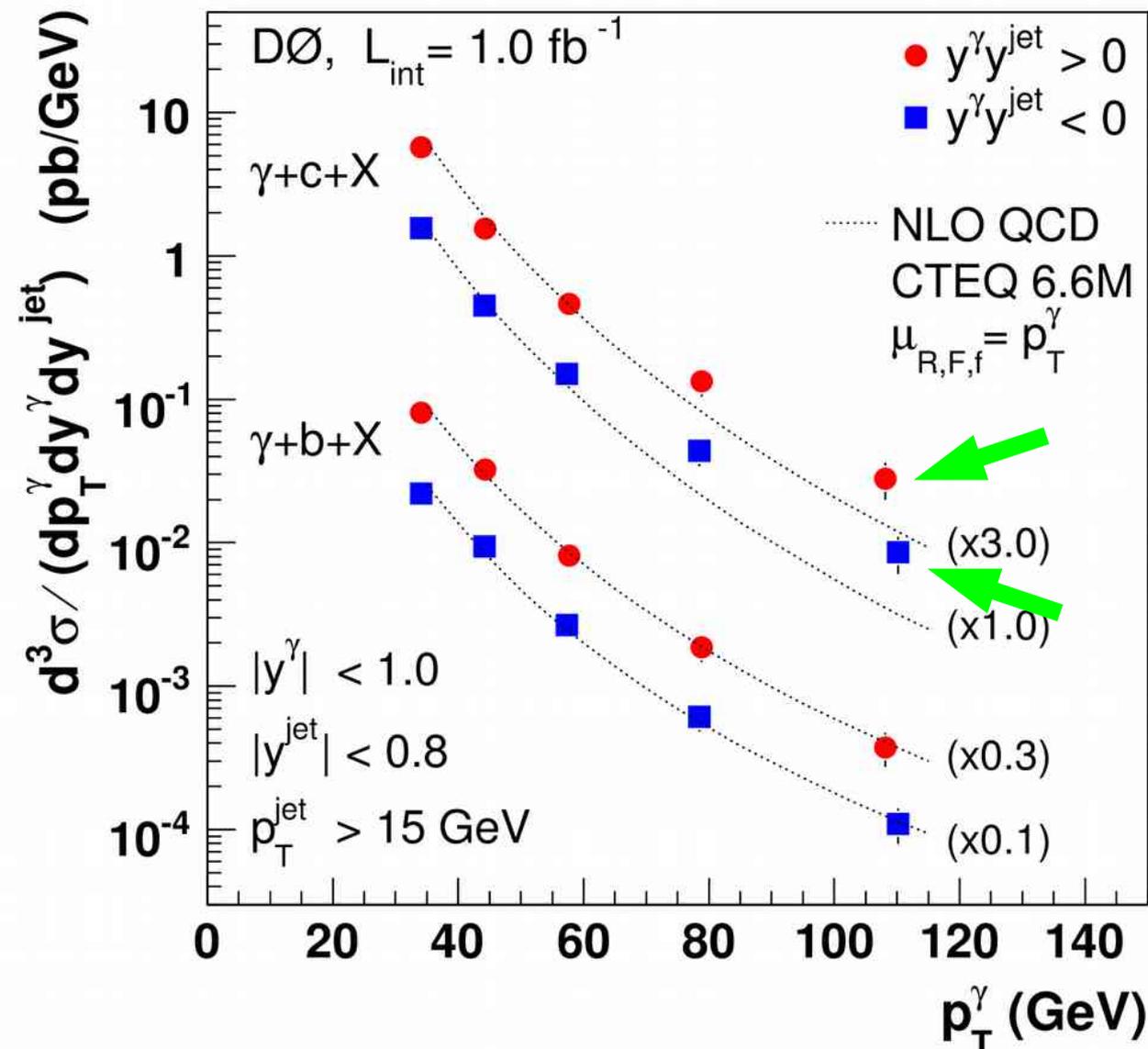


$$c \ g \rightarrow c \ \gamma$$

$$b \ g \rightarrow b \ \gamma$$

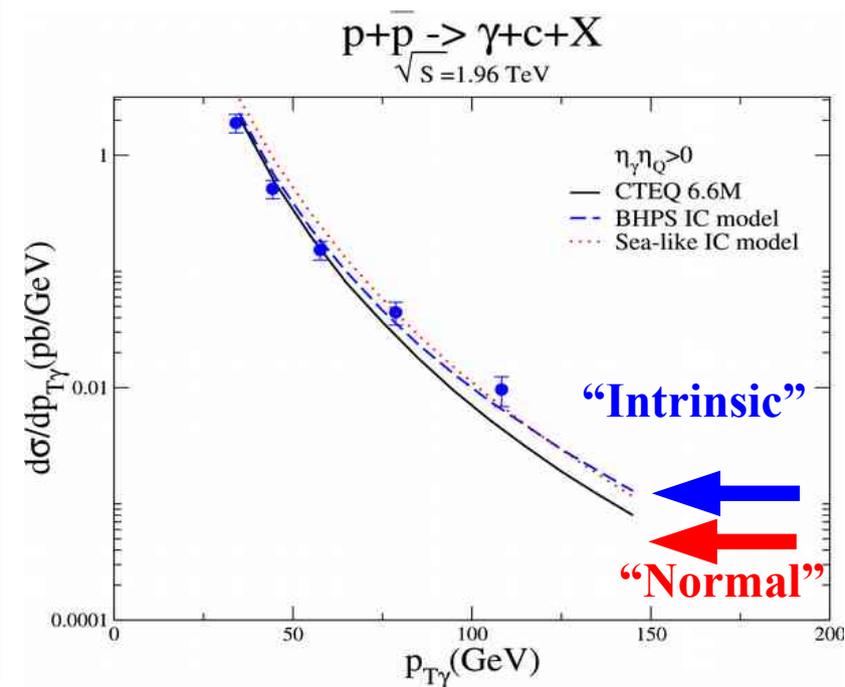
$$s \ g \rightarrow c \ W$$

$$c \ g \rightarrow b \ W$$

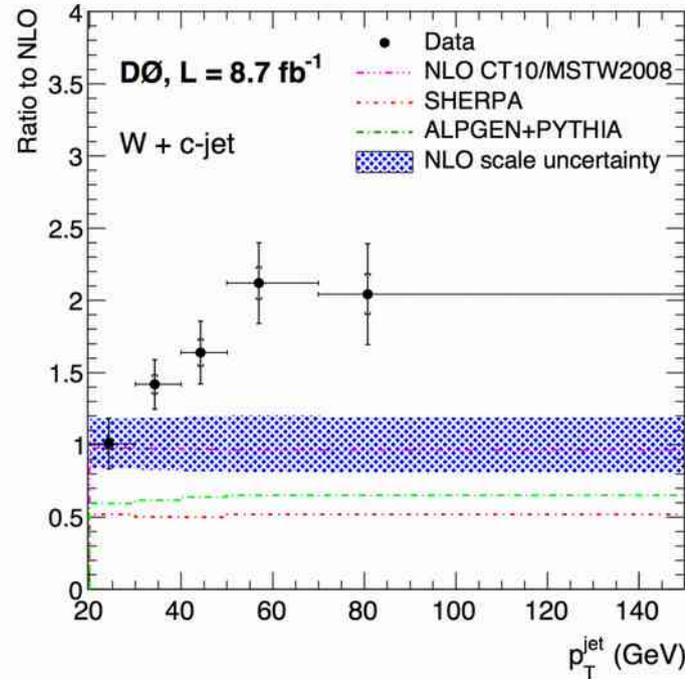
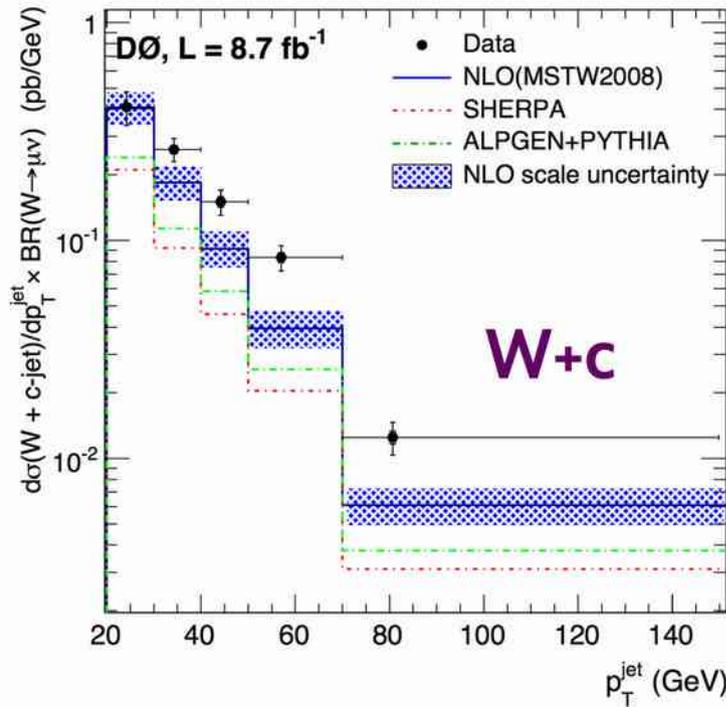


Excess in Charm,  
NOT Bottom

only at high PT



Extracted W+c production rates corrected for efficiency and acceptance:  
4–7% statistical and 12–17% systematic uncertainties, dominantly from c/b-jet ID, selection efficiency, and luminosity



Cross-section compared to predictions from NLO pQCD (corrected for non-perturbative effects), and Sherpa/AlpGen+Pythia MC models.

Unlike W+b, see a clear trend developing to higher jet  $p_T$   
High  $p_T$  range where gluon splitting becomes increasingly important.