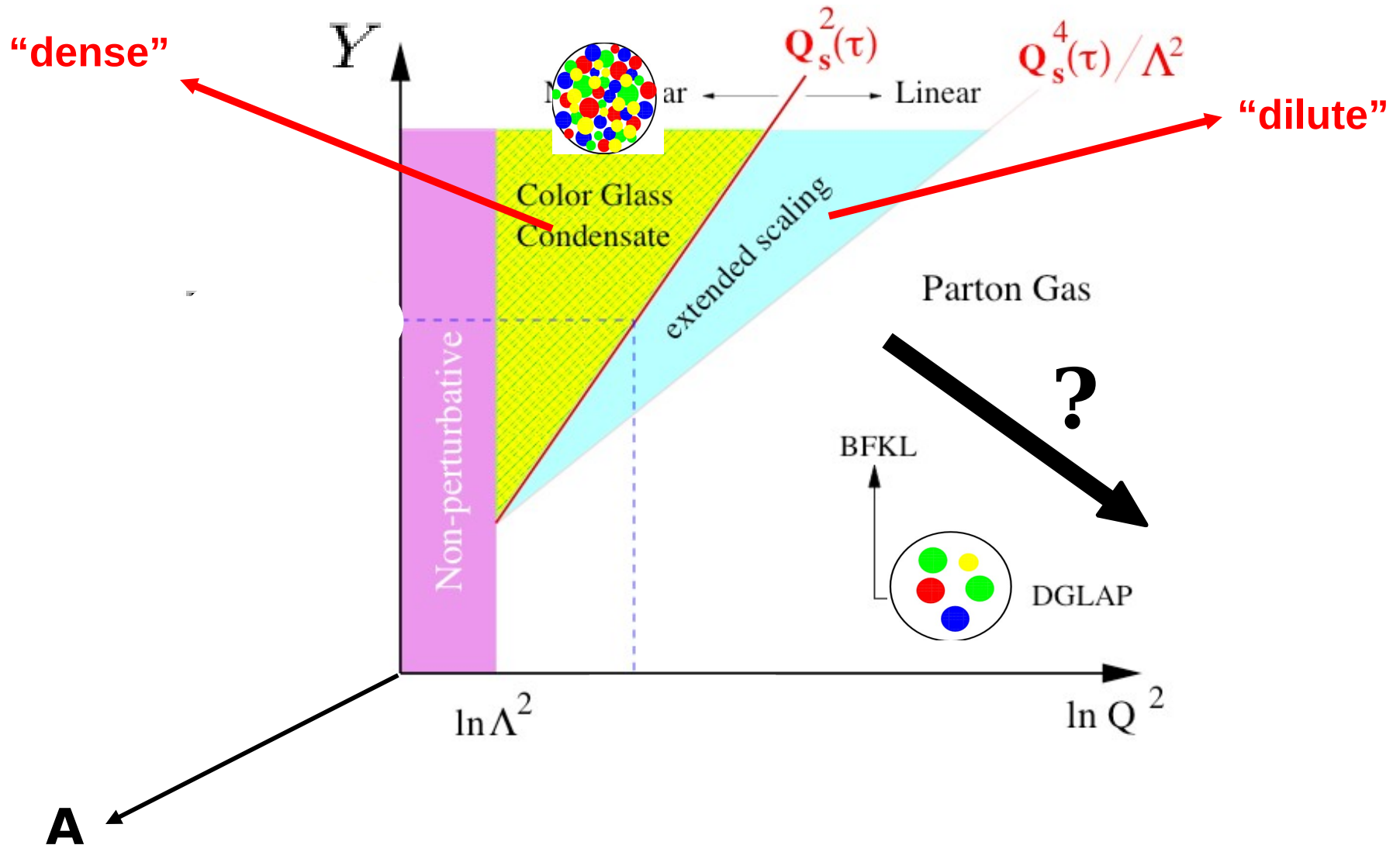


# **LO three-jet and NLO di-jet correlations in DIS at small $x$**

***Jamal Jalilian-Marian  
Baruch College  
New York, NY***

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Ecole Polytechnique, Palaiseau, France***

# Road Map of QCD Phase Space



# ***Probing CGC: observables***

***dense-dense (AA, pA, pp) collisions***

***dilute-dense (pA, forward pp ) collisions***

***DIS***

*structure functions (diffraction)*

*particle production*

*single inclusive*

***double inclusive***

***triple inclusive***

*related work by:*

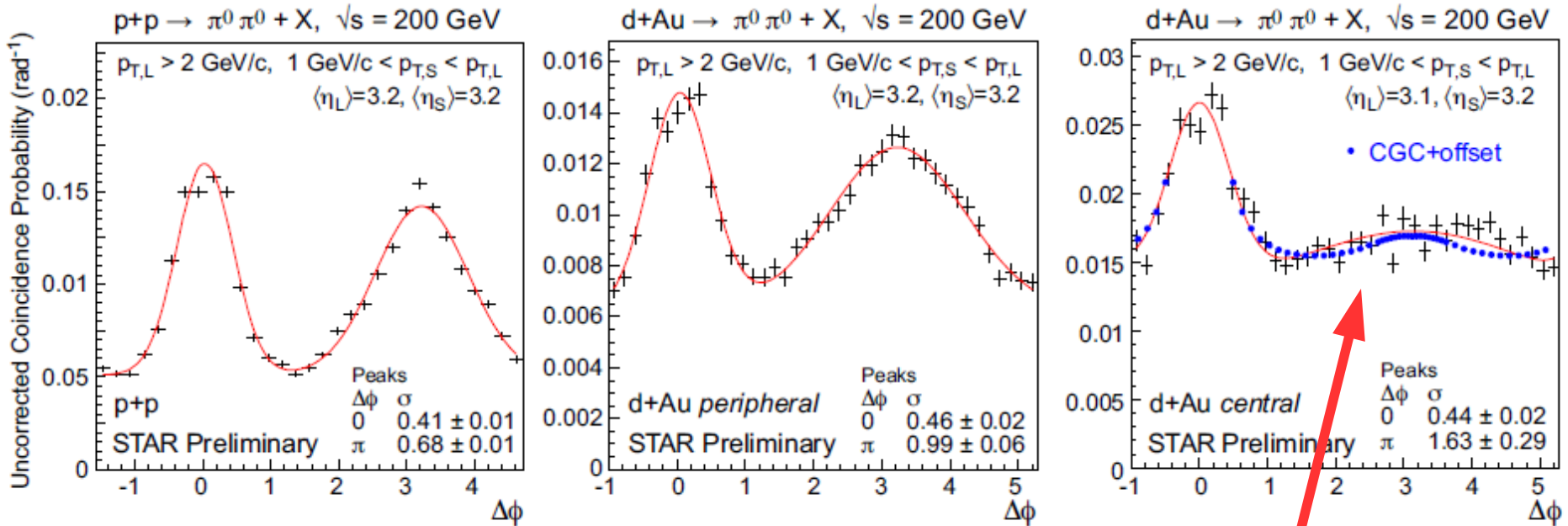
*Boussarie, Grabovsky, Szymanowski, Wallon, JHEP1409, 026 (2014)*

*Balitsky, Chirilli, PRD83 (2011) 031502, PRD88 (2013) 111501*

*Beuf, PRD85, (2012) 034039*

# Azimuthal correlations in pA

Recent STAR measurement (arXiv:1008.3989v1):



Marquet, NPA (2007), Albacete + Marquet, PRL (2010)

Tuchin, NPA846 (2010)

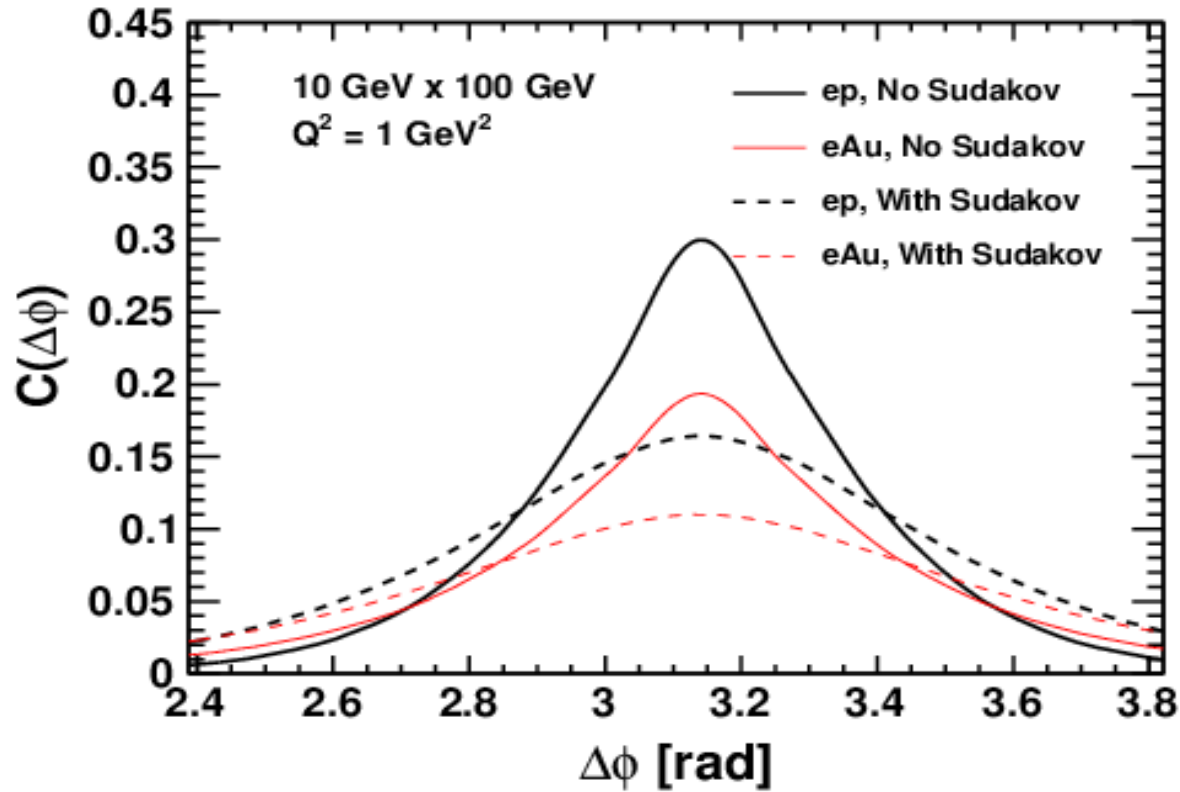
A. Stasto + B-W. Xiao + F. Yuan, PLB716 (2012)

T. Lappi + H. Mantysaari, NPA908 (2013)

**multiple scatterings  
de-correlate  
the hadrons**

shadowing+energy loss: Z. Kang, I. Vitev, H. Xing, PRD85 (2012) 054024

# Azimuthal correlations in DIS



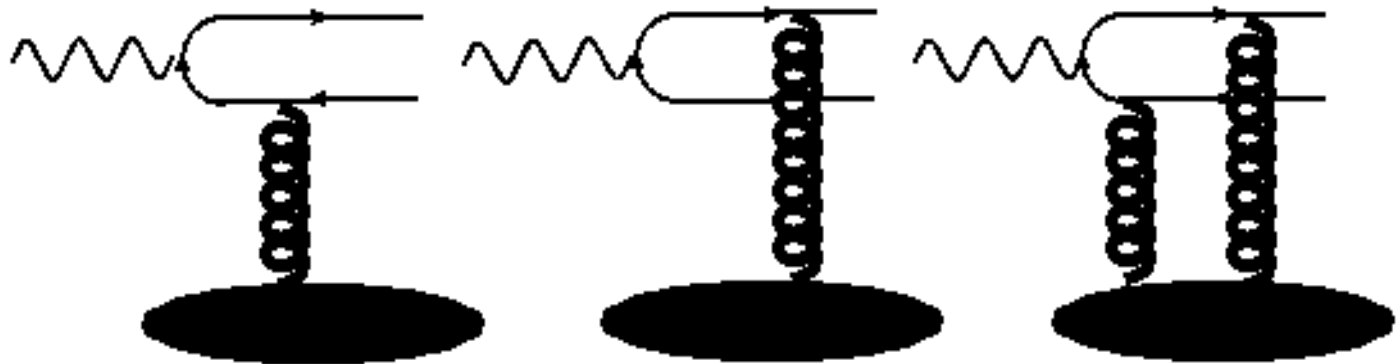
Zheng + Aschenauer + Lee + Xiao, *PRD89* (2014)7, 074037

# Azimuthal correlations in DIS

*DIS total cross section ( $F_L, F_2$ ): dipoles  $\langle \text{Tr } V V^\dagger \rangle$*

*di-jet production in DIS: quadrupoles  $\langle \text{Tr } V V^\dagger V V^\dagger \rangle$*

LO:  $\gamma^* T \rightarrow q \bar{q} X$

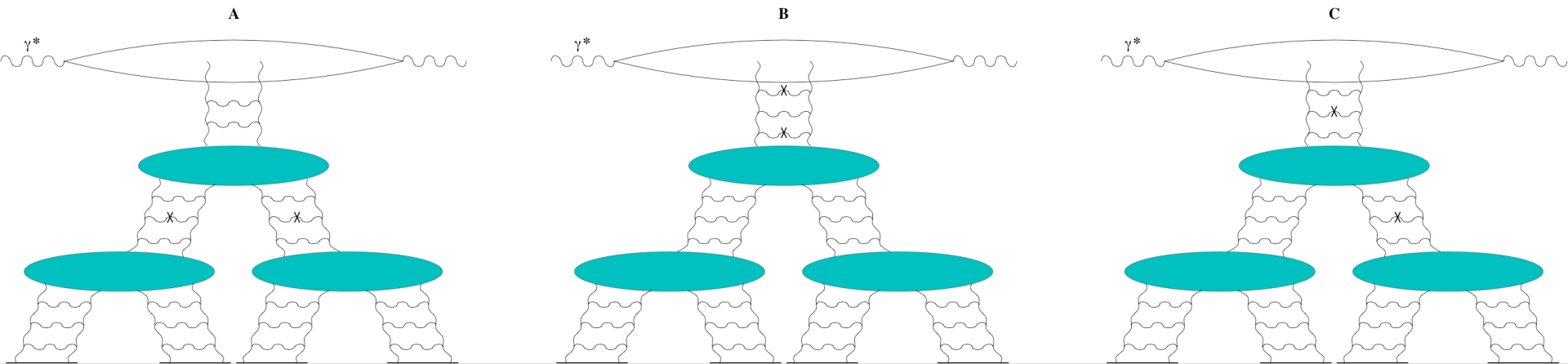


# Azimuthal correlations in DIS

*di-jet production in DIS: quadrupoles*  $\langle \text{Tr } \mathbf{V} \mathbf{V}^\dagger \mathbf{V} \mathbf{V}^\dagger \rangle$

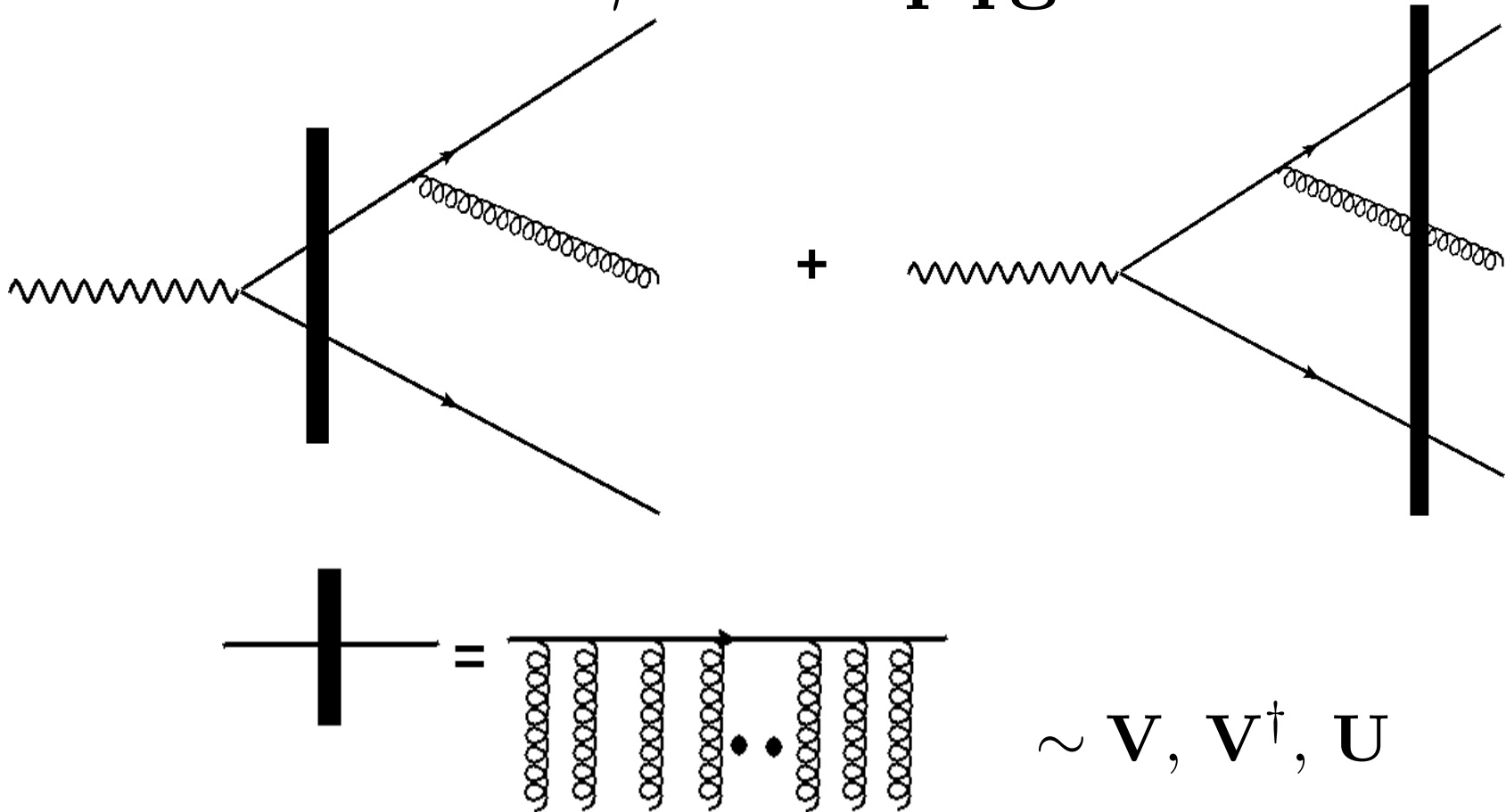
LO:  $\gamma^* \mathbf{T} \rightarrow \mathbf{g} \mathbf{g} \mathbf{X}$  JJM+ Y. Kovchegov, PRD (2004)

*gluons widely separated in rapidity*



# Azimuthal correlations in DIS: 3-jets

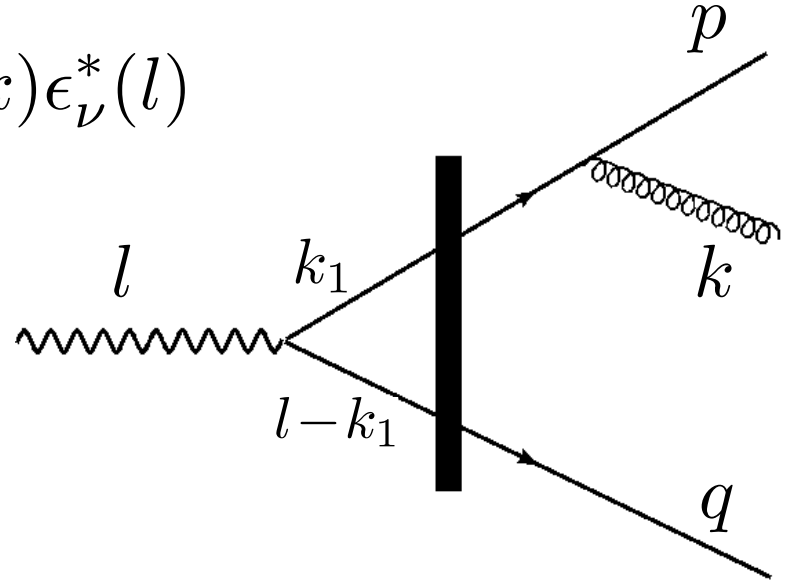
LO:  $\gamma^* T \rightarrow q \bar{q} g X$



*Ayala, Hentschinski, JJM, Tejada-Yeomans, in progress*



$$\mathcal{A} \equiv -eg \bar{u}(p) [A]^{\mu\nu} v(q) \epsilon_\mu(k) \epsilon_\nu^*(l)$$



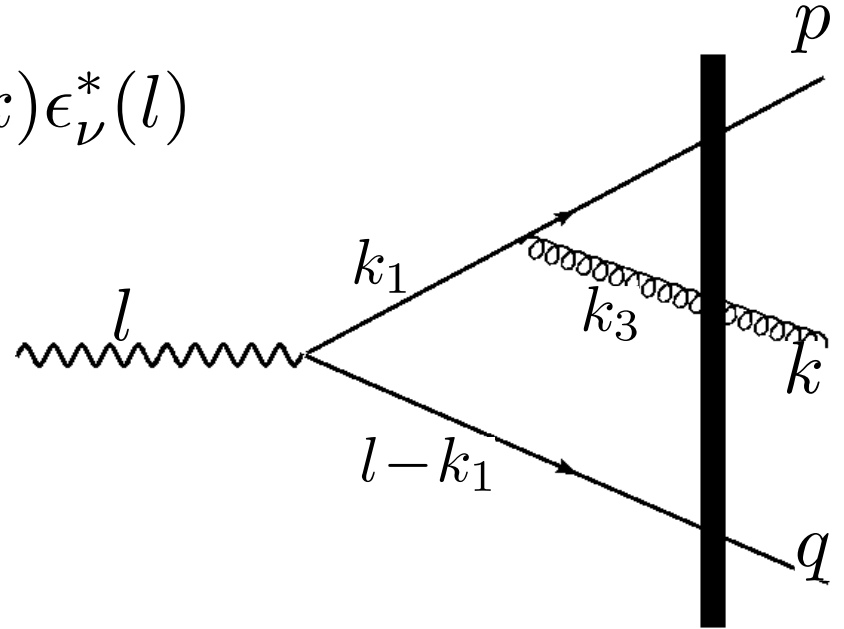
$$A_1^{\mu\nu} = \gamma^\mu t^a S_F^0(p+k) \tau_F(p+k, k_1) S_F^0(k_1) \gamma^\nu S_F^0(l-k_1) \tau_F(l-k_1, q) \frac{d^4 k_1}{(2\pi)^4}$$

with interactions given by

$$\tau_F(p, q) \equiv (2\pi) \delta(p^- - q^-) \gamma^- \int d^2 z_t e^{-i(p_t - q_t) z_t} [\theta(p^-) V(z_t) - \theta(-p^-) V^\dagger(z_t)]$$

integrations can be done and give  $K_0$

$$\mathcal{A} \equiv -eg \bar{u}(p) [A]^{\mu\nu} v(q) \epsilon_\mu(k) \epsilon_\nu^*(l)$$



$$A_2^{\mu\nu} = \tau_F(p, k_1 - k_3) S_F^0(k_1 - k_3) \gamma^\mu t^a S_F^0(k_1) \gamma^\nu S_F^0(l - k_1) \tau_F(l - k_1, q) \\ G_\mu^{0\lambda}(k_3) \tau_g^{ac}(k_3, k) \frac{d^4 k_1}{(2\pi)^4} \frac{d^4 k_3}{(2\pi)^4}$$

all integrations (except one) can be done analytically

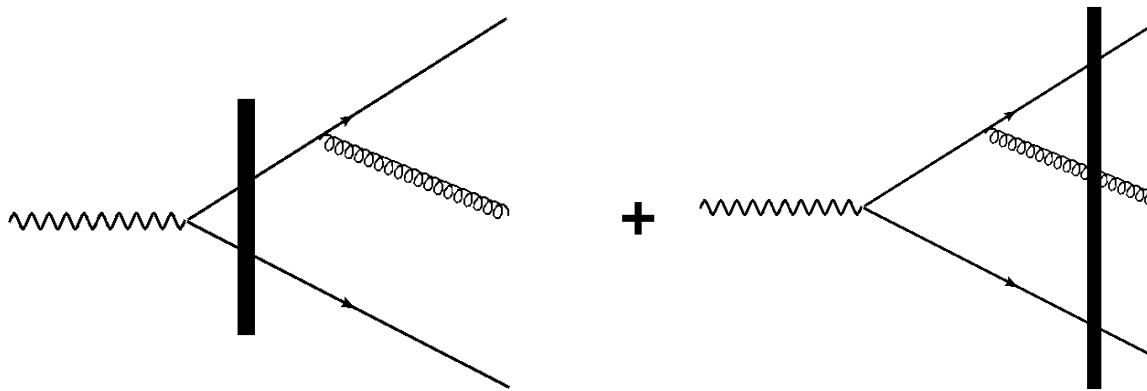
$$A = A_1 + A_2 + \text{radiation from anti-quark}$$

# Azimuthal correlations in DIS

## *di-jet production in DIS: **NLO***

*real contributions:*  $\gamma^* \mathbf{T} \rightarrow q \bar{q} g \mathbf{X}$

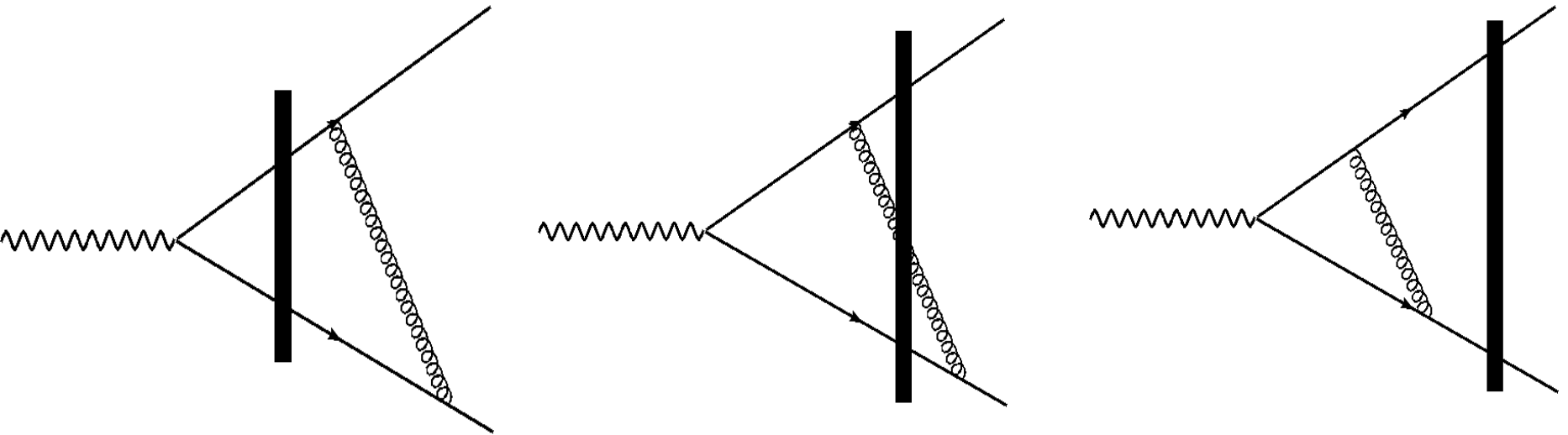
*integrate out one of the produced partons*



*work in progress: Ayala, Hentschinski, Jalilian-Marian, Tejeda-Yeomans*

# di-jet azimuthal correlations in DIS

*virtual contributions:*  $\gamma^* \mathbf{T} \rightarrow q \bar{q} \mathbf{X}$



+ “*self-energy*” diagrams

# di-jet azimuthal correlations in DIS

$$\text{NLO: } \gamma^* \mathbf{T} \rightarrow \mathbf{h h X}$$

*integrate out one of the produced partons - there are divergences:*

*rapidity divergences: JIMWLK evolution of n-point functions*

*colinear divergences: DGLAP evolution of fragmentation functions*

*infrared divergences cancel*

***the finite pieces are written as a factorized cross section***

***work in progress: Ayala, Hentschinski , Jalilian-Marian, Tejeda-Yeomans***

# ***SUMMARY***

***Di-jet angular correlations offer a unique probe of CGC***

***3-hadron/jet correlations should be even more discriminatory***

***Leading Log CGC works (too) well for a qualitative/semi-quantitative description of data, NLO is needed***

***Need to eliminate/minimize late time/hadronization effects***

***an EIC is needed for precision CGC studies***