



# Status and Plan for the Analyses of $t\bar{t}b\bar{b}$ near threshold at the ILC

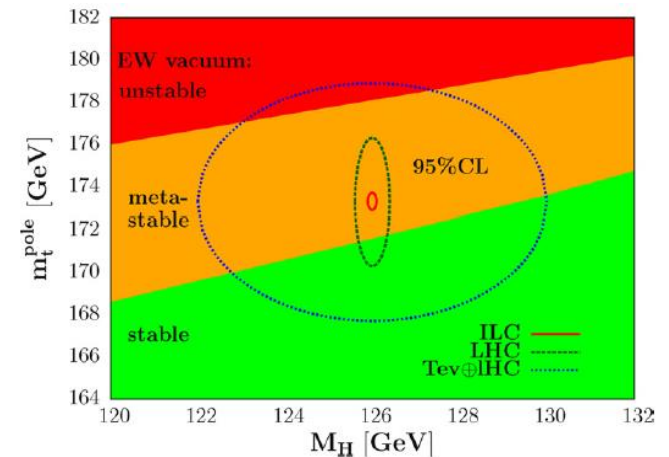
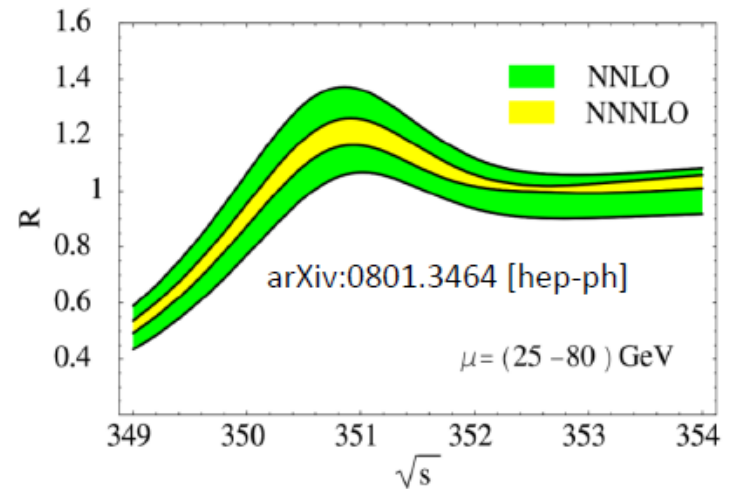
Akimasa Ishikawa  
(Tohoku University)

Top Physics at Lepton Colliders@Valencia (Remote)

*Analysis was done by T. Horiguchi*

# ttbar at threshold

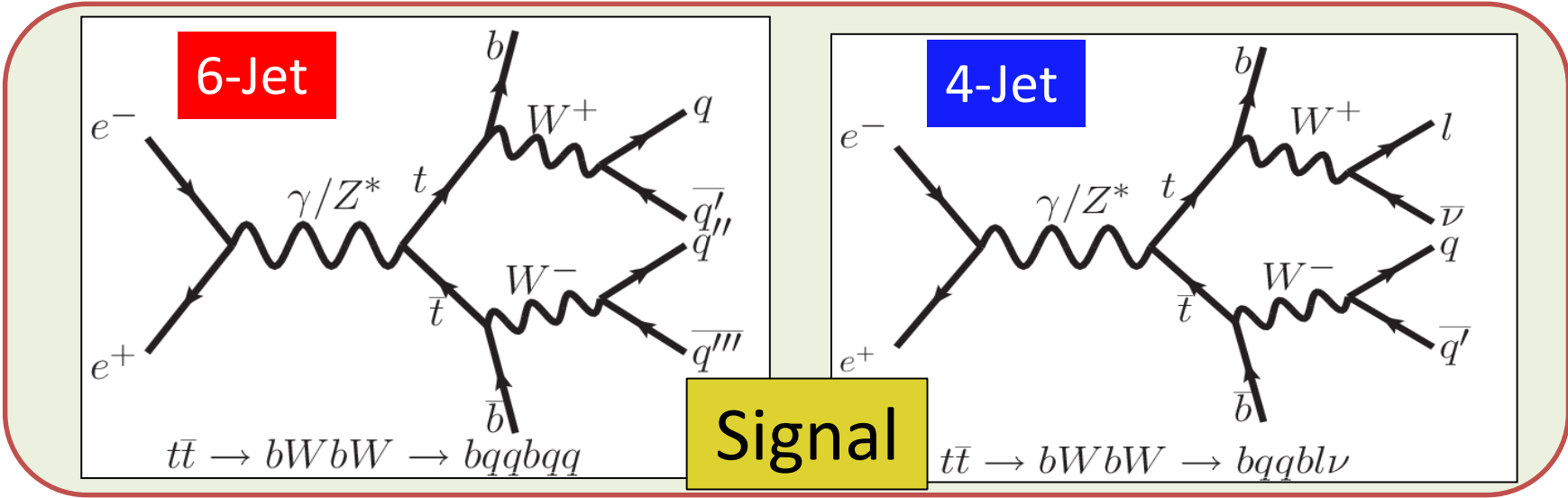
- $\sigma_{tt}$  VS  $\sqrt{s}$  is sensitive to
  - $M_t$ 
    - Theoretically well-defined running mass
    - Vacuum instability in the SM
  - $\Gamma_t$  (or  $V_{tb}$ )
    - Deviated from SM if new physics in decays
  - $y_t$ 
    - Higgs exchange diagram gives 9% enhancement
  - $\alpha_s$ 
    - not yet done
- Fit to  $\sigma_{tt}$  to obtain  $m_t$ ,  $\Gamma_t$  and  $y_t$  simultaneously.



# Simulation Setup for $\sigma_{tt}$

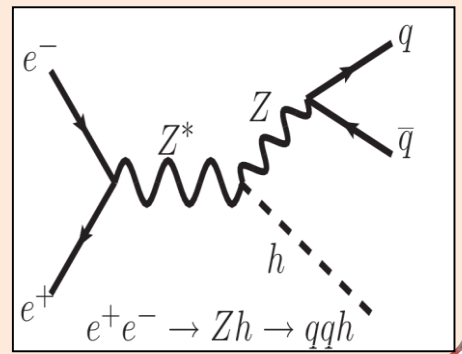
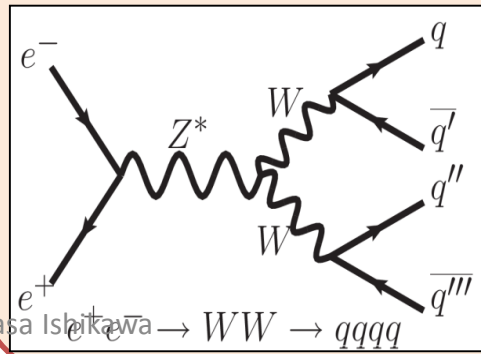
Top quark mass	174 GeV
$\sqrt{s}$ ( <u>threshold scan</u> )	<u>341 - 350 GeV (every 1 GeV, 10 points)</u>
<u>Polarization</u>	$p(e^+, e^-) = (-30\%, +80\%), (+30\%, -80\%)$ (In this talk, I call them “ <b>Right</b> ” and “ <b>Left</b> ”)
Integrated Luminosity	5 fb <sup>-1</sup> (each $\sqrt{s}$ & pol, <b>total 100fb<sup>-1</sup></b> )
Event Generation	Physsim (LO ,QCD enhancement, on ISR/ beamstrahlung/beam energy spread)
Simulation	ILD_01_v05 ( <b>DBD ver.</b> )

# Signal and Backgrounds



**background**

SM bkg. which have 4 or 6 fermions in final state  
Main bkg.: WW, ZZ, ZH



Branching Ratio	
6-Jet	45%
4-Jet	44%
2-Jet	11%

# Reconstruction

Reconstruction method	6-Jet	4-Jet
Isolated Lepton( $l_{iso}$ ) finding using cone energy cut ( $\cos\theta_{cone} > 0.96$ , $P_{track} > 15$ GeV, $E_{cone} < 10$ GeV)	# of $l_{iso} = 0$	# of $l_{iso} = 1$
Jet clustering using Durham algorithm	6jets	4jets
Extraction of 2 b-likeness jets		
Reconstruction of top quark pair and finding the best candidate by $\chi^2$ from invariant mass	(b+q+q') $\times$ 2	(b+q+q') & (b+ $l_{iso}$ +v)

$$\chi_{6-Jet}^2 = \frac{(m_{3j^a \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{3j^b \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{2j^a \text{reco.}} - m_w)^2}{\sigma_w^2} + \frac{(m_{2j^b \text{reco.}} - m_w)^2}{\sigma_w^2}$$

$$\chi_{4-Jet}^2 = \frac{(m_{3j \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{1j \nu \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{2j \text{reco.}} - m_w)^2}{\sigma_w^2}$$

# Cut-flow for 350GeV

Table : 6-Jet Left handed

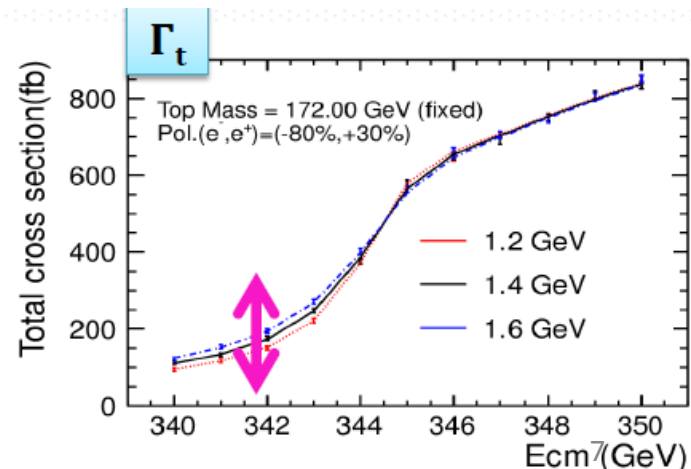
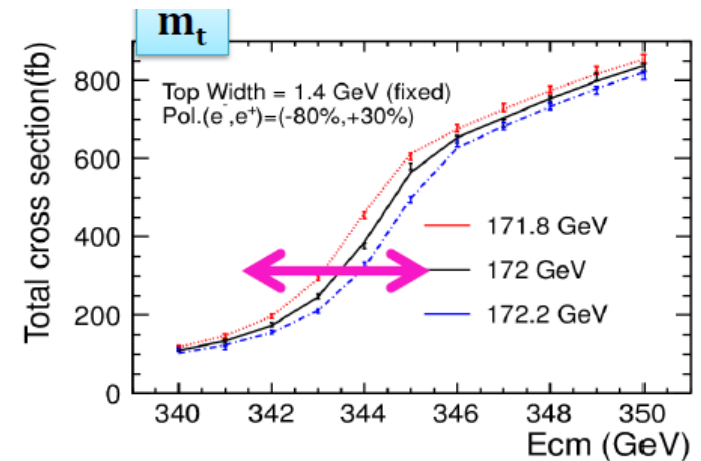
$$\int \mathcal{L}(t)dt = 5(\text{fb}^{-1}) \quad S = \frac{N_{Sig}}{\sqrt{N_{Sig} + N_{BG.}}}$$

<b>(e+,e-)=(+30,-80%)</b>	<b>tt6j</b>	<b>tt4j</b>	<b>tt2j</b>	<b>SM bkg.</b>	<b>S<sub>6j</sub></b>	<b>ε<sub>6j</sub></b>
<b>Generated</b>	1643	1583	381	0.13M	4.4	100
# of lepton = 0	1590	353	18	0.11M	5.0	96.8
btag > 0.09 × 2	1499	330	17	19336	10.3	91.2
Thrust<0.825	1439	285	11	2447	22.3	87.6
Evis>300 GeV	1424	61	0	1092	28.0	86.6
m <sub>t</sub> >107 GeV × 2	1383	37	0	492	31.6	84.1
# of pfos>84	1376	33	0	442	32.0	83.8
y <sub>45</sub> > 0.0012						
y <sub>56</sub> >0.0006	1362	31	0	392	32.2	82.9
<b>Sphericity&gt;0.22</b>	<b>1347</b>	<b>24</b>	<b>0</b>	<b>329</b>	<b>32.7</b>	<b>82.0</b>

<b>vs=350 GeV</b>	<b>S<sub>n-Jet</sub></b>	<b>ε<sub>n-Jet</sub></b>
6-Jet (e+,e-)=(-30, +80%)	23.5	84.6
4-Jet (e+,e-)=(+30, -80%)	31.0	66.3
4-Jet (e+,e-)=(-30, +80%)	21.9	68.2

# Fitting with templates

- fit to  $\sigma_{tt}$  with template to extract three variables,  $m_t$ ,  $\Gamma_t$  and  $y_t$  simultaneously.
  - Two dimensional template ( $m_t$ ,  $\Gamma_t$ )
  - $y_t$  from normalization
  - $\alpha_s$  is fixed at 0.12
- Template is made from
  - Theoretical  $\sigma_{tt}(s)$  from Y. Kiyo-san (NLO calc)
  - Efficiency from Physsim (LO) and DBD setup



# Results

Stat. Error ( $m_t, \Gamma_t$ :MeV/ $y_t$ :%)	6-Jet			4-Jet		
	$m_t^{\text{PS}}$	$\Gamma_t$	$y_t$	$m_t^{\text{PS}}$	$\Gamma_t$	$y_t$
Left(50fb <sup>-1</sup> )	47	65	9.6	52	71	11
Right(50fb <sup>-1</sup> )	68	94	14	75	106	16
Left (50fb <sup>-1</sup> ) + Right(50fb <sup>-1</sup> )	<b>39</b>	<b>53</b>	<b>7.9</b>	<b>43</b>	<b>59</b>	<b>9.1</b>

## Combined ALL

$m_t^{\text{PS}}$ (GeV)	$\Gamma_t$ (GeV)	$y_t$
$172 \pm 0.029$	$1.4 \pm 0.039$	<b>5.9 %</b>

- Error estimated in arXiv:1310.0563 is wrong and should be replaced to above.
- $y_t$  uncertainty from theory (error on total cross section  $\sim 4\%$ ) is 22%
  - M. Beneke et al pointed out in Arxiv.1506.06865, that 4.2% error is not likely and we fully agree (and we did not say the error is determined only from exp. stat.). Theoretical uncertainty should be reduced if we want to observe Higgs exchange effect with  $5\sigma$ .
- Uncertainty from luminosity spectrum to be estimated.



# Comparison with (2+1) and 3

- (2+1) par fit :  $m_t$  and  $\Gamma_t$  simultaneously.  $y_t$  from normalization
- 3 par fit : all simultaneously
- Mt worse than (2+1) fit
- Simultaneous fit gives correct error matrix

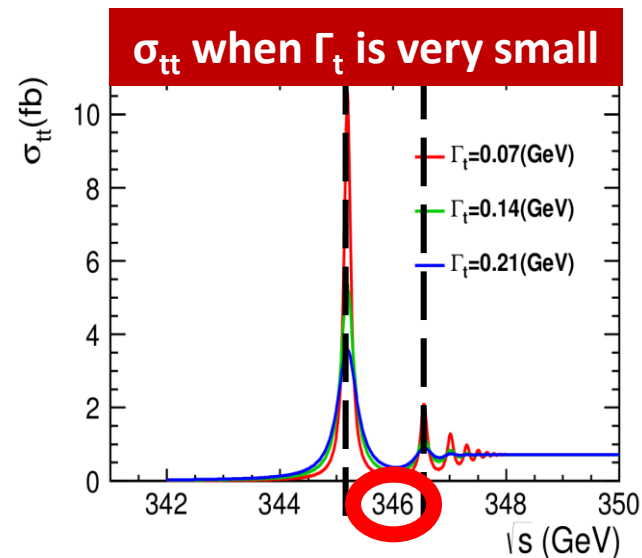
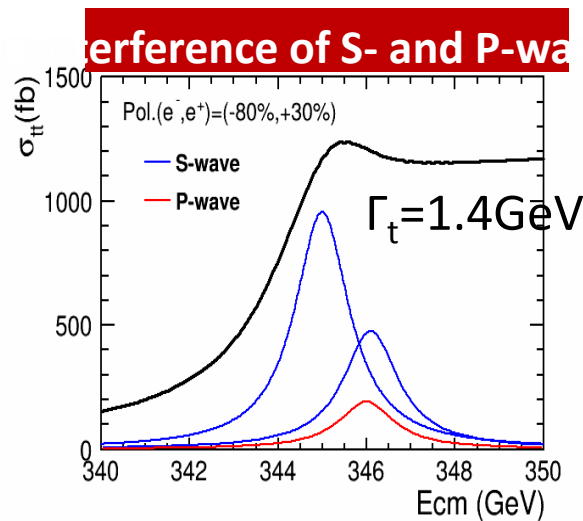
error	(2 + 1) param fit	3 param fit
$m_t$	19 MeV	29 MeV
$\Gamma_t$	38 MeV	39 MeV
$y_t$	4.6%	5.9%

Correlation	(2 + 1) param fit	3 param fit
$m_t$ vs $\Gamma_t$	0.52	0.57
$m_t$ vs $y_t$	-	0.72
$\Gamma_t$ vs $y_t$	-	0.33

A<sub>FB</sub>

# Forward-Backward Asymmetry

- From S and P waves interference,  $A_{FB}$  is generated at threshold which is sensitive to  $\Gamma_t$  and  $\alpha_s$  which control the overlap of S and P waves.



- To identify the charge, 4jets+lepton mode is used.
- We choose the  $\sqrt{s} = 346 \text{ GeV}$  which gives the maximum interference

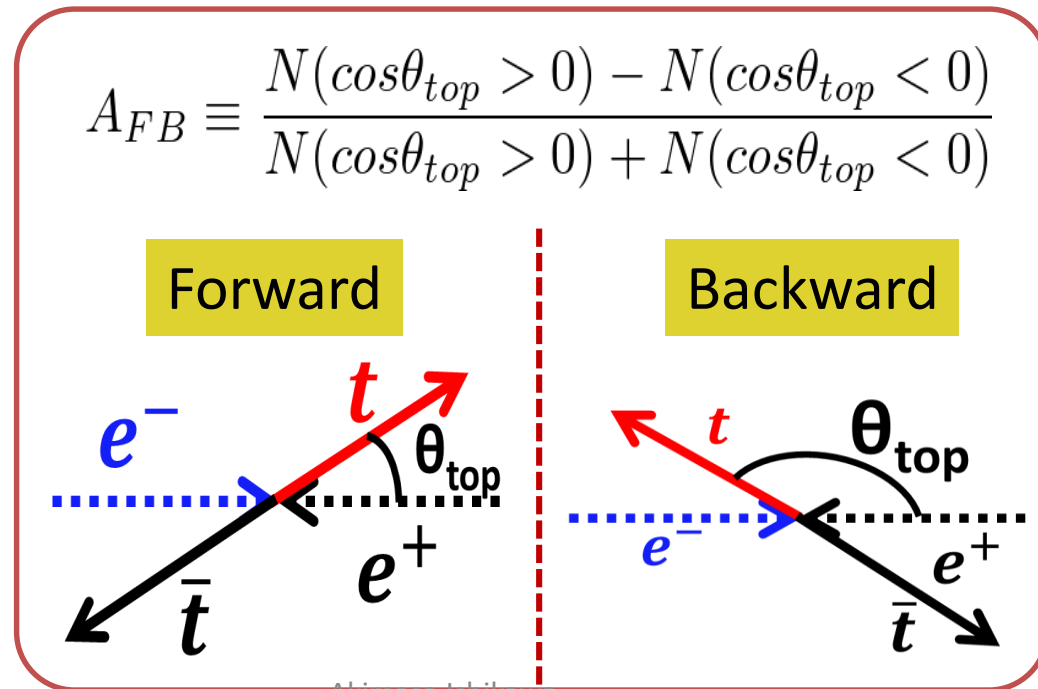
# Setup

$\sqrt{s} = 346 \text{ GeV}$  (between S- and P- wave)

$\mathcal{L} = 50 \text{ fb}^{-1}$  ( $e^+, e^-$ ) = (+0.3, -0.8)

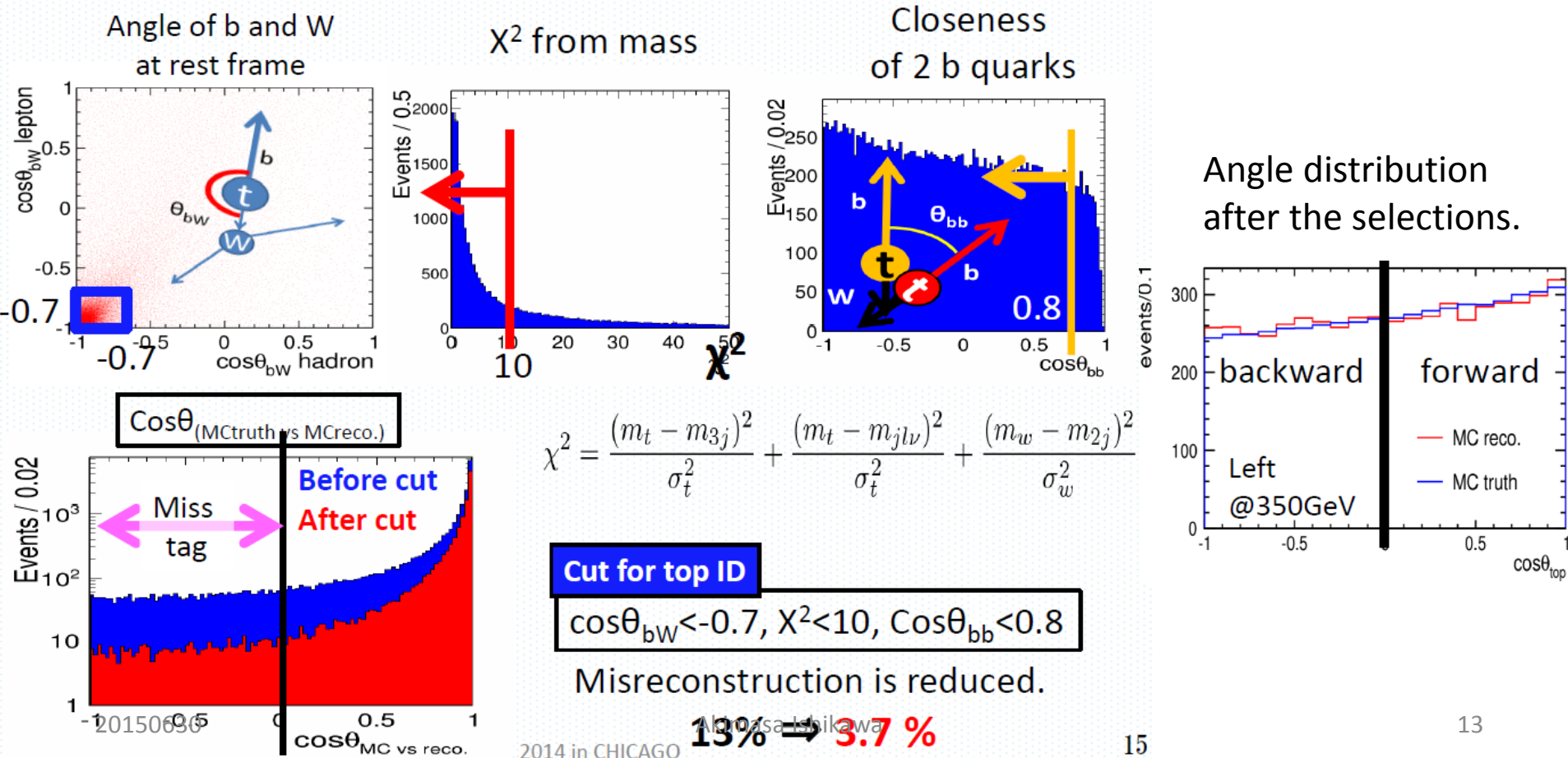
$\mathcal{L} = 50 \text{ fb}^{-1}$  ( $e^+, e^-$ ) = (-0.3, +0.8)

$$A_{FB} \equiv \frac{N(\cos\theta_{top} > 0) - N(\cos\theta_{top} < 0)}{N(\cos\theta_{top} > 0) + N(\cos\theta_{top} < 0)}$$



# Reconstruction

- To get correct combination, several selections are applied.
- 38% efficiency

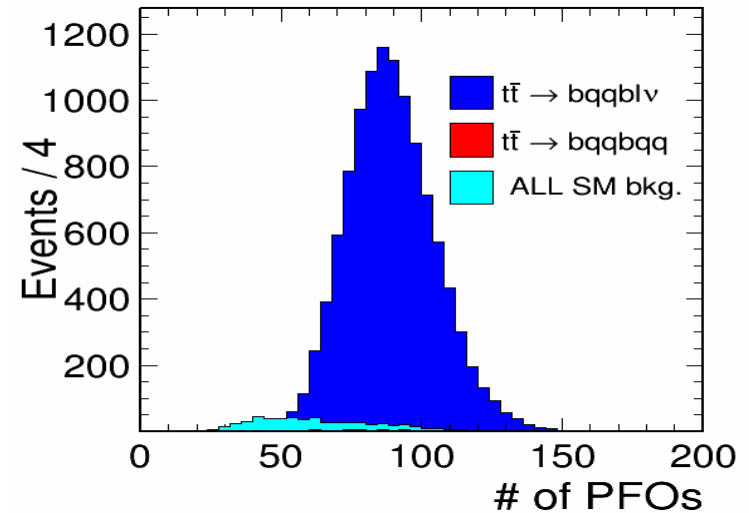


# Cut flow tables

- To maximize the significance ( $S_{top}$ ), bkg. are rejected.

$$S_{top} = \frac{N_{signal}}{\sqrt{N_{signal} + N_{bkg.}}}$$

- # of PFOs is used except top tagging cut (previous page).



Left 50fb <sup>-1</sup>	tt4j	tt6j	tt2j	SM bkg.	$S_{top}$	Efficiency
Gen.	12619	13101	3039	1 M	12.2	100
# of $l_{iso} = 1$	9648	418	909	0.3M	16.9	76.5
$\cos\theta_{bW} < -0.7$	8989	397	834	0.2M	18.4	71.2
$\chi^2 < 10$	6856	65	164	13134	48.2	54.3
$\cos\theta_{bb} < 0.8$	4881	3	6	271	67.9	38.7
# of PFOs > 50	4872	3	4	182	<b>68.5</b>	<b>38.6</b>

# Results

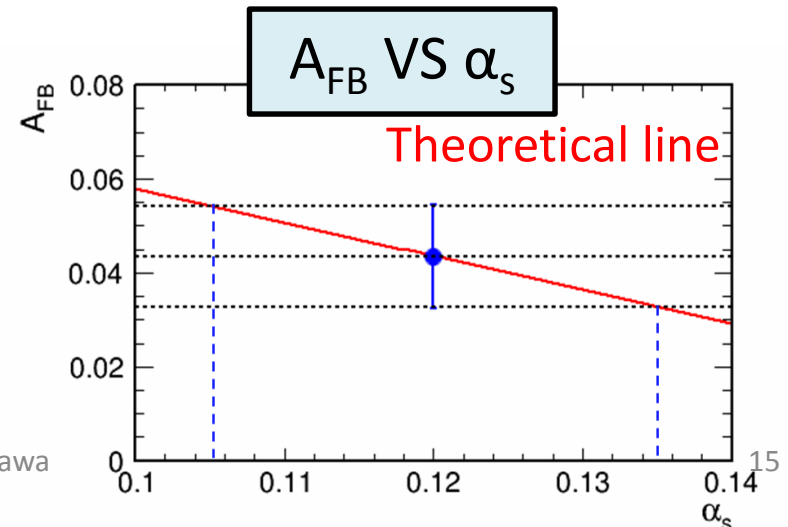
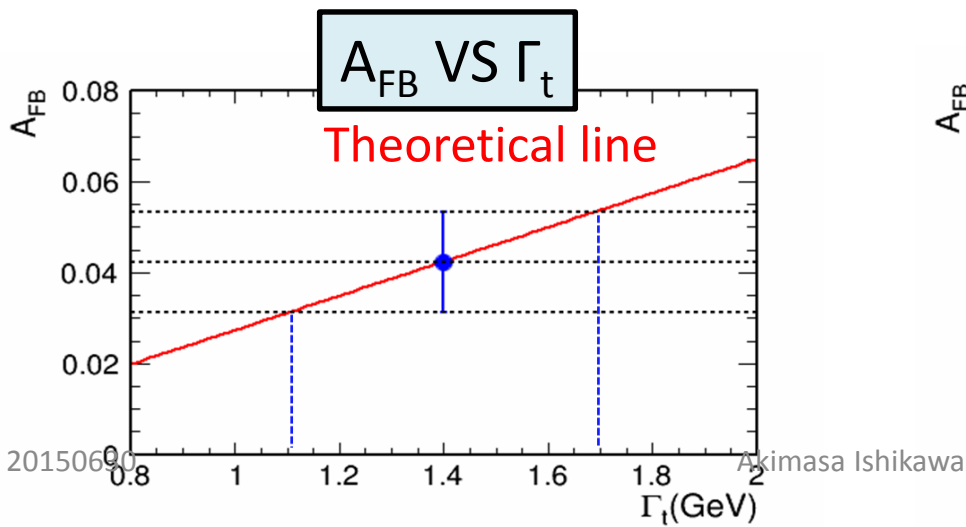
- From the  $1\sigma$  error of  $A_{\text{FB}}$ , we estimated statistical errors of  $\Gamma_t$  and  $\alpha_s$ .

- $-\ \delta\Gamma_t = 290 \text{ MeV}$

- $-\ \delta\alpha_s = 0.015$

- Input  $A_{\text{FB}} = 0.0427$

50 fb <sup>-1</sup>	# of events (NNLO)	$\delta A_{\text{FB}}$
Left handed	5537	0.013
Right handed	2564	0.020
Left + Right (100 fb <sup>-1</sup> )	8101	0.011



# Summary

- We measured  $m_t$ ,  $\Gamma_t$  and  $y_\tau$  from cross section VS  $\sqrt{s}$ 
  - $\delta m_t = 29\text{MeV}$
  - $\delta \Gamma_t = 39\text{MeV}$
  - $\delta y_\tau = 5.9\%$
- We also measured AFB to extract  $\alpha_s$  and  $\Gamma_t$ 
  - $\delta \Gamma_t = 290\text{MeV}$
  - $\delta \alpha_s = 0.015$  (not so sensitive)
  - We need some improvement



# Plan

- Publication. Horiguchi is preparing the paper draft.
- New student Ozawa will study
  - Top momentum (to measure  $\Gamma_t$  and  $\alpha_s$ )
  - Systematic error from beam spectrum
    - Which is also important for  $\sigma_{ZH}$ ,  $m_H$  (and  $m_W$ ) measurement.
  - Perform combined fit to  $\sigma_{tt}$ ,  $A_{FB}$  and top momentum simultaneously to extract four parameters :  $M_t$ ,  $\Gamma_t$ ,  $Y_t$  and  $\alpha_s$ 
    - But  $\alpha_s$  can be measured precisely from other measurements?
- Coupling measurements
  - Angular analysis with polarized beam

# backup