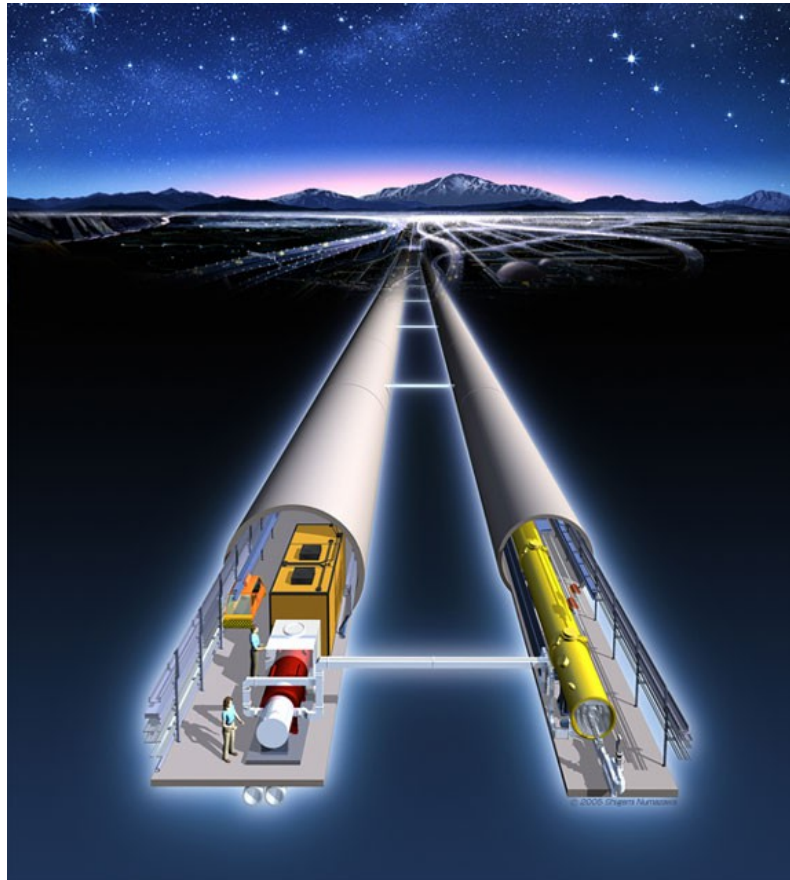


Top electroweak couplings at Linear Colliders



Roman Pöschl

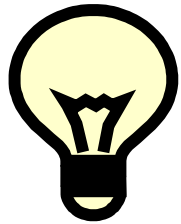
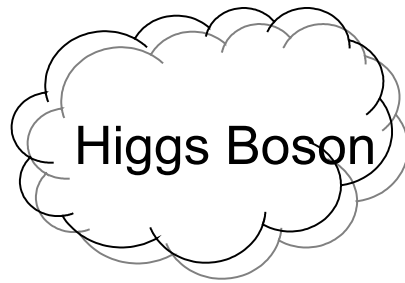


On behalf of

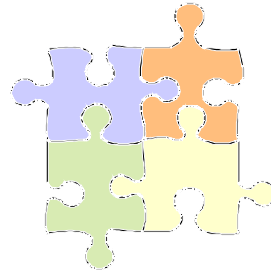


... and the ILD Detector Concept

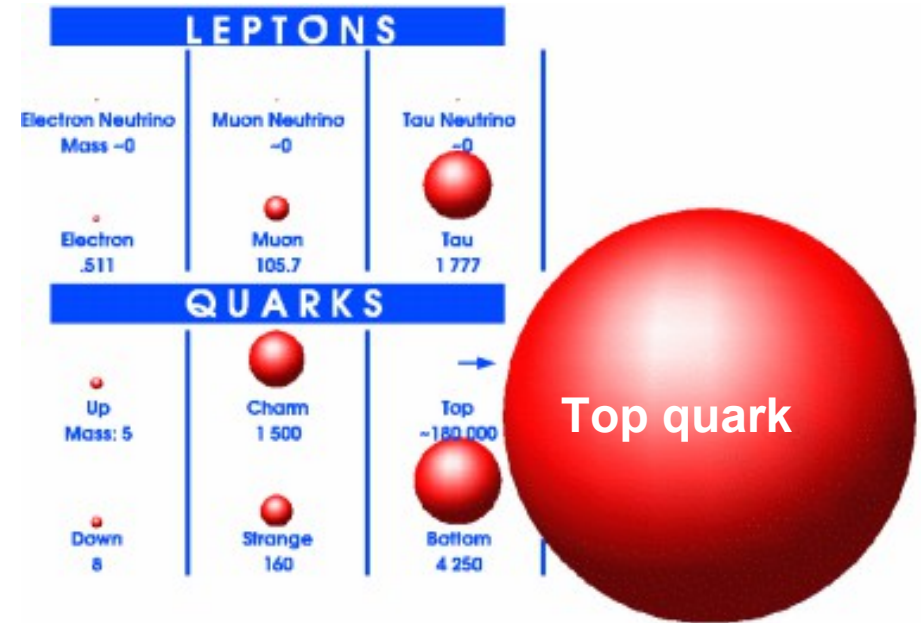
Top@LC15 – Valencia/Spain July 2015



Elementary Scalar?



Composite object?



- Higgs and top quark are intimately coupled!

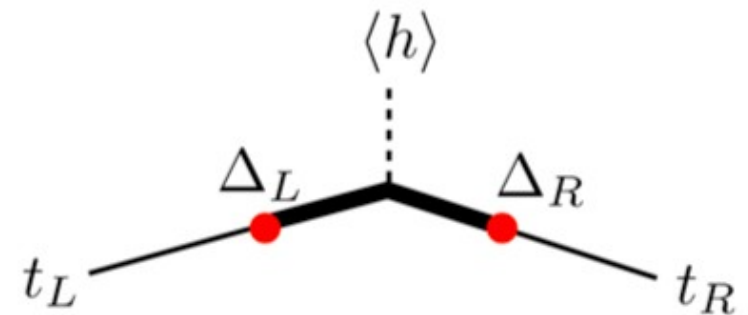
Top Yukawa coupling $O(1)$!

=> Top mass important SM Parameter

- New physics by compositeness?

Higgs and top composite objects?

- LC perfectly suited to decipher both particles



Courtesy of S. Rychkov

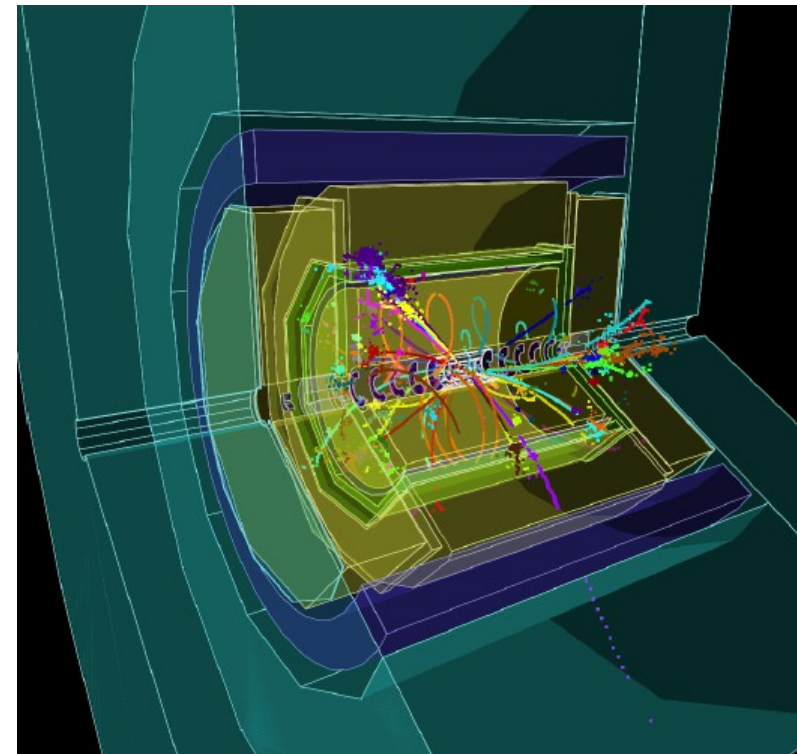
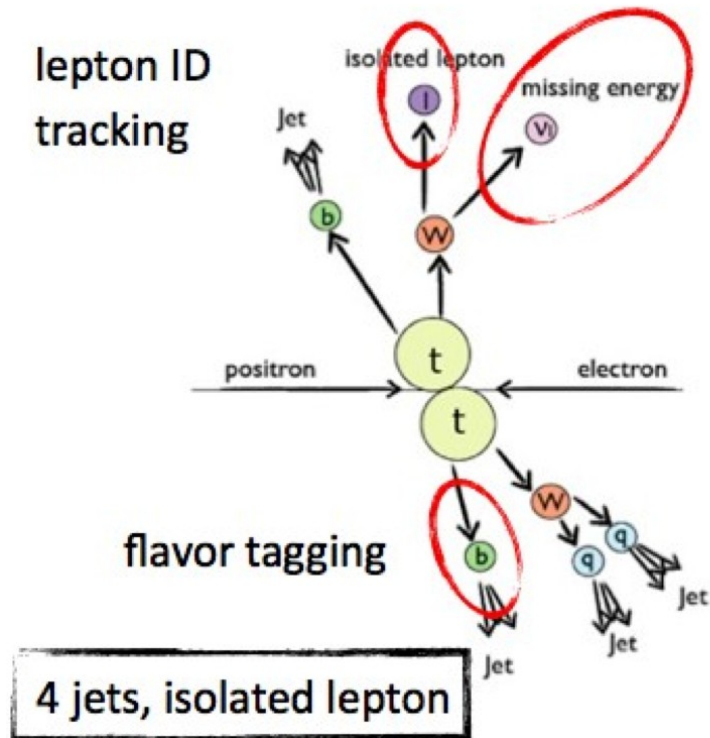
Three different final states:

1) Fully hadronic (46.2%) → 6 jets

2) Semi leptonic (43.5%) → 4 jets + 1 charged lepton and a neutrino

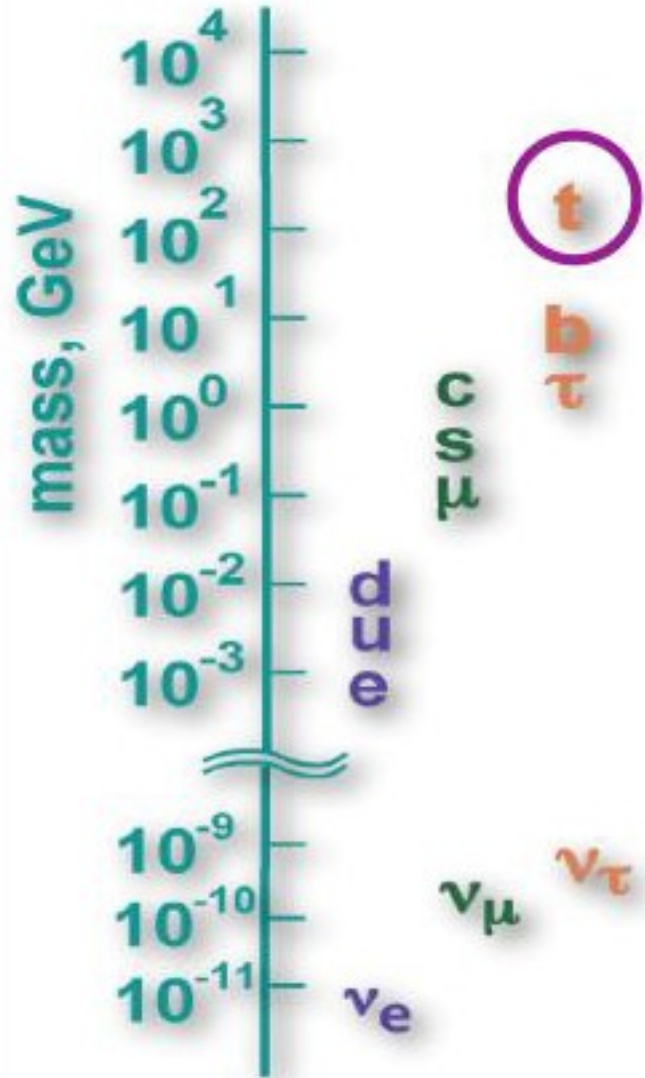
3) Fully leptonic (10.3%) → 2 jets + 4 leptons

$$t\bar{t} \rightarrow (bW)(bW) \rightarrow (bqq')(bl\nu)$$



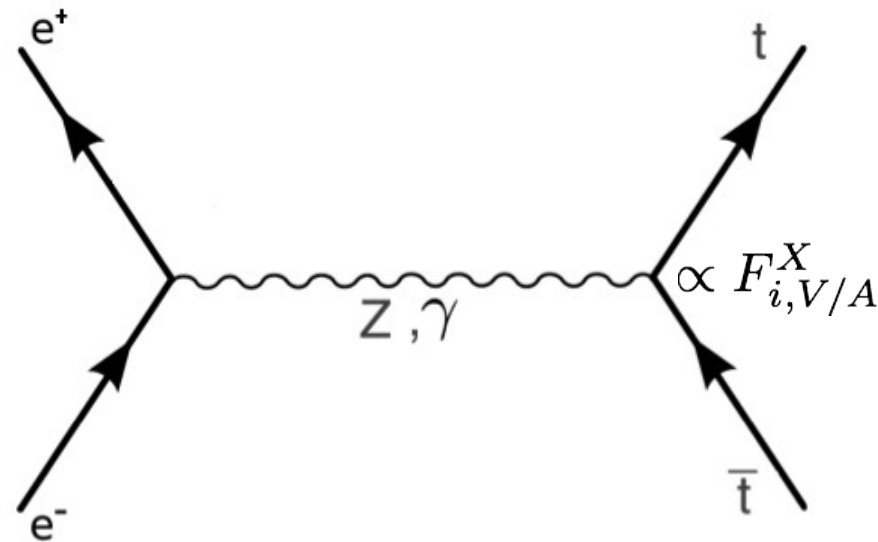
Final state reconstruction uses all detector aspects

Results shown in the following are based on full simulation of ILD Detector at $\sqrt{s} = 500 \text{ GeV}$



- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale
 - A_{FB} anomaly at LEP for b quark

Strong motivation to study chiral structure of top vertex in high energy e⁺e⁻ collisions



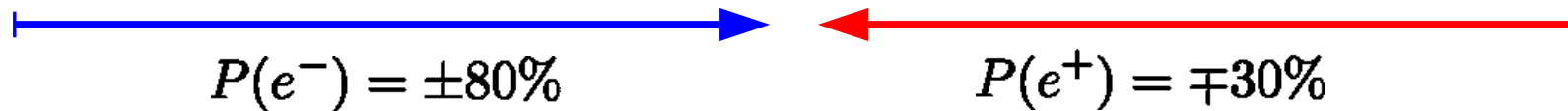
$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\}, \quad (2)$$

Pure γ or pure Z^0 : $\sigma \sim (F_i)^2 \Rightarrow$ No sensitivity to sign of Form Factors

Z^0/γ interference : $\sigma \sim (F_i) \Rightarrow$ Sensitivity to sign of Form Factors

At ILC **no** separate access to ttZ or $t\bar{t}\gamma$ vertex, but ...

ILC 'provides' two beam polarisations



There exist a number of observables sensitive to chiral structure, e.g.

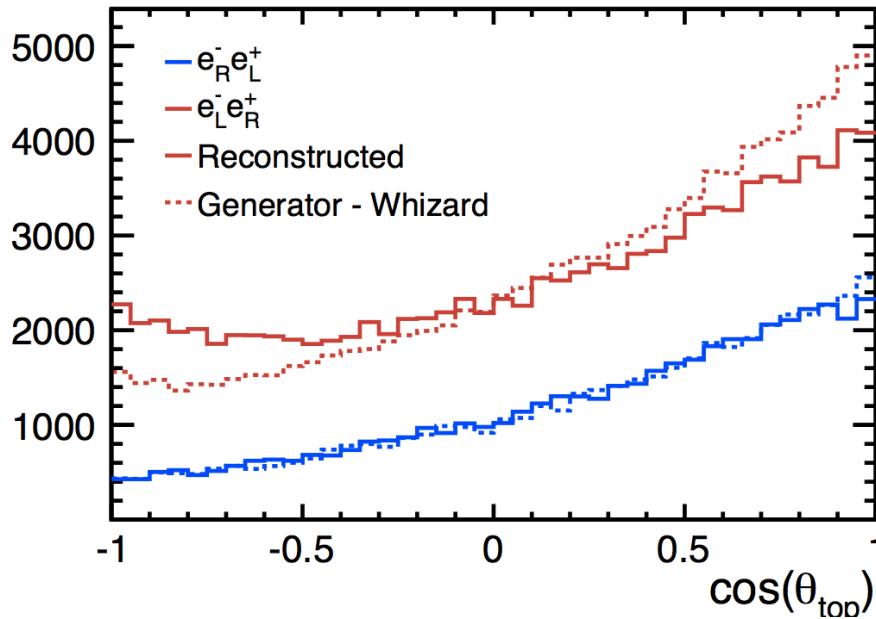
σ_I	$A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$	$(F_R)_I = \frac{(\sigma_R)_I}{\sigma_I}$
x-section	Forward backward asymmetry	Fraction of right handed top quarks



Extraction of relevant unknowns

$$F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \quad \text{or equivalently} \quad g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

$$F_{2V}^\gamma, F_{2V}^Z$$



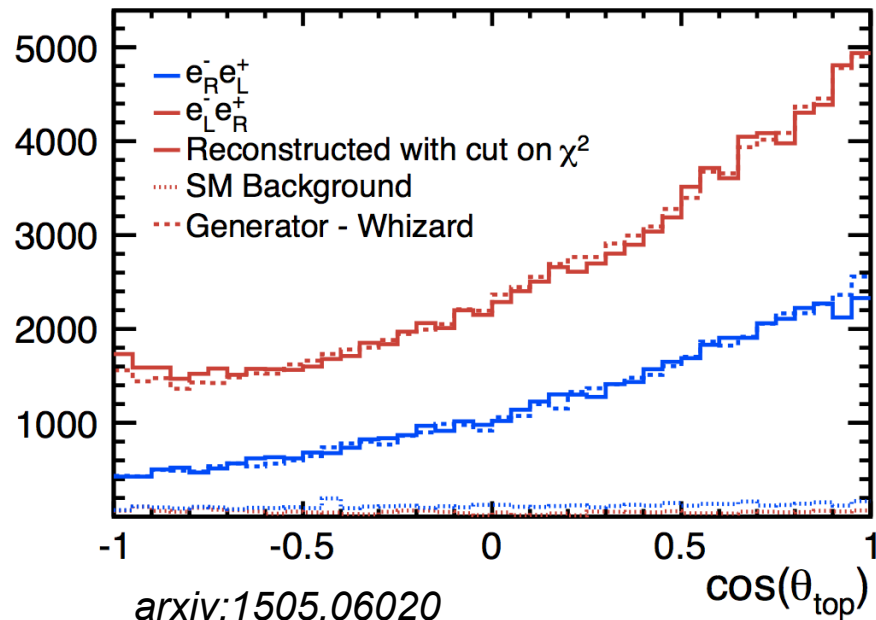
- ← Ambiguities in case of **left** handed electron beams
Due to V-A structure at ttX vertex
- ← Precise reconstruction of θ_{top}
in case of **right** handed electron beams

Remedy to address ambiguities:
Select cleanly reconstructed events by χ^2 analysis
or
Reconstruction of b quark charge

Precise reconstruction for both beam polarisations

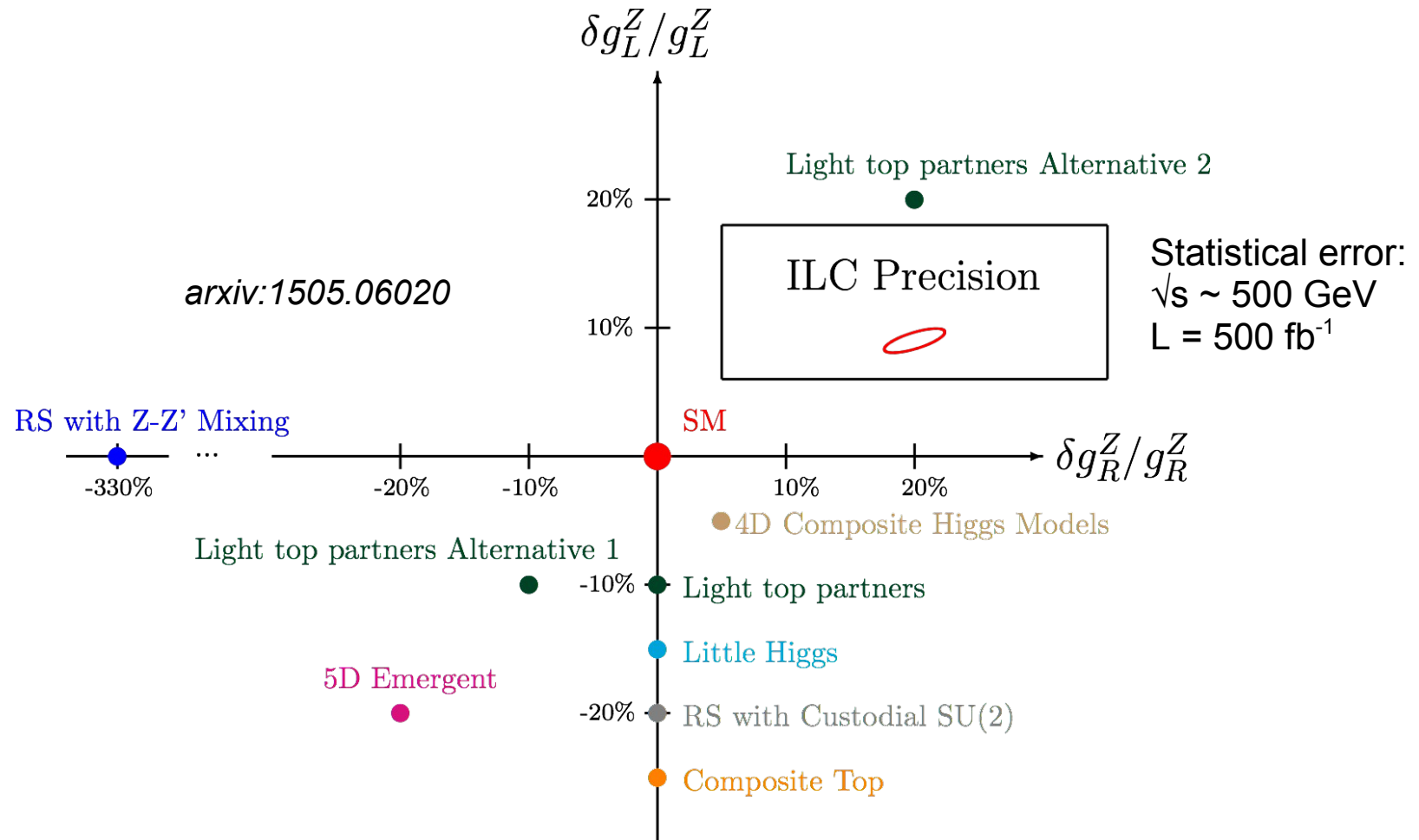
- Efficiency Penalty for e_L
- ϵ_{tot} : $e_R \sim 50\%$, $e_L \sim 30\%$

Precision on $A_{FB} \sim 2\%$



arxiv:1505.06020

Top is primary candidate to be a messenger new physics in many BSM models
Incorporating compositeness and/or extra dimensions

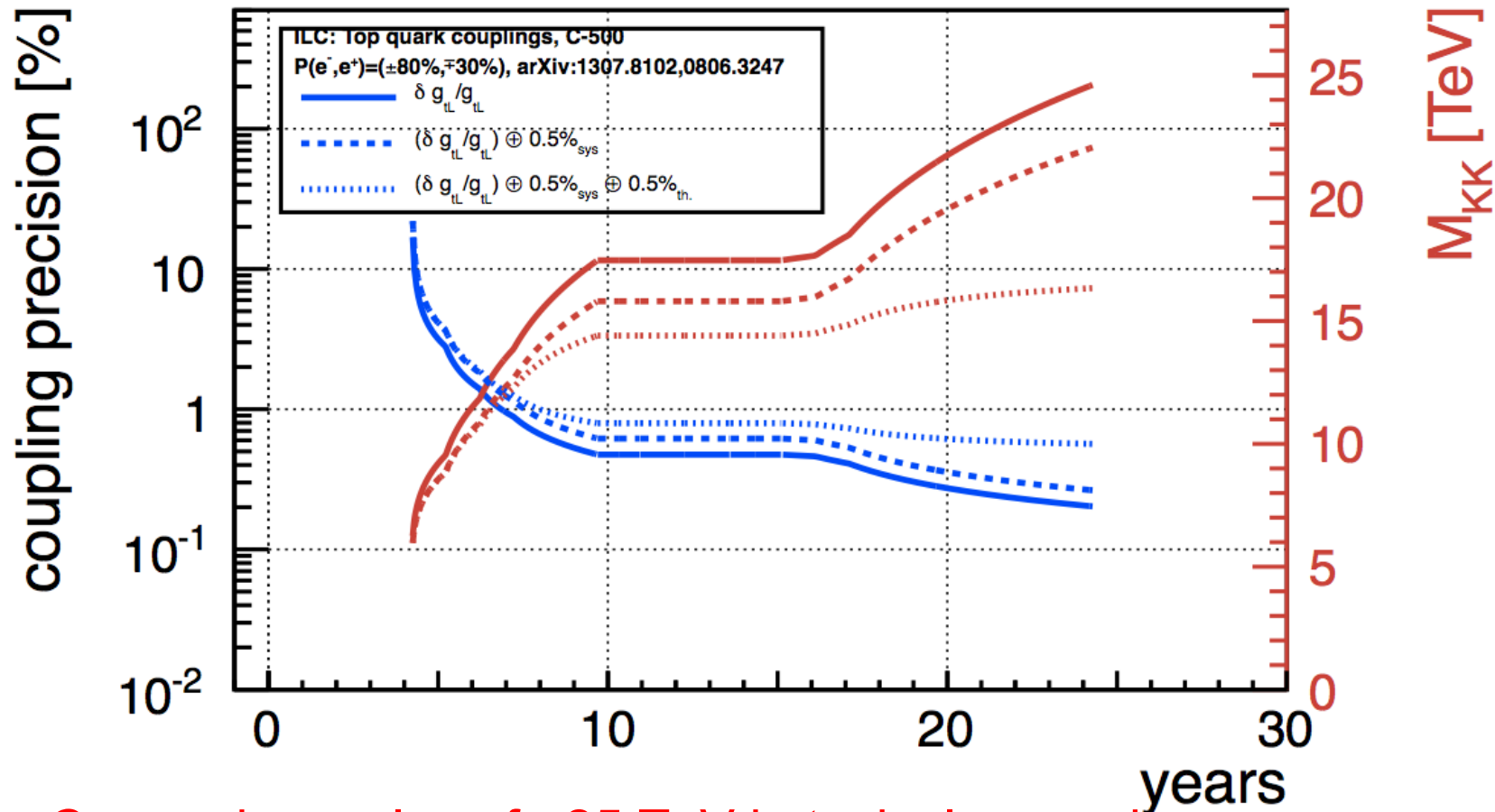


Precision expected for top quark couplings will allow to distinguish between models

Remark: All presented models are compatible with LEP elw. precision data

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247



Can probe scales of ~ 25 TeV in typical scenarios

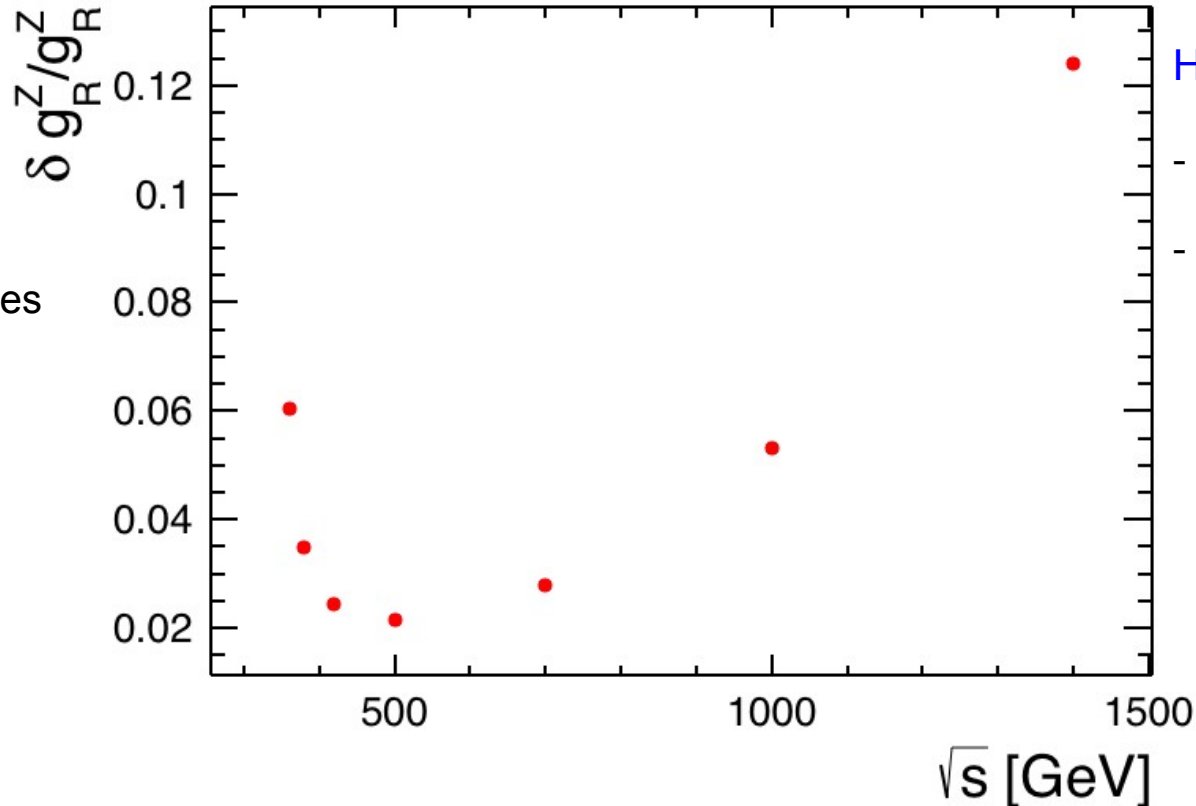
(... and up to 80 TeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider

... simplified discussion (same lumi at each cms)

Small cms energies:

- Vanishing axial vector coupling
- On top (not shown) large QCD uncertainties ... and
- Lumi decreases at linear colliders



High cms energies:

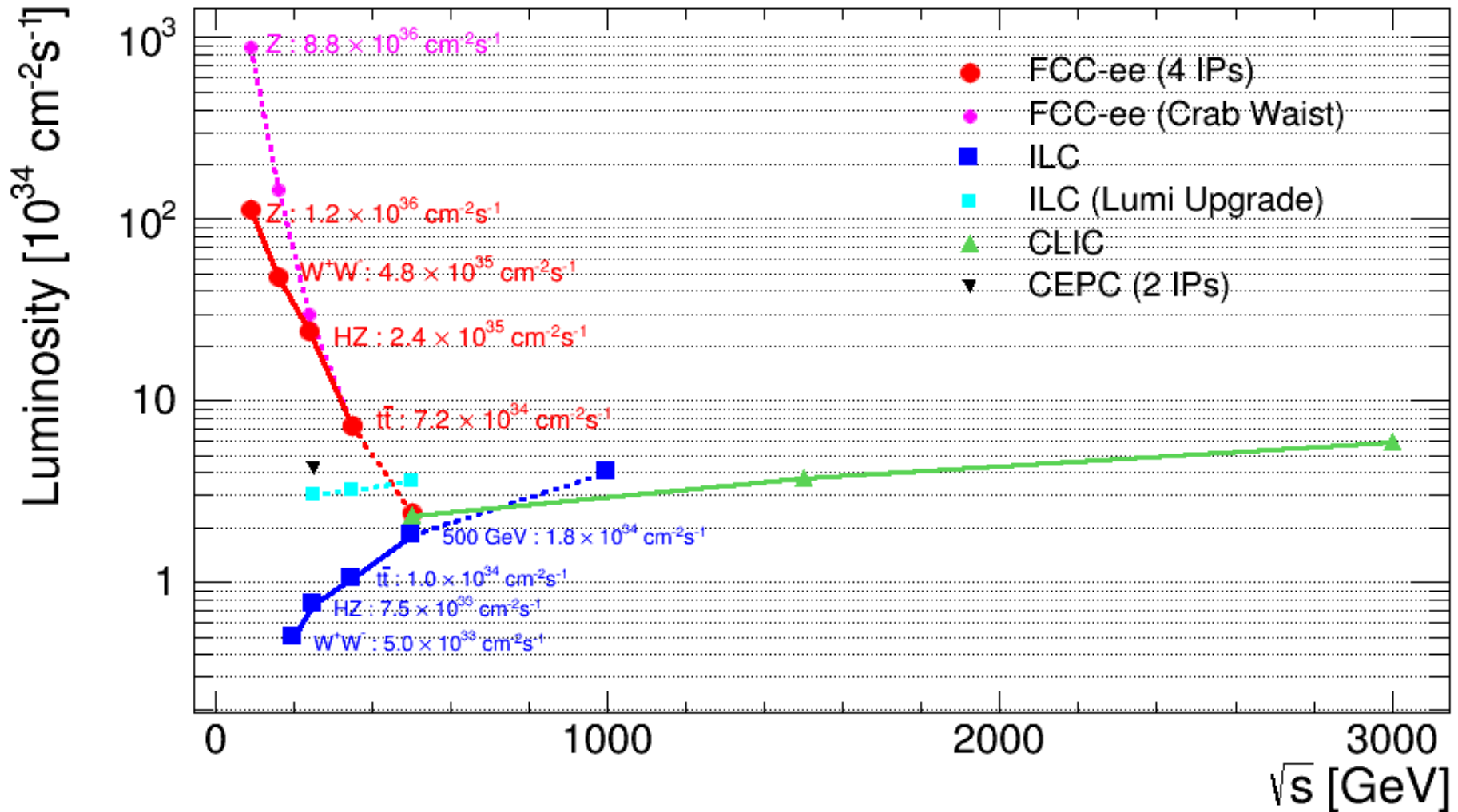
- Quickly decreasing cross section
- ... partially compensated by increasing luminosity

Broad minimum between 400 and 700 GeV

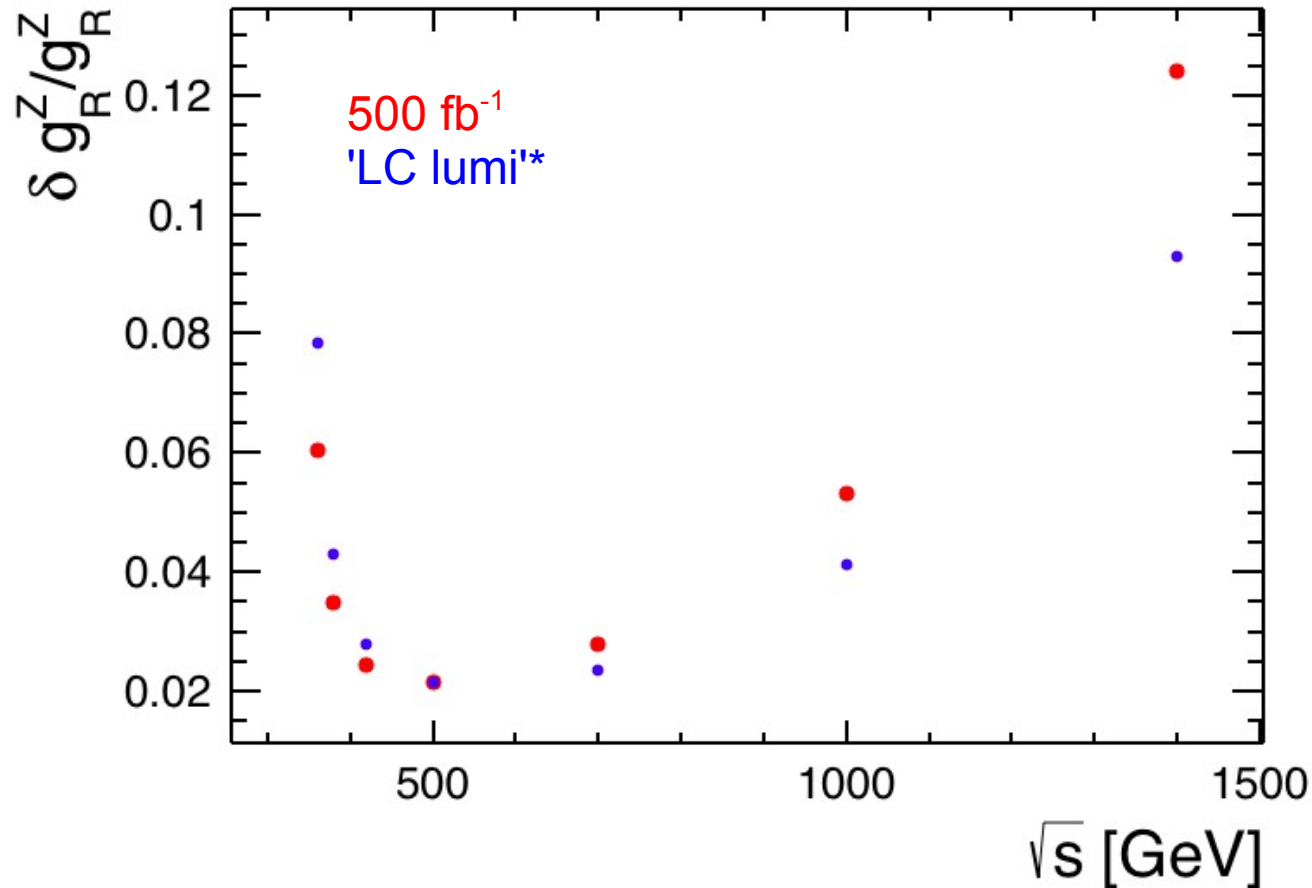
$\sqrt{s} \sim 500$ GeV is “sweet spot” for coupling measurements

However:

- Sensitivity to CP violating Higgs at smaller cms energies (see later)
- New physics at higher energies may increase cross section



Linear Colliders



*from fit to combined ILC and CLIC spectrum

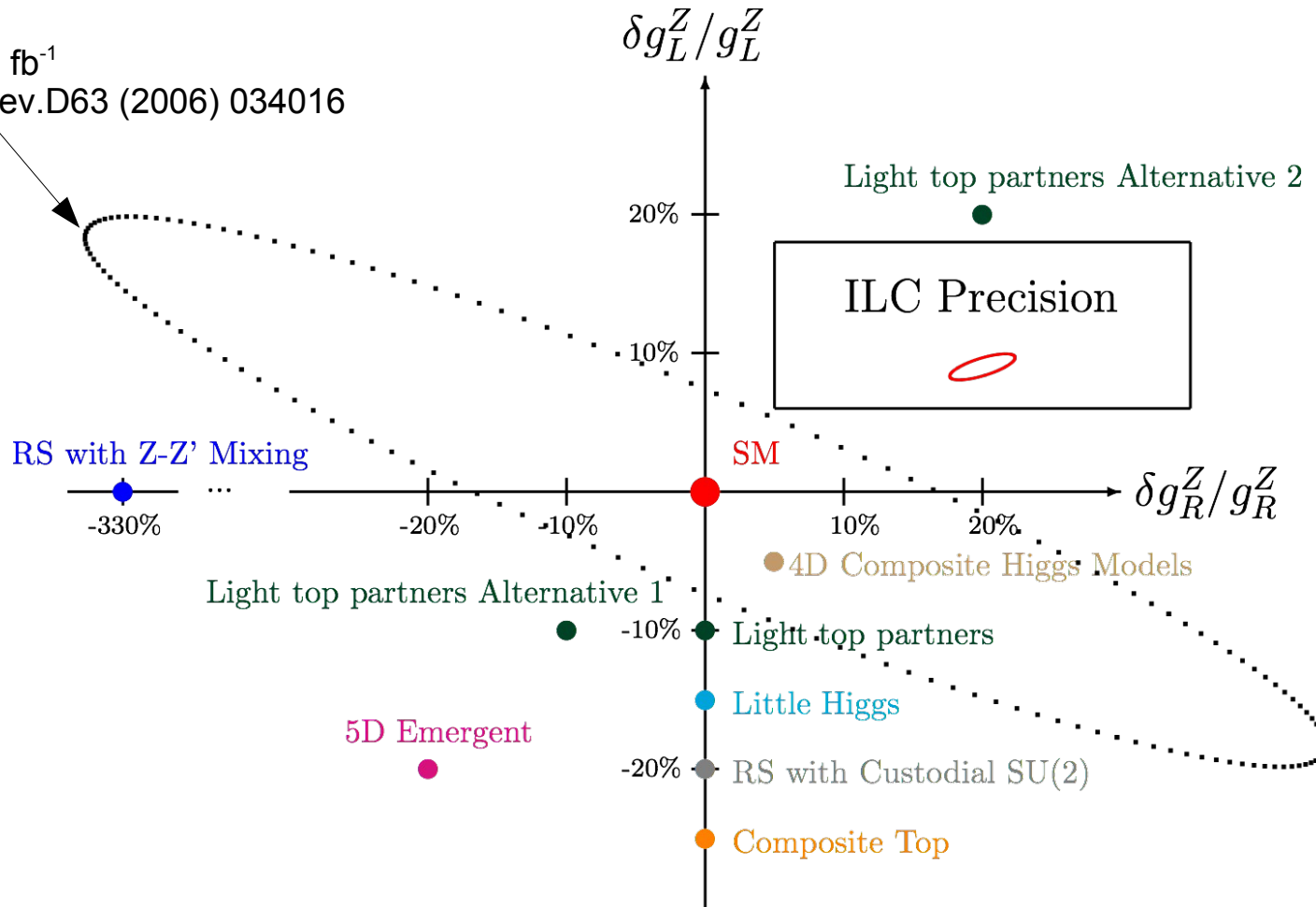
- **Luminosity:** Critical for cross section measurements
Expected precision 0.1% @ 500 GeV
- **Beam polarisation:** Critical for asymmetry measurements
Expected to be known to 0.1% for e- beam
and 0.35% for e+ beam
- **Migrations/Ambiguities:** Critical for A_{FB} :
PFLOW important for selection of 'clean events' but maybe subleading w.r.t. jet clustering
Control of b charge is most relevant topic !!!!
- **Other effects:** b-tagging, passive material etc.
LEP1 claims 0.2% error on R_b -> guiding line for LC

Under discussion with theory groups:

- Consideration full 6f final state (Interference with single top and ZWW)
- Electroweak NLO predictions (Correction LO \rightarrow NLO \sim 15%)
- Update and maintenance of event generators (WHIZARD, MADGRAPH etc.)

LHC14, 3000 fb⁻¹

From Phys.Rev.D63 (2006) 034016



Linear Collider will outperform LHC results

- Particular poor constraint on g_R (this holds also for flavor physics results)
- LHC LO QCD analysis, ~30% improvement through NLO QCD
- LHC may still be capable to exclude models

<i>ttW and ttZ measurements</i>		ttW				ttZ			
		Cross section		Significance		Cross section		Significance	
Data	Analysis	Theory*	Obs.	Exp.	Obs.	Theory*	Obs.	Exp.	Obs.
7 TeV (5 fb ⁻¹)	CMS ^[1]	147 ⁺¹⁴ -16	-	-	-	137 ⁺¹² -16	280 ⁺¹⁵⁰ -110	?	3.3
	ATLAS ^[2]		-	-	-		< 710	-	-
8 TeV (20 fb ⁻¹)	CMS ^[3]	203 ⁺²⁰ -22	170 ⁺¹¹⁰ -100	2.0	1.6	206 ⁺¹⁹ -24	200 ⁺⁹⁰ -80	3.1	3.1
	ATLAS ^[4]		300 ⁺¹⁴⁰ -110	2.3	3.1		150 ⁺⁵⁸ -54	3.4	3.1
	CMS Preliminary		382⁺¹¹⁷ -102	3.5	4.8		242⁺⁶⁵ -55	5.7	6.4

Preliminary documentation: twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsTOP14021

[1] CMS: *Phys. Rev. Lett.* 110 (2013) 172002

[3] CMS: EPJ C74 (2014) 3060

* NLO cross sections with scale uncertainties from

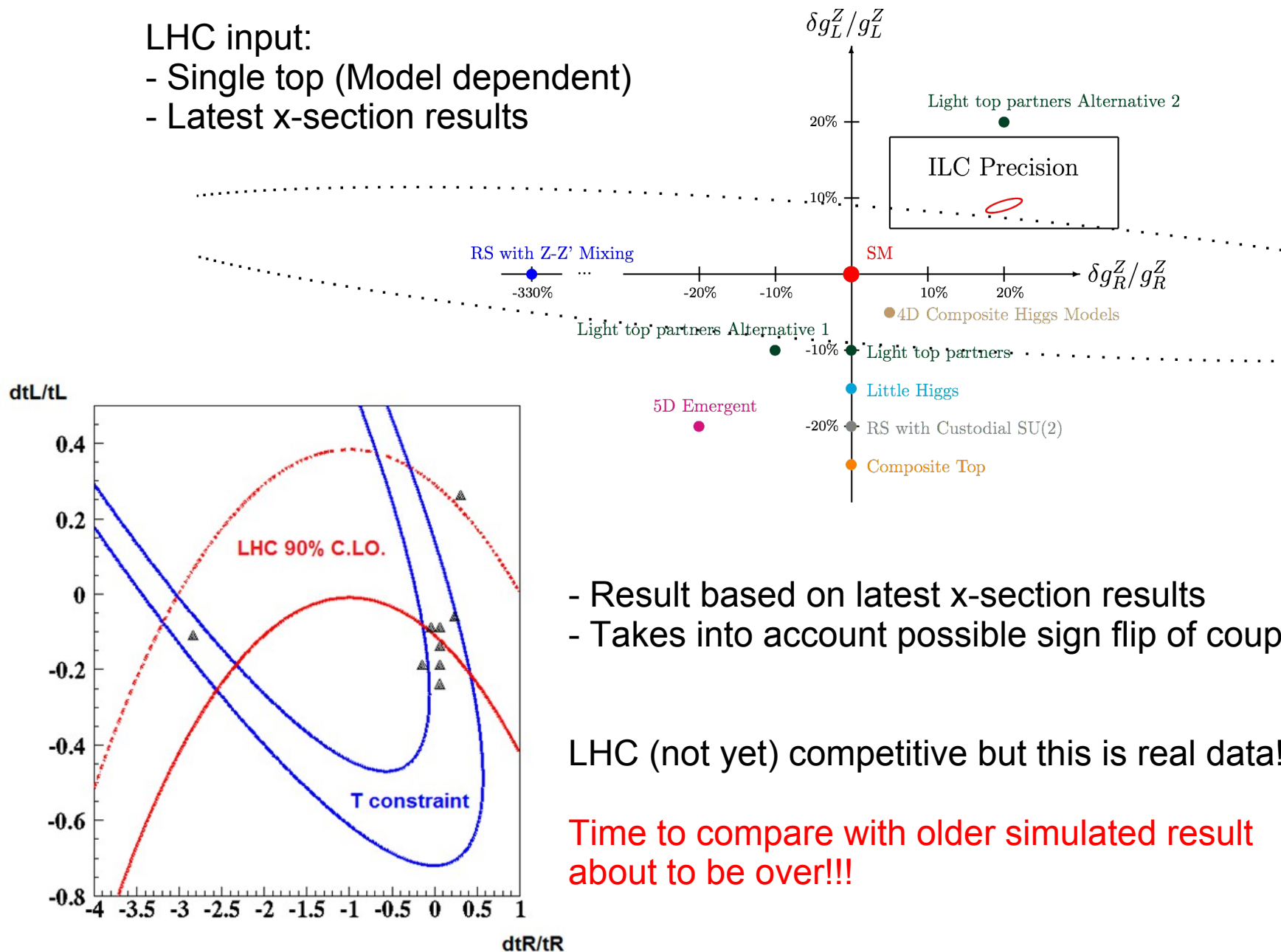
[2] ATLAS-CONF-12-126

[4] ATLAS-CONF-2014-038

Garzelli et. al., JHEP 11 (2012) 056

Comparison with current LHC results

- LHC input:
- Single top (Model dependent)
 - Latest x-section results



- Result based on latest x-section results
- Takes into account possible sign flip of couplings

LHC (not yet) competitive but this is real data!!!

Time to compare with older simulated result about to be over!!!

Here Rontsch and Schulze

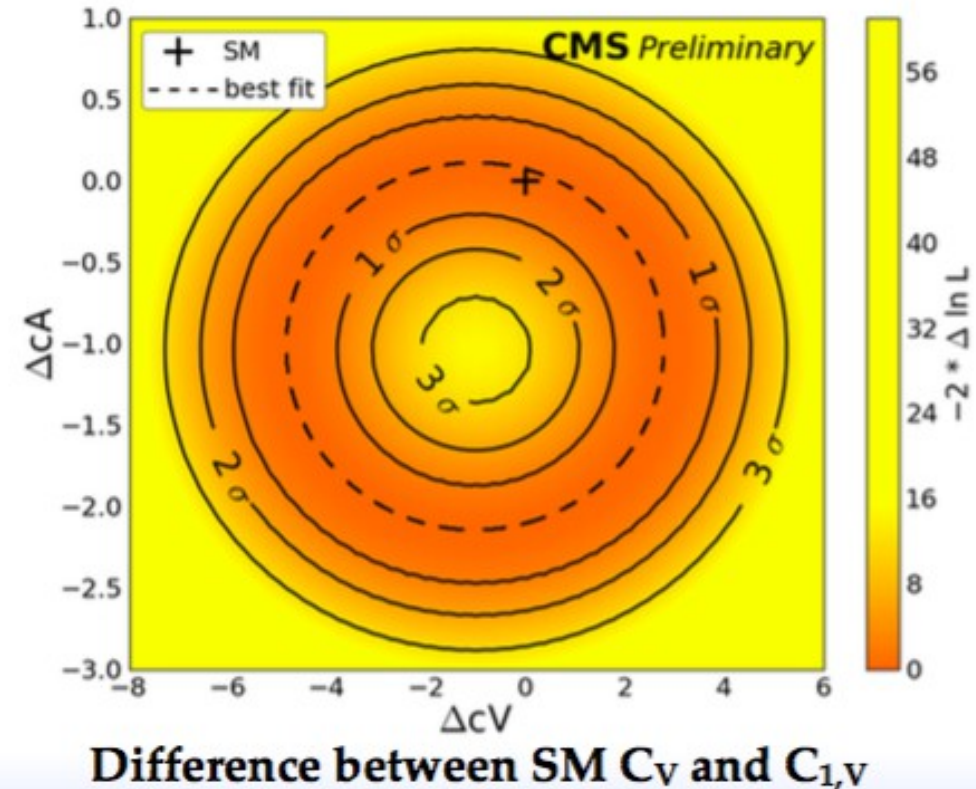
- Some dimension six operators would specifically affect the vector and axial components of top-Z coupling
- Interpret $t\bar{t}Z$ cross section measurement in terms of best fit to, and limits on $C_{1,V}$ and $C_{1,A}$

PRELIMINARY

$$C_{1,V} = C_{1,V}^{\text{SM}} + \left(\frac{v^2}{\Lambda^2}\right) \text{Re} \left[C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} - C_{\phi u}^{33} \right]$$

$$C_{1,A} = C_{1,A}^{\text{SM}} + \left(\frac{v^2}{\Lambda^2}\right) \text{Re} \left[C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} + C_{\phi u}^{33} \right]$$

*From <http://arxiv.org/abs/1404.1005>



For details see arxiv: 1503.04247

Basic idea: Final state top polarisation contains information about factors

$$\begin{aligned}
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi}
 \end{aligned}$$

=> different sensitivities in different individual matrix elements:

$$\omega_i = \frac{\partial |\mathcal{M}|^2(\alpha)}{\partial \alpha_i} \Big|_{\alpha^0} \frac{1}{|\mathcal{M}|^2(\alpha^0)} \quad \text{For each alpha (=ff) there is one (measurable) } \omega_i$$

Using full matrix element information -> Full event reconstruction

$$d\text{Lips} \propto d \cos \theta_t \, d \cos \theta_b \, d\phi_b \, d \cos \theta_{\bar{b}} \, d\phi_{\bar{b}} \, d \cos \theta_{l+} \, d\phi_{l+} \, d \cos \theta_{l-} \, d\phi_{l-} \, dq_t^2 \, dq_{\bar{t}}^2 \, dq_W^2$$

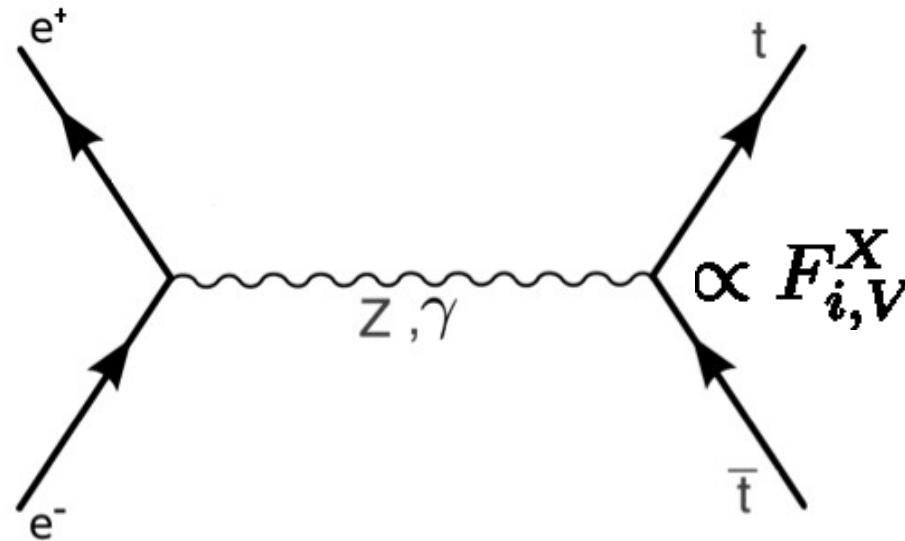
Parton level analysis with GRACE using fully leptonic final state

Simultaneous extraction of 10 FF including CP violation Ffs and disentangling of F1V F2V

$\mathcal{R}e \delta \tilde{F}_{1V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1V}^Z$	$\mathcal{R}e \delta \tilde{F}_{1A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1A}^Z$	$\mathcal{R}e \delta \tilde{F}_{2V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2V}^Z$	$\mathcal{R}e \delta \tilde{F}_{2A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2A}^Z$	$\mathcal{I}m \delta \tilde{F}_{2A}^\gamma$	$\mathcal{I}m \delta \tilde{F}_{2A}^Z$
0.0037	-0.18	-0.09	+0.14	+0.62	-0.15	0	0	0	0
	0.0063	+0.14	-0.06	-0.13	+0.61	0	0	0	0
		0.0053	-0.15	-0.05	+0.09	0	0	0	0
			0.0083	+0.06	-0.04	0	0	0	0
				0.0105	-0.19	0	0	0	0
					0.0169	0	0	0	0
						0.0068	-0.15	0	0
							0.0118	0	0
								0.0069	-0.17
									0.0100

No particular improvement through beam polarisation

- No background, no smearing
- Needs experimental study



$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 \underbrace{F_{2A}^X(k^2)}_{(2)}) \right\},$$

CP Violation through electric and weak dipole moment

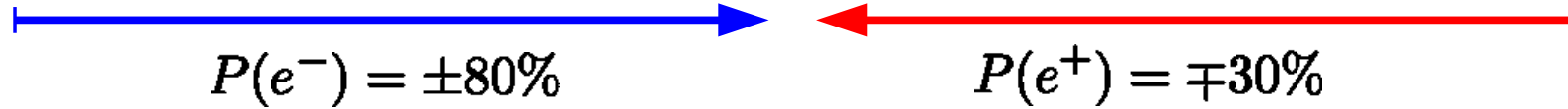
$$d^X = (e/2m_t) F_{2A}^X, X = \gamma, Z$$

F_{2A} is a complex number

$$F_{2A} = \lambda_{Re} Re(F_{2A}) + \lambda_{Im} Im(F_{2A})$$

CP Violation – What's been done?

ILC 'provides' two beam polarisations



$$P(e^-) = \pm 80\%$$

$$P(e^+) = \mp 30\%$$

$$t \bar{t} \rightarrow \ell^+(\mathbf{q}_+) + \nu_\ell + b + \bar{X}_{\text{had}}(\mathbf{q}_{\bar{X}}),$$

$$t \bar{t} \rightarrow X_{\text{had}}(\mathbf{q}_X) + \ell^-(\mathbf{q}_-) + \bar{\nu}_\ell + \bar{b} ,$$

'Optimal' observables to measure F2A

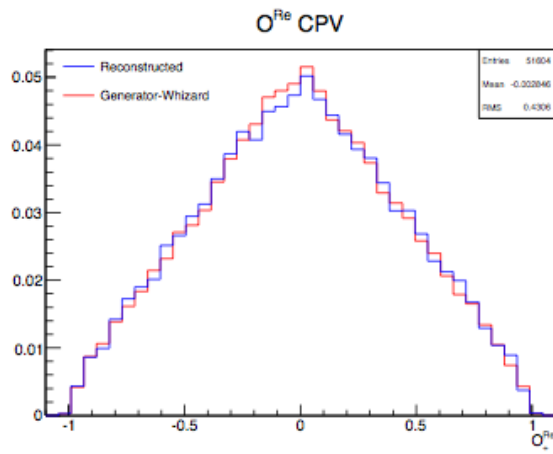
$$O_+^{\text{Re}} = (\hat{k}_{\bar{t}} \times \hat{q}_+) \hat{e}_+ \quad O_-^{\text{Re}} = (\hat{k}_t \times \hat{q}_-) \hat{e}_+$$

$$O_+^{\text{Im}} = -\left[1 + \left(\frac{\sqrt{s}}{2m_t} - 1\right)(\hat{q}_{\bar{X}} \times \hat{e}_+)^2\right] \hat{q}_+^* \cdot \hat{q}_{\bar{X}} + \frac{\sqrt{s}}{2m_t} \hat{q}_{\bar{X}} \cdot \hat{e}_+ \hat{q}_+^* \cdot \hat{e}_+$$

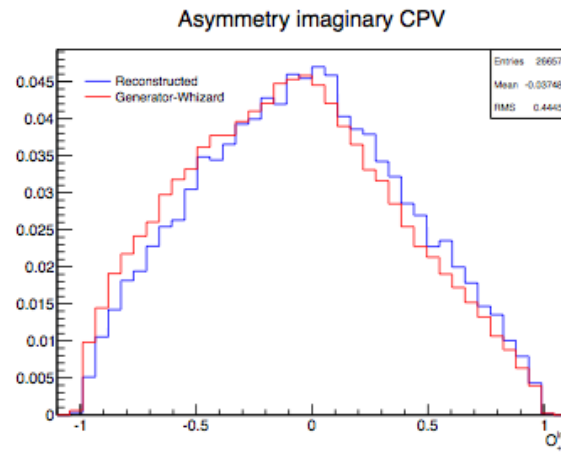
Extraction of four unknowns due to beam polarisation P

$$A_{\gamma,Z}^{\text{Re}} = \langle O_+^{\text{Re}} \rangle - \langle O_-^{\text{Re}} \rangle = c_\gamma [P \text{Re}(F_{2A}^\gamma) + KZ \text{Re}(F_{2A}^Z)]$$

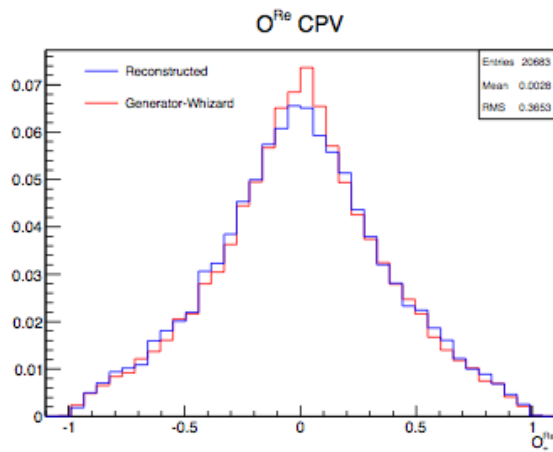
$$A_{\gamma,Z}^{\text{Im}} = \langle O_+^{\text{Im}} \rangle - \langle O_-^{\text{Im}} \rangle = d_\gamma [\text{Im}(F_{2A}^\gamma) + PKZ \text{Im}(F_{2A}^Z)]$$



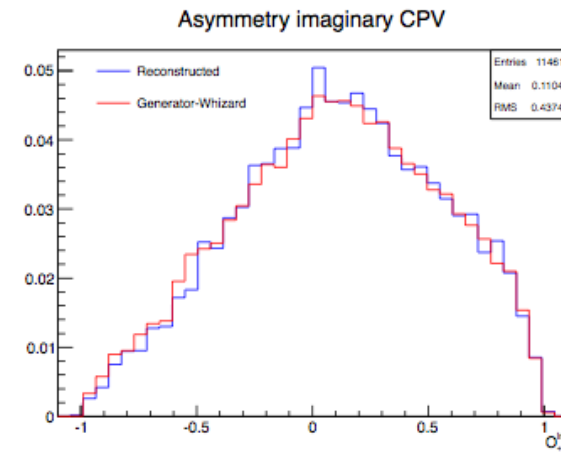
(a) O_+^{Re} P=-1



(b) O_+^{Im} P=-1



(c) O_+^{Re} P=1



(d) O_+^{Im} P=1

CPV obs	Generated	Reconstructed
$\langle O_+^{Re} \rangle$	-0.00285	-0.00206
$\langle O_-^{Re} \rangle$	0.00296	0.00116
$\langle O_+^{Im} \rangle$	-0.08922	-0.0375
$\langle O_-^{Im} \rangle$	-0.08654	-0.0341
RMS	0.43	0.44
δ_{stat}	0.0014	0.002

	Generated	Reconstructed
$A_{\gamma,Z}^{Re}$	-0.0058 ± 0.002	-0.0032 ± 0.003
$A_{\gamma,Z}^{Im}$	-0.0027 ± 0.002	-0.0034 ± 0.003

Study by Francois Richard

Higgs sector

- It should be noted that for what concerns the Higgs sector (non-minimal) contribution there could be a much larger enhancement for the 3d generation $\mathbf{df} \sim \mathbf{m}^3 \mathbf{f}$ at one-loop
- Higgs exchange is larger near threshold and the sensitivity for $\text{Re}(F2A)$ drops to 0 at 500 GeV

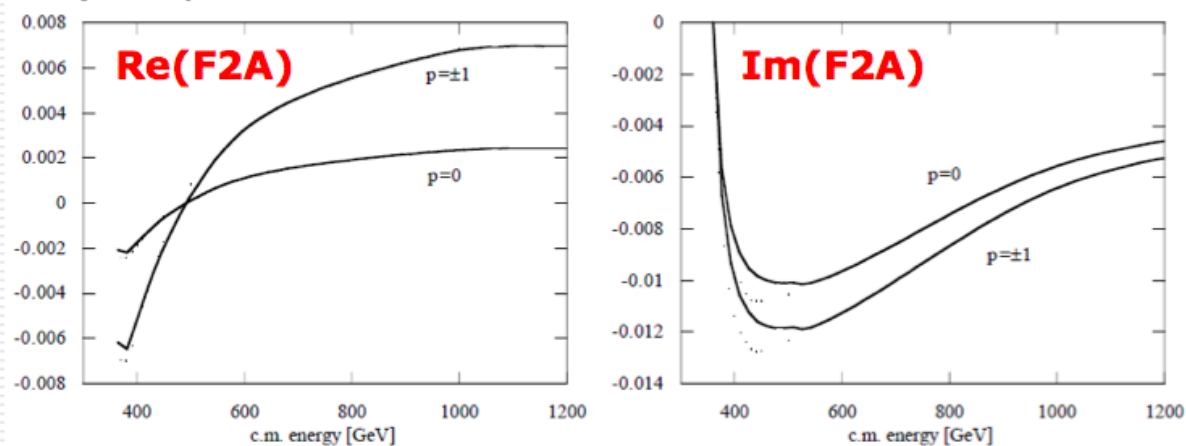


Fig 1: Ratios r_1 (left figure) and r_2 (right figure) for the optimized dispersive and absorptive observables $\mathcal{O}_{\pm}(i)$, $i = 1, 2$ defined in [6] for $m_t = 180$ GeV, $m_{\varphi_1} = 100$ GeV, and $\gamma_{CP} = 1$.

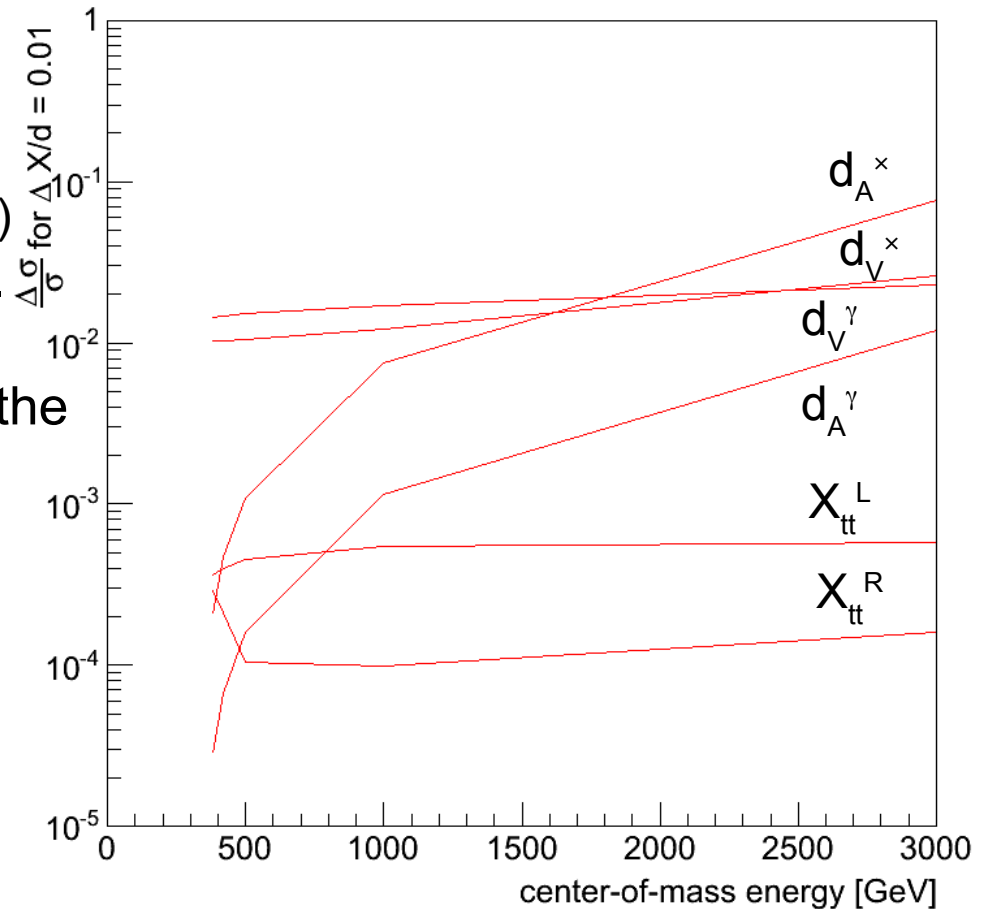
8

Exchange of CP Violating Higgs is most probable source of CP violation
In $t\bar{t}$ production (dixit Werner Bernreuther)

Dimension 6 effective operators
(~equivalent role to anomalous form factors)
have been implemented in WHIZARD...

Allow to map the dependence on \sqrt{s} of the
impact of new physics on given
observable

May help to explore the sensitivity of
new/additional observables



- **First iteration of study on anomalous form factor finished**
 - Demonstration of outstanding potential of high-precision measurements
 - Outperforming of LHC precisions (incoming results will be observed with great interest)
 - Essential pillar of LC physics program
- **Precision on form factors and couplings of the order of 1%**
 - No sign ambiguity
 - Sensitivity to new physics up to several 10 TeV
- **Beam polarisation is major asset for control of theoretical and experimental ambiguities**
- **Still, a lot has to be done**
 - b-charge measurement (\Rightarrow FF from $t\bar{t} \rightarrow$ hadrons, A_{FB} as function of fermion mass)
 - Step $t\bar{t} \rightarrow WbWb$
 - understanding of large elw. NLO corrections to A_{FB} and x-section
 - Matrix element method \leftrightarrow 'robust' experimental quantities (understanding of drawbacks and advantages)
 - Experimental study of ME Method needed
 - How to address CP violation (Experimental observables or ME Method?)
 - EFT approaches w.r.t. Complete models
- **tt analysis enters new phase**

Backup

ILC design parameters	
\sqrt{s}	91-500 GeV
\mathcal{L}	$2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
P_{e^-}	>80%
P_{e^+}	upto 30%
Length	~31 km

Comment

500 GeV is baseline
Option to upgrade to 1 TeV

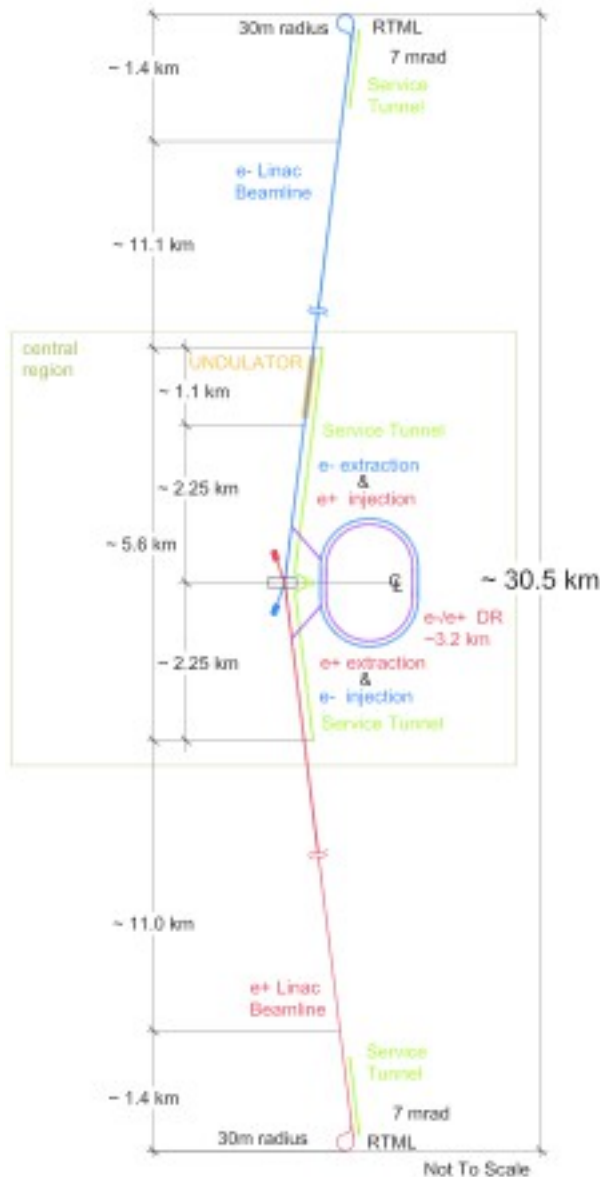
~Factor 4 technically possible

Proven by SLC

~Conservative estimate

Current site allows for 50km

- Discussion on possible running scenarios has started
- Luminosity and running time to achieve at a ~25 years research programme
That includes running at 250 GeV, 350 GeV, 500 GeV and 1 TeV
- No official statement yet but integrated luminosities indicated in following transparencies are realistic



• SCRF Technology

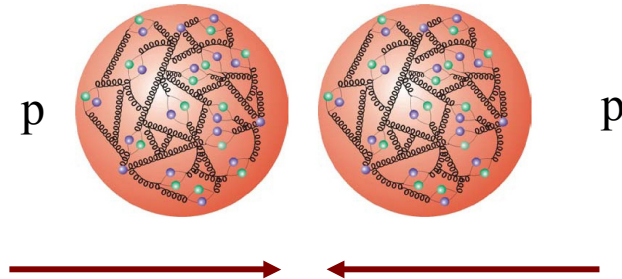
- 1.3GHz SCRF with 31.5 MV/m
- 17,000 cavities
- 1,700 cryomodules
- 2×11 km linacs

Luminosity

$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\epsilon_{n,y}}} H_D$$

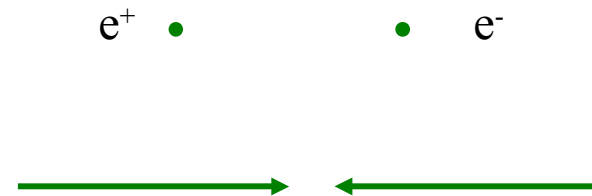
$\eta_{RF} \sim 40\%$ for SCRF technology

-> efficient technology



Proton:

Composed particle (hadron)
 Unknown energy of collision partners
 Parasitic reactions
 Strong interaction
 => Considerable physics background
 Advantage: Scan of energy
 Range within one experiment

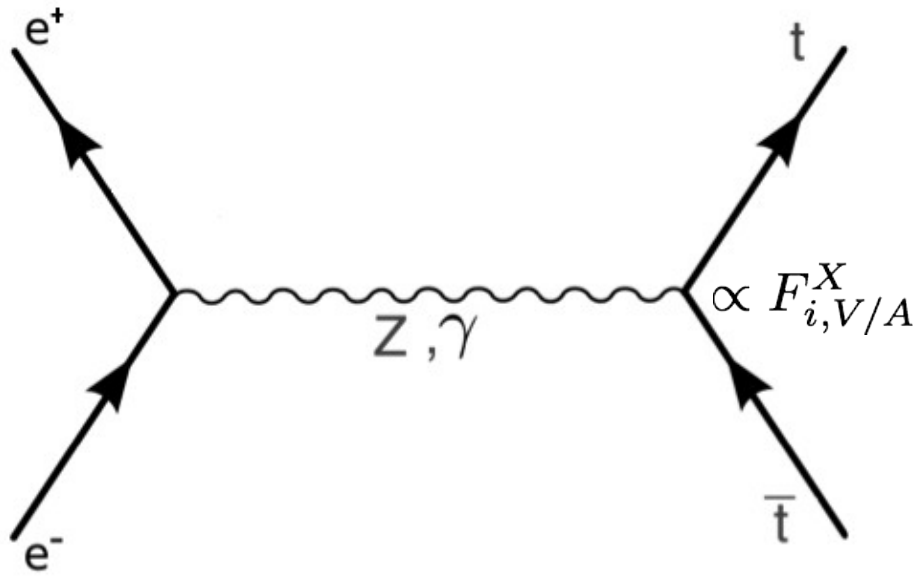


Electron:

Elementary particle
 Well known and adjustable energy of collision partners

 Each energy point needs a New set of machine parameters

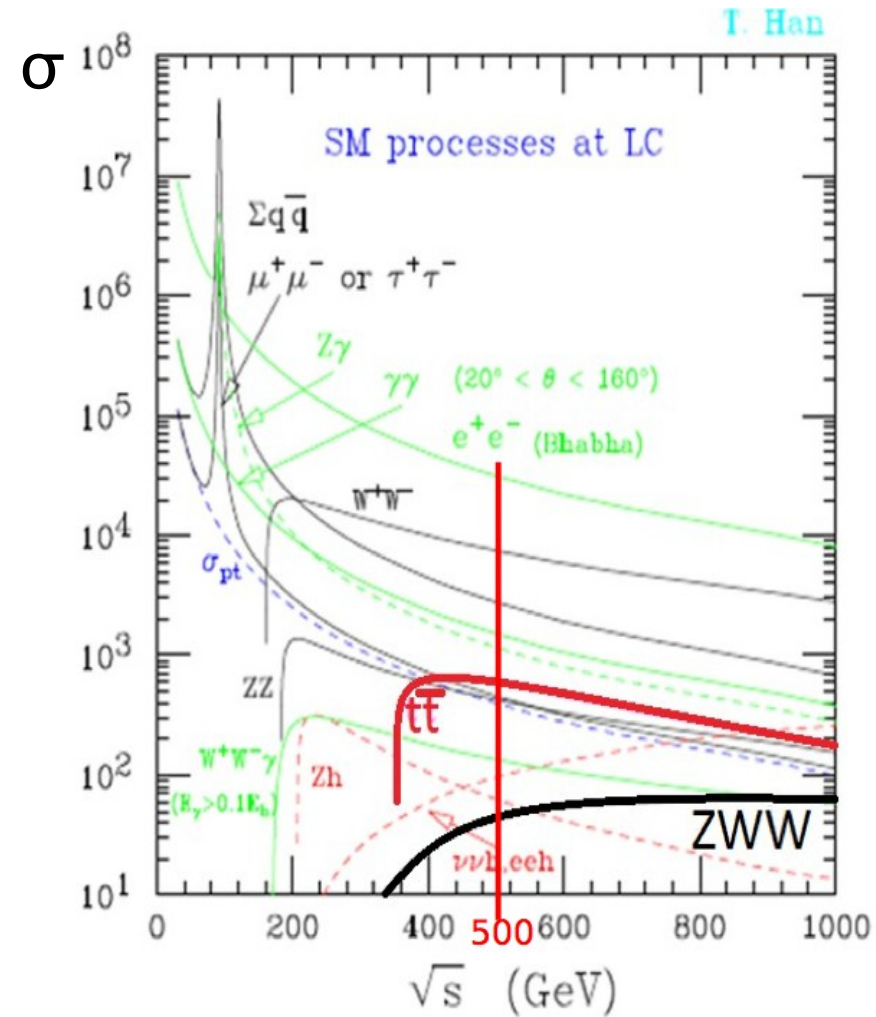
High precision measurements



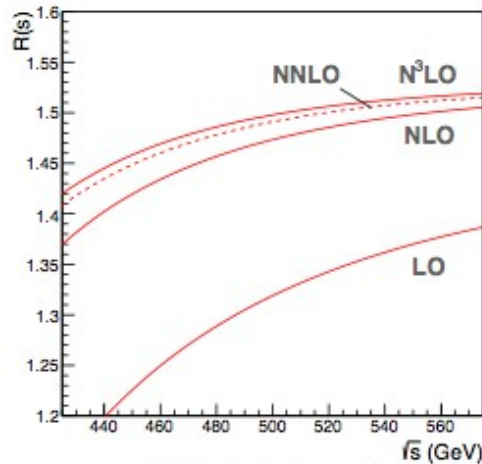
- Top quark production through electroweak processes
no competing QCD production => Small theoretical errors!

- High precision measurements

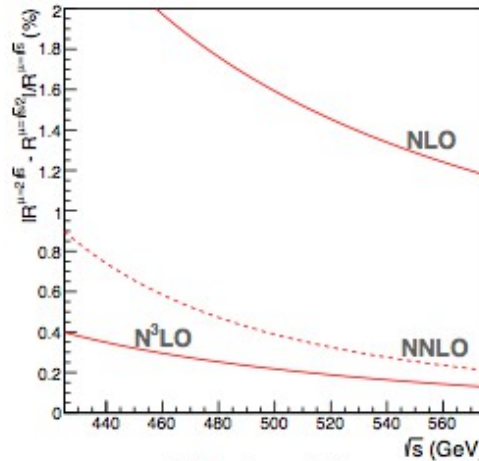
- Top quark mass at ~ 350 GeV through threshold scan
- Polarised beams allow testing chiral structure at $t\bar{t}X$ vertex
=> Precision on form factors F and couplings g



*QCD corrections are known up to N³LO



(a) Perturbation series

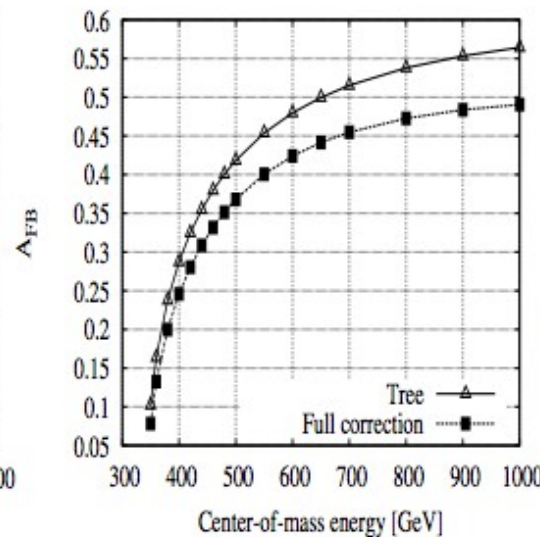
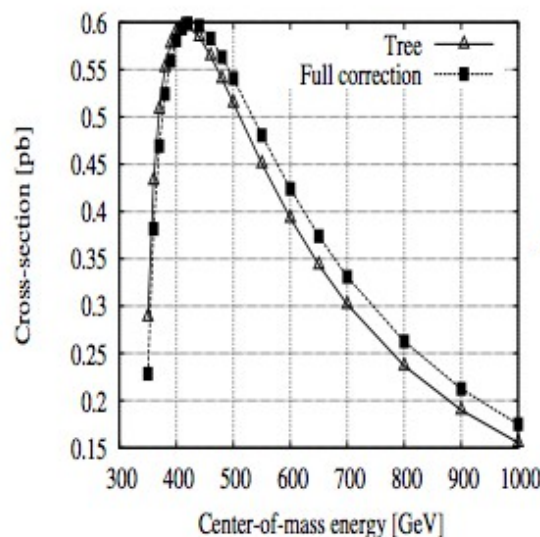


(b) Scale variations

QCD correction (N³LO) is
at the per mil level

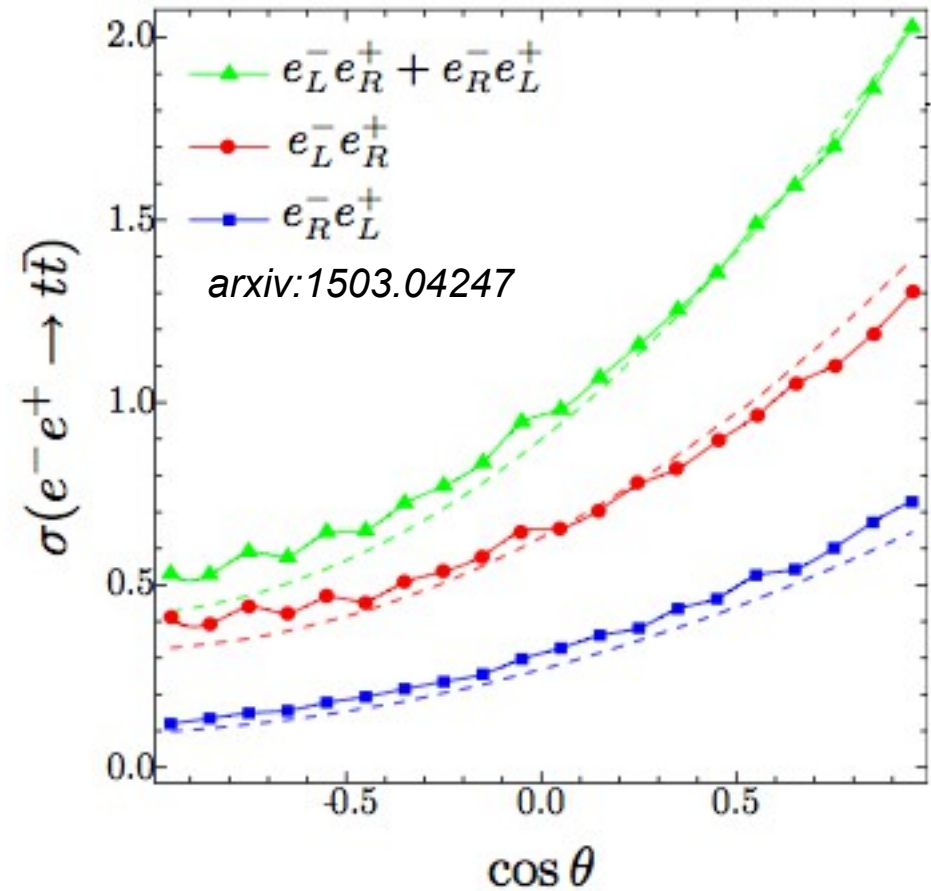
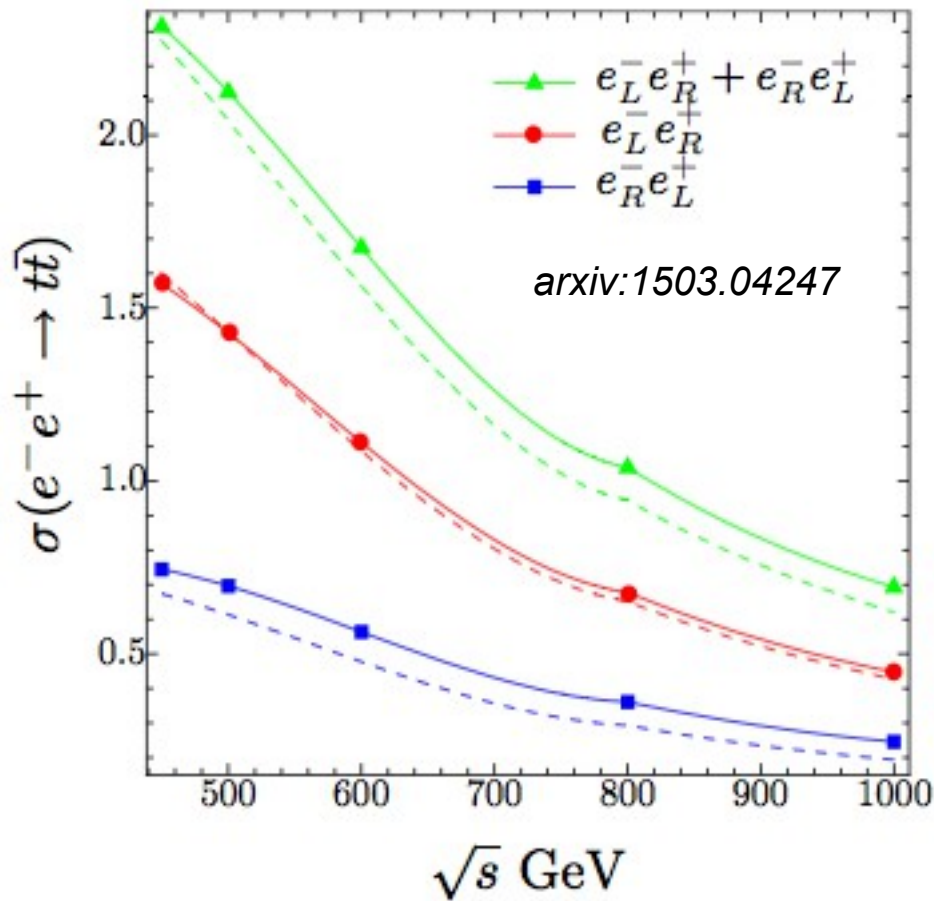
Kiyo, Maier, Maierhofer, Marquard, NCP B823 ('09)
*Bernreuther, Bonciani, Gehrmann, Heinesch,
Leineweber. NPB750 ('06)*
Hoang, Mateu, Zebarjad, NPB813 ('09)

*Electroweak corrections are known at one-loop level



EW correction at one-loop is
~5% for cross section
~10% for A_{FB}

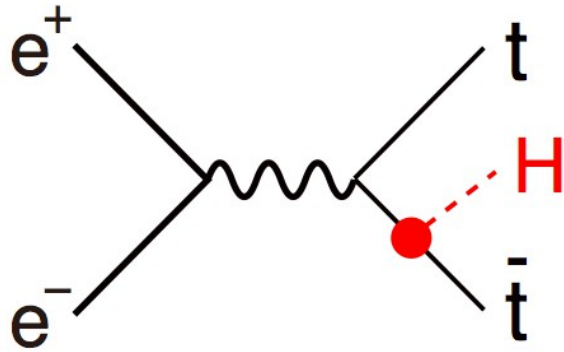
Fleischer, Leike, Riemann, Werthenbach, EJPC31 ('03)
*Kheim, Fujimoto, Ishikawa, Kaneko, Kato,
arXiv:1211.1112*



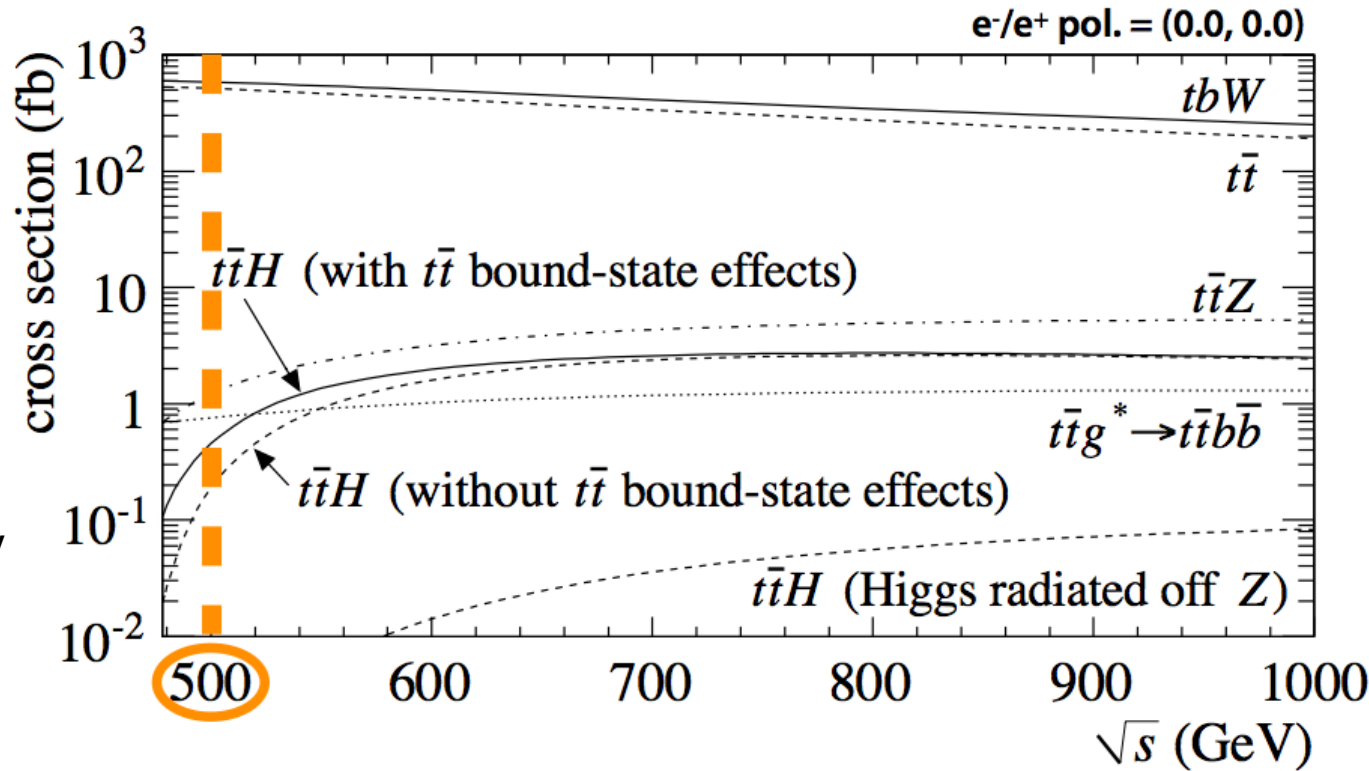
- Electroweak corrections manifest themselves differently for different beam polarisations

- **Beam polarisation important asset to disentangle SM and effects of new physics**

Configuration $e_R^-e_L^+$ seems to lead to “simpler” corrections



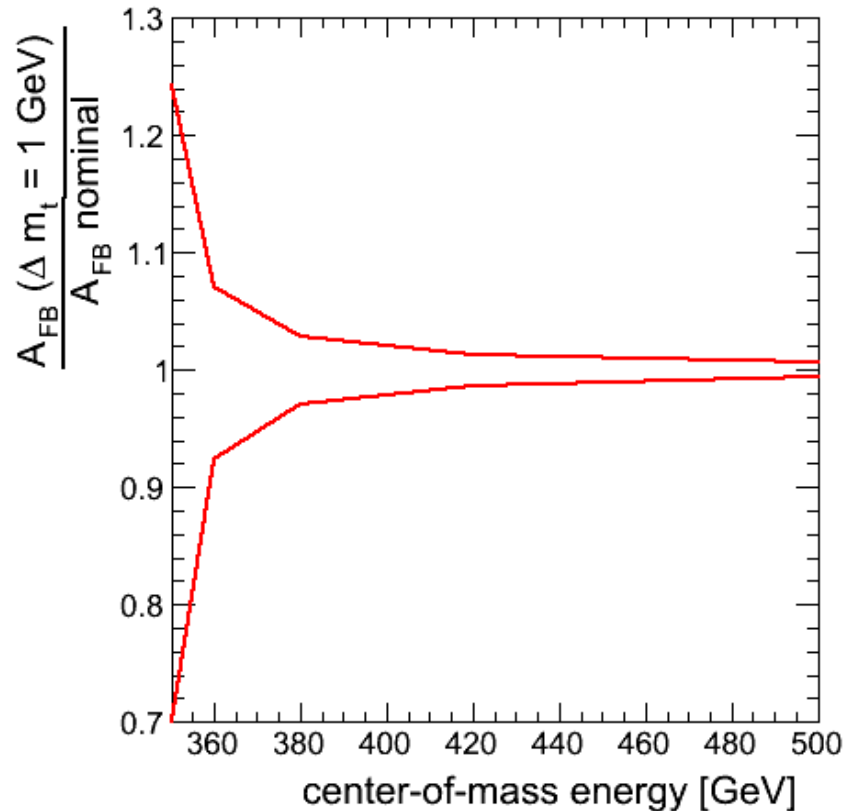
- Coupling of Higgs to heaviest particle known today
- Up to eight final state jets



$\Delta g_{ttH} / g_{ttH}$	500 GeV	500 GeV + 1 TeV
Canonical	14%	3.2%
LumiUP	7.8%	2.0%

← ILC TDR
← Technically possible

R. Horiguchi et al.
T. Tanabe, T. Price

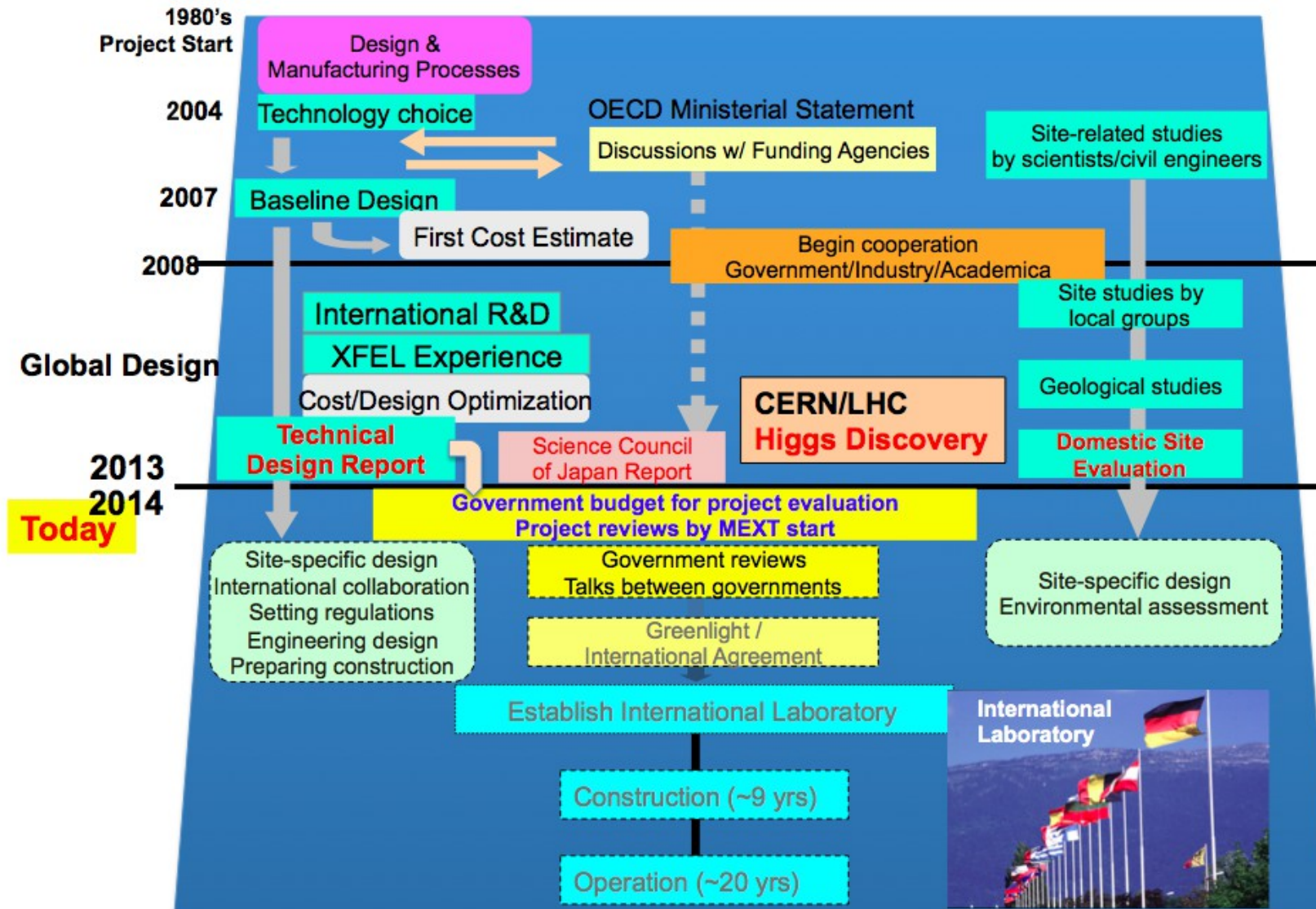


Influence of the top quark mass on x -sec and A_{FB}

- very pronounced below $\sqrt{s} = 360$ GeV
- 2.9%/GeV at $\sqrt{s} = 380$ GeV
- 1.3%/GeV at $\sqrt{s} = 420$ GeV
- 0.6%/GeV at $\sqrt{s} = 500$ GeV

With the assumption of a 100 MeV pole mass measurement at threshold, the remaining uncertainty is one per mil or less above 420 GeV

Timeline of ILC



Remark R.P.: MEXT report in March 2016