

# Top quark mass determination at Hadron Colliders

*(a short report)*



**Workshop on Top physics at the LC 2015**

*Valencia, 30th June 2015*



***Adrián Irlles***

**1) Motivation.**

**2) Direct top quark mass measurements.**

+ interpretation.

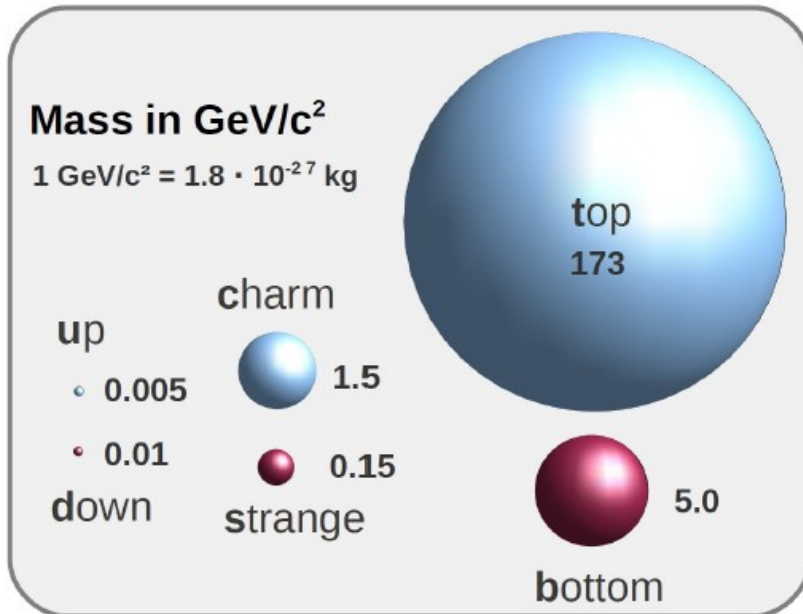
**3) Top quark mass determination from NLO observables.**

**4) Summary**

*What is not in the slides:*

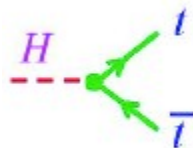
- many of the measurements (just a personal selection)
- top quark mass schemes definitions (see A. Hoang & P. Marquard talks)

## The heaviest elementary particle discovered so far



$m_t \sim 173 \text{ GeV}$ :

- Fundamental parameter of the Standard Model (SM)
- Important for precise tests of the SM



$$y_t = \frac{\sqrt{2}}{v} m_t = 2^{3/4} G_F^{1/2} m_t = 1 \quad (0.995)$$

- Test of new physics scenarios.

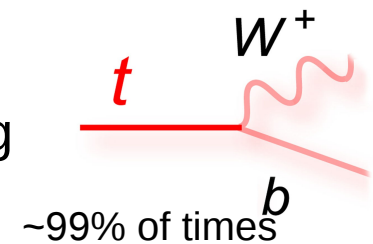
## A peculiar quark

Discovered in 1995, only observed in two colliders.

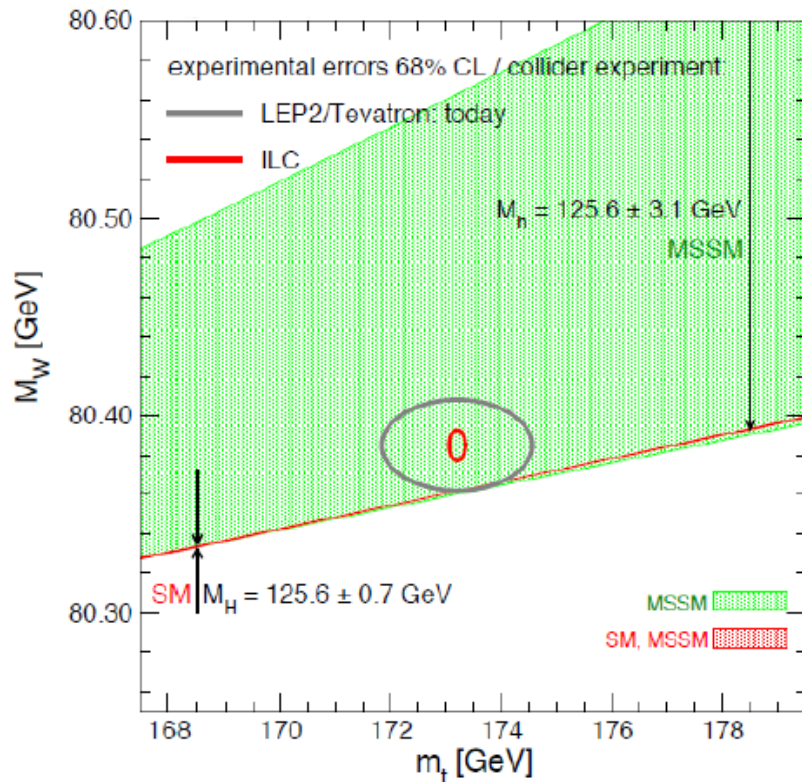
Mainly produced in pairs



Decays before hadronizing



## Consistency of the SM and BSM

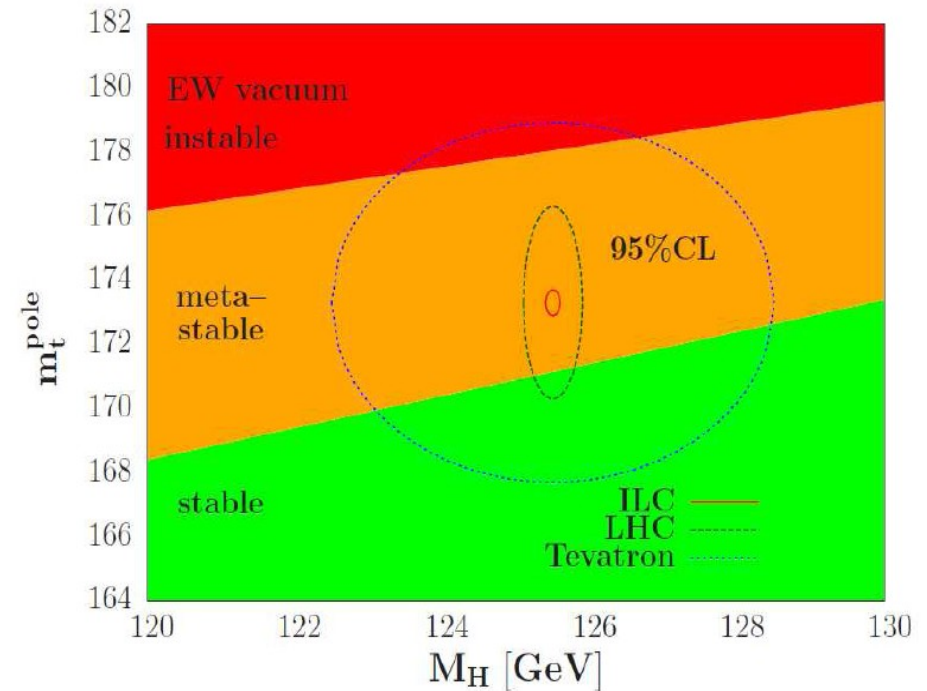


[Heinemeyer et al updated to summer 2014]

Enter in all loop corrections (reduce parametric uncertainty)

$$M_W = M_W^{LO} + \Delta r_{top} + \Delta r_H$$

## SM Vacuum stability



$$M_H > 129.6 \text{ GeV} + 2.0 \left( m_t^{pole} - 173.34 \text{ GeV} \right) - 0.5 \text{ GeV} \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \pm 0.3 \text{ GeV}$$

[Degrassi, Di Vita, Elias-Miro, Spinosa, Giudici '12, Alekhin, Djouadi, Moch '12]

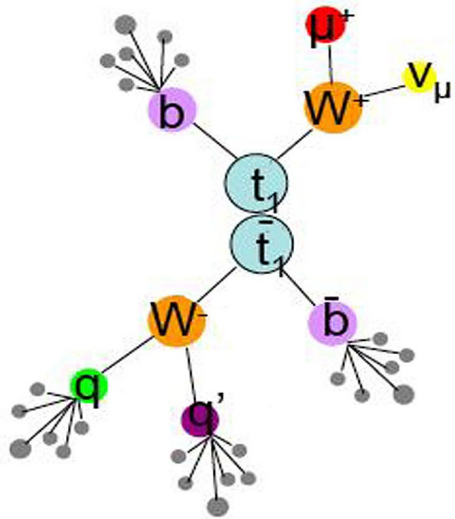
Strong dependence with the Higgs and top-quark mass.

Assumption: no New Physics up to the Planck scale



# Direct top quark mass measurements

Inferring the top quark mass from the kinematic properties of its decay products.



## Matrix Element method (ME):

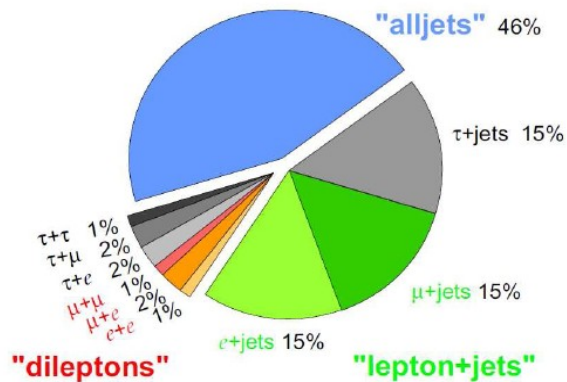
Calculates event probability densities from differential cross sections and detector resolutions.

- Maximizes the statistical information.
- Current implementations at LO.

## Ideogram method:

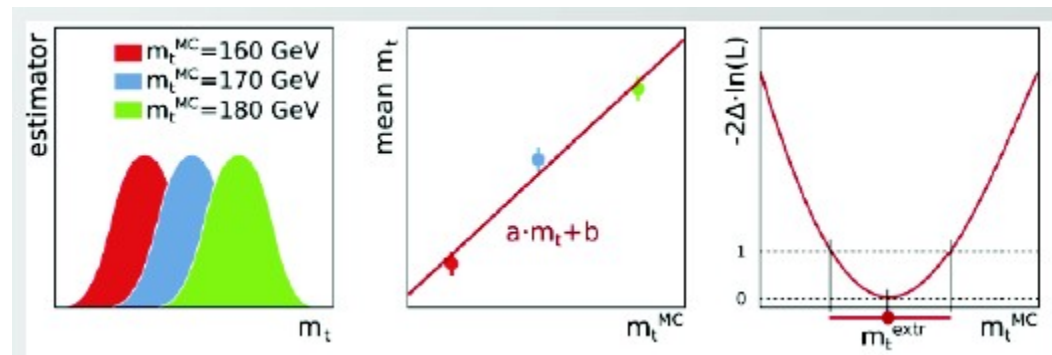
Event likelihood function to test compability of event kinematics with the decay hypothesis convoluted with detector resolutions.

Top Pair Branching Fractions



## Template method:

Compare histograms in data to simulations.



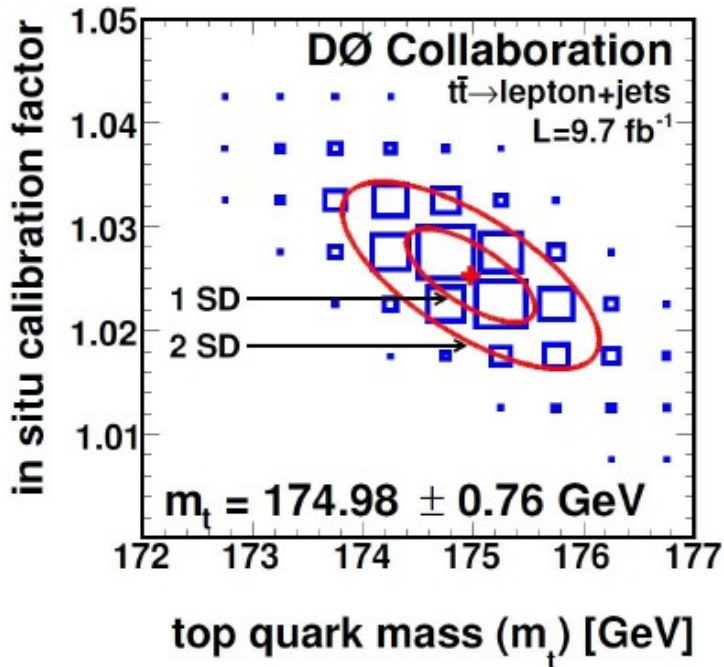
These methods measure the kinematic MC mass

# Direct top quark mass measurements: Matrix Element



## Most precise measurement at Tevatron

$$P(x, m_t) = \frac{1}{\sigma(m_t)} \int \sum \frac{d\sigma(y, m_t)}{\text{LO ME}} dq_1 dq_2 \frac{f(q_1)f(q_2)}{\text{PDFs}} \frac{W(y, x, k_{\text{JES}})}{\text{Transfer function}}$$



Simultaneous fit of  $m_t$  and  $k_{\text{JES}}$  (global factor for the Jet Energy Scale -JES-, used for in situ calibration using the hadronic W decay)

Improvements:

Full Run II data → statistics

Improved objects ID (e, mu, b)

Faster method that allowed dramatic increase in MC statistics

Typical statistical uncertainty: ●  
~0.25 GeV → ~0.01 – 0.05 GeV

$$m_t^{MC} = 174.98 \pm 0.58 \text{ (stat + JES)} \pm 0.49 \text{ (syst)} \text{ GeV}$$

$$m_t^{MC} = 174.98 \pm 0.76 \text{ GeV}$$

Larger unc:

Had. and UE → 0.26 GeV

Residual JES → 0.21 GeV

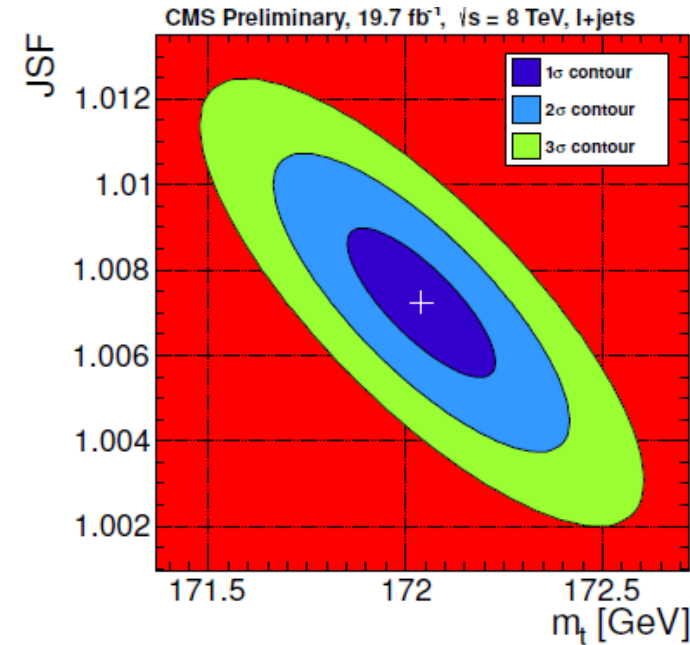
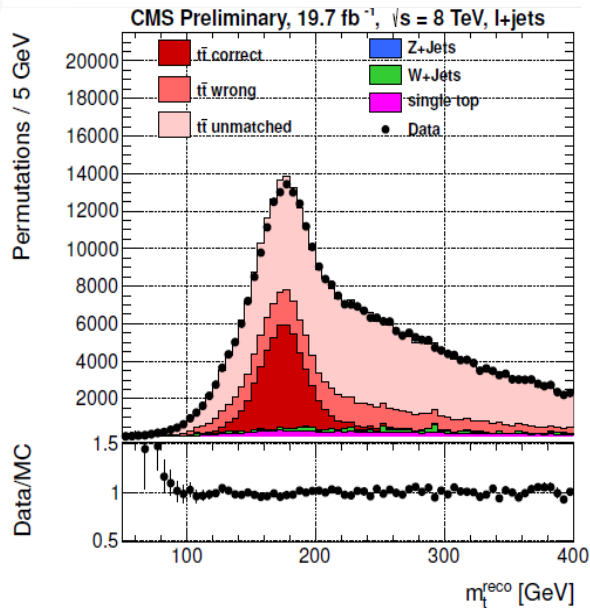
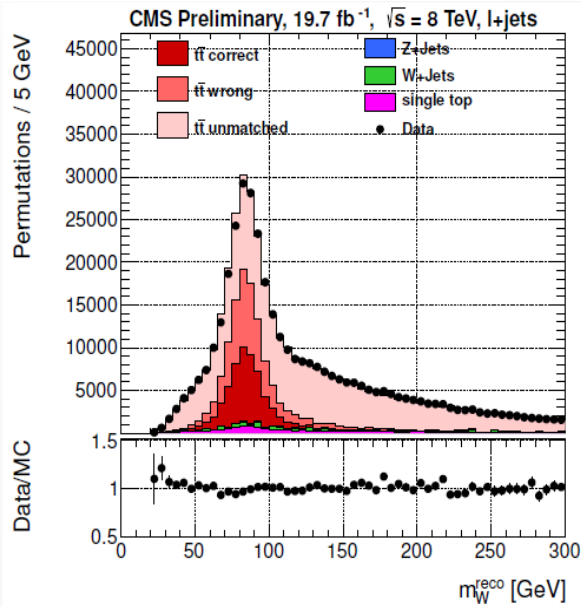
PRL [arxiv:1405:1756]

**Single most precise measurement!!**

# Direct top quark mass measurements: Ideogram Method

## Most precise measurement at the LHC

CMS, lepton+jets, using 8 TeV data.  
 Ideogram method using all permutations.  
 Estimators:  $m_t$  and  $m_w$ .  
 Simultaneous fit of  $m_t$  and **JSF**



$$m_t^{MC} = 172.04 \pm 0.19 (stat + JSF) \pm 0.75 (syst) GeV$$

$$m_t^{MC} = 172.04 \pm 0.77 GeV$$

Larger unc:

**Flavour JSF** → 0.41 GeV

**JES** → 0.26 GeV

**Pile-up** → 0.27 GeV



# Direct top quark mass measurements: Template Method

Most precise measurement at the ATLAS experiment

lepton+jets channel, using 7 TeV data.  
3D fit of  $m_t$ , JES and bJSF.



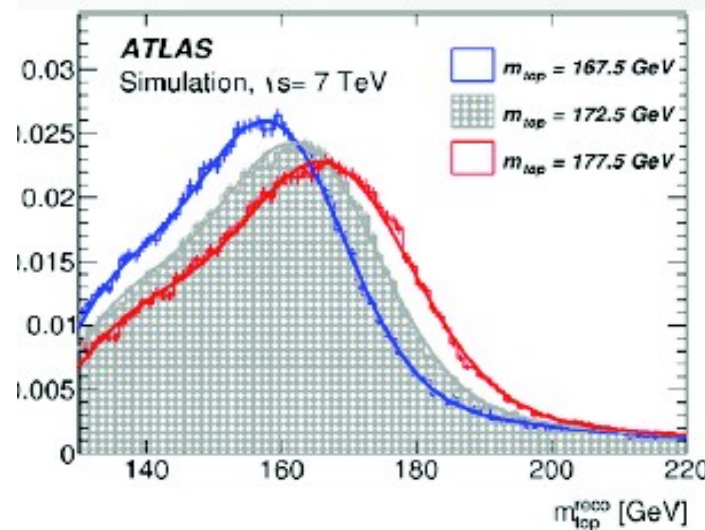
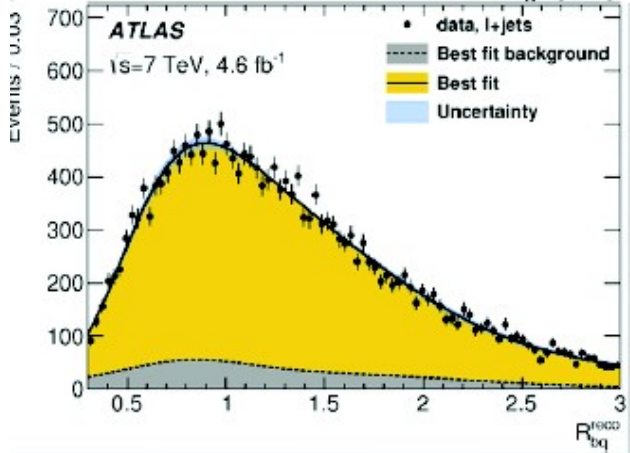
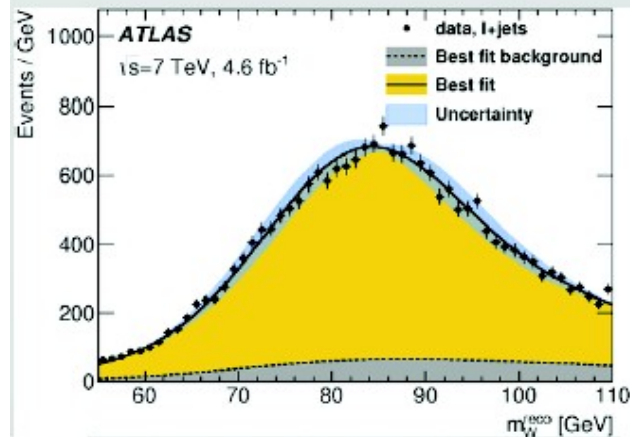
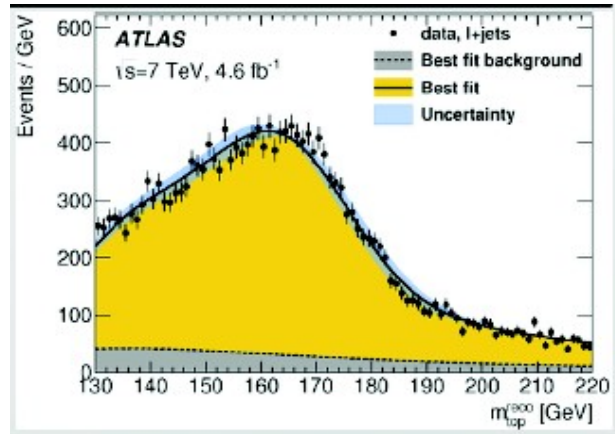
arXiv:1503.05427

$m_t^{\text{reco}}$   
 $m_W^{\text{reco}}$   
 $R_{bq}^{\text{reco}}$

$$R_{lb}^{\text{reco},2b} = \frac{p_T^{b_{\text{had}}} + p_T^{b_{\text{lep}}}}{p_T^{W_{\text{jet}1}} + p_T^{W_{\text{jet}2}}},$$

$$R_{lb}^{\text{reco},1b} = \frac{p_T^{b_{\text{tag}}}}{(p_T^{W_{\text{jet}1}} + p_T^{W_{\text{jet}2}})/2}$$

Uncertainties on JES and bJES and hadronization are reduced.



Larger unc:

- JES → 0.51 GeV
- Btag → 0.50 GeV
- ISR/FSR → 0.32 GeV

$$m_t^{MC} = 172.33 \pm 0.75 \text{ (stat + JSF + bJSF)} \pm 1.02 \text{ (syst)} \text{ GeV}$$

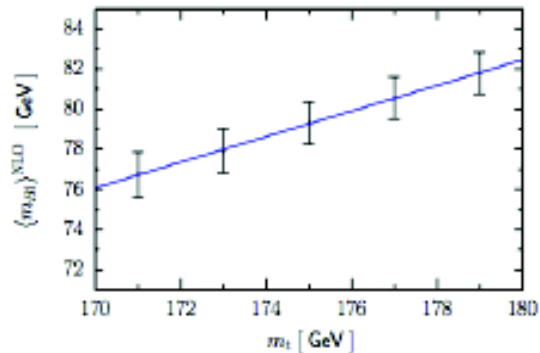
$$m_t^{MC} = 172.33 \pm 1.27 \text{ GeV}$$



# Top quark mass extraction from lepton+b-jet invariant mass

- CMS @ 8 TeV using di-lepton channel ( $\mu e$ ) :

CMS PAS-TOP-14-014



S. Biswas, K. Melnikov, M. Schulze, JHEP 1008 (2010) 048

## $\langle M_{B\ell} \rangle$ at NLO accuracy in QCD

- Theoretical predictions are forward-folded through the detector

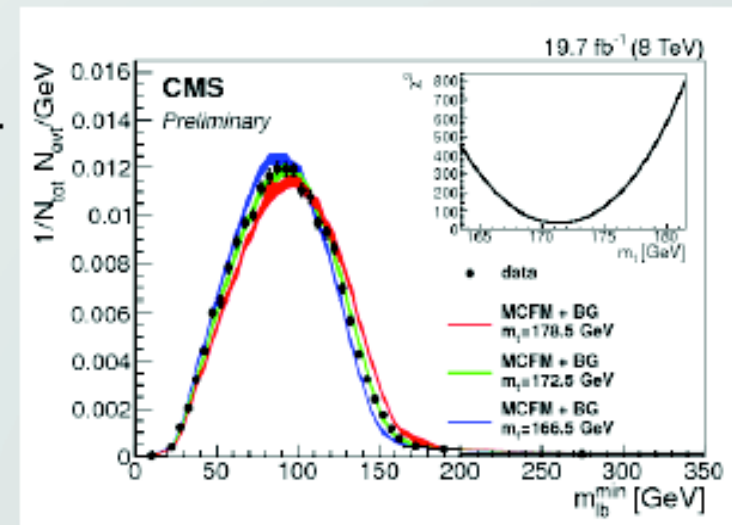
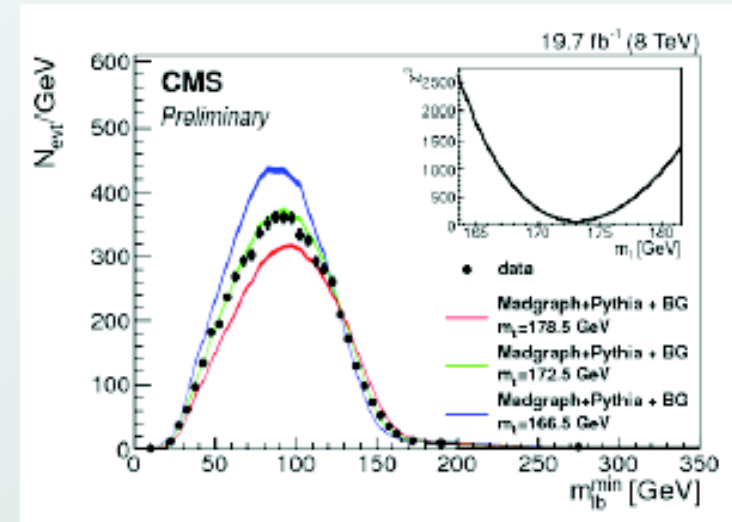
- MadGraph fit to  $m_{lb}^{reco}$  (rate and shape)

$$m_{t,8TeV}^{shape} = 172.3 \pm 0.3(stat) \pm 1.3(syst) GeV$$

- MCFM@NLO fit to  $m_{lb}^{reco}$  (NLO production, LO decay, shape)

$$m_{t,8TeV}^{shape} = 171.4 \pm 0.4(stat) \pm 1.0(syst) GeV$$

- Main uncertainties:  $\sigma(\mu_{R/F})=0.51$  GeV;  $\sigma(\text{b-frag})=0.40$  GeV



# Top quark mass extraction from lepton+b-jet invariant mass

## ATLAS measurement using dilepton channel

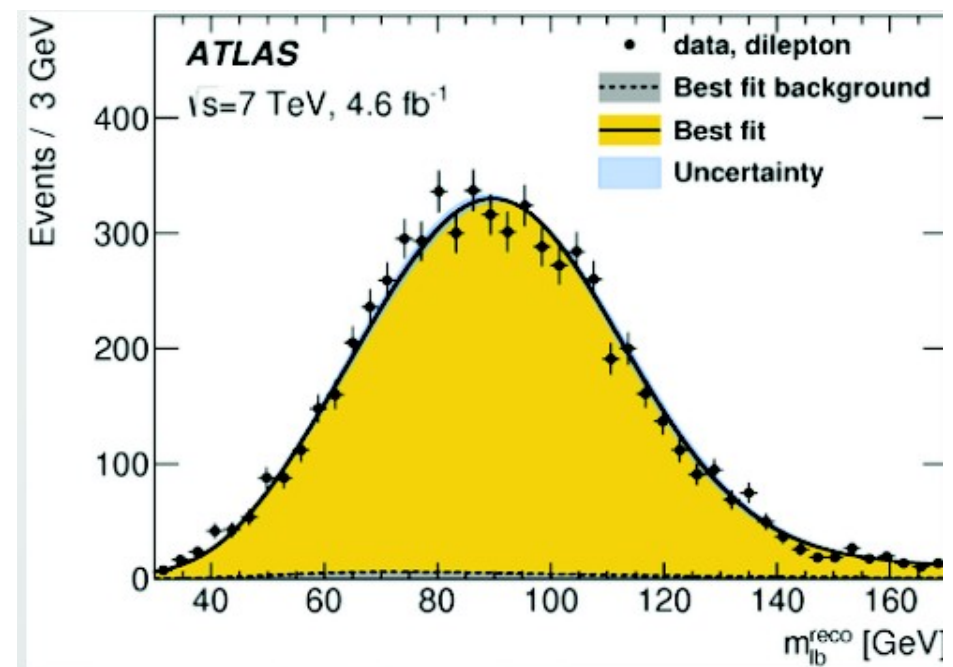
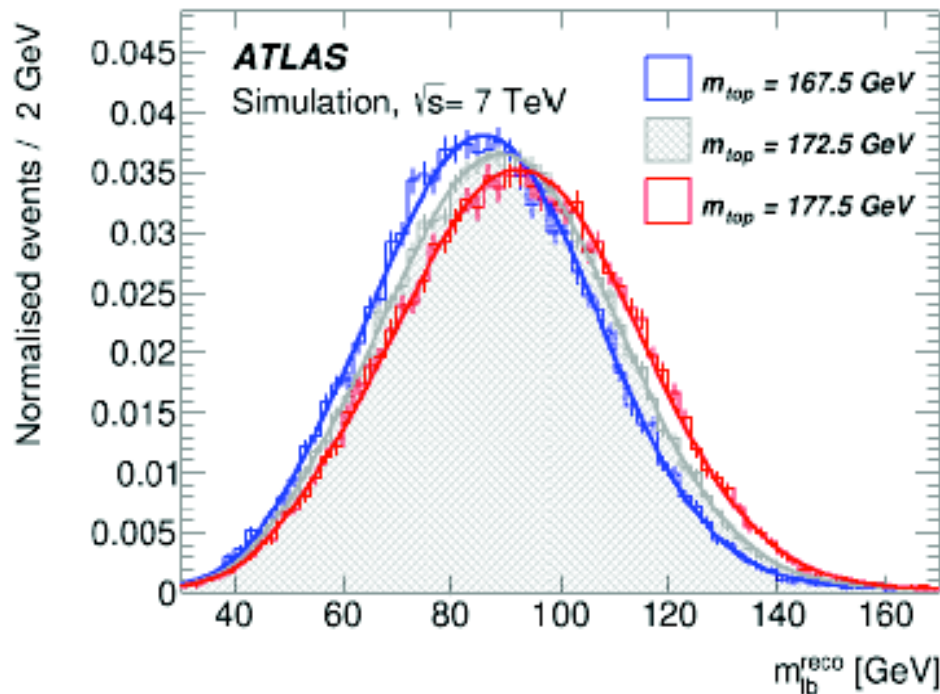
arXiv:1503.05427



dilepton channel, using 7 TeV data.

Template method fitting the  $m_{lb}^{reco}$  distribution (lepton + b-jet invariant mass)

Compared with simulations at NLO(production) with LO decay



$$m_t^{MC} = 173.79 \pm 0.54 (\text{stat}) \pm 1.30 (\text{syst}) \text{ GeV}$$

$$m_t^{MC} = 173.79 \pm 1.41 \text{ GeV}$$

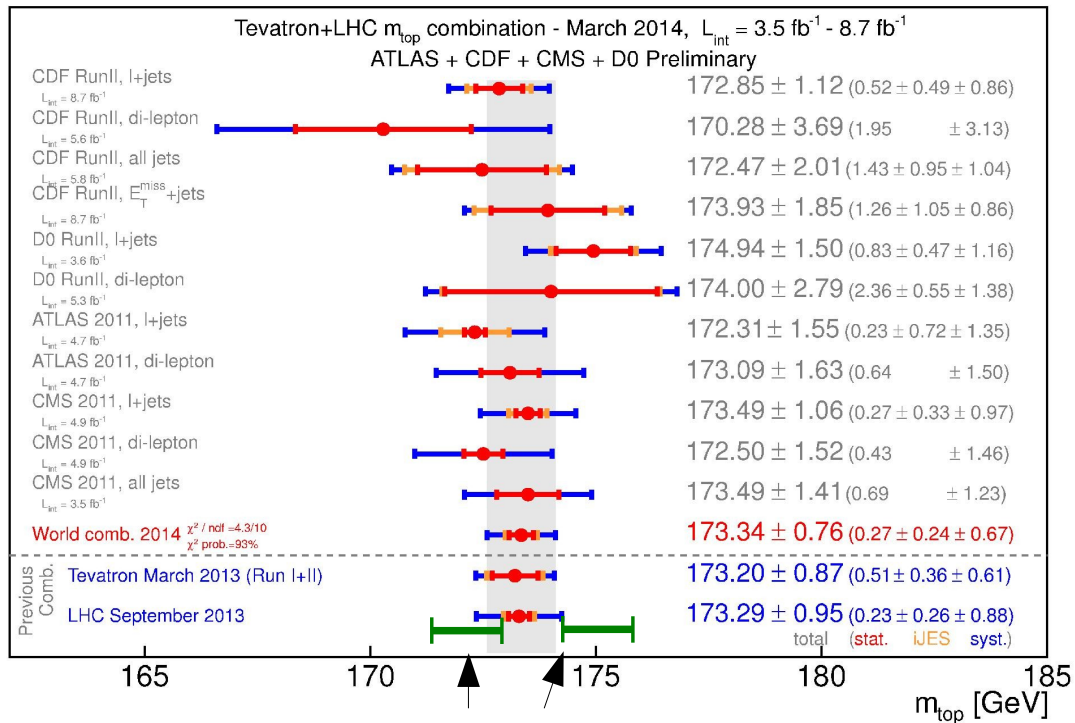
Larger unc:

**JES** → **0.75 GeV**

**Btag** → **0.68 GeV**

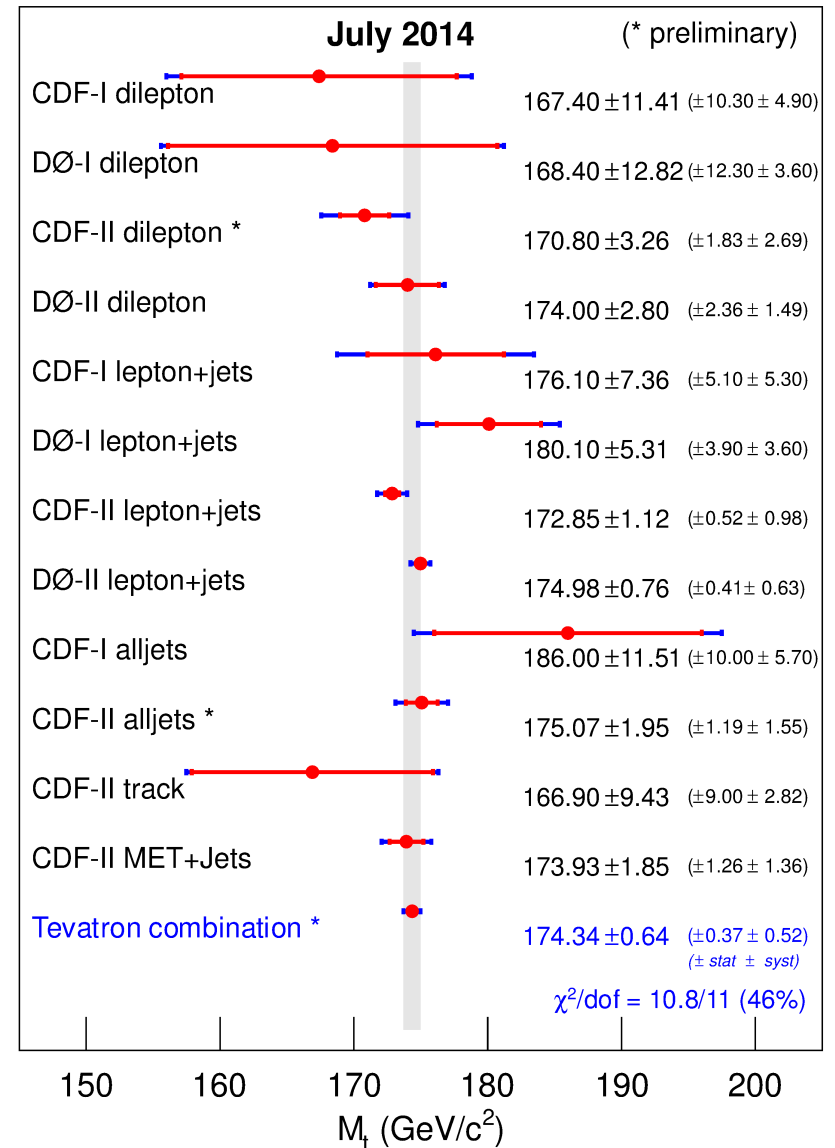
**ISR/FSR** → **0.53 GeV**

# Direct Top quark mass measurements: summary

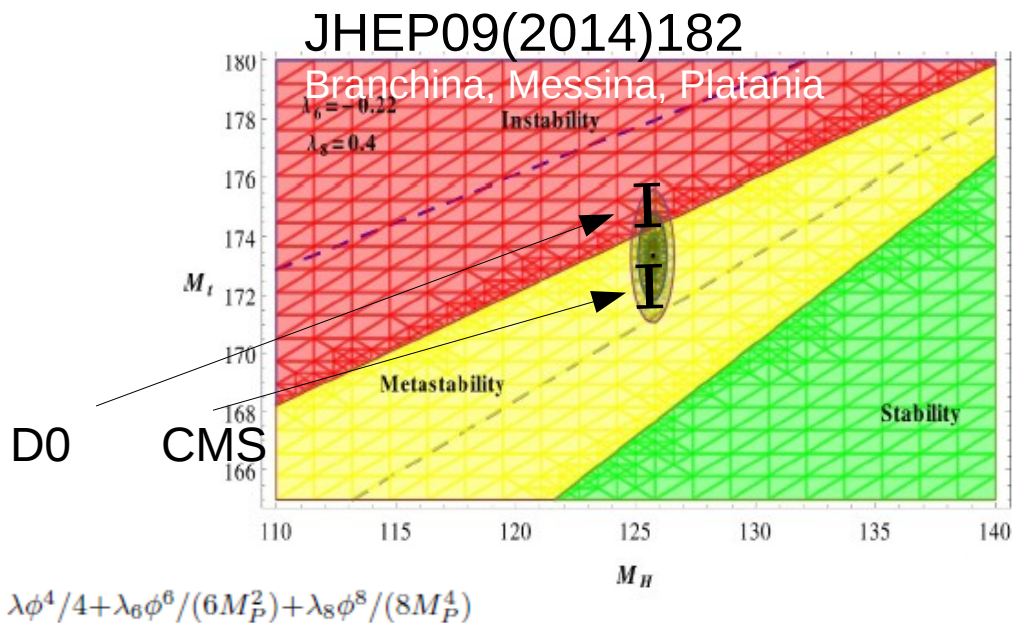
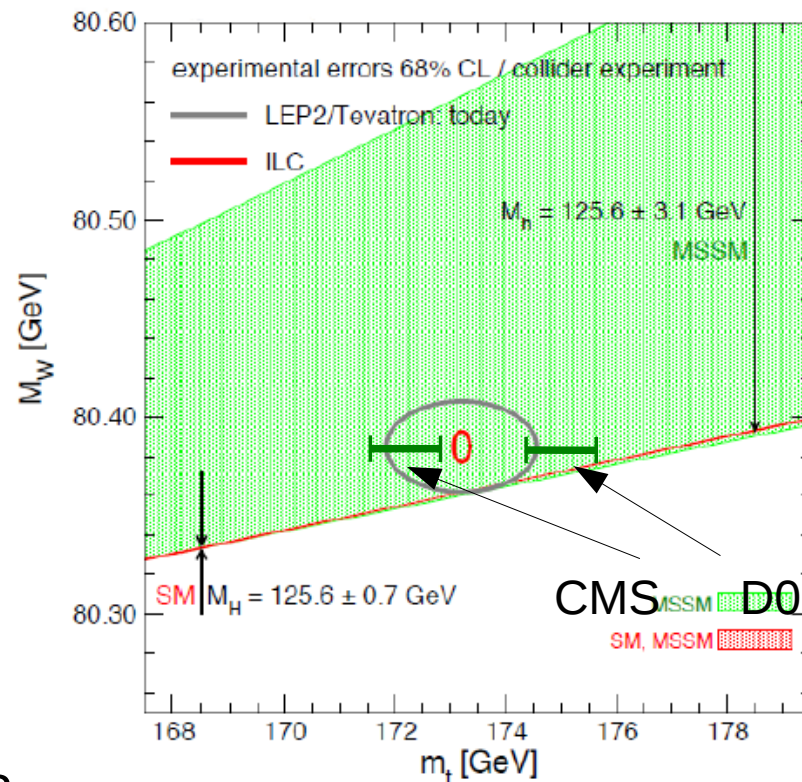
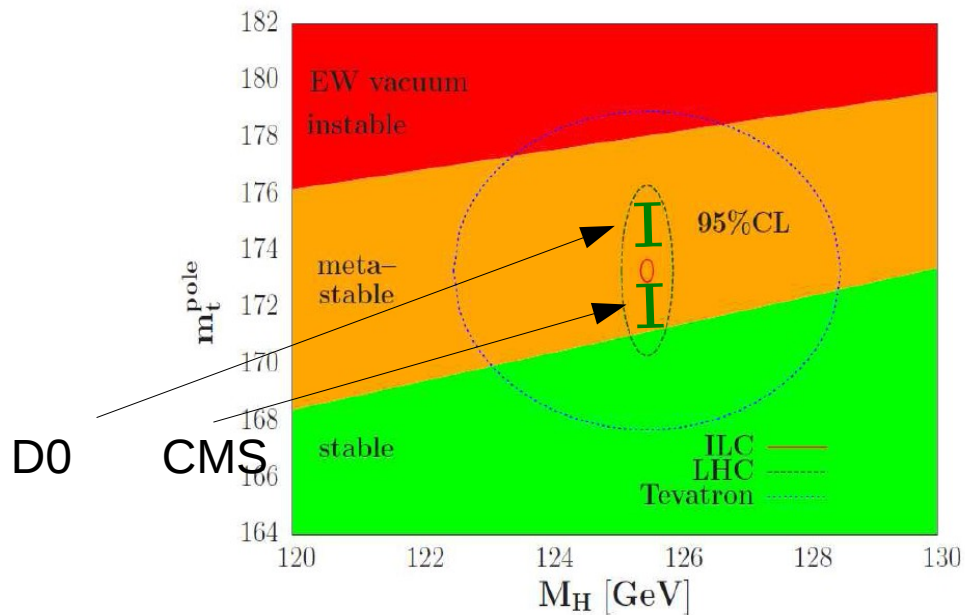


CMS D0  
Most precise individual measurements (not included in the comb.)

## Mass of the Top Quark

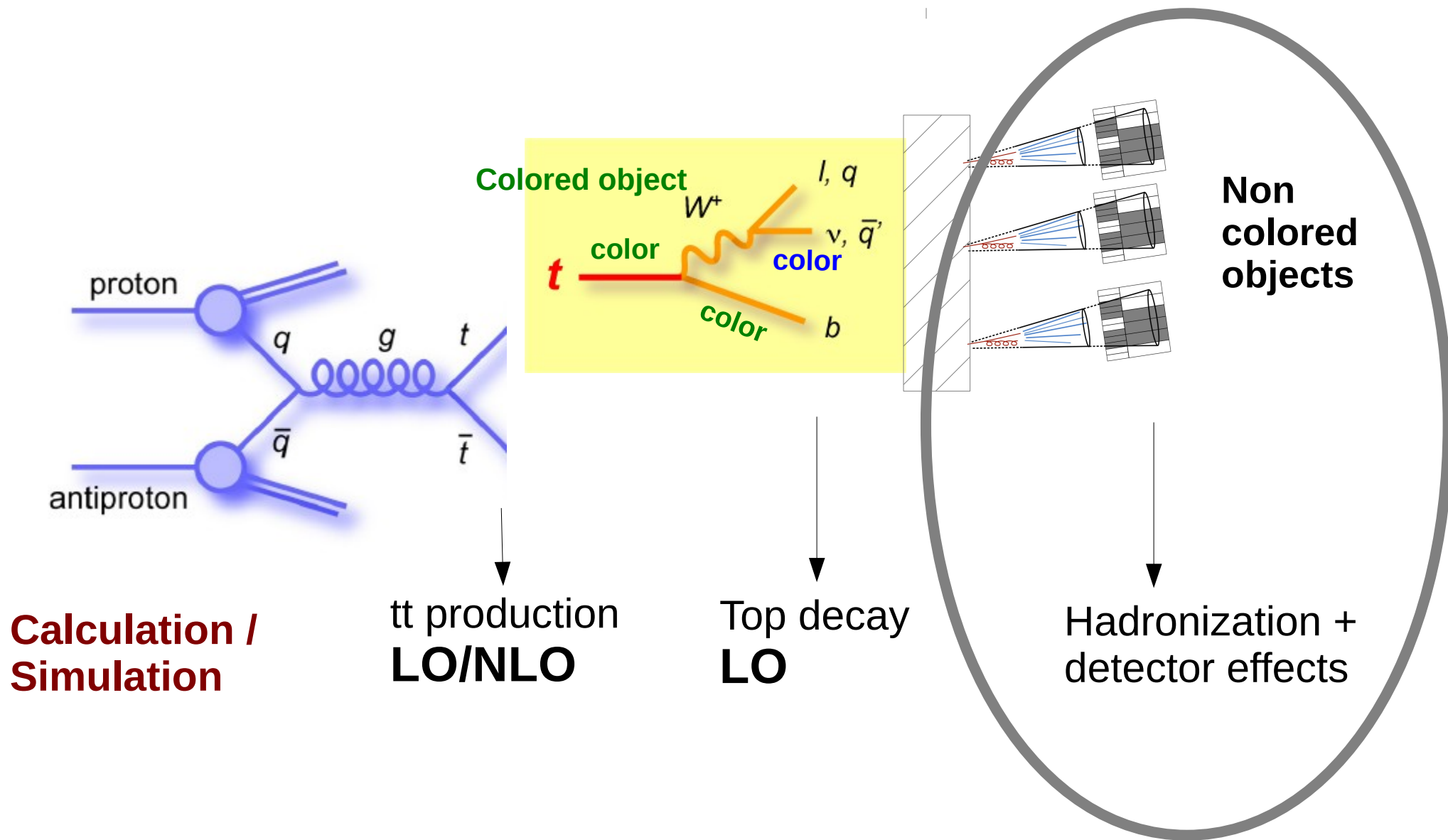


# Direct Top quark mass measurements: summary





# "Direct" Top quark mass measurements: MC tools used



The world combination achieves an improvement of the total  $m_{\text{top}}$  uncertainty of 28% relative to the most precise single input measurement [16] and  $\approx 13\%$  relative to the previous most precise combination [6]. The total uncertainty of the combination is 0.76 GeV, and is currently dominated by systematic uncertainties due to jet calibration and modelling of the  $t\bar{t}$  events. Given the current experimental uncertainty on  $m_{\text{top}}$ , clarifying the relation between the top quark mass implemented in the MC and the formal top quark pole mass demands further theoretical investigations. The dependence of the result on the correlation assumptions between mea-

## LHC/Tevatron NOTE

ATLAS-CONF-2014-008  
CDF Note 11071  
CMS PAS TOP-13-014  
D0 Note 6416

There is no well defined prescription that relates  $m_t^{\text{MC}}$  and  $m_t^{\text{pole}}$

Is the same MC mass for both colliders? And for the four experiments?

Current estimation of the uncertainty  $\sim O(1)$  GeV

Current precision in  $m_t^{\text{MC}} \sim 0.7$  GeV

- S. Moch et al., arXiv:1405.4781,
- ATLAS, CDF, CMS and D0 Collaborations, arXiv:1403.4427,
- A. H. Hoang and I. W. Stewart, 500 Nuovo Cimento B123 (2008) 1092–1100,
- A. Buckley et al., arXiv:1101.2599
- A. H. Hoang, arXiv:1412.3649.

# Requirements for a precise top quark mass determination

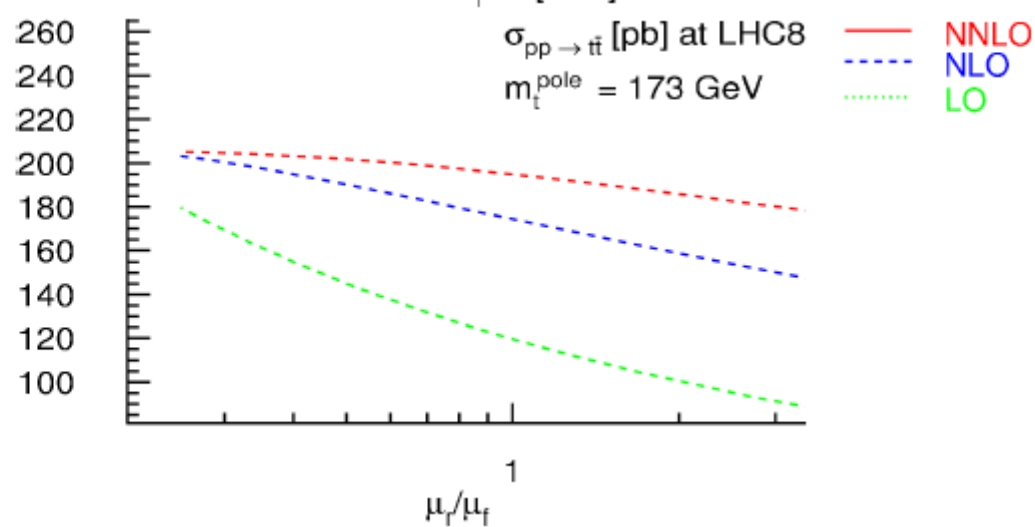
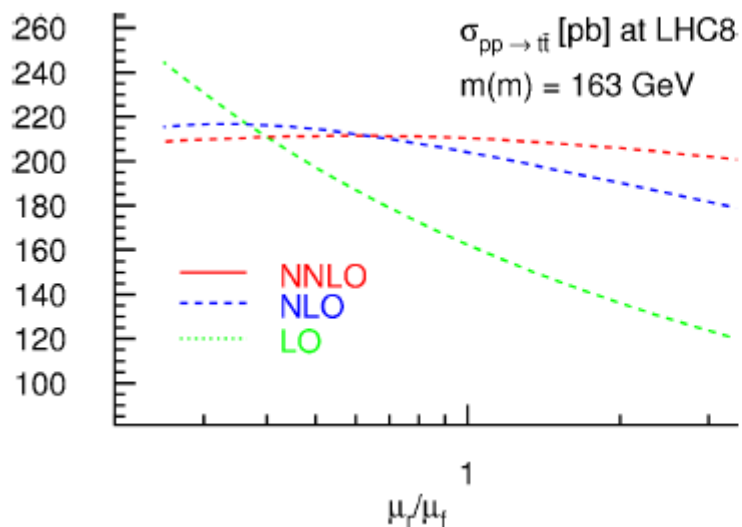
1) Define an observable which should show **good sensitivity**

$$\frac{\Delta O}{O} \leftrightarrow \frac{\Delta m_t}{m_t}$$

2) Small theoretical uncertainties.

3) Well defined **mass scheme** → **NLO calculations!**

4) Measured observables are corrected to the parton level where they are compared with calculations

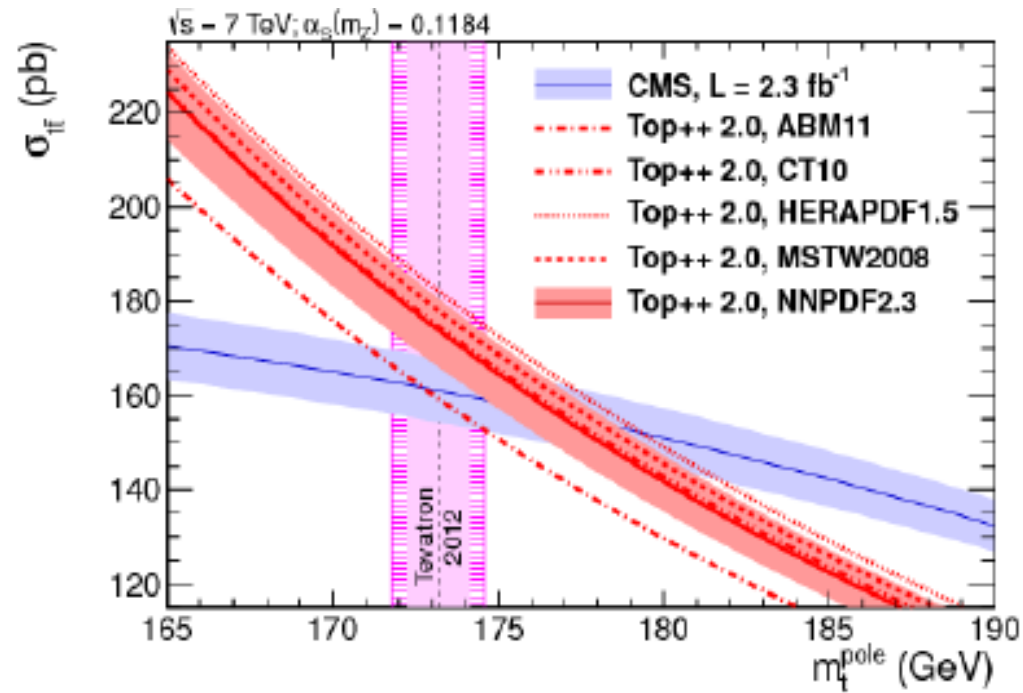


Langenfeld, Moch, Uwer PRD 80, 054009 (2009)

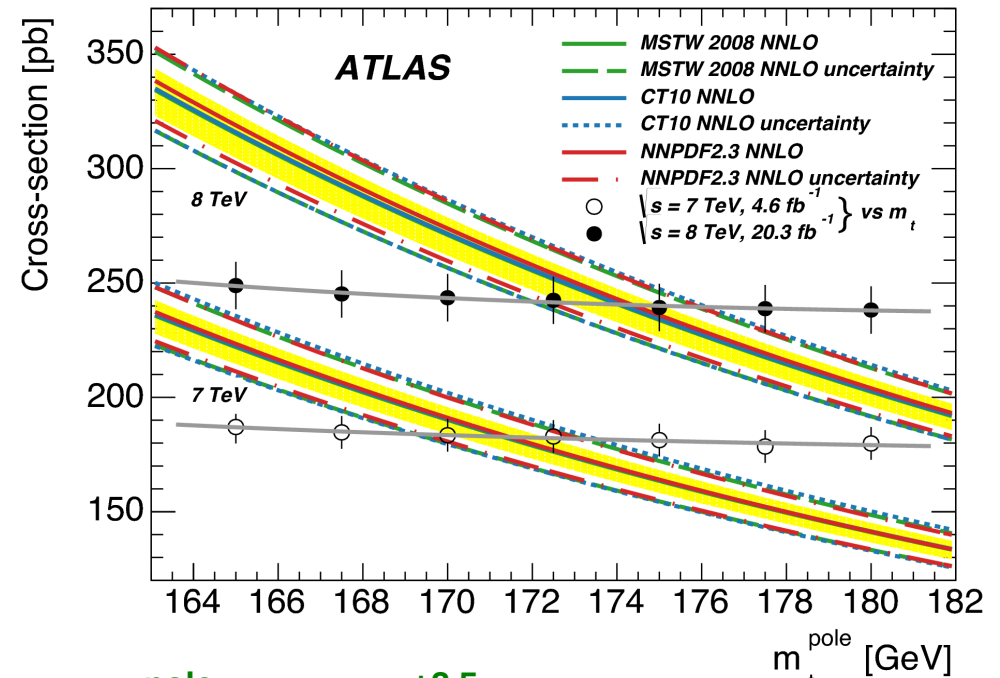
Czakon, Fiedler, Mitov hep-ph/1303.6254

P. Uwer,  
 La Thuile, Feb. 2013

# Top quark pole mass extraction from inclusive cross section



$$m_t^{\text{pole}} = 176.7^{+3.0}_{-2.8} \text{ GeV} \quad \text{CMS, Phys. Lett B 728 (2014) 496}$$



$$m_t^{\text{pole}} = 172.9^{+2.5}_{-2.6} \text{ GeV} \quad \text{ATLAS, Eur. Phys. J. C74 (2014) 3109}$$

- Dilepton channel
- MC simulations are used to correct for event efficiency selection and acceptance
- $m_t^{\text{pole}}$  inferred from the inclusive  $t\bar{t}$  cross section at NNLO(+NNLL).
- “Limited” theoretical sensitivity:  $\Delta\sigma_{tt}/\sigma_{tt} \approx -5 \Delta m_t/m_t$

Larger unc:

- PDF  $\rightarrow \sim 1.5 \text{ GeV}$
- Scale  $\rightarrow \sim 1.0 \text{ GeV}$
- Lum.  $\rightarrow \sim 0.7 \text{ GeV}$



# Top quark pole mass determination from the jet rates

$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s), \quad \rho_s = \frac{2m_0}{\sqrt{S_{t\bar{t}j}}}$$

$m_0 = 170 \text{ GeV}$

## - $t\bar{t}+1\text{-jet}$

The production of extra gluons(quarks) depend on the top-quark mass

## - differential

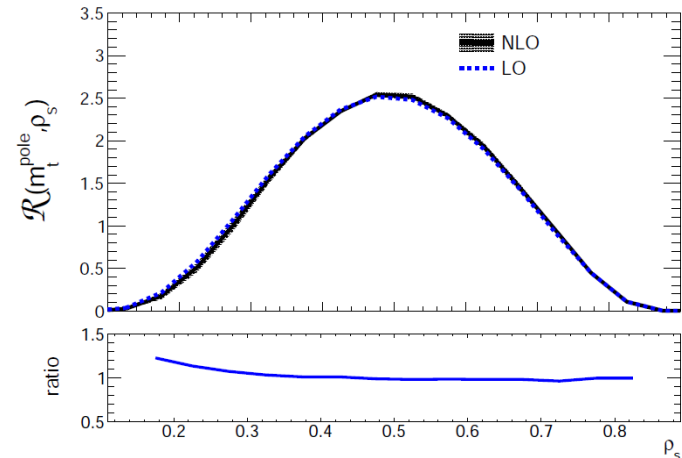
Mass dependence enhanced in certain regions of the phase space

## - normalized

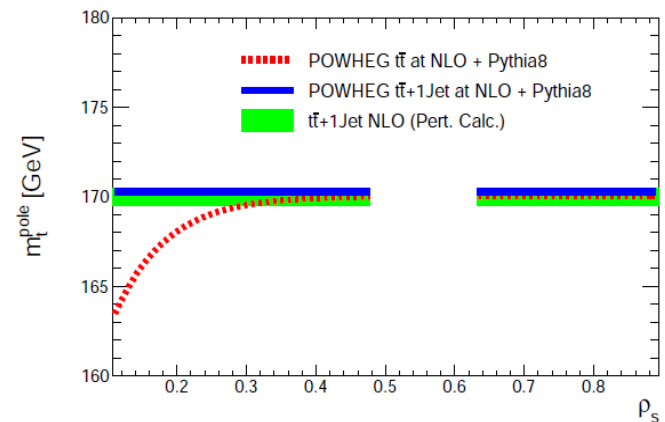
Cancelation and reduction of systematic uncertainties (theoretical and experimental)

- Large event rates at LHC ~ 30% of the inclusive cross section

- NLO & NLO+PS corrections available.



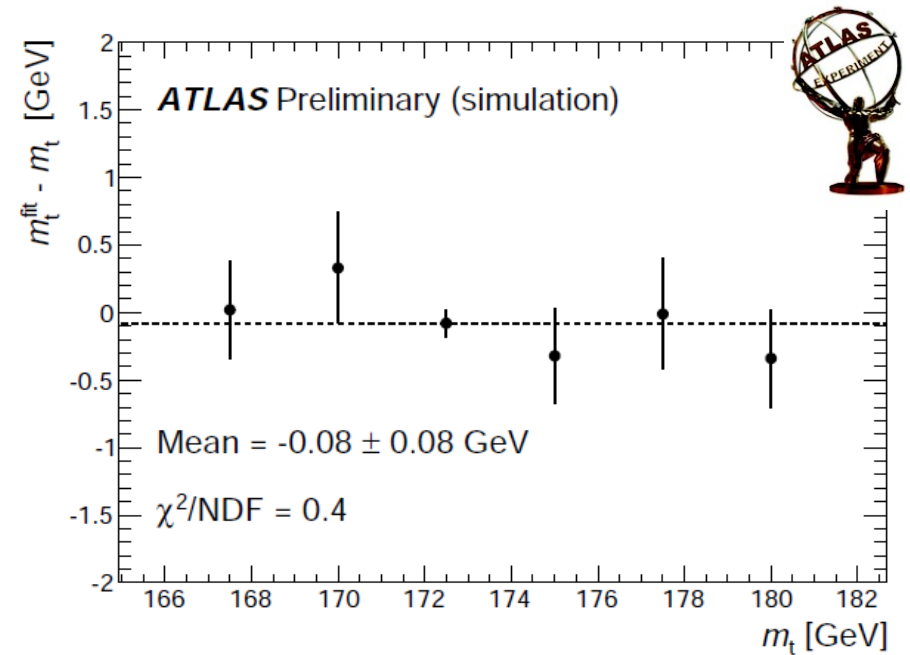
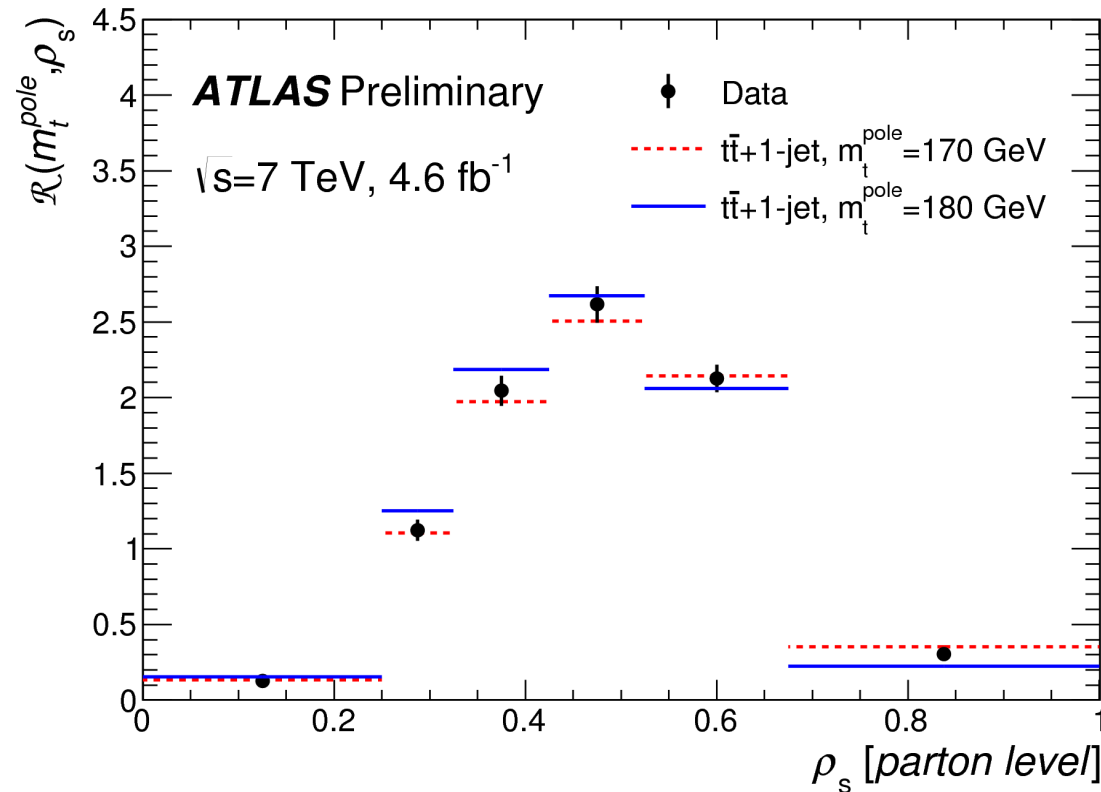
NLO → small corrections



*Eur.Phys.J. C73 (2013) 2438*<sup>17</sup>

Alioli, Fernández, Fuster, A.I., Moch, Uwer, Vos

# Top quark pole mass determination from the jet rates



$$m_t^{\text{pole}} = 173.7^{+2.3}_{-2.1} \text{ GeV}$$

ATLAS CONF 2014-053

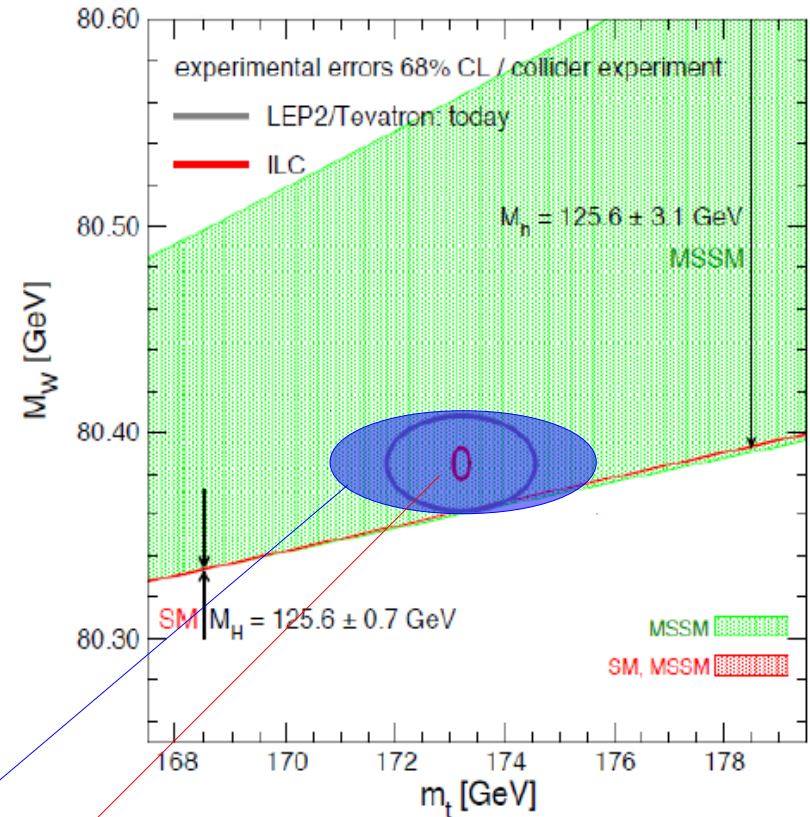
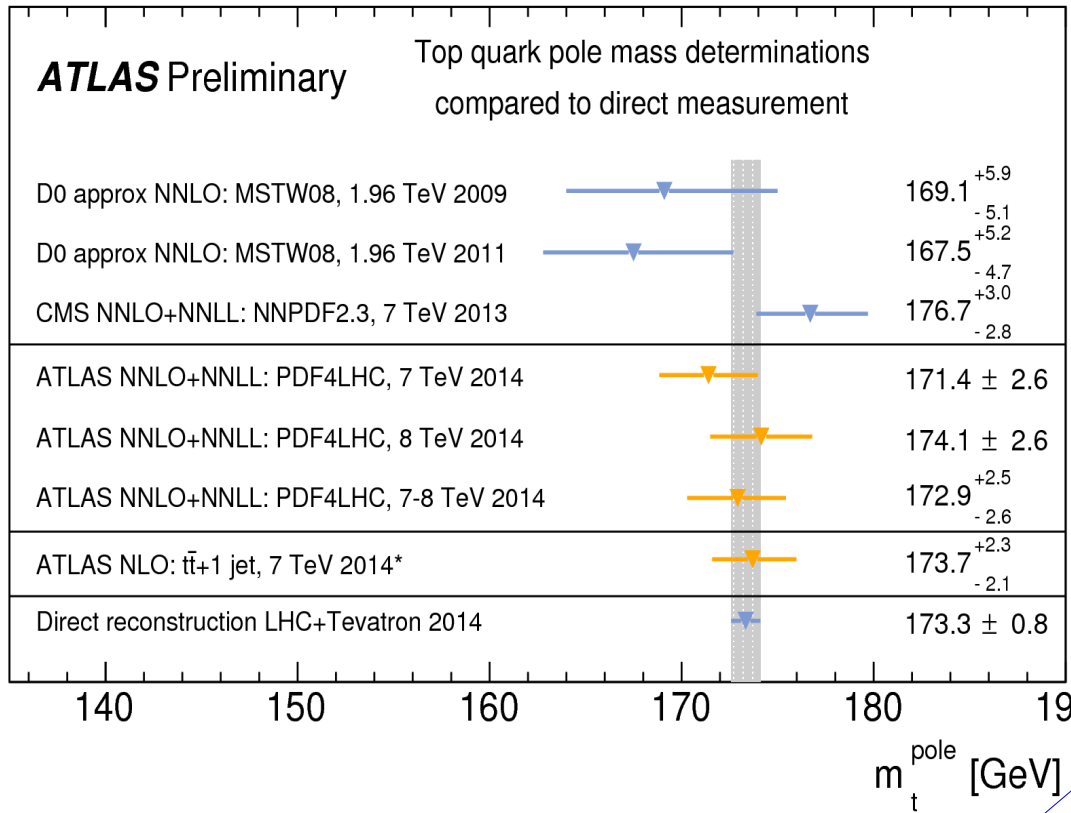
- ATLAS 7 TeV, semileptonic decay
- MC simulations are used to correct to parton level for event efficiency selection and acceptance
- $m_t^{\text{pole}}$  inferred from the  $t\bar{t}+1\text{Jet}$  cross section at NLO(+PS) with  $p_T(\text{Jet}) > 50$  GeV.
- No dependence on the MC mass used in the correction procedure

Larger unc:

**JES** → **0.94 GeV**  
**ISR/FSR** → **0.72 GeV**  
**Scale** → **0.93 GeV**

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# Top quark pole mass determination: summary



Best top-quark pole mass measurement so far.

ILC prospects

[Heinemeyer et al updated to summer 2014] + “non authorised” ellipses

- **Precise top quark mass** determinations are mandatory to **test and probe the SM** and BSM.
- Current direct top quark **kinematic mass** determinations reach **precisions better than 0.5%...**
  - What is its **interpretation**?
  - What is the **theoretical uncertainty** associated to this interpretations?
- **Unambiguously scheme defined top quark mass determinations** need to compare measurements with **NLO calculations**.
  - Theoretical uncertainties of the order of 1-1.8 GeV
  - Traditionally, less precise (experimentally) methods.
  - Last results show great advances in the increase of experimental precision of these methods.

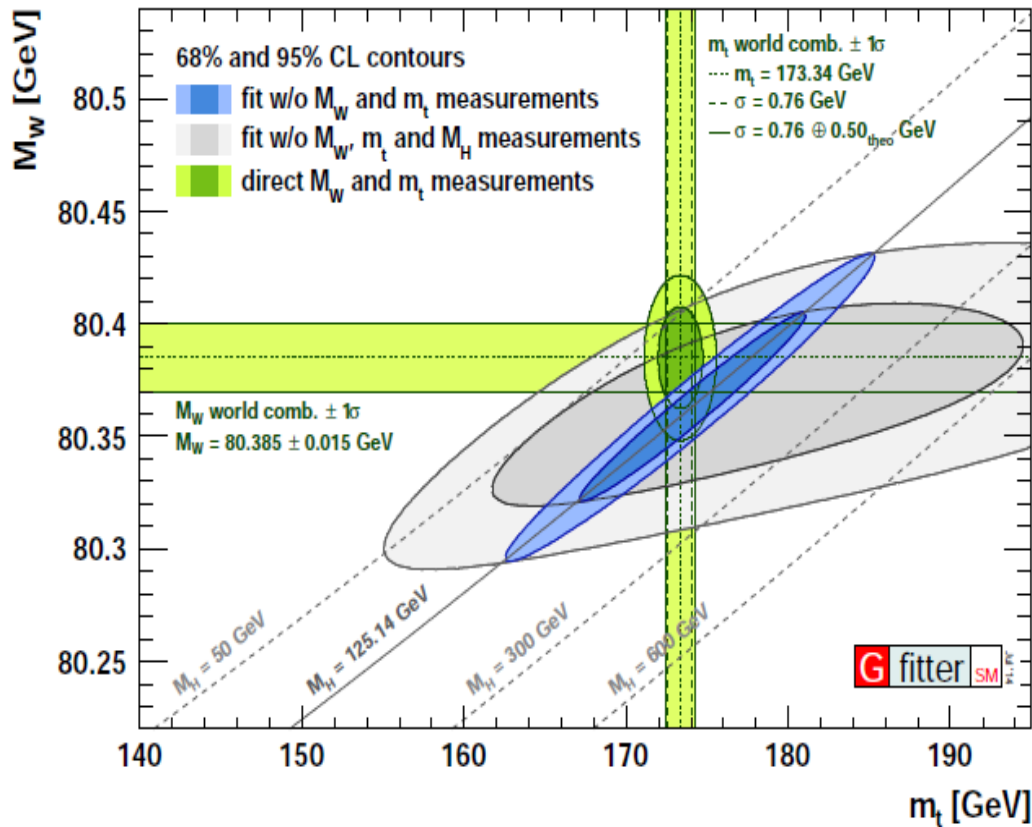


*Thanks to J. Fuster, A. Jung, M. Vos and many others for interesting discussions and the slides that I've borrow from them*

**Back up slides**

# The top-quark mass: why so important?

## SM consistency



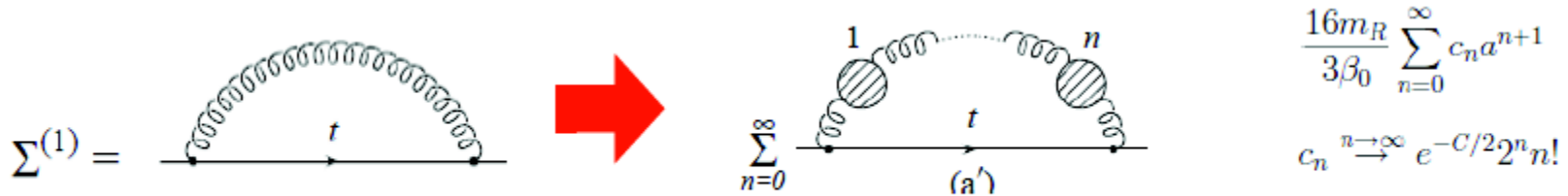
Enter in all loop corrections  
(reduce parametric uncertainty)

Relation H, W, t mass → EW fit  
(SM and BSM)

$$M_W = M_W^{LO} + \Delta r_{top} + \Delta r_H$$

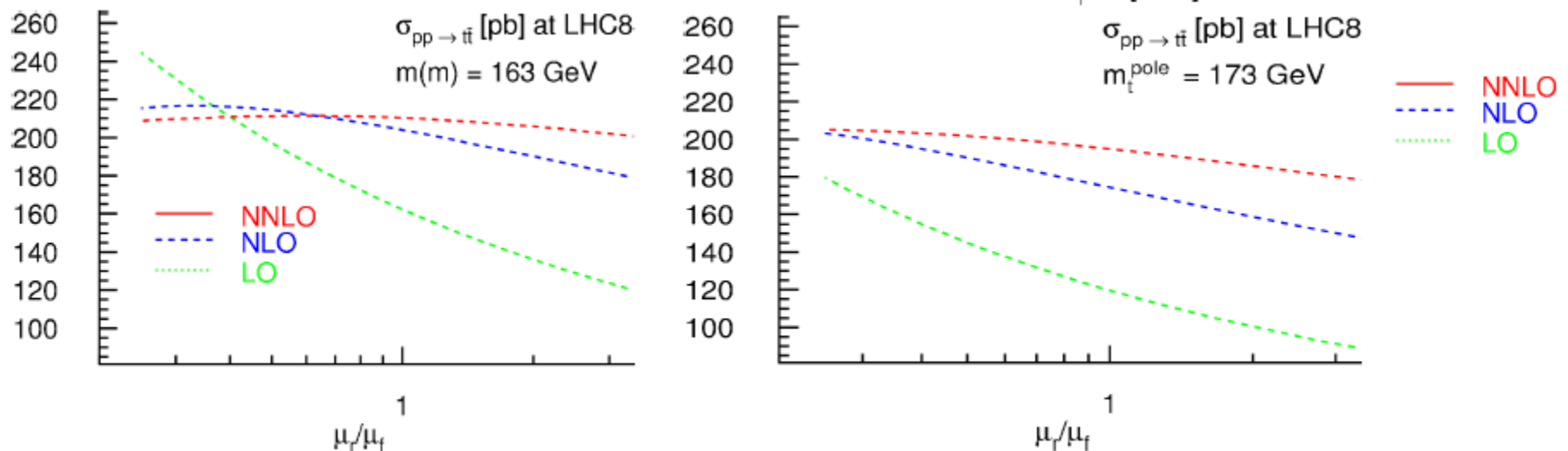
$$\Delta r_{top} \simeq -\frac{3G_F m_t^2}{8\sqrt{2}\pi^2} \frac{1}{\tan\theta_W}$$

$$\Delta r_H \simeq \frac{11G_F M_Z^2 \cos\theta_W}{24\sqrt{2}\pi^2} \ln \frac{M_H^2}{M_Z^2}$$



[Bigi, Shifman, Uraltsev, Vainshtein 94 Beneke, Braun,94 Smith, Willenbrock 97]

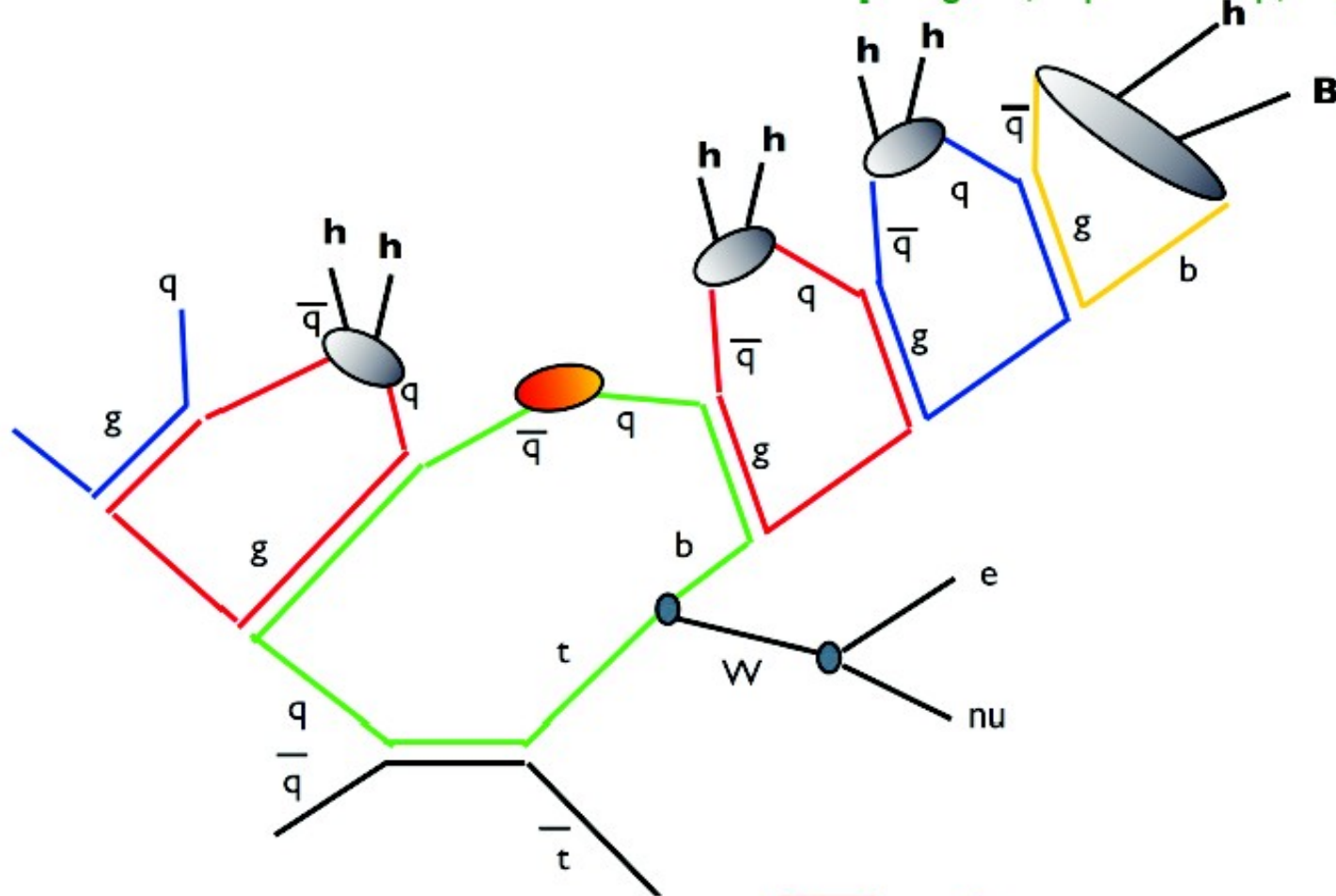
Pole mass has an intrinsic ambiguity of the order of  $\Lambda_{\text{QCD}}$



Running mass definition provides better perturbative stability (tt)

# What is it measured?

[Mangano, Top workshop, July 2012, CERN]



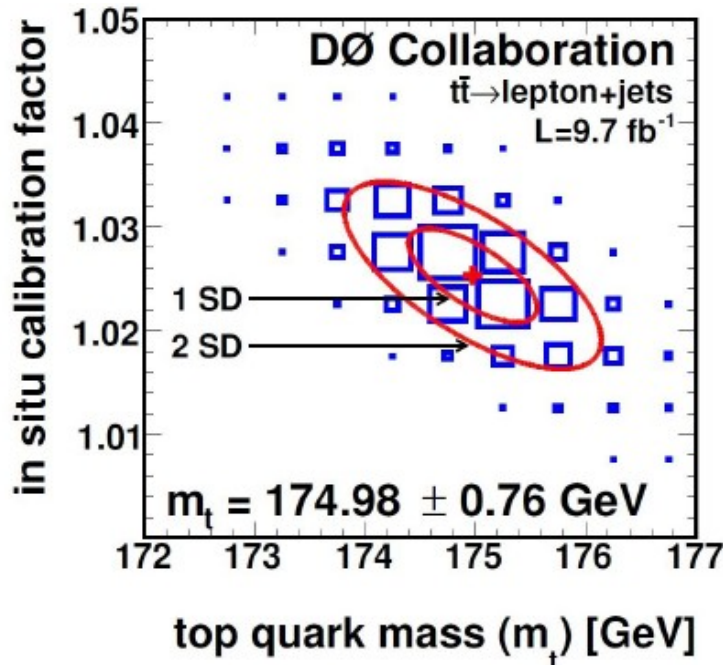
$$p_t \neq p_W + \sum_i p_{\text{had}}^i$$



# Direct top quark mass measurements: Matrix Element



## Most precise measurement at Tevatron



Source of uncertainty	Effect on $m_t$ (GeV)
<i>Signal and background modeling:</i>	
Higher order corrections	+0.15
Initial/final state radiation	$\pm 0.09$
Hadronization and UE	+0.26
Color reconnection	+0.10
Multiple $p\bar{p}$ interactions	-0.06
Heavy flavor scale factor	$\pm 0.06$
$b$ -jet modeling	+0.09
PDF uncertainty	$\pm 0.11$
<i>Detector modeling:</i>	
Residual jet energy scale	$\pm 0.21$
Flavor-dependent response to jets	$\pm 0.16$
$b$ tagging	$\pm 0.10$
Trigger	$\pm 0.01$
Lepton momentum scale	$\pm 0.01$
Jet energy resolution	$\pm 0.07$
Jet ID efficiency	-0.01
<i>Method:</i>	
Modeling of multijet events	+0.04
Signal fraction	$\pm 0.08$
MC calibration	$\pm 0.07$
<i>Total systematic uncertainty</i>	$\pm 0.49$
<i>Total statistical uncertainty</i>	$\pm 0.58$
<i>Total uncertainty</i>	$\pm 0.76$

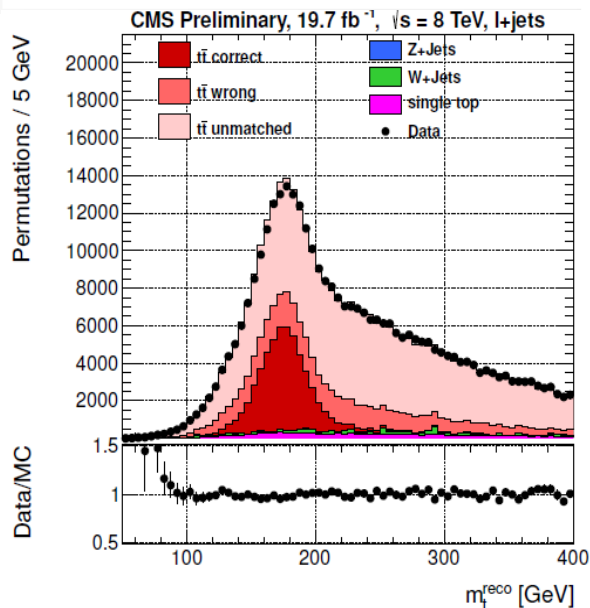
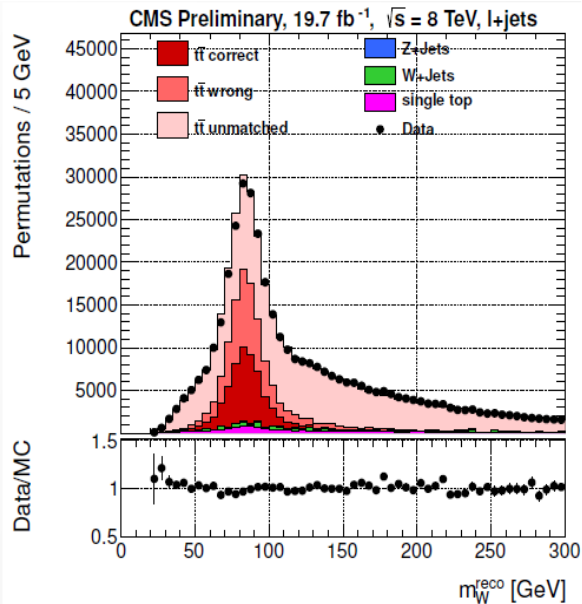
TABLE I: Summary of uncertainties on the measured top quark mass. The signs indicate the direction of the change in  $m_t$  when replacing the default by the alternative model.

# Direct top quark mass measurements: Ideogram Method

## Most precise measurement at the LHC

Table 1: List of systematic uncertainties for the combined fit to the entire lepton+jets data set.

	$\delta m_t^{2D}$ (GeV)	$\delta JSF$	$\delta m_t^{1D}$ (GeV)
<b>Experimental uncertainties</b>			
Fit calibration	0.10	0.001	0.06
$p_T$ - and $\eta$ -dependent JES	0.18	0.007	1.17
Lepton energy scale	0.03	<0.001	0.03
MET	0.09	0.001	0.01
Jet energy resolution	0.26	0.004	0.07
b tagging	0.02	<0.001	0.01
Pileup	0.27	0.005	0.17
Non- $t\bar{t}$ background	0.11	0.001	0.01
<b>Modeling of hadronization</b>			
Flavor-dependent JSF	0.41	0.004	0.32
b fragmentation	0.06	0.001	0.04
Semi-leptonic B hadron decays	0.16	<0.001	0.15
<b>Modeling of the hard scattering process</b>			
PDF	0.09	0.001	0.05
Renormalization and factorization scales	$0.12 \pm 0.13$	$0.004 \pm 0.001$	$0.25 \pm 0.08$
ME-PS matching threshold	$0.15 \pm 0.13$	$0.003 \pm 0.001$	$0.07 \pm 0.08$
ME generator	$0.23 \pm 0.14$	$0.003 \pm 0.001$	$0.20 \pm 0.08$
<b>Modeling of non-perturbative QCD</b>			
Underlying event	$0.14 \pm 0.17$	$0.002 \pm 0.002$	$0.06 \pm 0.10$
Color reconnection modeling	$0.08 \pm 0.15$	$0.002 \pm 0.001$	$0.07 \pm 0.09$
<b>Total</b>	<b>0.75</b>	<b>0.012</b>	<b>1.29</b>



$$m_t^{MC} = 172.04 \pm 0.19 (stat + JSF) \pm 0.75 (syst) GeV$$

$$m_t^{MC} = 172.04 \pm 0.77 GeV$$



# Direct top quark mass measurements: Template Method



	$t\bar{t} \rightarrow \text{lepton+jets}$			$t\bar{t} \rightarrow \text{dilepton}$	Combination	
	$m_{\text{top}}^{l+jets}$ [GeV]	JSF	bJSF	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{comb}}$ [GeV]	$\rho$
Results	172.33	1.019	1.003	173.79	172.99	
Statistics	0.75	0.003	0.008	0.54	0.48	0
– Stat. comp. ( $m_{\text{top}}$ )	0.23	n/a	n/a	0.54		
– Stat. comp. (JSF)	0.25	0.003	n/a	n/a		
– Stat. comp. (bJSF)	0.67	0.000	0.008	n/a		
Method	$0.11 \pm 0.10$	0.001	0.001	$0.09 \pm 0.07$	0.07	0
Signal MC	$0.22 \pm 0.21$	0.004	0.002	$0.26 \pm 0.16$	0.24	+1.00
Hadronisation	$0.18 \pm 0.12$	0.007	0.013	$0.53 \pm 0.09$	0.34	+1.00
ISR/FSR	$0.32 \pm 0.06$	0.017	0.007	$0.47 \pm 0.05$	0.04	–1.00
Underlying event	$0.15 \pm 0.07$	0.001	0.003	$0.05 \pm 0.05$	0.06	–1.00
Colour reconnection	$0.11 \pm 0.07$	0.001	0.002	$0.14 \pm 0.05$	0.01	–1.00
PDF	$0.25 \pm 0.00$	0.001	0.002	$0.11 \pm 0.00$	0.17	+0.57
W/Z+jets norm	$0.02 \pm 0.00$	0.000	0.000	$0.01 \pm 0.00$	0.02	+1.00
W/Z+jets shape	$0.29 \pm 0.00$	0.000	0.004	$0.00 \pm 0.00$	0.16	0
NP/fake-lepton norm.	$0.10 \pm 0.00$	0.000	0.001	$0.04 \pm 0.00$	0.07	+1.00
NP/fake-lepton shape	$0.05 \pm 0.00$	0.000	0.001	$0.01 \pm 0.00$	0.03	+0.23
Jet energy scale	$0.58 \pm 0.11$	0.018	0.009	$0.75 \pm 0.08$	0.41	–0.23
$b$ -jet energy scale	$0.06 \pm 0.03$	0.000	0.010	$0.68 \pm 0.02$	0.34	+1.00
Jet resolution	$0.22 \pm 0.11$	0.007	0.001	$0.19 \pm 0.04$	0.03	–1.00
Jet efficiency	$0.12 \pm 0.00$	0.000	0.002	$0.07 \pm 0.00$	0.10	+1.00
Jet vertex fraction	$0.01 \pm 0.00$	0.000	0.000	$0.00 \pm 0.00$	0.00	–1.00
$b$ -tagging	$0.50 \pm 0.00$	0.001	0.007	$0.07 \pm 0.00$	0.25	–0.77
$E_{\text{T}}^{\text{miss}}$	$0.15 \pm 0.04$	0.000	0.001	$0.04 \pm 0.03$	0.08	–0.15
Leptons	$0.04 \pm 0.00$	0.001	0.001	$0.13 \pm 0.00$	0.05	–0.34
Pile-up	$0.02 \pm 0.01$	0.000	0.000	$0.01 \pm 0.00$	0.01	0
Total	$1.27 \pm 0.33$	0.027	0.024	$1.41 \pm 0.24$	0.91	–0.07

Table 3: The measured values of  $m_{\text{top}}$  and the contributions of various sources to the uncertainty in the  $t\bar{t} \rightarrow \text{lepton+jets}$  and the  $t\bar{t} \rightarrow \text{dilepton}$  analyses. The corresponding uncertainties in the measured values of the JSF and bJSF are also shown for the  $t\bar{t} \rightarrow \text{lepton+jets}$  analysis. The statistical uncertainties associated with these values are typically 0.001 or smaller. The result of the  $m_{\text{top}}$  combination is shown in the rightmost columns, together with the correlation ( $\rho$ ) within each uncertainty group as described in Sect. 8. The symbol n/a stands for not applicable. Values quoted as 0.00 are smaller than 0.005. Finally, the last line refers to the sum in quadrature of the statistical and systematic uncertainty components.



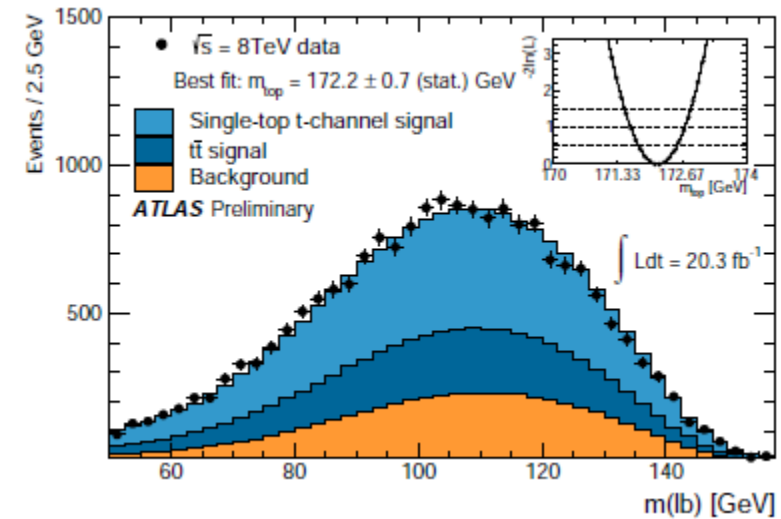
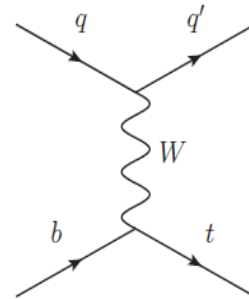
# Alternative measurements

## Using single-top events (t-channel)

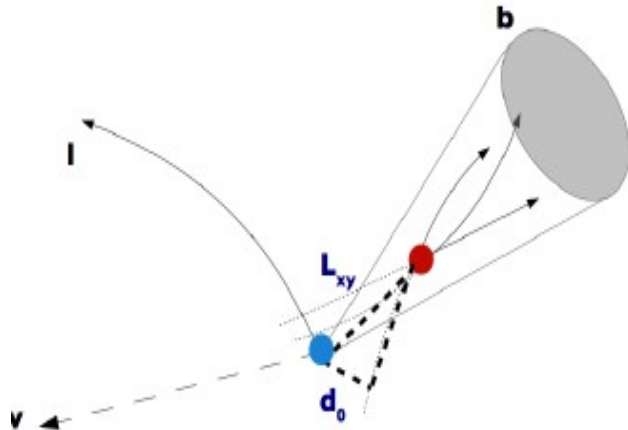
dominant systematic uncertainties:

- ▷ JES (1.5 GeV)
- ▷ (*t*-channel) hadronisation (0.7 GeV)
- ▷ background (0.6 GeV)

ATLAS-CONF-2014-055



## B-hadron Lifetime / lepton p<sub>T</sub>



Phys.Rev.D81 032002 (2010)

$$m_t = 170.7 \pm 6.3 \text{ (stat.)} \pm 2.6 \text{ (syst.) GeV}$$

Simultaneous fit to both kin. distributions **CDF**

CMS PAS TOP-12-030

$$m_t = 173.5 \pm 1.5 \text{ (stat.)} \pm 1.3 \text{ (syst.)} \pm 2.6 \text{ (} p_T^{\text{top}} \text{) GeV}$$

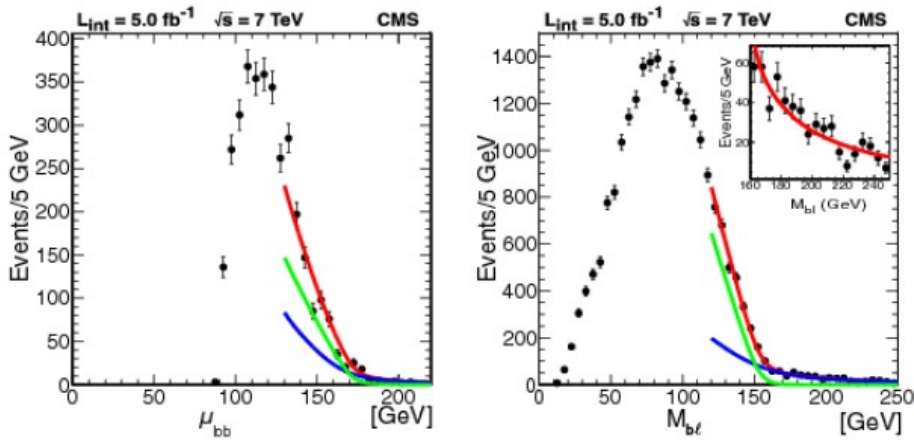
- ▷ dominant sources of systematic uncertainty:

- ▷ top  $p_T$  modelling
- ▷ background in  $\ell + \text{jets}$
- ▷ hadronisation model

Fit to median  $L_{xy}$  **CMS**

# Alternative measurements

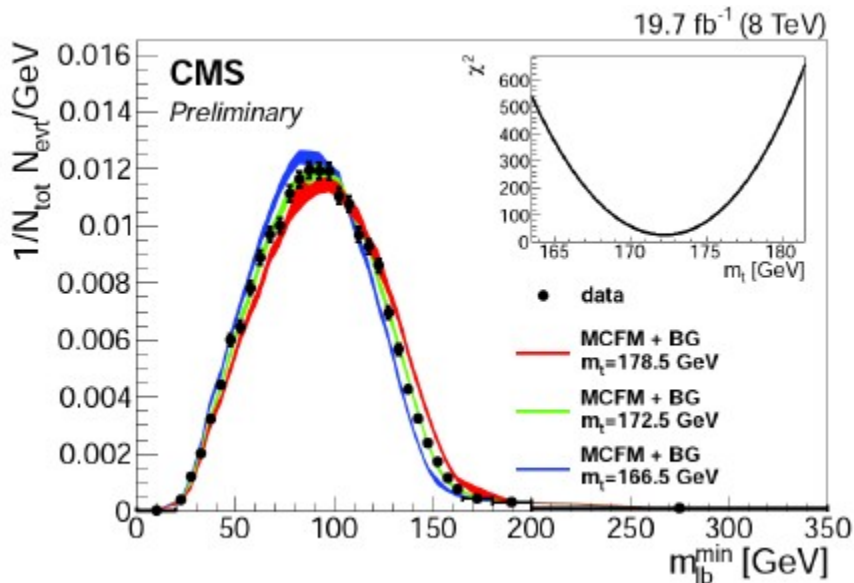
## Kinematic endpoints



$$m_t = 173.9 \pm 0.9 \text{ (stat.)}_{-2.2}^{+1.7} \text{ (syst.) GeV}$$

Eur. Phys. J. C 73 (2013) 2494

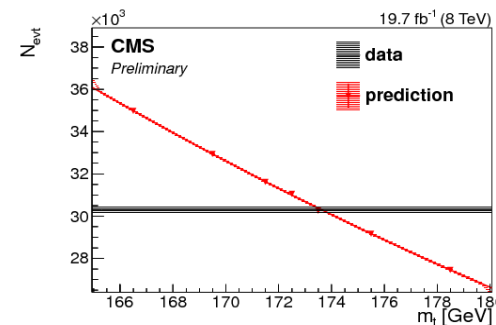
## Mlb and forward folding



$$\vec{X}_{reco} = \mathcal{L} \mathcal{M}^{resp} \vec{X}_{pred} \quad m_t = 171.4_{-1.1}^{+1.0} \text{ GeV}$$

From the rate

$$m_t = 173.7_{-3.4}^{+3.5} \text{ GeV}$$



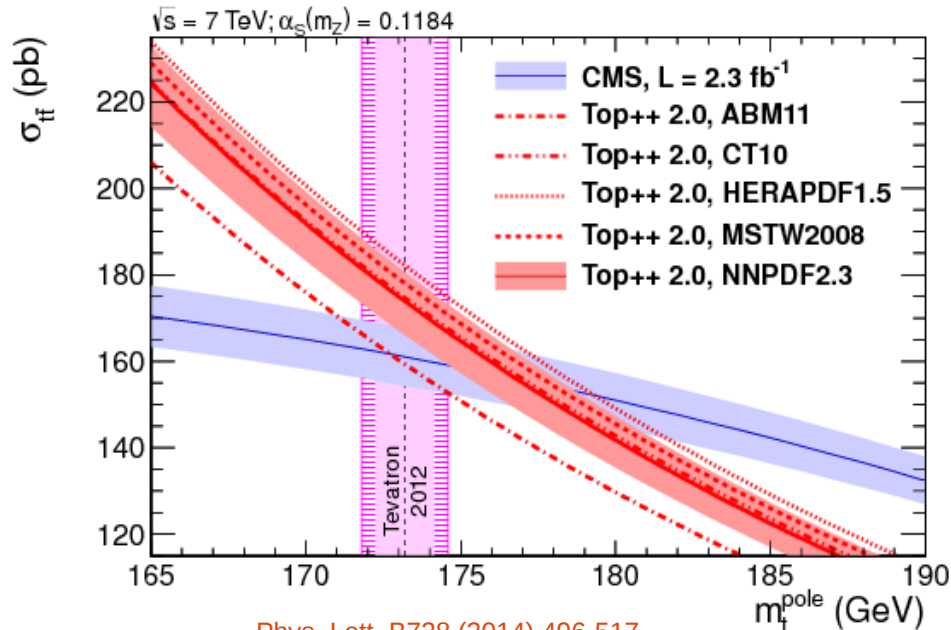
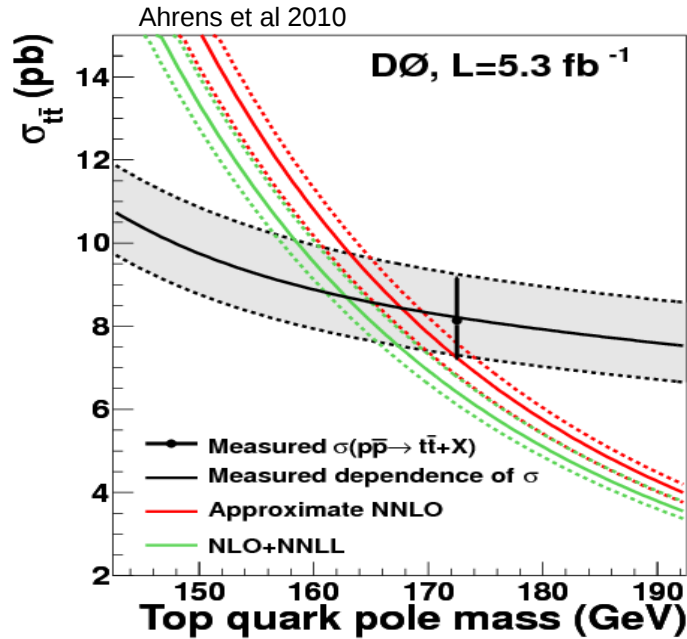
CMS PAS TOP-14-014

S. Adomeit Top14



# Mt from cross section

Langenfeld U Moch S and Uwer P 2009



Phys. Lett. B728 (2014) 496-517

$\sqrt{s}$ Uncertainty (inclusive $\sigma_{t\bar{t}}$ )	$\Delta\epsilon_{e\mu}/\epsilon_{e\mu}$ (%)	7 TeV $\Delta C_b/C_b$ (%)	$\Delta\sigma_{t\bar{t}}/\sigma_{t\bar{t}}$ (%)
Data statistics			1.69
$t\bar{t}$ modelling	0.71	-0.72	1.43
Parton distribution functions	1.03	-	1.04
QCD scale choice	0.30	-	0.30
Single-top modelling	-	-	0.34
Single-top/ $t\bar{t}$ interference	-	-	0.22
Single-top $Wt$ cross-section	-	-	0.72
Diboson modelling	-	-	0.12
Diboson cross-sections	-	-	0.03
$Z$ +jets extrapolation	-	-	0.05
Electron energy scale/resolution	0.19	-0.00	0.22
Electron identification	0.12	0.00	0.13
Muon momentum scale/resolution	0.12	0.00	0.14
Muon identification	0.27	0.00	0.30
Lepton isolation	0.74	-	0.74
Lepton trigger	0.15	-0.02	0.19
Jet energy scale	0.22	0.06	0.27
Jet energy resolution	-0.16	0.08	0.30
Jet reconstruction/vertex fraction	0.00	0.00	0.06
$b$ -tagging	-	0.18	0.41
Misidentified leptons	-	-	0.41
Analysis systematics ( $\sigma_{t\bar{t}}$ )	1.56	0.75	2.27
Integrated luminosity	-	-	1.98
LHC beam energy	-	-	1.79
Total uncertainty ( $\sigma_{t\bar{t}}$ )	1.56	0.75	3.89

Eur.Phys.J. C74 (2014) 3109

# The R observable: calculations

$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s), \quad \rho_s = \frac{2m_0}{\sqrt{S_{t\bar{t}j}}}$$

**$m_0 = 170 \text{ GeV}$**

## Calculations:

- Fixed NLO calculations  
(Dittmaier et al arXiv:0810.0452)
- Mass scheme fixed  
(pole mass)

$m_t^{\text{pole}}$ [GeV]	$\sigma_{t\bar{t}+1\text{-jet}}$ [pb] $p_T(\text{jet}) > 50 \text{ GeV},  \eta(\text{jet})  < 2.5$	
	LO	NLO
160	66.727(5)	60.04(8)
165	57.615(4)	52.25(9)
170	49.910(3) <sup>+30</sup> <sub>-17</sub>	45.45(6) <sup>+1</sup> <sub>-6</sub>
172.5	46.508(3) <sup>+28</sup> <sub>-15</sub>	42.37(6) <sup>+1</sup> <sub>-6</sub>
175	45.372(3)	39.46(6)
180	37.800(2)	34.73(5)

Pole mass scheme chosen, small NLO corrections

# Off shell corrections to $t\bar{t}$ production.

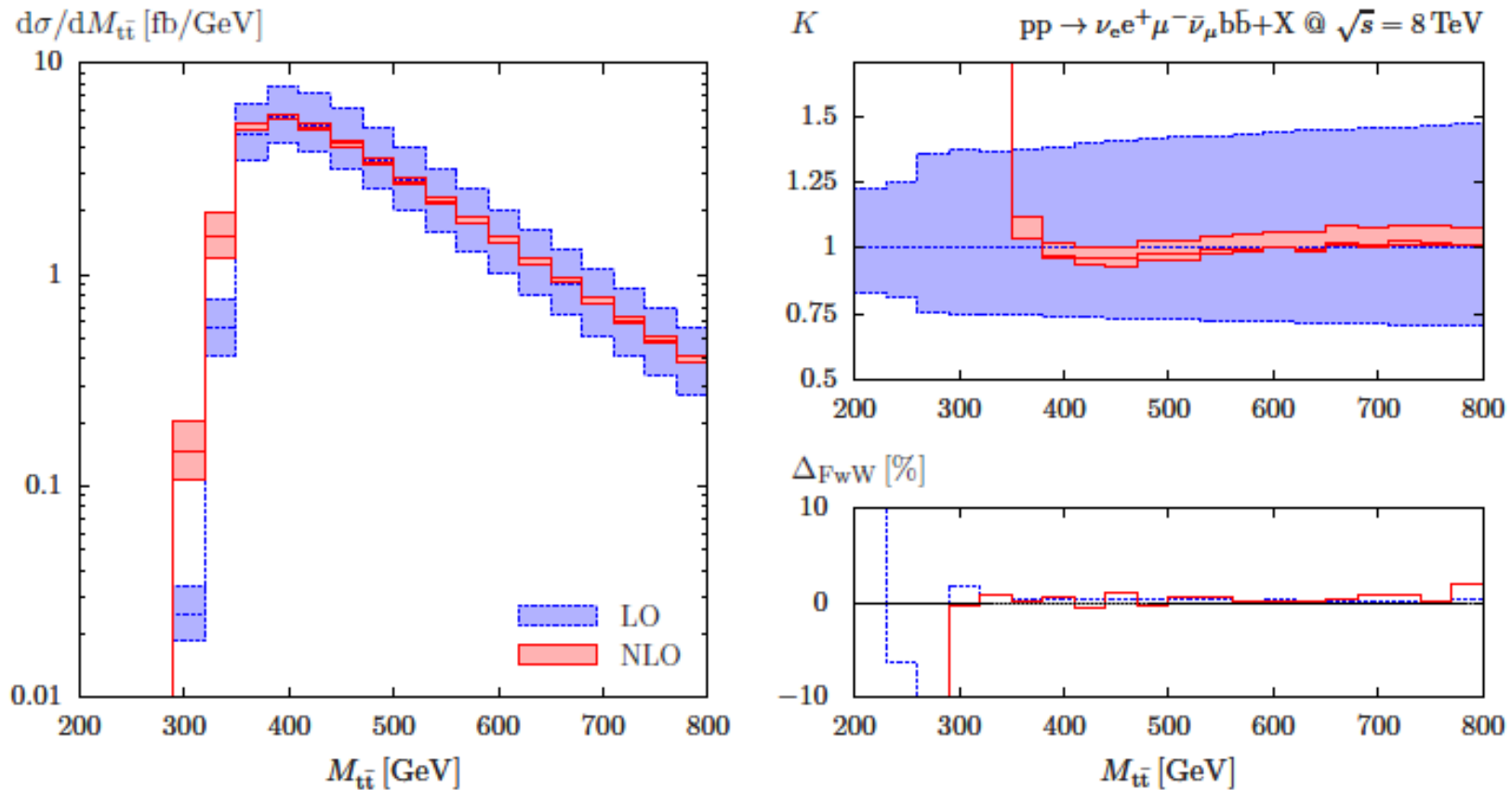


Figure 20: Distribution in the invariant mass of the  $t\bar{t}$  pair with standard cuts for the LHC at  $\sqrt{s} = 8$  TeV for dynamical scale  $\mu_0 = E_T/2$ .

arXiv:1207.5018v2