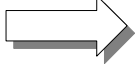


# Short recap

Last lecture (yesterday) we have learned that:

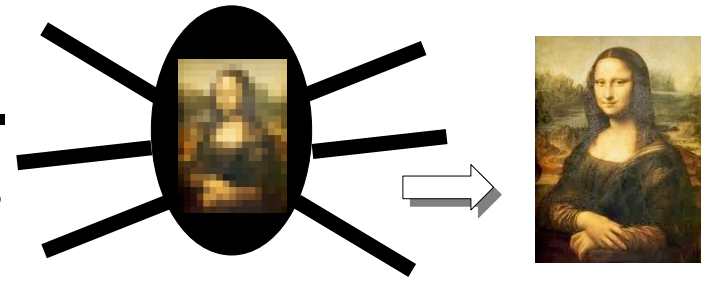
- (Effective) BSM models with TeV-scale new particles cannot have a generic flavor structure: **NP flavor problem**
- Effective Lagrangians that satisfy the **Minimal Flavor violating hypothesis** can satisfy experimental flavor constraints more easily  
     TeV scale NP is allowed
- MFV models are **highly predictive** (ex.  $B_s \rightarrow \mu^+\mu^- / B_d \rightarrow \mu^+\mu^-$ )

This lecture:

- (More) UV complete models: 2HDMs & SUSY
- Flavor physics at high energy:  
    Higgs and top flavor violating decays
- Experimental prospects for the coming years

# How to discover a new d.o.f.

High energy vs. high precision experiments



## Synergy

Producing new particles on shell at high energy experiments

Collision of protons/electrons at high energy producing directly new particles and observe their decay products

### Most recent examples from the past

- Tevatron at Fermilab (center of mass energy 1.96 TeV)  
**discovery of the top quark 1995**
- Large Hadron Collider at CERN (center of mass energy 8 TeV)  
**discovery of the Higgs boson 2012**

What is next?

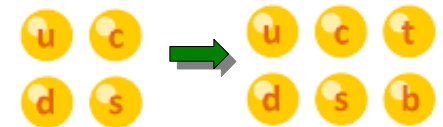
Testing new particles through flavor and CP transitions

### Some examples from the past

- Measurement of the tiny branching ratio of the decay  $K_L \rightarrow \mu^+ \mu^-$

⇒ prediction of the charm quark (Glashow, Iliopoulos, Maiani, 1970)

- Observation of CP violation in kaon anti-kaon oscillations
- ⇒ prediction of the 3rd generation (Kobayashi, Maskawa, 1973)



What is next?

# 1. A Two Higgs Doublet Model (2HDM)

- Several extensions of the SM involve an **extended Higgs sector**, with more than one Higgs doublet.

Most studied example: SUSY

- A two Higgs doublet:  $H_1 = (1, 2, -1/2)$ ,  $H_2 = (1, 2, 1/2)$   $\xrightarrow{\text{SM doublet}}$  Physical fields:  $h, H, A, H^\pm$

- Most general Lagrangian

$$V(H_1, H_2) = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + (bH_1H_2 + \text{h.c.}) + \frac{\lambda_1}{2} |H_1|^4 + \frac{\lambda_2}{2} |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1H_2|^2 + \left[ \frac{\lambda_5}{2} (H_1H_2)^2 + \lambda_6 |H_1|^2 H_1H_2 + \lambda_7 |H_2|^2 H_1H_2 + \text{h.c.} \right]$$

These coefficients are generically complex.  
Possible new sources of CP violation

$$\mathcal{H}_Y^{\text{gen}} = \bar{Q}_L X_{d1} D_R H_1 + \bar{Q}_L X_{u1} U_R H_1^c + \bar{Q}_L X_{d2} D_R H_2^c + \bar{Q}_L X_{u2} U_R H_2$$

Each Higgs doublet can generically couple to up and down quarks.

# FCNCs in 2HDMs

$$\mathcal{H}_Y^{\text{gen}} = \bar{Q}_L X_{d1} D_R H_1 + \bar{Q}_L X_{u1} U_R H_1^c + \bar{Q}_L X_{d2} D_R H_2^c + \bar{Q}_L X_{u2} U_R H_2$$

We can rotate to the basis in which only one Higgs has a VEV

$$\begin{pmatrix} \Phi_v \\ \Phi_H \end{pmatrix} = \begin{pmatrix} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{pmatrix} \begin{pmatrix} H_1 \\ H_2^c \end{pmatrix} \quad \langle \Phi_v^\dagger \Phi_v \rangle = v^2/2, \\ \langle \Phi_H^\dagger \Phi_H \rangle = 0$$

$$\mathcal{H}_Y^{\text{gen}} = \bar{Q}_L \left[ \frac{\sqrt{2}}{v} M_d \Phi_v + Z_d \Phi_H \right] D_R \quad \tan \beta \equiv \frac{\langle H_2 \rangle}{\langle H_1 \rangle}$$

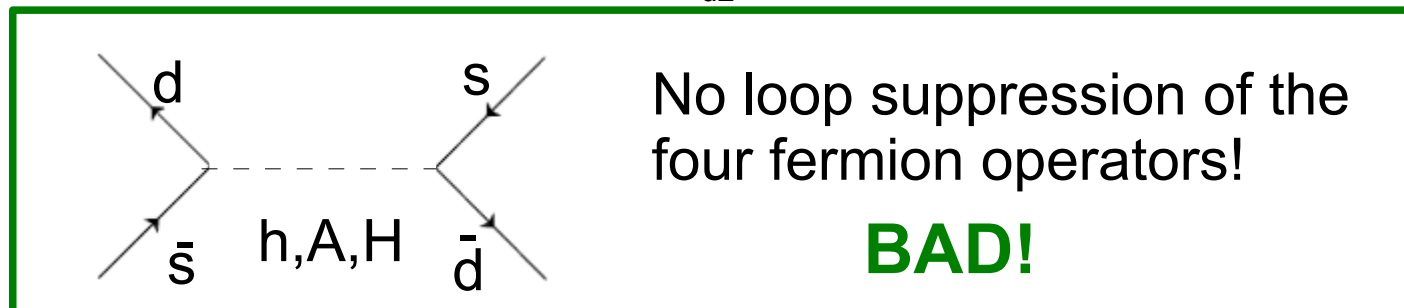
3x3 matrices

$$\begin{cases} Z_d = \cos \beta X_{d2} - \sin \beta X_{d1} \\ M_d = \frac{v}{\sqrt{2}} (\cos \beta X_{d1} + \sin \beta X_{d2}) \end{cases}$$

(analogous in the up sector)

Generically not proportional to each other!  $\Rightarrow$  It is not possible to diagonalize them simultaneously

Exercise: what are the conditions on  $X_{d1}$  and  $X_{d2}$  not to have FCNCs at tree level?



# Minimal Flavor Violating 2HDMs

$$\mathcal{H}_Y^{\text{gen}} = \bar{Q}_L X_{d1} D_R H_1 + \bar{Q}_L X_{u1} U_R H_1^c + \bar{Q}_L X_{d2} D_R H_2^c + \bar{Q}_L X_{u2} U_R H_2$$

$$X_{d1} = Y_d$$

$$X_{u1} = \epsilon_u Y_u + \epsilon'_1 Y_u^\dagger Y_u Y_u + \epsilon'_2 Y_d^\dagger Y_d Y_u + \dots$$

$$X_{d2} = \epsilon_b Y_d + \epsilon_1 Y_d^\dagger Y_d Y_d + \epsilon_2 Y_u^\dagger Y_u Y_d + \dots$$

$$X_{u2} = Y_u$$

higher orders in the  
small Yukawa couplings

The  $\epsilon_i$  are in general complex coefficients

Exercise: convince your-self that the several terms are invariant under

$$SU(3)_Q \times SU(3)_U \times SU(3)_D$$

# Minimal Flavor Violating 2HDMs

$$\mathcal{H}_Y^{\text{gen}} = \bar{Q}_L X_{d1} D_R H_1 + \bar{Q}_L X_{u1} U_R H_1^c + \bar{Q}_L X_{d2} D_R H_2^c + \bar{Q}_L X_{u2} U_R H_2$$

$$X_{d1} = Y_d$$

$$X_{u1} = \epsilon_u Y_u + \epsilon'_1 Y_u^\dagger Y_u Y_u + \epsilon'_2 Y_d^\dagger Y_d Y_u + \dots$$

$$X_{d2} = \epsilon_b Y_d + \epsilon_1 Y_d^\dagger Y_d Y_d + \epsilon_2 Y_u^\dagger Y_u Y_d + \dots$$

$$X_{u2} = Y_u$$

higher orders in the small Yukawa couplings

The  $\epsilon_i$  are in general complex coefficients

- The most studied 2HDMs are the so called **Type I, II, III, IV**: these are models where up and down quarks only couple to one Higgs type.

Example: **Type II**:  $U_R$  only couple to  $H_2$  and  $D_R$  only coupled to  $H_1$

$$(X_{u1} = X_{d2} = 0)$$

- All these models are a particular limit of a MFV 2HDM

**Footnote:**

The MSSM can be approximated with a Type II 2HDM

# Flavor phenomenology of MFV 2HDMs

- Constraints from meson mixing observables

$$\begin{aligned} \text{Kaon} &\sim \frac{A_0}{M_H^2} \tan^4 \beta m_s m_d [V_{ts}^* V_{td}]^2 \\ B_d &\sim \frac{A_1}{M_H^2} \tan^4 \beta m_b m_d [V_{tb}^* V_{td}]^2 \\ B_s &\sim \frac{A_2}{M_H^2} \tan^4 \beta m_b m_s [V_{tb}^* V_{ts}]^2 \end{aligned}$$

Larger NP effect



$A_i$  are combinations of the  $\varepsilon_i$  of the previous slide

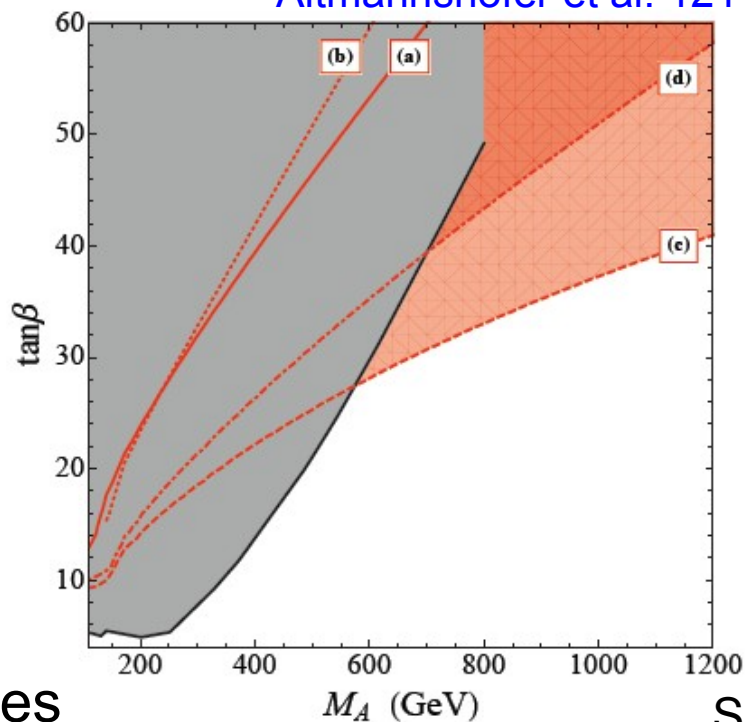
Altmannshofer et al. 1211.1976

- Some possible NP in rare B-decays

$$\frac{\text{Br}(B_q \rightarrow \mu^+ \mu^-)}{\text{Br}(B_q \rightarrow \mu^+ \mu^-)_{\text{SM}}} = (|1 + R_q|^2 + |R_q|^2)$$

$$R_q \propto \frac{M_{B_q}^2 t_\beta^3}{M_H^2}$$

Interplay  
with direct searches

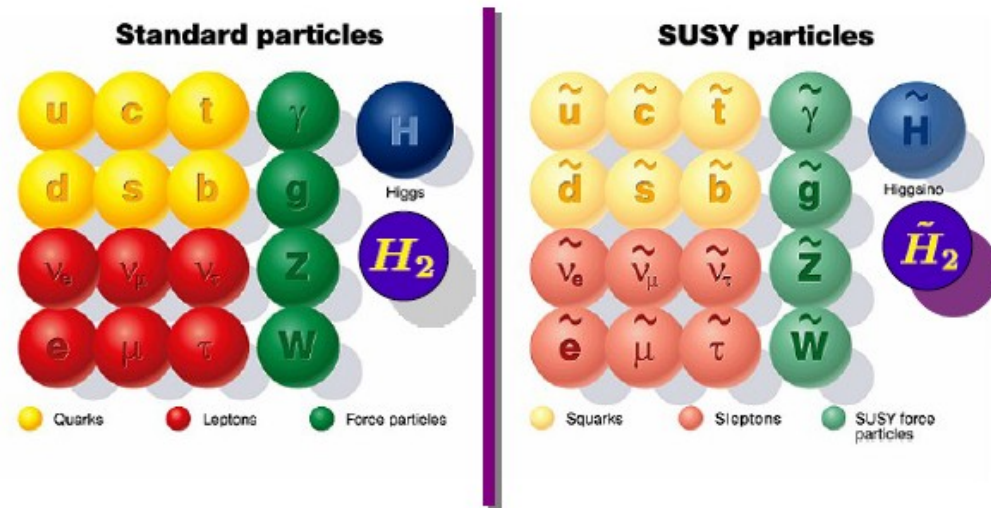


S.Gori

# 2. SUSY models (intro). The MSSM

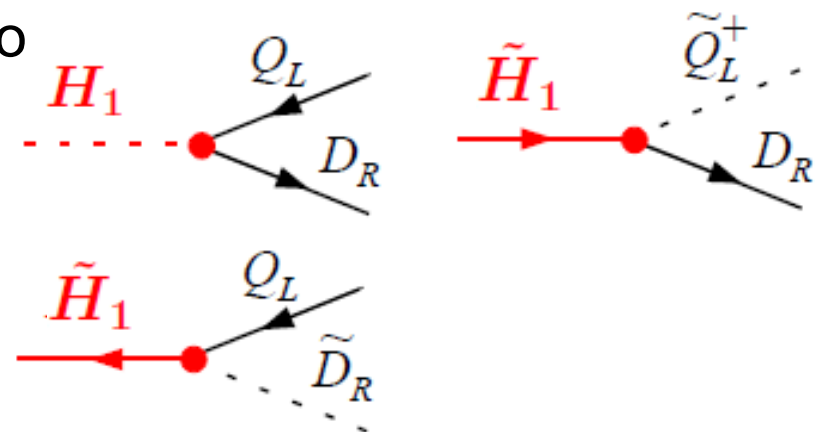
The Minimal Supersymmetric extension of the SM includes:

- (i) scalar partners of the ordinary quarks and leptons;
- (ii) spin-1/2 partners of the ordinary gauge bosons [*gauginos*];
- (iii) Two Higgs doublets [ $H_1, H_2$ ] with their corresponding spin 1/2 partners



- The SUSY version of  $L_{\text{gauge}}$  is completely determined by its symmetry properties
- The SUSY version of  $L_{\text{Yukawa}}$  ( $\mathcal{L}_Y^{\text{MSSM}}$ ) is also strongly constrained

$$\mathcal{L}_Y^{\text{MSSM}} = \bar{Q}_L Y_D D_R H_1 + \bar{Q}_L Y_U U_R H_2 + \bar{\tilde{Q}}_L^+ Y_D D_R \tilde{H}_1 + \bar{\tilde{Q}}_L^+ Y_U U_R \tilde{H}_2 + \dots$$





# SUSY models & new sources of FCNCs

"Problems" arise when we consider SUSY breaking.  
Large number of degrees of freedom!



$$\mathcal{L}_{soft} = (M_f)_{ij} \chi_i \chi_j + (M_s^2)_{ij} \phi_i \phi_j + A_{ijk} \phi_i \phi_j \phi_k$$

gaugino/higgsino masses     squark/slepton masses     trilinear scalar couplings

Potential new sources of  
flavor symmetry breaking

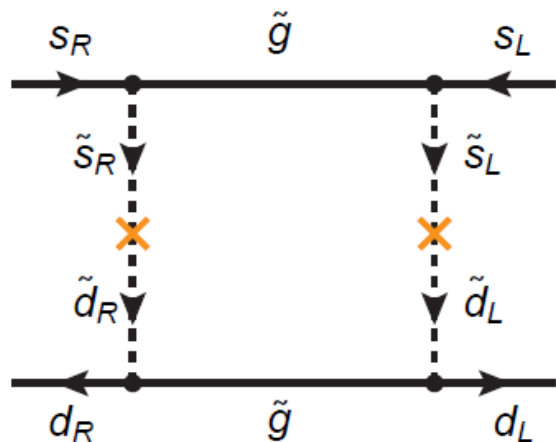
For example, in the down-squark sector:

$$\begin{pmatrix} \tilde{Q}_L^i & \tilde{D}_R^i \end{pmatrix} \begin{pmatrix} (M_{LL}^2)_{ij} & (M_{LR}^2)_{ij} \\ (M_{LR}^2)_{ij}^\dagger & (M_{RR}^2)_{ij} \end{pmatrix} \begin{pmatrix} \tilde{Q}_L^i \\ \tilde{D}_R^i \end{pmatrix}$$

If the off-diagonal entries in these mass matrices are not sufficiently small, the model is ruled out by flavor physics...

# The SUSY flavor problem

Going back to our meson mixings...



If these **mass parameters** are of  $O(1)$ :

$$\mathcal{M} = M_{\tilde{q}} \begin{pmatrix} \mathcal{O}(1)_{3 \times 3} & \mathcal{O}(1)_{3 \times 3} \\ \mathcal{O}(1)_{3 \times 3} & \mathcal{O}(1)_{3 \times 3} \end{pmatrix}$$

squark masses have to be larger than  $\sim 10^3$  TeV


Tension with the idea of TeV-scale SUSY  $\Rightarrow$  **SUSY flavor problem**

If we take a **MFV SUSY scenario**, the soft masses are highly non-generic:

$$\left\{ \begin{aligned} M_{LL}^2 &= \tilde{m}_Q^2 \left( \mathbf{I}_{3 \times 3} + b_1 Y_u Y_u^\dagger + b_2 Y_d Y_d^\dagger + \right. \\ &\quad \left. + b_3 Y_d Y_d^\dagger Y_u Y_u^\dagger + b_3^* Y_u Y_u^\dagger Y_d Y_d^\dagger + \dots \right) \\ M_{RR}^2 &= \tilde{m}_D^2 \left( \mathbf{I}_{3 \times 3} + b_5 Y_d^\dagger Y_d + \dots \right) \end{aligned} \right.$$

$\Rightarrow$  **Squark masses as light as few hundred GeV are allowed!**

# Take home messages (for NP models)

- Complete NP models generically show a **rich flavor structure**  
 too large breaking of the flavor symmetry  
of the SM gauge interactions
- **If we ask for MFV, it is easier to evade the constraints.**  
At the same time it is **possible to have deviations** from the SM  
prediction of some flavor observables  
(example:  $B_s \rightarrow \mu^+ \mu^-$  vs.  $B_d \rightarrow \mu^+ \mu^-$ )
- **Complementarity with LHC direct searches** of new physics particles  
(example: additional Higgs bosons, ...)

# Some discrepancy. Hints for NP?

Z.Ligeti

In the last ~30 years, there have been a tremendous experimental progress in testing the flavor structure of the SM

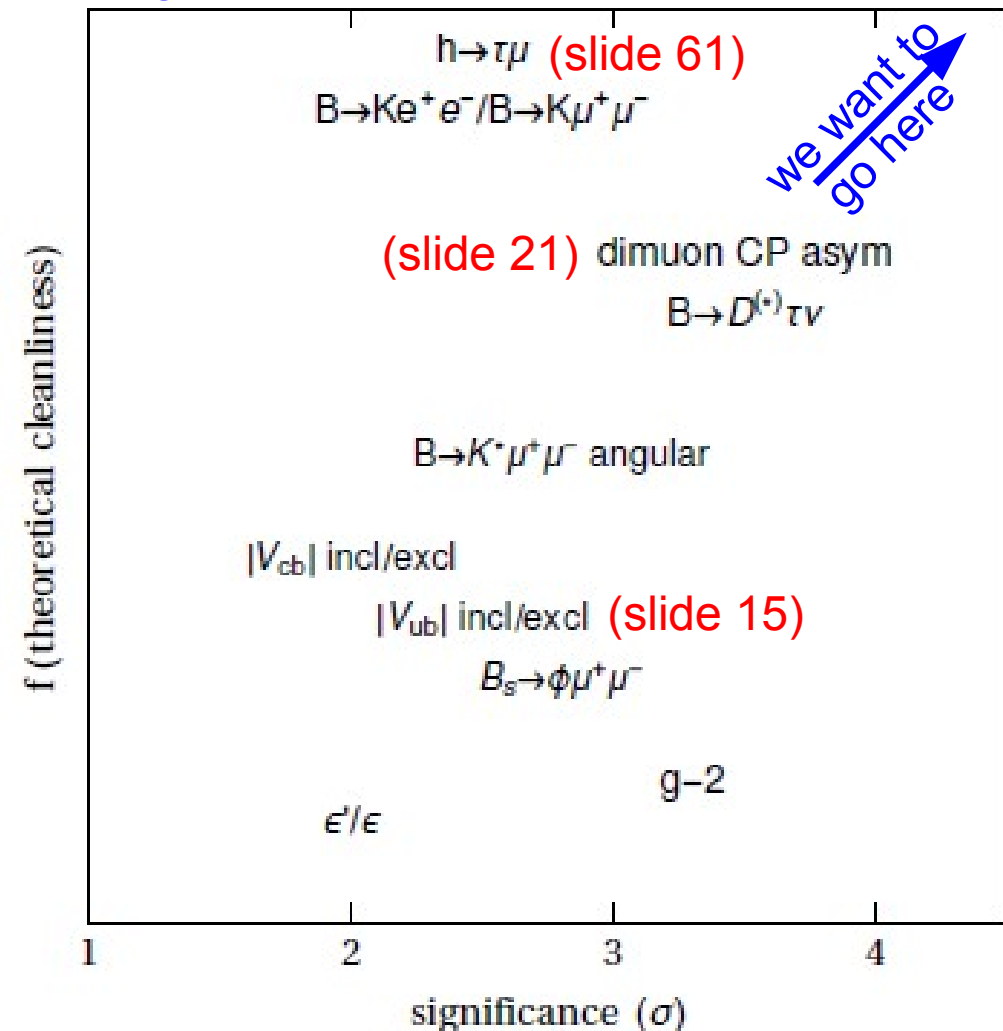
Overall, we have a good agreement

**Nevertheless**

There are some measurements of flavor observables that show some (small?) deviation with respect to the SM prediction

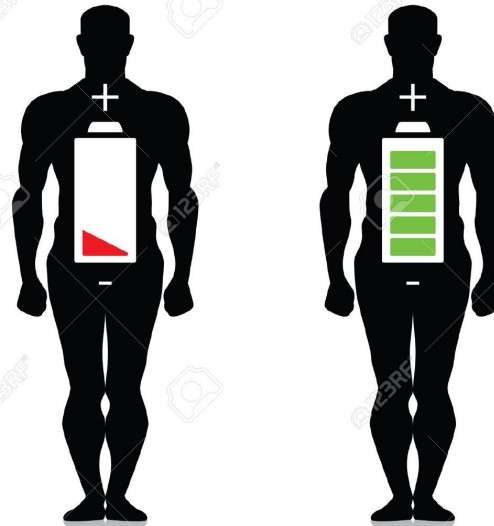
**Some would be unambiguous NP signals**

Except for theoretically cleanest modes, cross-checks needed to build a robust case for NP



# Flavor at high energy?

1. Up to now we have learned about **low energy flavor observables**
2. Can we say something using more massive particles?  
Can we test flavor transitions at **high energy** environments?



Low energy

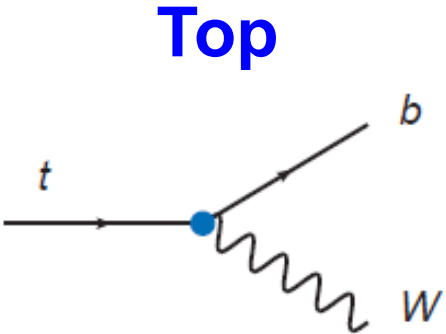
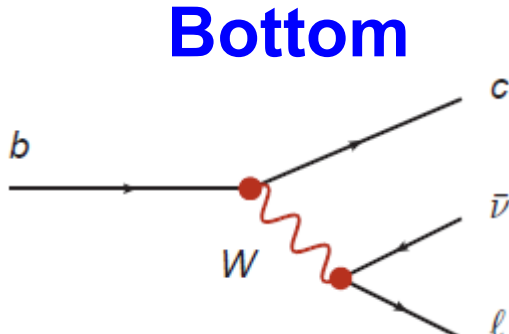
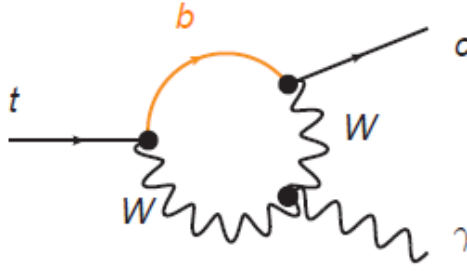
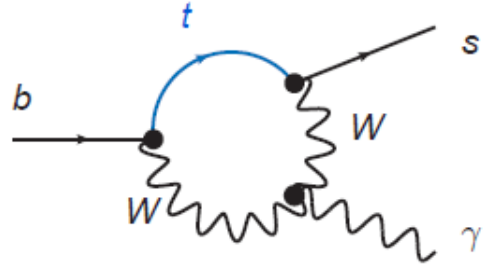
We have studied:  
**Meson transitions**

High energy

We will study:  
**Top & Higgs**

# Top flavor changing decays

- The top was discovered in 1995 at Tevatron.  
By now, we know its properties quite well **BUT...**
- Let us compare the top quark to the bottom quark

	<b>Top</b>	<b>Bottom</b>
Main decay mode	 <p style="text-align: center;"><math>\frac{\Gamma_t}{m_t} \simeq 1\%</math></p>	 <p style="text-align: center;"><math>\frac{\Gamma_{B_d}}{m_{B_d}} \simeq 8.2 \times 10^{-13}</math></p>
Some possible Rare decay	 <p style="text-align: center;"><math>\mathcal{A}_{t \rightarrow c\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_b^2}{m_W^2} V_{tb} V_{cb}^*</math></p>	 <p style="text-align: center;"><math>\mathcal{A}_{b \rightarrow s\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^*</math></p>

# Top flavor changing decays

- The top was discovered in 1995 at Tevatron.  
By now, we know its properties quite well **BUT...**
- Let us compare the top quark to the bottom quark

**Top**

**Bottom**

Main d  
mod

**SM predictions:**

Aguilar-Saavedra 0409342

$$BR(t \rightarrow c\gamma) \simeq 5 \times 10^{-14} \quad , \quad BR(t \rightarrow u\gamma) \simeq 4 \times 10^{-16}$$

$$BR(t \rightarrow cg) \simeq 5 \times 10^{-12} \quad , \quad BR(t \rightarrow ug) \simeq 4 \times 10^{-14}$$

$$BR(t \rightarrow cZ) \simeq 1 \times 10^{-14} \quad , \quad BR(t \rightarrow uZ) \simeq 8 \times 10^{-17}$$

Som  
possi

$$BR(t \rightarrow ch) \simeq 3 \times 10^{-15} \quad , \quad BR(t \rightarrow uh) \simeq 2 \times 10^{-17}$$

Rare decay

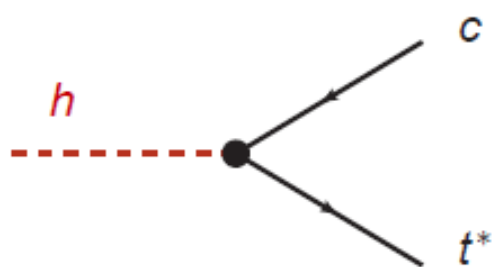
$$\mathcal{A}_{t \rightarrow c\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_b^2}{m_W^2} V_{tb} V_{cb}^*$$

$$\mathcal{A}_{b \rightarrow s\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^*$$

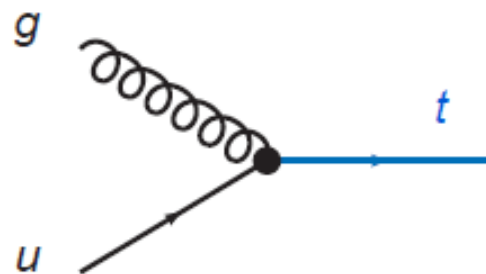
# Top flavor changing couplings at LHC

Flavor changing top interactions are not only probed by searches of rare top decays. Other probes include:

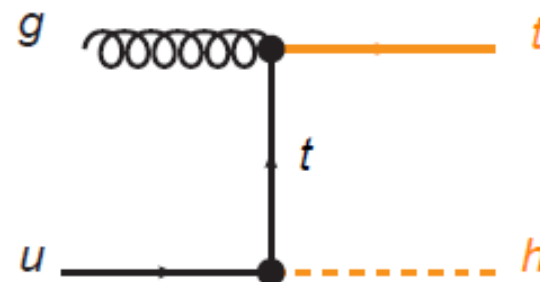
Higgs decay



Single top production



Single top+Higgs production



Process	Br Limit	Search	Dataset
$t \rightarrow Zq$	$5 \times 10^{-4}$	CMS $t\bar{t} \rightarrow Wb + Zq \rightarrow l\nu b + llq$	$19.7 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow Zq$	$7.3 \times 10^{-3}$	ATLAS $t\bar{t} \rightarrow Wb + Zq \rightarrow l\nu b + llq$	$2.1 \text{ fb}^{-1}$ , 7 TeV
$t \rightarrow gu$	$3.1 \times 10^{-5}$	ATLAS $qg \rightarrow t \rightarrow Wb$	$14.2 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow gc$	$1.6 \times 10^{-4}$	ATLAS $qg \rightarrow t \rightarrow Wb$	$14.2 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow \gamma u$	$1.6 \times 10^{-4}$	CMS $qg \rightarrow t\gamma \rightarrow Wb\gamma$	$19.1 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow \gamma c$	$1.8 \times 10^{-3}$	CMS $qg \rightarrow t\gamma \rightarrow Wb\gamma$	$19.1 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow hq$	$7.9 \times 10^{-3}$	ATLAS $t\bar{t} \rightarrow Wb + hq \rightarrow l\nu b + \gamma\gamma q$	$20 \text{ fb}^{-1}$ , 8 TeV
$t \rightarrow hq$	$5.6 \times 10^{-3}$	CMS $t\bar{t} \rightarrow Wb + hq \rightarrow l\nu b + llqX$	$19.5 \text{ fb}^{-1}$ , 8 TeV

Bounds are much much larger than the SM prediction



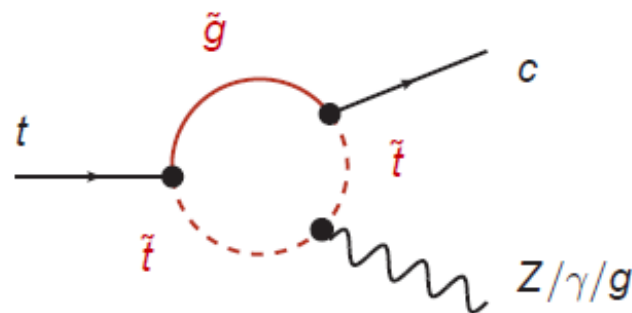
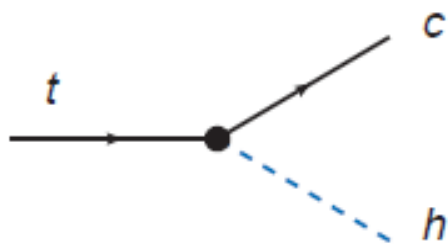
# NP models and top flavor changing decays

- Several NP models can sizably enhance the BR for top flavor changing decays, while satisfying direct and "indirect" low energy constraints

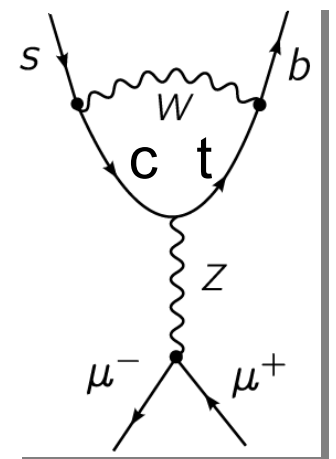
Some example:

2HDM

MSSM



Example of indirect constraint:



$B_s \rightarrow \mu^+ \mu^-$

Reminder for the SM:

$10^{-14}$

$5 \times 10^{-14}$

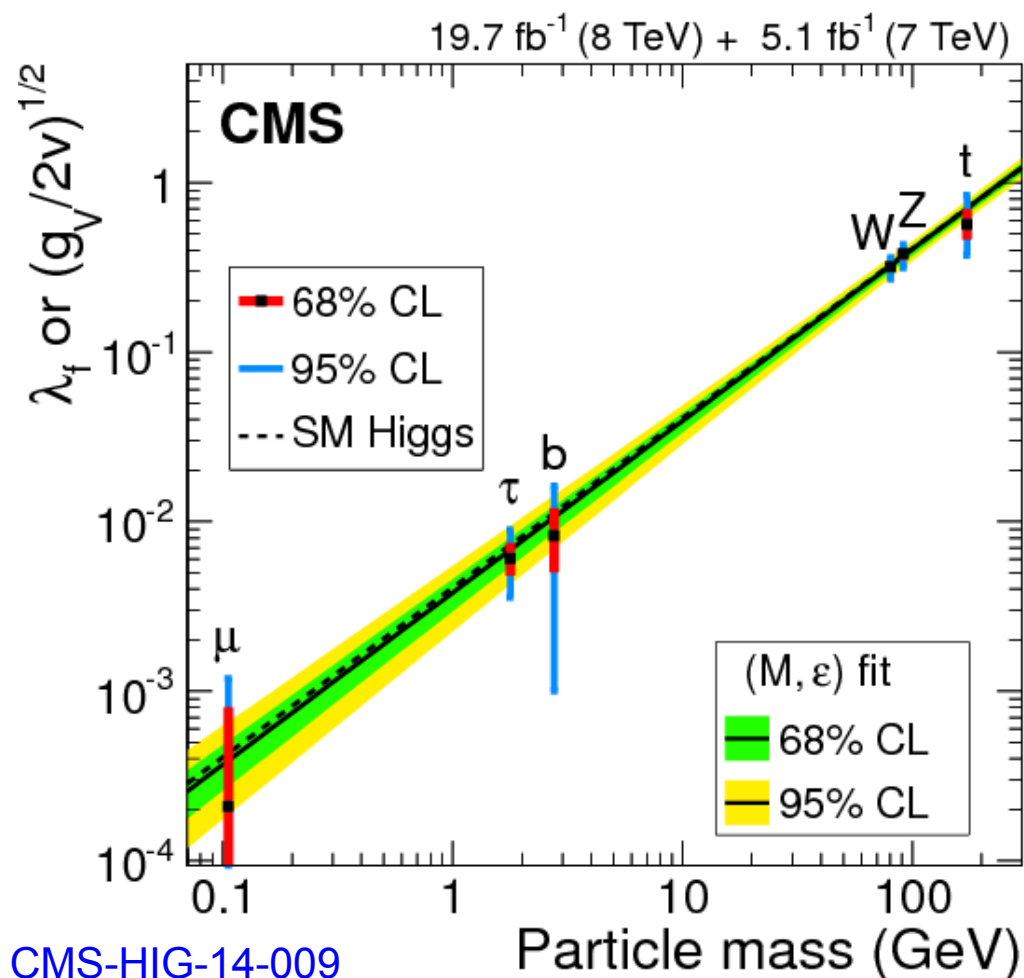
$5 \times 10^{-12}$

$3 \times 10^{-15}$

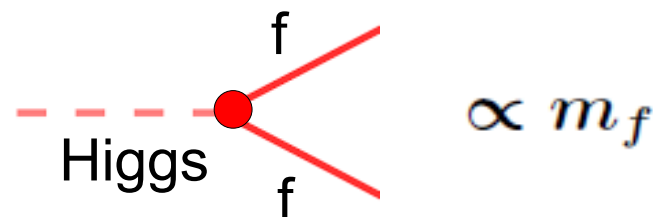
	2HDM <sup>1)</sup>	MSSM <sup>2)</sup>
$t \rightarrow cZ$	$\lesssim 10^{-6}$	$\lesssim 10^{-7}$
$t \rightarrow c\gamma$	$\lesssim 10^{-7}$	$\lesssim 10^{-8}$
$t \rightarrow cg$	$\lesssim 10^{-5}$	$\lesssim 10^{-7}$
$t \rightarrow ch$	$\lesssim 10^{-2}$	$\lesssim 10^{-5}$

# The Higgs flavor conserving couplings

- LHC will measure more and more precisely the couplings of the Higgs to the massive particles of the SM



LHC Run1 tests for the relations



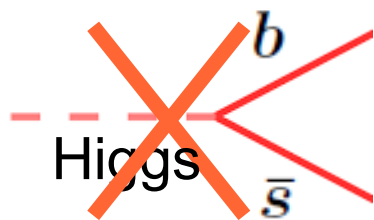
(note: we are speaking about flavor conserving couplings!)

We do not know (yet) how the **Higgs couples to light flavors** (muons? electrons? charm quarks?)

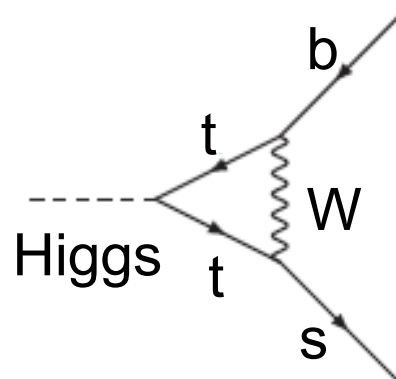
We know, for example, that it couples **non-universally** with muons and taus but we do not know more than this...

# The Higgs flavor violating couplings (1)

- We have seen that, in the SM, the Higgs does not have flavor changing couplings at the tree level



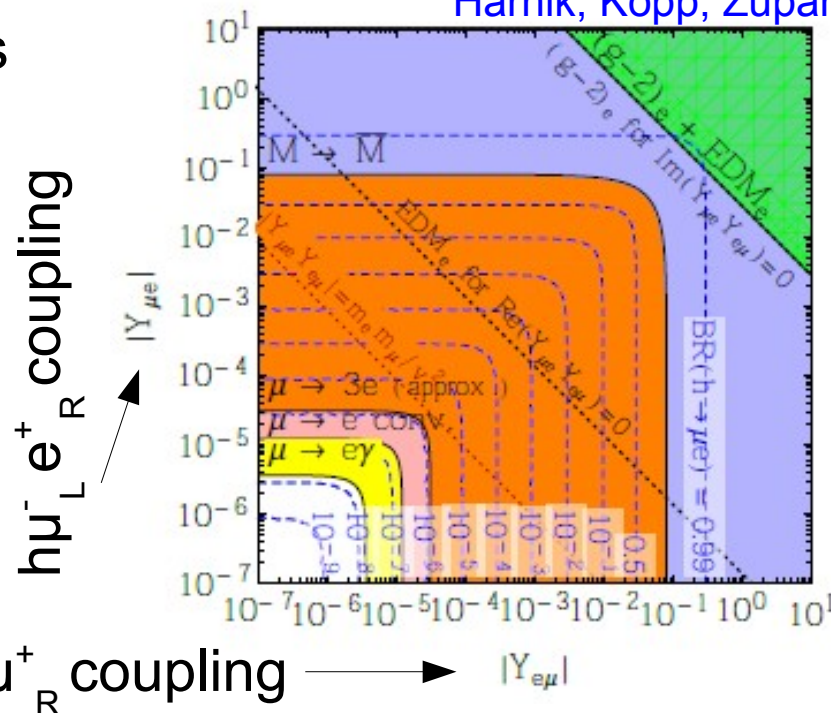
Still, these couplings are generated at one loop in perturbation theory:



Tiny BRs are predicted by the SM

Harnik, Kopp, Zupan, 1209.1397

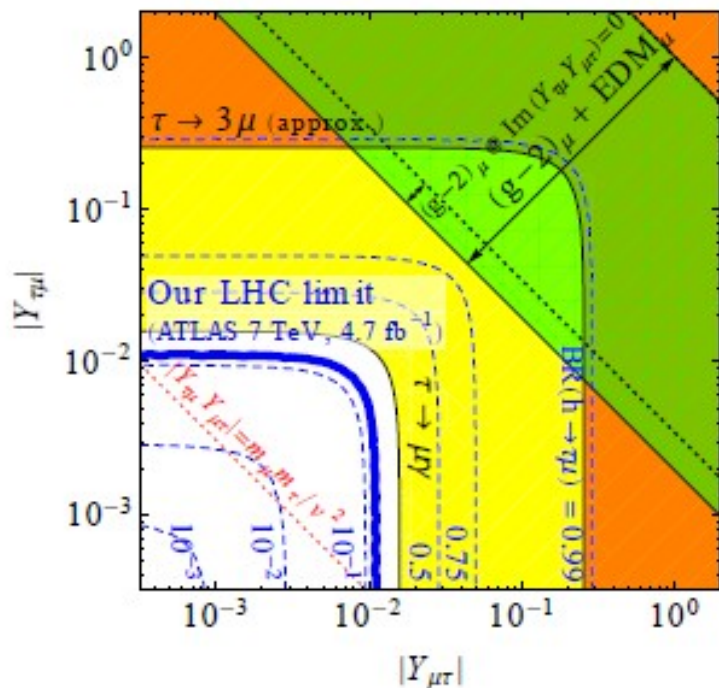
- Some of these "effective" couplings are strongly constrained by low energy measurements:



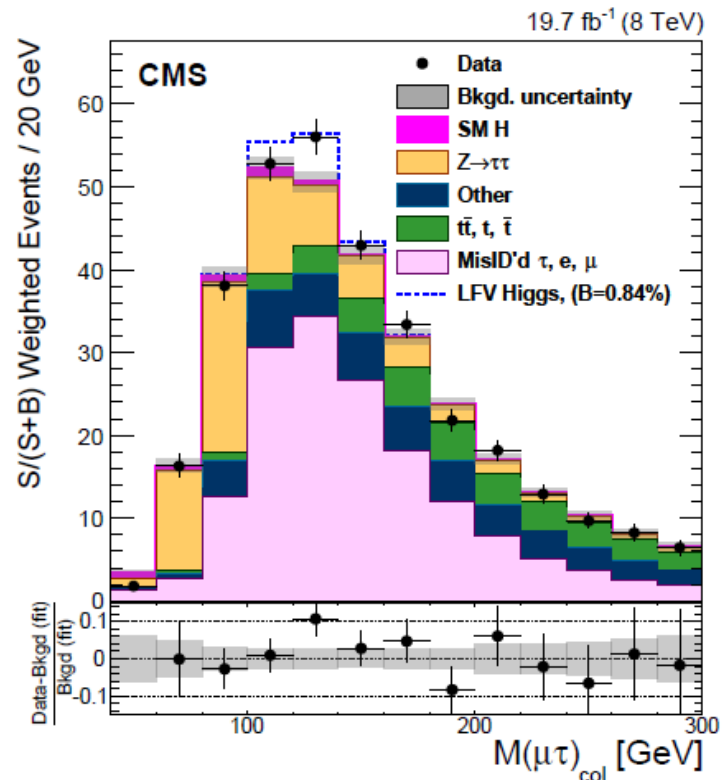
# The Higgs flavor violating couplings (2)

- Some other coupling is instead much more weakly constrained by low energy measurements

Harnik, Kopp, Zupan, 1209.1397



- Some interesting ATLAS and CMS search...



- CMS, 1502.07400

$$\text{BR}(h \rightarrow \mu\tau) < 1.51\%, \text{ 95\% C.L.}$$

$$\text{BR}(h \rightarrow \mu\tau) = (0.84^{+0.39}_{-0.37})\%$$

- ATLAS, 1508.03372

$$\text{BR}(h \rightarrow \mu\tau) < 1.85\%, \text{ 95\% C.L.}$$

$$\text{BR}(h \rightarrow \mu\tau) = (0.77 \pm 0.62)\%$$

# Take home messages

- The measurements of a few low energy flavor observables seem to show some (small) discrepancy, if compared to the SM prediction... **Looking for a theory and experimentally clean observables not agreeing with the SM prediction!**

We want to repeat: 

- **Opportunity of testing flavor, performing high energy measurements:** top and Higgs flavor changing couplings
- The **Higgs is the ultimate source of flavor**. Importance of testing its flavor structure (both flavor diagonal and off-diagonal couplings)

# A rich flavor experimental program ahead

Observables fulfilling the criteria:

- (i) sensitive to different NP,
- (ii) measurements can improve by order(s) of magnitude,
- (iii) not limited by hadronic uncertainties

## Belle II and LHCb (some highlight)

- Difference of CP asymmetries  $S_{\psi K_S}$ ,  $S_{\phi K_S}$ ,  $S_{\psi\phi}$  etc.
- $\gamma$  from CP asymmetries in tree-level decays (e.g.  $B \rightarrow D K$ )
- CP asymmetry in semileptonic B decays
- CP asymmetry in the radiative decay  $S_{K_S \pi^0 \gamma}$
- B meson decay searches:  
 $B_{s,d} \rightarrow \mu\mu$ ,  $B_{s,d} \rightarrow \tau\tau$ ,  $B^\pm \rightarrow \tau\nu$ ,  
 $B \rightarrow K^{(*)} \ell^+ \ell^-$ ,  $B_s \rightarrow \phi\gamma$ , ...
- Search for CP violation in  $D - \bar{D}$  mixing
- Search for charged lepton flavor violation

## LHC (some highlight)

### High energy measurements

- Top flavor changing couplings (in decay and in production)
- Couplings of the Higgs to light Generation quarks/leptons?
- Flavor changing Higgs couplings

# Concluding remarks on flavor/CP

- We cannot (yet) predict the SM flavor/CP structure
  - from first principles (SM flavor puzzle)
- The SM is very well tested by low energy flavor measurements
  - ⇒ Overall good consistency
- Great opportunity for testing NP using low and high energy flavor measurements



Evidence for BSM?		FLAVOR	
		yes	no
ATLAS & CMS	yes	Complementary info	Distinguish models
	no	Tells us where to look next	Flavor is the best probe

