

# Automated NNLL+NLO resummation for jet-veto cross sections

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# What are we looking at?

Production cross section of one or several **weak bosons**

$$Z, W^+, W^-, H$$

with a **jet veto**, which only allows for jets with low transverse momentum

$$p_T^{\text{Jet}} < p_T^{\text{Veto}} \sim 15 - 30 \text{ GeV}$$

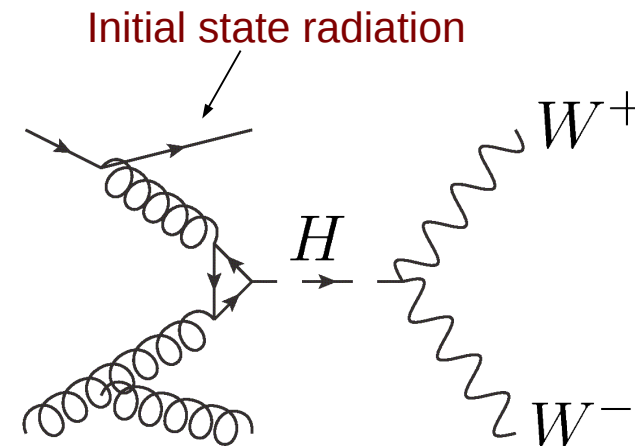
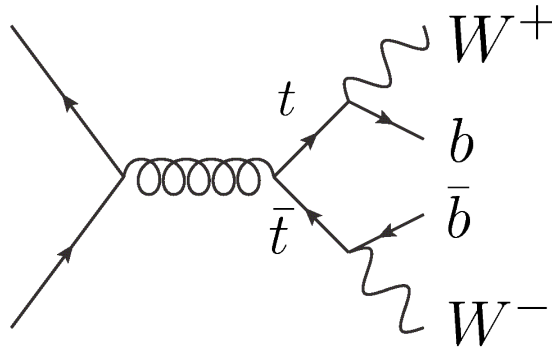
## Why?

- Analysis is done in jet bins, needs precise prediction of the 0-jet bin.
- Suppress background
- Excess in  $W^+W^-$  cross section measured at the LHC. New Physics?

# Role of the Jet Veto

Suppression of top-quark background in processes involving  $W$  bosons

- For example in  $H \rightarrow W W^*$



**Multiple scales**  $\implies$  **enhancement by large Sudakov logarithms**

$$\alpha_s^n \ln \left( \frac{p_T^{\text{veto}}}{Q} \right)^k \quad k \leq 2n$$

$Q$  Invariant mass of the boson system

$\implies$  **Resummation**

# Resummation for the Jet Veto

Recently, several papers have addressed this issue:

- $W^+ W^-$  production:

Jaiswal, Okui '14; Meade, Ramani, Zeng '14; Monni, Zanderighi '14;  
Becher, Frederix, Neubert, LR '14

- Higgs production:

Banfi, Salam, Zanderighi '12; +Monni '12; Becher, Neubert '12; + LR  
'13; Tackmann, Walsh, Zuberi '12; + Stewart '13; Liu, Pertiello '13; +  
Boughezal, Tackmann, Walsh '14

I will present our work and discuss how it is related to these.

In the following I will discuss the case of  $W^+ W^-$  production but our formalism applies to any number of massive color-singlet particles.

# Resummation by SCET

Resummation in general can be achieved using Soft-Collinear Effective Theory (SCET) or QCD based resummation techniques.

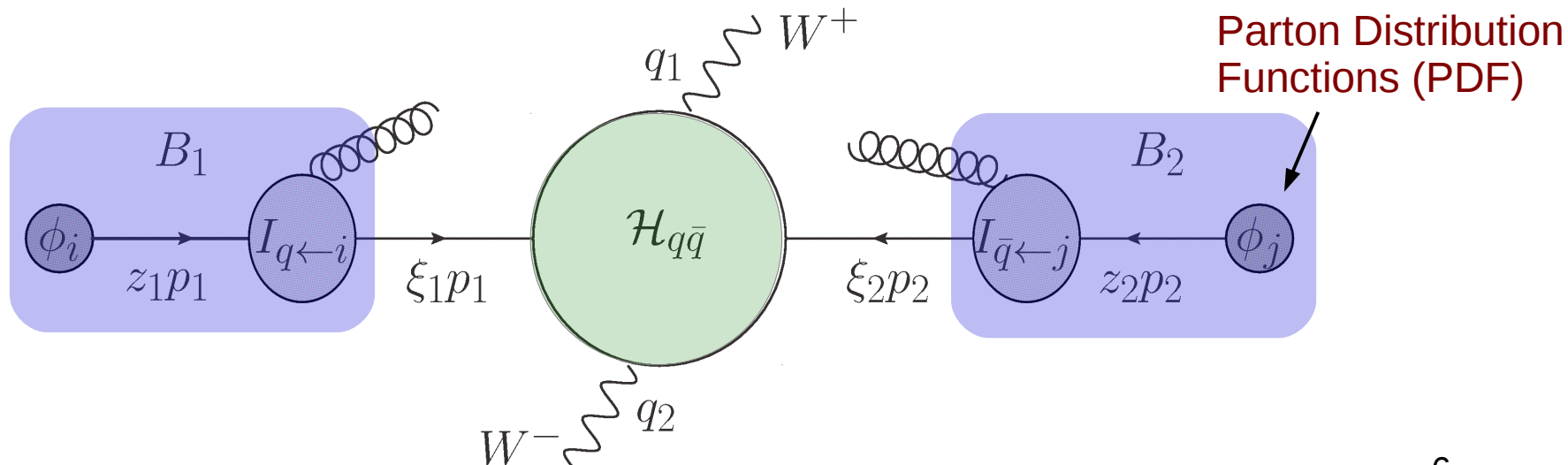
SCET framework:

- Low-energy degrees of freedom: **Soft** and **Collinear** fields
- Off-shell modes are integrated out. Hard-scattering encoded in the **Wilson coefficients** of the operators.
- Advantages:
  - Operator definition (manifest gauge invariance).
  - Systematic scale separation. Resummation by **RG evolution**.
  - **Power corrections** can be included.

# All-order Factorization Theorem from SCET

$$\begin{aligned}
 \frac{d^3 \sigma(p_T^{\text{veto}})}{dy dQ^2 d\hat{t}} &= \underbrace{\sigma_0(Q^2, \hat{t}, \mu)}_{\text{Born-level CS}} \underbrace{\mathcal{H}_{q\bar{q}}(Q^2, \hat{t}, \mu_h) U_q(Q^2, \mu_h, \mu)}_{\text{Hard function Evolution factor}} \\
 &\times \underbrace{\left(\frac{Q}{p_T^{\text{veto}}}\right)^{-2F_q(p_T^{\text{veto}}, \mu)}}_{\text{Collinear Anomaly}} \underbrace{B_q(\xi_1, \mu, p_T^{\text{veto}}) B_{\bar{q}}(\xi_2, \mu, p_T^{\text{veto}})}_{\text{Beam-jet functions}}
 \end{aligned}$$

Factorization theorem up to **first order** power corrections  $p_T^{\text{veto}}/Q$  and non-perturbative effects  $\Lambda_{\text{QCD}}/p_T^{\text{veto}}$ .



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 \end{aligned}$$

For NNLL resummation:

- Perturbative kernels  $l_{i \leftarrow k}$ : 1-loop
- Anomaly exponent  $F_i$  : 2-loop
- Hard function  $\mathcal{H}_{ij}$  : 1-loop **process dependent!**

Resummed result has Born kinematics in the limit  $p_T^{\text{veto}} \rightarrow 0$ .

➡ First automated resummation (NNLL+NLO) in SCET using the event generator [MadGraph5\\_aMC@NLO](#).

# Advantages of an Automated Resummation

- Much more efficient and less error prone.



- Straightforward to **include decays** and **cuts** on the decay products.
  - Complicated in analytic computations.
- Code publicly available (recent [MadGraph5\\_aMC@NLO](#) release).
- Other work on automated resummation :
  - [Banfi, Monni, Salam, Zanderighi](#) (CAESAR, ARES)
  - [Farhi, Feige, Freytsis, Schwartz](#) '15
  - [Gerwick, Hoeche, Marzani, Schumann](#) '15



# Automated Resummation using aMC@NLO

Scheme A: NNLL from reweighting Born-level events.

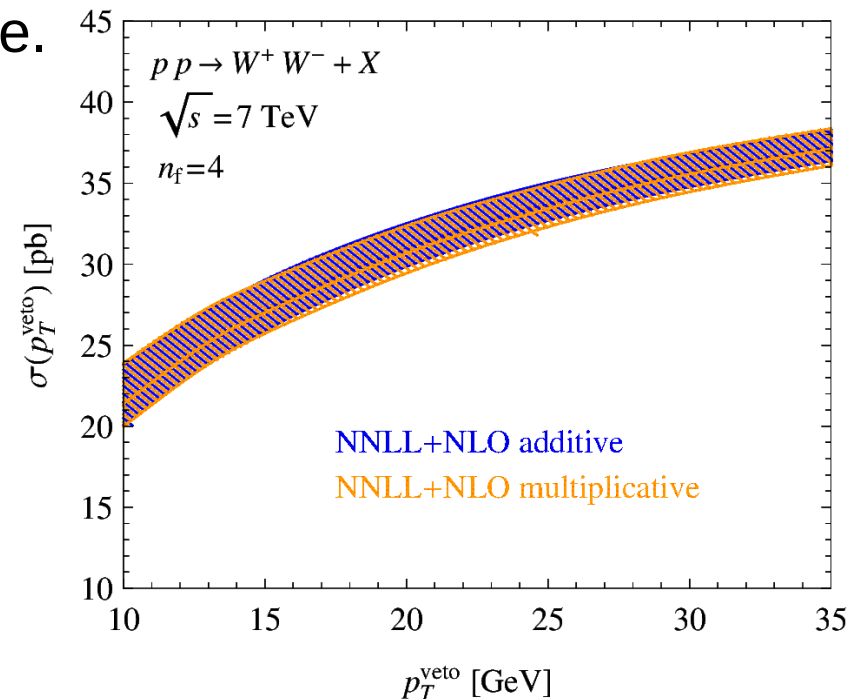
- Using a tree-level generator, rescale each event weight with the ratio to the resummed cross section.
- Beam functions included via modified PDFs.
  - Tabulate for a grid of values (same as for underlying PDF).
  - Use standard PDF interpolation routine.
- Hard function (only process dependent piece) computed using the [MadGraph5\\_aMC@NLO](#) code itself.
- Result is matched to NLO fixed-order in an purely additive way.

$$\sigma_{\text{NNLL+NLO}} = \sigma_{\text{NNLL}}(\mu, \mu_h) + \left( \sigma_{\text{NLO}}(\mu_m) - \sigma_{\text{NNLL}}(\mu_m) \Big|_{\text{expanded to NLO}} \right)$$

# Automated Resummation using aMC@NLO

Scheme B: NNLL+NLO with automated computation of the beam functions and matching corrections.

- Run [aMC@NLO](#) in fixed-order mode, subtract the logarithmically enhanced pieces and multiply them back in resummed form.
- Matching is multiplicative.
- Advantage: Beam functions and matching are computed on the fly.
- Disadvantage: Matching corrections cannot be extracted separately; extension to higher order is not possible.
- Numerically the two schemes are almost indistinguishable.



# Phenomenological Result

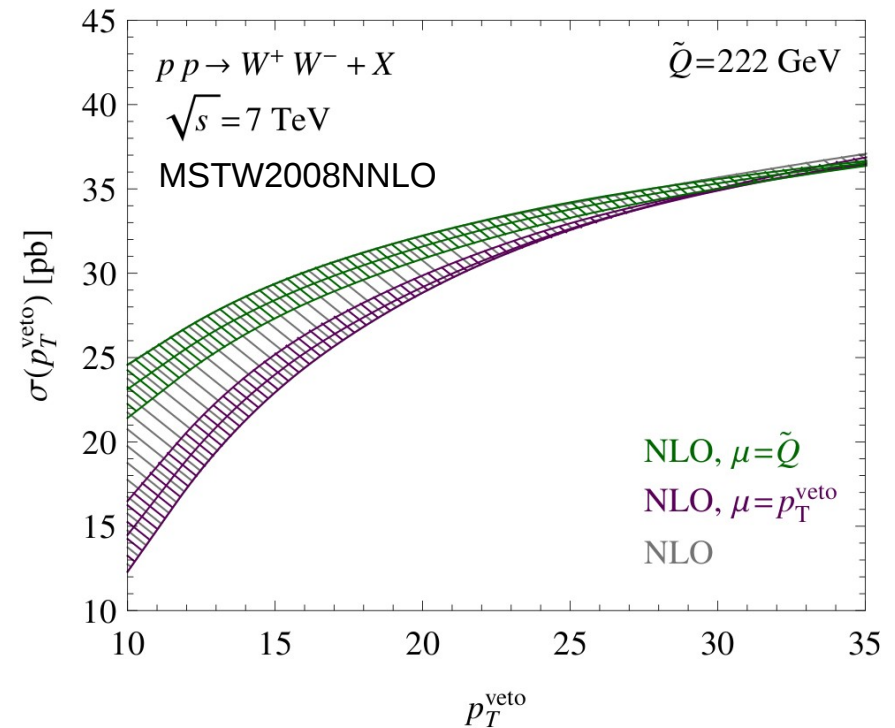
In the following I will show phenomenological results for a center of mass energy of 7 TeV and jet radius  $R = 0.4$ .

Scales are varied independently by factors of 2 about their default values  $\mu = p_T^{\text{veto}}$  and  $\mu_h = Q$ .

For fixed-order expressions at NLO we vary the scale form

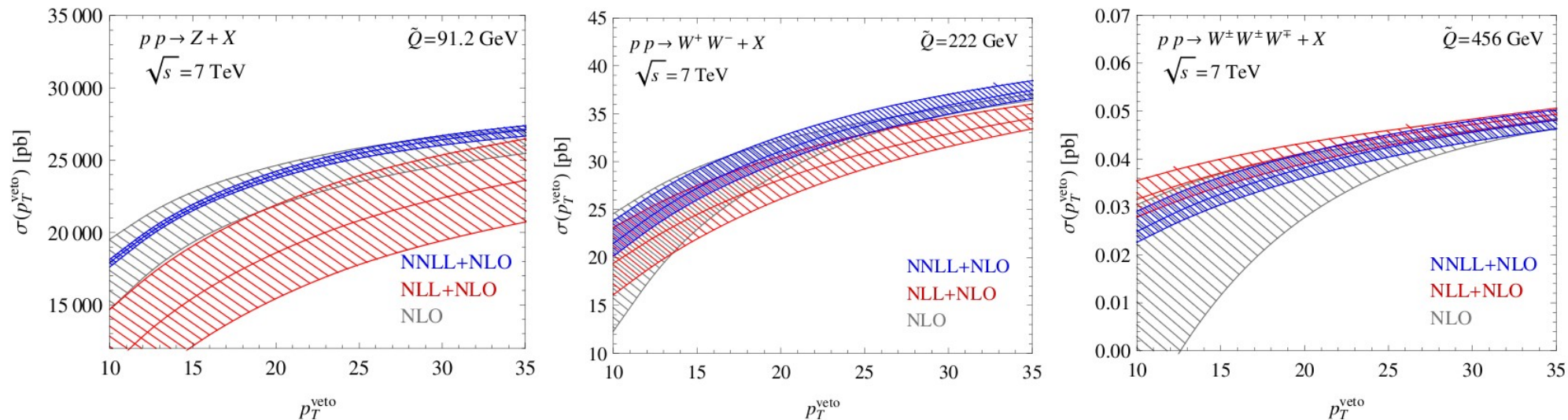
$$p_T^{\text{veto}}/2 < \mu < 2\tilde{Q}$$

The average hard scale is defined by the median value  $\tilde{Q}$  of the invariant-mass distribution.



# Weak Boson Production with a Jet Veto

Numerical results for  $Z, W^+W^-, W^+W^-W^\pm$  production

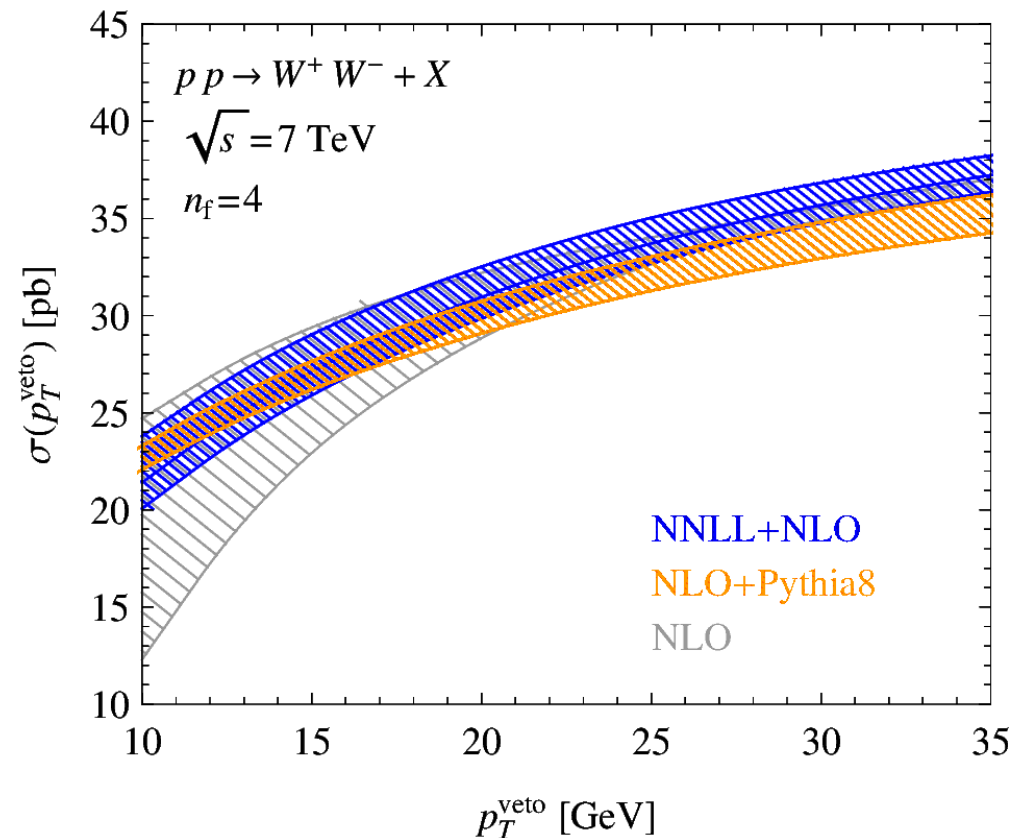


- NNLL+NLO lies close to NLO at the high scale  $\mu = Q$ .
- Width of the uncertainty band for resummed results depends weakly on the veto scale.
- Matching corrections to NNLL:  
Grow linearly up to 3% at  $p_T^{\text{veto}} = 80$  GeV in all cases (matching can be safely ignored at low  $p_T^{\text{veto}}$  values).

# Resummation vs NLO + Parton Shower

Observation: At higher values of  $p_T^{\text{veto}}$  the matched parton shower leads to lower results, which is not expected.

Unitarity of the shower, leads to compensation of changes at low transverse momentum.



Use of a matched parton shower underestimates jet-veto cross section!

In line with conclusions of [Monni, Zanderighi '14](#).

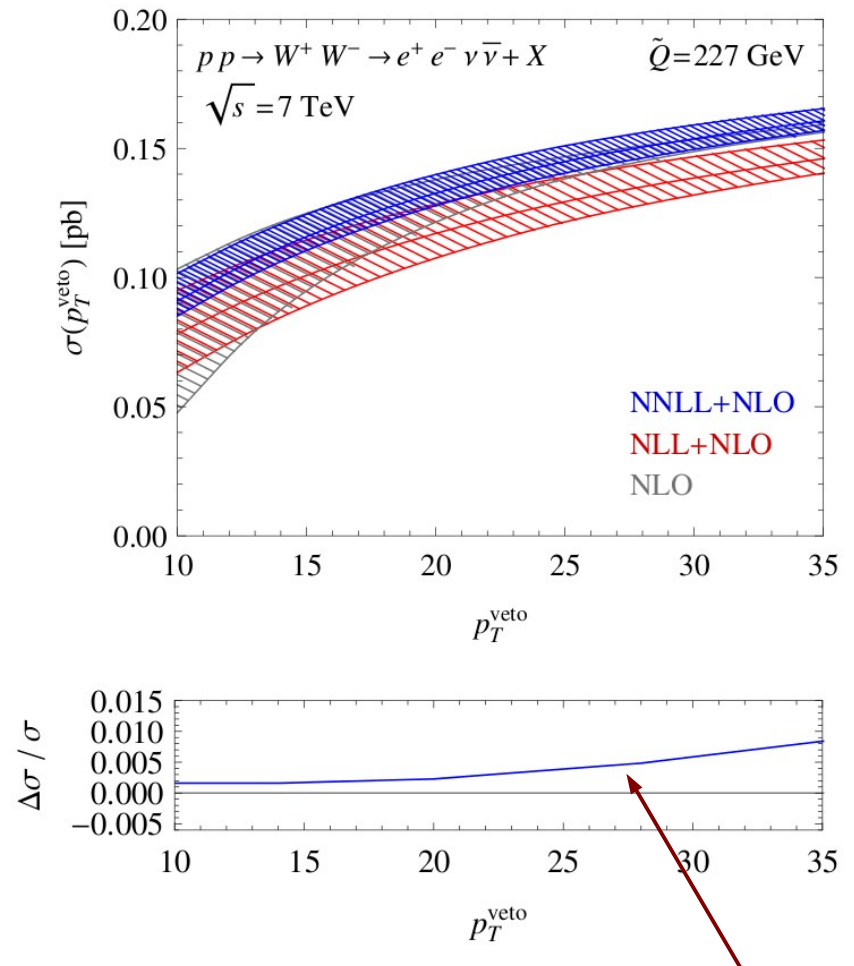
# Decays and Cuts

## Advantage of our framework:

Straightforward to include the decay of the vector bosons and cuts on the final state leptons.

Cuts imposed in the ATLAS analysis for the  $e^+e^-$  channel

- Lepton  $p_T > 20$  GeV
- Leading lepton  $p_T > 25$  GeV
- Lepton pseudorapidity  
 $\eta_e < 1.37$  or  $1.52 < \eta_e < 2.47$
- Dilepton invariant mass  
 $m_{e^+e^-} > 15$  and  $|m_{e^+e^-} - m_Z| > 15$



Matching corrections remain small

# Summary

We have an **automated framework** for theoretical predictions for the production cross section of any number of weak bosons with a jet veto at NNLL+NLO accuracy.

Is based on a factorization theorem derived in SCET and implemented within the [MadGraph5\\_aMC@NLO](#) code.

- Public code (easily accessible).
- Straightforward to include decays and cuts on the decay products.
- Two schemes (additive and multiplicative matching) that allow for a cross check.
- The scheme with additive matching, can be easily extended to higher accuracy if the necessary ingredients are provided.

The hard function for  $W^+ W^-$  production can be extracted from recent two-loop results (1408.6409, 1503.04812).

# Conclusions concerning $W^+W^-$ Production

- NNLL resummation effects are small (NNLL+NLO in good agreement with NLO at  $\mu_f \sim \mu_r \sim Q$ ).
- Several effects can lead to sizable changes in the jet veto cross section:

- **Hard scale choice** can lead up to  $\sim 7\%$  higher NNLL+NLO results.
- **NNLO effects** increase the total rate by  $\sim 9\%$ .
- **Two loop beam functions** are enhanced by logarithms of the jet radius starting at this order. This enhancement is not captured by one loop scale variation.

In Higgs production: NNLL+NLO  $\xrightarrow{-15\%}$  N<sup>3</sup>LL+NNLO (at  $R = 0.4$ )

- **Matched parton shower** underestimates jet-veto cross section.
- **Non-perturbative corrections** are logarithmically enhanced and can be underestimated by Pythia hadronization effects.

Accounting for all these effects will be important before drawing any conclusions from the two sigma excess.



# Outlook: Effective Theory for Jet Processes

- Jet processes: SCET not very successful so far, problem of so-called non-global logarithms (NGLs).
- Usual H\*J\*S factorization does not achieve complete scale separation.
- In [Becher, Neubert, LR, Shao \(1508.06645\)](#) we perform an EFT analysis of cone-jet cross sections:
  - Find additional mode (besides soft, collinear), describing soft small angle radiation.
  - Factorized form (full scale separation).

$$\tilde{\sigma}(\tau) = \sigma_0 H(Q) \tilde{S}(Q\tau) \left[ \sum_{m=1}^{\infty} \left\langle \mathcal{J}_m(Q\delta) \otimes \tilde{\mathcal{U}}_m(Q\delta\tau) \right\rangle \right]^2$$

- Solving the associated (highly non-trivial) RG equations resums all large logs (also NGLs). Framework not limited to leading logs or leading color.

# Backup Slides

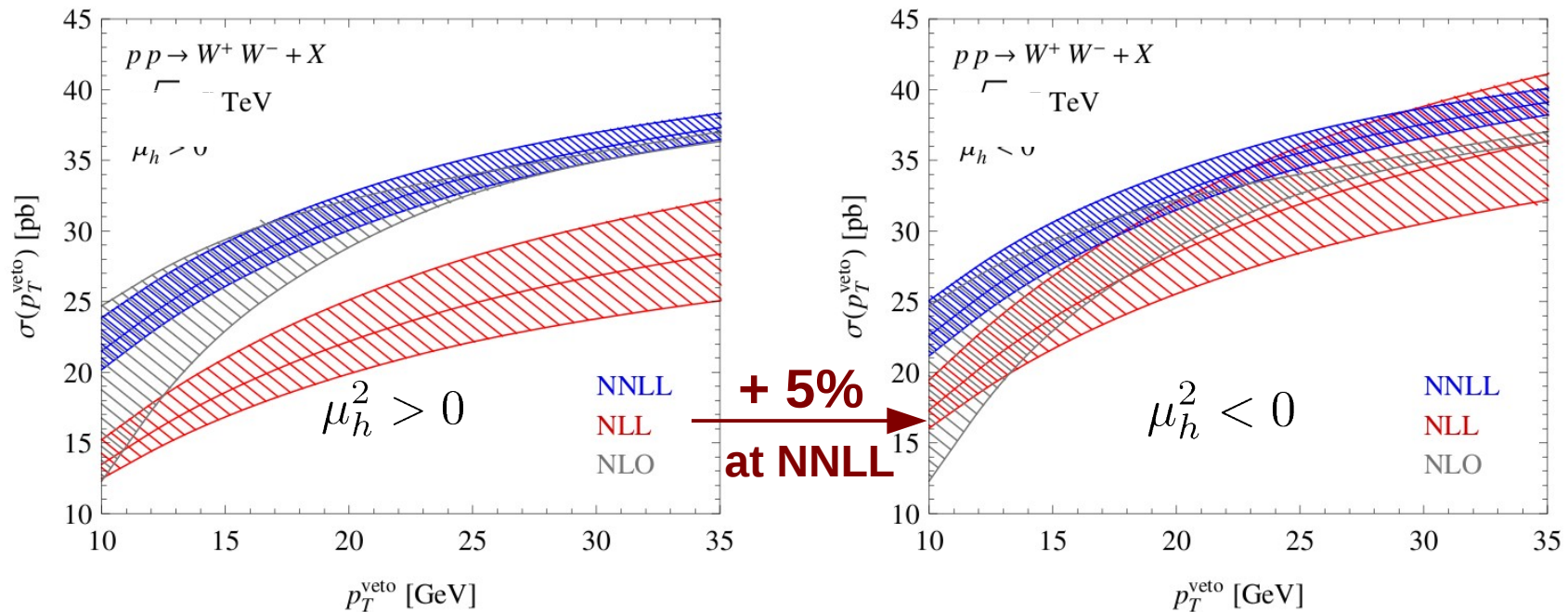
# Choice of the Hard Scale

Standard choice for the hard matching scale:  $\mu_h^2 \approx Q^2$

We also consider using an imaginary value:  $\mu_h^2 \approx -Q^2$

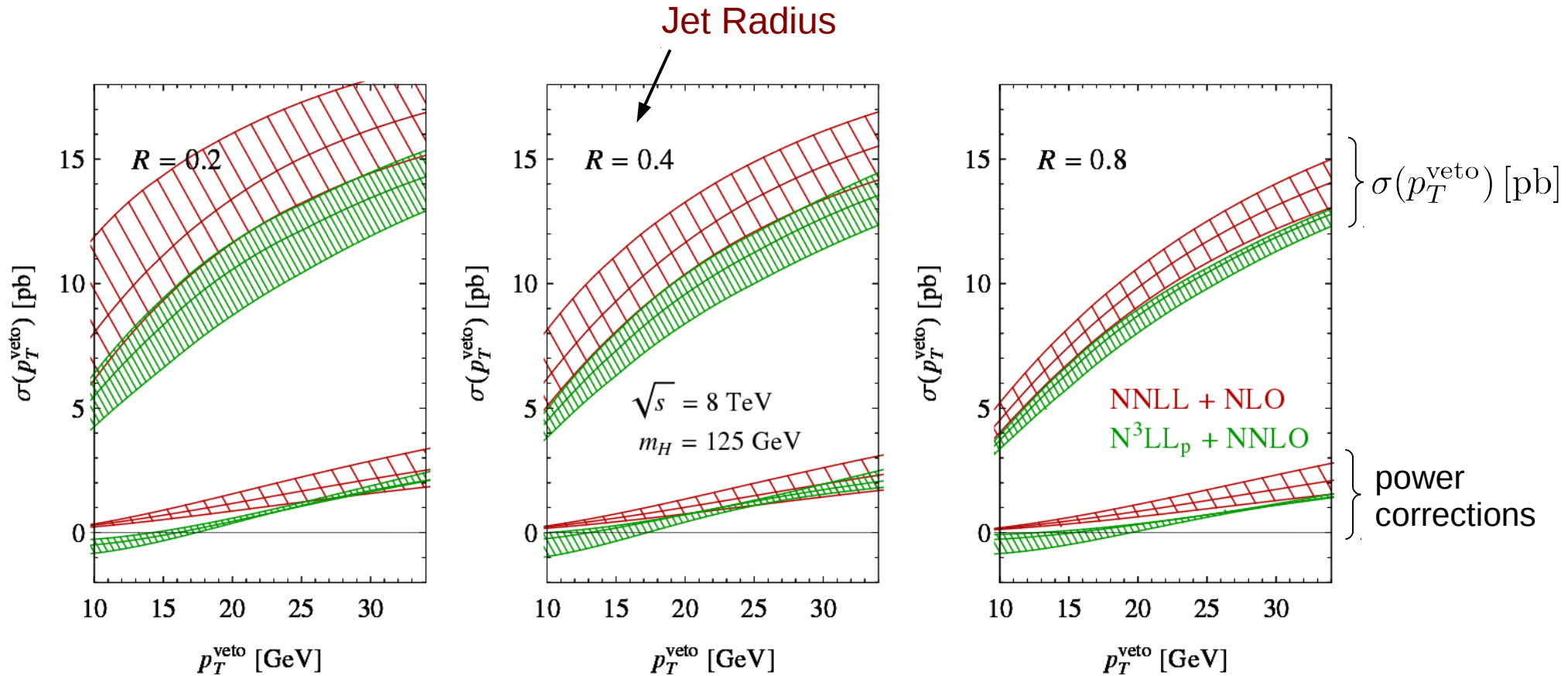
Imaginary choice resums  $(\alpha_s \pi^2)^n$  terms in single boson production.

For multiparticle final states, no suitable choice that maps the hard function onto a Euclidean quantity ( $\ln^2(-1)$  terms irrespective of scale choice).



Note: There is an ambiguity  $\mu_h^2 = -Q^2 \pm i\epsilon$  for imaginary scale choice and depending on that choice the result can be 2% higher.

# Higgs Production Cross Section with a Jet Veto



- We choose a scheme where scale variations are done separately and then quadratically added (avoid accidental cancellation and ensures good control over different sources of large corrections)
- Power corrections are small/suppressed ( $p_T/m_H$ )

# Including photons

- $W \gamma$  resummed result: huge corrections from matching
- Indicates something is missing  $\rightarrow$  Photon must be treated as a jet, therefore the zero jet framework is not the appropriate scheme.

