

APFEL

Improvements and Developments

[arXiv:1310.1394](https://arxiv.org/abs/1310.1394)

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CERN



HERAFitter External Meeting

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In collaboration with Stefano Carrazza and Juan Rojo

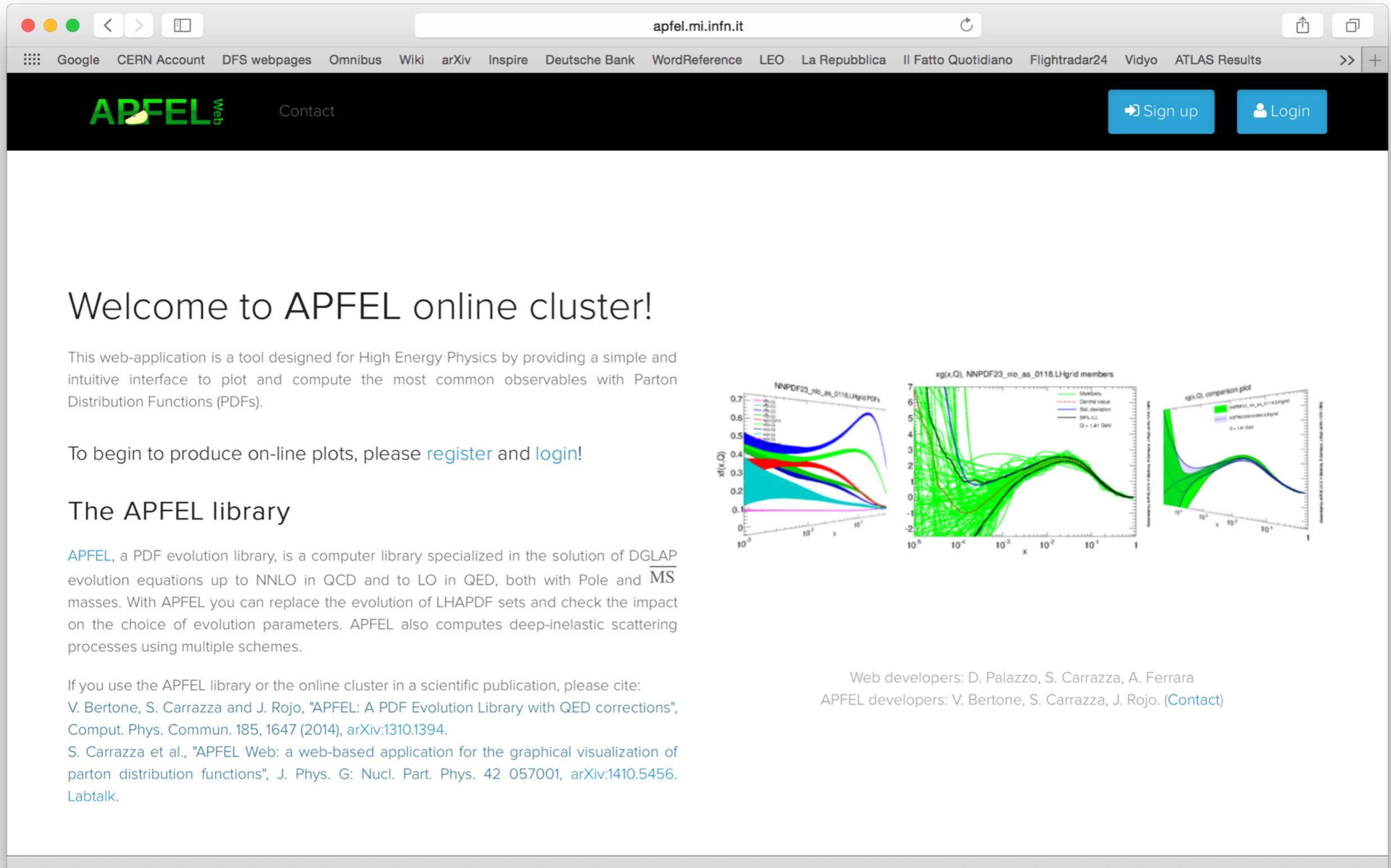
Recap on APFEL

Main Features

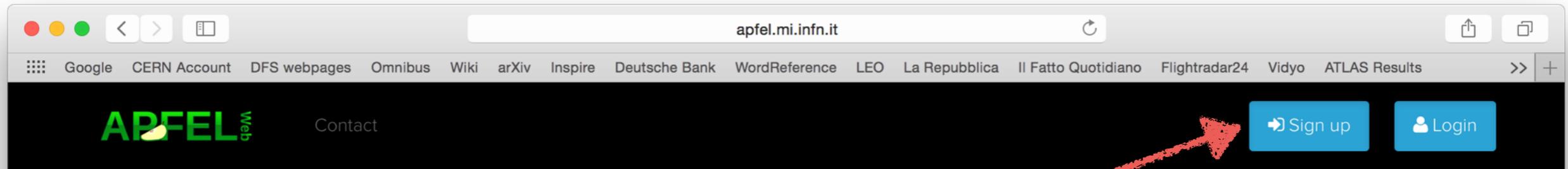
🍏 APFEL is a **public** library with:

- 🍏 QCD+QED DGLAP evolution up to NNLO in QCD and LO in QED.
- 🍏 Module for the computation of DIS NC and CC observables up to NNLO in different mass schemes (ZM-VFNS, FFNS and FONLL).
- 🍏 Pole and $\overline{\text{MS}}$ heavy quark masses.
- 🍏 interfaces to FORTRAN, C/C++ and Python.
- 🍏 interfaced to LHAPDF 5 and 6 (both input and output).
- 🍏 Graphical User Interface (GUI).
- 🍏 publicly available from <http://apfel.hepforge.org>.
- 🍏 Amazing Web Interface: <http://apfel.mi.infn.it>

The Web Interface



The Web Interface



APFEL registration

Please complete the form below to access to the APFEL website:

Enter your e-mail address

Enter your password

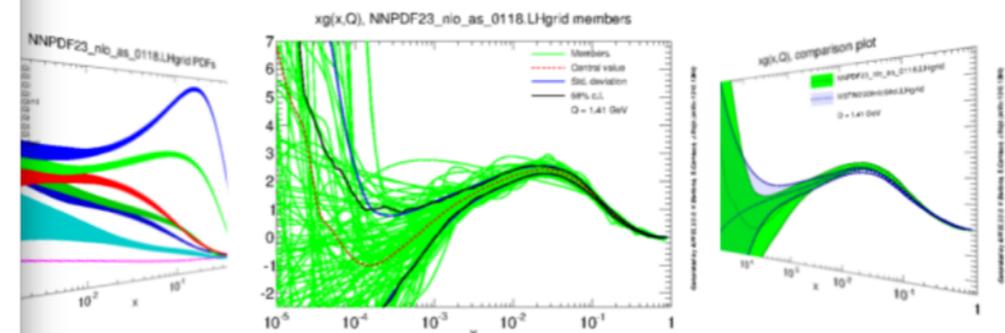
Confirm your password

Spin of the Standard Model Higgs?

Register

Mobile website:

ANDROID APP ON Google play



If you use the APFEL library or the online cluster in a scientific publication, please cite:
V. Bertone, S. Carrazza and J. Rojo, "APFEL: A PDF Evolution Library with QED corrections",
Comput. Phys. Commun. 185, 1647 (2014), arXiv:1310.1394.
S. Carrazza et al., "APFEL Web: a web-based application for the graphical visualization of
parton distribution functions", J. Phys. G: Nucl. Part. Phys. 42 057001, arXiv:1410.5456.
Labtalk

Web developers: D. Palazzo, S. Carrazza, A. Ferrara
APFEL developers: V. Bertone, S. Carrazza, J. Rojo. ([Contact](#))

Free registration (100 MB of disk space)

The Web Interface

The screenshot displays the APFEL Web interface in a browser window. The address bar shows `apfel.mi.infn.it`. The browser's address bar contains several bookmarks: Google, CERN Account, DFS webpages, Omnibus, Wiki, arXiv, Inspire, Deutsche Bank, WordReference, LEO, La Repubblica, Il Fatto Quotidiano, Flightradar24, Vidyo, and ATLAS Results. The APFEL Web logo is in the top left, with a "Contact" link. A "Logout" button is in the top right.

The main content area is titled "My APFEL Gallery". Below the title, it says: "Below you find a gallery with your recent jobs. If the gallery is empty [start a new job!](#)".

The gallery contains a 3x3 grid of plots. The top row shows "xg(x,Q), comparison" plots. The middle row shows "F₂(x,Q), NNPDF23_nlo_as_0118" plots. The bottom row shows "F₂(x,Q), NNPDF23_nlo_as_0118" plots. Each plot compares different models and includes a legend.

On the left side, there is a "Workspace" sidebar with the following options:

- Home
- My Profile
- PDF MANAGER
 - My PDF sets
 - Add PDF set
 - Import a LHAPDF grid
- TOOLS
 - Plotting Tools
- DOWNLOAD RESULTS
 - View jobs

On the right side, there is a vertical flow of instructions:

- Prepare PDF (with a red arrow icon)
- Select a plotting tool (with a green arrow icon)
- Collect the result (with a blue arrow icon)

The Web Interface

The screenshot shows a web browser window with the URL `apfel.mi.infn.it`. The browser's address bar and tabs are visible at the top. The page header features the APFEL logo and a 'Logout' button. The main content area is titled 'Select your PDF and choose a plotting tool'. Below this title, there is a paragraph explaining the tool's purpose and a link to 'View jobs'. A section titled 'Select your PDF and a Plotting Tool' contains a list of 15 PDF sets, each with a checkbox. To the right of this list is a vertical stack of 8 buttons for plotting and computing. On the left side of the page, there is a sidebar menu with sections for 'Workspace', 'PDF MANAGER', 'TOOLS', and 'DOWNLOAD RESULTS'. The 'Plotting Tools' option in the 'TOOLS' section is highlighted.

Workspace

- Home
- My Profile

PDF MANAGER

- My PDF sets
- Add PDF set
- Import a LHAPDF grid

TOOLS

- Plotting Tools**

DOWNLOAD RESULTS

- View jobs

Select your PDF and choose a plotting tool

Perform PDF comparison, luminosities and DIS observables with your personalized PDF sets. Some jobs like luminosities require some time to be finalized so after submitting your job visit the [View jobs](#) page. The plotting tools can be used for both LHAPDF libraries: [LHAPDF5](#) and [LHAPDF6](#) libraries.

Select your PDF and a Plotting Tool

- NNPDF23_nnlo_as_0118 (LHAPDF6)
- NNPDF23_nnlo_as_0118_central (LHAPDF6)
- NNPDF3.0 NNLO LHA (LHAPDF6)
- NNPDF3.0 NNLO APFEL NF5 (LHAPDF6) [APFEL]
- Vicini (LHAPDF6)
- NNPDF3.0 NNLO APFEL NF6 (LHAPDF6) [APFEL]
- NNPDF30NNLO_LHAPDF (LHAPDF6)
- NNPDF30NNLO_APFEL_exact (LHAPDF6) [APFEL]
- NNPDF30NNLO_APFEL_expanded (LHAPDF6) [APFEL]
- NNPDF30NLO_LHAPDF (LHAPDF6)
- NNPDF30NLO_APFEL_exact (LHAPDF6) [APFEL]
- NNPDF30NLO_APFEL_expanded (LHAPDF6) [APFEL]
- CT10NNLO(LHAPDF) (LHAPDF5)

- Plot PDF Members
- Plot all PDF flavors
- Plot Multiple PDFs (x)
- Plot Multiple PDFs (Q)
- Compute Luminosity
- Compute DIS(x)
- Compute DIS(Q)
- APPLgrid observables

The Web Interface

The screenshot shows a web browser window with the URL `apfel.mi.infn.it`. The browser's address bar and tabs are visible at the top. The page header includes the APFEL logo, a 'Contact' link, and a 'Logout' button. The main content area features a large red handwritten-style text 'Variety of plotting tools' with a red arrow pointing to a vertical stack of buttons on the right. The central text reads 'Select your PDF and choose a plotting tool' and provides instructions on how to use the tools. Below this is a list of PDF sets with checkboxes, and a sidebar on the left with navigation options.

Workspace

- Home
- My Profile

PDF MANAGER

- My PDF sets
- Add PDF set
- Import a LHAPDF grid

TOOLS

- Plotting Tools**

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Variety of plotting tools

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Select your PDF and a Plotting Tool

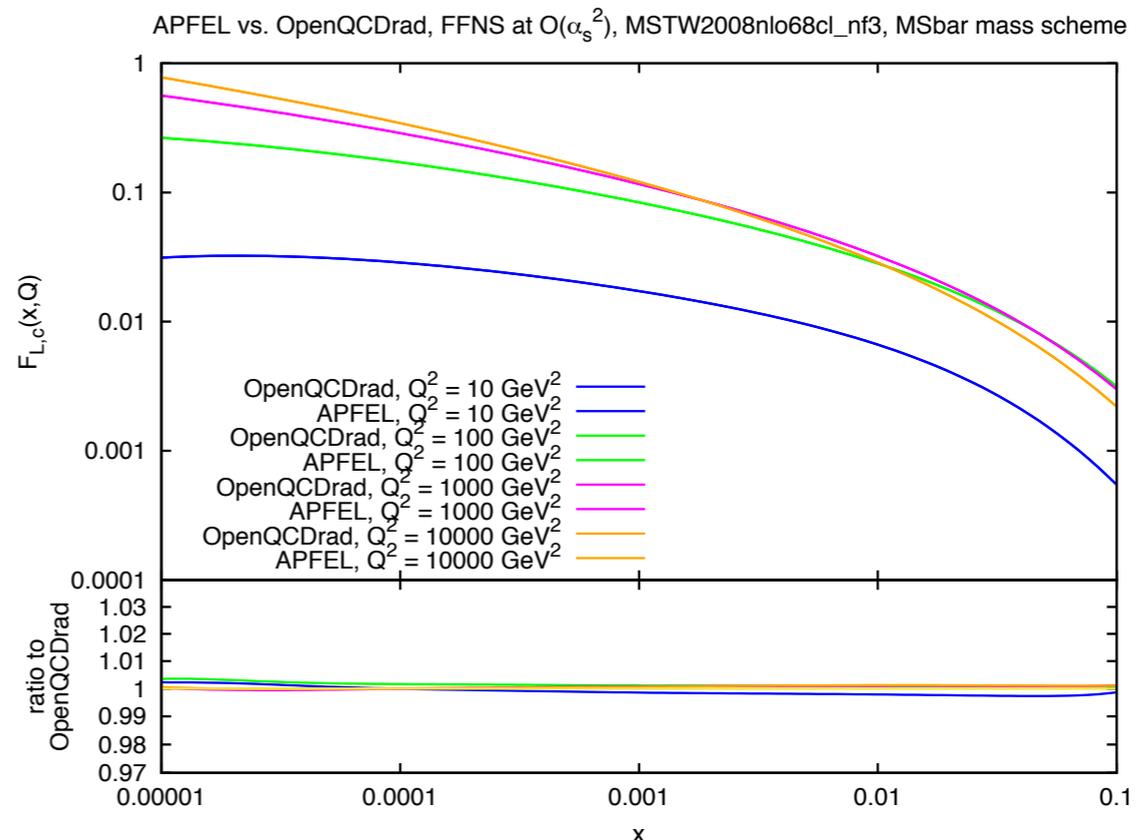
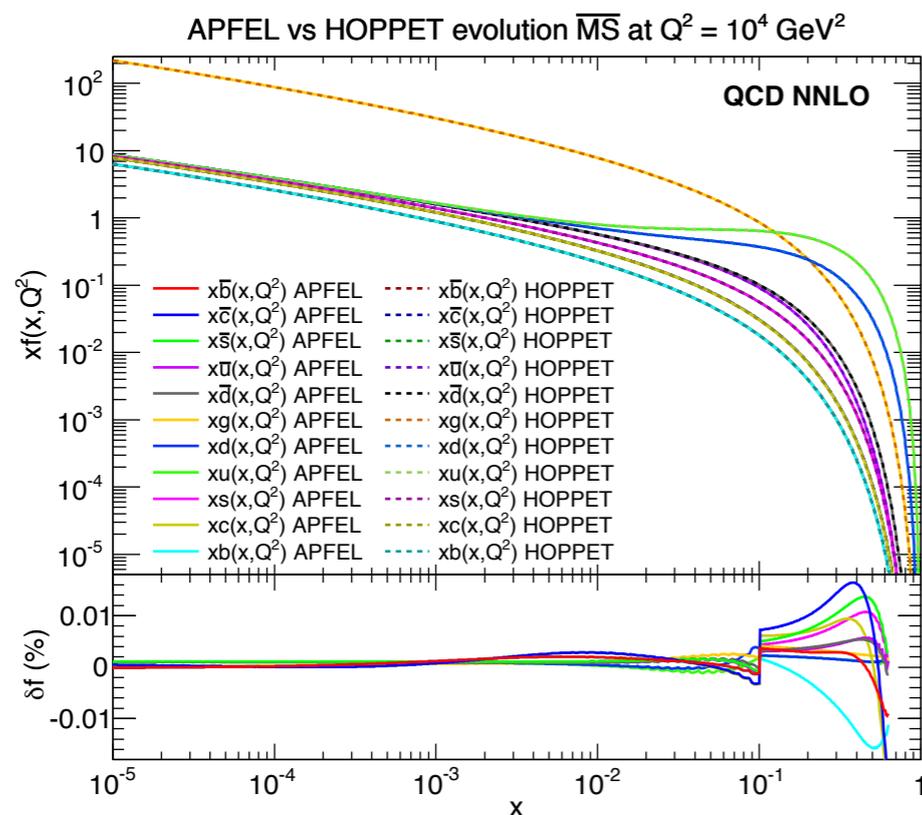
- NNP23_nnlo_as_0118 (LHAPDF6)
- NNP23_nnlo_as_0118_central (LHAPDF6)
- NNP3.0 NNLO LHA (LHAPDF6)
- NNP3.0 NNLO APFEL NF5 (LHAPDF6) [APFEL]
- Vicini (LHAPDF6)
- NNP3.0 NNLO APFEL NF6 (LHAPDF6) [APFEL]
- NNP30NNLO_LHAPDF (LHAPDF6)
- NNP30NNLO_APFEL_exact (LHAPDF6) [APFEL]
- NNP30NNLO_APFEL_expanded (LHAPDF6) [APFEL]
- NNP30NLO_LHAPDF (LHAPDF6)
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- NNP30NLO_APFEL_expanded (LHAPDF6) [APFEL]
- CT10NNLO(LHAPDF) (LHAPDF5)

- Plot PDF Members
- Plot all PDF flavors
- Plot Multiple PDFs (x)
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- Compute Luminosity
- Compute DIS(x)
- Compute DIS(Q)
- APPLgrid observables

Recent Developments

FONLL Structure Functions with \overline{MS} Masses

- 🍏 APFEL implements also the \overline{MS} scheme for the treatment of the heavy quark masses.
- 🍏 When considering \overline{MS} masses in a PDF fit, there are two aspects to be considered:
 1. different threshold matching conditions for the evolution of PDFs, α_s and (possibly) heavy quark masses themselves (relevant at NNLO in the VFNS),
 2. expressing the massive structure functions in terms of the \overline{MS} masses.



Recent Developments

FONLL Structure Functions with \overline{MS} Masses

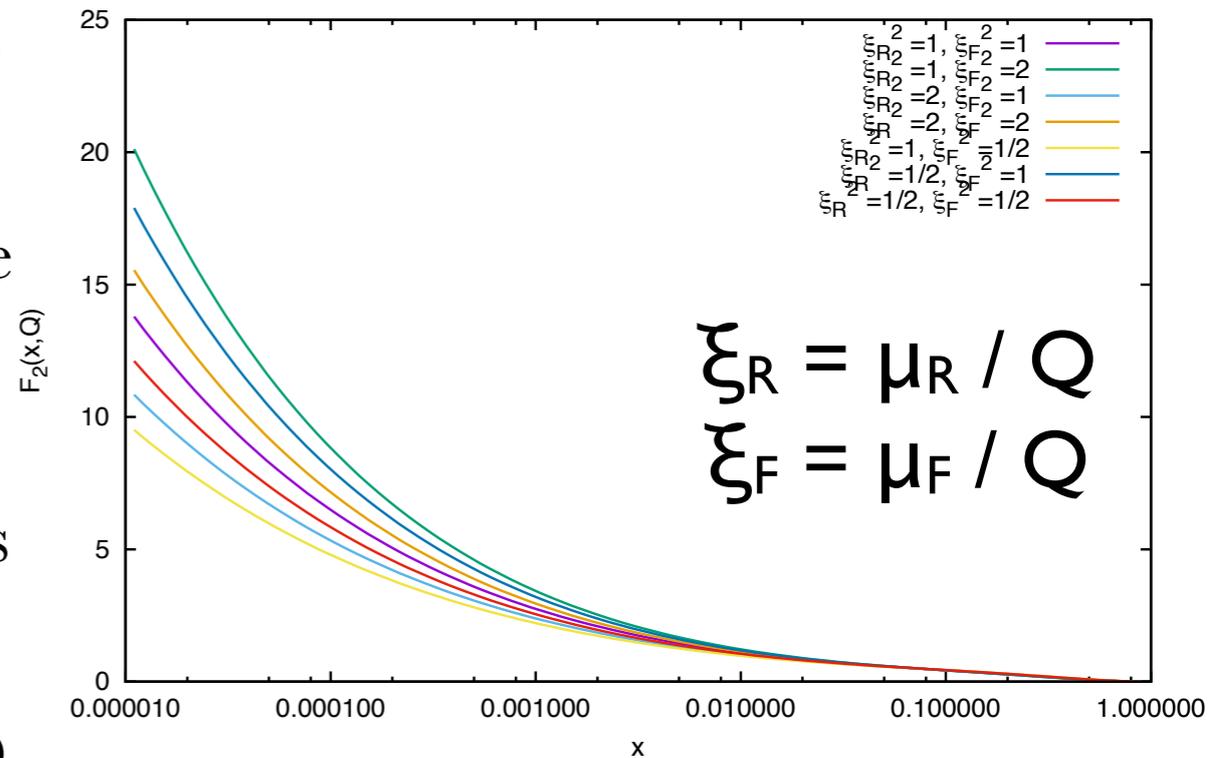
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 2. expressing the massive structure functions in terms of the \overline{MS} masses.
- 🍏 Both these modifications are implemented in APFEL. Two possible approaches to the second aspect:
 - 🍏 the conversion *pole* \rightarrow \overline{MS} masses is done at the heavy quark mass scale m and the dependence on the renormalization scale μ is restored by expressing $\alpha_s(m)$ in terms of $\alpha_s(\mu)$ (no running of the heavy quark masses).
 - 🍏 the conversion *pole* \rightarrow \overline{MS} masses is done at the arbitrary scale μ and the value of $m(\mu)$ is computed from the value $m(m)$ using the RG equation.

Recent Developments

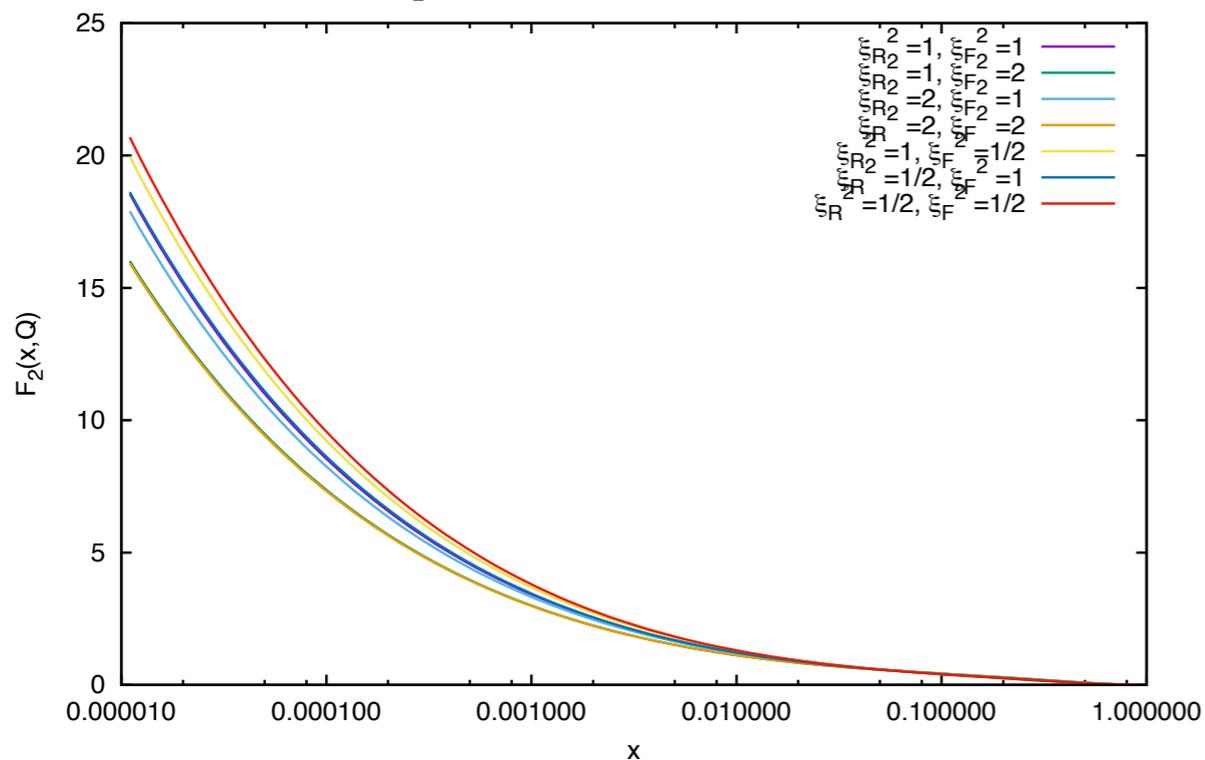
Renormalization and Factorization Scale Variations

- Renormalization and factorization scale variations provide an estimate of the theoretical error.
- When considering scale variations in a PDF fit, the variations must be done both in the evolution and in the structure functions.
- In the VFNS evolution the threshold matching has to be done consistently.
- Reduction of the spread going from LO to NNLO.

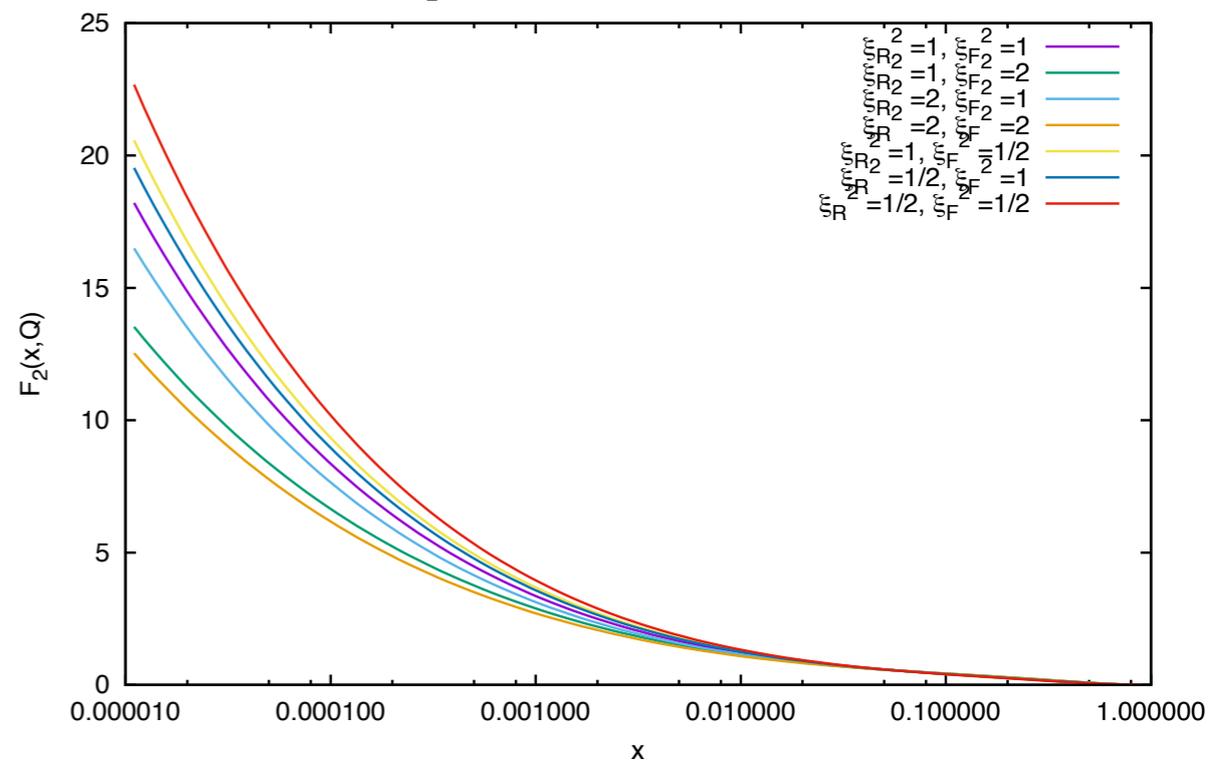
Scale variation for F_2 ZM-VFNS at LO with evolution from 2 to 10000 GeV^2



Scale variation for F_2 ZM-VFNS at NNLO with evolution from 2 to 10000 GeV^2



Scale variation for F_2 ZM-VFNS at NLO with evolution from 2 to 10000 GeV^2

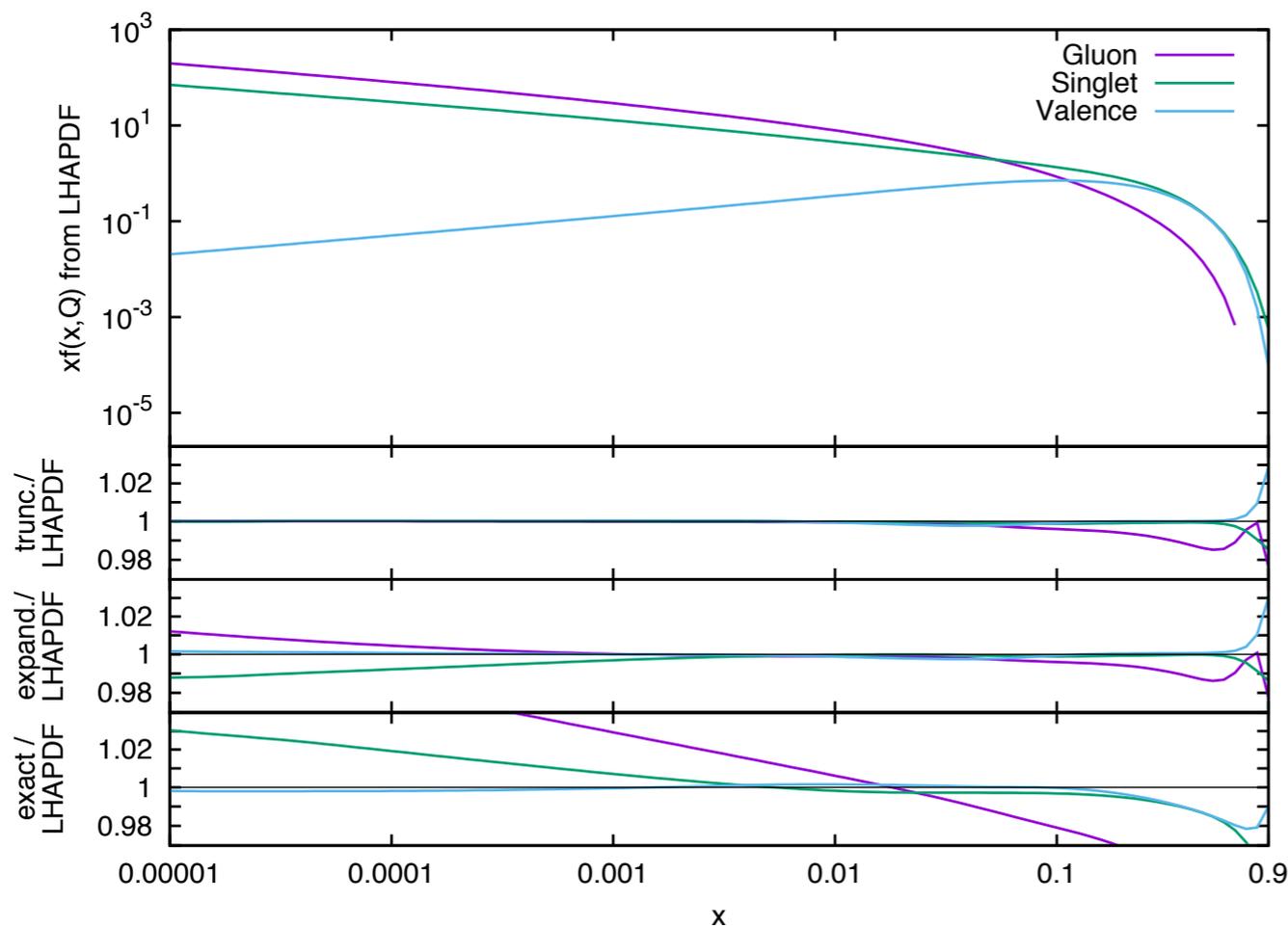


Recent Developments

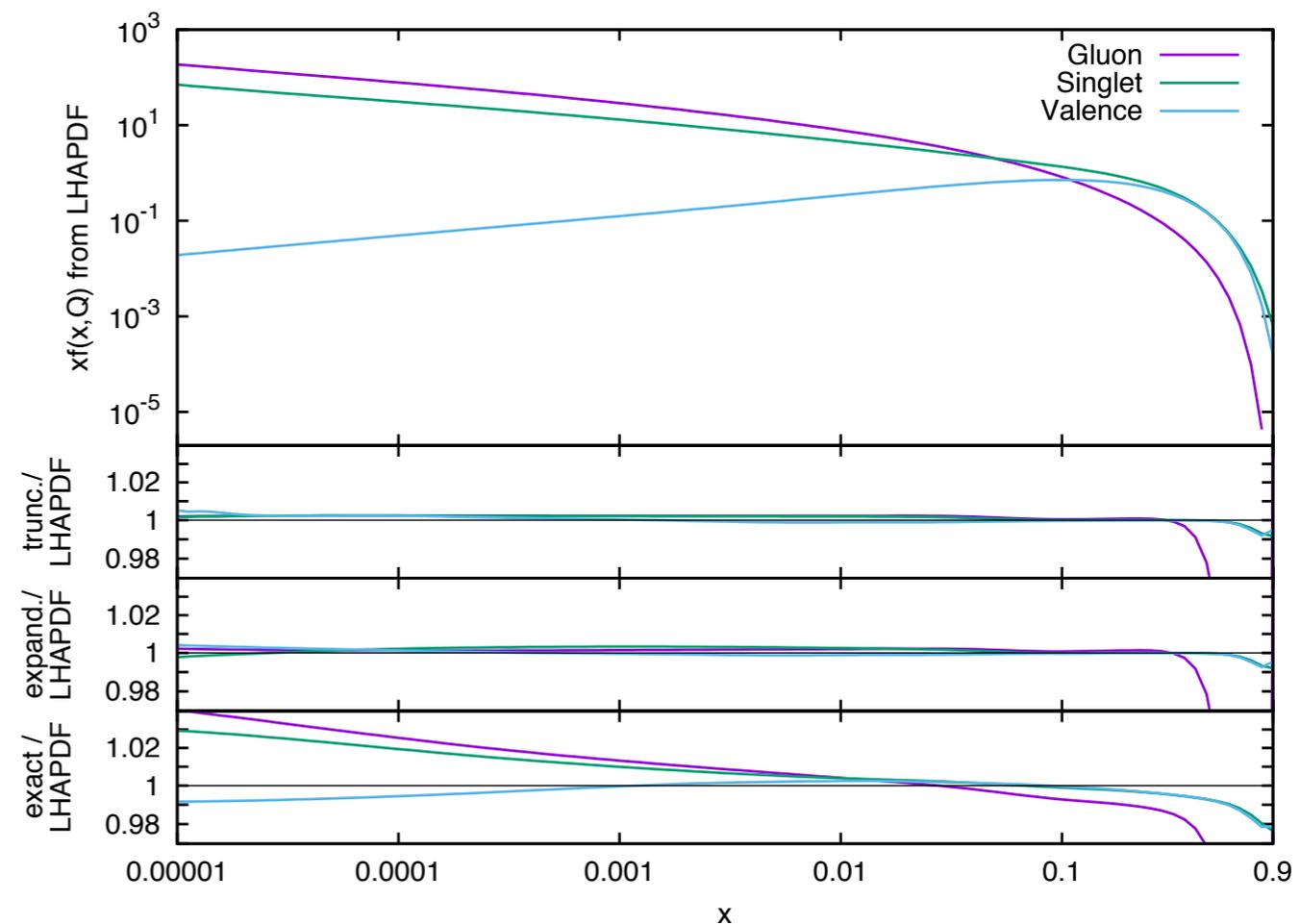
Solutions of the DGLAP Equation

- 🍏 A further way to estimate the theory error in the PDF evolution consists in considering different solutions of the DGLAP equation that do not spoil the logarithmic accuracy.
- 🍏 APFEL implements three different solutions of the DGLAP equation:
 - 🍏 “**exact**” solution: most common solution adopted in most of the PDF fits,
 - 🍏 “**expanded**” solution,
 - 🍏 “**truncated**” solution: used in the NNPDF fits.

APFEL evolution vs. LHAPDF evolution of NNPDF30_nlo_as_0118 from 1 to 100 GeV



APFEL evolution vs. LHAPDF evolution of NNPDF30_nnlo_as_0118 from 1 to 100 GeV



Recent Developments

Tools for the Fitting of Fragmentation Function

- 🍏 The framework used for PDF fits can also be used also for fitting Fragmentation Functions (FFs).
- 🍏 The main modifications to be done are:
 1. space-like evolution \Rightarrow time-like evolution,
 2. DIS cross sections \Rightarrow Single-Inclusive e^+e^- Annihilation (SIA) cross section.
- 🍏 APFEL implements the time-like evolution:
 - 🍏 for the first time the time-like evolution is available in a public code up to NNLO accuracy.
 - 🍏 See [arXiv:1501.00494](https://arxiv.org/abs/1501.00494) for a detailed description and benchmark of the evolution.
- 🍏 Since recently APFEL implements also the SIA cross-sections up to NNLO accuracy.

Recent Developments

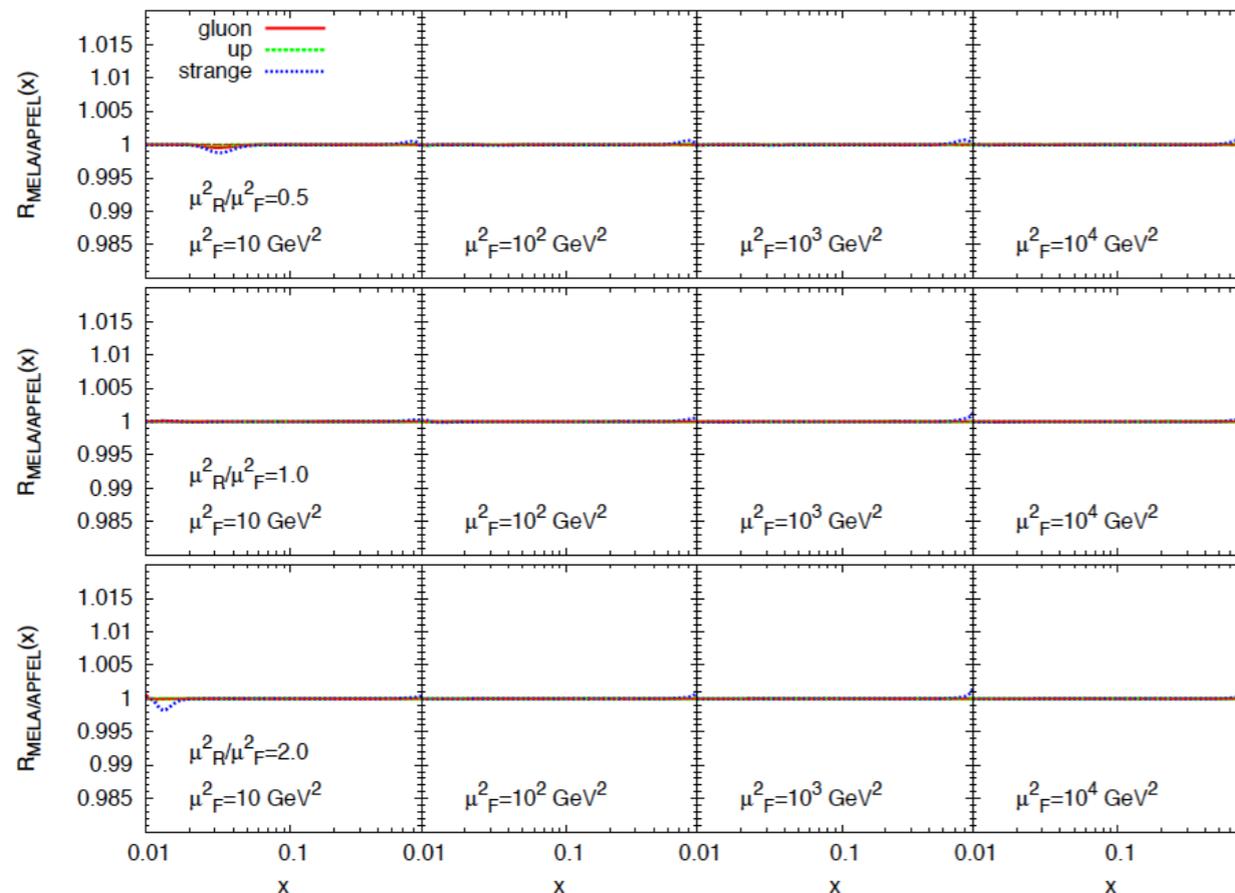
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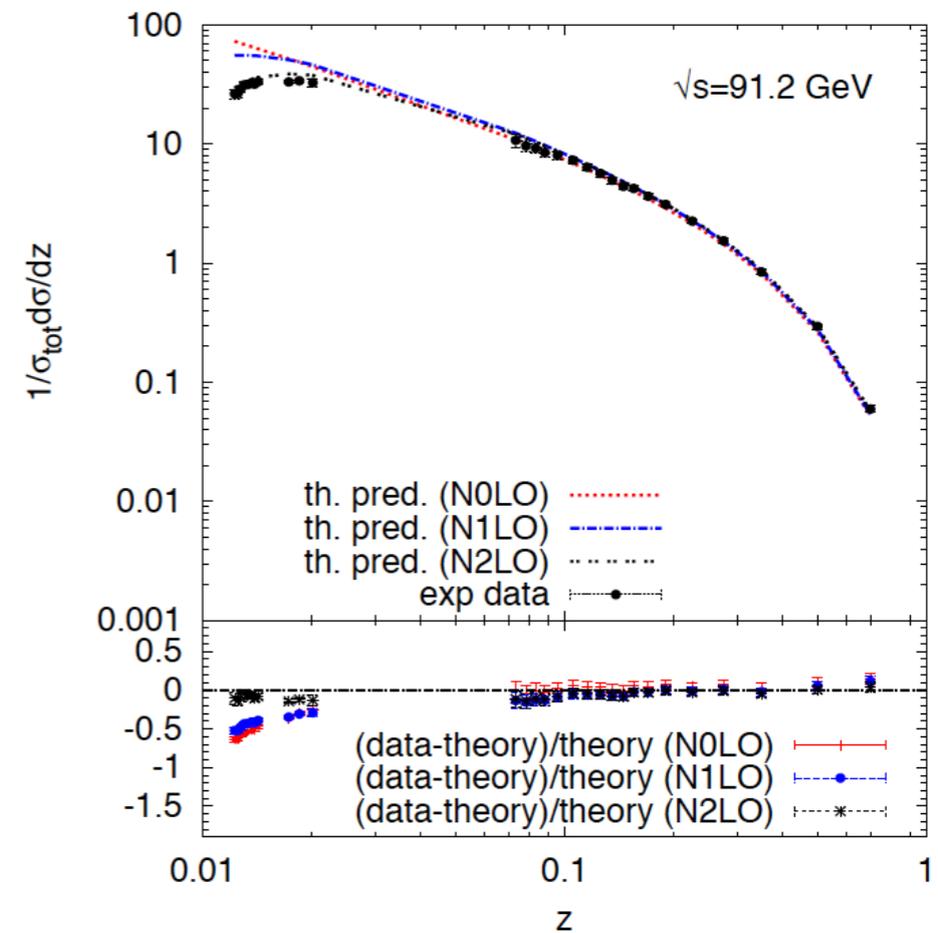
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APFEL vs. MELA: FFNS at NNLO



ALEPH K^\pm (KKP FF set)



Recent Developments

Lepton PDFs

- 🍏 The inclusion of QED corrections to a PDF fit immediately implies the appearance of a photon PDF.
- 🍏 The photon PDF can be determined either by means of a fit (*e.g.* NNPDF2.3QED) or through a theory ansatz (*e.g.* MRST2004QED).
- 🍏 However, the presence of photons in the proton also implies the presence of leptons \Rightarrow lepton PDFs.
- 🍏 Lepton PDFs are expected to be very small and thus a fit is not a viable option for the moment.
- 🍏 Alternatively, assuming that leptons are produced only by photon splitting, at LL accuracy the respective PDFs at the initial scale can be inferred as:

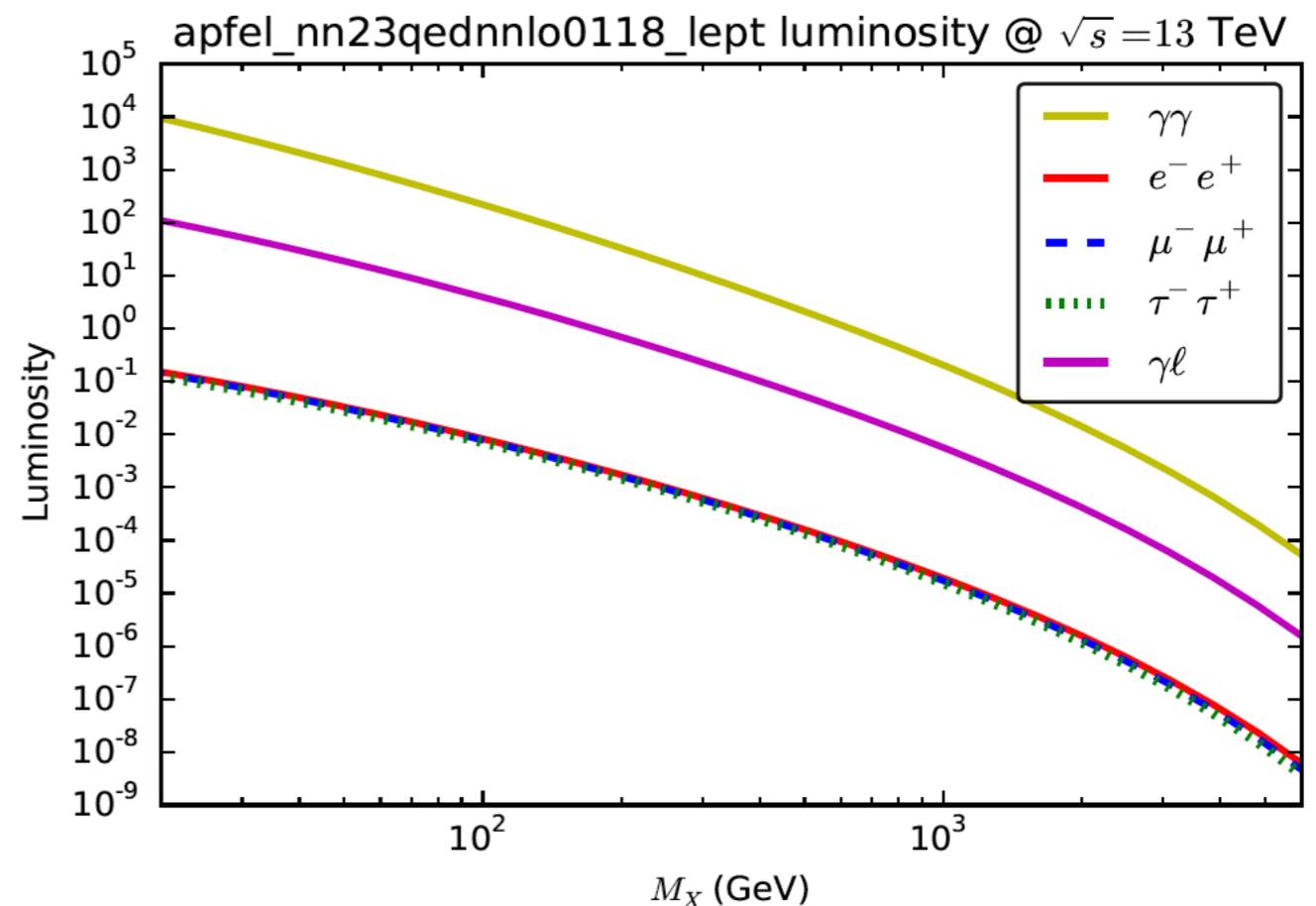
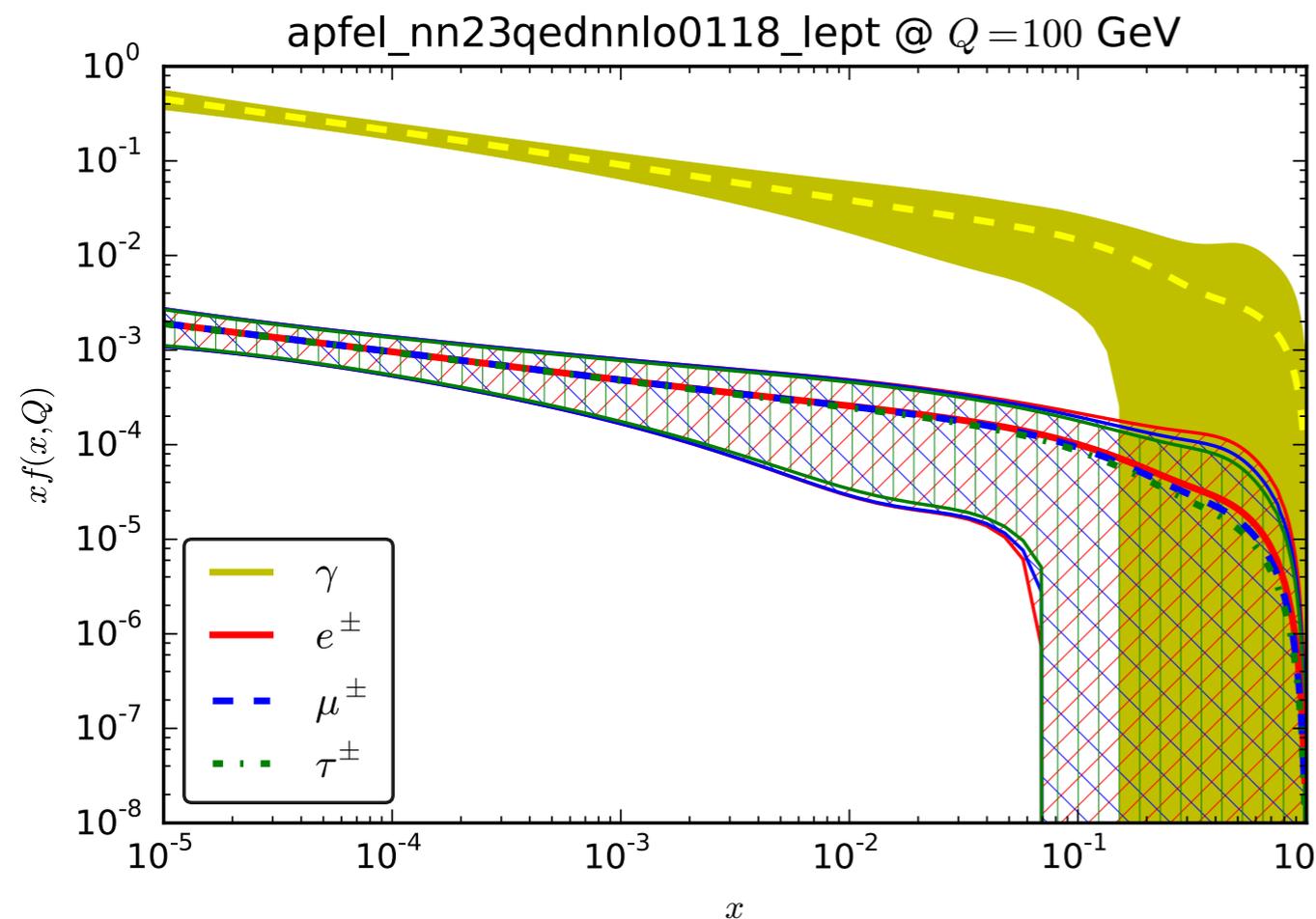
$$\ell_{\beta}(x, Q_0) = \bar{\ell}_{\beta}(x, Q_0) = \frac{\alpha(Q_0)}{4\pi} \ln \left(\frac{Q_0^2}{m_{\beta}^2} \right) \int_x^1 \frac{dy}{y} P_{\ell\gamma}^{(0)} \left(\frac{x}{y} \right) \gamma(y, Q_0)$$

- 🍏 and then evolved up using the proper **extended** DGLAP evolution implemented in APFEL.

Recent Developments

Lepton PDFs

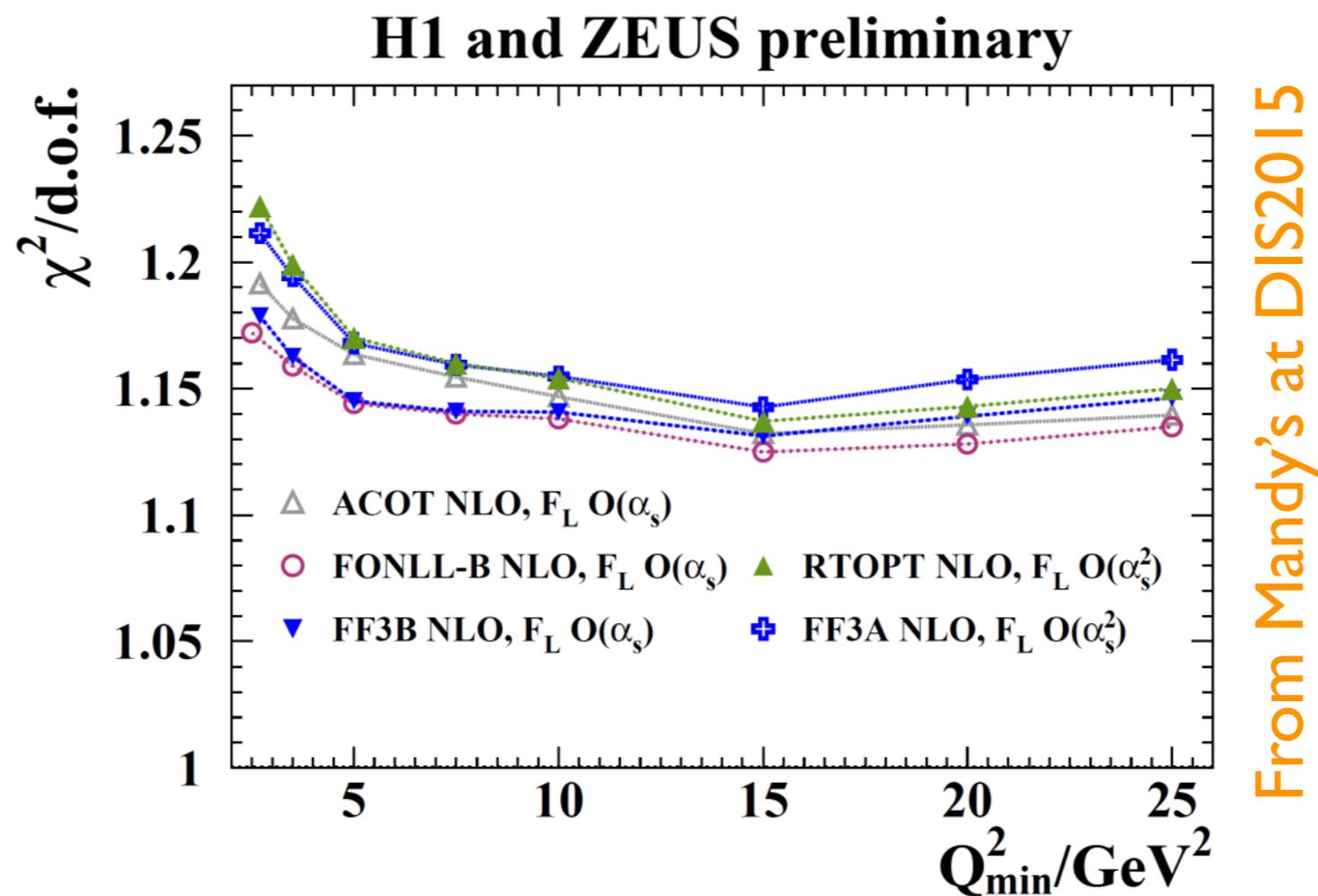
- With APFEL we have produced and made public a bunch of PDF sets containing lepton PDFs produced starting from the NNPDF2.3QED and MRST2004QED sets.
- As expected, the lepton PDFs are very small.
- Same for the lepton-lepton and lepton-photon luminosities but the presence of leptons might be relevant for some hadron collider observables (?).



APFEL in HERAFitter

... a Fruitful Collaboration

- 🍏 APFEL has recently been interfaced to HERAFitter.
- 🍏 Presently, HERAFitter benefits of the APFEL DGLAP QCD evolution and of the FONLL structure functions up to NNLO.



- 🍏 The FONLL scheme provides a very good description of the HERA data.
- 🍏 In addition, APFEL is very performing as compared to the other schemes.

APFEL in HERAFitter

... a Fruitful Collaboration

🍏 As already mentioned, APFEL implements also the $\overline{\text{MS}}$ definition for the heavy quark masses.

🍏 Since recently, this option is available also in HERAFitter:

● FONLL-B scheme (NLO) with pole masses:

```
After minimisation      547.21   582   0.940
Dataset 1      107.95   145   NC cross section HERA-I H1-ZEUS combined e-p.
Dataset 2      388.85   379   NC cross section HERA-I H1-ZEUS combined e+p.
Dataset 3       20.25    34   CC cross section HERA-I H1-ZEUS combined e-p.
Dataset 4       30.17    34   CC cross section HERA-I H1-ZEUS combined e+p.
```

● FONLL-B scheme (NLO) with $\overline{\text{MS}}$ masses

```
After minimisation      539.90   582   0.928
Dataset 1      108.39   145   NC cross section HERA-I H1-ZEUS combined e-p.
Dataset 2      381.68   379   NC cross section HERA-I H1-ZEUS combined e+p.
Dataset 3       20.13    34   CC cross section HERA-I H1-ZEUS combined e-p.
Dataset 4       29.70    34   CC cross section HERA-I H1-ZEUS combined e+p.
```

Improvement of the χ^2 in the $\overline{\text{MS}}$ scheme

🍏 The $\overline{\text{MS}}$ mass seems to improve on the description of the HERA data (especially at the lowest scales).

🍏 It would be interesting to use this framework to fit the heavy quark masses.

Conclusions

- 🍏 APFEL has some features that can be of interest for HERAFitter:
 - 🍏 QCD+QED DGLAP evolution \Rightarrow photon PDF,
 - 🍏 FONLL structure functions,
 - 🍏 different solutions of the DGLAP equation,
 - 🍏 scale variations,
 - 🍏 ...
- 🍏 APFEL is a solid code: it will be used for the next generation of the NNPDF fits (NNPDF3.1).
- 🍏 Presently, HERAFitter benefits of the APFEL DGLAP QCD evolution and of the FONLL structure functions up to NNLO.
- 🍏 The next step is the fit of the photon PDF with HERAFitter using APFEL.