

# Measurement of the Cross Section for open b-Quark Production in Two-Photon Interactions at LEP

Alex Finch for the ALEPH Collaboration

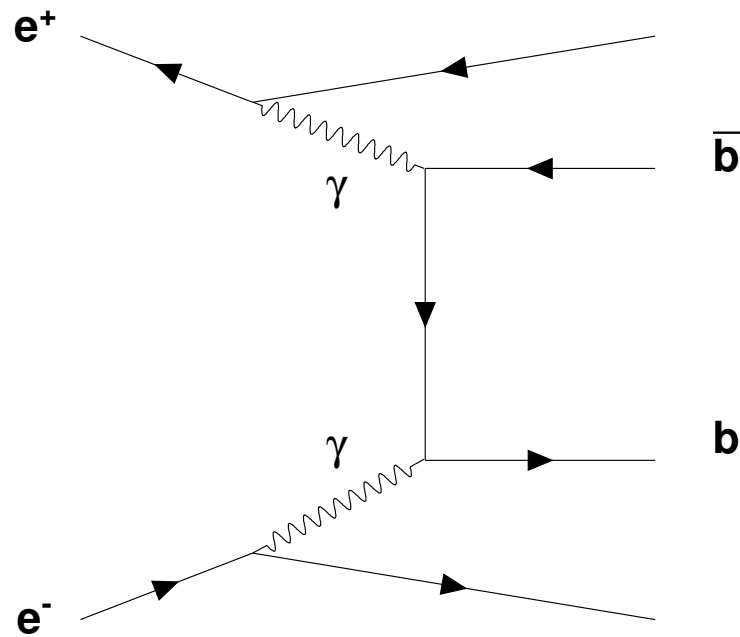
- Measurement of open b-quark production in LEP II data  
 $698 \text{ pb}^{-1}$  ,  $\sqrt{s} = 130 \sim 209 \text{ GeV}$
- First use of lifetime information to identify heavy flavour quarks in  $\gamma\gamma$

## Contents

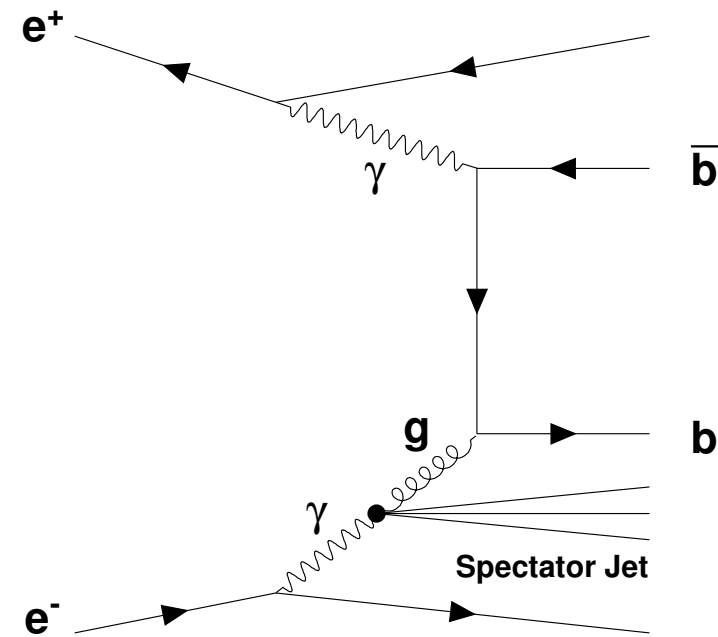
- Background
- “Tools of the Trade”
- PreSelection, and Selection
- Weighted Selection “IDA”
- Systematic Errors
- Cross checks
- Conclusions

## Introduction

- $\sigma(\gamma\gamma \rightarrow b\bar{b}X)$  **reliably** calculable in NLO QCD due to b quark mass.
- $\sigma = 2.1 \sim 4.5 \text{ pb}$ ,  $\sim 0.01 \times \sigma(\gamma\gamma \rightarrow c\bar{c}X) \sim 0.01 \times \sigma(\gamma\gamma \rightarrow uds)$



Direct



Single Resolved

# Existing Results

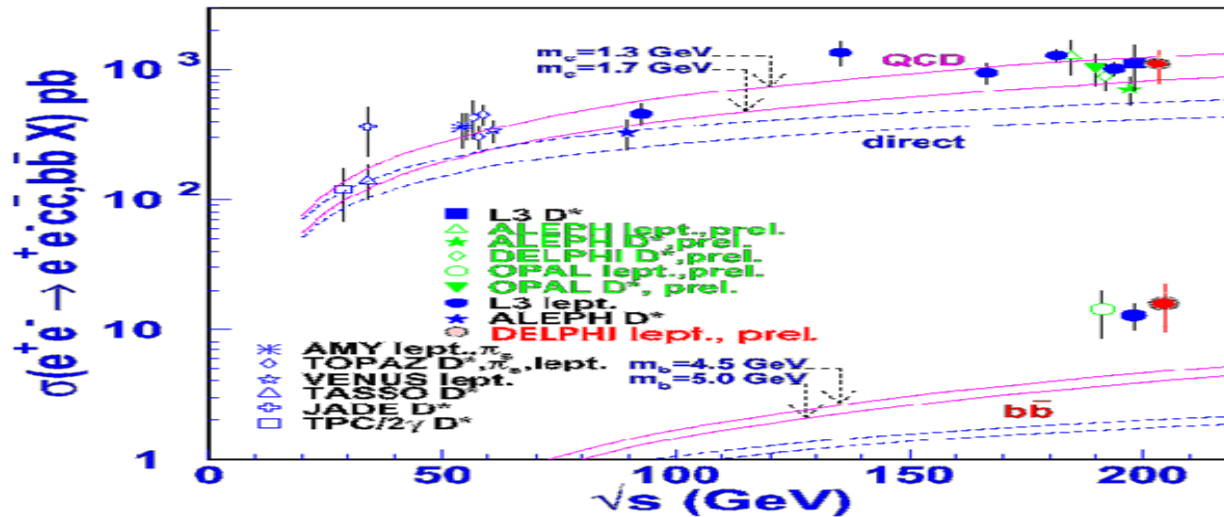
- One published measurement by

L3 ( $12.8 \pm 1.7_{\text{stat}} \pm 2.3_{\text{syst}}$ ) pb.

- Two conference reports:

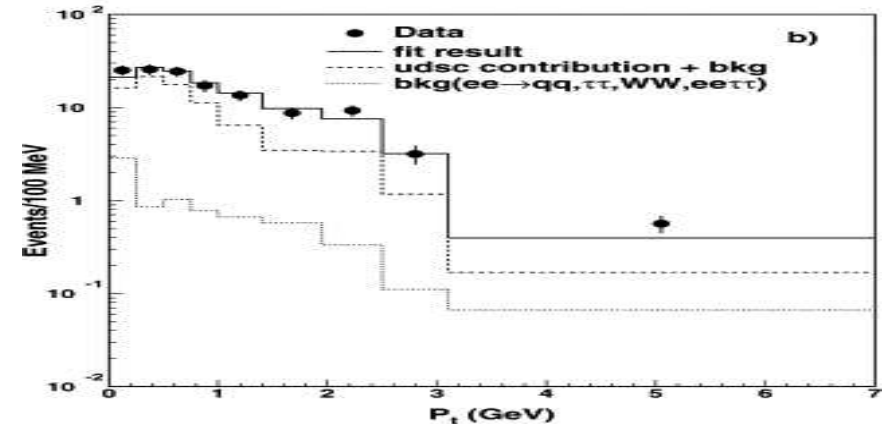
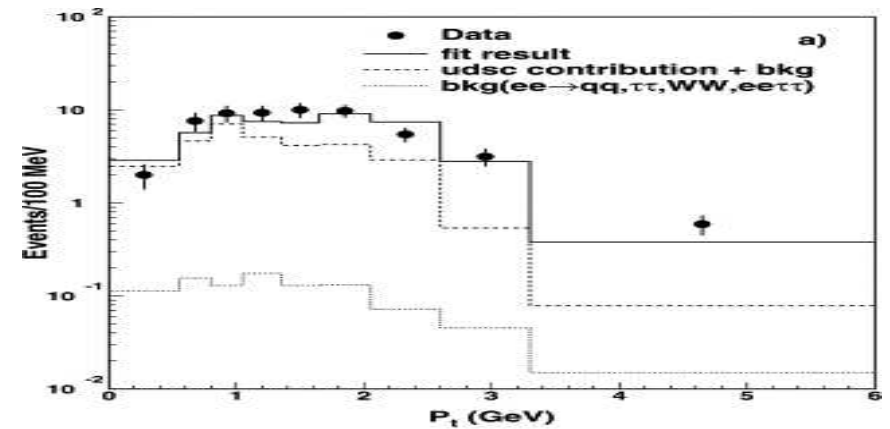
OPAL ( $14.2 \pm 2.5_{\text{stat}} \pm 5.3_{\text{syst}}$ ) pb.  
(Photon 2000)

DELPHI ( $14.9 \pm 3.3_{\text{stat}} \pm 3.4_{\text{syst}}$ ) pb  
(Photon 2003).

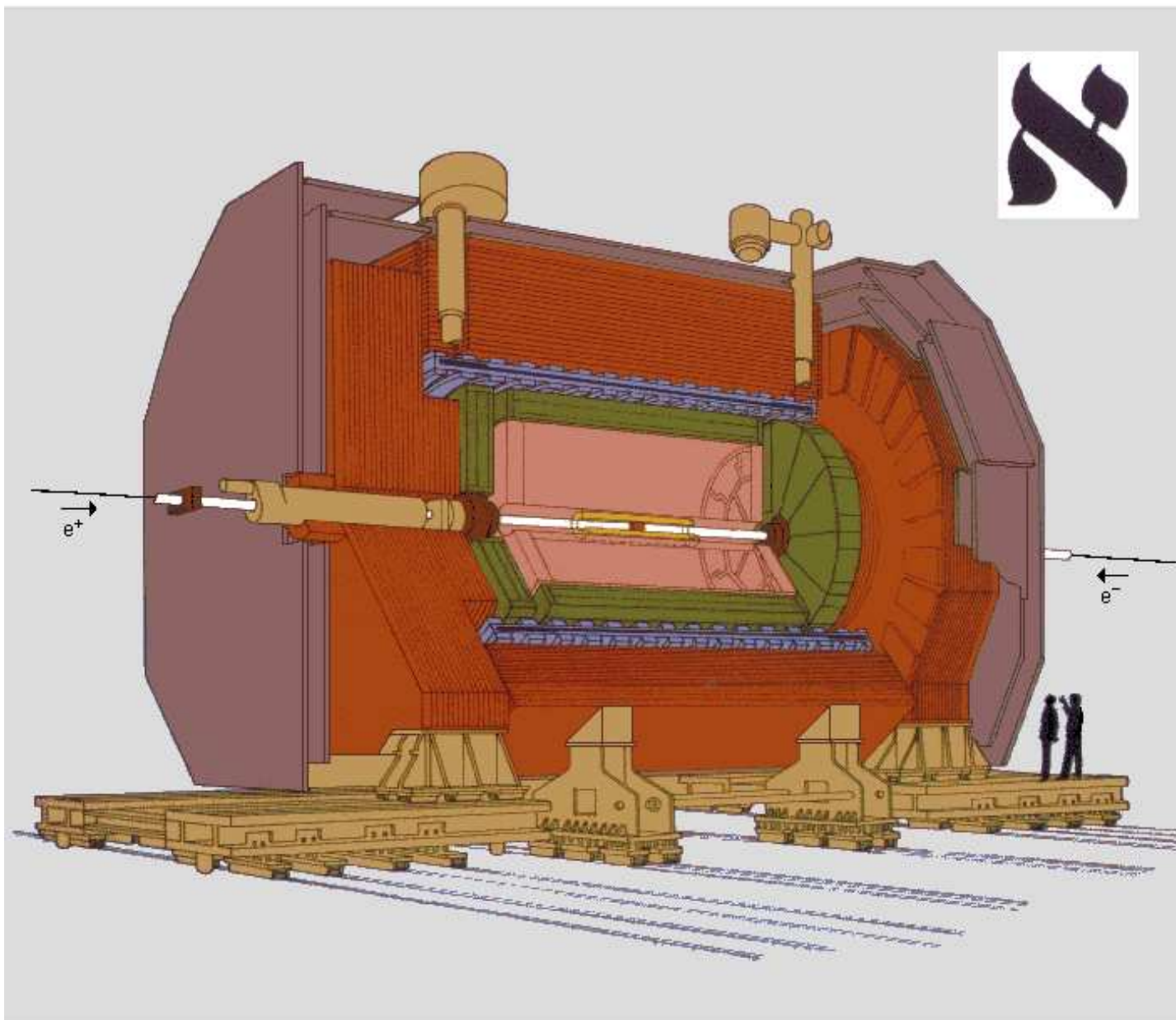










Charm agrees with QCD prediction  
Beauty is significantly above

All measured using high  $p_t$  leptons.



L3 results for (a) electrons and (b) muons



-  Vertex Detector
-  Inner Tracking Chamber
-  Time Projection Chamber
-  Electromagnetic Calorimeter
-  Superconducting Magnet Coil
-  Hadron Calorimeter
-  Muon Chambers
-  Luminosity Monitors

**The ALEPH Detector**

## Tools of the Trade (Software)

### Monte Carlo

- **PYTHIA 6.1** for all  $\gamma\gamma \rightarrow X$   
b and c, direct and resolved - massive matrix elements.  
( resolved: photon's pdf was SaS 1D)
- $e^+e^- \rightarrow q\bar{q}$  -" KK " Monte Carlo
- **HERWIG** used to model  $\gamma\gamma \rightarrow b\bar{b}X$   
(for systematic error calculations)

### Jet Finding

- Non standard Jet Finder 'PTCLUS' used.
- Similar to LUCLUS
- Better for the resolved events than DURHAM style jet finders.
- Optimized so that b jets in direct and resolved are similar.
- Ask me at the end if you need a detailed description!

Note: "Jet 1" has mass nearest 5.0, "Jet 2" next nearest etc.

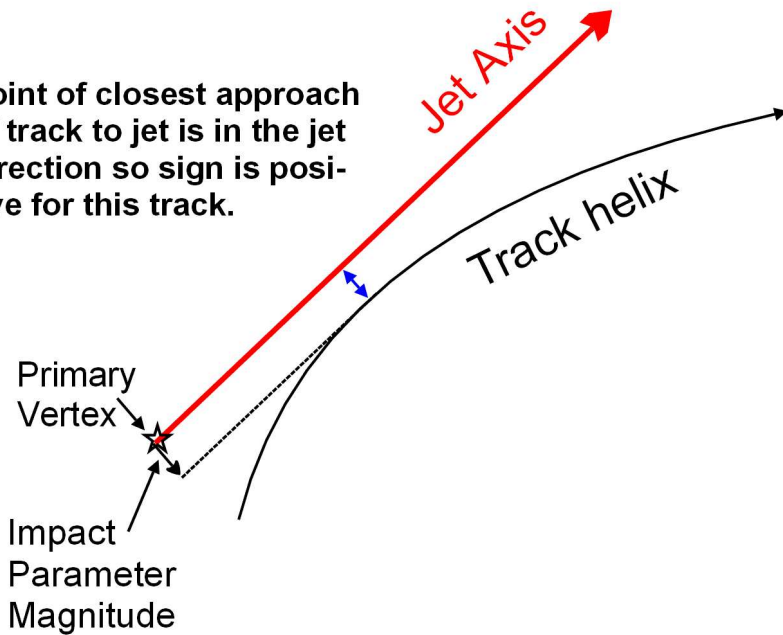
# Tools of the trade ... b tagging

Based on

## Signed Impact Parameter

Definition of Signed Impact Parameter

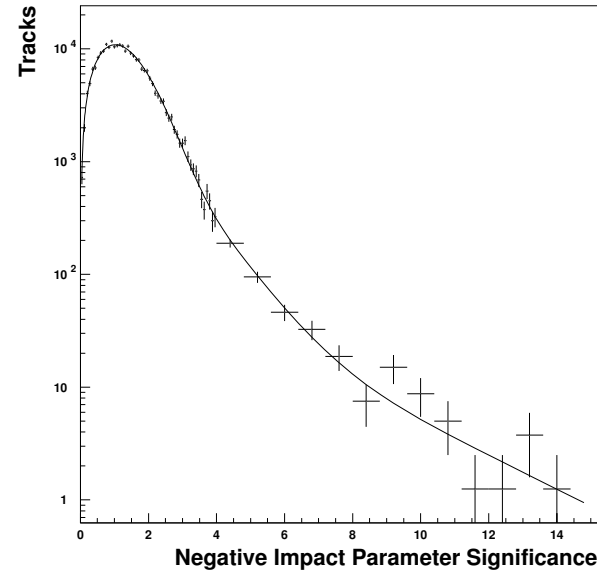
Point of closest approach of track to jet is in the jet direction so sign is positive for this track.



Calculate significance  $S$

$$S = \frac{\text{Impact parameter}}{\text{error}}$$

Fit negative  $S \Rightarrow$



Derive probability that track is from main vertex.

Combine probabilities to calculate:

$P_{\text{jet}}$  - probability that all tracks in jet came from main vertex

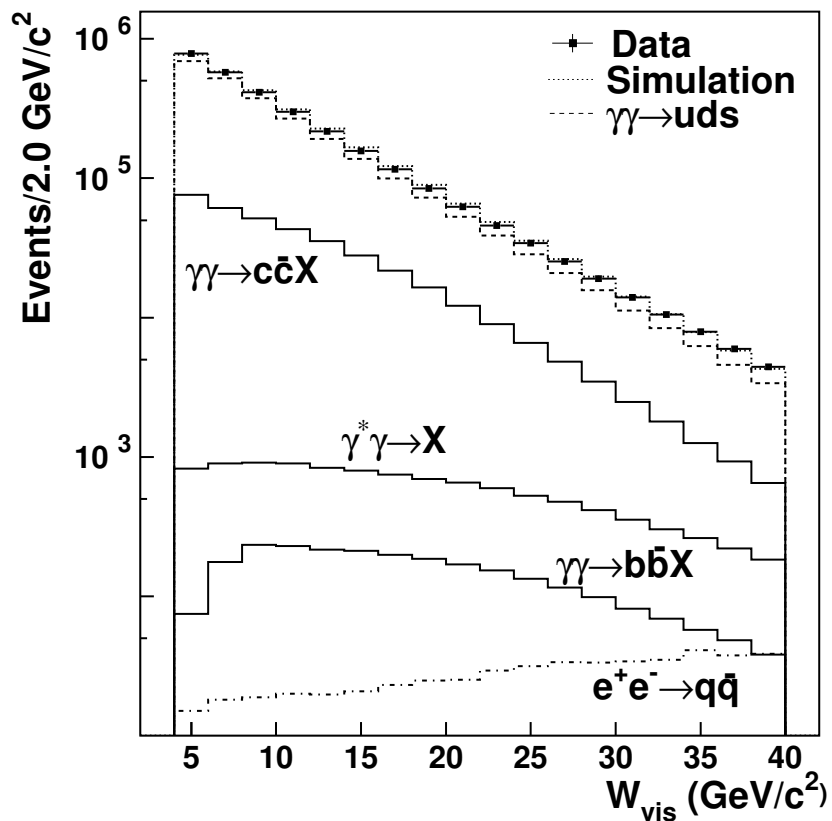
$P_{\text{event}}$  - likewise for all tracks in event

## Event Preselection

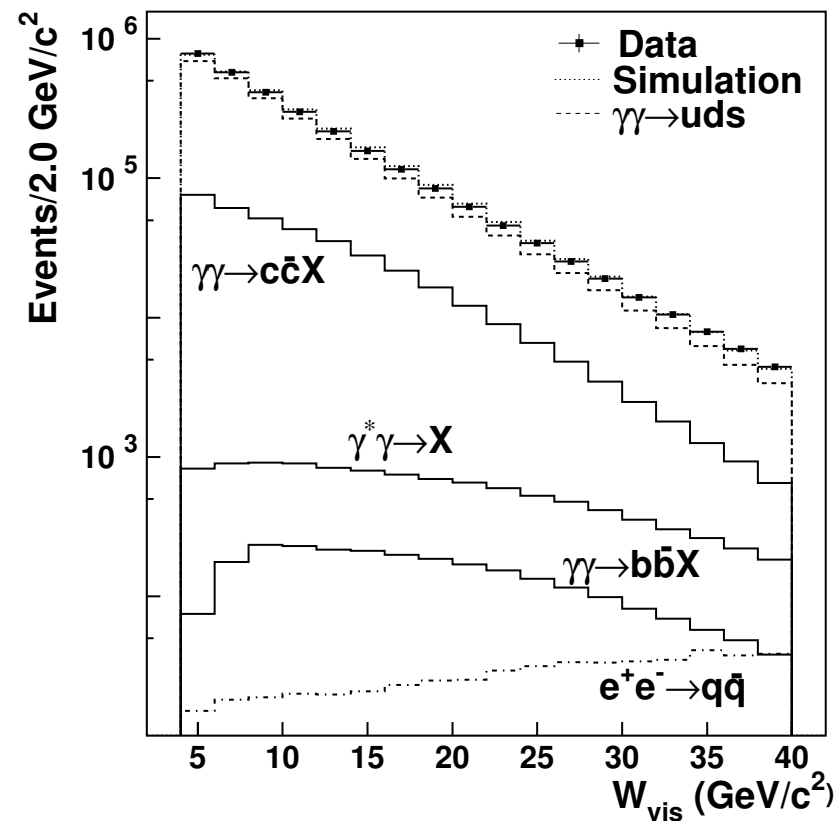
Select  $\gamma\gamma \rightarrow \text{hadrons}$ 

- $> 4$  charged tracks
- $4 < W_{vis} < 40 \text{ GeV}/c^2$
- Energy in luminosity calorimeters  $< 30 \text{ GeV}$
- $p_t$  of event  $< 6 \text{ GeV}/c$
- Thrust  $< 0.97$

ALEPH



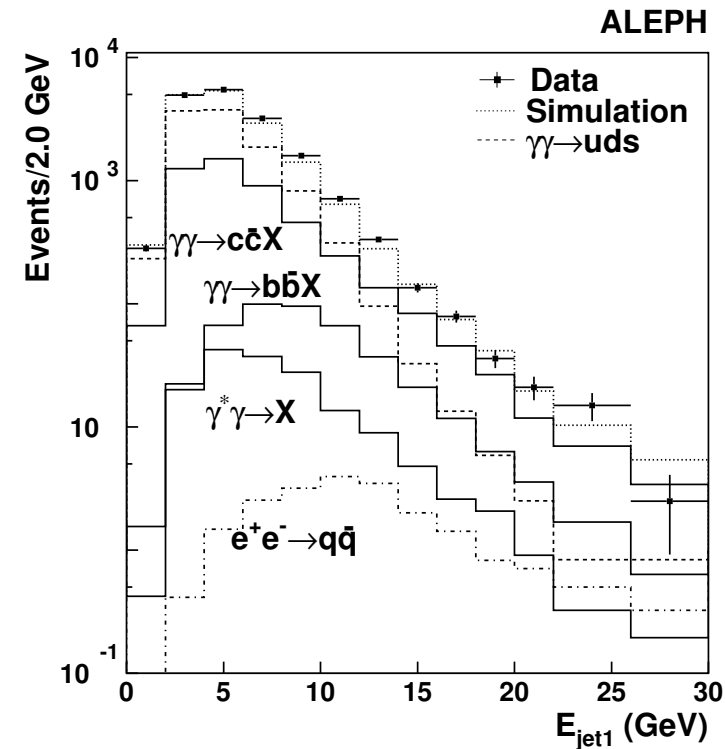
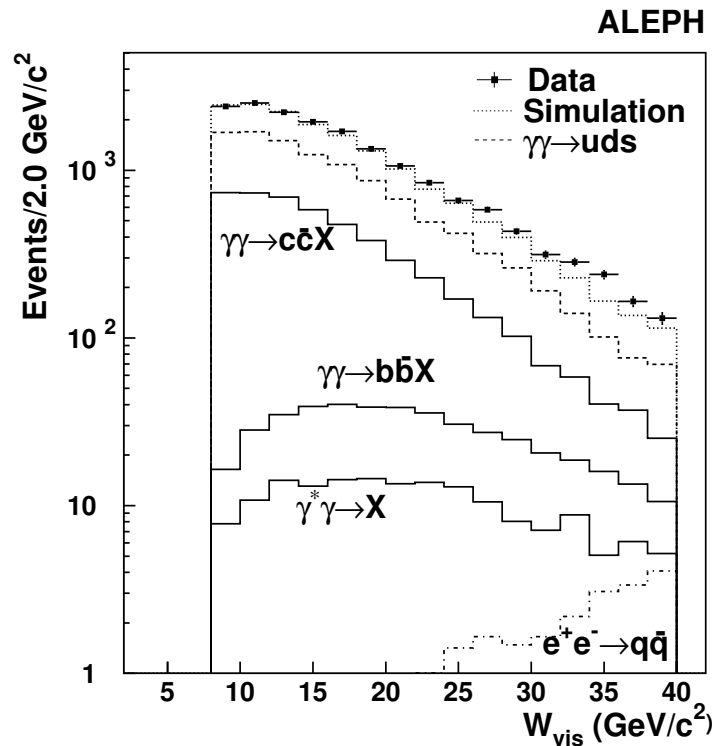
ALEPH



## Event Selection

Enhance  $\gamma\gamma \rightarrow b\bar{b}X$ 

- $> 6$  charged tracks
- $8 < W_{vis} < 40 \text{ GeV}/c^2$
- at least two jets
- $P_{\text{event}} < 0.05$
- the third largest impact parameter significance  $S > 0$
- the fourth largest impact parameter significance  $S > -10$





# Iterative Discriminant Analysis (Overview)

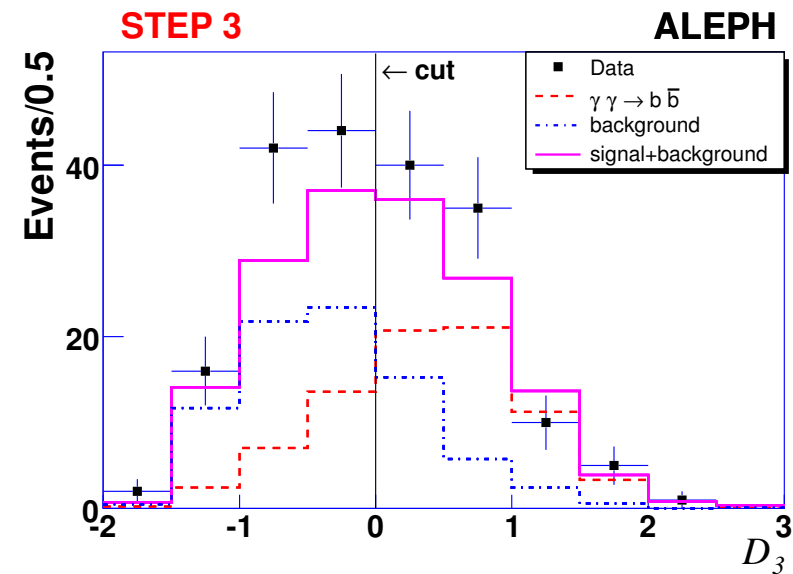
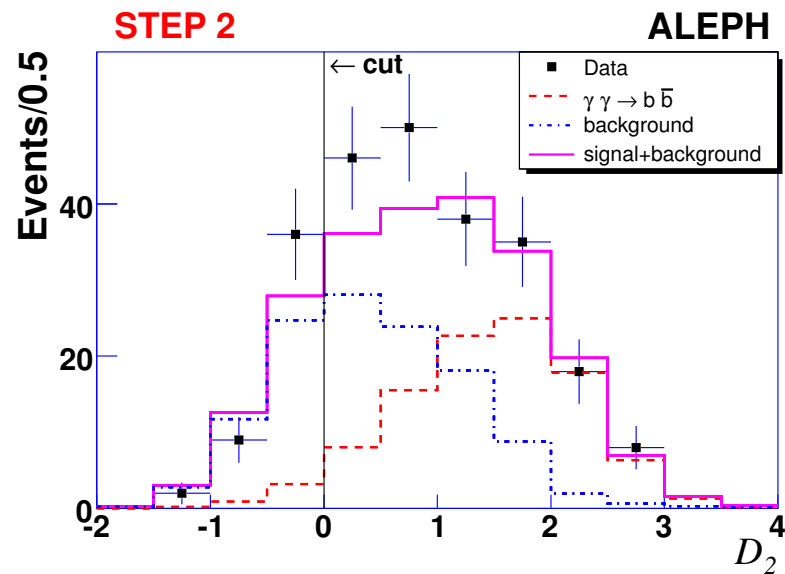
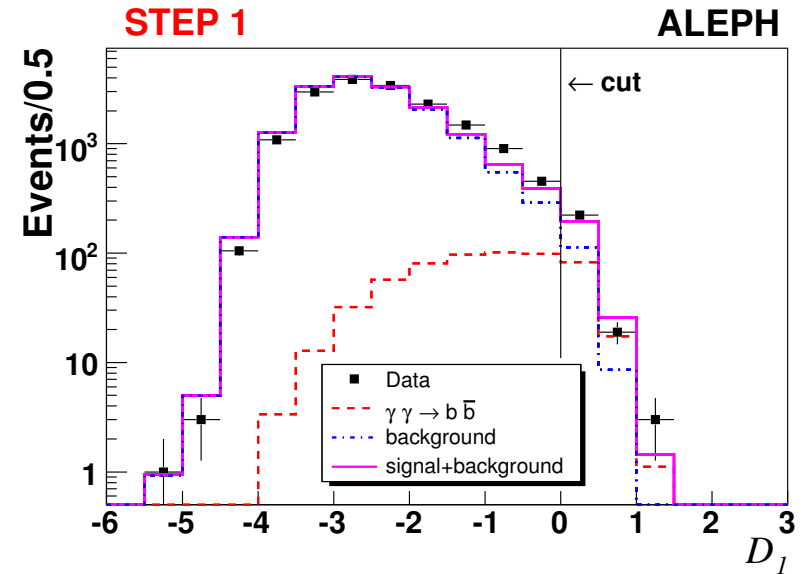
IDA, an event weighting method...

- **Input:**
  - variables which can distinguish signal / background.
- **Output:**
  - a single number -
    - high values are signal
    - low values are background.
- “Trained” on Monte Carlo.
- Extension of standard linear discrimination.
- Includes products of variables.
- Analytical method (just one matrix inversion).
- “Iterative” means
  - A selection may be applied and a new discriminant calculated for the remaining events
- Ask me at the end if you need a detailed description!

# IDA as used in this analysis

## IDA Input:

- $P_{\text{event}}, P_{\text{jet1}}, P_{\text{jet2}}$
- mass and  $p_t$  of Jet 1
- 5 largest  $S$
- the thrust of the event



# Efficiency Calculation

Efficiencies : 0.022 (direct), 0.016 (resolved)

To find mean efficiency - need to know how much Direct and how much Resolved.

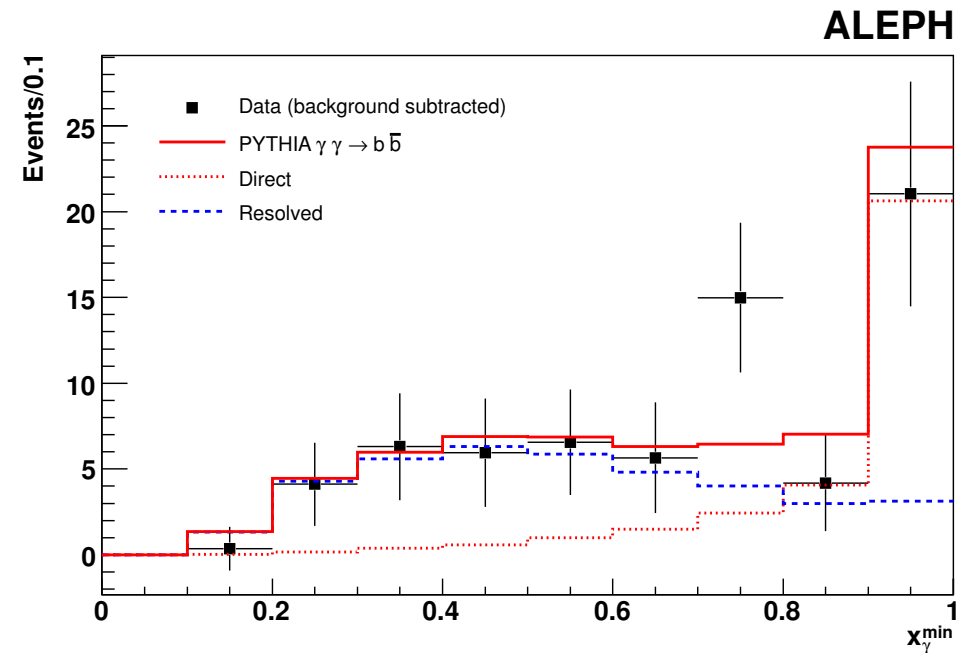
Fit to  $x_\gamma^{\min}$  to find out.

$$x_\gamma^{\min} = \min(x_\gamma^+, x_\gamma^-)$$

$$x_\gamma^\pm = \frac{\sum_{i=1,2} (E^i \pm p_z^i)}{(E^{\text{tot}} \pm p_z^{\text{tot}})}$$

$E^i, p_z^i$  are the energy and longitudinal momentum of jet  $i$   
 $E^{\text{tot}}$  and  $p_z^{\text{tot}}$  are the energy and longitudinal momentum of the whole event

Result: Mean Efficiency is  $0.0184 \pm 0.0009$



## Results and Systematic Uncertainties

Final selection of 93 events with a background of 24.2

$$\begin{aligned} 77\% & \quad \gamma^* \gamma \rightarrow c\bar{c}X \\ 17\% & \quad \gamma^* \gamma \rightarrow X \quad (Q^2 > 6) \\ 7\% & \quad e^+e^- \rightarrow q\bar{q} \end{aligned}$$

### Systematic Uncertainties

12% error on the background

from uncertainty on measured cross sections

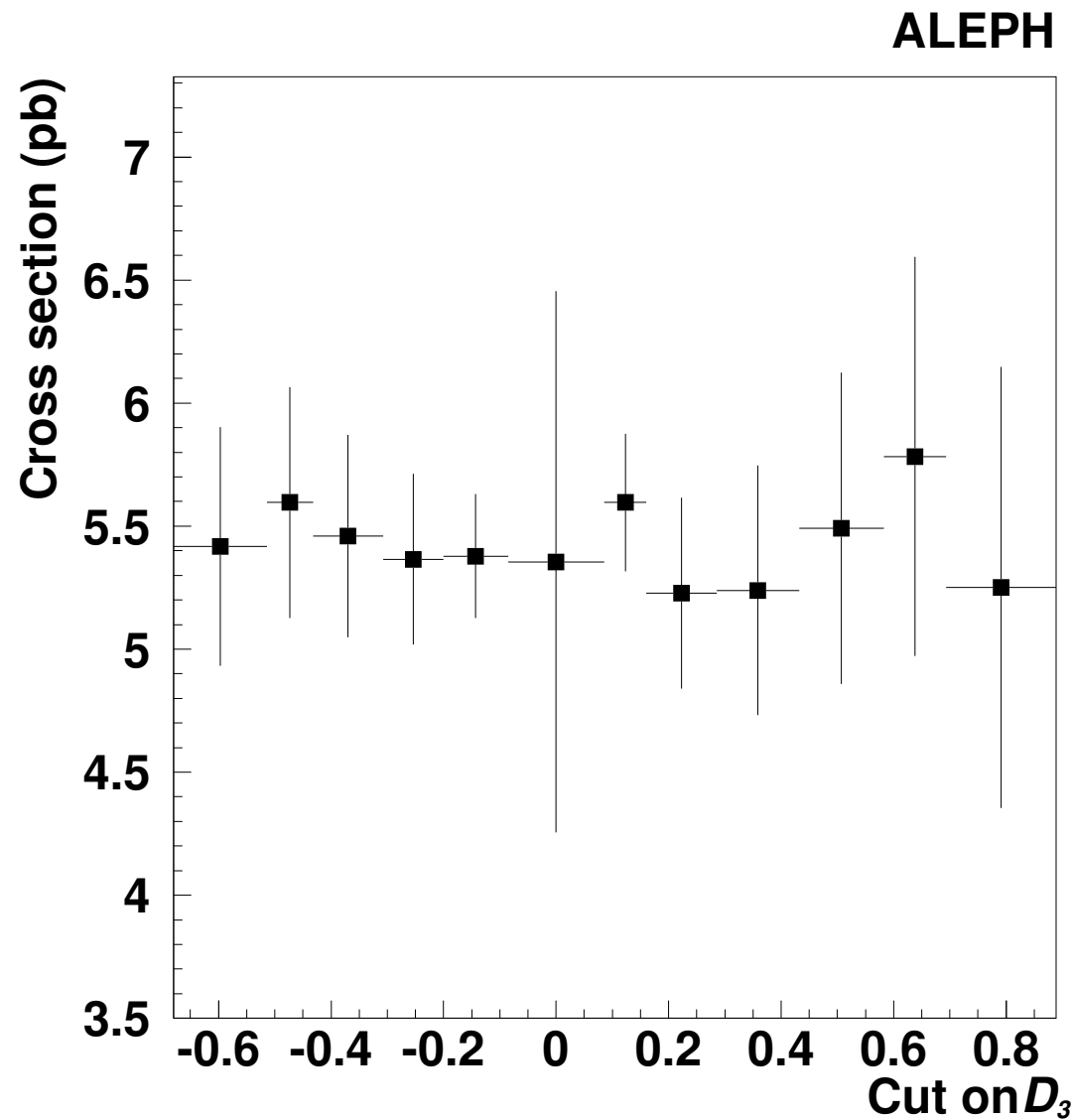
8.6% uncertainty on the efficiency

found by using HERWIG

11% difference due to  $W_{\text{vis}}$  dependence

by setting maximum  $W_{\text{vis}}$  cut 30 GeV/c<sup>2</sup>

# Stability Cross Check

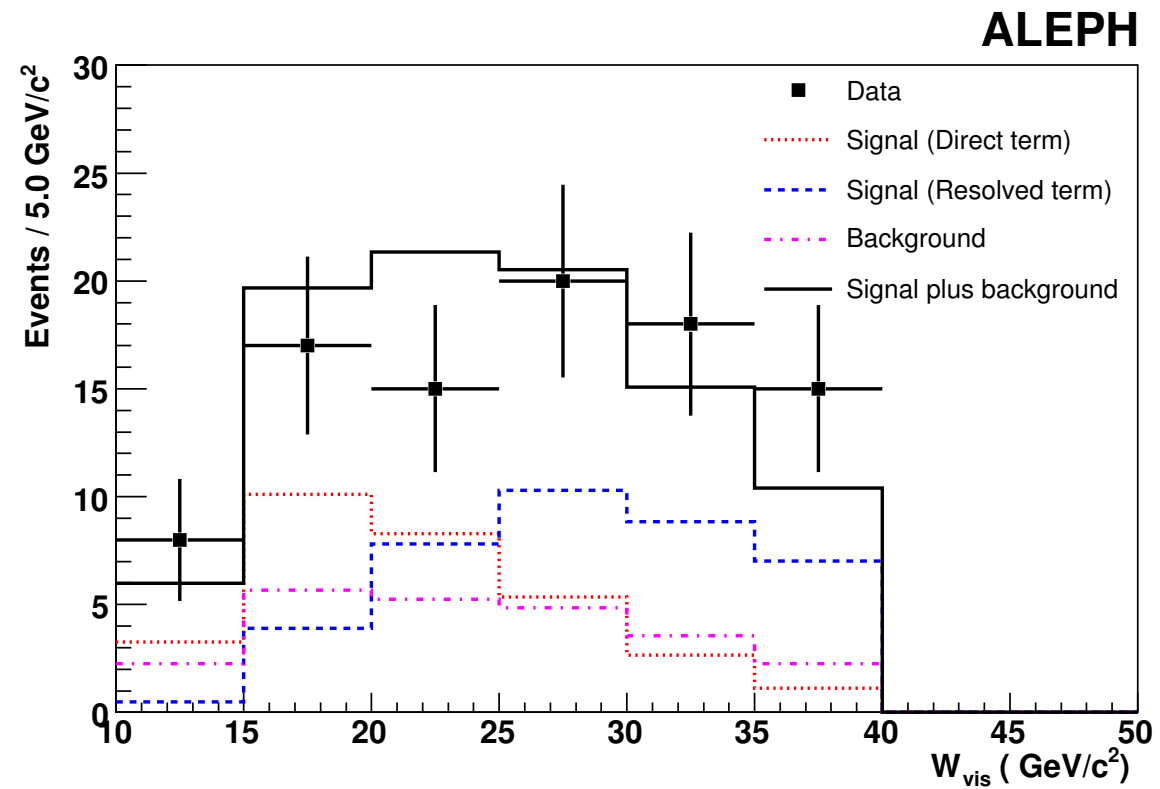


Vary final cut across a large range  
(From 143 to 33 selected events)

**Result is stable.**

$W_{\text{vis}}$  Cross Check

$W_{\text{vis}}$  not used in IDA  
Check of direct/resolved fit



# Lepton $p_t$ Cross Check

## Expect

$\sim 14 e^\pm$  &  $\sim 14 \mu^\pm$   
in 74  $b\bar{b}$  events.

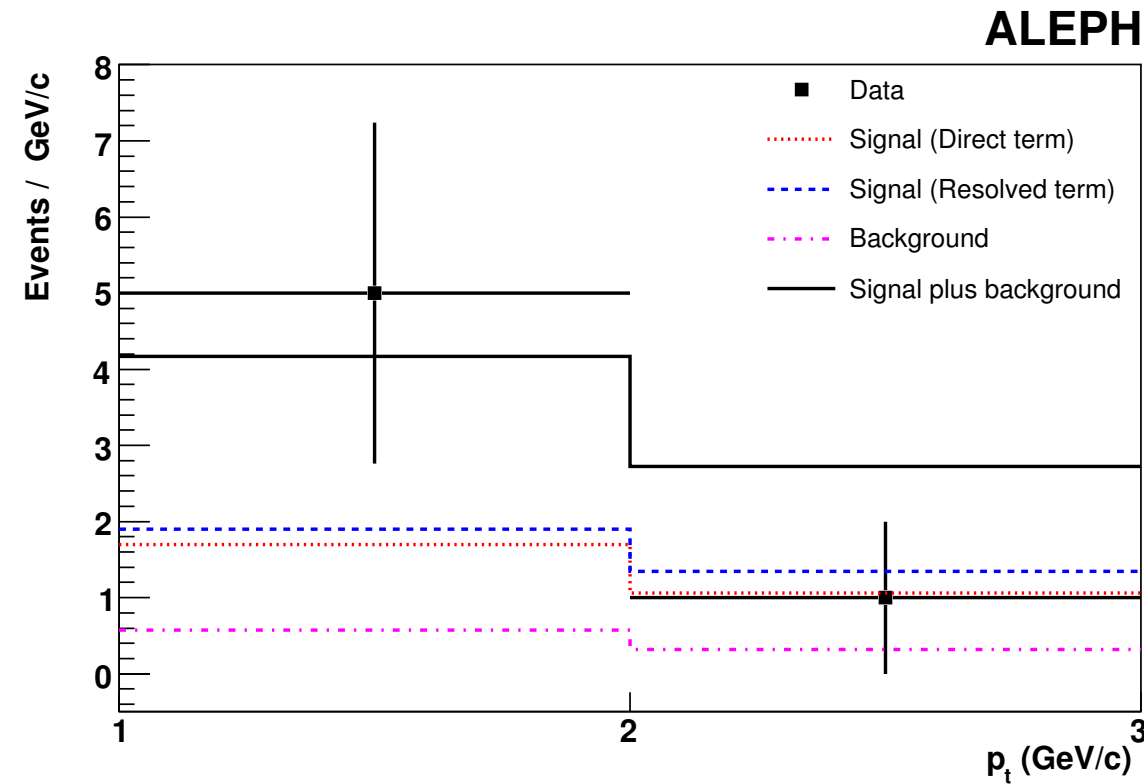
Large b quark mass

$\Rightarrow$  leptons have high  $p_t$  wrt jet.

After selection, expect :

6 leptons from signal  
+ 0.9 from background

See 6 leptons - **consistent.**



## Conclusions

The cross section for the process  $e^+e^- \rightarrow e^+e^-b\bar{b}X$   
has been measured to be

$$\sigma(e^+e^- \rightarrow e^+e^-b\bar{b}X) = (5.4 \pm 0.8_{\text{stat}} \pm 0.8_{\text{syst}}) \text{ pb}$$

which is consistent with the prediction of NLO QCD  
of between 2.1 and 4.5 pb

but barely consistent with the result quoted by the L3 Collaboration,  
( $12.8 \pm 1.7_{\text{stat}} \pm 2.3_{\text{syst}}$ ) pb.

For more details see: <http://arxiv.org/abs/0706.3150>



**PTCLUS**

- Start from most energetic Eflow object.
  - ⇒ Loop through objects in order of decreasing energy.
  - ⇒ If angle between object and jet  $< 90^\circ$   
and  $p_t$  with respect to  $p + p_{\text{jet}} < 0.5 \text{ GeV}/c$  then add object to jet.
  - ⇒ Otherwise object starts a new jet
  - ⇒ Repeat until all objects assigned.
- Close Jets are merged
  - Distance between jets  $Y = M^2/E_{\text{vis}}^2$   
 $M$  is the invariant mass of pair of jets, assumed to be massless,  
 $E_{\text{vis}}$  is the visible energy.
  - Pair with smallest  $Y$  is merged provided  
 $Y < 0.1$  and they are within  $90^\circ$
- Objects with larger  $p_t$  with respect to their jet than to another jet.
  - ⇒ reassign object to the other jet.
  - A maximum of five reassignments per merger.

The last two steps are repeated until no pair of jets has  $Y < 0.1$ .

## Iterative Discriminant Analysis (Detailed)

- For each event fill a vector  $y$  containing the  $n$  variables and  $(n^2 - n)/2$  products of those variables.
- Calculate the variance matrix  $V = V_s + V_b$ , where  $V_s$  is the variance matrix of the signal and  $V_b$  is the variance matrix of the background.  $V_s$  and  $V_b$  are weighted so that they have equal importance.
- Calculate  $\Delta\mu$ , the difference in the means of the signal and background, for each element of  $y$ .
- Invert the variance matrix  $V$  and multiply by  $\Delta\mu$ , to obtain the vector of coefficients  $a = V^{-1}\Delta\mu$ .
- For each event calculate  $D = y^T a y$ .

If necessary apply a selection to the events at some value of  $D$  and repeat the procedure as required. The IDA process does not prescribe how such a cut should be chosen, or how many iterations should be performed.

## Summary of the analysis in numbers

Sample	Cross section (pb)	Analysis stage					
		Presel	Selection	IDA 1	IDA 2	IDA 3	
$\gamma\gamma \rightarrow uds$	<b>16000</b>	<b>89</b>	<b>73</b>	<b>12</b>	<b>9</b>	<b>0</b>	per- cent of total events
$\gamma\gamma \rightarrow c\bar{c} X$	<b>930</b>	<b>10</b>	<b>25</b>	<b>40</b>	<b>35</b>	<b>23</b>	
$\gamma^*\gamma \rightarrow X$	<b>84</b>	<b>0</b>	<b>1</b>	<b>4</b>	<b>5</b>	<b>5</b>	
$e^+e^- \rightarrow q\bar{q}$	<b>83</b>	<b>0</b>	<b>0</b>	<b>2</b>	<b>2</b>	<b>2</b>	
$\gamma\gamma \rightarrow b\bar{b} X$	<b>4</b>	<b>0</b>	<b>1</b>	<b>41</b>	<b>50</b>	<b>70</b>	
<b>data</b>	-	<b>2696021</b>	<b>16810</b>	<b>244</b>	<b>197</b>	<b>93</b>	