

Photon and proton structure - overview

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- ❖ Warsaw to Paris
- ❖ Proton PDFs
- ❖ Photon PDFs
- ❖ Common ground – γp dijets
- ❖ Outlook



From Warsaw 2005 to Paris 2007

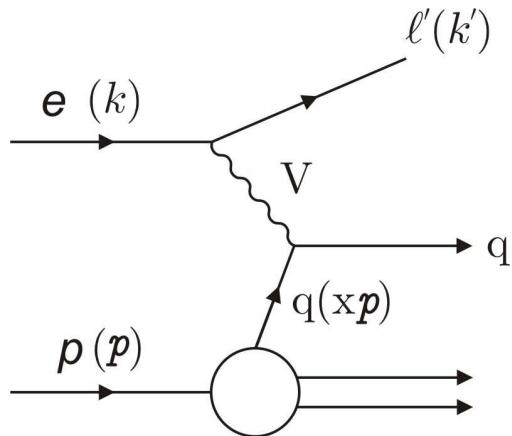
❖ Photon2005

- new photon PDFs (AFG04, CJK, SAL)
- ZEUS proton PDF fit (F_2 + jets)
- $F_2(\gamma)$ data from LEP2 (L3)
- data from HERA
 - CC DIS cross-sections with polarised $e^{+/-}$ beams
 - $F_2(cc)$ & $F_2(bb)$ (H1 using vertex detector impact parameters)
- NNLO splitting fcns for $F_2(\gamma)$ (Vogt et al)

❖ Photon2007

- further LEP2 measurements (leptonic SF from L3, $\gamma^*\gamma \rightarrow \bar{b}b$ ALEPH)
- data from Tevatron Run-II on proton PDF constraints
- 3 talks on polarised DIS from COMPASS (Stolarski, Reggiani, Schill)
- promise of complete HERA-II data-sets
- progress and challenges on theory questions

Deep Inelastic Scattering at HERA



Neutral Current

$$ep \rightarrow eX, \quad V = \gamma \text{ or } Z^0$$

Charged Current

$$ep \rightarrow \nu X, \quad V = W^\pm$$

Kinematics

$$\begin{aligned} Q^2 &= -(k - k')^2 & x &= \frac{Q^2}{2p \cdot q} & y &= \frac{p \cdot q}{p \cdot k} & q &= k - k' \\ s &= (k + p)^2 & Q^2 &= sxy & Y_\pm &= 1 \pm (1 - y)^2 \end{aligned}$$

$$\frac{d^2\sigma^{NC}(e^\pm p)}{dxdQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2^{NC}(x, Q^2) \mp Y_- x F_3^{NC}(x, Q^2) \right]^\dagger$$

$$\frac{d^2\sigma^{CC}(e^\pm p)}{dxdQ^2} = \frac{G_F^2}{4\pi x} \frac{M_W^4}{(Q^2 + M_W^2)^2} \left[Y_+ F_2^{CC}(x, Q^2) \mp Y_- x F_3^{CC}(x, Q^2) \right]^\dagger$$

$$F_2^{NC} \simeq \sum_i e_i^2 x(q_i + \bar{q}_i) \quad (\gamma \text{ only}); \quad F_2^{CC} = \sum_i x(q_i + \bar{q}_i); \quad x F_3^{CC} = \sum_i x(q_i - \bar{q}_i)$$

$q_i(x, Q^2)$ - momentum density of quark flavour i in proton

\dagger F_L has been ignored

Proton PDF Q^2 evolution

Parton densities evolve in Q^2 with homogeneous DGLAP eqns

$$\frac{\partial \Sigma}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} (\Sigma \otimes P_{qq} + g \otimes P_{qg})$$

$$\frac{\partial g}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} (\Sigma \otimes P_{gq} + g \otimes P_{gg})$$

$$\frac{\partial q_f^{NS}}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} q^{NS} \otimes P_{qq}$$

PDFs related to physical quantities by coefficient functions

$$\frac{F_2(x, Q^2)}{x} = \sum_f e_f^2 q_f \otimes C_f + \bar{e}^2 g \otimes C_g$$

various factorisation schemes, most popular now is $\overline{\text{MS}}$

• P_{ij} and C_i given by QCD, **now to NNLO**

• $x f(x, Q_0^2) = p_1 x^{p_2} (1-x)^{p_3} (1+p_4 x)$, typical PDF parameterisation at Q_0^2

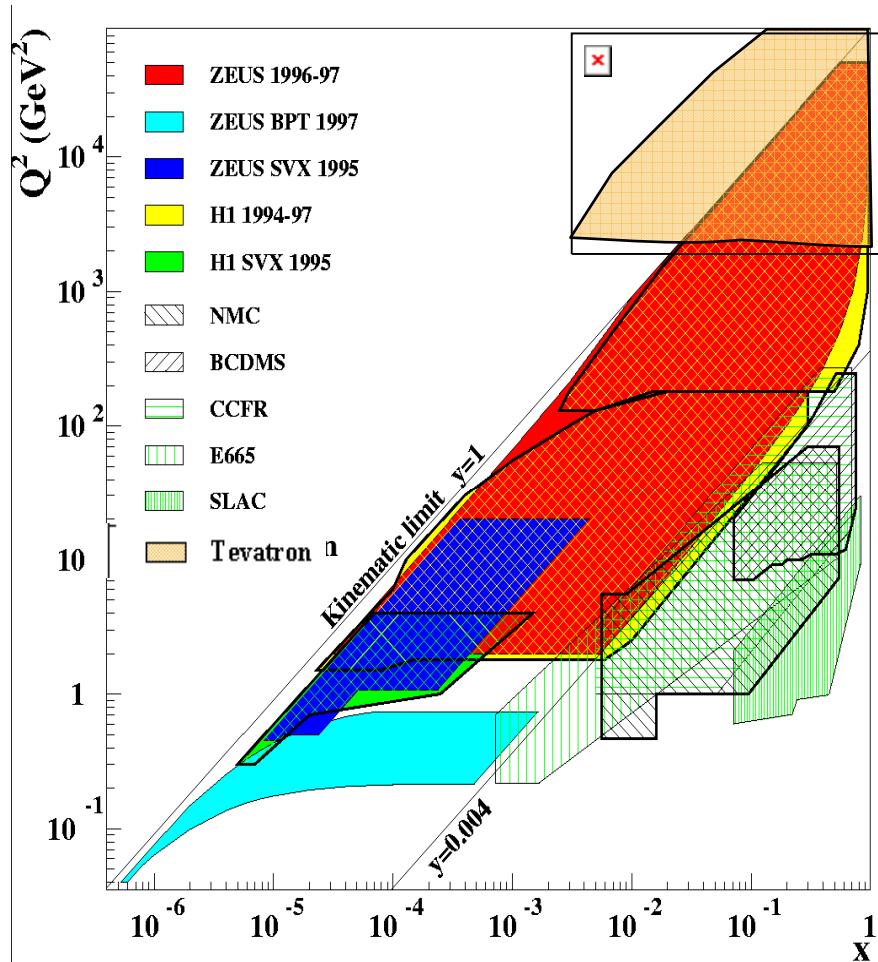
For a global fit, using sum-rule constraints, ~ 12 free parameters

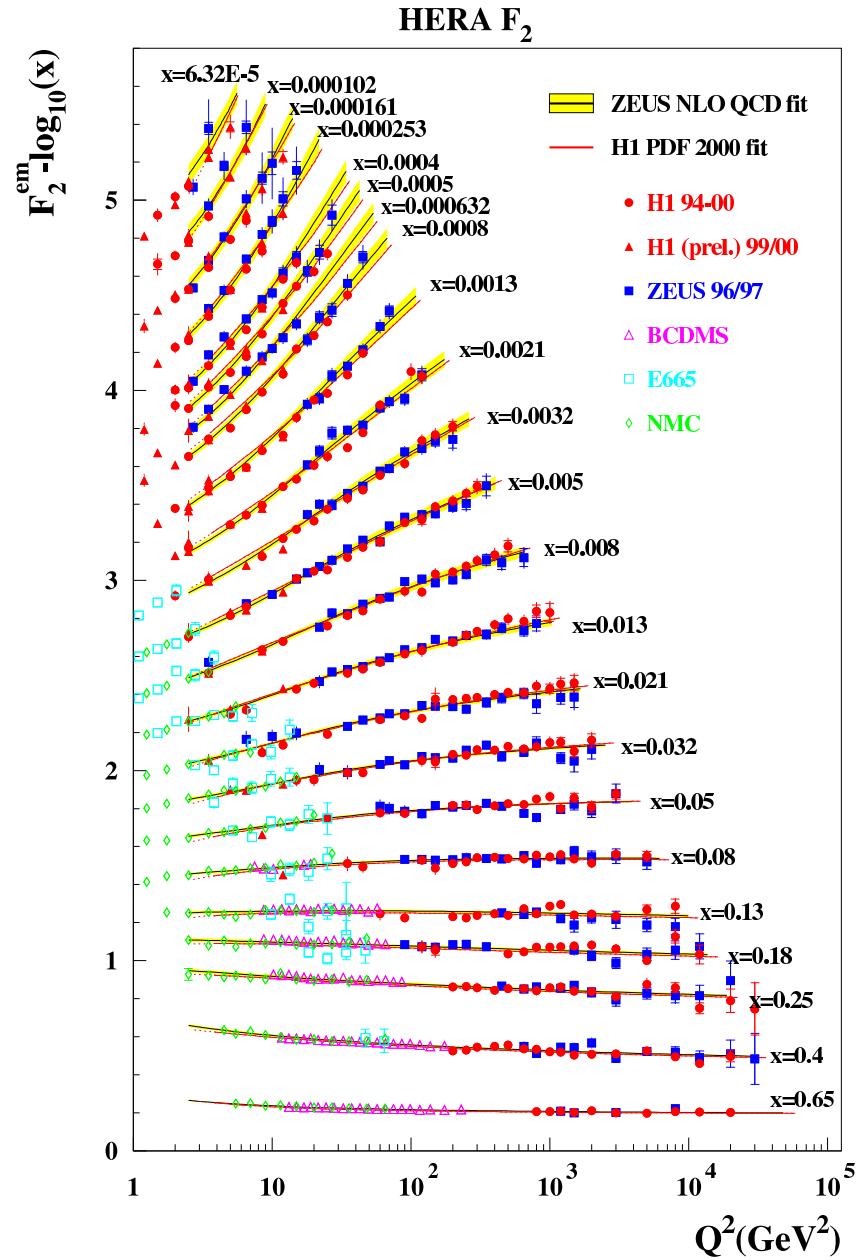
Data for proton structure

- deep inelastic scattering
 - fixed target
 - HERA
- jets ($e p$, γp , $\bar{p} p$)
- $\bar{p} p \rightarrow W^\pm X, Z^0 X$
 - leptonic decay asymmetries
- heavy flavour
 - $e p \rightarrow e Q\bar{Q}X$ (γ -g fusion)

Talks by
Kupco – Tevatron jets
Lancaster – W, Z

Perez
Overview of proton PDFs





F_2^p data

HERA
 E_e 27.5, E_p 920 (820) GeV

Physics luminosity:

HERA-I (1992 – 2000)
~ 140 pb⁻¹ (mainly e⁺p)

HERA-II (2003 – 2007)
~ 400 pb⁻¹ (e⁺/⁻, P⁺/⁻)
21 pb⁻¹ (E_p 460, 575 GeV)

(2005 only 140 pb⁻¹)

← now probing large x and Q^2

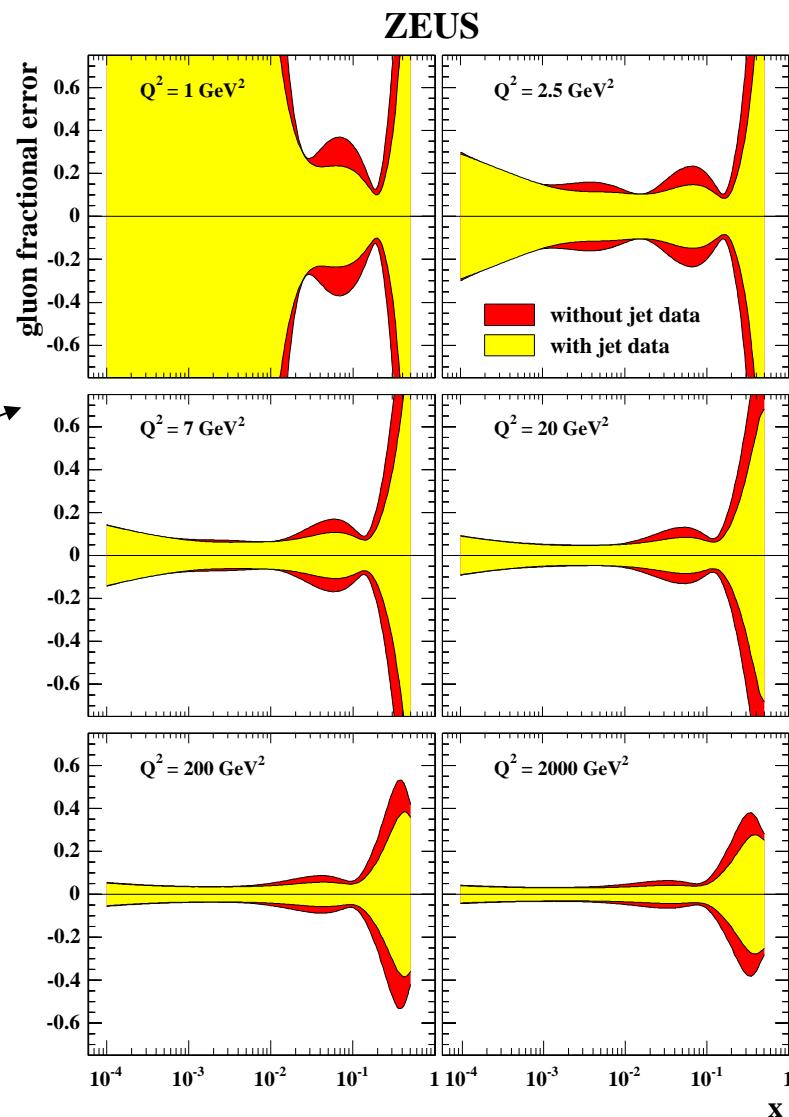
getting at the glue in the proton - g^p

- Scaling violations $\frac{\partial F_2}{\partial \ln Q^2} \sim x g$

particularly at low x

- jet data ($e p$, γp , $p\bar{p}$)
 - example from ZEUS-jets fit constraint at larger x

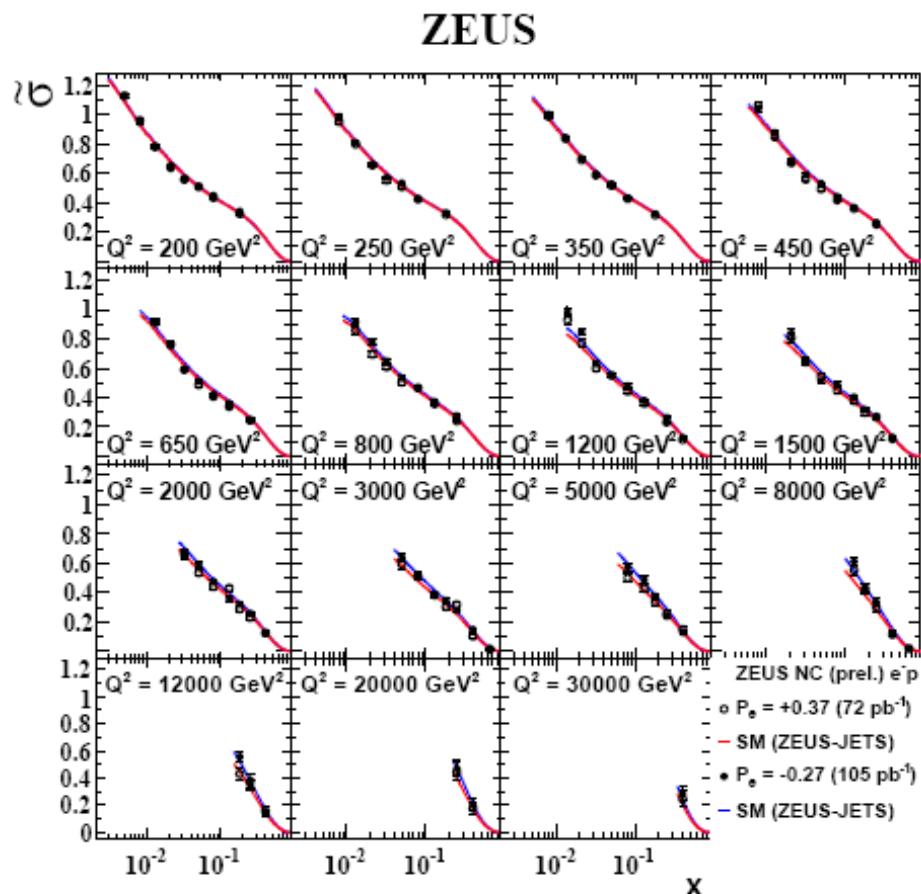
- heavy flavour production (?)



New data from HERA-II

- ❖ Quick look at
 - high Q^2 NC cross-sections
 - high y cross-sections
 - charm production

Reduced cross section for polarised electrons



$$\tilde{\sigma}^\pm = F_2(x, Q^2) \mp \frac{Y_-}{Y_+} \cdot x F_3(x, Q^2)$$

$$F_2(x, Q^2) = F_2^\gamma + P_e a_e \chi_Z F_2^{\gamma Z}$$

$$P^- (L) > P^+ (R) \quad (a_e = -0.5)$$

Measured cross sections are in good agreement with SM predictions over whole kinematic region

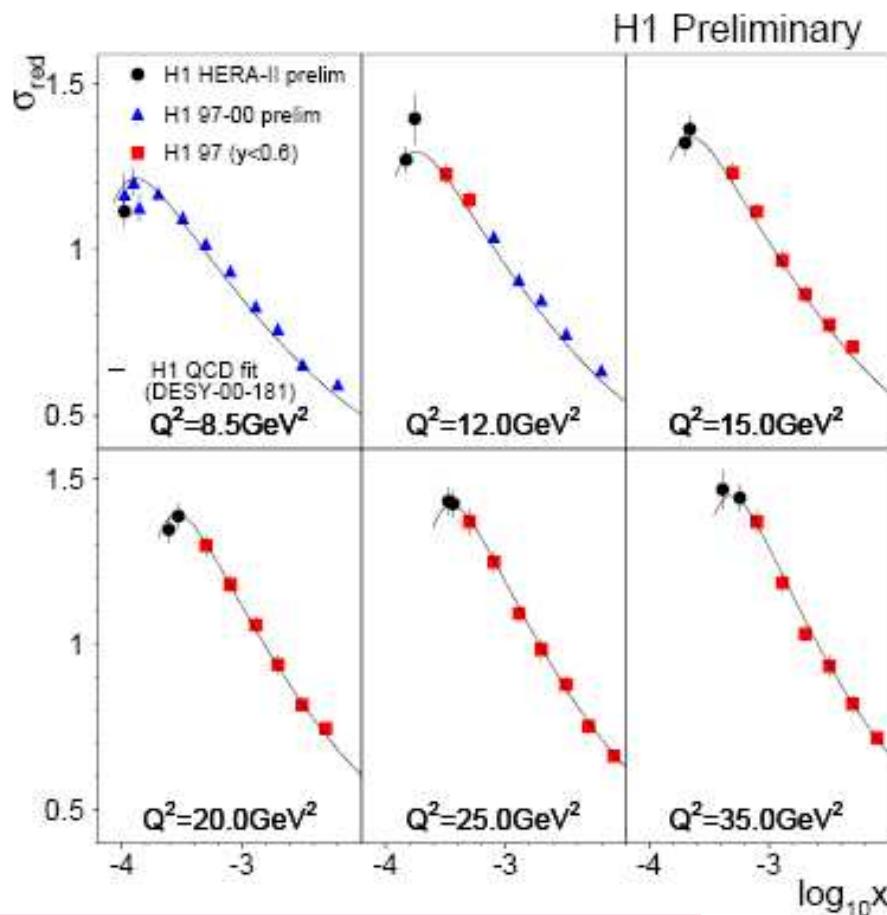
$e^- (R) \sim 71.8 \text{ pb}^{-1}$ @ $P_e \sim +29.7 \%$
 $e^- (L) \sim 105.4 \text{ pb}^{-1}$ @ $P_e \sim -27.0 \%$

details in talk by Petrukin

Sampa Bhadra, DIS2007

ZEUS Preliminary

H1 – σ_r at high y



N. Raicevic

DIS 2007, 16-20 April, 2007

$$\sigma_r = F_2 - \frac{y^2}{Y_+} F_L$$

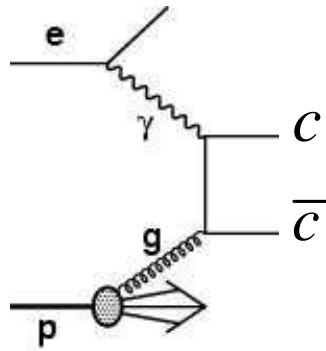
- HERA-II data points based on 96pb^{-1}

$$Q^2 = sxy$$

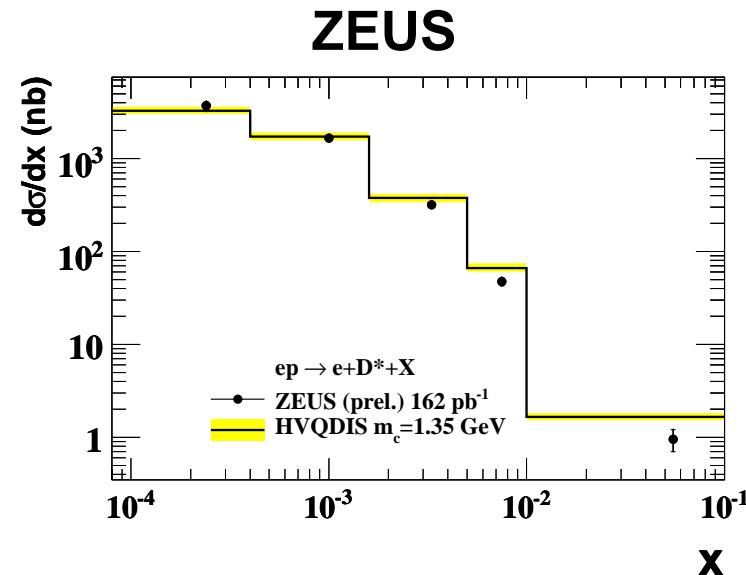
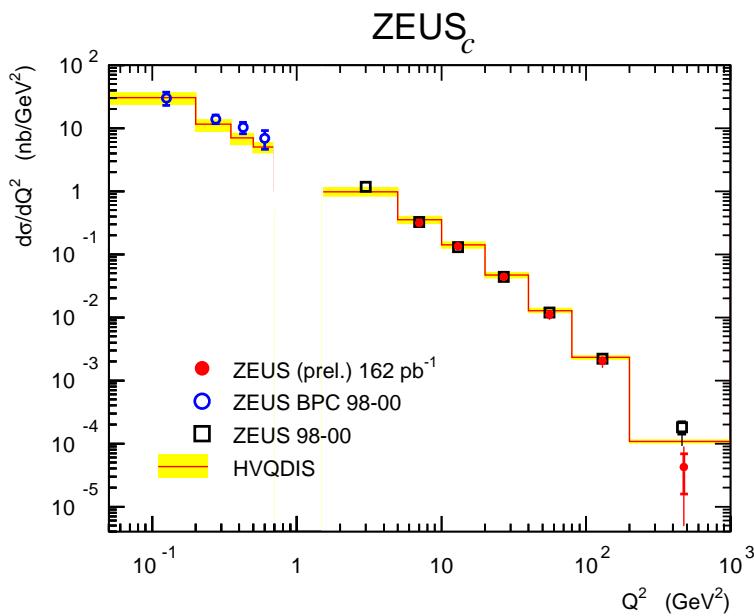
so, for fixed s and Q^2
high $y \leftrightarrow$ low x

'Warm up' for F_L

g^p from charm production in DIS



- dominant process is photon-gluon fusion
- NLO calculation for cross-sections – HVQDIS
- HERA data not yet used directly in PDF determination but agreement using HERA gluons is good
- HVQDIS requires FFNS – work needs to be done to reconcile this with high Q^2 ZM-VFNS

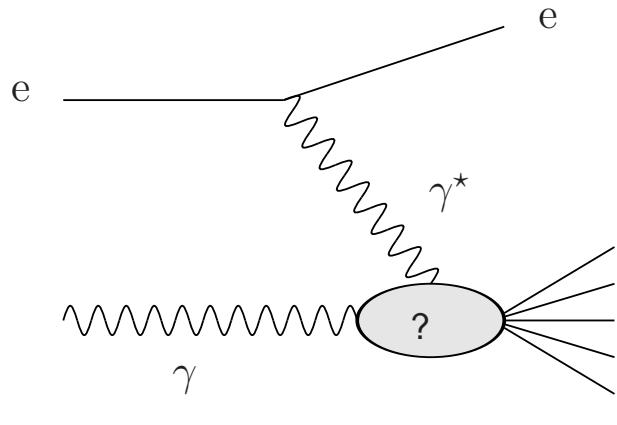


see also talk by Boenig

Summary on proton PDFs

- ❖ Principal players are:
 - H1, ZEUS, CTEQ, MSTW (MRST), Alekhin
- ❖ Sophisticated methods for handling experimental uncertainties
- ❖ Still a lot of HERA-II data to come (high x and Q^2)
- ❖ Combined QCD-EW fits ([talk by Stella](#))
- ❖ Work on combining the H1 and ZEUS data (F_2 and other data) is underway – smaller overall errors and the definitive HERA PDFs
 - (some early ideas in the HERA-LHC workshop)
- ❖ More high precision data from the Tevatron to come
- ❖ NNLO for the inclusive processes already in use
- ❖ More work to be done on including more jet data and charm(?) to help constrain the gluon (and on NNLO calculations)
- ❖ For details, [Emmanuelle Perez](#) later in this session

$\gamma^*\gamma$ to X -- DIS on a photon target



Similar variables to proton DIS -
 x, y, Q^2 - but more difficult to measure

$$Q^2 = 2E_{beam}E_{tag}(1 - \cos\theta_{tag})$$

$$x = \frac{Q^2}{Q^2 + W^2}, \quad W^2 = \left(\sum_i p_i^{hads} \right)^2$$

$$y = 1 - \frac{E_{tag}}{E_{beam}} \cos^2 \left(\frac{\theta}{2} \right)$$

$$\frac{d^3\sigma}{dxdydz} = \frac{2\pi\alpha^2}{Q^4 x} \left[Y_+ F_2^\gamma(x, Q^2) - y^2 F_L^\gamma(x, Q^2) \right] \Phi_\gamma(x, y)$$

Φ_γ is the flux of photons radiated by the untagged beam electron

since $y \ll 1$, the contribution of F_L^γ is neglected

photon PDF Q^2 evolution

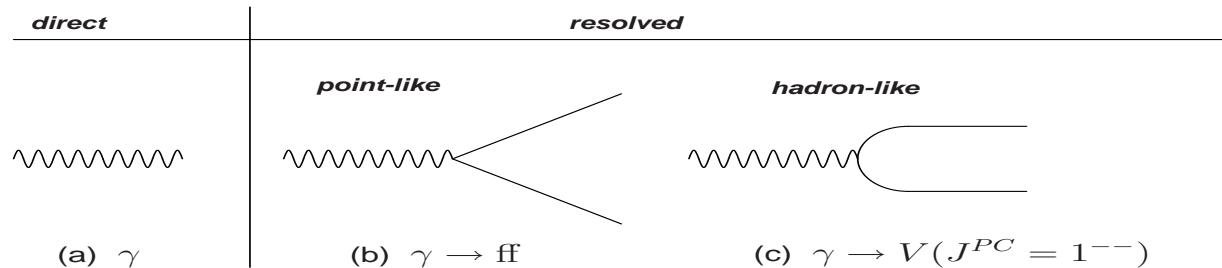


diagram
from
Nisius
Phys. Rep.

Parton densities evolve in Q^2 with **inhomogeneous** DGLAP eqns

$$\frac{\partial \Sigma^\gamma}{\partial \ln Q^2} = \mathbf{k}_q + \frac{\alpha_s}{2\pi} (\Sigma^\gamma \otimes P_{qq} + g^\gamma \otimes P_{qg})$$

$$\frac{\partial g^\gamma}{\partial \ln Q^2} = \mathbf{k}_g + \frac{\alpha_s}{2\pi} (\Sigma^\gamma \otimes P_{gq} + g^\gamma \otimes P_{gg})$$

$$\frac{\partial q_f^{NS}}{\partial \ln Q^2} = \sigma_f^{NS} \mathbf{k}_q + \frac{\alpha_s}{2\pi} q^{NS} \otimes P_{qq}, \quad \sigma_f^{NS} = (e_f^2 - 1)/n_f$$

P_{ij} and k_i calculated from QCD & QED - P_{ij} to NNLO (Vogt et al 2005)

Sasaki this
session

photon PDFs

- PDFs related to physical quantities by coefficient functions

$$\frac{F_2^\gamma(x, Q^2)}{x} = \sum_f e_f^2 q_f \otimes C_f + \bar{e}^2 g^\gamma \otimes C_g + C_\gamma \quad (C_\gamma \text{ is the direct photon term})$$

various factorisation schemes, $\overline{\text{MS}}$ and DIS_γ

- PDFs parameterised using a 'valence like' functional form

$$xf^\gamma(x, Q_0^2) \sim x^a(1-x)^b \quad (a, b \text{ are fit parameters})$$

using VMD connection $f^\gamma = \kappa \frac{4\pi\alpha}{f_\rho^2} f^\pi$, with κ determined from the fit

- Number of free parameters in 'global photon' fit in range 2 - 6
far fewer than for proton, but then much less data

Data for photon structure

- inclusive $e^+e^- \rightarrow e^+e^- X$
 - $\gamma^*\gamma \rightarrow X$
 - PETRA, TRISTAN, LEP
- jets $\gamma p \rightarrow jjX$ (HERA)
- Other possibilities
 - $\gamma^*\gamma \rightarrow jjX$ (LEP)
 - $\gamma^*\gamma \rightarrow \gamma jX$ (LEP)
 - $\gamma^*\gamma \rightarrow Q\bar{Q}X$ (LEP)
 - $\gamma p \rightarrow \gamma jX$ (HERA)
 - $\gamma p \rightarrow c\bar{c}X$ (HERA)
- Note that access to small x_γ is limited

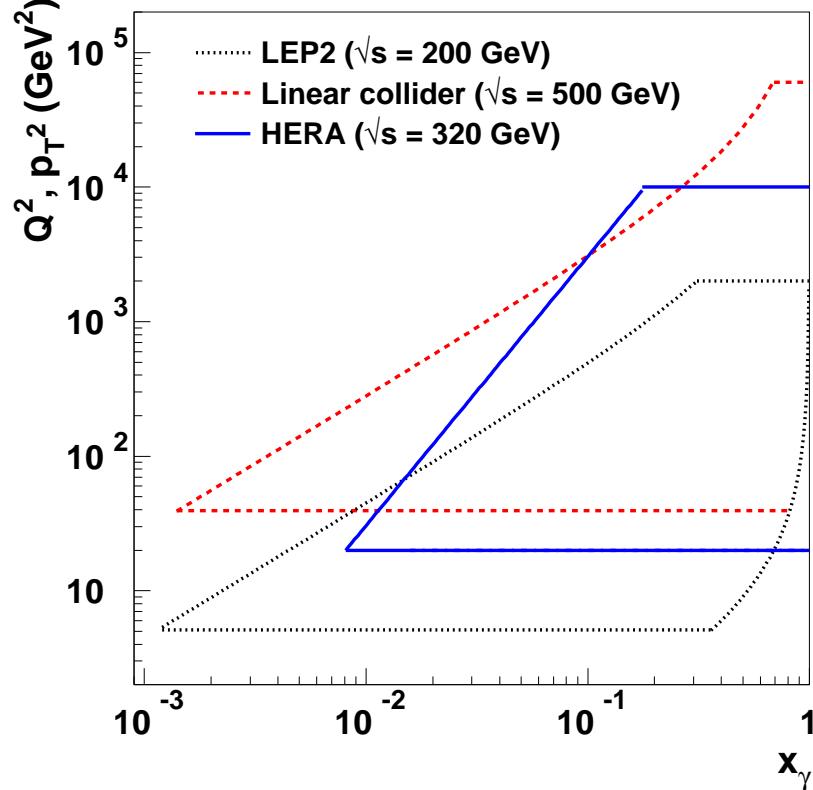
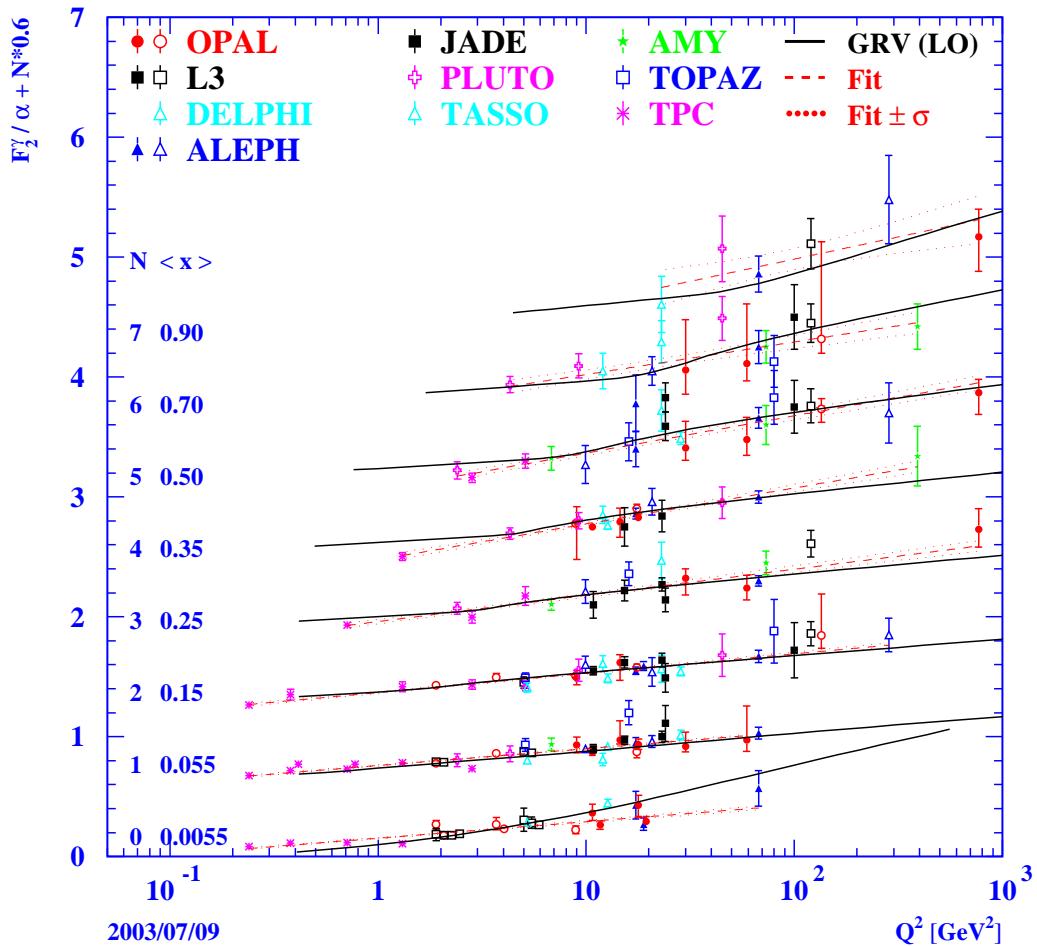


diagram from Butterworth & Wing, Rep. Prog. Phys.

F_2^γ data



Difficult !

Compare $F_2(p)$ on p6:

- lower precision

- smaller range in $\ln Q^2$

but

Provides the dominant input for photon PDF determination

figure from Nisius, Phys. Rep.

R Devenish Photon2007

Photon PDFs

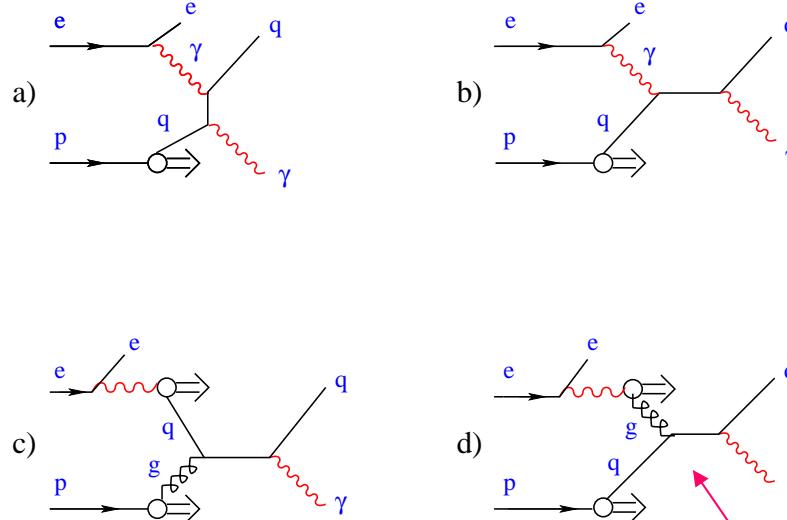
- ❖ New at time of PHOTON2005
 - almost all LEP data and improved heavy flavour treatments
- ❖ AFG04 (update of AFG-HO 1994) Aureneche, Fontannaz, Guillet
 - $F_2(\gamma)$ data from PETRA, TRISTAN and LEP
- ❖ CJK04 Cornet, Jankowski, Krawczyk
 - $F_2(\gamma)$ data from PETRA, TRISTAN and LEP
 - checks on compatibility of LEP data
 - different gluon
- ❖ SAL – perhaps the most ambitious Slominski, Abramowicz, Levy
 - $F_2(\gamma)$ data from PETRA, TRISTAN and LEP
 - HERA dijet photoproduction, and low x $F_2(\gamma)$ from Gribov factorisation
- ❖ Older GRV-HO (1992) and AFG-HO, still in use
 - did not use LEP data

Other processes for photon PDFs

- ❖ Other processes with jets and/or hard FS photons
 - $\gamma p \rightarrow \gamma jX$ (perhaps for the future)
 - $\gamma p \rightarrow jjX$ (more on this - again)
 - talk by Grindhammer on HERA processes
- ❖ getting at the photon glue
 - $F_2(\gamma)$ scaling violations – lack of data at low x and small $\ln Q^2$ range
 - also masked by scaling violation of pointlike $\gamma \rightarrow q\bar{q}$ term
 - $\gamma^* \gamma \rightarrow \bar{b}b$ (LEP) talk by Finch (generated a lot of discussion!)
 - also reference in his talk to LEP $\gamma^* \gamma \rightarrow \bar{c}c$ (experiments agree with each other and with NLO calculation) – sensitivity to photon PDF
 - probably masked by uncertainty in charm mass.

γp to $\gamma j X$ - H1

HERA-I 109 pb^{-1}



NLO calculations:

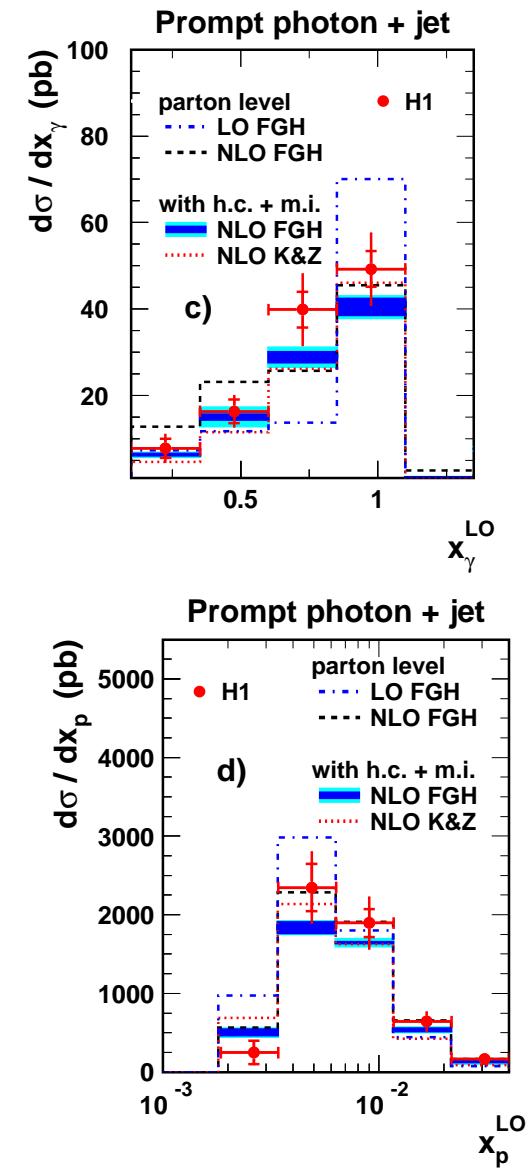
FGH – Fontannaz, Guillet, Heinrich

K&Z – Krawczyk & Zembrzuski

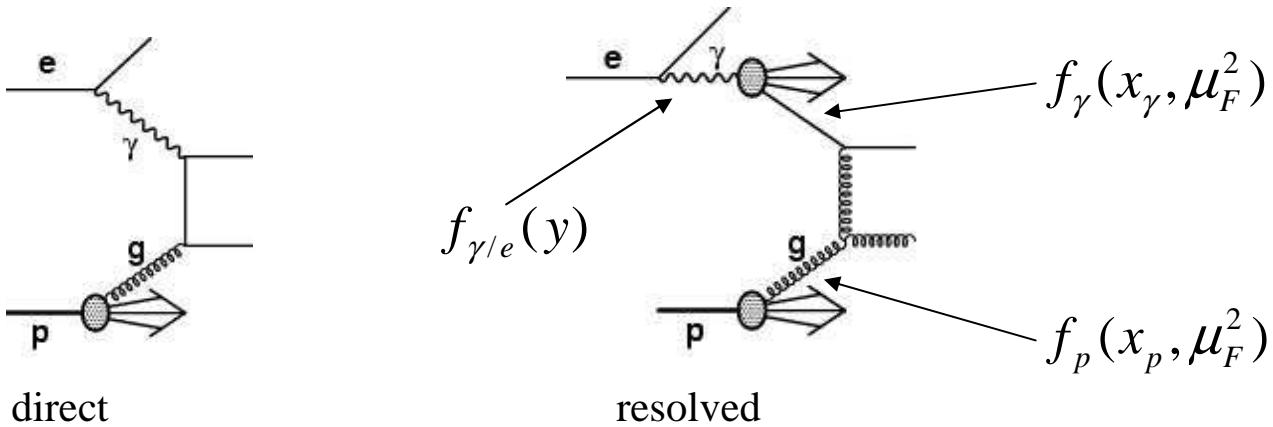
AFG-HO photon, MRST2 proton PDFs

in principle sensitivity to resolved γ

similar measurements by ZEUS (talk by Brownson)



γp to jjX – important for both p & γ PDFs



hard scale provided by $E_T^{jet} > 20$ GeV

$$d\sigma_{ep}(\text{resolved}) = \int dy f_{\gamma/e}(y) \int dx_p dx_\gamma f_p(x_p, \mu_F^2) f_\gamma(x_\gamma, \mu_F^2) d\hat{\sigma}_{ab}(x_p, x_\gamma, \mu_R^2)$$

with LO estimators for x_γ and x_p :

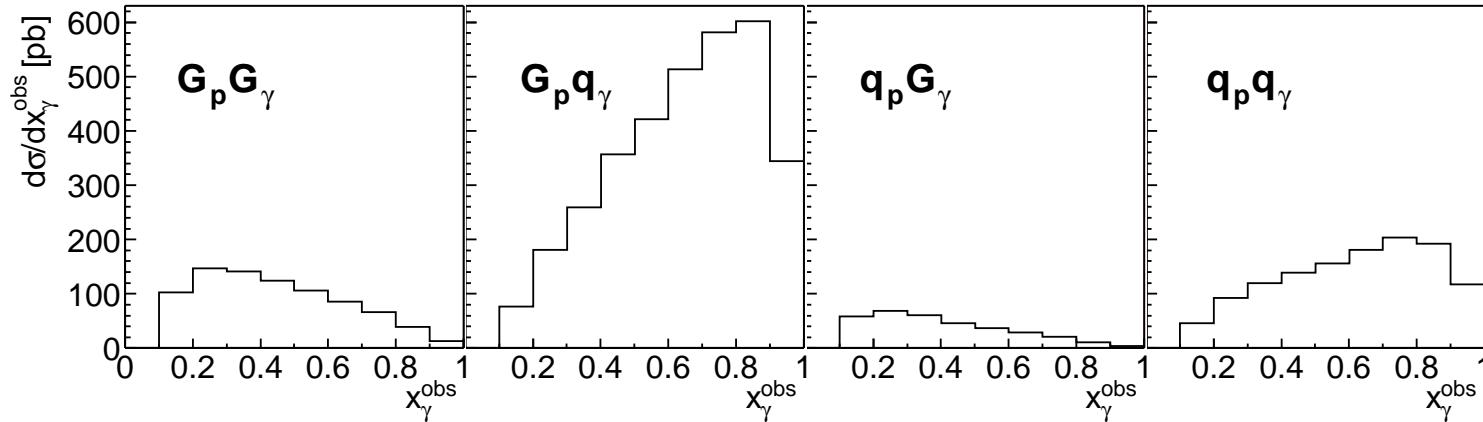
$$x_{\gamma}^{obs} = \frac{E_T^{j1} e^{-\eta^{j1}} + E_T^{j2} e^{-\eta^{j2}}}{2yE_e}; \quad x_p^{obs} = \frac{E_T^{j1} e^{\eta^{j1}} + E_T^{j2} e^{\eta^{j2}}}{2E_p}$$

$x_\gamma^{obs} > 0.75$ 'direct enriched', $x_\gamma^{obs} < 0.75$ 'resolved enriched'

proton PDFs

photon PDFs

Sensitivity to PDFS

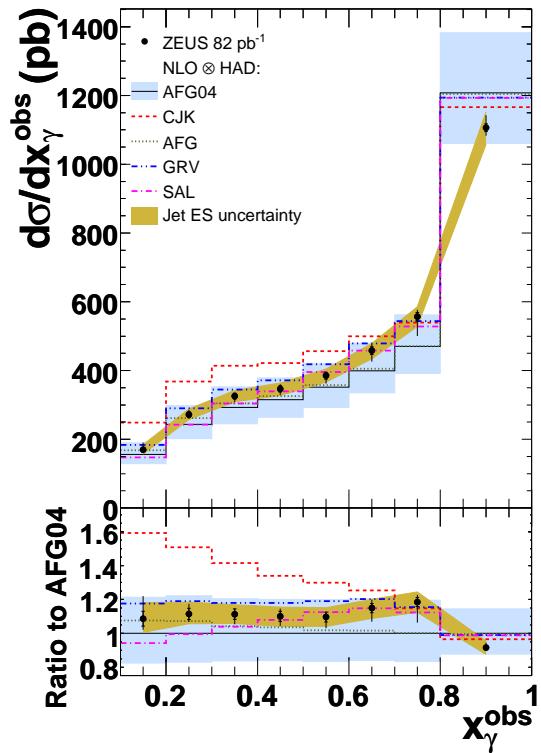


❖ From SAL

- contribution to cross-section as function of x_γ^{obs}
- Frixione-Ridolfi NLO code, CTEQ5M proton PDFs & SAL photon PDFs
- E_T in the range 14 – 17 GeV
- shows sensitivity to combinations of proton and photon PDFs
- notice the dominance of G_p (g^p)

γp to jjX (ZEUS & H1- details in talk by Bussey)

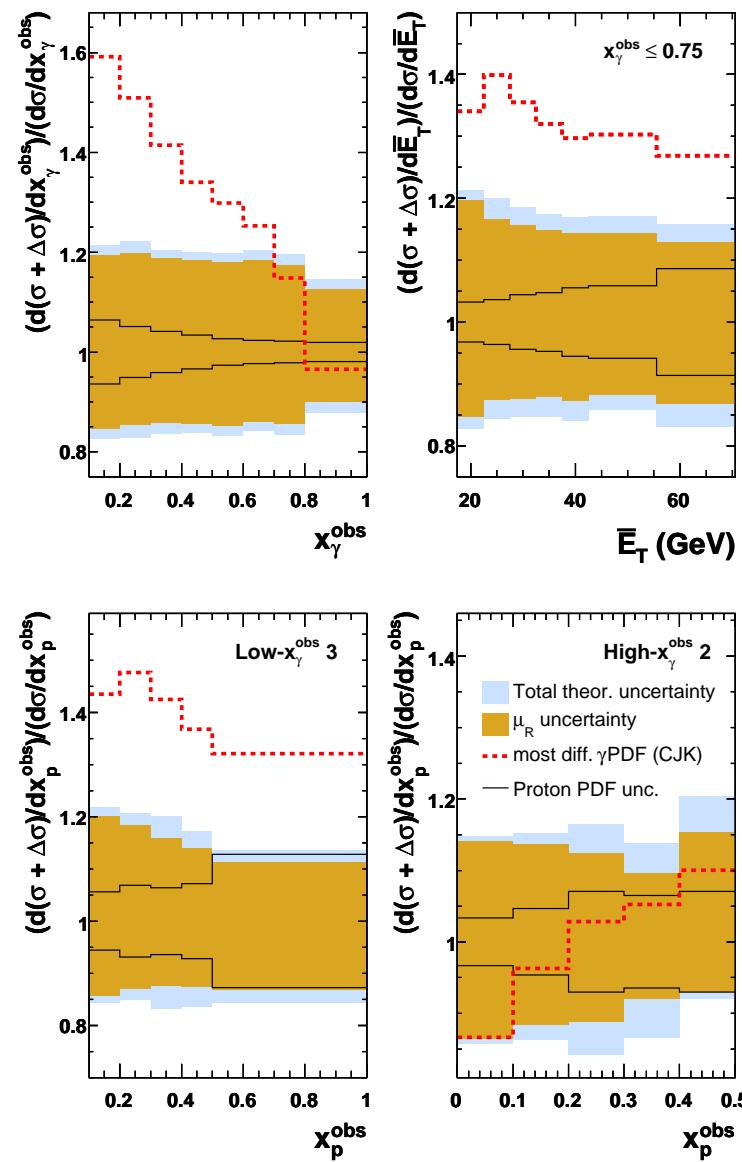
ZEUS



82 pb⁻¹ HERA-I data

$E_T^{\text{jet}1} > 20 \text{ GeV}, E_T^{\text{jet}2} > 15 \text{ GeV}$

$-1 < \eta^{\text{jet}1,1} < 3$



Uncertainties

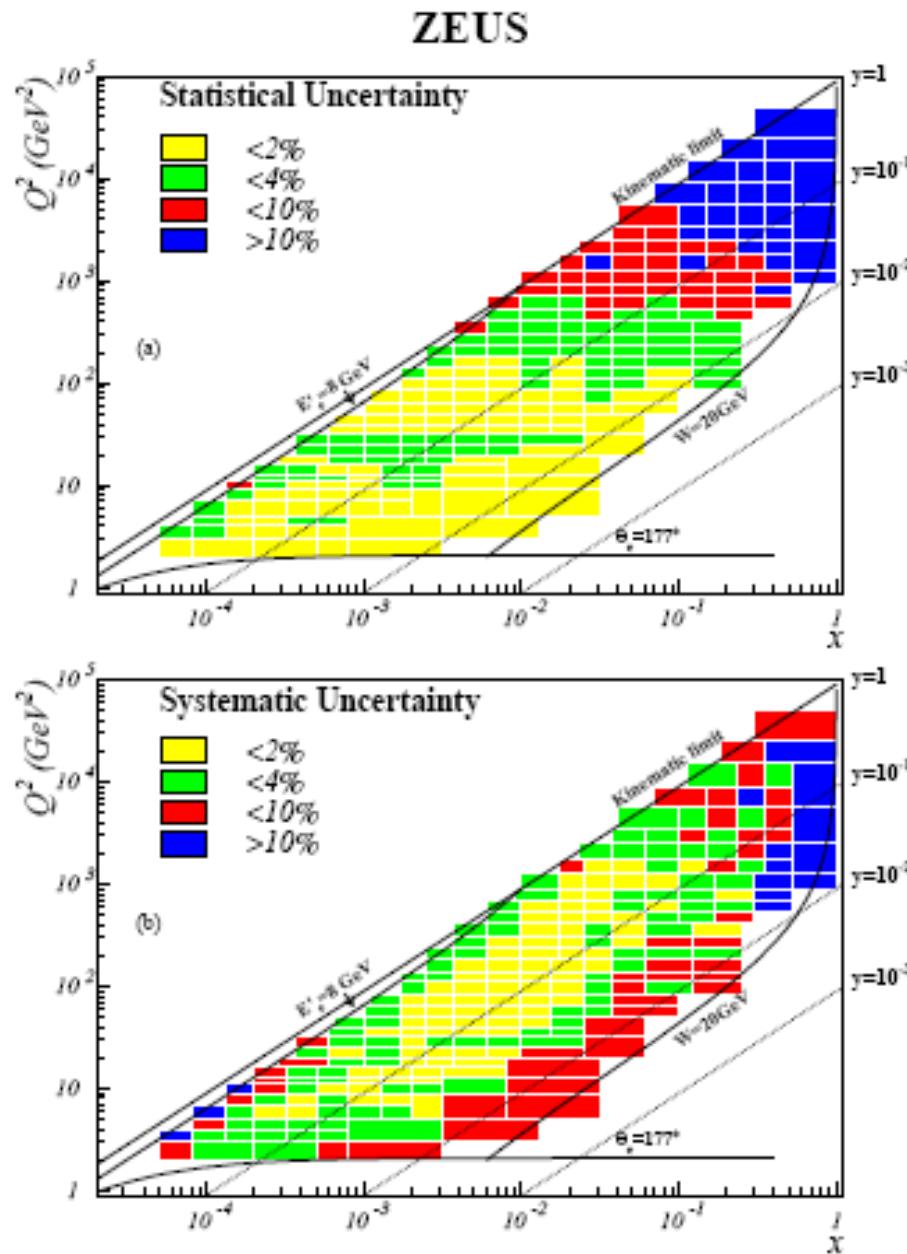
shaded band
from μ_R
up to 20%

full line is
propagation of
ZEUS-JETS
PDF fit errors
large at large
 x_p^{obs}

ZEUS 96/97 $F_2(p)$

statistical and
systematic uncertainties

- 30 pb^{-1} at $\sqrt{s} = 300 \text{ GeV}$
data taken 1996/7
published 2001
- high statistics F_2^p
already systematics limited
over central region of
kinematic plane
- now have $\sim 10\times$ luminosity
will give significantly improved
results at very high Q^2 and x



Outlook

- ❖ Many interesting talks to come in this session
- ❖ A lot of high statistics measurements are in progress
 - many results presented here are from HERA-I data
 - HERA-II will extend measured region at large x and Q^2
 - already some very precise data from Tevatron Run-II
 - for both larger luminosity allows access to higher jet E_T
 - but systematics limit HERA and Tevatron measurements
- ❖ On the theory side
 - good news is that NNLO calculations are available for $F_2(p)$ and on the way for $F_2(\gamma)$
 - bad news is that promise of sensitivity of jet measurements to proton and photon PDFs is limited by scale uncertainties (at NLO)
 - **real and urgent need for NNLO jet calculations**