

# Study of $\pi\pi$ production in two-photon collisions at Belle



S.Uehara (KEK)

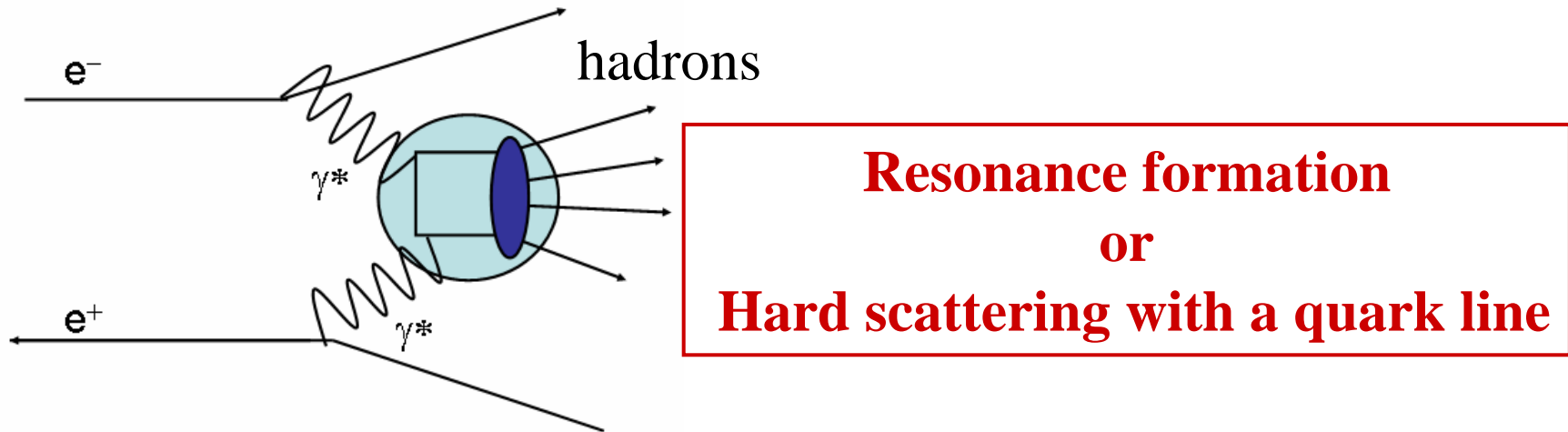


*on behalf of* **The Belle Collaboration**

*Photon2007, 9 July, 2007, Paris*



# Motivation of two-photon physics



Hadron production from two quasi-real photons

( $|q^2| < 0.001 \text{ GeV}^2$ , with no-tag condition)

Exclusive processes with  $W_{\gamma\gamma} = 0.6 - 4.5 \text{ GeV}$  at KEKB/Belle

Wide energy region --- Various physics aspects

can be studied simultaneously.

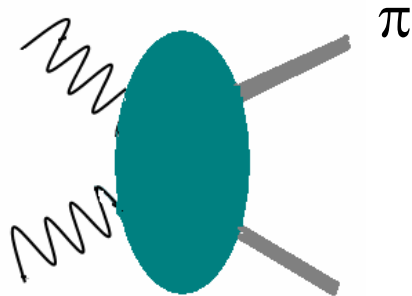
Light-quark resonances, Charmonia

Perturbative / Non-perturbative QCD,

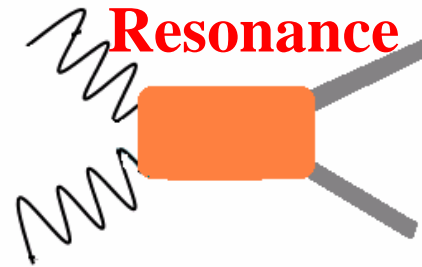
Hadron production mechanism



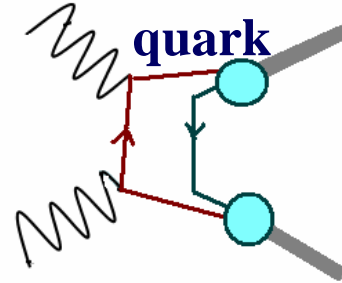
# General physics in $\gamma\gamma \rightarrow \pi^+\pi^-/\pi^0\pi^0$ final states



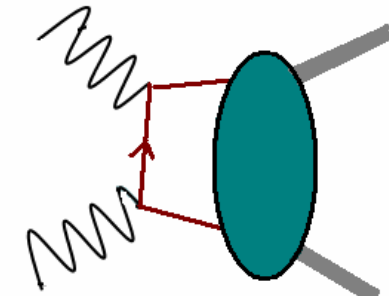
soft production  
of mesons



**Resonance**



**quark**



soft hadron  
exchange

$\pi^+\pi^-$  and  $\pi^0\pi^0$ :

Physics is almost the same, but gives independent information

Electromagnetic production as mesons:  $\sigma(\pi^0\pi^0) \ll \sigma(\pi^+\pi^-)$

Resonances ( $I=0, J^{PC}=0^{++}$ ) decaying via strong interaction:

$$\sigma(\pi^0\pi^0) : \sigma(\pi^+\pi^-) = 1 : 2$$

Test of QCD:  $\sigma(\pi^0\pi^0) / \sigma(\pi^+\pi^-) : \sim 0.03$  (LO) – 0.5 (“handbag”)

c.m.-energy ( $W$ ) and angular dependences must also be examined.



# KEKB Accelerator and Belle Detector

- Asymmetric  $e^- e^+$  collider  
8 GeV  $e^-$  (HER) x 3.5 GeV  $e^+$  (LER)

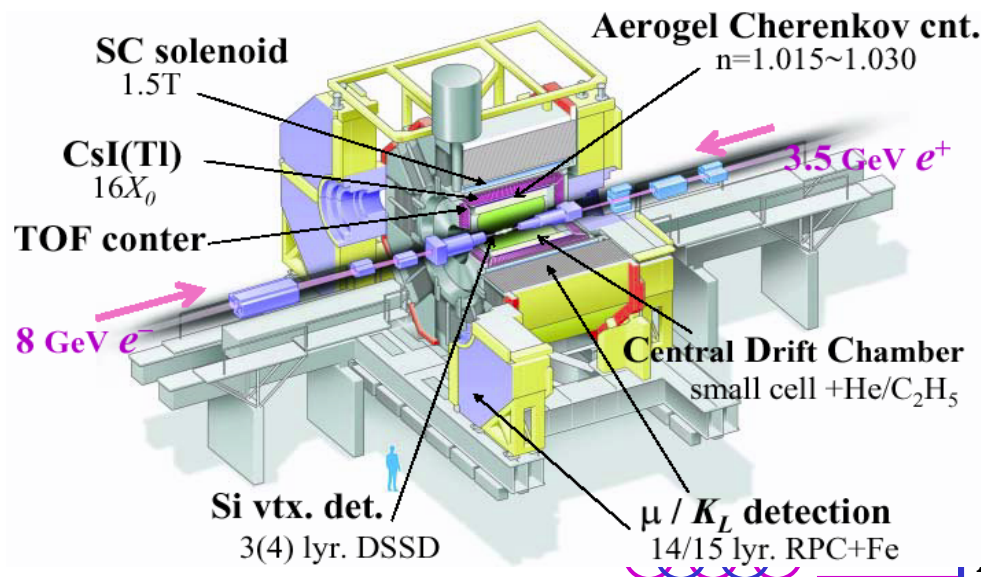
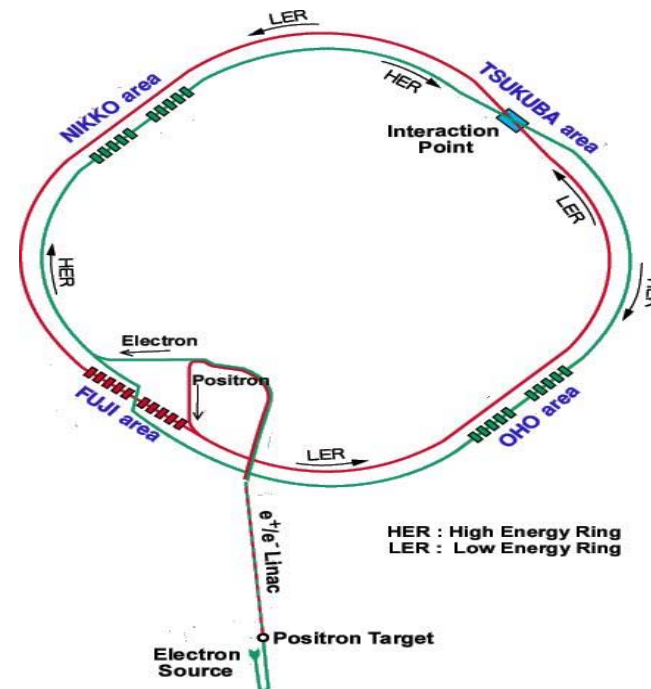
$$\sqrt{s} = 10.58 \text{ GeV} \Leftrightarrow \Upsilon(4S)$$

Beam crossing angle: 22mrad

- Continuous injection
- Luminosity

$$L_{\text{max}} = 1.71 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

$$\int L dt \sim 710 \text{ fb}^{-1}$$



High momentum/energy resolutions

CDC+Solenoid, CsI

Vertex measurement – Si strips

Particle identification

TOF, Si-aerogel, CDC-dE/dx,

RPC for  $K_L$ /muon

# Results of $\gamma\gamma\rightarrow\pi^+\pi^-$

Belle Collaboration

**W = 0.8 – 1.5 GeV** Phys. Rev. D **75**, 051101(R) (2007)  
arXiv:0704.3538[hep-ex],  
to appear in J. Phys. Soc. Jpn. (2007)

**W = 2.4 – 4.1 GeV** Phys. Lett. B **615**, 39 (2005)



# $f_0(980)$ in $\gamma\gamma \rightarrow \pi^+\pi^-$

$f_0(980)$

$85.9\text{fb}^{-1}$

- is an ordinary  $q\bar{q}$  meson?
- an exotic state?
- some special theory needed?

Its two-photon coupling is a crucial key.

Prediction of  $\Gamma_{\gamma\gamma}$  :

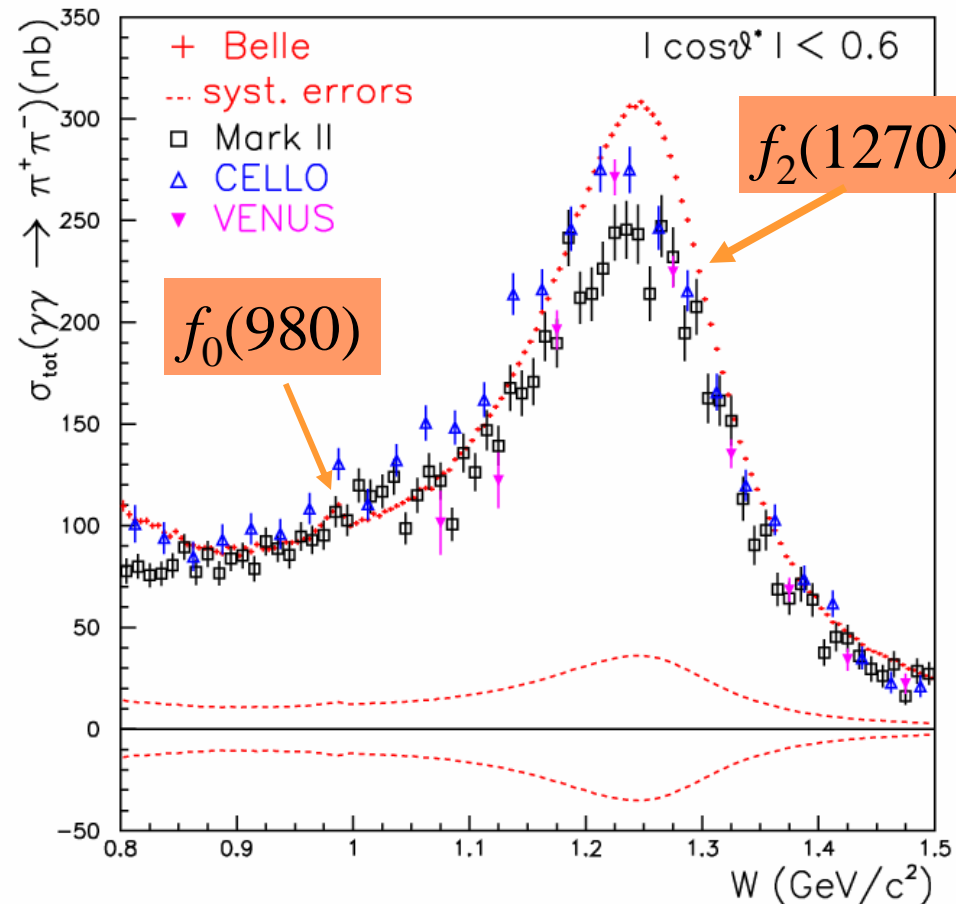
$u\bar{u}, d\bar{d}$  --- 1.3 – 1.8 keV

$s\bar{s}$  --- 0.3 – 0.5 keV

$K\bar{K}$  molecule --- 0.2 – 0.6 keV

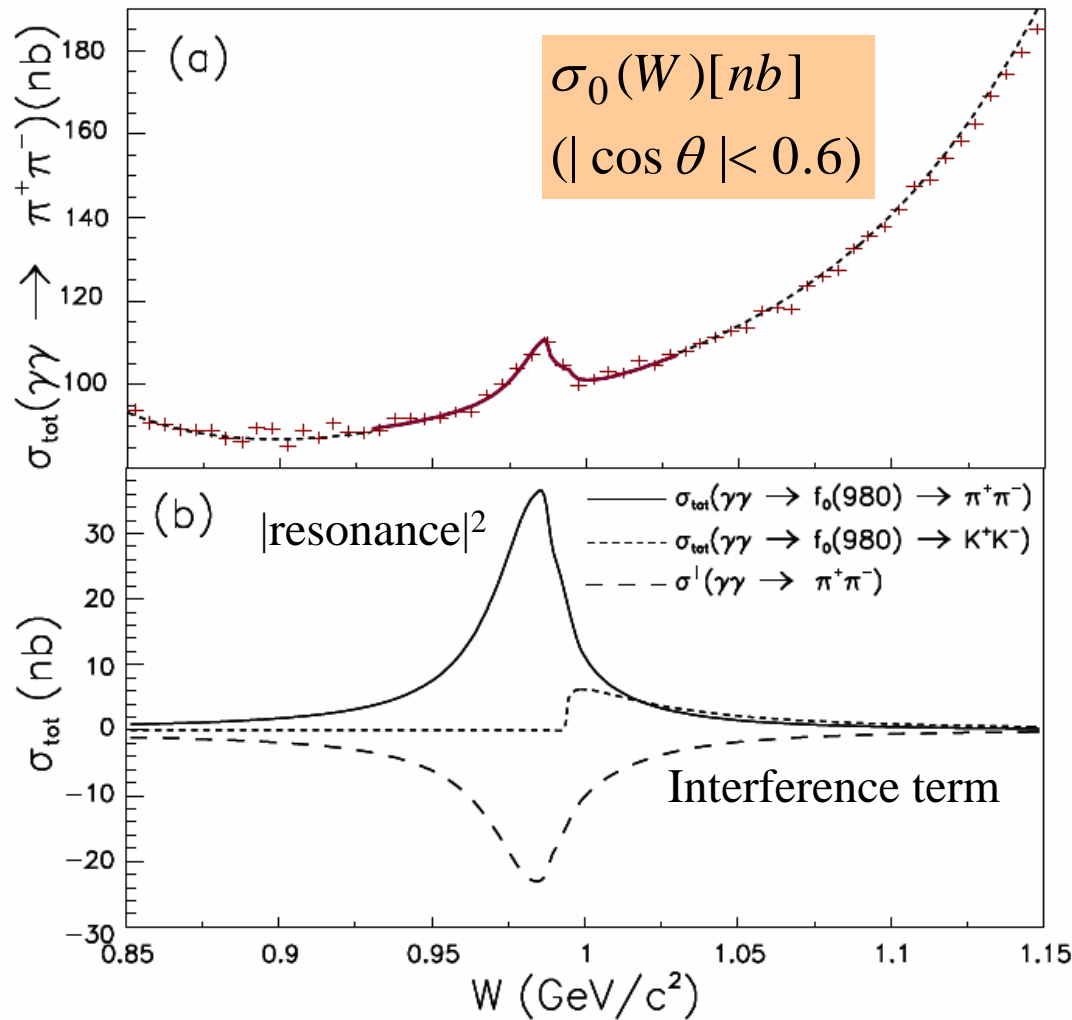
$\pi/\mu$  separation:

by comparing energy deposit in the CsI calorimeter between data and MC



$f_0(980)$  appears as a small but statistically significant peak.

# Fit to the $f_0(980)$ line shape



$$f_0(980) \rightarrow \pi^+\pi^-$$

$$M = 985.6_{-1.5-1.6}^{+1.2+1.1} \text{ MeV}/c^2$$

$$\Gamma_{\pi^+\pi^-} = 34.2_{-11.8-2.5}^{+13.9+8.8} \text{ MeV}$$

$$\Gamma_{\gamma\gamma} = 205_{-83-117}^{+95+147} \text{ eV}$$



# New upper limit for $Br(\eta' \rightarrow \pi^+\pi^-)$

No  $\eta' \rightarrow \pi^+\pi^-$  enhancement is seen near  $958\text{MeV}/c^2$

This is a  $\mathcal{P}$  and  $\mathcal{CP}$  mode;

previous upper limit:

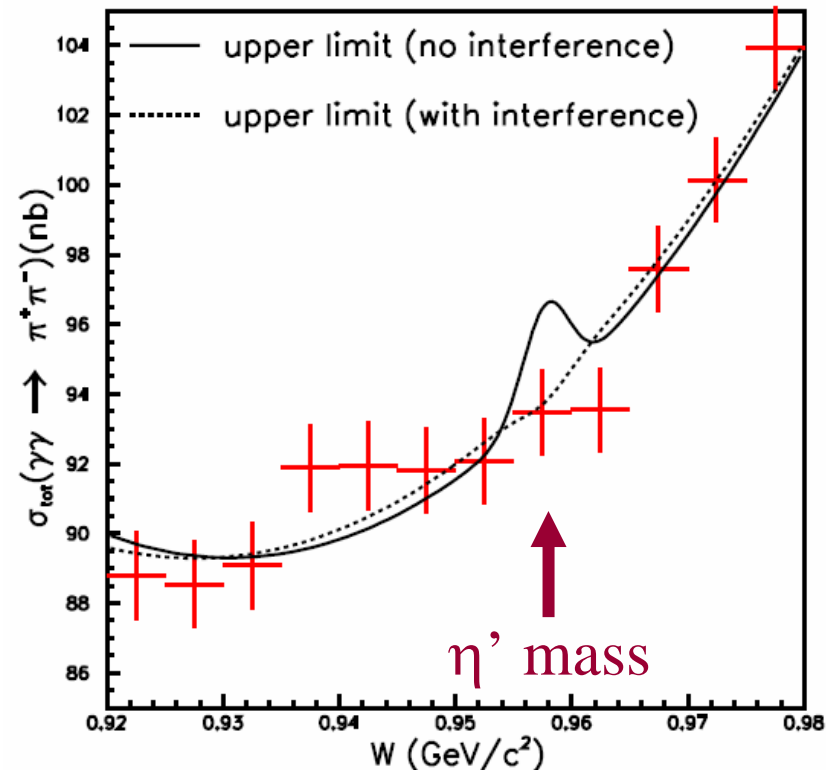
$Br(\eta' \rightarrow \pi^+\pi^-) < 0.02$  (HBC (1969))

New upper limit for

$Br(\eta' \rightarrow \pi^+\pi^-) < 2.8 \times 10^{-3}$

(interference with the non-resonant process allowed)

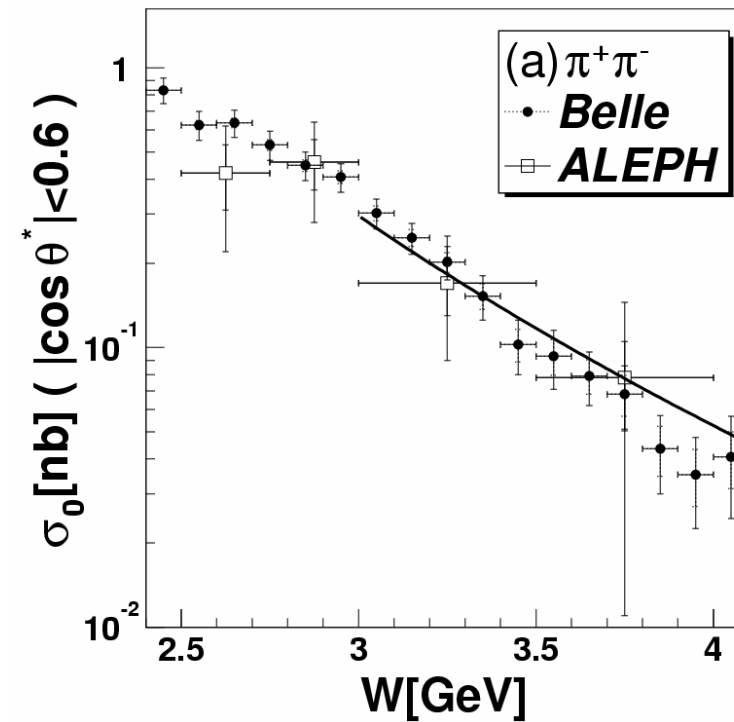
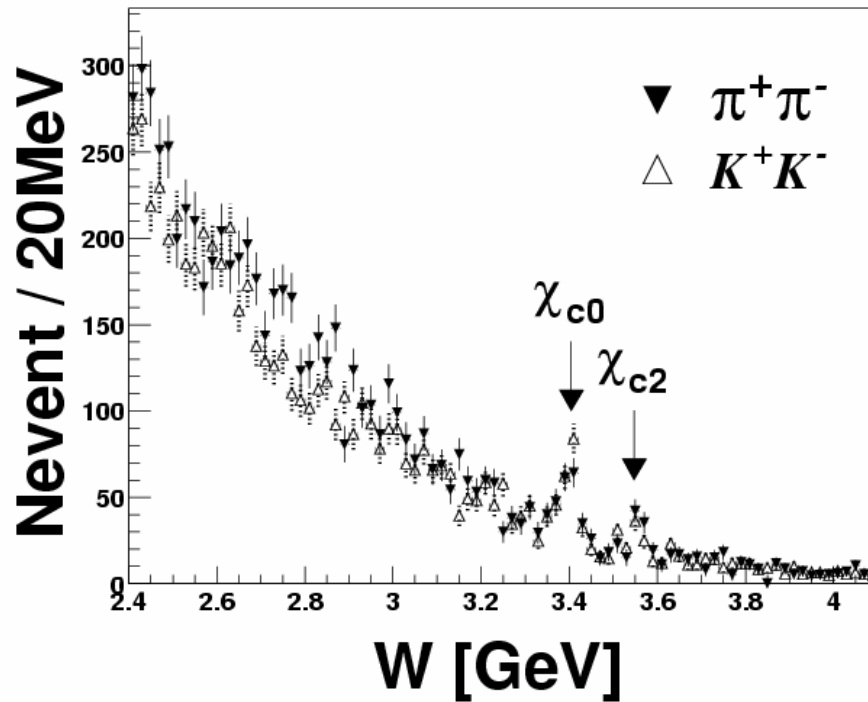
$< 3.3 \times 10^{-4}$  (no interference)





# $\pi^+\pi^-$ measurements at high energies

PLB 615, 39 (2005)



Two-photon measurements of  $\Gamma_{\gamma\gamma}(\chi_{cJ})Br$  (eV)

$$\Gamma_{\gamma\gamma}Br(\chi_{c0} \rightarrow \pi^+\pi^-) = 15.1 \pm 2.1 \pm 2.3$$

$$\Gamma_{\gamma\gamma}Br(\chi_{c0} \rightarrow K^+K^-) = 14.3 \pm 1.6 \pm 2.3$$

$$\Gamma_{\gamma\gamma}Br(\chi_{c2} \rightarrow \pi^+\pi^-) = 0.76 \pm 0.14 \pm 0.11$$

$$\Gamma_{\gamma\gamma}Br(\chi_{c2} \rightarrow K^+K^-) = 0.44 \pm 0.76 \pm 0.14$$



# Preliminary results of $\gamma\gamma\rightarrow\pi^0\pi^0$



# Selection of $\pi^0\pi^0$ candidates

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Based on data with an integrated luminosity of  $95 \text{ fb}^{-1}$

Only 4 photons are visible

- Triggered by Calorimeter triggers

- No reconstructed track with

$$p_t > 0.1 \text{ GeV}/c, \text{ dr} < 5 \text{ cm}, |dz| < 5 \text{ cm}$$

- 2 or more photons OR 1 or more  $\pi^0$ s

-----  
- Just 2  $\pi^0$ s with  $E(\text{decay product photon}) > 70 \text{ MeV}$ ,  $p_t > 0.15 \text{ GeV}/c$

- Transverse-momentum ( $p_t$ )-balance of the two  $\pi^0$ 's

$$|\Sigma \mathbf{p}_t| < 0.05 \text{ GeV}/c$$

- Satisfying a rough trigger condition at offline:

$$N_{\text{gamma}} = 4 \text{ or } E_{\text{sum\_lab}} > 1.25 \text{ GeV}$$

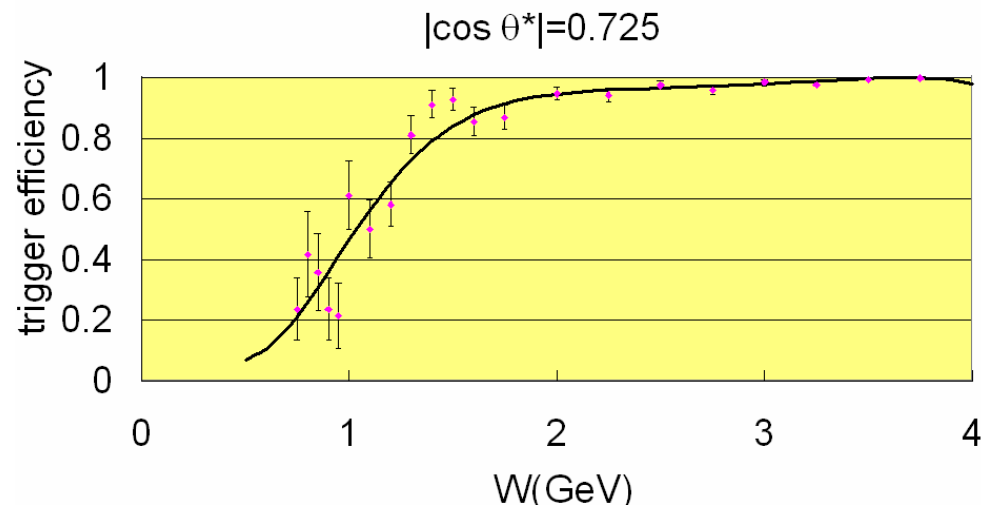
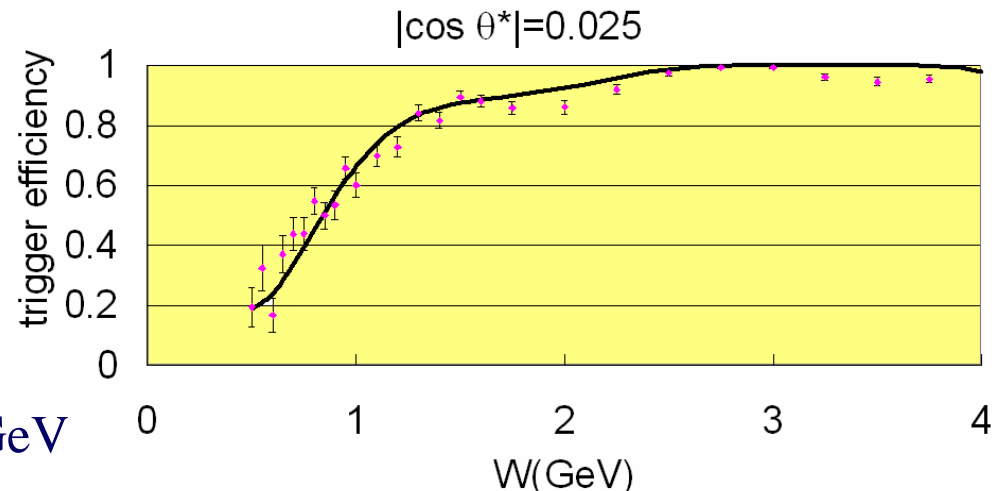
$$\text{in the ECL-trigger region, } 17 < \theta_{\text{lab}} < 128.7 \text{ deg}$$



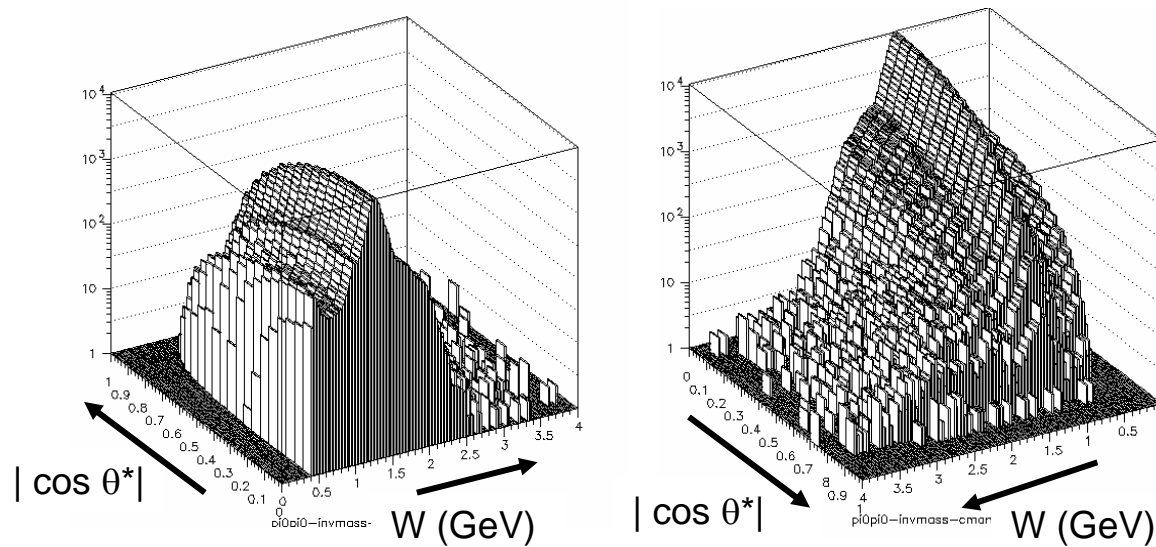
# Trigger efficiency from the simulation

Trigger efficiency is determined by the trigger simulator, *tsim* after tunings of the energy thresholds for the total energy trigger (HiE) – 1.15 GeV and for counting number of clusters (Clst4) – 110 MeV

In each of 16 c.m. angular bins  $0.0 < |\cos \theta^*| < 0.8$ , Fitted by a two-dimensional function of  $(W, |\cos \theta^*|)$

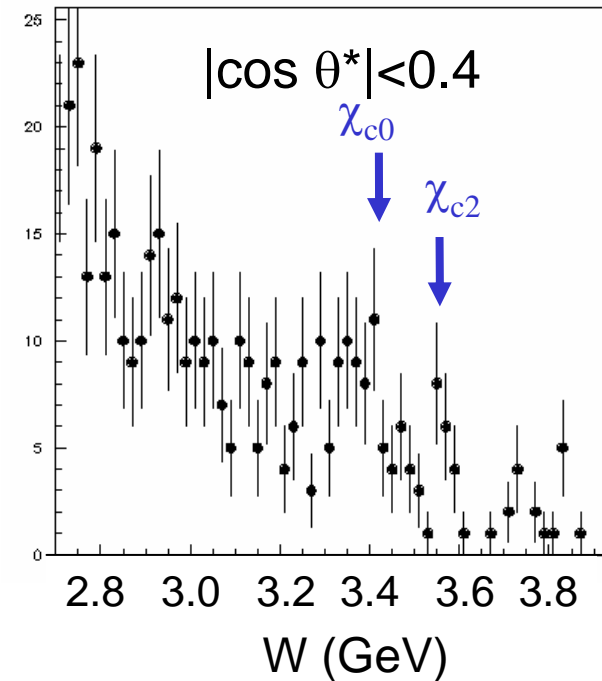
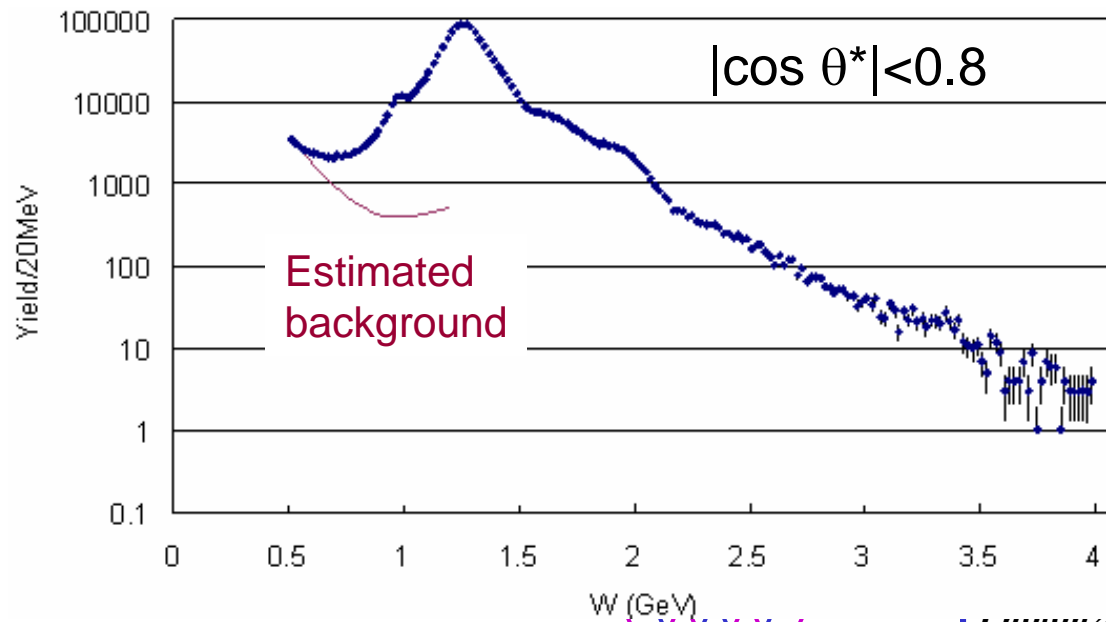


# Raw-event distribution of $\pi^0\pi^0$



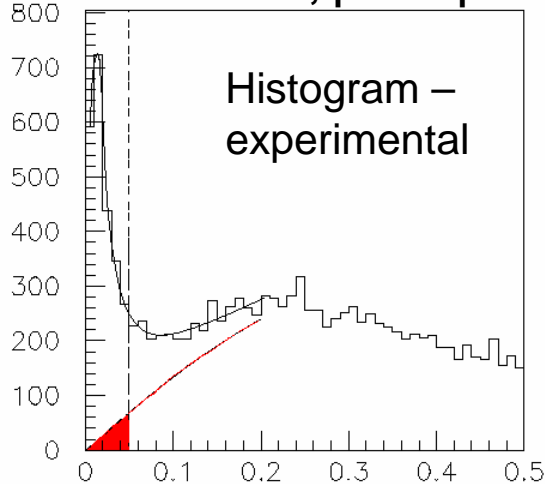
$$W = M(\pi^0\pi^0)$$

About 1.26M events (before the background subtraction)

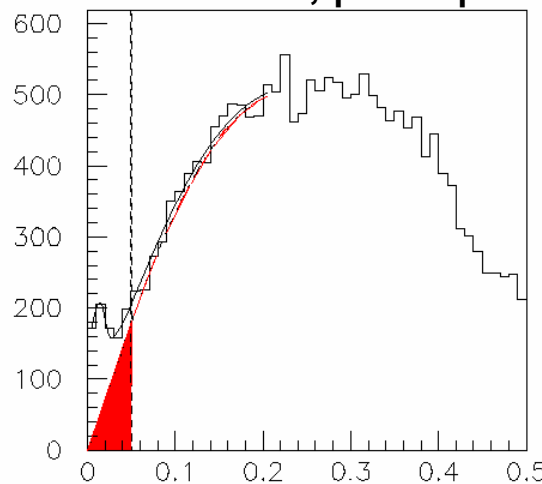


# $p_t$ -balance distributions and backgrounds

$W=0.90\text{GeV}, |\cos\theta^*|=0.05$



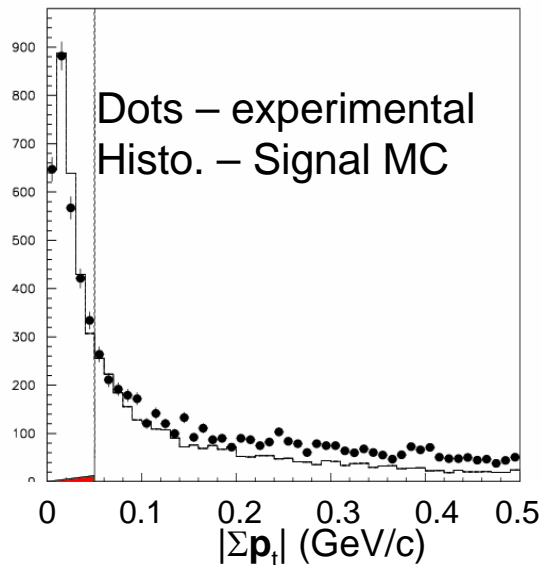
$W=0.66\text{GeV}, |\cos\theta^*|=0.05$



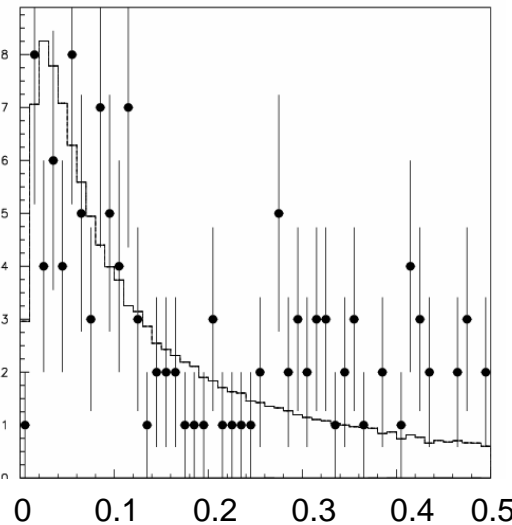
$p_t$ -unbalanced backgrounds are seen in  $W < 1.2 \text{ GeV}$

← Low-energy beam-background photons

$W=1.18\text{GeV}, |\cos\theta^*|=0.65$



$W > 3.6\text{GeV}, |\cos\theta^*| < 0.4$



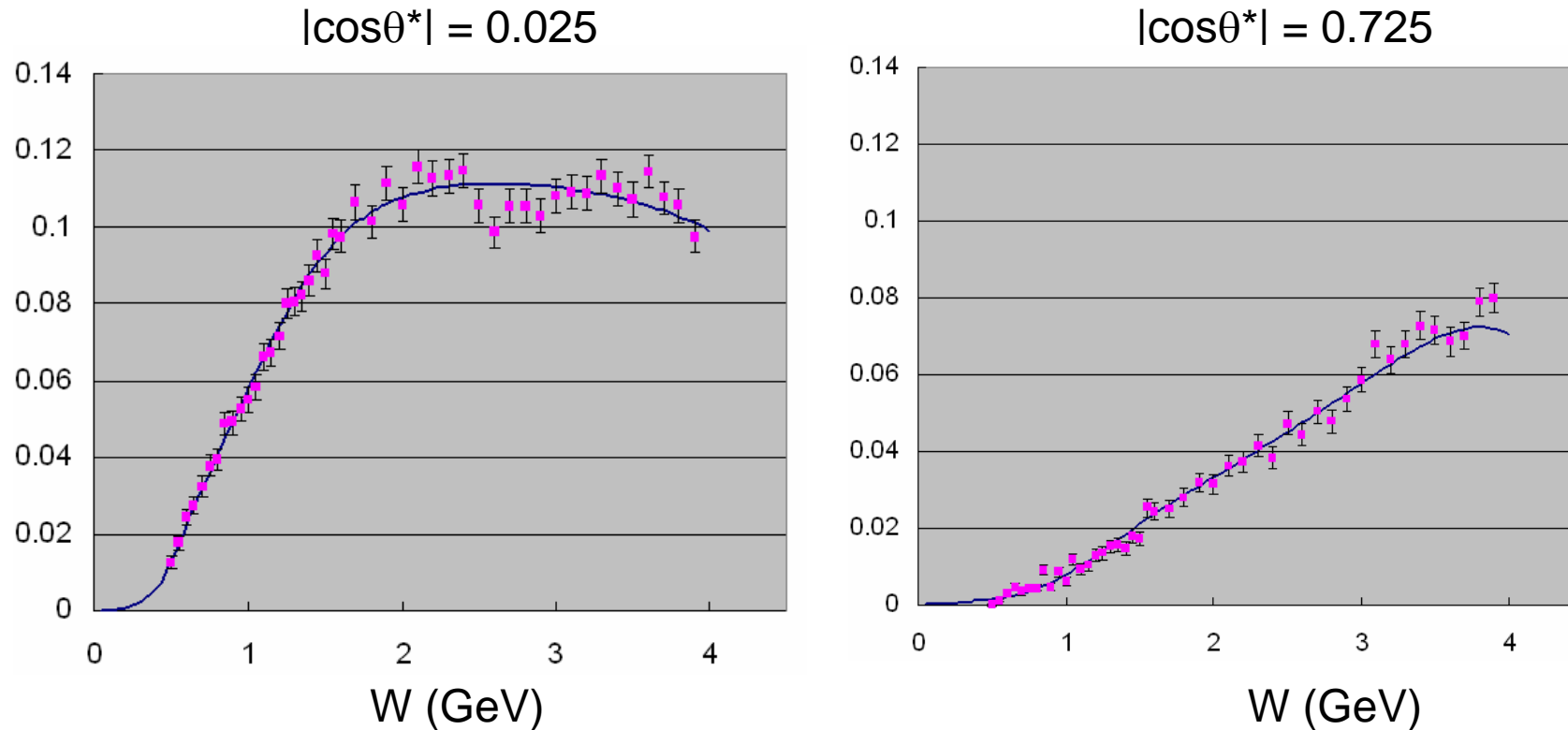
← Intermediate or Higher energies

Non-exclusive process sources not significantly seen



# Detector acceptance not including trigger

Calculated from signal MC simulation and fitted by a smooth function



Around 11% at maximum, typically 5 %

Large angular dependence due to geometrical condition of the detector

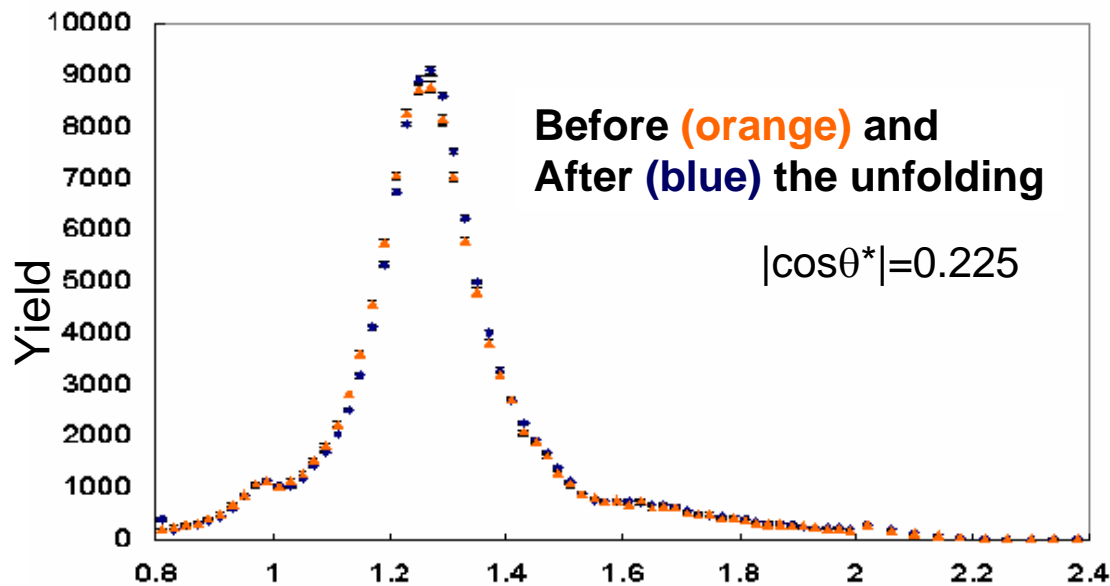
**Overall efficiency = Acceptance \* trigger efficiency**



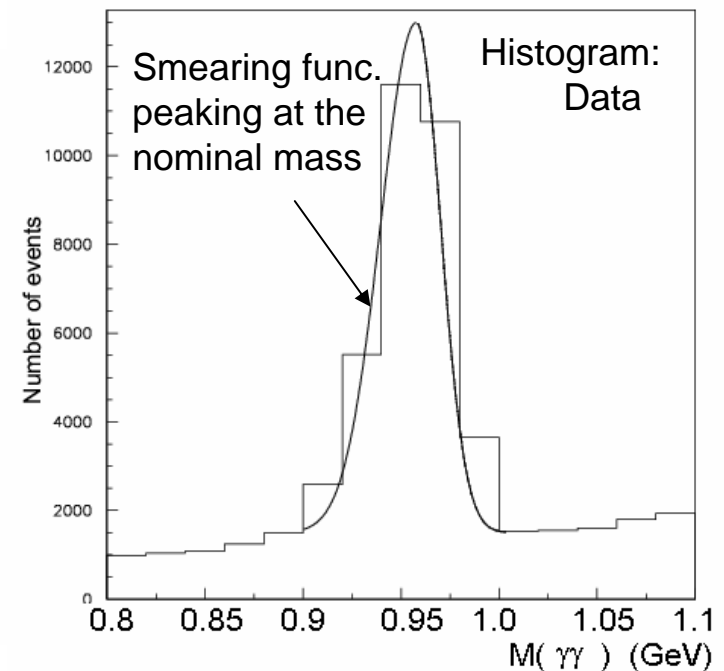
# Invariant-mass resolution and Unfolding

**W resolution** ---  $\sim 1.4\% \times W$ , almost independently of  $W$  (from signal MC)  
Apply **Unfolding** to the experimental  $W$  distribution (in each angle region)  
for the smearing effect in the  $W$  direction  
using an **asymmetric Gaussian** (1.3% higher side and 1.9 % lower side).

Unfolding is applied in  $0.9 \text{ GeV} < W < 2.4 \text{ GeV}$ .  
Wider bin-widths than the resolution are used  
in the other  $W$  regions.

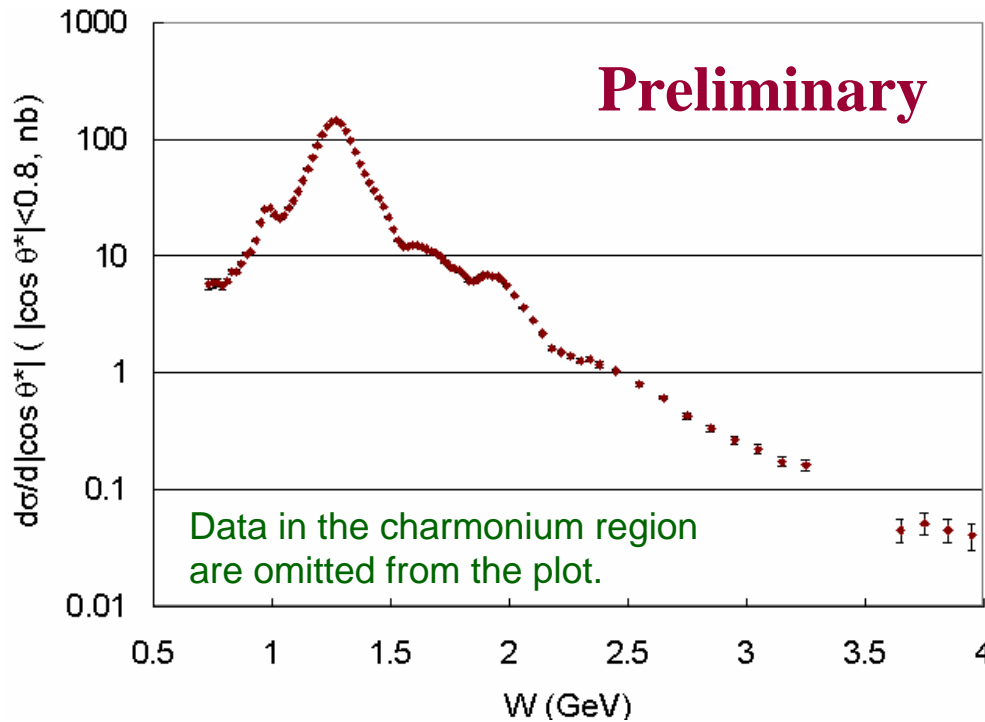


Experimental sample of  $\eta' \rightarrow \gamma\gamma$





# Cross sections of $\gamma\gamma \rightarrow \pi^0\pi^0$



Obtain first  $d\sigma/d|\cos\theta^*|$  in each  $\Delta|\cos\theta^*|=0.05$  bin  
Then, accumulate them over the angle

**Important note:**

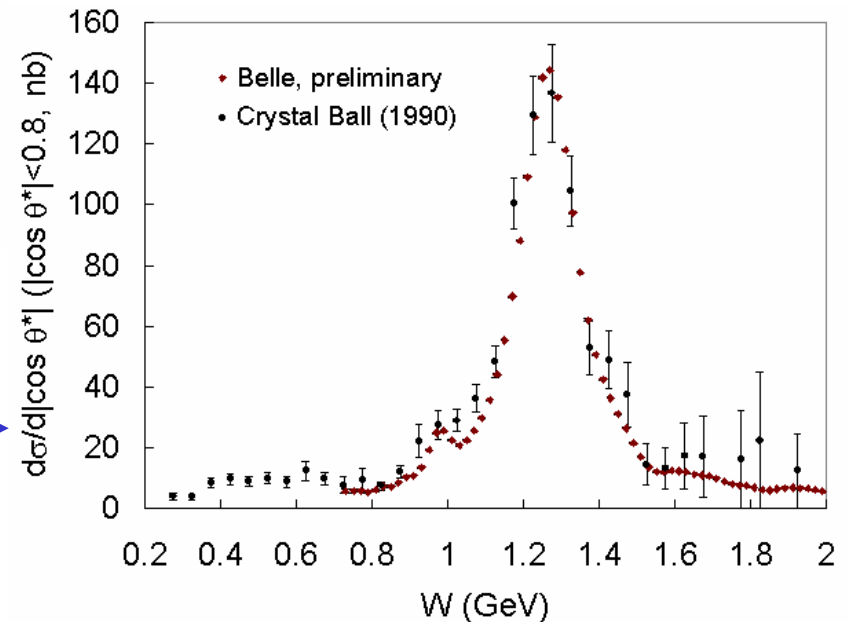
After the Unfolding, different data bins and errors are no longer independent of each other.

**Comparison with Crystal Ball at DORIS II (1990)** →

**They are consistent.**

**Belle has  $\sim 10^3$  times more data.**

Statistical errors only.



# Systematic-error sources

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- Trigger efficiency - - - 4% @  $W > \sim 1.1$  GeV (HiE)  
5% - 30% @  $W < \sim 1.1$  GeV (Clst4)
  
- $-\pi^0$  reconstruction efficiency - - - 6%
  
- Acceptance (dominated by pt-balance cut) - - 3% - 5%
  
- Background subtraction - - - 20% of the subtraction component  
3% in High W where no subtraction applied.
  
- Luminosity function - - - 4% - 5%

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Total	55% - 10%	@ $W < \sim 1.05$ GeV
	~9%	@ $1.05 \text{ GeV} < W < \sim 2.7$ GeV
	10% - 11%	@ $W > \sim 2.7$ GeV



# Differential cross section (Angular dependence)

$$\gamma\gamma \rightarrow \pi^0\pi^0$$

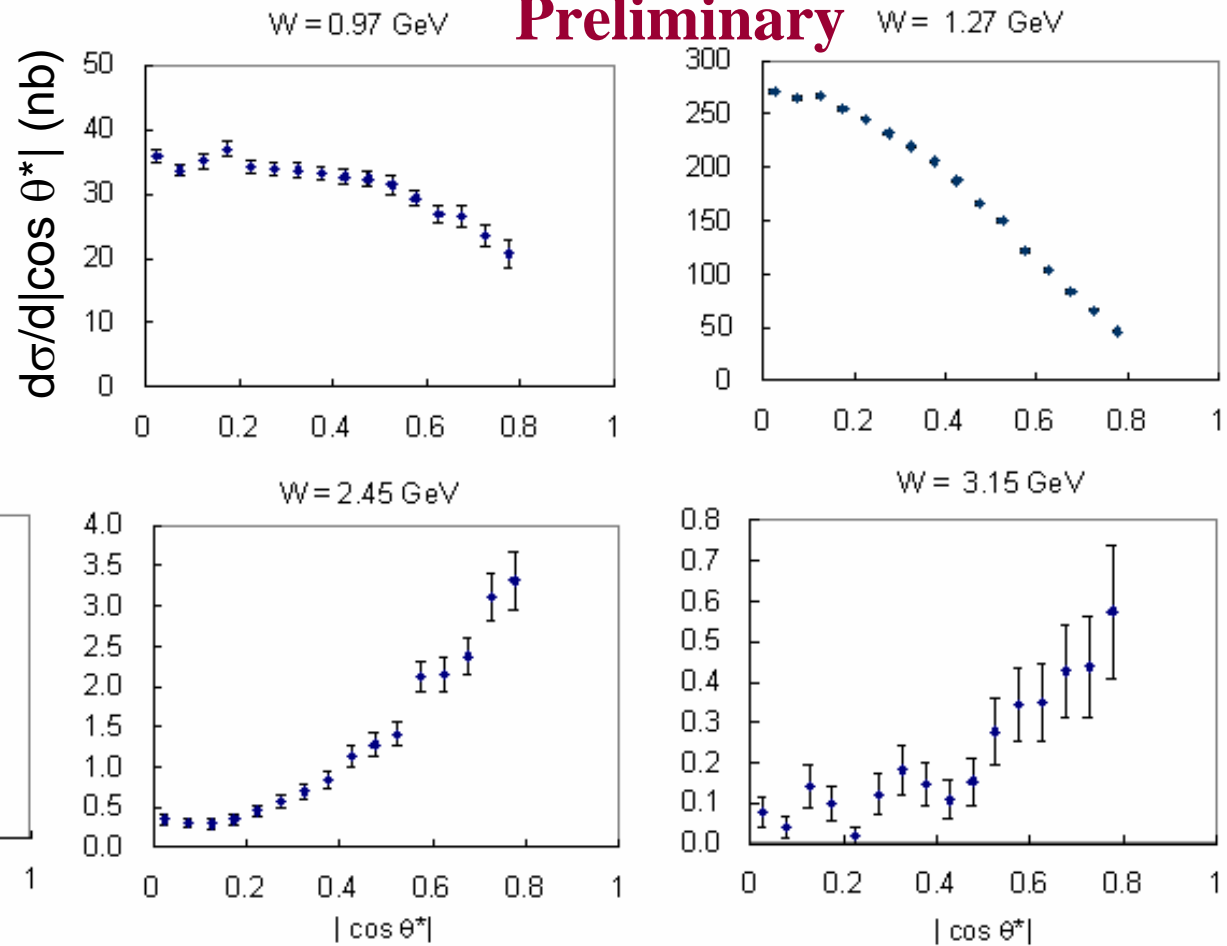
**Low W**  $\rightarrow$  **High-W**

Large angle enhancement  
appears  $\rightarrow$  disappears

Small angle enhancement  
disappears  $\rightarrow$  appears

**Change  $\uparrow$   $\sim$  2.0 GeV**

**Preliminary**



# Resonant structures

## Resonances:

Clearly seen:  $f_0(980), f_2(1270), \sim 1.65 \text{ GeV}, \sim 1.95 \text{ GeV}$

Hints with a lower significance :  $\sim 1.45 \text{ GeV}, \chi_{c0}, \chi_{c2}$

## Sizes of the charmonia

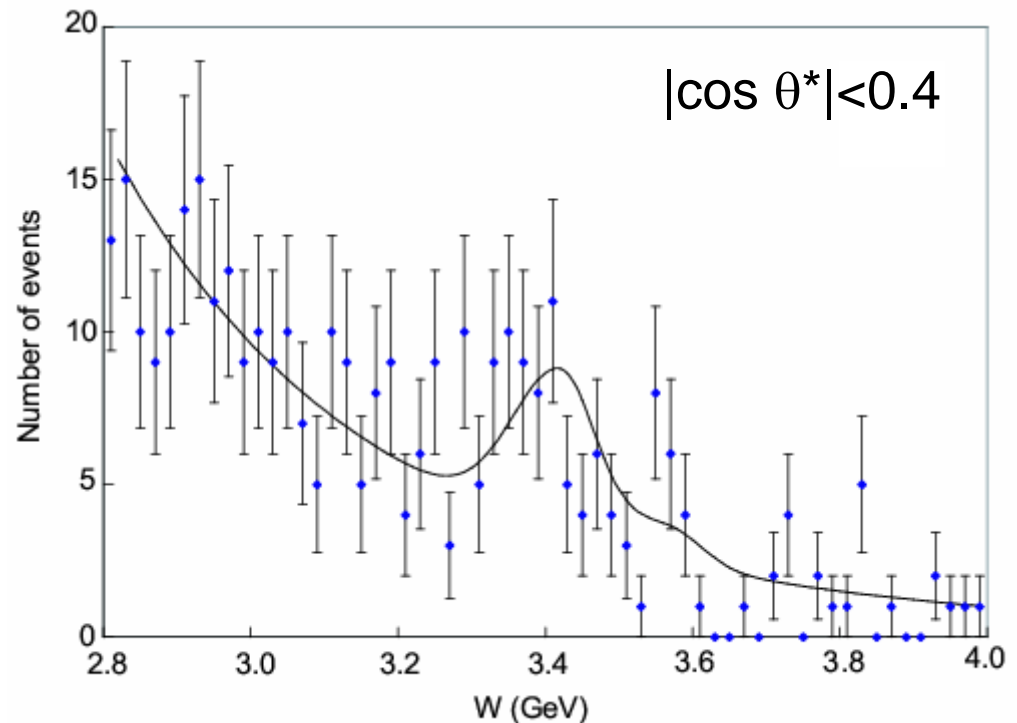
$$\Gamma\gamma\gamma(\chi_{c0})B(\chi_{c0}\rightarrow\pi^0\pi^0): \\ 8.4 \pm 2.2 \pm 0.8 \text{ eV} \quad (4.5\sigma)$$

$$\Gamma\gamma\gamma(\chi_{c2})B(\chi_{c2}\rightarrow\pi^0\pi^0): \\ 0.29 \pm 0.23 \pm 0.03 \text{ eV} \quad (1.4\sigma)$$

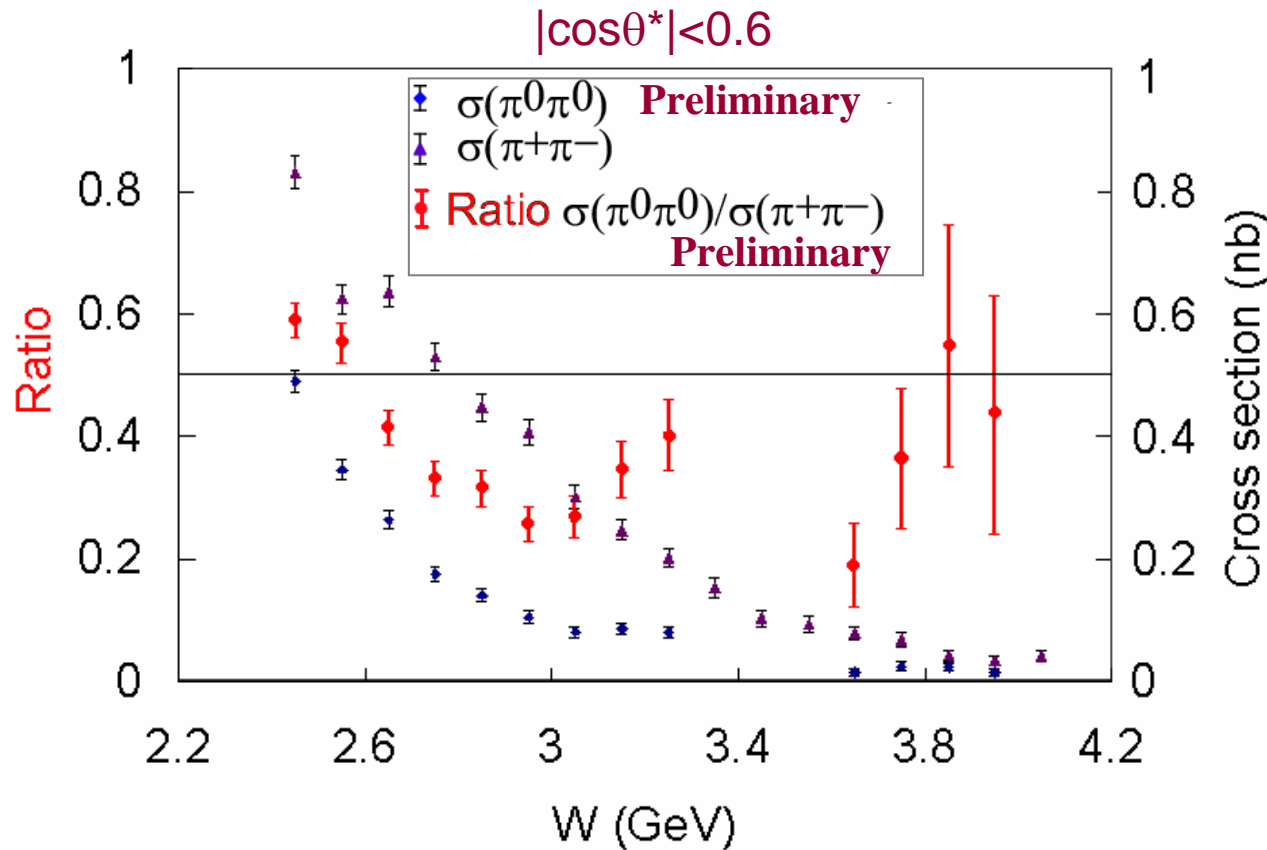
$$\text{Upper limit} < 0.75 \text{ eV} \quad (90\% \text{CL})$$

**Preliminary**

The central values are consistent with the expectations from isospin invariance between the  $\pi^+\pi^-/\pi^0\pi^0$  decays



# Cross section ratio $\sigma(\pi^0\pi^0)/\sigma(\pi^+\pi^-)$



Error bars are statistical only.

Systematic errors:  
About 10% at each measurement point, except  $\pi^+\pi^-$  above the charmonium masses (~25%).

Charmonium region is omitted from the plot.

The ratio is 0.3 – 0.4 at  $W > 2.7$  GeV



# Conclusion of $\pi^+\pi^-$ measurement

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- We measure the process  $\gamma\gamma \rightarrow \pi^+\pi^-$  with  $85.9 \text{ fb}^{-1}$  data.
- The differential cross sections are obtained in  $0.8 \text{ GeV} < W < 1.5 \text{ GeV}$  and  $|\cos \theta^*| < 0.6$  in the  $\gamma\gamma$  c.m. frame.  
(# We separately published before for the region  $2.4 \text{ GeV} < W < 4.1 \text{ GeV}$ )
- We confirm small but statistically significant peak from  $f_0(980)$ .
- New upper limit for P and CP violating process  $\eta' \rightarrow \pi^+\pi^-$  is obtained.



# Summary for $\pi^0\pi^0$ measurement

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- We measure the process  $\gamma\gamma \rightarrow \pi^0\pi^0$  with  $95\text{fb}^{-1}$  data.
- Preliminary results of the differential cross sections are obtained in  $0.6\text{ GeV} < W < 4.0\text{ GeV}$  and  $|\cos \theta^*| < 0.8$  in the  $\gamma\gamma$  c.m. frame.
- Several resonant structures are seen, including a statistically significant peak from  $f_0(980)$ .
- Behavior of the angular dependence (forward- and/or large-angle enhancements) changes drastically at around  $W = 2.0\text{ GeV}$ .
- The cross section ratio  $\sigma(\pi^0\pi^0)/\sigma(\pi^+\pi^-)$  in 3 GeV region is obtained.



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# BACKUP slides





# Measurements of two-photon processes at Belle

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$\gamma\gamma \rightarrow \chi_{c2} \rightarrow \gamma J/\psi$	PLB 540, 33(2002)
$\gamma\gamma \rightarrow (f_2'(1525) \text{ etc. } \rightarrow ) K^+ K^-$ (1.4 - 2.4 GeV)	EPJC 32, 323 (2003)
$\gamma\gamma \rightarrow (\chi_{c0}, \chi_{c2} \rightarrow) \pi^+ \pi^-, K^+ K^-$ (2.4 - 4.1 GeV)	PLB 615, 39 (2005)
$\gamma\gamma \rightarrow (\eta_c \rightarrow) p \bar{p}$ (2.025 - 4.0 GeV)	PLB 621, 41 (2005)
$\gamma\gamma \rightarrow \chi_{c2}' \rightarrow D \bar{D}$	PRL 96, 082003 (2006)
$\gamma\gamma \rightarrow (f_0(980) \text{ etc. } \rightarrow) \pi^+ \pi^-$ (0.8 - 1.5 GeV)	PRD 75, 051101(R) (2007), arXiv:0704.3538[hep-ex], to appear in Jour. Phys. Soc. Jpn. (2007)
$\gamma\gamma \rightarrow (\chi_{c0}, \chi_{c2} \rightarrow) K^+ K^-$ (2.4 - 4.0 GeV)	hep-ex/0609042v2, submitted to PLB
$\gamma\gamma \rightarrow (\eta_c, \chi_{c0}, \chi_{c2} \rightarrow) \pi^+ \pi^- \pi^+ \pi^-, K^+ K^- \pi^+ \pi^-, K^+ K^- K^+ K^-$	arXiv:0706.3955[hep-ex], submitted to EPJC
$\gamma\gamma \rightarrow a_2's \rightarrow -\pi^+ \pi^- \pi^0$ (1.2 - 3.0 GeV)	hep-ex/0610022
$\gamma\gamma \rightarrow (\eta_c \rightarrow) \Lambda \bar{\Lambda}, \Sigma^0 \bar{\Sigma}^0$ (2.3-4.0 GeV)	hep-ex/0609048



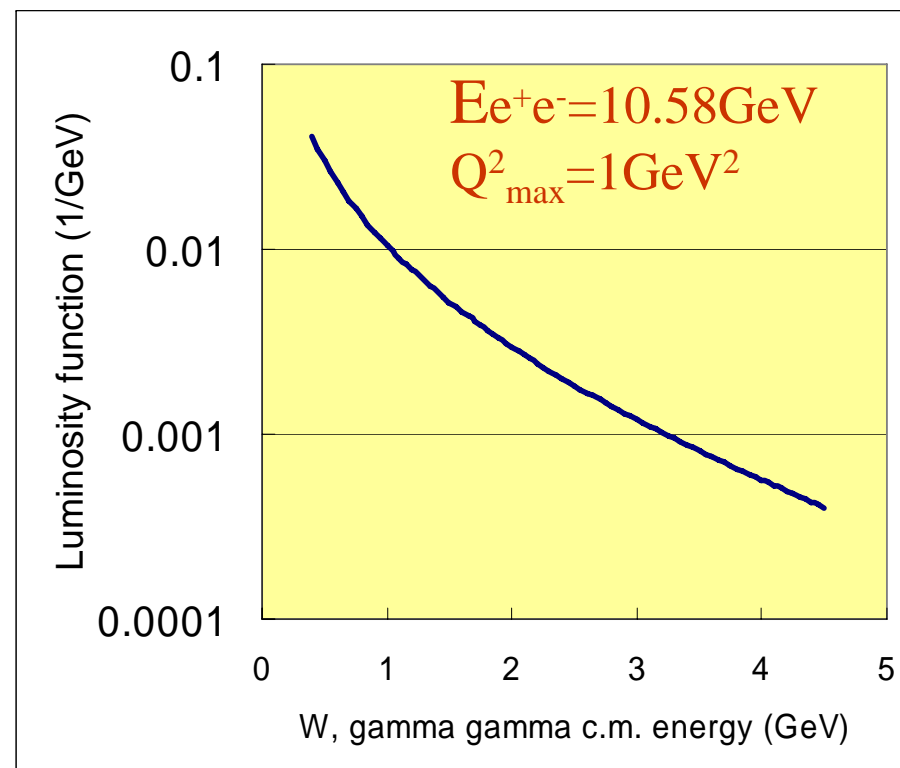
# Reactions at KEKB/Belle

The cross sections observable there

$e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}$	---	1.1 nb
$e^+e^- \rightarrow q\bar{q}$ (uds)	---	2.1 nb
$e^+e^- \rightarrow c\bar{c}$	---	1.2 nb
$e^+e^- \rightarrow \tau^+\tau^-$	---	0.9 nb
$\gamma\gamma \rightarrow \text{hadrons}$ ( $W_\gamma > 0.8\text{GeV}$ )	---	$\sim 1$ nb
(within the acceptance)		

Luminosity Function  
for quasi-real  $\gamma\gamma$  collisions

$$d\sigma_{(\text{in } ee)} = \sigma_{(\text{in } \gamma\gamma)} L_{\gamma\gamma}(W) dW$$

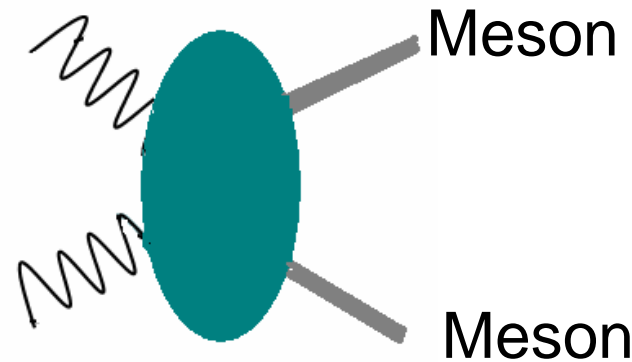


Calculated with equivalent-photon approximation



# Two-meson exclusive final states

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**C = + resonances:** Peak structure in the invariant mass distribution

**Test of QCD:** c.m.-energy ( $W$ ) dependence and angular dependence in high energies

## General Analysis strategy

Invariant-mass of hadron pair =  $W$  (c.m. energy of  $\gamma\gamma$ )

Quasi-real two-photon collisions with final state fully reconstructed

--- strict transverse momentum balance is required

$$(|\Sigma \mathbf{p}_t| < 50 - 200 \text{ MeV}/c)$$

This gives efficient background rejection



# Selection of $\pi^+\pi^-$ candidates

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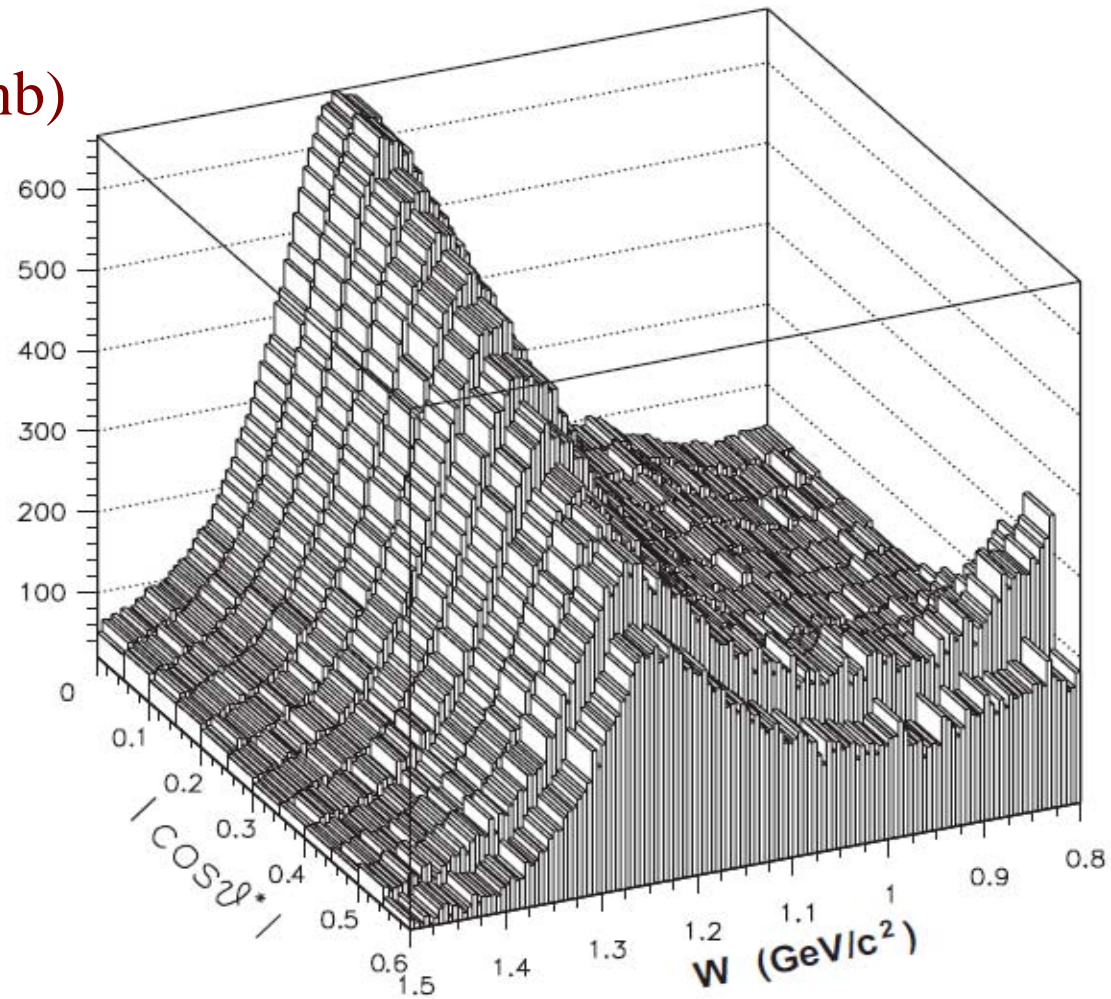
Based on data with an integrated luminosity of  $85.9\text{fb}^{-1}$

- Two charged tracks (oppositely charged)  
with  $p_t > 0.3 \text{ GeV}/c$ ,  $-0.47 < \cos \theta_{\text{lab}} < +0.82$
- $|\Sigma \mathbf{p}_t^*|$  (in  $e+e^-$  c.m.s)  $< 0.1 \text{ GeV}/c$
- $\pi/K$ ,  $\pi/p$  separations  
using TOF, Aerogel-Cherenkov and  $dE/dx$
- Muon background subtraction  
with fitting the **energy-deposit distribution** on ECL  
KLM (muon detector with iron filter) cannot be  
available in these low energies

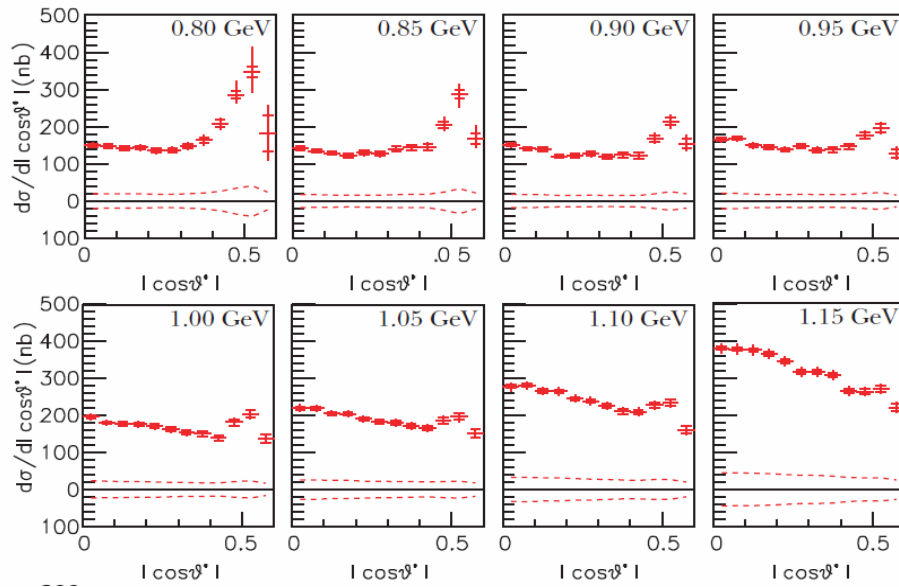


# Differential cross section

$d\sigma/d|\cos \theta^*|$  (nb)



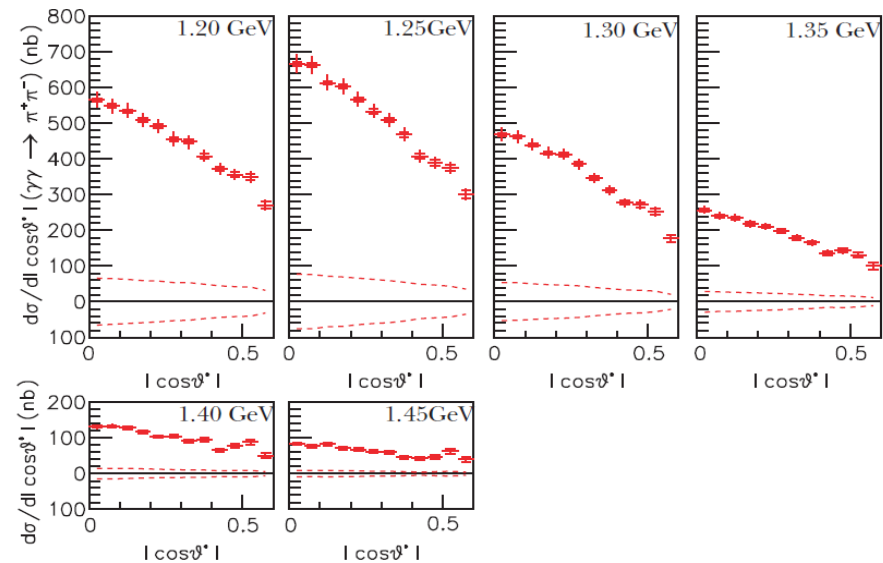
# Angular dependences at some energy points



Red dashed lines ---

Size of point-to-point systematic error

Systematic structure near  $|\cos \theta^*|=0.45-0.55$   
could be due to a measurement bias



# Fitting formula for $f_0(980)$

$$\sigma = \left| \frac{\sqrt{4.8\pi\beta_\pi}}{W} \mathcal{F}^{f_0} e^{i\varphi} + \sqrt{\sigma_0^{\text{BG}}} \right|^2 + \sigma^{\text{BG}} - \sigma_0^{\text{BG}}, \quad (1)$$

where the factor 4.8 includes the fiducial angular acceptance  $|\cos\theta^*| < 0.6$ ,  $\beta_X = \sqrt{1 - \frac{4M_X^2}{W^2}}$  is the velocity of the particles  $X$  with mass  $M_X$  in the two-body final states,  $\mathcal{F}^{f_0}$  is the amplitude of the  $f_0(980)$  meson, which interferes with the helicity-0-background amplitude  $\sqrt{\sigma_0^{\text{BG}}}$  with relative phase  $\varphi$ , and  $\sigma^{\text{BG}}$  is the total background cross section. The amplitude  $\mathcal{F}^{f_0}$  can be written as

$$\mathcal{F}^{f_0} = \frac{g_{f_0\gamma\gamma} g_{f_0\pi\pi}}{16\pi} \cdot \frac{1}{D_{f_0}}, \quad (2)$$

where  $g_{f_0XX}$  is related to the partial width of the  $f_0(980)$  meson via  $\Gamma_{XX}(f_0) = \frac{\beta_X g_{f_0XX}^2}{16\pi M_{f_0}}$ . The factor  $D_{f_0}$  is given as follows [16]:

$$D_{f_0}(W) = M_{f_0}^2 - W^2 + \Re\Pi_\pi^{f_0}(M_{f_0}) - \Pi_\pi^{f_0}(W) \\ + \Re\Pi_K^{f_0}(M_{f_0}) - \Pi_K^{f_0}(W),$$

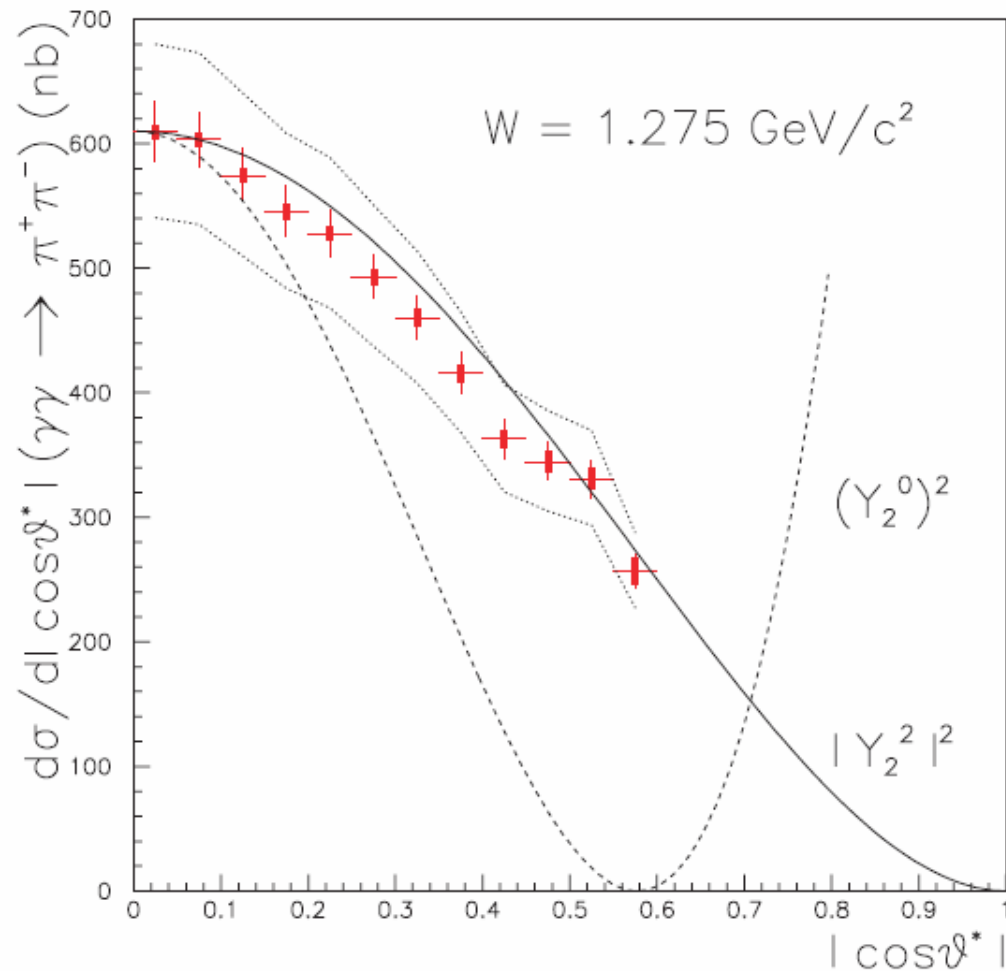
where for  $X = \pi$  or  $K$ ,

$$\Pi_X^{f_0}(W) = \frac{\beta_X g_{f_0XX}^2}{16\pi} \left[ i + \frac{1}{\pi} \ln \frac{1 - \beta_X}{1 + \beta_X} \right]. \quad (3)$$

The factor  $\beta_K$  is real in the region  $W \geq 2M_K$  and becomes imaginary for  $W < 2M_K$ . The mass difference between  $K^\pm$  and  $K^0$  ( $\overline{K^0}$ ) is included by using  $\beta_K = \frac{1}{2}(\beta_{K^\pm} + \beta_{K^0})$ .



# Angular dependence in $f_2(1270)$ region



Close to  $|Y_2^2|^2$

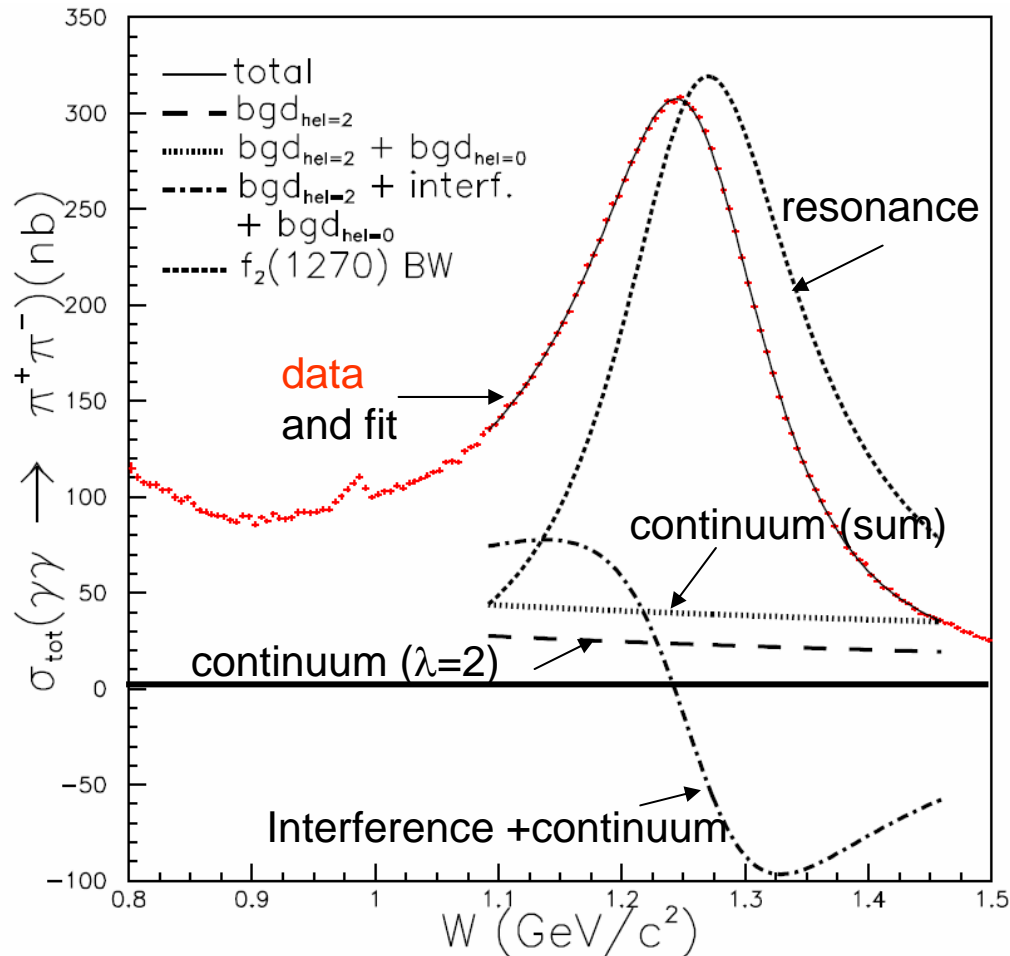
Consistent with  
pure  $J=2$  and  $\lambda=2$

But, mathematically  
the partial waves cannot be  
fully separated taking into  
account the interference  
between  $J=0$  and  $2$ .





# Fit to $f_2(1270)$ line shape



Components:

$f_2(1270)$  resonance

Smooth continuum:

Interfering component ( $l=2$ )

No-interfering component ( $l=0$ )

This is for consistency check:  
Known mass and width of  
 $f_2(1270)$  (PDG2006) are used.

The continuum and relative phase  
parameters etc. were floated.



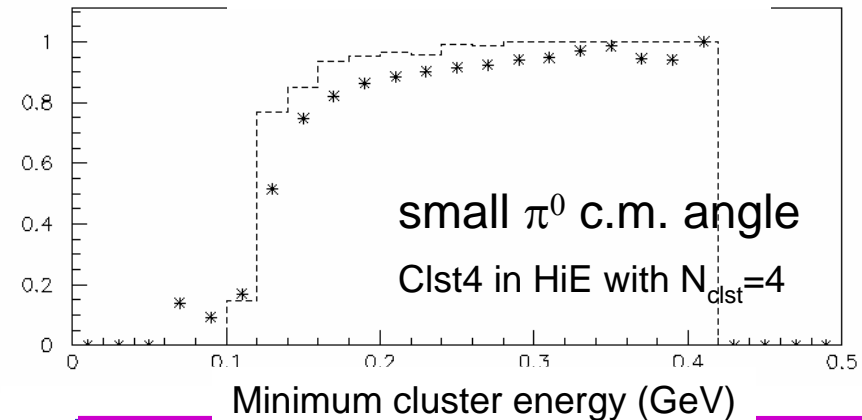
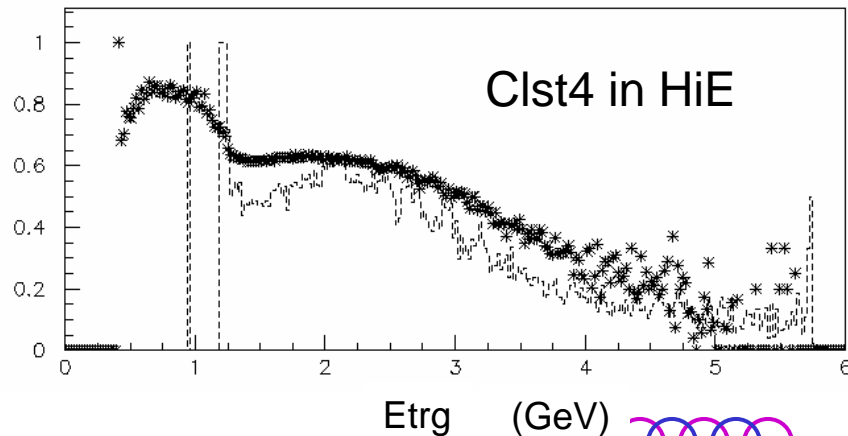
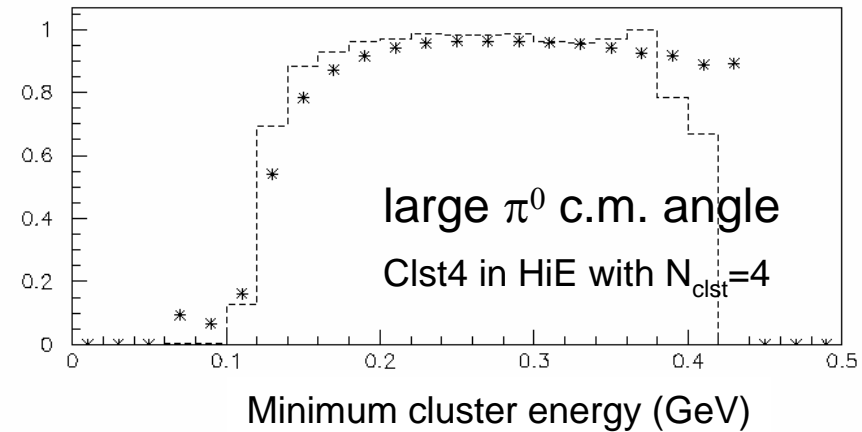
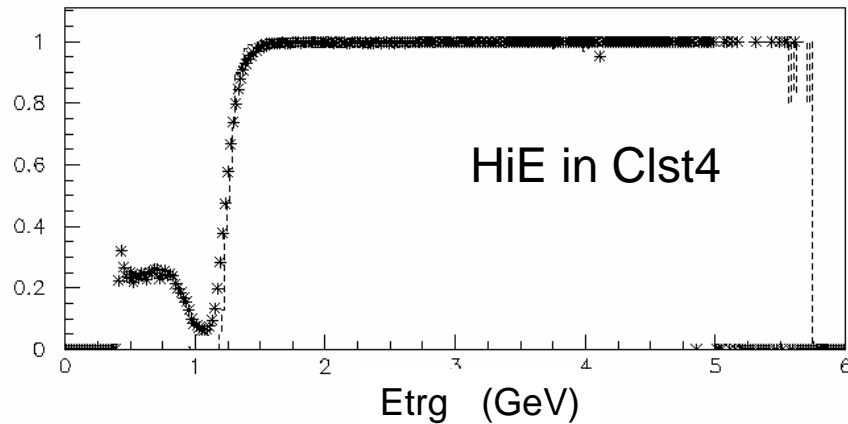
# Trigger efficiency study

Correlation between the two triggers:

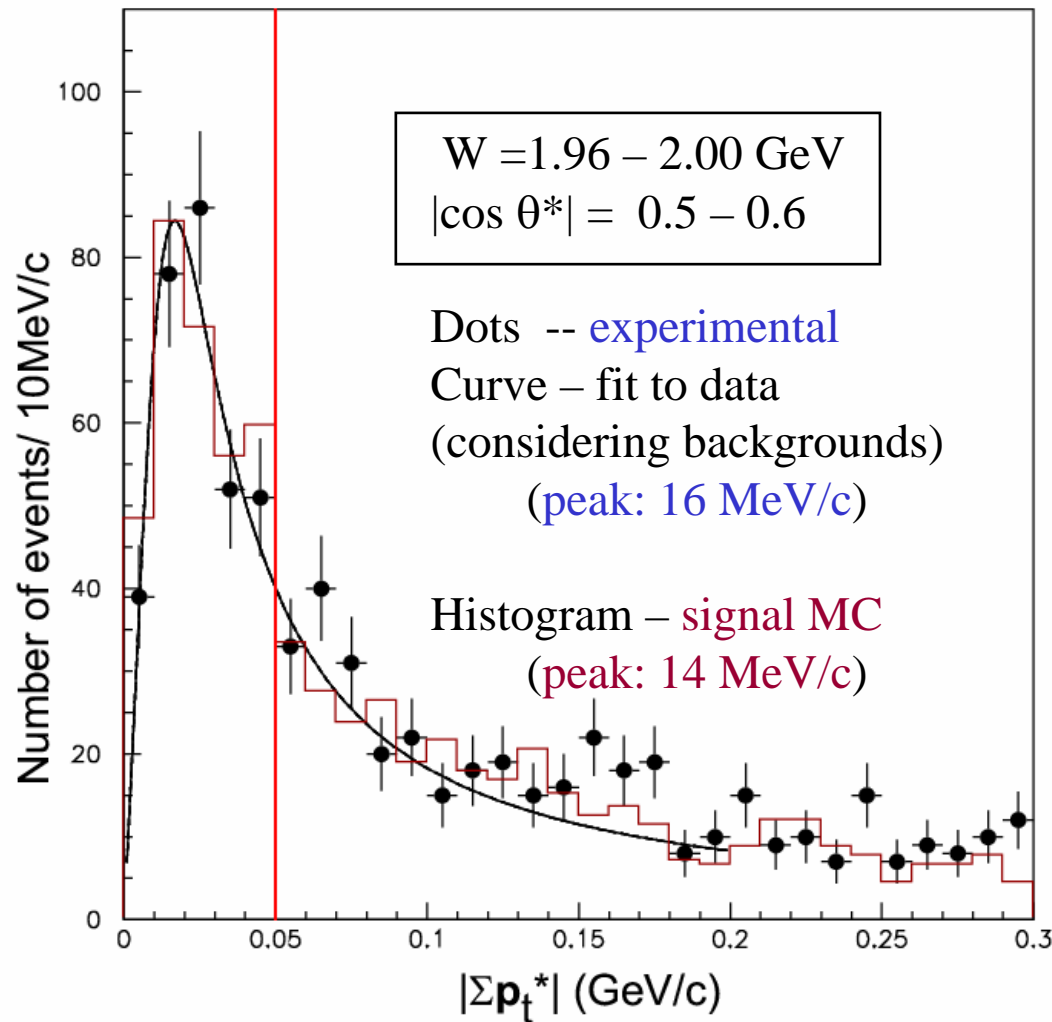
**HiE** ( $E_{\text{tot\_trg}} > 1.15 \text{ GeV}$ ), **Clst4** ( $\geq 4$  clusters each with  $> 110 \text{ MeV}$ )

(The thresholds have been tuned.)

\* -- data,      dashed histogram – trigger simulator (tsim)



# $p_t$ -balance resolution and correction to efficiency



the  $p_t$ -balance cut

Efficiency is affected by  
 $p_t$ -balance resolution.

The resolution in the experimental  
data is by ~15% worse than the MC.

Correction factor: 5% - 10%,  
depending on W and  $|\cos \theta^*|$

