



# Transversity Measurements at COMPASS



Christian Schill  
Universität Freiburg

On behalf of the COMPASS Collaboration

- Transverse spin physics
- COMPASS results on asymmetries
  - Transversity distribution function
  - Sivers distribution function
- Conclusions and outlook – GPDs

new COMPASS result  
for leading hadron-pairs

new COMPASS result  
for exclusive  $\rho$  production

Photon 2007, Paris, July 11



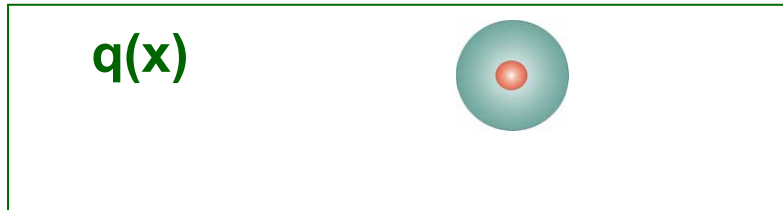
bmb+f - Förderschwerpunkt

COMPASS

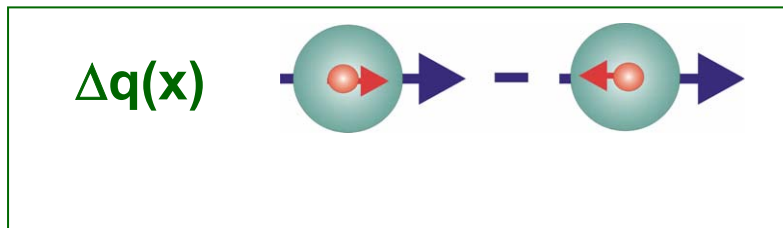
Großgeräte der physikalischen  
Grundlagenforschung

# Transverse Spin Physics

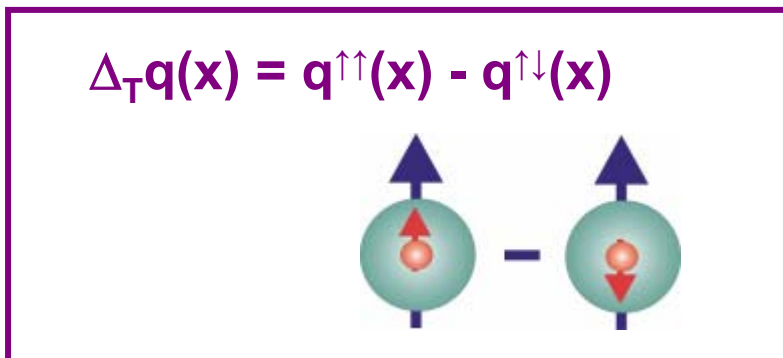
3 distribution functions are necessary to describe the spin structure of the nucleon at LO:



**momentum distribution**  
well known - unpolarized DIS



**helicity distribution**  
known - polarized DIS



**transversity distribution**  
still unknown

$\Delta_T q(x)$  decouples from inclusive DIS:  
helicity flip of quark  
→ SIDIS experiment

# Transversity: How to measure it in SIDIS?

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Transversity  $\Delta_{Tq}(x)$  chiral odd: observable effect only in combination with chiral odd **fragmentation function**

## Suggested quark polarimeters in SIDIS:

- Azimuthal distribution of single hadrons  
**Collins fragmentation function**
- Azimuthal dependence of the plane containing a hadron pair  
**2-hadron interference fragmentation function**
- Measure transverse polarization of  $\Lambda$   
**fragmentation function  $q \rightarrow \Lambda$**

# Transversity Data Sample

**transversely polarized deuteron target**  
**~ 20% of the running time**

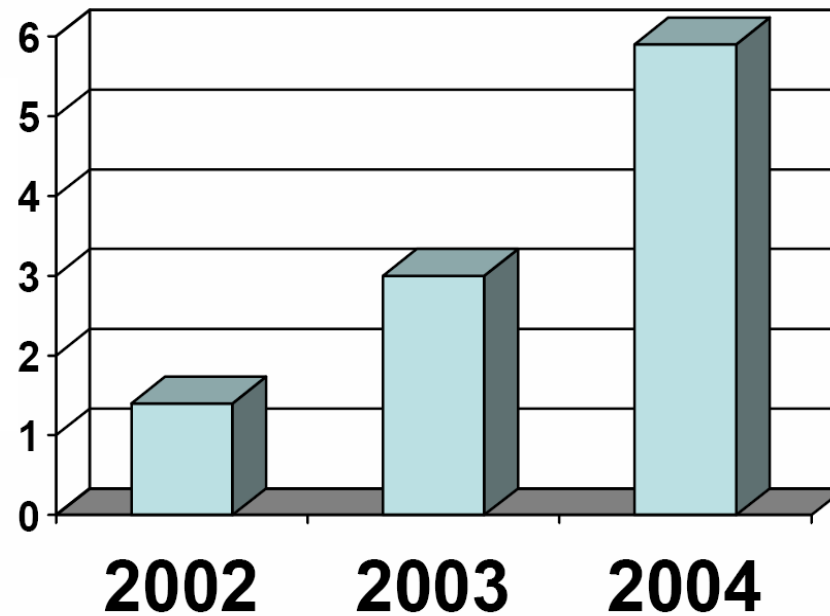
**2002** 11 days of data taking

**2003** 9 days of data taking

**2004** 14 days of data taking

trigger (large  $x$ ,  $Q^2$ )  
+ PID (ECAL, RICH)

reconstructed  
DIS events  
( $10^6$ )



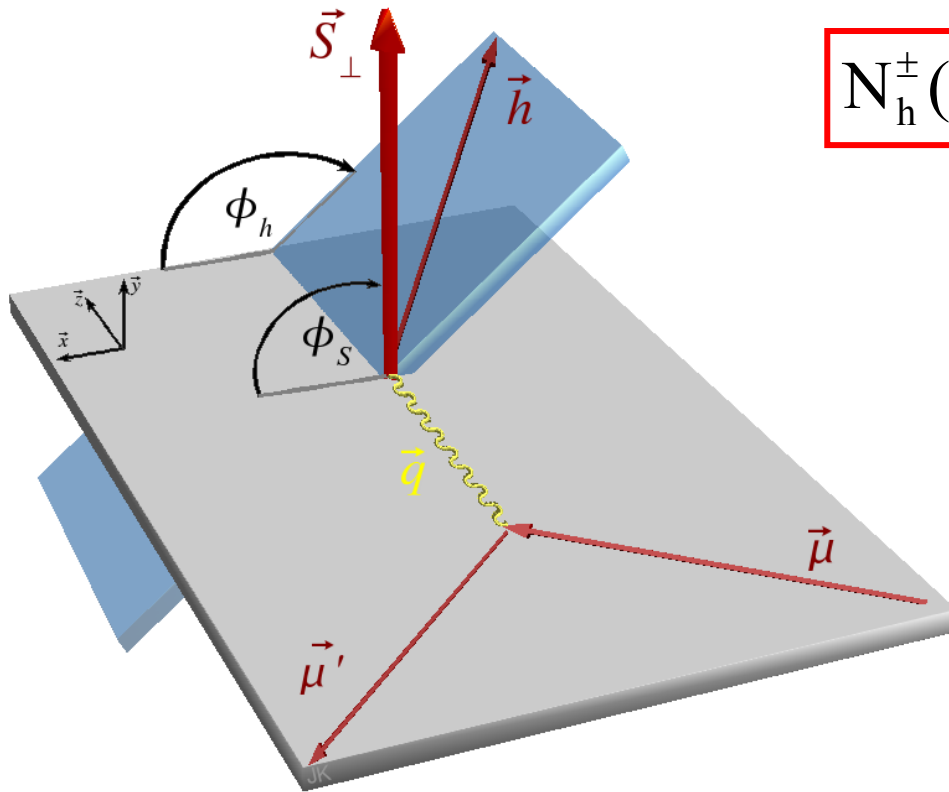
10 Mill.  
DIS events

# Collins Asymmetry

SIDIS on a transversely polarized target:  $I N^\uparrow \rightarrow I' h X$

Fragmentation of a transversely polarized quarks into hadrons

→ azimuthal asymmetry:



$$N_h^\pm(\Phi_{\text{Coll}}) = N_h^0 \{1 \pm A_C^h \cdot \sin \Phi_{\text{Coll}}\}$$

In SIDIS, the Collins angle  $\Phi_{\text{Coll}}$  is defined as:

$$\Phi_{\text{Coll}} = \phi_h + \phi_S - \pi$$

# Collins Asymmetry

The measured asymmetry  $A_{\text{Coll}}$  gives access to the transversity distribution times the Collins fragmentation function:

$$A_{\text{Coll}} = \frac{A_C^h}{f P_T D_{\text{nn}}} = \frac{\sum_q e_q^2 \Delta_T q(x) \cdot \Delta_T^0 D_q^h}{\sum_q e_q^2 q(x) \cdot D_q^h}$$

$f$ : Dilution factor  $\approx 0.38$   
 $D_{\text{nn}}$ : Depolarization factor  
 $D_{\text{nn}} = 2(1-y)/(1+(1-y)^2)$   
 $P_T$ : Target polarization  $\approx 0.5$

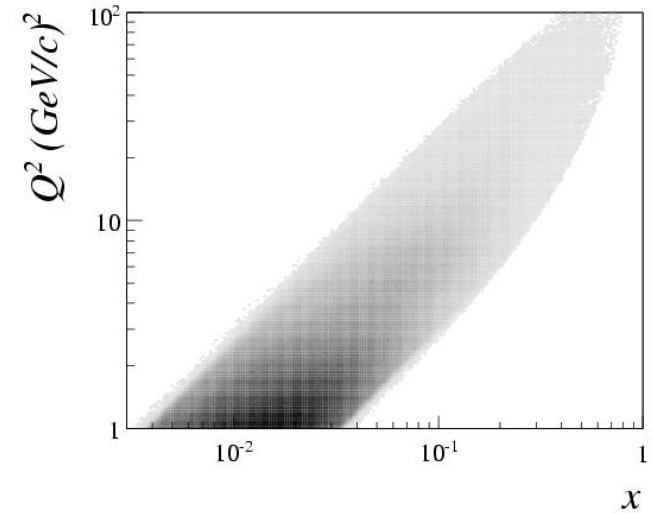
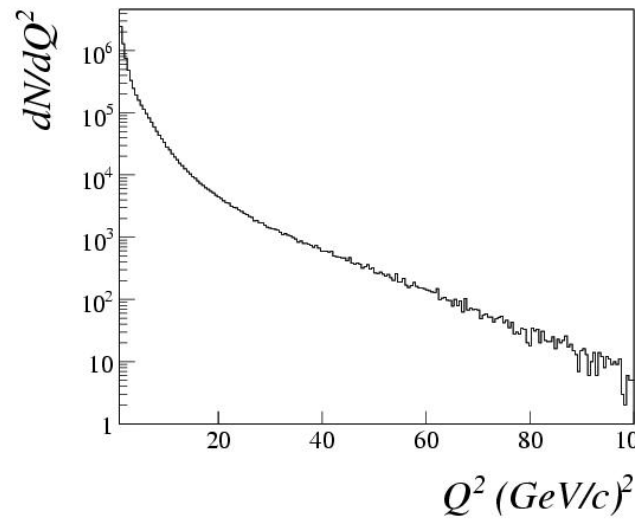
$\Delta_T q(x)$ : Transversity distribution

$\Delta_T^0 D_q^h$ : Collins fragmentation function (measured in  $e^+e^-$  at BELLE)

# Selection of SIDIS Events

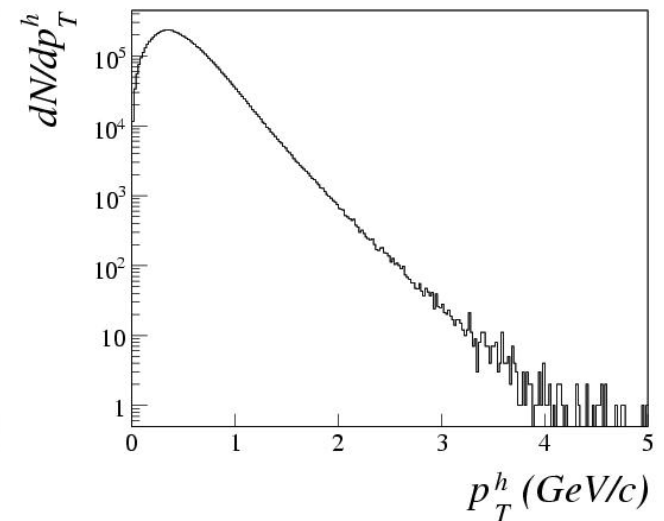
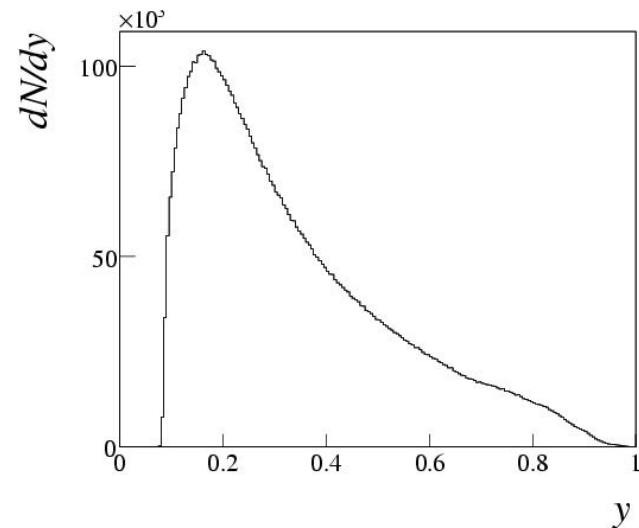
## DIS cuts:

- $Q^2 > 1 \text{ (GeV/c)}^2$
- $0.1 < y < 0.9$
- $W > 5 \text{ GeV/c}^2$



## hadron selection:

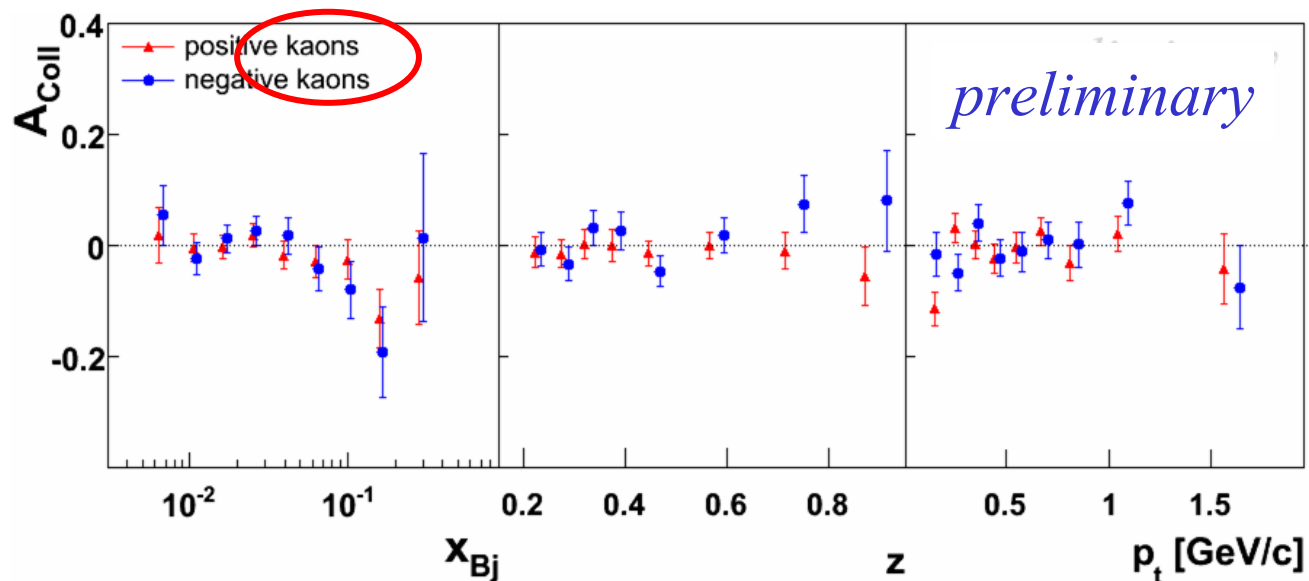
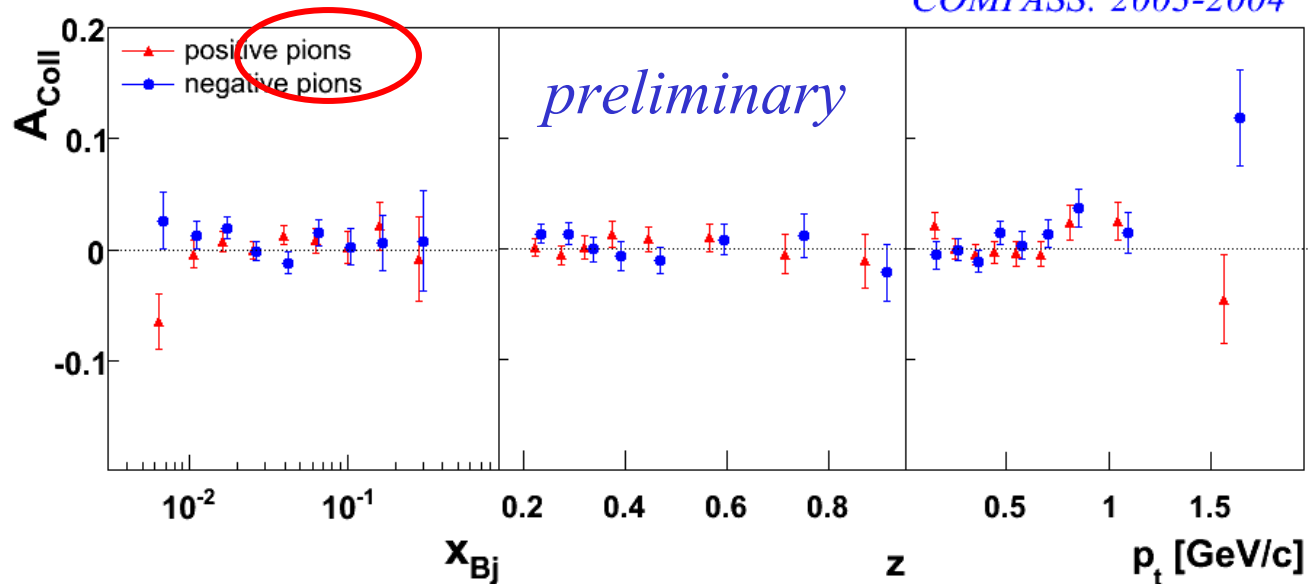
- $z > 0.2$
- $p_t > 0.1 \text{ GeV/c}$



# COMPASS Results: Collins Effect

Deuteron target

COMPASS: 2003-2004



only statistical errors shown (systematical errors considerably smaller)



# Interpretation

- naive interpretation: parton model, valence region:

$$A_{\text{Coll}}^{\text{d},\pi^+}(\mathbf{x}) \cong \frac{\Delta_{\text{T}}u_{\text{v}}(\mathbf{x}) + \Delta_{\text{T}}d_{\text{v}}(\mathbf{x})}{u_{\text{v}}(\mathbf{x}) + d_{\text{v}}(\mathbf{x})} \cdot \frac{4\Delta_{\text{T}}^0D_1 + \Delta_{\text{T}}^0D_2}{4D_1 + D_2}$$

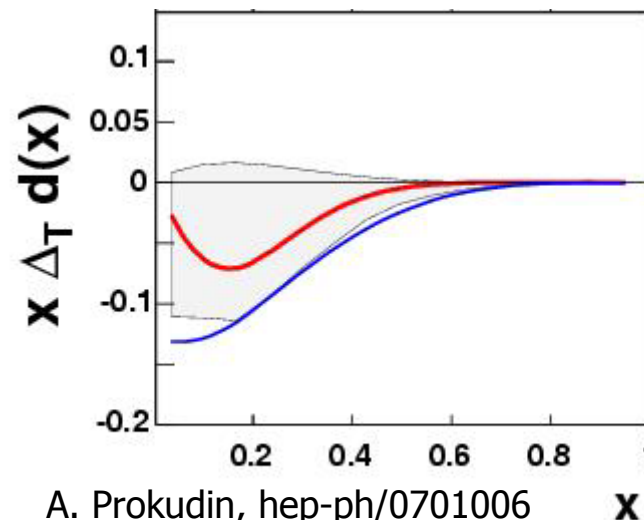
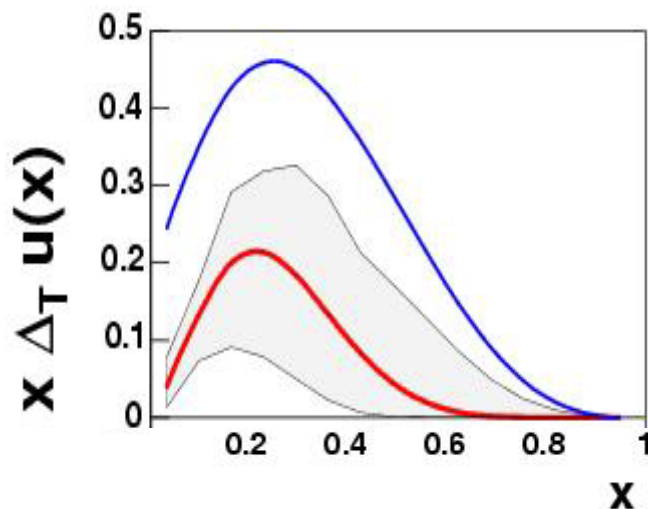
isospin-symmetric  
deuteron target

$$A_{\text{Coll}}^{\text{d},\pi^-}(\mathbf{x}) \cong \frac{\Delta_{\text{T}}u_{\text{v}}(\mathbf{x}) + \Delta_{\text{T}}d_{\text{v}}(\mathbf{x})}{u_{\text{v}}(\mathbf{x}) + d_{\text{v}}(\mathbf{x})} \cdot \frac{\Delta_{\text{T}}^0D_1 + 4\Delta_{\text{T}}^0D_2}{D_1 + 4D_2}$$

$D_1$ : favored FF  
 $D_2$ : disfavored FF

Small asymmetries  $\rightarrow$  cancellation between  $\Delta_{\text{T}}u(x)$  and  $\Delta_{\text{T}}d(x)$

- Extraction of transversity distribution from COMPASS (deuteron), HERMES (proton) and BELLE (Collins FF) data:



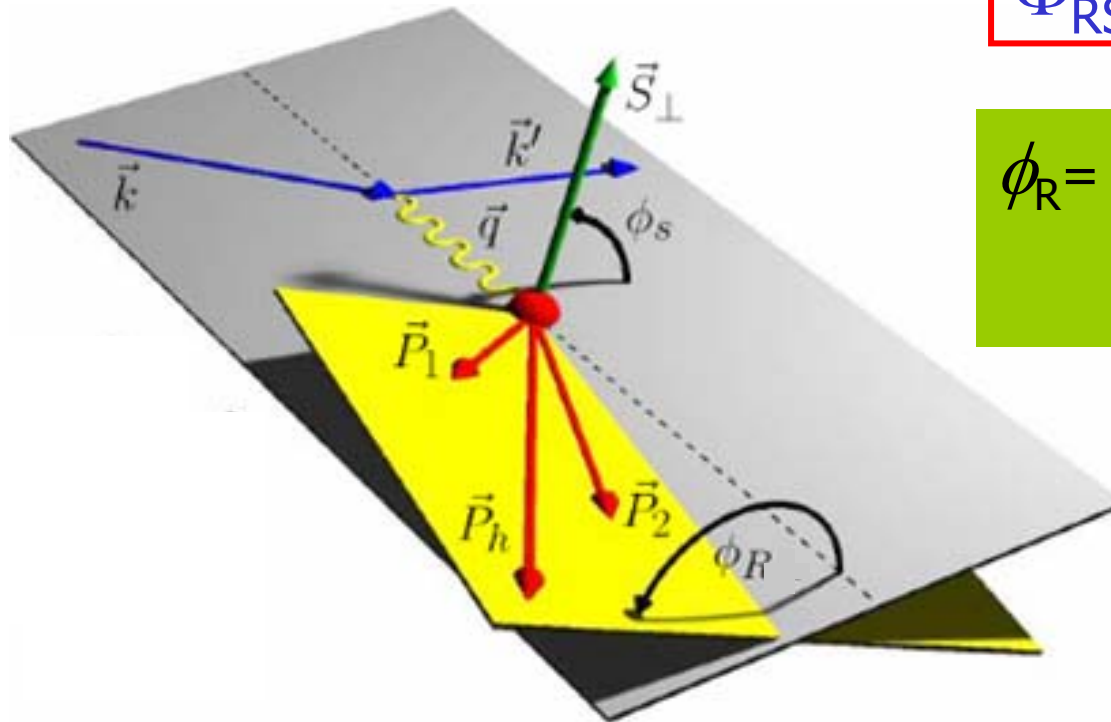
— Soffer bound  
— fit to  
COMPASS,  
HERMES,  
BELLE

# Transversity in Hadron-Pair Production

Collins-Angle replaced by:

$$\Phi_{RS} = \phi_R + \phi_S - \pi$$

$\phi_R$  = angle between lepton scattering plane and two-hadron plane



(A. Bacchetta, M. Radici, hep-ph/0407345)

(X. Artru, hep-ph/0207309)

# Azimuthal Asymmetry for Hadron-Pair Production

Target single spin asymmetry  $A_{RS}(x, z, M_h^2)$ :

$$z = z_1 + z_2$$

$$A_{RS}(x, z, M_h^2) = \frac{1}{fP_T D} \cdot \frac{\sum_q e_q^2 \Delta_T q(x) H_q^{\angle h}(z, M_h^2)}{\sum_q e_q^2 q(x) D_q^h(z, M_h^2)}$$

(X. Artru, hep-ph/0207309)

$H_q^{\angle h}(z, M_h^2)$ : Two-hadron interference fragmentation function

$D_q^h, H_q^{\angle h}$



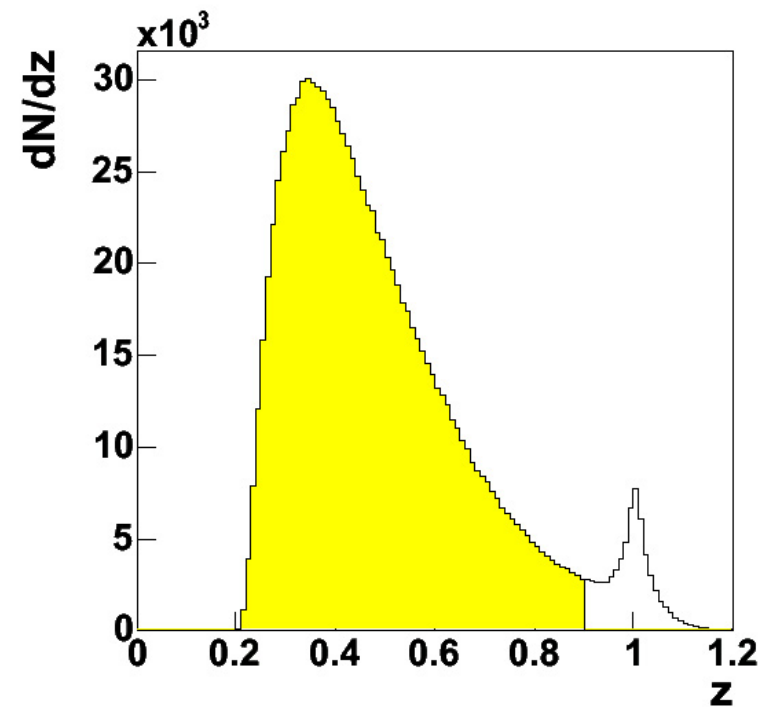
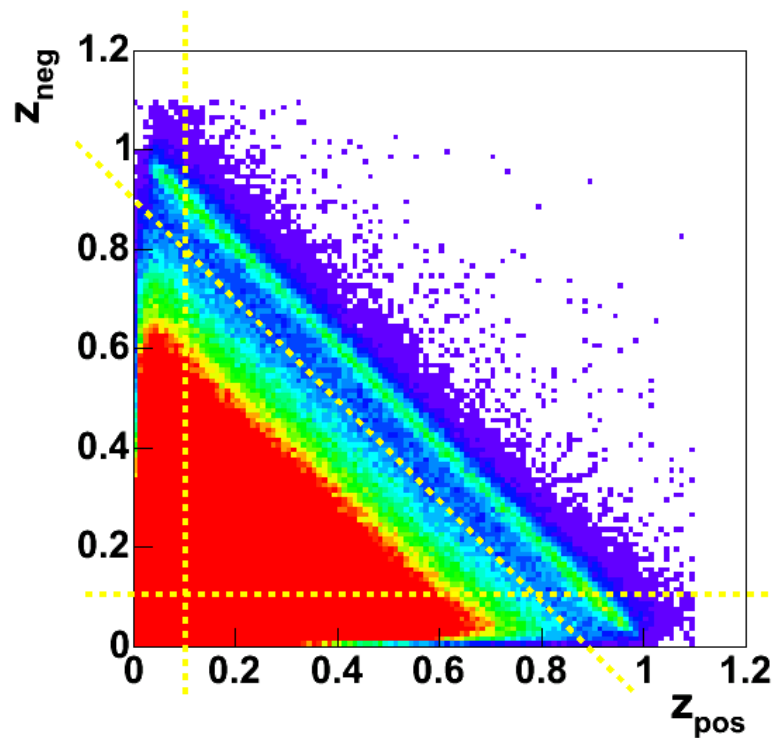
presently unknown  
can be measured  
in  $e^+e^-$  (BELLE)

expected to depend on the hadron  
pair invariant mass

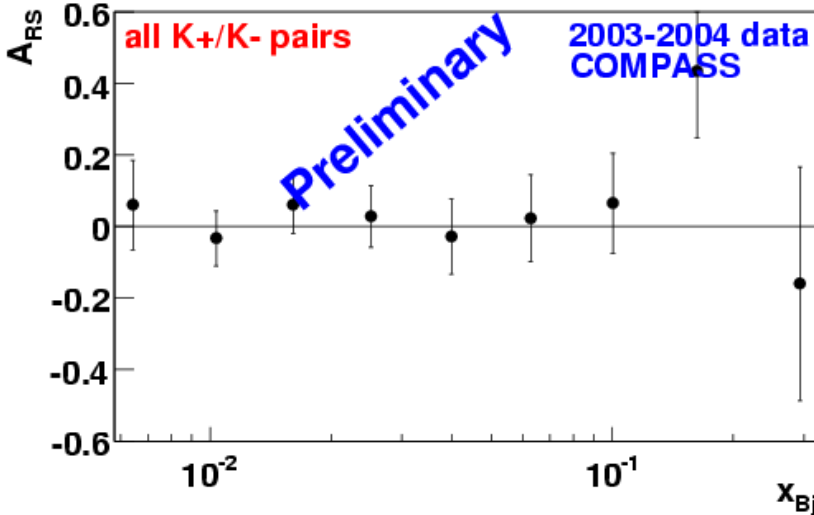
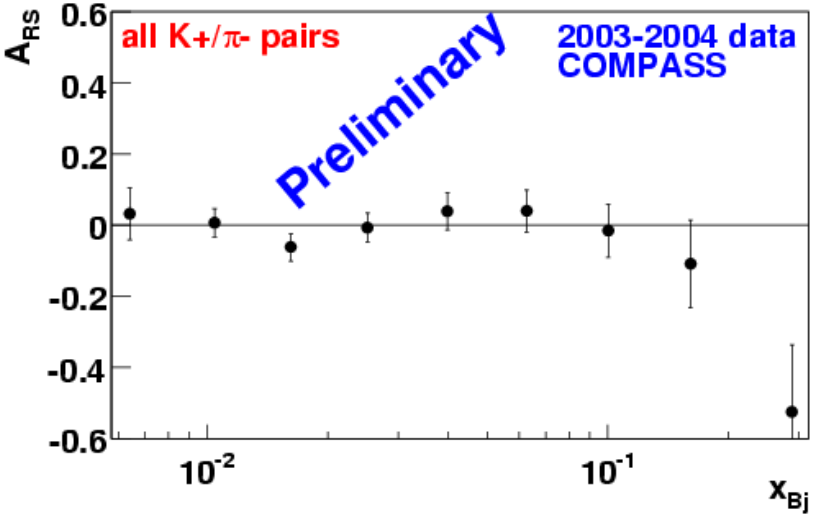
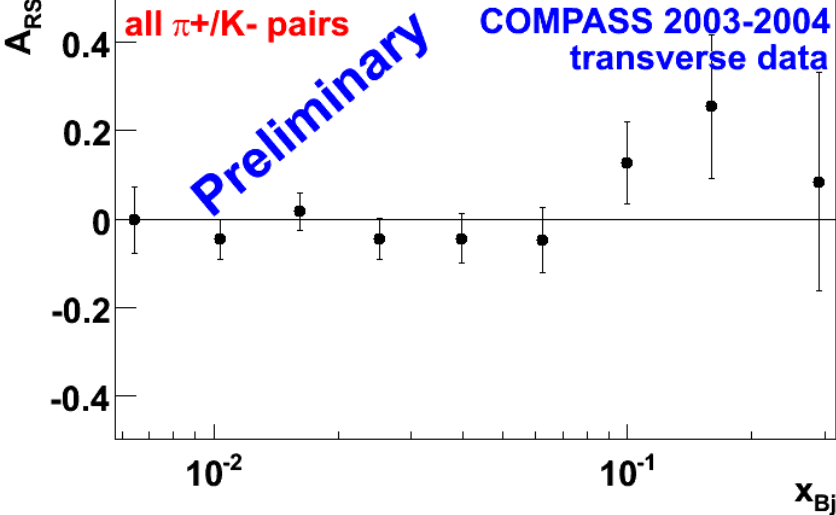
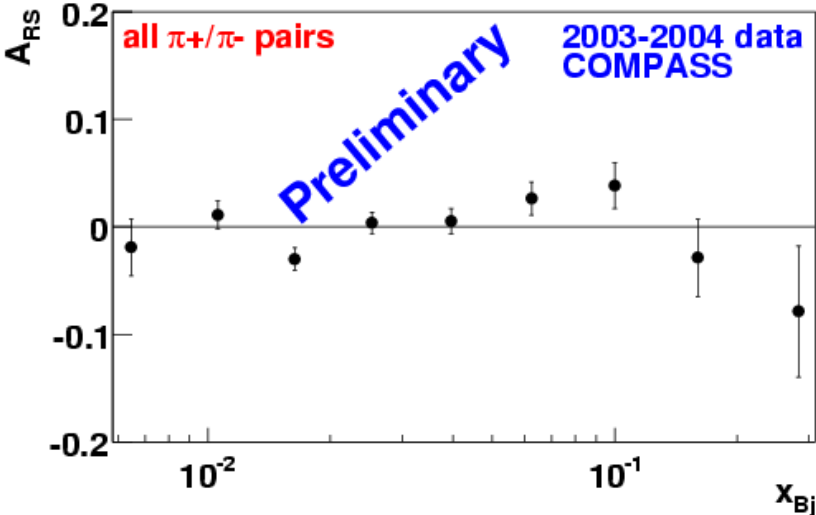
# Event Selection

## Hadron pair selection:

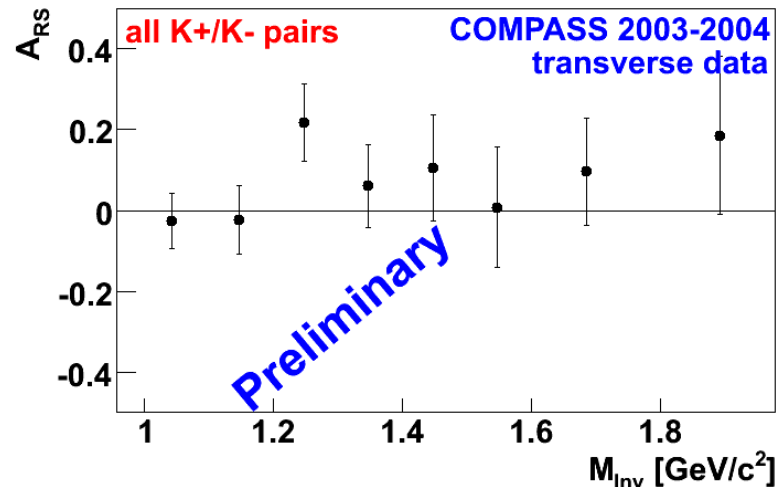
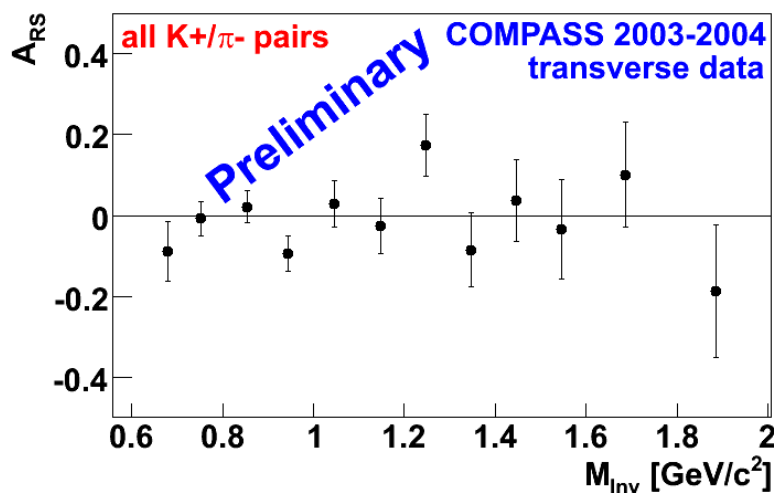
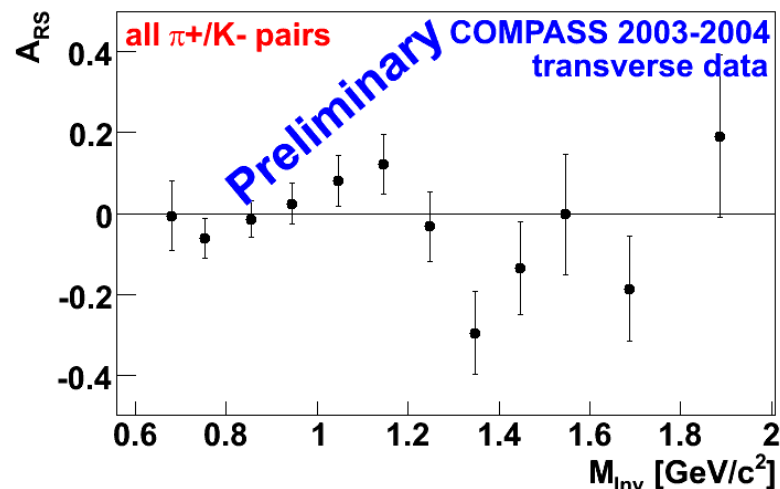
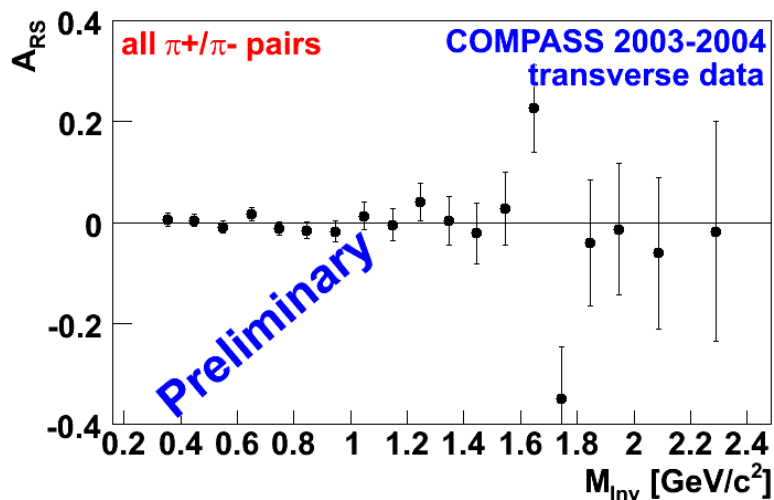
- $z_{1,2} > 0.1$  (current fragmentation)
- $x_{F1,2} > 0.1$
- $z_1 + z_2 < 0.9$  (exclusive meson production)
- RICH identification of  $\pi$ ,  $K$



# COMPASS Results for Hadron Pairs



# COMPASS Results for Hadron Pairs



Model calculations suggest  
(A. Bacchetta, M. Radici,  
hep-ph/0608037):

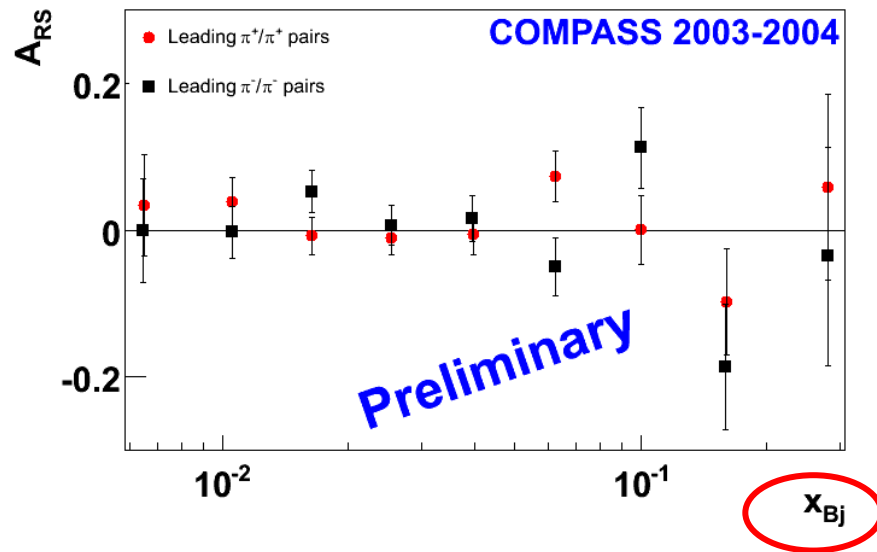
cancellation between  $\Delta_T u_v(x)$  and  $\Delta_T d_v(x)$

# New Results: Leading Hadron Pairs z-ordered

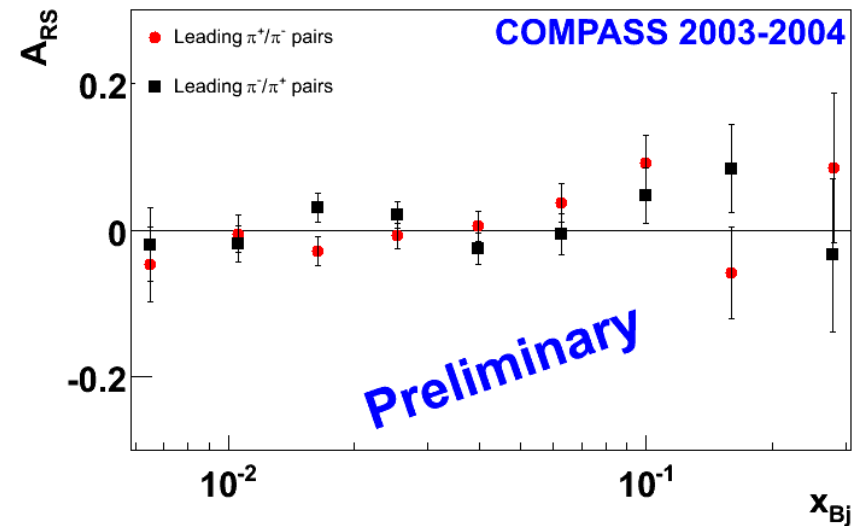
Leading hadrons may carry more information about the fragmenting quark

- z-ordered hadron pairs:  $z_1 > z_2$
- $z = z_1 + z_2 > 0.25$

$h_1$ : leading hadron  
 $h_2$ : sub-leading hadron



$\pi^+ \pi^+$   
 $\pi^- \pi^-$



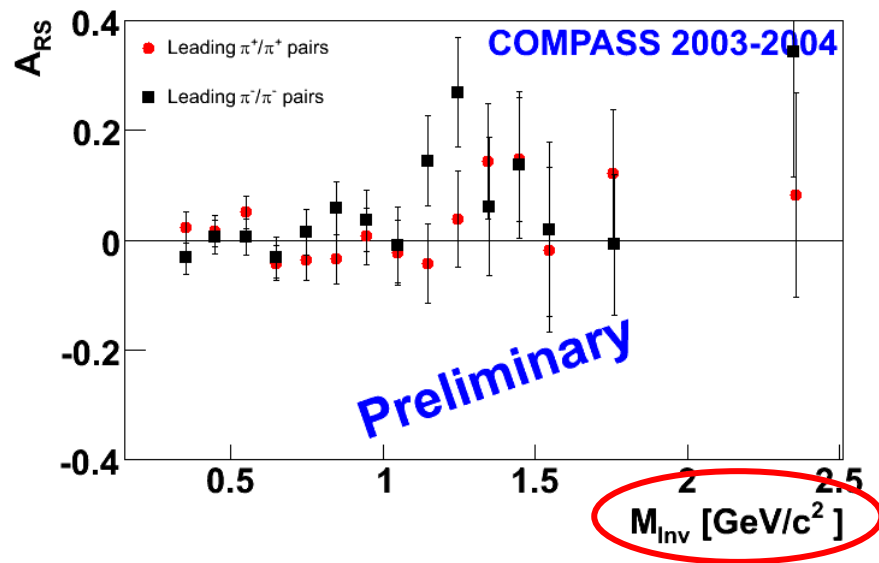
$\pi^+ \pi^-$   
 $\pi^- \pi^+$

# New Results: Leading Hadron Pairs z-ordered

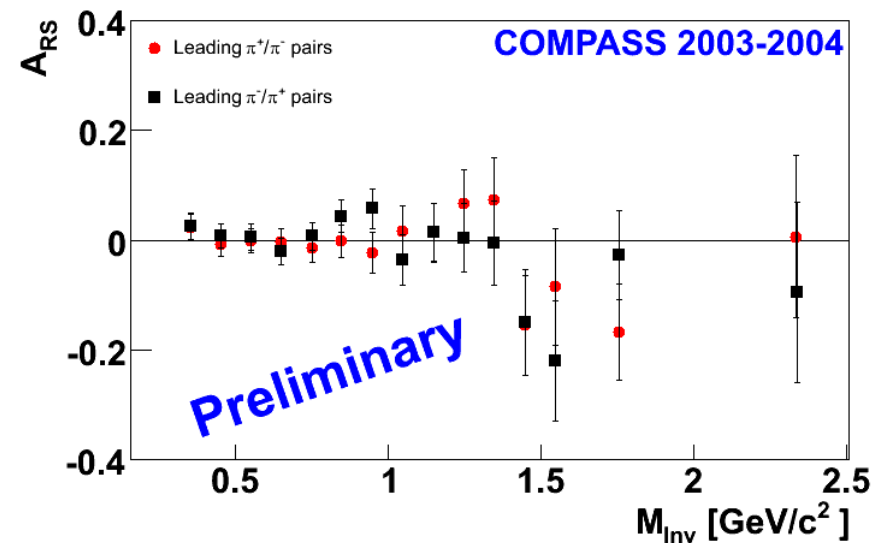
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$h_1$ : leading hadron  
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$\pi^+ \pi^+$   
 $\pi^- \pi^-$



$\pi^+ \pi^-$   
 $\pi^- \pi^+$



# Sivers Effect

- Intrinsic transverse momentum of unpolarized quarks in a transversely polarized nucleon → azimuthal asymmetry

$$N_h^\pm(\Phi_{\text{Siv}}) = N_h^0 \{ 1 \pm A_S^h \cdot \sin \Phi_{\text{Siv}} \}$$

$$\Phi_{\text{Siv}} = \phi_h - \phi_s$$

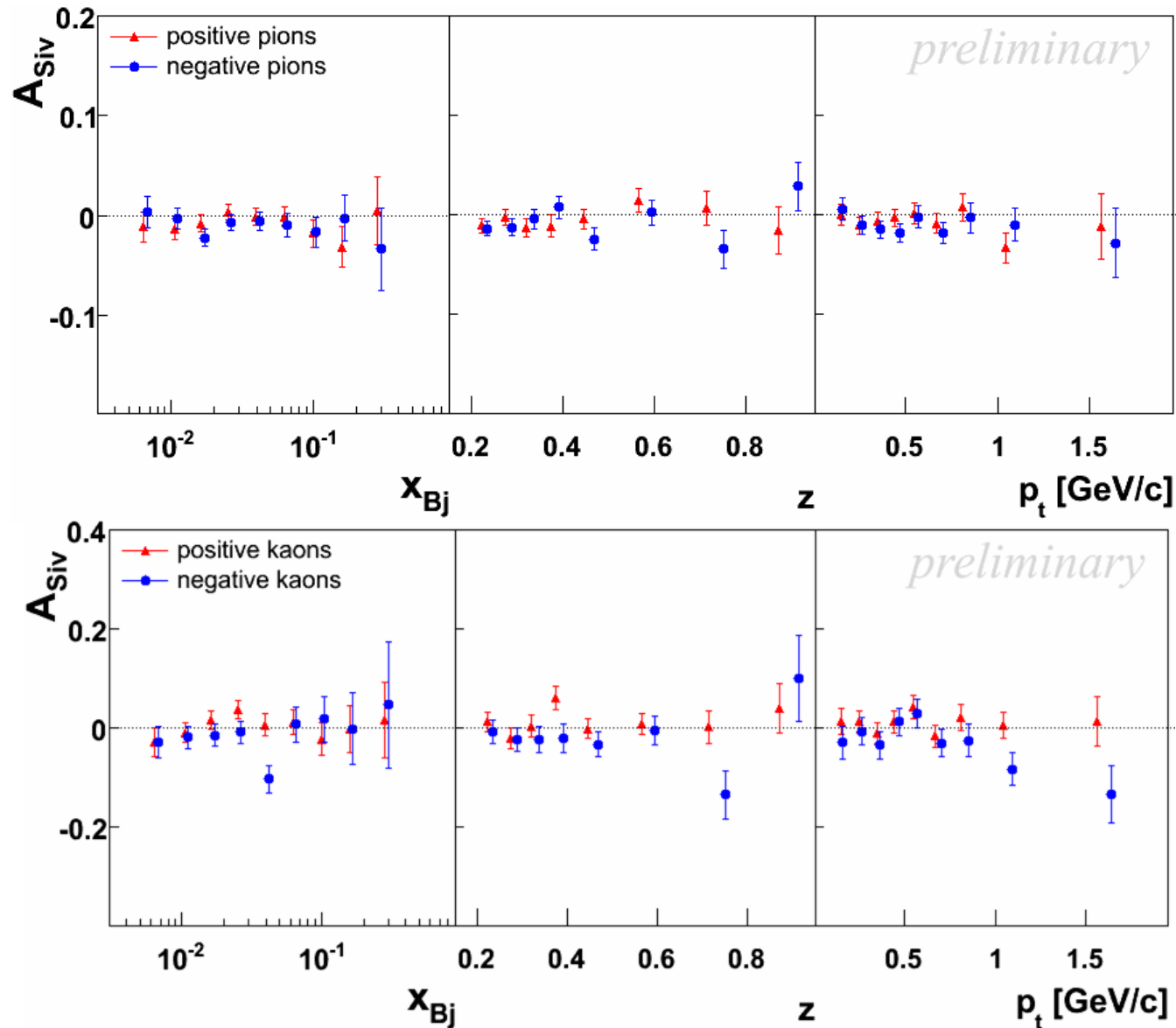
Sivers angle independent of Collins angle:  
measure both in the same data

The Sivers asymmetry:

$$A_{\text{Siv}} = \frac{A_S^h}{f P_T} = \frac{\sum_q e_q^2 \Delta_0^T q(x) \cdot D_q^h}{\sum_q e_q^2 q(x) \cdot D_q^h}$$

$\Delta_0^T q(x)$ : Sivers function

# COMPASS Results: Sivers effect



only statistical errors shown (systematical errors considerably smaller)

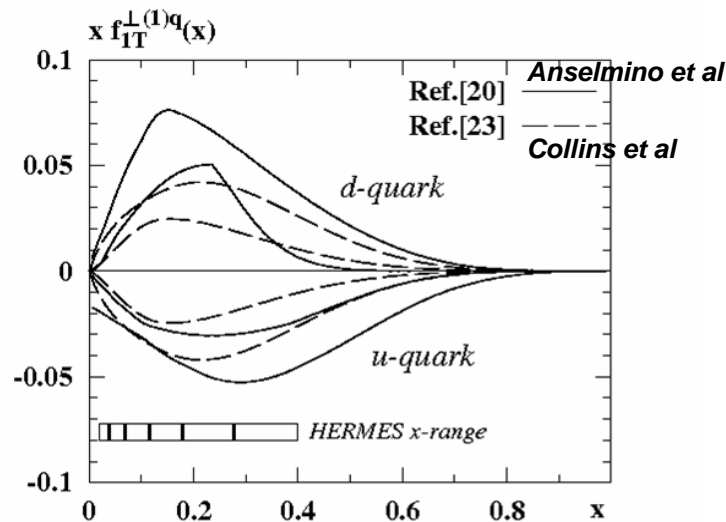
# Interpretation

- naive interpretation: parton model, valence region:

$$A_{\text{Siv}}^{\text{d},\pi^+}(\mathbf{x}) \approx A_{\text{Siv}}^{\text{d},\pi^-}(\mathbf{x}) \approx \frac{\Delta_0^{\text{T}} \mathbf{u}_v(\mathbf{x}) + \Delta_0^{\text{T}} \mathbf{d}_v(\mathbf{x})}{\mathbf{u}_v(\mathbf{x}) + \mathbf{d}_v(\mathbf{x})}$$

Small asymmetries suggest  $\Delta_0^{\text{T}} \mathbf{d}_v(\mathbf{x}) \cong -\Delta_0^{\text{T}} \mathbf{u}_v(\mathbf{x})$

- Data on the proton (HERMES experiment) different from zero, extraction of the Sivers function from COMPASS & HERMES:



Anselmino et al. hep-ph/0511017

# Beyond Collins and Sivers Mechanism

SIDIS cross-section in one-photon exchange approximation:  
**8 transverse target spin dependent azimuthal modulations**

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right.$$

**Sivers**

$$+ |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

**Collins**

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

**6 further modulations**

$$+ \left. \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right.$$

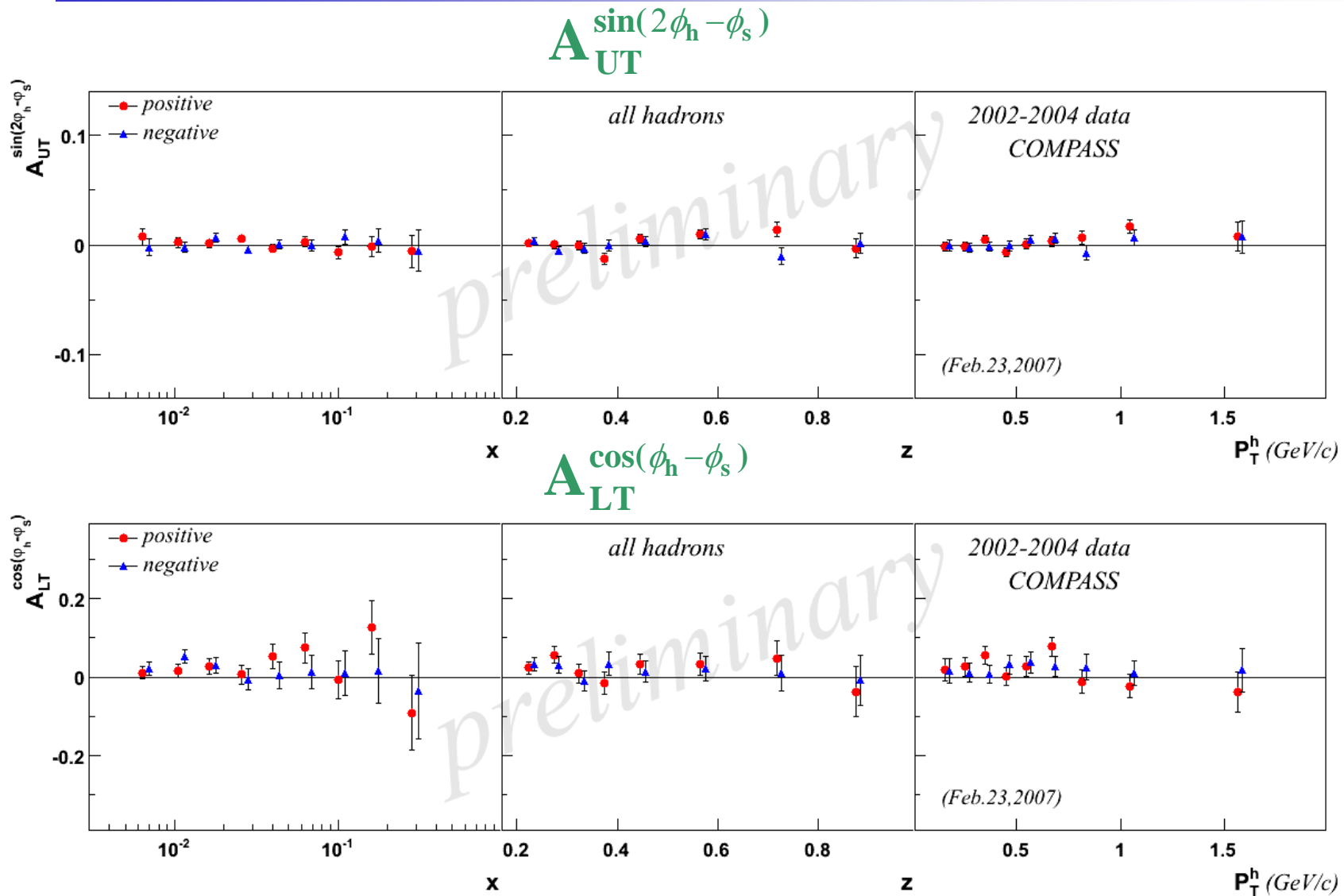
$$+ |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

$\varepsilon$ -photon flux

M. Diehl, S. Sapeta,  
 Eur.Phys.J **C41** (2005) 515-533  
 hep-ph/0503023

# Beyond Collins and Sivers Mechanism



all new asymmetries small and compatible with zero

# Conclusions and Outlook

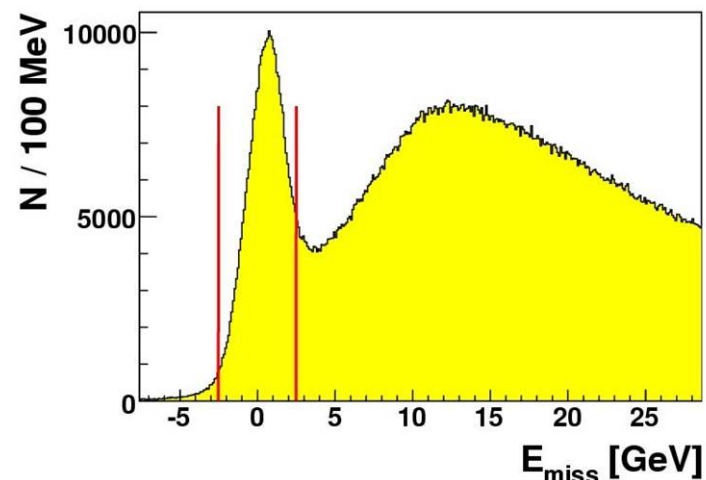
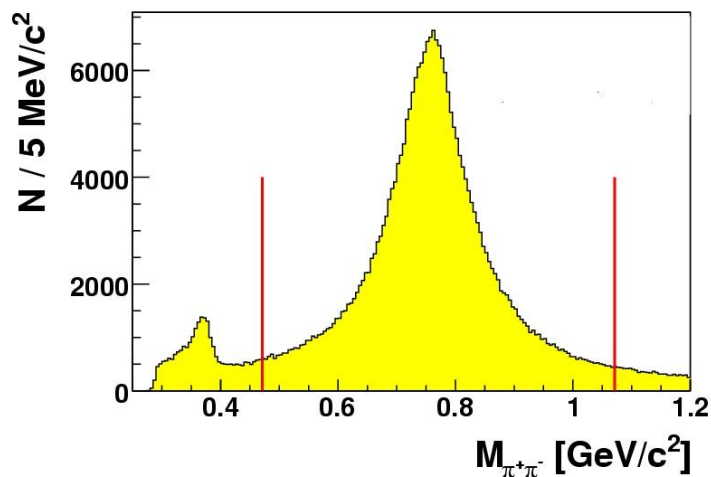
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- Precise COMPASS data for transverse spin asymmetries on the **deuteron**
- Channels investigated so far:
  - **Collins** asymmetries on positive and negative hadrons,  $\pi^\pm$ ,  $K^\pm$
  - **Hadron pair** asymmetries
  - **Sivers** asymmetries
  - **6 new observables** beyond Collins and Sivers
- All measured asymmetries very **small and compatible with zero**
- Combined analysis of **deuteron** (COMPASS) and **proton** (COMPASS/HERMES) data allows extraction of transversity  $\Delta_T q(x)$

## Outlook:

- COMPASS data taking on a transversely polarized **proton** target started in June 2007
- Analysis of single spin asymmetries in **exclusive reactions** to get access to GPDs

# Outlook: SSA for Exclusive Rho Production



Exclusive Rho:

- $Q^2 > 1 \text{ (GeV/c)}^2$
- $0.1 < y < 0.9$
- $W > 5 \text{ GeV/c}$

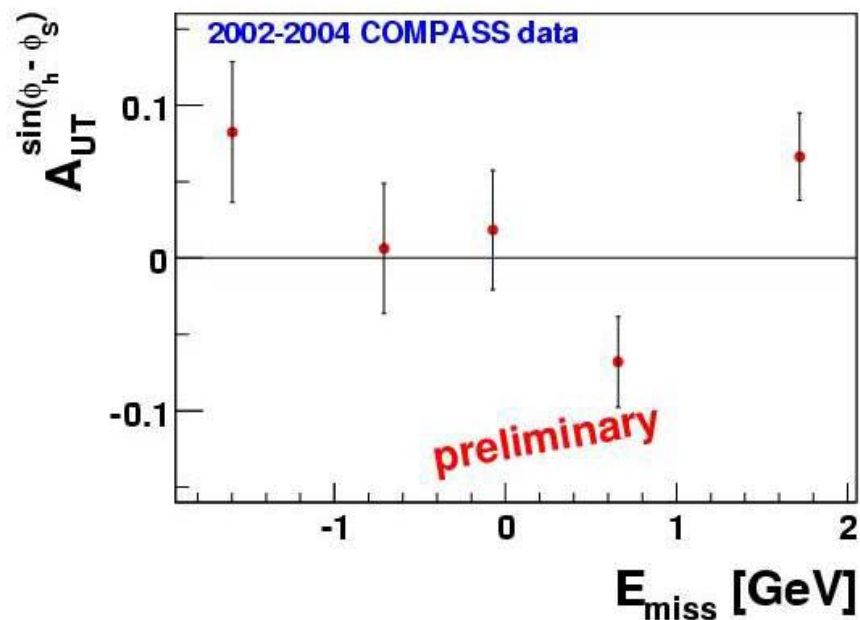
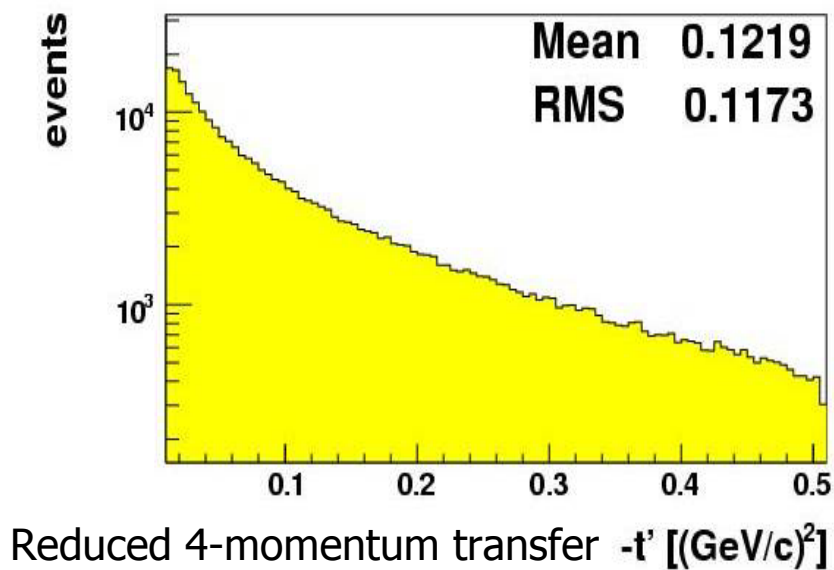
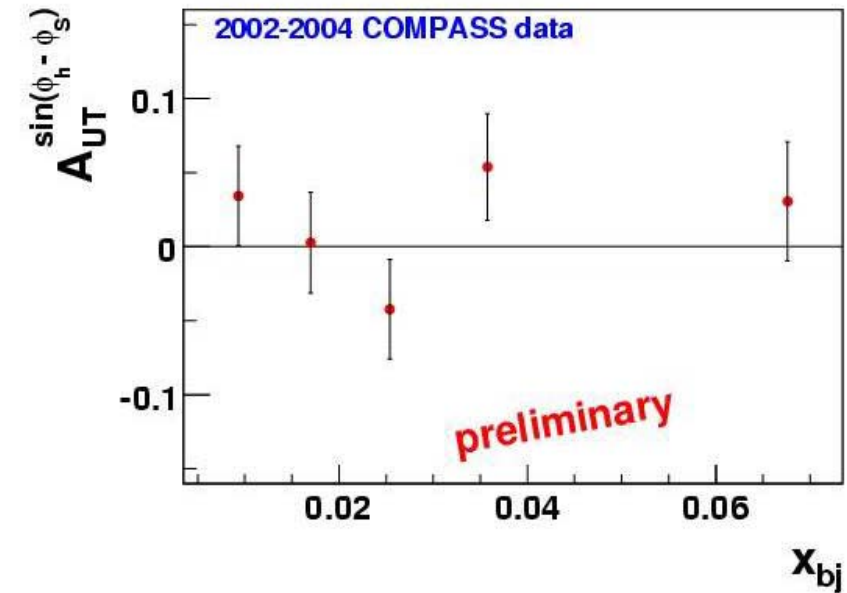
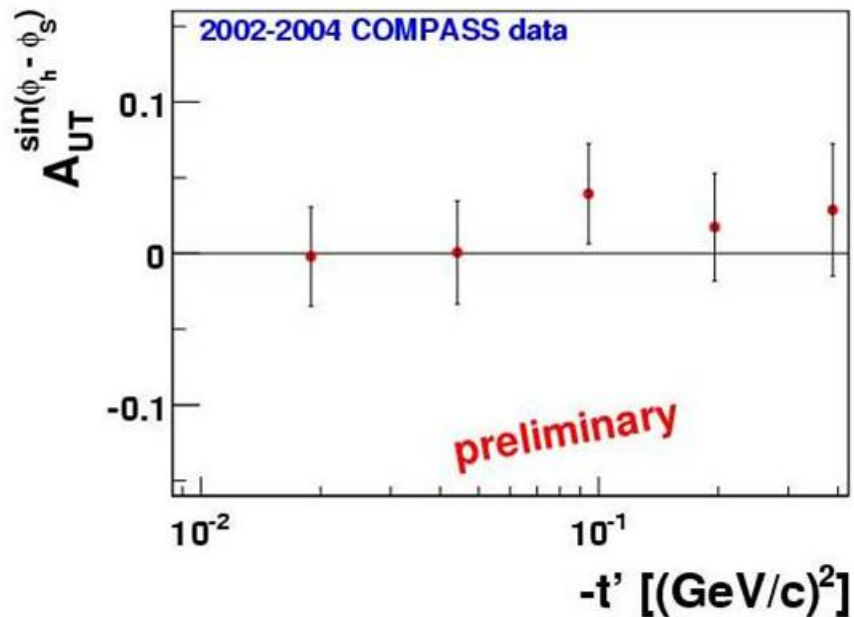
$$\begin{aligned}
 -2.5 \text{ GeV} < E_{\text{miss}} < 2.5 \text{ GeV} \\
 0.01 \text{ (GeV/c)}^2 < p_T^2 < 0.5 \text{ (GeV/c)}^2 \\
 -0.3 \text{ (GeV/c)}^2 < M_{\pi\pi} - M_\rho < 0.3 \text{ (GeV/c)}^2
 \end{aligned}$$

- Exclusive vector meson production on the deuteron sensitive to the GPD H

Berger, Cano, Diehl et al.  
hep-ph/0106192

- GPDs may give access to total angular momentum of quarks in the nucleon

# New Results: SSA for Exclusive Rho Production

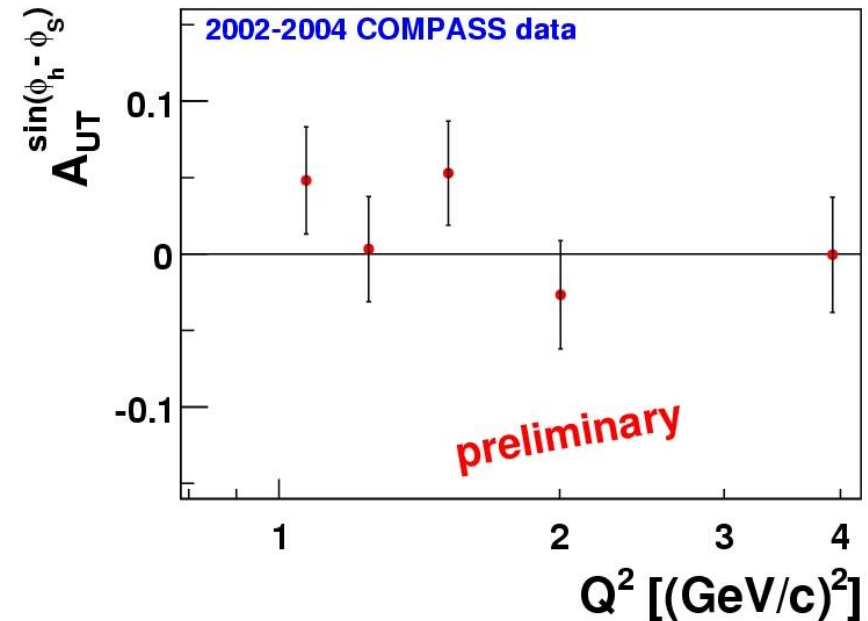
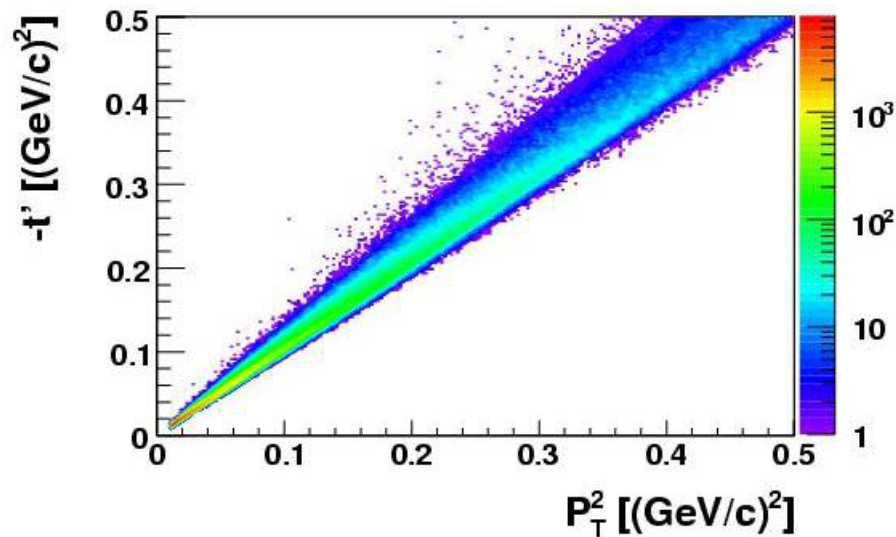
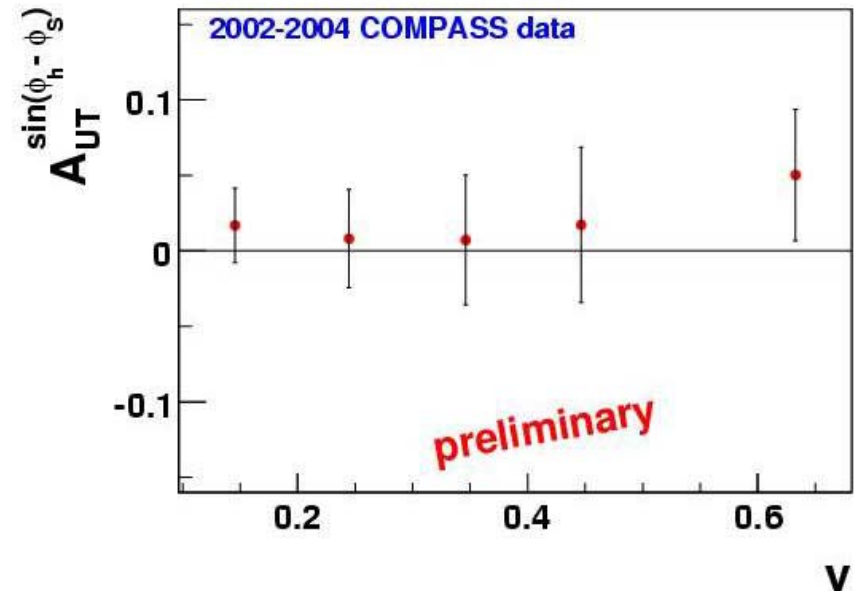
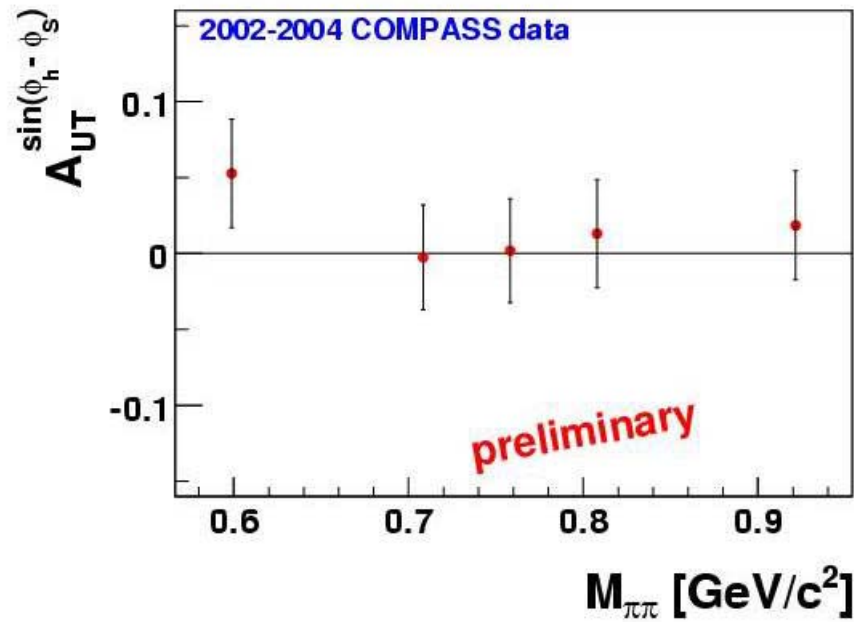




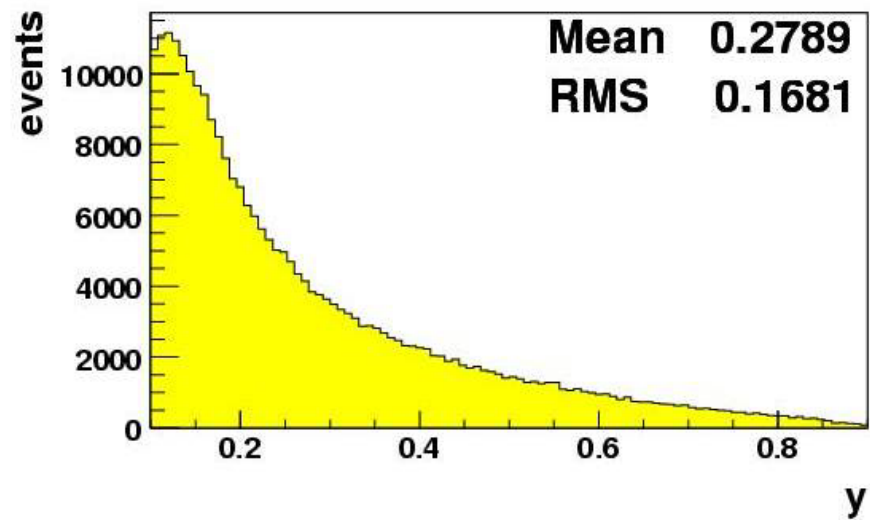
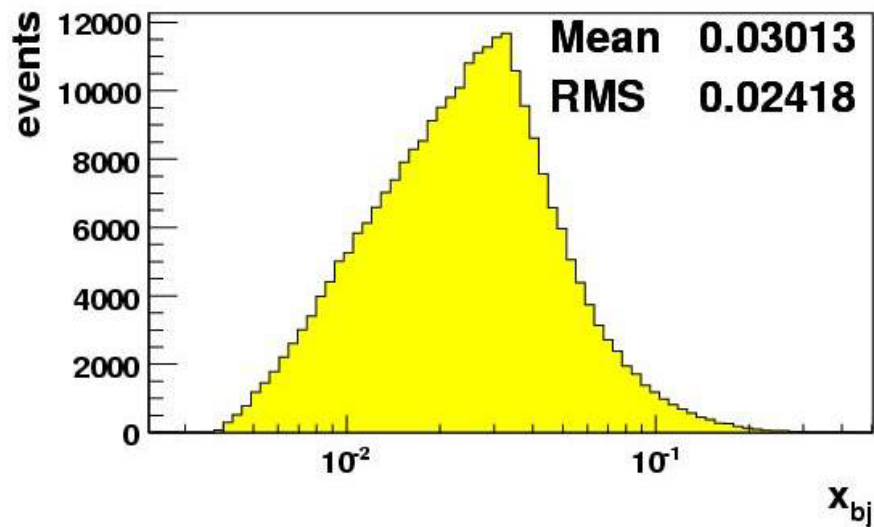
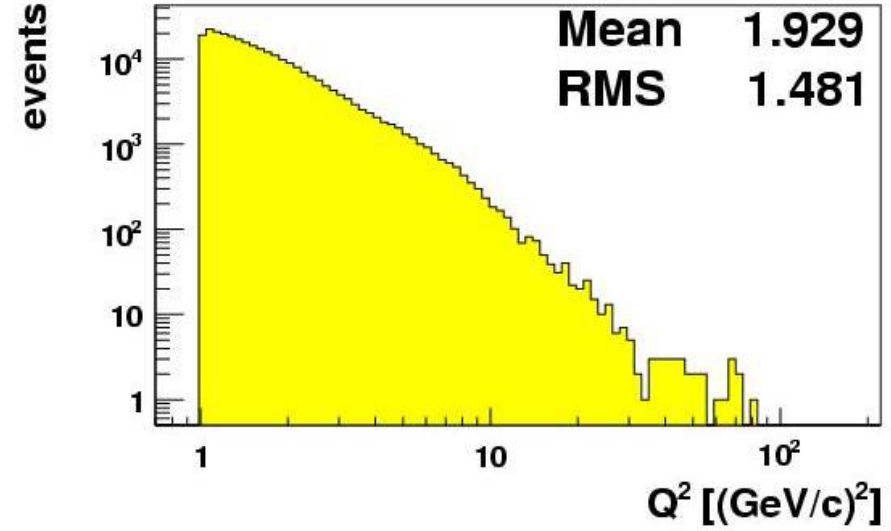
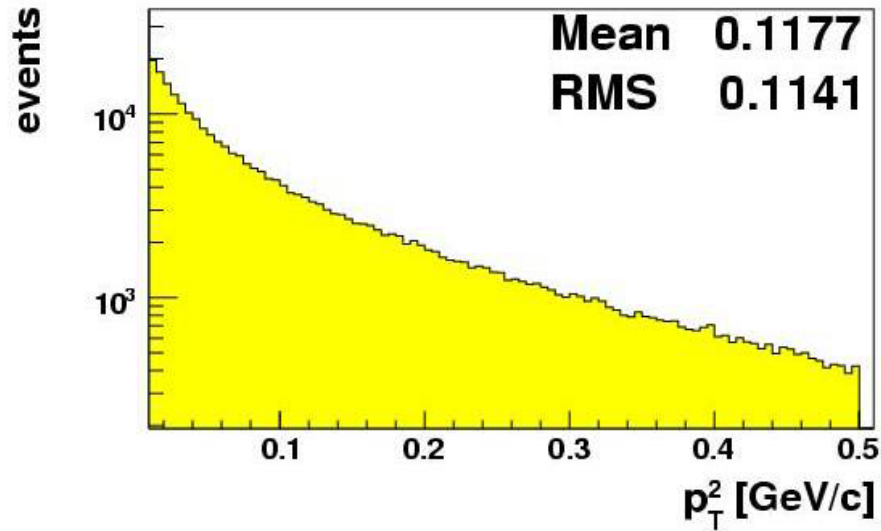
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Thank you!

# New Results: SSA for Exclusive Rho Production

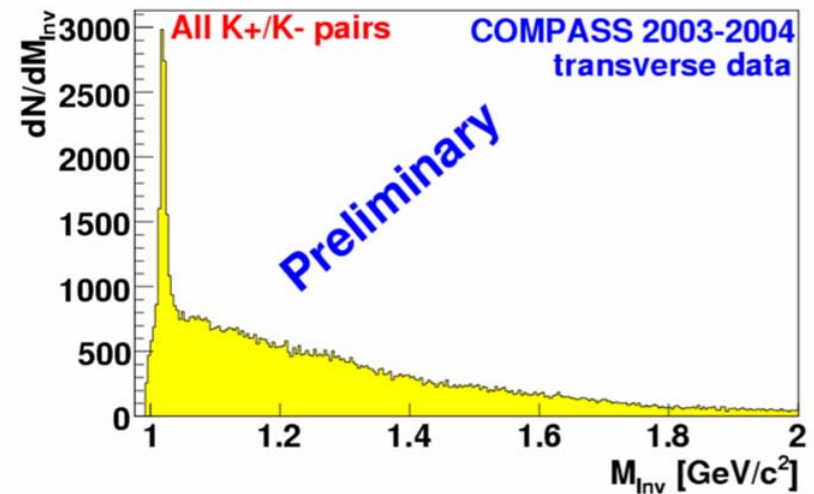
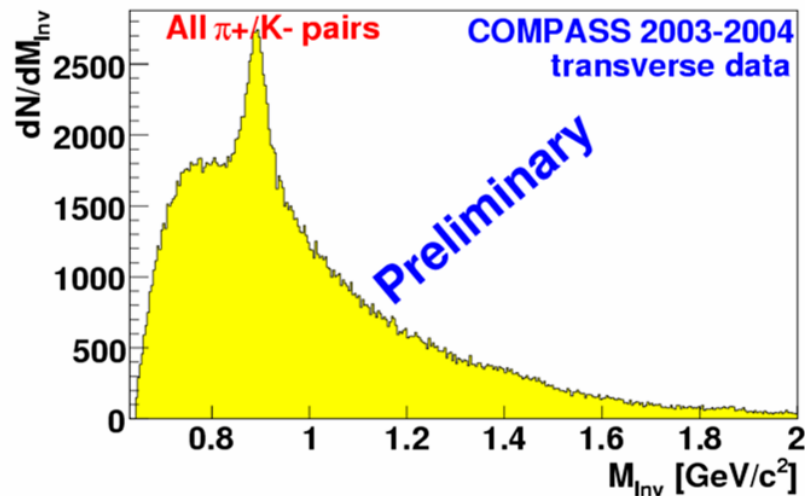
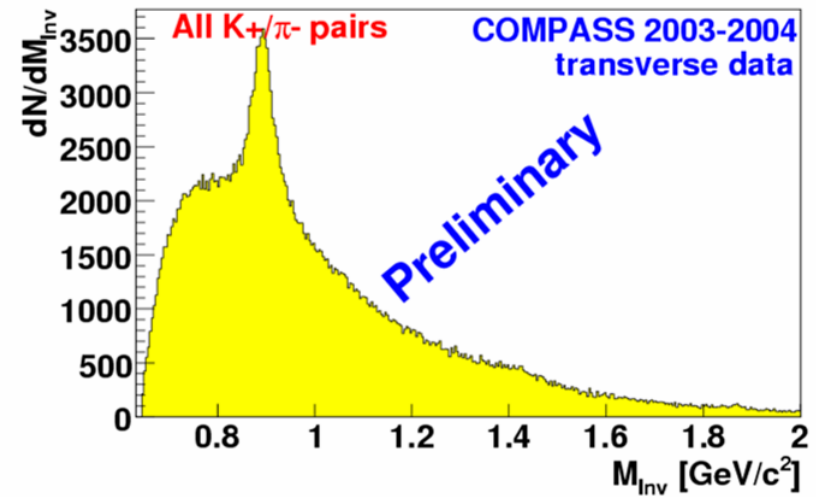
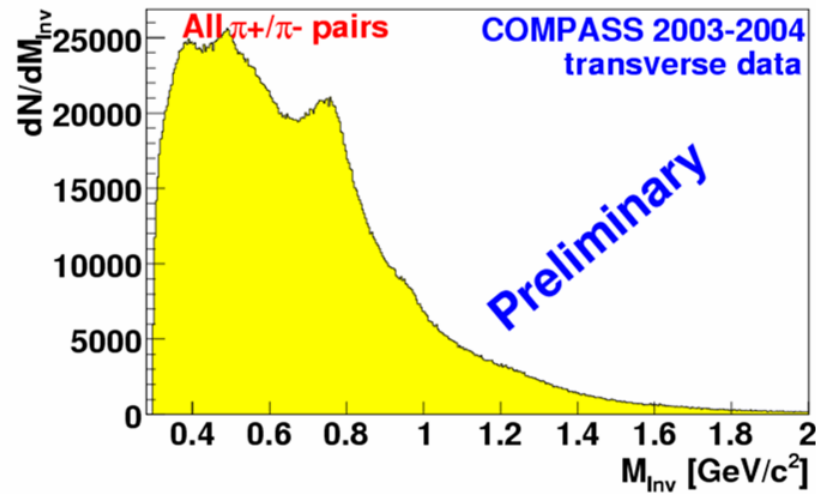


# New Results: SSA for Exclusive Rho Production



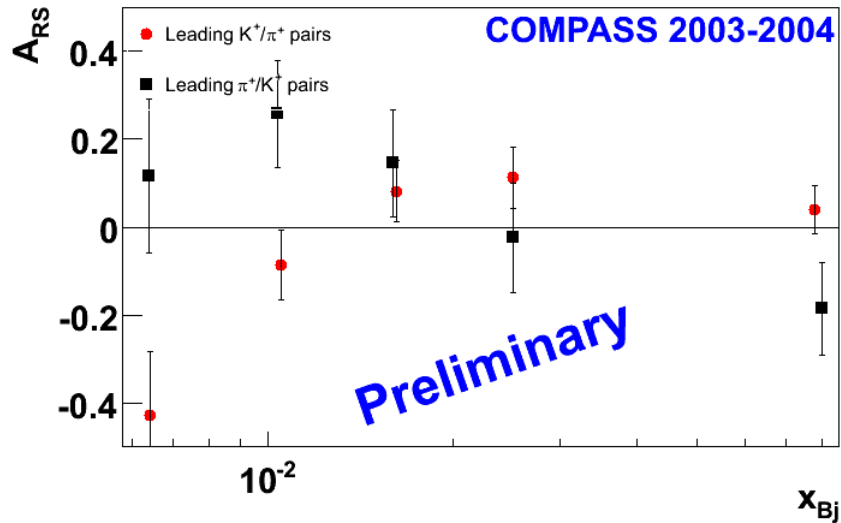
# Hadron Pairs Invariant Mass Spectra

all hadron pairs: 5.3 M

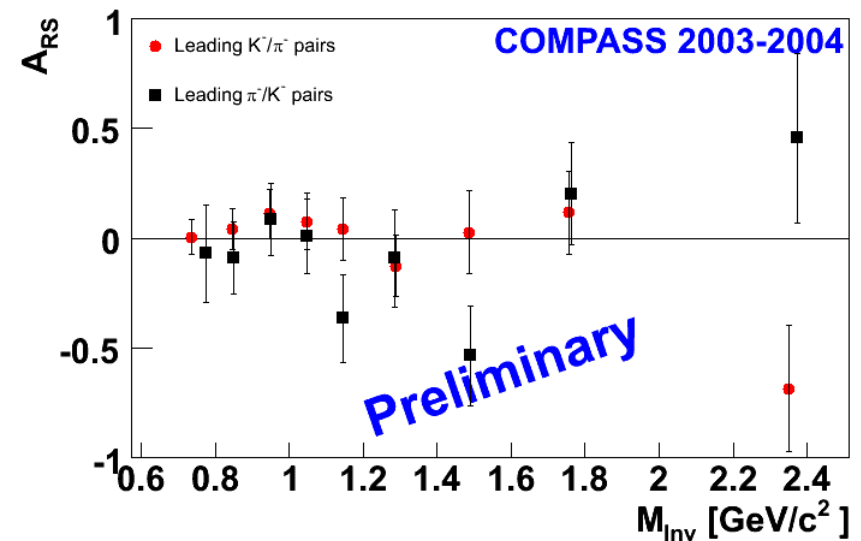
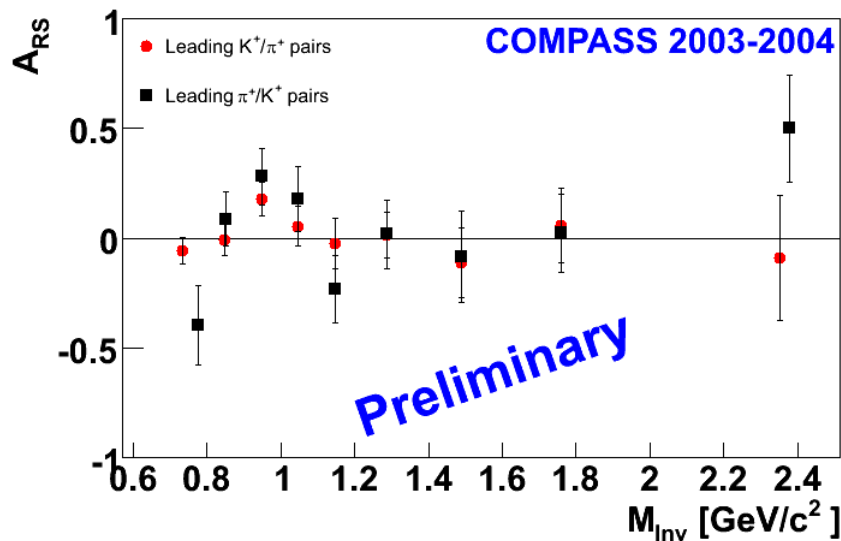
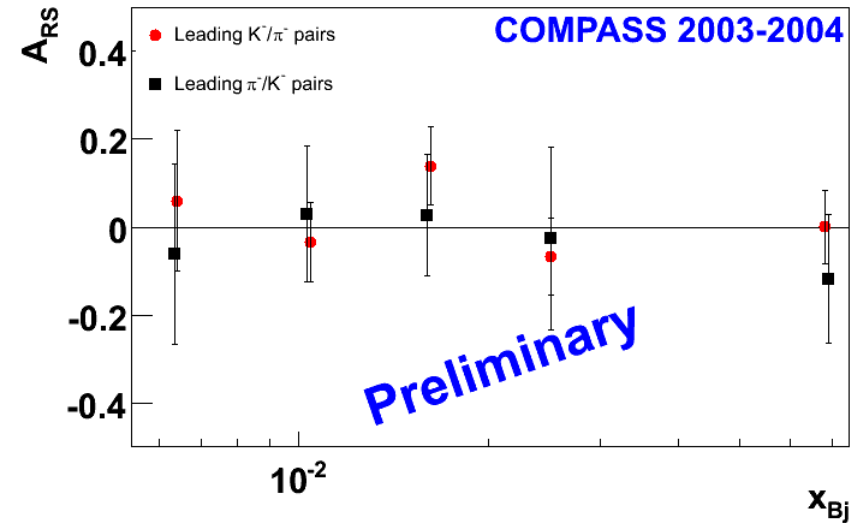


# New Results: Leading $\pi/K$ Pairs z-ordered

$K^+\pi^+$   
 $\pi^+K^+$

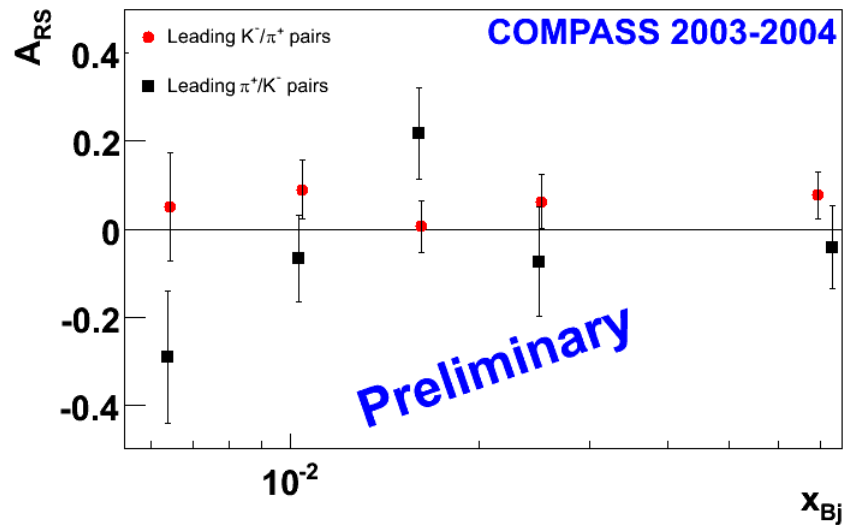


$K^-\pi^-$   
 $\pi^-K^-$

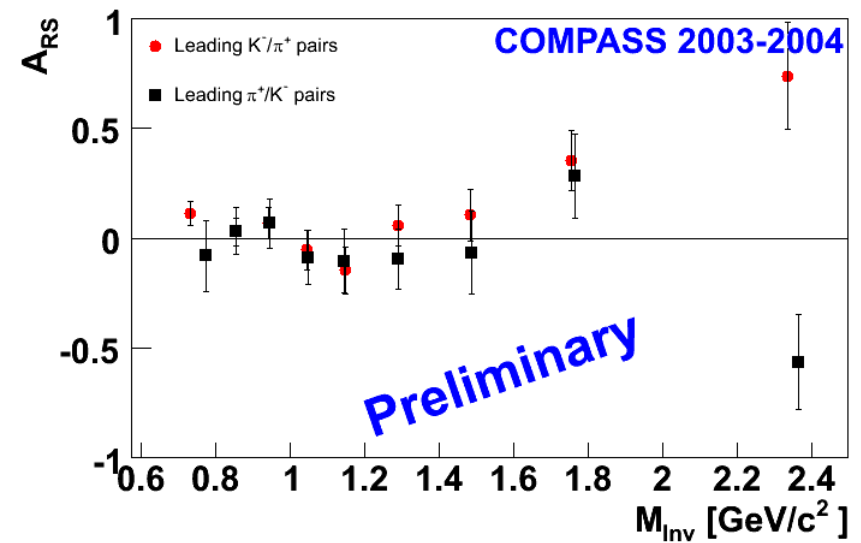
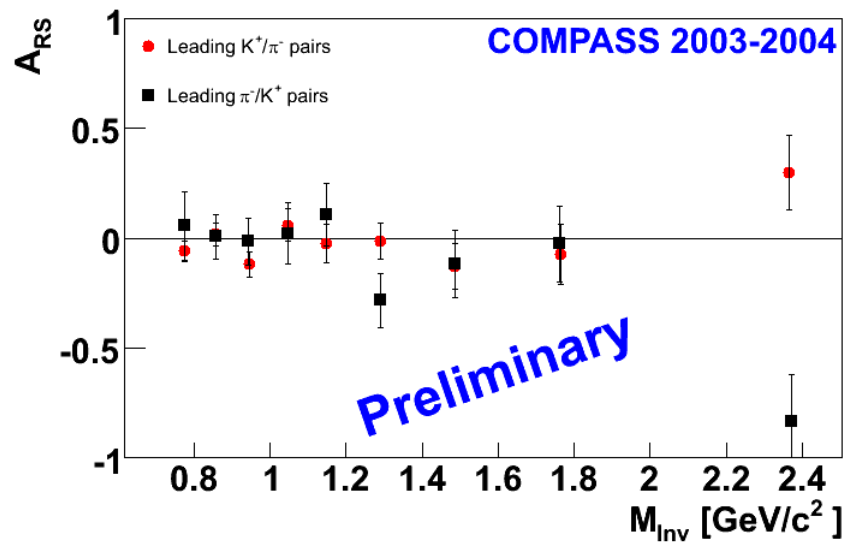
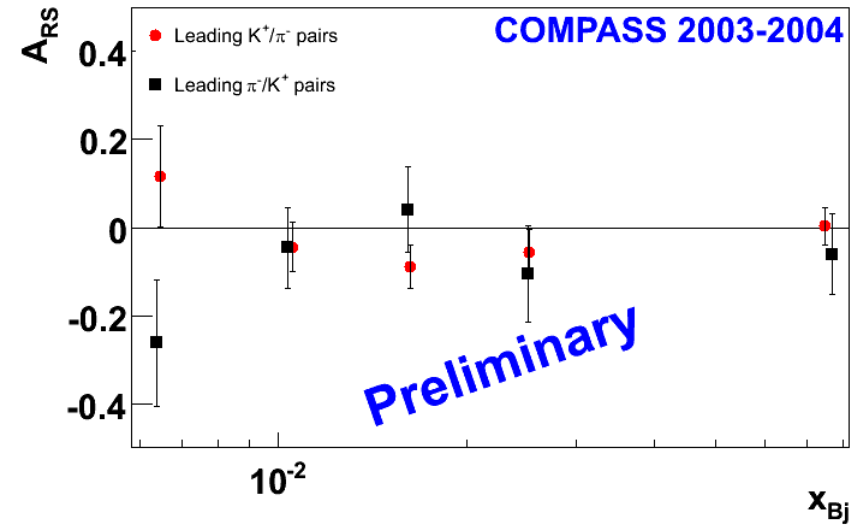


# New Results: Leading $\pi/K$ Pairs z-ordered

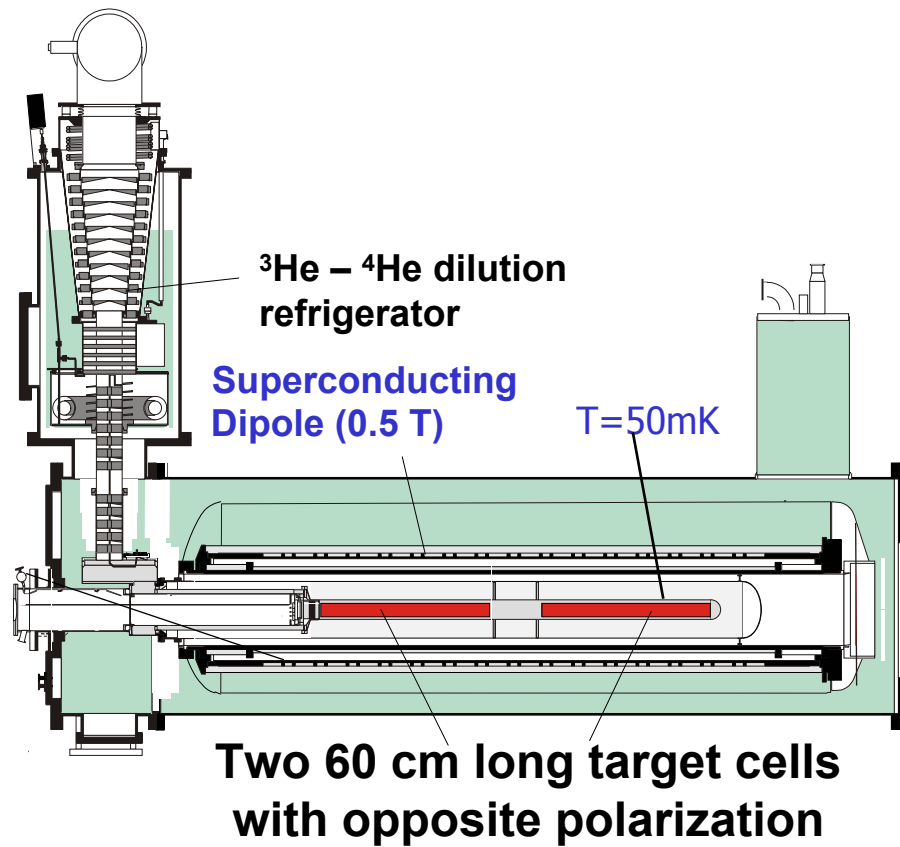
$K^- \pi^+$   
 $\pi^+ K^-$



$K^+ \pi^-$   
 $\pi^- K^+$

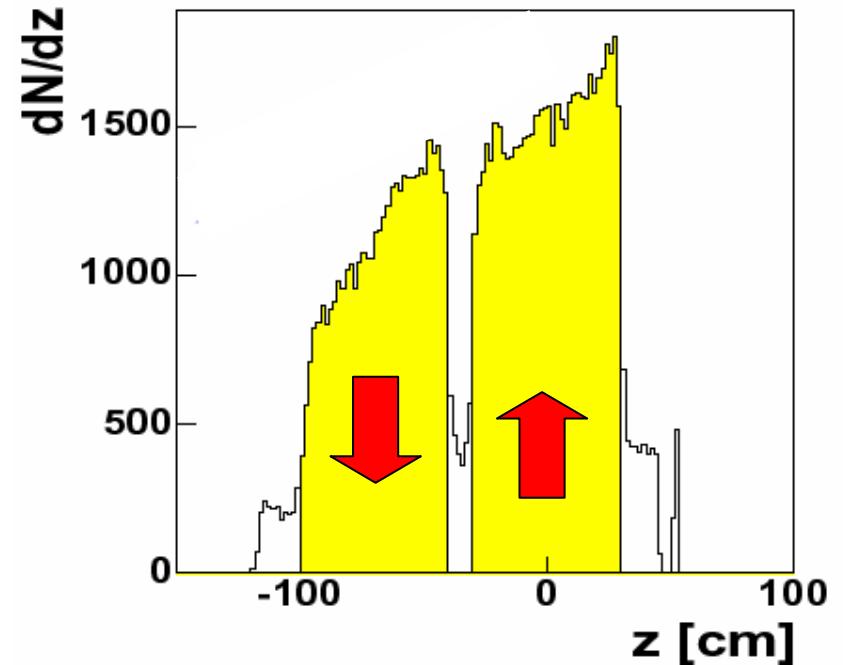


# The polarised ${}^6\text{LiD}$ -Target



**Transverse target polarization:**  
Reversed one a week

Vertex distribution:



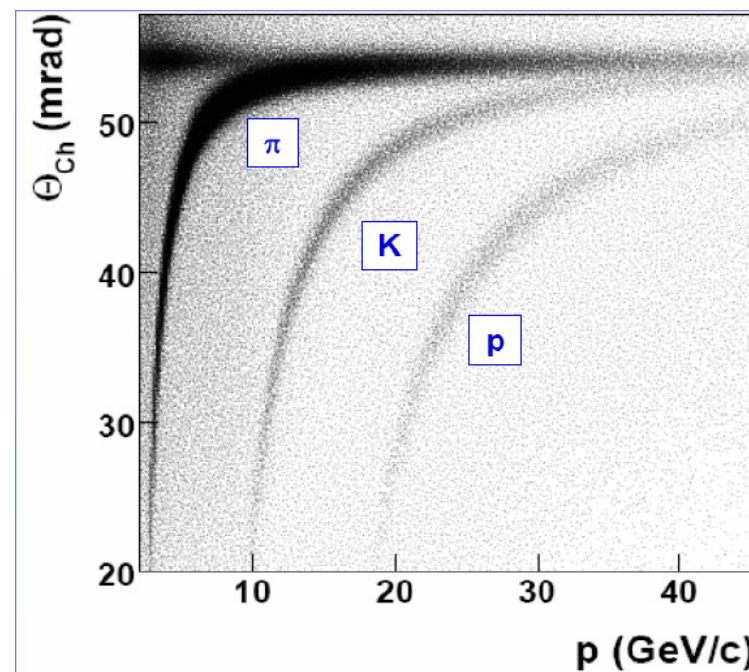
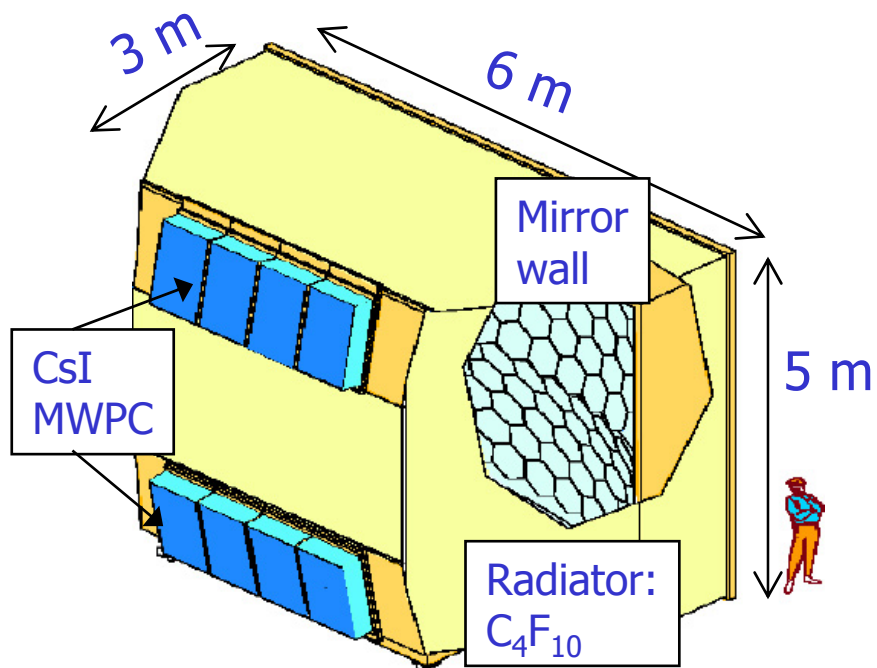
**Polarization: 50 %**  
**Dilution factor: 0.38**

# Ring Imaging Cherenkov Detector

Identification of  $\pi$ , K and protons

Cherenkov thresholds:  $\pi \approx 3 \text{ GeV}/c$   
 $K \approx 9 \text{ GeV}/c$   
 $p \approx 17 \text{ GeV}/c$

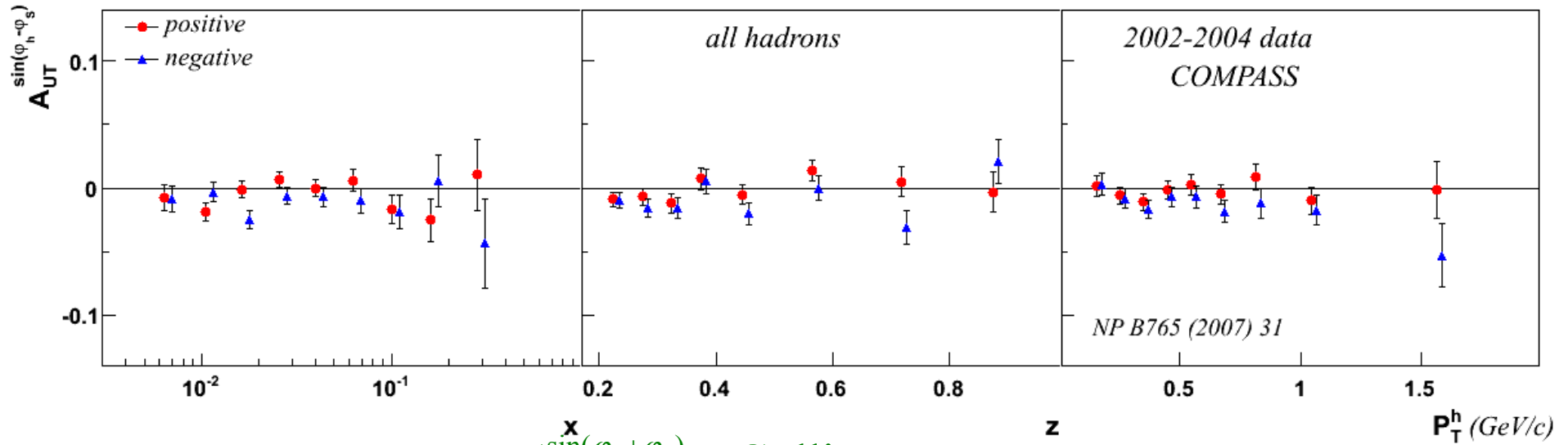
$2\sigma$   $\pi/K$  separation at  $43 \text{ GeV}/c$



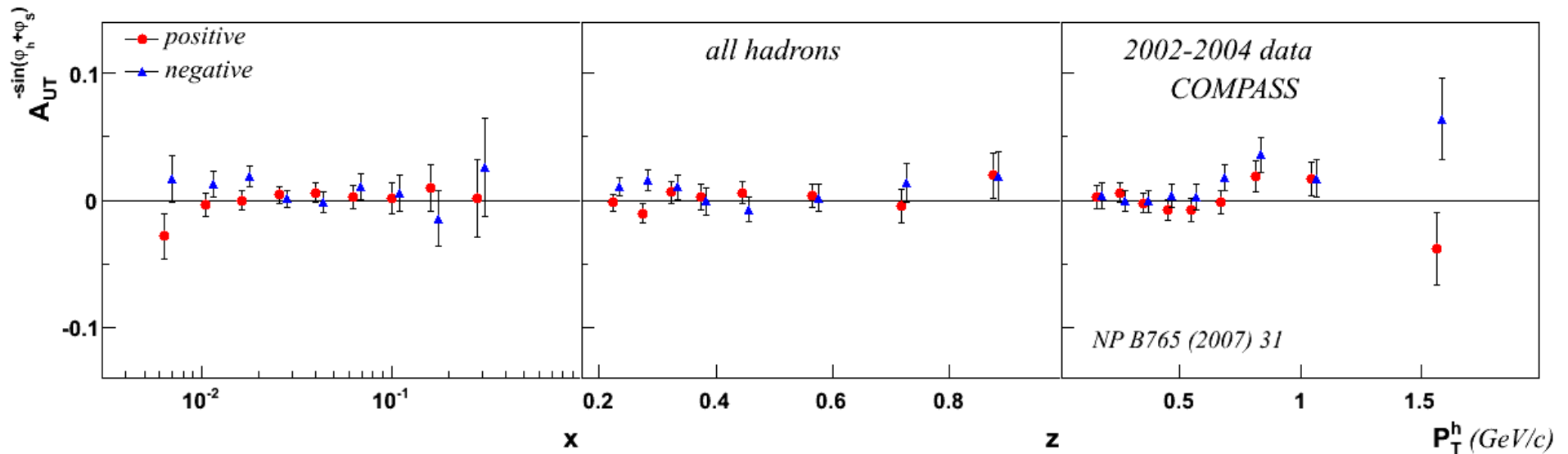


# Results for all hadrons

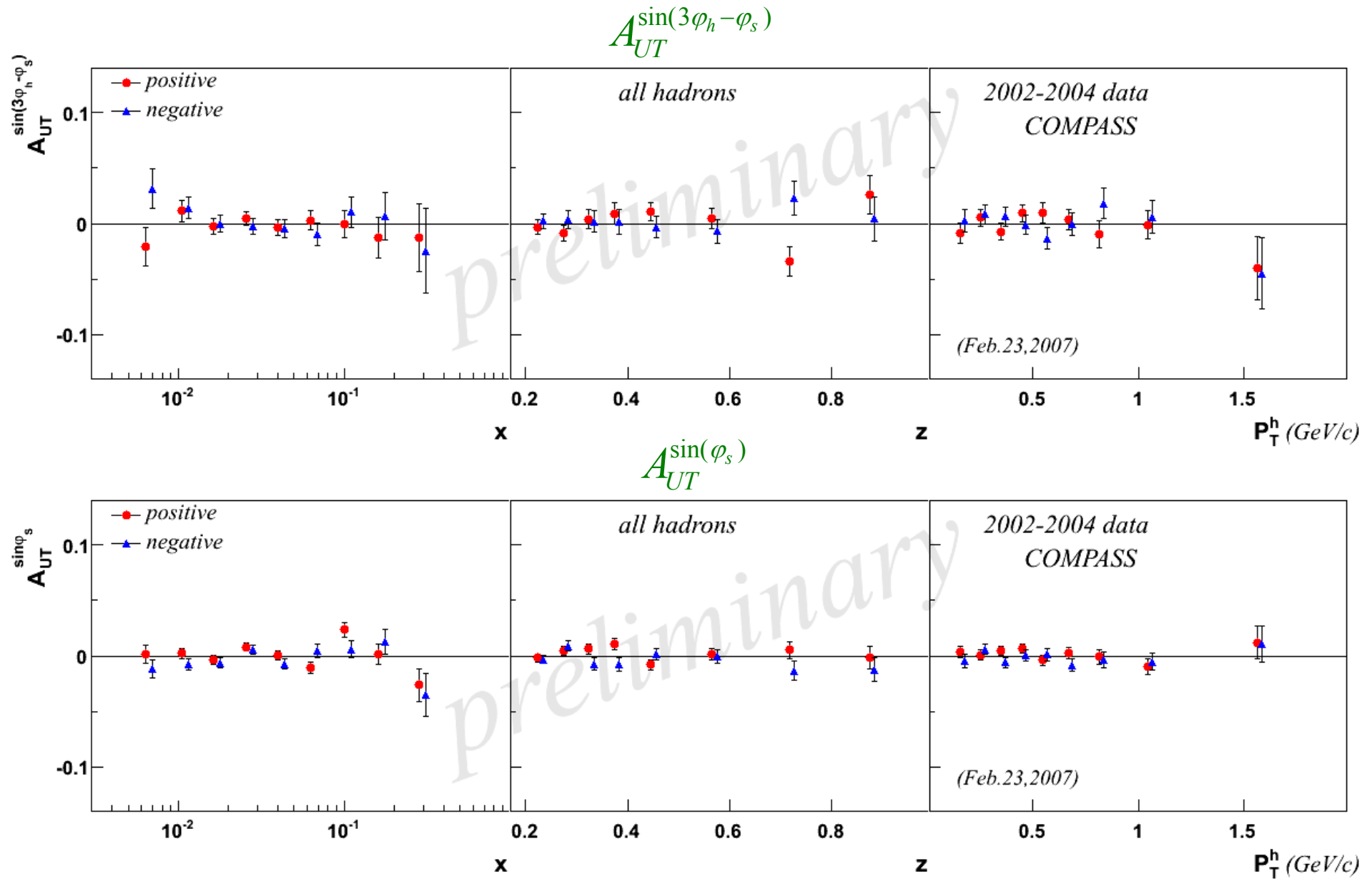
$A_{UT}^{\sin(\varphi_h - \varphi_s)}$  - Sivers asymmetry



$-A_{UT}^{\sin(\varphi_h + \varphi_s)}$  - Collins asymmetry

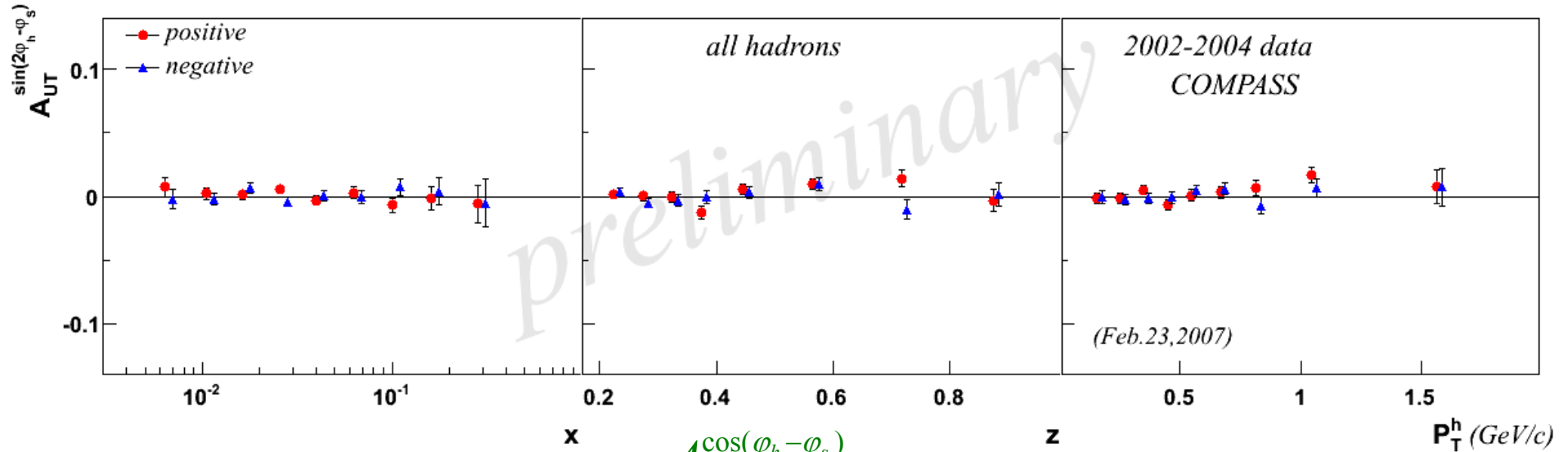


# Results beyond Collins and Sivers

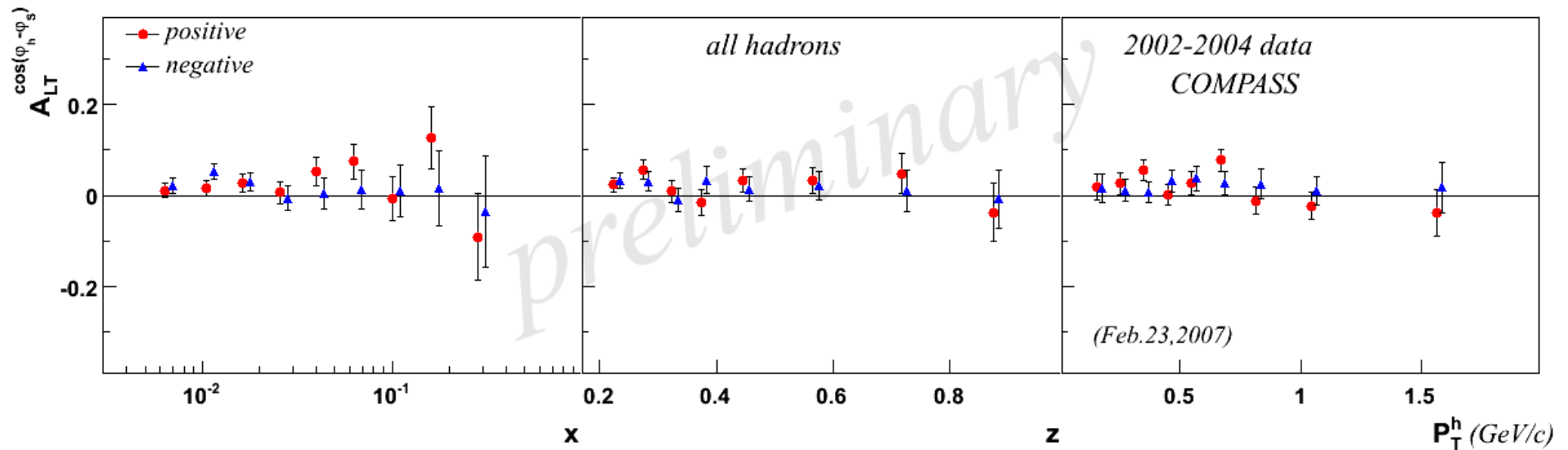


# Results beyond Collins and Sivers

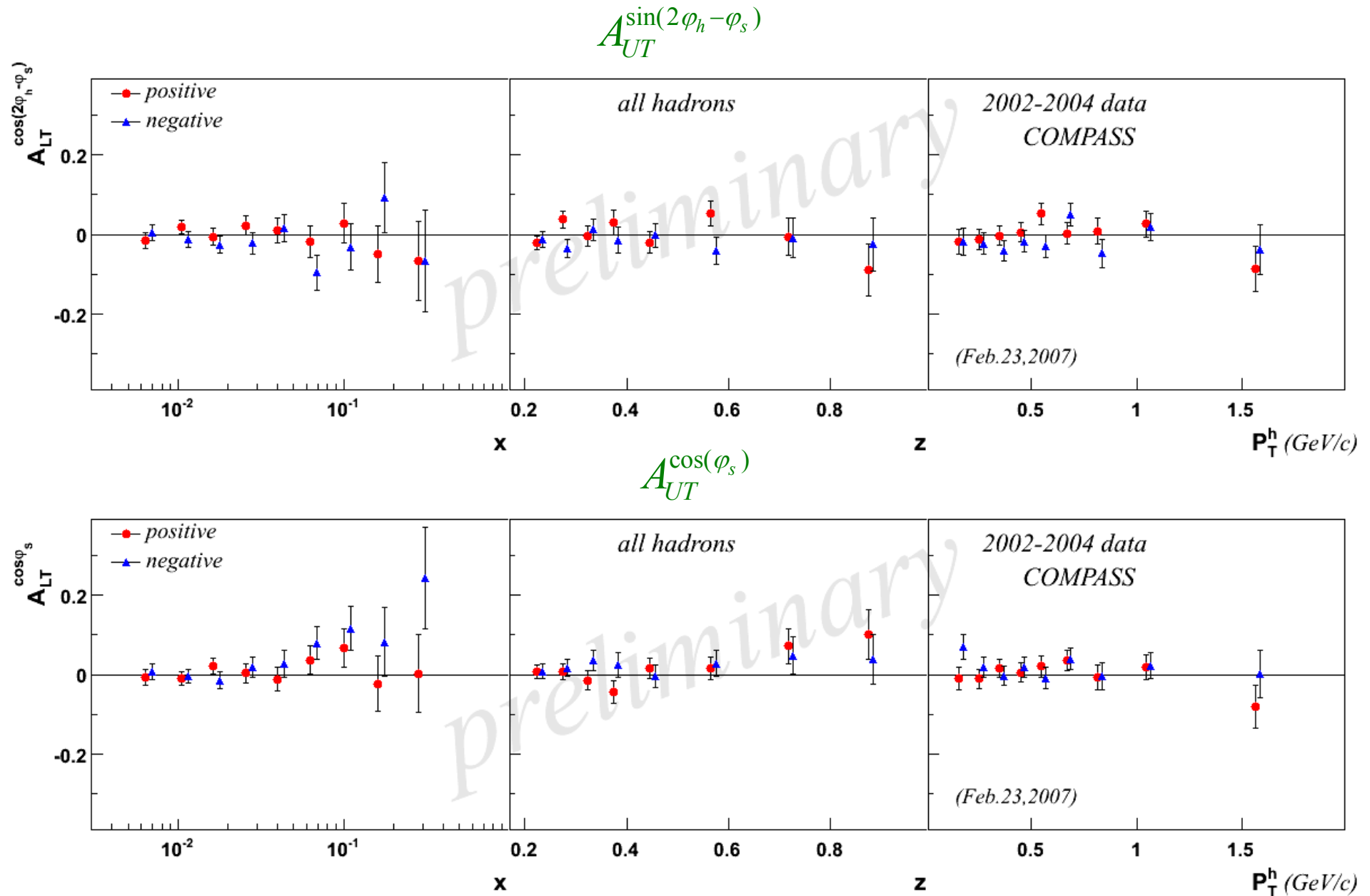
$$A_{UT}^{\sin(2\varphi_h - \varphi_s)}$$



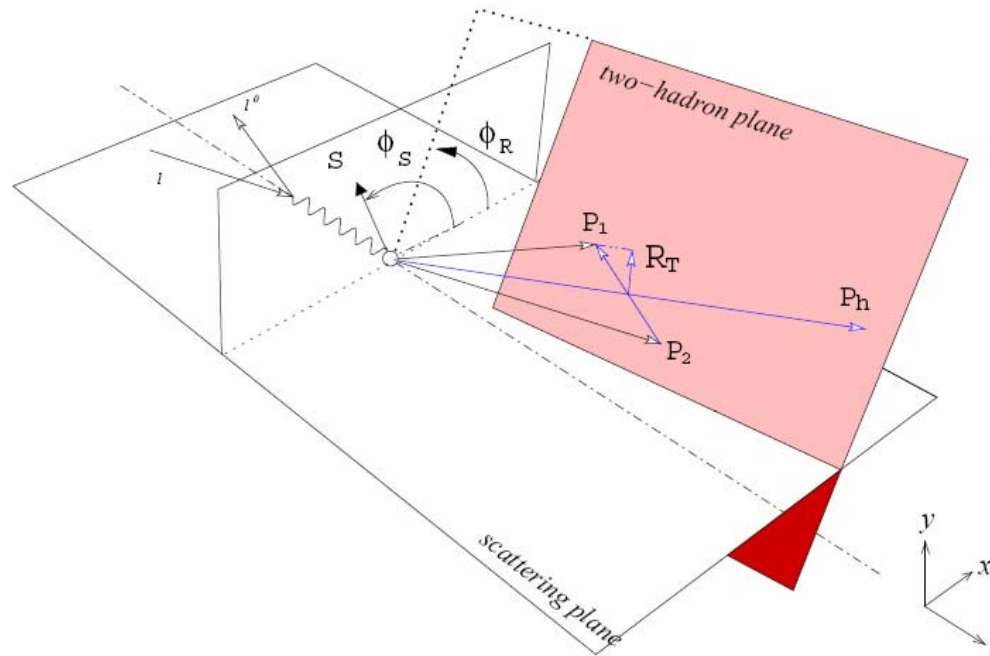
$$A_{LT}^{\cos(\varphi_h - \varphi_s)}$$



# Results beyond Collins and Sivers



# Frame independent definition of $\phi_R$



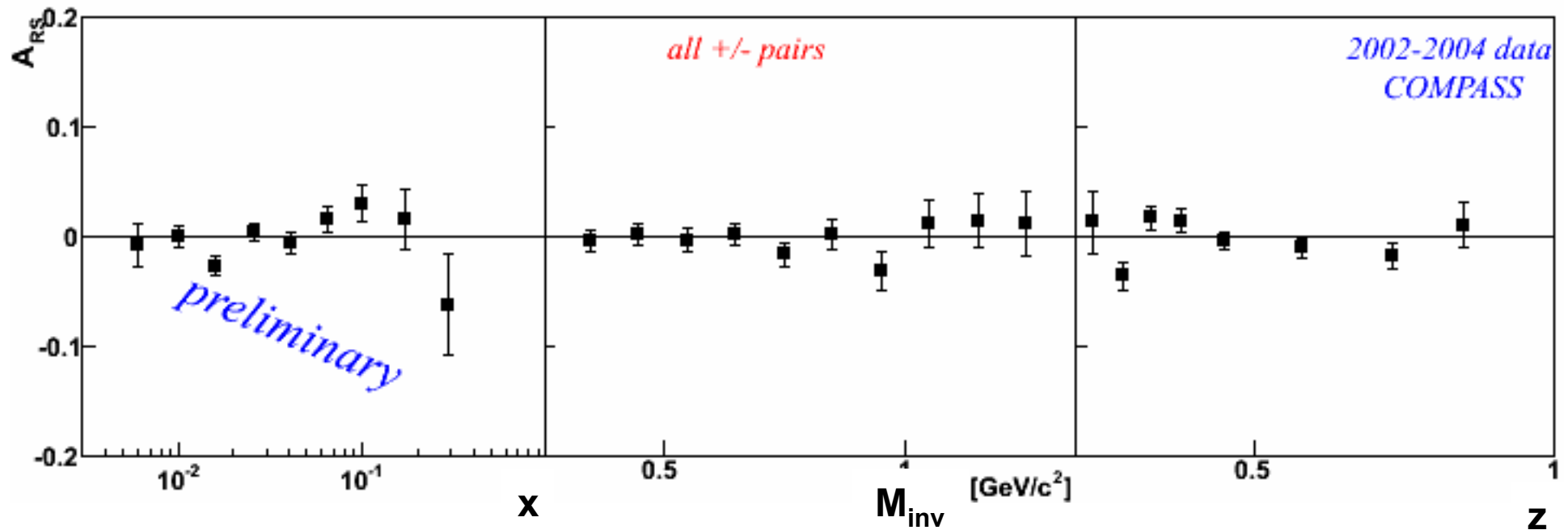
A. Baccetta,  
hep-ph/0608037

with: 
$$R_T = \frac{z_2 P_{1T} - z_1 P_{2T}}{z_1 + z_2}$$
 where  $P_{1T}$  and  $P_{2T}$  are the transverse components of the hadron momenta

we define: 
$$\cos \phi_R = \frac{(\mathbf{q} \times \mathbf{l}) \cdot (\mathbf{q} \times \mathbf{R}_T)}{|\mathbf{q} \times \mathbf{l}| |\mathbf{q} \times \mathbf{R}_T|} \quad \sin \phi_R = \frac{(\mathbf{l} \times \mathbf{R}_T) \cdot \mathbf{q}}{|\mathbf{q} \times \mathbf{l}| |\mathbf{q} \times \mathbf{R}_T|}$$

# Results for two unidentified hadrons

all combinations  
of + (h1) and - (h2) hadrons



2002-2004 COMPASS data

# Double Ratio Method

---

double ratio:  $F(\Phi_{\text{Coll}}) = \frac{N_{\text{up}}^{\uparrow}(\Phi_{\text{Coll}}) \cdot N_{\text{down}}^{\uparrow}(\Phi_{\text{Coll}})}{N_{\text{up}}^{\downarrow}(\Phi_{\text{Coll}}) \cdot N_{\text{down}}^{\downarrow}(\Phi_{\text{Coll}})}$

$N_{\text{up/down}}$ : upstream / downstream target cell

$N^{\uparrow\downarrow}$ : target polarization vector pointing up / down

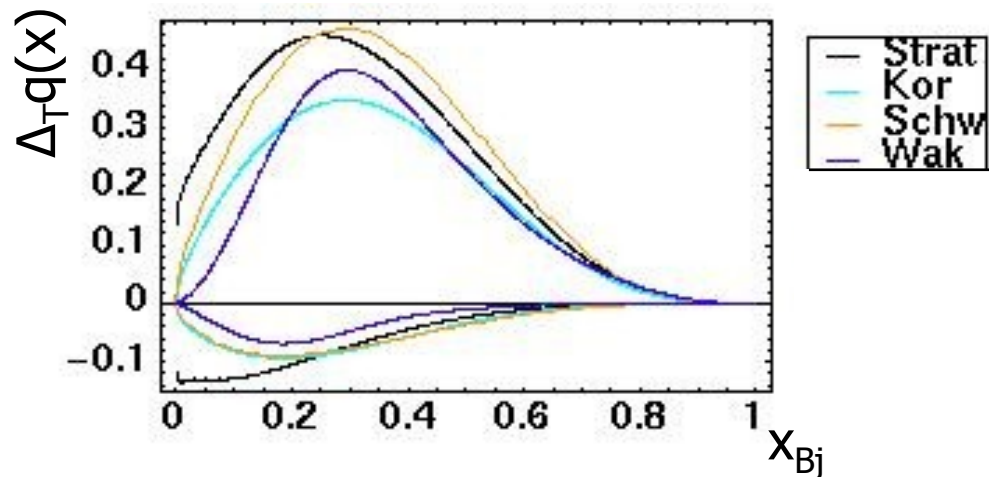
fit function:  $F(\Phi_{\text{Coll}}) = c \cdot (1 + 4 \cdot A_C^h \sin \Phi_{\text{Coll}})$

final asymmetry:  $A_{\text{Coll}} = \frac{1}{f P_T D} A_C^h$

# Comparison with Theory

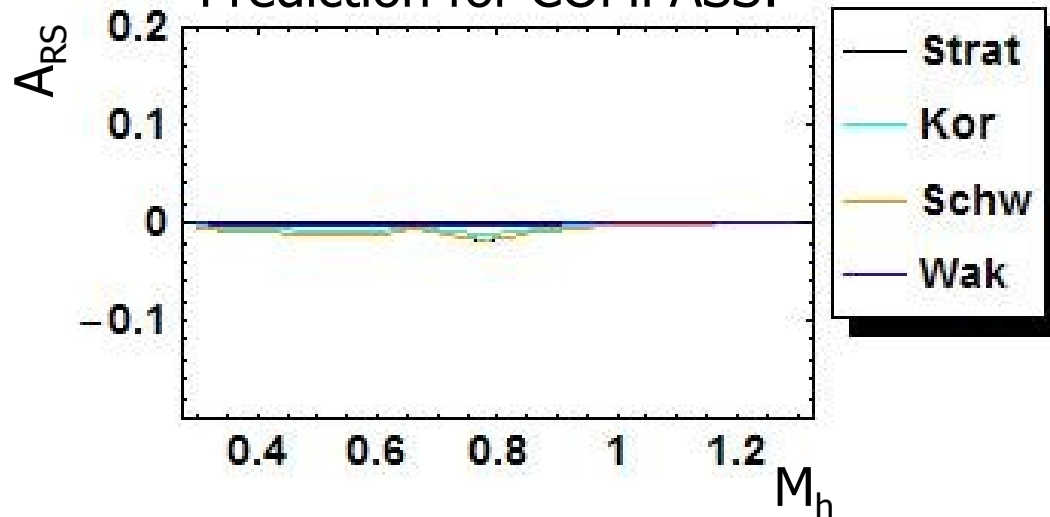
Model calculations for COMPASS kinematics (M. Radici, QCDN 06, hep-ph/0608037):

Model for transversity:



- Soffer, Stratmann, Vogelsang, P.R. D65 (02) 114024
- Korotkov, Nowak, Oganessian, E.P.J. C18 (01) 639
- Schweitzer et al., P.R. D64 (01) 034013
- Wakamatsu P.L. B509 (01) 59

Prediction for COMPASS:

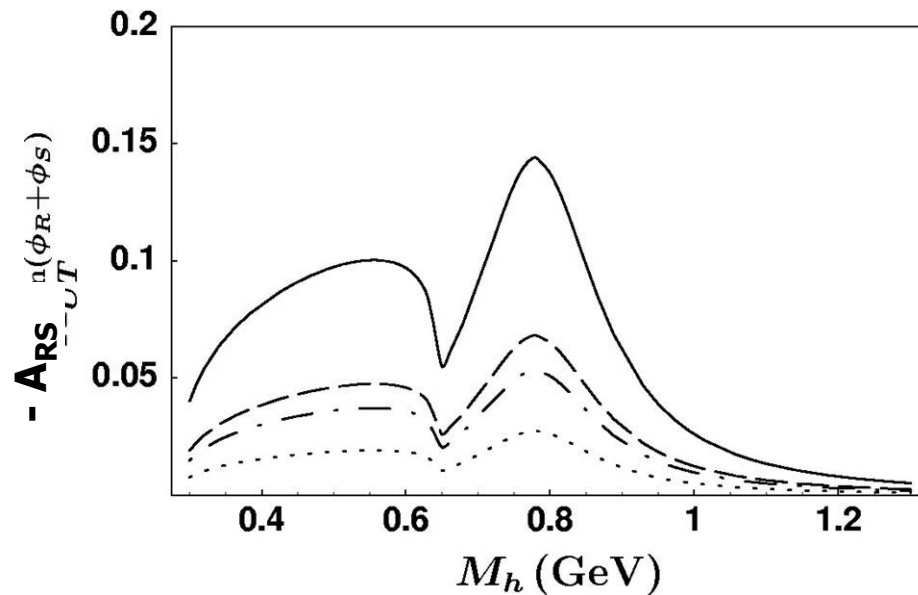


→ small asymmetries on the deuteron



# Predictions for Asymmetries on the Proton

Predictions for two-hadrons asymmetries on the **proton** at COMPASS:



(M. Radici, hep-ex/0608037)

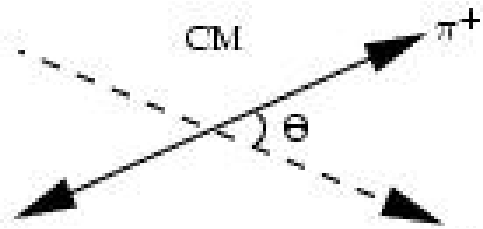
- Soffer, Stratmann, Vogelsang, P.R. D65 (02) 114024
- Korotkov, Nowak, Oganessian, E.P.J. C18 (01) 639
- Wakamatsu P.L. B509 (01) 59

# sinθ Dependence

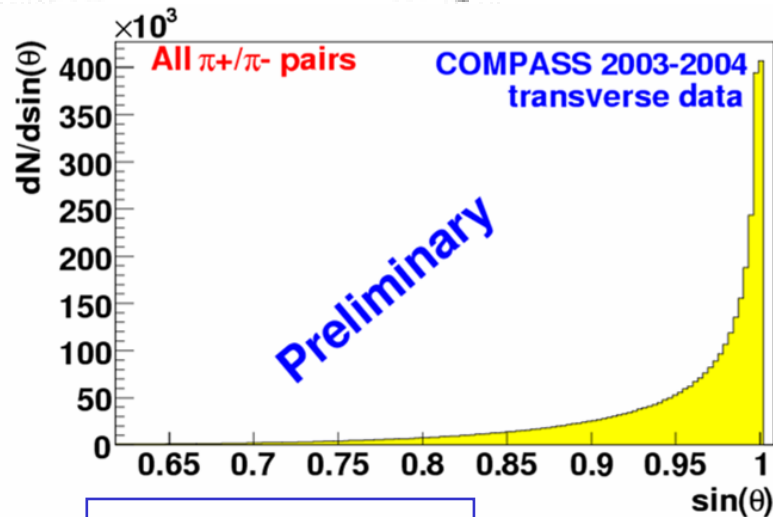
Cross section  $\sigma_{UT}$  for two- $\pi$  fragmentation depends on  $\sin\theta$ :  
(Interference of s- and p-wave of the  $2\pi$ -state)

$$\sigma_{UT} \propto \sum_q e_q^2 |S_T| \sin\theta \sin\phi_{RS} \Delta_T q(x) H_q^{z,h}(z, M_h^2)$$

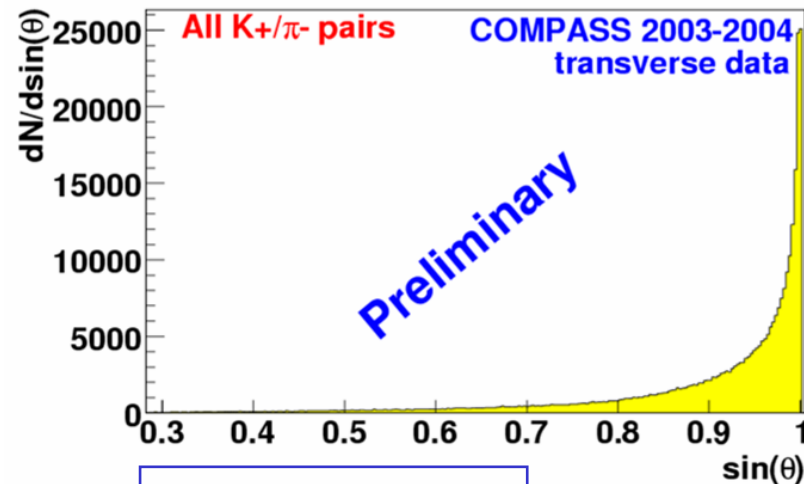
(A. Bacchetta and M. Radici,  
hep-ph/0212300)



$\theta$  : Angle of  $h_1$  in the two-hadrons CMS  
to the direction of  $P_h = P_{h1} + P_{h2}$



$$\langle \sin\theta \rangle = 0.95$$

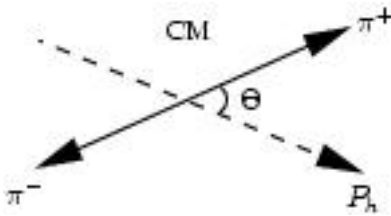


$$\langle \sin\theta \rangle = 0.90$$

→ small contribution in the kinematical region of COMPASS

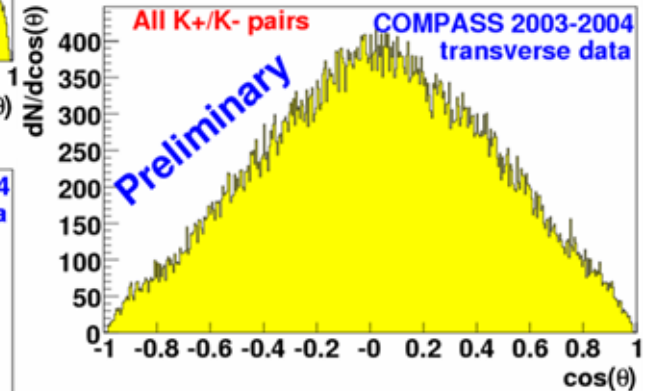
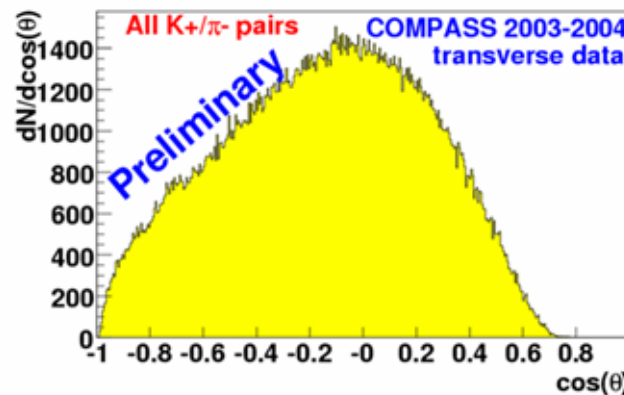
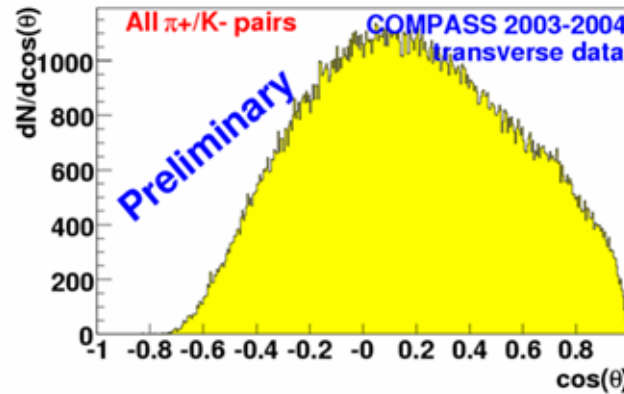
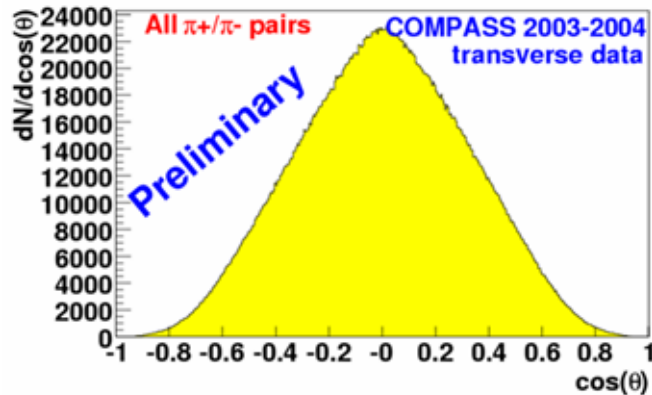
# Partial wave expansion of $H_q^{\angle h}(z)$

$$H_q^{\angle h}(z, \cos \theta, M_h^2) = H_{q,0t}^{\angle h}(z, M_h^2) + H_{q,1t}^{\angle h}(z, M_h^2) \cos \theta$$



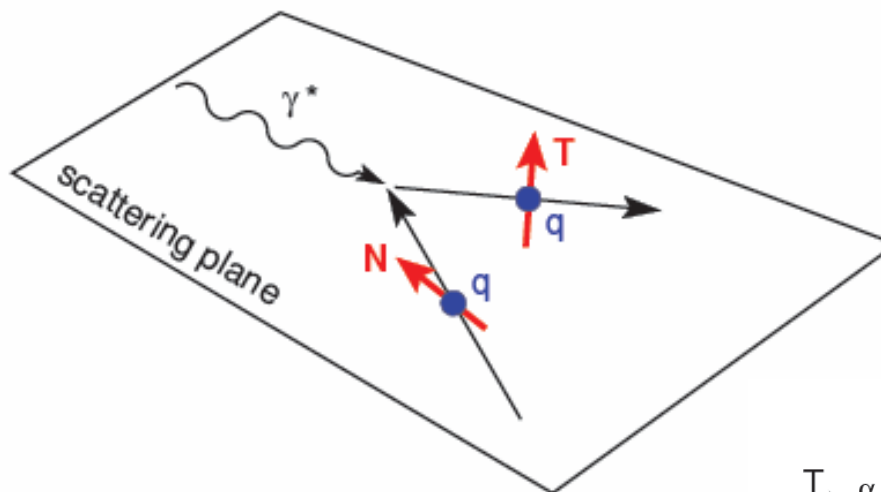
A. Baccetta, hep-ph/0708037

cosθ-Distributions  
of our data:



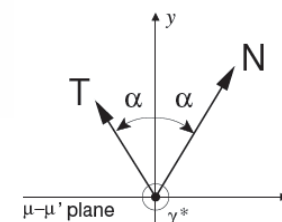
# Transverse $\Lambda$ Polarization

$$\mu N^\uparrow \rightarrow \mu' \Lambda^\uparrow X$$



**N**: component of target spin perpendicular to  $p_{\gamma^*}$

**T**: symmetric of N wrt. the normal to the scattering plane



$$P_{T,\text{exp}}^\Lambda = \frac{d\sigma^{\mu N^\uparrow \rightarrow \mu' \Lambda^\uparrow X} - d\sigma^{\mu N^\downarrow \rightarrow \mu' \Lambda^\uparrow X}}{d\sigma^{\mu N^\uparrow \rightarrow \mu' \Lambda^\uparrow X} + d\sigma^{\mu N^\downarrow \rightarrow \mu' \Lambda^\uparrow X}} = f P_N D(y) \frac{\sum_q e_q^2 \Delta_T q(x) \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 q(x) D_{\Lambda/q}(z)}$$

$f$  = target dilution factor,  $P_N$  = target polarization,

$D(y)$  = virtual photon depolarization factor

$$\Delta_T D_{\Lambda/q}(z) = D_{\Lambda^\uparrow/q^\uparrow}(z) - D_{\Lambda^\downarrow/q^\uparrow}(z)$$

# Transverse $\Lambda$ Polarization

