

AAPCOS 2015

# Direct detection of dark matter in universal bound states

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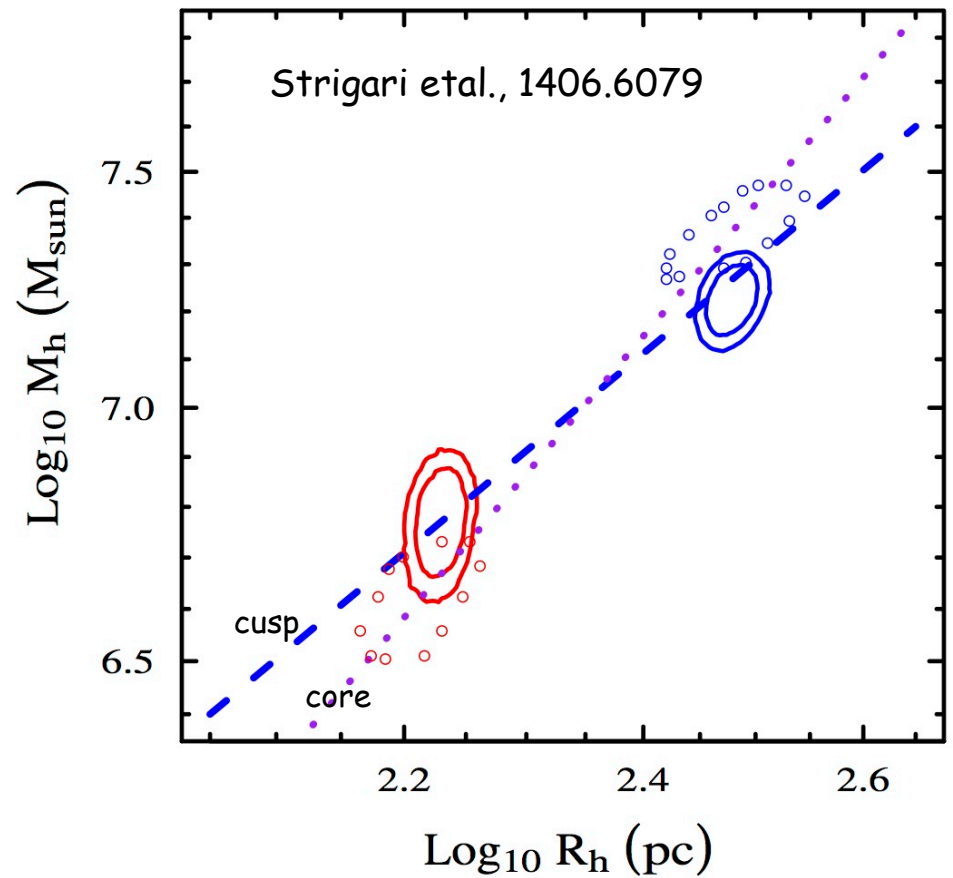
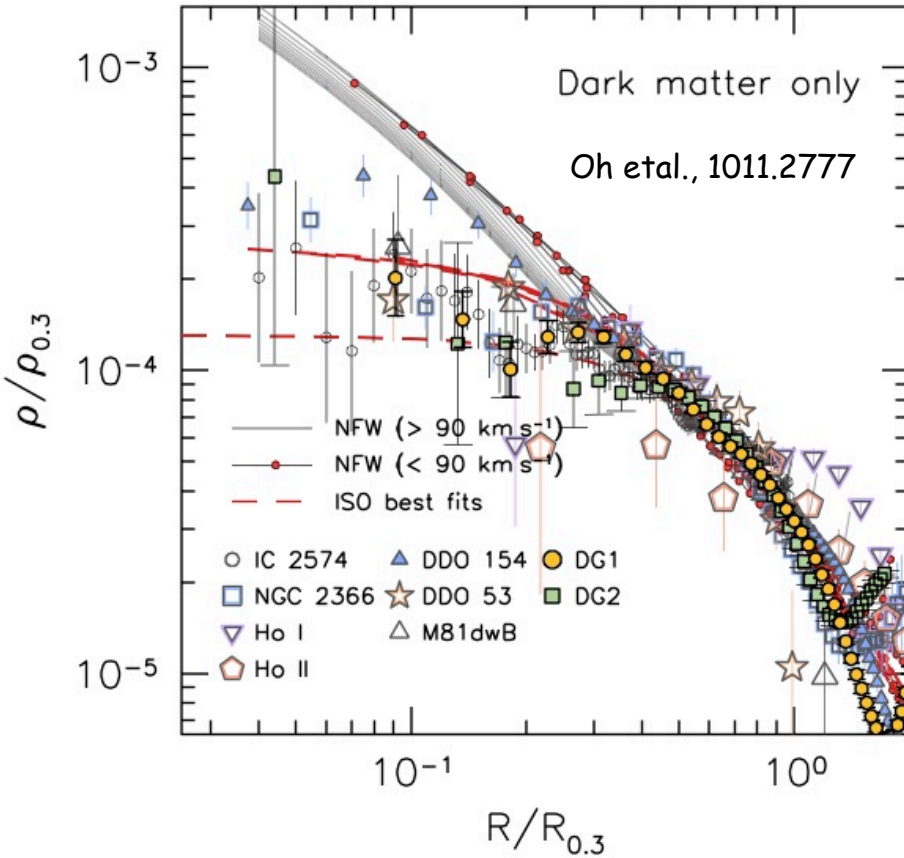


Thanks to my collaborator: E Braaten

1311.6368 PRD and 1505.02772 PRD

# The small-scale crisis of $\Lambda$ CDM

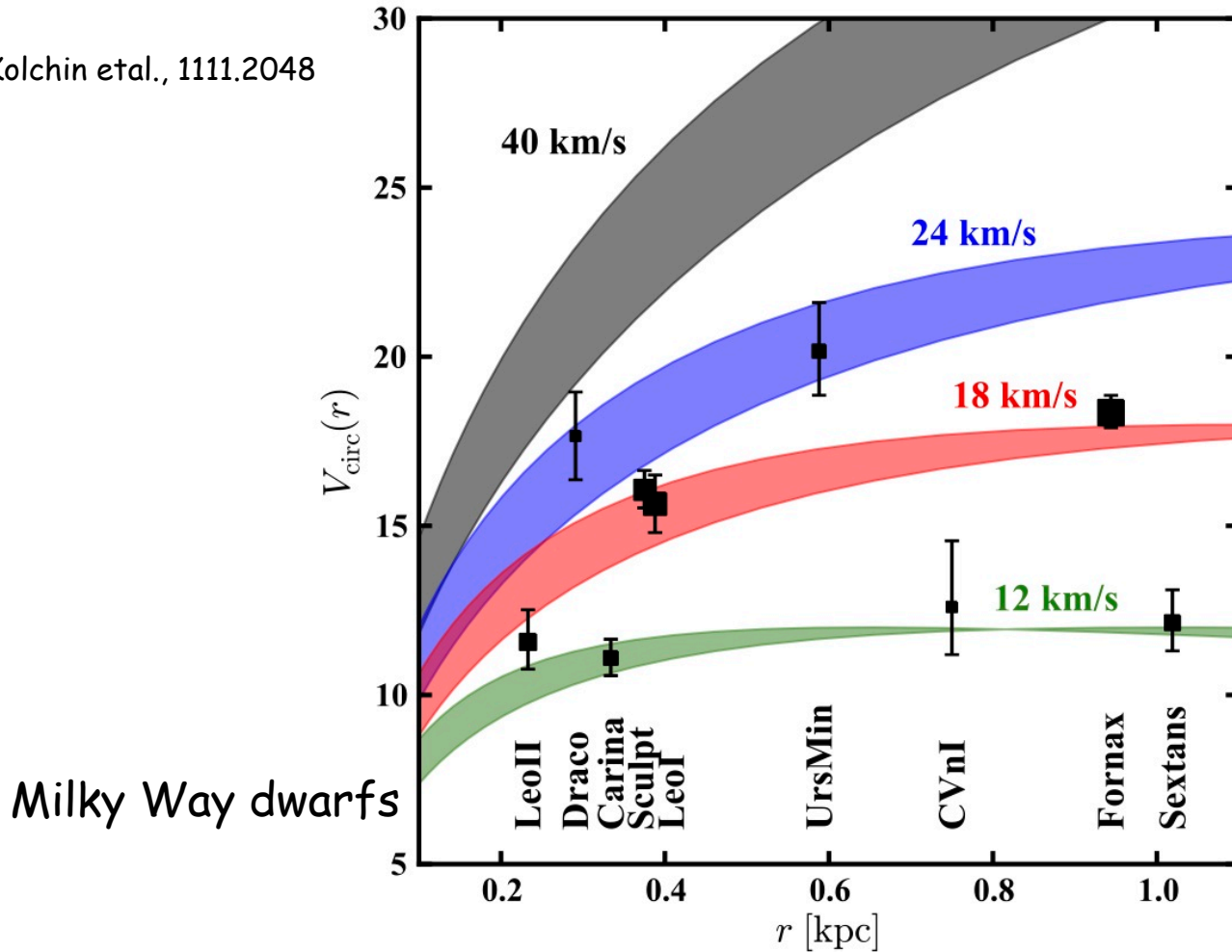
# Core vs cusp problem



Controversy about this issue not yet settled

# Too big to fail problem

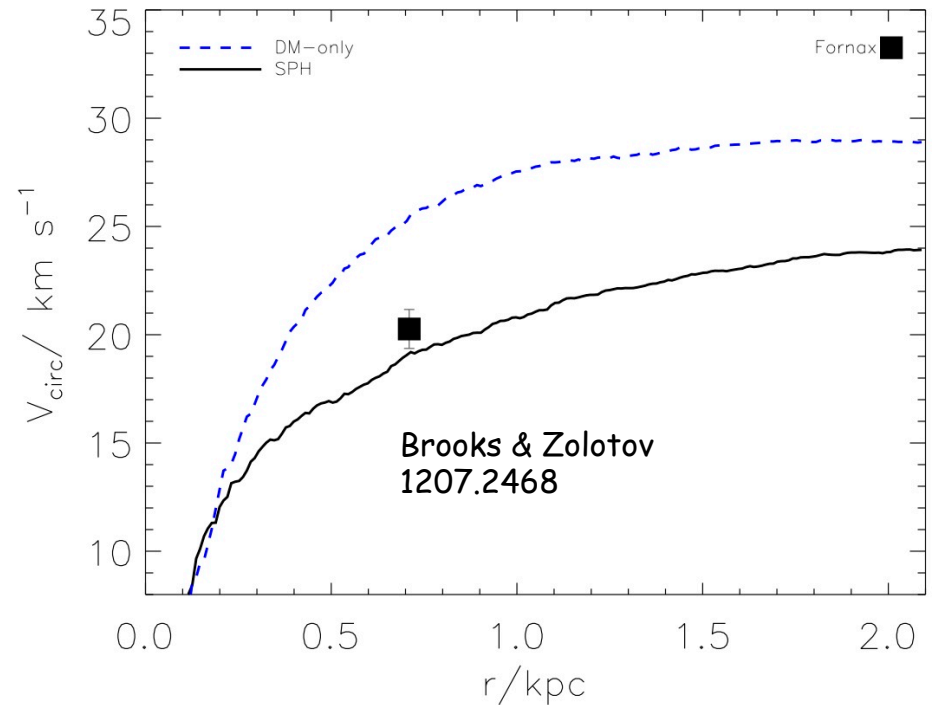
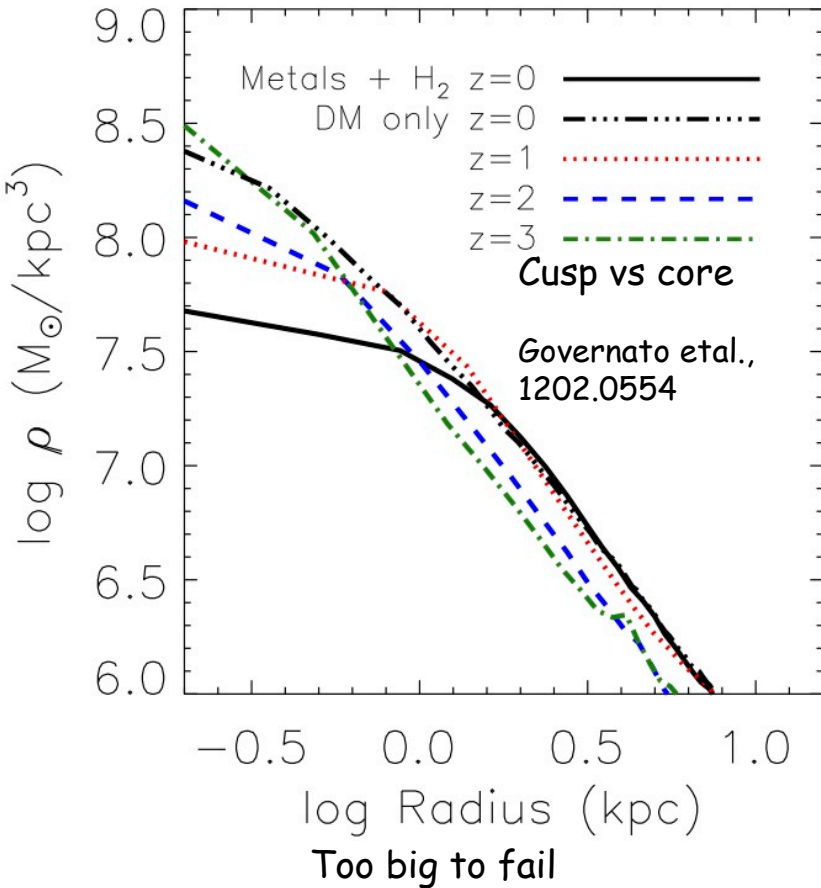
Boylan-Kolchin et al., 1111.2048



The Milky Way dwarfs are not in the most massive dark matter halos --- predicted satellites are too dense

Potential solution to these problems

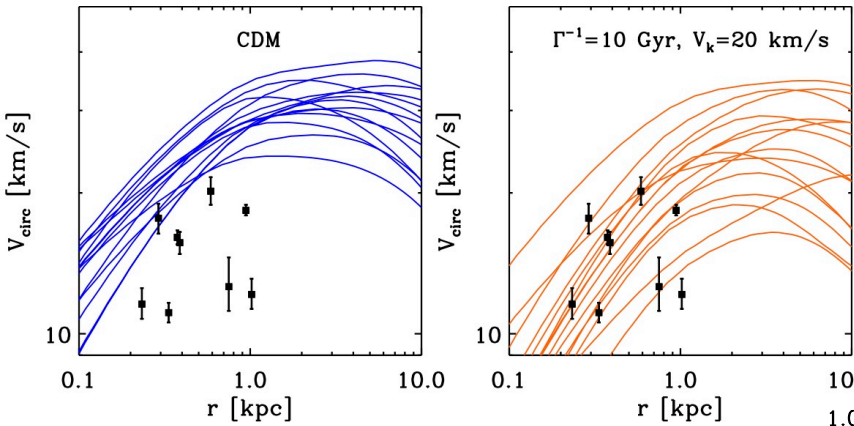
# Baryons matter



Baryons have the potential to solve **all** these problems

# Alternative dark matter models

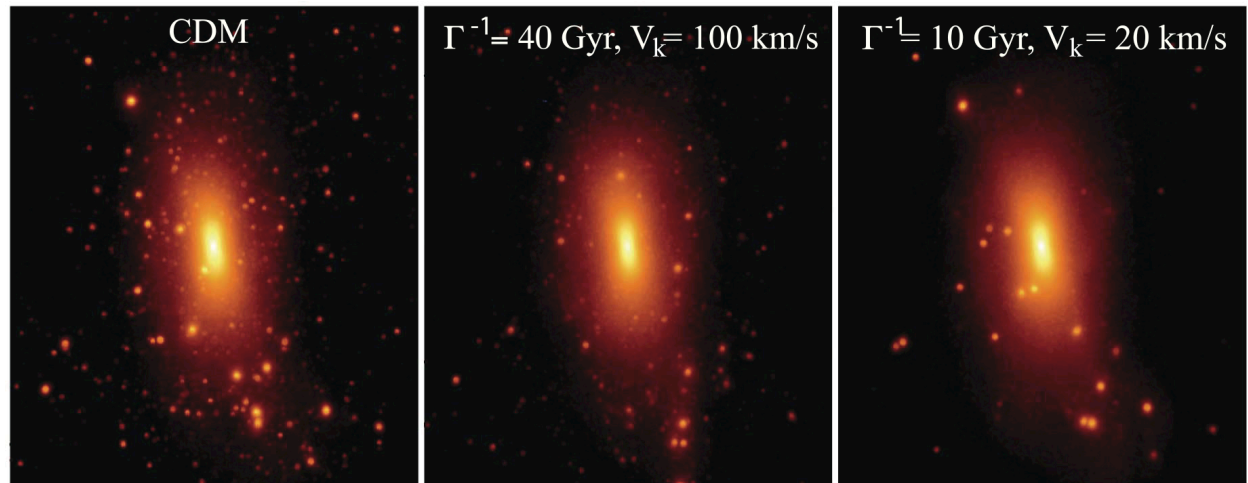
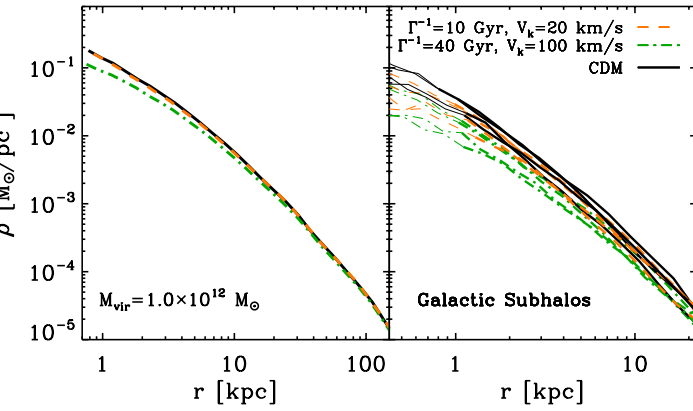
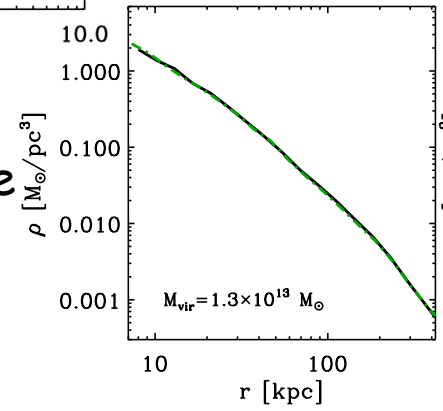
Decaying dark matter (Strigari et al., 0606281, Wang et al., 1406.0527)



✓ Solves too big to fail

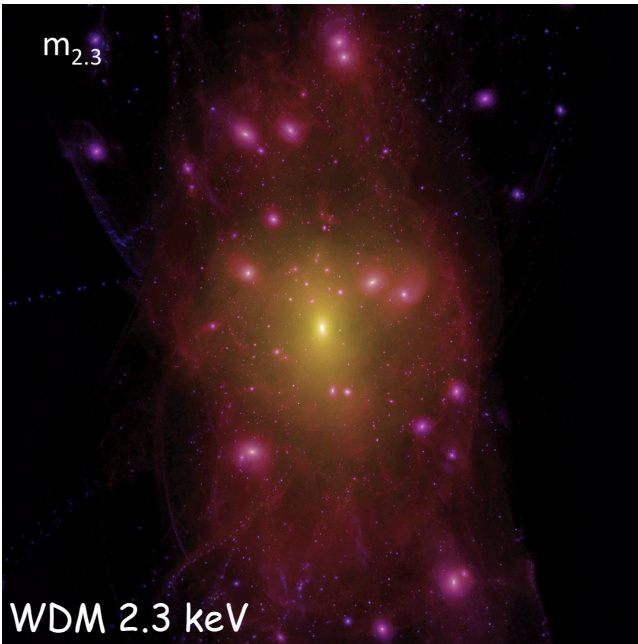
✗ Cannot solve cusp vs core

Include baryons?



✓ Lowers the number of satellites

# Warm dark matter

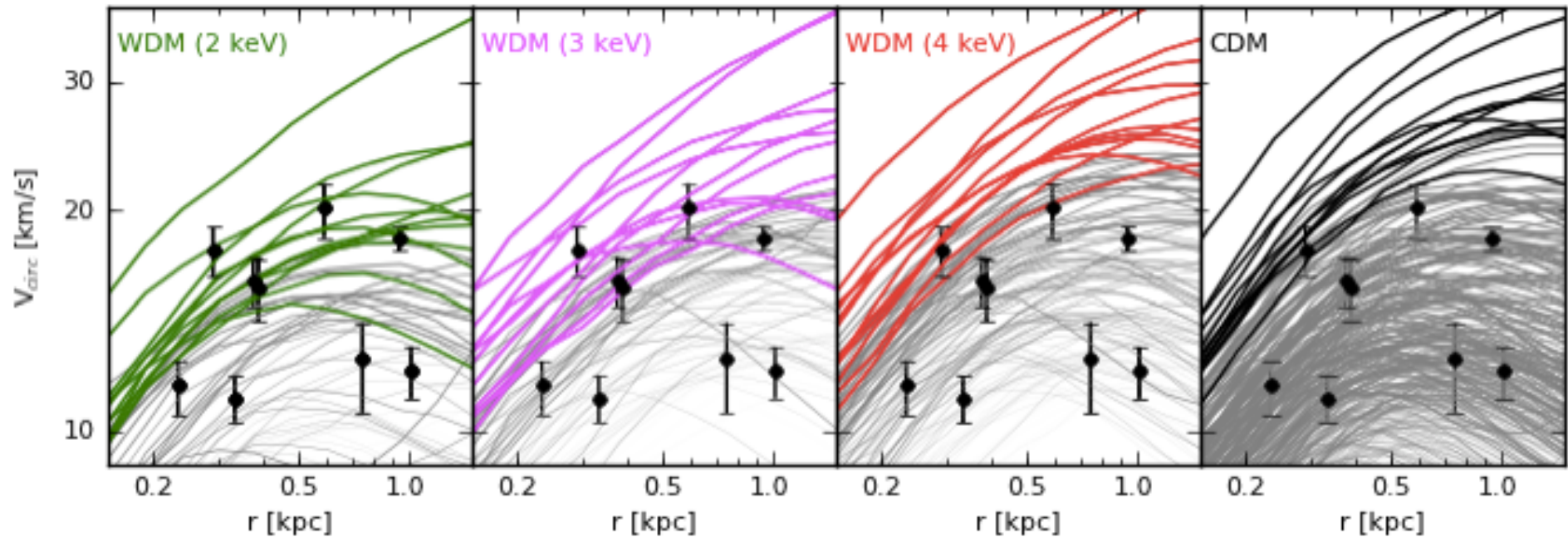
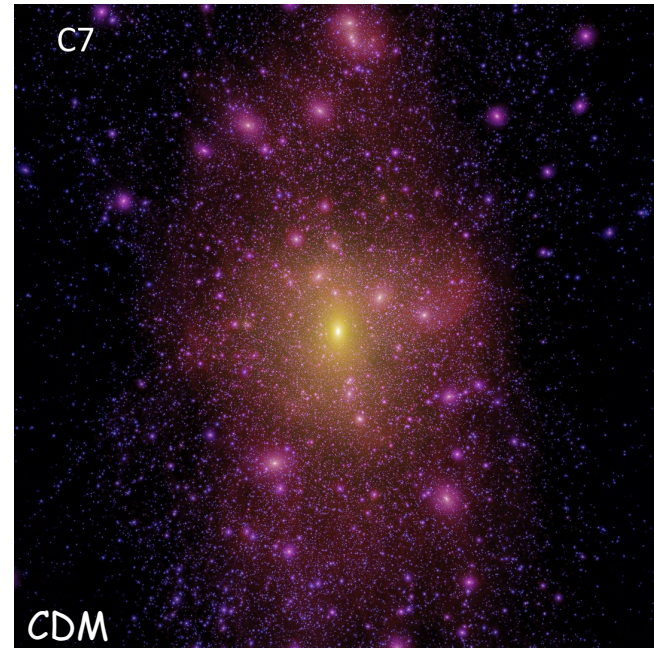


✓ Lowers the number of satellites

Lovell et al., 1308.1399  
Schneider et al., 1309.5960

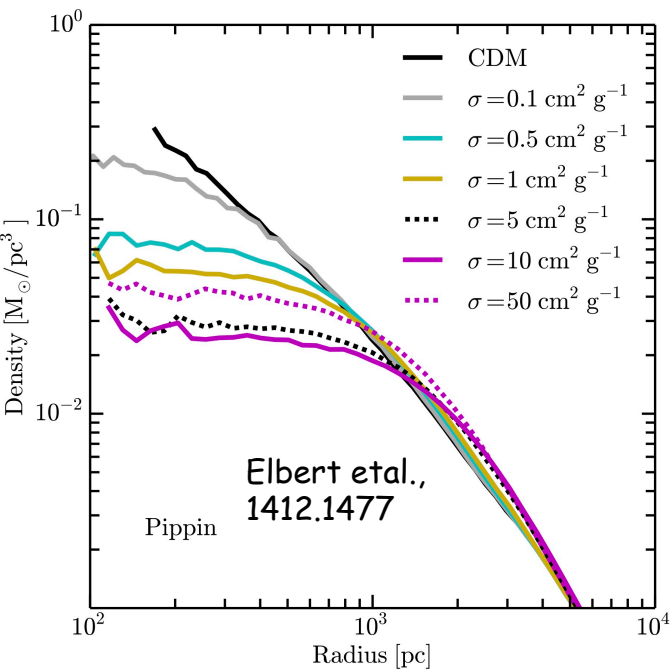
✓ Solves too big to fail  
✗ Core is too small

Ruled out by Lyman- $\alpha$ ?



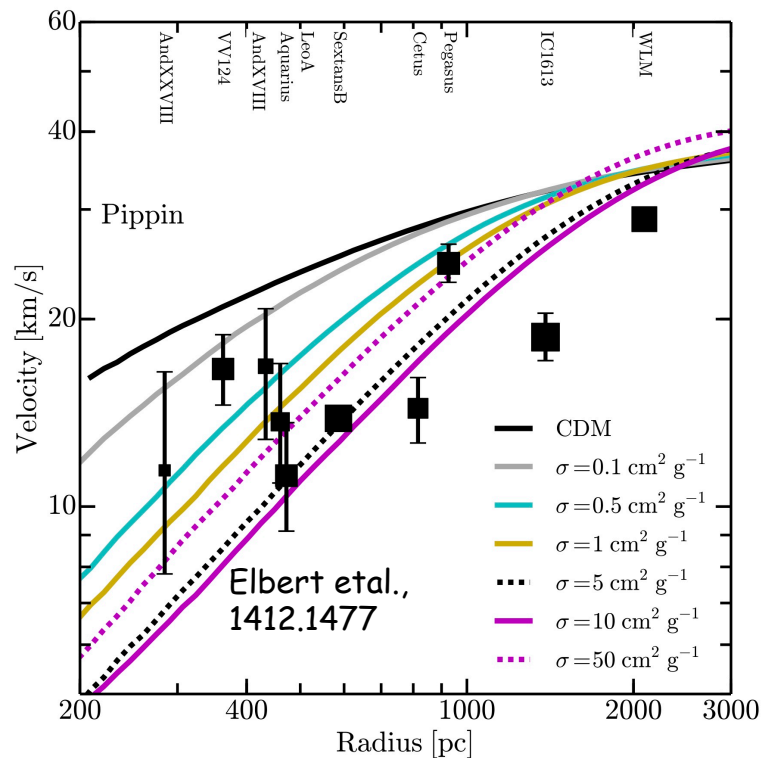


# Self-interacting dark matter (SIDM) (Spergel & Steinhardt 9909386)



✓ Solves the core vs cusp problem

✓ Solves too big to fail



Are baryons important in SIDM simulations?  
 See: Kaplinghat et al., 1311.6524, Fry et al., 1501.00497

Self-interacting dark matter

# Self-scattering cross-section

$$\Gamma = n\sigma v = \frac{\rho}{m}\sigma v$$

$$\Gamma^{-1} \sim \text{Gyr} \quad \rho = 0.4 \text{ GeV cm}^{-3} \quad v = 10^{-3}$$

$$\sigma/m \approx 1 \text{ cm}^2 \text{ g}^{-1} \quad \text{Nuclear physics cross-sections!}$$

Dark matter will interact with itself during lifetime of the Galaxy

Energy exchange and heat transport

Dark matter is **collisional** --- scatter before reaching the center for the halo

# Small scale structure problems in $\Lambda$ CDM

1. Core vs cusp problem
2. "Too big to fail" problem

Baryonic solutions exist, but can dark matter solve it?

Need self-interacting cross sections at low velocities

$$\frac{\sigma_{\text{el}}}{m} \approx 1 \text{ cm}^2 \text{ g}^{-1} \quad \text{at} \quad v \approx 10 \text{ km s}^{-1}$$

Talk to Kamakshya P Modak for discussions about the microphysical models of SIDM  
KP Modak 1509.00874

# Universality

A **predictive formalism** to obtain "strong" interactions at non relativistic physics is to have a near threshold *s*-wave resonance for a pair of particles

Egs. **Deuteron** (bound state of proton and neutron)

**X(3872)** --- probably

**Diatomic He<sup>4</sup> molecule** --- binding energy of  $10^{-7}$  eV

.....

Accidental fine-tuning of an *s*-wave resonance near the appropriate threshold

Numerous examples in cold atom physics

Can we use these ideas in dark matter physics?

# Near threshold S-wave resonance

- Non relativistic enhancements can be explained by the presence of a near threshold S-wave resonance
- If S-wave resonance is sufficiently close to threshold, all mechanisms give same universal behavior
- **Universal** = independent of microphysics

Elastic cross section  $\sigma_{\text{el}} \sim 1/v^2$

Annihilation rate  $v\sigma_{\text{ann}} \sim 1/v^2$

- A **single complex parameter**, the S-wave scattering length, governs all the lower-energy behavior of the dark matter

S-wave scattering length =  $a$

$$a = 1/\gamma$$

$\gamma$  = inverse scattering length

# Universal cross sections

Small complex inverse scattering length  $|\gamma| \ll 1/\text{range}$

$k$  = relative momentum

Elastic cross section

$$\sigma_{\text{el}} = \frac{8\pi}{|-ik - \gamma|^2}$$

Annihilation cross section

$$\sigma_{\text{ann}} = \frac{8\pi \text{Im } \gamma}{k|-ik - \gamma|^2}$$

These are for indistinguishable particles

# Universal bound state

- If the resonance is below the threshold, it is a bound state of the two identical dark matter particles - "darkonium"
- The resonance can be thought of as a dark deuteron
- Binding energy  $E_B = \frac{(\text{Re } \gamma)^2 - (\text{Im } \gamma)^2}{m}$
- Decay width  $\Gamma_{\text{darkonium}} = \frac{4(\text{Re } \gamma)(\text{Im } \gamma)}{m}$
- Stability of the darkonium implies  $\text{Im } \gamma \rightarrow 0$  and that also implies that  $\sigma_{\text{ann}} \rightarrow 0$



# Dark matter in universal bound states

- If dark matter is **asymmetric**, the resonance is stable and can act as the dark matter candidate
- Assume that the bound state survives the cosmic evolution
- Look for the signatures of the bound state in direct detection experiment
- For elastic scattering, the bound state will leave an imprint of its structure (**form factor**) and it can also **break up**; novel signature of bound state dark matter in this context

# Interplay between self-interaction cross section and binding energy

$$\sigma_{\text{el}}/m = 1 \text{ cm}^2 \text{ g}^{-1} \quad \text{at} \quad v = 10 \text{ km s}^{-1}$$

implies  $E_B = 0.52 \text{ keV}$  for  $m = 100 \text{ GeV}$

and

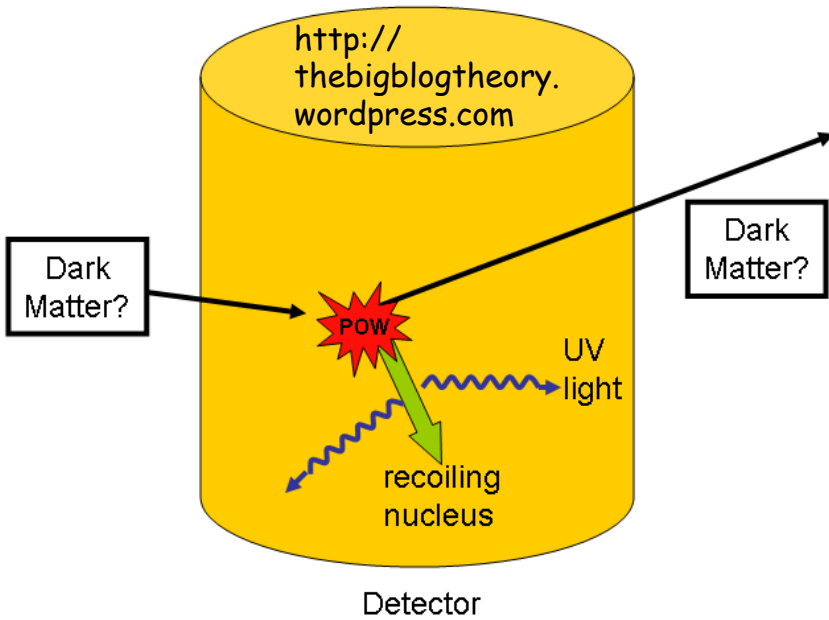
$$E_B = 54 \text{ keV} \quad \text{for} \quad m = 10 \text{ GeV}$$

Larger the elastic cross section, smaller the binding energy

$$E_B = \frac{8\pi}{m\sigma_{\text{el}}} - \frac{k^2}{m}$$

Direct detection of darkonium

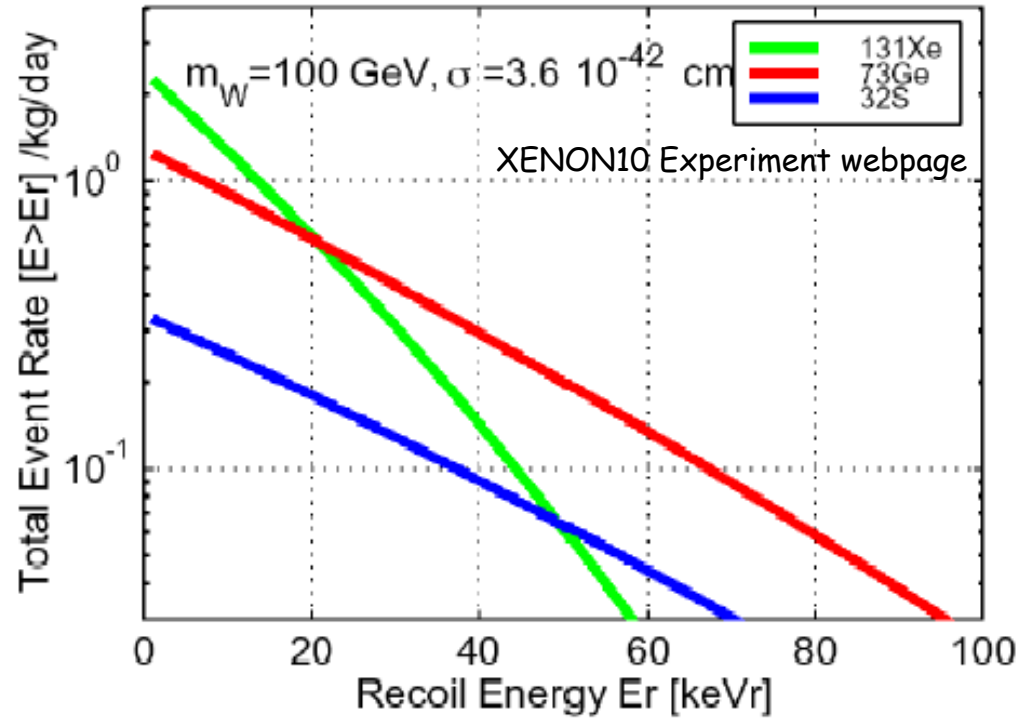
# Direct detection



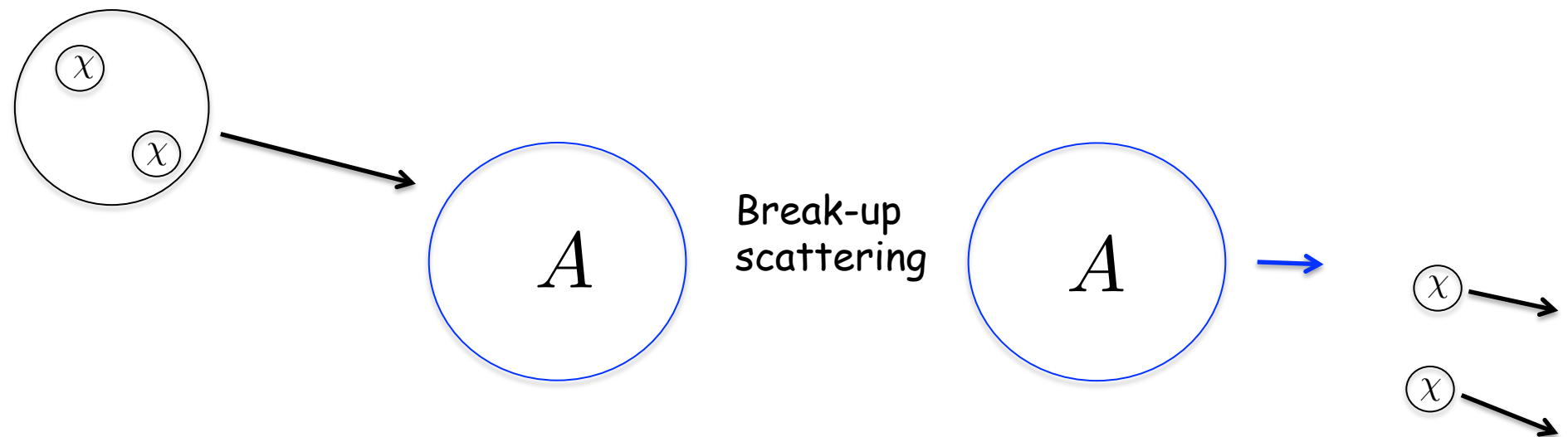
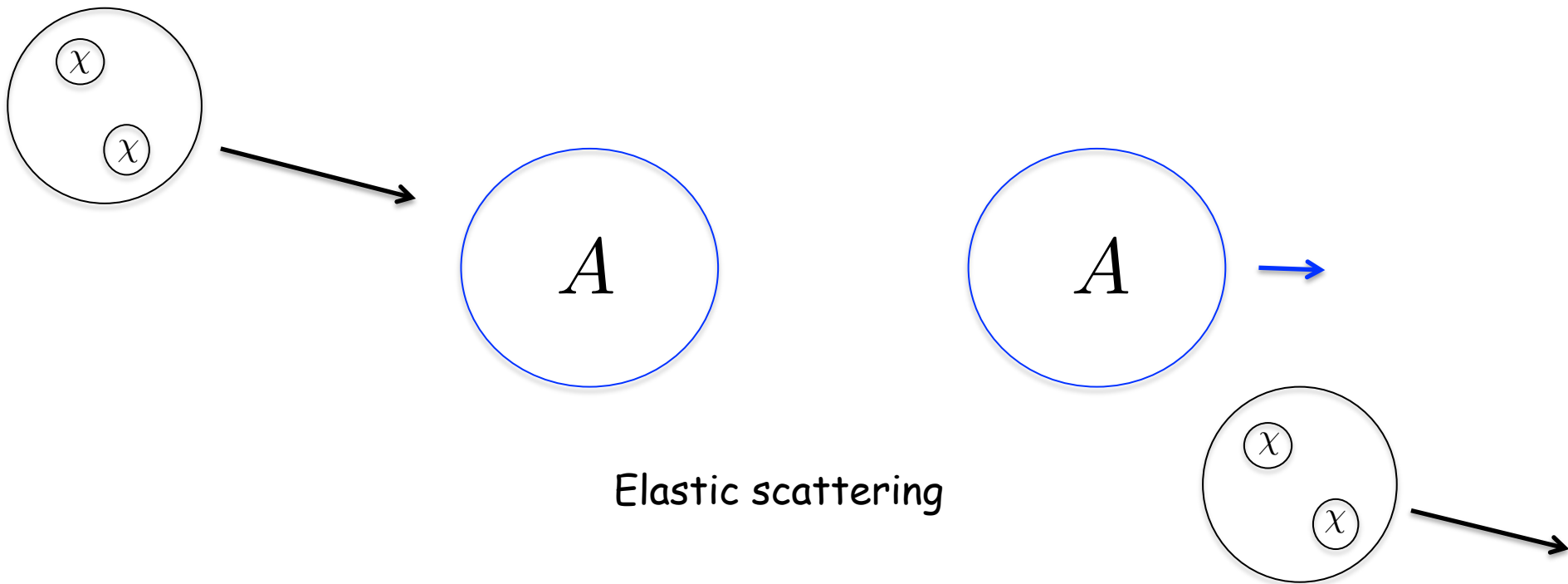
$$\text{DM} + \text{SM} \rightarrow \text{DM} + \text{SM}$$

Search for interaction of dark matter particles with Standard Model particles

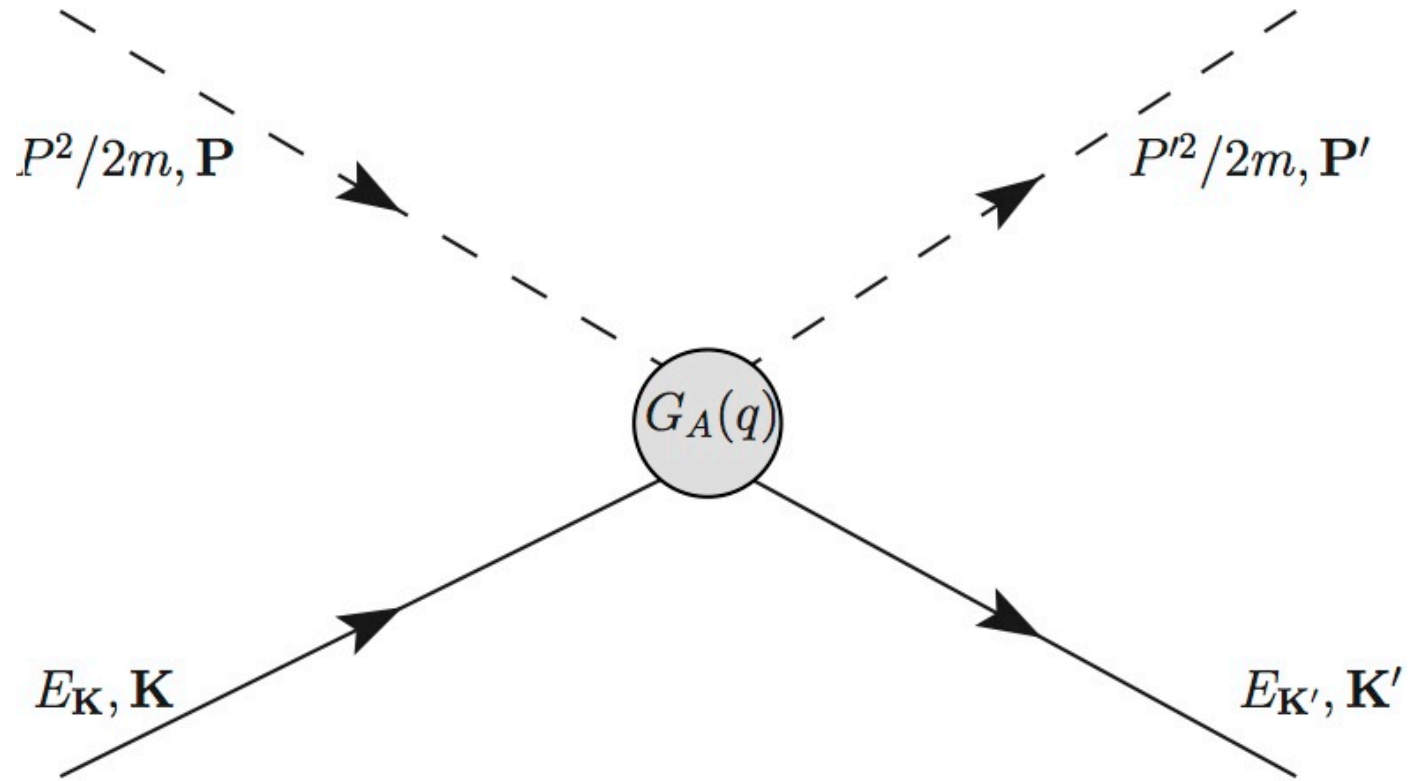
Can detect the **incoming direction** of the dark matter particle



See talk by P Gondolo, V Zacek

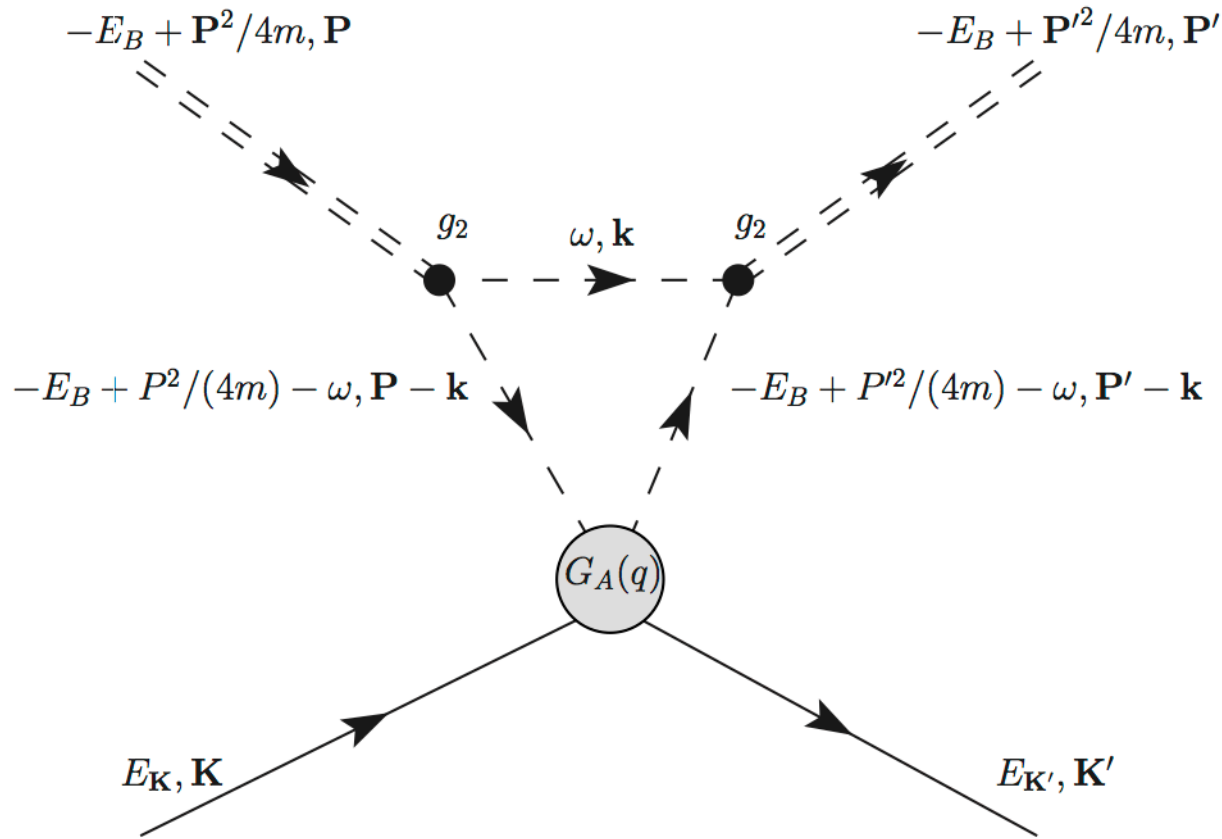


# Particle scattering



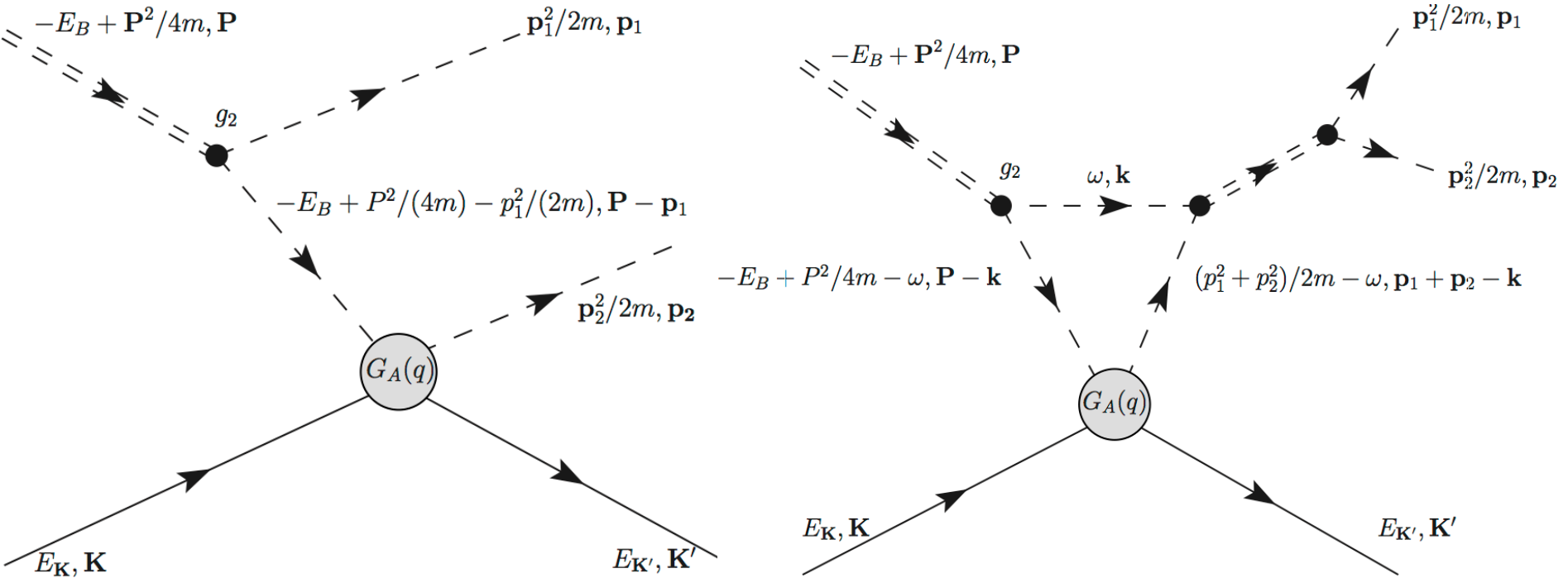
The interaction between the dark matter particle and nuclei is an arbitrary constant

# Darkonium elastic scattering



Form factor of darkonium 
$$F(q) = \frac{4\gamma}{q} \tan^{-1} \frac{q}{4\gamma}$$

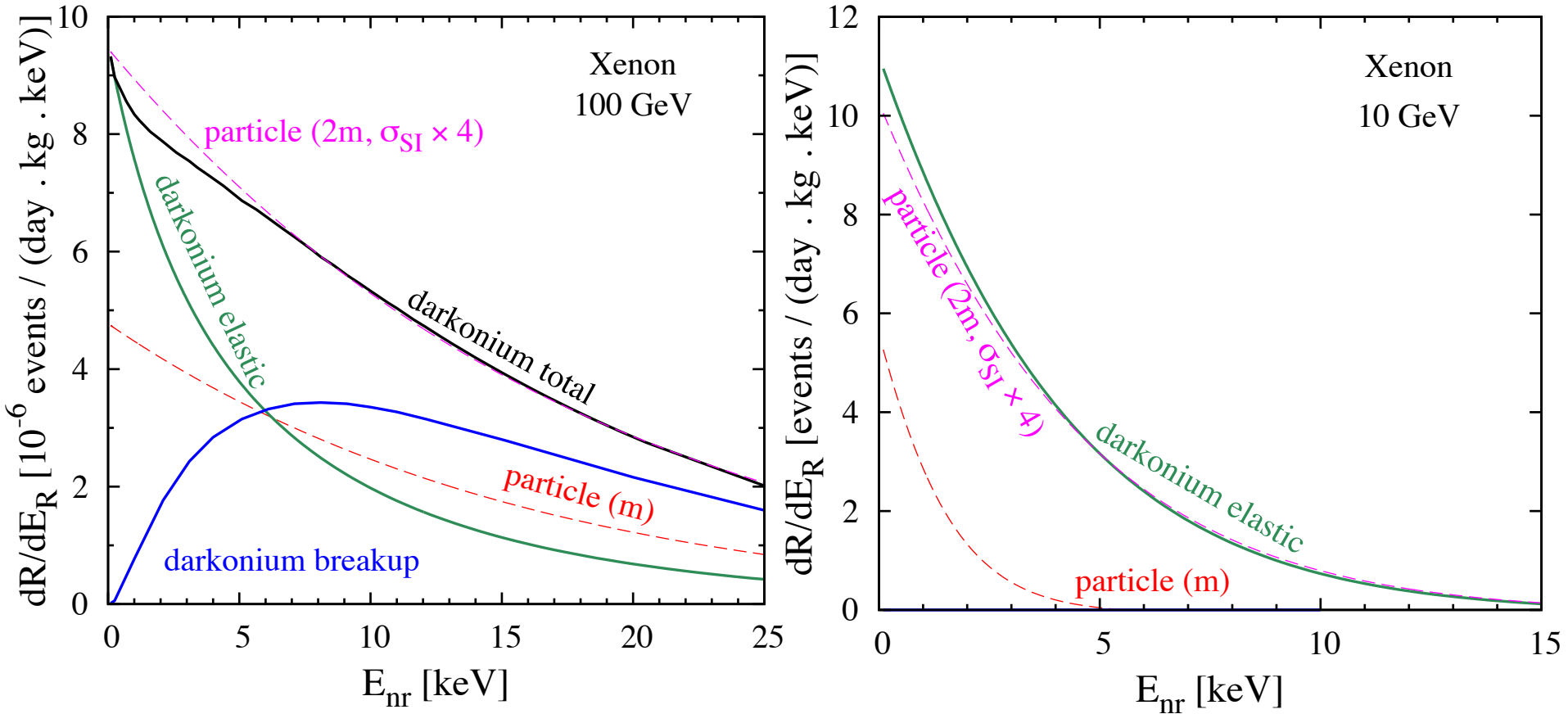
# Darkonium breakup



Darkonium breakup only possible for low enough binding energy



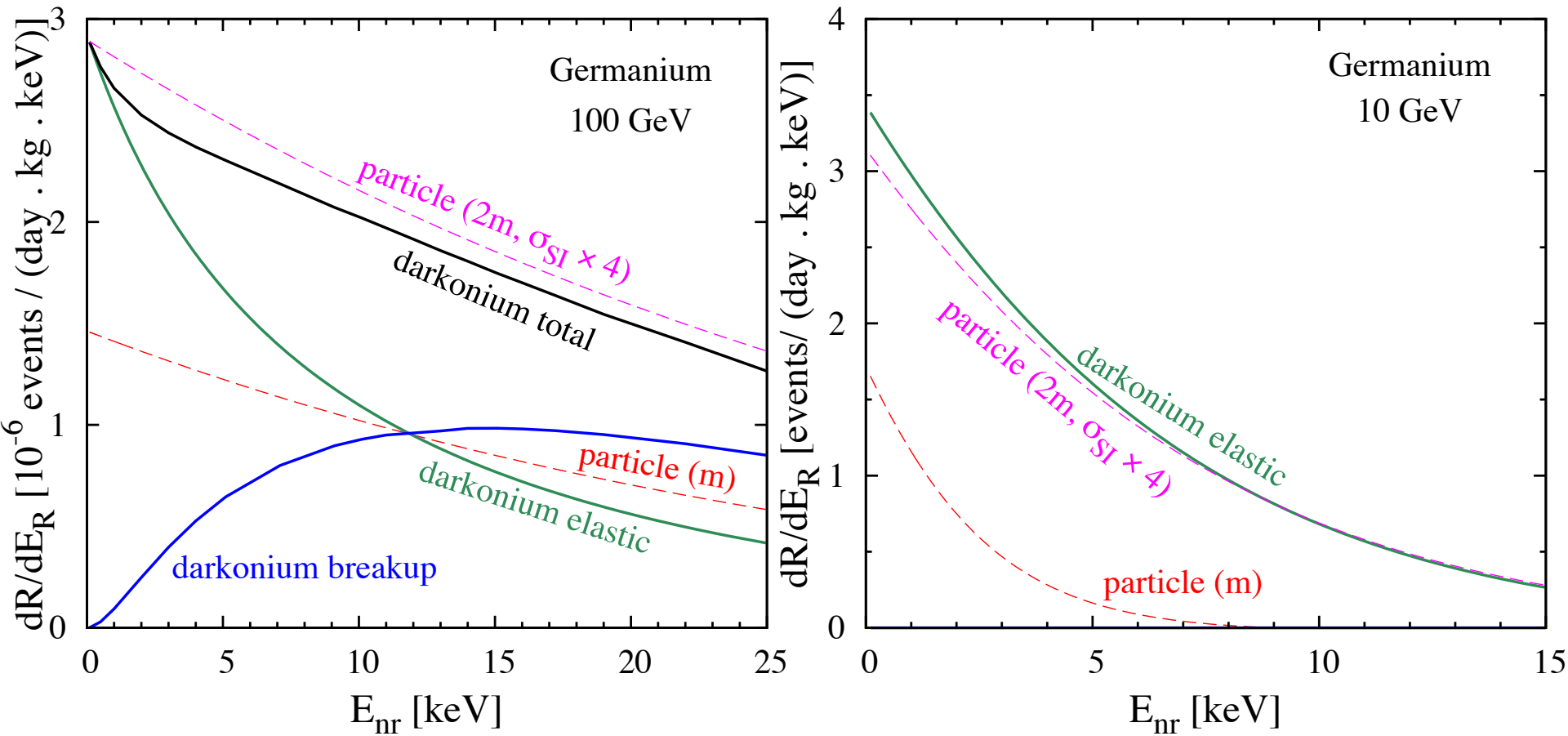
# Recoil spectrum in Xenon detectors



We assume spin-independent coupling between dark matter and nucleon

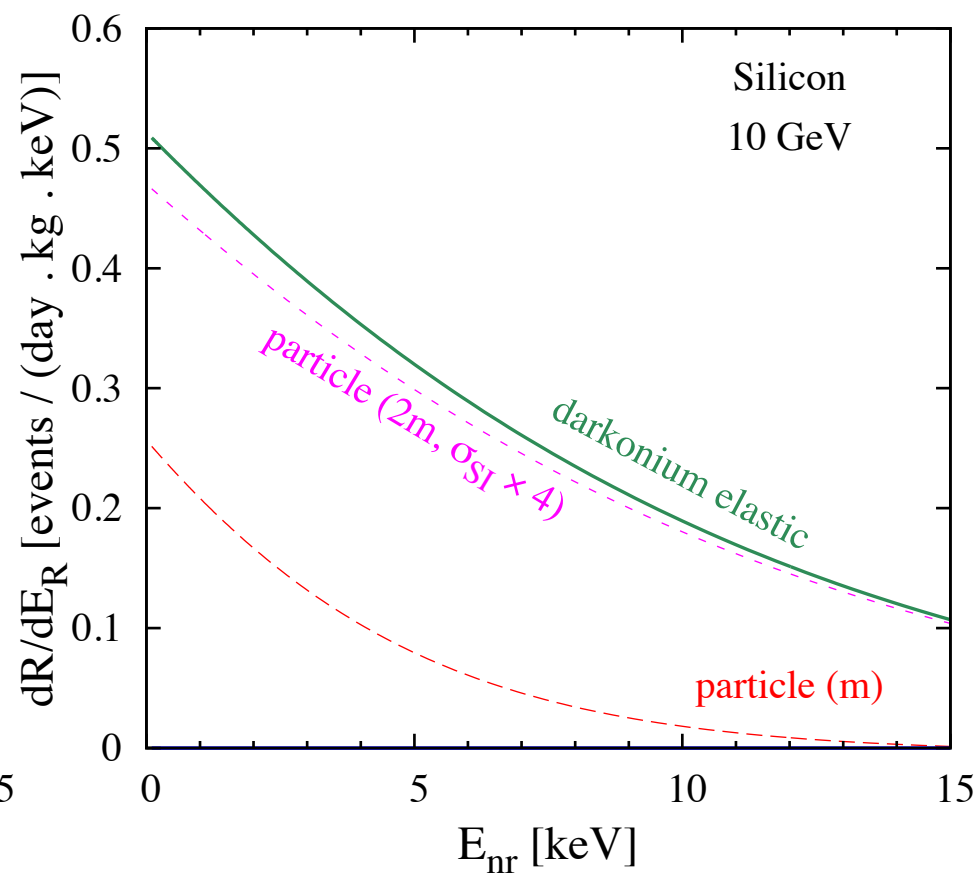
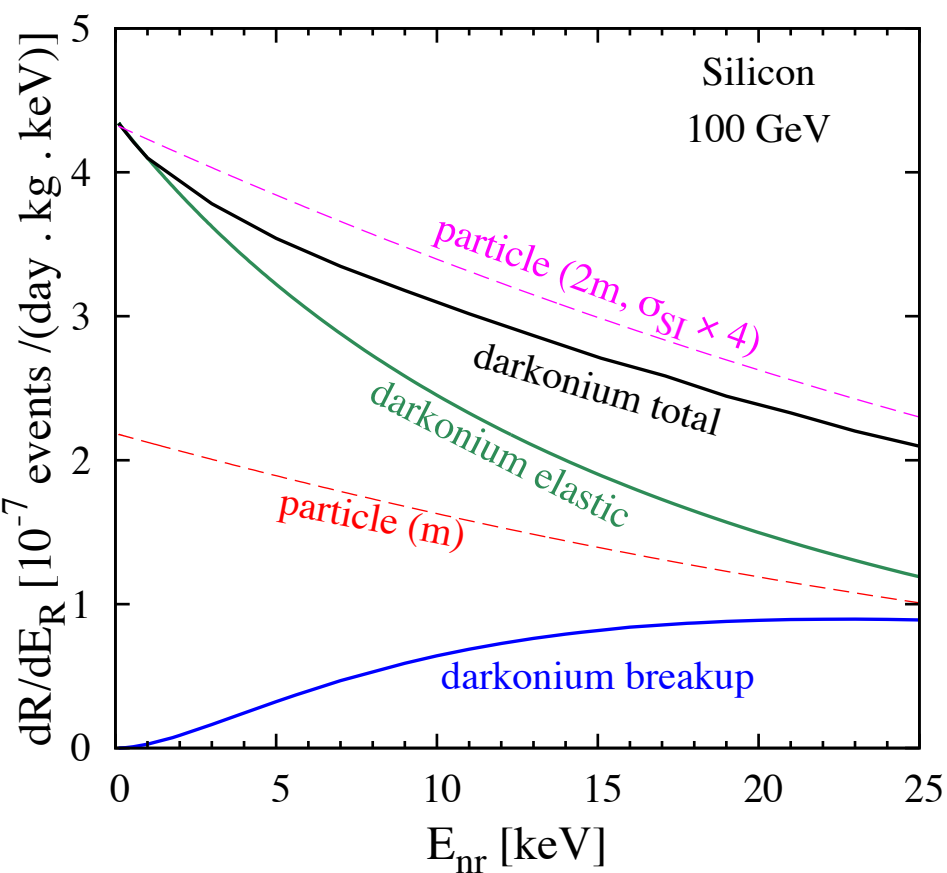
The exact value of  $\sigma_{SI}$  is just a normalization constant

# Recoil spectrum in Germanium detectors

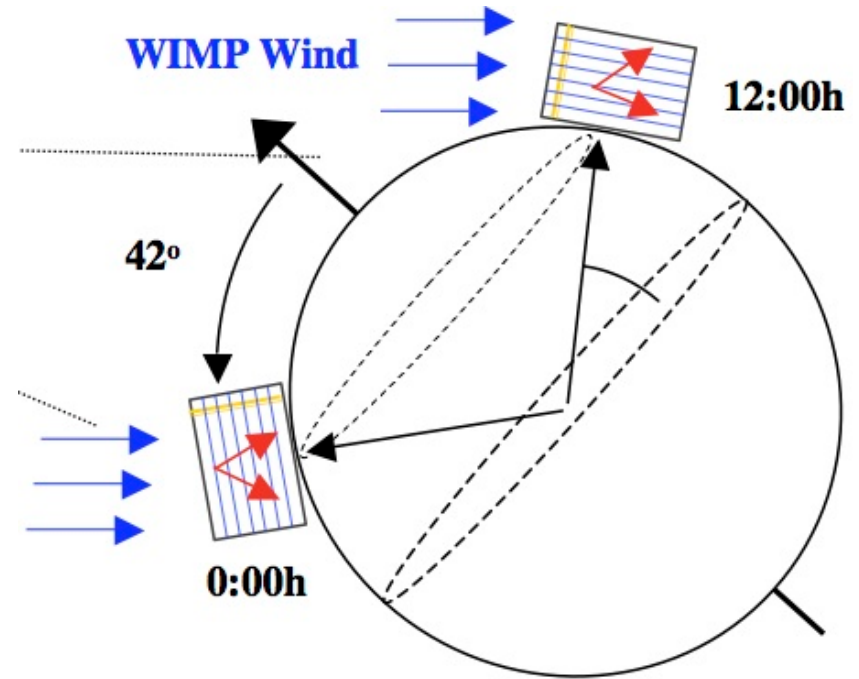
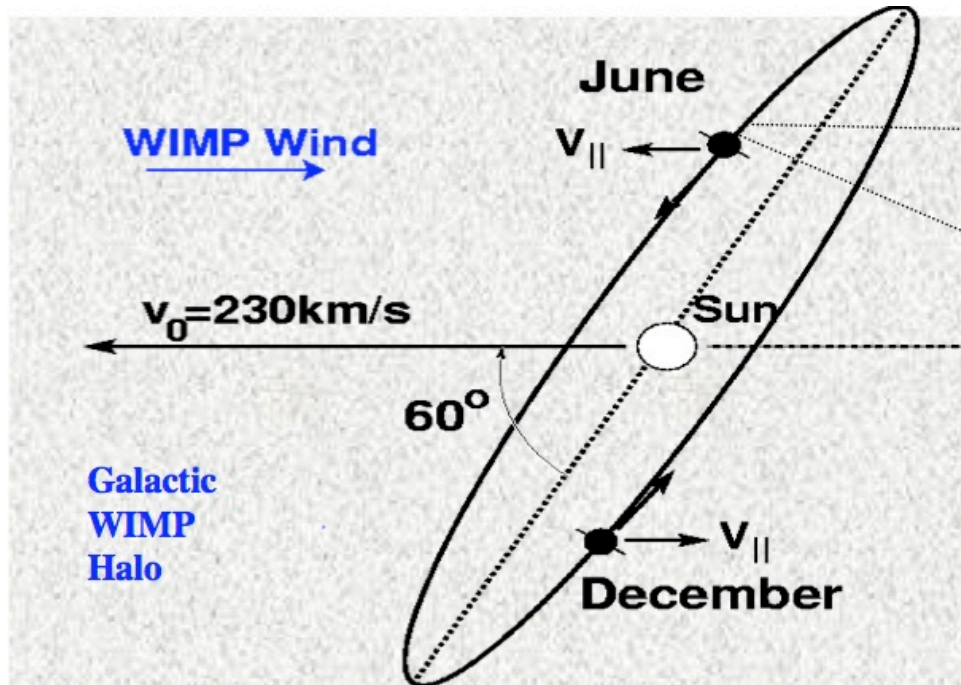


A larger value of the self-interaction cross section will produce a more dramatic signal

# Recoil spectrum in Silicon detectors

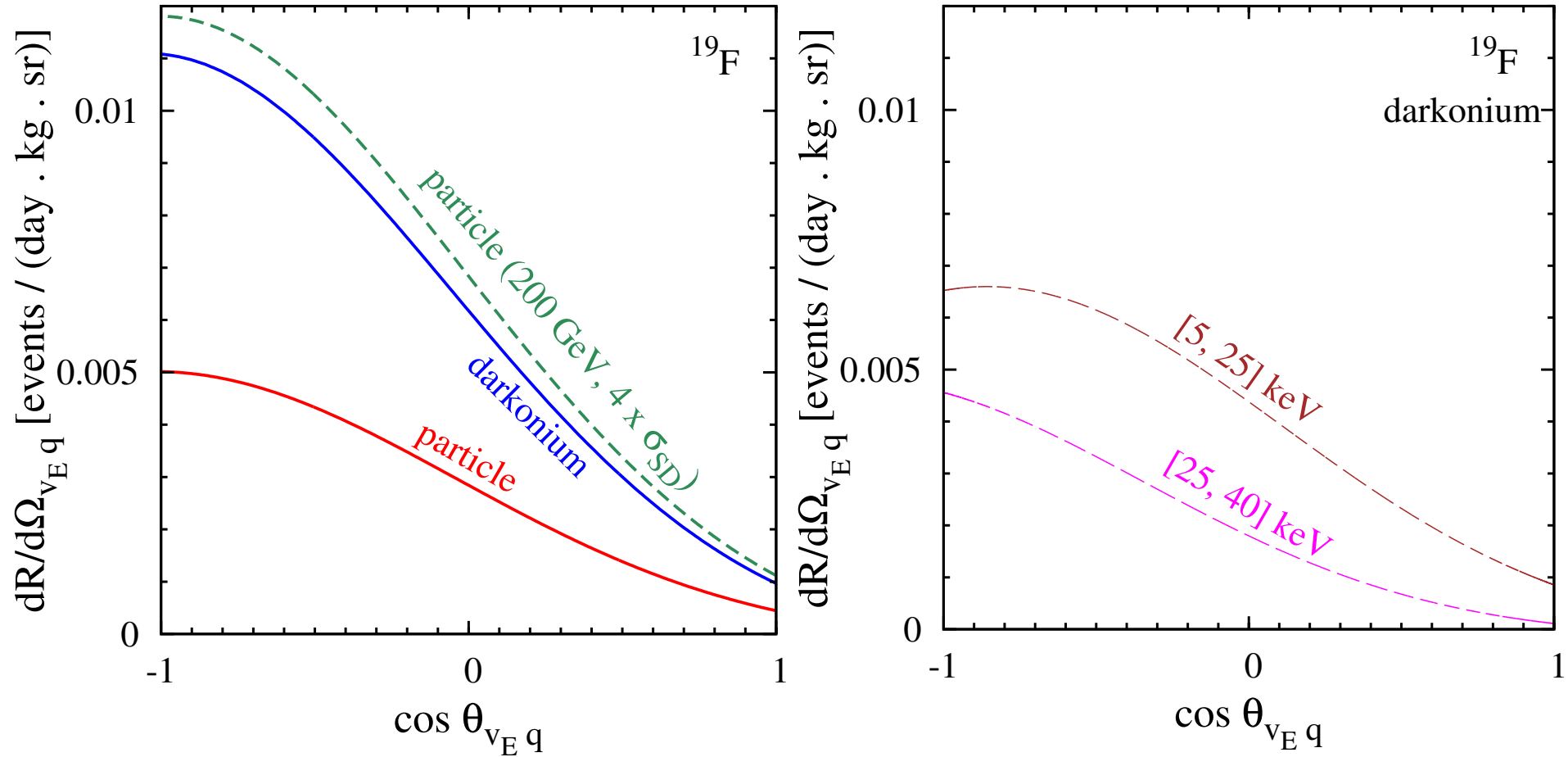


# Directional detection of dark matter



From D Loomba TeVPA/ IDM 2014

# Angular recoil spectrum

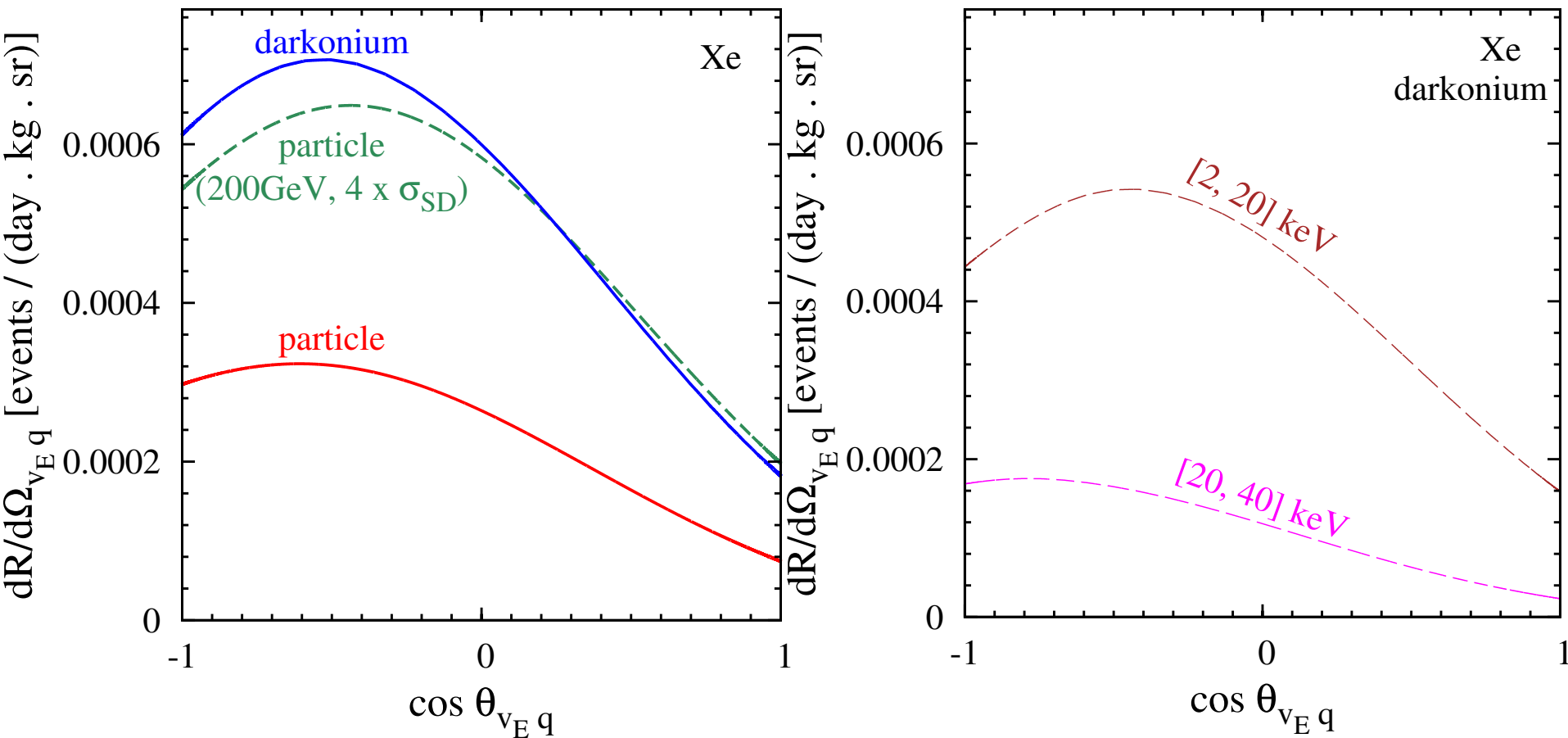


Dark matter particle mass = 100 GeV

Target =  $^{19}\text{F}$

Spin-dependent cross section =  $10^{-39} \text{ cm}^2$  (arbitrary normalisation)

# Angular recoil spectrum



Target Xenon nuclei

Isotopes relevant to spin-dependent interactions considered

# Conclusions

- Strong self-interaction between two dark matter particles can be due to a near threshold S-wave resonance
- Universality implies that the s-wave scattering length determines all the scattering properties
- The resultant bound state of dark matter can leave novel signatures in dark matter direct detection experiments
- These signatures will give confirmation about dark matter self interactions

# Some formulas

- We denote the inverse scattering length by  $\gamma$

$$\sigma_{\text{el}} = \frac{8\pi}{| -ik - \gamma |^2}$$

$$\sigma_{\text{ann}} = \frac{8\pi \text{Im } \gamma}{k | -ik - \gamma |^2}$$

$$E_B = \frac{(\text{Re } \gamma)^2 - (\text{Im } \gamma)^2}{m}$$

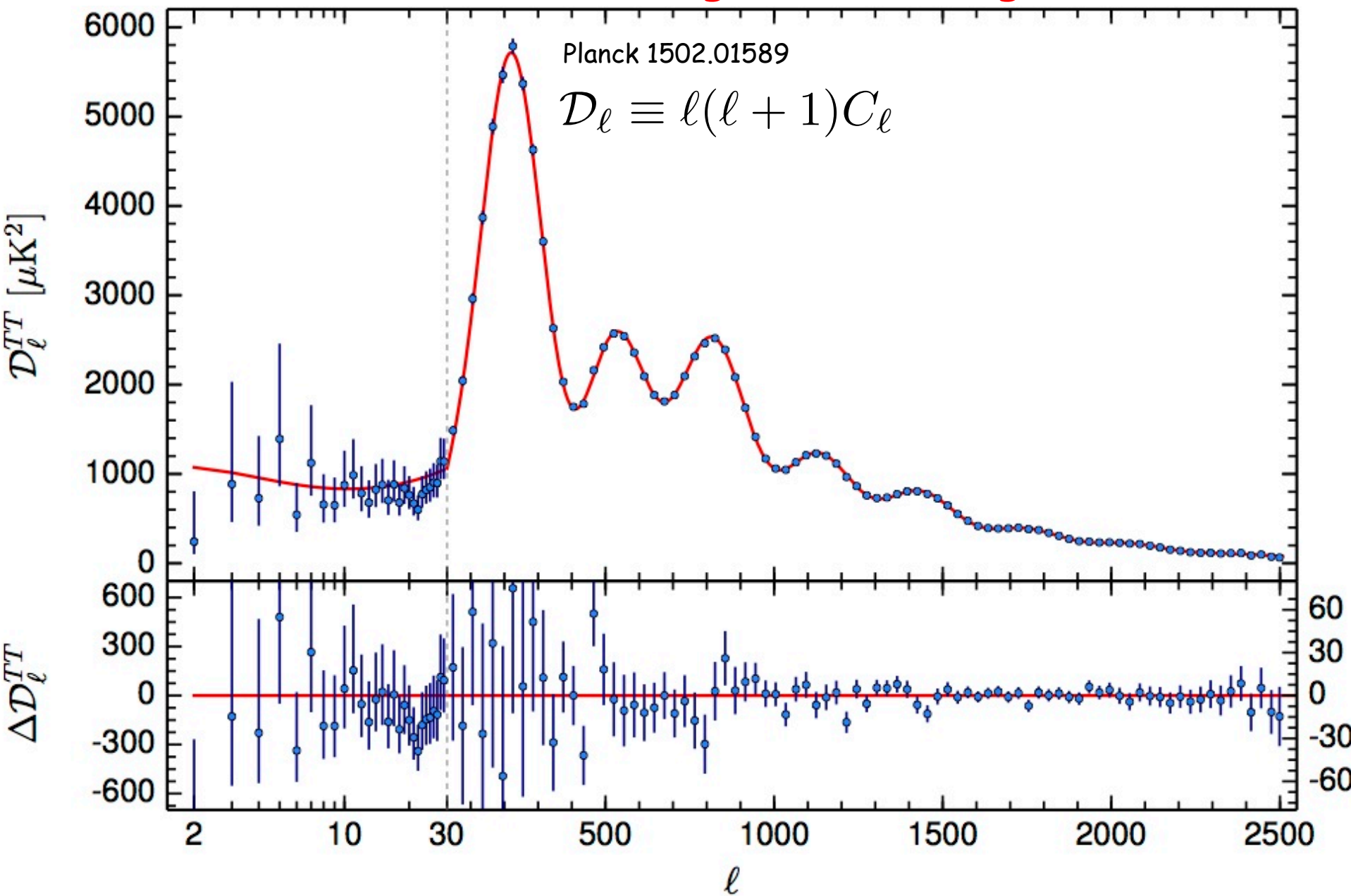
$$\Gamma_{\text{darkonium}} = \frac{4(\text{Re } \gamma)(\text{Im } \gamma)}{m}$$

- Stability of the darkonium implies  $\text{Im } \gamma \rightarrow 0$  and that also implies that  $\sigma_{\text{ann}} \rightarrow 0$
- We calculate  $\gamma$  by assuming that  $\sigma_{\text{el}}/m = 1 \text{ cm}^2/\text{g}$  at  $v = 10 \text{ km/s}$
- The “small scale structure problem” are most severe at dwarf galaxies



The success of  $\Lambda$ CDM

# Cosmic Microwave Background --- largest scales



# Illustris Simulation



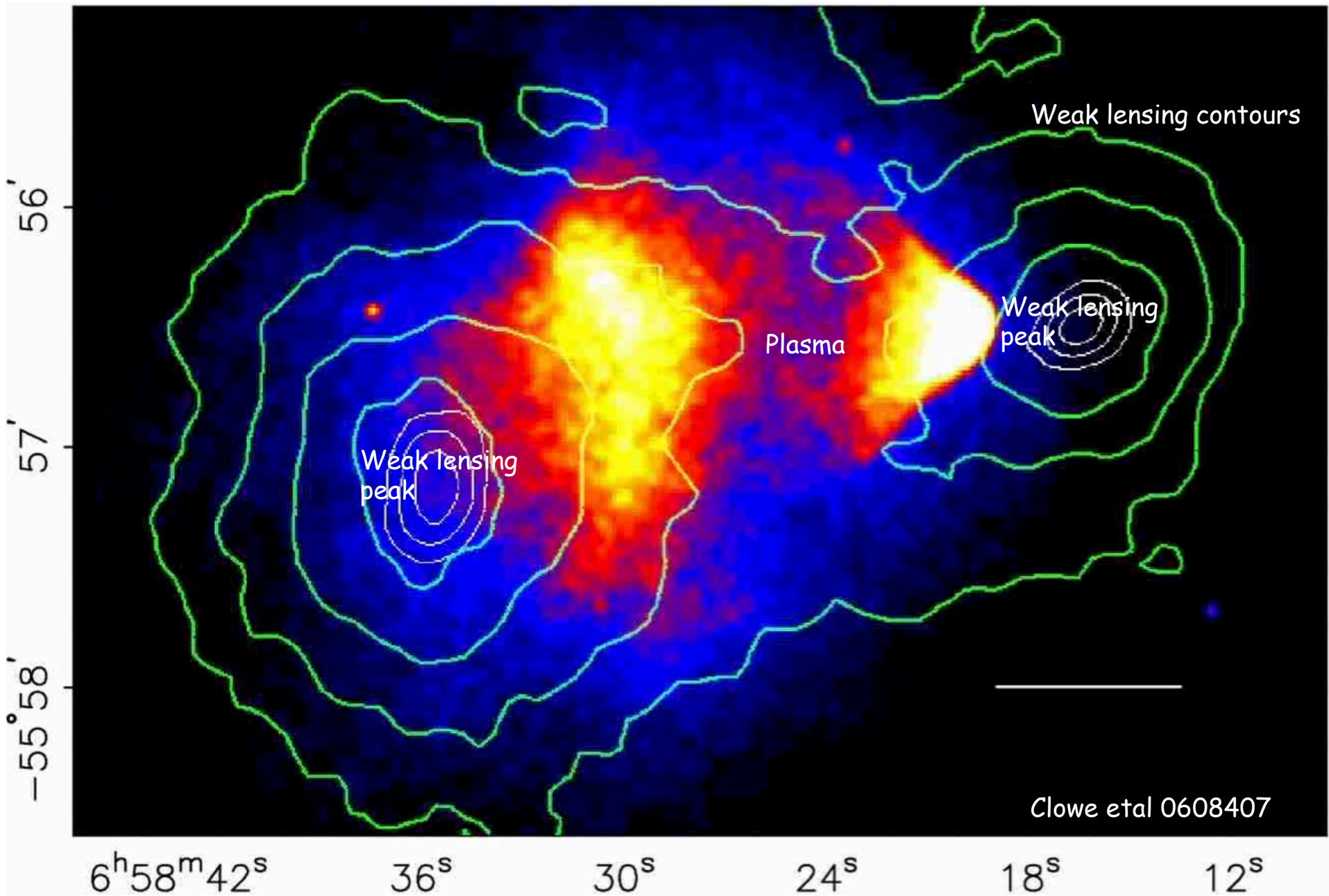
Credit: NASA/ESA, STScI/MAST, Illingworth, et al. 2013  
<http://archive.stsci.edu/prepds/edf/>

**Real** observation from Hubble eXtreme Deep Field  
Observations: **left** side

<http://www.illustris-project.org/media/>

**Mock** observation from Illustris: **right** side

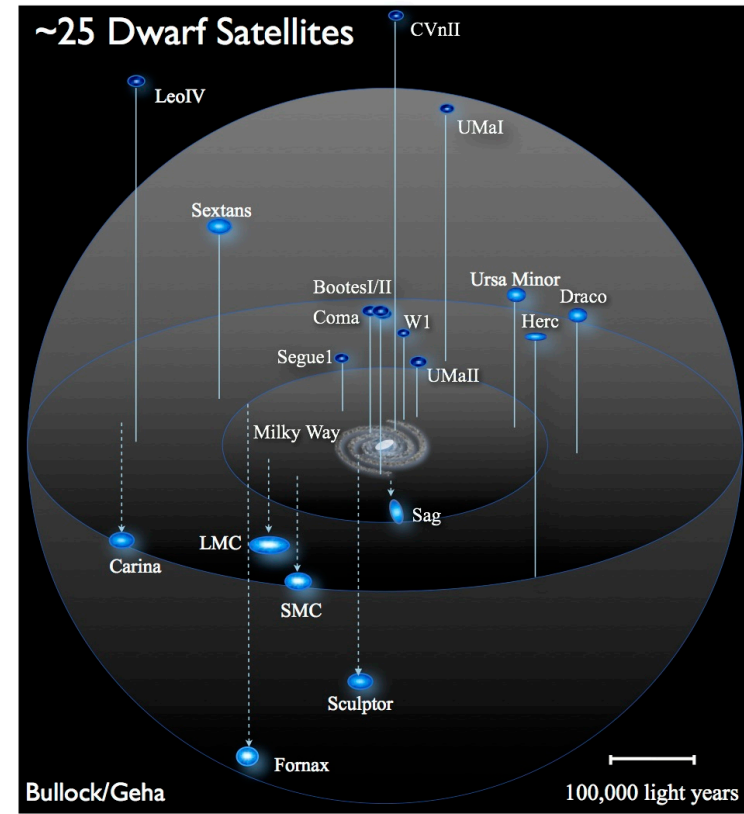
# Cluster collision



# Missing satellites problem



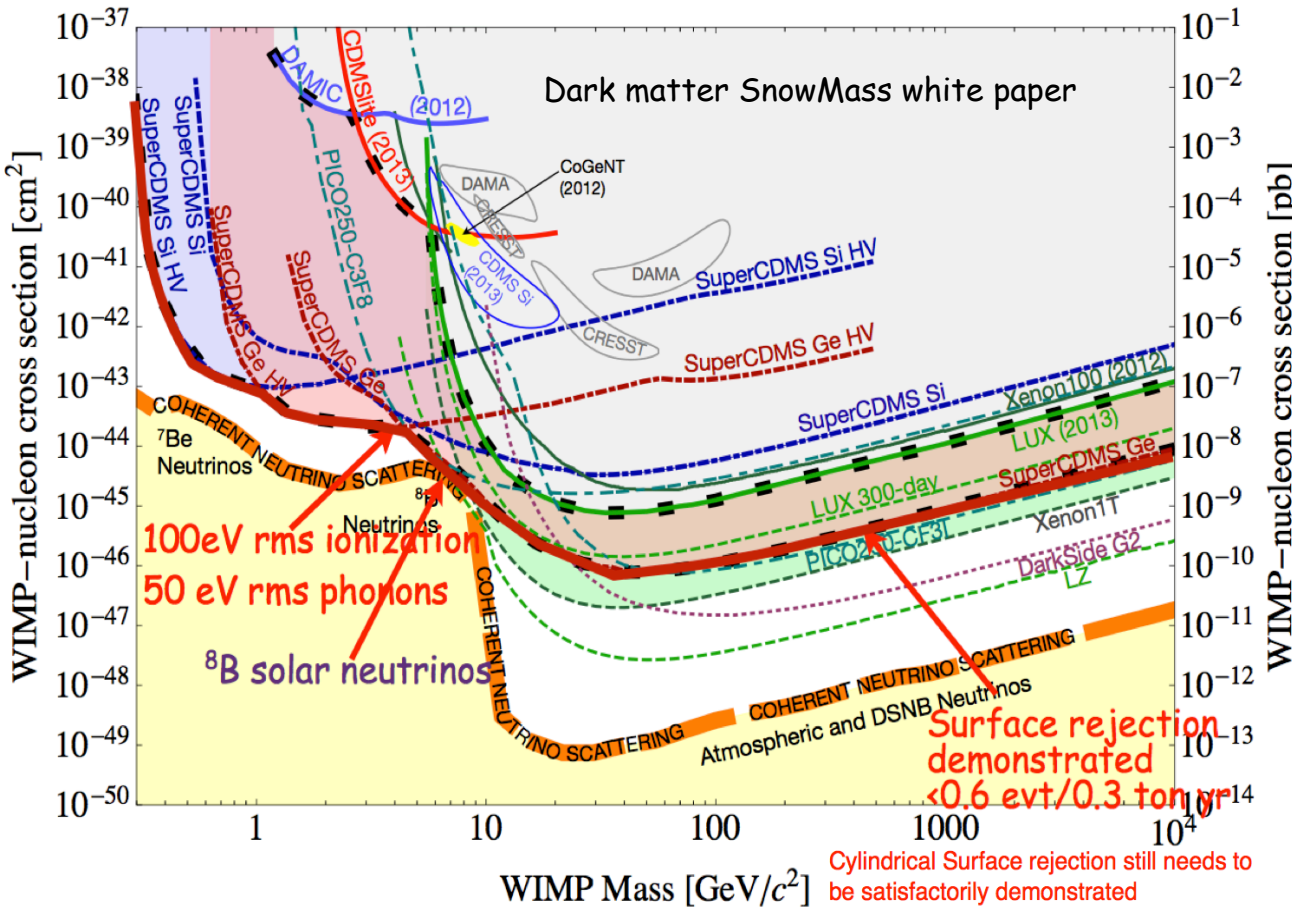
Simulation Aquarius project



Approximately **an order of magnitude** of "missing satellites"

Will increased sky coverage help? Yes!

# Direct detection limits



Typically all "anomalies" are near the threshold of the detector

Direct probe of the local dark matter density and velocity profile

No discovery yet

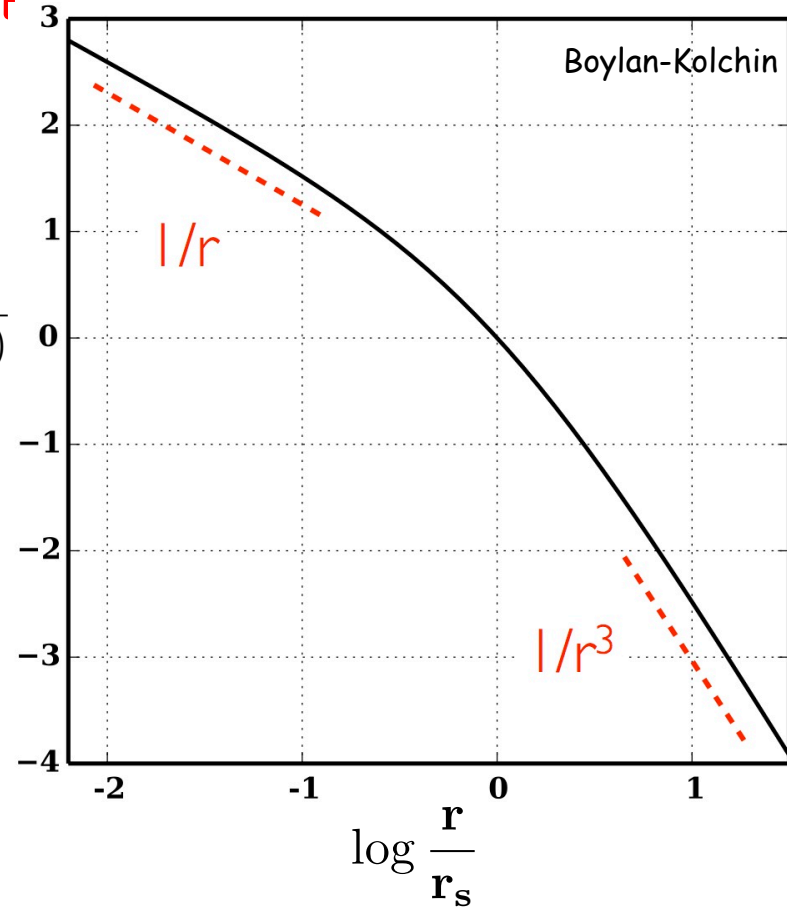
Can soon re-discover neutrinos using this technique!

# Core vs cusp problem

From simulations

$$\rho(r) = \frac{\rho_s}{\left(\frac{r}{r_s}\right) \left(1 + \frac{r}{r_s}\right)^2}$$

$$\log \frac{\rho(\mathbf{r})}{\rho(\mathbf{r}_s)}$$



2 free parameters:  $\rho_s$  and  $r_s$

Typically replaced by more meaningful parameters from simulations:

$$M_{\text{vir}} \text{ and } C_{\text{vir}} = r_{\text{vir}}/r_s$$