Higgs and Precision Observables at the ILC and TLEP/FCC-ee

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CERN, 06/2015

- 1. Introduction
- 2. Electroweak Precision Observables
- 3. Higgs Observables
- 4. Conclusions

Experimental situation:

LHC/ILC/FCC-ee/TLEP/... will provide (high!) accuracy measurements!

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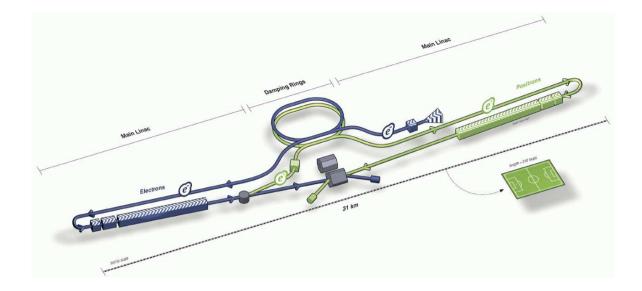
Theoretical calculations should be viewed as an essential part of all (current and future)

High Energy Physics programs

ILC: Linear e^+e^- collider, $\sqrt{s} = 250 - 1000$ GeV

based on superconducting cavities (cold technology)

Schematic:



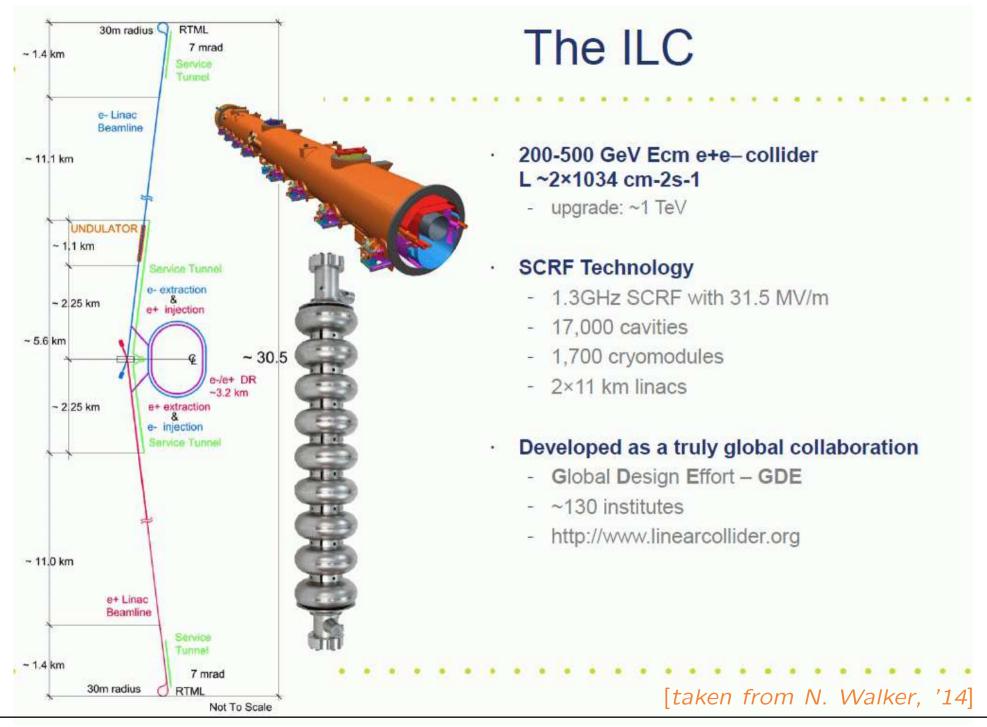
Energies: $\sqrt{s} = 250$ GeV, 350 GeV, 500 GeV ... 1000 GeV

Possible features:

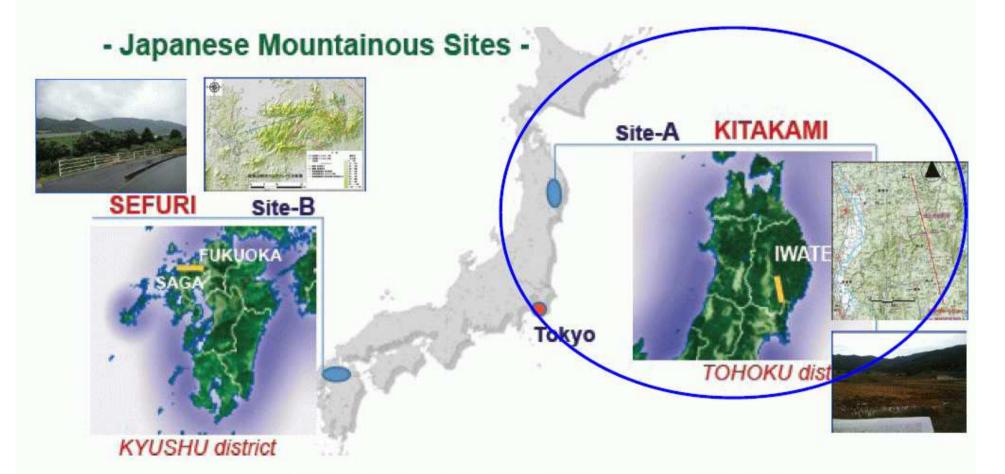
- two detectors in one interaction region (push-pull)
- undulator based e^+ source
- polarized beams for e^- and e^+ ($P_{e^-}=80\%$, $P_{e^+}=60\%$)
- tunable energy

Other ILC options:

- GigaZ: running with high luminosity at low energies (Z pole, WW threshold)
- $\underline{\gamma\gamma}$: use both beams to produce high-energy photons (e.g. heavy Higgs production in the s channel, $\Gamma(H \to \gamma\gamma)$, ...)
- $\underline{e^-\gamma}$: use one e^- beam to produce high-energy photons produce charged particles in the s channel
- e^-e^- : produce doubly charged particles in the s channel
- ⇒ to optimize physics potential!



Possible candidate sites



LCC technical efforts focused on Kitakami site (Ratified in independent technical evaluation by KEK and LCC) No "formal" political decision taken yet.

[taken from N. Walker, '14]

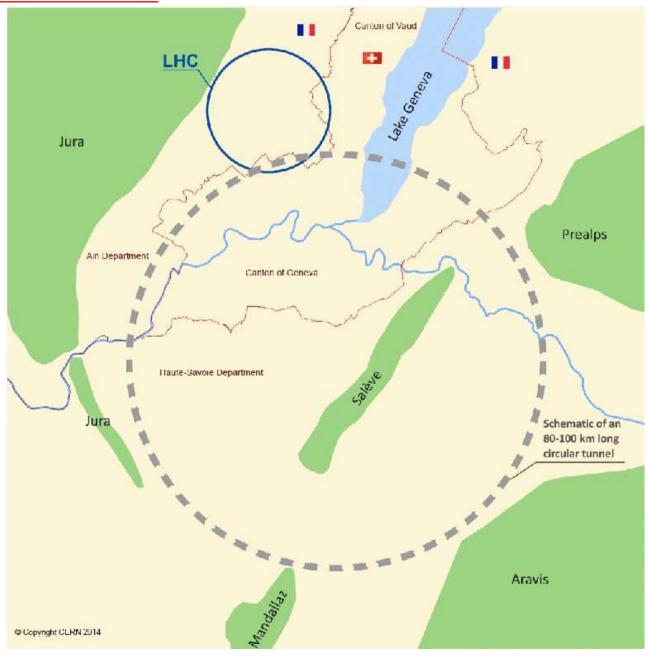
ilc

Outlook

- The ILC is a mature project.
 - Main technologies exist
 - But clearly much engineering" to be done (requiring substantial funding)
- The primary hurdles now are political
- Focus on Japan
 - MEXT evaluation should be complete by next Spring
 - Further evaluation by SCJ
 - Expecting some statement from Japan in 2016
- European and US HEP strategies both make positive statements on a "Japanese hosted ILC"
 - But negotiations with governments has not yet started waiting for Japan to make "first move"
- International technical effort (LCC) focused on site-dependent design
 - But we are totally under resourced!
 - Making progress where we can
 - US funding situation (post-P5) looks better
- All scenarios put first physics towards the end of 2020's
 - 10 construction & commissioning schedule
 - Can't possibly start before 2016 (and likely to be later).

[taken from N. Walker, '14]

FCC: a 100 km ring . . .



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FCC: a 100 km ring for 3 colliders:



FCC-hh: pp

FCC-ee: $e^+e^- \leftarrow \text{focus here}$

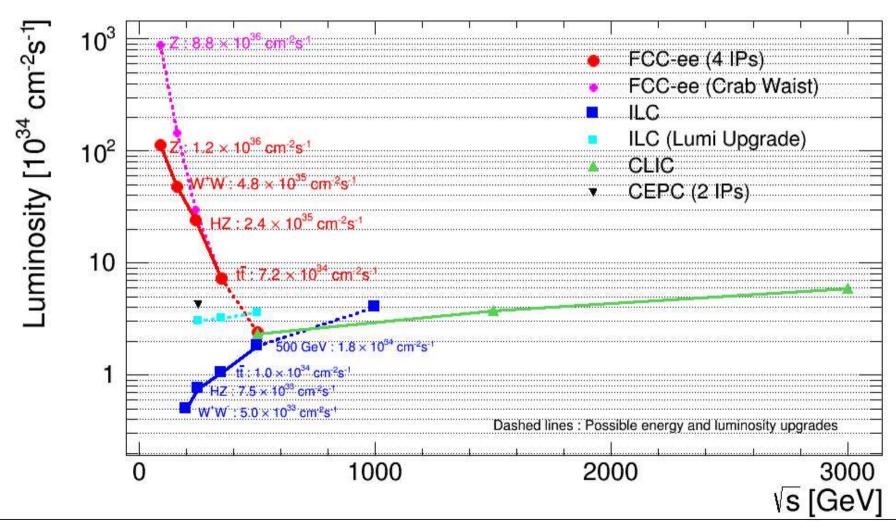
FCC-eh: pe

FCC-ee:

 e^+e^- collisions in a 100 km tunnel with $\sqrt{s}\lesssim$ 350 GeV

 $\mathcal{L} \sim 6 \times 10^{34} \, \text{cm}^{-2} \, \text{s}^{-1}$ (for Higgs physics)

4 interaction regions for maxium luminosity



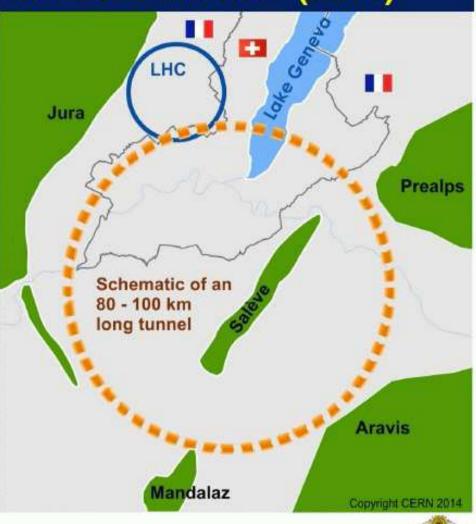
Future Circular Collider Study - SCOPE CDR and cost review for the next ESU (2018)

Forming an international collaboration to study:

pp-collider (FCC-hh)
 → defining
 infrastructure

~16 T \Rightarrow 100 TeV pp in 100 km ~20 T \Rightarrow 100 TeV pp in 80 km

- e⁺e⁻ collider (FCC-ee) as potential intermediate step ECM=90-400 GeV
- p-e (FCC-he) option
- 80-100 km infrastructure in Geneva area Alain Blondelus Colliders





TLEP: PARAMETERS & STATISTICS

 $(e^+e^- \rightarrow ZH, e^+e^- \rightarrow W^+W^-, e^+e^- \rightarrow Z, [e^+e^- \rightarrow t\bar{t}])$

	TLEP-4 IP, per IP	statistics	
circumference	80 km		
max beam energy	175 GeV		
no. of IPs	4		
Luminosity/IP at 350 GeV c.m.	1.3x10 ³⁴ cm ⁻² s ⁻¹	10 ⁶ tt pairs	
Luminosity/IP at 240 GeV c.m.	6.0x10 ³⁴ cm ⁻² s ⁻¹	2 10 ⁶ ZH evts	
Luminosity/IP at 160 GeV c.m.	1.6x10 ³⁵ cm ⁻² s ⁻¹	10 ⁸ WW pairs	
Luminosity/IP at 90 GeV c.m.	2. 10 ^{35/36} cm ⁻² s ⁻¹	10 ^{12/13} Z	
		decays	

at the Z pole repeat the LEP physics programme in a few minutes...





Phenomenology working groups:

Phenomenology studies

The phenomenological studies are coordinated by John Ellis and Chistophe Grojean, and are organized in five working groups:

- Working Group 1: QCD and yy physics (joint exp/th). Convener: Peter Skands □
- Working Group 2: Precision EW calculations. Convener: Sven Heinemeyer
- Working Group 3: Flavour physics (joint exp/th). Convener: Jernej Kamenik™
- Working Group 4: Model building and new physics. Convener: Andreas Weiler ₪
- Working Group 5: Global analysis, combination, complementarity. Convener: John Ellis ₪

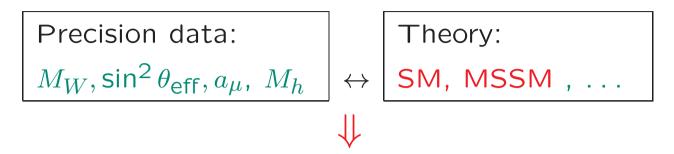
 \Rightarrow here mostly relevant: WG2 :-)

My personal time scale wish/estimate:

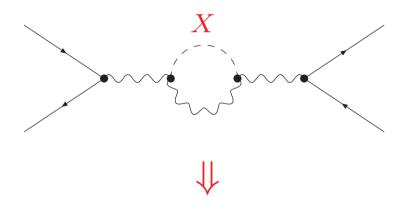
- 1. exploit the LHC
- 2. construct the ILC as quickly as possible in Japan
- 3. after LHC construct the FCC at CERN depending on physics outcome of LHC/ILC: decide whether to start with FCC-ee or FCC-hh

2. Electroweak Precision Observables

Comparison of observables with theory:



Test of theory at quantum level: Sensitivity to loop corrections, e.g. X



SM: limits on M_H , BSM: limits on M_X

Very high accuracy of measurements and theoretical predictions needed ⇒ only models "ready" so far: SM, MSSM

Precision observables in the SM and the MSSM

$$M_W$$
, $\sin^2 \theta_{\rm eff}$, M_h , $(g-2)_{\mu}$, b physics, ...

A) Theoretical prediction for M_W in terms

of
$$M_Z,\alpha,G_\mu,\Delta r$$
:
$$M_W^2\left(1-\frac{M_W^2}{M_Z^2}\right)=\frac{\pi\,\alpha}{\sqrt{2}\,G_\mu}(1+\Delta r)$$

$$\updownarrow$$
 loop corrections

Evaluate Δr from μ decay $\Rightarrow M_W$

One-loop result for M_W in the SM:

[A. Sirlin '80], [W. Marciano, A. Sirlin '80]

$$\Delta r_{1-\mathsf{loop}} = \Delta \alpha - \frac{c_{\mathsf{W}}^2}{s_{\mathsf{W}}^2} \Delta \rho + \Delta r_{\mathsf{rem}}(M_H)$$
 $\sim \log \frac{M_Z}{m_f} \sim m_t^2 \log (M_H/M_W)$
 $\sim 6\% \sim 3.3\% \sim 1\%$

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loop corrections

B) Effective mixing angle:

$$\sin^2\theta_{\mathrm{eff}} = \frac{1}{4\,|Q_f|} \left(1 - \frac{\mathrm{Re}\,g_V^f}{\mathrm{Re}\,g_A^f} \right)$$

Higher order contributions:

$$g_V^f o g_V^f + \Delta g_V^f, \quad g_A^f o g_A^f + \Delta g_A^f$$

Corrections to M_W , $\sin^2\theta_{\rm eff} \to {\rm approximation}$ via the ρ -parameter:

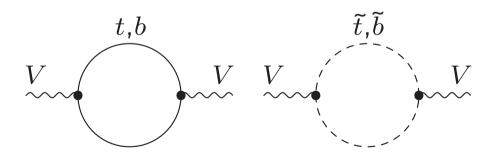
ho measures the relative strength between neutral current interaction and charged current interaction

$$\rho = \frac{1}{1 - \Delta \rho} \qquad \qquad \Delta \rho = \frac{\Sigma_Z(0)}{M_Z^2} - \frac{\Sigma_W(0)}{M_W^2}$$

(leading, process independent terms)

 $\triangle \rho$ gives the main contribution to EW observables:

$$\Delta M_W \approx \frac{M_W}{2} \frac{c_{\rm W}^2}{c_{\rm W}^2 - s_{\rm W}^2} \Delta \rho, \qquad \Delta \sin^2 \theta_W^{\rm eff} \approx -\frac{c_{\rm W}^2 s_{\rm W}^2}{c_{\rm W}^2 - s_{\rm W}^2} \Delta \rho$$



$$\Delta \rho^{\rm SUSY} \ {\rm from} \ \tilde{t}/\tilde{b} \ {\rm loops} > 0 \\ \Rightarrow M_W^{\rm SUSY} \gtrsim M_W^{\rm SM}, \ \sin^2\theta_{\rm eff}^{\rm SUSY} \lesssim \sin^2\theta_{\rm eff}^{\rm SM}$$

 $\Delta
ho^{
m SUSY}$ from $ilde{t}/ ilde{b}$ loops >0 $\Rightarrow M_W^{
m SUSY} \gtrsim M_W^{
m SM}$, $\sin^2 heta_{
m eff}^{
m SUSY} \lesssim \sin^2 heta_{
m eff}^{
m SM}$

SM result for M_W and $\sin^2\theta_{\rm eff}$:

- full one-loop
- full two-loop
- leading 3-loop via $\Delta \rho$
- leading 4-loop via $\Delta \rho$

Our MSSM result for M_W and $\sin^2 \theta_{\rm eff}$:

- full SM result (via fit formel)
- full MSSM one-loop (incl. complex phases)
- all existing two-loop $\Delta \rho$ contributions
- \Rightarrow non- $\Delta \rho$ one-loop and $\Delta \rho$ two-loop contributions sometimes non-negligible!

The W boson mass

Experimental accuracy:

```
Today: LEP2, Tevatron: M_W^{\rm exp} = 80.385 \pm 0.015 \; {\rm GeV}
ILC/TLEP: — polarized threshold scan
                     - kinematic reconstruction of W^+W^-
                                                                                                       [G. Wilson '13]
                     - hadronic mass (single W)
       \delta M_{W}^{\mathrm{exp,ILC(TLEP)}} \lesssim 3(1) MeV (from thr. scan) \leftarrow TU neglected
Theoretical accuracies:
intrinsic today: \delta M_W^{\rm SM,theo} = 4 \ {\rm MeV}, \quad \delta M_W^{\rm MSSM,today} = 5 - 10 \ {\rm MeV}
intrinsic future: \delta M_W^{\text{SM,theo,fut}} = 1 \text{ MeV}, \quad \delta M_W^{\text{MSSM,fut}} = 2 - 4 \text{ MeV}
parametric today: \delta m_t = 0.9 GeV, \delta(\Delta \alpha_{\rm had}) = 10^{-4}, \delta M_Z = 2.1 MeV
 \delta M_W^{\mathrm{para},m_t} = 5.5 \; \mathrm{MeV}, \quad \delta M_W^{\mathrm{para},\Delta\alpha_{\mathrm{had}}} = 2 \; \mathrm{MeV}, \quad \delta M_W^{\mathrm{para},M_Z} = 2.5 \; \mathrm{MeV}
parametric future: \delta m_{\star}^{\rm ILC/TLEP} = 0.1 GeV, \delta (\Delta \alpha_{\rm had})^{\rm fut} = 5 \times 10^{-5}
                  \Delta M_W^{\mathsf{para},\mathsf{fut},m_t} = 1 \; \mathsf{MeV}, \quad \Delta M_W^{\mathsf{para},\mathsf{fut},\Delta\alpha_{\mathsf{had}}} = 1 \; \mathsf{MeV}
```

The effective weak leptonic mixing angle: $\sin^2\theta_{\rm eff}$

Experimental accuracy:

Today: LEP, SLD: $\sin^2 \theta_{\text{eff}}^{\text{exp}} = 0.23153 \pm 0.00016$

GigaZ/TeraZ: both beams polarized, Blondel scheme

$$\delta \sin^2 \theta_{\text{eff}}^{\text{exp,ILC(TLEP)}} = 13(3) \times 10^{-6} \quad \Leftarrow \text{TU neglected}$$

Theoretical accuracies: $[10^{-6}]$

intrinsic today: $\delta \sin^2 \theta_{\text{eff}}^{\text{SM,theo}} = 47$ $\delta \sin^2 \theta_{\text{eff}}^{\text{MSSM,today}} = 50 - 70$

intrinsic future: $\delta \sin^2 \theta_{\text{eff}}^{\text{SM,theo,fut}} = 15$ $\delta \sin^2 \theta_{\text{eff}}^{\text{MSSM,fut}} = 25 - 35$

parametric today: $\delta m_t = 0.9$ GeV, $\delta(\Delta \alpha_{had}) = 10^{-4}$, $\delta M_Z = 2.1$ MeV

$$\delta \sin^2 \theta_{\rm eff}^{{\rm para},m_t} = 70, \quad \delta \sin^2 \theta_{\rm eff}^{{\rm para},\Delta\alpha_{\rm had}} = 36, \quad \delta \sin^2 \theta_{\rm eff}^{{\rm para},M_Z} = 14$$

parametric future: $\delta m_t^{\rm ILC/TLEP}=0.1$ GeV, $\delta (\Delta \alpha_{\rm had})^{\rm fut}=5\times 10^{-5}$

$$\Delta \sin^2 \theta_{\text{eff}}^{\text{para,fut},m_t} = 4$$
, $\Delta \sin^2 \theta_{\text{eff}}^{\text{para,fut},\Delta\alpha_{\text{had}}} = 18$

The top quark mass: m_t

What is the top mass?

Particle masses are not direct physical observables one can only measure cross sections, decay rates, . . .

Additional problem for the top mass:

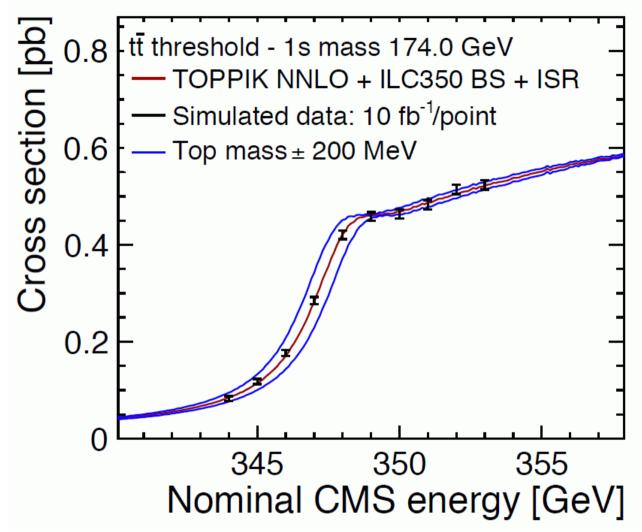
what is the mass of a colored object?

Top pole mass is not IR safe (affected by large long-distance contributions), cannot be determined to better than $\mathcal{O}(\Lambda_{QCD})$

Measurement of m_t :

- At Tevatron, LHC: kinematic reconstruction, fit to invariant mass distribution \Rightarrow "MC" mass, close to "pole" mass? $\delta m_t^{\rm exp,LHC} \lesssim 1~{\rm GeV}$
- At e^+e^- colliders: unique possibility threshold scan \Rightarrow threshold mass \Rightarrow SAFE! transition to other mass definitions possible, $\delta m_t^{\rm exp,ILC} \lesssim 0.03~{\rm GeV}$

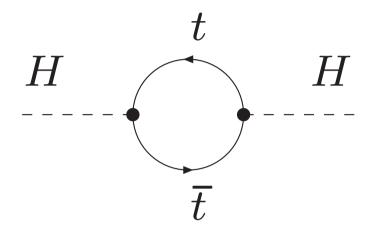
threshold scan \Rightarrow threshold mass \Rightarrow **SAFE!**



transition to other mass definitions possible $\Rightarrow \delta m_t^{\rm exp+theo} \lesssim 0.1~{\rm GeV}$ \Rightarrow dominated by theory uncertainty! \Rightarrow ILC and TLEP so far similar!

Top/Higgs physics in BSM:

Nearly any model: large coupling of the Higgs to the top quark:

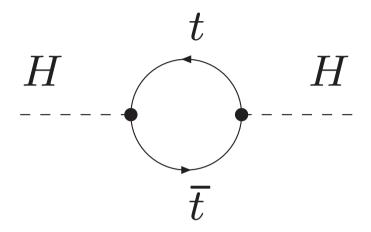


- \Rightarrow one-loop corrections $\Delta M_H^2 \sim G_\mu m_t^4$
- $\Rightarrow M_H$ depends sensitively on m_t in all models where M_H can be predicted (SM: M_H is free parameter)

SUSY as an example: $\Delta m_t \approx \pm 1 \text{ GeV} \Rightarrow \Delta M_h \approx \pm 1 \text{ GeV}$

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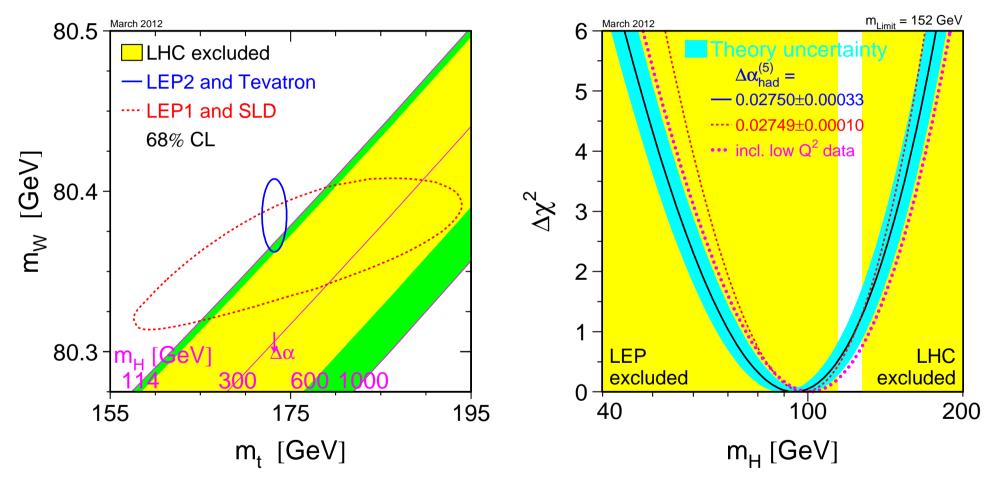
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⇒ Precision Higgs physics needs ILC/TLEP precision top physics

Precision Tests of the SM (and beyond)

⇒ indirect prediction of the Higgs mass in the SM

[LEPEWWG '12]



⇒ fits with today's precision

Improvements with the ILC:

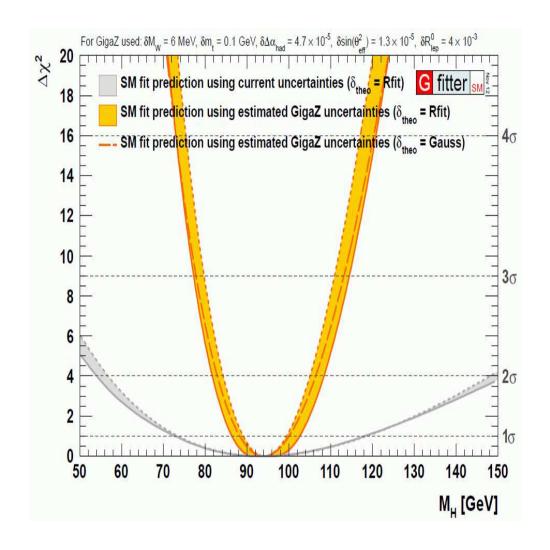
Experimental errors of the precision observables:

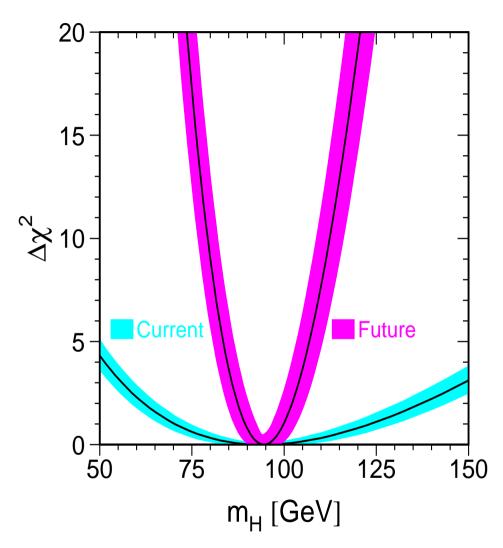
	today	Tev./LHC	ILC	GigaZ
$\delta \sin^2 \theta_{\rm eff} (\times 10^5)$	16	16	_	1.3
δM_W [MeV]	15	$\lesssim 15$	3-4	3-4
δm_t [GeV]	0.9	$\lesssim 1$	0.1	0.1

 M_W : from direct reconstruction and threshold scan [G. Wilson '13]

 $\sin^2 \theta_{\rm eff}$: 1/2 year GigaZ run, polarization important

 α_s : Improvement from GigaZ run





 $\Rightarrow \delta M_H^{
m ind} \lesssim 6~{
m GeV}$

← no TLEP analysis done so far

⇒ extremely sensitive test of SM (and BSM) possible

3. Higgs observables: Higgs couplings

LHC always measures $\sigma \times BR$

 \Rightarrow Total width $\Gamma_{H, \text{tot}}$ cannot be measured without further theory assumptions.

Recommendation of the LHCHXSWG:

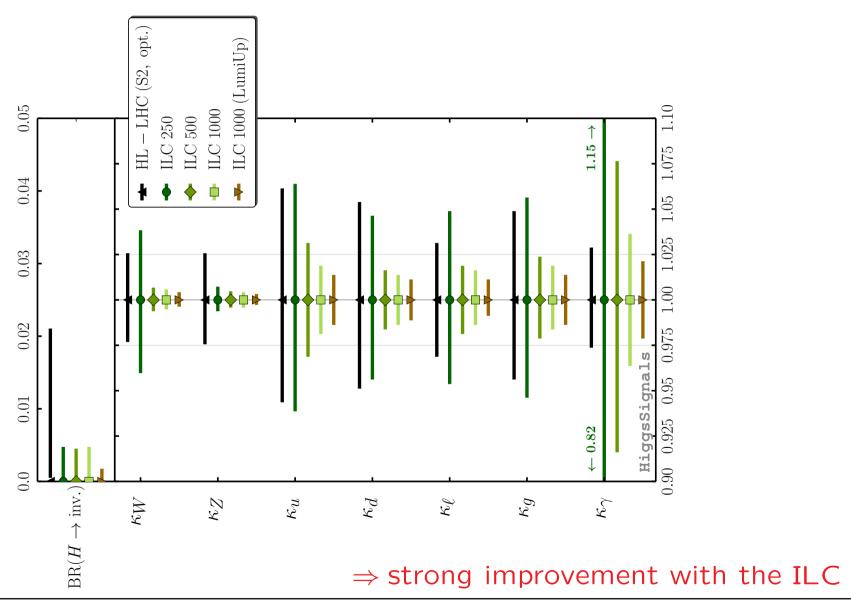
 \Rightarrow Higgs coupling strength scale factors: κ_i For each benchmark (except overall coupling strength) various versions are proposed: with and without additinal theory assumptions

- no additional theory assumptions:
- \Rightarrow Determination of ratios of scaling factors, e.g. $\kappa_i \kappa_j/\kappa_H$
- additional theory assumptions (on $\Gamma_{H, \text{tot}}$ or $\kappa_{W, Z}$ or $H \to \text{NP}$)
- \Rightarrow Determination of κ_i (evaluated to NLO QCD accuracy)

HL-LHC vs. ILC in the most general κ framework:

[P. Bechtle, S.H., O. Stål, T. Stefaniak, G. Weiglein '14]

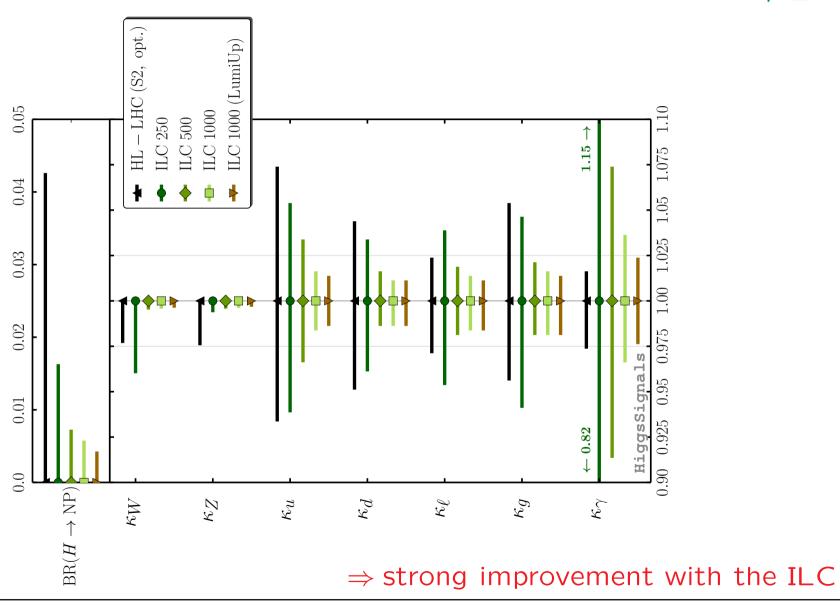
assumption: $BR(H \rightarrow NP) = BR(H \rightarrow inv.)$



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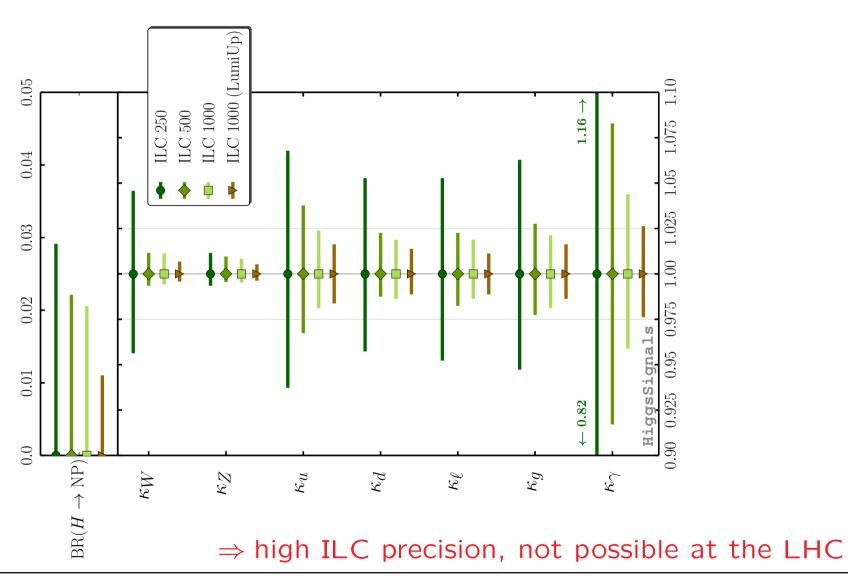
assumption: $\kappa_V \leq 1$



HL-LHC vs. ILC in the most general κ framework:

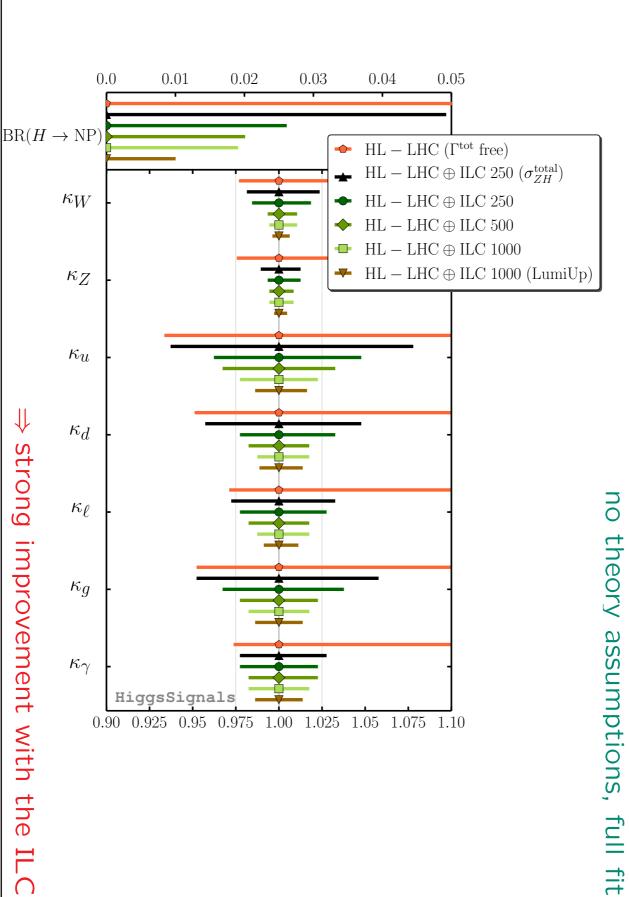
[P. Bechtle, S.H., O. Stål, T. Stefaniak, G. Weiglein '14]

no theory assumptions, full fit

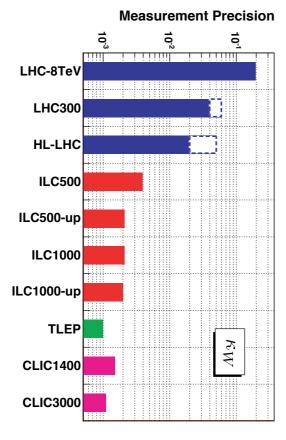


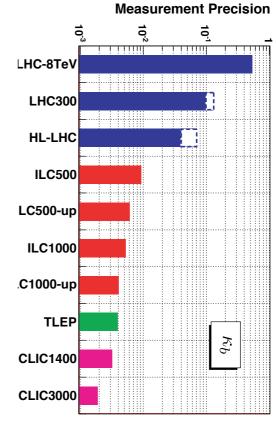
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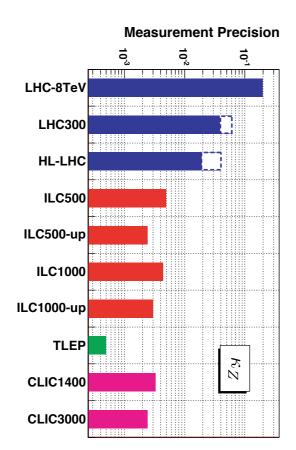
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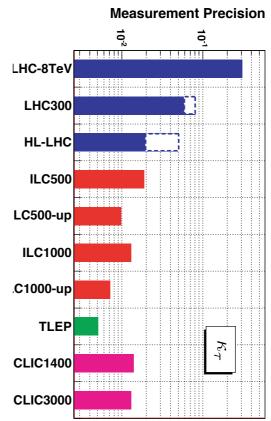


the sub-percent/permille level be matched by theory?









Higgs coupling determination at e^+e^- collider

Some specifics:

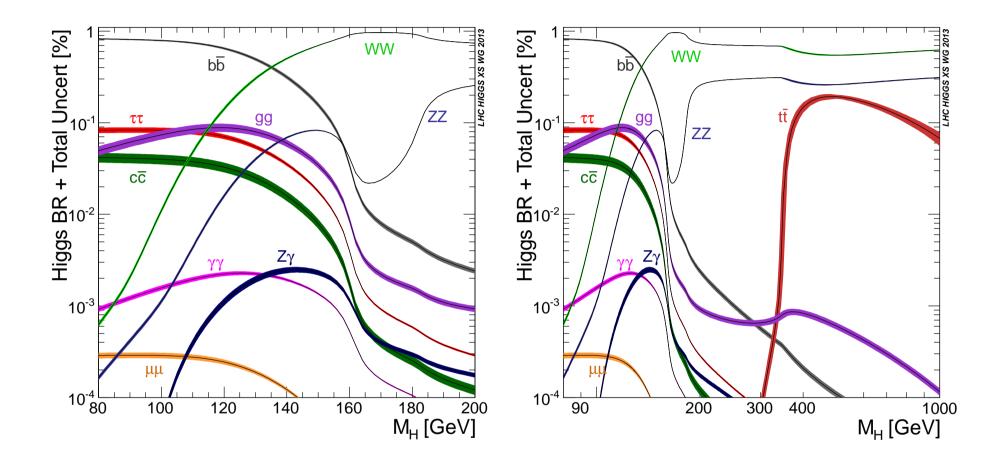
recoil method: $e^+e^- \rightarrow ZH$, $Z \rightarrow e^+e^-$, $\mu^+\mu^-$

- ⇒ total measurement of Higgs production cross section
- ⇒ NO additional theoretical assumptions needed for absolute determination of partial widths
- ⇒ all observable channels can be measured with high accuracy

- \Rightarrow SM cross section predictions at the 1% accuracy level
- ⇒ improvements necessary ... full 2-loop calculations and more ...?!

⇒ concentrate on theory BR uncertainties from now on

Latest SM Higgs BR predictions:



Based on HDECAY and Prophecy4f:

$$\Gamma_H = \Gamma^{\text{HD}} - \Gamma^{\text{HD}}_{ZZ} - \Gamma^{\text{HD}}_{WW} + \Gamma^{\text{P4f}}_{4f}$$

1. Parametric Uncertainties: $p \pm \Delta p$

- Evaluate partial widths and BRs with p, $p + \Delta p$, $p \Delta p$ and take the differences w.r.t. central values
- Upper $(p + \Delta p)$ and lower $(p \Delta p)$ uncertainties summed in quadrature to obtain the Combined Parametric Uncertainty

2. Theoretical Uncertainties:

- Calculate uncertainty for partial widths and corresponding BRs for each theoretical uncertainty
- Combine the individual theoretical uncertainties linearly to obtain the Total Theoretical Uncertainty
- ⇒ estimate based on "what is included in the codes"!

3. Total Uncertainty:

Linear sum of the Combined Parametric Uncertainty and the Total Theoretical Uncertainties

Current parametric uncertainties:

Parameter	Central Value	Uncertainty	$m_q(m_q)$	
$\alpha_s(M_Z)$	0.119	±0.002(90% CL)		
m_c	1.42 GeV	$\pm 0.03~{ m GeV}(2\sigma)$	1.28 GeV	
m_b	4.49 GeV	$\pm 0.06~{ m GeV}(2\sigma)$	4.16 GeV	
m_t	172.5 GeV	±2.5 GeV	165.4 GeV	

- m_b , m_c : one-loop pole masses those masses accidentally show negligible dependence on α_s , so that their variation can be done independently from α_s
- $-m_b$, m_c uncertainties:

[K. Chetyrkin, J. Kühn, A. Maier, P. Maierhöfer, P. Marquard, M. Steinhauser, C. Sturm [arXiv:0907.2110]]

- ⇒ Lattice data much more optimistic . . .
- ⇒ but no consensus, not even in the lattice community . . . ?!

Current theoretical uncertainties:

Partial Width	QCD	Electroweak	Total
$H o b\overline{b}/c\overline{c}$	$\sim 0.1\%$	\sim 1–2% for $M_H\lesssim$ 135 GeV	$\sim 2\%$
$H \to \tau^+ \tau^- / \mu^+ \mu^-$		\sim 1–2% for $M_H\lesssim$ 135 GeV	$\sim 2\%$
$H o t \overline{t}$	$\lesssim 5\%$	\lesssim 2–5% for $M_H <$ 500 GeV	\sim 5%
		$\sim 0.1 (rac{M_H}{1~ ext{TeV}})^4$ for $M_H > 500~ ext{GeV}$	\sim 5–10%
H o gg	$\sim 3\%$	$\sim 1\%$	\sim 3%
$H o \gamma \gamma$	< 1%	< 1%	$\sim 1\%$
$H o Z \gamma$	< 1%	\sim 5%	\sim 5%
H o WW/ZZ o 4f	< 0.5%	\sim 0.5% for $M_H <$ 500 GeV	$\sim 0.5\%$
		$\sim 0.17 (rac{M_H}{1~ ext{TeV}})^4$ for $M_H > 500~ ext{GeV}$	$\sim 0.515\%$

- QCD corrections: scale change by factor 2 and 1/2
- Different uncertainties on a given channel added linearly
- \Rightarrow Strong improvement in \sim 20 years possible, but . . .
 - ... they have to be consistently implemented into codes!
- ⇒ intrinsic uncertainty can/will be sufficiently under control?!

Channel	Γ [MeV]	$\Delta \alpha_s$	Δm_b	Δm_c	Δm_t	THU
$H o b \overline{b}$	2.36	-2.3% +2.3%	+3.3% -3.2%	+0.0% -0.0%	+0.0% -0.0%	+2.0% -2.0%
$H \to \tau^+ \tau^-$	$2.59 \cdot 10^{-1}$	+0.0% +0.0%	+0.0% -0.0%	+0.0% -0.0%	$+0.1\% \\ -0.1\%$	+2.0% -2.0%
$H \to \mu^+\mu^-$	$8.99 \cdot 10^{-4}$	+0.0% +0.0%	+0.0% -0.0%	$-0.1\% \\ -0.0\%$	$+0.0\% \\ -0.1\%$	+2.0% -2.0%
$H \to c\overline{c}$	$1.19 \cdot 10^{-1}$	-7.1% +7.0%	$-0.1\% \\ -0.1\%$	+6.2% -6.1%	$+0.0\% \\ -0.1\%$	+2.0% -2.0%
$H \to gg$	$3.57 \cdot 10^{-1}$	+4.2% -4.1%	$-0.1\% \\ -0.1\%$	+0.0% -0.0%	-0.2% +0.2%	+3.0% -3.0%
$H \to \gamma \gamma$	$9.59 \cdot 10^{-3}$	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+1.0% $-1.0%$
$H \to Z \gamma$	$6.84 \cdot 10^{-3}$	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.1%	+0.0% -0.1%	+5.0% -5.0%
$H \to WW^*$	$9.73 \cdot 10^{-1}$	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+0.5% -0.5%
$H o ZZ^*$	$1.22 \cdot 10^{-1}$	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+0.0% -0.0%	+0.5% -0.5%

Data available for $M_H = 122 \text{ GeV}, 126 \text{ GeV}, 130 \text{ GeV}$

 \Rightarrow substantially larger than κ precision at ILC/TLEP

Future theory uncertainties?

Parametric uncertainties:

- largely driven by $\delta m_b \Rightarrow$ improvement unclear (to me) lattice community does not seem to agree
- some improvement in α_s possible

Intrinsic uncertainties:

```
H \to b \bar b, H \to c \bar c: EW corrections can be included (they are known at 1L) H \to \tau^+ \tau^-, H \to \mu^+ \mu^-: EW corrections can be included (they are known at 1L) H \to gg: improvement difficult H \to \gamma \gamma: already very precise . . . H \to Z \gamma: EW corrections could help . . . H \to WW^*, H \to ZZ^*: already very precise, two-loop corrections unclear \to intrinsic uncertainty can/will be sufficiently under control?!
```



Input Parameters

Lepage, Mackenzie, Peskin [arXiv:1404.0319]

- How well can the Higgs BRs be predicted in the future?
- Limitation due to parametric errors?
- use lattice gauge theory to improve α_s , m_b , and m_c (e.g. using current-current correlators) (stated errors already now quite small)
- optimistic projection for lattice improvements:

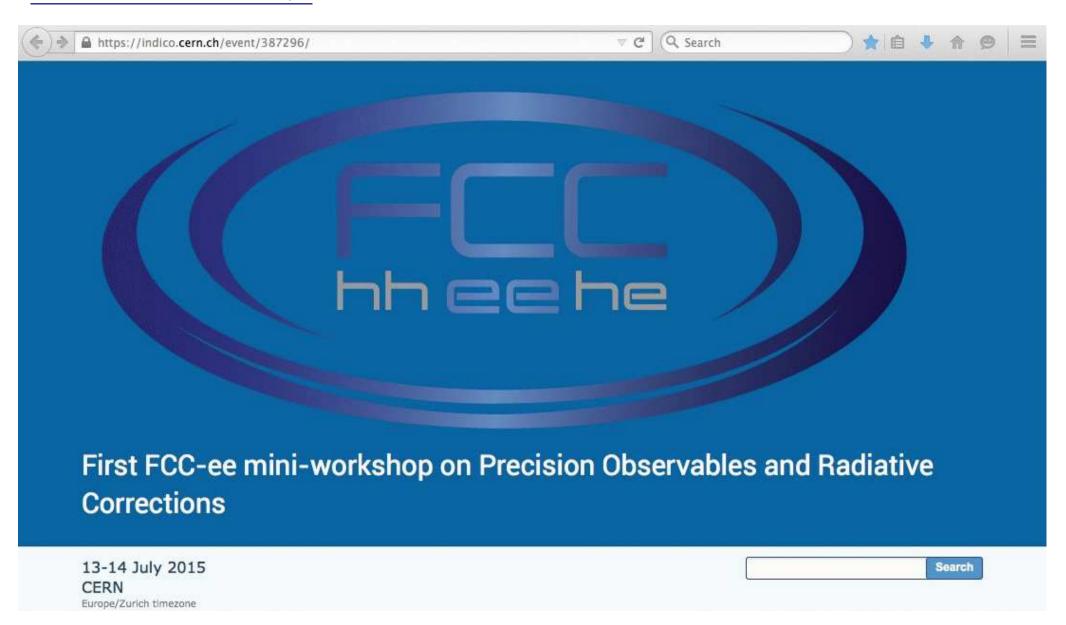
		$\delta m_b(10)$	$\delta \alpha_s(m_Z)$	$\delta m_c(3)$	δ_b	δ_c	δ_g	
_	current errors [10]	0.70	0.63	0.61	0.77	0.89	0.78	
	+ PT	0.69	0.40	0.34	0.74	0.57	0.49	
	+ LS	0.30	0.53	0.53	0.38	0.74	0.65	
	$+ LS^2$	0.14	0.35	0.53	0.20	0.65	0.43	
	+ PT + LS	0.28	0.17	0.21	0.30	0.27	0.21	
	$+ PT + LS^2$	0.12	0.14	0.20	0.13	0.24	0.17	
	$+ PT + LS^2 + ST$	0.09	0.08	0.20	0.10	0.22	0.09	
	ILC goal				0.30	0.70	0.60	(errors in ^o

time-scale: 10-15 years

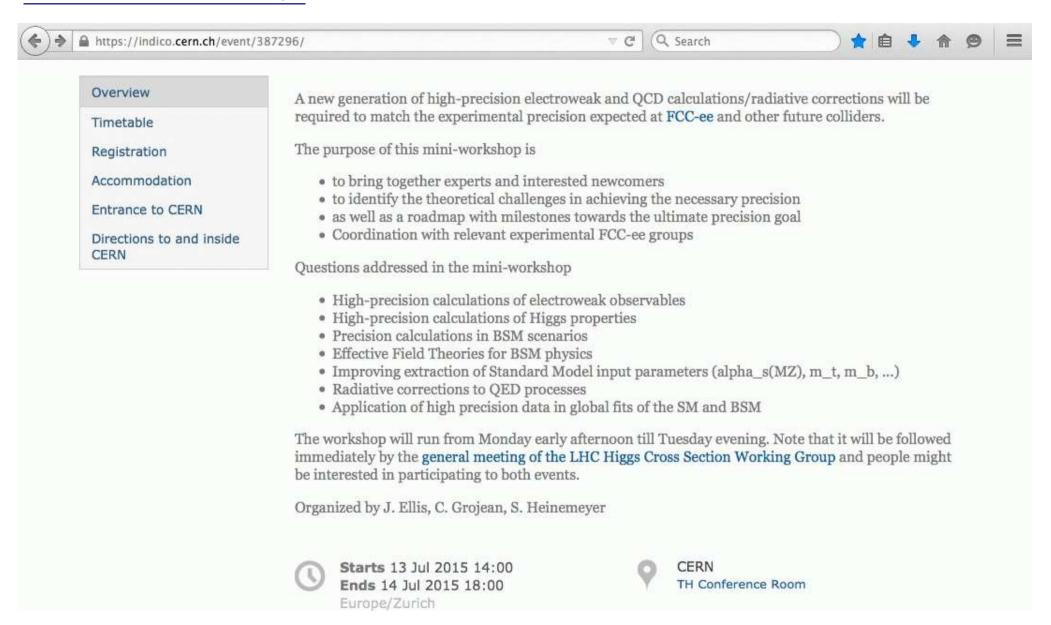
BR report - Alexander Mück - p.7/ 13



Dedicated workshop:



Dedicated workshop:



4. Conclusions

- Experimental precision must be matched with theory precision!
- EWPO can give valuable information about SM, BSM \rightarrow only SM, MSSM "ready" Most relevant: M_W , $\sin^2\theta_{\rm eff}$, (m_t) , . . .
- Current theory uncertainties of M_W , $\sin^2\theta_{\rm eff}$ not sufficient Future theory uncertainties: M_W in SM: TLEP goals hard to match M_W in MSSM: even harder $\sin^2\theta_{\rm eff}$ in SM: more than a \mathcal{O} (10) missing $\sin^2\theta_{\rm eff}$ in MSSM: even worse
- Top quark mass: mainly theory driven. No improvement at TLEP?!
- Higgs couplings: XS and BR have to be under control
 Can sub-percent/permille level be matched?
 - XS: 1% possible, full 2-loop calculations needed?!
 - BR: intrinsic uncertainties could be brought down below 1% parametric uncertainties have (to me) unclear perspective

Back-up

More complete future options:

LHC300, HL-LHC, ILC250, ILC500, ILC1000, ILC1000-LumiUp

Future scenario	PDF	α_s	m_c, m_b, m_t	$\mathrm{THU^1}$	$BR(H \to NP)$ constraint
LHC300 (S1)	100%	100%	all 100%	100%	conservative, Eq. (13)
LHC300 (S2, csv.)	50%	100%	all 100%	50%	conservative, Eq. (13)
LHC300 (S2, opt.)	50%	100%	all 100%	50%	optimistic, Eq. (15)
HL-LHC (S1)	100%	100%	all 100%	100%	conservative, Eq. (14)
HL-LHC (S2, csv.)	50%	100%	all 100%	50%	conservative, Eq. (14)
HL-LHC (S2, opt.)	50%	100%	all 100%	50%	optimistic, Eq. (16)
ILC250		50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
ILC500		50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
ILC1000	-	50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
ILC1000-LumiUp	-	50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
HL-LHC \oplus ILC250 $(\sigma_{ZH}^{\text{total}})^2$	50%	50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
$\text{HL-LHC} \oplus \text{ILC250}$	50%	50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
$\text{HL-LHC} \oplus \text{ILC500}$	50%	50%	all 50%	50%	$\sigma(e^-e^+ o ZH)$
$\text{HL-LHC} \oplus \text{ILC1000}$	50%	50%	all 50%	50%	$\sigma(e^-e^+ \to ZH)$
HL-LHC ⊕ ILC1000-LumiUp	50%	50%	all 50%	50%	$\sigma(e^-e^+ o ZH)$