CERN Summer School 2015
Introduction to Accelerator Physics

Part IV

by
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What's next?

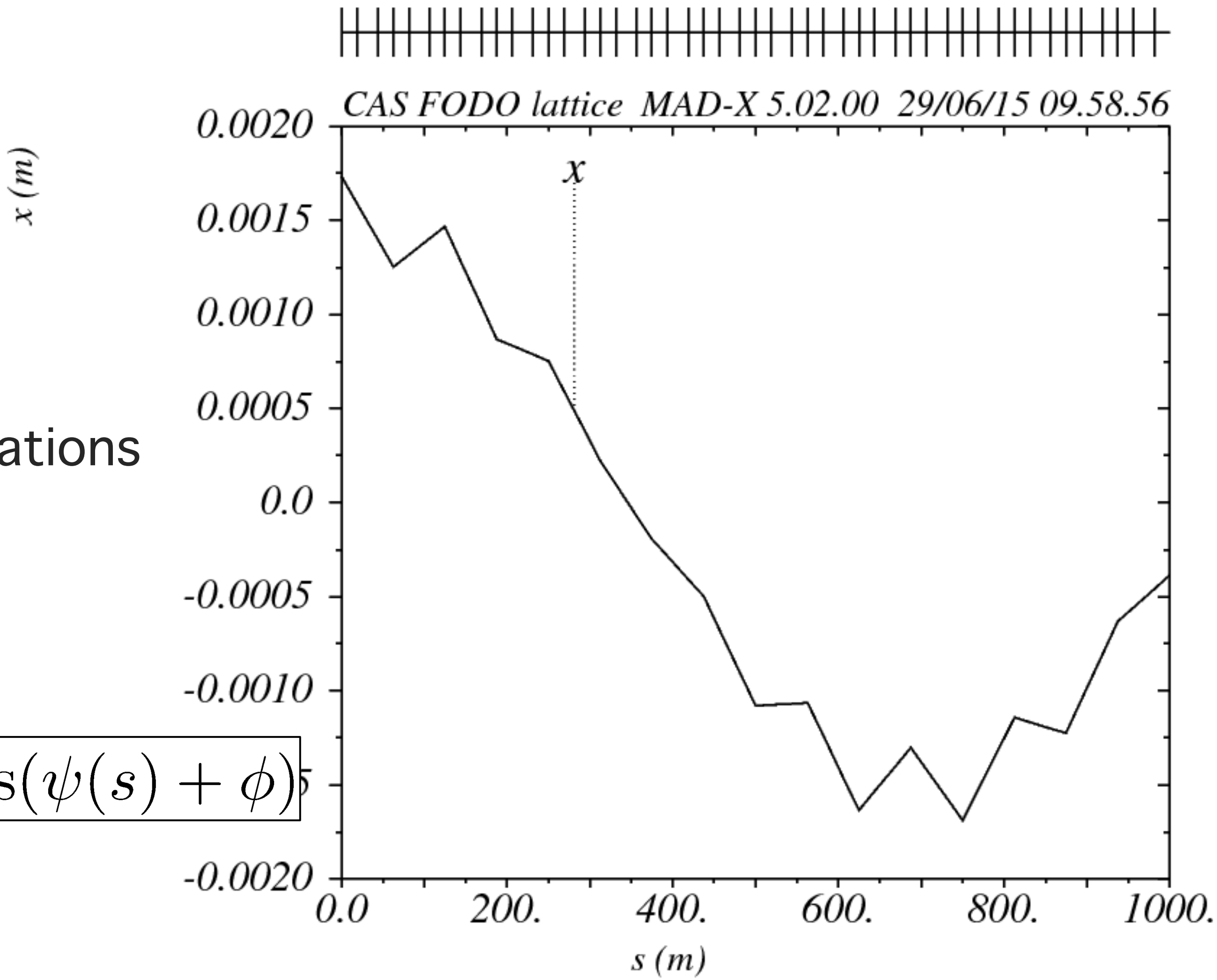
- Imperfections, collective effects

- Electron Cloud Instability

Reminder: The trajectory around the ring

Where as the beta functions are several 100 m

The trajectories are in ~ mm

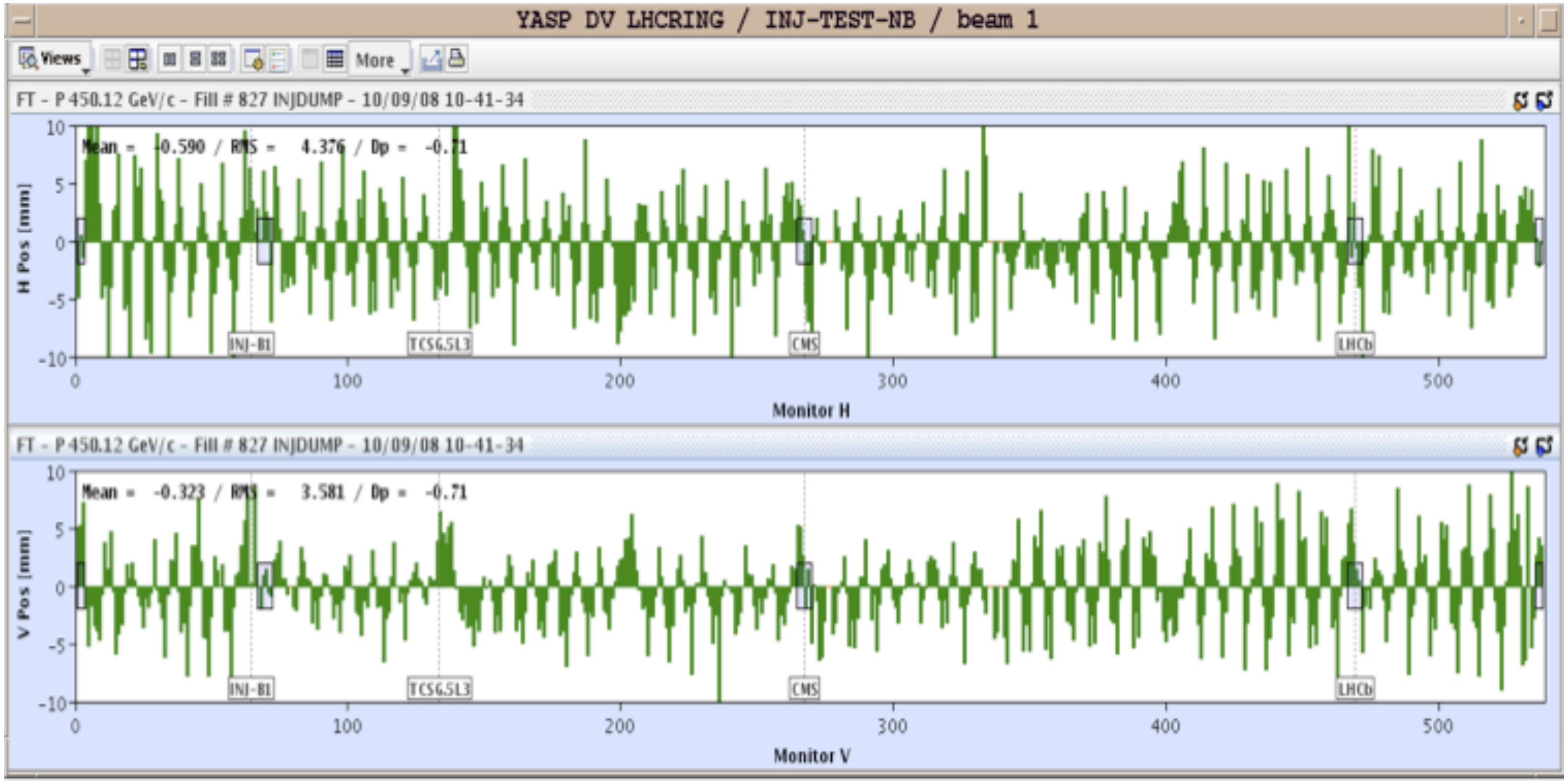


The number of oscillations around the ring is less than 1.

$$x(s) = \sqrt{\epsilon}\sqrt{\beta(s)}\cos(\psi(s)+\phi)$$

Reminder: LHC example

Tunes $Q_x = 64.28$, $Q_y = 59.31$



Reminder: The Tune

The number of oscillations per turn is called "tune"

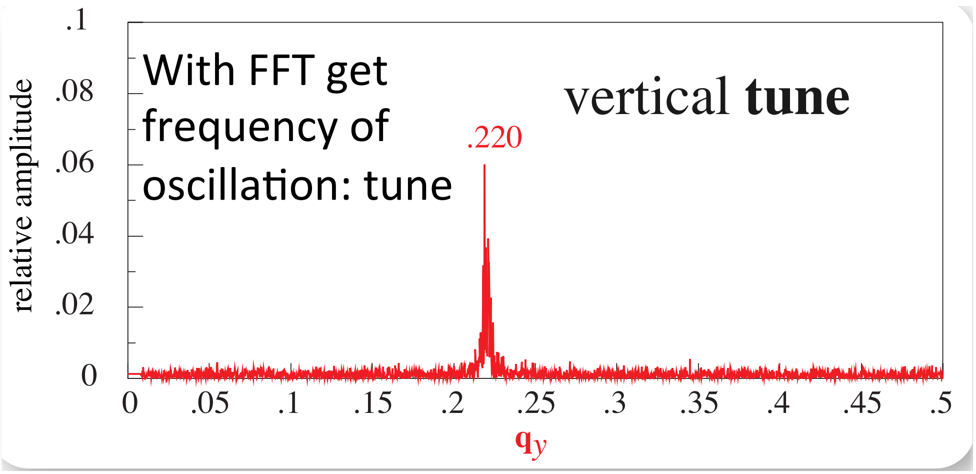
$$Q = \frac{\psi(L_{turn})}{2\pi} = \frac{1}{2\pi} \oint \frac{ds}{\beta(s)}$$

The tune is an important parameter for the stability of motion over many turns.

It has to be chosen appropriately, measured and corrected.

Measure beam position at one location turn by turn

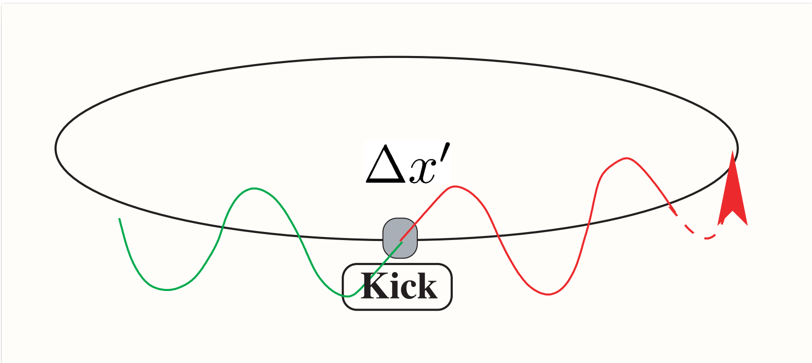
Beam position will change with $\propto \cos(2\pi Q i)$



The Tune

The choice of phase advance per cell or tune and hence the focusing properties of the lattice have important implications.

Misalignment of quadrupoles or dipole field errors create orbit perturbations



The perturbation at one location has an effect around the whole machine

$$\begin{pmatrix} x \\ x' - \Delta x' \end{pmatrix} = M_{turn} \cdot \begin{pmatrix} x \\ x' \end{pmatrix}$$

$$x(s) = \frac{\Delta x'}{2} \cdot \sqrt{\beta(s_0)\beta(s)} \frac{\cos(\pi Q - \psi_{s_0 \to s})}{\sin(\pi Q)}$$

➔ diverges for Q = N, where N is integer.

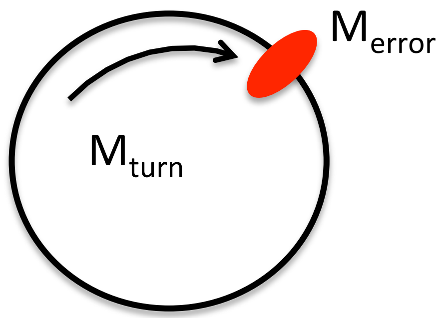
Gradient Error

What happens if there is an error in the quadrupole field?

Assume at one location in the ring quadrupole error of Δk over a distance l.

The effect on the focusing properties: the distorted one-turn matrix

$$M_{dist} = M_{error} \cdot M_{turn}$$



Remember: can write M from s_0 to s as function of β, α and ψ.

$$M = \begin{pmatrix} \sqrt{\frac{\beta}{\beta_0}}(\cos\psi + \alpha_0 \sin\psi) & \sqrt{\beta\beta_0}\sin\psi \\ \frac{(\alpha_0 - \alpha)\cos\psi - (1 + \alpha\alpha_0)\sin\psi}{\sqrt{\beta\beta_0}} & \sqrt{\frac{\beta_0}{\beta}}(\cos\psi - \alpha\sin\psi) \end{pmatrix}$$

Gradient Error

$$M = \begin{pmatrix} \sqrt{\frac{\beta}{\beta_0}}(\cos\psi + \alpha_0 \sin\psi) & \sqrt{\beta\beta_0}\sin\psi \\ \frac{(\alpha_0-\alpha)\cos\psi-(1+\alpha\alpha_0)\sin\psi}{\sqrt{\beta\beta_0}} & \sqrt{\frac{\beta_0}{\beta}}(\cos\psi - \alpha\sin\psi)) \end{pmatrix}$$

One-turn matrix: $\psi_{turn} = 2\pi Q$

$$M_{turn} = \begin{pmatrix} \cos 2\pi Q + \alpha \sin 2\pi Q & \beta \sin 2\pi Q \\ -\gamma \sin 2\pi Q & \cos 2\pi Q - \alpha \sin 2\pi Q \end{pmatrix}$$

$$M_{dist} = M_{error} \cdot M_{turn}$$

Assuming a small error over a short length:

$$M_{error} = \begin{pmatrix} \cos(\sqrt{k}s) & \frac{1}{\sqrt{k}}\sin(\sqrt{k}s) \\ -\sqrt{k}\sin(\sqrt{k}s) & \cos(\sqrt{k}s) \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 \\ -\Delta kl & 1 \end{pmatrix}$$

Gradient Error

The new one-turn matrix:

$$M_{turn_{dist}} = \begin{pmatrix} \cos 2\pi Q + \alpha \sin 2\pi Q & \beta \sin 2\pi Q \\ -\gamma \sin 2\pi Q & \cos 2\pi Q - \alpha \sin 2\pi Q \end{pmatrix} =$$

$$= \begin{pmatrix} 1 & 0 \\ -\Delta k l & 1 \end{pmatrix} \cdot \begin{pmatrix} \cos 2\pi Q_0 + \alpha \sin 2\pi Q_0 & \beta \sin 2\pi Q_0 \\ -\gamma \sin 2\pi Q_0 & \cos 2\pi Q_0 - \alpha \sin 2\pi Q_0 \end{pmatrix}$$

With $Q = Q_0 + \Delta Q$, ΔQ small and $\mathrm{Trace}(M_{dist}) = \mathrm{Trace}(M_{error}.M_{turn})$:

$$\Delta Q = \frac{1}{4\pi} \beta \Delta k \cdot l$$

β at the error location

The quadrupole error leads to a tune change. The higher the β, the higher the effect.

And also a change of the beta functions.

Gradient Error

A gradient error also leads to changes of the beta functions: beta-beat

The relative beta function change:

$$\frac{\Delta\beta(s)}{\beta(s)} = -\frac{1}{2\sin 2\pi Q}\beta(s_0)\cos[2(\psi(s_0)-\psi(s))-2\pi Q]\cdot\Delta k\cdot l$$

➔ diverges for Q = N, N/2; where N is integer.

Non-linear imperfections

Non-linear equation of motion:

$$\frac{d^2x}{ds^2} + K(s) \cdot x = \frac{F_x}{v \cdot p}$$

The Lorentz force from the non-linear magnetic field

The magnetic field of multipole order n:

$$B_y(x,y) + i \cdot B_x(x,y) = (B_n(s) + iA_n(s)) \cdot (x + iy)^n$$

The normal and skew coefficients:

$$B_n(s) = \frac{1}{(n)!} \frac{\partial^n B_y}{\partial x^n} \qquad A_n(s) = \frac{1}{(n)!} \frac{\partial^n B_x}{\partial x^n}$$

Linear and Non-linear Imperfections - Resonances

Amplitudes grow for Q = N or N/2 in case of quadrupole error

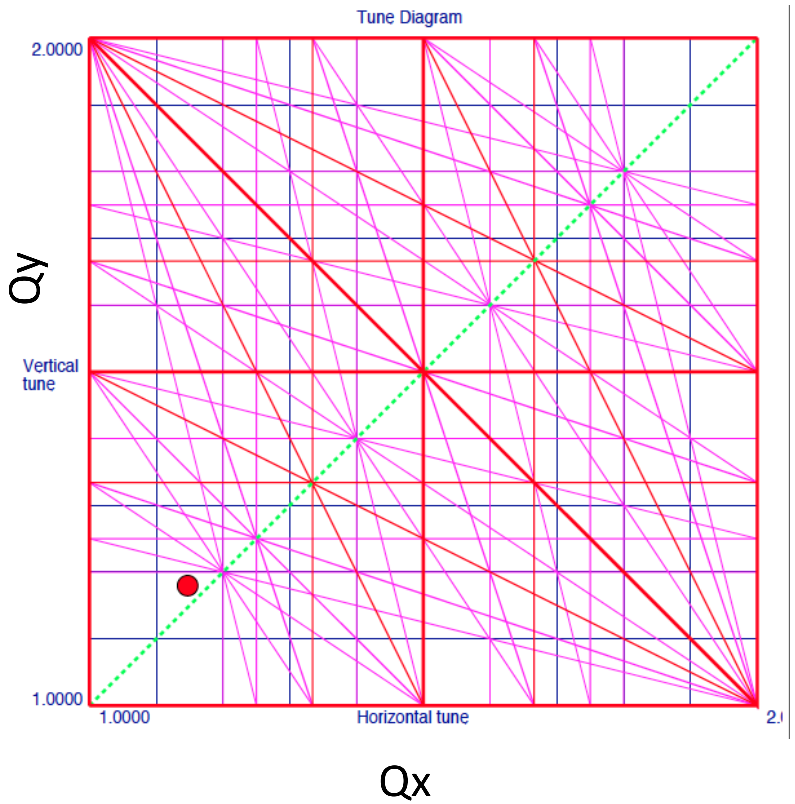
Sextupole perturbation: Q = N or N/3

Octupole perturbation: Q = N, N/2, N/4 etc.

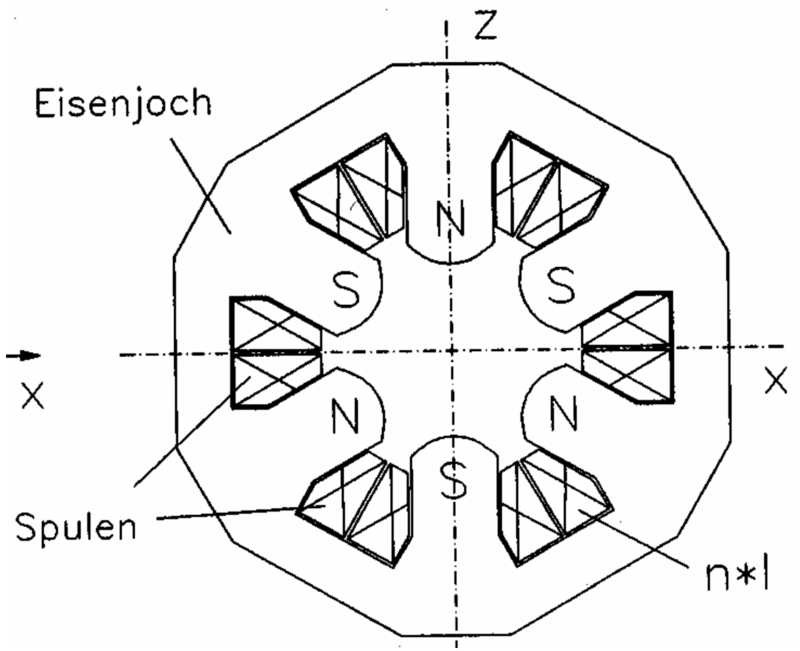
In general: avoid small integers n,m, N where

$$nQ_x + mQ_y = N$$

Working point has to be carefully chosen!!



Example: sextupole



$$B_x = \tilde{g}xy$$

$$B_y = \frac{1}{2}\tilde{g}(x^2 - y^2)$$

↓

$$\frac{\partial B_x}{\partial y} = \frac{\partial B_y}{\partial x} = \tilde{g}x$$

Linear rising "gradient"

The equations of motion become:

$$x'' + K_x(s) = -\frac{1}{2}m_{sext}(s)(x^2 - y^2)$$

$$y'' + K_y(s) = m_{sext}(s)xy$$

Effect of sextupoles on phase-space

Sextupoles create non-linear fields.

Depending on the tune the phase-space becomes more and more distorted. Motion becomes unstable close to the third order resonance.

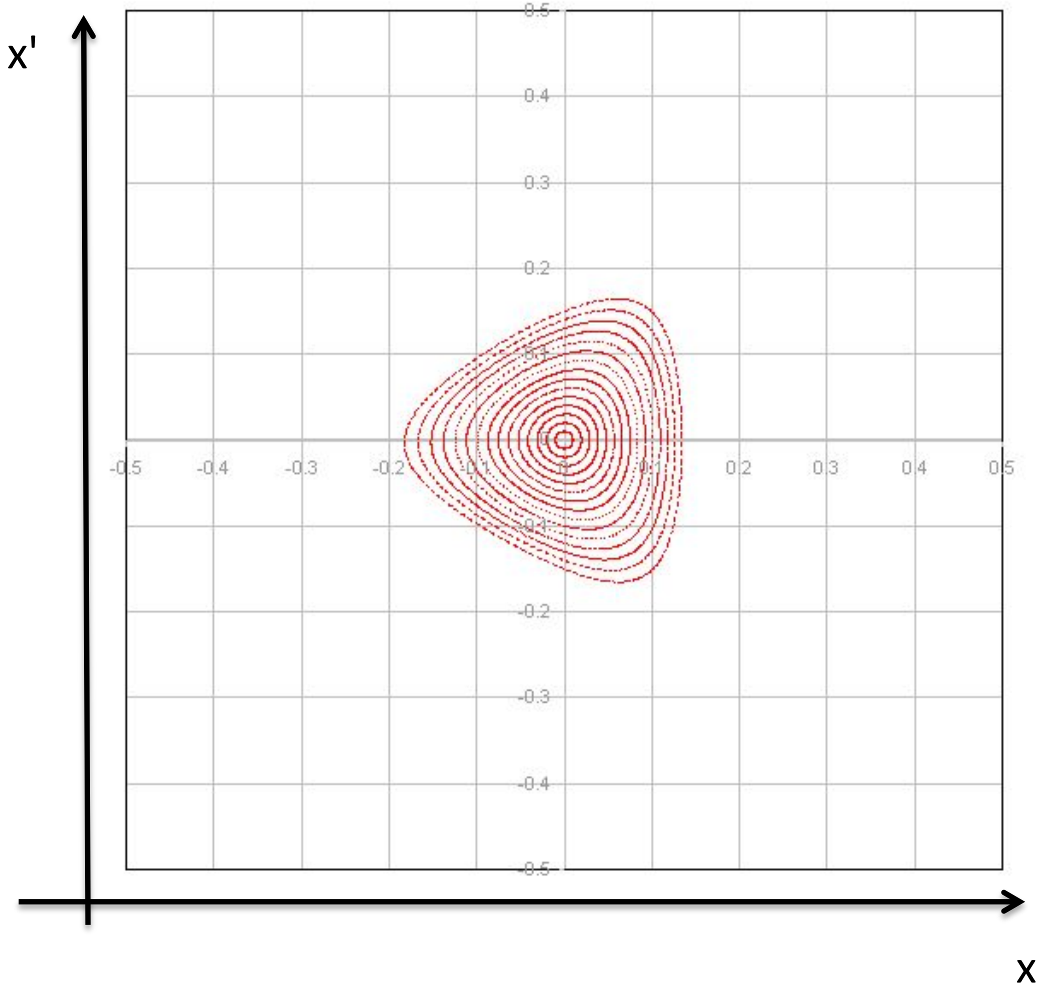
The sextupole kicks:

$$\Delta x' = -\frac{1}{2} m_{sext} l (x^2 - y^2)$$

$$\Delta y' = m_{sext} l x y$$

Amplitude of separatrix (unstable fixed points):

$$\propto \frac{Q - \frac{p}{3}}{m_{sext}}$$



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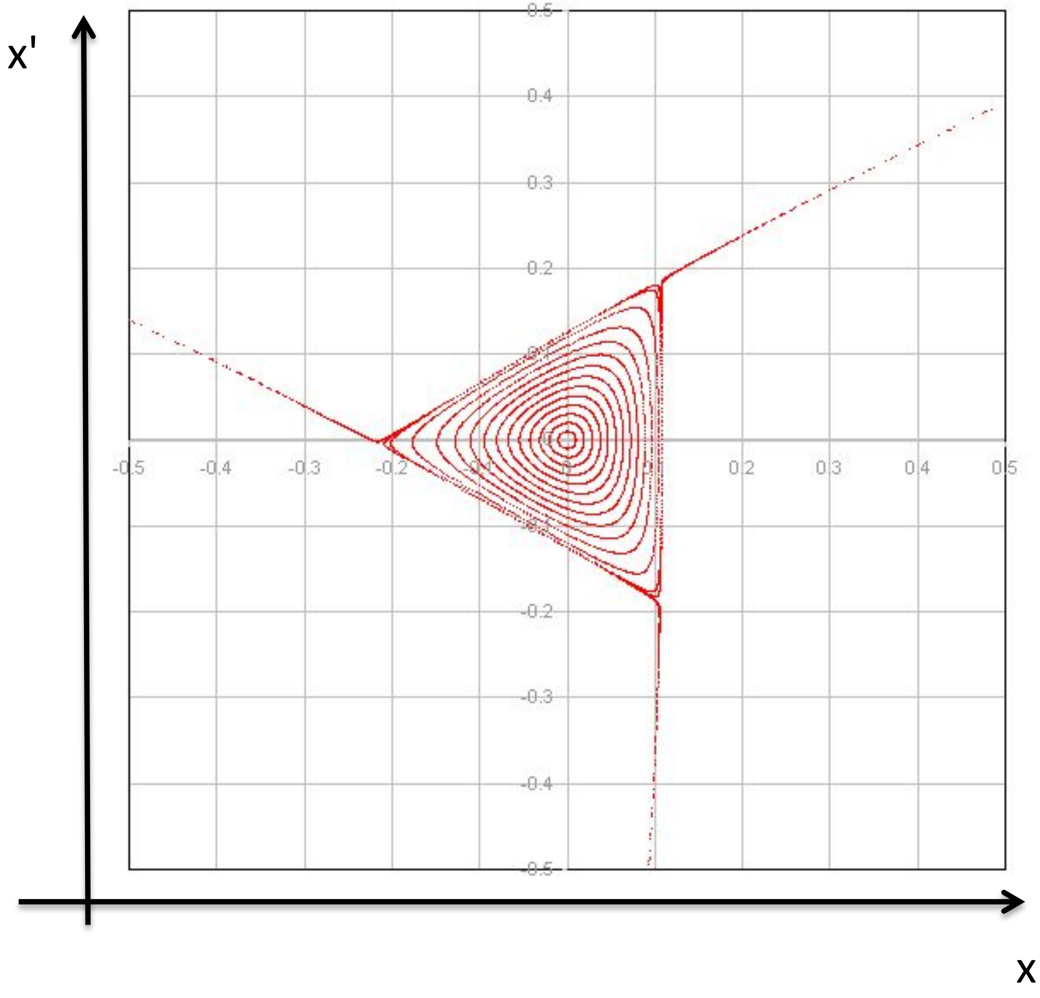


Chromaticity

The normalized quadrupole gradient is defined as

$$k = \frac{g}{p/e} \qquad\qquad p = p_0 + \Delta p$$

$$k = \frac{eg}{p_0 + \Delta p} \approx \frac{e}{p_0}\left(1 - \frac{\Delta p}{p_0}\right)g = k_0 + \Delta k$$

$$\Delta k = -\frac{\Delta p}{p_0} k_0$$

...a gradient error. Particles with different Δp/p will have different tunes.

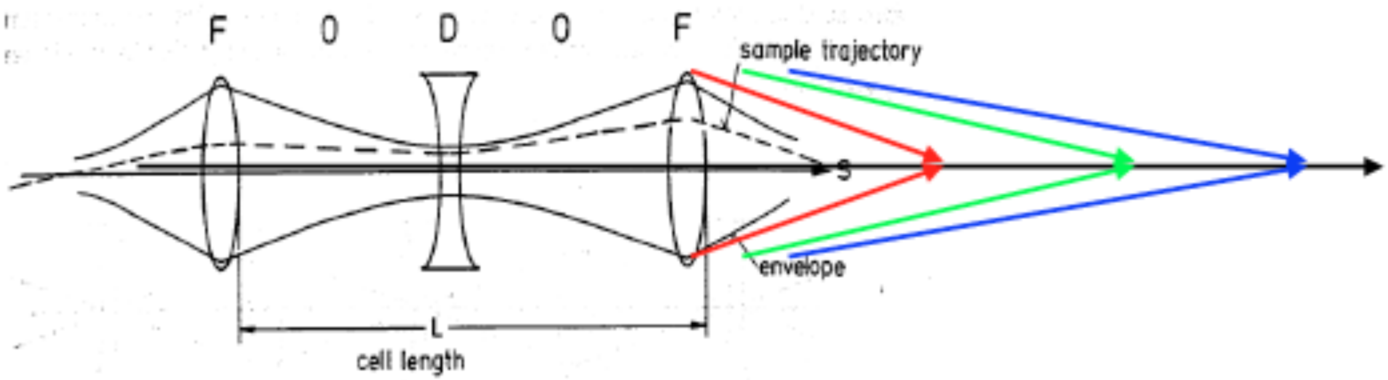


Figure 29: FODO cell

Chromaticity: Q'

The tune change for different Δp/p:

$$\Delta Q = \frac{1}{4\pi}\beta \Delta k \cdot l \quad \rightarrow \quad \Delta Q = -\frac{1}{4\pi}\frac{\Delta p}{p_0} k_0 \beta l$$

Definition of chromaticity:

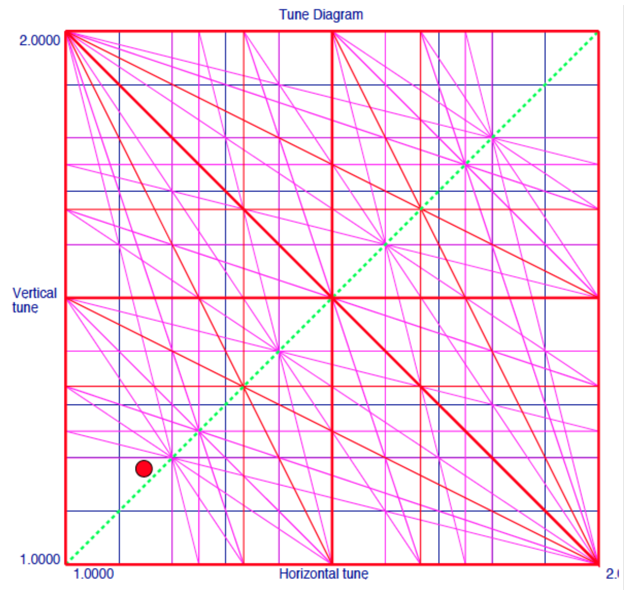
$$\Delta Q = Q' \frac{\Delta p}{p}$$

$$Q' = -\frac{1}{4\pi}\oint k(s)\beta(s)ds$$

With the beam momentum spread indicates the size of the tune spot in the tune diagram.

Chromaticity is created by quadrupole fields in the horizontal and vertical plane.

Chromaticity: Q'



We cannot leave chromaticity uncorrected:

Example LHC
Q'= 250 [no units]
$\Delta p/p$ = +/- 0.2 × 10^{-3}

ΔQ = 0.256 … 0.36 !!!! ➔ Particles will go across resonance lines and will be lost.

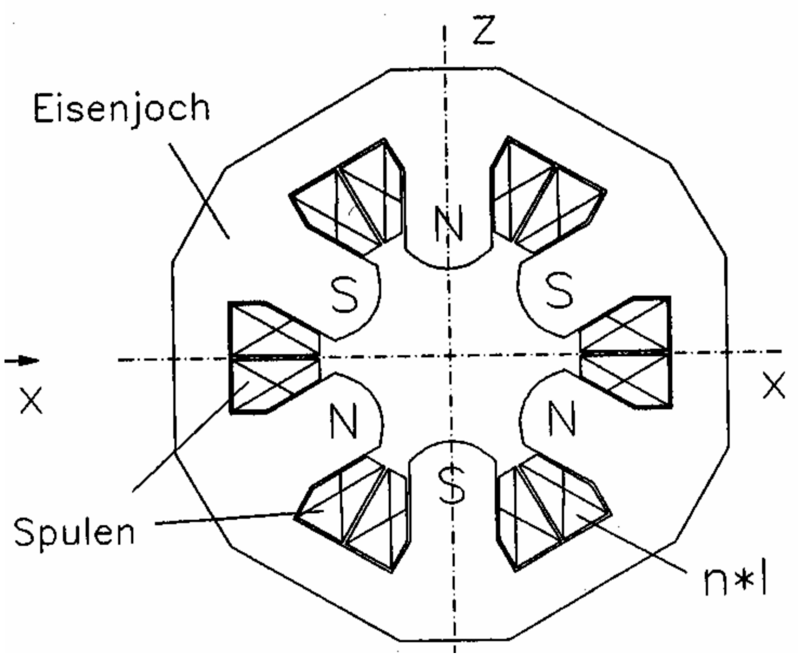
How to correct chromaticity?

Sextupole fields at locations of dispersion:

1) Sort the particles according to momentum: $x_D(s) = D(s)\frac{\Delta p}{p}$
2) Magnetic field with linear rising "gradient" ➔ prop. to x^2

Correcting chromaticity

Sextupole magnets:



$$B_x = \tilde{g}xy$$

$$B_y = \frac{1}{2}\tilde{g}(x^2 - y^2)$$

↓

$$\frac{\partial B_x}{\partial y} = \frac{\partial B_y}{\partial x} = \tilde{g}x$$

Linear rising “gradient"

Sextupoles give a normalized quadrupole strength of:

$$k_{sext} = \frac{\tilde{g}x}{p/e} = m_{sext}x \rightarrow k_{sext} = m_{sext}D\frac{\Delta p}{p}$$

Correcting chromaticity

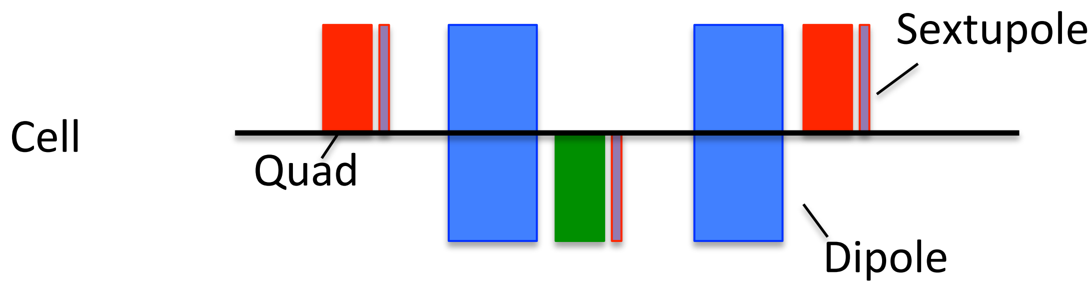
Only need dispersion in horizontal plane to correct chromaticity in horizontal and vertical plane.

$$Q' = -\frac{1}{4\pi} \oint \{k(s) - m(s)D(s)\}\beta(s)ds$$

Calculate m such that chromaticity vanishes.

(...we are neglecting collective effects.)

Add two families of sextupoles in your regular FODO lattice at the location with maximum dispersion: next to the quadrupoles



For completeness: orbit correctors and BPM locations

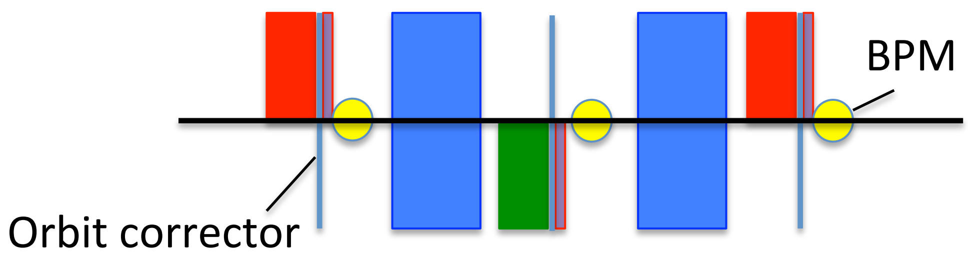
Response from dipole error Δx'

$$x(s) = \frac{\Delta x'}{2} \cdot \sqrt{\beta(s_0)\beta(s)} \frac{\cos(\pi Q - \psi_{s_0 \to s})}{\sin(\pi Q)}$$

Typical quadrupole alignment errors ~0.5 mm

Example SPS @ 450 GeV.: $\Delta x' = 0.5\, mm \cdot k \cdot l = 22 \mu rad$

Maximum amplitude orbit: $x \approx 1\, mm$

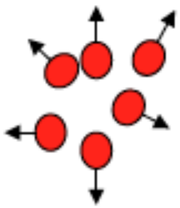


Different orbit correction algorithms MICADO, SVD...

Collective Effects

Three categories: can cause beam instabilities, emittance blow-up, beam loss,...

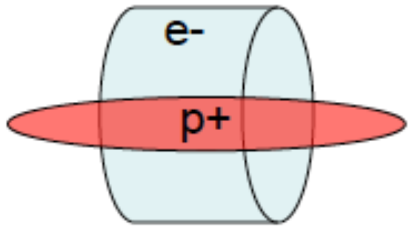
Beam-self: beam interacts with itself through space charge.



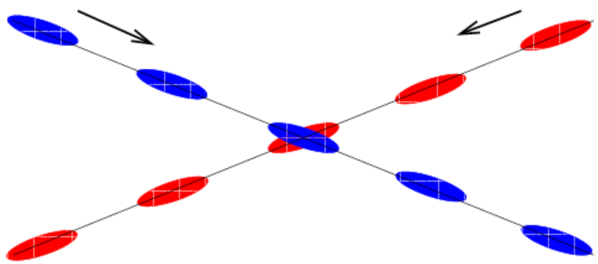
Tune spread $\propto \frac{1}{\beta^2\gamma^3}$

THE limitation in low energy machines

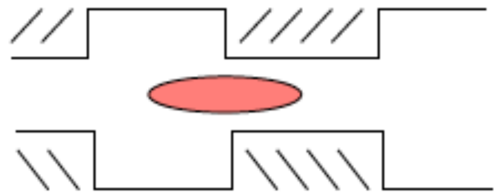
Beam-beam: colliding beams in colliders or ambient electron clouds (e-p instability).



Colliding beams. Tune spread/shift due to head-on collisions and long range collisions.



Beam-environment: beam interacts with machine (impedance-related instabilities).



Beam induces field in accelerator environment. Wake fields.
Wake fields can act back on trailing beam.

Fourier transform of Wake field is impedance.

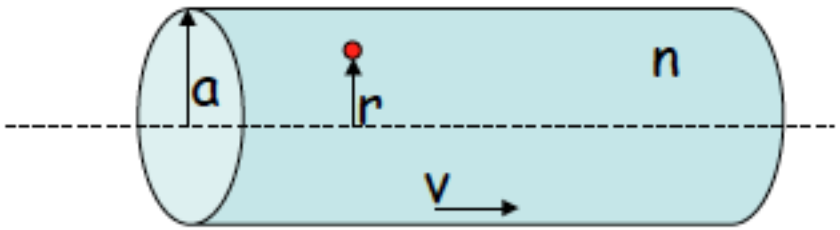
Can lead to component heating and/or instability.

Space-Charge Effect

The simplest and most fundamental of all collective effects

A simple approximation (direct space charge): beam as long cylinder.

Total force (E, B fields) on test particle in beam: uniformly charged cylinder of current I



$$F_r = F_E + F_B = \frac{eI}{2\pi c\beta\varepsilon_0\gamma^2 a^2} r$$

$$F_x = \frac{eI}{2\pi c\beta\varepsilon_0\gamma^2 a^2} x$$

$$x''(s) + K(s)x = \frac{F_{SC}}{m\gamma\beta^2 c^2}$$

Space charge ➔ gradient error

➔Defocusing

➔ Tune shift

$$x''(s) + \left(K(s) - \frac{2r_0 I}{ea^2\beta^3\gamma^3 c}\right) x = 0$$

$$r_0 = \frac{e^2}{4\pi\varepsilon_0 m_0 c^2}$$ Classical particle radius

Space-Charge Effect

Tune shift from gradient error

$$\Delta Q_x = \frac{1}{4\pi}\int_0^{2\pi R}\beta(s)\Delta K_{SC}(s)ds = -\frac{r_0 RI}{e\beta^3\gamma^3 c}\left\langle\frac{\beta_x(s)}{a^2(s)}\right\rangle$$

For cylindrical beam

$$\Delta Q_x = -\frac{n r_0}{2\pi\varepsilon_x\beta^2\gamma^3}$$

$$\varepsilon_x = \frac{a^2}{\beta_x}$$

$$I = \frac{ne\beta c}{2\pi R}$$

$$\propto \frac{n}{\varepsilon_{x,y}}$$

$$\propto \frac{1}{\gamma^3}$$

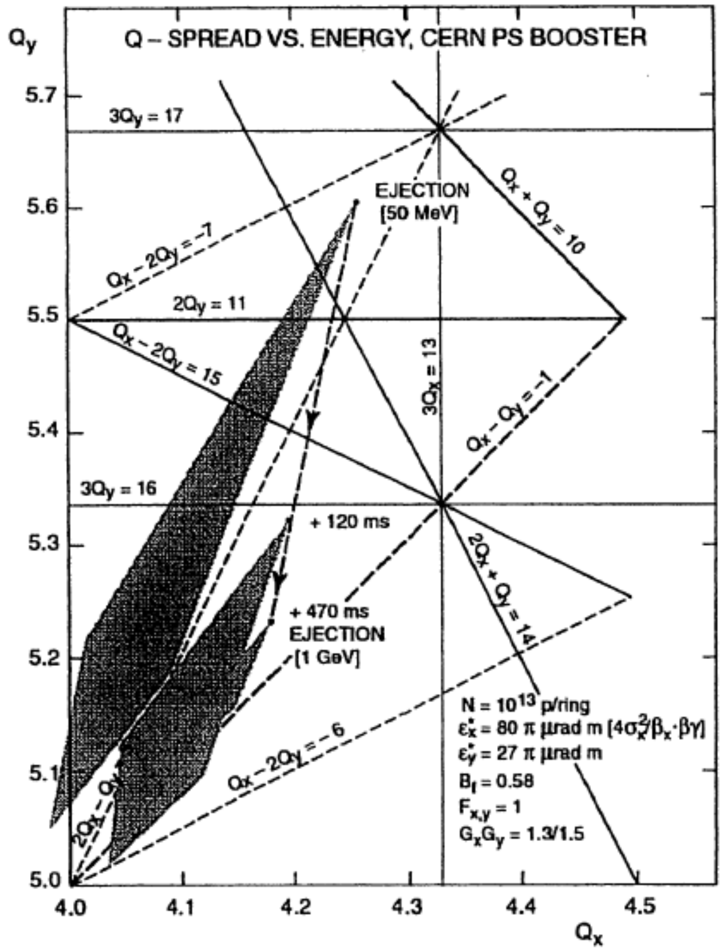
Not all particles in a beam will receive the same tune shift.

Variation in particle density, variation of space charge tune shift across bunch

➔ Tune spread

Space-Charge Effect

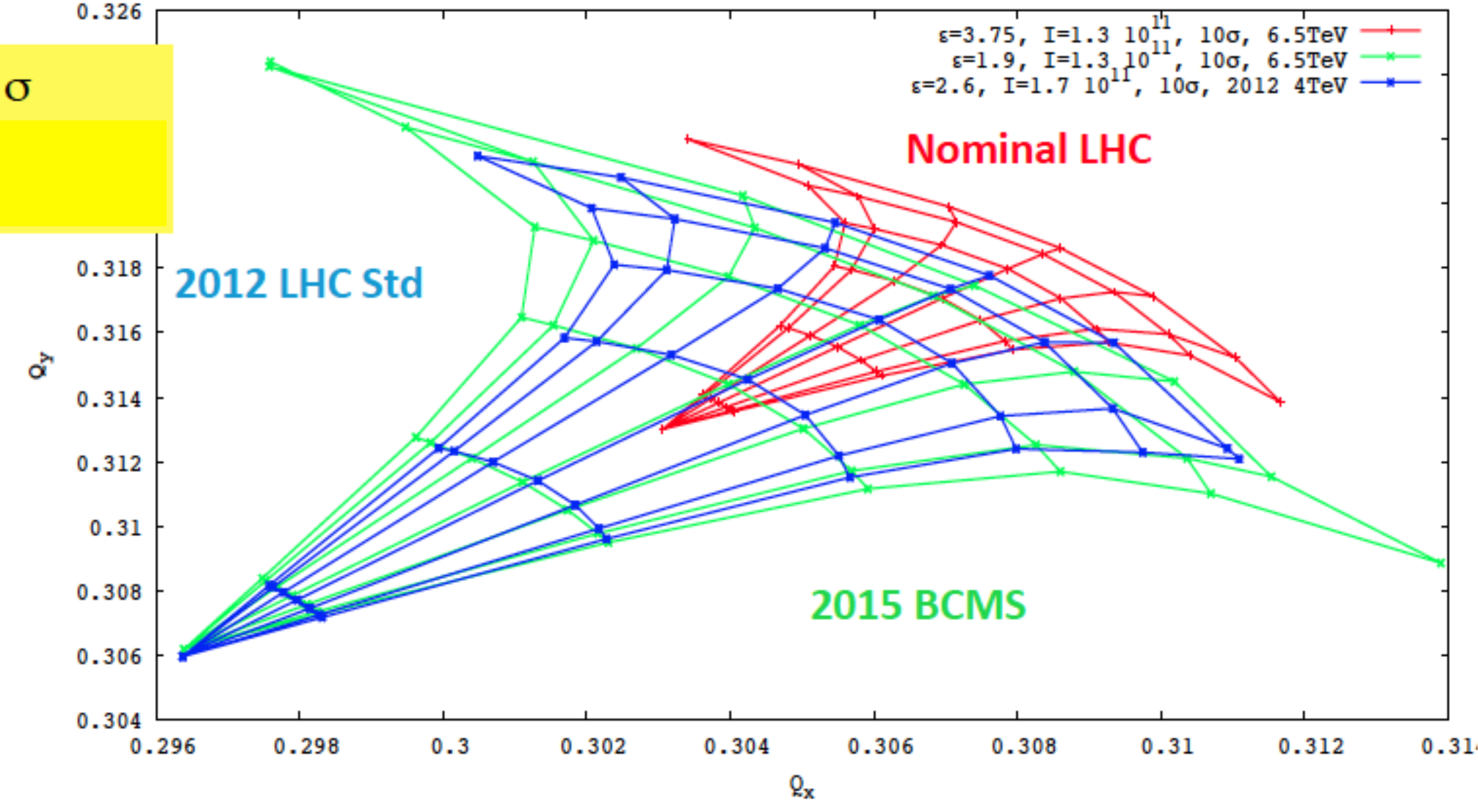
Space charge in the CERN PS booster for high intensity beams:



Not so easy to avoid resonances!!

Beam-beam tune footprint

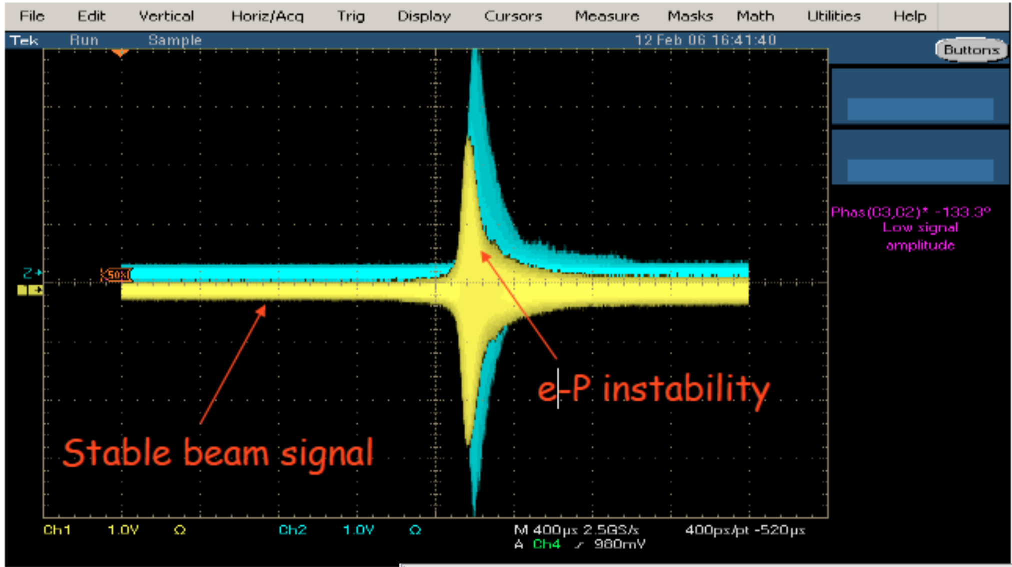
LR separation 10 σ

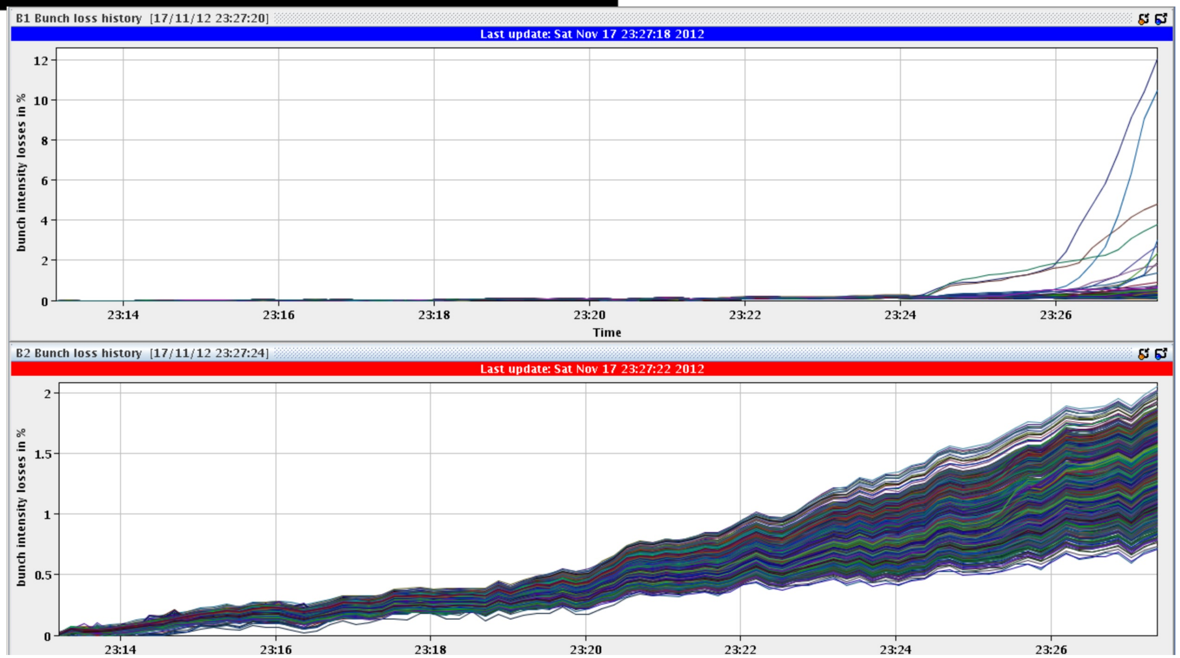


Courtesy T. Pieloni

Instability – what does it look like?

E.g. Fast rising coherent oscillation, beam losses, emittance blow-up





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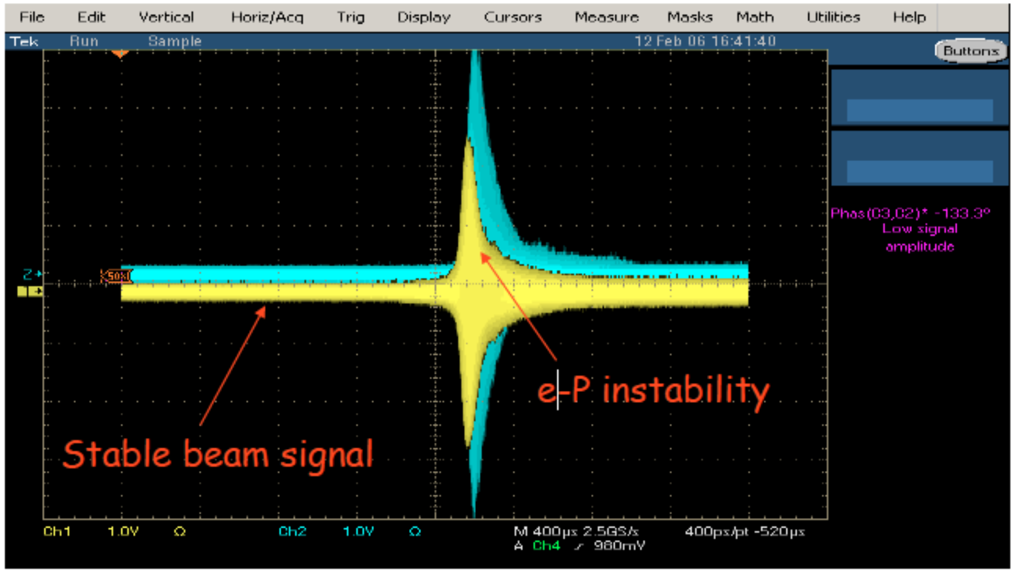
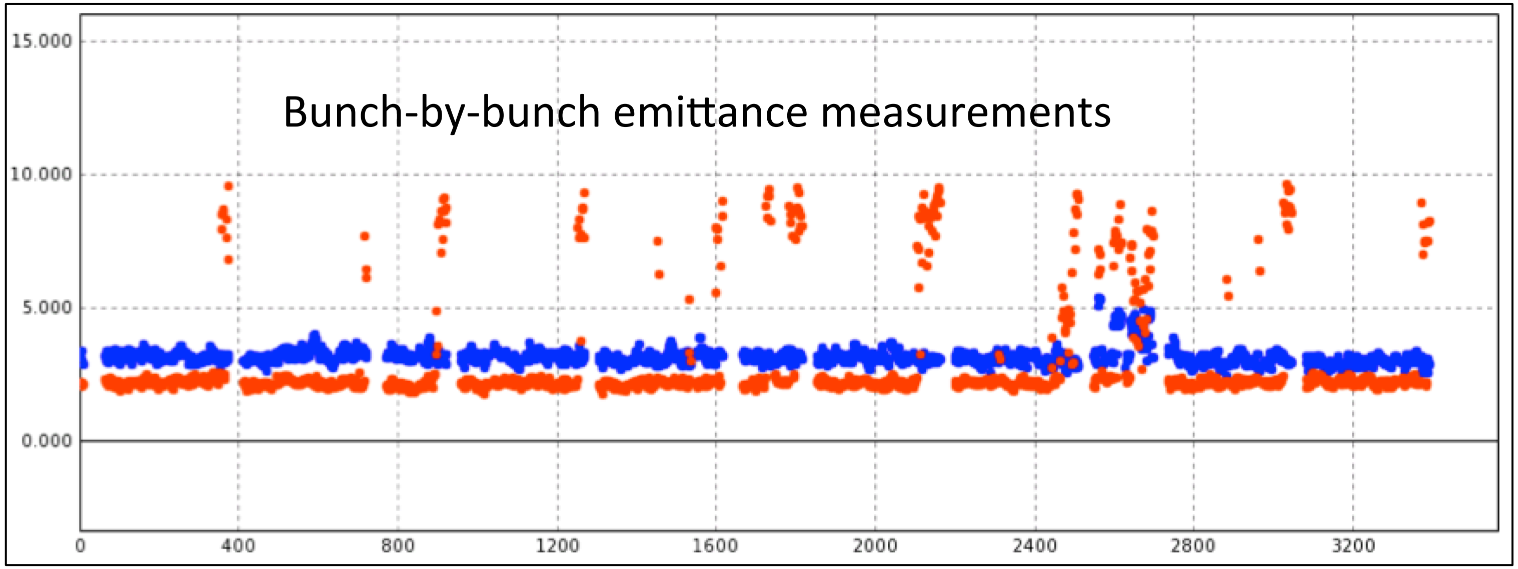




Instabilities - Mitigation

Diagnostics, diagnostics, diagnostics: To identify instability and mitigation mechanisms

- Beam loss monitors: e.g. ionization chambers
  where is the beam lost? High dispersion areas
- Beam position monitors to measure trajectories: bunch-by-bunch
- Beam profile monitors: bunch-by-bunch
- Beam Current Transformers to measure intensity: bunch-by-bunch

Possible mitigation:

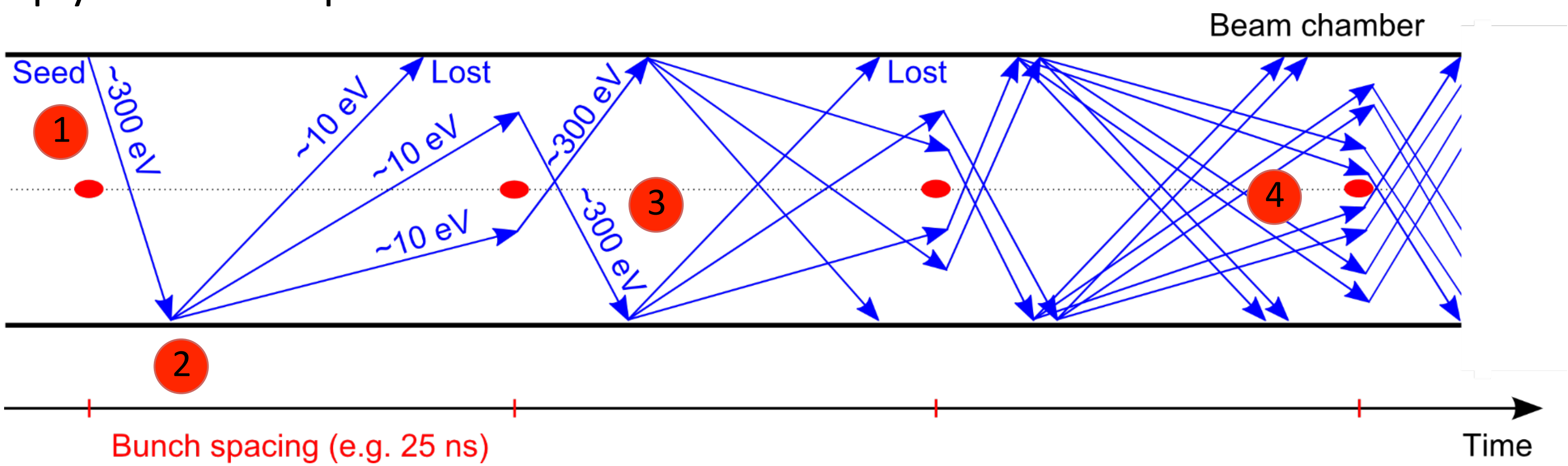
Transverse feedback with sufficient bandwidth

Increase tune spread for Landau Damping: higher chromaticity, octupole fields, tune spread from head-on collisions

Landau Damping: coherent oscillation at frequency within beam frequency spread is generally not excited.

Electron cloud – One of the LHC Challenges

In high intensity accelerators with positively charged beams and closely spaced bunches electrons liberated from vacuum chamber surface can multiply and build up a cloud of electrons.



1) Seed electrons accelerated by beam
2) Produce secondary electrons when hitting chamber
3) Secondary electrons accelerated, producing more electrons on impact
4) May lead to exponential growth of electron density (multipacting)

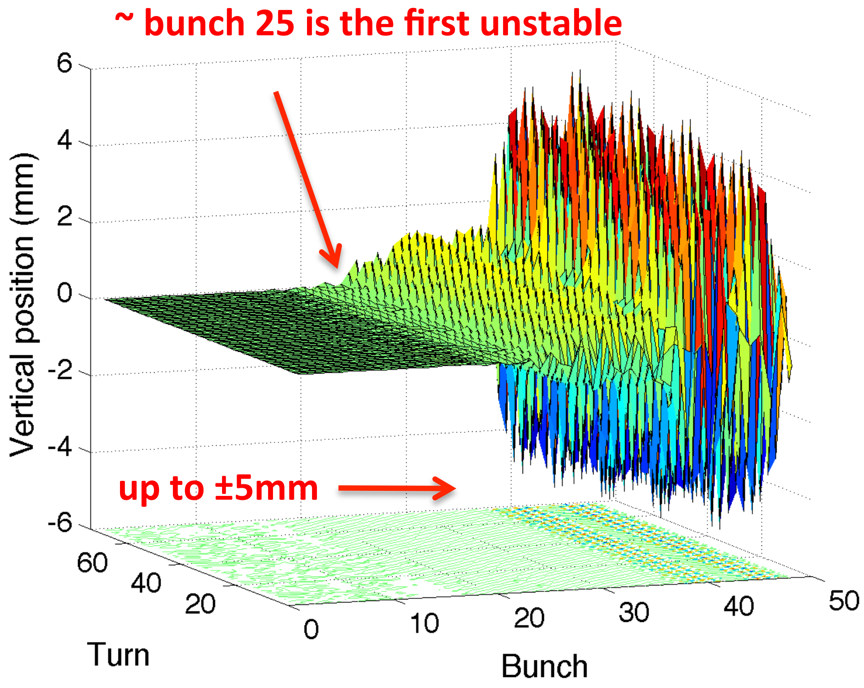
- Trailing bunches of train interact with dense e-cloud
  - Transverse instabilities
  - Transverse emittance blow-up
  - Particle losses
- Other unwanted effects:
  - Heat load on the beam chamber
  - Vacuum degradation

The e⁻ - cloud instability

The LHC nominal bunch spacing is 25 ns. During LHC run 1 25 ns operation was not possible due to e-cloud instability

First injection tests with a train of 25 ns 48 bunches on 26/08/2011:

Typical signature: the tails of the batches are more affected.



Beam becomes unstable immediately after injection.

The beam dump was triggered shortly afterwards due to high losses.

Electron cloud mitigation

- Strong reduction of e-clouds with larger bunch spacing:
  - E.g. 50 ns bunch spacing

- A key parameter is the secondary electron emission yield (SEY) of electrons of the vacuum chambers.

  = ratio between emitted and impacting electrons

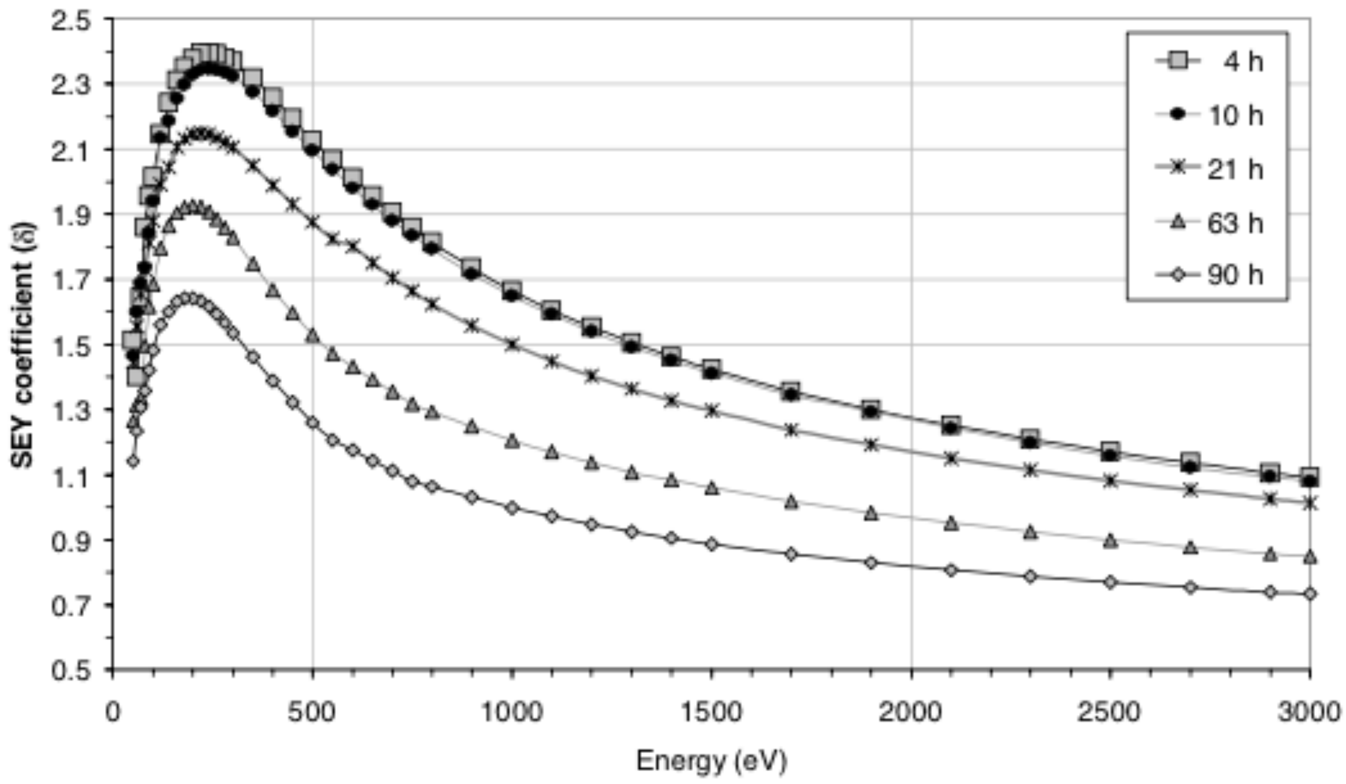
- The e-cloud can 'cure itself': the impact of the electrons cleans the surface (Carbon migration), reduces the electron emission probability and eventually the cloud disappears**.**
- ***'Beam scrubbing'*** consists in producing e-cloud deliberately with the beams in order to reduce the SEY until the cloud 'disappears'.
  - *Done at 450 GeV injection energy – to first order e-cloud energy independent.*
- In April 2011 25 ns beams were used to '***scrub'*** the LHC vacuum chamber at 450 GeV to prepare operation with 50 ns.

Electron Cloud – Self-conditioning of the surface

Exposure to high electron currents and emission can induce structural changes in surface

Leads to lower yield of secondary electrons

From M. Jimenez et al, Proc of Mini-ecloud WS 2003



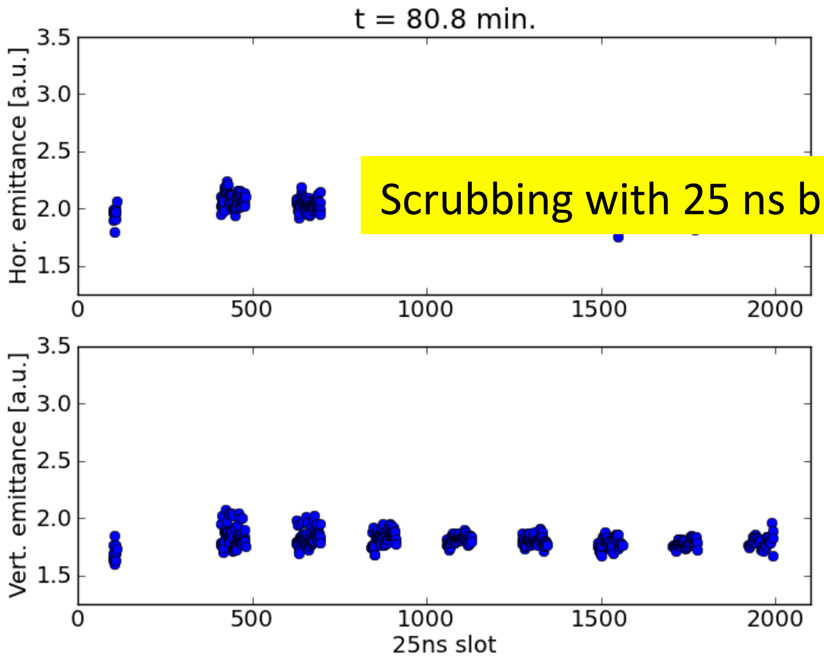
The e⁻ - cloud instability

At the end of 2012 after an extended scrubbing period, the instability was still not under control for long bunch trains.

Emittance blow-up at the end of the trains.

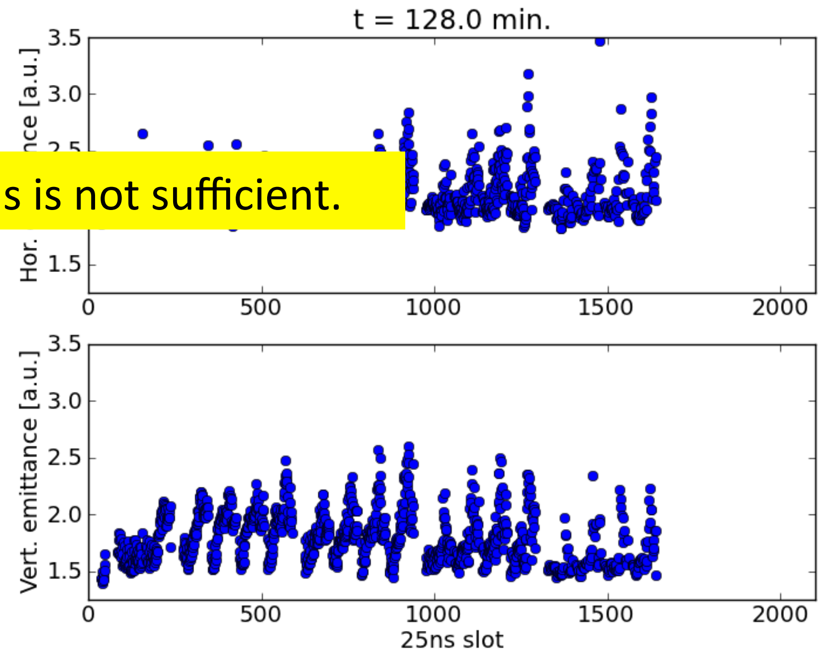
The LHC needs to be filled with 12 injections of 288 bunches with spacing of 25 ns.

Fill of trains with 72 bunches



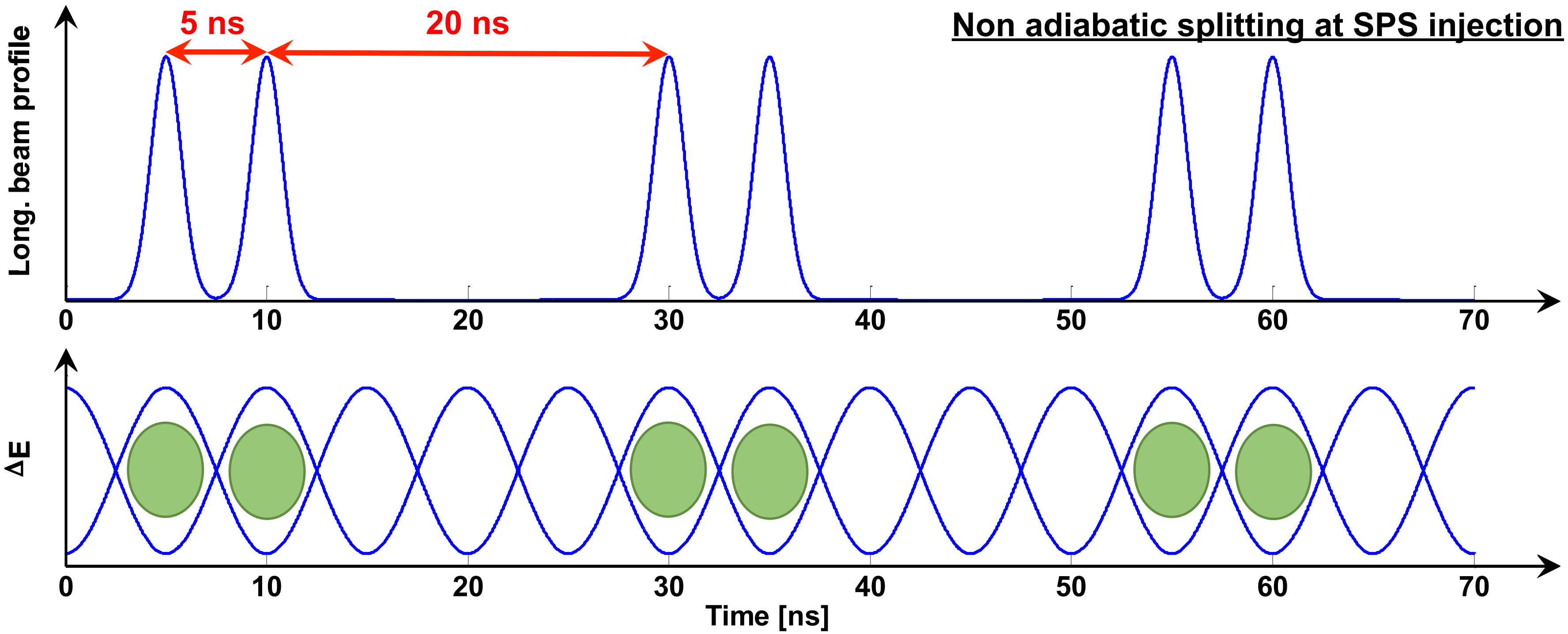
Scrubbing with 25 ns beams is not sufficient.

Fill of trains with 288 bunches



Special LHC scrubbing beam - doublets

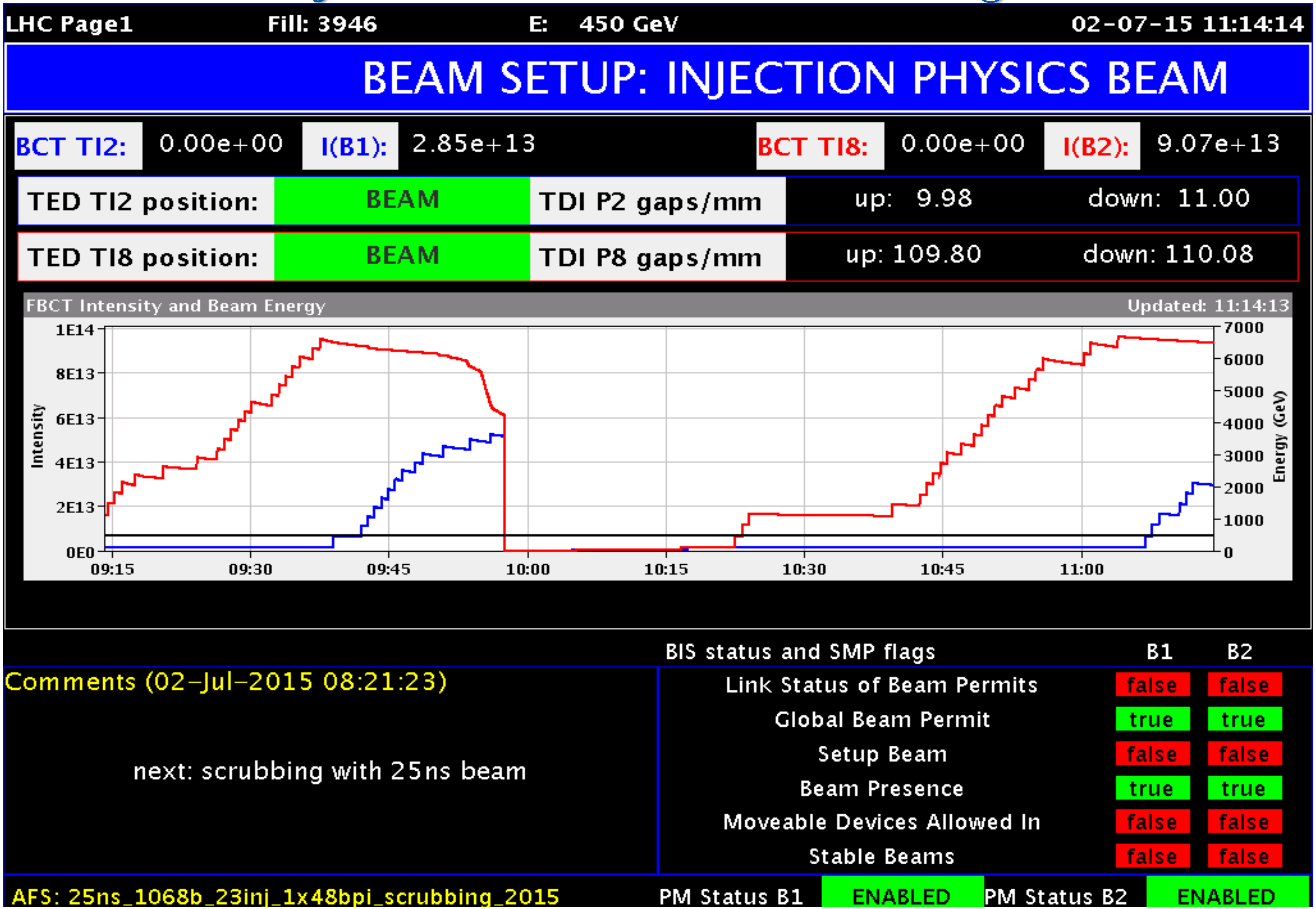
Doublet beam: more electron cloud than 25 ns



The LHC instrumentation, RF, transverse damper has not been designed for this beam. Challenging....

Courtesy G. Iadarola and G. Rumolo

The LHC just finished the first Scrubbing Period..



Scrubbing Status

Summary

- Very productive day
  - Several fills with ~1000 bunches
  - up to 72 bunches per injection
- Main limitation for injections of 25 ns beams is still the vacuum in the MKI
  - Using the solenoids up to 8A during injection – what is the limit?
- Status after the first scrubbing
  - Machine is ready for operation with 50 ns beams
  - Still “some” scrubbing to be done for 25 ns ;-)

Summary from end of first scrubbing run last Friday

Tomorrow

The Large Hadron Collider….