

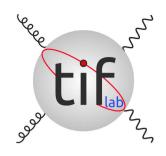
PERTURBATIVE QCD AT THE LHC

STEFANO FORTE Università di Milano & INFN





St. Petersburg, Sept. 4, 2015



QCD IN THE HIGGS ERA

STEFANO FORTE Università di Milano & INFN

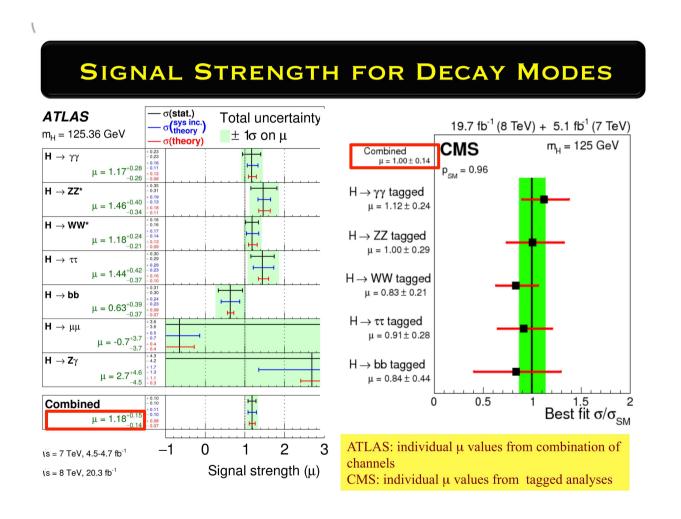




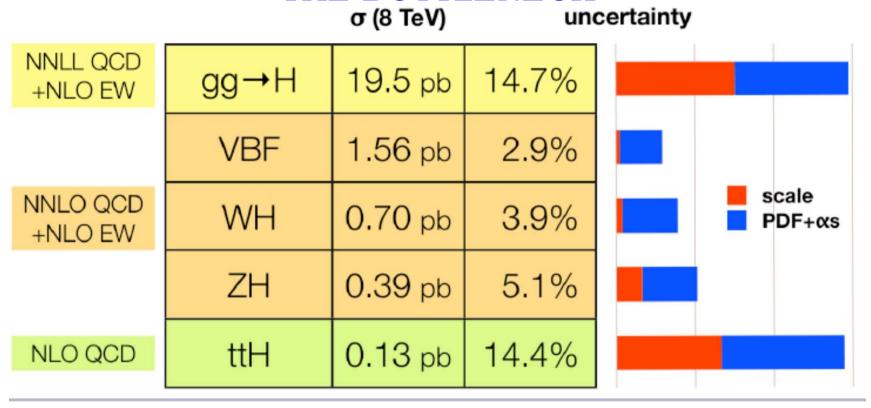
St. Petersburg, Sept. 4, 2015

THE CHALLENGE

HIGGS SIGNAL STRENGTH



THE BOTTLENECK



(J. Campbell, HCP2012)

- QCD, PERTURBATIVE & NONPERTURBATIVE, IS THE DOMINANT SOURCE OF UNCERTAINTY
- MANY UNCERTAINTIES IMPROVING (OR ABOUT TO IMPROVE)

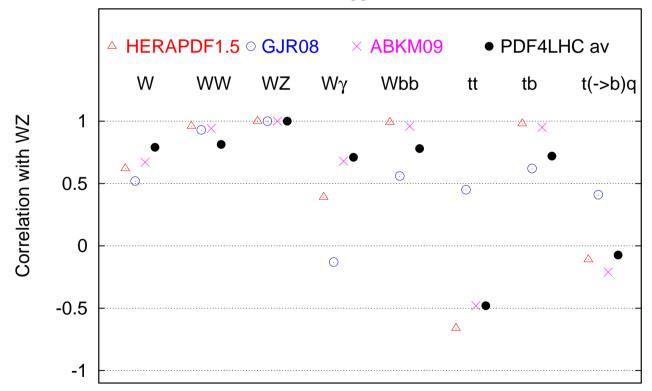
INTERLOCKED KNOWLEDGE

- QCD TALKS TO THE REST OF THE SM!
- CORRELATED UNCERTAINTIES BETWEEN SM PROCESSES

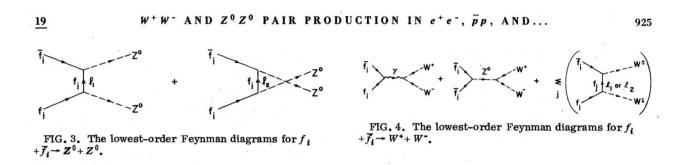
CORRELN. OF PDF UNCERTAINTIES

HIGGS BACKGROUND PROCESSES

LHC HiggsXSWG 2011



AN EXAMPLE GAUGE BOSON PAIR PAIR PRODUCTION



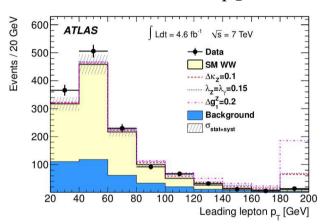
Brown & Mikaelian, 1979

- SENSITIVE TO TRIPLE-GAUGE COUPLINGS & UNITARITY VIOLATION
- IMPORTANT BACKGROUND TO HIGGS PRODUCTION
- CAN BE USED TO BOUND THE HIGGS WIDTH FROM INTERFEROMETRY/OFF-SHELL MEASUREMENTS
- W^+W^- has largest rate, more challenging final state
- NLO QCD CORRECTIONS LONG KNOWN
- NLO ELECTROWEAK CORRECTIONS DETERMINED
- VERY RECENT PROGRESS ON HIGHER ORDER CORRECTIONS & RESUMMATION

W PAIR PRODUCTION

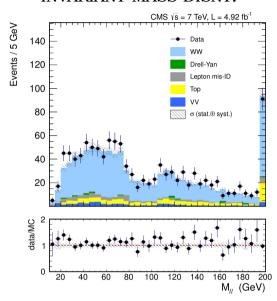
THE DATA

LEADING LEPTON p_T



ATLAS 2013

INVARIANT MASS DISNT.



CMS 2013

- TOTAL CROSS-SECTION MEASURED BY ATLAS & CMS
- SLIGHT EXCESS OVER SM:

 51.9 ± 2.0 STAT. ± 3.9 SYST. ± 2.0 LUM. (ATLAS)

 52.4 ± 2.0 STAT. ± 4.5 SYST. ± 2.0 LUM. (CMS)

VS. 47.0 ± 2.0 MC ± 4.5 SCALE ± 3.0 PDF PB (CAMPBELL, ELLIS, WILLIAMS, 2012)

PDFs

W PAIR PRODUCTION PDF UNCERTAINTIES

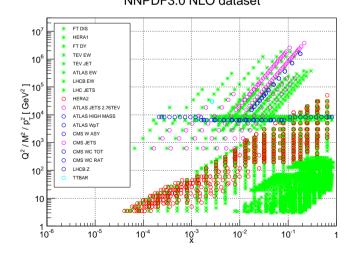
- UNCERTAINTY ON THE TH PREDICTION QUOTED BY ATLAS IS OBTAINED USING MSTW08
- PDF UNCERTAINTY USED IN THE ANALYSIS FROM MSTW08, WITH MSTW08-CT10 DIFFERENCE ADDED

PDF PROGRESS:

MORE FEATURES

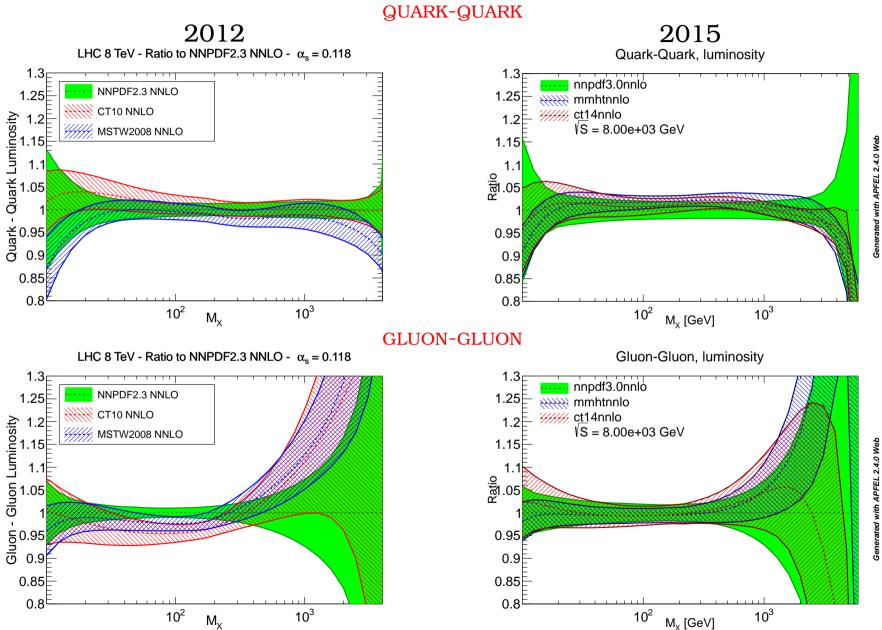
	NNPDF3.0	MMHT14	CT14
No. of fitted PDFs	7	7	6
Parametrization	NEURAL NETS	$x^a(1-x)^b$	$x^a(1-x)^b$
		× CHEBYSCHEV	\times Bernstein
FREE PARAMETERS	259	37	30-35
UNCERTAINTIES	REPLICAS	HESSIAN	HESSIAN
TOLERANCE	None	DYNAMICAL	DYNAMICAL
CLOSURE TEST	✓	×	×
REWEIGHTING	REPLICAS	EIGENVECTORS	EIGENVECTORS

MORE DATA NNPDF3.0 NLO dataset



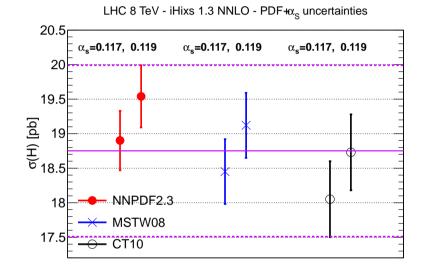
PDFs: RECENT PROGRESS

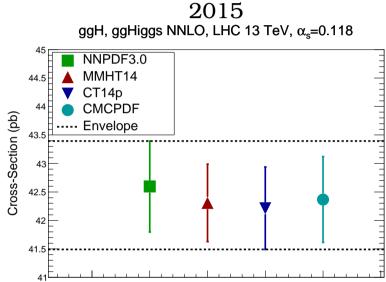
PARTON LUMINOSITIES



PDFs: RECENT PROGRESS HIGGS IN GLUON FUSION

HIGGS IN GLUON FUSION
2012



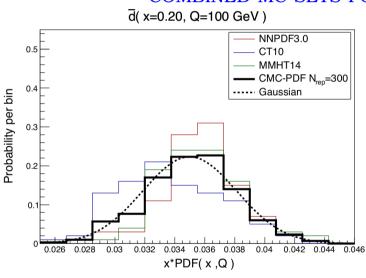


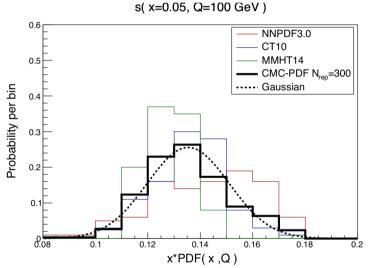
- PDF4LHC PRESCRIPTION 2012: ENVELOPE, PDF UNCERTAINTY $\sim 6\%$

THE NEW PDF4LHC PRESCRIPTION

- CONVERT ALL SETS INTO MONTE CARLO
- HESSIAN SETS CAN BE CONVERTED BY PERFORMING MONTE CARLO IN PARAMETER SPACE (Watt, Thorne, 2012)
- COMBINE MONTE CARLO REPLICAS INTO SINGLE SET







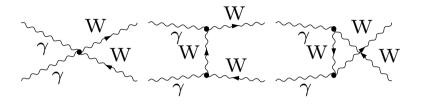
- COMBINED SET CONVERTED INTO MANAGEABLE FORMATS:
 - COMPRESSED MONTE CARLO: MC100

(Carrazza, Latorre, Rojo, Watt, 2015)

- ULTRAFAST OR ULTRAPRECISE HESSIAN: H30 & H100

(Gao, Nadolsky, 2014; Carrazza, SF, Kassabov, Latorre, Rojo, 2015)

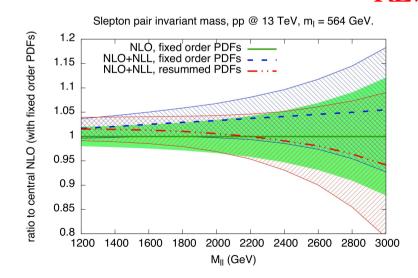
PDF EXOTICA QED PDFs



- ullet PHOTON COUPLES DIRECTLY TO W
- ullet Photon-induced W pair production comparable to quark-induced for large

NNPDF2.3QED, Carrazza et al. 2013 RESUMMED PDFS

INVARIANT MASS



10 NNPDF2.3QED, qq̄
NNPDF2.3QED, γγ
NNPDF2.3QED, γγ
NNPDF2.3QED, γγ
MRST2004QED, γγ
10⁻²
10⁻³
200 400 600 800 1000 1200
M_{WW} (GeV)

WW production @ LHC √s = 8 TeV

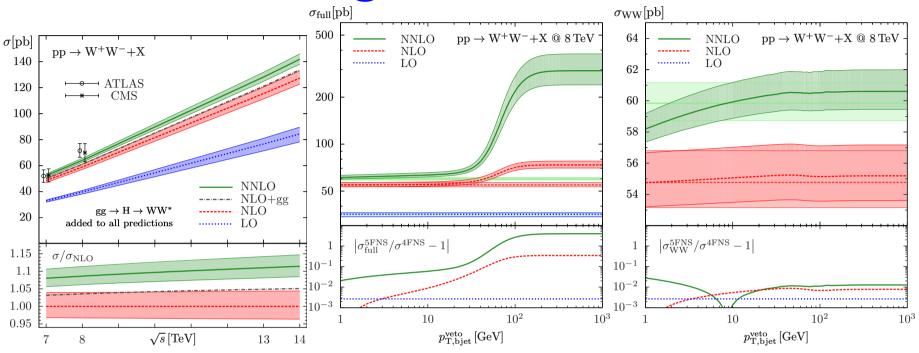
- THRESHOLD RESUMMATION AFFECTS LARGE x
- CORRECTION COMPARABLE IN SIZE TO THAT ON MATRIX ELEMENT
- COMPENSATION BETWEEN CORRN
 TO PDF & ME

 $PDFS \Rightarrow HEAVY FINAL STATES$

Bonvini, Marzani, Rojo, Rottoli, Ubiali et al., 2015

NNLO & HEAVY QUARKS

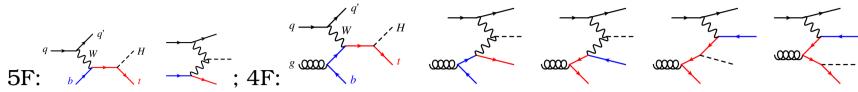
W PAIR PRODUCTION NNLO QCD CORRECTIONS



(Gehrmann, Grazzini, Kallweit, Maierhöfer, von Mantteuffel, Pozzorini, Rathlev, Tancredi, 2014)

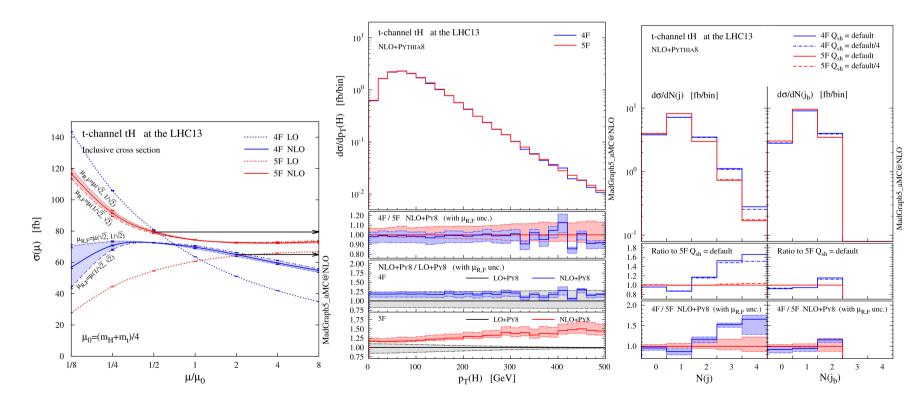
- NLO QCD, NNLO GLUON CHANNEL, NLO EW CORRNS KNOWN, NNLO COMPUTED RECENTLY: $\sim 10\%$ enhancement w.r. to NLO, underestimated by scale variation (new partonic subchannels)
- 5-flavor vs 4 flavor scheme: in 5FS, huge resonant pp o Wt o WWb
- CANNOT JUST REJECT B WITH $p_T^b < p_{T, \, veto}^b \Rightarrow \ln p_T/m_b$ DEPENDENCE, AMBIGUITY
- SUBTRACT RESONANT USING DEPENDENCE ON WIDTH Γ_t

5FS vs 4FS HIGGS+SINGLE TOP

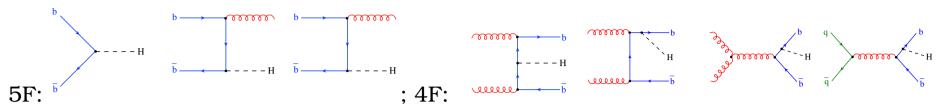


(Demartin, Maltoni, Mawatari, Zaro, 2014)

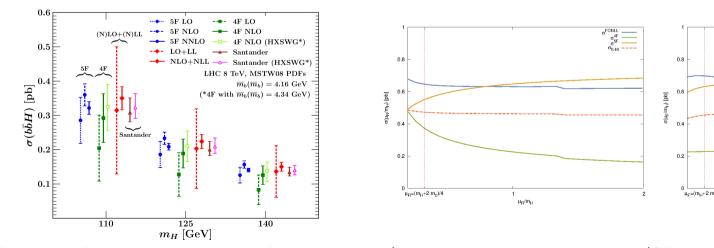
- 5FS EASIER AT HIGHER ORDERS, BUT 4FS MORE REALISTIC FINAL STATE
- GOOD AGREEMENT FOR INCLUSIVE OBSERVABLES ALREADY AT NLO
- AGREEMENT FOR SINGLE DISTRIBUTIONS, 5FS MORE ACCURATE FOR MULTIPARTICLE FS



5FS vs 4FS bb Higgs



- LARGE DIFFERENCES BETWEEN 4FS & 5FS, ALLEVIATED BY LOW SCALE CHOICE & HIGHER ORDER IN THE 4FS COMPUTATION
- MATCHED RESULT AVAILABLE IN FONLL (4FS LO+ 5FS NNLL) & SCET (4FS NLO+ 5FS NLL) APPROACH: DIFFER BY SUBLEADING TERMS, FONLL ALLOWS FOR ANY COMBINATION OF ORDERS
- FONLL shows that pure mass corrections to massless NNLL $\sim 10\%$, but affected by large scale dependence
- NAIVE 'SANTANDER' MATCHING NOT VERY RELIABLE



(Bonvini, Papanastasiou, Tackmann, 2015);

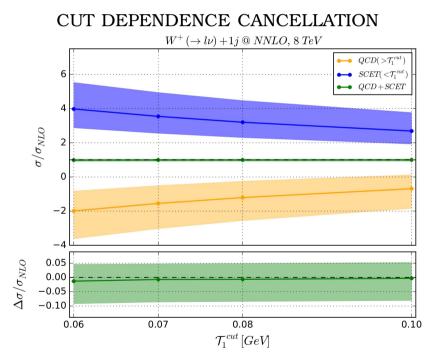
(SF, Napoletano, Ubiali, 2015)

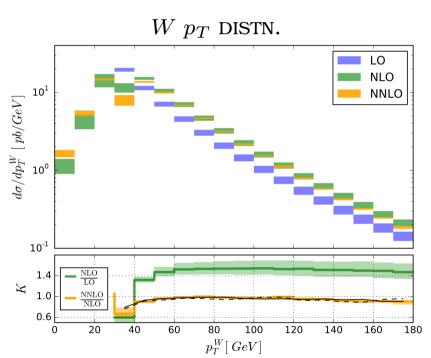
NNLO PROGRESS W+JET; W p_T : JETTINESS SUBTRACTION

- CATANI-GRAZZINI-LIKE SUBTRACTION FOR COLORED FINAL STATES
- CANCEL INFRARED DIVERGENCE USING UNIVERSAL BEHAVIOUR OF RESUMMED RESULT:

N-JETTINESS \mathcal{T}_N AS RESUMMED OBSERVABLE

- FOR $\mathcal{T}_N > \mathcal{T}_N^{\mathrm{cut}}$, NNLO=NLO+ONE JET
- FOR $\mathcal{T}_N < \mathcal{T}_N^{\mathrm{cut}}$ EXPAND OUT RESUMMED RESULT



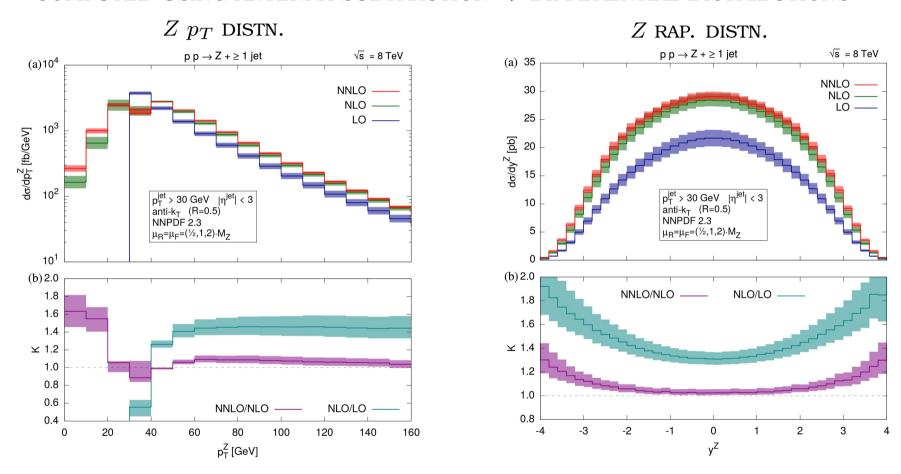


(Boughezal, Focke, Giele, Liu, Petriello, 2015)

- NNLO CORRECTIONS TO W p_T COMPUTED: MODERATE
- METHOD ALSO APPLIED TO HIGGS+JET: ALL-CHANNEL NNLO

NNLO PROGRESS Z+JET

- IMPORTANT FOR PDF DETERMINATION: SIZE OF THE GLUON
- COMPUTED USING ANTENNA SUBTRACTION ⇒ DIFFERENTIAL DISTRIBUTIONS

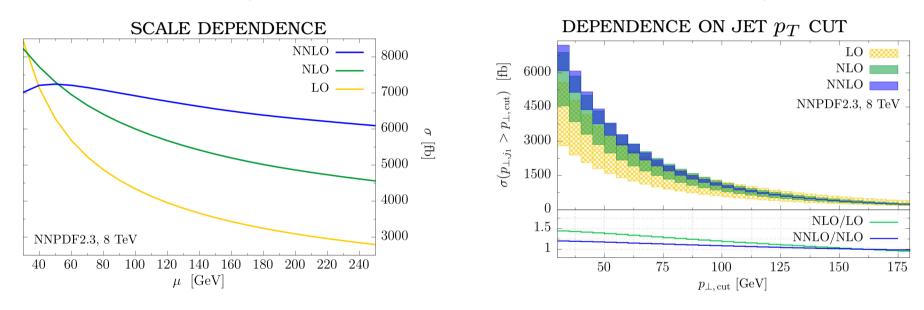


(Gehrmann-de Ridder, Gehrmann, Glover, Huss, Morgan, 2015)

- MODERATE NNLO CORRECTIONS
- ullet CORRECTIONS IN DIFFERENTIAL DISTRIBUTIONS NON UNIFORM \Rightarrow CANNOT JUST GIVE K-FACTOR

NNLO PROGRESS HIGGS+JET: FULL COMPUTATION

- FULLY DIFFERENTIAL, ALL-CHANNEL ANALYTIC RESULT
- MAIN DIFFICULTY:
 - DIFFERENT MULTIPLICITIES CANNOT BE COMBINED ⇒ PHASE-SPACES DIFFERENT
 - FULLY ANALYTIC \Rightarrow NO INTEGRATION OVER HIGHER MULTIPLICITIES
- SOLUTION: SECTOR IMPROVED RESIDUE SUBTRACTION FOR PHASE-SPACE PARAMETRIZATION (Czakon 2010; Boughezal, Melnikov, Petriello 2012)



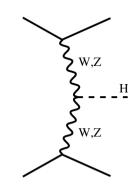
(Boughezal, Caola, Melnikov, Petriello, Schulze, 2015)

- SIZABLE NNLO CORRECTIONS
- SIZE OF CORRNS DEPENDS STRONGLY ON MINIMUM p_T OF THE JET
- FIDUCIAL RESULTS (INCLUDING HIGGS DECAY) NOW AVAILABLE (Caola, Melnikov, Schulze, 2015)

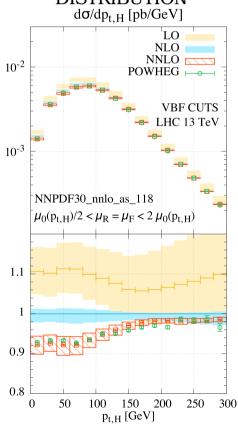
NNLO PROGRESS

FULLY DIFFERENTIAL HIGGS IN W FUSION

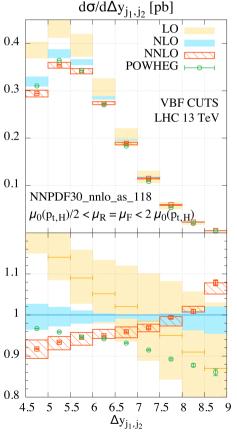
(Cacciari, Dreyer, Karlberg, Salam, Zanderighi, 2015)



HIGGS p_T DISTRIBUTION



RAPIDITY SEP. LEADING JETS



- STRUCTURE FUNCTION APPROX: SQUARE OF DIS
- NNLO DIS KNOWN AT INCLUSIVE LEVEL: DIFFERENTIAL INFO LOST
- PROJECTION TO BORN:
 - INCLUSIVE 2 LOOP HAS BORN KINEMATICS!
 - DOUBLE REAL & PROJECTED ONE-LOOP SINGLE REAL IN BORN KINEMATICS
 - EXCLUSIVE PART FROM VBF H+3J AT NLO (Figy, Hankele, Jäger, Schissler, Zeppenfeld 2008-2014)

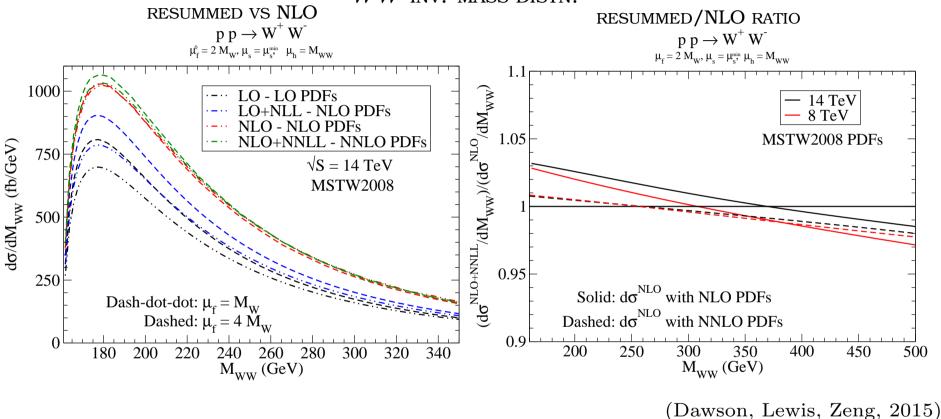
RESULTS

- LARGE NNLO CORRNS: NLO FIRST ORDER AT WHICH NON-INCLUSIVENESS MATTERS
- CAPTURED BY PARTON SHOWER-ING FOR p_T DISN, NOT FOR RAPIDITY SEPARATION

SOFT GLUON RESUMMATION

W PAIR PRODUCTION SOFT GLUON RESUMMATION

WW INV. MASS DISTN.



- RESUMMATION PERFORMED IN SCET AT NNLL (CORRESP. TO $NN^{1/2}LL$)
- 3-4% enhancement at the peak, $\lesssim 1\%$ enhancement of total xsect.
- MOST OF THE EFFECT DUE TO USE OF NNLO PDFS \Rightarrow APPROXIMATE NNLO

Q: WHEN IS RESUMMATION USEFUL?

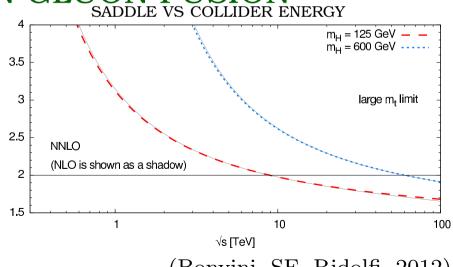
- PARTONIC CROSS SECTIONS $\hat{\sigma}(z,\alpha_s)$ ARE DISTRIBUTIONS, $0 \le z = \frac{M_h^2}{s} \le 1$, CONVOLUTED WITH LUMINOSITY TO GIVE HADRONIC CROSS-SECTION
- THEIR MELLIN TRANSFORMS $\hat{\sigma}(N, \alpha_s)$ ARE ORDINARY FUNCTIONS
- FOR GIVEN m_H^2 AND s ONLY ONE "SADDLE" N VALUE CONTRIBUTES; POSITION OF SADDLE DETERMINED ESSENTIALLY BY PDF \Rightarrow PDF TELLS YOU WHICH FRACTION OF HADRON MOMENTUM GOES INTO PARTONIC PROCESS

A: WHEN SADDLE N IS LARGE!

- SOFT RESUMMATION INCLUDES TO ALL ORDERS $\alpha_s \ln(1-z)$, $z = \frac{M_X^2}{s} \Leftrightarrow \alpha_s \ln N$
- SOFT $\leftrightarrow z \to 1 \leftrightarrow N \to \infty$.

EXAMPLE: HIGGS IN GLUON FUSION

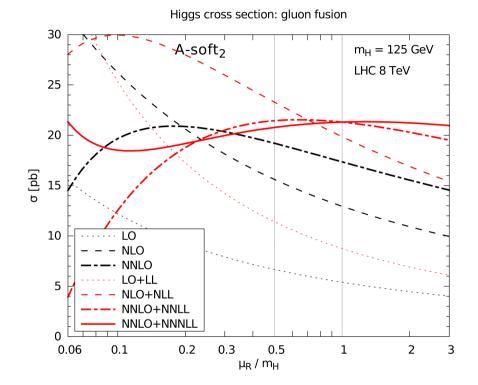
- RESUMMATION CURRENTLY INCLUDED IN HXSWG RECOMMENATION: NNLO+NNLL
- BUT $N_{
 m saddle} \sim 2$, \Rightarrow RESUMMATION SUMS UP $\beta_0 \alpha_s \ln 2 \approx 0.04 \ll 1$



(Bonvini, SF, Ridolfi, 2012)

HIGGS IN GLUON FUSION: DOES RESUMMATION HELP? NO? YES!

$$\begin{split} M\left[\eta_{gg}^{(3)}\right](N) &\simeq 36 \log^6 N & (\rightarrow 0.0013\%) \\ &+ 170.679 \ldots \log^5 N & (\rightarrow 0.0226\%) \\ &+ 744.849 \ldots \log^4 N & (\rightarrow 0.2570\%) \\ &+ 1405.185 \ldots \log^3 N & (\rightarrow 1.0707\%) \\ &+ 2676.129 \ldots \log^2 N & (\rightarrow 4.0200\%) \\ &+ 1897.141 \ldots \log N & (\rightarrow 5.1293\%) \\ &+ 1783.692 \ldots & (\rightarrow 8.0336\%) \\ &+ 108 \frac{\log^5 N}{N} & (\rightarrow 0.0105\%) \\ &+ 615.696 \ldots \frac{\log^4 N}{N} & (\rightarrow 0.1418\%) \\ &+ 2036.407 \ldots \frac{\log^3 N}{N} & (\rightarrow 0.9718\%) \\ &+ 3305.246 \ldots \frac{\log^2 N}{N} & (\rightarrow 2.9487\%) \\ &+ 3459.105 \ldots \frac{\log N}{N} & (\rightarrow 5.2933\%) \\ &+ 703.037 \ldots \frac{1}{N} & (\rightarrow 1.7137\%). \end{split}$$



(Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger, 2014)

- "LEADING" LOGS DO NOT PROVIDE THE DOMINANT CONTRIBUTION
- ullet EXPANSION IN POWERS OF 1/N CONVERGES VERY SLOWLY

Bonvini and Marzani, 2014

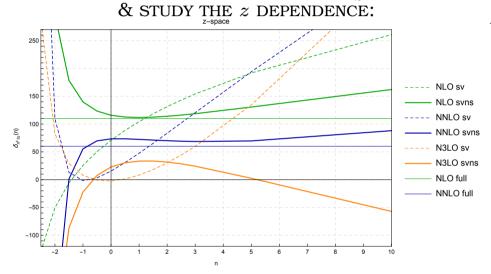
- RESUMMED EXPANSION CONVERGES FASTER THAN UNRESUMMED ONE
- SCALE DEPENDENCE ALWAYS SMALLER AT RESUMMED LEVEL

HIGGS IN GLUON FUSION: APPROXIMATE N³LO?

IS THERE A PREFERRED WAY OF EXPANDING?

NO?

PERFORM SOFT EXPANSION OF $\frac{\hat{\sigma}(z)}{z^{n+1}}$

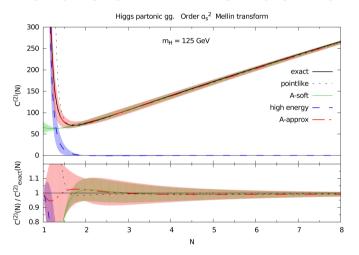


(Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger, 2014)

- SOFT EXPANSION DEPENDS STRONGLY ON WHAT ONE EXPANDS
- NO SIGN OF CONVERGENCE WITHIN THE KNOWN ORDERS

YES!

COMBINE SMALL AND LARGE N SINGULARITIES, ALLOWING FOR UNCERTAINTY DUE TO UNKNOWN ONES:

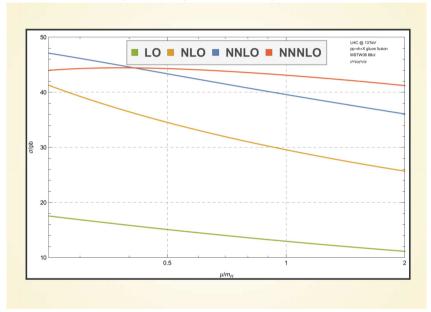


(Ball, Bonvini, SF, Marzani, Ridolfi, 2013)

- ASYMPTOTIC CONSTRAINTS STRONGLY BOUND BEHAVIOUR IN THE MIDDLE
- AT KNOWN ORDERS, EXACT RESULT NICELY BRACKETED

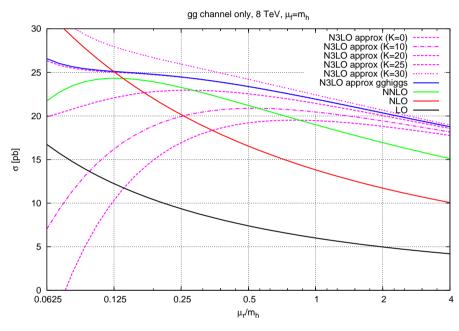
HIGGS IN GLUON FUSION: EXACT N³LO!

SCALE DEP.
VS PERTURBATIVE ORDER



(Anastasiou, Duhr, Dulat, Herzog, Mistlberger, 2015)

SCALE DEP. OF N3LO VS. SIZE COMPARED TO APPROX N3LO

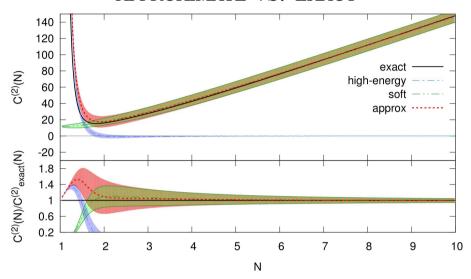


(Bühler, Lazopoulos, 2013)

- EXACT N³LO PUBLISHED OBTAINED AS SERIES EXPANSION ABOUT THE SOFT LIMIT, IN POINTLIKE APPROX
- SMALL SCALE DEPENDENCE \Rightarrow PERTURBATIVE STABILITY!
- IN GOOD AGREEMENT WITH RESUMMATION/APPROX.!

TOP PRODUCTION AT APPROXIMATE N³LO

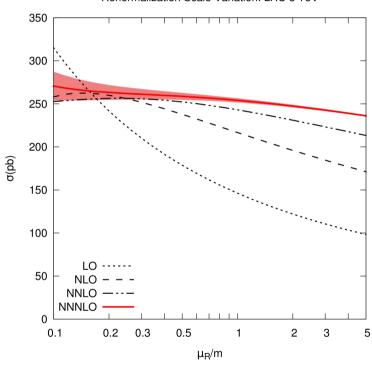
NNLO MELLIN-SPACE RESULT APPROXIMATE VS. EXACT



- FULL NNLO TOP PRODUCTION COMPUTED RECENTLY! (Czakon, Mitov et al., 2012-2013)
- AGREES WELL WITH "ANALYTIC" NNLO APPROXIMATION
- CAN CONSTRUCT APPROXIMATE \mathbb{N}^3 LO \rightarrow
- SIGNIFICANTY REDUCES SCALE DEPENDENCE, $\sim 10\%$ CORRECTION AT LHC8

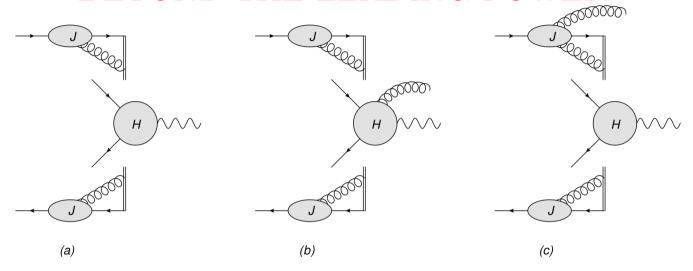
TOTAL CROSS-SECTION SCALE DEPENDENCE

Renormalization Scale Variation: LHC 8 TeV



(Bonvini, S.F., Muselli, Ridolfi, 2015)

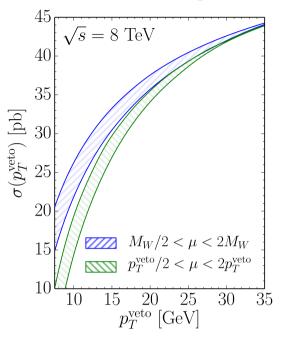
SOFT RESUMMATION BEYOND THE LEADING POWER

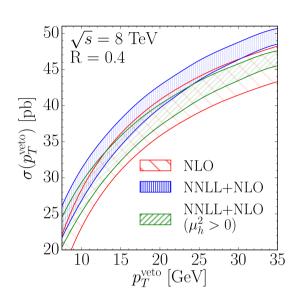


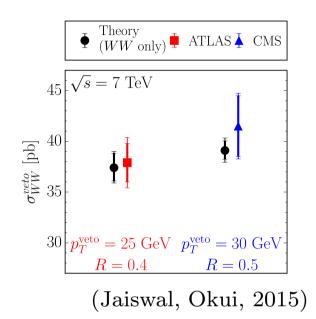
- IMPRESSIVE PROGRESS IN THE ORGANIZATION OF RESUMMATION BEYOND THE EIKONAL LEVEL: NEXT-TO-EIKONAL $\frac{\ln^k N}{N}$; NEXT-TO-NEXT-TO-EIKONAL $\frac{\ln^k N}{N^2}$ ETC (Laenen, Magnea, C.White+ Bonocore, Melville, Stavenga, Vernazza, 2012-2105)
- "METHOD OF REGIONS": SEPARATE INTEGRATION REGIONS OVER MOMENTA THROUGH APPROPRIATE SCALING
- COMBINE WITH FACTORIZATION TO CLASSIFY EMISSIONS FROM INTERNAL BLOBS, DRESSED WITH RADIATION FROM EXTERNAL LINES

P_T RESUMMATION AND JETS

W PAIR PRODUCTION JET VETO RESUMMATION

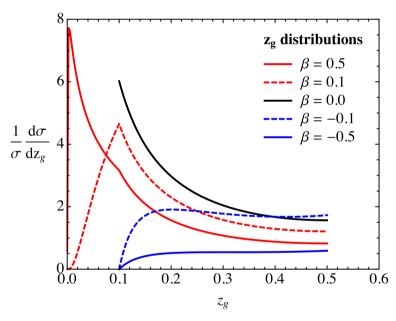






- JET VETO $p_T < p_{T, \, veto}$ IS IMPOSED BY ATLAS, CMS TO REDUCE BACKGROUND FROM TOP
- K-factor reduced by $\sim 40\%$ by jet veto \Rightarrow large cancellation between virtual corrections and small p_T real emission: Strong scale dependence
- CROSS-SECTION FOR HIGGS+ AT LEAST ONE JET CONTAINS DOUBLE LOGS OF MINIMAL p_T OF JET \Rightarrow CROSS SECTION WITH JET VETO CONTAINS DOUBLE LOGS OF p_t^{veto} : $\sigma_{>1} \sim (\alpha L^2)^n$; $\sigma_{\text{tot}} \sim \alpha^n \to \sigma_o \equiv \sigma_{\text{tot}} \sigma_{>1} \sim (\alpha L^2)^n$;
- RESUMMED UP TO NNLL (Jaiswal, Okui, 2015); AGREEMENT AT FIDUCIAL LEVEL, EXTRAPOLATION WITH POWHEG LEADS TO OVERESTIMATE THE TOTAL CROSS SECTION, GOOD AGREEMENT IF EXTRAPOLATION PERFORMED USING ANALYTIC RESUMMATION (Zanderighi, Monni, 2015)

JETS: COLLINEAR SAFETY AND SUDAKOV SAFETY



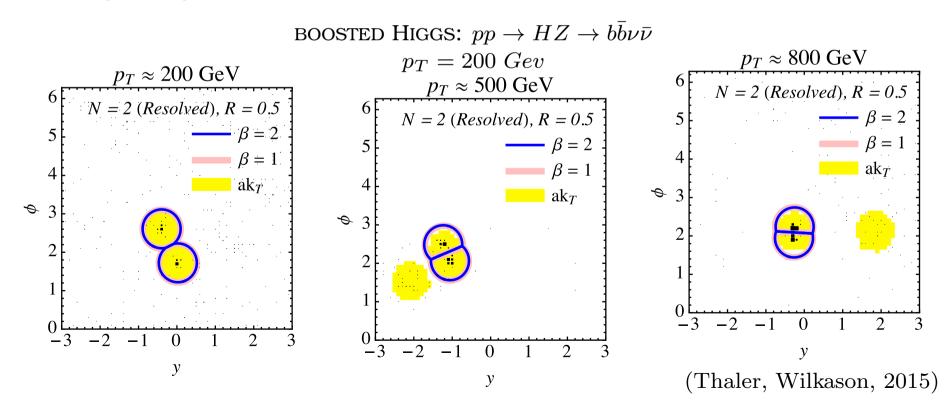
(Larkoski, Marzani, Thaler, 2015)

- PROGRESS IN THE DEVELOPMENT OF TOOLS FOR JET DEFINITION AND CHARACTERIZATION
- JET-SHAPE OBSERVABLES CHARACTERIZING A SINGLE JET (JET MASS, BROADENING) DEFINED, NON-GLOBAL LOGS RESUMMED, ANALYTIC RESULTS FOR JET SUBSTRUCTURE TOOLS
- SUDAKOV SAFE: NO α_s EXPANSION, BUT CALCULABLE AT RESUMMED LEVEL
- EXAMPLE: MOMENTUM SHARING $z_g \equiv \frac{\min(p_t^1, p_t^2)}{p_t^1 + p_T^2}$; USED FOR SOFT-DROP DECLUSTERING, \Rightarrow REMOVE WIDE-ANGLE SOFT RADIATION (REDUCE CONTAMINATION), $z_g > z_{cut} \left(\frac{R_{12}}{R_0}\right)^{\beta}$, R_0 JET RADIUS
- z_g NOT IRC SAFE IF $\beta > 0$
- SUDAKOV SAFE IF z_g CONDITIONAL TO VALUE OF $\frac{R_{12}}{R_0}$, RESUMMING THE DISTN. OF THE LATTER

JETS: THE XCONE ALGORITHM

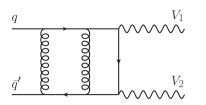
(Stewart, Tackmann, Thaler, Vermilion, Wilkason, 2015)

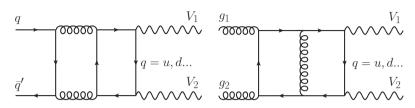
- A NEW EXCLUSIVE JET ALGORITHM DEFINED BY MINIMIZING N-JETTINESS: $\mathcal{T}_N = \sum_i \{\min \rho_{\rm jet}(p_i, n_1) \dots \rho_{\rm jet}(p_i, n_N), \rho_{\rm beam}(p_i)\}; \ \rho_{\rm jet}(p_i, nA) \ \text{DISTANCE TO } A$ -TH AXIS, $\rho_{\rm beam}(p_i)$ DISTANCE TO THE BEAM; OPTIMIZED CHOICE OF MEASURE; ITERATIVE MINIMIZATION WITH SUITABLE SEED CHOICE
- INTERPOLATES SMOOTHLY BETWEEN RESOLVED AND BOOSTED KINEMATICS
- IN VERY BOOSTED CASE, INCLUSIVE ALGORITHMS (SUCH AS ANTI- k_T) TEND TO MERGE JETS AND IDENTIFY ISR AS 2ND JET, WHILE XCONE MAINTAINS GOOD PERFORMANCE

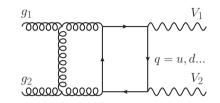


OFF-SHELL

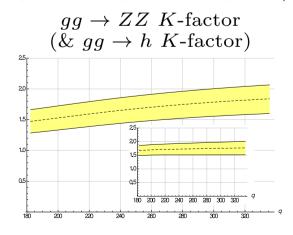
W/Z PAIR PRODUCTION OFF-SHELL EFFECTS AND GLUON FUSION







- NO WS IN FINAL STATE: FOR ACCURATE PHENOMENOLOGY, MUST COMPUTE $pp \to V_1 V_2 \to (l_1 \bar{l}_1')(l_2 \bar{l}_2')$ \Rightarrow TWO-LOOP HELICITY AMPLITUDES IN QUARK-ANTIQUARK CHANNEL RECENTLY COMPLETED (Caola, Henn, Melnikov, Smirnov², 2014) \Rightarrow MADE NNLO RESULT POSSIBLE!
- GLUON FUSION CONTRIBUTION STARTS AT NNLO, AMOUNTS TO ABOUT 5%: WHAT IF IT IS OFF BY A FACTOR 2 DUE TO RADIATIVE CORRNS.?:
 - TWO-LOOP CONTRIBUTION MEDIATED BY MASSLESS QUARK LOOPS JUST COMPLETED, AVAILABLE WITH OFF-SHELL GAUGE BOSONS (Caola, Henn, Melnikov, Smirnov², 2015)
 - * CONTRIBUTION FOR OFF-SHELL ZZ MEDIATED BY TOP LOOP IN $m_t \to \infty$ LIMIT JUST COMPLETED (Melnikov, Dowling, 2015)
 - * BEHAVIOUR OF K-FACTOR SIMILAR TO THAT OF $gg \to H$ K-FACTOR; IN GOOD AGREEMENT WITH PREVIOUS ANALYTIC APPROX. (Bonvini, Caola, SF, Marzani, Melnikov, 2013)



OFF-SHELL HIGGS PRODUCTION

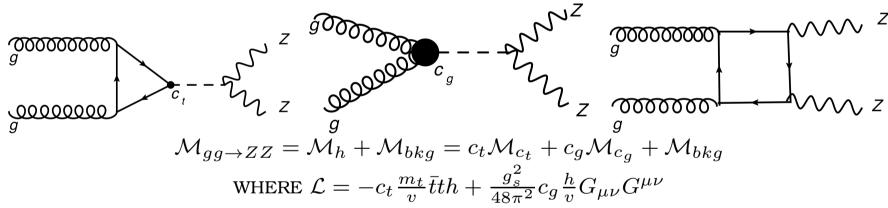
SIMPLE OBSERVATION (Caola, Melnikov, 2013):

$$\sigma_{\mathrm{on-shell}}(gg \to H \to e^- e^+ \mu^- \mu^+) \sim \frac{g_i^2 g_f^2}{\Gamma} \text{ BUT } \sigma_{\mathrm{off-shell}}(gg \to H \to e^- e^+ \mu^- \mu^+) \sim g_i^2 g_f^2$$

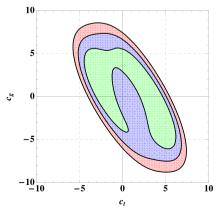
- OFF-SHELL/ON-SHELL RATIO ⇒ WIDTH DETERMINATION (CMS, ATLAS)
- OFF-SHELL MEASUREMENTS ⇒ COUPLINGS INDEPENDENT OF WIDTH

CAN PLAY THE SAME GAME WITH VBF HIGGS PRODUCTION $\Rightarrow \kappa_V$ COUPLINGS FROM $qq \to WWqq$ (Campbell, K.Ellis, 2015)

SETTING LIMITS ON COUPLINGS

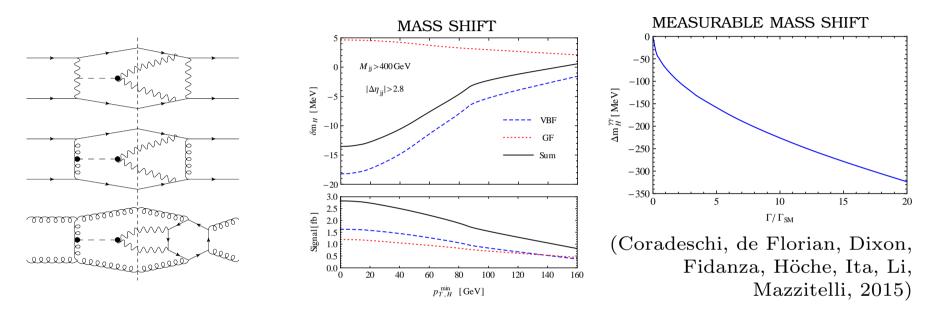


- ON-SHELL CAN INTEGRATE OUT TOP, $\sigma \sim |c_t + c_q|^2$
- OFF-SHELL, CAN MEASURE c_t , c_g INDEPENDENTLY; IN SM $c_t + c_g = 1$, NO MODEL-INDEP CONSTRAINT YET (Azatov, Grojean, Paul, Salvioni, 2014)



HIGGS WIDTH & INTERFEROMETRY

SIMPLE OBSERVATION: SIGNAL-BACKGROUND INTEFERENCE SHIFTS HIGGS MASS; SHIFT PROPORTIONAL TO WIDTH, CAN BE USED TO CONSTRAIN IT (Dixon, Li, 2013)



- MASS SHIFT IN $pp \to H(\to \gamma \gamma) + 2j + X$ MUCH SMALLER THAN IN INCLUSIVE CHANNEL
- CANCELLATION BETWEEN VBF AND GG CHANNEL (SEPARATION WELL DEFINED DUE TO COLOR AT TREE LEVEL, INTERFERENCE SMALL BEYOND IT)
- CANCELLATION CAN BE ENHANCED WHILE KEEPING SIZABLE SIGNAL BY CHOICES OF CUTS IN p_T , $\Delta \eta_{jj}$
- DEFINE MEASURABLE MASS SHIFT: $\Delta m_H^{\gamma\gamma} \equiv \delta m_H^{\gamma\gamma, \, \text{INCL}} \delta m_H^{\gamma\gamma, \, \text{VBF}}$: SMALL BUT STRONGLY DEP. ON WIDTH, REASONABLE SIGNAL

THE STRONG COUPLING

THE VALUE OF α_s

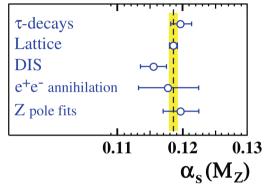
PDG VALUE (AUGUST 2014): $\alpha_s(M_Z) = 0.1185 \pm 0.0006$

- LATTICE UNCERTAINTY CURRENTLY ESTIMATED BY FLAG (arXiv:1310.8555) TO BE TWICE THE PDG VALUE (±0.0012) (IF PDG WERE TO ADOPT THIS, COMBINED UNCERTAINTY LIKELY TO DOUBLE)
- IT IS AN AN AVERAGE OF AVERAGES
- SOME SUB-AVERAGES (E.G. DIS) INCLUDE MUTUALLY INCONSISTENT VALUES
- ullet SOME SUB-AVERAGES (E.G. au OR JETS) INCLUDE DETERMINATIONS WHICH DIFFER FROM EACH OTHER BY EVEN FOUR-FIVE σ
- AVERAGING THE TWO MOST RELIABLE VALUES (GLOBAL EW FIT & τ , BOTH N^3LO , NO DEP. ON HADRON STRUCTURE) GIVES

$$\alpha_s = 0.1196 \pm 0.0010$$

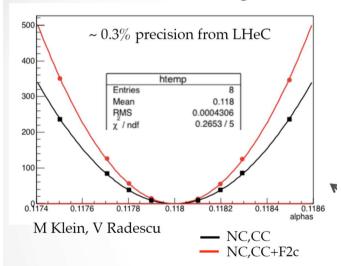
- LITTLE PROGRESS FOR MANY YEARS: PDG 1998-2006 $\Delta \alpha_s(M_Z) = 0.002$; PDG 2010-2014 $\Delta \alpha_s(M_Z) = 0.0006 \div 0.0008$ (CHANGE OF AUTHOR)
- UNLIKELY TO CHANGE SHOULD DETERMINE α_s FROM HIGGS IN GLUON FUSION?





 $lpha_s$ at the LHeC

combined fit to PDFs+αs using LHeC data



• COULD BE DETERMINED ACCURATELY AT THE LHEC OR AT A NEUTRINO FACTORY!

SUMMARY I

THEORETICAL PROGRESS IS KEEPING PACE WITH EXPERIMENTAL PROGRESS:

- PDF DETERMINATION: UNCERTAINTIES
- NNLO AND BEYOND
- THRESHOLD RESUMMATION AS A TOOL FOR APPROXIMATE H.O.
- JET RESUMMATION, CHARACTERIZATION & DEFINITION
- OFF-SHELL

"...the period of the famous triumph of quantum field theory. And what a triumph it was, in the old sense of the word: a glorious victory parade, full of wonderful things brought back from far places to make the spectator gasp with awe and laugh with joy" (Sydney Coleman, 1988)

SUMMARY II:

QCD IS NOT PLUMBING

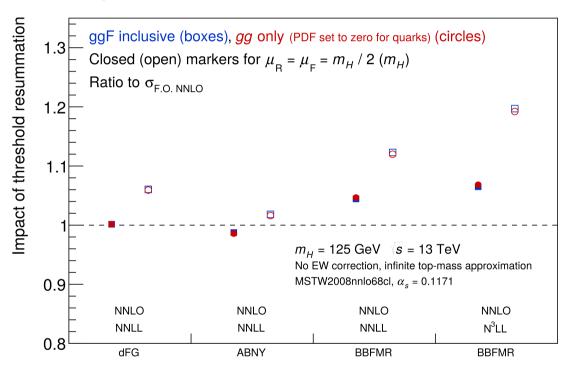


EXTRAS

HIGGS IN GLUON FUSION: RESUMMATION AMBIGUITIES

- LARGE SUBLEADING TERMS ⇒ LARGE AMBIGUITIES
- SCET RESUMMATION SMALLER, DUE TO 1/N TERMS (Bonvini, SF, Ridolfi, Rottoli)
- RESUMMATION EFFECTIVELY AMOUNTS TO APPROXIMATE HIGHER ORDERS

RESUMMED/UNRESUMMED RATIO (NO CONST. EXPONENTIATION)

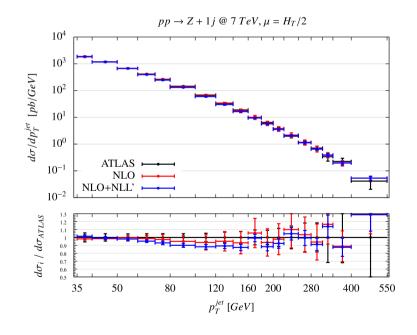


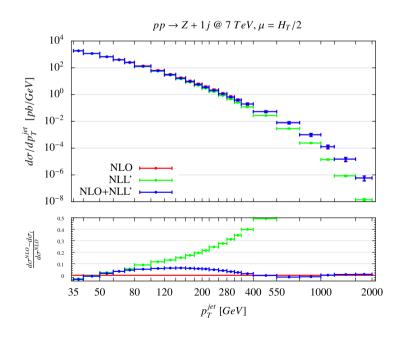
note k factor computed wr to NNLO at respective scale

- ullet De Florian, Grazzini (DFG) (HXSWG REFERENCE) RESUM $\ln N$
- Becher, Neubert et al. (ABNY): SCET (z SPACE) APPROACH TO NNLL (REALLY N^3LL^*)
- Ball et al. (BBFMR): RESUM ln N, DIFFERS FROM DFG BECAUSE OF 'ANALYTIC' RESUMMATION (correct small-N singularities when expanded to finite order)
- BBFMR: N³LL ALSO AVAILABLE

Z+JET PRODUCTION JET VETO RESUMMATION VS. ISOLATION CRITERIA

- JET VETO RESUMMATION RECENTLY EXTENDED TO 0, 1-JET BINS FOR HIGGS PRODUCTION
- GAUGE BOSON+ JET "STANDARD CANDLE"; NNLO CALCULATION RECENTLY AVAILABLE (Boughezal, Focke, Liu, Petriello, 2015)
- ATLAS DATA SURPRISINGLY AGREE WITH NLO RESULT: NO JET VETO?
- "GIANT K-FACTOR" (Rubin, Salam, Sapeta, 2010): ATLAS ISOLATION CRITERION ACCEPTS TWO-JET EVENTS WITH ONE JET ALMOST COLLINEAR TO Z, COMPENSATES SUPPRESSION DUE TO JET VETO
- GOES AWAY WITH DIFFERENT JET ISOLATION CRITERION



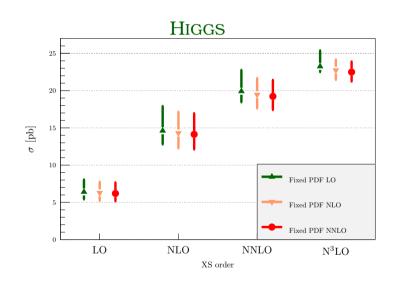


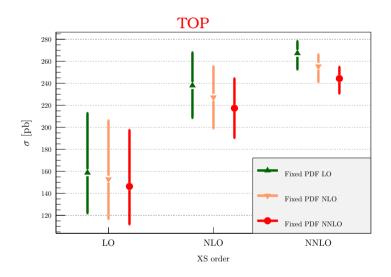
(Boughezal, Focke, Liu, 2015)

N³LO PDFs:

- NEEDED AT THE 1% ACCURACY LEVEL
- IMPACT OF N^3 LO DEPENDS ON PROCESS:
 - Higgs gluon fusion: perturbative dep. of PDF negligible in comparison to matrix element \Rightarrow N^3LO not needed
 - TOP: PERTURBATIVE DEP. OF PDF SMALLER, BUT NOT NEGLIGIBLE IN COMPARISON TO MATRIX ELEMENT, ANTICORRELATED TO IT $\Rightarrow N^3LO$ NECESSARY

SCALE UNCERTAINTY & DEP. ON PERTURBATIVE ORDER





(s.f., Isgrò, Vita, 2014)

WHEN WILL WE HAVE THEM?

- N³LO DIS COEFFICIENT FUNCTIONS KNOWN
- BOTTLENECK: N^3 LO ANOMALOUS DIMENSIONS
- ANOMALOUS DIMENSIONS: LO: 1974; NLO: 1981; NNLO: 2004; N³LO: 2030?

HIGGS IN GLUON FUSION: EXACT N³LO!

 $XH = VBF + VH + t\bar{t}H + b\bar{b}H$

Tot. uncert. (scale, N³LO approx. ⊕ PDF+α_s)

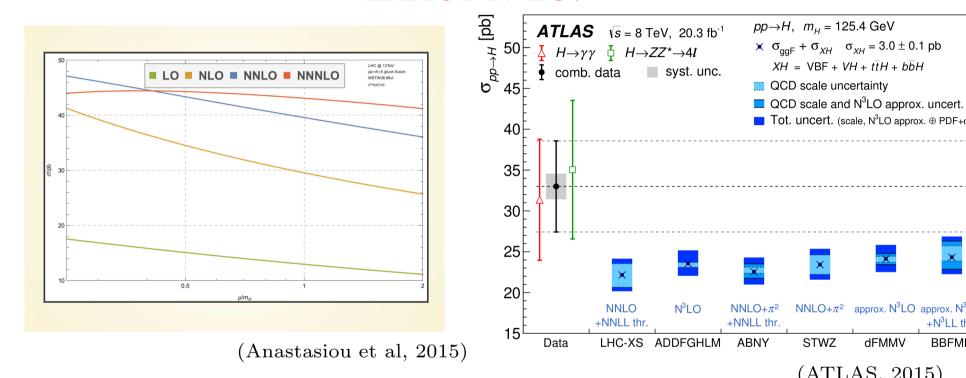
NNLO+ π^2 approx. N³LO approx. N³LO

(ATLAS, 2015)

STWZ

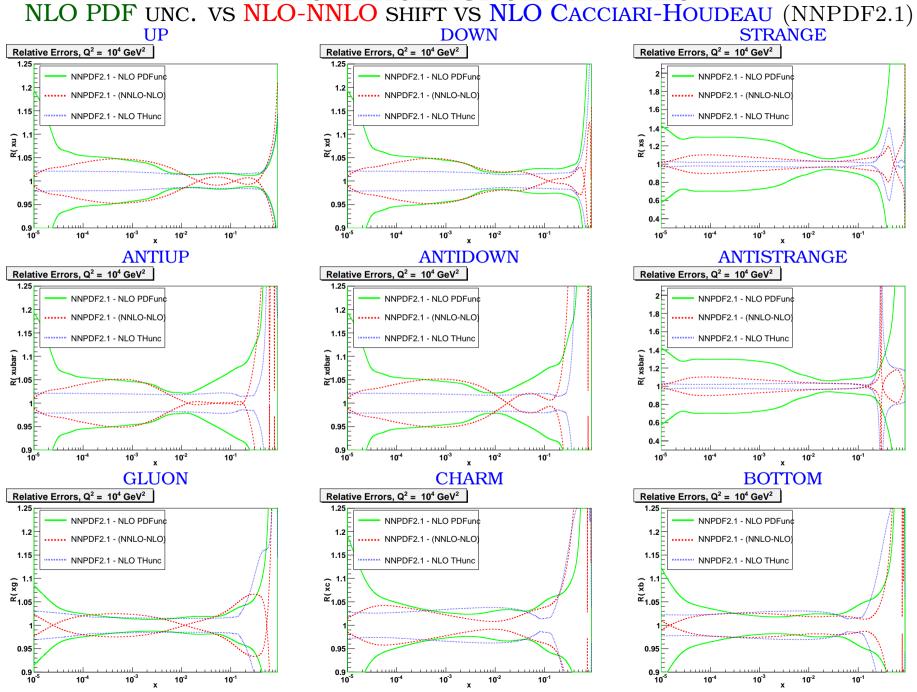
+N³LL thr.

BBFMR



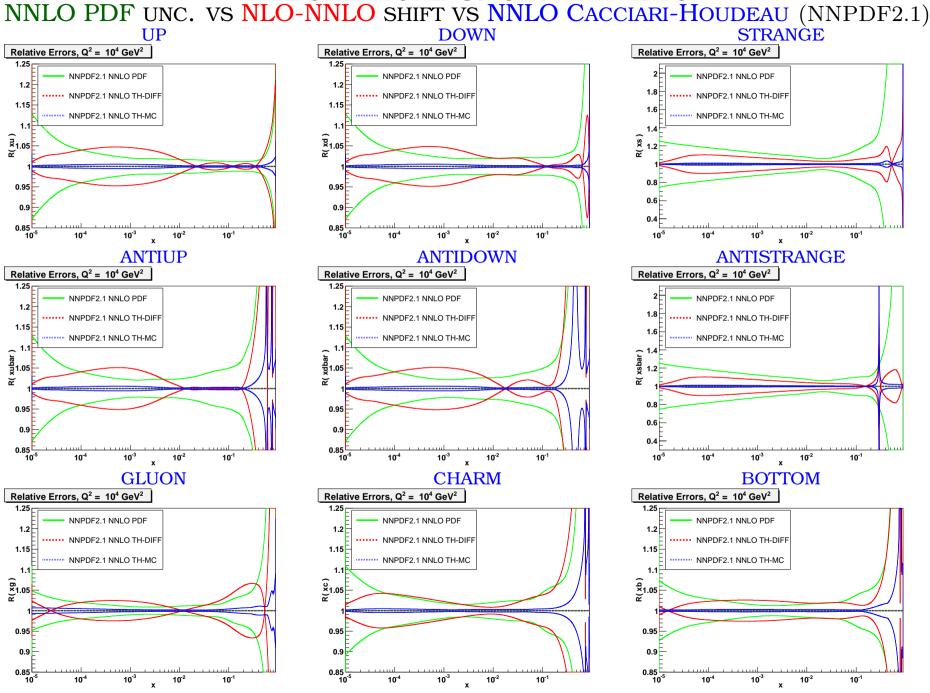
- \bullet Exact N^3LO published in preliminary form, obtained as series expansion about the soft limit, in pointlike approx
- HAS THE SERIES CONVERGED?
- IN GOOD AGREEMENT WIH RESUMMATION!

THEORETICAL UNCERTAINTIES



THEORETICAL UNCERTAINTY ON NLO PDF IS ORDER 5% \Rightarrow COMPARABLE TO PDF UNCERTAINTY

THEORETICAL UNCERTAINTIES



THEORETICAL UNCERTAINTY ON NNLO PDF IS ORDER $1\% \Rightarrow$ SMALLER THAN PDF UNCERTAINTY