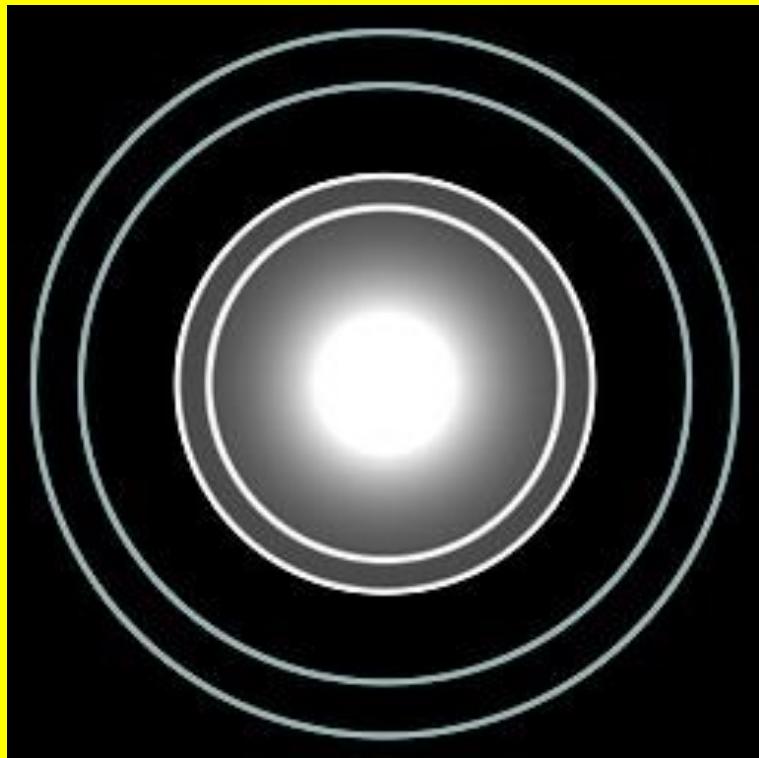


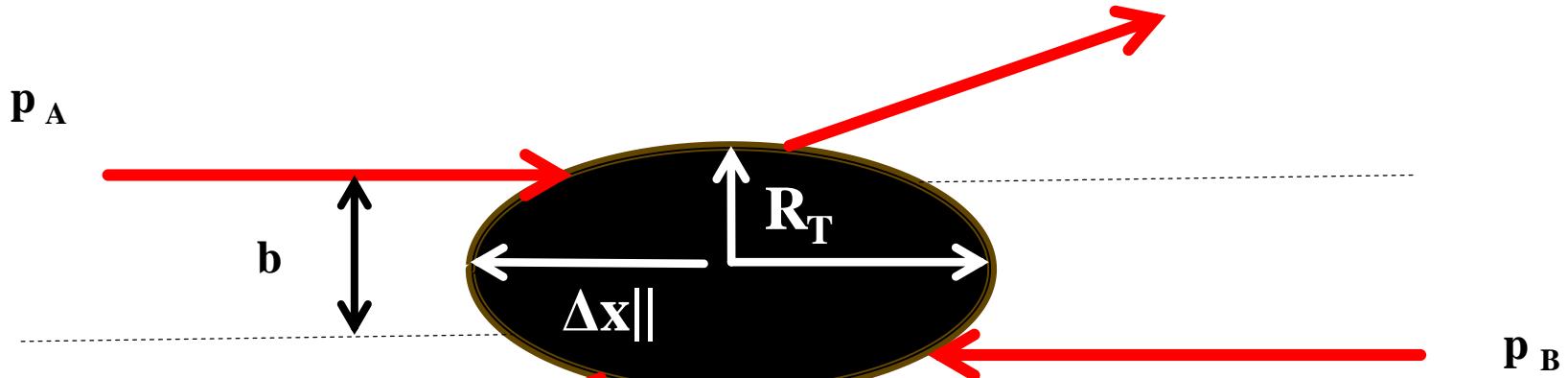
Diffractive Studies at the LHC: What Can We Learn (If Any)?



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Characteristic Scales



Heisenberg:

$$|p_{A,B}| = \sqrt{s}/2$$

$$\langle b^2 \rangle^{1/2} = R_T = \langle \Delta x_{\perp} \rangle > 1/\sqrt{\langle -t \rangle} \approx 1 \text{ fm}$$

$$\langle \Delta x_{||} \rangle > \sqrt{s} / (2 \sqrt{\langle t^2 \rangle - \langle t \rangle^2}) \approx 10^4 \text{ fm at LHC}$$

$$(\Delta x)^2 \equiv \langle x^2 \rangle - \langle x \rangle^2$$

$$r_{\text{Compton}}(\text{Higgs}) = 1.6 \cdot 10^{-3} \text{ fm}$$

Elementary Geometry of Collision

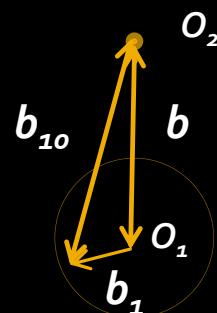
High Energies

Pointlike
particle

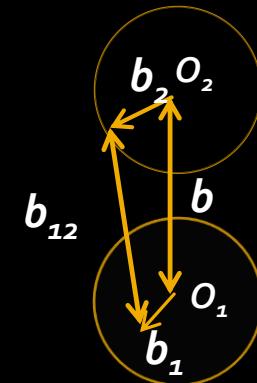


Pointlike
particle

Pointlike
particle



Extended
particle



$$\langle \mathbf{b}_1 \mathbf{b}_2 \rangle = \langle \mathbf{b}_1 \mathbf{b}_{12} \rangle = \langle \mathbf{b}_2 \mathbf{b}_{12} \rangle = 0$$

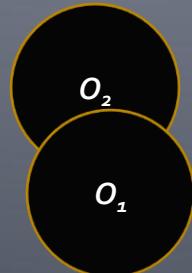
$$\mathbf{b} = \mathbf{b}$$

$$\mathbf{b} = \mathbf{b}_1 + \mathbf{b}_{01}$$

$$\mathbf{b} = \mathbf{b}_1 - \mathbf{b}_2 + \mathbf{b}_{12}$$

$$\langle \mathbf{b}^2 \rangle = \langle \mathbf{b}_1^2 \rangle + \langle \mathbf{b}_2^2 \rangle + \langle \mathbf{b}_{12}^2 \rangle \geq \langle \mathbf{b}_1^2 \rangle + \langle \mathbf{b}_2^2 \rangle$$

Low Energies



$$\begin{aligned}\langle \mathbf{b}_1 \mathbf{b}_2 \rangle &\neq 0 \\ \langle \mathbf{b}_1 \mathbf{b}_{12} \rangle &\neq 0 \\ \langle \mathbf{b}_2 \mathbf{b}_{12} \rangle &\neq 0\end{aligned}$$

Uneasy Separation

$\langle b^2 \rangle, \text{ fm}^2$

$$B(s) = d[\ln(d\sigma/dt)]/dt \ (t=0) = \frac{1}{2}\langle b^2 \rangle$$

0.8

$$\langle b^2 \rangle \approx 2 \langle b^2 \rangle_p$$

$$\langle b^2 \rangle_p \approx (0.68 \text{ fm})^2$$

$$\begin{aligned}\langle b^2 \rangle &\approx (1.26 \text{ fm})^2 \\ &= 2 \langle b^2 \rangle_p + (0.81 \text{ fm})^2\end{aligned}$$

NB: Internucleon distances in nuclei: 1.2 – 2.0 fm

1

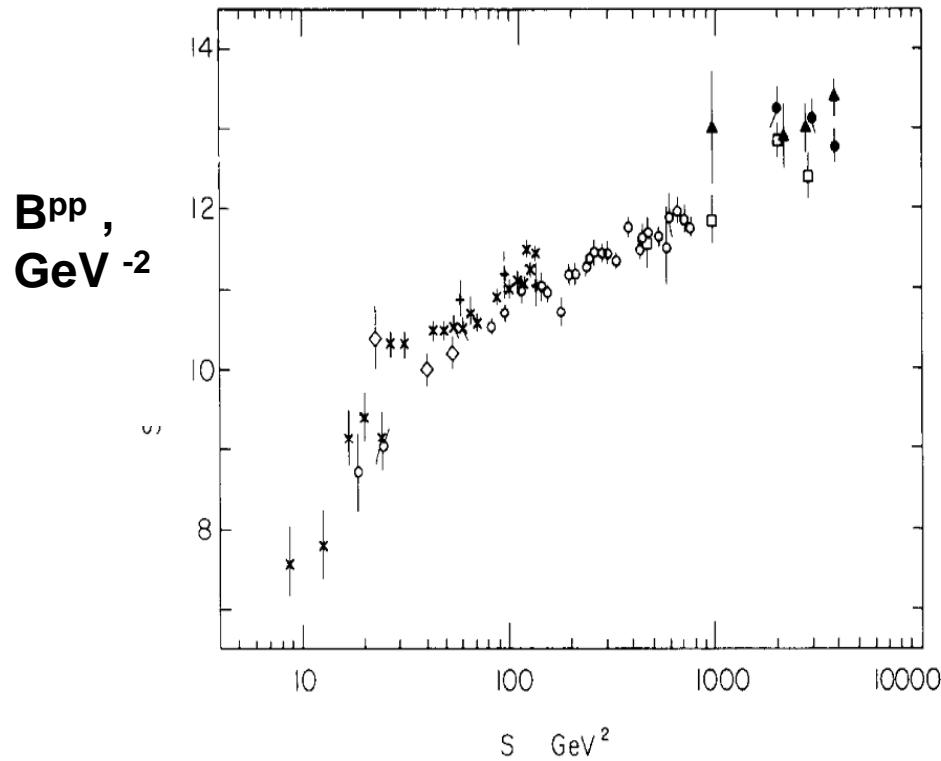
10

10^2

10^3

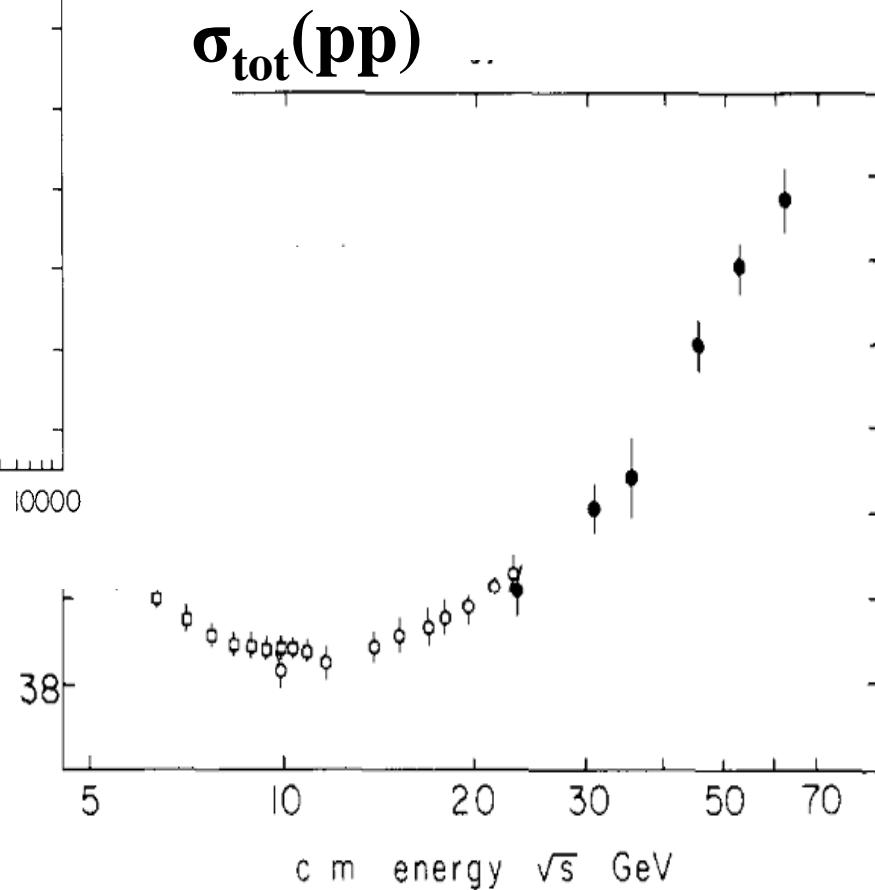
$\sqrt{s} (GeV)$

Two phenomena to be related

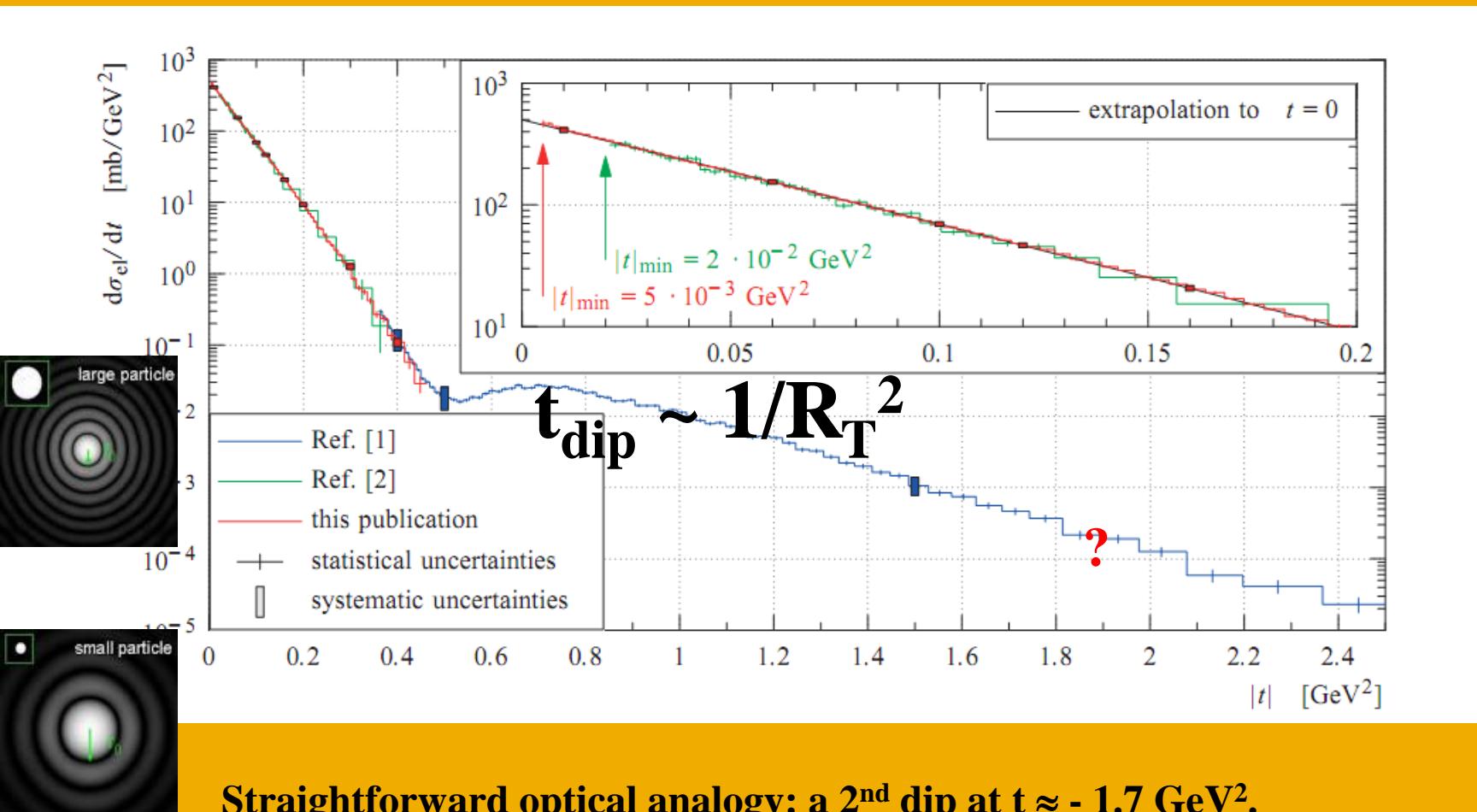


Change of the growth
rate at $\approx 7 \div 15 \text{ GeV}^2$

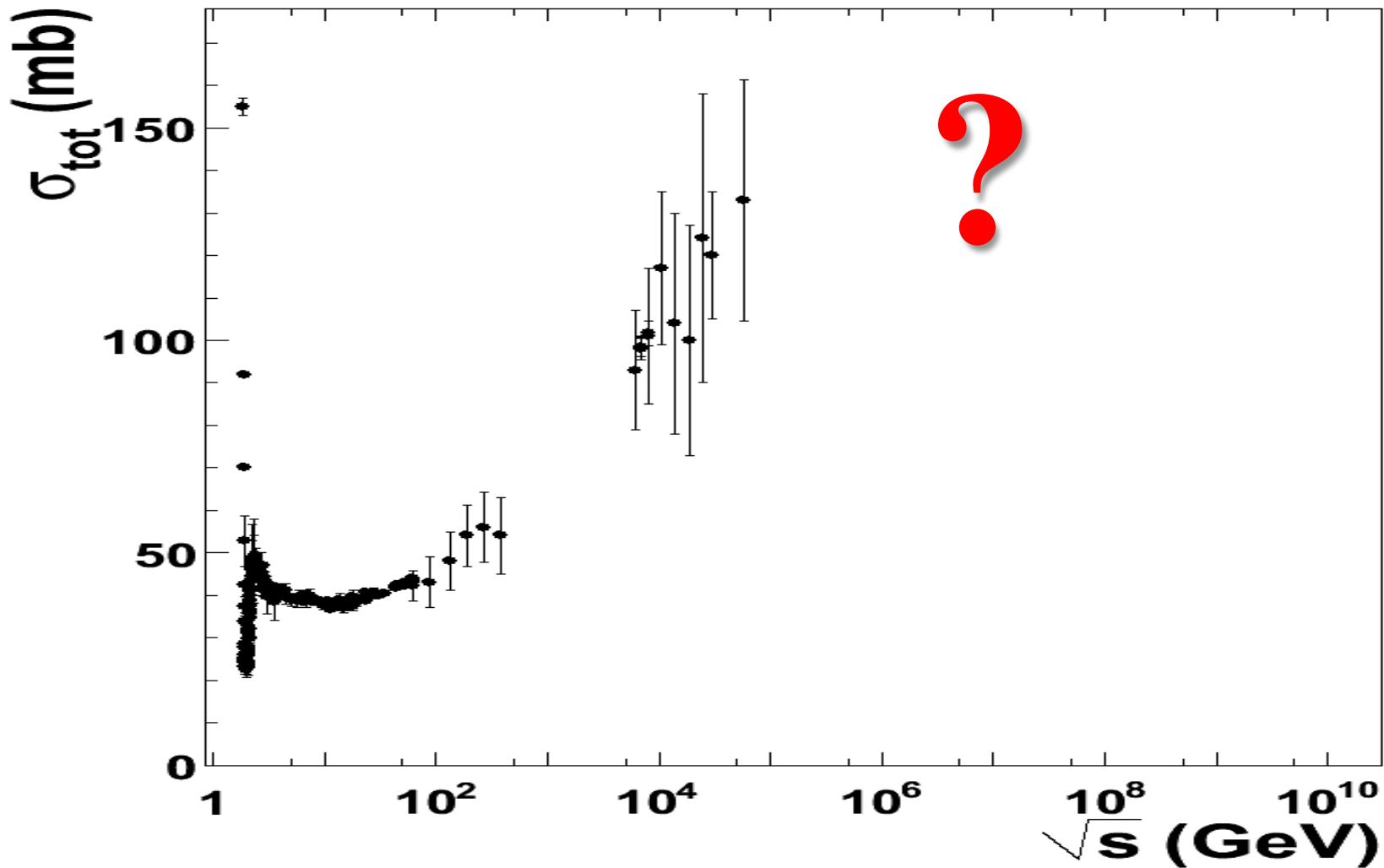
Stop of the decrease at $\approx 7 \div 15 \text{ GeV}$



Diffraction Pattern at the LHC



Past, present



Where Lies the “Asymptopia”?



Sizes of nucleons

$$\langle \mathbf{r}^2 \rangle_{\text{ch}} = \sum_i e_i \langle \mathbf{r}^2 \rangle_i$$

Physical nucleon radius

$$\langle \mathbf{r}^2 \rangle(\text{nucleon}) = \max_i \langle \mathbf{r}^2 \rangle_i = 0.711 \text{ fm}^2$$

$$\langle \mathbf{b}^2 \rangle(\text{nucleon}) = (2/3) \langle \mathbf{r}^2 \rangle(\text{nucleon}) = 0.474 \text{ fm}^2 = 11.85 \text{ GeV}^{-2}$$

$B = B_{\text{cr}} = 11\text{-}12 \text{ GeV}^2$ at the “knee”

$$\langle \mathbf{b}^2 \rangle(7 \text{ TeV}) = 40 \text{ GeV}^{-2} = 2 \langle \mathbf{b}^2 \rangle(\text{nucleon}) + 16.3 \text{ GeV}^{-2}$$

Asymptopia: $\langle b^2 \rangle \gg 2 \langle b^2 \rangle(\text{nucleon})$

$\langle \mathbf{b}^2 \rangle = 5 \langle \mathbf{b}^2 \rangle(\text{nucleon})$ ($B = 27\text{-}30 \text{ GeV}^{-2}$)
at $O(>100 \text{ TeV})$?

Asymptotic theory:

Asymptotic expectations (“ $s \rightarrow \infty$ ”):

$$\begin{aligned}\sigma_{\text{tot}} &\approx 8\pi\alpha'_P(0)(\alpha_P(0) - 1)\ln^2(s) + \dots \\ &\approx 8\pi B(s)\end{aligned}$$

“Popular values”: $\alpha_P(0) = 0.08,$

$$\alpha'_P(0) = 0.25 \text{ GeV}^{-2}$$

$$\infty = ? \text{ 7 TeV} \rightarrow \sigma_{\text{tot}} \approx 43 \text{ mb}, B(s) \approx 4.3 \text{ GeV}^{-2}$$

LHC: $\sigma_{\text{tot}} \approx 100 \text{ mb}, B \approx 20 \text{ GeV}^{-2}$

$$\sigma_{\text{tot}} \ll 8\pi B$$

“Theory”

$$T(s,t) = \beta(t)s^{\alpha(t)}$$

$$\text{QCD: } \alpha(t) = A(t/\Lambda_{QCD}^2),$$

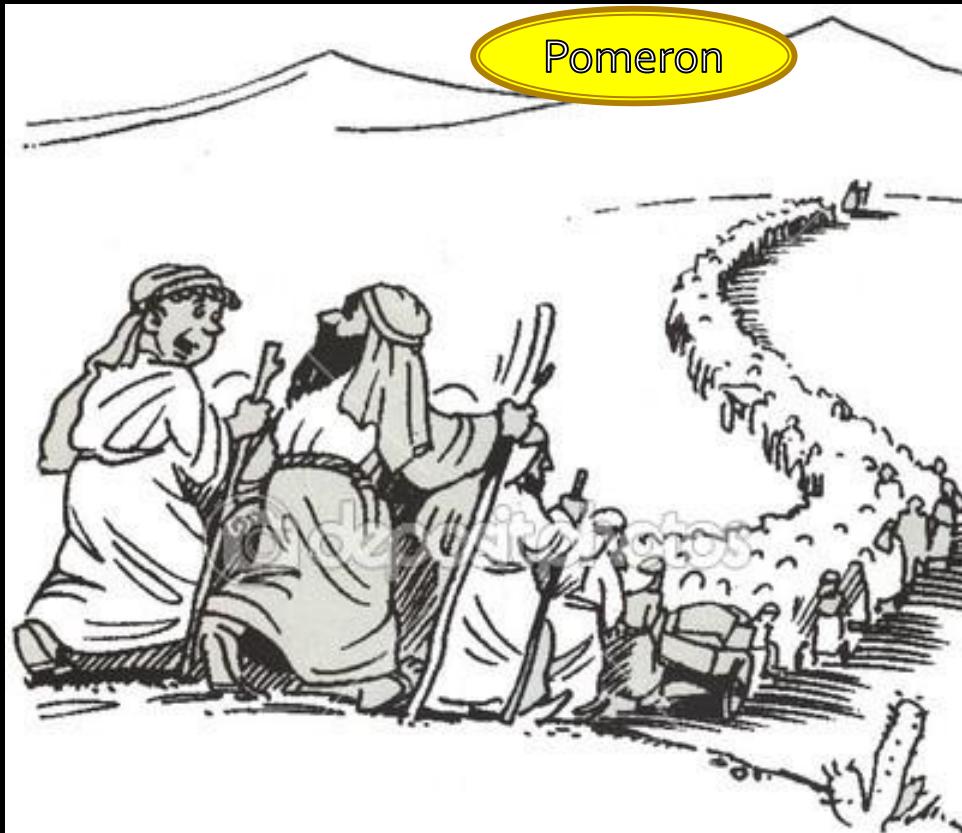
$$\Lambda_{QCD}^2 = \mu^2 \exp\left(-1/\beta_0 g^2\right). \quad \alpha(0) = A(0).$$

40 years of a hard work

$$\alpha(t) \rightarrow \alpha_k(t) > 1, k = 1, 2, \dots, \infty$$

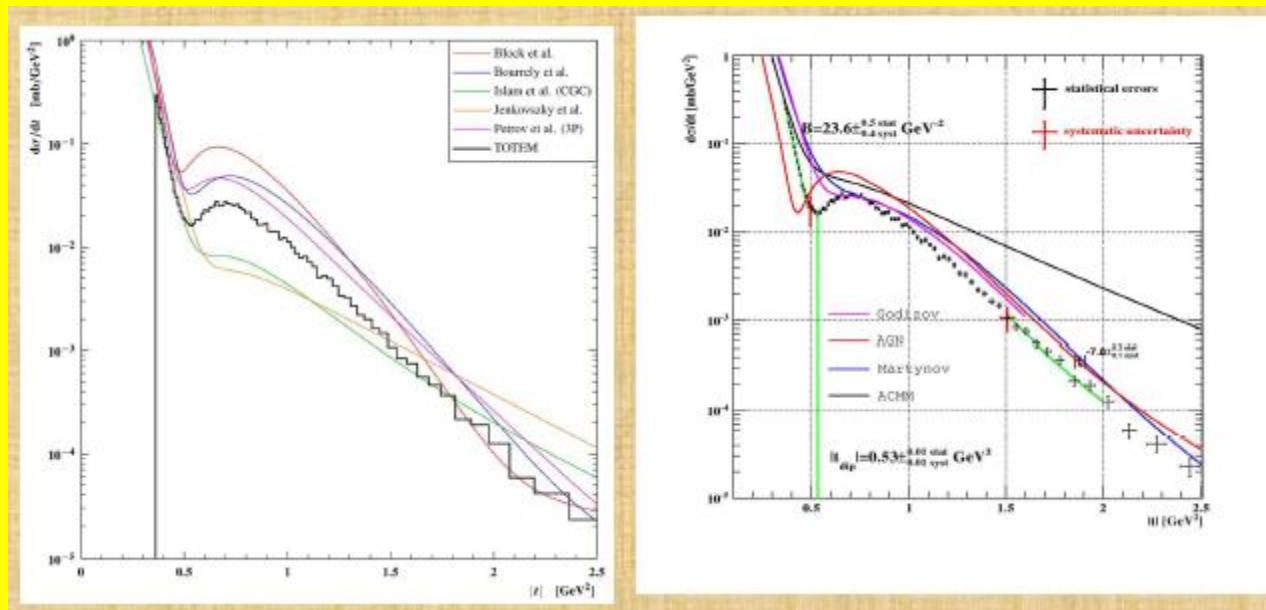
$$\alpha_k^{\mathbb{P}}(t) \rightarrow 1, -t \rightarrow \infty; \quad \alpha(0)_{\infty}^{\mathbb{P}} = 1$$

A la recherche du Pomeron perdu



“If I had known we would be
in the desert for 40 years
I would have better chosen cosmology...

LHC against models



General Failure...

QCD against the Diffraction Data



Damned Questions

- ♣ Why do cross-sections rise?
- ♣ Where are other dips?
- ♣ Where the Asymptopia lies?
- ♣ Etc, etc...

Conclusions

(1st movement. Lamentation)

- 1. All the models gave wrong predictions for the diffractive picture at the LHC (7 TeV)
- 2. Some models gave good predictions for “global” characteristics (σ_{tot} , σ_{el} , B , t_{DIP})
- No consequences for QCD ! No commonly significant consequences at all.

Outlook:

- Stop arbitrary modelling!
- Go deep into QCD at large distances!

Conclusions *(2nd Movement. Consolation)*

At the LHC we seem to be still far from
the “truly asymptotic” region **but**

**“There is still plenty of good
music to be written
in C major.”**

Arnold Schönberg