

# $\alpha_s$ from $e^+e^-$ event shapes

Stefan Kluth

MPI für Physik

FCC-ee workshop on high precision

$\alpha_s$  measurements

12 Oct 2015

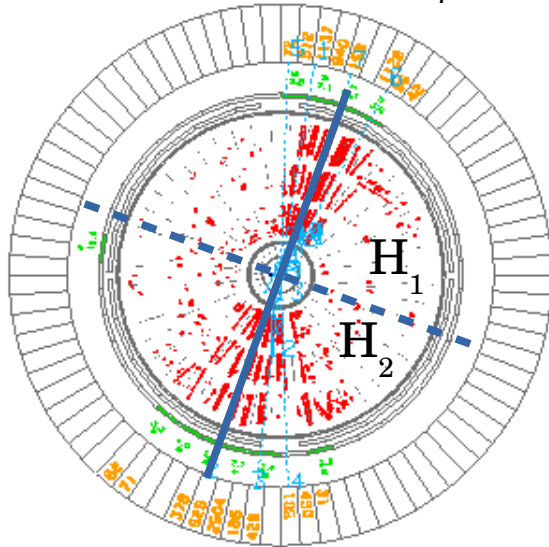
# Overview

- Experimental
  - Experiment
  - Simulation
  - Analysis procedure
- Theory
  - Fixed order and resummation
  - Integration with hadronisation models
  - Other issues
- Summary

# Event Shape Observables

Thrust 1-T:

$$1-T = 1 - \max_{\vec{n}} \frac{\sum_i \vec{p}_i \cdot \vec{n}}{\sum_i |\vec{p}_i|}$$



Heavy Jet Mass  $M_H$ :

larger invariant mass in hemispheres  $H_1$  and  $H_2$  w.r.t. thrust axis  $n$

Jet Broadening  $B_T$  and  $B_W$ :

$$B_{1,2} = \frac{\sum_{i \in H_{1,2}} p_{t,i}}{2 \sum_i |\vec{p}_i|}$$

$$B_T = B_1 + B_2$$

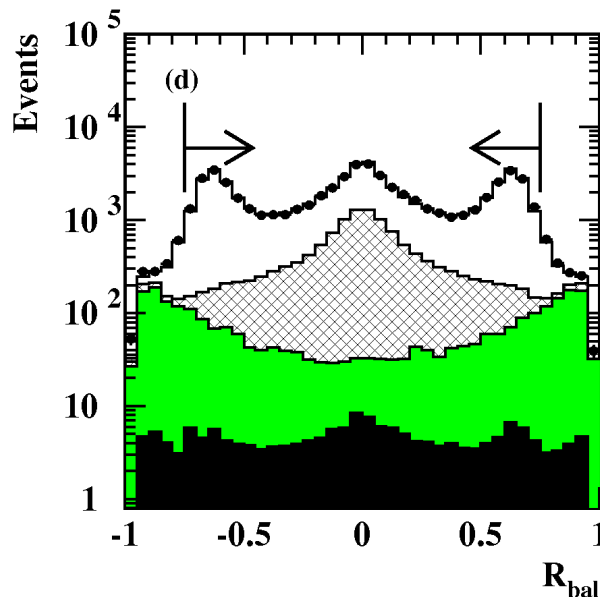
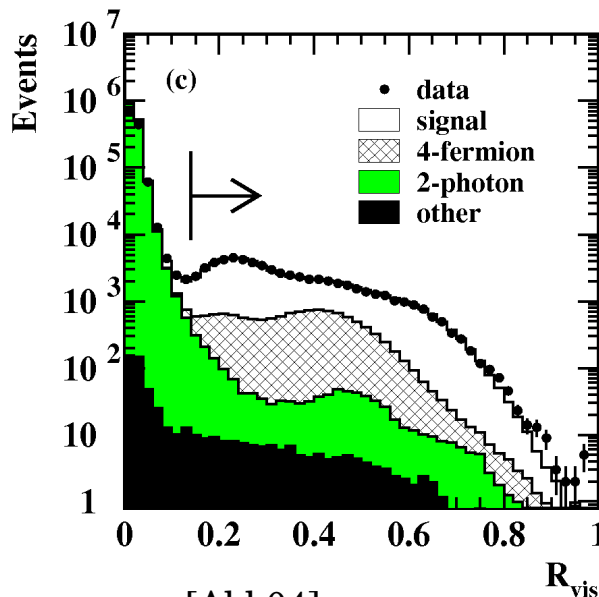
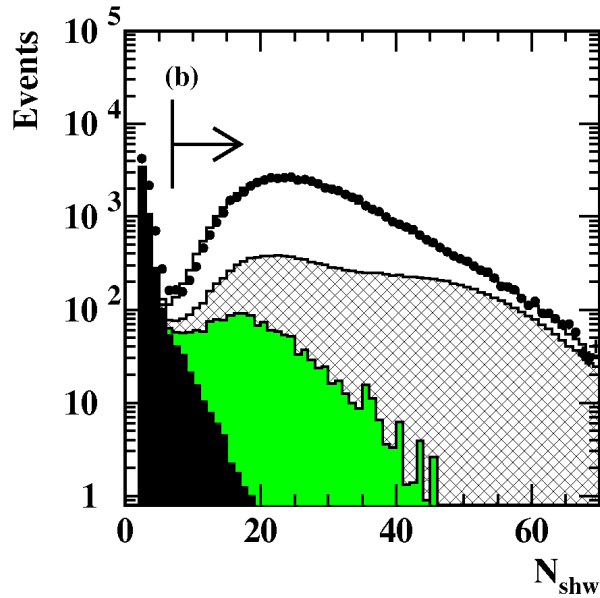
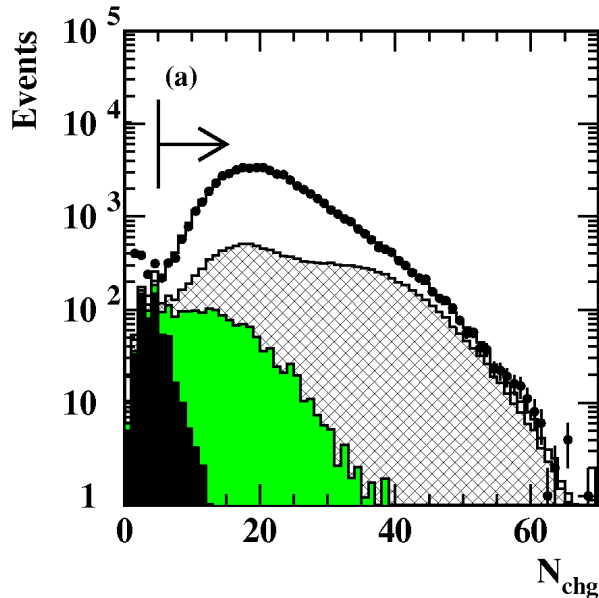
$$B_W = \max(B_1, B_2)$$

C-parameter:

$$C = \frac{3}{2} \frac{\sum_{i,j} |\vec{p}_i| |\vec{p}_j| \sin(\Theta_{ij})}{(\sum_i |\vec{p}_i|)^2}$$

# Event selection

OPAL  $e^+e^- \rightarrow \text{hadrons}$  189-209 GeV



Hadronic events:

a) charged particle multiplicity  $N_{\text{chg}}$

b) calorimeter multiplicity  $N_{\text{shw}}$

c)  $R_{\text{vis}} = \sum E_{\text{clus}} / Q$

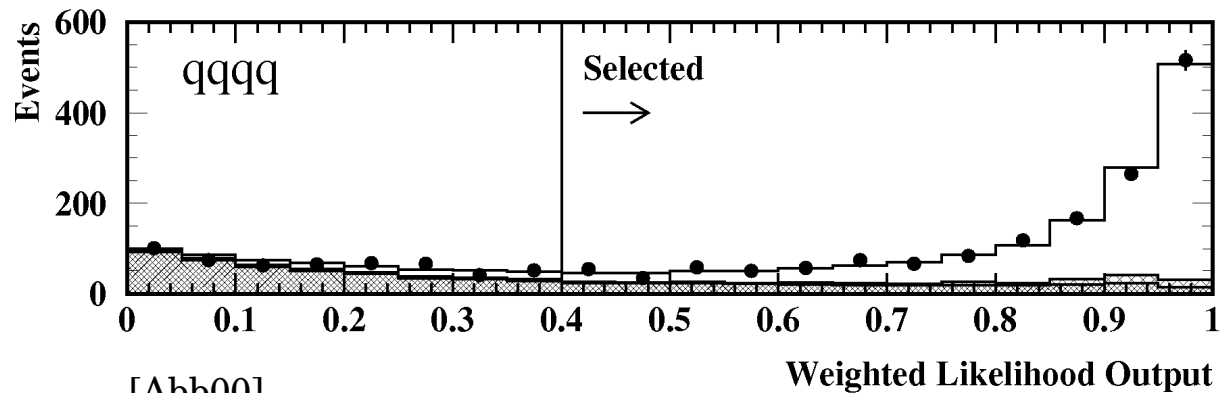
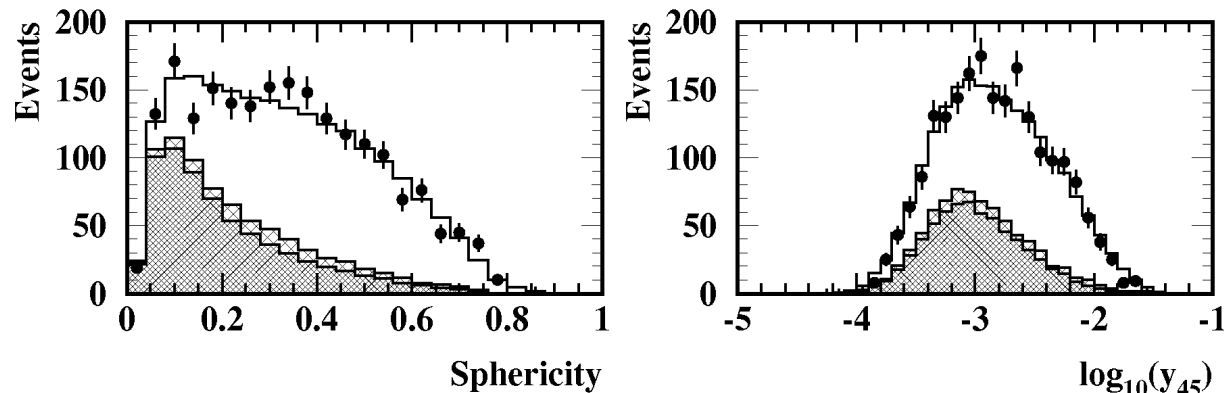
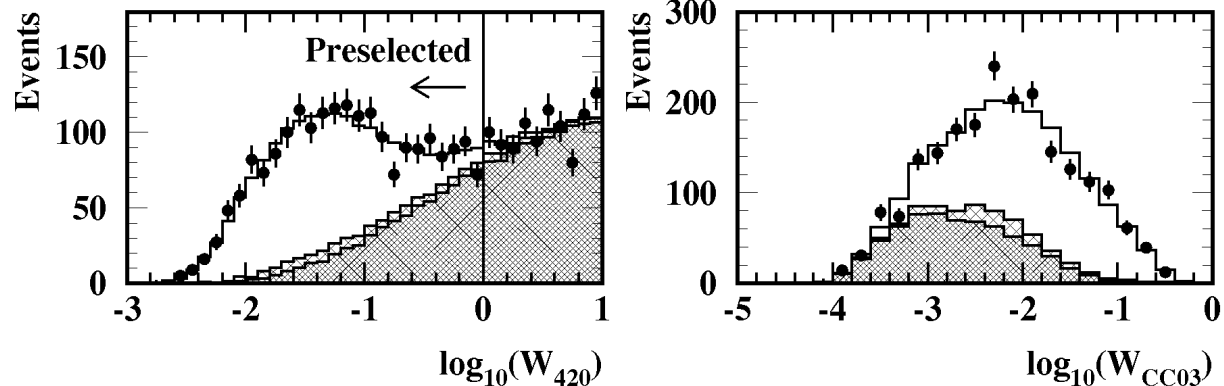
d)  $R_{\text{bal}} = \sum E_{\text{clus}} \cos \theta_{\text{clus}} / \sum E_{\text{clus}}$

Similar at LEP 1 ( $m_Z$ )

[Abb04]

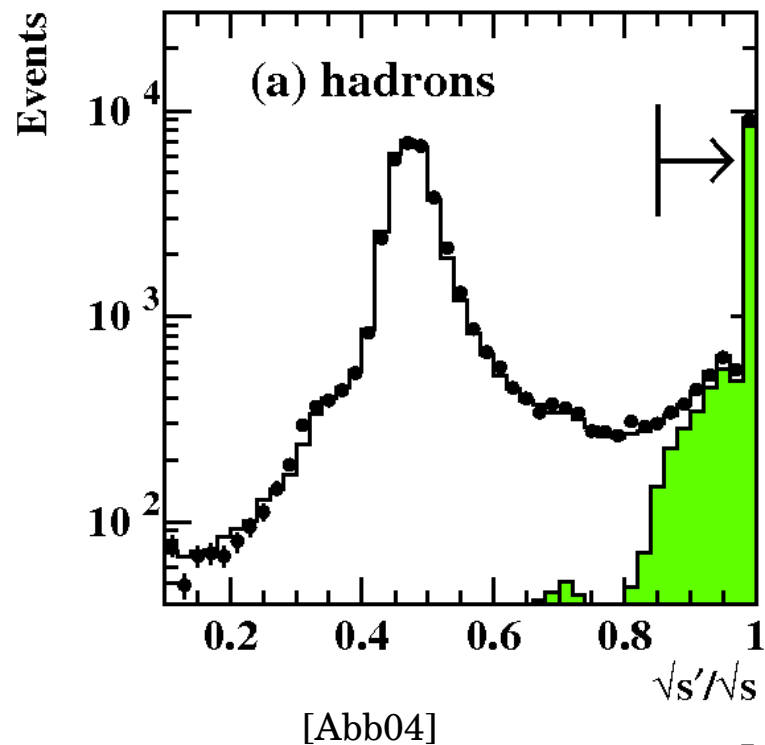
# Event selection

OPAL  $\sqrt{s}=189$  GeV



At high energies reject  $e^+e^- \rightarrow W^+W^- \rightarrow \text{hadrons}$   
 $\rightarrow$  cut on “4-jet” observables

Radiative return  $\rightarrow$  find effective cm energy  $s'$

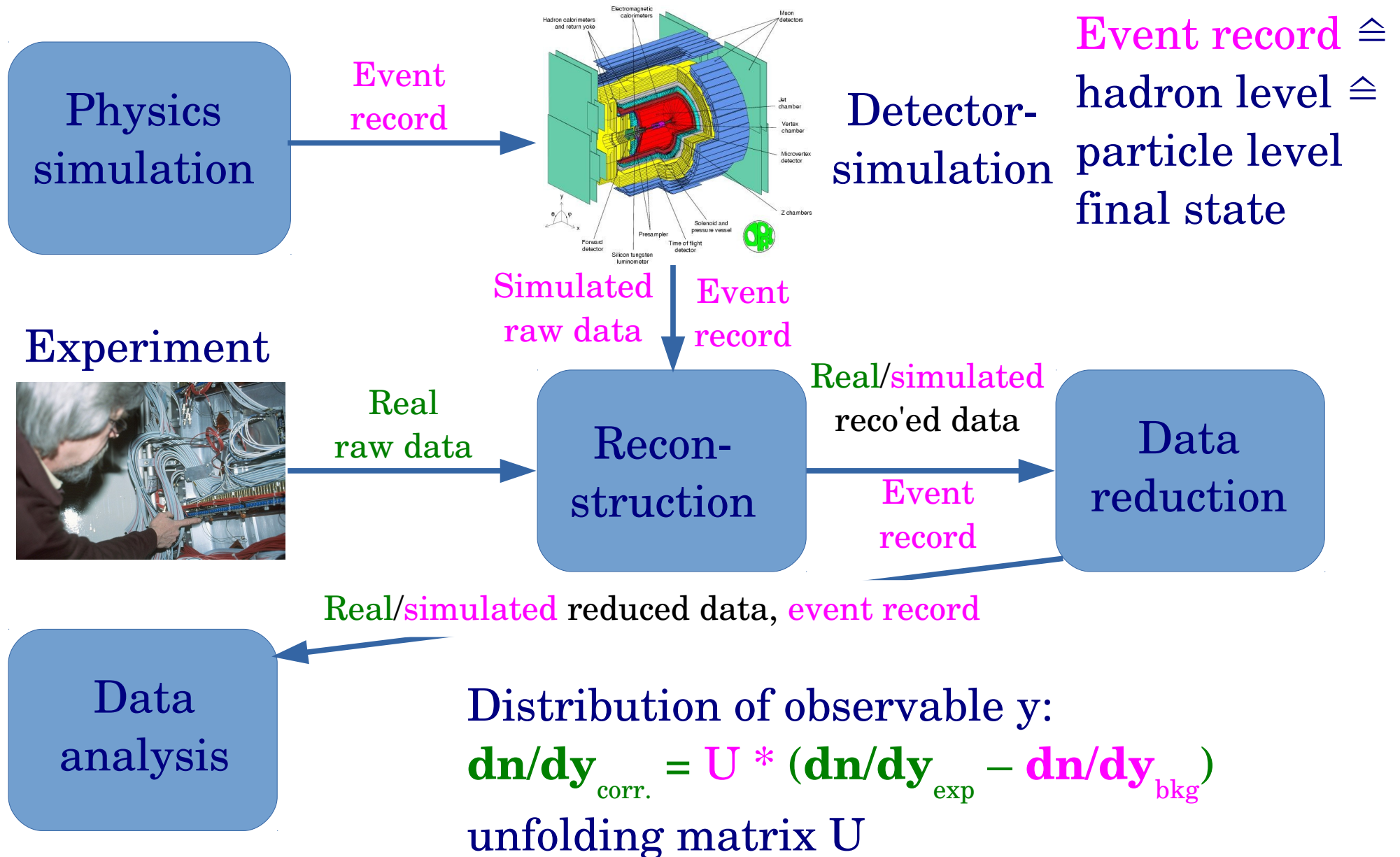


[Abb00]

[Abb04]

event shapes

# Experimental procedure



# Experimental problems

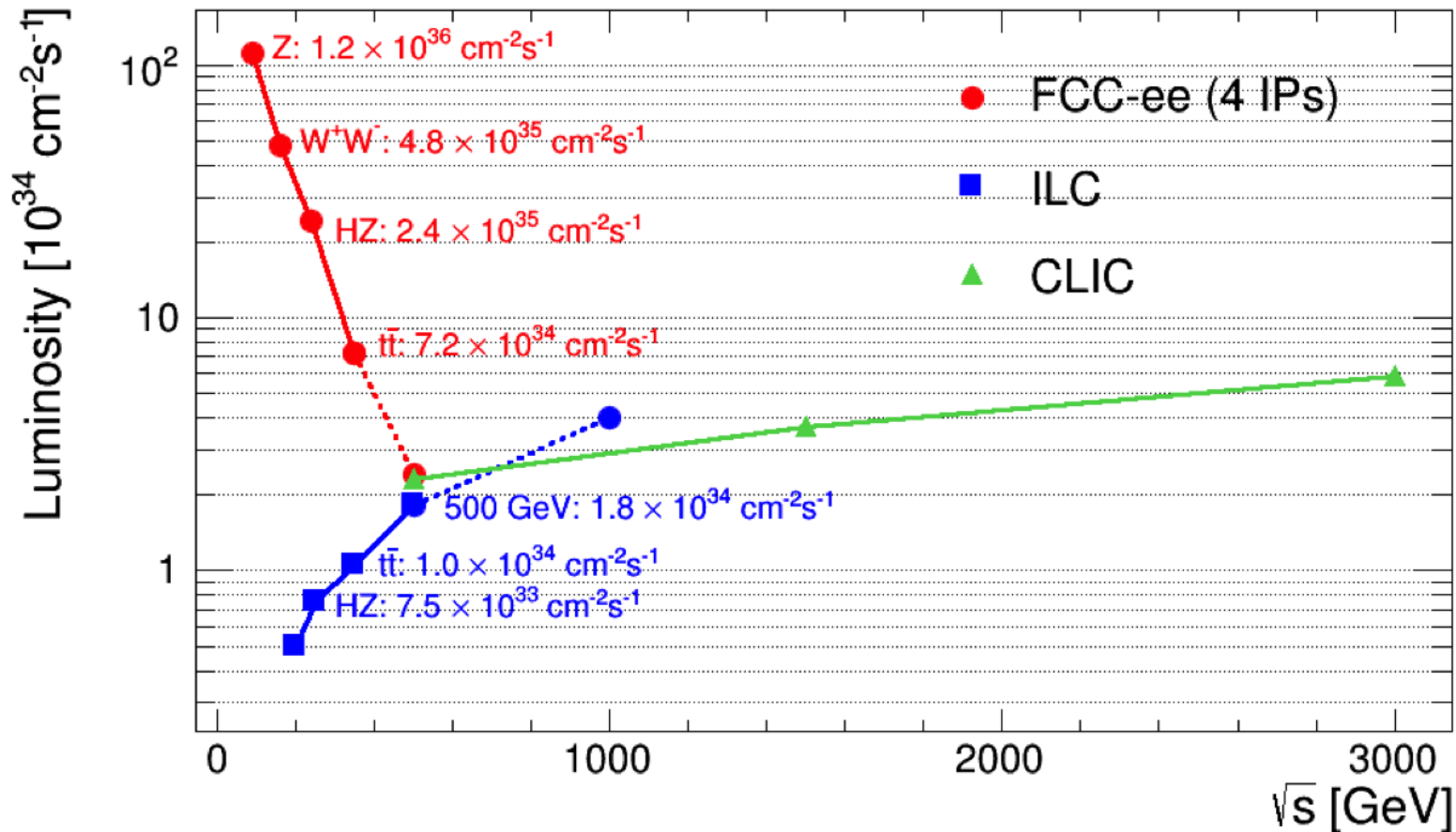
- Quality of detector model
  - unfolding incl. phase space extrapolation
  - improved resolution will help
- Physics model dependence of unfolding
  - “Pythia vs Herwig” unfolding, data driven tests
  - depends also on MC tuning quality
- Background subtraction
  - Improved resolution will help against W-pairs
- Background modelling
  - MC based subtraction or data driven procedure?

# Massive (b) quarks

- Massive QCD
  - NLO “only”, NNLO possible?
  - Resummation basically missing, possible?
  - Irreducible theory systematics
- Need to treat experimentally
  - b-(anti-)tagging  $\Rightarrow$  b vs udsc separated samples
    - LEP experiments have done / could do this
  - Will add (small) experimental systematics
    - Si vertex detector resolution
    - Precision detector simulation



# (Low) Energy points?



[arXiv:1412.2928,  
ICHEP 2014]

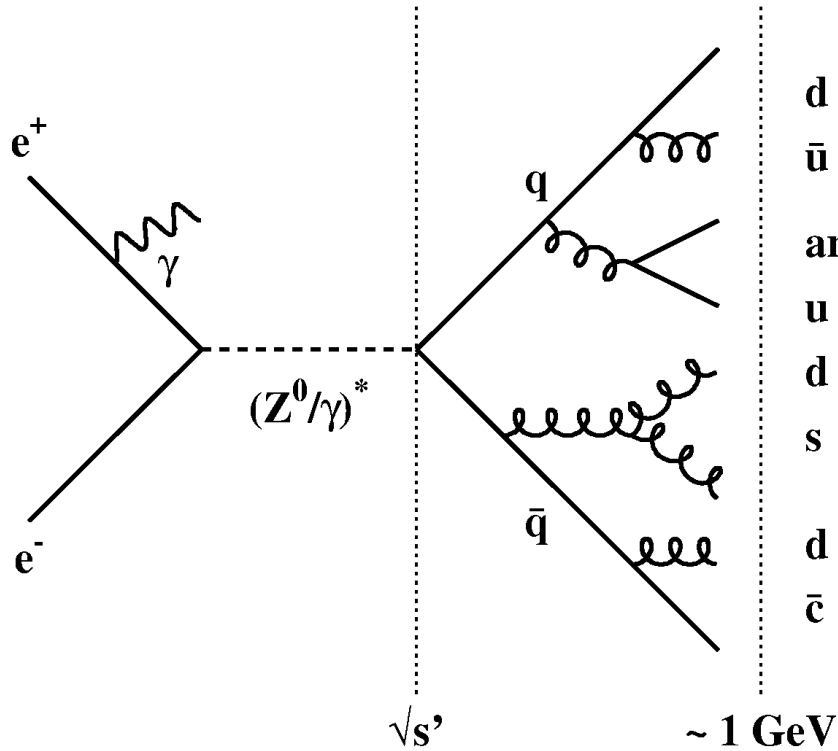
A few days of data taking at  $\sqrt{s} < m_Z$  reproduces PETRA / JADE with flavour tagging and improved resolution added  
Global fits / PC analyses dependent on low energy data to disentangle soft and hard QCD effects

# Using the predictions

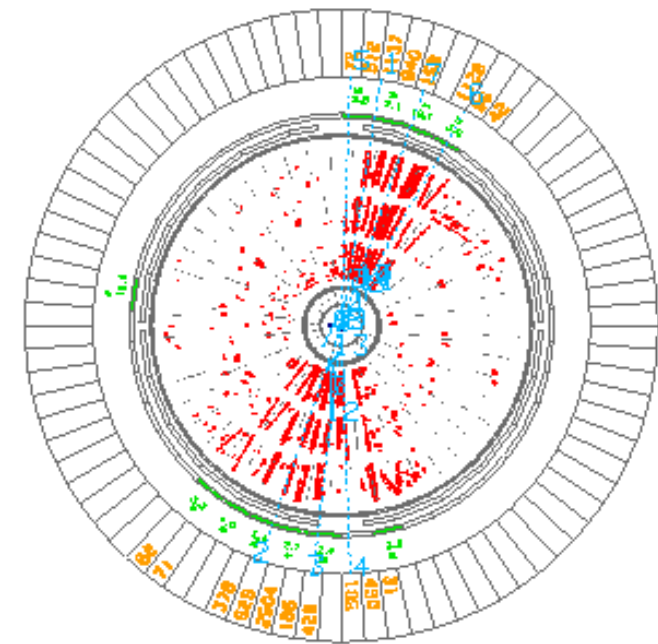
Electro-weak Production

Parton Shower

Hadronisation



$d$   
 $\bar{u}$  }  $\pi^-$   
 and many more  
 $u$   
 $d$  }  $\Lambda^0 \rightarrow \pi^- p^+$   
 $s$   
 $d$   
 $\bar{c}$  }  $D^+ \rightarrow K^0 \pi^+$



*Parton Level*

*Hadron Level*

*Detector Level*

[Kluth, Rept.Prog.Phys.69(2006)1771]

Perturbative process

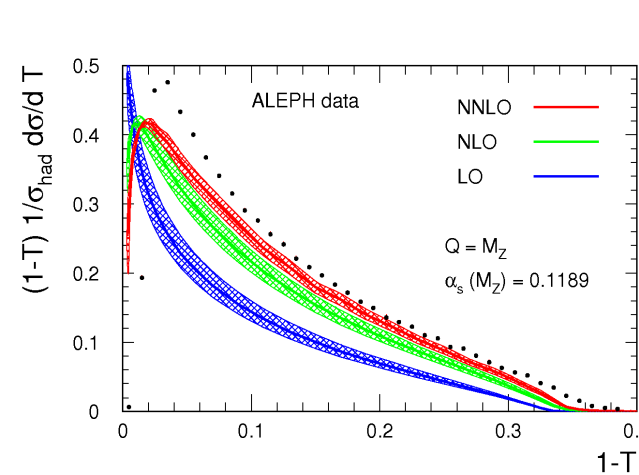


Hadronisation effects

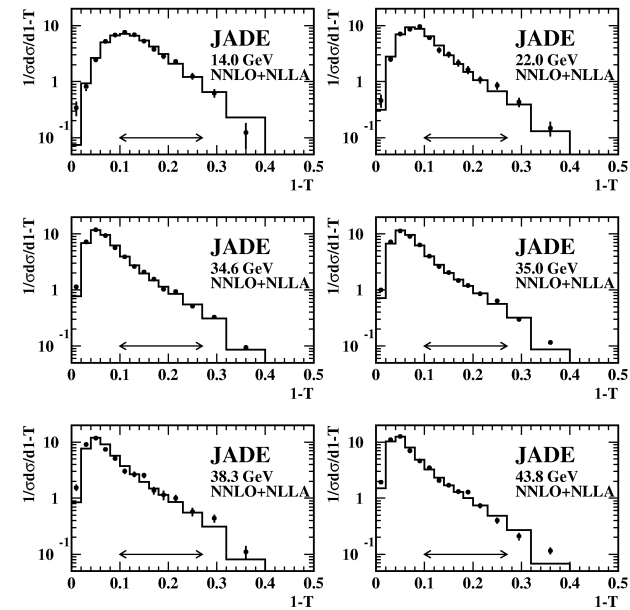
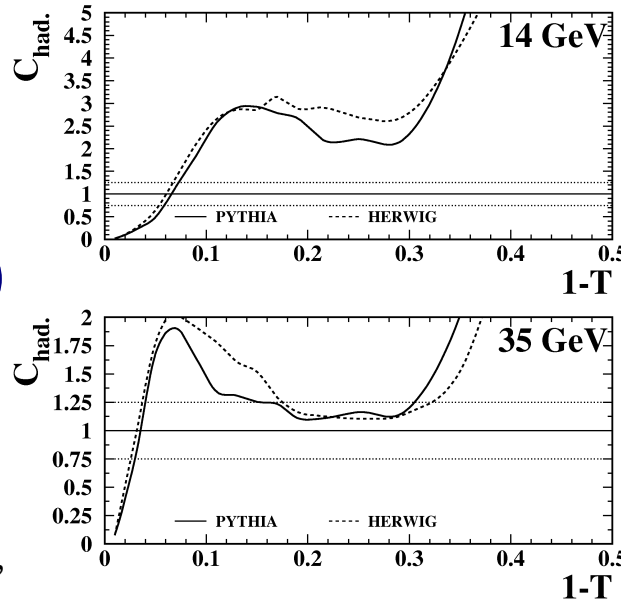


Experimental effects

# pQCD plus MC had. Corr.



[Gehrmann, Gehrmann-deRidder, Glover, Heinrich, JHEP12(2007)094]



[JADE, Eur.Phys.J.C64(2009)351]

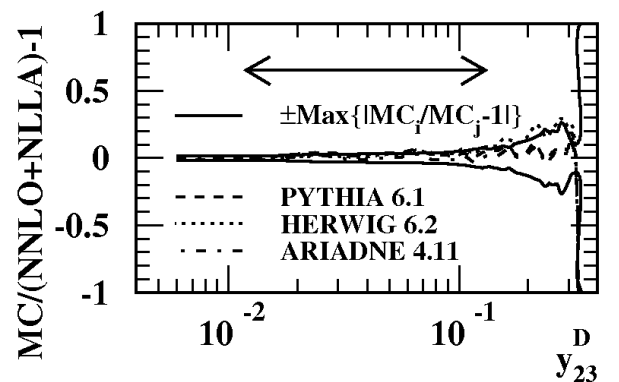
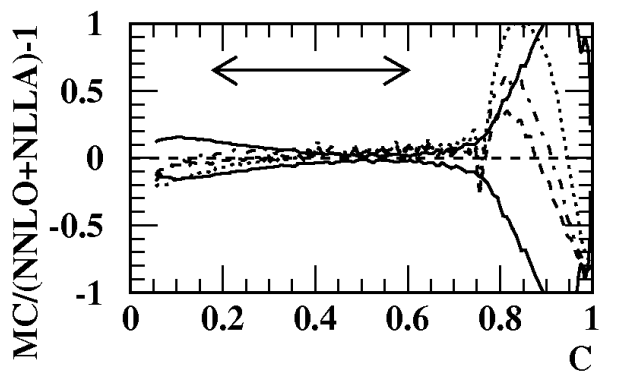
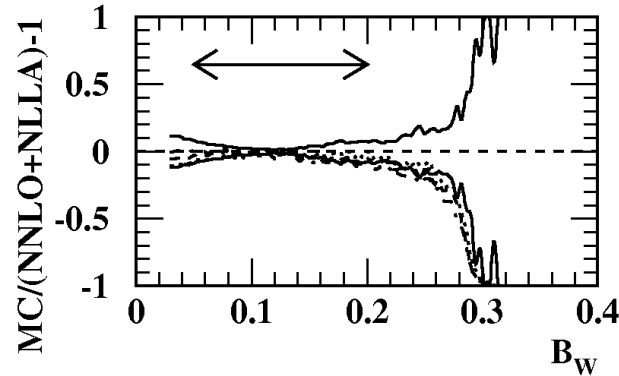
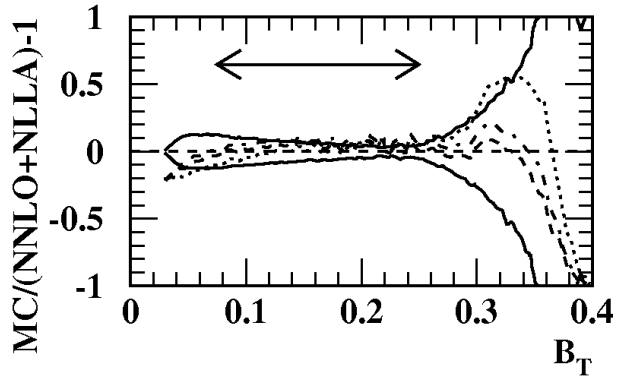
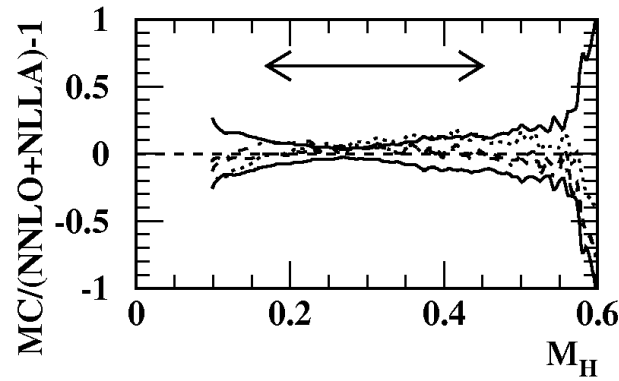
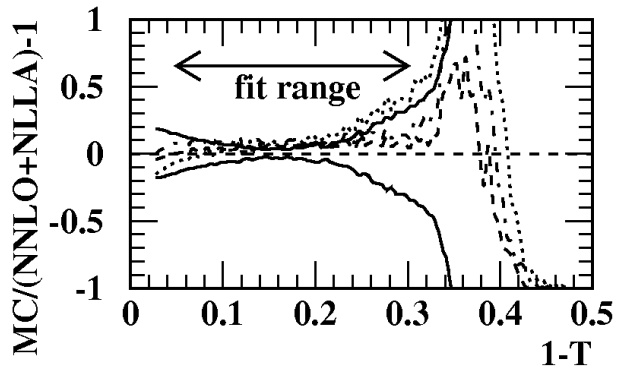
Perturbative prediction  
 Fixed order (+ resum.)  
 EVENT2, nlojet++,  
 EERAD3, ...

Hadronisation correction  
 strings or clusters  
 Pythia, Herwig, Sherpa, ...

Particle level  
 comparison/fit

- ☹ Parton level in pert. prediction and MCs not equal, limits precision to present few %, pert. - non-pert. correlation?
- ☺ Universal

# MC vs pQCD parton level



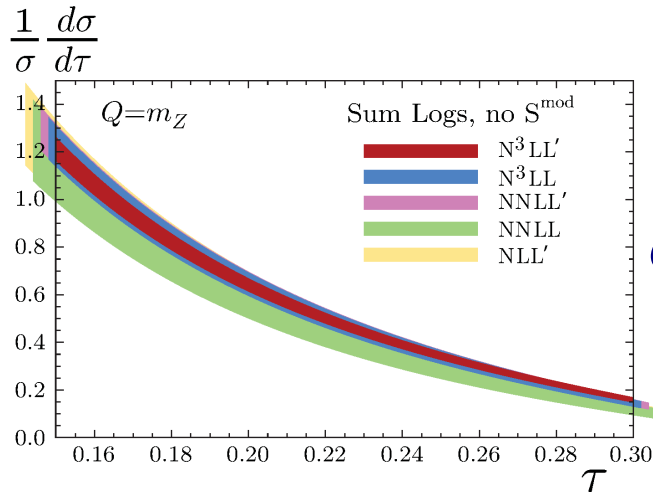
Compare MC parton level to pQCD (NNLO+NLLA)

Compare with differences between MCs

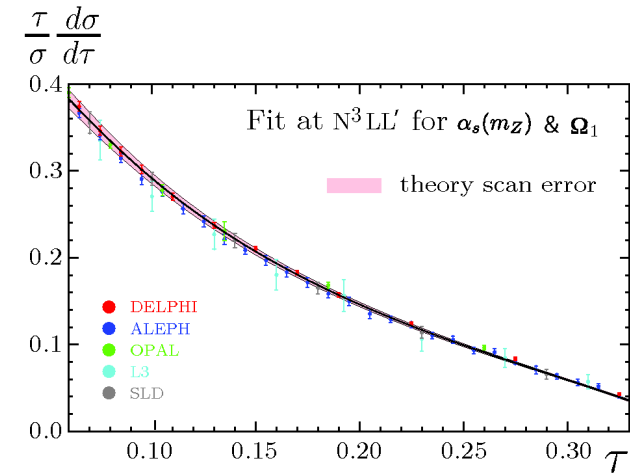
Parton levels consistent within MC model differences

[Eur. Phys. J. C71 (2011) 1733]

# pQCD $\oplus$ had. corr. models



“+” Power corrections  
 Dispersive model, =  
 SCET, SDG, ...



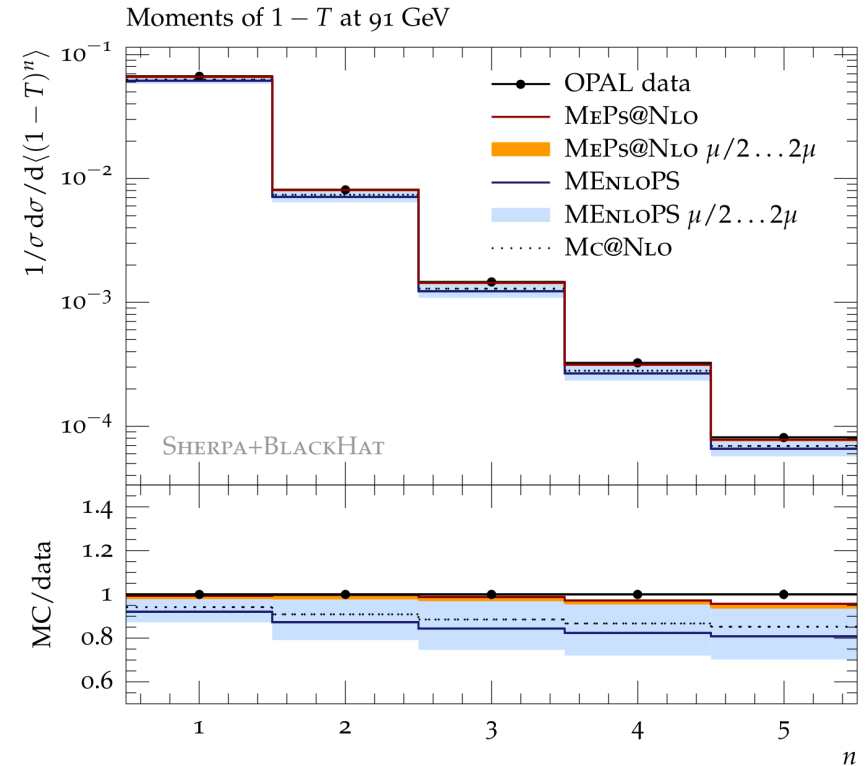
[Abbate, Fickinger, Hoang, Mateu, Stewart, Phys. Rev. D83 (2011) 074021,  
 Davison, Webber, Eur. Phys. J. C59 (2009) 13-25]

- ☺ Simultaneous fit of pert. prediction and power correction (had. correction) not limited by parton level inconsistency, take pert. - non-pert. correlation into account: much better precision limited by theory (and experiment)
- ☺ Most complete resummation so far with SCET
- ☹ Not universal, observable specific calculation

# pQCD $\oplus$ MC tuning

MEPS@NLO: NLO (automated)  
matched to parton shower;  
merged for  $2 \rightarrow n$  processes;  
Hadronisation model (strings,  
clusters)

[Gehrmann, Höche, Krauss, Schönherr, Siegert,  
JHEP 1301 (2013) 144]



- ☺ Improved perturbative uncertainties, simultaneous fit (MC tuning) takes account of pert. - non-pert. correlation
- ☺ Universal
- ☺ 4-jet and 5-jet observables possible
- ☹ NLO only, parton shower formally LL, in practice almost NLL, subleading logs? NNLO? Merging scale?

# pQCD ⊕ MC tuning

GENEVA MC: (NLO+NNLL) ⊕ PS ⊕ had'n (Pythia8) for thrust

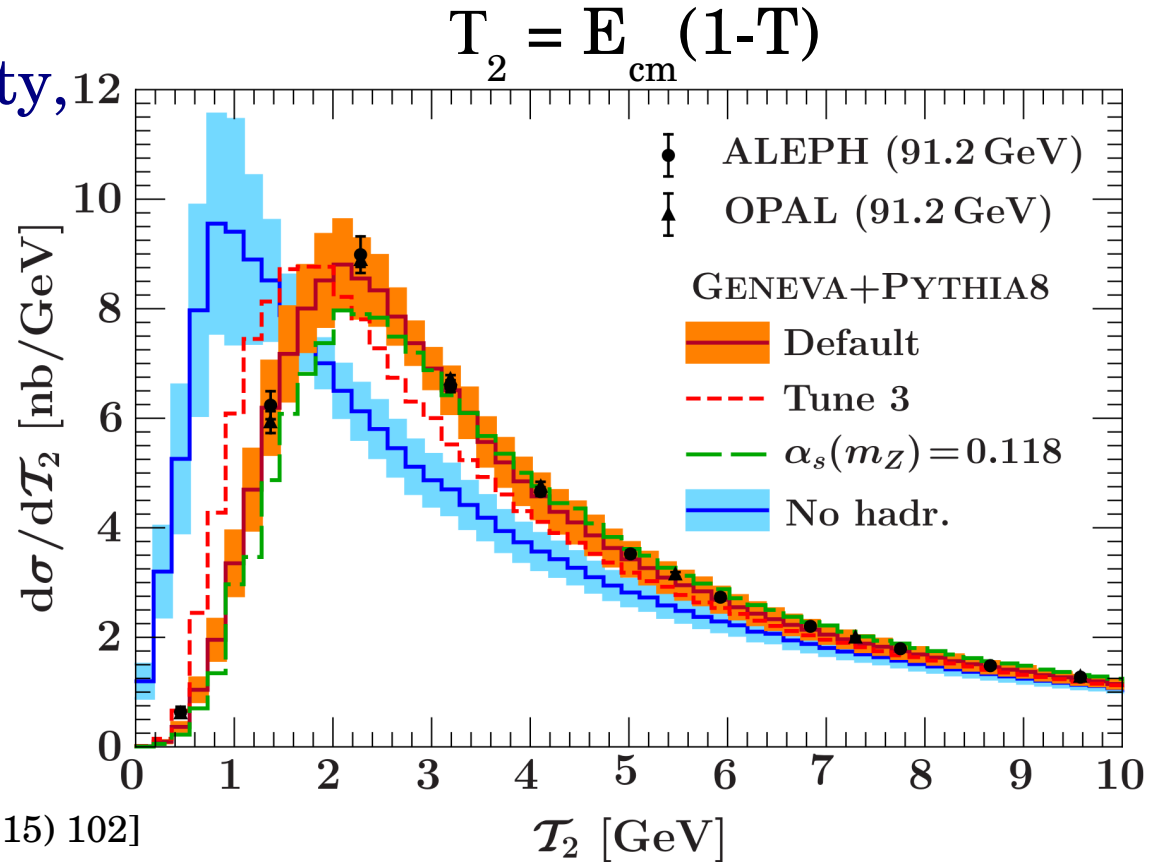
Solves parton shower ambiguity,  
i.e. NLO+NNLL+PS+had.

Other event shapes? Predicted by GENEVA based on  $T_2$ ; self-consistent calculation desirable

NNLL from ARES?

[Banfi, McAslan, Monni, Zanderighi, JHEP 1505 (2015) 102]

NNLO matching? Needs  $N^3LL$  ...



Alioli, Bauer, Berggren, Hornig, Tackmann, Vermilion, Walsh, Zuberi, JHEP 1309 (2013) 120]

# Other theory aspects

- $N^3LO$  corrections?

- Discussion about NNLO  $pp \rightarrow Z + \text{jets}$  implies this?

Maître, Sapeta, Eur. Phys. J. C73 (2013) 2663

- NNLL corrections

- 1-T,  $T_{\text{maj}}$ , C,  $M_H$ ,  $B_T$ ,  $B_W$ , O, EEC; ARES

- Numerically important

- Jet resolution distributions?

- $N^3LL$  possible? Needed for NNLO, on the wishlist ...

- Theory error estimates

- e.g. some NNLL corrections outside band of NNLO

- Discuss procedure ( $x_\mu; x_L^*/2$ )?



# Summary

- Field is theory driven
  - Exp. uncertainty on  $\alpha_s$  from 1-T  $\sim 1.3\%$  (OPAL)
    - Combination with e.g. ALEPH possible
    - Much smaller in “global fits”
  - Still to be matched by theory+had'n uncertainty
  - Wishlist:  $N^3LL$ , MC PS matching,  $N^3LO$
- Revisit systematic  $\alpha_s$  studies
  - Well understood data and errors
  - Several (many?) observables at same level of prediction
  - New/better observables? Let us know!