

# Extraction of the Strong Coupling $\alpha_s$ Through W-boson Hadronic Decays

[Workshop on high-precision  $\alpha_s$  measurements: From LHC to FCC-ee]

Matej Srebre<sup>1</sup>, David d'Enterria

CERN

[matej.srebre@cern.ch](mailto:matej.srebre@cern.ch), [dde@cern.ch](mailto:dde@cern.ch)

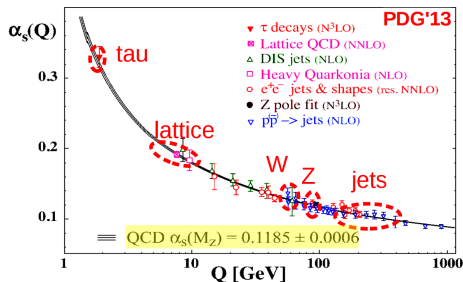
October 2015

---

<sup>1</sup>University of Ljubljana, currently master's student at LMU Munich

# Motivation

Extraction of  $\alpha_s$  through comparison of various experimental observables to different perturbative QCD predictions.



- 1 Hadronic  $\tau$  decays:  $R_\tau = \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} = S_{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n (\frac{\alpha_s}{\pi})^n + \mathcal{O}(\alpha_s^5) + \delta_{np})$  (N<sup>3</sup>LO)
- 2 Lattice QCD: Various short-distance quantities:  $K^{\text{NP}} = K^{\text{PT}} = \sum_{i=0}^n c_i \alpha_s^i$  (NNLO)
- 3 Hadronic Z decays:  $R_Z = \frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow \ell)}$  =  $R_Z^{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n (\frac{\alpha_s}{\pi})^n + \mathcal{O}(\alpha_s^5) + \delta_m + \delta_{np})$  (N<sup>3</sup>LO)
- 4  $e^+e^- \rightarrow q\bar{q}(g)$ : Event-shapes, jet rates:  $\frac{1}{\sigma} \frac{d\sigma}{dY} = \frac{dA}{dY} \hat{\alpha}_s + \frac{dB}{dY} \hat{\alpha}_s^2 + \frac{dC}{dY} \hat{\alpha}_s^3$  (NNLO)
- 5  $e^\pm p \rightarrow \text{hadrons}$  (PDF):  $\sigma(\text{jet}), \frac{\partial}{\partial \ln Q^2} D_i^h(x, Q^2) = \sum_j \int_x^1 \frac{dz}{z} \frac{\alpha_s}{4\pi} P_{ji}(\frac{x}{z}, Q^2) D_j^h(z, Q^2)$  (NLO, NNLO)
- 6  $pp, p\bar{p} \rightarrow t\bar{t}, \text{jets}$  (NNLO, NLO)
- 7 Hadronic W decays:
  - What is the theoretical and experimental status?
  - Can we extract  $\alpha_s$  through hadronic W decays? With which precision?

## Theoretical Calculation of $\Gamma_W(\text{hadronic})$

The hadronic W-boson decay width has not been used so far for  $\alpha_s$  extraction because:

- a complete N<sup>3</sup>LO/NNLO formula with all computed corrections [1] was not available until recently [2] (albeit with a few approximations),
- the 2% relative experimental uncertainty on  $\Gamma_W(\text{hadronic})$  was significantly large compared to 0.1% of  $\Gamma_Z(\text{hadronic})$ .

We recalculated  $\Gamma_W(\text{hadronic})$  through implementation in *MATHEMATICA* the  $\mathcal{O}(\alpha_s^4)$  or N<sup>3</sup>LO formula using [2]:

$$\Gamma_W(\text{hadronic}) = \sum_{i=0}^4 \Gamma_{\text{QCD}}^{(i)} + \Gamma_{\text{EW}}^{(1)} + \Gamma_{\text{Mixed}}^{(2)} = \frac{\sqrt{2}G_F m_W^3}{4\pi} \left[ \sum_{i,j} |V_{i,j}|^2 \right] \left( 1 + \sum_{k=1}^4 \left( \frac{\alpha_s}{\pi} \right)^k + \delta_{\text{EW}} + \delta_{\text{Mixed}} \right),$$

where

- $\Gamma_{\text{QCD}}^{(k)}$  is the leading order decay width and QCD corrections of order  $\mathcal{O}(\alpha_s^k)$  and  $k = 1, \dots, 4$ ,
- $\Gamma_{\text{EW}}^{(1)}$  electroweak corrections of order  $\mathcal{O}(\alpha)$ ,
- $\Gamma_{\text{Mixed}}^{(2)}$  mixed corrections of order  $\mathcal{O}(\alpha\alpha_s)$ .

[1] - A. Denner, B. Kniehl, J. Kühn, K. Chetyrkin, ...

[2] - D. Kara, Nucl. Phys. B 877, 3 (2013)

## Improvements with Respect to Previous $\Gamma_W$ (hadronic) Calculations

In our calculations we carry out the following improvements compared to previous works:

- 1 implement **finite quark masses** in the dominant  $\Gamma_W$ (hadronic) terms: Born and first-order QCD corrections,
- 2 use **NNLO  $\alpha_s$  running instead of LO** (between  $m_W$  and  $m_Z$ ),
- 3 use **current PDG world average values** for parameters of the Standard Model ( $\alpha_{\text{QED}}$ ,  $G_F$ ,  $m_q$ ,  $m_\ell$ ,  $m_W$ ,  $m_Z$ ,  $m_H$ , *CKM matrix elements*  $|V_{i,j}|$ ),
- 4 determination of associated **theoretical** and **parametric** uncertainties.

# Hadronic W-boson Decay Width - Numerical Results

Previous state-of-the-art [2]:  $\Gamma_W(\text{hadronic}) = (1458.820 \pm 6 \times 10^{-3}) \text{ MeV}$ ,

$$\Gamma_W(\text{hadronic}) = (1428.803 \pm 0.030_{\text{theor.}} \pm 22.608_{\text{param.}}) \text{ MeV},$$

$$\Gamma_W(\text{hadronic}, V_{ij} V_{kj} = \delta_{ik}) = (1411.546 \pm 0.030_{\text{theor.}} \pm 0.742_{\text{param.}}) \text{ MeV}.$$

Partial width	$\Gamma_{\text{QCD}}^{(0)}$	$\Gamma_{\text{QCD}}^{(1)}$	$\Gamma_{\text{QCD}}^{(2)}$	$\Gamma_{\text{QCD}}^{(3)}$	$\Gamma_{\text{QCD}}^{(4)}$	$\Gamma_{\text{EW}}^{(1)}$	$\Gamma_{\text{Mixed}}^{(2)}$
$\Gamma_W(\text{hadronic})$ of [2]	1408.980	54.087	2.927	-1.018	-0.245	-5.132	-0.779
$\Gamma_W(\text{hadronic})$	1379.851	53.080	2.873	-1.000	-0.241	-5.002	-0.757
$\Gamma_W(\text{hadronic}, V_{ij} V_{kj} = \delta_{ik})$	1363.186	52.439	2.838	-0.988	-0.238	-4.942	-0.749

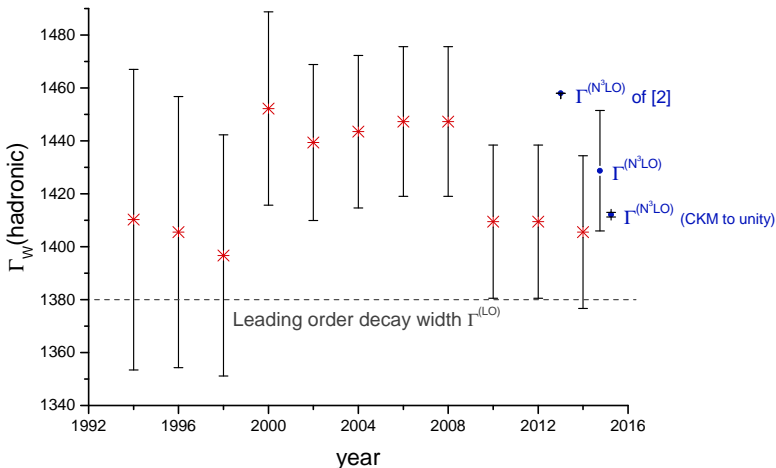
Numerical values of the partial decay widths. All values given in MeV.

The following uncertainties are present in  $\Gamma_W(\text{hadronic})$ :

- parametric uncertainty (modifying all PDG parameters by  $\pm\sigma$ , adding changes in quadrature)
  - $\pm 22.608 \text{ MeV}$  (the dominant parametric uncertainty is  $V_{cs}$ ),
  - $\pm 0.742 \text{ MeV}$  for  $V_{ij} V_{kj} = \delta_{ik}$  (dominated by  $m_W$ ),
- higher-order corrections (assumed equal to  $\Gamma_Z$ , from  $N^3\text{LO}$  to  $N^4\text{LO}$ ):  $\pm 0.0195 \text{ MeV}$ ,
- non-perturbative uncertainties (assuming power-corrections of order  $\mathcal{O}\left(\frac{\Lambda^4}{m_W^4}\right)$ ):  $\pm 7 \times 10^{-8} \text{ MeV}$ ,
- finite quark masses beyond LO corrections:  $\pm 0.0042 \text{ MeV}$ ,
- mixed corrections from [2]:  $\pm 0.006 \text{ MeV}$ .

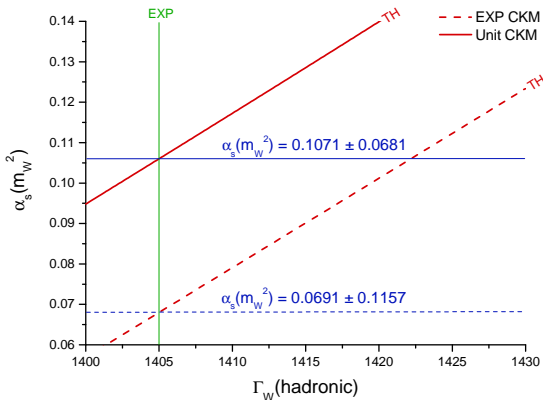
## $\Gamma_W(\text{hadronic})$ : Historical Data Versus Theory

Evolution of the PDG world average value of  $\Gamma_W^{\text{EXP}}(\text{hadronic})$  (current value is  $(1405 \pm 29)$  MeV) by year compared to theoretically predicted decay widths.



# Extraction of $\alpha_s$ from $\Gamma_W(\text{hadronic})$

Using the  $\mathcal{O}(\alpha_s^4)$  W-boson decay width formula we can extract  $\alpha_s$  by comparing it to the experimental value which is  $\Gamma_W^{\text{EXP}}(\text{hadronic}) = (1405 \pm 29) \text{ MeV}$ .



$\Rightarrow$  Current large parametric ( $\pm 23 \text{ MeV}$ ) and experimental ( $\pm 29 \text{ MeV}$ ) uncertainties on  $\Gamma_W(\text{hadronic})$  propagate into a **huge  $\alpha_s$  uncertainty**  $\sim 60\%$ .

Experimental priorities should be:

- measure  $|V_{cs}|$  with better precision (current **1.6%**),
- significantly reduce uncertainty of  $\Gamma_W(\text{hadronic})$  measurement to a **few MeV**,
- reduce  $m_W$  uncertainty (now it propagates to  $\pm 0.8 \text{ MeV}$  on  $\Gamma_W(\text{hadronic})$ ).

	$\alpha_s(m_W^2)$	$\alpha_s(m_Z^2)$
Experimental CKM	$0.0691 \pm 0.0513_{\text{param.}} \pm 0.0644_{\text{exp.}}$	$0.0683 \pm 0.0509_{\text{param.}} \pm 0.0638_{\text{exp.}}$
Unit CKM, $V_{ij}V_{kj} = \delta_{ik}$	$0.1071 \pm 0.0017_{\text{param.}} \pm 0.0664_{\text{exp.}}$	$0.1053 \pm 0.0016_{\text{param.}} \pm 0.0657_{\text{exp.}}$

# Alternative Approach: $\alpha_s$ Extraction via $BR_W(\text{hadronic}) = \frac{\Gamma_W(\text{hadronic})}{\Gamma_W(\text{total})}$

$\Gamma_W(\text{hadronic})$  has a 2% experimental uncertainty,  $BR_W(\text{hadronic})$  has an uncertainty of 0.4%.

⇒ We try  $BR_W(\text{hadronic}) = \frac{\Gamma_W(\text{hadronic})}{\Gamma_W(\text{total})}$  to extract  $\alpha_s$  instead of  $\Gamma_W(\text{hadronic})$ .

For the total decay width  $\Gamma_W(\text{total})$  we use the ZFitter NNLO (includes up to  $\mathcal{O}(\alpha_s^3)$  QCD,  $\mathcal{O}(\alpha)$  electroweak and  $\mathcal{O}(\alpha\alpha_s)$  mixed corrections) fitted result by [3] which is parametrized as

$$\Gamma_W(\text{total}) = G_W^0 m_W^3 \quad \text{and} \quad G_W^0 = 4.0279 \times 10^{-6} (1 + 0.00095x_H - 0.0024x_H^2 + 0.0016x_H^3 + 000065x_s) \text{ GeV}^{-2},$$

where  $x_s = f(\alpha_s)$ ,  $x_H = f(m_H)$ .

We also computed the associated parametric uncertainties as done for  $\Gamma_W(\text{hadronic})$ .

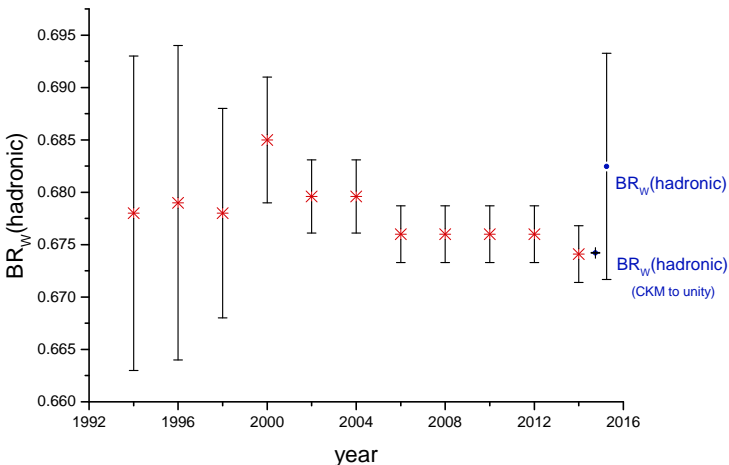
$\Gamma_W(\text{hadronic})$	$(1428.803 \pm 22.638) \text{ MeV}$
$\Gamma_W(\text{hadronic}, V_{ij}V_{kj} = \delta_{ik})$	$(1411.546 \pm 0.772) \text{ MeV}$
$\Gamma_W(\text{total})$	$(2093.591 \pm 1.172_{\text{param.}}) \text{ MeV}$
$BR_W(\text{hadronic})$	$0.6825 \pm 0.0108_{\text{param.}}$
$BR_W(\text{hadronic}, V_{ij}V_{kj} = \delta_{ik})$	$0.67422 \pm 0.00003_{\text{param.}}$
$BR_W(\text{hadronic})^{\text{EXP}}$	$0.6741 \pm 0.0027$

[3] - G. C. Cho, K. Hagiwara, Y. Matsumoto and D. Nomura, JHEP 111, 068 (2011)



## $BR_W(\text{hadronic})$ : Historical Data Versus Theory

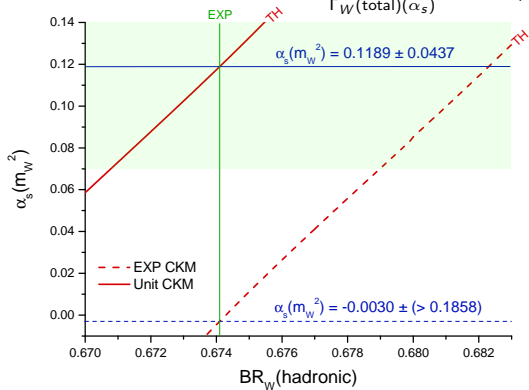
Evolution of the PDG world average value of  $BR_W(\text{hadronic})$  (current value is  $0.6741 \pm 0.0027$ ) by year compared to theoretically predicted decay widths.



# Alternative Approach: $\alpha_s$ Extraction via $BR_W(\text{hadronic}) = \frac{\Gamma_W(\text{hadronic})}{\Gamma_W(\text{total})}$

We can extract  $\alpha_s$  by comparing the theoretical hadronic branching ratio formula to the experimental world average value

$$\frac{\Gamma_W(\text{hadronic})(\alpha_s)}{\Gamma_W(\text{total})(\alpha_s)} = BR_W(\text{hadronic})^{\text{EXP.}}$$



⇒ Setting the CKM matrix to unit matrix instead of using experimental values, we can extract  $\alpha_s$  with 35% uncertainty.

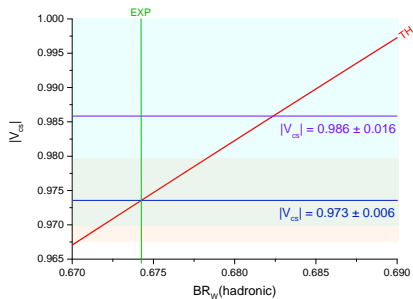
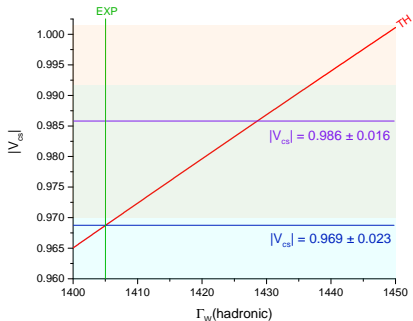
To extract  $\alpha_s$  with a higher precision:

- reduce the uncertainty of  $|V_{cs}|$  as mentioned earlier,
- reduce the uncertainty of  $m_W$  (measured to 0.02%) which becomes dominant once the  $|V_{cs}|$  uncertainty is reduced below 0.05%,
- measure  $BR_W(\text{hadronic})$  with a better precision than today (0.4% now).

	$\alpha_s(m_W^2)$	$\alpha_s(m_W^2)$	$\Delta\alpha_s(m_W^2)$
Experimental CKM	$-0.0030 \pm (> 0.1505_{\text{param.}}) \pm 0.0353_{\text{exp.}}$	/	/
Unit CKM	$0.1189 \pm 0.0004_{\text{param.}} \pm 0.0433_{\text{exp.}}$	$0.1167 \pm 0.0004_{\text{param.}} \pm 0.0430_{\text{exp.}}$	$\pm 37\%$

## Extra: Indirect Determination of $|V_{cs}|$

The large experimental  $BR_W(\text{hadronic})^{\text{EXP}}$  uncertainty precludes an accurate extraction of  $\alpha_s$ , but we can use  $BR_W(\text{hadronic})^{\text{EXP}}$  to determine  $|V_{cs}|$  (fixing  $\alpha_s$  to world average).



Extraction method	$ V_{cs} $ value
$\Gamma_W(\text{hadronic})$	$0.969 \pm 0.002_{\text{param.}} \pm 0.021_{\text{exp.}}$
$BR_W(\text{hadronic})$	$0.973 \pm 0.002_{\text{param.}} \pm 0.004_{\text{exp.}}$

$\Rightarrow$  We can extract  $|V_{cs}|$  with an uncertainty of **0.6%** compared to **1.6%** of the experimental measurement  $|V_{cs}|^{\text{EXP}} = 0.986 \pm 0.016$ .

## Future Perspectives: LHC & FCC-ee

To determine  $\alpha_s$  with a **higher precision** we need more precise measurement of  $\Gamma_W$ (total) and/or  $BR_W$ (hadronic) with reduced uncertainties.

- Uncertainties at LHC ( $5 \times 10^5$  high- $m_T$  W's at  $\sqrt{s} = 8$  TeV,  $20 \text{ fb}^{-1}$ ):
    - Statistical:  $\sim 3$  MeV (30 MeV at Tevatron, with  $5 \times 10^3$  high- $m_T$  W's)
    - Systematics:  $\sim 15$  MeV (down from  $\sim 40$  MeV at Tevatron, reduced PDF uncertainties)
- Improved result:**  $\Gamma_W$ (hadronic)  $\sim (1429 \pm 12)$  MeV (i.e. **0.8%** uncertainty instead of **2%**)

	$\alpha_s(m_W^2)$	$\Delta\alpha_s(m_W^2)$
Unit CKM	$0.1208 \pm 0.0004_{\text{param.}} \pm 0.0275_{\text{exp.}}$	$\pm 23\%$

$\Rightarrow$  Improved  $\Gamma_W$ (hadronic) at LHC allows to extract  $\alpha_s$  with  $\sim 23\%$  uncertainty.

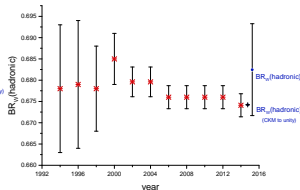
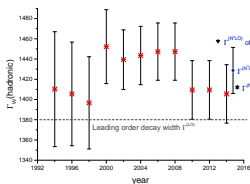
- Uncertainties at FCC-ee ( $5 \times 10^8$  W's at  $\sqrt{s} = m_W$ ):
  - Statistical:  $\sim 0.005\%$  (0.4% at LEP with  $8 \times 10^4$  W's)

**Final result:**  $BR_W$ (hadronic)  $\sim 0.67410 \pm 0.00003$

	$\alpha_s(m_W^2)$	$\Delta\alpha_s(m_W^2)$
Unit CKM	$0.1208 \pm 0.0004_{\text{exp.}}$	$\pm 0.3\%$

$\Rightarrow$  FCC-ee would provides us a value for  $\alpha_s$  with a relative uncertainty of  $\sim 0.3\%$ .

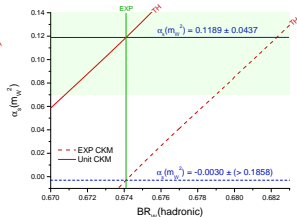
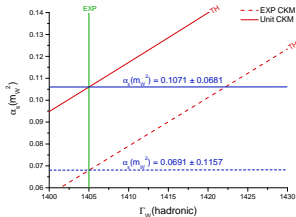
# Summary



⇒ We computed  $\Gamma_W(\text{hadronic})$  and  $BR_W(\text{hadronic})$  using state-of-the-art  $N^3\text{LO}/\text{NNLO}$  calculations, removing some of the previously applied approximations:

$$\Gamma_W(\text{hadronic}) = (1411.546 \pm 0.772) \text{ MeV},$$

$$BR_W(\text{hadronic}) = 0.67422 \pm 0.00003.$$



⇒ Current experimental  $\Gamma_W(\text{hadronic})$ ,  $BR_W(\text{hadronic})$  and  $|V_{cs}|$  uncertainties preclude precise extraction of  $\alpha_S$ .

⇒ Improvements at LHC, and in particular FCC-ee, will allow one to incorporate  $\Gamma_W(\text{hadronic})$  and  $BR_W(\text{hadronic})$  into the PDG  $\alpha_S$ .

	$\alpha_S(m_W^2)$	$\alpha_S(m_Z^2)$	$\Delta\alpha_S(m_W^2)$
Today (Unit CKM)	$0.1189 \pm 0.0004_{\text{param.}} \pm 0.0433_{\text{exp.}}$	$0.1167 \pm 0.0004_{\text{param.}} \pm 0.0430_{\text{exp.}}$	$\pm 37\%$
LHC (Unit CKM)	$0.1208 \pm 0.0004_{\text{param.}} \pm 0.0271_{\text{exp.}}$	$0.1185 \pm 0.0004_{\text{param.}} \pm 0.0260_{\text{exp.}}$	$\pm 23\%$
FCC-ee	$0.1208 \pm 0.0004_{\text{exp.}}$	$0.1185 \pm 0.0004_{\text{exp.}}$	$\pm 0.3\%$

⇒ FCC-ee will allow us to measure  $\alpha_S$  with  $\sim 0.3\%$  uncertainty.

Thank you. Any questions?

# Backup slides

## Experimental Hadronic Width Measurement

- Experimental hadronic  $\Gamma_W(\text{hadronic})$  from  $\Gamma_W(\text{total})$  via  $\text{BR}_W(\text{hadronic})^2$ :

$$\begin{aligned}\Gamma_W(\text{hadronic}) &= \Gamma_W(\text{total}) \times \text{BR}_W(\text{hadronic}) \\ &= (2085 \pm 42) \times (0.6741 \pm 0.0027) \text{ MeV} \\ &= (1405 \pm 29) \text{ MeV} \text{ (i.e. 2\% uncertainty)}\end{aligned}$$

- $\Gamma_W(\text{total})$  in  $e^+e^- \rightarrow W^+W^- \rightarrow 4q, 2q + \ell\nu$

Where: LEP ( $\sqrt{s} = 161 - 209 \text{ GeV}$ ) & FCC-ee ( $\sqrt{s} = 161, 240, 350 \text{ GeV}$ )

How: **Maximum-likelihood fit of  $m_W$  Breit-Wigner** with  $\Gamma_W(\text{total})$  as free parameter.

- $\Gamma_W(\text{total})$  in  $p\bar{p}, pp \rightarrow W + X$ , with  $W \rightarrow e\nu, \mu\nu$

Where: Tevatron ( $\sqrt{s} = 1.8, 1.96 \text{ TeV}$ ) & LHC ( $\sqrt{s} = 7, 8, 13, 14 \text{ TeV}$ )

How: **Maximum likelihood fit of high  $m_T(W)$  tail** with  $\Gamma_W(\text{total})$  as free parameter (and via  $\sigma(W)/\sigma(Z)$  ratios).

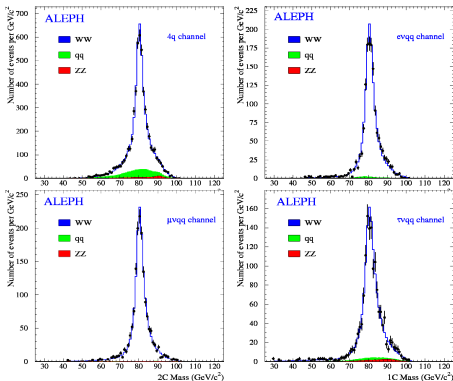
---

<sup>2</sup>0.4 % uncertainty measured in  $e^+e^-$



# LEP-2 W-boson Width Measurement [arXiv:1302.3415]

- $e^+e^- \rightarrow W^+W^- \rightarrow 4q, 2q + \ell\nu$  at  $\sqrt{s} = 161 - 209$  GeV
- Statistics:  
N(W's in all channels / experiments)  $\sim 40.000$  pairs
- Binned likelihood fit to  $m_W$  Breit-Wigner with  $\Gamma_W$ (total) as free parameter:



Source	Systematic Uncertainty in MeV			
	on $m_W$			on $\Gamma_W$
	$q\bar{q}\ell\nu_\ell$	$q\bar{q}q\bar{q}$	Combined	
ISR/FSR	8	5	7	6
Hadronisation	13	19	14	40
Detector effects	10	8	9	23
LEP energy	9	9	9	5
Colour reconnection	–	35	8	27
Bose-Einstein Correlations	–	7	2	3
Other	3	10	3	12
Total systematic	21	44	22	55
Statistical	30	40	25	63
Statistical in absence of systematics	30	31	22	48
Total	36	59	34	83

- Final result:  $\Gamma_W$ (total) =  $(2495 \pm 63_{\text{stat.}} \pm 55_{\text{syst.}})$  MeV

# CDF W-boson Width Measurement [PRL 100, 071801 (2008)]

- $p\bar{p} \rightarrow W + X$ , with  $W \rightarrow e\nu, \mu\nu$  at  $\sqrt{s} = 1.96$  TeV ( $L_{int.} \sim 350$  pb $^{-1}$ )
- Statistics:  
N(W's)=3.436+2.619 with  $90 < M_T < 200$  GeV
- Binned likelihood fit to ( $90 < M_T < 200$  GeV) spectra with  $\Gamma_W$ (total) as free parameter:

$$M_T = \sqrt{2(p_T^l p_T^\nu - \vec{p}_T^l \cdot \vec{p}_T^\nu)}$$

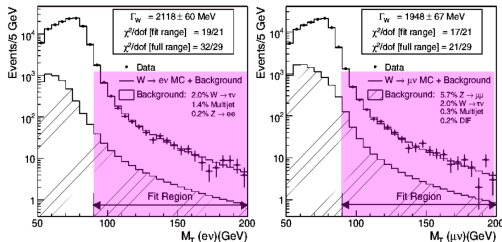


TABLE I. The sources of uncertainty (in MeV) on  $\Gamma_W$  for the  $W \rightarrow e\nu$  and  $W \rightarrow \mu\nu$  measurements. If there is a correlated source of error between the two measurements its contribution to each measurement is listed in the third column, labeled C.

Source	$\Delta\Gamma_W^{e\nu}$	$\Delta\Gamma_W^{\mu\nu}$	C
Statistics	60	67	
Lepton $E$ or $p$ scale	21	17	12
Lepton $E$ or $p$ resolution	31	26	
Electron energy loss simulation	13		
Recoil model	54	49	
$p_T^W$	7	7	7
Backgrounds	32	33	
PDFs	20	20	20
$M_W$	9	9	9
EW radiative corrections	10	6	6
Lepton ID/acceptance	10	7	
<b>Total systematic</b>	<b>79</b>	<b>71</b>	<b>27</b>
Total (statistic + systematic)	99	98	27

- Final result:  $\Gamma_W(\text{total}) = (2032 \pm 45_{\text{stat.}} \pm 57_{\text{ syst.}})$  MeV

# Tevatron W-boson Width Combined [arXiv: 1003.2826]

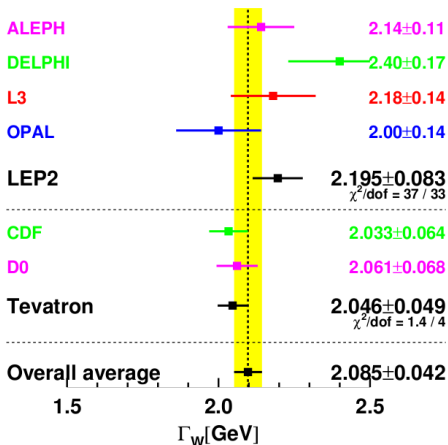
- CDF + D0 combined (BLUE method)  $p\bar{p} \rightarrow W + X$ , with  $W \rightarrow e\nu, \mu\nu$  at 1.8 and 1.96 TeV.
- Improved likelihood fits to  $M_T$  spectra with updated underlying parameters:

	Run-I			Run-II	
	CDF-Ia	CDF-Ib	D0-Ib	CDF	D0
$\Gamma_W$ (published)	2,110	2,042.5	2,231	2,032	2,028.3
Total uncertainty (published)	329	138.3	172.8	72.4	72
$M_W$ used in publication	80,140	80,400	80,436	80,403	80,419
Correction to $\Gamma_W$ from $M_W$	-78	0.3	11.1	1.2	6.0
$\Gamma_W$ (corrected)	2,032	2,042.8	2,242.1	2,033.2	2,034.3
Total uncertainty (corrected)	329.3	138.3	172.4	72.4	71.9
Uncorrelated uncertainty (corrected)	327.6	136.8	167.4	68.7	68.5
PDF uncertainty (published)	0	15	39	20	20
PDF uncertainty (this analysis)	15	15	39	20	20
EWK RC uncertainty	28	10	10	6	7
$M_W$ uncertainty (published)	0	10	15	9	5
$M_W$ uncertainty (this analysis)	7	7	7	7	7
$M_W$ extrapolation	26	0	4	0	2

- Final result:  $\Gamma_W(\text{total}) = (2046 \pm 49) \text{ MeV} \begin{matrix} \pm 39 \text{ MeV (stat.)} \\ \pm (20+7.4+7.4) \text{ MeV (PDF + } m_W\text{+EW. corr.)} \end{matrix}$

# W-boson Width: Tevatron + LEP Combined [PDG]

- World average of all LEP + Tevatron measurements:



Final result:  $\Gamma_W(\text{total}) = (2.085 \pm 0.042)$  GeV (i.e. 2% uncertainty)

Note:  $\Gamma_Z(\text{total}) = (2.4952 \pm 0.0023)$  GeV (i.e. 0.1 % uncertainty)

## List of References



A. Denner, B. Kniehl, J. Kühn, K. Chetyrkin, ...



Dominik Kara *Corrections of Order  $\alpha\alpha_s$  to  $W$  boson decays*, Nucl. Phys. B 877, 3 (2013)



G. C. Cho, K. Hagiwara, Y. Matsumoto and D. Nomura, *The MSSM confronts the precision electroweak data and the muon  $g - 2$* , JHEP 111 (2011), 068



K.A. Olive et al. (Particle Data Group), Chin. Phys. C, 38, 090001 (2014)