



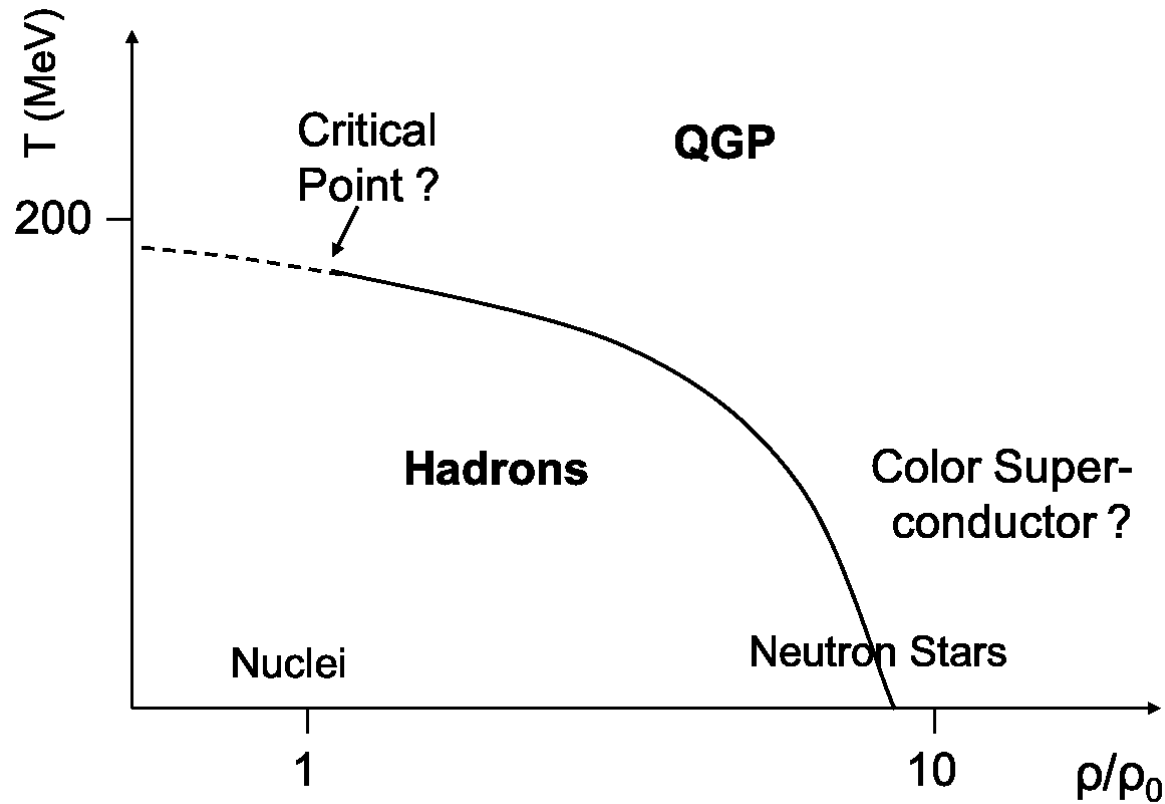
# Measurements of event-by-event mean transverse momentum fluctuations with ALICE at the LHC

Stefan Heckel  
on behalf of the ALICE Collaboration

HIC for FAIR Workshop on Fluctuation and Correlation Measures in Nuclear  
Collisions 2015

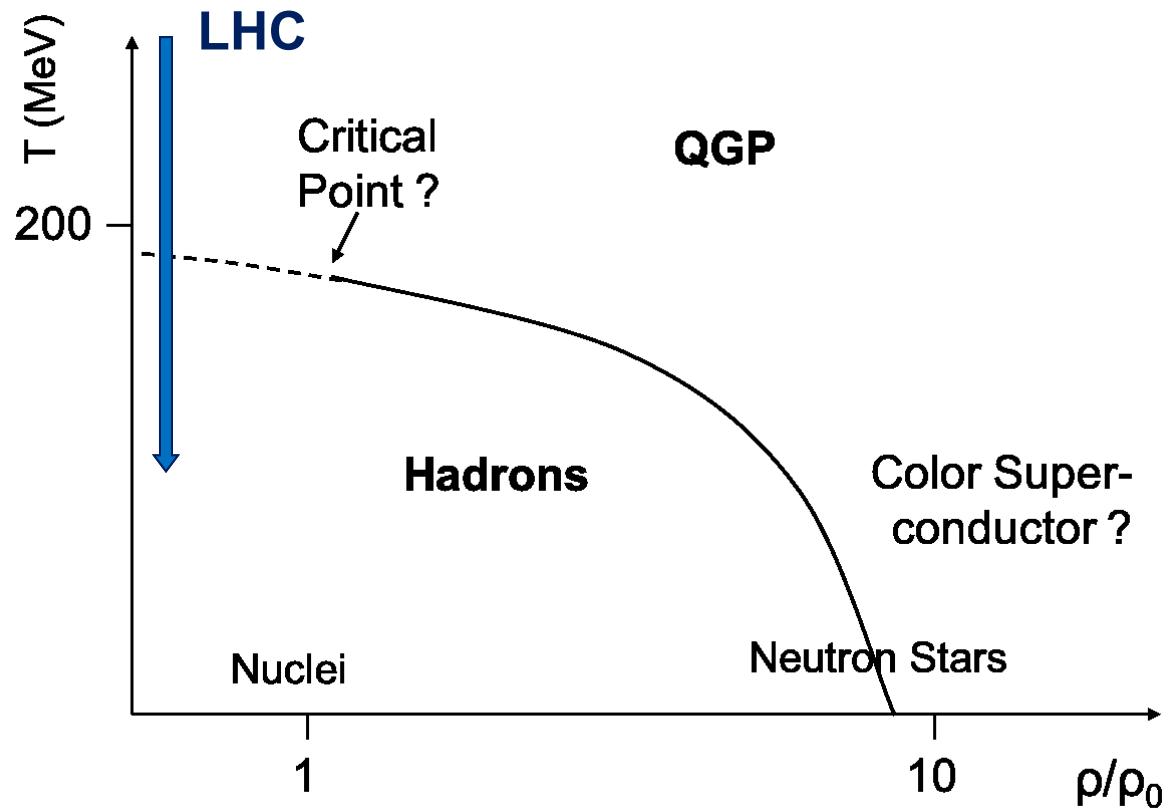
July 29, 2015

# Motivation



- Fluctuations of thermodynamic quantities suggested as a signal for a phase transition and especially a potential critical endpoint

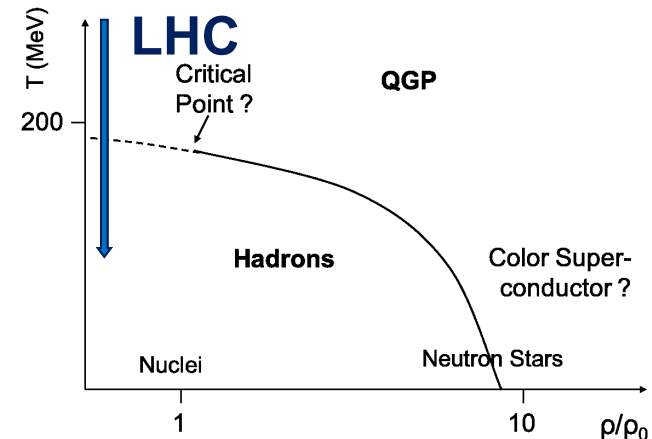
# Motivation



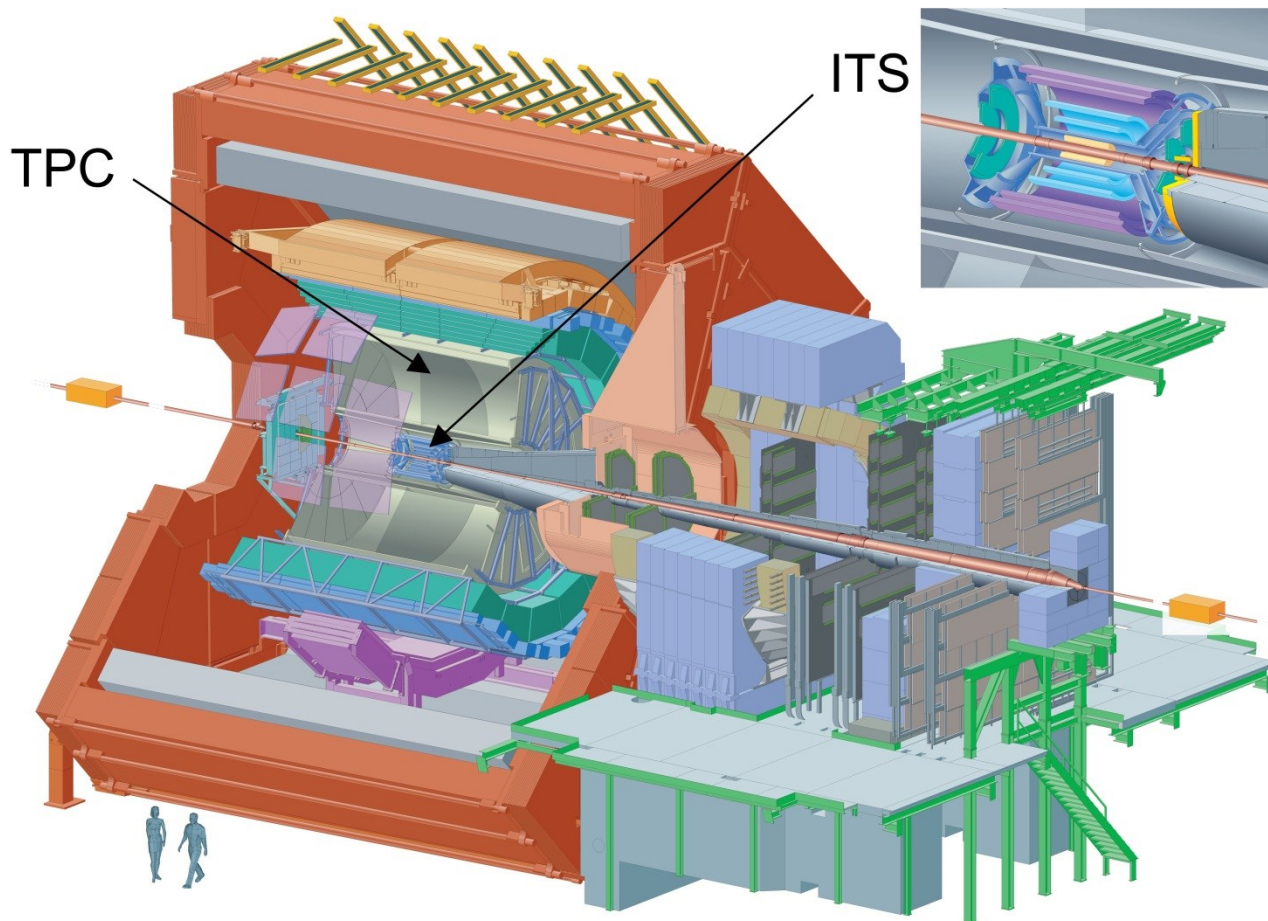
- Fluctuations of thermodynamic quantities suggested as a signal for a phase transition and especially a potential critical endpoint
- At the LHC: Main focus on phase transition and QGP properties

# Motivation

- One of the observables proposed: event-by-event fluctuations of the mean transverse momentum
- Heavy-ion collisions ( $A-A$ ): complex system with potentially many different effects
- Start with a much more simple system: pp collisions
- At first: experiment, data sets, observables ...



# ALICE detector setup



Main detectors used  
in this analysis:

**Time  
Projection  
Chamber**

(Tracking, Vertex)

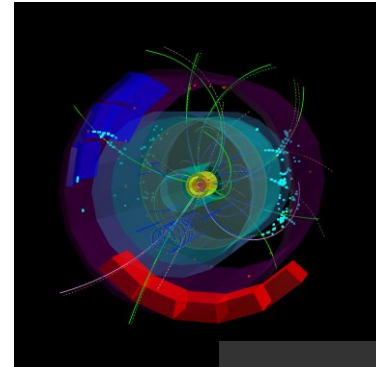
**Inner  
Tracking  
System**

(Vertex)

## Data sets and acceptance

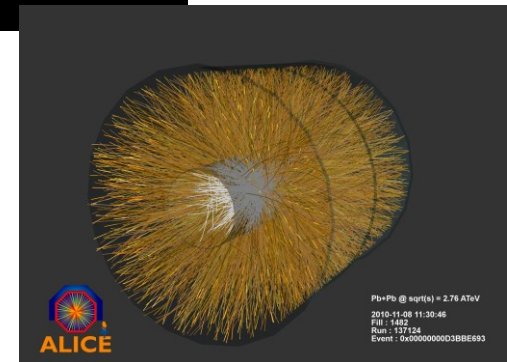
### pp collisions:

- $\sqrt{s} = 0.9$  TeV, 6.9 M events
- $\sqrt{s} = 2.76$  TeV, 66 M events
- $\sqrt{s} = 7$  TeV, 290 M events



### Pb–Pb collisions:

- $\sqrt{s_{NN}} = 2.76$  TeV, 19 M events



### Acceptance:

Pseudorapidity range:  $|\eta| < 0.8$

Transverse momentum range:  $0.15 < p_T < 2$  GeV/c

## Getting started: The mean transverse momentum

True mean transverse momentum in an event  $k$ :

$$\langle p_T \rangle_k = \frac{1}{N_{\text{ch},k}} \cdot \sum_{i=1}^{N_{\text{ch},k}} p_{T,i}$$

Cannot be measured event-by-event, approximated by the measured raw quantity:

$$M(p_T)_k = \frac{1}{N_{\text{acc},k}} \cdot \sum_{j=1}^{N_{\text{acc},k}} p_{T,j}$$

$N_{\text{ch},k}$  : True number of particles in event  $k$

$N_{\text{acc},k}$  : Measured raw number of particles in event  $k$

## Observables: The dispersion

The dispersion quantifies the total fluctuations:

$$D(M(p_T)) = \left[ \langle M^2(p_T) \rangle - \langle M(p_T) \rangle^2 \right]^{1/2}$$

Dominated by statistical fluctuations!

Assumption: non-statistical contribution not depending on multiplicity  $n$

⇒ Square of normalized dispersion described by the fit:

$$\left[ D_n(M(p_T)) / M(p_T) \right]^2 = \frac{\langle M^2(p_T) \rangle_n - \langle M(p_T) \rangle_n^2}{M^2(p_T)} = A + \frac{B}{n}$$



## Observables: The dispersion

$$\left[ D_n(M(p_T)) / M(p_T) \right]^2 = \frac{\langle M^2(p_T) \rangle_n - \langle M(p_T) \rangle_n^2}{M^2(p_T)} = A + \frac{B}{n}$$

For large multiplicities  $\left(\frac{1}{n} \rightarrow 0\right)$  the non-statistical contribution  $R$  yields:

$$R = \left[ D_n(M(p_T)) / M(p_T) \right]_{n \rightarrow \infty} = A^{1/2}$$

Has been measured by SFM at the ISR [1]

Can we do better?  $\Rightarrow$  Two-particle transverse momentum correlator

[1] K. Braune *et al.*, Phys.Lett. **B123**  
(1983) 467

## Observables: Two-particle correlator

The mean of covariances of all particle pairs  $i$  and  $j$

$$C = \langle \Delta p_{T,i}, \Delta p_{T,j} \rangle = \frac{1}{\sum_{k=1}^{n_{ev}} N_k^{pairs}} \cdot \sum_{k=1}^{n_{ev}} \sum_{i=1}^{N_k} \sum_{j=i+1}^{N_k} (p_{T,i} - M(p_T)) \cdot (p_{T,j} - M(p_T))$$

[2] S. Voloshin *et al.*, Phys.Rev. **C60**  
(1999) 024901

[3] D. Adamová *et al.*, Nucl.Phys. **A811**  
(2008) 179

[4] J. Adams *et al.*, Phys.Rev. **C72**  
(2005) 044902

$n_{ev}$ : Number of events

$N_k$ : Number of particles in event  $k$

$N_k^{pairs} = 0.5 \cdot N_k \cdot (N_k - 1)$ : Number of pairs in event  $k$

$M(p_T)$ : Mean  $p_T$  of all tracks in all events

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$C = 0$  for only statistical fluctuations

Robust quantity!

$n_{\text{ev}}$ : Number of events

$N_k$ : Number of particles in event  $k$

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$C = 0$  for only statistical fluctuations

$$\frac{\sqrt{C}}{M(p_T)}$$

$n_{ev}$ : Number of events

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$N_k^{\text{pairs}} = 0.5 \cdot N_k \cdot (N_k - 1)$ : Number of pairs in event  $k$

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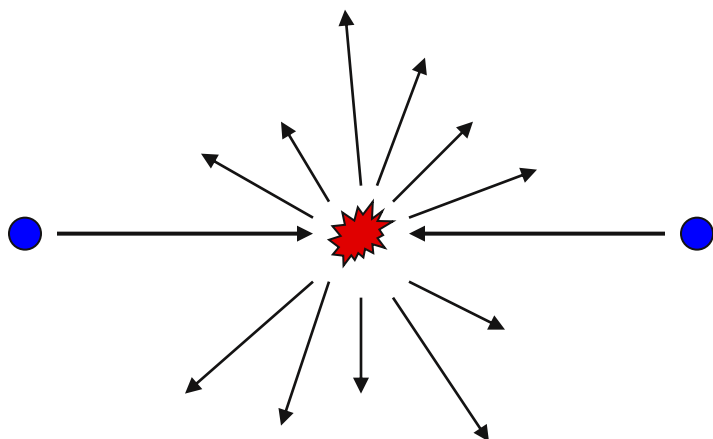
Measure fluctuations relative to  $M(p_T)$ :

- Dimensionless
- Reduced systematic uncertainties

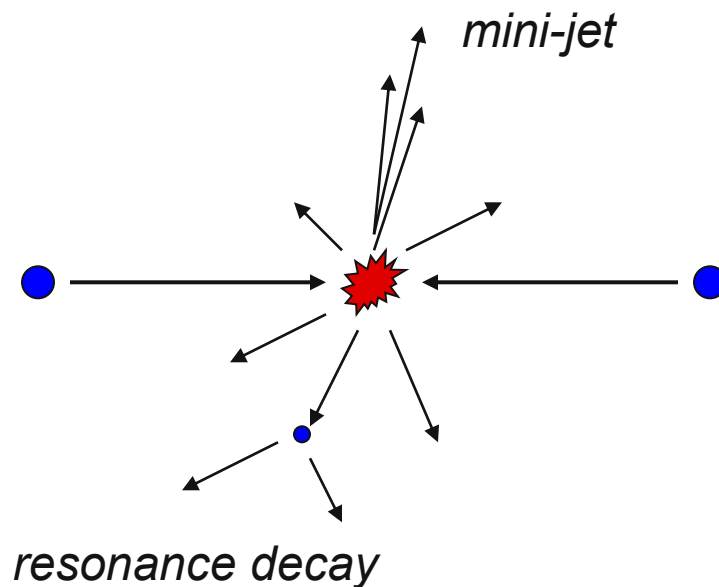
## Motivation: pp collisions

On top of statistical fluctuations there are dynamical sources of correlations, e.g. resonance decays, (mini-)jets, quantum correlations

Statistical fluctuations:



Dynamical fluctuations:

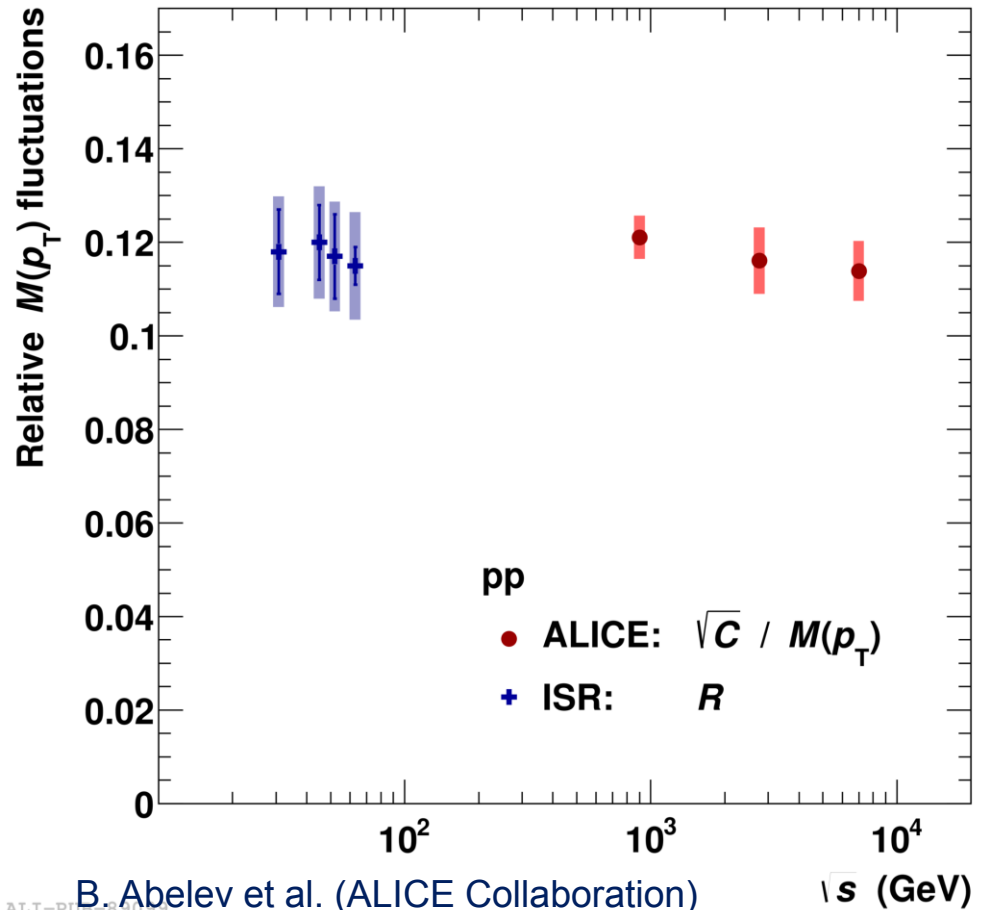


pp also interesting as reference measurement for heavy-ion collisions

# Results in pp collisions

## Inclusive results as a function of $\sqrt{s}$

- Significant dynamical fluctuations
- ALICE measures no significant dependence on collision energy
- Comparison to  $R$  measured at ISR [1]
- No significant dependence over a large range of collision energies



B. Abelev et al. (ALICE Collaboration)  
 Eur.Phys.J. **C74** (2014) 3077

[1] K. Braune *et al.*, Phys.Lett. **B123** (1983) 467

# Two-particle correlator

## As a function of multiplicity

- First measurement of non-statistical mean  $p_T$  fluctuations as a function of multiplicity in pp collisions!
- Differential studies can bring more insight in the origin of the fluctuations

$$C_m = \langle \Delta p_{T,i}, \Delta p_{T,j} \rangle_m = \frac{1}{\sum_{k=1}^{n_{ev}} N_k^{\text{pairs}}} \cdot \sum_{k=1}^{n_{ev}} \sum_{i=1}^{N_k} \sum_{j=i+1}^{N_k} (p_{T,i} - M(p_T)_m) \cdot (p_{T,j} - M(p_T)_m)$$

$C_m = 0$  for only statistical fluctuations

$$\frac{\sqrt{C_m}}{M(p_T)_m}$$

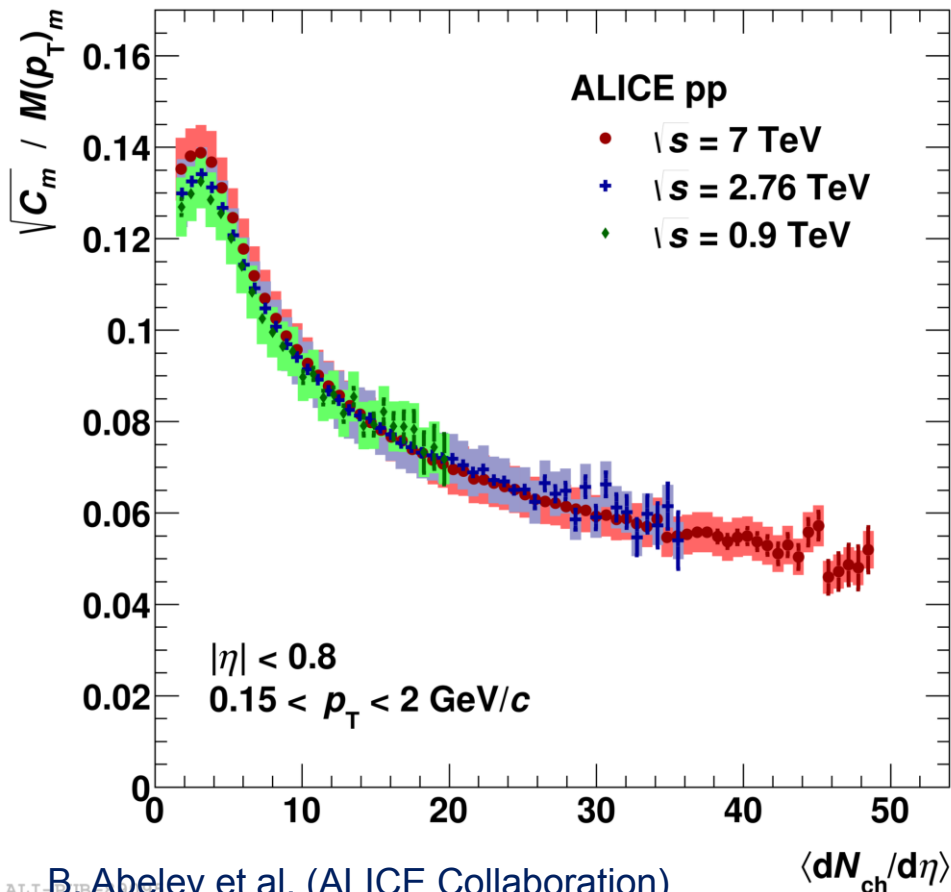
## Multiplicity determination

- Measured multiplicity  $N_{acc,k}$  = number of tracks in event  $k$  which survive the track selection criteria
- The two-particle correlator is calculated in intervals of  $\langle N_{acc} \rangle$
- Afterwards, the multiplicity axis is corrected to obtain  $\langle dN_{ch}/d\eta \rangle$ 
  - In Pb–Pb collisions: Linear relation between  $\langle N_{acc} \rangle$  and published ALICE  $\langle dN_{ch}/d\eta \rangle$
  - In pp collisions: Detector response matrix from MC simulation + unfolding procedure



# Results in pp collisions

As a function of the charged-particle multiplicity density



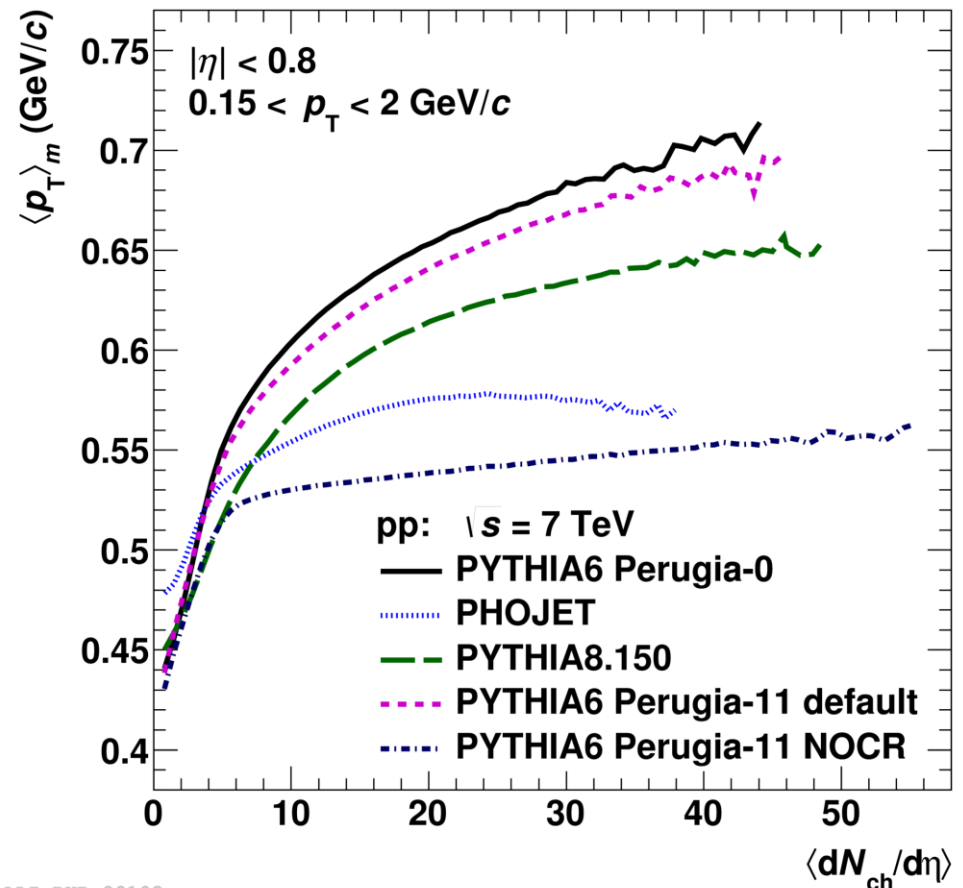
- Significant dynamical fluctuations
- Strong decrease with multiplicity
- Inclusive value of  $\approx 12\%$  has underlying structure
- No significant collision energy dependence

## Systematic uncertainties

- Most important contributions:
    - MC generator level versus MC reconstructed – up to 6%
    - Tracking scheme: TPC standalone versus TPC+ITS combined tracking – up to 5%
  - Further contributions:
    - Vertex position criteria and vertex calculation – up to 2%
    - Track selection criteria – up to 3%
- ⇒ **Data can be compared to MC generator level (i.e. theory without detector response) within the systematic uncertainties!**

# Monte Carlo event generators

- All Monte Carlo simulations performed on the generator level
- True  $\langle p_T \rangle$  is available!
- Color reconnections (CR) important to describe the increase with multiplicity, PYTHIA6 NOCR almost flat
- PHOJET also differs from the others (and from data)



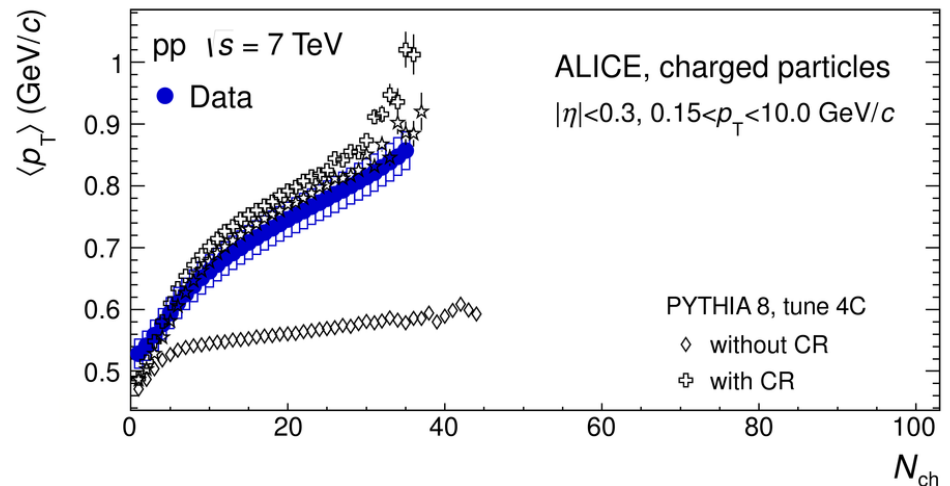
ALI-PUB-09103

B. Abelev et al. (ALICE Collaboration)  
 Eur.Phys.J. **C74** (2014) 3077

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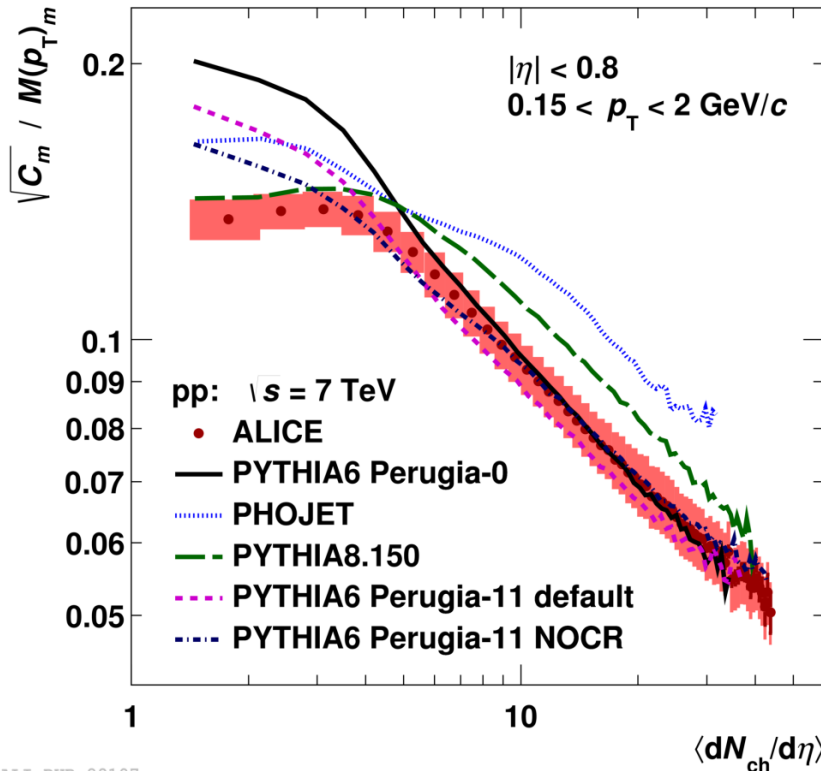
ALICE published  $\langle p_T \rangle$



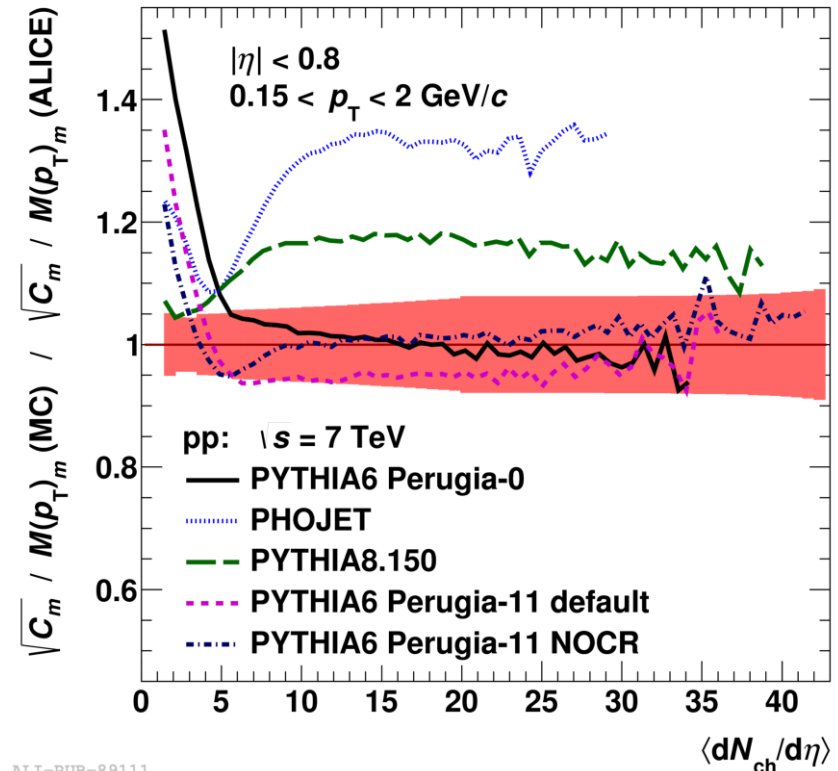
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 Phys.Lett. **B727** (2013) 371

# Results in pp collisions

## Comparison to Monte Carlo generators



ALI-PUB-89107

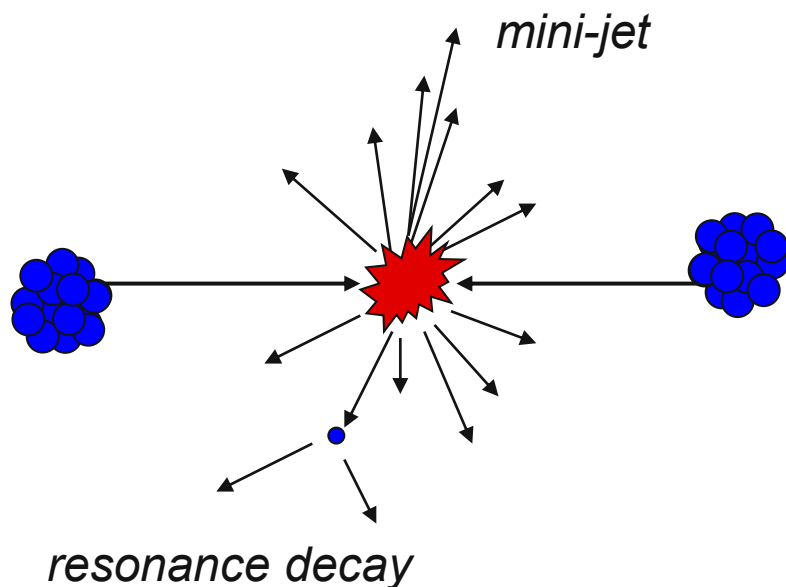


ALI-PUB-89111

- For  $\langle dN_{ch} / d\eta \rangle > 5$ :
- Reasonable description by most of the generators
  - Color reconnections have no influence on the slope!

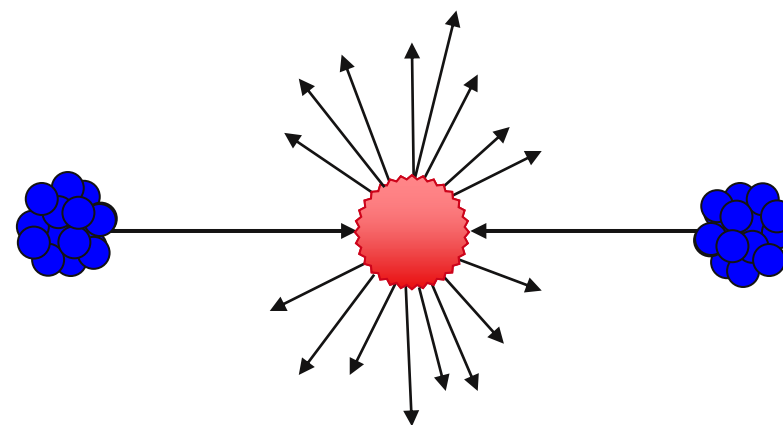
## Motivation: From pp to Pb–Pb collisions

Contributions also  
observed in pp collisions:



pp collisions important as  
reference measurement!

Contributions unique to  
heavy-ion collisions:

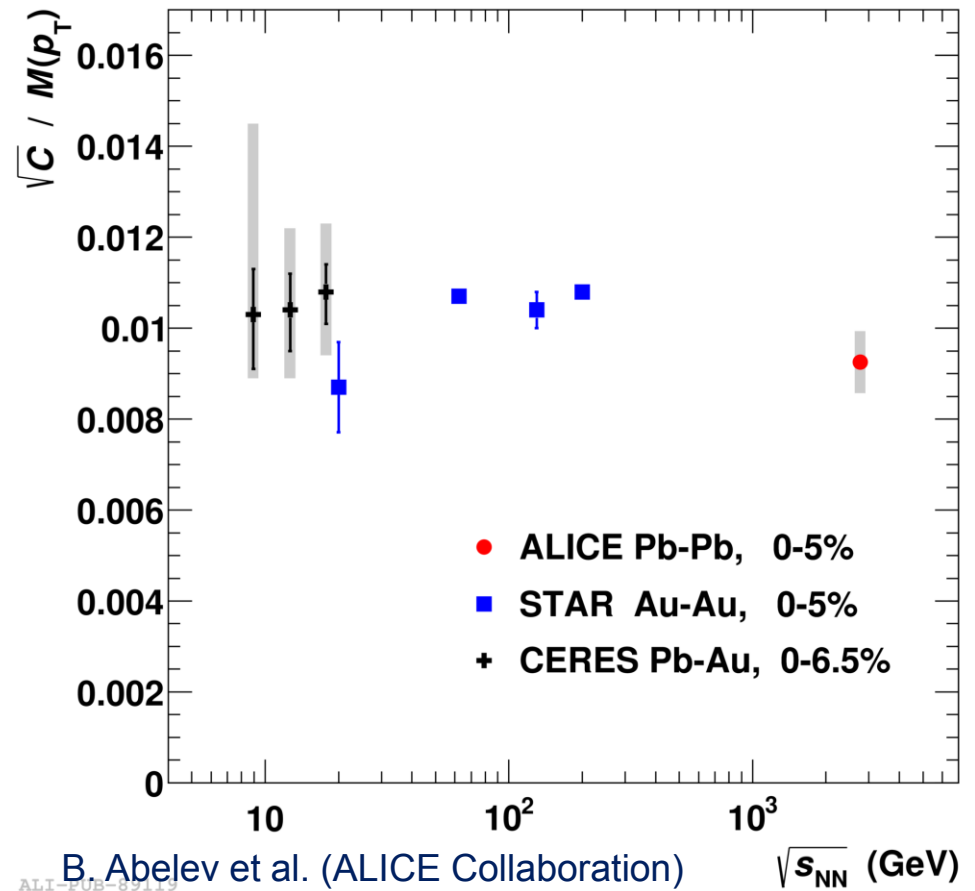


- Thermalization
- Collectivity
- Phase transitions
- Initial state fluctuations
- ...

# Results in Pb–Pb collisions

## Central A–A collisions as a function of $\sqrt{s}$

- Significant dynamical fluctuations
- Much smaller values than in pp
- Comparison to data from CERES [3] and STAR [4]
- No significant collision energy dependence



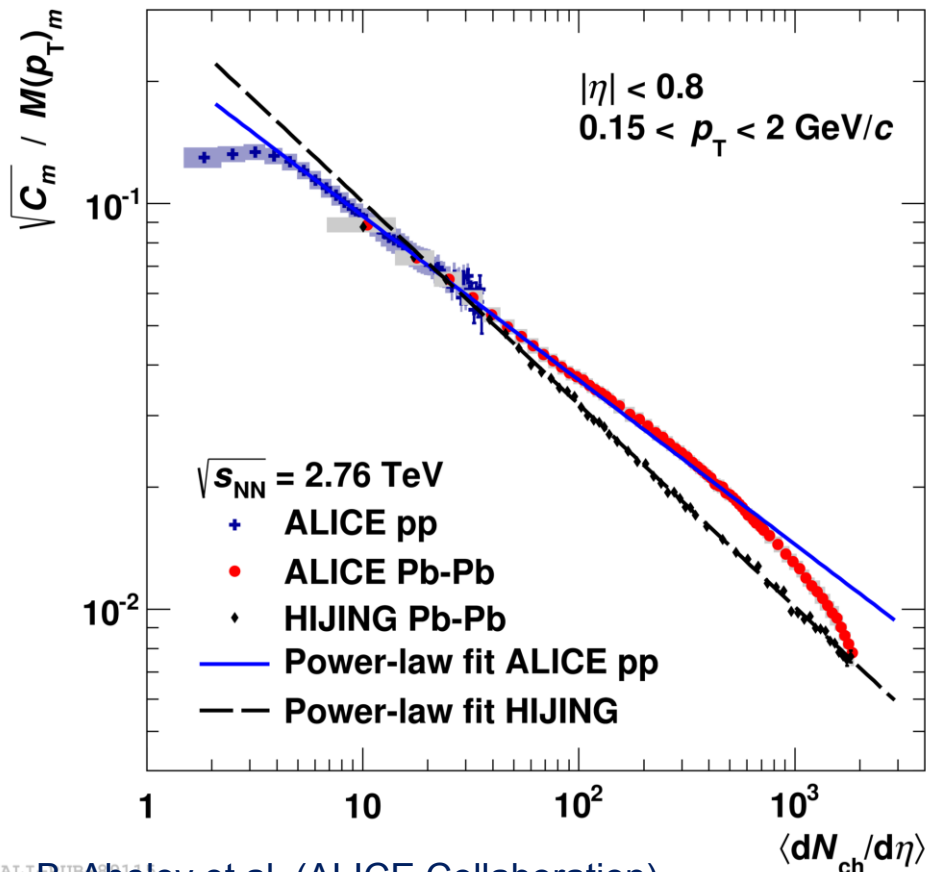
[3] D. Adamová *et al.*, Nucl.Phys. **A811** (2008) 179

[4] J. Adams *et al.*, Phys.Rev. **C72** (2005) 044902

B. Abelev *et al.* (ALICE Collaboration)  
Eur.Phys.J. **C74** (2014) 3077

# Results in Pb–Pb collisions

## Comparison to pp collisions as a function of the multiplicity



- Peripheral Pb–Pb in agreement with pp baseline:

$$\propto \langle dN_{ch} / d\eta \rangle^b$$

$$b = -0.405 \pm 0.002(\text{stat.}) \pm 0.036(\text{syst.})$$

- Deviation in central Pb–Pb

- Not described by HIJING:

$$b = -0.499 \pm 0.003(\text{stat.}) \pm 0.005(\text{syst.})$$

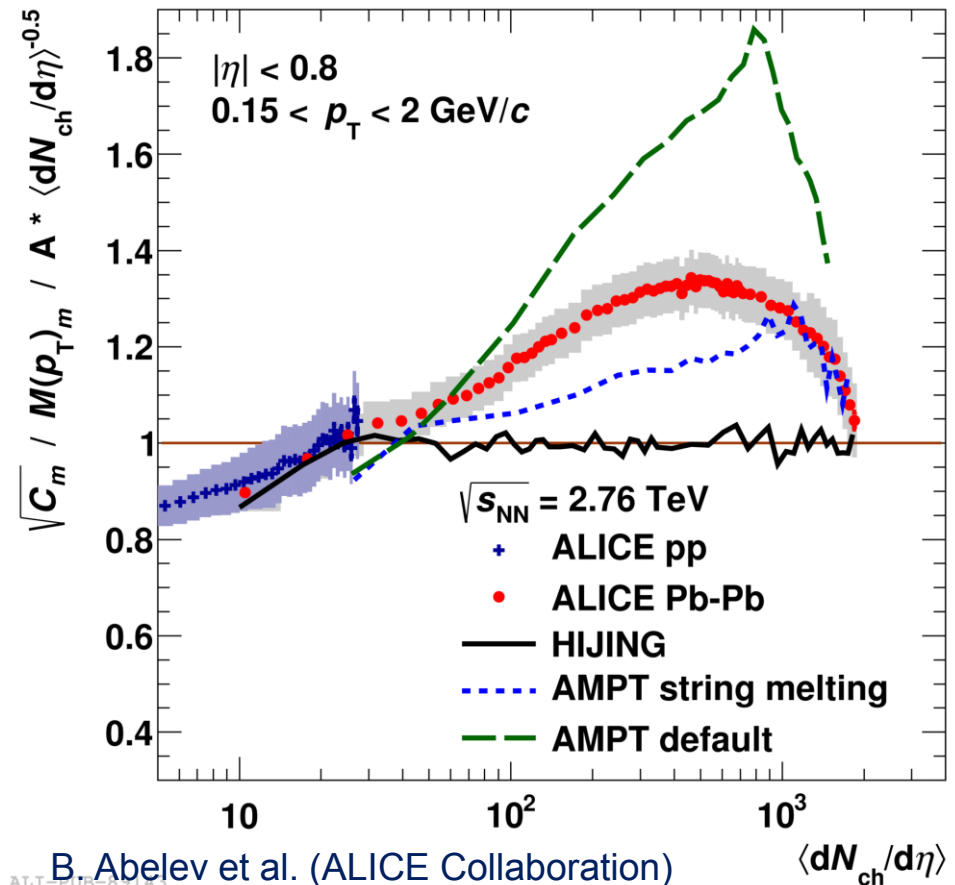
corresponds to simple superposition expectation



# Results in Pb–Pb collisions

## Comparison to Monte Carlo generators

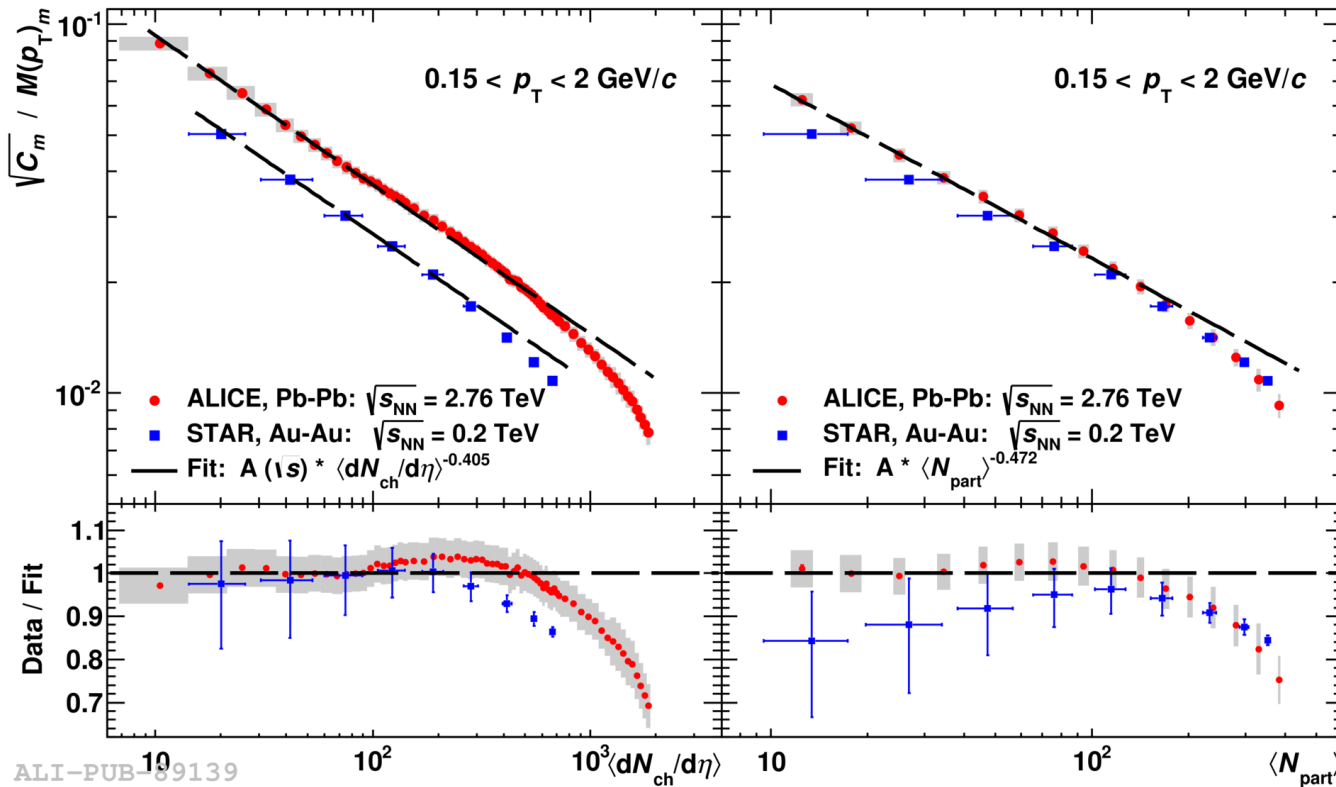
- HIJING shows behaviour  $\propto \langle dN_{\text{ch}} / d\eta \rangle^{-0.5}$  and cannot describe the data
- AMPT (includes collective effects) both versions:
  - Increase above simple superposition expectation
  - Decrease towards central events
  - Fail in terms of absolute values



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# Results in Pb–Pb collisions

## Comparison to STAR [4] results in Au–Au collisions



Left:

Power of fits from ALICE pp:

$$\langle dN_{ch} / d\eta \rangle^{-0.405}$$

Right:

In terms of  $\langle N_{part} \rangle$

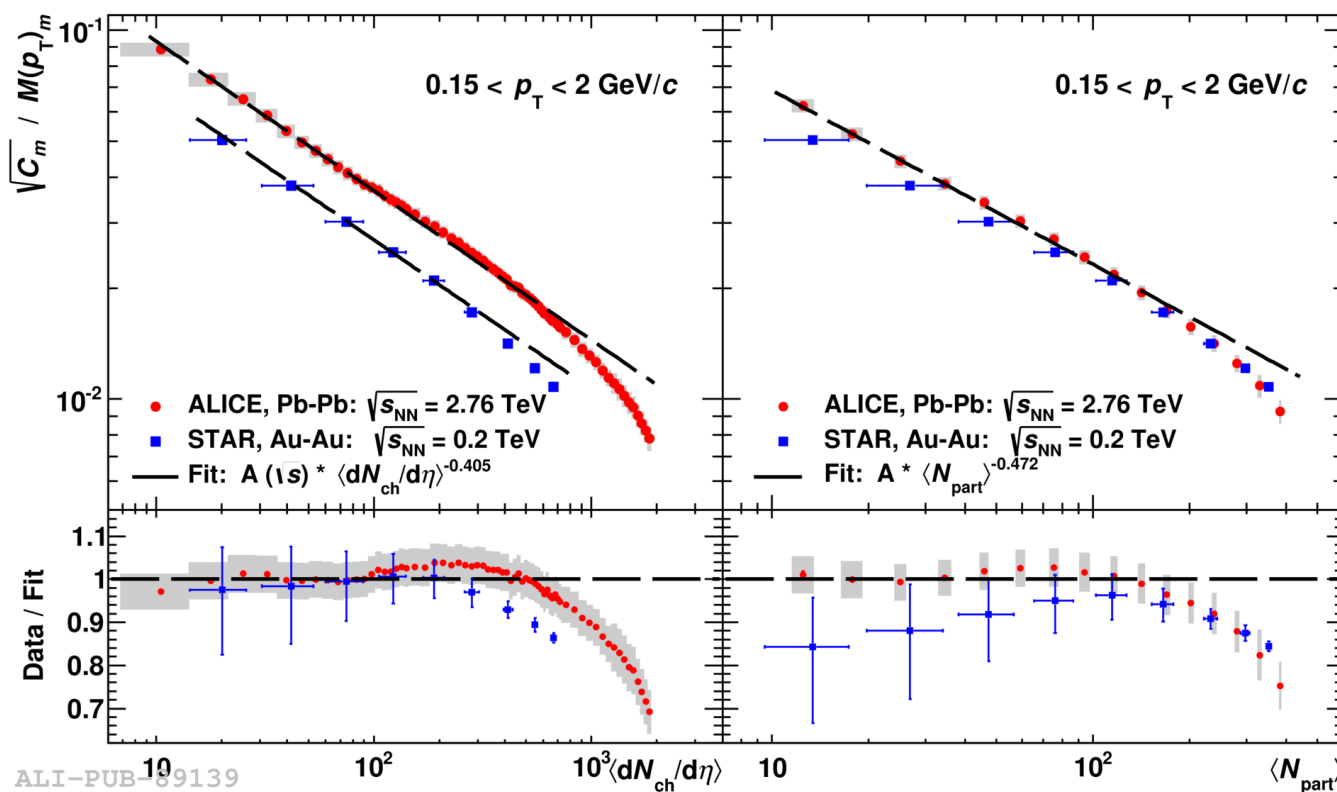
Deviation from fit at same centrality

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[4] J. Adams et al., Phys.Rev. **C72**  
 (2005) 044902

# Results in Pb–Pb collisions – going back to pp!



Left:

scaling with  
multiplicity density

$$\langle dN_{ch} / d\eta \rangle$$

Right:

scaling with number  
of participants

$$\langle N_{part} \rangle$$

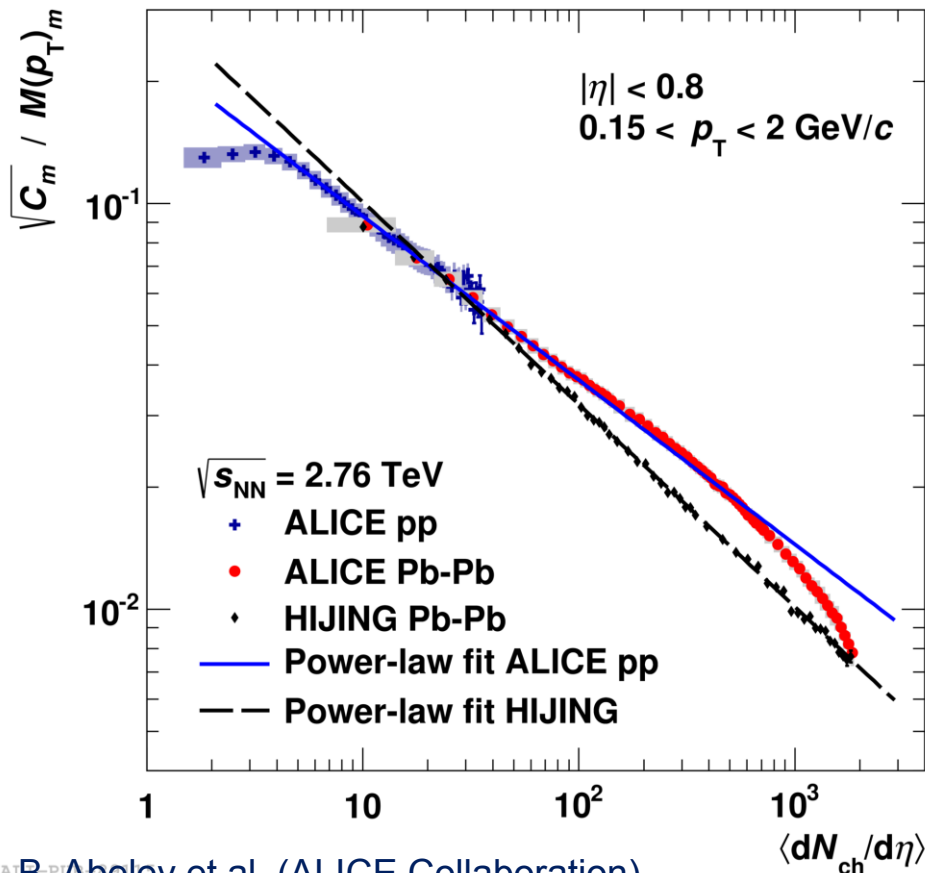
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[4] J. Adams et al., Phys.Rev. **C72**  
(2005) 044902

**Naive expectation in pp:  
Single point at  $N_{part} = 2$**

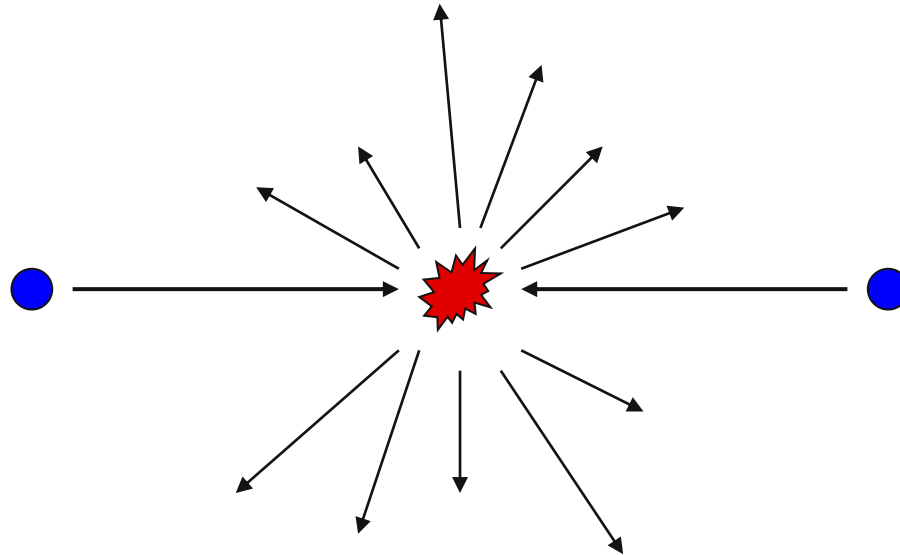
# Recap: Comparison of pp and Pb–Pb



- Results for pp collisions indeed scale with multiplicity
- Good agreement of pp and peripheral Pb–Pb collisions

$\Rightarrow$  If dependence in Pb–Pb is understood as superposition of  $N_{part}$ , what is it in pp?

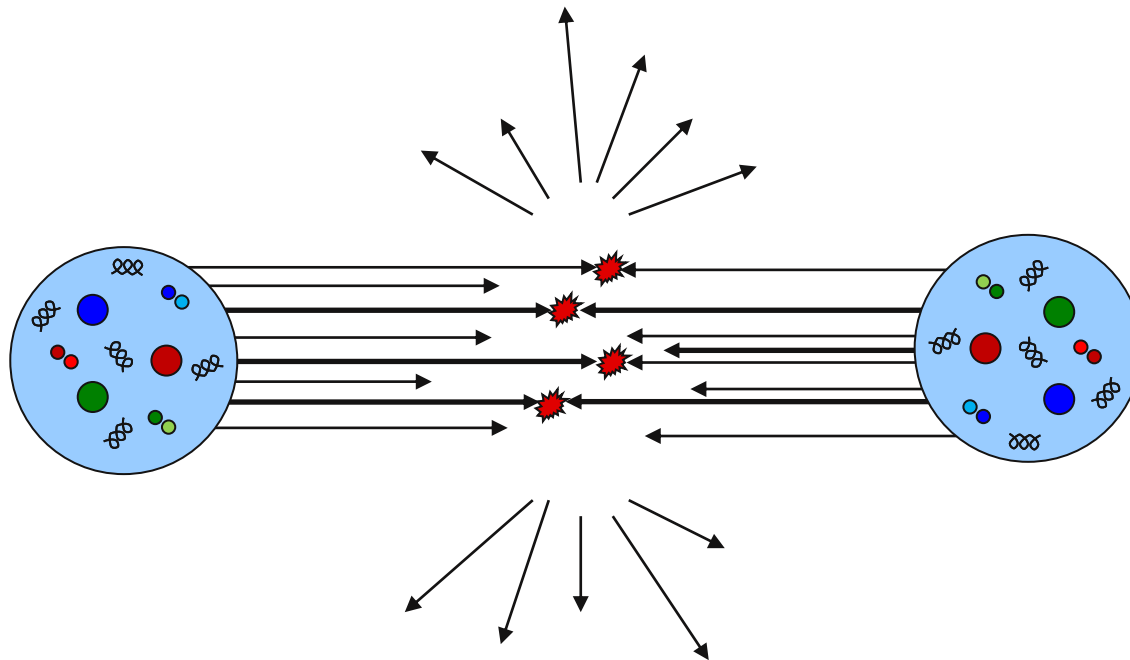
## pp in detail: multi-parton interactions



At low collision energies:

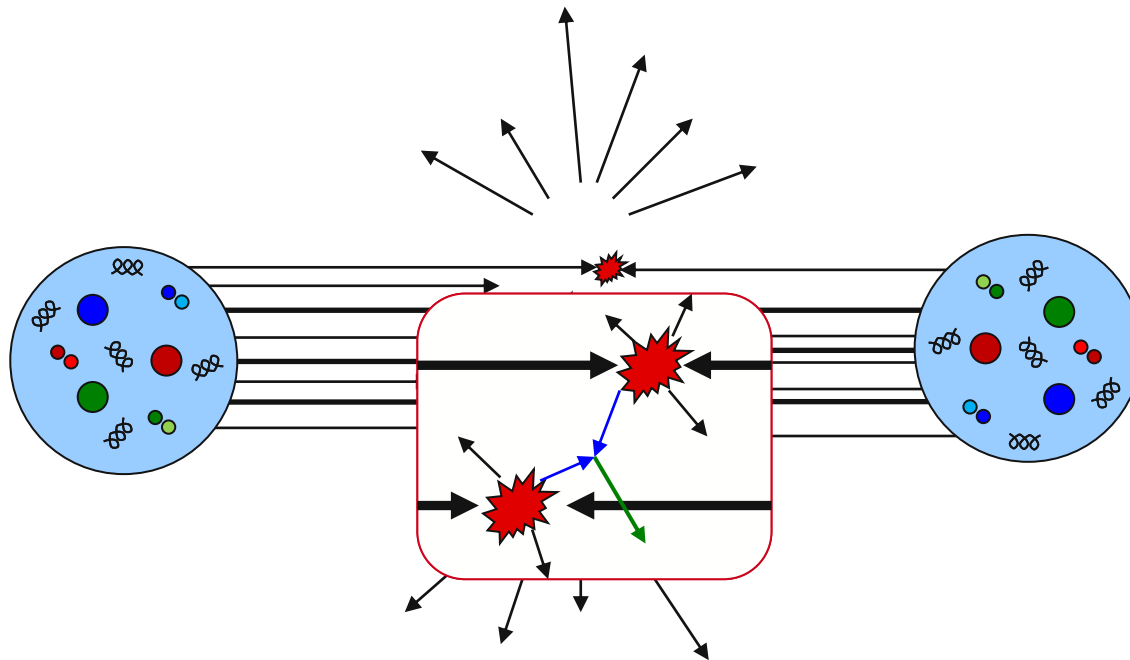
proton-proton collision = **1 nucleon-nucleon collision**

## pp in detail: multi-parton interactions



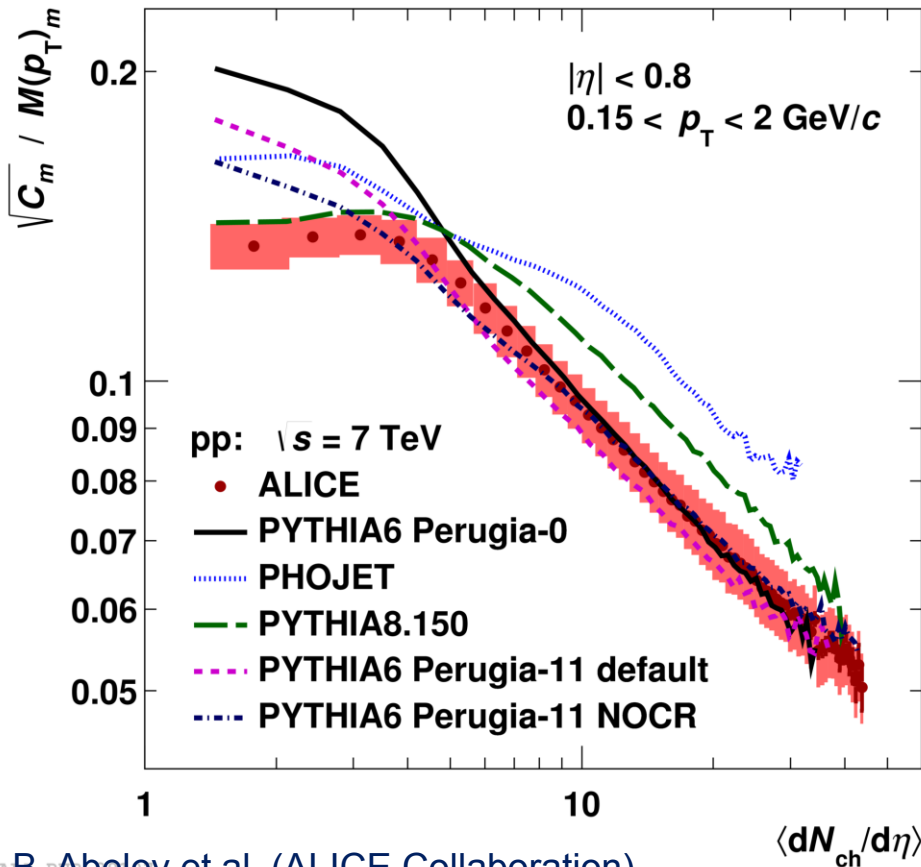
At high collision energies, reached at the LHC:  
proton-proton collision = **multiple parton-parton interactions (MPI)**

# pp in detail: multi-parton interactions



At high collision energies, reached at the LHC:  
 proton-proton collision = multiple parton-parton interactions (MPI)  
 → particles from different scattering centers can recombine via  
**color reconnections (CR)**

## Recap: Comparison to Monte Carlo studies



- Reasonable description by the PYTHIA generators (all with MPIs)
- Worst description by PHOJET (no MPIs)
- Color reconnections have no influence on the slope!

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# Monte Carlo simulations

## With multi-parton interactions (MPIs)

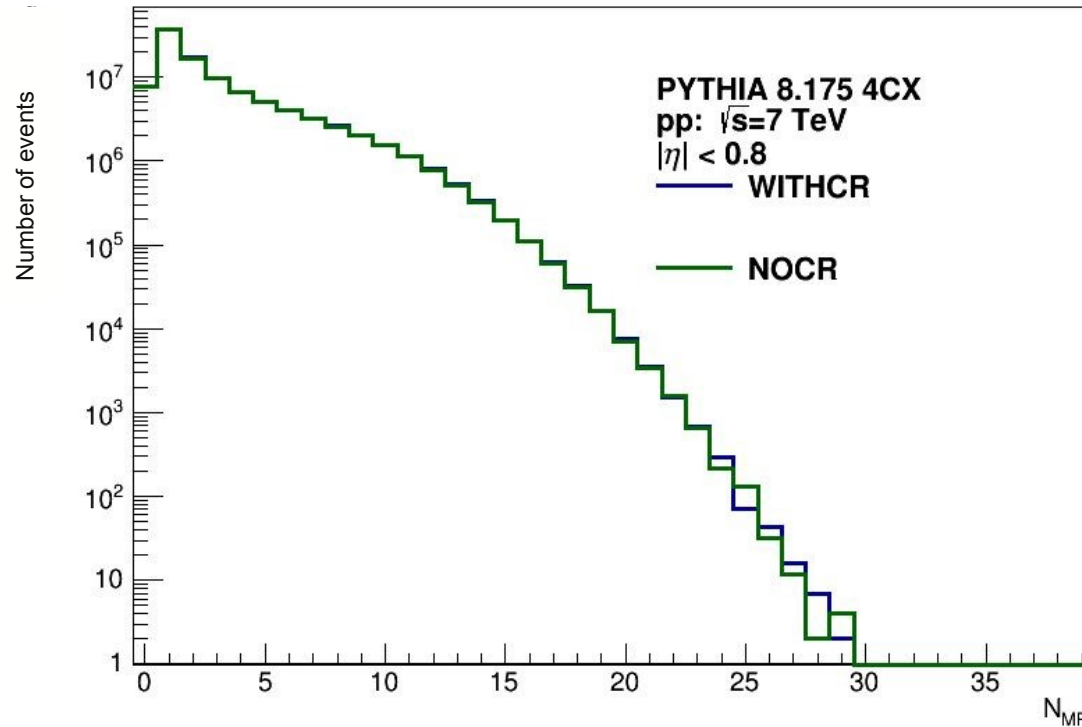
Bachelor Thesis by  
Bernhard Schütz

- MC generator: PYTHIA 8.175
- MC tune: 4CX
- Pure MC generator level, no ALICE detector simulation
- Two simulations with 100 M events each:
  - Default tune 4CX including Color Reconnections (WITHCR)
  - Modified version without Color Reconnections (NOCR)\*
- MPIs are included in PYTHIA and important for the creation of high multiplicity pp events

\*Note: CR has just been switched off, this is not a complete tune.  
Results are of qualitative nature only.

# Basic distributions I

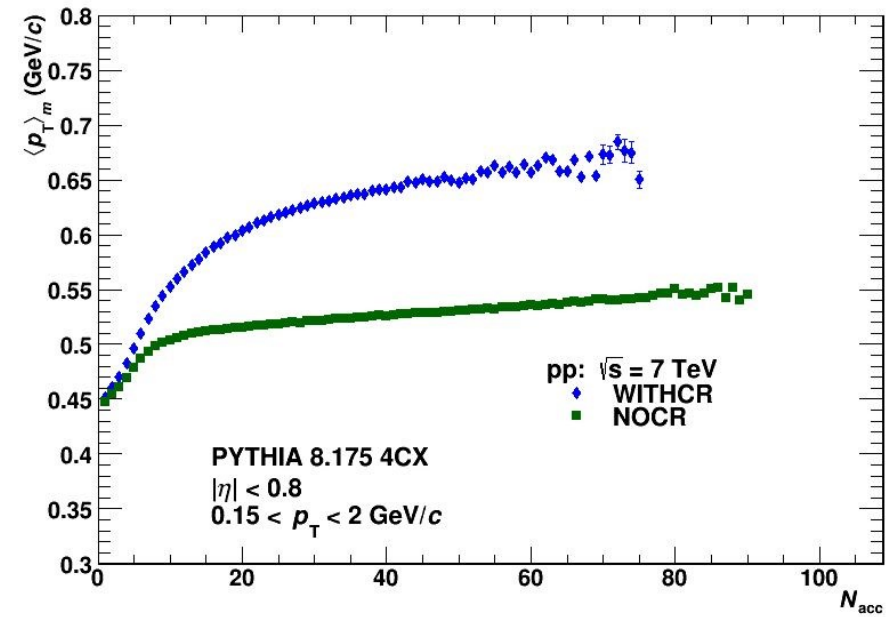
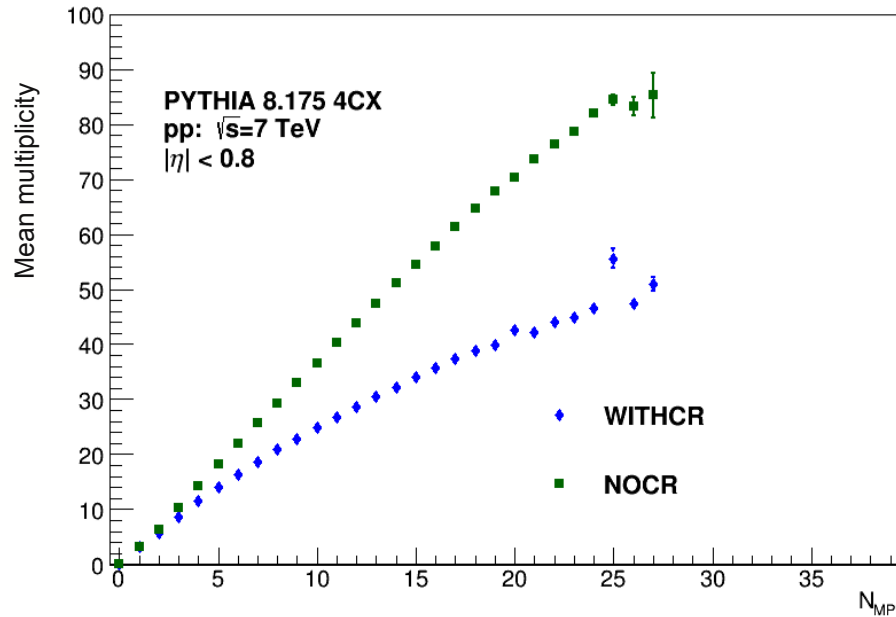
## Number of events versus number of parton-parton interactions



- $N_{MPI}$  = Number of Multi-Parton Interactions
- Peak at  $N_{MPI} = 1$  (about 35%), maximum at  $N_{MPI} \approx 30$

# Basic distributions II

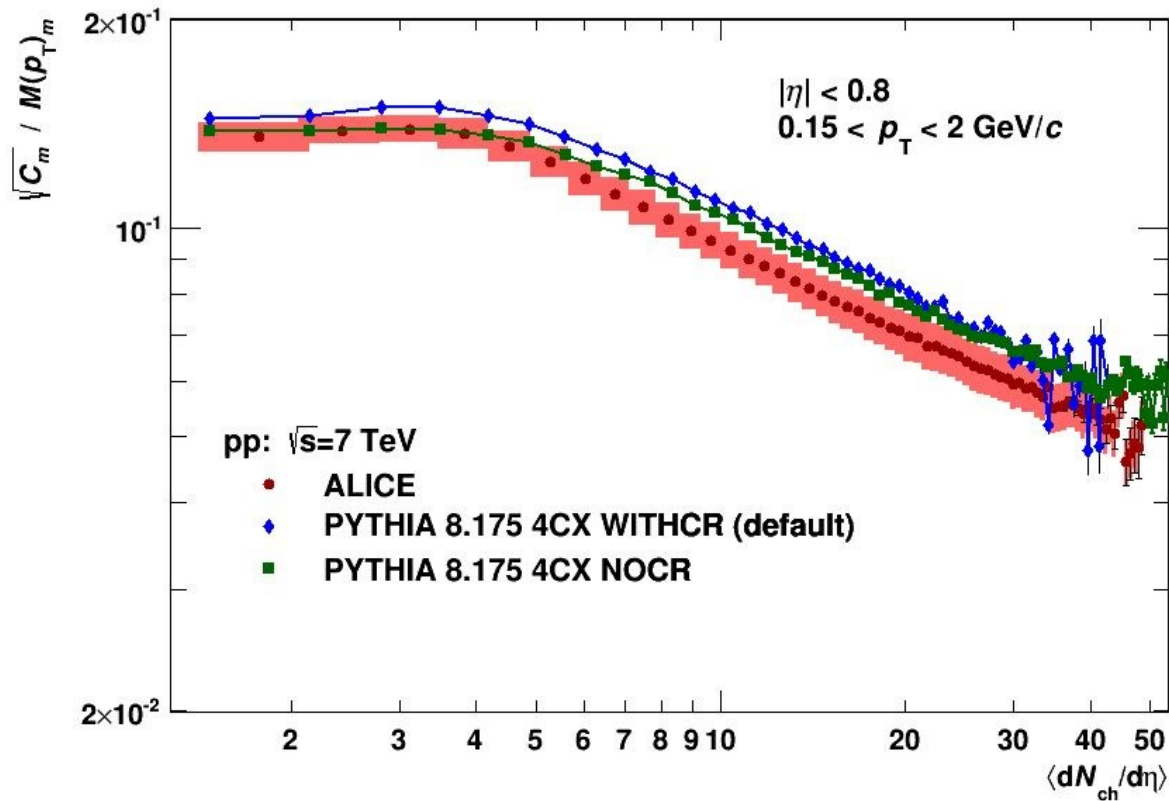
## Mean multiplicity versus $N_{\text{MPI}}$ and mean $p_T$ versus multiplicity



- As expected, the mean multiplicity increases with  $N_{\text{MPI}}$
- Multiplicities are larger in the NOCR scenario

- $\langle p_T \rangle$  increases with multiplicity in WITHCR and is almost flat in NOCR
- WITHCR consistent with data

# Results for relative dynamical fluctuations

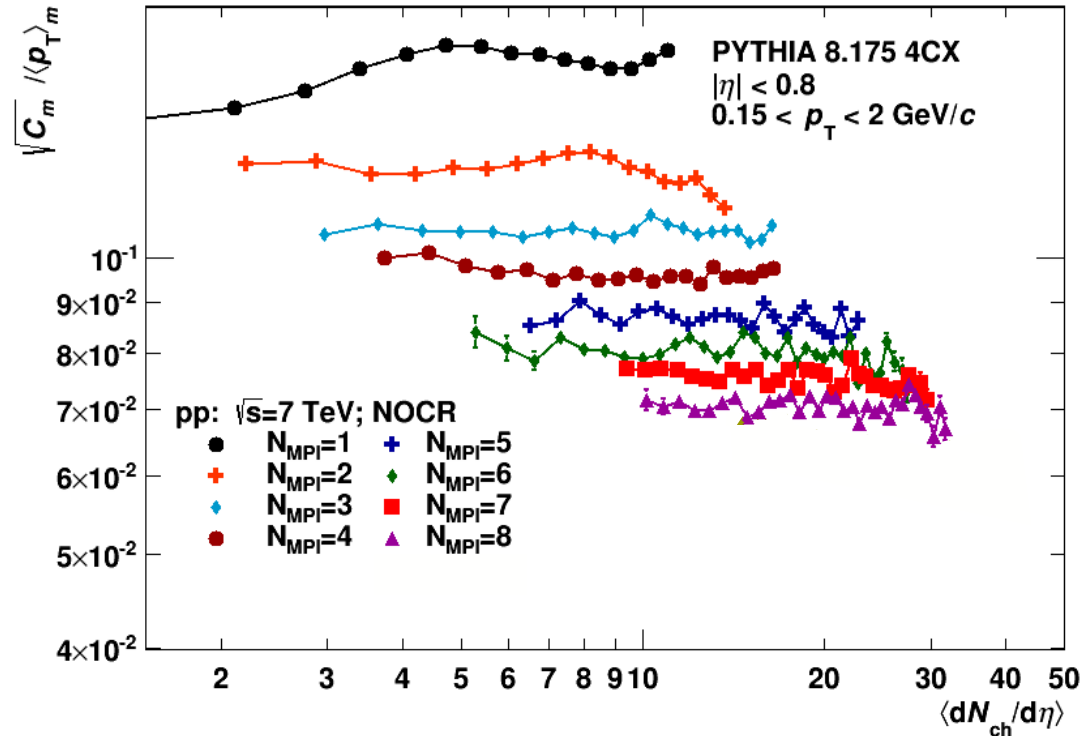


ALICE data from:  
 B. Abelev et al.  
 Eur.Phys.J. **C74** (2014) 3077

- Results show similar behavior as ALICE data
- Can we learn more in an  $N_{MPI}$ -dependent analysis?

# Results for relative dynamical fluctuations

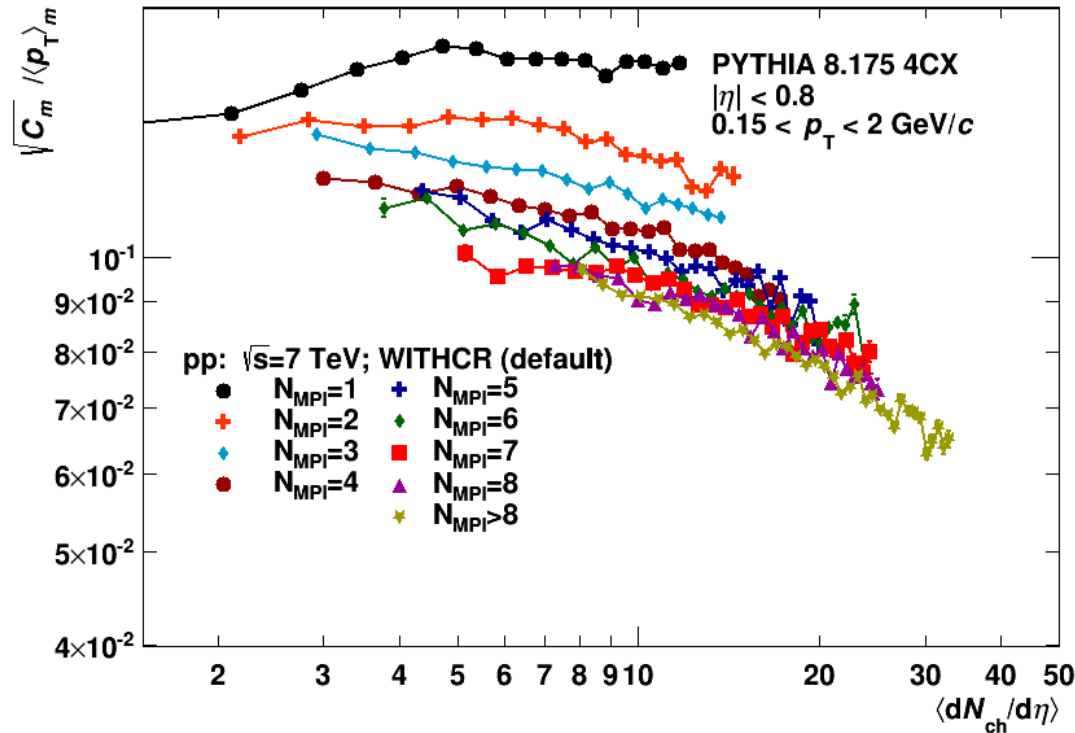
## Detailed analysis without color reconnections (NOCR)



- All samples almost flat as a function of multiplicity
- Parton-parton interactions = independent sources of particle production

# Results for relative dynamical fluctuations

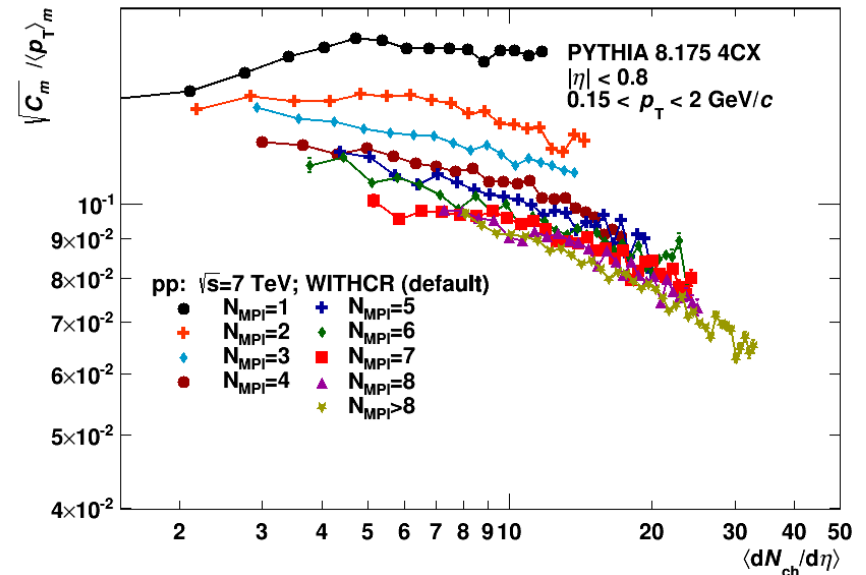
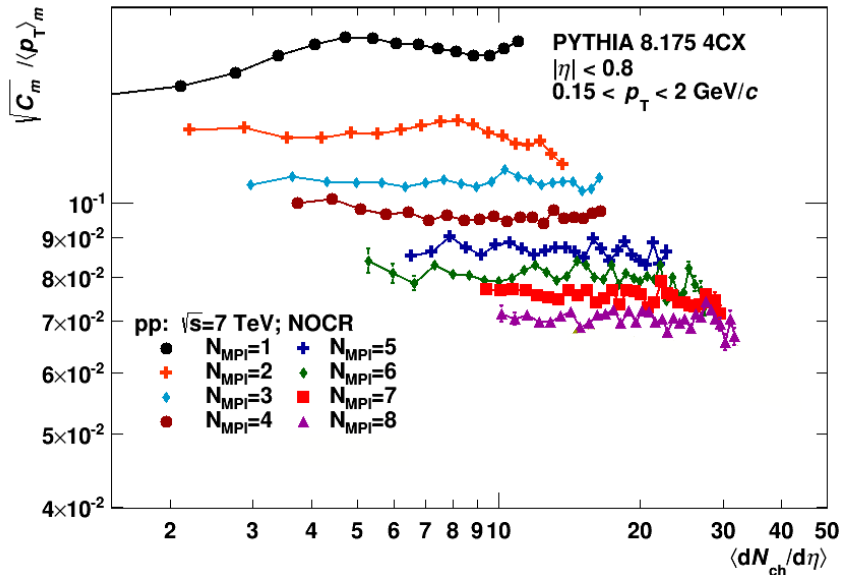
## Detailed analysis with color reconnections (WITHCR)



- $N_{MPI} = 1$ : almost flat as a function of multiplicity
- $N_{MPI} > 1$ : decreasing trend with increasing multiplicity, getting more pronounced for higher  $N_{MPI}$ , not independent anymore!

# Results for relative dynamical fluctuations

## Comparison of NOCR and WITHCR



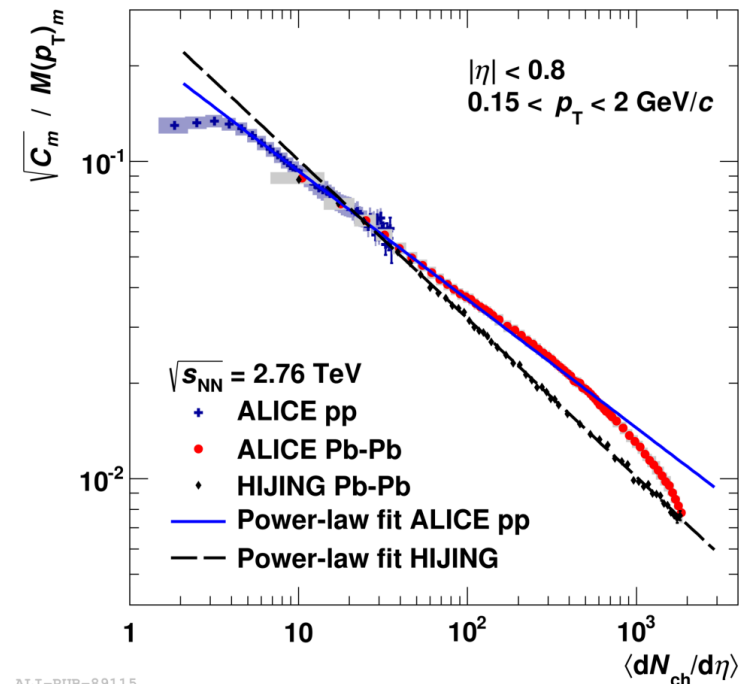
- Independent sources of particle production
- Flat as a function of multiplicity

- Sources of particle production not independent
- Decreasing trend with multiplicity

⇒ Integrated observables comparable, experimentally not distinguishable

## Conclusions

- Event-by-event mean  $p_T$  fluctuations measured by ALICE
- Observable: Two-particle correlator
- Significant dynamical fluctuations decreasing with multiplicity
- No significant energy dependence
- Peripheral Pb–Pb agrees with a pp extrapolation, central Pb–Pb deviates
- Monte Carlo generators describe pp rather well, Pb–Pb is not described as well
- MC studies with MPIs: Interesting differences with and without color reconnections



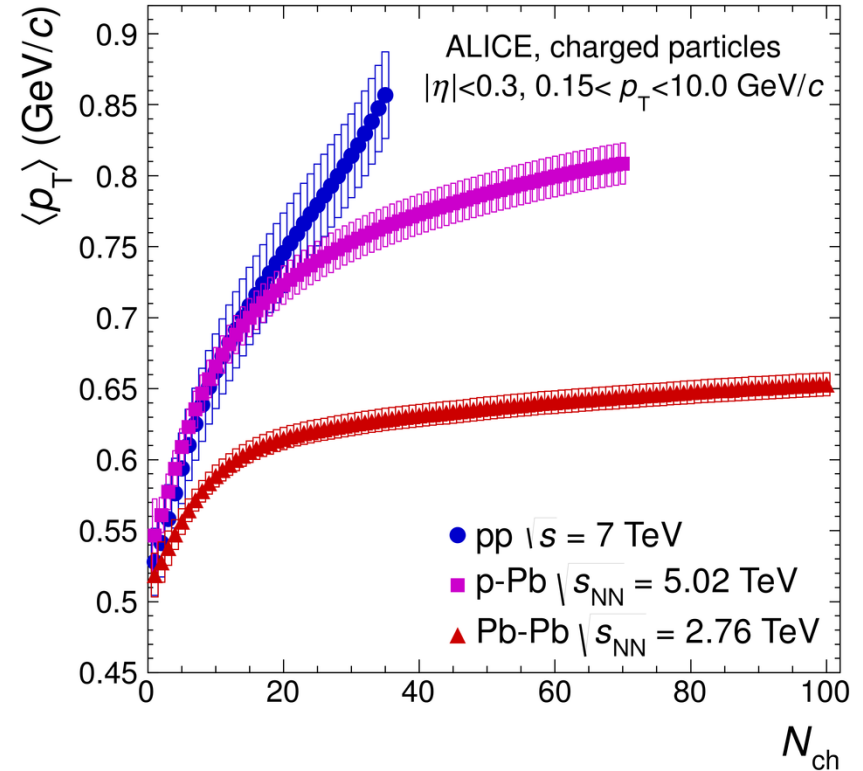
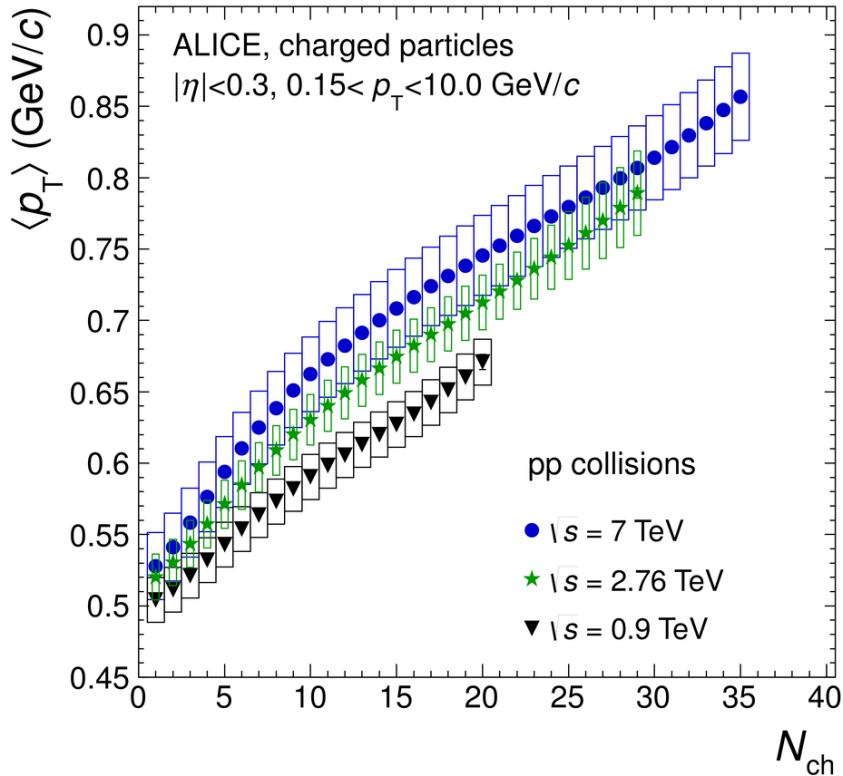
ALI-PUB-89115

B. Abelev et al. (ALICE Collaboration)  
 Eur.Phys.J. **C74** (2014) 3077



# BACKUP

# Mean transverse momentum – ALICE published

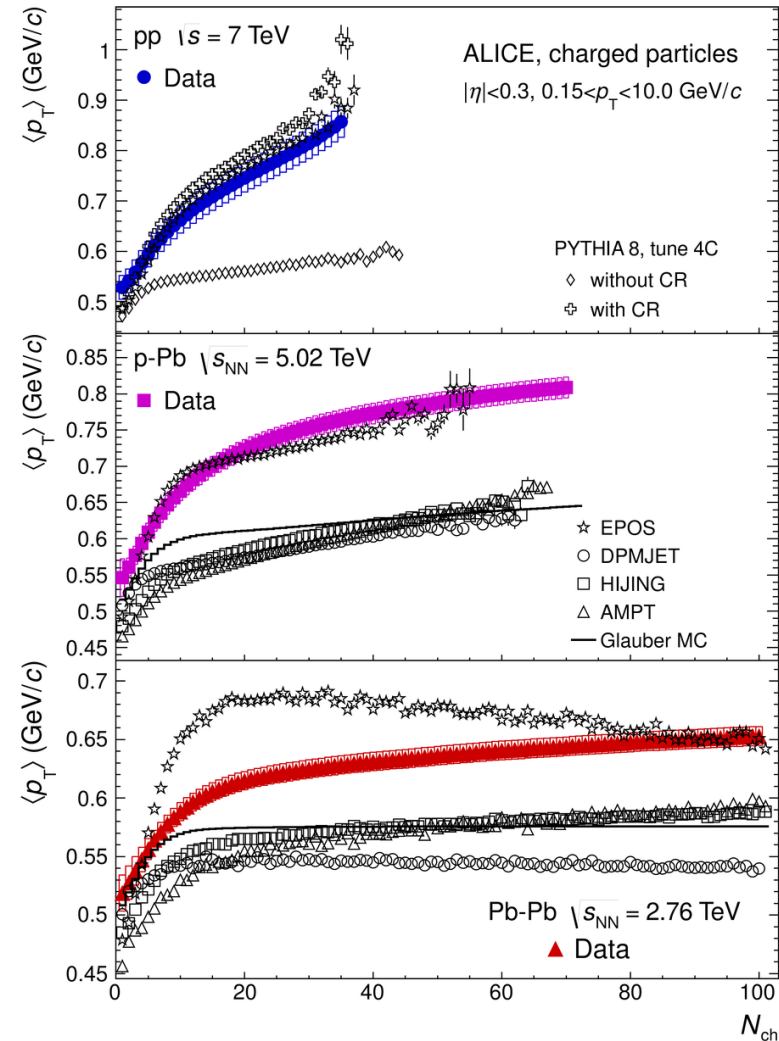


B. Abelev et al. (ALICE Collaboration)  
 Phys.Lett. **B727** (2013) 371

# Mean transverse momentum – ALICE published

- Comparison of pp, p–Pb and Pb–Pb data to several Monte Carlo simulations
- Color reconnections needed to describe the increase of  $\langle p_T \rangle$  with multiplicity in pp

B. Abelev et al. (ALICE Collaboration)  
 Phys.Lett. **B727** (2013) 371



## Event and track selection

### Event selection:

- Minimum bias trigger
- Maximum distance of the vertex to the nominal position in beam direction
- ...

### Track selection:

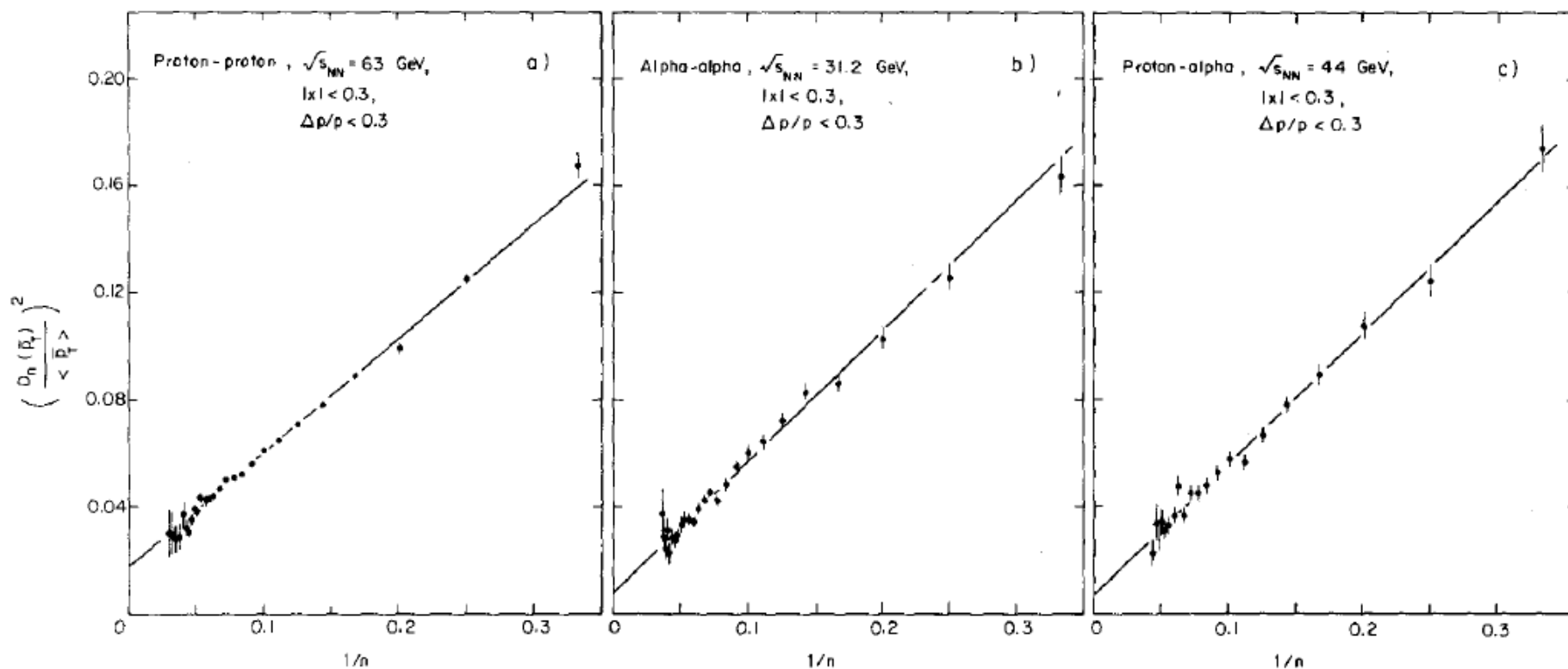
- Minimum number of clusters in the TPC
- Maximum  $\chi^2$  per space point in the TPC
- Restriction of the distance to closest approach to the primary vertex along the beam and in the transverse plane
- Pseudorapidity range:  $|\eta| < 0.8$
- Transverse momentum range:  $0.15 < p_T < 2 \text{ GeV}/c$
- ...

# Systematic uncertainties

Complete list of systematic uncertainties:

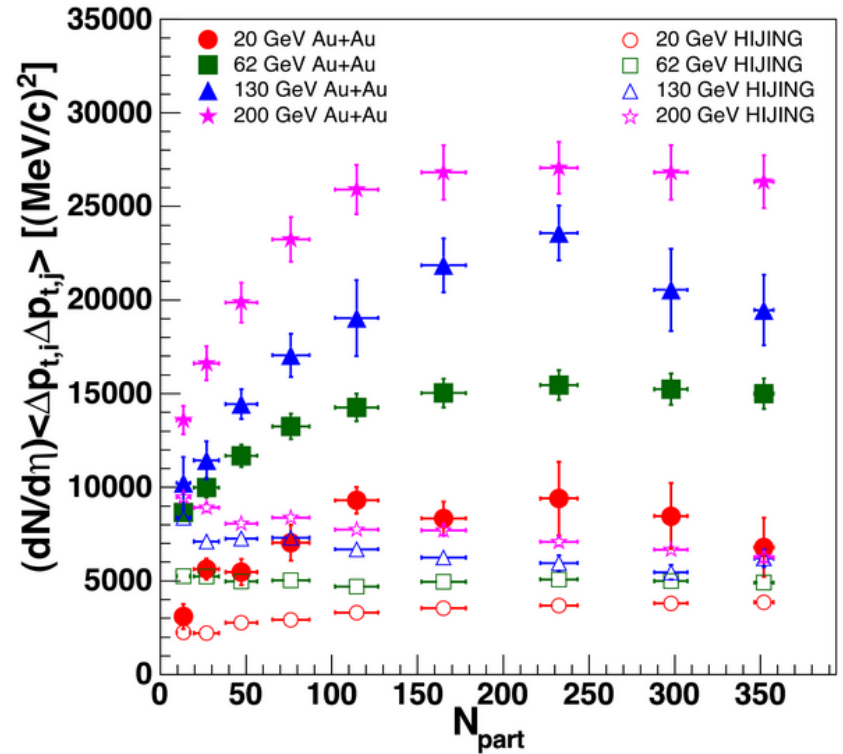
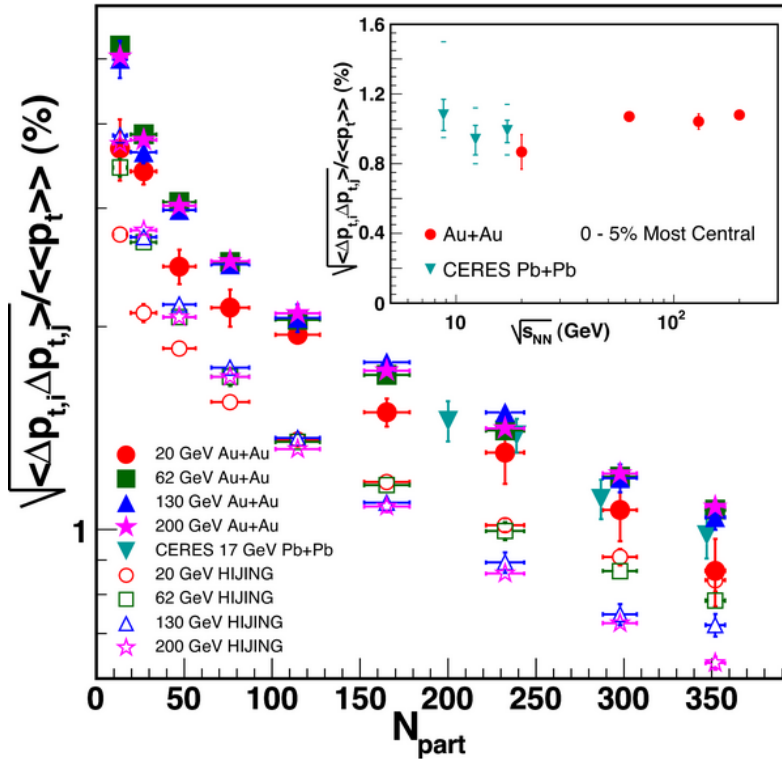
Collision system $\sqrt{s_{NN}}$	pp 0.9 TeV	pp 2.76 TeV	pp 7 TeV	Pb–Pb 2.76 TeV
Vertex $z$ -position cut	0–0.5 %	<0.1 %	<0.1 %	0.5–1 %
Vertex calculation	0–2 %	0.5–2 %	0.5–2 %	<0.1 %
Vertex difference cut	0–1.5 %	0–3 %	0–2 %	0–2 %
Min. TPC space points	1.5–3 %	1–2 %	1–3 %	2–3 %
TPC $\chi^2$ / d.o.f.	<0.1 %	<0.1 %	<0.1 %	<0.1 %
DCA to vertex	1 %	1–1.5 %	0.5–1 %	0.5–1 %
B-field polarity	0.5 %	0.5 %	0.5 %	0.5 %
Centrality intervals	–	–	–	1–3 %
TPC-only vs. hybrid	4 %	4 %	4 %	1–5 %
MC generator vs. full sim.	0–6 %	0–6 %	0–6 %	0–4 %
<b>Total</b>	<b>4.4–7.7 %</b>	<b>4.4–7.6 %</b>	<b>4.4–7.9 %</b>	<b>4.2–7.4 %</b>

# The dispersion measured at the ISR



[1] K. Braune *et al.*, Phys.Lett. **B123**  
(1983) 467

# The two-particle correlator measured by STAR



[4] J. Adams *et al.*, Phys.Rev. **C72** (2005) 044902