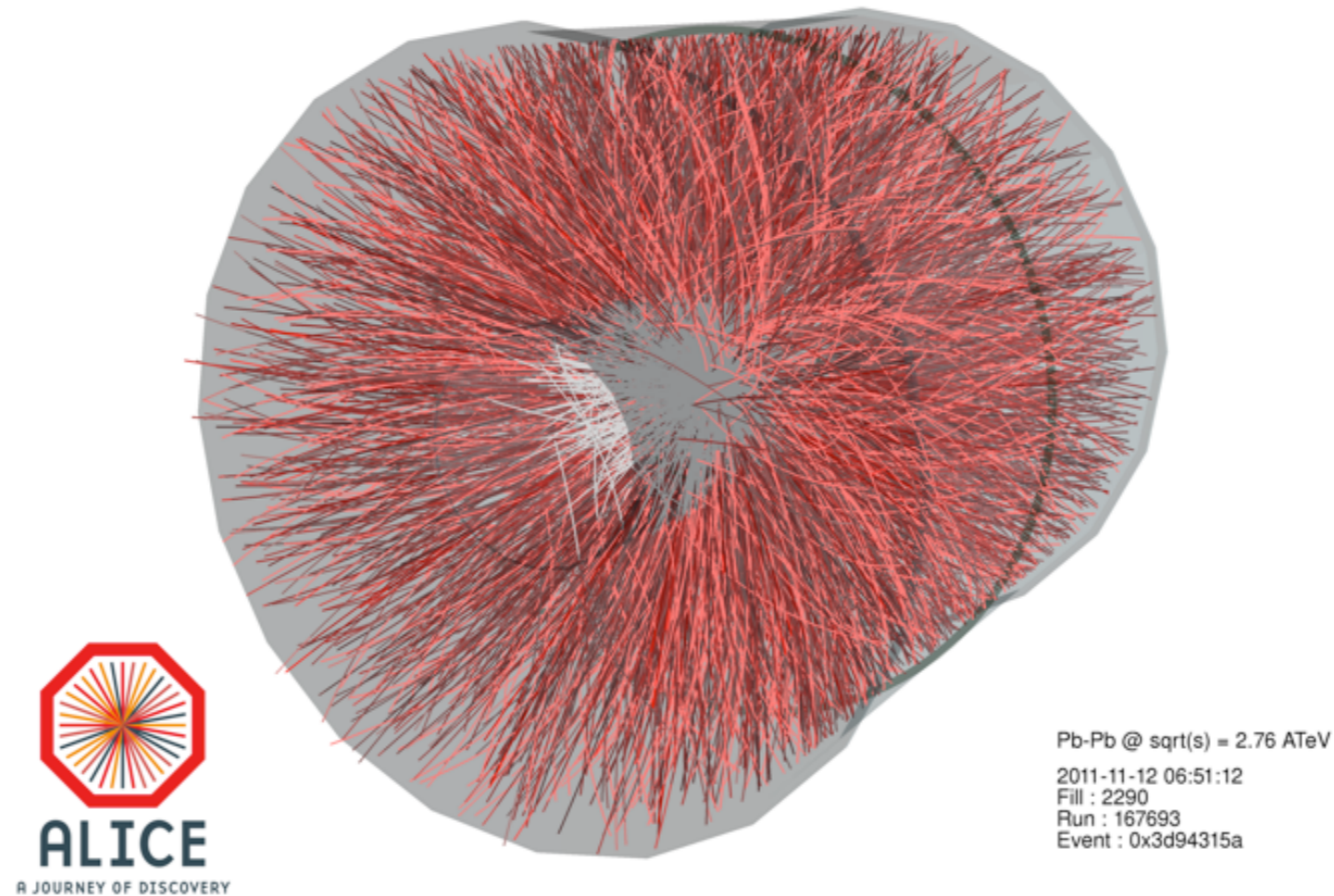


Measurement of event-by-event fluctuations and chemical freeze-out conditions at LHC energies with ALICE

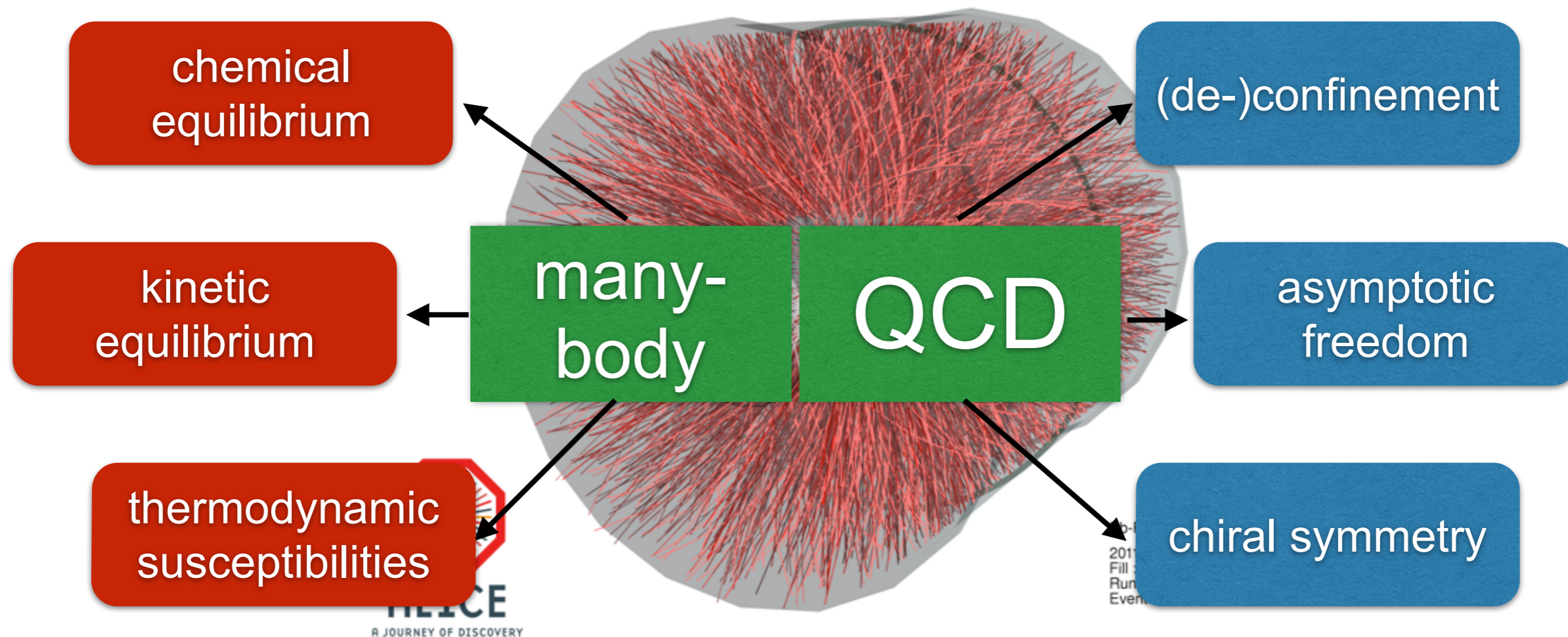
A. Kalweit, *CERN*
on behalf of the ALICE collaboration

Many-body QCD and light flavor hadron production



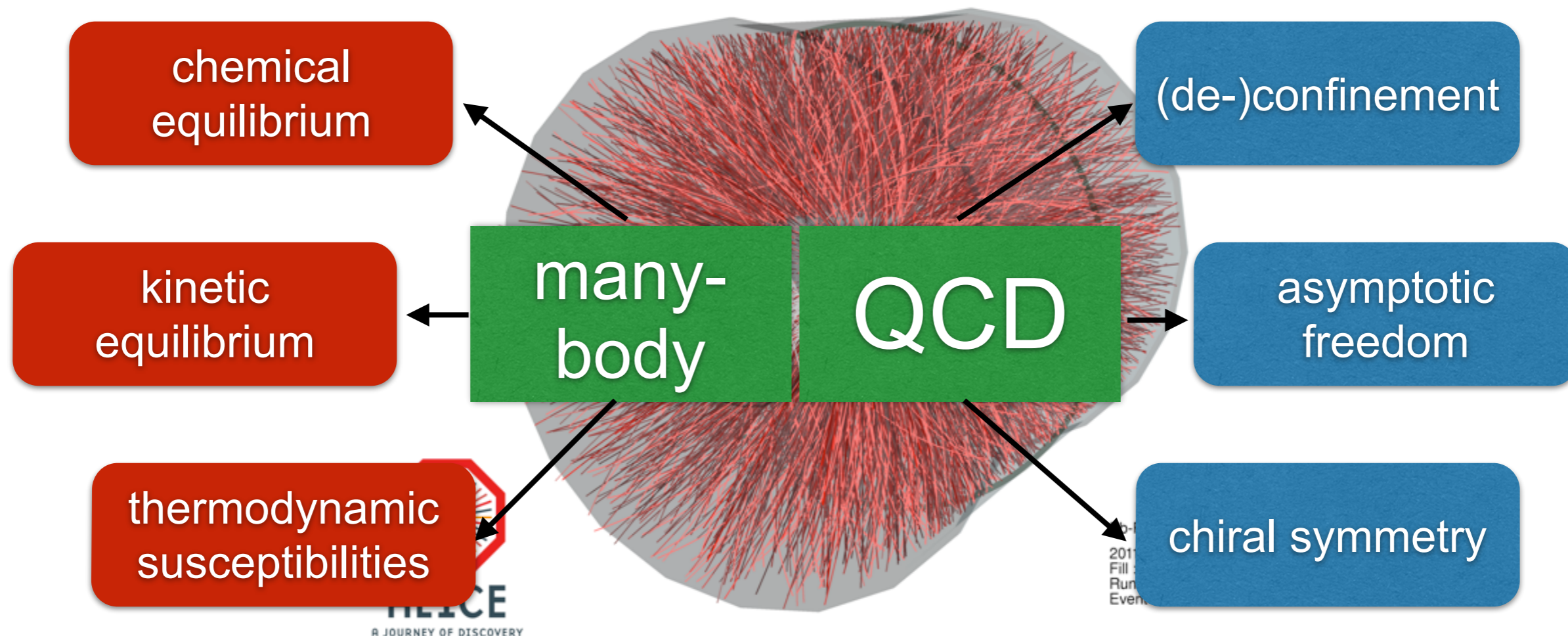
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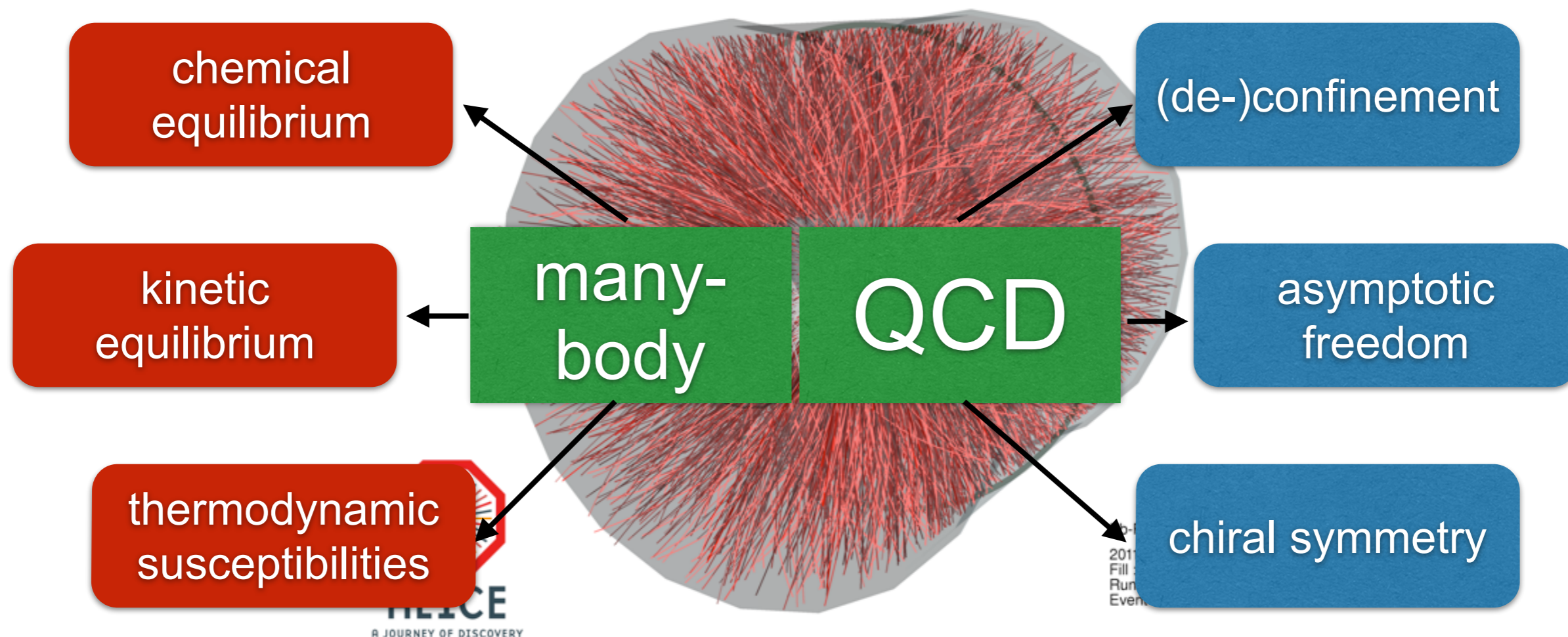
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98% of all particles are produced with $p_T < 2$ GeV/c \rightarrow thermal particle production in a non-perturbative regime
 \Rightarrow **thermodynamics**
 \Rightarrow **LATTICE QCD** calculations

Introduction (1)

- Measurement of the production *yields* of identified particles and chemical freeze-out conditions:
 - Hadron resonance gas approach in thermal-statistical *models*

- Measurement of event-by-event *fluctuations* of conserved quantities:
 - net-charge fluctuations
 - plans for future measurements
 - allows direct comparison of measurements to ab initio calculations

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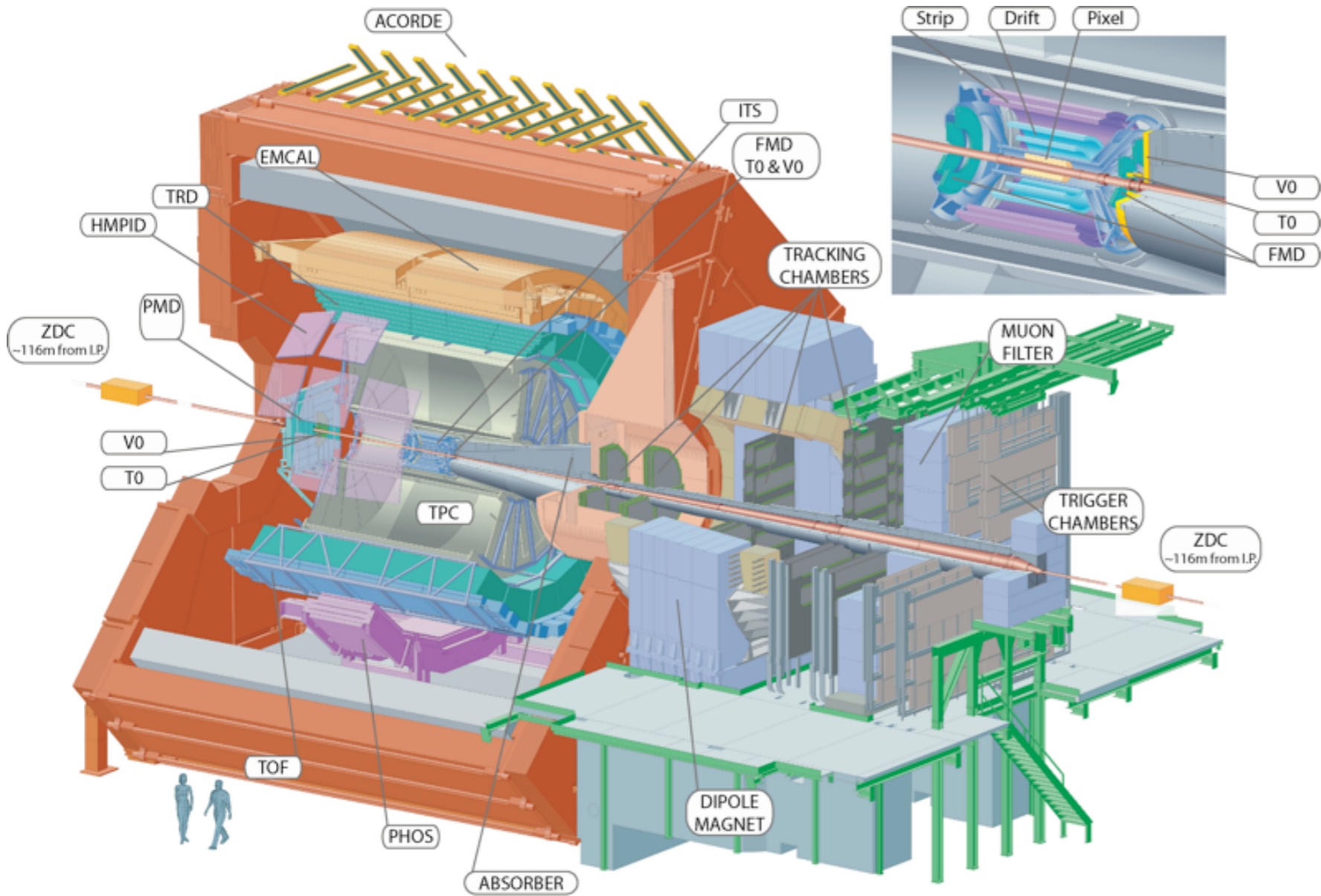
Very sensitive to critical behavior.

Still a lot of work to do at LHC energies.. Many questions are still open.

Introduction (2)

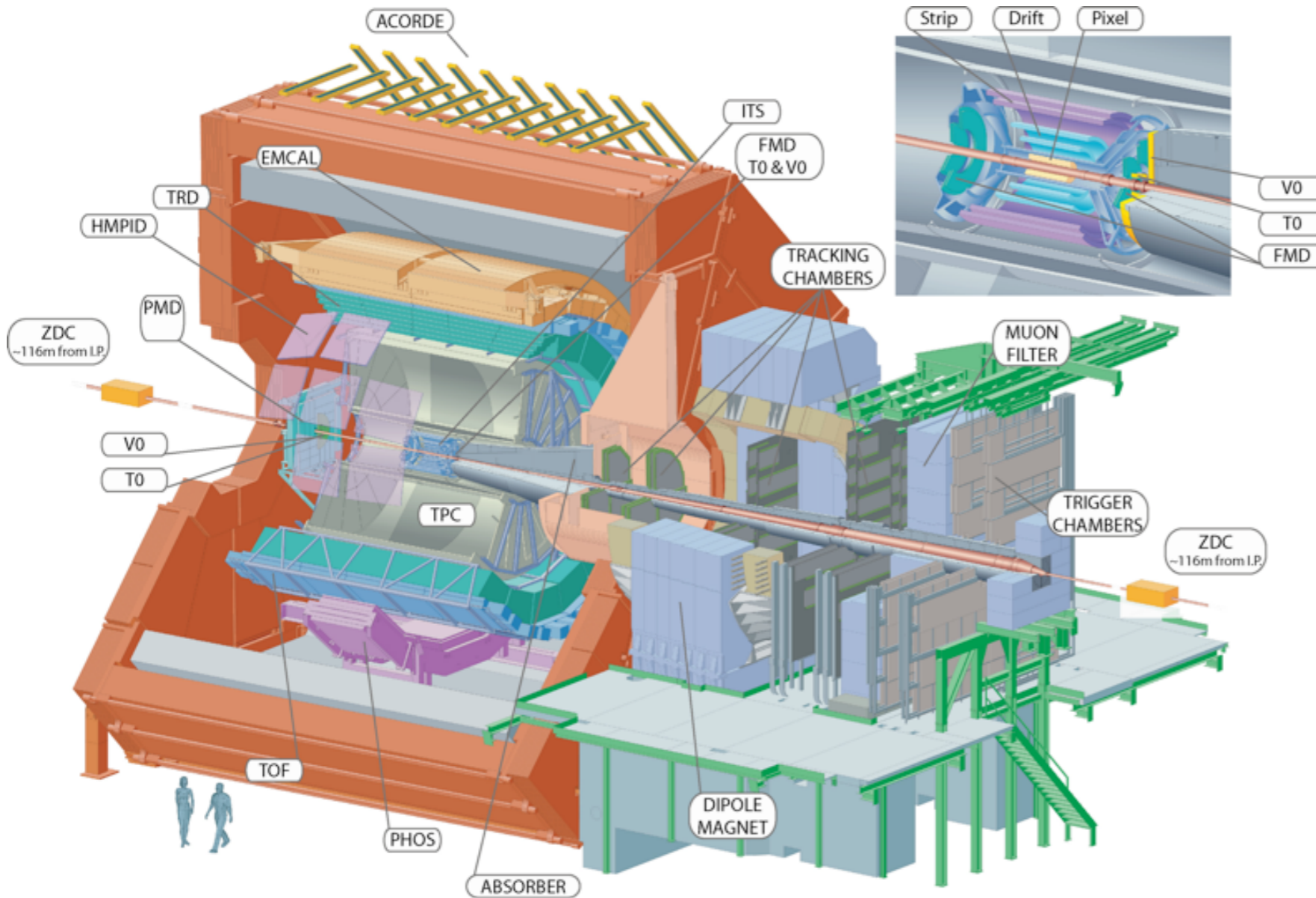
- Fluctuations can be of **statistical** or **dynamical** origin and we must carefully distinguish them. Dynamical fluctuations arise from physical phenomena.
- Ongoing and completed fluctuation analyses in ALICE:
 - **net-charge fluctuations**
 - **net-strangeness**
 - **balance functions**
 - **mean p_T fluctuations** → see next talk by Stefan Heckel
 - multiplicity fluctuations
 - higher moments of net-charge and net-baryon fluctuations
 - temperature fluctuations

The ALICE detector



The ALICE detector

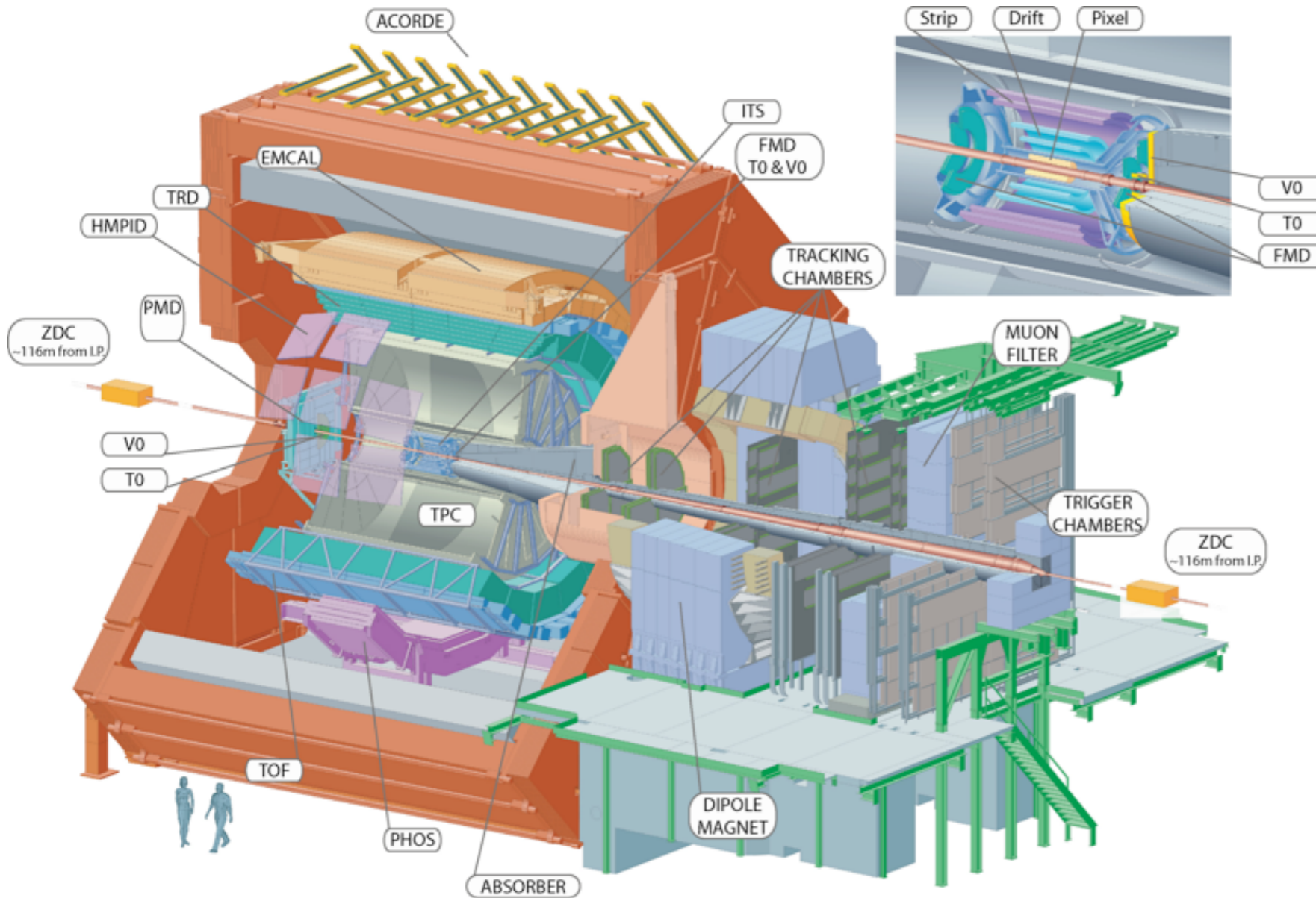
ITS+TPC+TRD: excellent track reconstruction capabilities in a high track density environment.



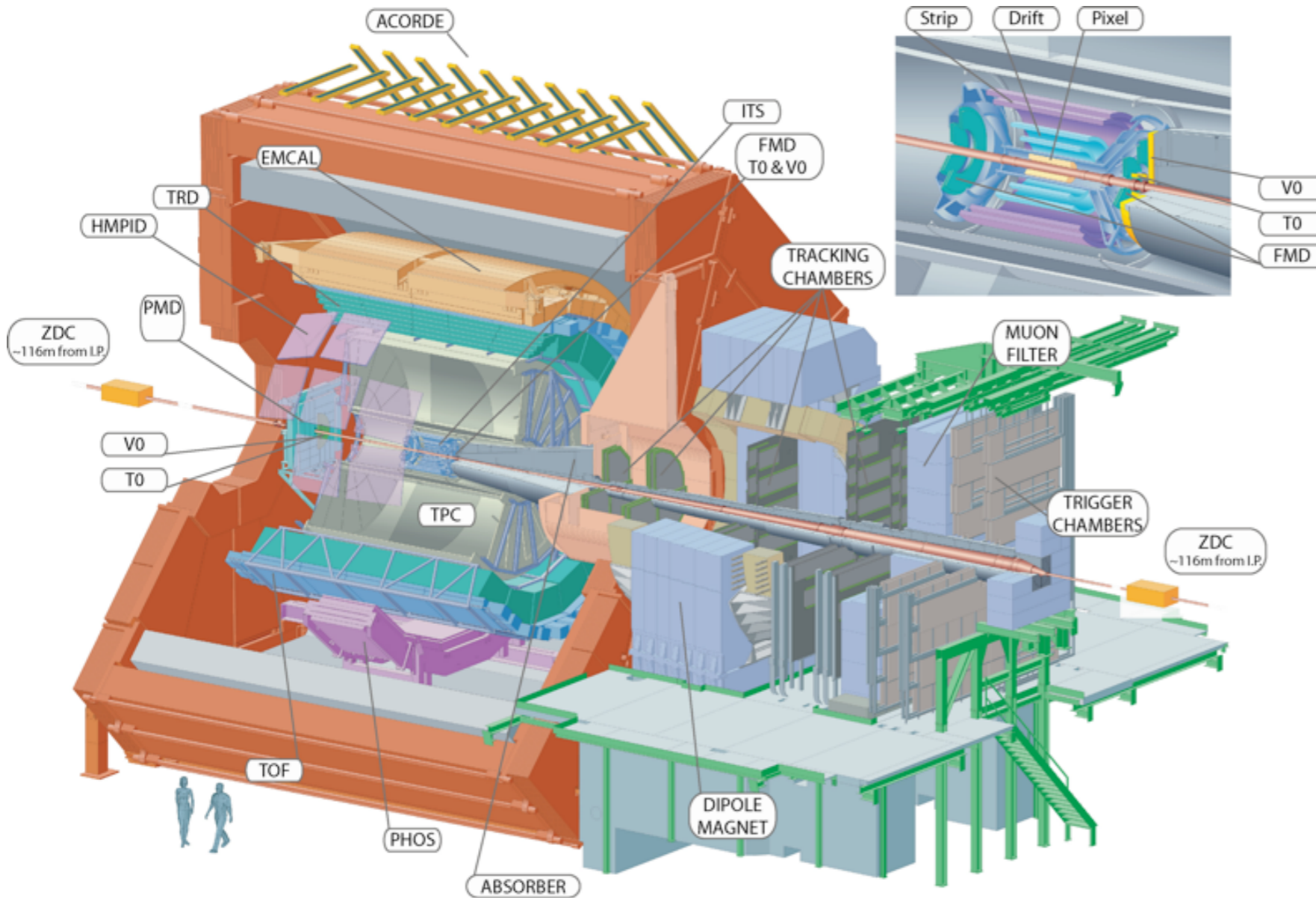
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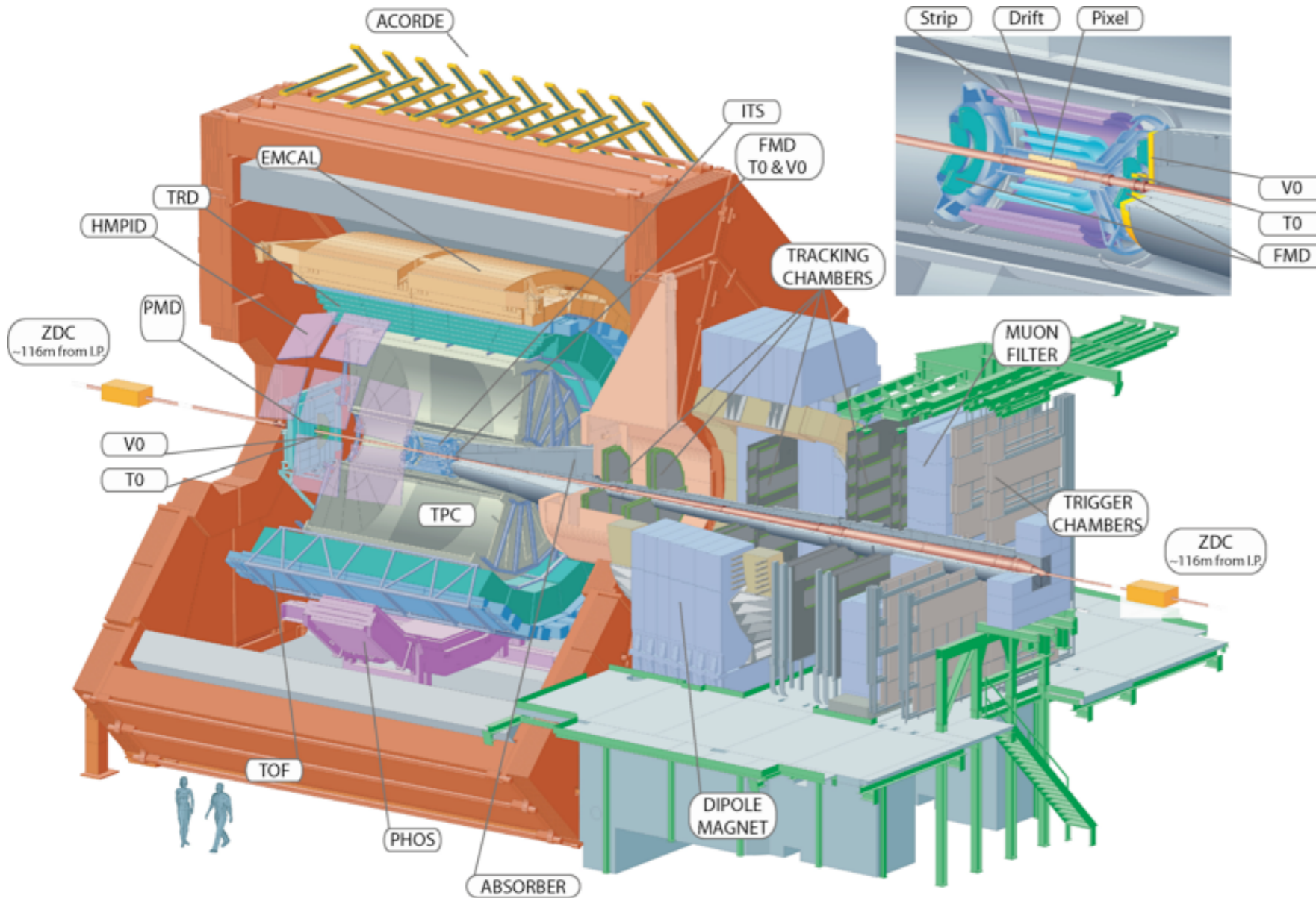


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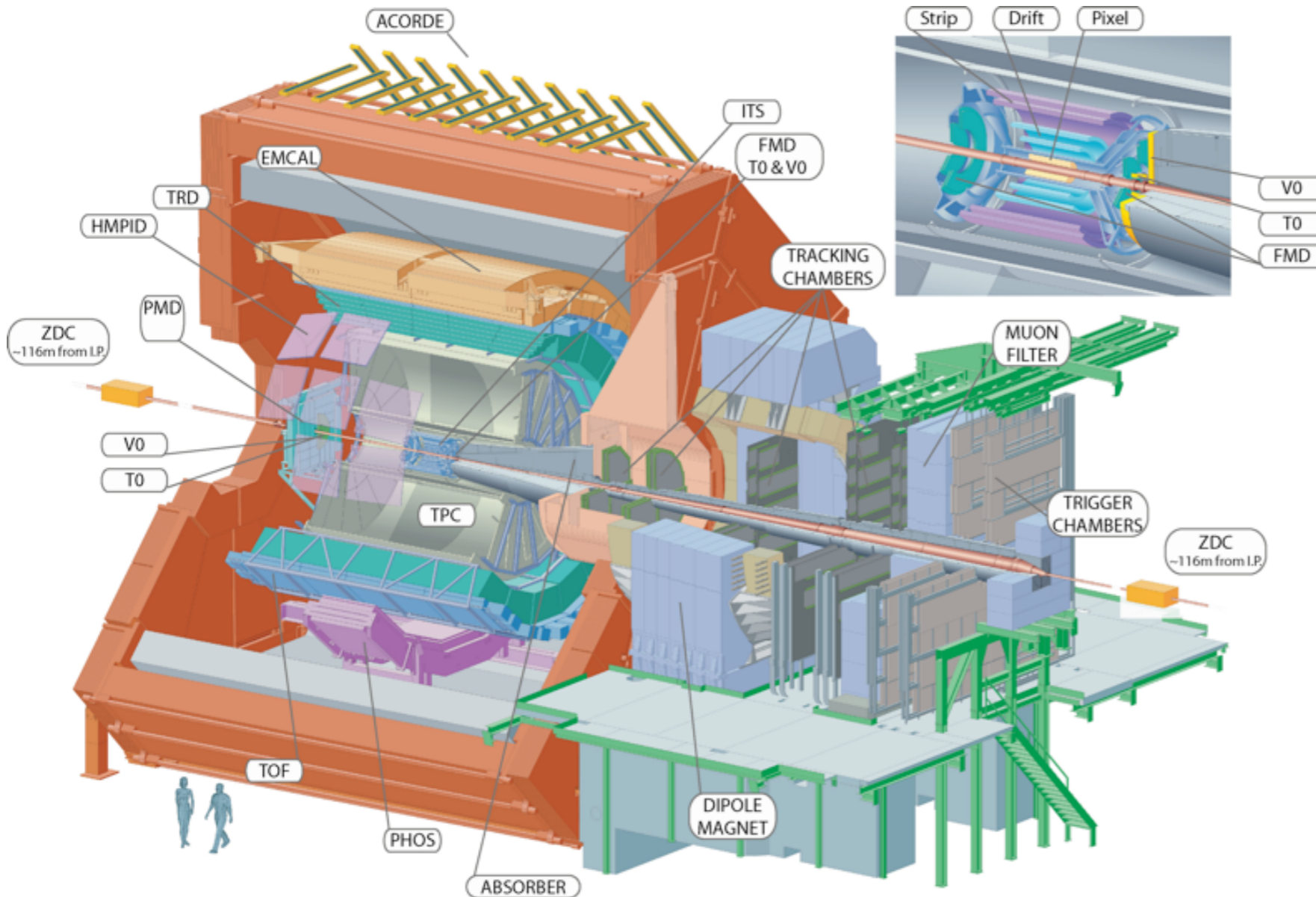
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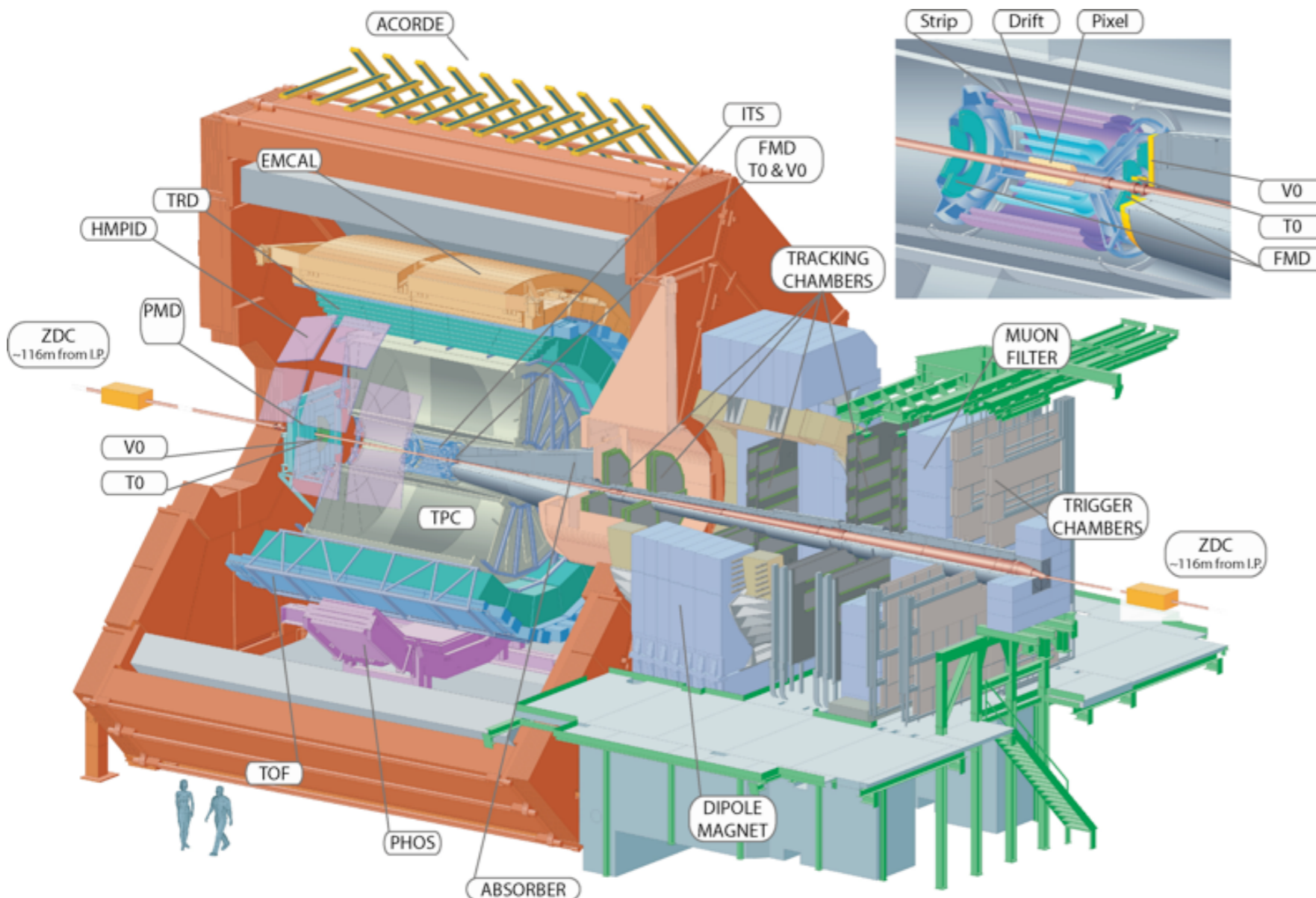
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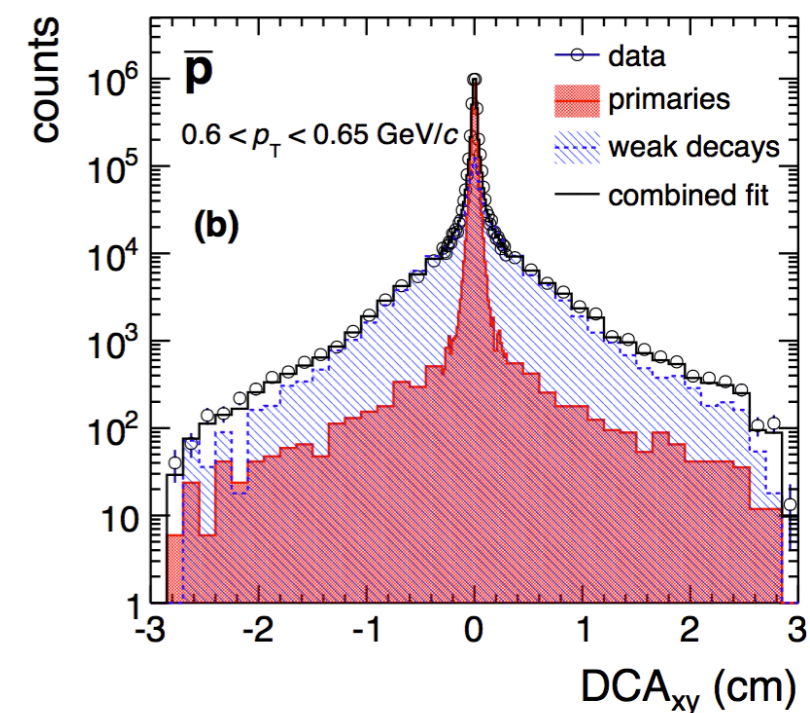
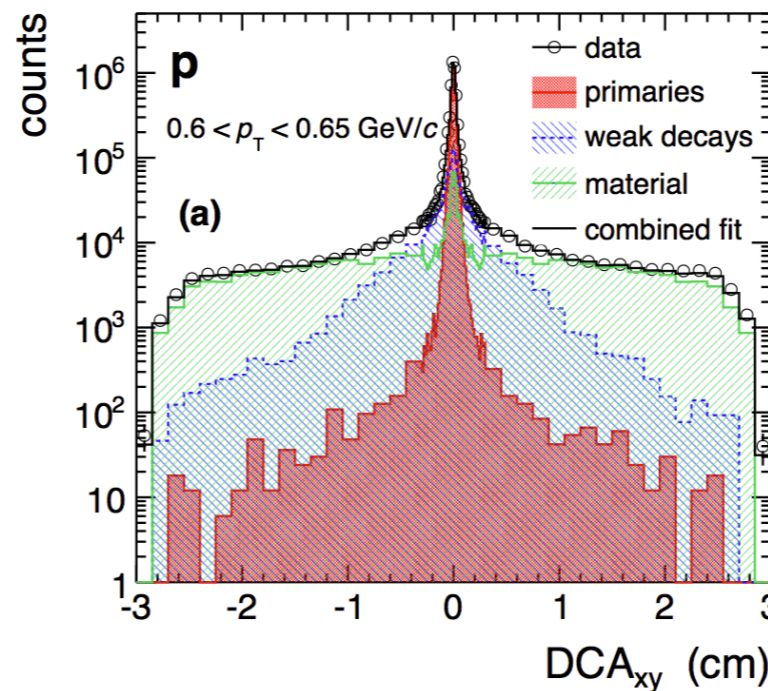
ALICE is ideally suited for the measurement of light flavor hadrons on an event-by-event basis.

Bulk particle production

- Investigate matter in local thermal equilibrium => Look at the hadrons made up of the most abundantly produced quarks: u,d,s.

$\pi, K, p, \Lambda, \Xi, \Omega, \Phi, K^{*0}, d, {}^3\text{He}, {}^3\Lambda\text{H}, {}^4\text{He}$

- Decays of strange particles feed into the states with lower mass and need to be carefully subtracted for consistent data \leftrightarrow model comparisons:



[Phys. Rev. C 88, 044910 (2013)]

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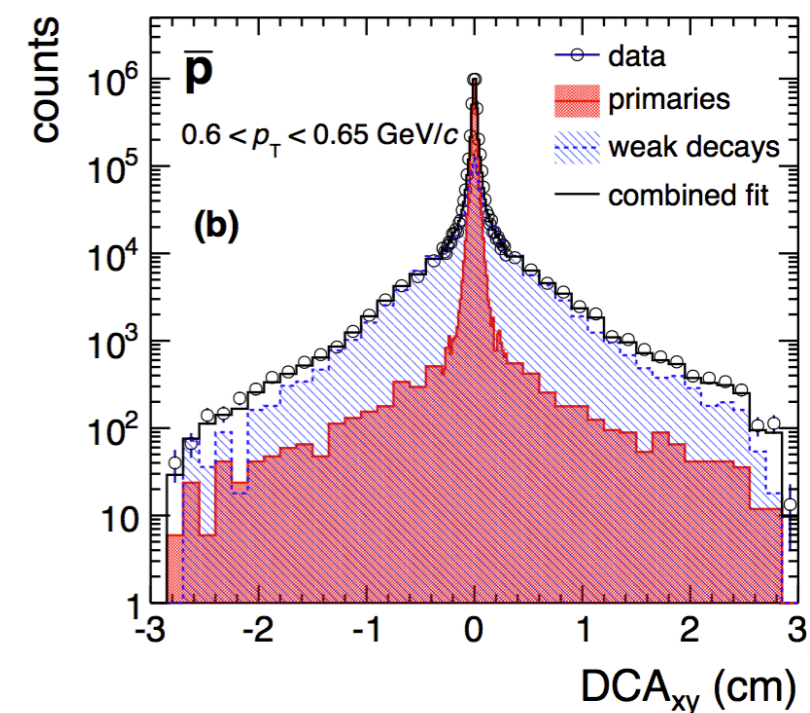
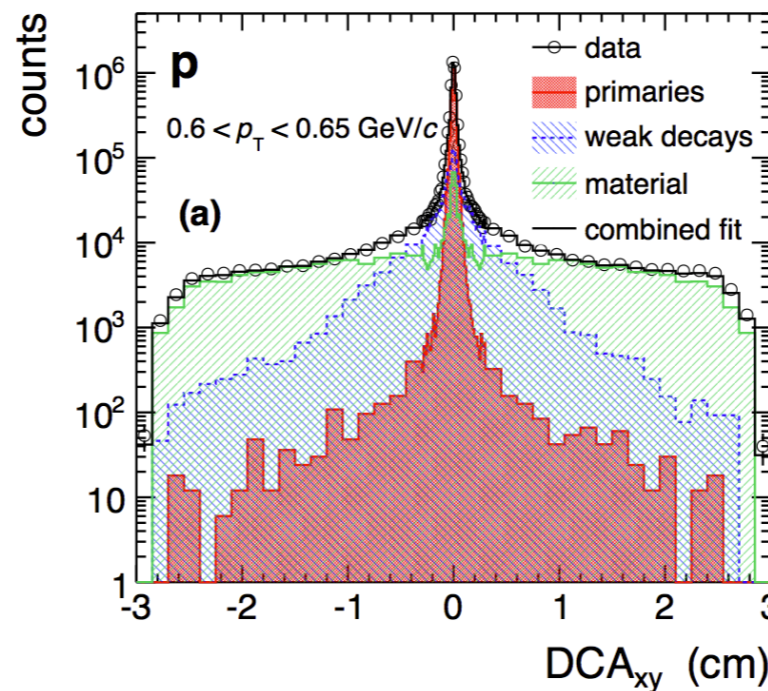
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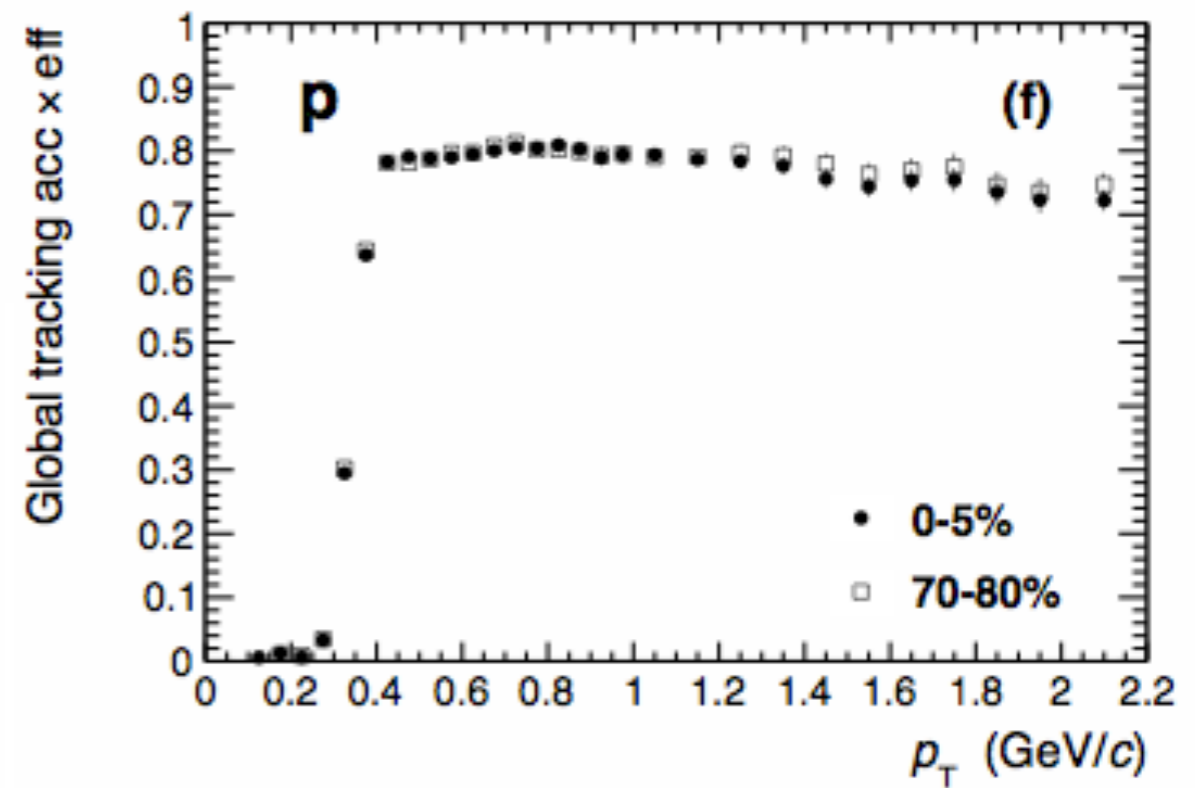
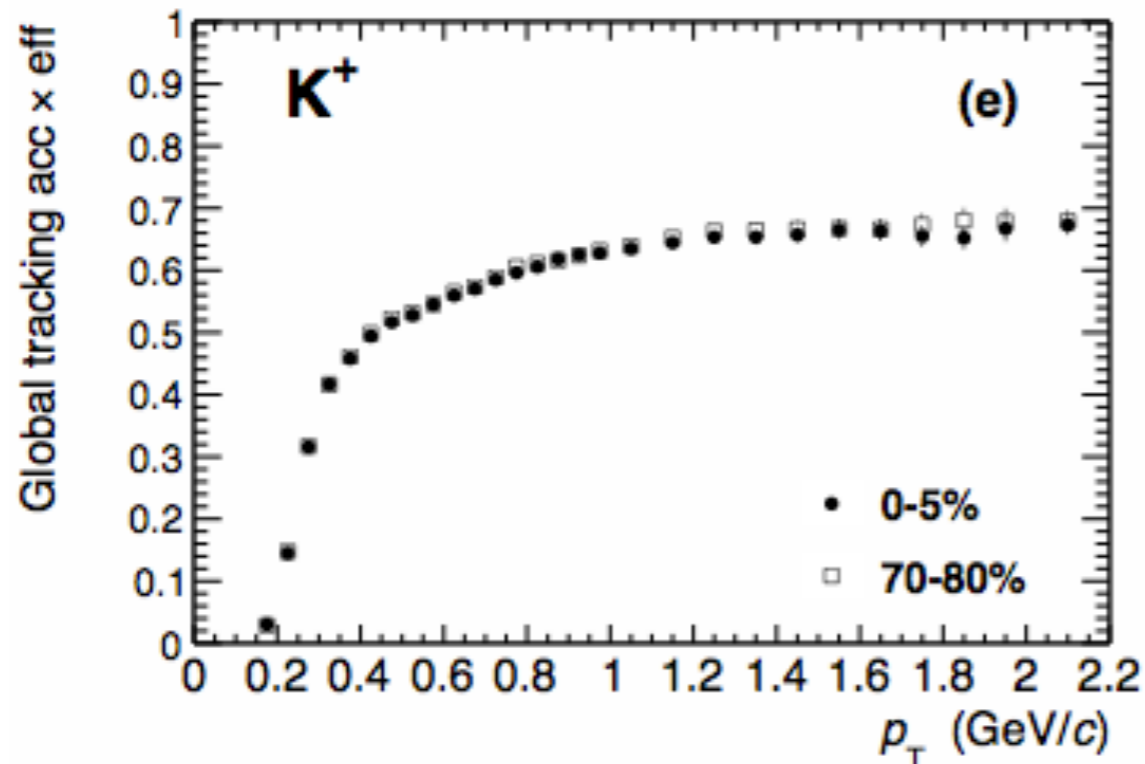
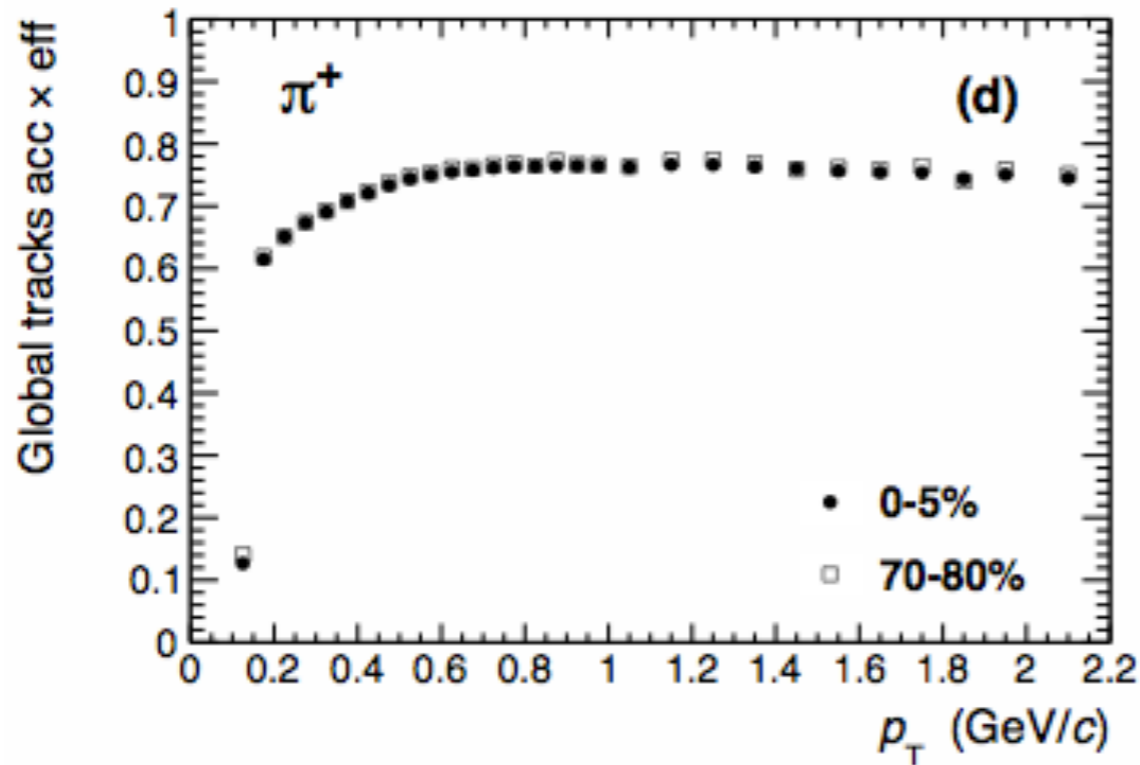


(ALICE Definition) *Primary particles* are defined as prompt particles produced in the collision including all decay products, except products from weak decays of light flavor hadrons and of muons.



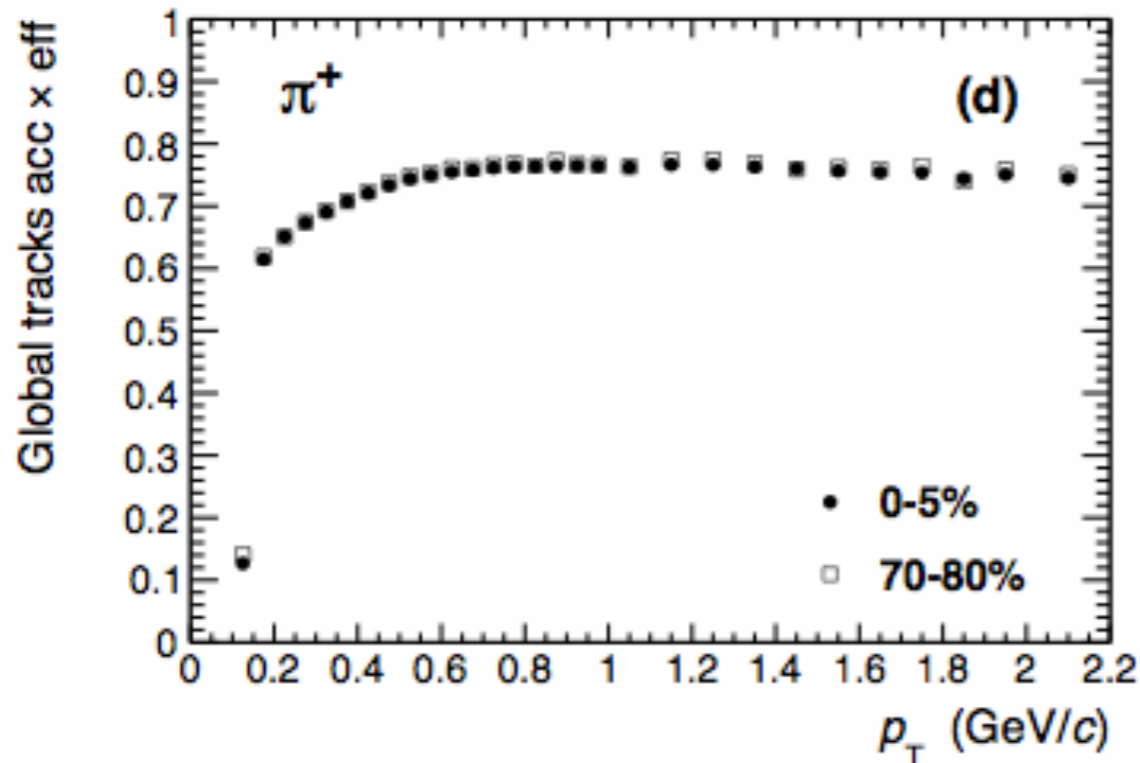
[Phys. Rev. C 88, 044910 (2013)]

Detector efficiencies

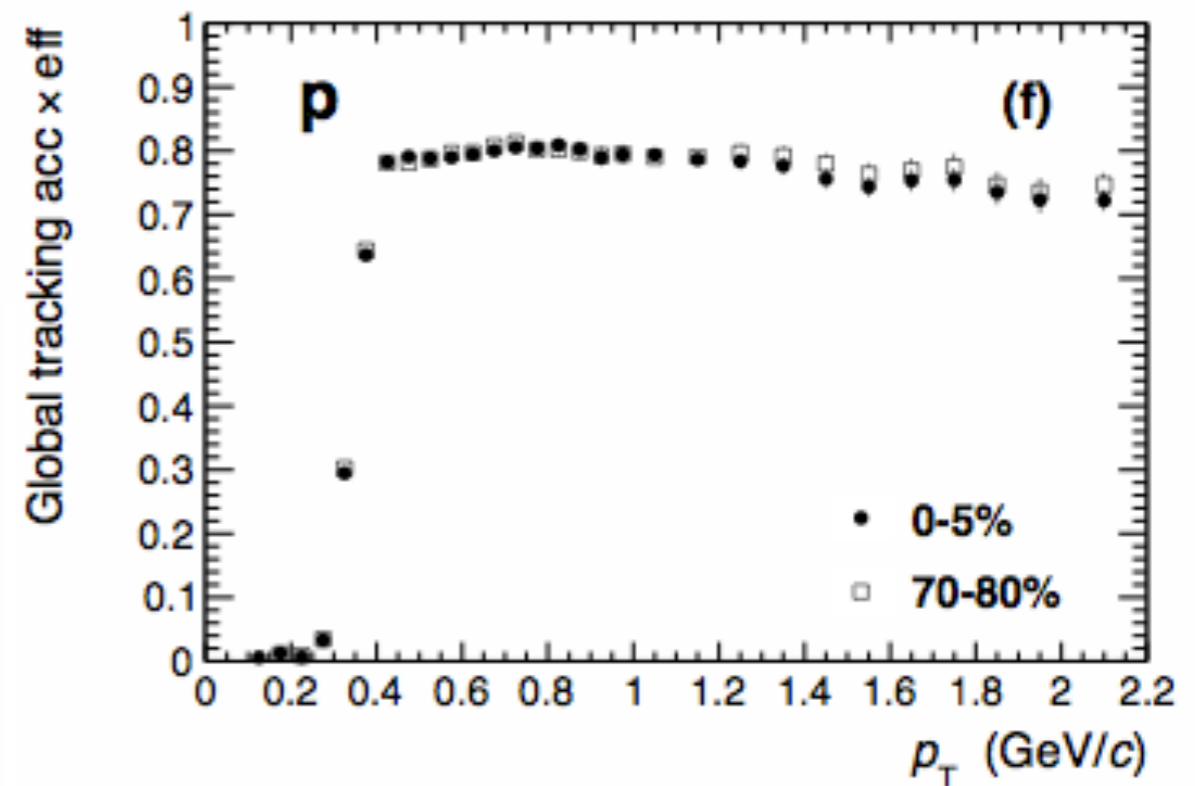
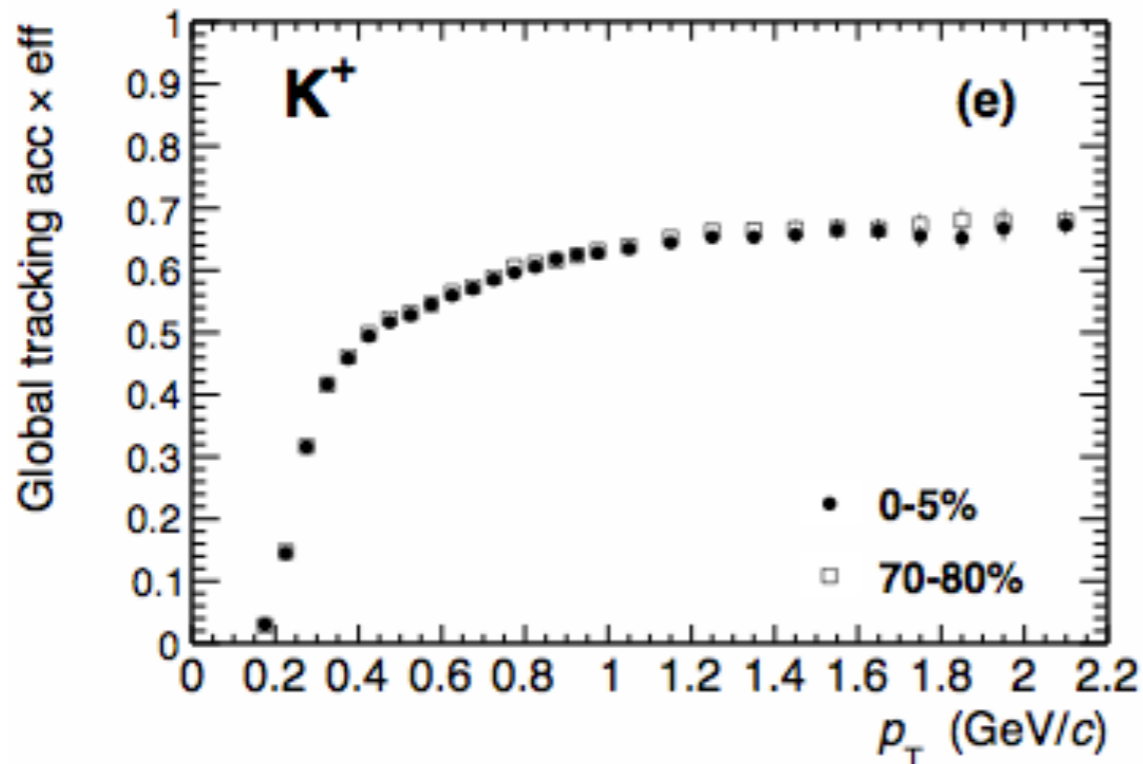


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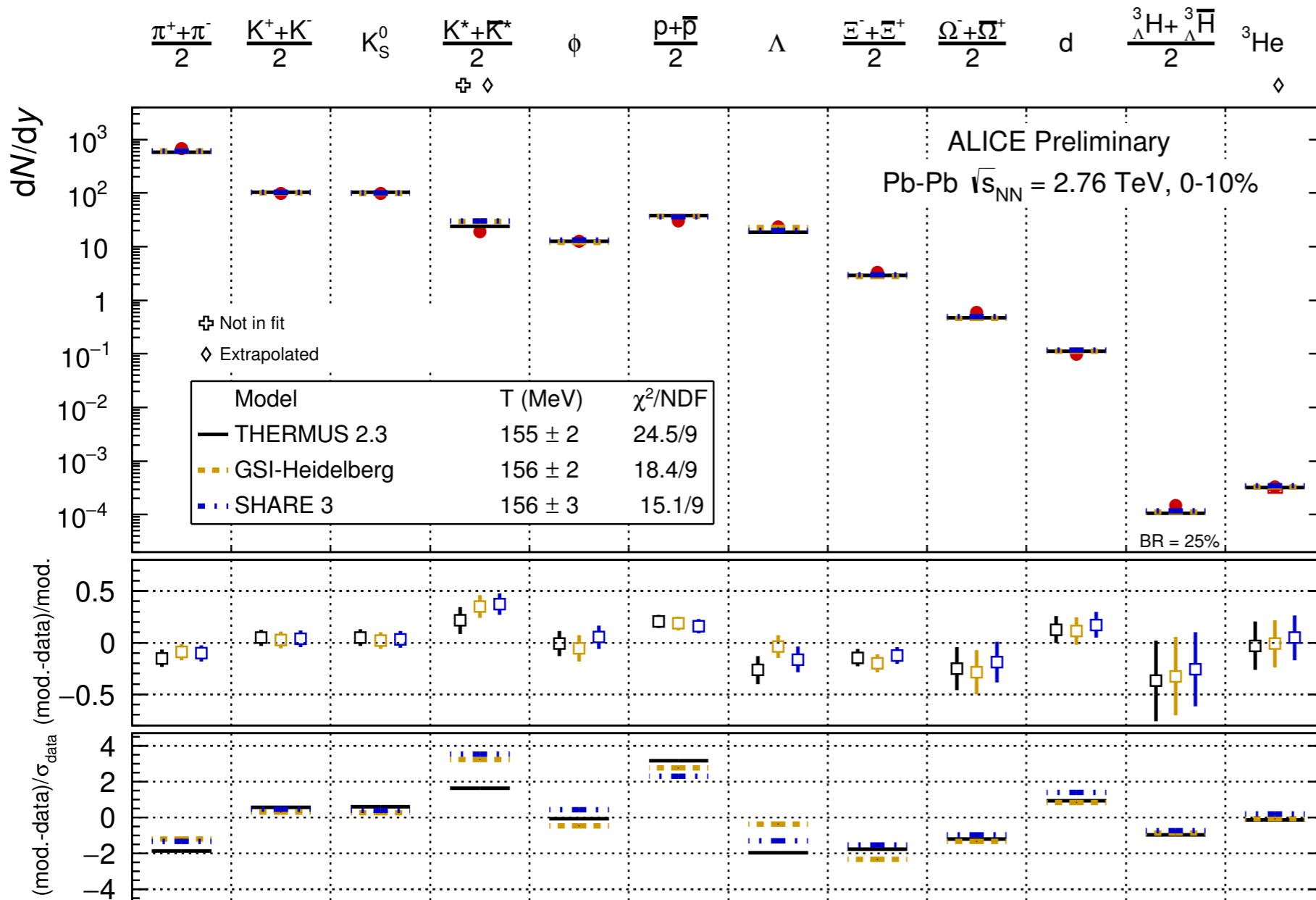
Detector originally optimised for $dN/dy = 8000$
 \Rightarrow negligible dependence of detector efficiencies on centrality.



[Phys. Rev. C 88, 044910 (2013)]

Chemical freeze-out and thermal model calculations

Pb-Pb: Thermal fits to ALICE data

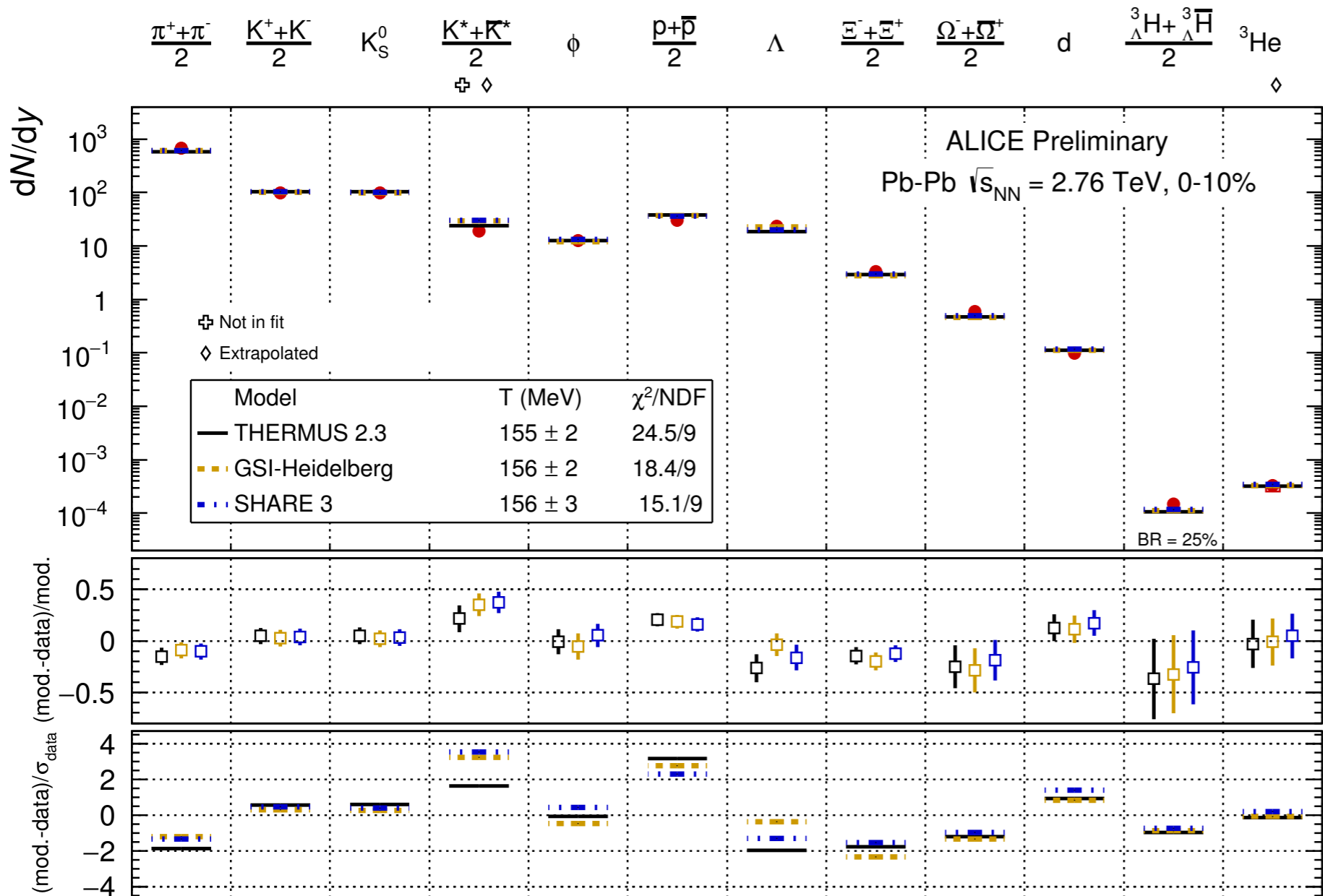


ALI-PREL-94600

[Wheaton et al, Comput.Phys.Commun, 180 84]
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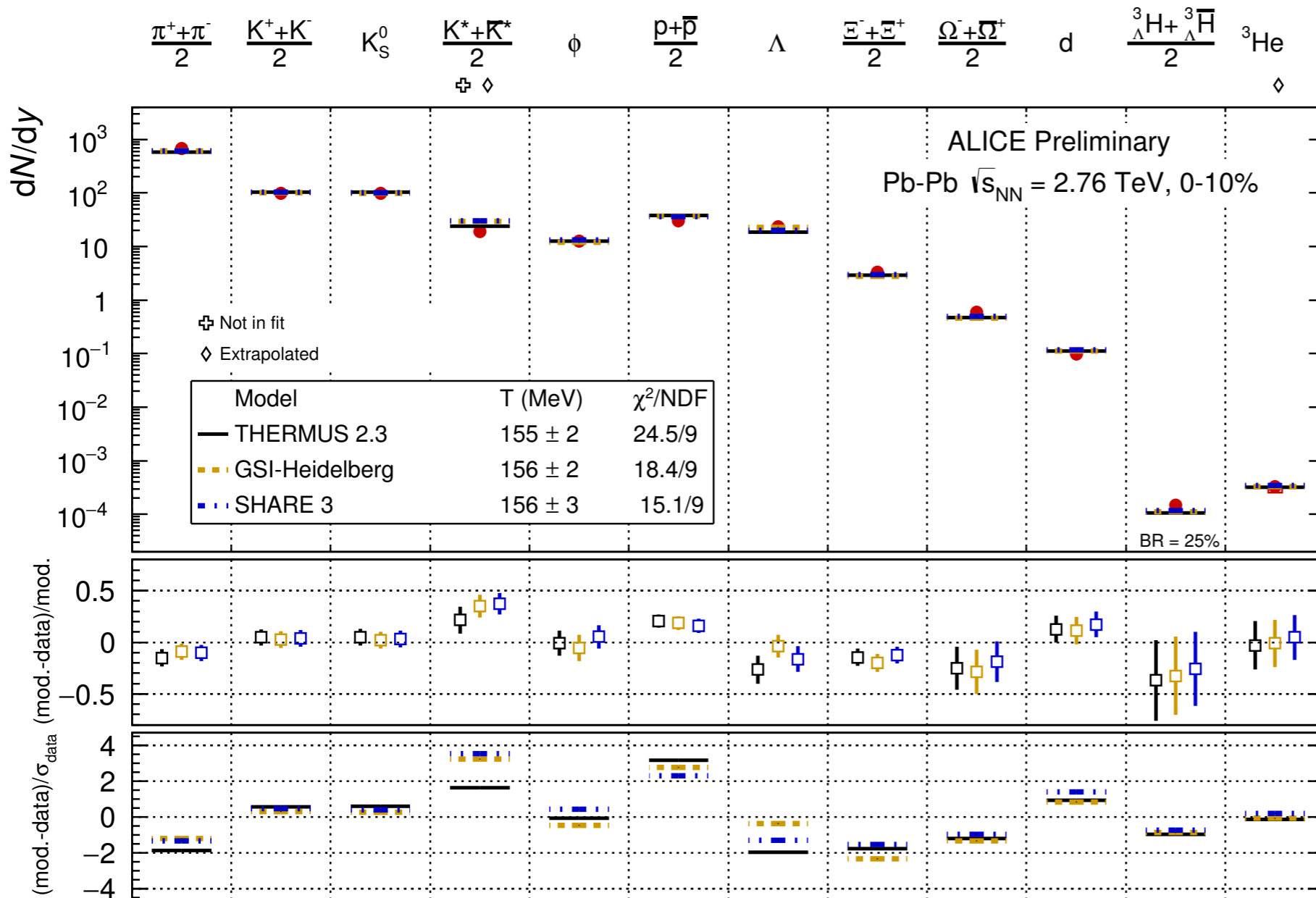
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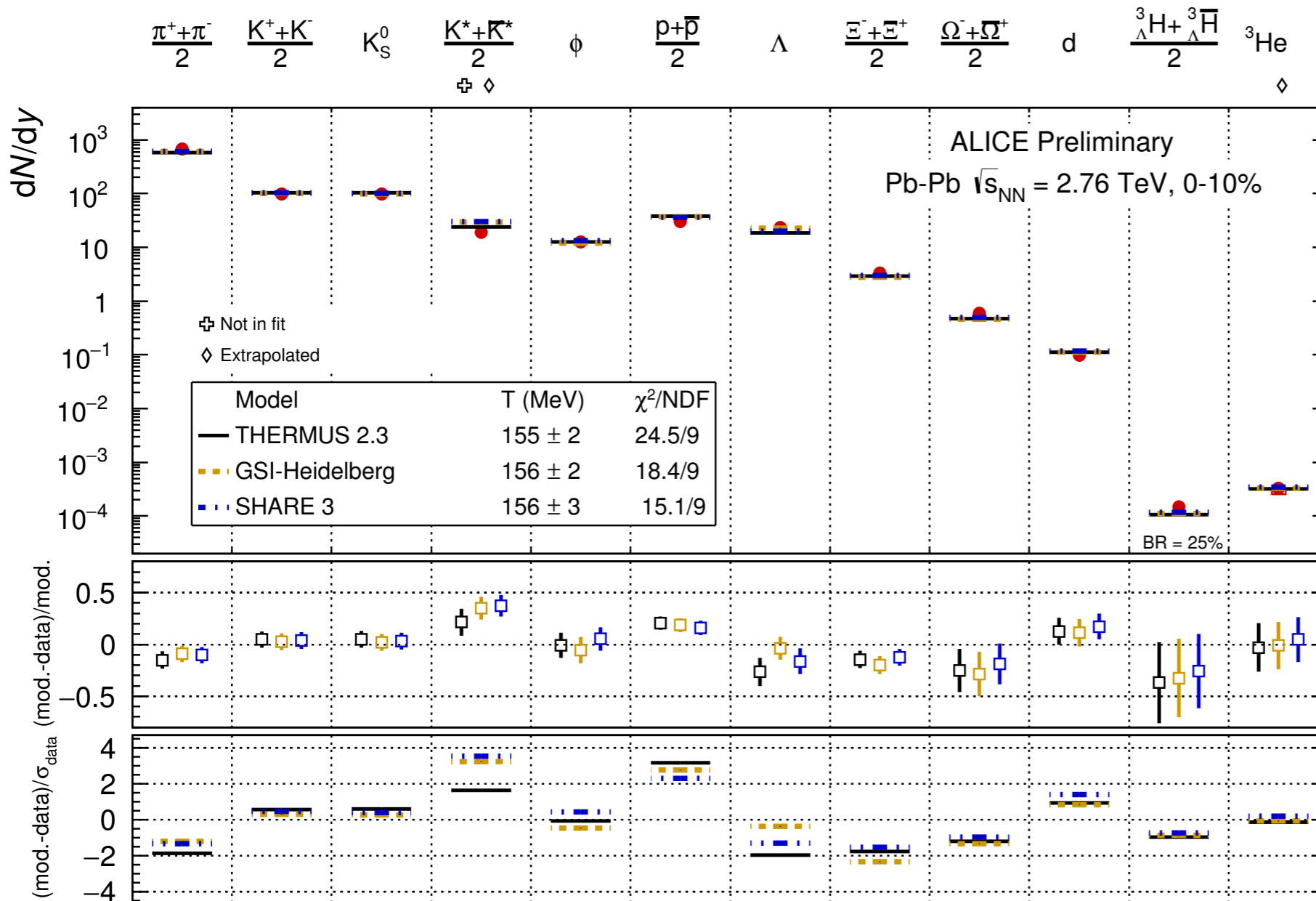
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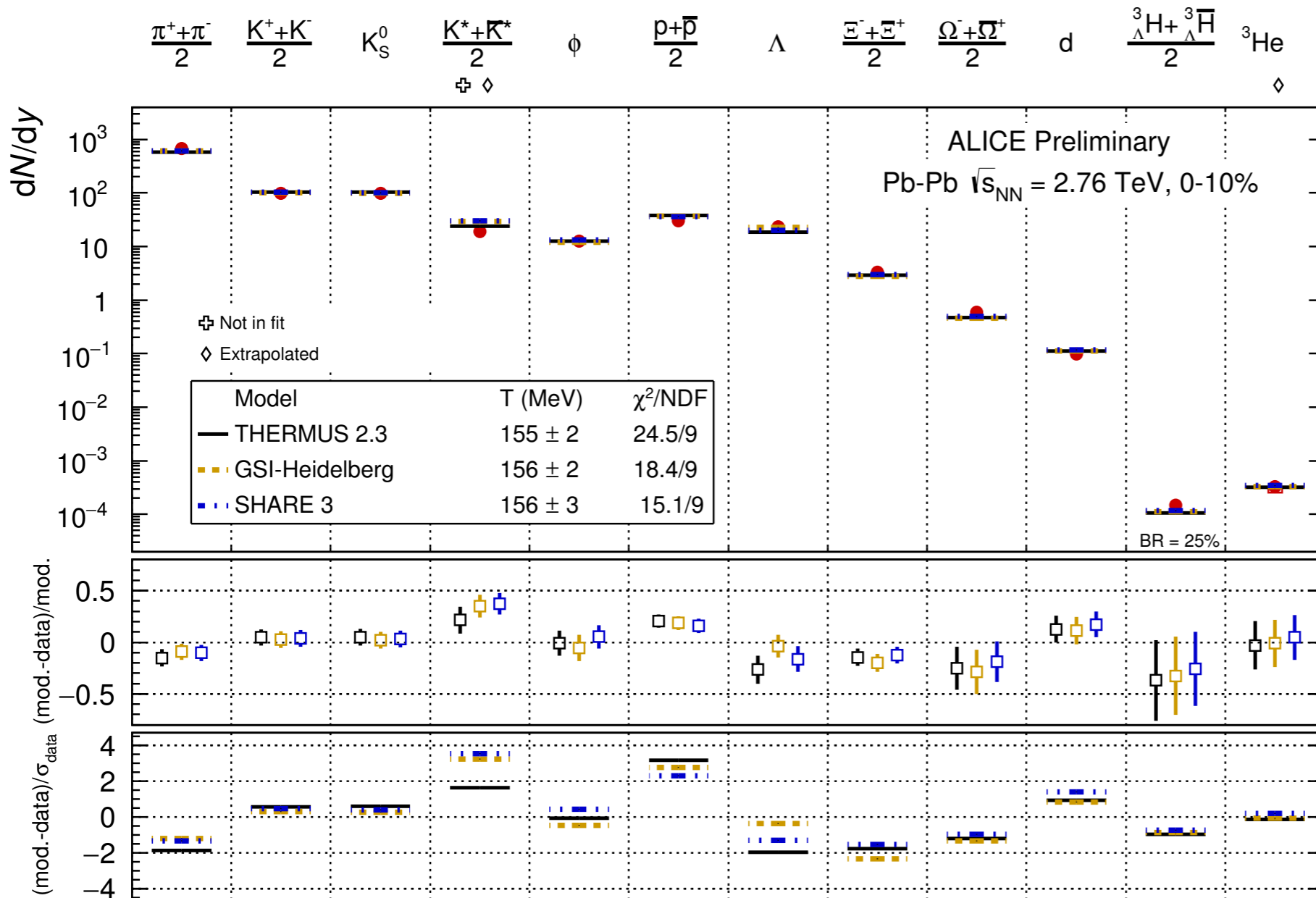
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Three different versions of thermal model implementations give similar results.

ALI-PREL-94600

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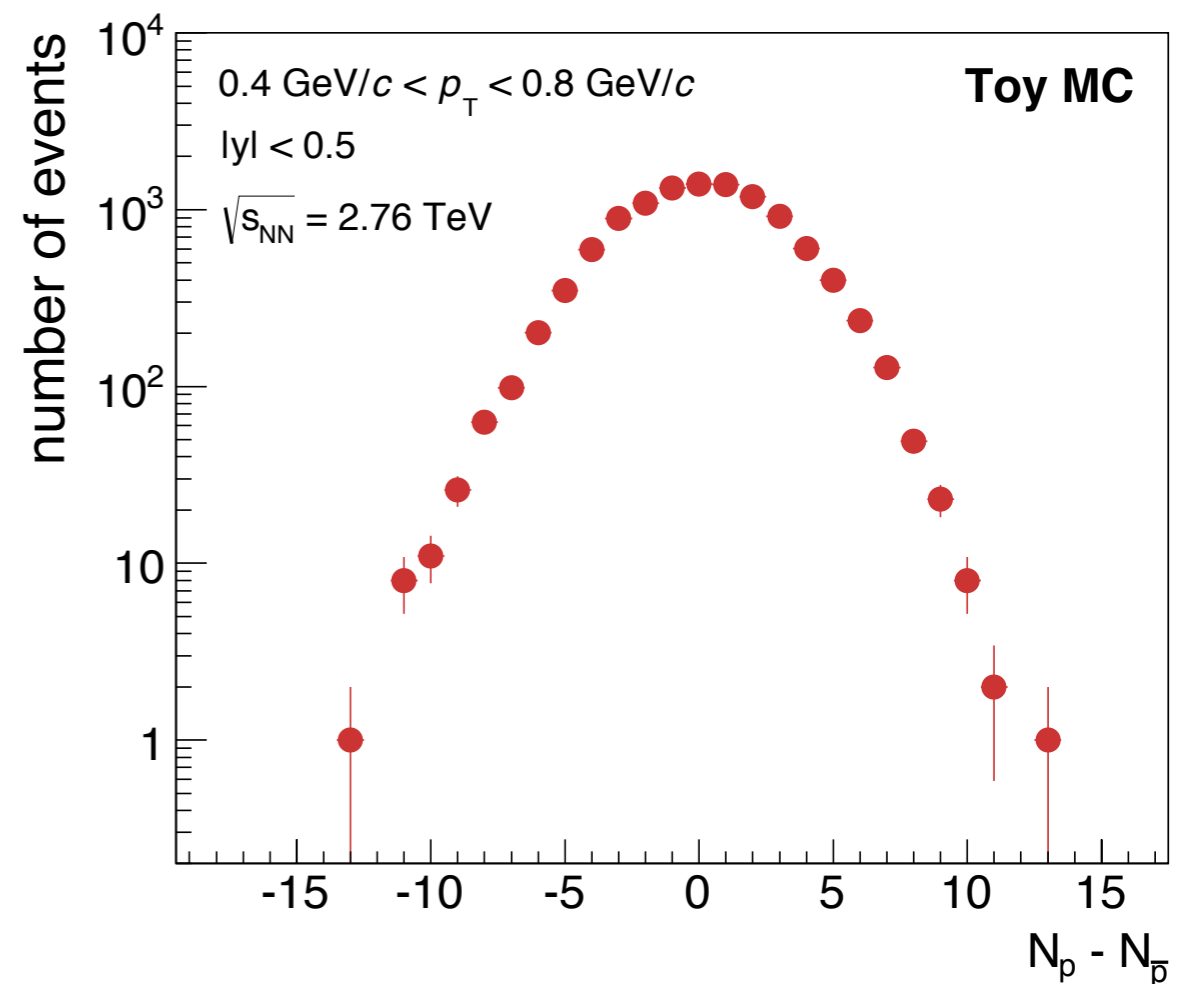
Event-by-event fluctuations of conserved quantities

Thermodynamic susceptibilities

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$$\chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n}(P/T^4)}{\partial(\mu_B/T)^l \partial(\mu_S/T)^m \partial(\mu_Q/T)^n}$$

- Statistical distribution of conserved quantities are quantified by their (central) moments or cumulants.



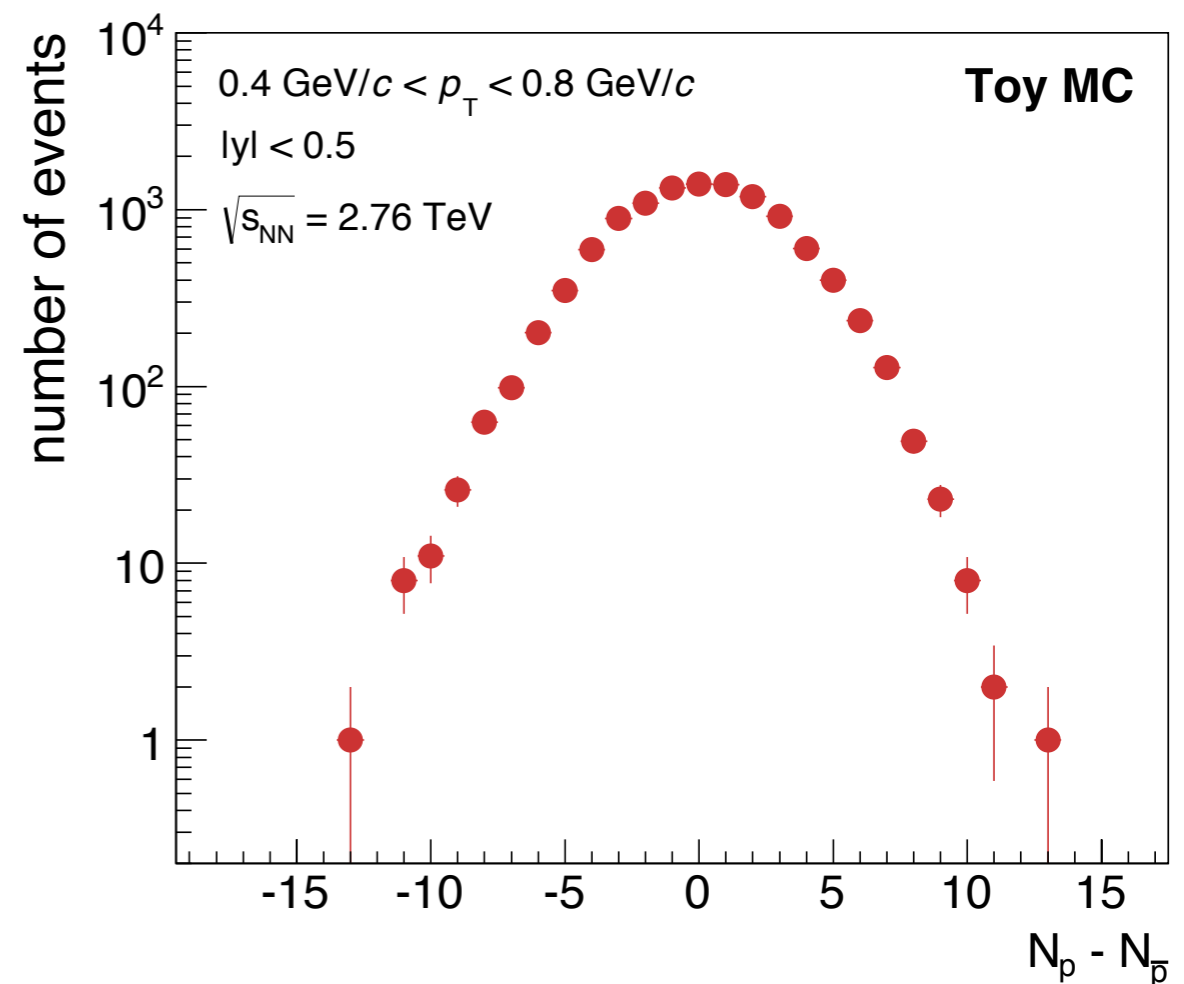
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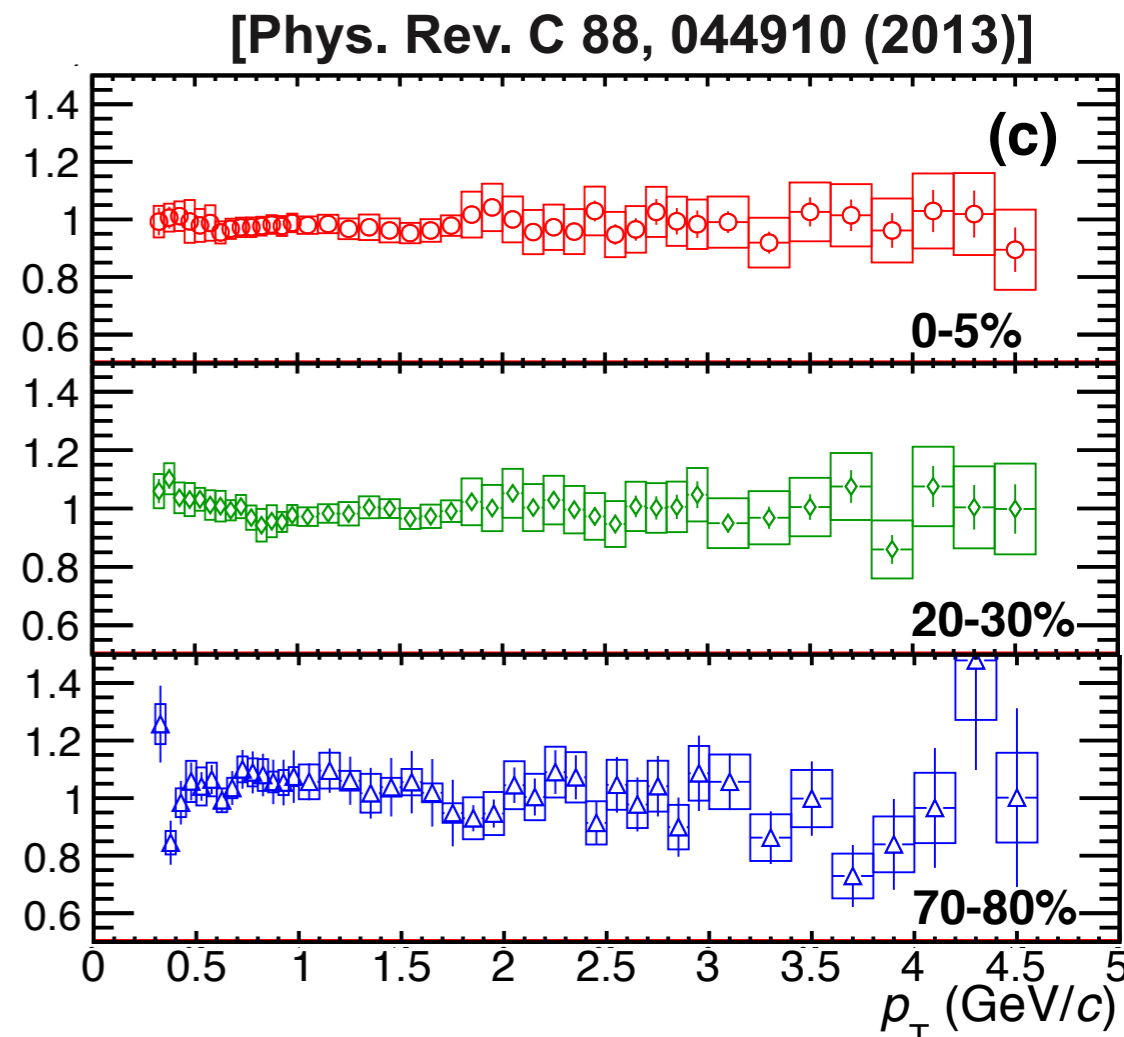
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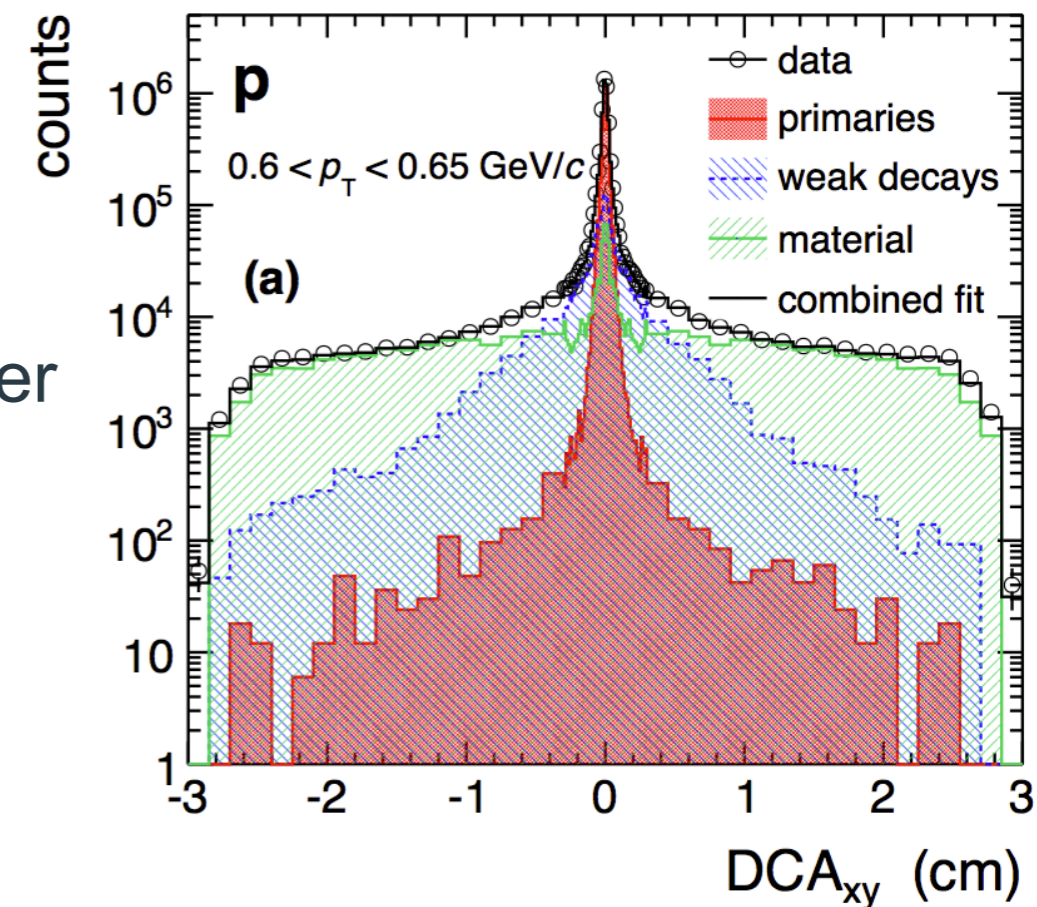
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Towards a measurement of net-baryon number at LHC...

- The measurement is experimentally very challenging:
 - Correction for detector efficiency (N.B.: efficiencies differ for protons and anti-protons due to absorption).
 - Auto-correlations with centrality estimator.
-> use forward detectors to avoid them.
 - Contamination from protons from material.
 - Contamination from weak decays:
 - Does the inclusion of them bring us closer to the total baryon number B ?
 - Can one separate cleanly χ_B and χ_S ?
 - Misidentified particles.
- However, we already know how to correct for these effects on average for particle spectra..

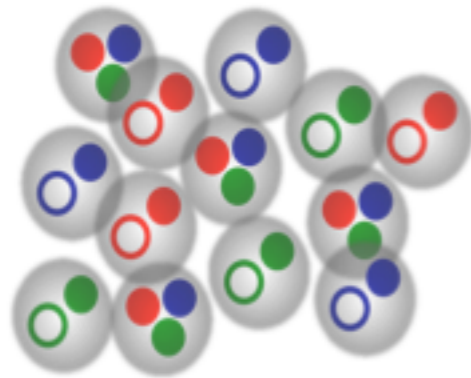


[Phys. Rev. C 88, 044910 (2013)]

Net charge fluctuations

Net charge fluctuations — introduction

- So far, only a net-charge measurement corresponding to the second order moment has been finalised at LHC energies: **[Phys. Rev. Lett. 110, 152301]**.
- Simplified picture:



Hadronic phase:
 $q = \pm 1$
 $\Rightarrow q^2 = \pm 1$



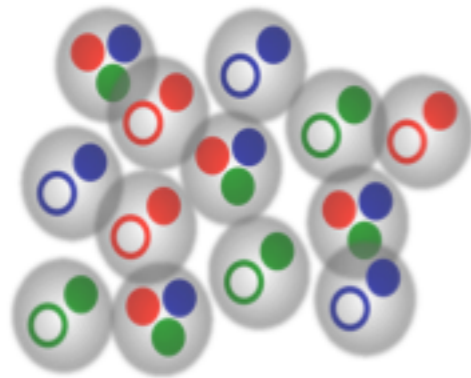
Partonic phase:
 $q = \pm(2/3), \pm(1/3)$
 $\Rightarrow q^2 = \pm(4/9), \pm(1/9)$

- v_{dyn} as robust variable to quantify dynamical fluctuations and to identify relevant charge carriers:

$$v_{(+-, \text{dyn.})} = \frac{\langle N_+(N_+ - 1) \rangle}{\langle N_+ \rangle^2} + \frac{\langle N_-(N_- - 1) \rangle}{\langle N_- \rangle^2} - 2 \frac{\langle N_+ N_- \rangle}{\langle N_+ \rangle \langle N_- \rangle}$$

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Substantially smaller value of the correlation function is expected in the QGP phase than in the hadronic phase.

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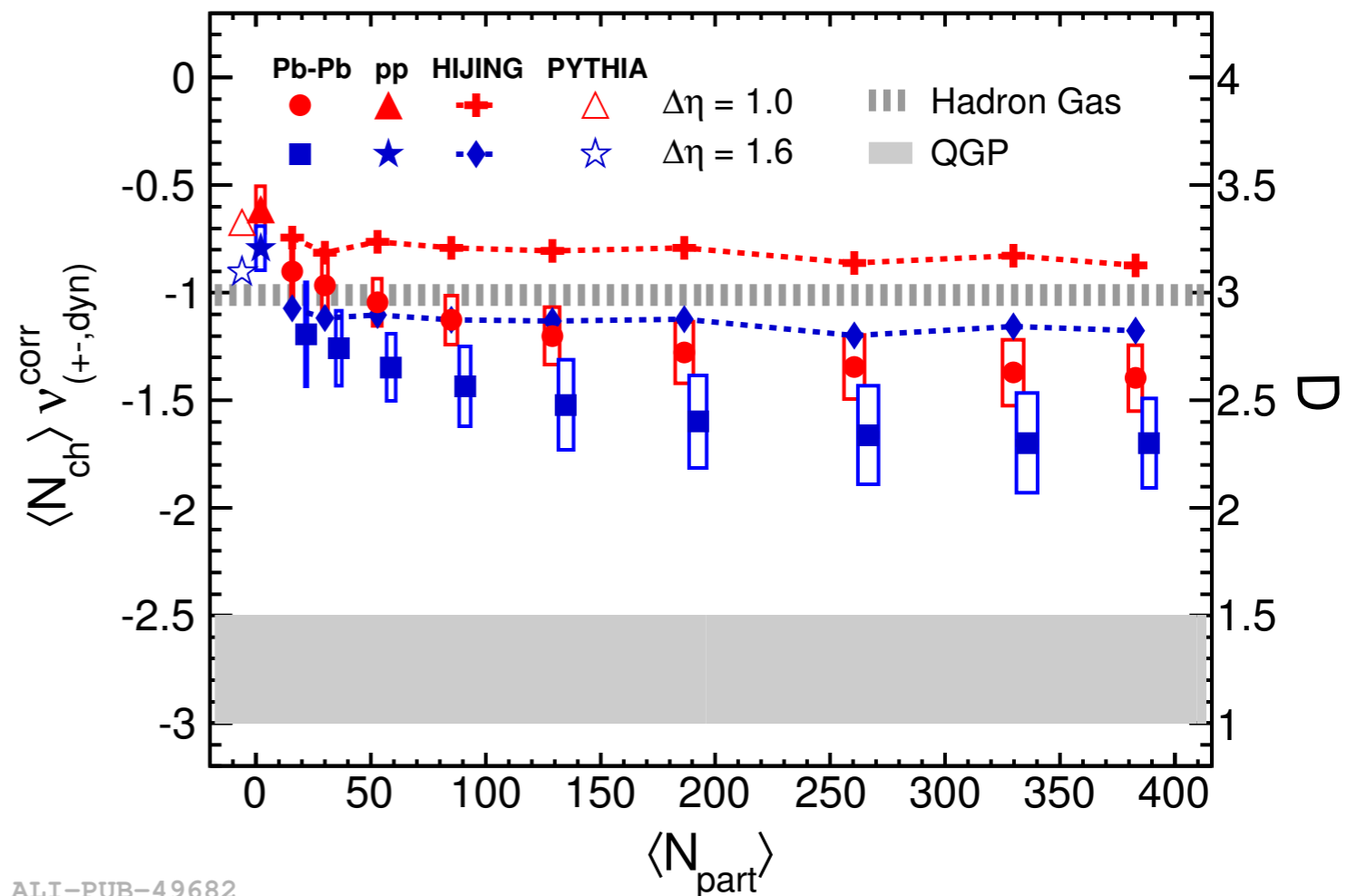
D-measure of net-charge fluctuations

- v_{dyn} can be connected to the entropy of the system via the D-measure in order to relate it to theoretical expectations (corrected for acceptance and global charge conservation):

$$D = \langle N_{ch} \rangle \langle \delta R^2 \rangle$$

$$D \approx 4 \frac{\langle \delta Q^2 \rangle}{\langle N_{ch} \rangle} \approx \begin{cases} 3 & \text{HRG} \\ 1-1.5 & \text{QGP} \end{cases}$$

$$D - 4 \approx \langle N_{ch} \rangle v_{(+-, \text{dyn})}^{\text{corr}}$$



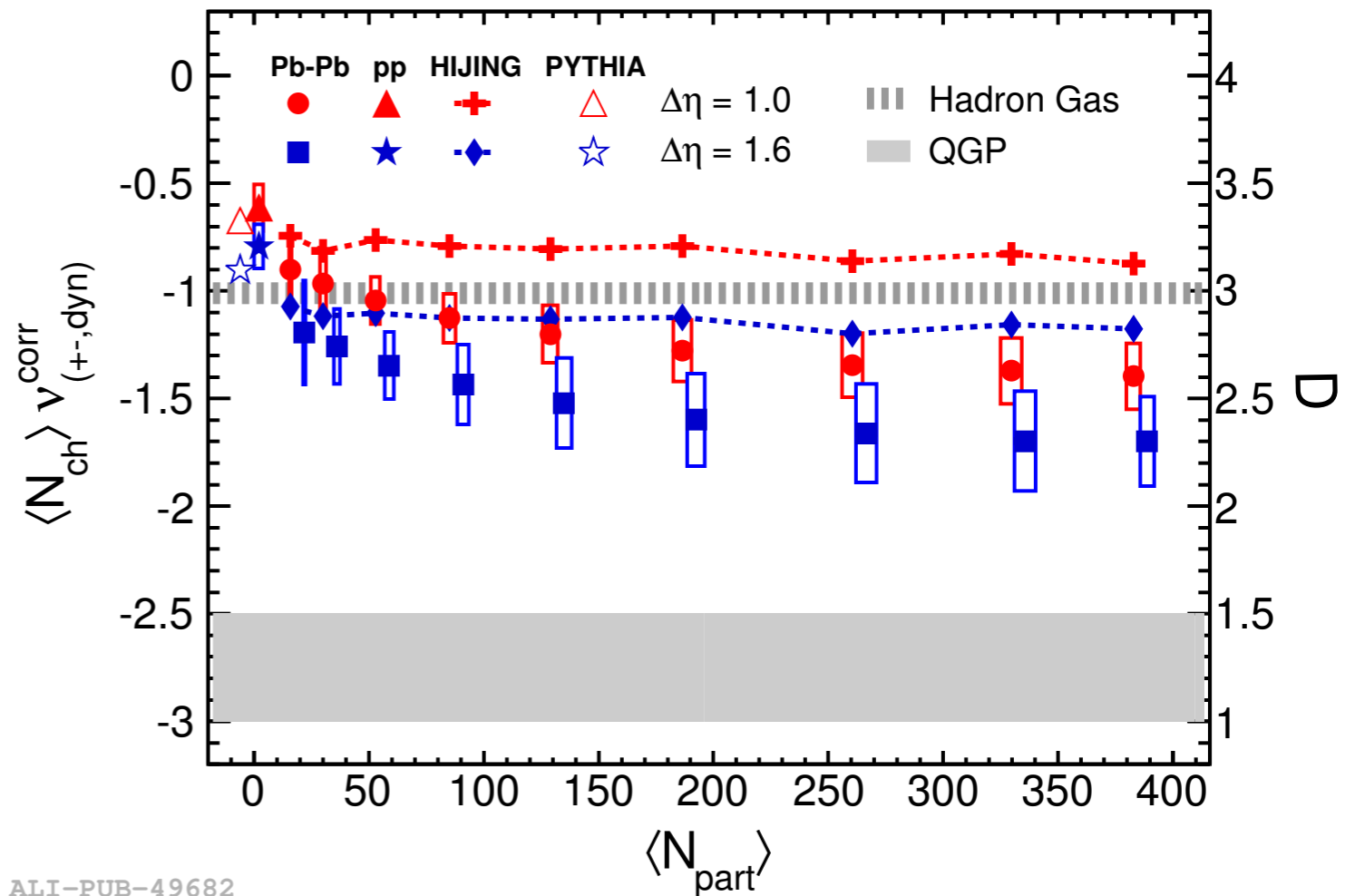
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ALI-PUB-49682

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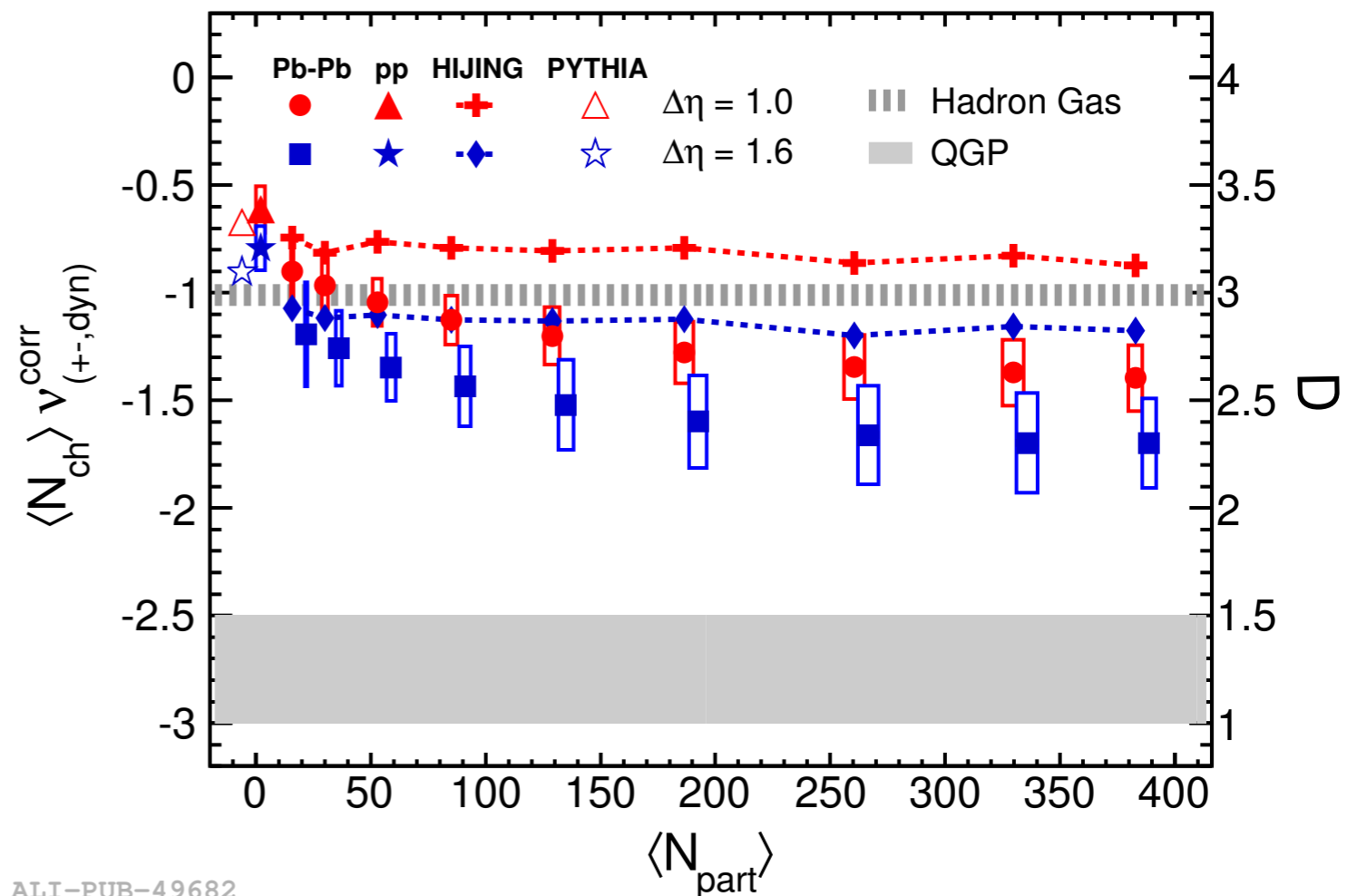
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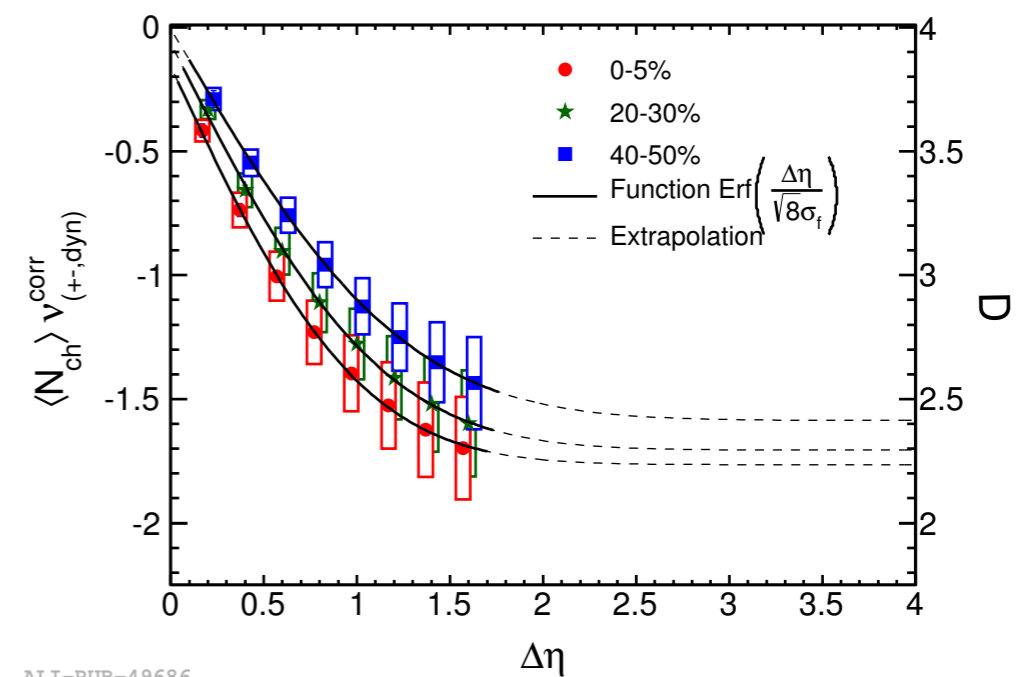
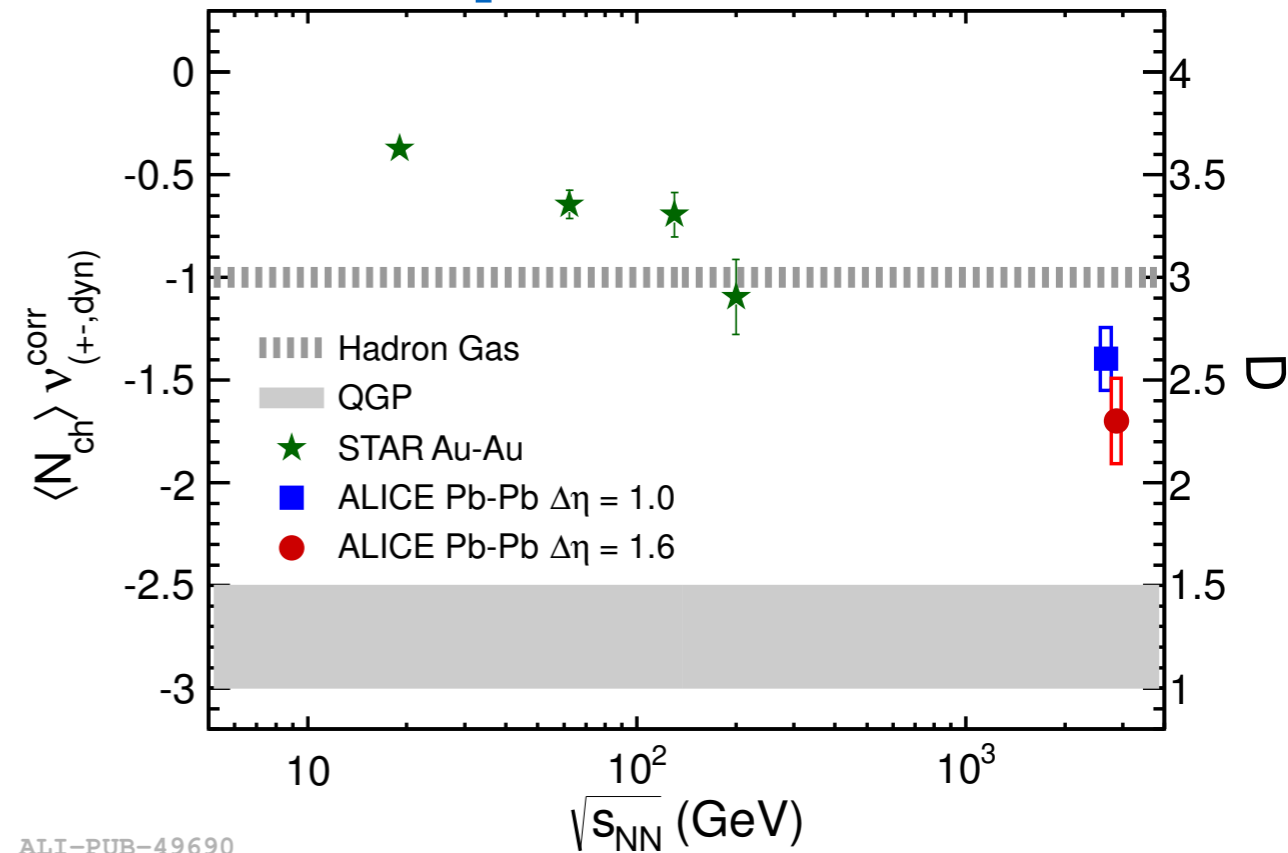
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HIJING shows no centrality dependence and larger values than the data.



Energy and rapidity window dependence

- Results are shown for 0-5% most central collisions.
- Decreasing trend with increasing center-of-mass energy is observed.
- ALICE values significantly lower than the hadron gas expectation while RHIC measurements are still compatible.
- Strong dependence on rapidity window observed which seems to saturate above $\Delta\eta \approx 2.3$ assuming diffusion functions. Initial fluctuations are diluted by final state interactions and limited experimental acceptance. Extending it further in η would be nice.



Balance function

Balance function

• Definition:

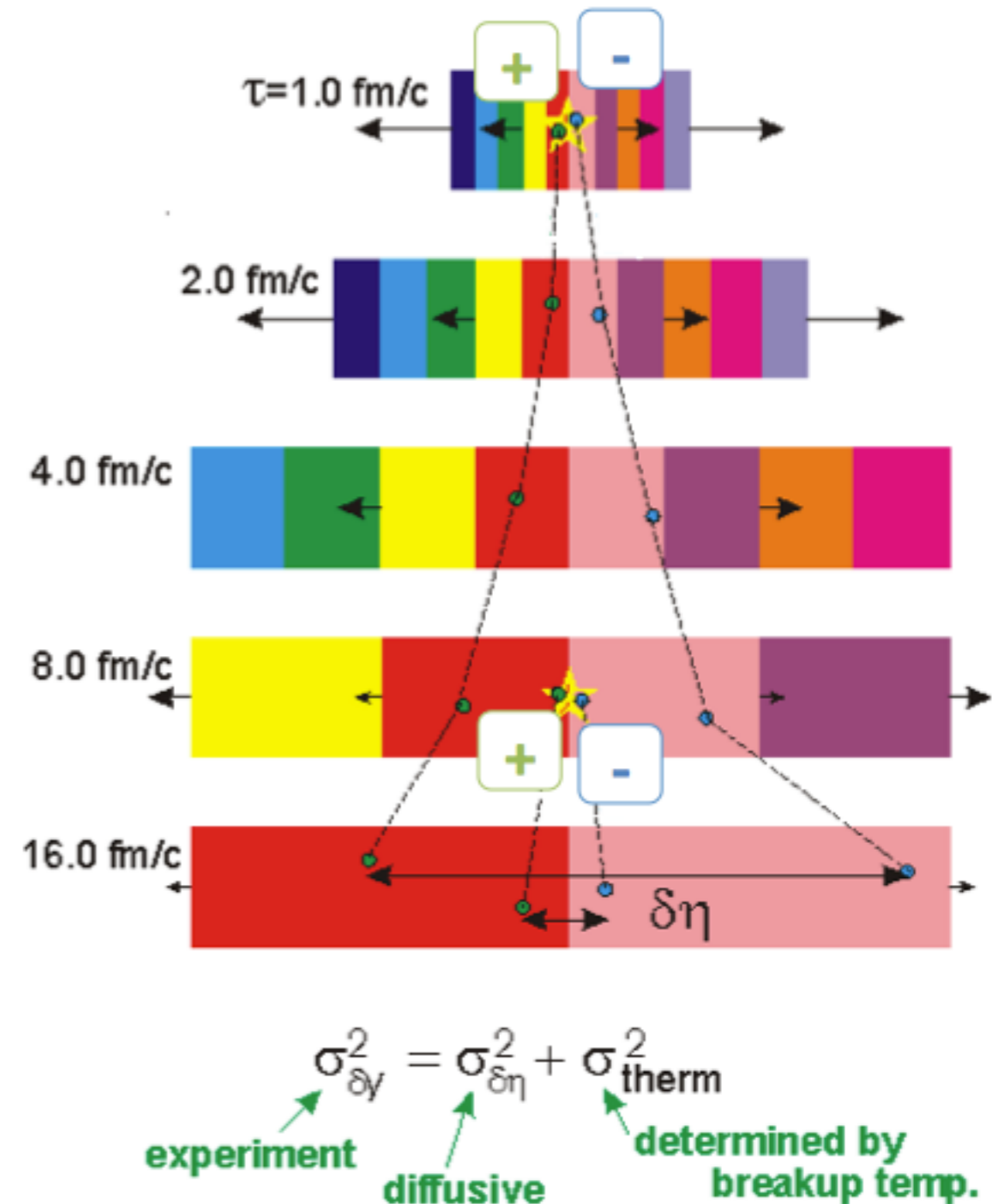
$$B(\Delta\eta, \Delta\varphi) = \frac{S(\Delta\eta, \Delta\varphi)_{US}}{B(\Delta\eta, \Delta\varphi)_{US}} - \frac{S(\Delta\eta, \Delta\varphi)_{LS}}{B(\Delta\eta, \Delta\varphi)_{LS}}$$

$$US = +- / -+$$

$$LS = ++ / --$$

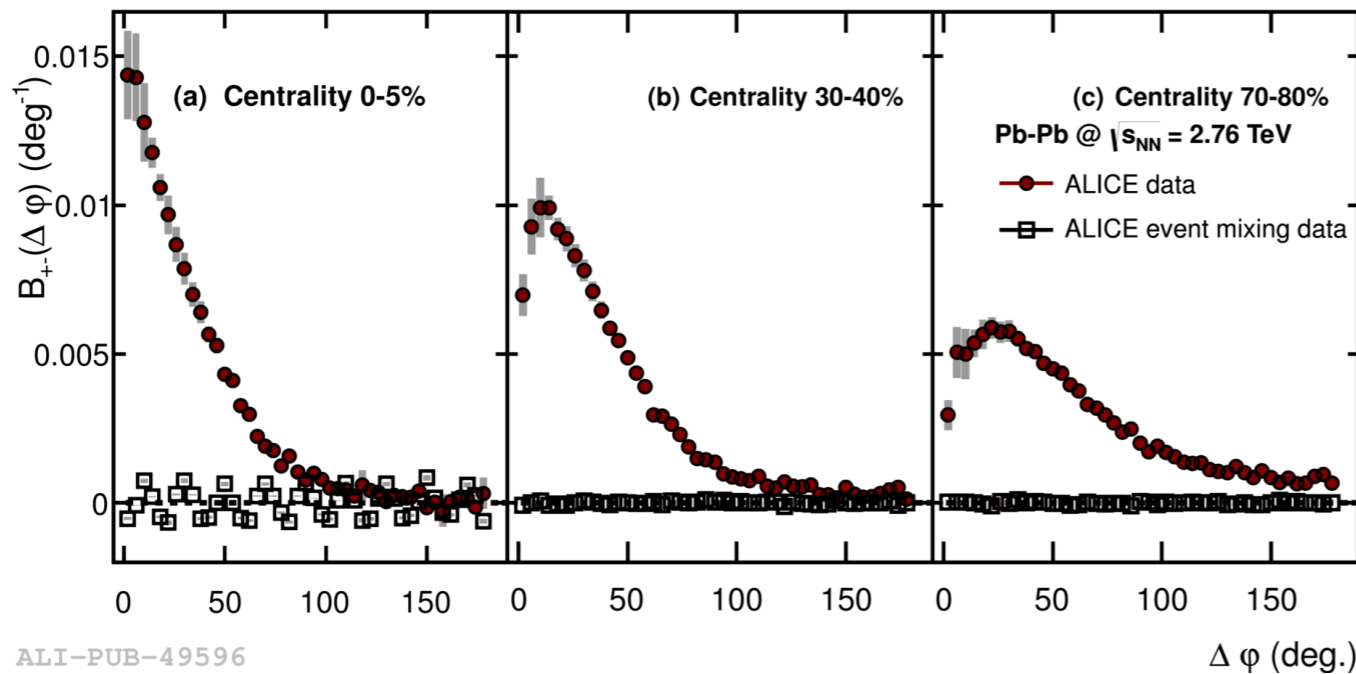
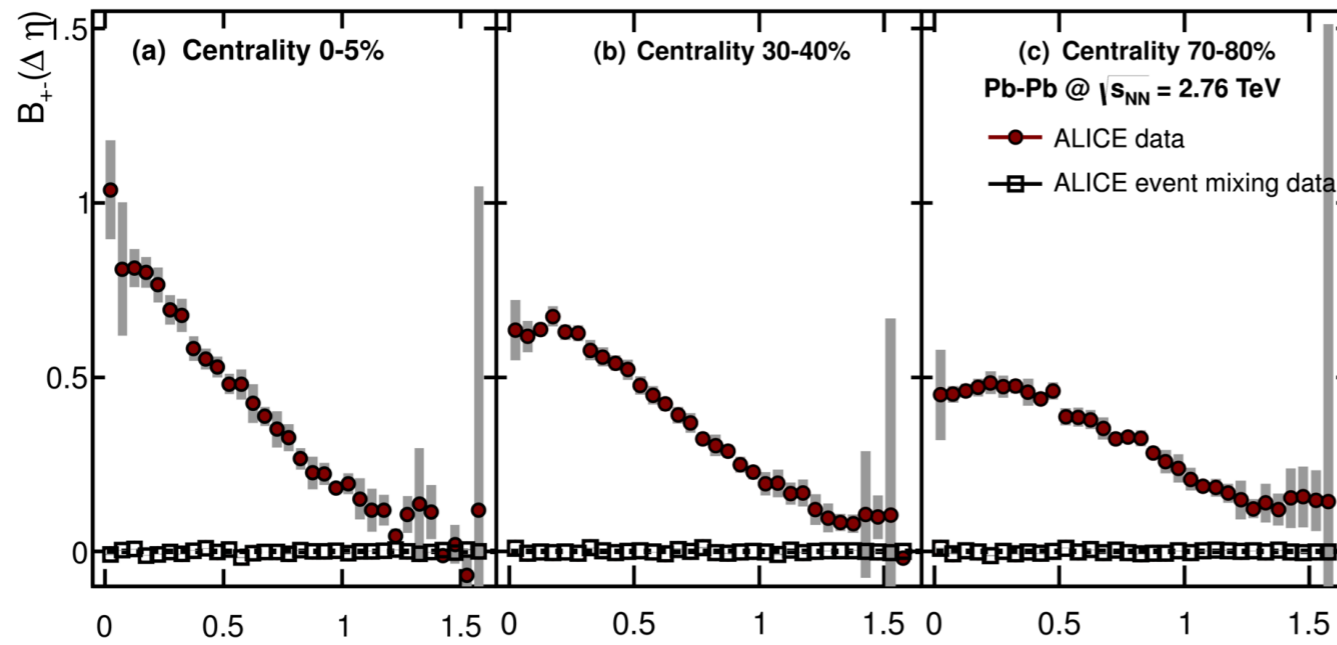
• Motivation:

- Creation of balancing charges in rapidly expanding medium
- What is the time ordering of the collision?
- Can we detect different stages where charges are created?
- Early stage creation: large final separation, **wider balance function**
- Late stage creation: pairs more correlated, **narrower balance functions**
- **BUT:** stronger flow can also lead to a stronger correlation of pairs and a narrow balance function.



Balance function in Pb-Pb collisions

[PLB, 723 (2013), 267]

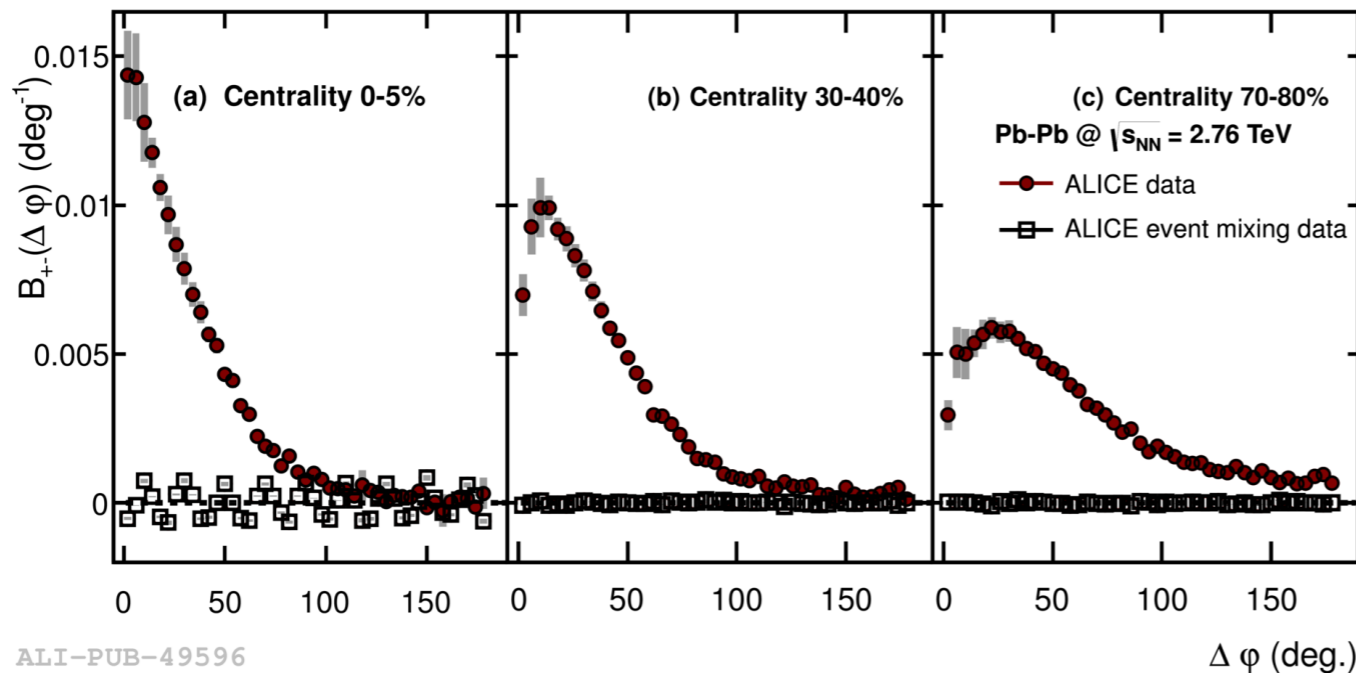
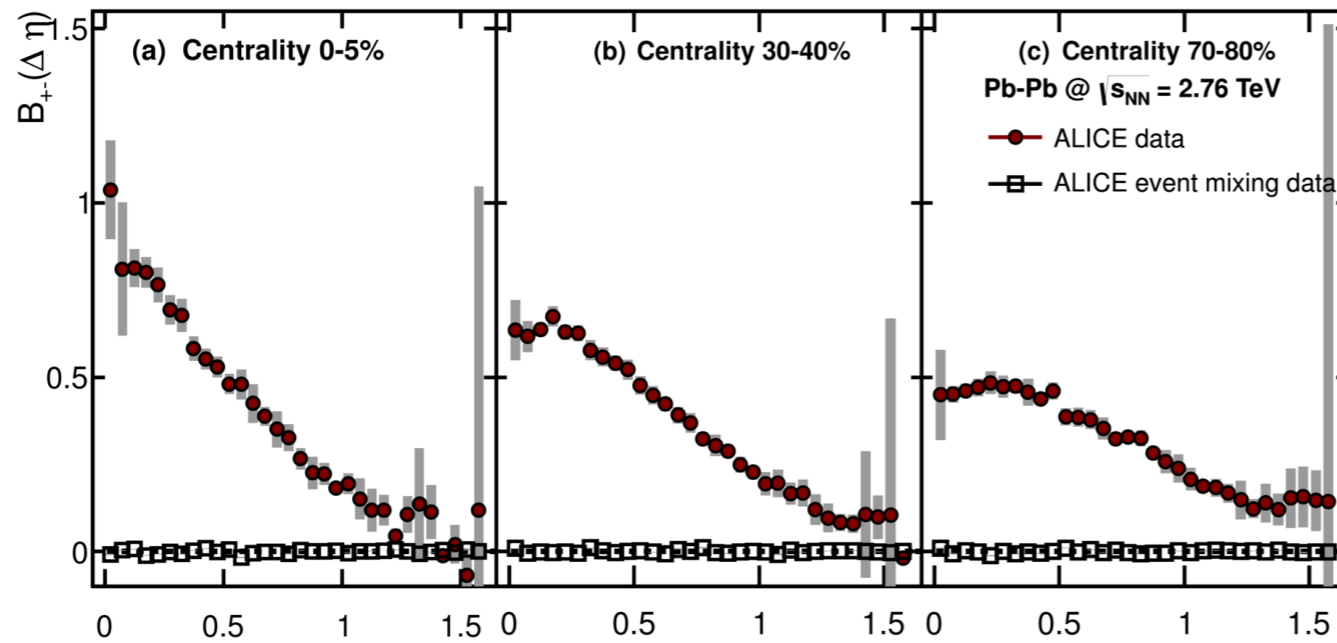


ALI-PUB-49596

Balance function in Pb-Pb collisions

[PLB, 723 (2013), 267]

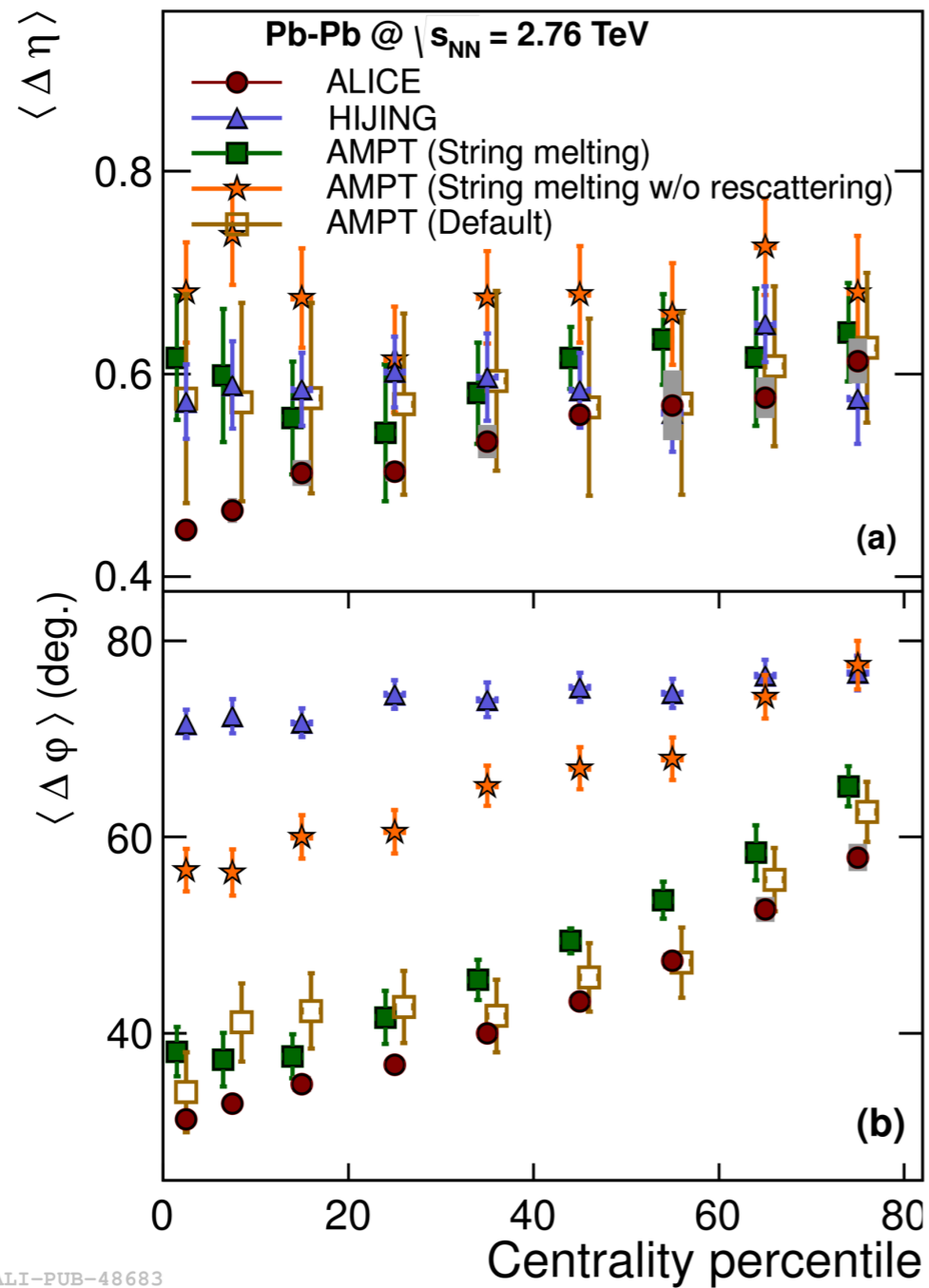
A narrowing is indeed observed in $\Delta\eta$ and $\Delta\phi$ going from peripheral to central collisions.



ALI-PUB-49596

Balance function in Pb-Pb collisions

[PLB, 723 (2013), 267]

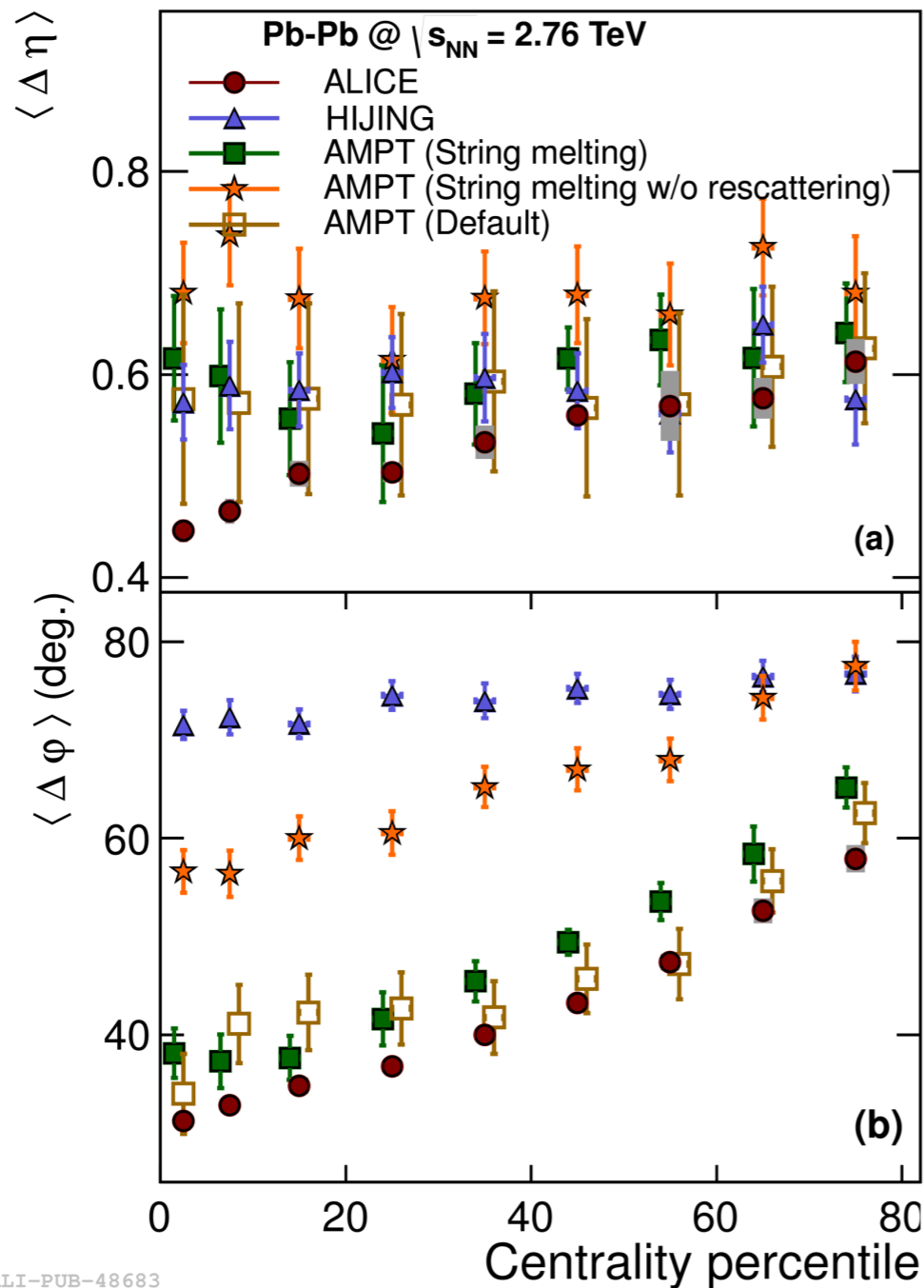


ALI-PUB-48683

A narrowing is indeed observed in $\Delta \eta$ and $\Delta \phi$ going from peripheral to central collisions.

Balance function in Pb-Pb collisions

[PLB, 723 (2013), 267]



ALI-PUB-48683

A narrowing is indeed observed in $\Delta\eta$ and $\Delta\phi$ going from peripheral to central collisions.

The observed centrality dependence is stronger than predicted by models even if they are tuned to reproduce the ALICE v_2 data (AMPT).

Summary & conclusion

Summary and conclusions

- Light flavor hadron yields at LHC energies can be described in a thermal fit based on the hadron resonance gas model with a chemical freeze-out temperature of $T_{\text{chem}} = 156 \text{ MeV}$.
- In order to find deviations from HRG, the measurements of event-by-event fluctuations of conserved quantities (charge, baryon number, strangeness) are on their way...
- Measurements of net-charge fluctuations indicate a reduction of fluctuations from RHIC to LHC (as expected), but also emphasise the importance of systematic studies w.r.t. to the acceptance window etc.

SUPPORTING SLIDES

Thermodynamic susceptibilities (2)

- Moments μ and cumulants K :

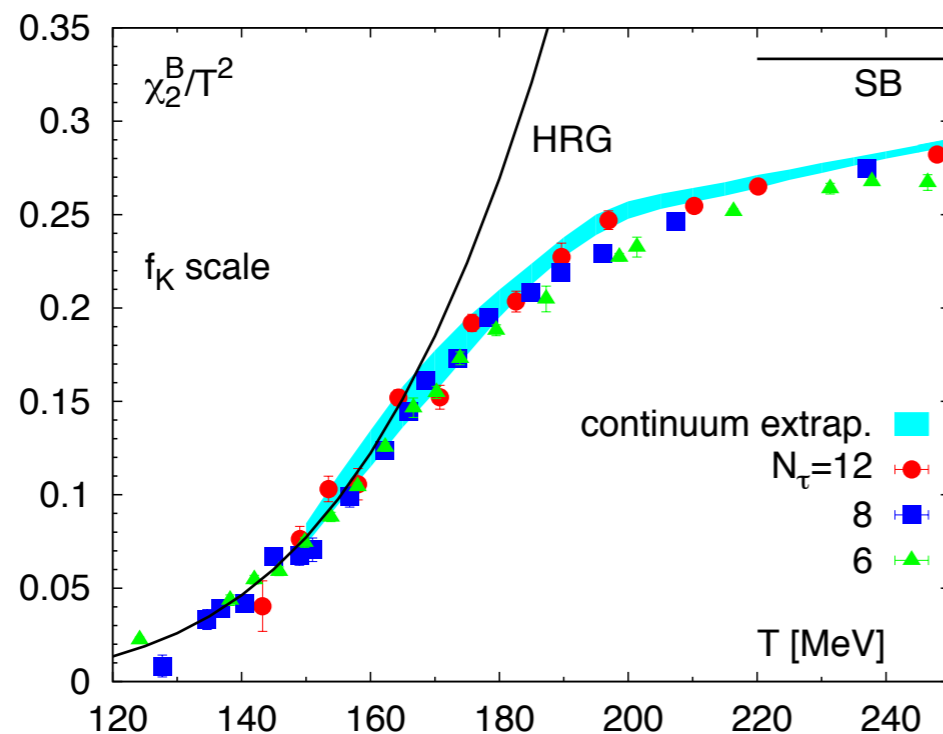
$$\begin{aligned}
 M &= K_1 = \mu = \langle N \rangle = VT^3 \cdot \chi_1 \\
 \sigma^2 &= K_2 = \mu_2 = \langle (\delta N)^2 \rangle = VT^3 \cdot \chi_2 \\
 S &= K_3/\sigma^3 = \mu_3/\sigma^3 = \langle (\delta N)^3 \rangle/\sigma^3 = VT^3 \cdot \chi_3 / (VT^3 \cdot \chi_2)^{3/2} \\
 \kappa &= K_4/\sigma^4 = (\mu_4 - 3\mu_2^2)/\mu_2^2 = \langle (\delta N)^4 \rangle/\sigma^4 - 3 = (VT^3 \cdot \chi_4) / (VT^3 \cdot \chi_2)^2
 \end{aligned}$$

- In ratios of cumulants, the volume dependence cancels:

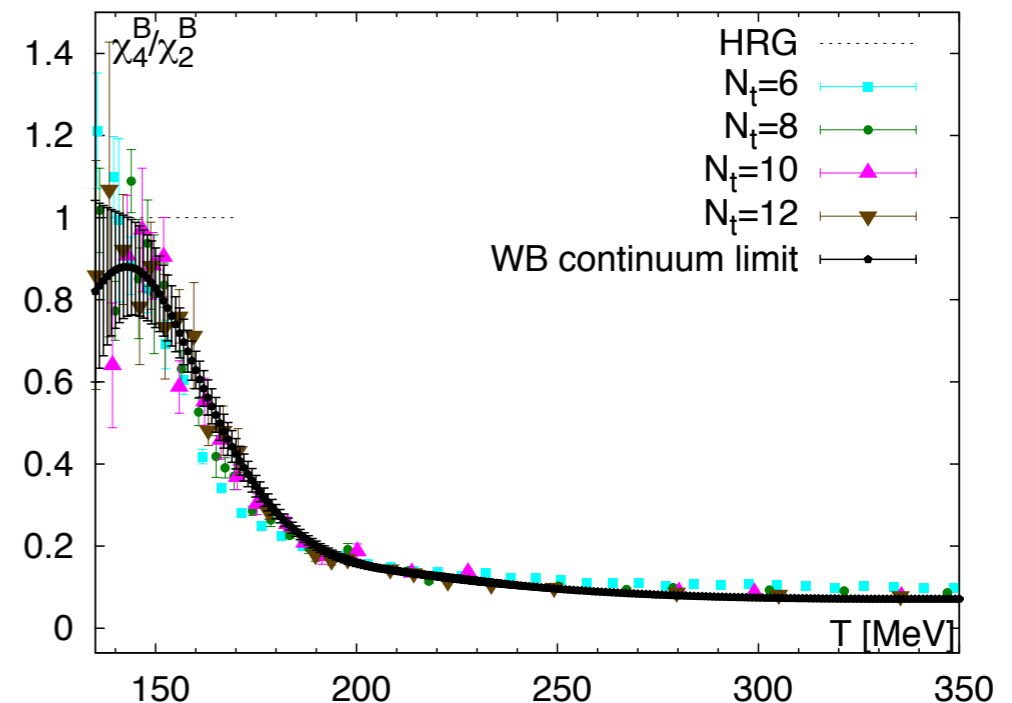
$$\begin{aligned}
 \chi_2/\chi_1 &= K_2/K_1 = \mu_2/\mu = \sigma^2/M \\
 \chi_3/\chi_1 &= K_3/K_1 = \mu_3/\mu = S \cdot \sigma^2/M \\
 \chi_3/\chi_2 &= K_3/K_2 = \mu_3/\mu_2 = S \cdot \sigma \\
 \chi_4/\chi_2 &= K_4/K_2 = (\mu_4 - 3\mu_2^2)/\mu_2^2 = \kappa \cdot \sigma^2 \\
 \chi_6/\chi_2 &= K_6/K_2 = (\mu_6 - 15\mu_4\mu_2 - 10\mu_3^2 + 30\mu_2^3)/\mu_2^2 \quad .
 \end{aligned}$$

Fluctuations and lattice QCD

- Thermodynamic susceptibilities at $\mu_B = 0$ can be directly calculated in lattice QCD.



[1203.0784]



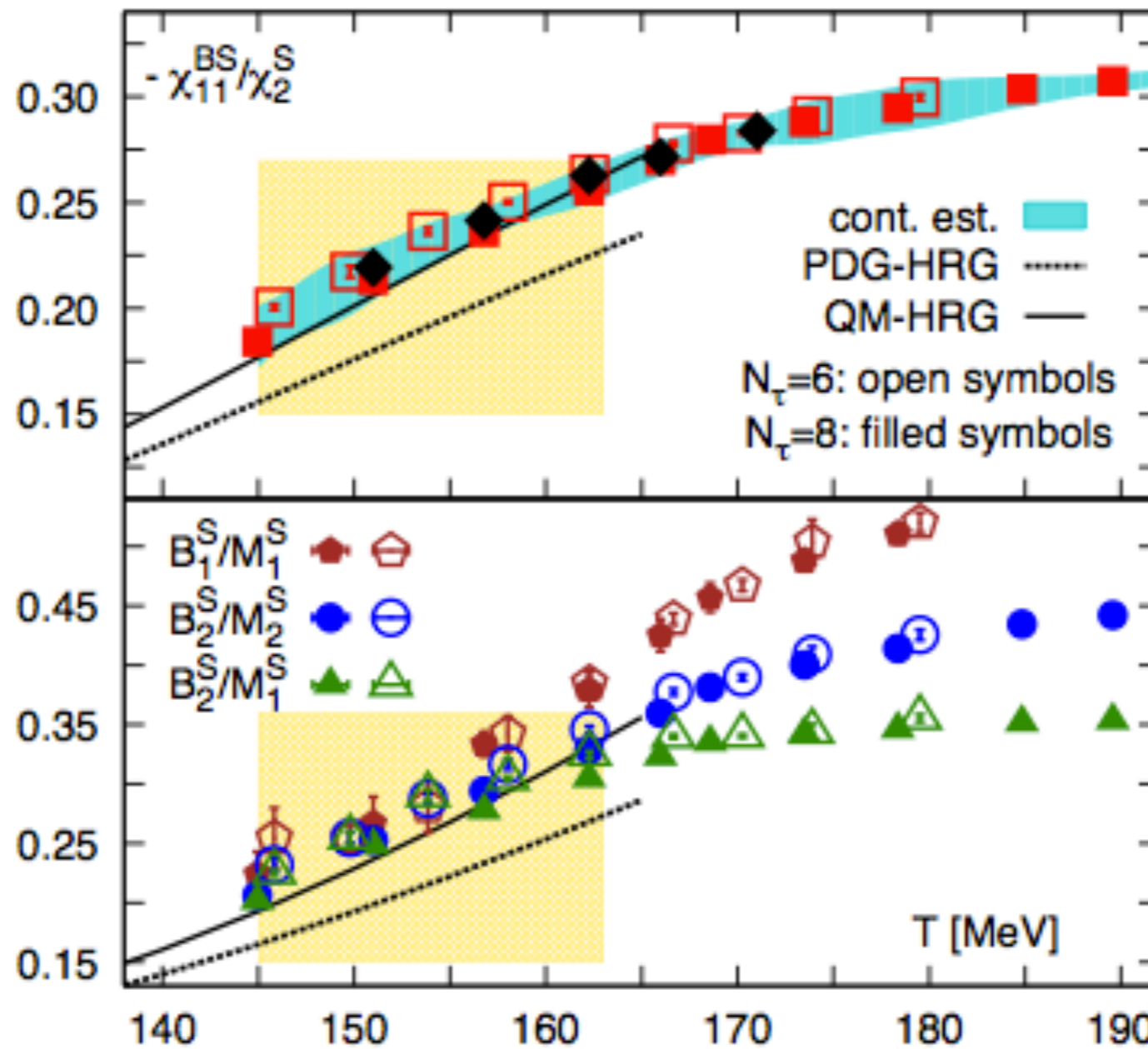
[1305.5161]

- The HRG is a very good approximation below T_c , but significant deviations at T_c are expected with increasing order of the moments due to remnants of the critical chiral behavior:

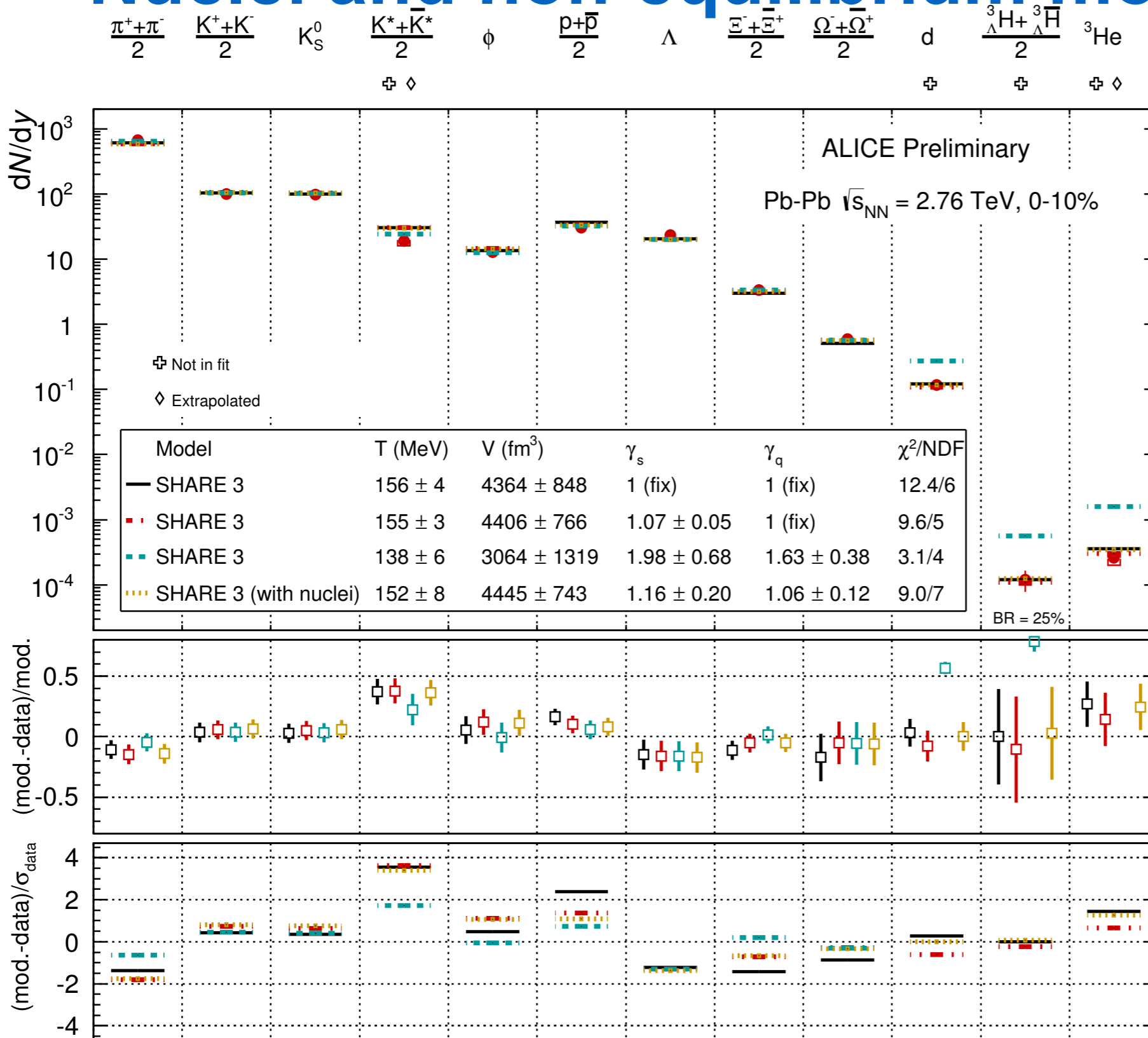
$$\chi_6/\chi_2 < 0 \text{ at } T_c \text{ in Lattice QCD and } \chi_6/\chi_2 = 1 \text{ in HRG}$$

Missing strange resonances (Lattice QCD)

[1404.6511]

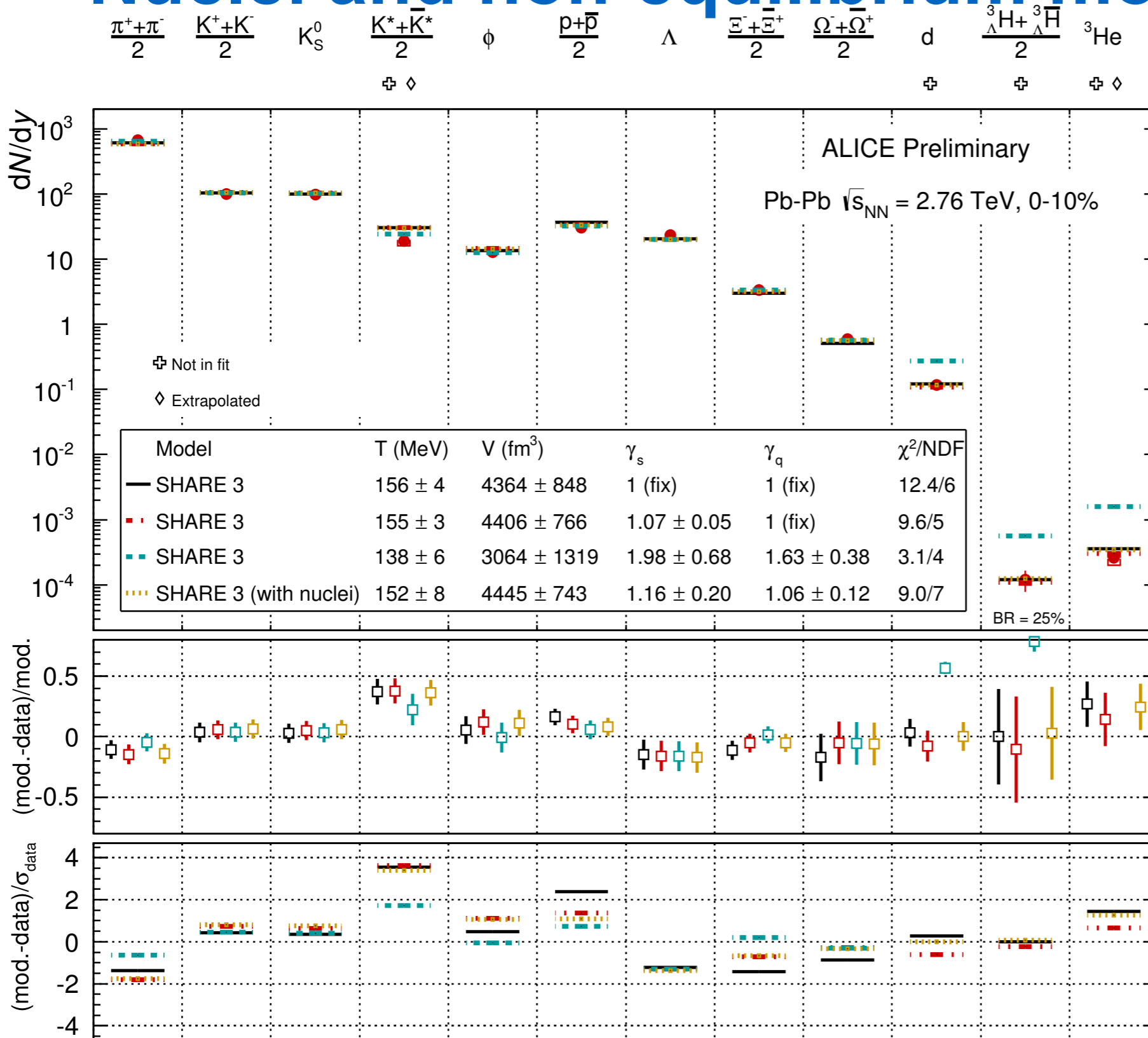


Nuclei and non-equilibrium models

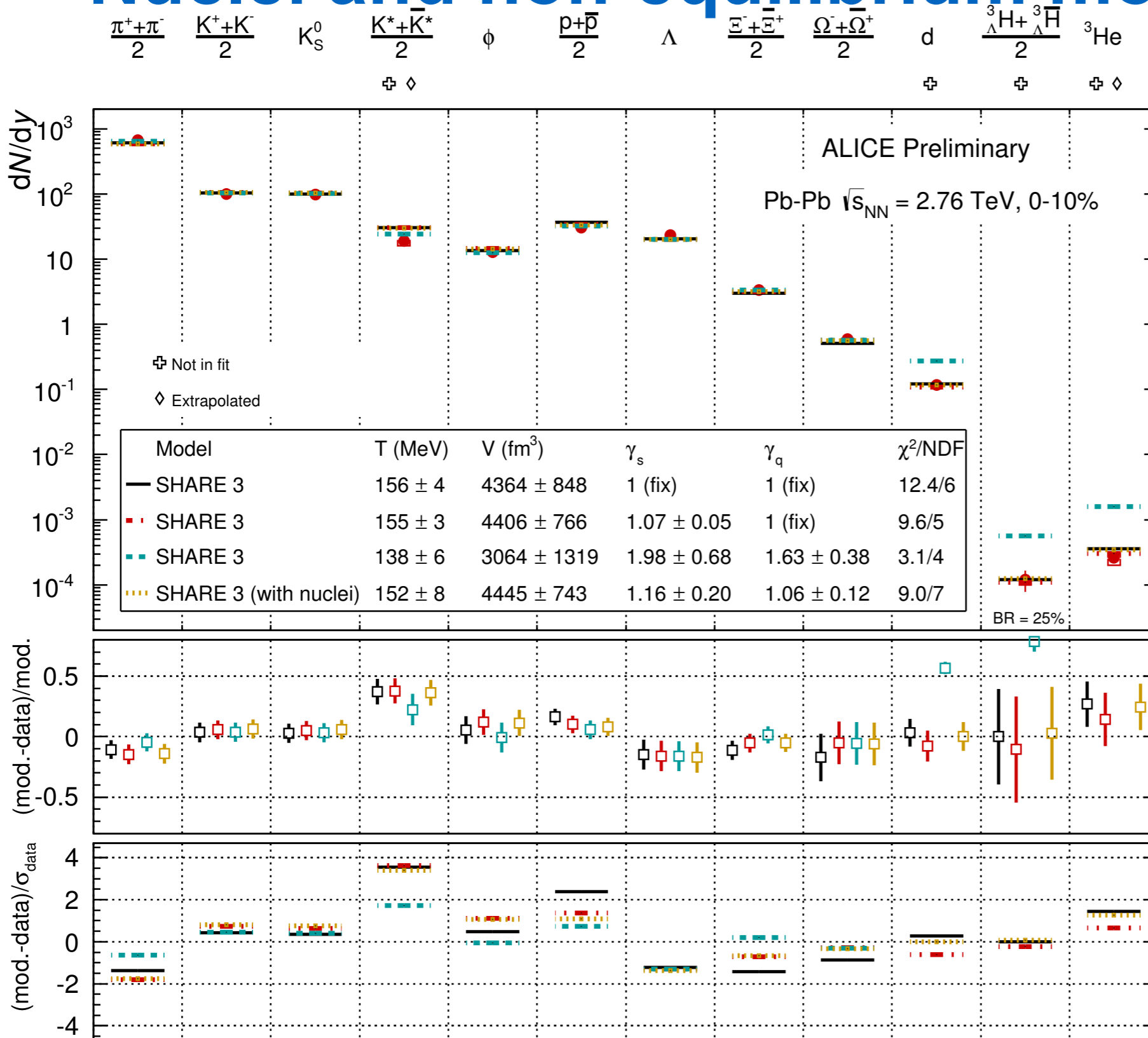


Nuclei and non-equilibrium models

SHARE performs a thermal fit in an equilibrium mode ($\gamma_q = \gamma_s = 1$) or in a non-equilibrium mode (γ_q and γ_s free).



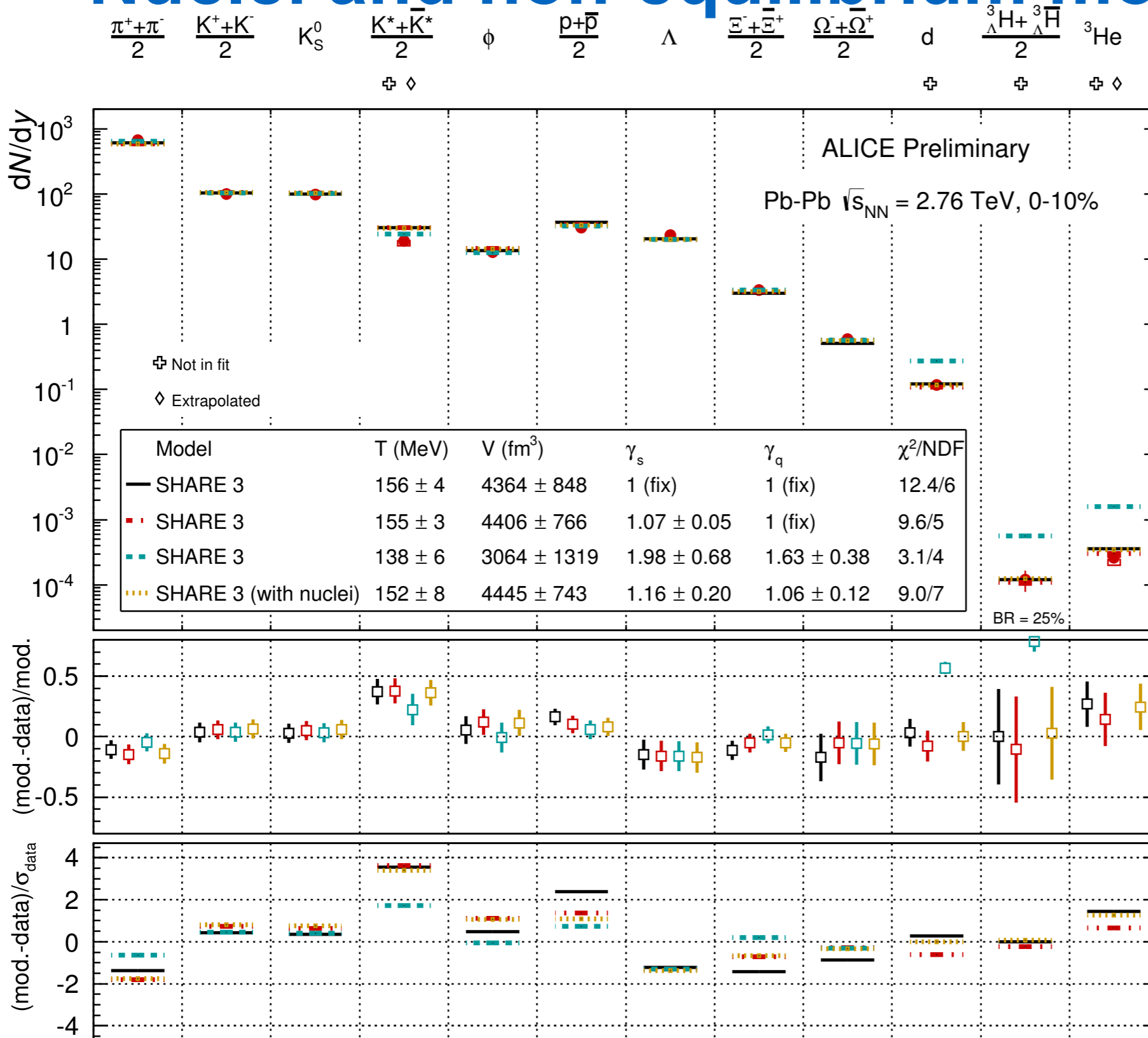
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In equilibrium mode, the model describes the nuclei yields.

Nuclei and non-equilibrium models

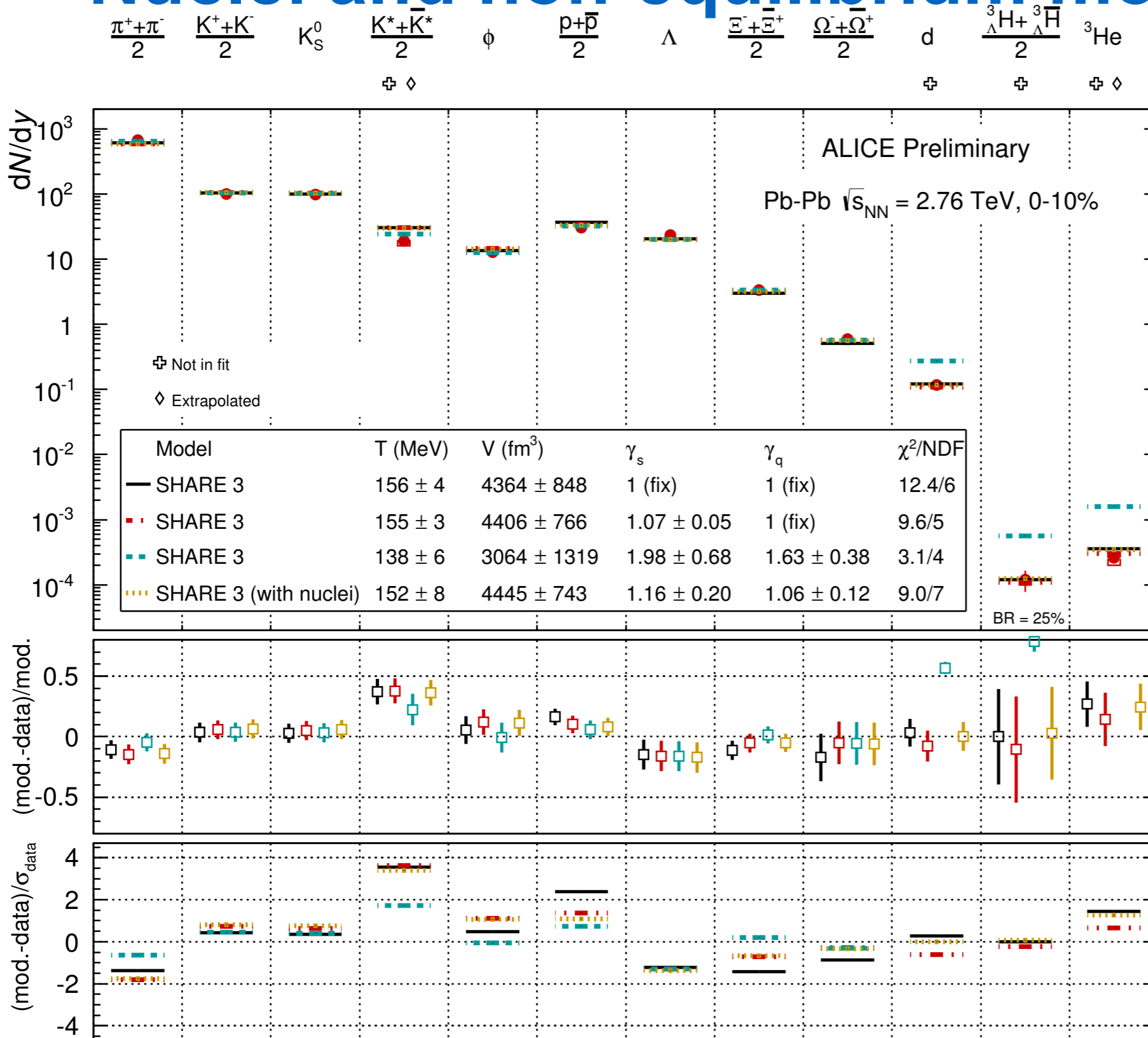


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In non-equilibrium mode and if nuclei are not included, the model converges to values of γ_q and γ_s which are significantly different from 1 and yields a slightly better description for protons and Ξ s.

Nuclei and non-equilibrium models

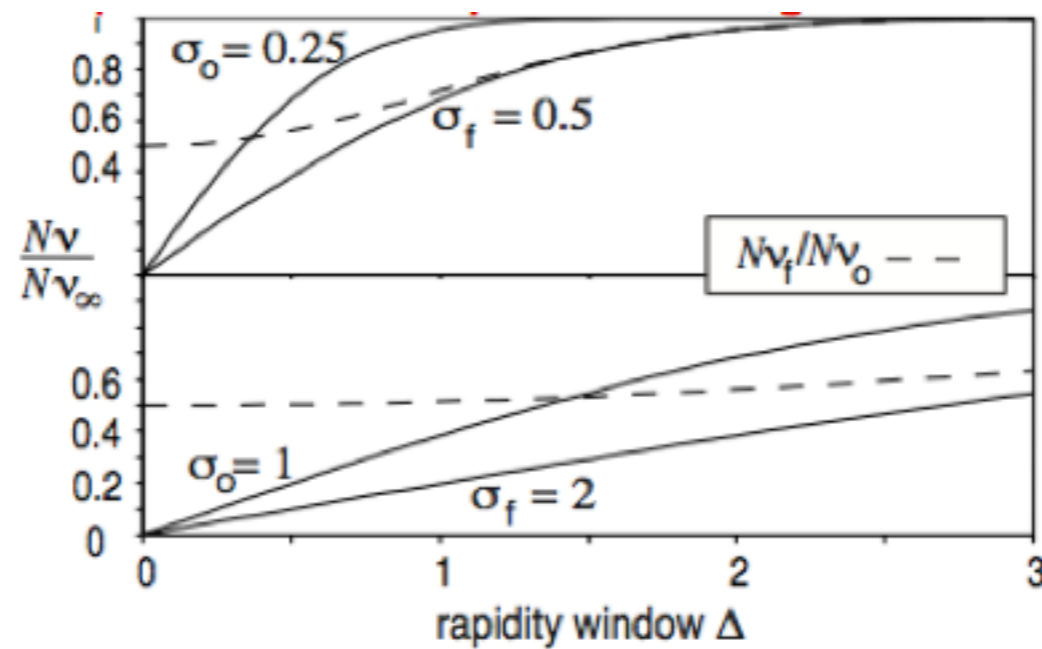


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In non-equilibrium mode and *if nuclei are included*, the model converges to values of γ_q and γ_s which are in agreement with 1.



Ratio indicates the decrease of fluctuations with increase of the width. Diffusion has increased the width from $\sigma_0 = 1$ to $\sigma_f = 2$ (bottom) and $\sigma_0 = 0.25$ to $\sigma_f = 0.5$ (top). σ = width of fluctuations

$$\langle N_{ch} \rangle_{\nu} = \langle N_{ch} \rangle_{\nu_{\infty}} \operatorname{erf} \left(\frac{\Delta \eta}{\sigma \sqrt{8}} \right)$$

[M Aziz and S. Gavin, PRC 70, 034905 (2004)]