

Higgs Physics at the ILC

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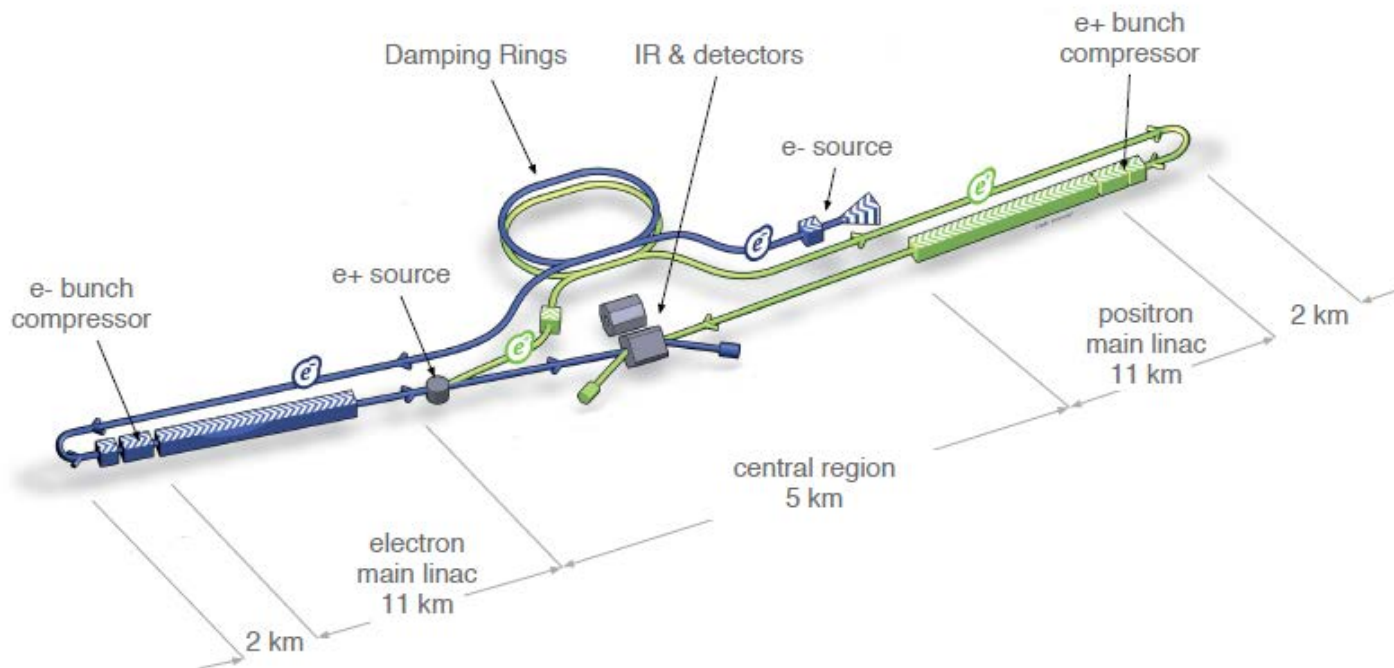
Sep 24, 2015

FCC-ee Workshop on Higgs Physics

ILC International Linear Collider

e^+e^- linear collider with Superconducting RF linac

$250 \leq \sqrt{s} \leq 500$ GeV 31 km in length



ILC Machine Parameters from TDR

			Baseline 500 GeV Machine			L Upgrade	E_{CM} Upgrade	
			250	350	500	500	A 1000	B 1000
Center-of-mass energy	E_{CM}	GeV	250	350	500	500	1000	1000
Collision rate	f_{rep}	Hz	5	5	5	5	4	4
Electron linac rate	f_{linac}	Hz	10	5	5	5	4	4
Number of bunches	n_b		1312	1312	1312	2625	2450	2450
Bunch population	N	$\times 10^{10}$	2.0	2.0	2.0	2.0	1.74	1.74
Bunch separation	Δt_b	ns	554	554	554	366	366	366
Pulse current	I_{beam}	mA	5.8	5.8	5.8	8.8	7.6	7.6
Main linac average gradient	G_a	MV m ⁻¹	14.7	21.4	31.5	31.5	38.2	39.2
Average total beam power	P_{beam}	MW	5.9	7.3	10.5	21.0	27.2	27.2
Estimated AC power	P_{AC}	MW	122	121	163	204	300	300
RMS bunch length	σ_z	mm	0.3	0.3	0.3	0.3	0.250	0.225
Electron RMS energy spread	$\Delta p/p$	%	0.190	0.158	0.124	0.124	0.083	0.085
Positron RMS energy spread	$\Delta p/p$	%	0.152	0.100	0.070	0.070	0.043	0.047
Electron polarization	P_-	%	80	80	80	80	80	80
Positron polarization	P_+	%	30	30	30	30	20	20
Horizontal emittance	$\gamma\epsilon_x$	μm	10	10	10	10	10	10
Vertical emittance	$\gamma\epsilon_y$	nm	35	35	35	35	30	30
IP horizontal beta function	β_x^*	mm	13.0	16.0	11.0	11.0	22.6	11.0
IP vertical beta function	β_y^*	mm	0.41	0.34	0.48	0.48	0.25	0.23
IP RMS horizontal beam size	σ_x^*	nm	729.0	683.5	474	474	481	335
IP RMS vertical beam size	σ_y^*	nm	7.7	5.9	5.9	5.9	2.8	2.7
Luminosity	L	$\times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.75	1.0	1.8	3.6	3.6	4.9
Fraction of luminosity in top 1%	$L_{0.01}/L$		87.1%	77.4%	58.3%	58.3%	59.2%	44.5%
Average energy loss	δ_{BS}		0.97%	1.9%	4.5%	4.5%	5.6%	10.5%
Number of pairs per bunch crossing	N_{pairs}	$\times 10^3$	62.4	93.6	139.0	139.0	200.5	382.6
Total pair energy per bunch crossing	E_{pairs}	TeV	46.5	115.0	344.1	344.1	1338.0	3441.0

Note there are two types of upgrades:

Luminosity upgrade: Install extra klystrons and modulators so number of bunches can be doubled; envisioned after 8 years of baseline running

Energy upgrade: Increase accel. gradient, lengthen linac, or both. TDR config assumes 49 km. length; envisioned after 20 years of running

Luminosity Upgrade for $E_{cm}=250$ GeV

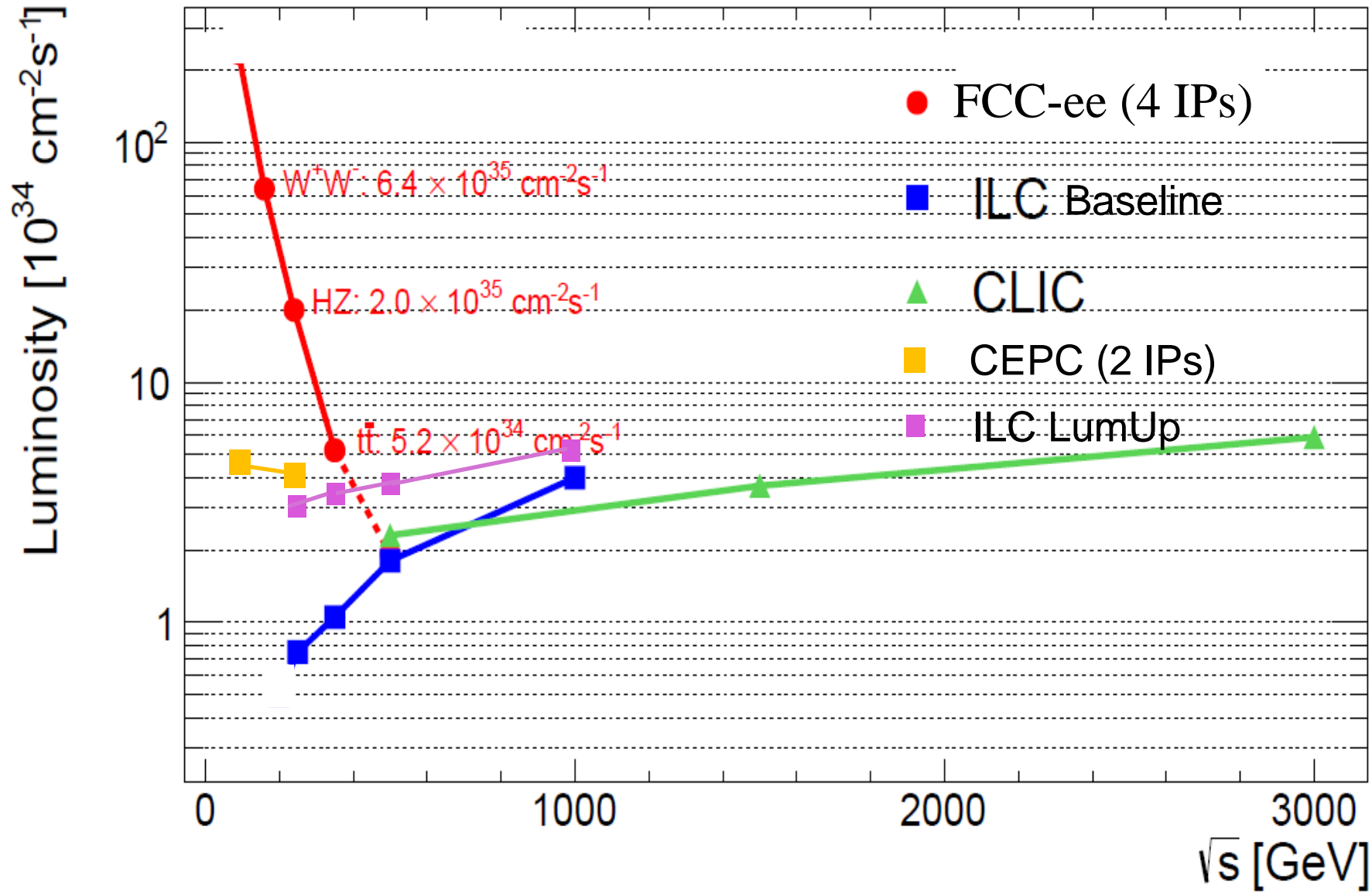
			Baseline ILC	Lumi Upgrade
Center-of-mass energy	E_{CM}	GeV	250	250
Collision rate	f_{rep}	Hz	5	10
Electron linac rate	f_{linac}	Hz	10	10
Number of bunches	n_b		1312	2625
Pulse current	I_{beam}	mA	5.8	8.75
Average total beam power	P_{beam}	MW	5.9	21
Estimated AC power	P_{AC}	MW	129	200
Luminosity	L	$\times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$	0.75	3.0

The $\sqrt{s} = 250$ GeV lumi is quadrupled by doubling the number of bunches *and* the collision rep rate

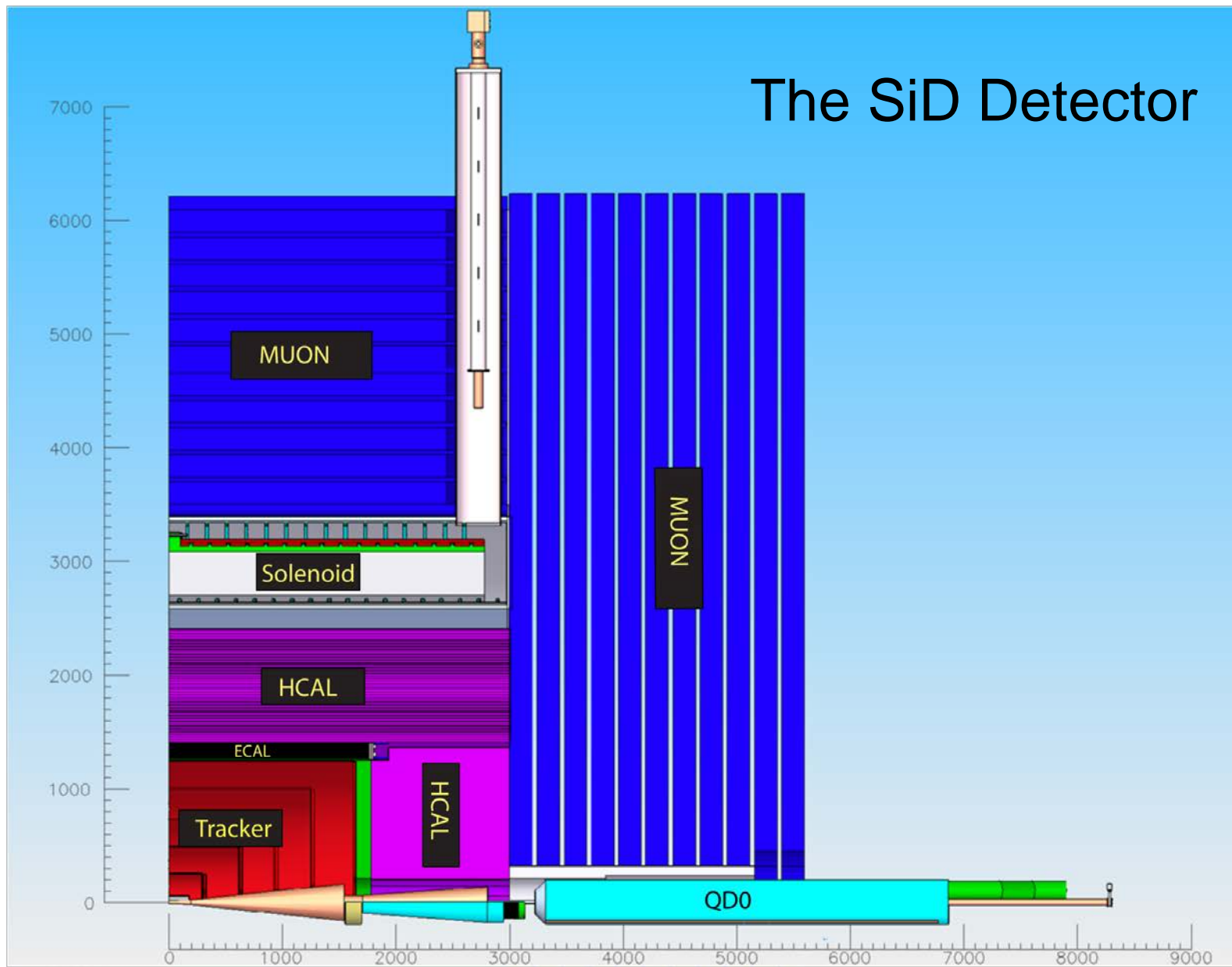
The 10 Hz operation which in the baseline was split between 5 Hz collision and 5 Hz e^+ production is now 100% collision in the lumi upgrade config. A longer undulator should be ready that can produce sufficient e^+ yield with 125 GeV electrons

Note the AC power is 200 MW, the same as the 5 Hz lumi upgrade power at $\sqrt{s} = 500$ GeV.

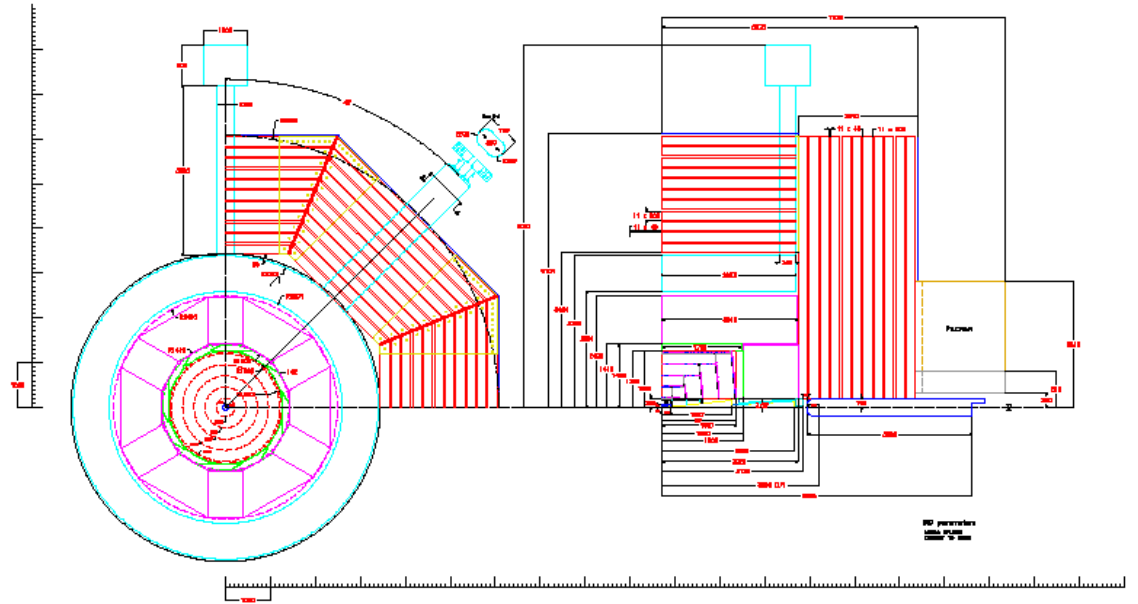
Also note that ILC produces $3 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ luminosity with 200 MW total AC power.



Full Simulation Performed with ILD and/or SiD Detector



SiD Global Parameters



Detector	Technology	Radius (m)		Axial (z) (m)	
		<i>Min</i>	<i>Max</i>	<i>Min</i>	<i>Max</i>
Vertex Detector	Pixels	0.014	0.06		0.18
Central Tracking	Strips	0.206	1.25		1.607
Endcap Tracker	Strips	0.207	0.492	0.85	1.637
Barrel Ecal	Silicon-W	1.265	1.409		1.765
Endcap Ecal	Silicon-W	0.206	1.25	1.657	1.8
Barrel Hcal	RPCs	1.419	2.493		3.018
Endcap Hcal	RPCs	0.206	1.404	1.806	3.028
Coil	5 tesla	2.591	3.392		3.028
Barrel Iron	RPCs	3.442	6.082		3.033
Endcap Iron	RPCs	0.206	6.082	3.033	5.673

Combining barrel and endcaps these trackers and calorimeters cover $|\cos \theta| \leq 0.99$

LumiCal and BeamCal are used for $|\cos \theta| > 0.99$

Pulsed power is possible due to low duty cycle 5 Hz rep rate: eliminates need for cooling

Construct 500 GeV from start

- 500 GeV scenarios study
 - TDR Baseline
 - Emphasizes higher energy - strength of ILC
- Study parameters
 - assume 20 years of operation
 - compare 3 scenarios (studied more)
 - G20, H20, I20
 - Snowmass white paper studied also for comparison
 - arXiv:1310.0763 [hep-ph]

Assumptions

- Full calendar year is assumed to be 8 months at a 75% efficiency (the RDR assumption). This corresponds to $Y = 1.6 \times 10^7$ seconds of integrated running. (significantly higher than a Snowmass year of 10^7 seconds.)
- A **ramp-up** of luminosity performance is in general assumed after:
 - (a) initial construction and after 'year 0' commissioning;
 - (b) after a downtime for a luminosity upgrade;
 - (c) a change in operational mode which may require some learning curve (e.g. going to 10-Hz collisions).
- For initial physics run *after construction and year 0 commissioning*, the RDR ramp of 10%, 30%, 60% and 100% is assumed over the first four years.
- The ramp *after the shutdowns for installation of the luminosity upgrade* is assumed slightly shorter (10%, 50%, 100%) with no year 0.
- *Going down in centre of mass energy* from 500 GeV to 350 GeV or 250 GeV is assumed to have no ramp, since there is no machine modification.
- *Going to 10-Hz operation at 50% gradient* does assume a ramp (25%, 75%, 100%), since 10-Hz affects the entire machine.
- A major 18 month shutdown is assumed for the luminosity upgrade.
- Unlike TDR: 10-Hz and 7-Hz operation assumed at 250 GeV and 350 GeV

Preferred Scenario

	\sqrt{s}	$\int \mathcal{L} dt$	L_{peak}	Ramp				T	T_{tot}	Comment
	[GeV]	[fb ⁻¹]	[fb ⁻¹ /a]	1	2	3	4	[a]	[a]	
Physics run	500	500	288	0.1	0.3	0.6	1.0	3.7	3.7	TDR nominal at 5 Hz
Physics run	350	200	160	1.0	1.0	1.0	1.0	1.3	5.0	TDR nominal at 5 Hz
Physics run	250	500	240	0.25	0.75	1.0	1.0	3.1	8.1	operation at 10 Hz
Shutdown								1.5	9.6	Luminosity upgrade
Physics run	500	3500	576	0.1	0.5	1.0	1.0	7.4	17.0	TDR lumi-up at 5 Hz
Physics run	250	1500	480	1.0	1.0	1.0	1.0	3.2	20.2	lumi-up operation at 10 Hz

Table 7: Scenario H-20: Sequence of energy stages and their real-time conditions.

H-20

	first phase	lumi upgrade	total	Snowmass Lum-up [†]
250 GeV	500 fb ⁻¹	1500 fb ⁻¹	2 ab ⁻¹	1.15 ab ⁻¹
350 GeV	200 fb ⁻¹		0.2 ab ⁻¹	
500 GeV	500 fb ⁻¹	3500 fb ⁻¹	4 ab ⁻¹	1.6 ab ⁻¹
time	8.1 yrs	10.6 yrs	20.2 yrs*	

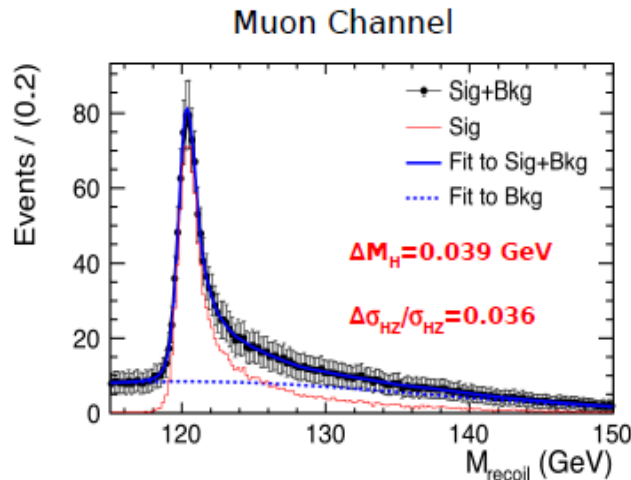
* includes 1.5 years for luminosity upgrade

† ILC Higgs whitepaper: arXiv:1310.0763

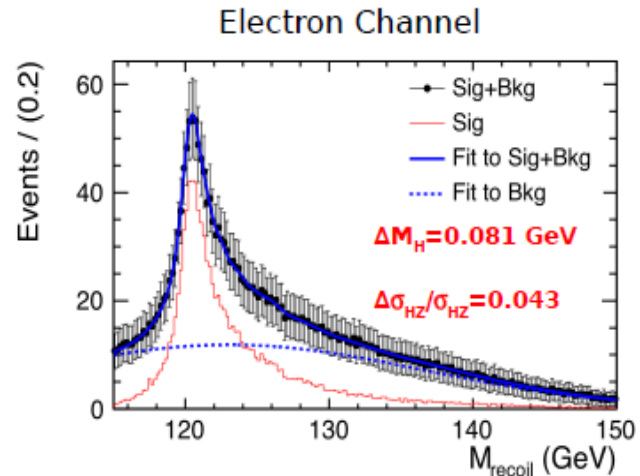
Higgs Physics at the ILC

ILC Measurement of $\sigma(e^+e^- \rightarrow ZH)$ $\sqrt{s} = 250$ GeV

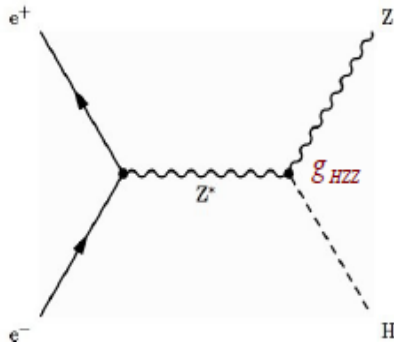
Higgs Recoil Measurement of Higgs Mass and Higgstrahlung Cross Section



Very Precise Measurement
S/B = 8 in Peak Region



Less Precise
Bremsstrahlung in detector material



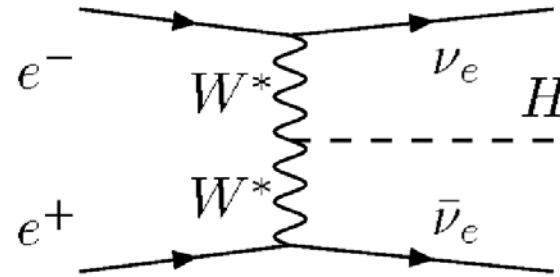
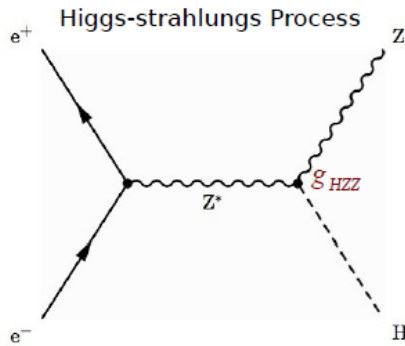
ILC: $\Delta M_H = .032$ GeV, $\Delta \sigma_{HZ} / \sigma_{HZ} = 2.5\%$ for $L = 250 \text{ fb}^{-1}$

$\Delta M_H = .015$ GeV, $\Delta \sigma_{HZ} / \sigma_{HZ} = 1.2\%$ for $L = 1150 \text{ fb}^{-1}$

$$\sigma_{HZ} \sim g_{HZZ}^2$$

$$\Rightarrow \Delta g_{HZZ} / g_{HZZ} = 1.3\% \text{ (0.6\%)} \text{ for } L = 250 \text{ (1150)} \text{ fb}^{-1}$$

$$e^+ e^- \rightarrow ZH, \nu\nu H \quad \sqrt{s} = 350 \text{ GeV}$$

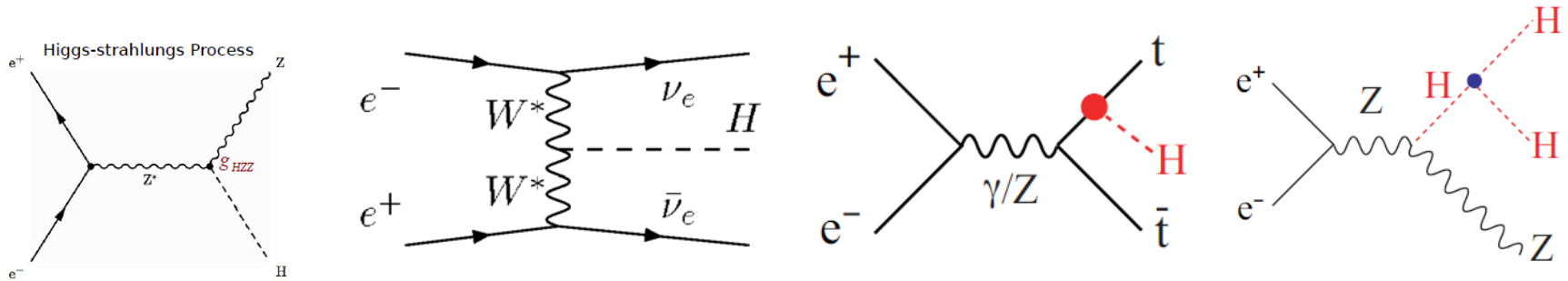


All of the Higgstrahlung studies that were done at $\sqrt{s} = 250 \text{ GeV}$ can also be done at $\sqrt{s} = 350 \text{ GeV}$. Precisions for $\sigma \cdot BR$ are comparable, as is the precision for $\sigma(ZH)$ once $Z \rightarrow q\bar{q}$ decays are included.

WW fusion production of the Higgs at $\sqrt{s} = 350 \text{ GeV}$ provides a much better measurement of g_{HWW} compared to $\sqrt{s} = 250 \text{ GeV}$. This gives a much improved estimate of the total Higgs width Γ_H which in turn significantly improves the coupling errors obtained from $\sigma \cdot BR$ measurements made at $\sqrt{s} = 250 \text{ GeV}$.

The recoil Higgs mass measurement is significantly worse at $\sqrt{s} = 350 \text{ GeV}$ with respect to $\sqrt{s} = 250 \text{ GeV}$. However, there is hope that direct calorimeter Higgs mass measurements using $e^+ e^- \rightarrow \nu\nu H$ will recover the precision.

$$e^+ e^- \rightarrow ZH, \nu\nu H, t\bar{t}H, ZHH \quad \sqrt{s} = 500 \text{ GeV}$$

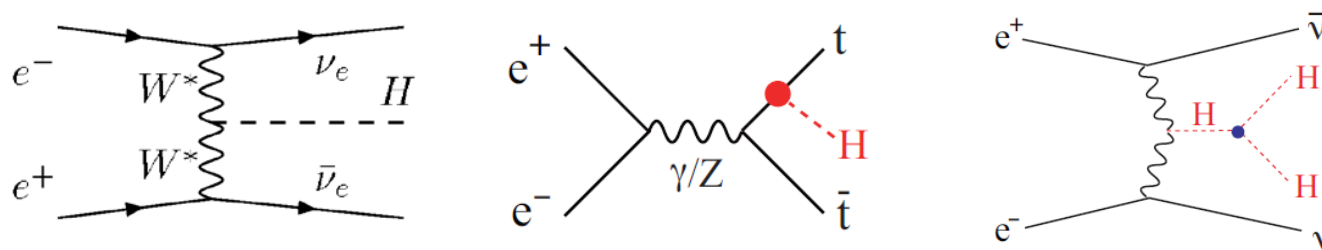


The g_{HWW} coupling can also be measured well at $\sqrt{s} = 500 \text{ GeV}$ through WW fusion production of the Higgs. Also the measurement of $\sigma(e^+e^- \rightarrow \nu\nu H) \times BR(H \rightarrow X)$ can be made for many Higgs decay modes $H \rightarrow X$.

Through $e^+e^- \rightarrow t\bar{t}H$ the top Yukawa coupling can be measured to $\Delta y_t / y_t = 16.6\%$ with 500 fb^{-1} at $\sqrt{s} = 500 \text{ GeV}$. With same luminosity at $\sqrt{s} = 550 \text{ GeV}$ the precision is $\Delta y_t / y_t = 6.73 \Rightarrow$ **strong motivation to increase nominal energy to $\sqrt{s} = 550 \text{ GeV}$**

The ZHH channel is open at $\sqrt{s} = 500 \text{ GeV}$. The Higgs self coupling can be measured to 27% with 4 ab^{-1} assuming the true value is the SM value.

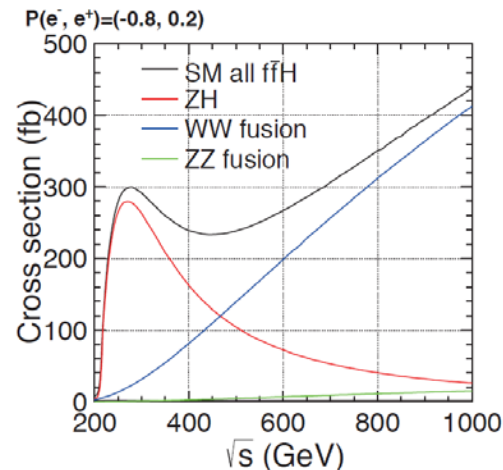
$e^+e^- \rightarrow \nu\nu H, ttH, \nu\nu HH$ ILC Energy Upgrade $\sqrt{s} = 1$ TeV



At $\sqrt{s} = 1$ TeV the ILC provides better measurements of the top Yukawa coupling and Higgs self coupling. For example the Higgs self coupling can be measured to an accuracy of 10% with 4 ab^{-1} at $\sqrt{s} = 1$ TeV (again, assuming the true value is the SM value).

Search for additional Higgs bosons that might have been missed at LHC.

In addition, the ILC becomes a Higgs factory again since the total Higgs cross section is larger than the total cross sections at 250 GeV, specially if polarized beams are used:



Summary of ILC Higgs Measurement Precisions

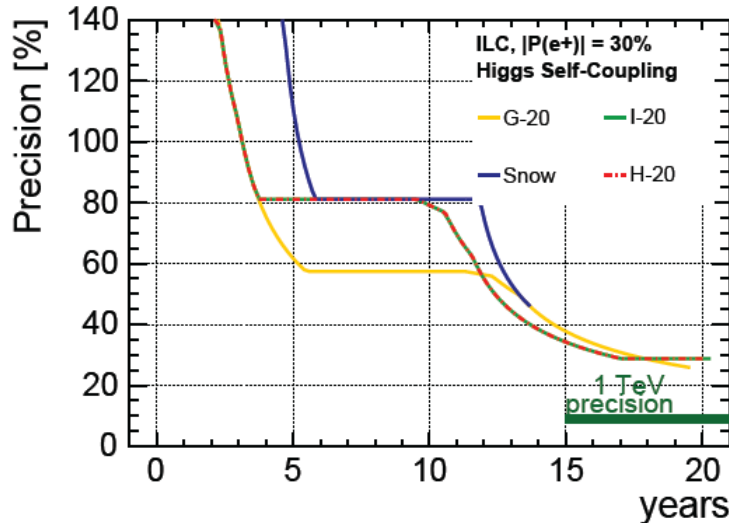
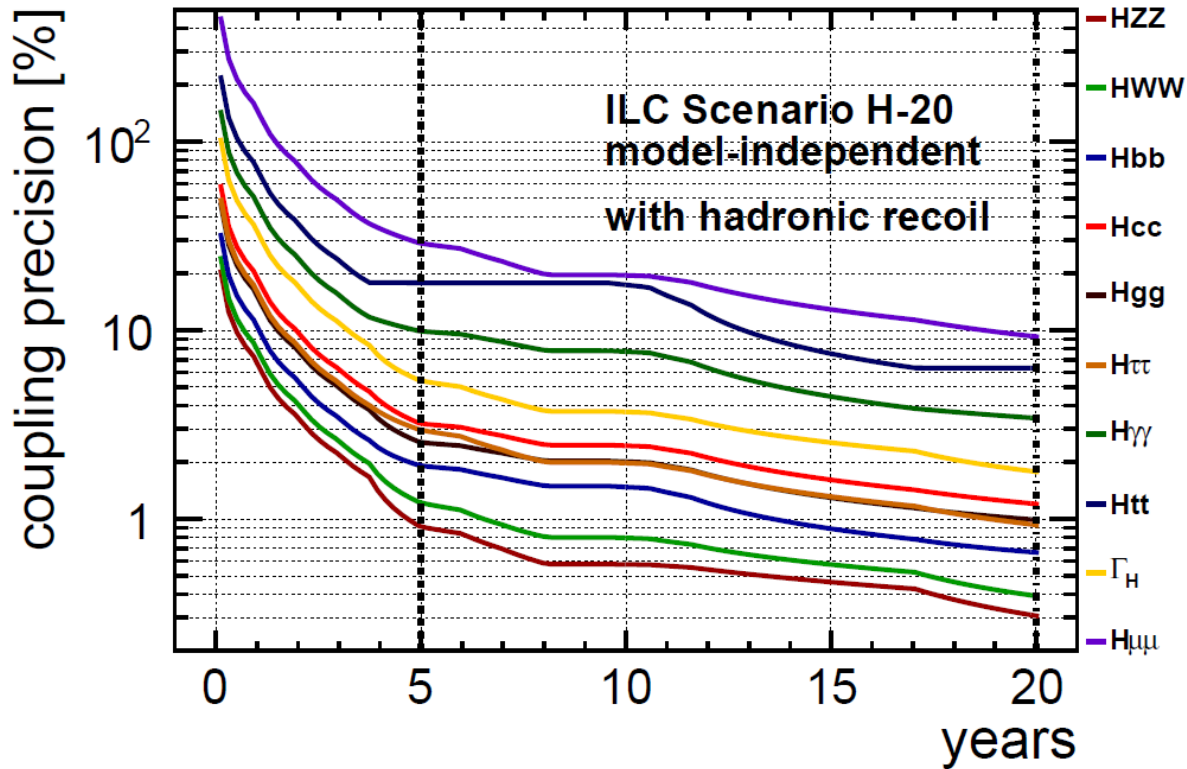
From "500 GeV ILC Operating Scenarios" arXiv : 1506.07830

$\int \mathcal{L} dt$ at \sqrt{s}	250 fb ⁻¹ at 250 GeV		330 fb ⁻¹ at 350 GeV		500 fb ⁻¹ at 500 GeV		
$P(e^-, e^+)$	(-80%, +30%)						
production	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	$t\bar{t}h$
$\Delta\sigma/\sigma$	[39] 2.0%	-	[10, 40] 1.6%	-	3.0	-	-
BR(invis.) [41]	< 0.9%	-	< 1.2%	-	< 2.4%	-	-
decay	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$						
$h \rightarrow bb$	1.2%	10.5%	1.3%	1.3%	1.8%	0.7%	28%
$h \rightarrow c\bar{c}$	8.3%	-	9.9%	13%	13%	6.2%	-
$h \rightarrow gg$	7.0%	-	7.3%	8.6%	11%	4.1%	-
$h \rightarrow WW^*$	6.4%	-	6.8%	5.0%	9.2%	2.4%	-
$h \rightarrow \tau^+\tau^-$	[42] 3.2%	-	[43] 3.5%	19%	5.4%	9.0%	-
$h \rightarrow ZZ^*$	19%	-	22%	17%	25%	8.2%	-
$h \rightarrow \gamma\gamma$	34%	-	34%	[44] 39%	34%	[44] 19%	-
$h \rightarrow \mu^+\mu^-$ [45]	72%	-	76%	140%	88%	72%	-

For scenario H-20 with 2 ab⁻¹ at 250 GeV and 4 ab⁻¹ at 500 GeV the ILC has

$$\frac{\Delta\sigma(ZH)}{\sigma(ZH)} = 0.59\% \quad \text{and} \quad \frac{\Delta\sigma(\nu\bar{\nu}H) \cdot BR(H \rightarrow b\bar{b})}{\sigma(\nu\bar{\nu}H) \cdot BR(H \rightarrow b\bar{b})} = 0.25\%$$

ILC Higgs Coupling Precision vs Time



Higgs Physics: ILC vs FCC-ee

Take FCC-ee errors on σ and $\sigma \cdot \text{BR}$ from arXiv:1308.6176 assuming 240+350 GeV with 10.0 + 2.6 ab^{-1} :

	TLEP 240
σ_{HZ}	0.4%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \text{bb})$	0.2%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \text{c}\bar{\text{c}})$	1.2%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \text{gg})$	1.4%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \text{WW})$	0.9%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \tau\tau)$	0.7%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \text{ZZ})$	3.1%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \gamma\gamma)$	3.0%
$\sigma_{\text{HZ}} \times \text{BR}(\text{H} \rightarrow \mu\mu)$	13%

$\sigma_{\text{WW} \rightarrow \text{H}} \times \text{BR}(\text{H} \rightarrow \text{b}\bar{\text{b}})$

\sqrt{s} (GeV)	TLEP
240 - 250	2.2%
350	0.6%

The additional events from the Higgs-strahlung process at 350 GeV allow the statistical precision for all the aforementioned measurements to be improved by typically 5% for TLEP with respect to the sole 240 GeV data.

→ Branching fraction to invisible tested directly to 0.19% @ 95% CL

Take ILC errors on σ and $\sigma \cdot \text{BR}$ from arXiv:1506.07830 assuming 250+350+500 GeV with either:

0.5+0.2+5.0 ab^{-1} (G-20 scenario) or 2.0+0.2+4.0 ab^{-1} (H-20 scenario)

Perform model independent fit of b,c,g,W, τ ,Z, γ , μ ,invis Higgs couplings and total width using standard program (from Michael Peskin) for ILC & FCC-ee separately and combined.

The coupling fit results I obtain for FCC-ee alone differ slightly from those reported in arXiv:1308.6176

Coupling	arXiv:1308.6176	My fit
g_{HZZ}	0.15%	0.19%
g_{HWW}	0.19%	0.35%
g_{Hbb}	0.42%	0.52%
g_{Hcc}	0.71%	0.78%
g_{Hgg}	0.80%	0.85%
$g_{H\tau\tau}$	0.54%	0.63%
$g_{H\mu\mu}$	6.2%	6.2%
$g_{H\gamma\gamma}$	1.5%	1.5%



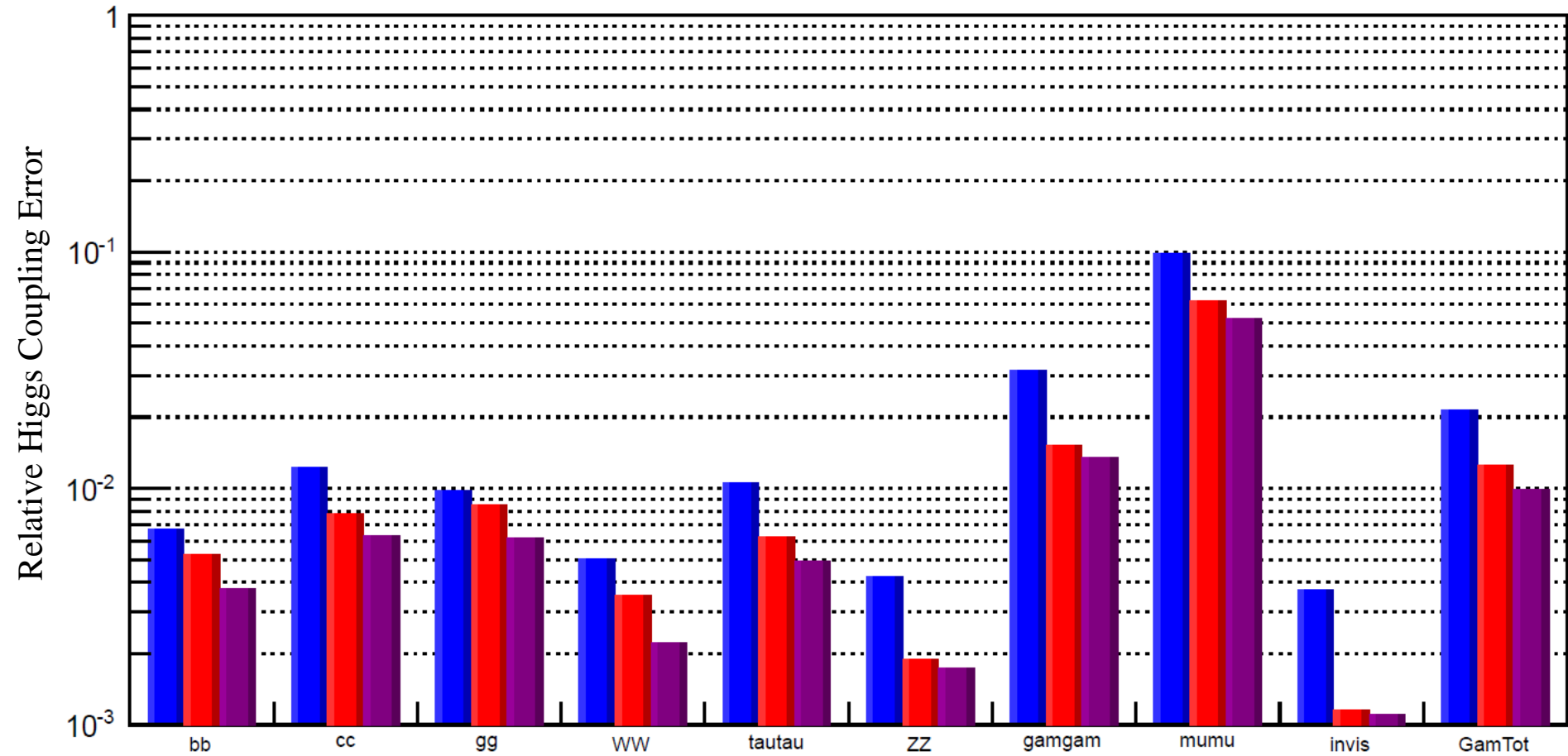
Because it is the only way to consistently combine FCC-ee and ILC results I will, for the rest of the talk, use these results for FCC-ee.

The discrepancy is not understood at this time -- will try to clear it up at a later date.

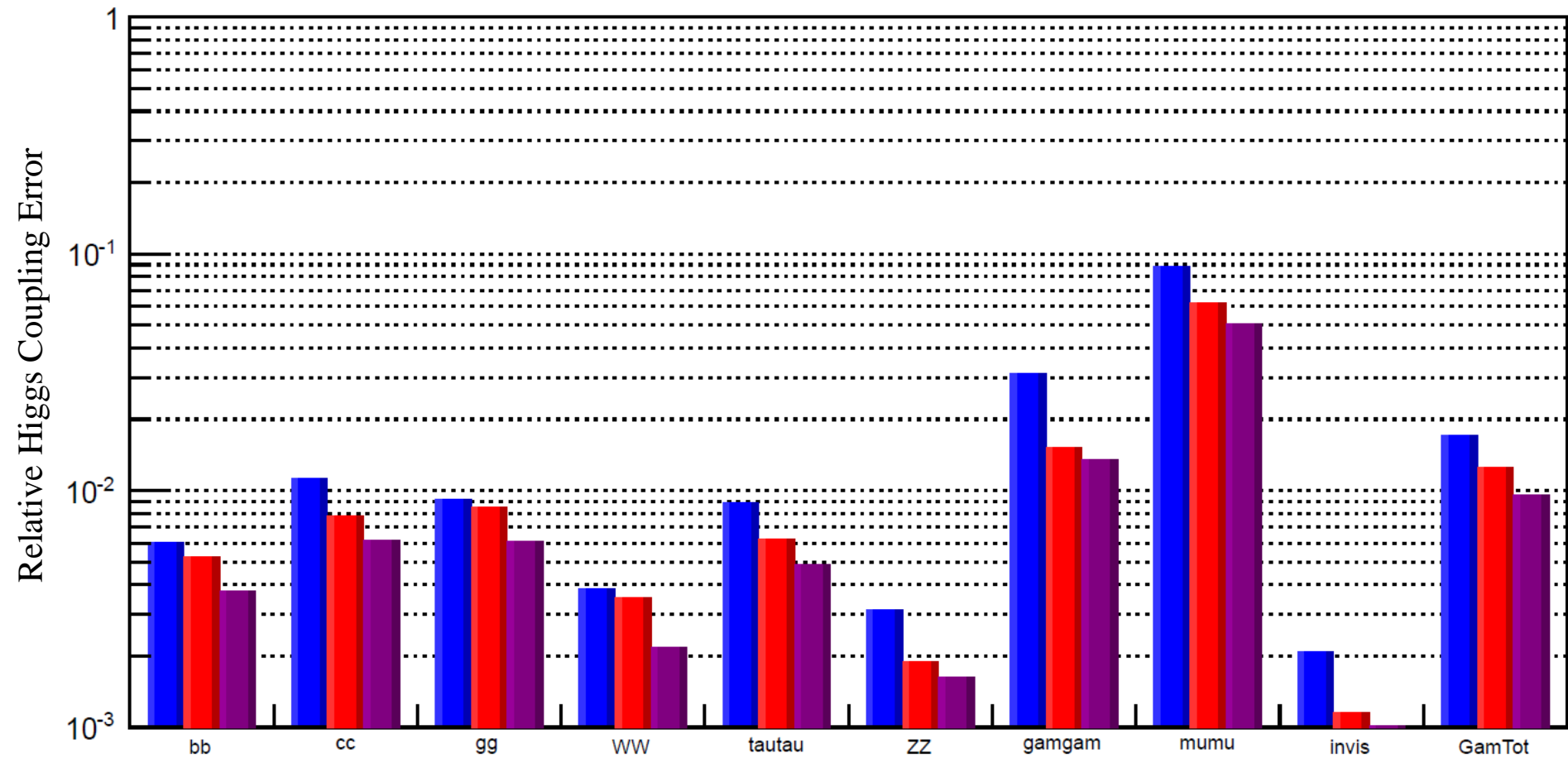
■ ILC 250+350+500 GeV with 0.5+0.2+5.0 fb⁻¹ (G-20 scenario)

■ FCC-ee 240+350 GeV with 10.0 + 2.6 ab⁻¹

■ ILC + FCC-ee under the conditions listed above



- ILC 250+350+500 GeV with 2.0+0.2+4.0 ab^{-1} (H-20 scenario)
- FCC-ee 240+350 GeV with 10.0 + 2.6 ab^{-1}
- ILC + FCC-ee under the conditions listed above

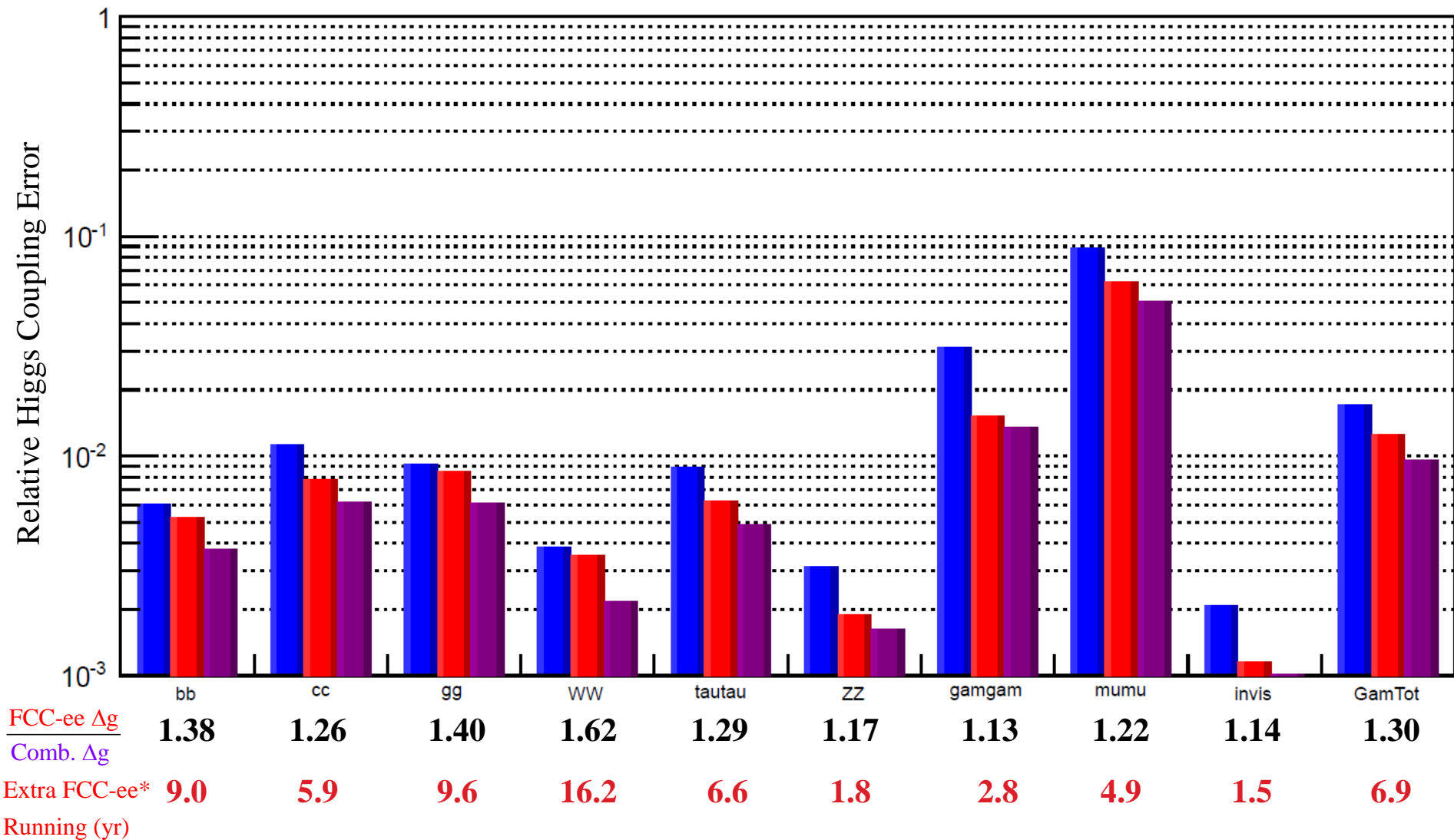


■ ILC 250+350+500 GeV with 2.0+0.2+4.0 ab^{-1} (H-20 scenario)

■ FCC-ee 240+350 GeV with 10.0 + 2.6 ab^{-1}

■ ILC + FCC-ee under the conditions listed above

How does ILC help FCC-ee?



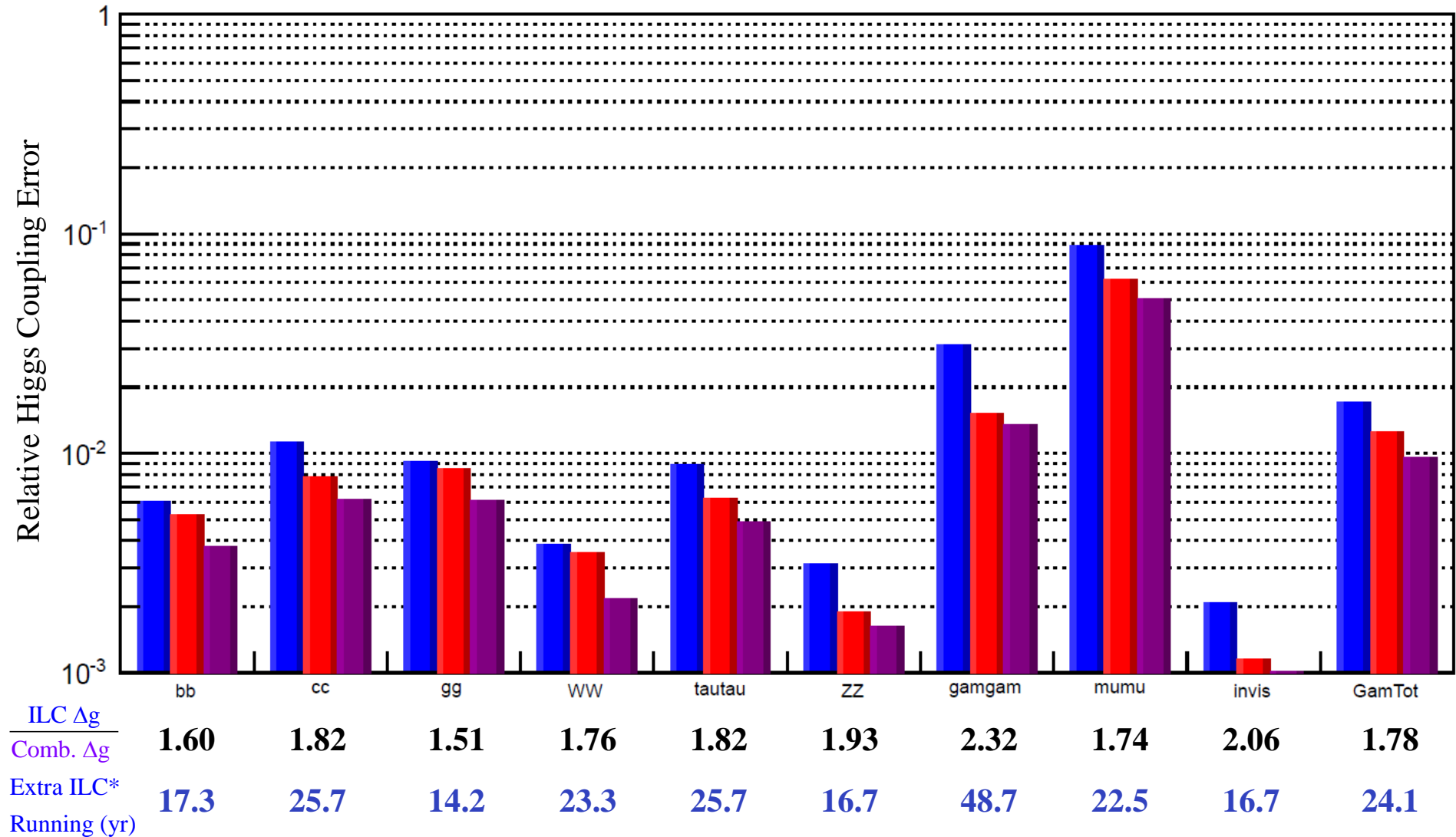
*Additional FCC-ee running required to match ILC contribution to Combination. Assumes the same 10:2.6 luminosity ratio for 240:350 GeV except ZZ & invis which assume that all extra running is at 240 GeV

■ ILC 250+350+500 GeV with 2.0+0.2+4.0 ab^{-1} (H-20 scenario)

■ FCC-ee 240+350 GeV with 10.0 + 2.6 ab^{-1}

■ ILC + FCC-ee under the conditions listed above

How does FCC-ee help ILC ?

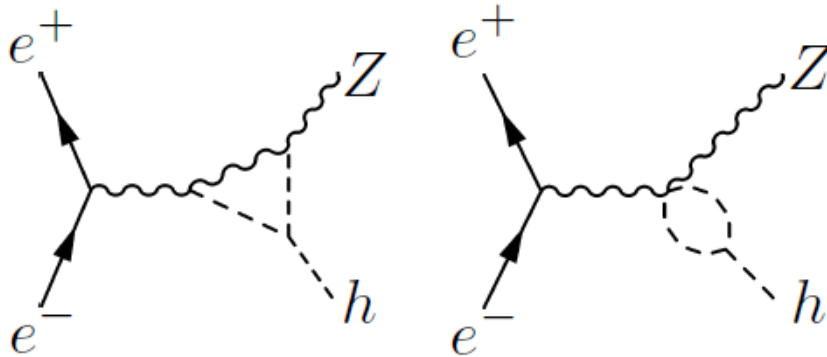


*Additional ILC running required to match FCC-ee contribution to Combination. Assumes the same 1:2 luminosity ratio for 250:500 GeV except ZZ & invis which assumes all extra running at 250 GeV.

Highlights of Combination of FCC-ee with ILC H-20

	ILC	FCC-ee	ILC+FCC-ee
Δg_{HZZ}	0.31%	0.19%	0.16%
Δg_{HWW}	0.38%	0.35%	0.22%
Δg_{Hbb}	0.60%	0.52%	0.38%
$\Delta g_{H\tau\tau}$	0.89%	0.63%	0.49%
Δg_{Hgg}	0.92%	0.85%	0.61%

FCC-ee Higgs Self Coupling Measurement at $E_{cm}=240$ GeV



M. McCullough, arXiv:1312.3322

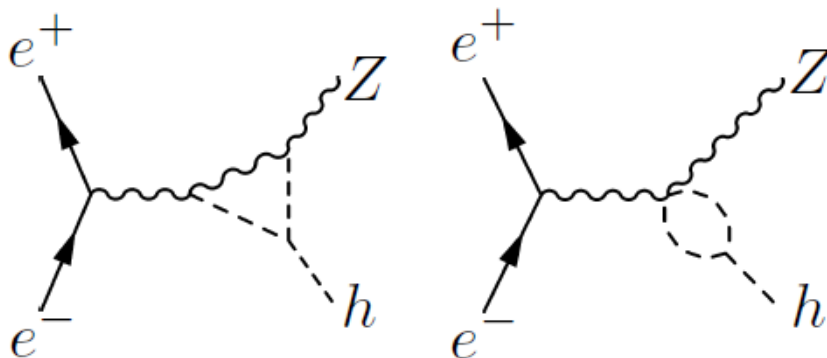
$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

g_{hZZ} fixed to SM value ($\delta_z = 0$)

g_{hhZZ} fixed to SM value

$$\Rightarrow \delta_H = \frac{\delta_{\sigma}^{240}}{0.014} = \frac{0.004}{0.014} = 29\%$$

FCC-ee Higgs Self Coupling Measurement at E_{cm}=240 GeV



M. McCullough, arXiv:1312.3322

$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

g_{hZZ} fixed to SM value ($\delta_z = 0$)

g_{hhZZ} fixed to SM value

$$\Rightarrow \delta_H = \frac{\delta_{\sigma}^{240}}{0.014} = \frac{0.004}{0.014} = 29\%$$

Examples of BSM physics with $\delta_z \neq 0$:

Neutral scalar partners

Canonically normalize kinetic term → shift all Higgs couplings

Shift drops out of all coupling ratios; can't be measured at LHC.

But measure $\delta\sigma_{Zh}$ directly at CEPC via Z recoils.

(Not-so) Hidden New Physics

Higgs mixes w/ heavy resonances, couplings dictated by symmetries (as in the chiral Lagrangian)

$\kappa_V \sim \sqrt{1 - \frac{v^2}{f^2}} \approx 1 - \frac{v^2}{2f^2} + \dots$

f = decay constant of pNGB Higgs

Coupling deviation contributes to precision electroweak

Pre-LHC constraints as good as reach of LHC Higgs coupling measurements

Neutral fermionic partners

e.g. *Twin Higgs*

No direct sensitivity @ LHC

Higgs is a pNGB, coupling deviations like those of composite Higgs models

$\kappa_V \sim \sqrt{1 - \frac{v^2}{f^2}} \approx 1 - \frac{v^2}{2f^2} + \dots$

f sets mass scale for neutral top partners; definitive and test of "neutral" naturalness.

Results: Inert Doublet

As expected, corrections to associated production are observable!

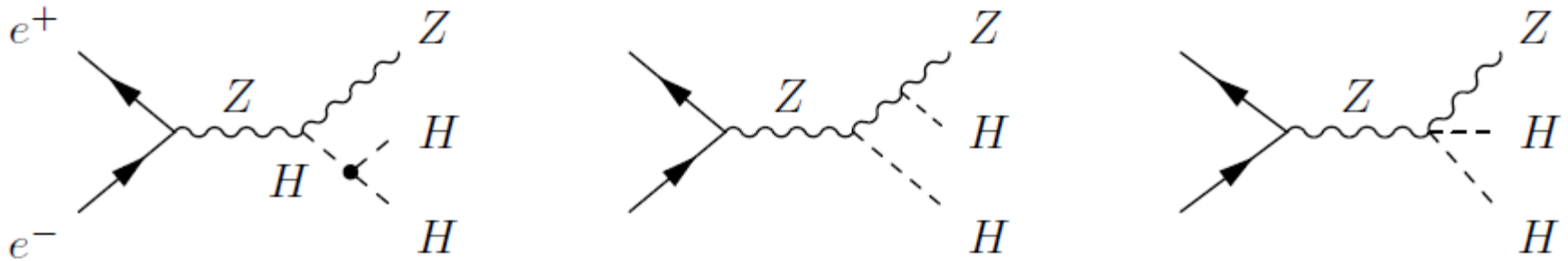
• Thus, due to **extremely high precision measurements**, in this very challenging scenario an e^+e^- collider offers the possibility of discovering the indirect effects of hidden particles.

• Cross section at CEPC modified by:

$$\delta\sigma_{Zh} = \frac{|c_h|^2 v^2}{8\pi^2 m_h^2} \left(1 + \frac{1}{4\sqrt{\tau_0}(\tau_0 - 1)} \log \left[\frac{1 - 2\tau_0 - 2\sqrt{\tau_0}(\tau_0 - 1)}{1 - 2\tau_0 + 2\sqrt{\tau_0}(\tau_0 - 1)} \right] \right)$$

where $\tau_0 = m_h^2/4m_0^2$ and $\delta\sigma_{Zh} = (\sigma_{Zh} - \sigma_{Zh}^{SM})/\sigma_{Zh}^{SM}$

ILC Higgs Self Coupling Measurement at $E_{cm}=500$ GeV



g_{hZZ} fixed to value from $\sigma(ZH)$ measurement

g_{hhZZ} fixed to SM value ← Needs to be more fully addressed in ILC studies

Extract g_{hhh} from measurement of $\sigma(ZHH)$

using $HH \rightarrow b\bar{b}b\bar{b}$ & $b\bar{b}W^+W^-$

$$\frac{\Delta\sigma(ZHH)}{\sigma(ZHH)} = 16\% \Rightarrow \frac{\Delta g_{hhh}}{g_{hhh}} = 27\% \text{ for ILC scenario H-20 @ 20 years.}$$

Note: This assumes SM g_{HHH} . If $g_{HHH} = 2 \times \text{SM}$ then $\frac{\Delta g_{hhh}}{g_{hhh}} = 27\% \Rightarrow \frac{\Delta g_{hhh}}{g_{hhh}} = 14\%$.

Other Higgs Measurements with FCC-ee & ILC H-20

	FCC-ee	ILC	<i>Combined</i>
	240 +350 GeV 10.0+2.6 ab ⁻¹	250 + 350 + 500(550) GeV 2.0 + 0.25 + 4.0 fb ⁻¹	
Δm_H	11 MeV	12.5 MeV	8.3 MeV
$\frac{\Delta g_{HHH}}{g_{HHH}}$	29 %*	27 %*	20 %
$\frac{\Delta g_{ttH}}{g_{ttH}}$	13%	5.9 (2.4) %	5.4 (2.4) %
$\frac{g_{eeH}}{g_{eeH}^{SM}}$	< 2.2 @ 3 σ	—	< 2.2 @ 3 σ

* Loop contribution to $\sigma(\text{ZH})$

* Tree-level contribution to $\sigma(\text{ZHH})$

Summary

▶ ILC helps FCC-ee:

- The 0.25% measurement of $\sigma(\nu\nu h) \times BR(H \rightarrow bb)$ reduces errors on all Higgs couplings
- The 2.4% Top Yukawa coupling measurement from ttH production improves upon the 13% measurement from the tt threshold scan.
- ILC $\sigma(ZHH)$ measurement provides a 27% tree-level determination of the Higgs self-coupling, and could help clarify a Higgs self-coupling interpretation of the precision FCC-ee $\sigma(ZH)$ measurement.

▶ FCC-ee helps ILC:

- Precision measurement of g_{HZZ} and various $\sigma \times BR$ at 240 GeV help turn the ILC 0.25% measurement of $\sigma(\nu\nu h) \times BR(H \rightarrow bb)$ into $\Delta g_{WW} = 0.22\%$
- Much better meas. of Higgs invisible width, BSM decays, rare decays such as $\gamma\gamma$ and $\mu\mu$ Note: $\sum BR_i = 1$ can be used to improve all coupling errors if $\Delta BR(H \rightarrow BSM) < 1\%$
- Unique access to Higgs coupling to 1st generation fermions.

▶ FCC-ee+ILC combination helps the particle physics community:

- Higgs Z coupling error $\Delta g_{HZ} = 0.16\%$
- Higgs W coupling error $\Delta g_{WW} = 0.22\%$
- Higgs b coupling error $\Delta g_{bb} = 0.38\%$
- Higgs self coupling error $\Delta g_{HHH} = 20\%$