



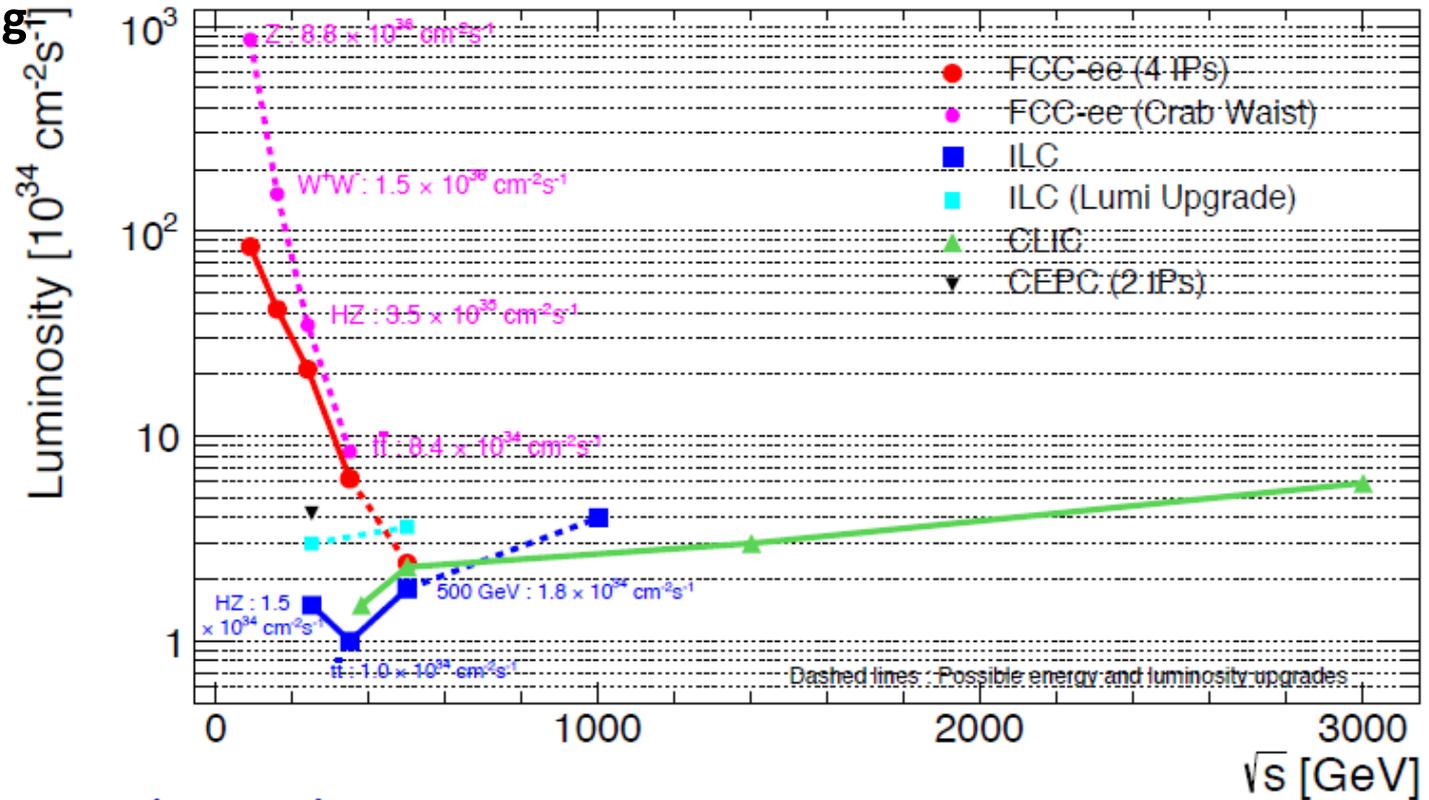
## FCC-ee: Precision measurements

references: talks by AB, Koratzinos, Piccinini, Tenchini, and many others



**Provide highest possible luminosity from Z to tt by exploiting b-factory technologies:**

- separate e- and e+ storage rings
- very strong focussing:  $\beta^* \gamma = 1\text{mm}$
- top-up injection
- crab-waist crossing

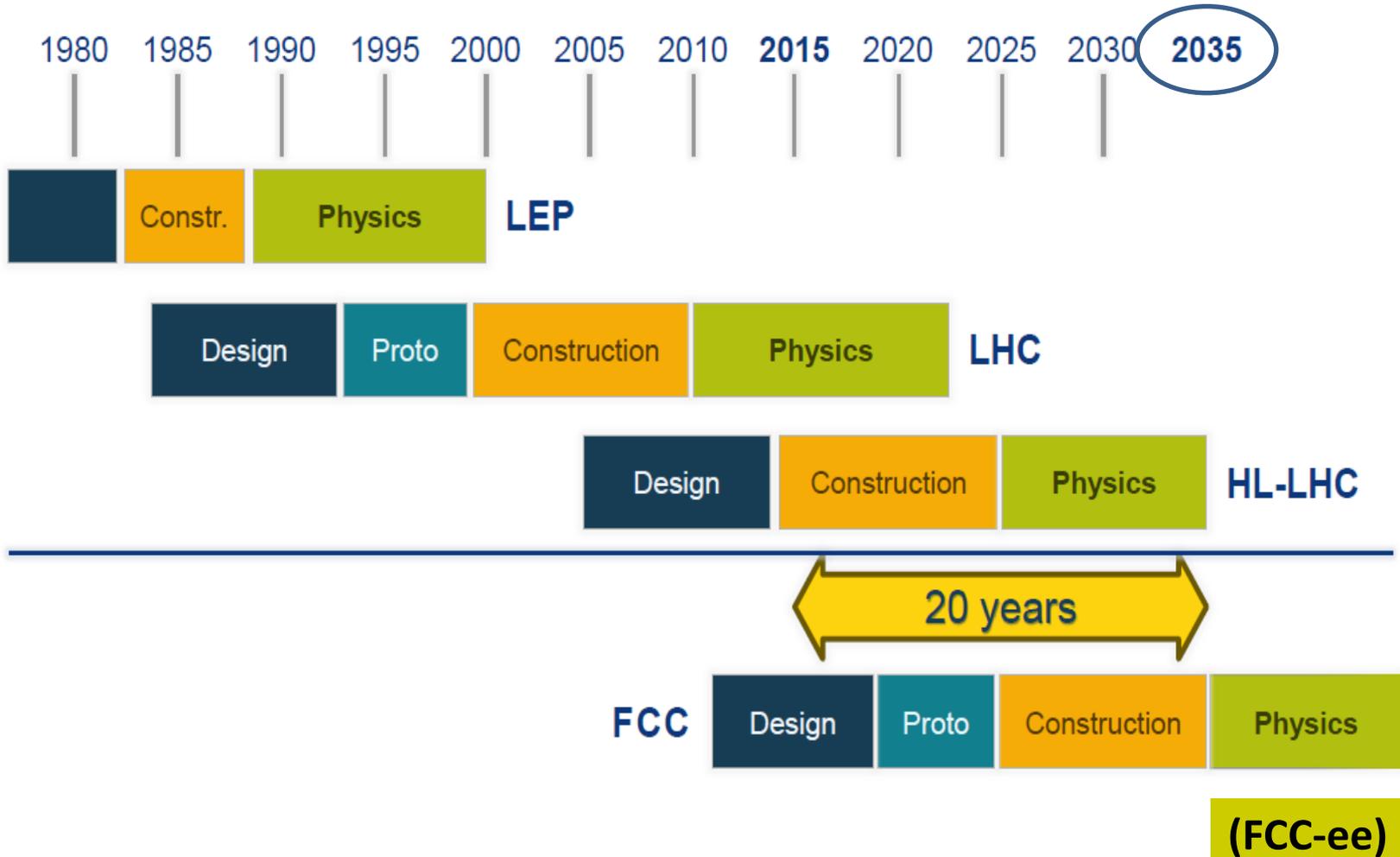


**Overlap in Higgs/top region, but differences and complementarities between linear and circular machines:**  
**Circ:** High luminosity, experimental environment (2 to 4 IP),  $E_{\text{CM}}$  calibration  
**Linear:** higher energy reach, longitudinal beam polarization





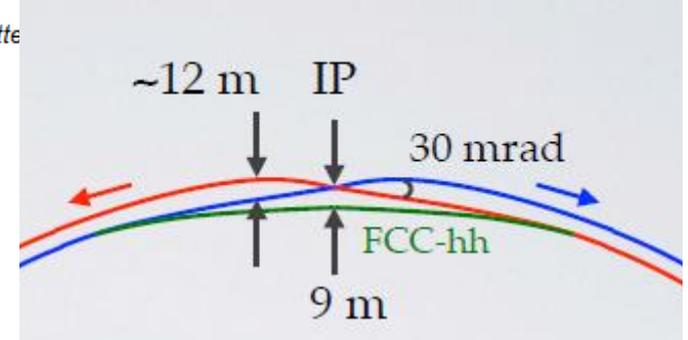
# CERN Circular Colliders and FCC



# Status and Challenges for FCC-ee

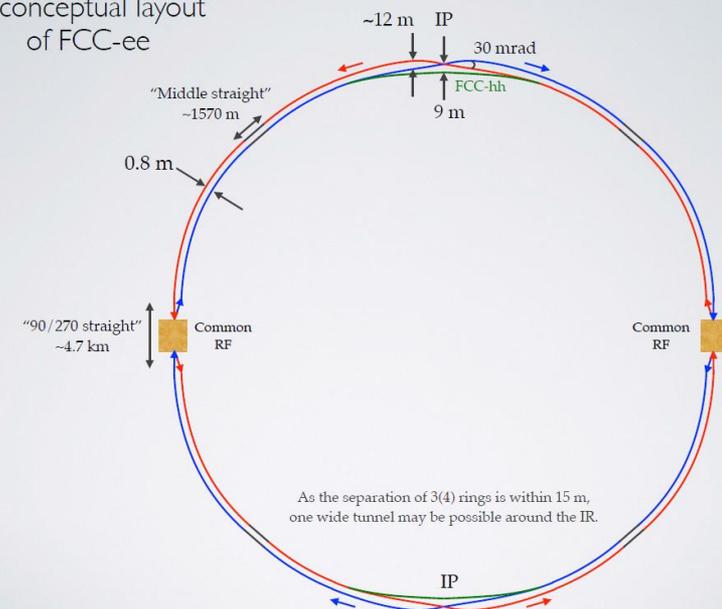
Michael Benedikt, Katsunobu Oide, Frank Zimmermann, Anton Wienands

(Submitted)



**new: asymmetric crossing to minimize SR to IP**

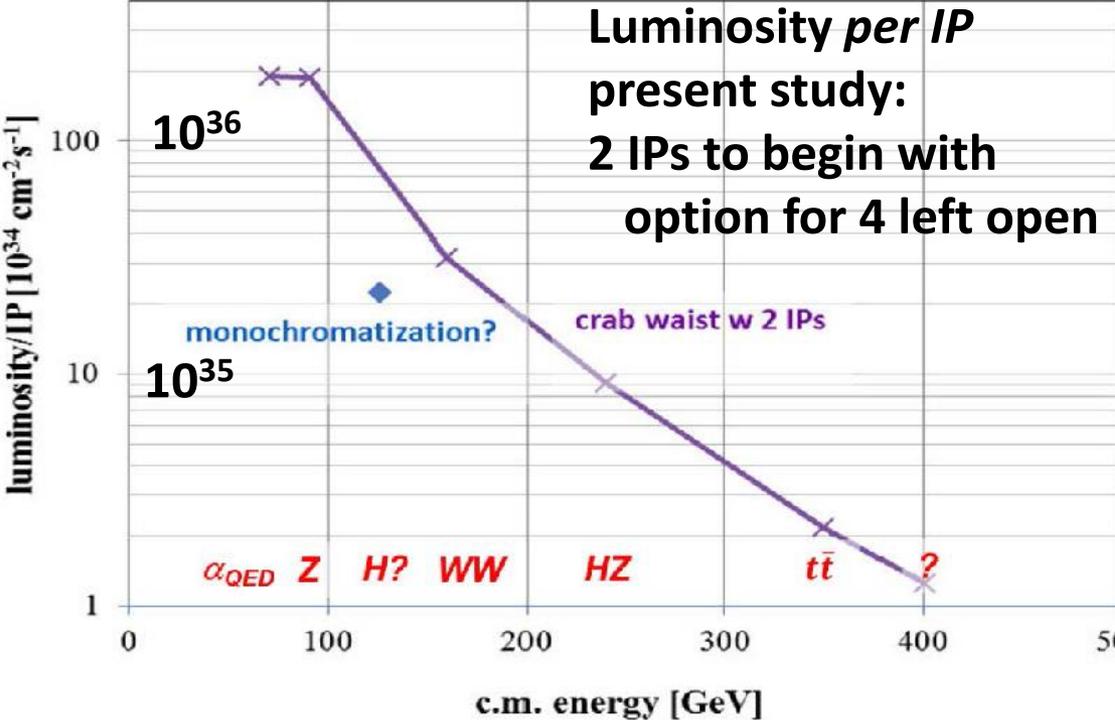
A conceptual layout of FCC-ee



**Table 1:** Key parameters for FCC-ee, at three beam energies, compared with LEP2. The parameter ranges indicated reflect a sensitivity to the number of IPs and to the choice of collision scheme (“baseline” [3] with varying arc cell length and small crossing angle, or a crab-waist scheme based on a larger crossing angle and constant cell length [4]).

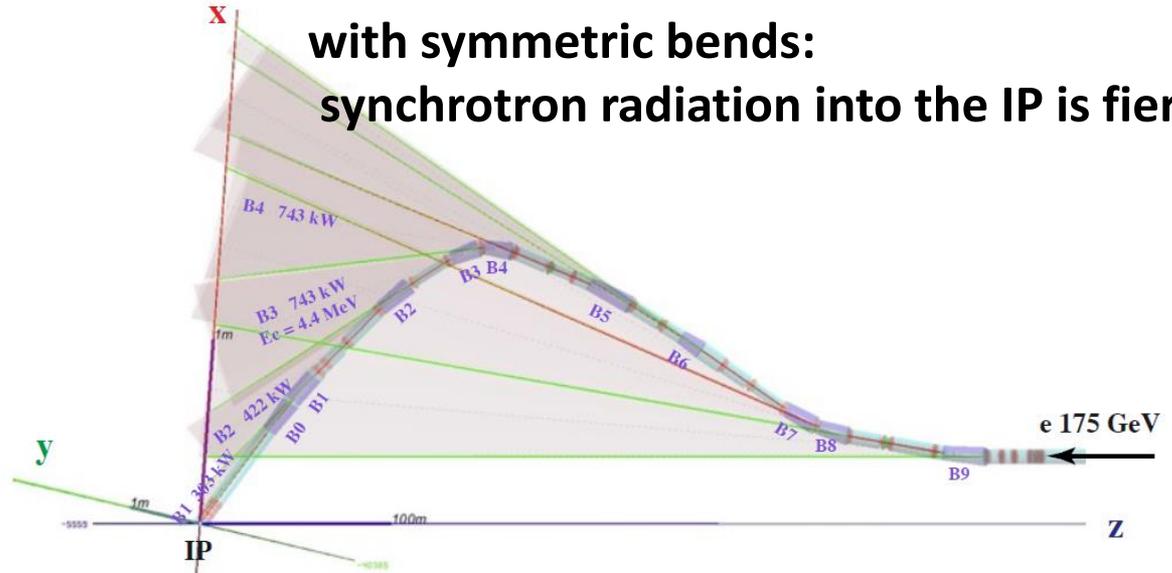
Parameter	FCC-ee			LEP2
	45	120	175	105
energy/beam [GeV]	45	120	175	105
bunches/beam	13000- 60000	500- 1400	51- 98	4
beam current [mA]	1450	30	6.6	3
luminosity/IP x 10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup>	21 - 280	5 - 11	1.5 - 2.6	0.0012
vertical IP β* [mm]	1	1	1	50
geom. hor. emittance [nm]	0.1-30	1	2	22
energy loss/turn [GeV]	0.03	1.67	7.55	3.34
synchrotron power [MW]	100			22
RF voltage [GV]	0.2-2.5	3.6-5.5	11	3.5

**Luminosity per IP**  
**present study:**  
**2 IPs to begin with**  
**option for 4 left open**



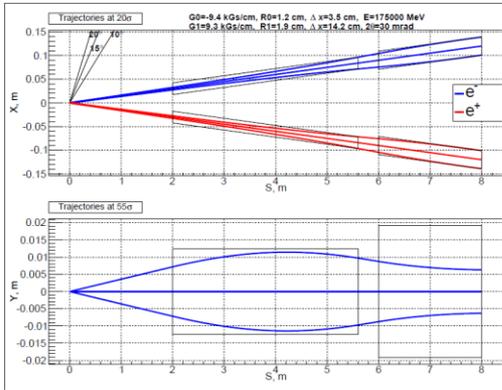
MDISIM/root/ 3d-OGL display

with symmetric bends:  
synchrotron radiation into the IP is fierce



Synchrotron radiation into IR major challenge : 2.3 MW / beam of MeV  $\gamma$ 's into detector region

Final Focus layout

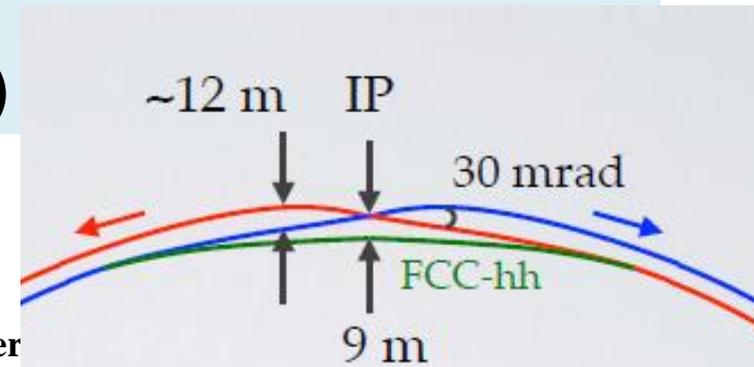


Rectangles represent bare apertures.

	L [m]
Q0	3.6
Q1	2

	R [m]
Q0	0.012
Q1	0.019

Asymmetric configuration (straight from the arcs to the IP and bend afterwards) reduce this problem to backscattered photons by eliminating the incoming bend NB this also saves magnets and energy loss and allows a layout consistent with FCC-hh (K. Oide)





## crab waist optics is being developed by BINP

### Parameters for crab waist

	Z	W	H	tt
Energy [GeV]	45	80	120	175
Perimeter [km]	100			
Crossing angle [mrad]	30			
Particles per bunch [ $10^{11}$ ]	1	4	4.7	4
Number of bunches	29791	739	127	33
Energy spread [ $10^{-3}$ ]	1.1	2.1	2.4	2.6
Emittance hor. [nm]	0.14	0.44	1	2.1
Emittance ver. [pm]	1	2	2	4.3
$\beta_x^* / \beta_y^*$ [m]	0.5 / 0.001			
Luminosity / IP [ $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ ]	212	36	9	1.3
Energy loss / turn [GeV]	0.03	0.3	1.7	7.7

**note very high  
-- and variable --  
number of bunches**

<b>Gain w.r.t. 'baseline optics'</b>	<b>8</b>	<b>3</b>	<b>1.5</b>	<b>~1</b>
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|

PHYS. REV. S.T. - AB 17, 041004 (2014)

A. Bogomyagkov (BINP)

FCC-ee crab waist IR and the arc

**AMBITIOUS and CHALLENGING: Excellent luminosity prospects, E aperture OK,  
but IR region is a great challenge ! Aim at decision in fall 2015**





# FCC-ee PHYSICS PROGRAM

- Z and W Electroweak physics ( $10^{13}Z$ ,  $10^8 WW$ )
  - precision energy calibration (100 KeV)  $\rightarrow m_Z, \Gamma_Z, m_W, \sin^2 \theta_W$
  - new** possibly precision measurement of  $\alpha_{QED}(m_Z)$
  - high luminosity search for rare Z decays
  - neutrino counting and search for RH neutrinos
- Higgs Physics at  $E_{CM} = 240$  GeV (ZH) and 350 GeV,  $2 \cdot 10^6$  ZH events
  - unique determination of ZH coupling and H width,
  - all fermion and boson couplings (except ttH and HHH)
  - rare decays
- top quark physics at 350 -370 GeV
  - top quark mass (essential for precision EW tests) to exp. precision of 10 MeV
  - new** top quark couplings (no need for beam polarization)
- investigating run at  $E_{CM} = m_H$  to determine H $\epsilon\epsilon$  coupling





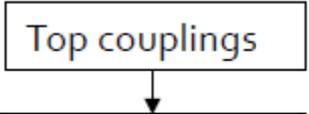
# Run Plan

Assuming 4 IP

P. Janot

## Time needed to achieve this ambitious programme

Number of events expected for each year of running at the FCC-ee



$\sqrt{s}$ (GeV)	90 (Z)	160 (WW)	240 (HZ)	350 (tt)	350+ (WW→H)
Lumi ( $\text{ab}^{-1}/\text{yr}$ )	86.0	15.2	3.5	1.0	1.0
Events/year	$3.7 \times 10^{12}$	$6.1 \times 10^7$	$7.0 \times 10^5$	$4.2 \times 10^5$	$2.5 \times 10^4$

Number of years needed to complete the core programme  $N_Z = 10^{(12)13}$

1 year =  $10^7$  s

# years	(0.3) 2.5	1	3	0.5	3
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With 4 IP can execute Z,W,H,t program in 10 years of full luminosity operation ( $10^7$  s/year) Commissioning etc, to be added -- but as usual, hard to guess

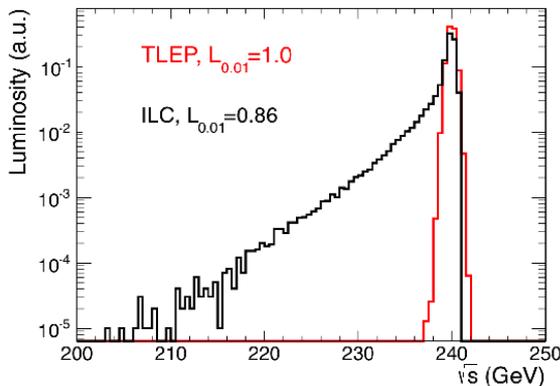
Staging is foreseen for RF:

1. low RF (5 GV/beam , 12 MW): begin with Z scan, develop crab waist, energy calibration + HZ at low luminosity
2. Complete power for High lumi ZH (and WW)
3. arrange RF to reach 10 GV/beam, run 350+ GeV  $E_{\text{CM}}$
4. run high statistics Z pole



# Experimental conditions

- 2-4 IPs  $L^* \sim 2\text{m}$
- bunch crossing spacing from 2-5 ns (Z) up to  $3\mu\text{s}$  (top)
- no pile-up ( $<0.001$  at FCC-Z/CrabWaist)
- beamstrahlung is mild for experiments



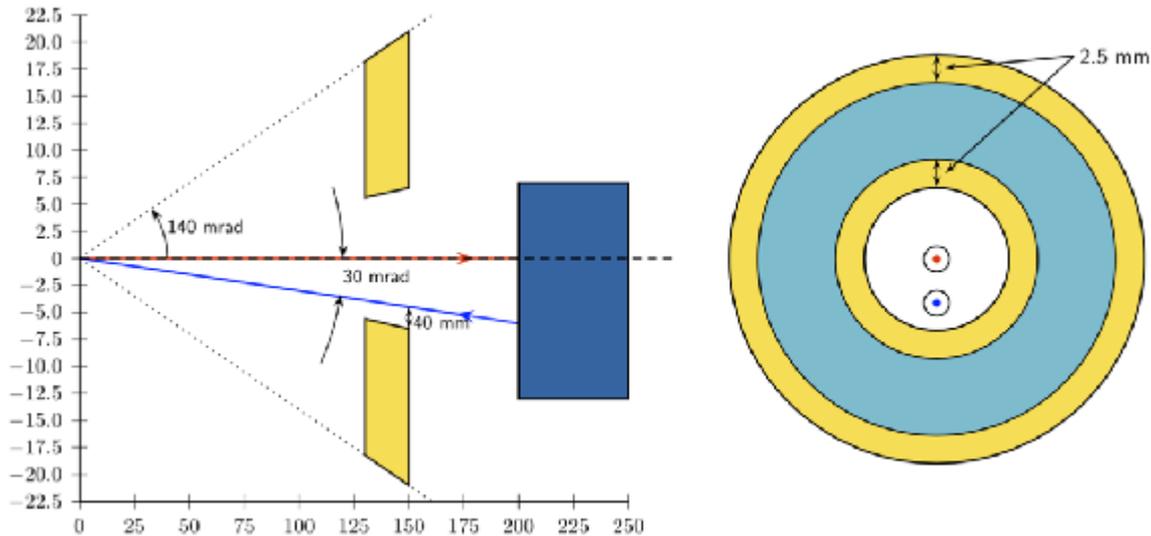
	FCCZ	FCCZ, c.w	CEPC	FCC ZH	ILC500
Npairs / BX	200	9900	3260	640	165000
Leading process	96% LL	65% LL	80% LL	90% LL	60% BH
Epairs / BX (GeV)	86	2940	2600	570	400000
Leading process	100% LL	100% LL	98% LL	96% LL	70% BH

*E. Perez,  
C. Leonidopoulos*

- Beam energy calibration for Z and W running
- IR design with crossing angle is not trivial
- ➔ a challenging magnet design issue.



## Of particular importance: luminosity monitors



M. Dam

### Requirements dominated by Z line shape and peak cross-section measurements

Shift in parameter for a shift of  $+10^{-4}$  in acceptance

$z_{\text{front}}$ [mm]	$r_{\text{min}}$ [mm]	$r_{\text{max}}$ [mm]	$\theta_{\text{min}}$ [mrad]	$\theta_{\text{max}}$ [mrad]	$\sigma$ [nb]	$\delta z_{\text{front}}$ [ $\mu\text{m}$ ]	$\delta r_{\text{min}}$ [ $\mu\text{m}$ ]	$\delta r_{\text{max}}$ [ $\mu\text{m}$ ]
1000	80	115	80	115	10	50	-2.1	6.1
1300	89	157	68	121	18	65	-3.0	17
1500	95	185	63	123	23	75	-3.5	26



# Input from Physics to the accelerator design

0. Nobody complains that the luminosity is too high (the more you get, the more you want)  
no pile up, even at the Z: at most 1ev /300bx

## 1. Do we need polarized beams?

-1- transverse polarization:

continuous beam Energy calibration with resonant depolarization

central to the precision measurements of  $m_Z$ ,  $m_W$ ,  $\Gamma_Z$

requires 'single bunches' and calibration of both e+ and e-

a priori doable up to W energies -- workarounds exist above (e.g.  $\gamma Z$  events)

large ring with small emittance excellent. Saw-tooth smaller than LEP for Z

need wigglers (or else inject polarized e- and e+) to polarize 'singles';

simulations ongoing (E. Gianfelice, M. Koratzinos, I.Kopp)

-2- longitudinal polarization requires spin rotators and is very difficult at high energies

-- We recently found that it is not necessary to extract top couplings (Janot)

-- improves Z peak measurements *if loss in luminosity is not too strong*

but brings no information that is not otherwise accessible

## 2. What energies are necessary?

-- in addition to Z, W, H and top listed the following are being considered

-- e+e-  $\rightarrow$  H(125.2) (requires monochromatization A. Faus) (under study)

-- e+e- at top threshold  $\sim$ 20 GeV for top couplings (E\_max up to 180 -185 GeV)

-- no obvious case for going to 500 GeV

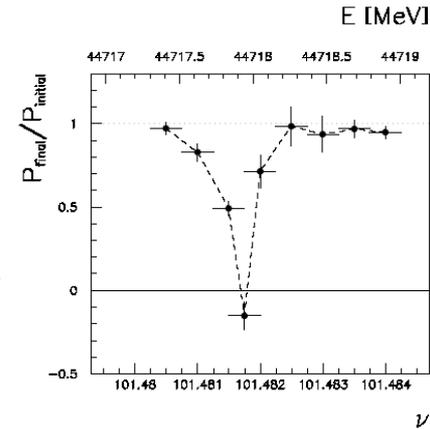


# Beam polarization and E-calibration @ FCC-ee

Precise measurement of  $E_{\text{beam}}$  by resonant depolarization

*~100 keV each time the measurement is made*

LEP →



At LEP transverse polarization was achieved routinely at Z peak.

*instrumental in  $10^{-3}$  measurement of the Z width in 1993*

*led to prediction of top quark mass ( $179 \pm 20$  GeV) in Mar'94*

Polarization in collisions was observed ( $40\%$  at  $BBTS = 0.04$ ) →

At LEP beam energy spread destroyed polarization above 61 GeV

$\sigma_E \propto E^2/\sqrt{\rho}$  → *At TLEP transverse polarization up to at least 81 GeV (WW threshold) to go to higher energies requires spin rotators and siberian snake (see spares)*

FCC-ee: use 'single' bunches to measure the beam energy continuously

→ *no interpolation errors due to tides, ground motion or trains etc...*

<< 100 keV beam energy calibration around Z peak and W pair threshold.

$\Delta m_Z \sim 0.1$  MeV,  $\Delta \Gamma_Z \sim 0.1$  MeV,  $\Delta m_W \sim 0.5$  MeV

Alain Blondel Higgs and Beyond June 2013 Sendai

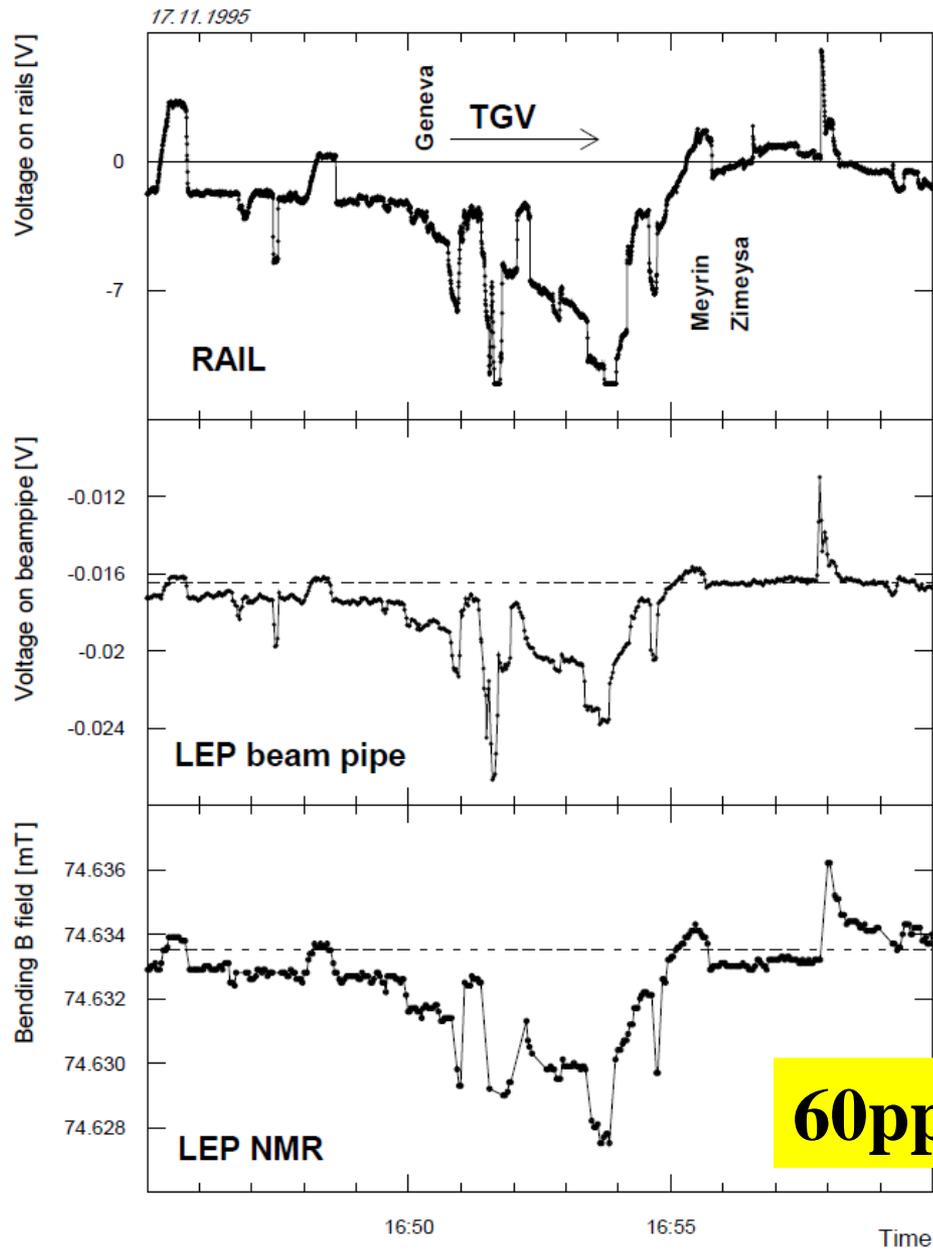


## Calibration of centre-of-mass energies at LEP1 for precise measurements of Z properties

*The LEP Energy Working Group*

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T. Camporesi<sup>1)</sup>, B. Dehning<sup>1)</sup>, A. Drees<sup>3)</sup>, G. Duckeck<sup>4)</sup>, J. Gascon<sup>5)</sup>, M. Geitz<sup>1,c)</sup>, B. Goddard<sup>1)</sup>,  
C.M. Hawkes<sup>6)</sup>, K. Henrichsen<sup>1)</sup>, M.D. Hildreth<sup>1)</sup>, A. Hofmann<sup>1)</sup>, R. Jacobsen<sup>1,d)</sup>, M. Koratzinos<sup>1)</sup>,  
M. Lamont<sup>1)</sup>, E. Lancon<sup>7)</sup>, A. Lucotte<sup>8)</sup>, J. Mnich<sup>1)</sup>, G. Mugnai<sup>1)</sup>, E. Peschardt<sup>1)</sup>, M. Placidi<sup>1)</sup>,  
P. Puzo<sup>1,e)</sup>, G. Quast<sup>9)</sup>, P. Renton<sup>10)</sup>, L. Rolandi<sup>1)</sup>, H. Wachsmuth<sup>1)</sup>, P.S. Wells<sup>1)</sup>, J. Wenninger<sup>1)</sup>,  
G. Wilkinson<sup>1,10)</sup>, T. Wyatt<sup>11)</sup>, J. Yamartino<sup>12,f)</sup>, K. Yip<sup>10,g)</sup>





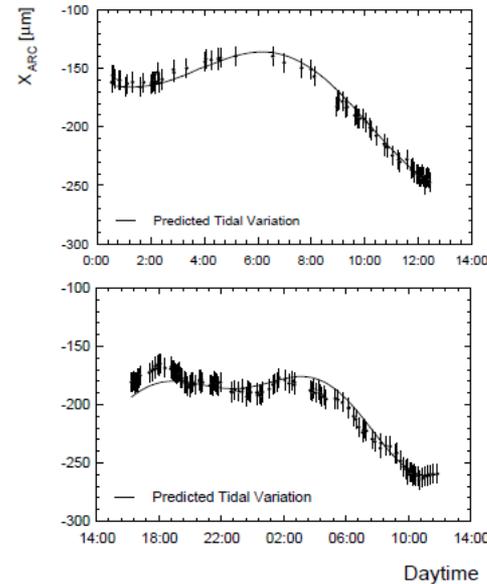
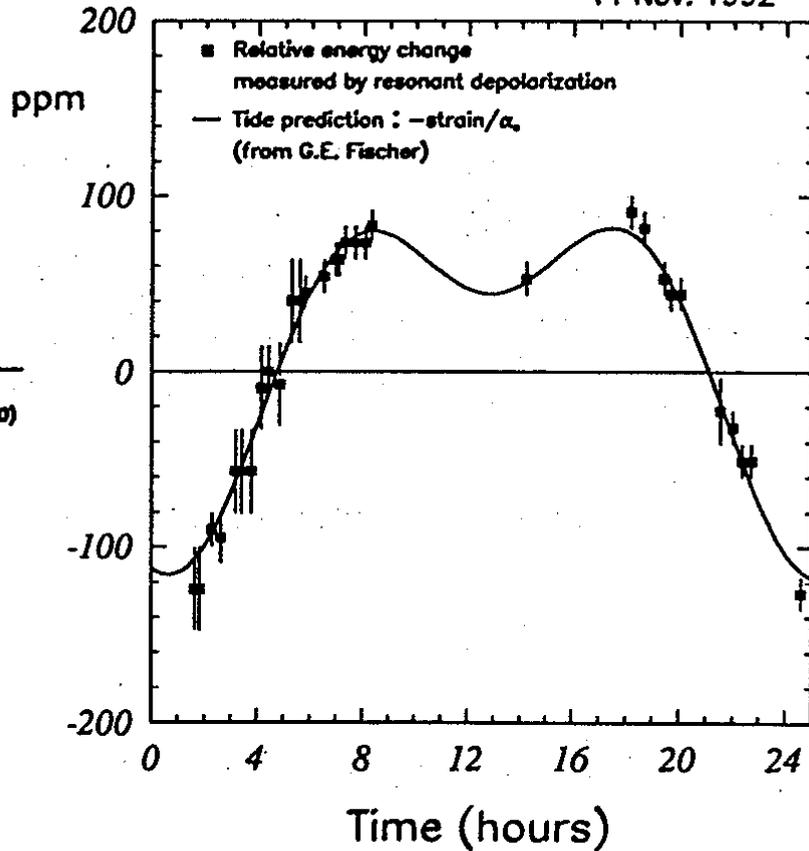
**60ppm in 5 minutes!**



# Tide correction...

## LEP TidExperiment

11 Nov. 1992

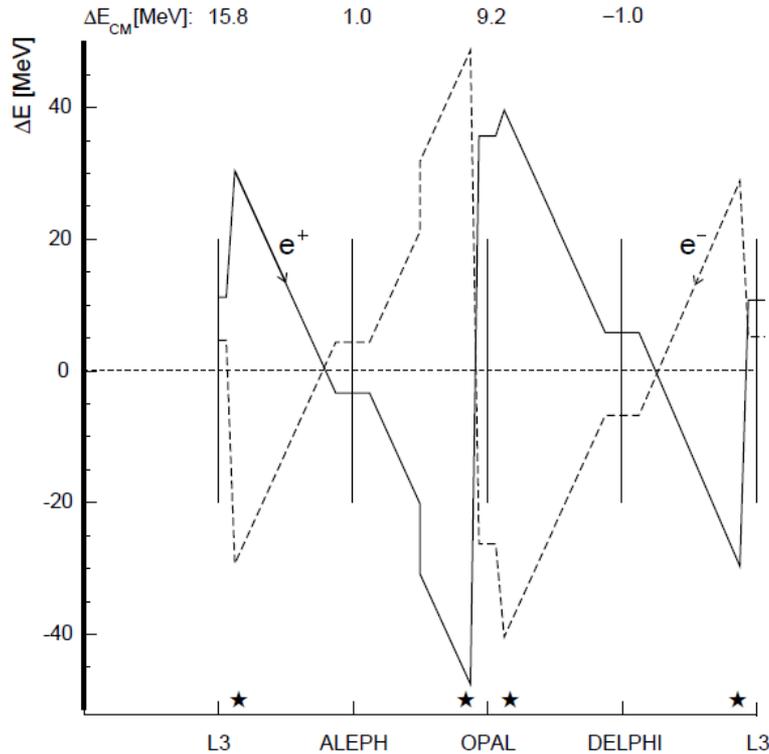


horizontal orbit position for two LEP fills. The predicted tidal variations are indicated figure (fill 1694) the agreement is excellent. In the bottom figure (fill 2260) the tidal orbit movements. The errors on each point are estimates.

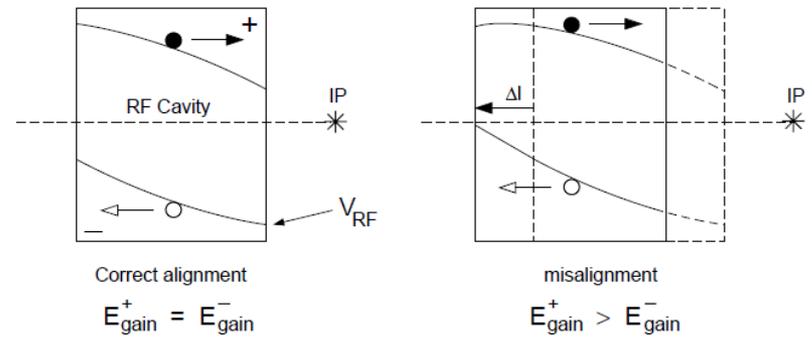
Figure 23: Beam energy variations measured over 24 hours compared to the expectation from the tidal LEP deformation.

are orbit measurements enough?

# RF corrections



Errors arise due to cavity misalignments primarily:



- At LEP cavity misalignment was assumed to be 1.4mm in 1995

Work is needed to reduce this error. For LEP the error was of the order of 500keV (leading to an error of 400/200keV for the mass/width of the Z. Need to reduce this error by (more than) a factor of 10! NB The effect smaller at FCC-ee (smaller  $E_{loss}$ )

# Most of these systematics, but not all, vanish with ‘single’ bunches calib.

Source	$\Delta E_{CM}$ (MeV)							Energy correlation	Year correlation	$\Delta m_Z$ (MeV)	$\Delta \Gamma_Z$ (MeV)
	P-2	P	P+2	P	P-2	P	P+2				
	93	93	93	94	95	95	95				
Normalization error	1.7	5.9	0.9	1.1	0.8	5.0	0.4	0.	0.	0.5	0.8
RD energy measurement	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.04	0.04	0.4	0.5
QFQD correction	0.2	0.2	0.2	0.0	0.0	0.0	0.0	0.75	[0., 0.75]	0.1	0.1
Horizontal correctors	0.0	0.4	-0.4	0.2	-0.2	-0.5	-0.2	$\pm 0.75$	$\pm 0.75$	0.2	0.1
Tide amplitude	0.0	-0.3	0.2	-0.1	-0.0	-0.0	-0.0	$\pm 1.$	1.	0.0	0.1
Tide phase	0.0	0.0	-0.1	0.1	-0.2	-0.0	0.0	$\pm 1.$	0.50	0.0	0.1
Ring temperature	0.1	0.4	0.4	0.2	0.4	0.3	0.4	0.75	0.75	0.3	0.2
B rise scatter+model	2.8	3.0	2.5	3.3	0.6	0.6	0.6	[0.47, 0.86]	0.50	1.5	0.5
B rise NMR48 T-coeff	0.6	0.3	0.6	0.5	1.0	1.0	1.1	0.75	0.75	0.8	0.3
Bending modulation jump	0.	0.	0.	0.	0.0	1.4	0.3	0.75	0.	0.1	0.1
e <sup>+</sup> Energy uncertainty	0.3	0.3	0.3	0.3	0.2	0.2	0.2	0.5	[0., 0.50]	0.2	0.1
RF corrections (Comb.)	0.5	0.5	0.5	0.6	0.7	0.7	0.7	[0.63, 0.96]	[0.18, 0.70]	0.4	0.2
Dispersion corr. (Comb.)	0.4	0.4	0.4	0.7	0.3	0.3	0.3	[0.50, 0.75]	[0., 0.50]	0.2	0.1
Energy spread											0.2

Table 19: Summary of errors (MeV) on the centre-of-mass energy determination. These are selected numbers shown for illustration, the exact errors are determined using the correlation matrix formalism. The energy correlation coefficients between energy points and between years are shown. Whenever the year-to-year or the energy-to-energy correlation coefficient is not fixed the range is indicated. The relative sign of the energy correlation coefficient is given by the relative sign of the error. The last two rows give average errors due to RF and dispersion effects when combining the 4 IPs with the respective correlation coefficients. The last two columns give estimates of the error contributions to the determination of  $m_Z$  and  $\Gamma_Z$  in MeV: the actual errors depend on the details of experimental samples.

# Resonant depolarization accuracy at TLEP/FCCee – extrapolation

Per beam, not ECM

Source	$\Delta E/E$	$\Delta E$ ( $E=45.6$ GeV)	Correlated/Z mass	Uncorrelated / Z width
Electron mass	$3 \cdot 10^{-7}$	15 keV	15keV	0keV
Revolution frequency	$10^{-10}$	0 keV	0keV	0keV
Frequency of the RF magnet	$2 \cdot 10^{-8}$	1 keV	1keV	0keV
Width of excited resonance	$2 \cdot 10^{-6}$	90 keV	1keV	1keV
Interference of resonances	$2 \cdot 10^{-6}$	90 keV	9keV	9keV
Spin tune shifts from long. fields	$1.1 \cdot 10^{-7}$	5 keV	5keV	5keV
Spin tune shifts from hor. fields	$2 \cdot 10^{-6}$	100 keV	3keV	1keV
Quadratic non-linearities	$10^{-7}$	5 keV	5keV	5keV
Total error	$4.4 \cdot 10^{-6}$	200 keV	~20keV	~12keV
			<b>IP specific errors total</b>	
			~40keV	~20keV
			~45keV	~23keV

- Statistical errors are divided by sqrt(10,000) - negligible
- This is a zeroth order working hypothesis
- The table should eventually also include effects that were negligible at the time of LEP



# 1. ELECTROWEAK PRECISION TESTS (EWPT)

Test of the 'closure' of the SM:

test the existence of electroweakly coupled new particles ...

-- if they are nearby in Energy scale

or

-- if they violate symmetries of the Standard Model (in which case, no «decoupling»)

e.g. Higgs boson  $\propto \alpha/\pi \log (m_H/m_Z)^2$  and top-bottom mass splitting  $\propto \alpha/\pi (m_t/m_b)^2$

# 2. TESTS OF ELECTROWEAK SYMMETRY BREAKING (EWSB)

Is the H(125) a Higgs boson?

→ couplings proportional to mass?

if not could be more complicated EWSB e.g. more Higgses

→ Higgs supposed to cancel WW scattering anomalies at TeV scale  
does this work?

# EWRCs

relations to the well measured

$$G_F m_Z \alpha_{\text{QED}}$$

at first order:

$$\Delta\rho = \alpha/\pi (m_{\text{top}}/m_Z)^2 - \alpha/4\pi \log(m_h/m_Z)^2$$

$$\epsilon_3 = \cos^2\theta_w \alpha/9\pi \log(m_h/m_Z)^2$$

$$\delta_{\text{vb}} = 20/13 \alpha/\pi (m_{\text{top}}/m_Z)^2$$

complete formulae at 2d order including strong corrections are available in fitting codes

e.g. ZFITTER, GFITTER

$$\Delta\rho \equiv \epsilon_1 \quad \Gamma_l = (1 + \Delta\rho) \frac{G_F m_Z^3}{24\pi\sqrt{2}} \left(1 + \left(\frac{g_{Vl}}{g_{Al}}\right)^2\right) \left(1 + \frac{3}{4} \frac{\alpha}{\pi}\right)$$

$$\epsilon_3 \quad \sin^2\theta_w^{\text{eff}} \cos^2\theta_w^{\text{eff}} = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} G_F m_Z^2} \frac{1}{1 + \Delta\rho} \frac{1}{1 - \frac{\epsilon_3}{\cos^2\theta_w}}$$

$$\delta_{\text{vb}} \quad \Gamma_b = (1 + \delta_{\text{vb}}) \Gamma_d \left(1 - \text{mass corrections} \propto m_b^2/M_Z^2\right)$$

$$\epsilon_2 \quad M_W^2 = \frac{\pi\alpha(M_Z^2)}{\sqrt{2} G_F \sin^2\theta_w^{\text{eff}}} \cdot \frac{1}{(1 - \epsilon_3 + \epsilon_2)}$$

$\sin^2\theta_w^{\text{eff}}$  is defined from

$$\sin^2\theta_w^{\text{eff}} = \frac{1}{4} \left(1 - \frac{g_{Vl}}{g_{Al}}\right) = \sin^2\theta_w^{\text{eff}} \Big|_{\text{lept}}$$

obtained from asymmetries at the Z.

also

$\Delta\alpha$

$$m_W^2 = \frac{\pi\alpha}{\sqrt{2} G_F} \cdot \frac{1}{\left(1 - \frac{m_W^2}{M_Z^2}\right)} \frac{1}{(1 - \Delta\alpha)}$$

$$\Delta\alpha = \Delta\alpha - \frac{\cos^2\theta_w}{\sin^2\theta_w} \Delta\rho + 2 \frac{G^2\theta_w}{\sin^2\theta_w} \epsilon_3 + \frac{C^2 - S^2}{S^2} \epsilon_2$$

# The main players

## Inputs:

$G_F = 1.1663787(6) \times 10^{-5} / \text{GeV}^2$	from muon life time	$6 \cdot 10^{-7}$
$M_Z = 91.1876 \pm 0.0021 \text{ GeV}$	Z line shape	$2 \cdot 10^{-5}$
$\alpha = 1/137.035999074(44)$	electron g-2	$3 \cdot 10^{-10}$

## EW observables sensitive to new physics:

$M_W = 80.385 \pm 0.015$	LEP, Tevatron	$2 \cdot 10^{-4}$
$\sin^2\theta_W^{\text{eff}} = 0.23153 \pm 0.00016$	WA Z pole asymmetries	$7 \cdot 10^{-4}$
+ $\Gamma_{\text{Rb}}$ etc...		

## Nuisance parameters:

$\alpha(M_Z) = 1/127.944(14)$	hadronic corrections to running alpha	$1.1 \cdot 10^{-4}$
$\alpha_s(M_Z) = 0.1187(17)$	strong coupling constant	$1.7 \cdot 10^{-2}$
$m_{\text{top}} = 173.34 \pm 0.76 \text{ GeV}$	from LHC+Tevatron combination	$4 \cdot 10^{-3}$
$m_H = 125.09 \pm 0.21 \text{ (stat.)} \pm 0.11 \text{ (syst.) GeV}/c^2$ (CMS+ATLAS)		$2 \cdot 10^{-3}$

## Example (from Langacker, Erler PDG 2014)

$$\Delta\rho = \varepsilon_1 = \alpha(M_Z) \cdot T$$

$$\varepsilon_3 = 4 \sin^2\theta_W \alpha(M_Z) \cdot S$$

From the EW fit

$$\rho_0 = 1.00040 \pm 0.00024 ,$$

$$\Delta\rho = 0.0004 \pm 0.00024$$

-- is consistent with 0 at  $1.7\sigma$  (0= SM)

-- is sensitive to non conventional Higgs bosons (e.g. in SU(2) triplet with 'funny v.e.v.s')

-- is sensitive to Isospin violation such as  $m_t \neq m_b$

$$\rho_0 = 1 + \frac{3 G_F}{8\sqrt{2}\pi^2} \sum_i \frac{C_i}{3} \Delta m_i^2 , \quad (10.63)$$

where the sum includes fourth-family quark or lepton doublets,  $(\begin{smallmatrix} t' \\ b' \end{smallmatrix})$  or  $(\begin{smallmatrix} E^0 \\ E^- \end{smallmatrix})$ , right-handed (mirror) doublets, non-degenerate vector-like fermion doublets (with an extra factor of 2), and scalar doublets such as  $(\begin{smallmatrix} \tilde{t} \\ \tilde{b} \end{smallmatrix})$  in Supersymmetry (in the absence of  $L-R$  mixing).

Measurement implies

$$\sum_i \frac{C_i}{3} \Delta m_i^2 \leq (50 \text{ GeV})^2.$$

The larger possible mass splitting of an SU(2) doublet is 50 GeV

***no matter what its mass is.***

Similarly

$$S = \frac{C}{3\pi} \sum_i \left( t_{3L}(i) - t_{3R}(i) \right)^2,$$

Would be sensitive to a doublet of new fermions where Left and Right have different masses etc... (neutrinos are already included)

**Note that often EW radiative corrections do not decouple with mass => a very powerful tool of investigation**

$$\Delta\rho = \alpha / \pi (m_{\text{top}}/m_Z)^2 - \alpha / 4\pi \log (m_h/m_Z)^2$$

$$\varepsilon_3 = \cos^2\theta_w \alpha / 9\pi \log (m_h/m_Z)^2$$

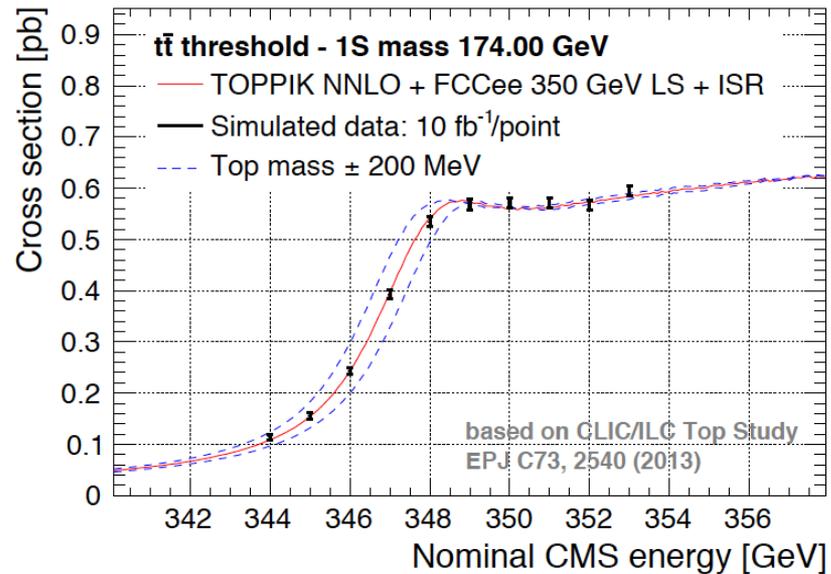
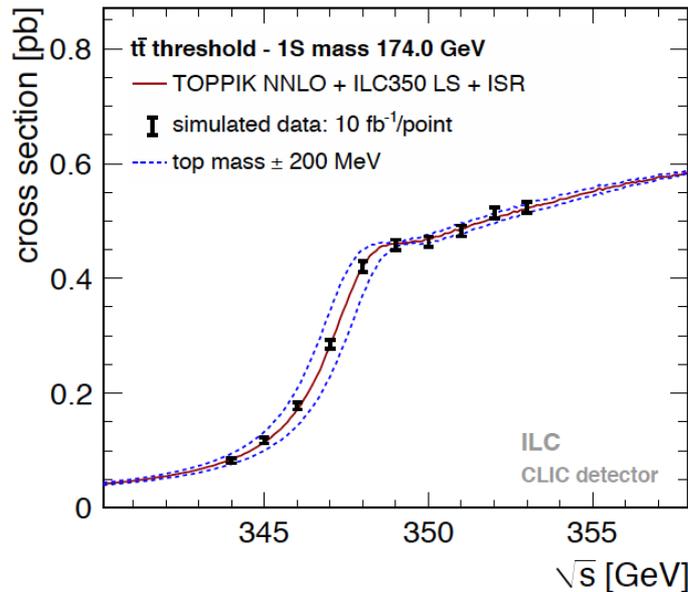
$$\delta_{\text{vb}} = 20/13 \alpha / \pi (m_{\text{top}}/m_Z)^2$$

# A Sample of Essential Quantities:

<b>X</b>	<b>Physics</b>	<b>Present precision</b>		<b>TLEP stat Syst Precision</b>	<b>TLEP key</b>	<b>Challenge</b>
<b>M<sub>Z</sub></b> MeV/c <sup>2</sup>	<b>Input</b>	91187.5 <b>±2.1</b>	Z Line shape scan	<b>0.005 MeV</b> <b>&lt;±0.1 MeV</b>	E_cal	QED corrections
<b>Γ<sub>Z</sub></b> MeV/c <sup>2</sup>	<b>Δρ (T)</b> <b>(no Δα!)</b>	2495.2 <b>±2.3</b>	Z Line shape scan	<b>0.008 MeV</b> <b>&lt;±0.1 MeV</b>	E_cal	QED corrections
<b>R<sub>ℓ</sub></b>	<b>α<sub>s</sub>, δ<sub>b</sub></b>	20.767 <b>± 0.025</b>	Z Peak	<b>0.0001</b> <b>± 0.002</b> <b>- 0.0002</b>	Statistics	QED corrections
<b>N<sub>v</sub></b>	<b>Unitarity of PMNS, sterile ν's</b>	2.984 <b>±0.008</b>	Z Peak  Z+γ(161 GeV)	<b>0.00008</b> <b>±0.004</b> <b>0.0004-0.001</b>	->lumi meast  Statistics	<b>QED corrections to Bhabha scat.</b>
<b>R<sub>b</sub></b>	<b>δ<sub>b</sub></b>	0.21629 <b>±0.00066</b>	Z Peak	<b>0.000003</b> <b>±0.000020 - 60</b>	Statistics, small IP	Hemisphere correlations
<b>A<sub>LR</sub></b>	<b>Δρ, ε<sub>3</sub>, Δα (T, S)</b>	0.1514 <b>±0.0022</b>	Z peak, polarized	<b>±0.000015</b>	4 bunch scheme	Design experiment
<b>M<sub>W</sub></b> MeV/c <sup>2</sup>	<b>Δρ, ε<sub>3</sub>, ε<sub>2</sub>, Δα (T, S, U)</b>	80385 <b>± 15</b>	Threshold (161 GeV)	<b>0.3 MeV</b> <b>&lt;1 MeV</b>	E_cal & Statistics	QED corections
<b>m<sub>top</sub></b> MeV/c <sup>2</sup>	<b>Input</b>	173200 <b>± 900</b>	Threshold scan	<b>10 MeV</b>	E_cal & Statistics	Theory limit at 100 MeV?

# 350 GeV: the top mass

- Advantage of a very low level of beamstrahlung in circular machines
  - **Could potentially reach 10 MeV uncertainty (stat) on  $m_{\text{top}}$**
  - **The main issue is relationship between  $t\bar{t}$  threshold and the loop corrections**
- Comparing ILC and FCCee - assuming identical detector performance



Simulated data points -  
same integrated luminosity

NB: Assuming unpolarized beams - LC  
beams can be polarized, increasing cross-  
sections / reducing backgrounds



# Potential of $\alpha_{\text{QED}}(m_Z)$ measurement (1)

For exploitation of precision EW measurements, need precise knowledge of  $\alpha_{\text{QED}}(m_Z)$

- Standard method involves extrapolation from  $\alpha_{\text{QED}}(0)$  to  $\alpha_{\text{QED}}(m_Z)$ 
  - Dispersion integral over hadronic cross section – low energy resonances:  $\delta\alpha/\alpha = 1.1 \times 10^{-4}$

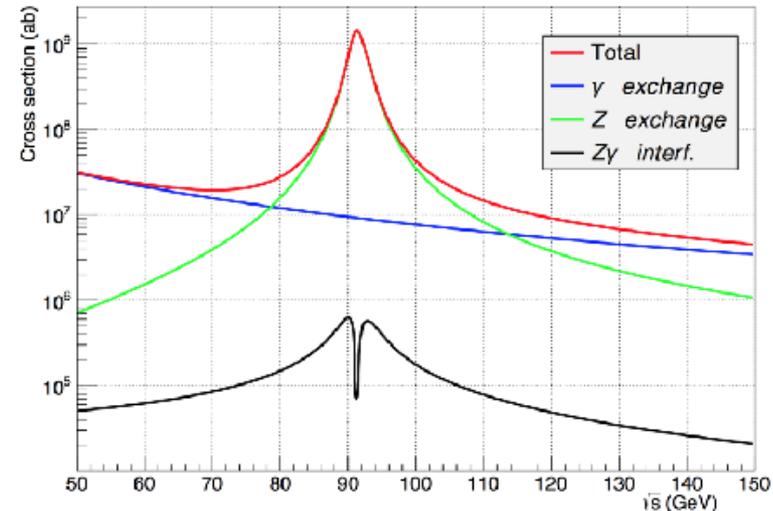
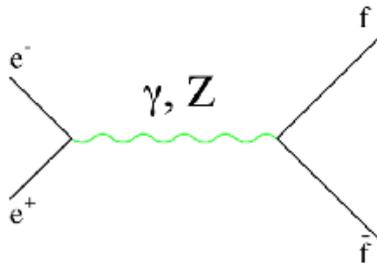
$$\alpha_{\text{QED}}^{-1}(m_Z) = 128.952 \pm 0.014$$

**New idea:** exploit large statistics of FCC-ee to measure  $\alpha_{\text{QED}}(m_Z)$  directly **close to  $m_Z$**

- Extrapolation error becomes negligible!

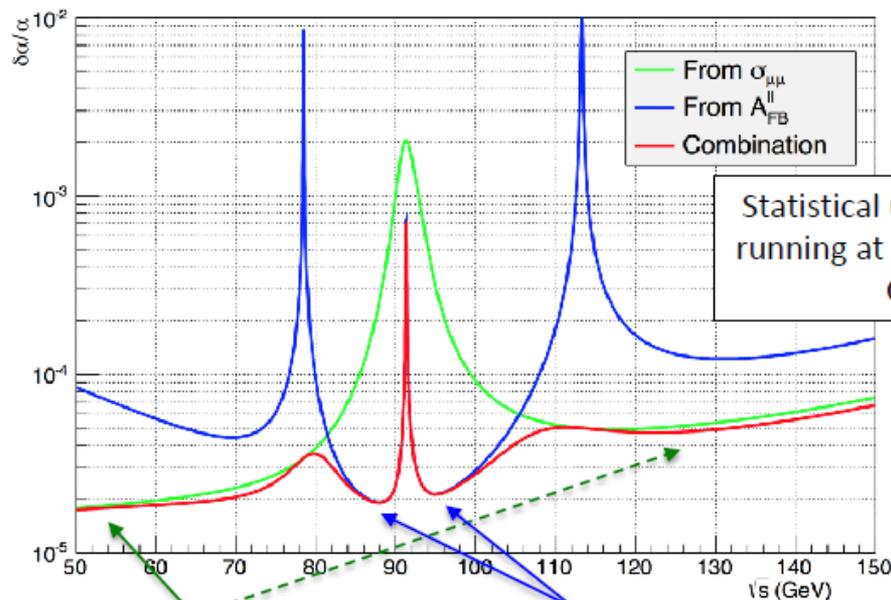
Two methods considered: Meast. of cross section,  $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ , and asymmetry,  $A_{\text{FB}}^{\mu\mu}$

- $\gamma$  exchange proportional to  $\alpha_{\text{QED}}^2(v_s)$
- $Z$  exchange independent of  $\alpha_{\text{QED}}(v_s)$
- $\gamma Z$  interference proportional to  $\alpha_{\text{QED}}(v_s)$



P. Janot: [FCC-ee Physics Vidyo Meeting, June 29<sup>th</sup> 2015](#)

# Potential of $\alpha_{\text{QED}}(m_Z)$ measurement (2)



Statistical uncertainty for one year of running at any centre-of-mass energy. Crab-waiste, 4 IP.

## From $\sigma_{\mu\mu}$ measurement

- Sensitivity best "far" away from Z peak, particularly at the low side
- Systematics (normalisation) probably a killer

## From $A_{\text{FB}}^{\mu\mu}$ measurement

- Sensitivity best at 88 and 95 GeV
- Experimental systs. looks controlable; further studies needed
- Theoretical systs. to large degree cancel by "averaging" over 88 and 95 GeV point

By running six months at each of 88 and 95 GeV points:

- Could potentially reach a precision of :  $\delta\alpha/\alpha = 2 \times 10^{-5}$

# Strong coupling constant, $\alpha_s(m_Z)$

At LEP, a precise  $\alpha_s(m_Z)$  measurement was derived from the Z decay ratio  $R_1 = \Gamma_{\text{had}}/\Gamma_1$ . Reinterpreting this measurement in light of: i) new  $N_3\text{LO}$  calculations; ii) improved  $m_{\text{top}}$ ; and iii) knowledge of the  $m_{\text{Higgs}}$ , the uncertainty is now something like:

$$\delta(\alpha_s(m_Z))_{\text{LEP}} = \pm 0.0038 \text{ (exp.)} \pm 0.0002 \text{ (others)}$$

$R_1$  measurement was statistics dominated: Foresee a factor  $\geq 25$  improvement at FCC-ee. From the Z-pole, therefore a reasonable experimental target is

$$\delta(\alpha_s(m_Z))_{\text{FCC-ee}} = \pm 0.00015$$

Similarly, from the WW threshold,  $\alpha_s(m_W)$  can be derived from the high stats measurement of  $B_{\text{had}} = (\Gamma_{\text{had}}/\Gamma_{\text{tot}})_W$

$$\delta(\alpha_s(m_W))_{\text{FCC-ee}} = \pm 0.00015$$

Combining the two above, a realistic target precision would be

$$\delta(\alpha_s(m_Z))_{\text{FCC-ee}} = \pm 0.0001$$



	$A_{FB}^{\mu\mu}$ @ FCC- ee		$A_{LR}$ @ ILC
visible Z decays	$10^{12}$	visible Z decays	$10^9$
muon pairs	$5 \cdot 10^{10}$	beam polarization	90%
$\Delta A_{FB}^{\mu\mu}$ (stat)	$4.6 \cdot 10^{-6}$	$\Delta A_{LR}$ (stat)	$4.2 \cdot 10^{-5}$
$\Delta E_{cm}$ (MeV)	0.1		2.2
$\Delta A_{FB}^{\mu\mu}$ ( $E_{CM}$ )	$9.2 \cdot 10^{-6}$	$\Delta A_{LR}$ ( $E_{CM}$ )	$4.1 \cdot 10^{-5}$
$\Delta A_{FB}^{\mu\mu}$	$1.0 \cdot 10^{-5}$	$\Delta A_{LR}$	$5.9 \cdot 10^{-5}$
$\Delta \sin^2 \theta_w^{lept}$	<b><math>5.9 \cdot 10^{-6}</math></b>		<b><math>7.5 \cdot 10^{-6}</math></b>

**PRESENT:**

$\Delta \sin^2 \theta_w^{lept}$	from $A_{FB}^{\mu\mu}$ LEP $2 \cdot 10^7 Z$ $5.3 \cdot 10^{-4}$	SLC, $5 \cdot 10^5 Z$ $2.6 \cdot 10^{-4}$	W.A. $1.6 \cdot 10^{-4}$	$\Delta \alpha$ $3.5 \cdot 10^{-5}$
---------------------------------	--	--	-----------------------------	--

from  $\alpha_{QED}$  (mZ)  $\Delta \alpha = 0.00002$

$\rightarrow \Delta \sin^2 \theta_w^{lept} = 7 \cdot 10^{-6}$





# Theoretical limitations

**FCC-ee**

*R. Kogler, Moriond EW 2013*

SM predictions (using other input)

$$\begin{aligned}
 M_W &= 80.3593 \pm \overset{0.000'2}{\textcircled{0.0056}}_{m_t} \pm 0.0026_{M_Z} \pm 0.0018_{\Delta\alpha_{\text{had}}} \\
 &\quad \pm 0.0017_{\alpha_S} \pm 0.0002_{M_H} \pm \textcircled{0.0040}_{\text{theo}} \\
 &= 80.359 \pm \overset{0.000'25}{0.011}_{\text{tot}}
 \end{aligned}$$

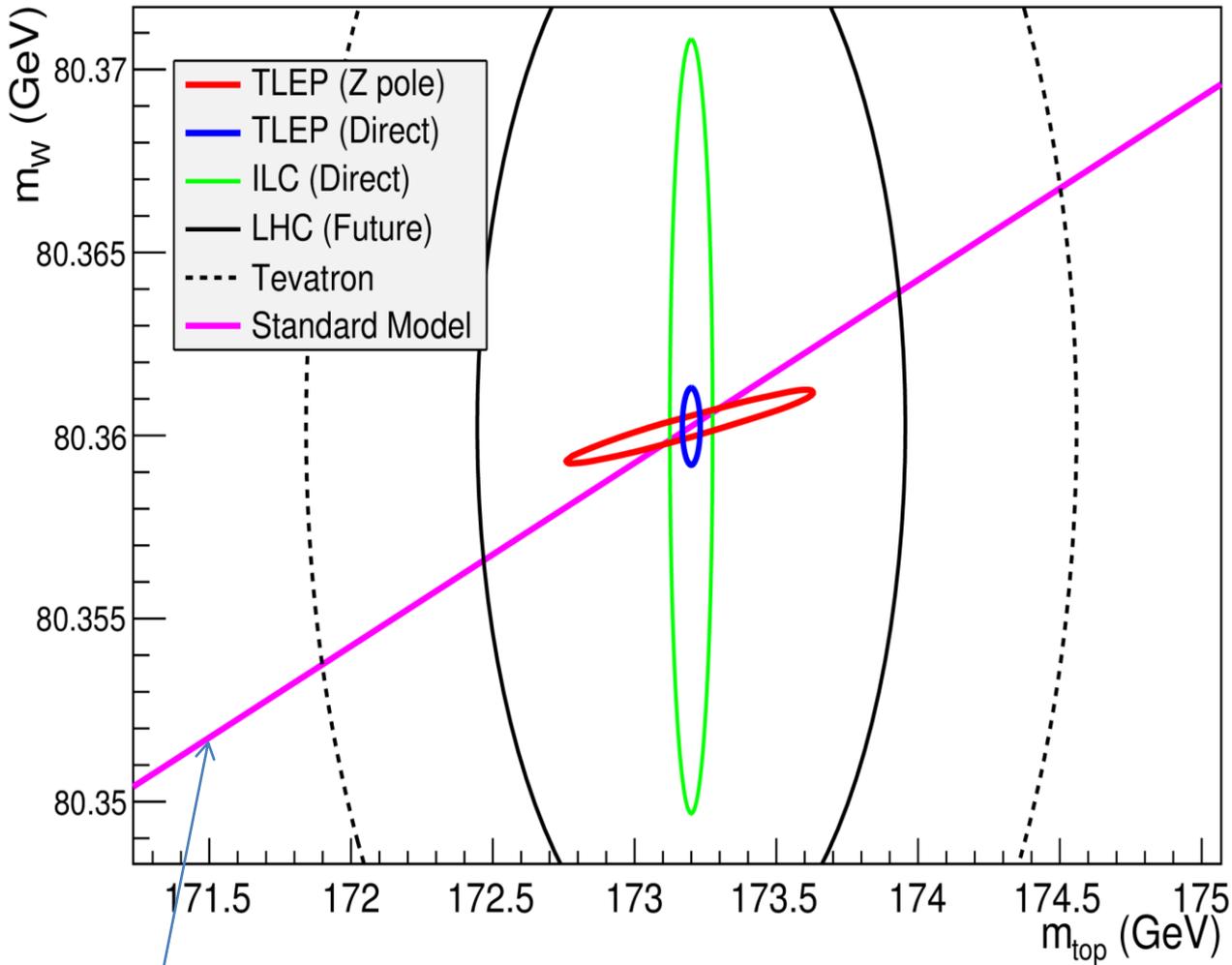
$$\begin{aligned}
 \sin^2\theta_{\text{eff}}^{\ell} &= 0.231496 \pm \overset{0.000'0015}{0.000030}_{m_t} \pm \overset{0.000'001}{0.000015}_{M_Z} \pm \overset{0.000'007}{\textcircled{0.000035}}_{\Delta\alpha_{\text{had}}} \\
 &\quad \pm 0.000010_{\alpha_S} \pm 0.000002_{M_H} \pm \textcircled{0.000047}_{\text{theo}} \\
 &= 0.23150 \pm \overset{0.000'0014}{0.00010}_{\text{tot}}
 \end{aligned}$$

Experimental errors at FCC-ee will be 20-100 times smaller than the present errors.

BUT can be typically 10 -30 times smaller than present level of theory errors

Will require significant theoretical effort and additional measurements!

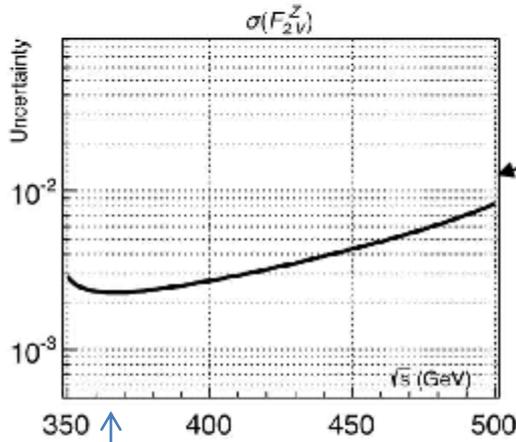
Radiative correction workshop 13-14 July 2015 stressed the need for 3 loop calculations for the future!  
Suggest including manpower for theoretical calculations in the project cost.



**NB width of this line : Z mass error. Without FCC-ee its 2.2 MeV!**

**in other words ...  $\Delta(\Delta\rho) = \pm 10^{-5}$  + several tests of same precision**

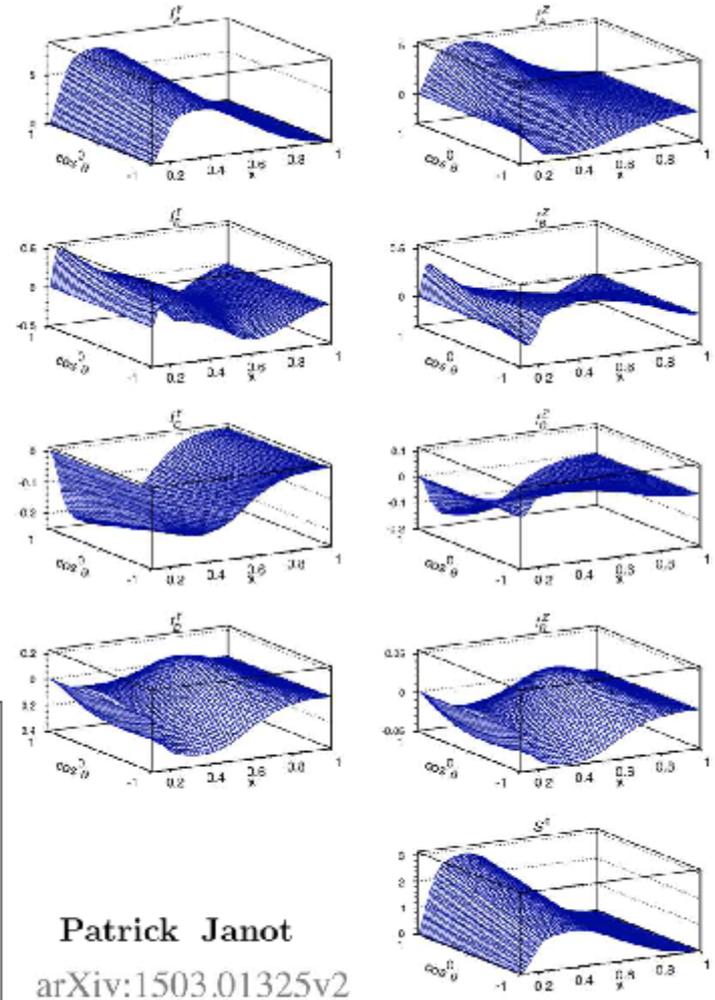
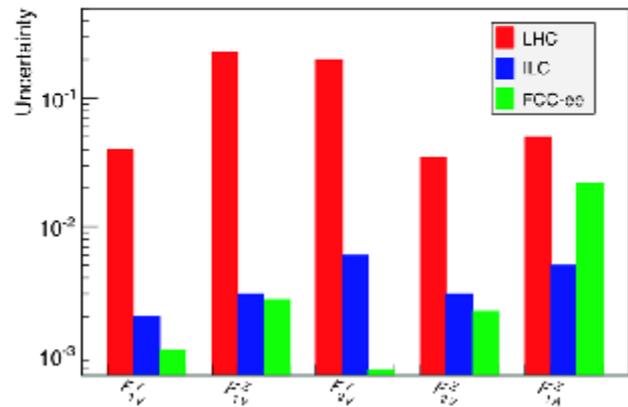
Determination of top-quark EW couplings via measurement of **top-quark polarization**.  
 In semileptonic decays, fit to lepton momentum vs scattering angle



Typically best sensitivity just above production threshold

Momenta up to: 175 GeV

no need for High Energy or beam polarization



Patrick Janot  
 arXiv:1503.01325v2



# Conclusions

**FCC-ee offers a coherent program of EW precision measurements on 'all fronts'**

## **In view of the accelerator design:**

- energy calibration is essential
- Jury is still open on longitudinal polarization
  - no obvious need except perhaps at the Z peak
- nobody complains about too much luminosity (pile-up < 0.001)
- for the EW fits, we need to cover Z,W, and top.

## **In view of the design study report:**

- unprecedented precisions can be achieved on all fronts
- All parametric errors can be considerably reduced to below the experimental uncertainties and reveal the

**absolute need to improve the theoretical accuracies**

**==> a plan for this has to be included in the design report.**

**more observables to investigate ( $A_{FB}^b$ ,  $R_b$ , etc... )**

- 9)
- the resulting precision in terms of reach for new physics can be quantified in various ways -- we need to work on this.

